

Filaments, surface density and scaling laws in star and structure formation

Marco Lombardi, University of Milan

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Marco Lombardi, University of Milan

with

Joao Alves, University of Vienna &
Charles Lada, CfA, Harvard

Penitenziagite

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M42/M43

1 pc



$z=z_{\odot}$

134606 yr



Matthew Bate
University of Exeter

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134606 yr



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We cannot see cold H₂

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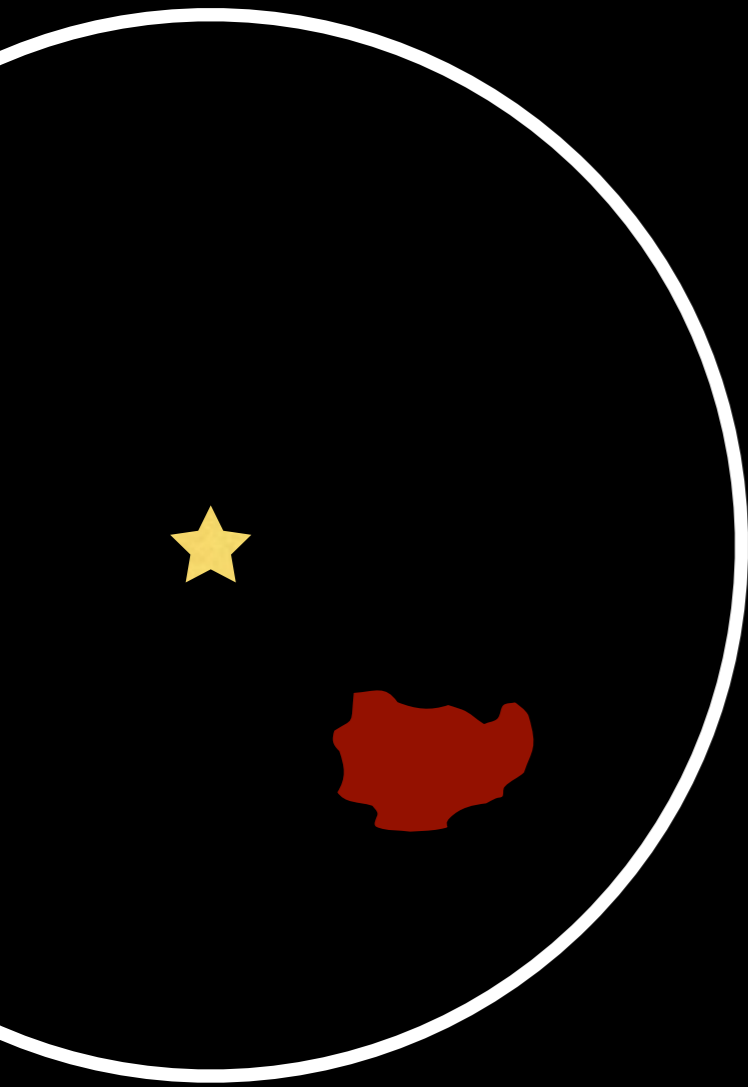
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- Each tracer has its own benefits and limitations!

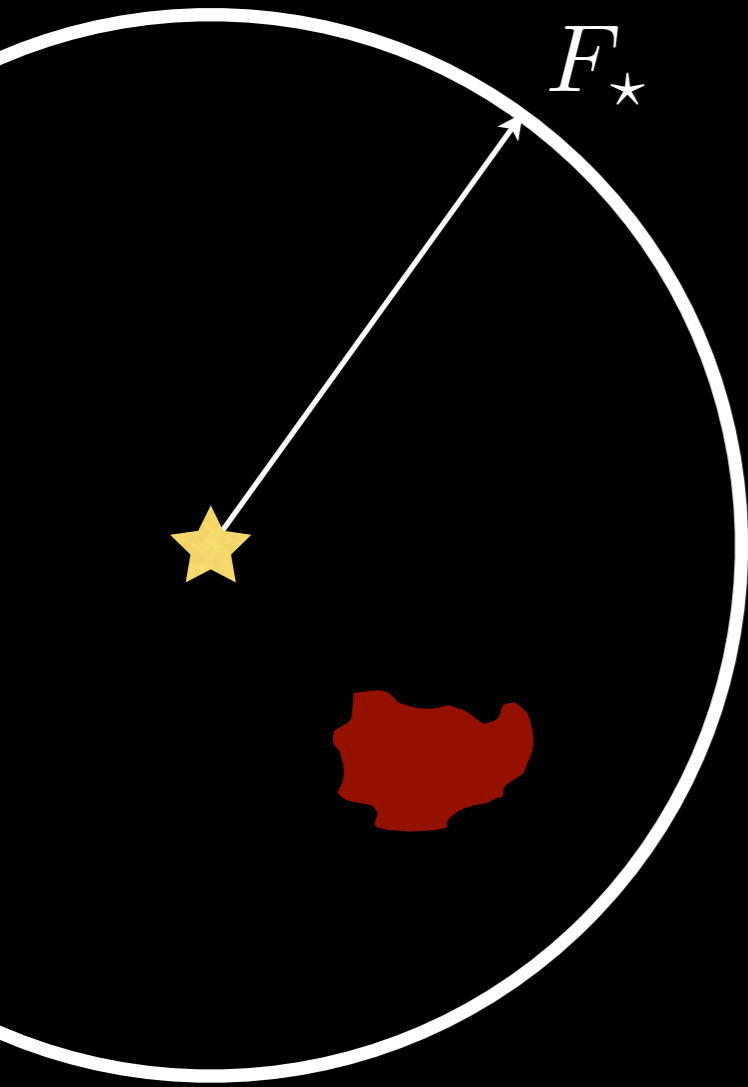
Extinction Primer



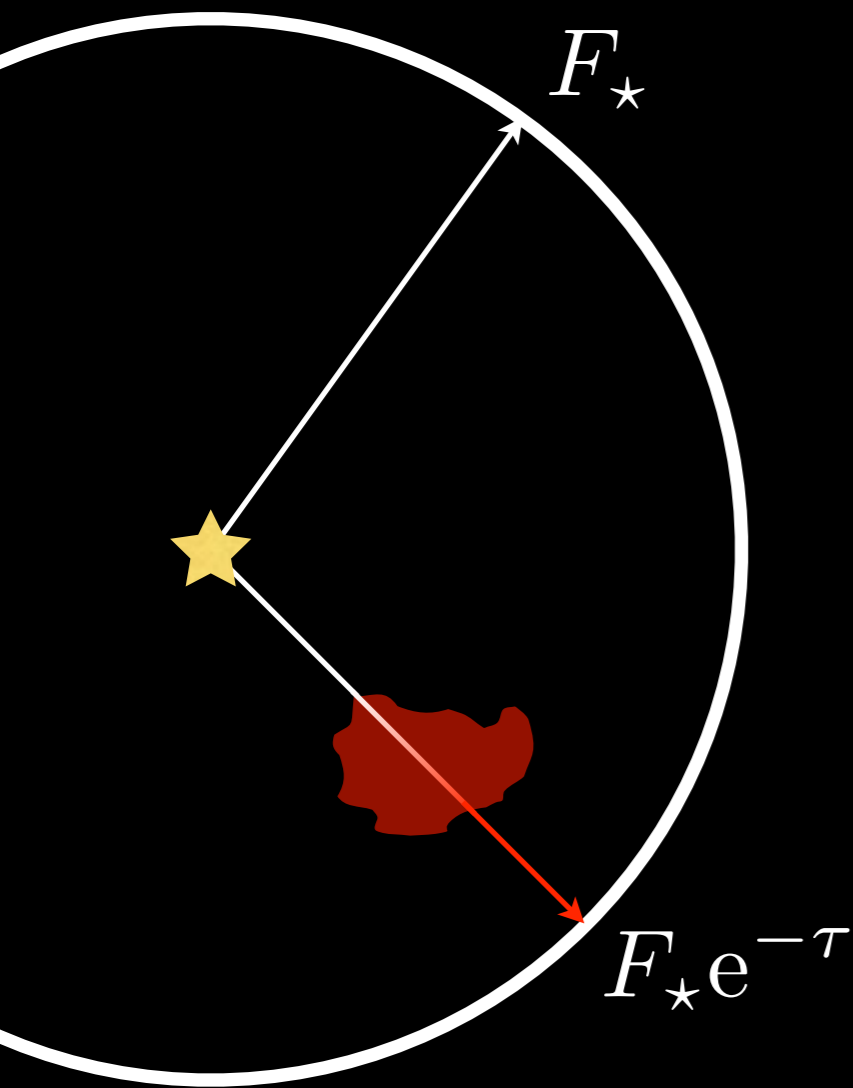
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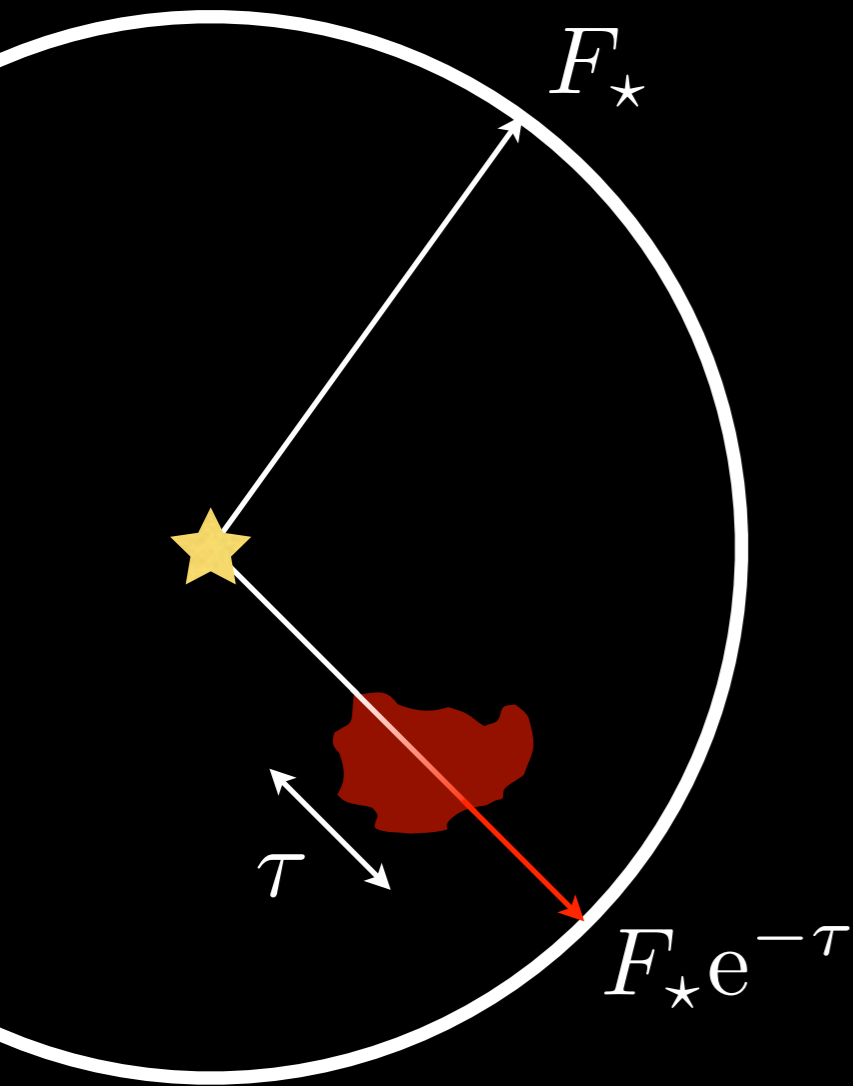
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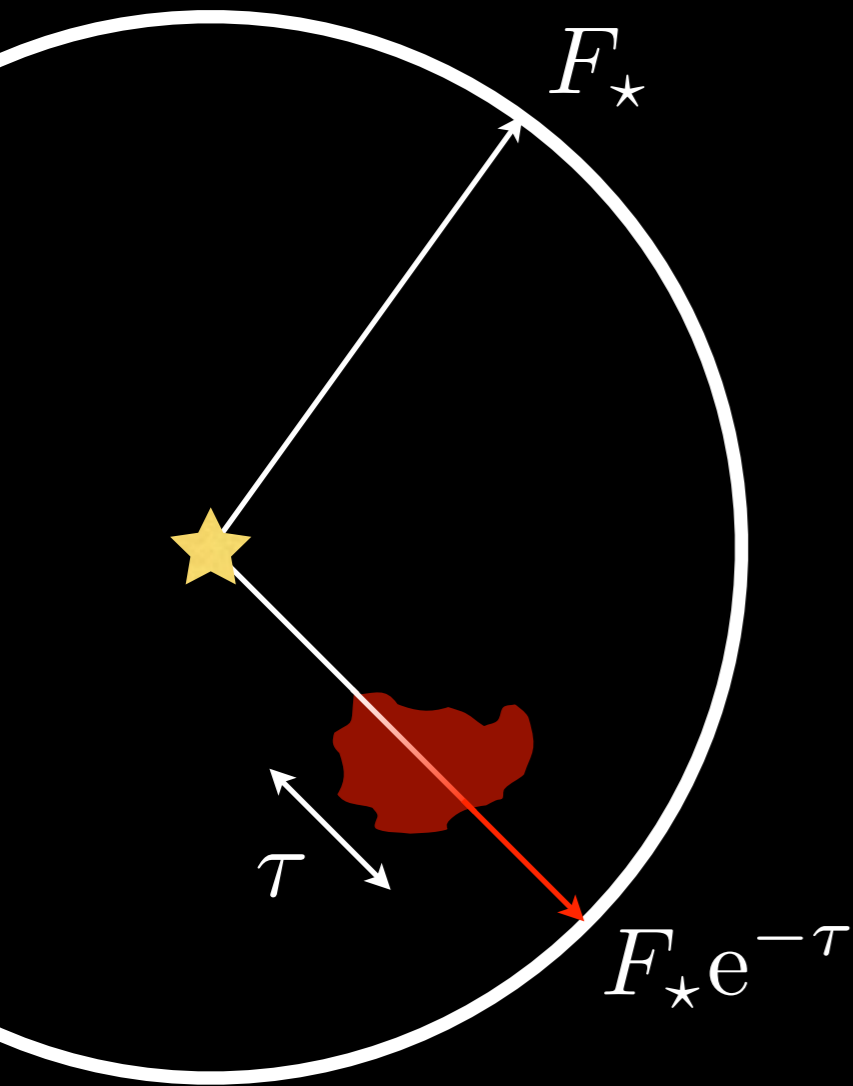
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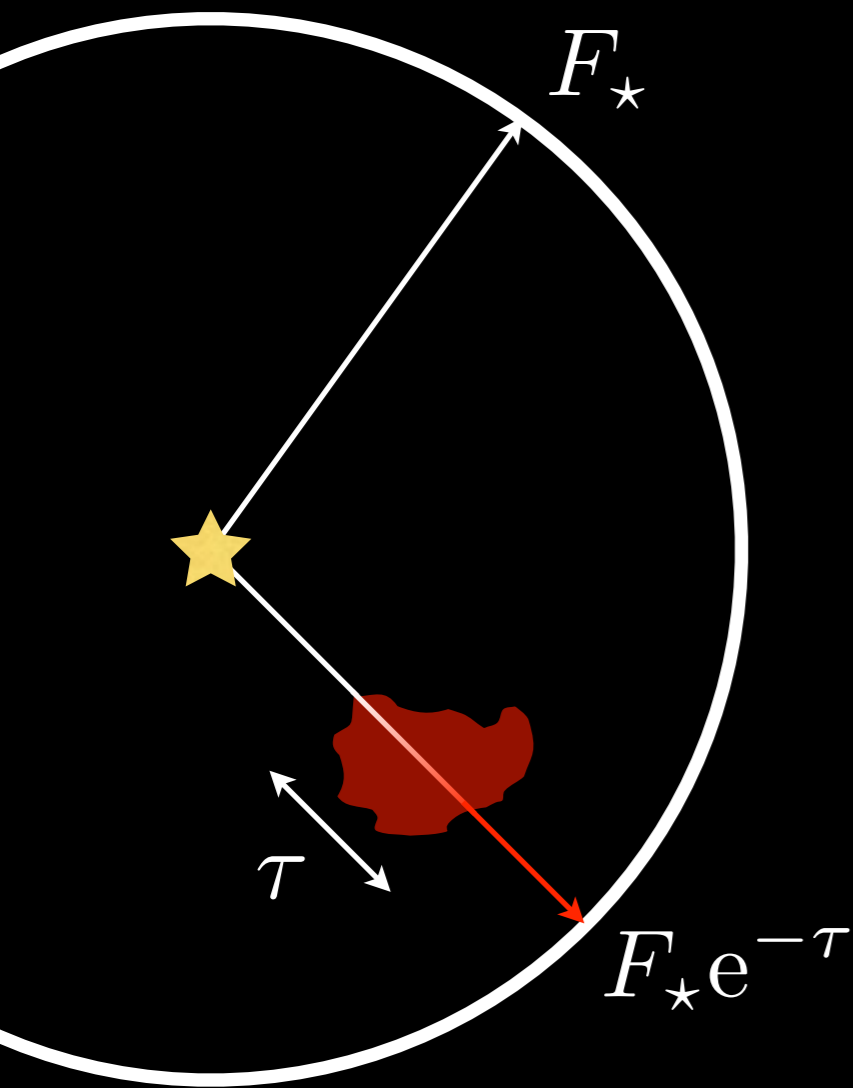


Brightness

$$m_{\text{obs}} = -2.5 \log (F_{\star} e^{-\tau})$$

$$= - \underbrace{2.5 \log F_{\star}}_{m_{\star}} + \underbrace{2.5 \tau \log e}_{A_V}$$

Extinction Primer



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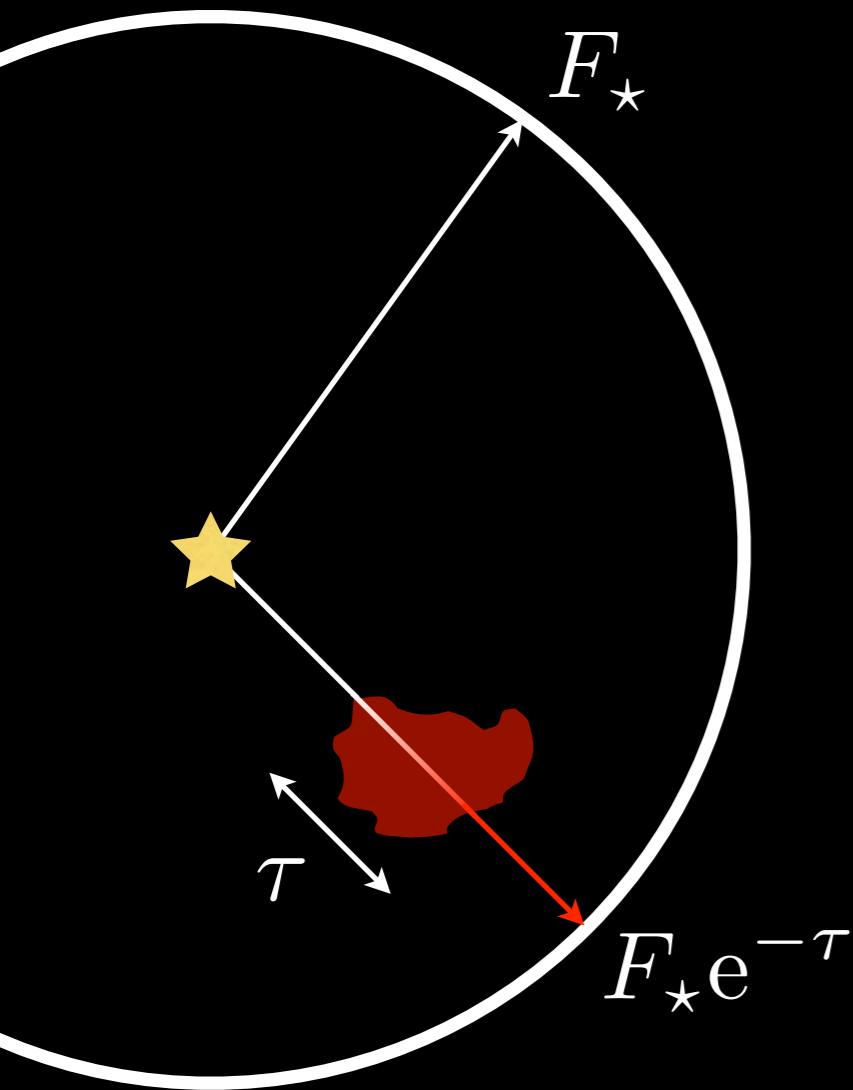
$$\begin{aligned} m_{\text{obs}} &= -2.5 \log (F_* e^{-\tau}) \\ &= -\underbrace{2.5 \log F_*}_{m_*} + \underbrace{2.5 \tau \log e}_{A_V} \end{aligned}$$

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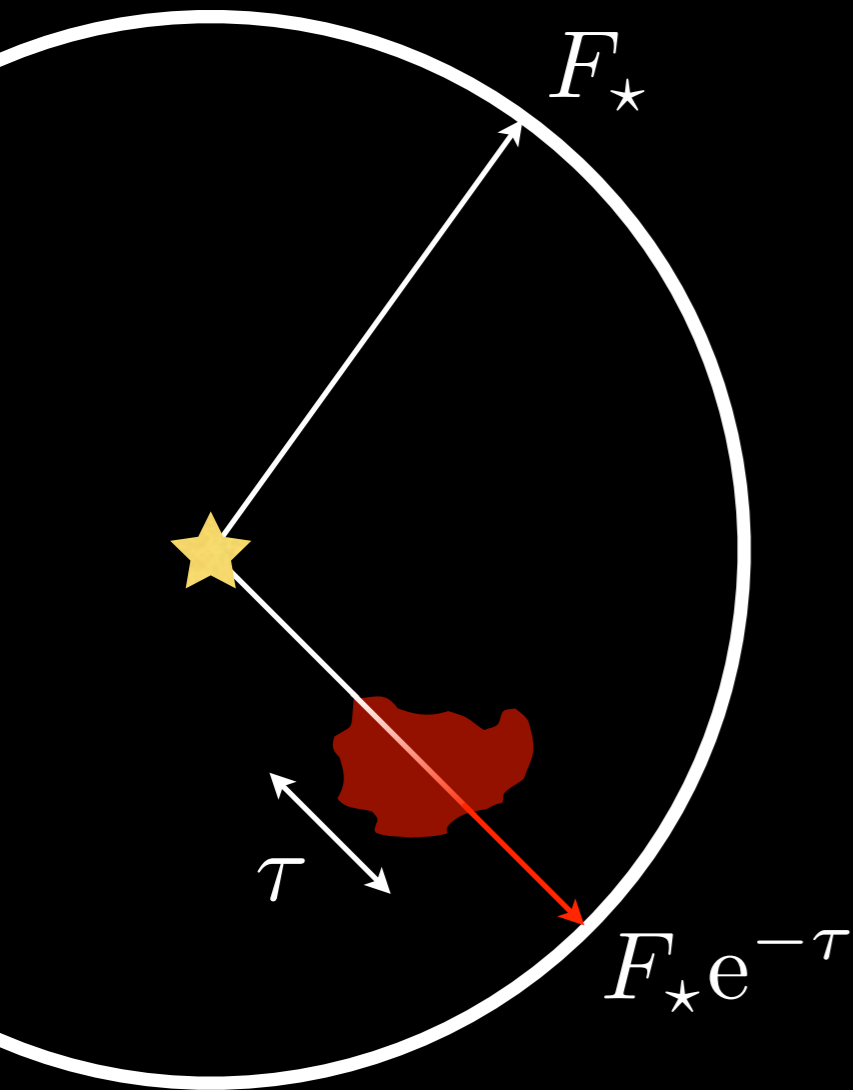


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Color

$$\Delta m = m_{\lambda_1} - m_{\lambda_2}$$



Extinction

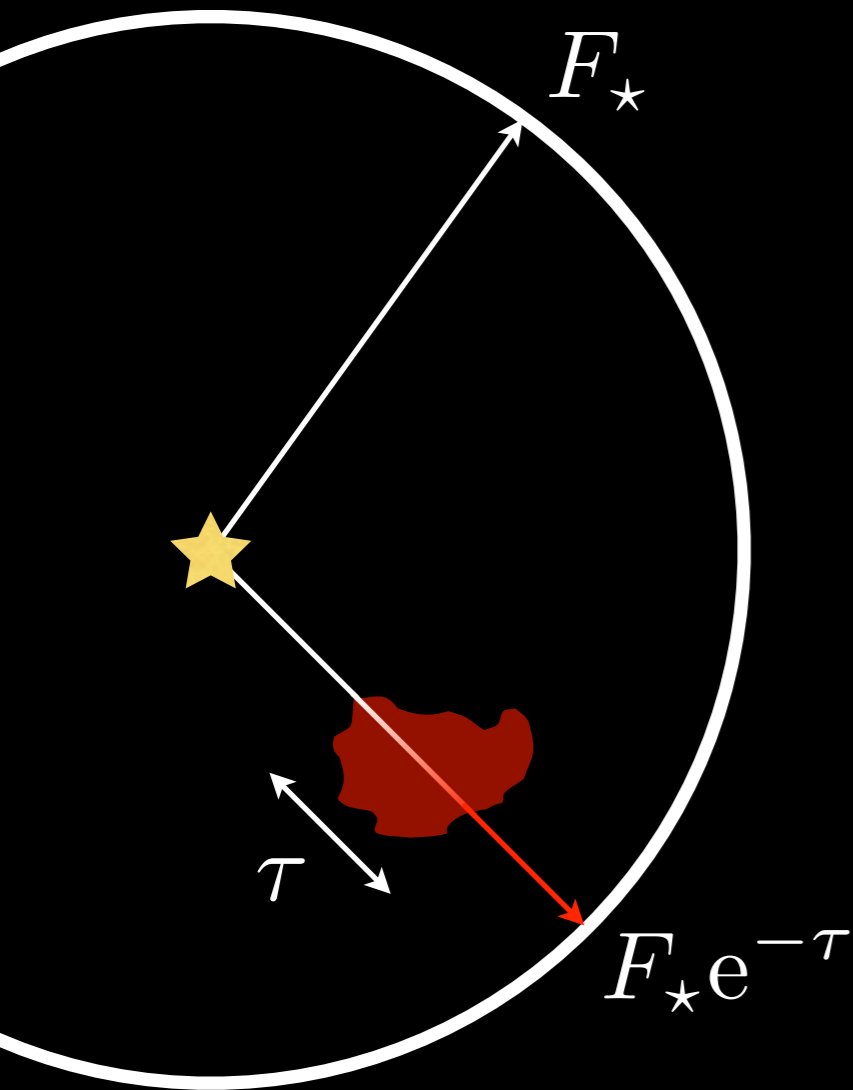
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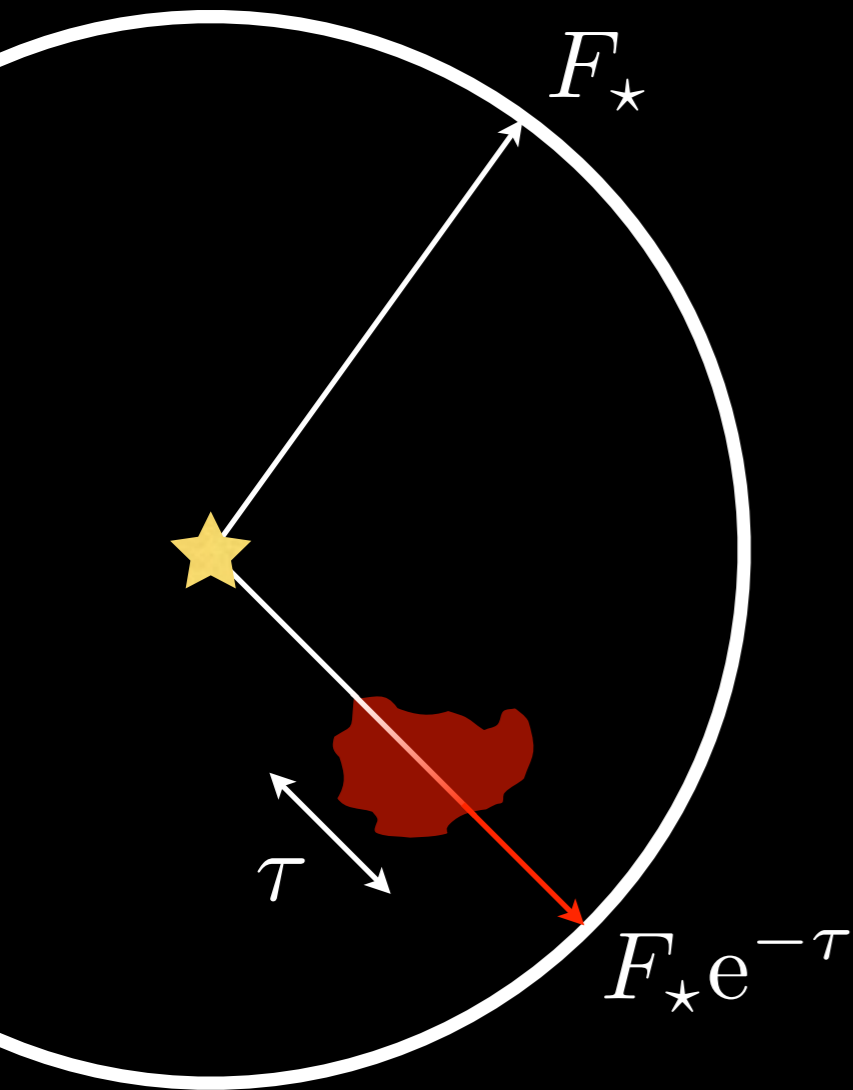
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$R_{1,2}$ parametrizes our knowledge (or ignorance) on the dust properties at the two frequencies λ_1 and λ_2

Making extinction maps



Alves et al. (2014)

Making extinction maps

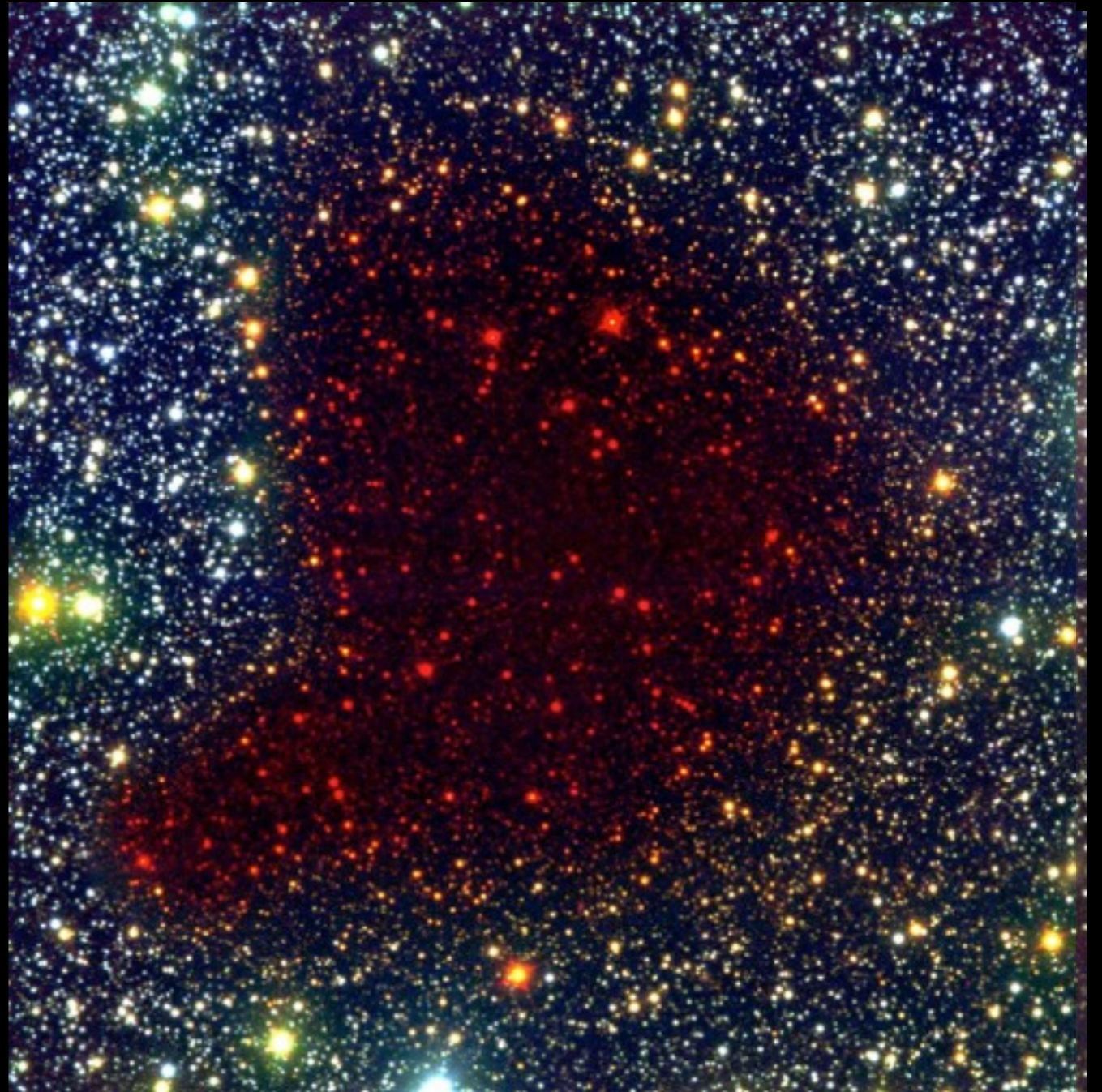
- Take a cloud



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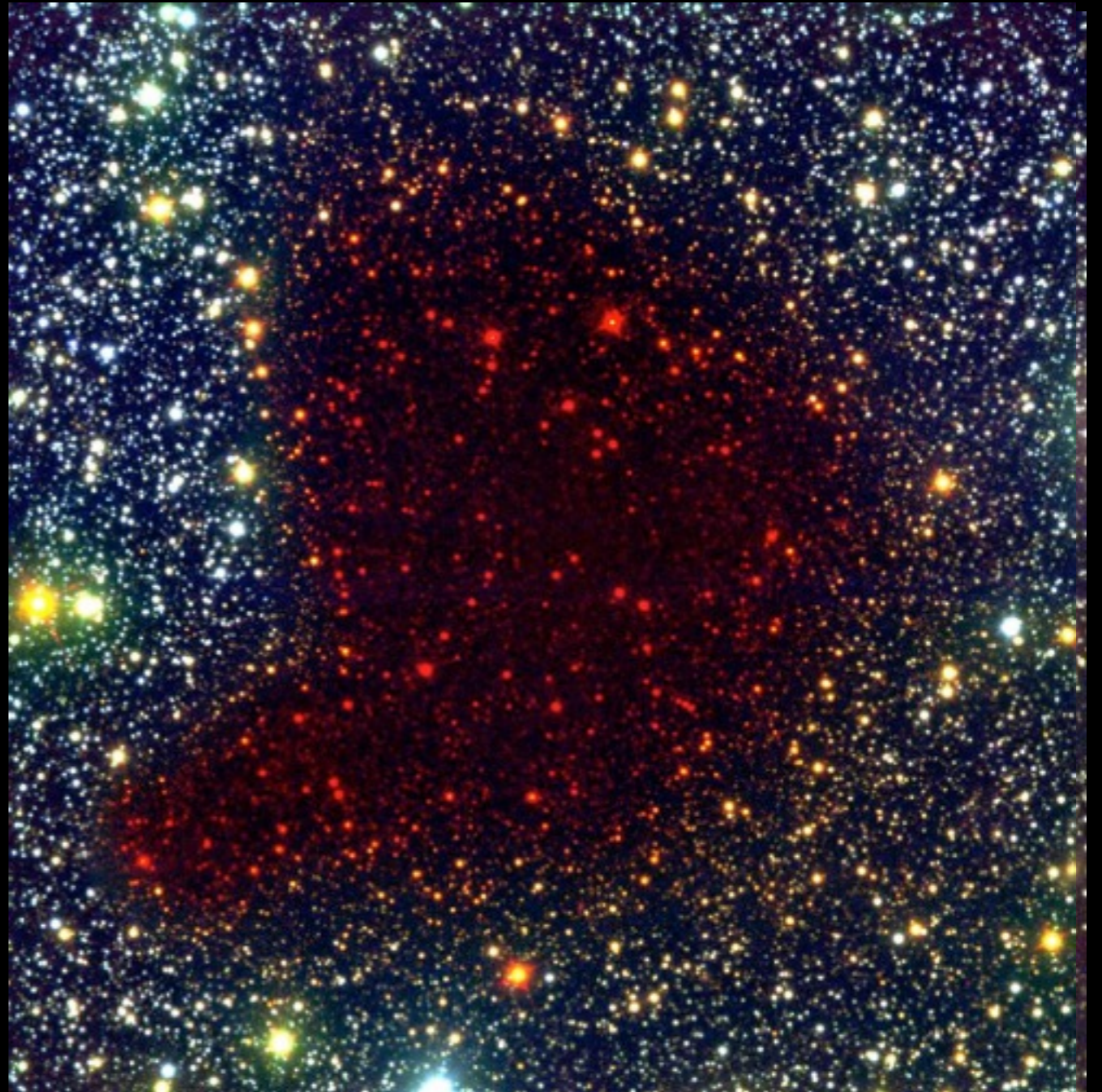
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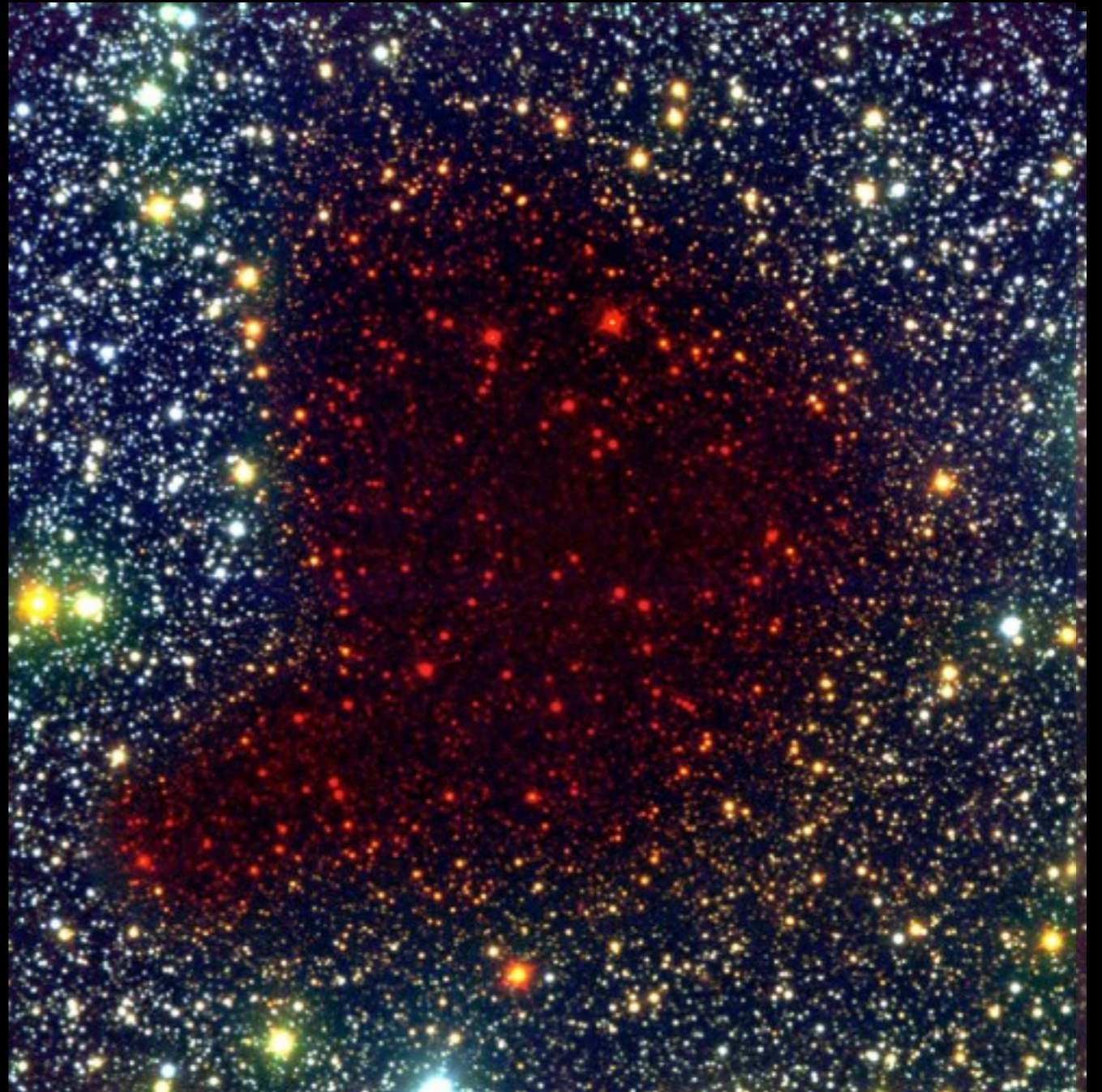
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$$\Sigma_{\text{gas}} \sim \Sigma_{\text{dust}} \sim E(H - K)$$



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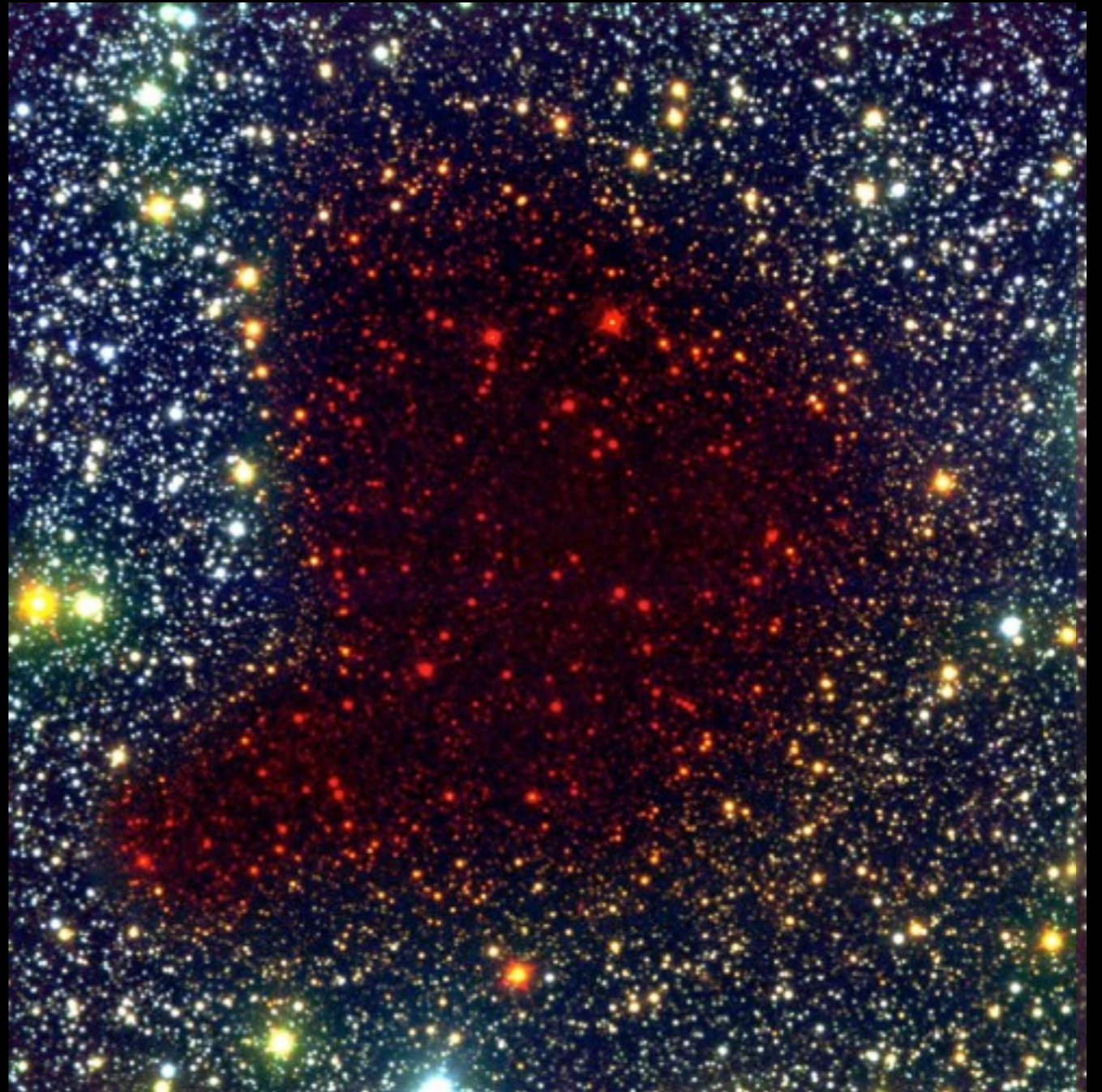
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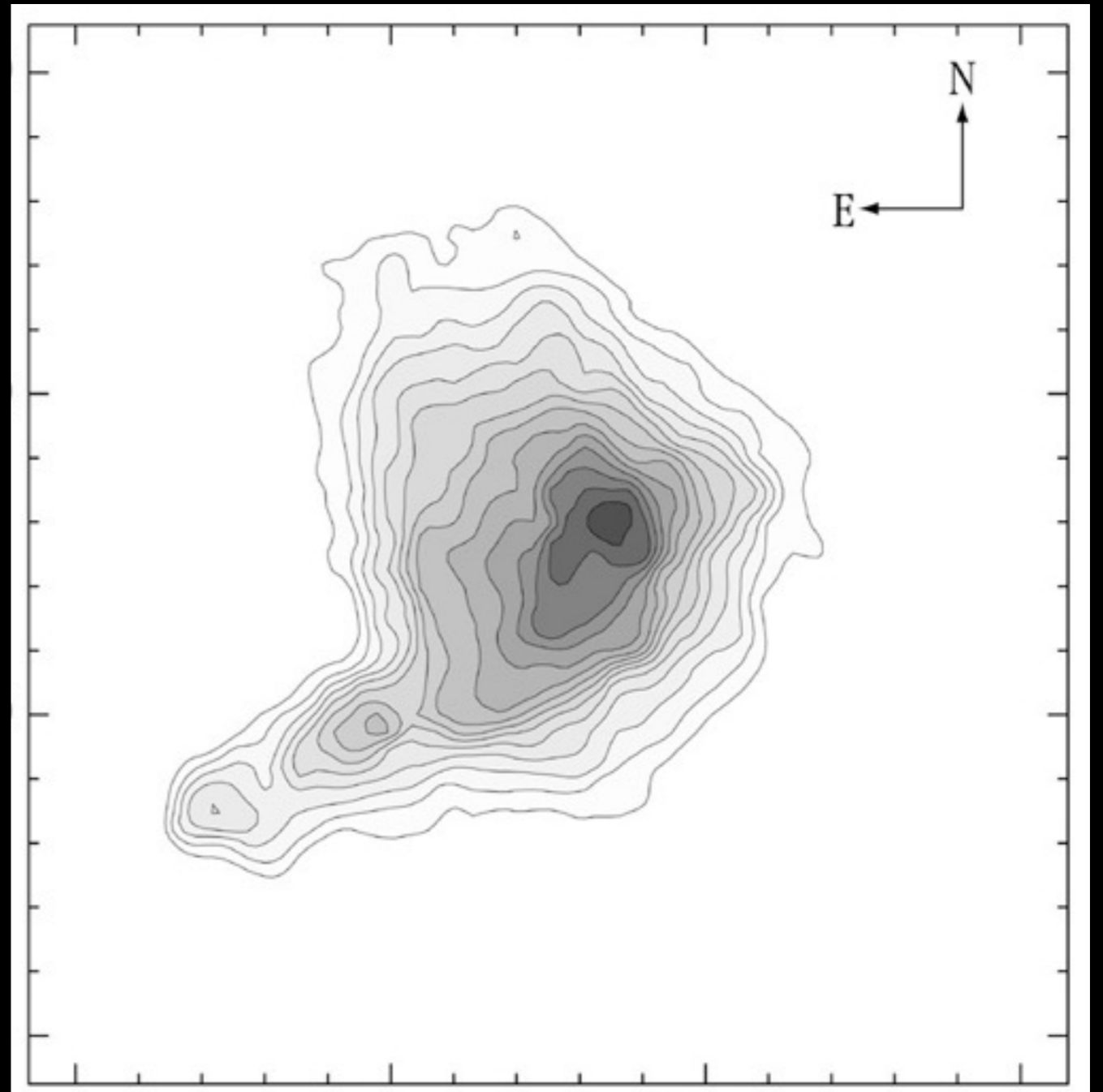
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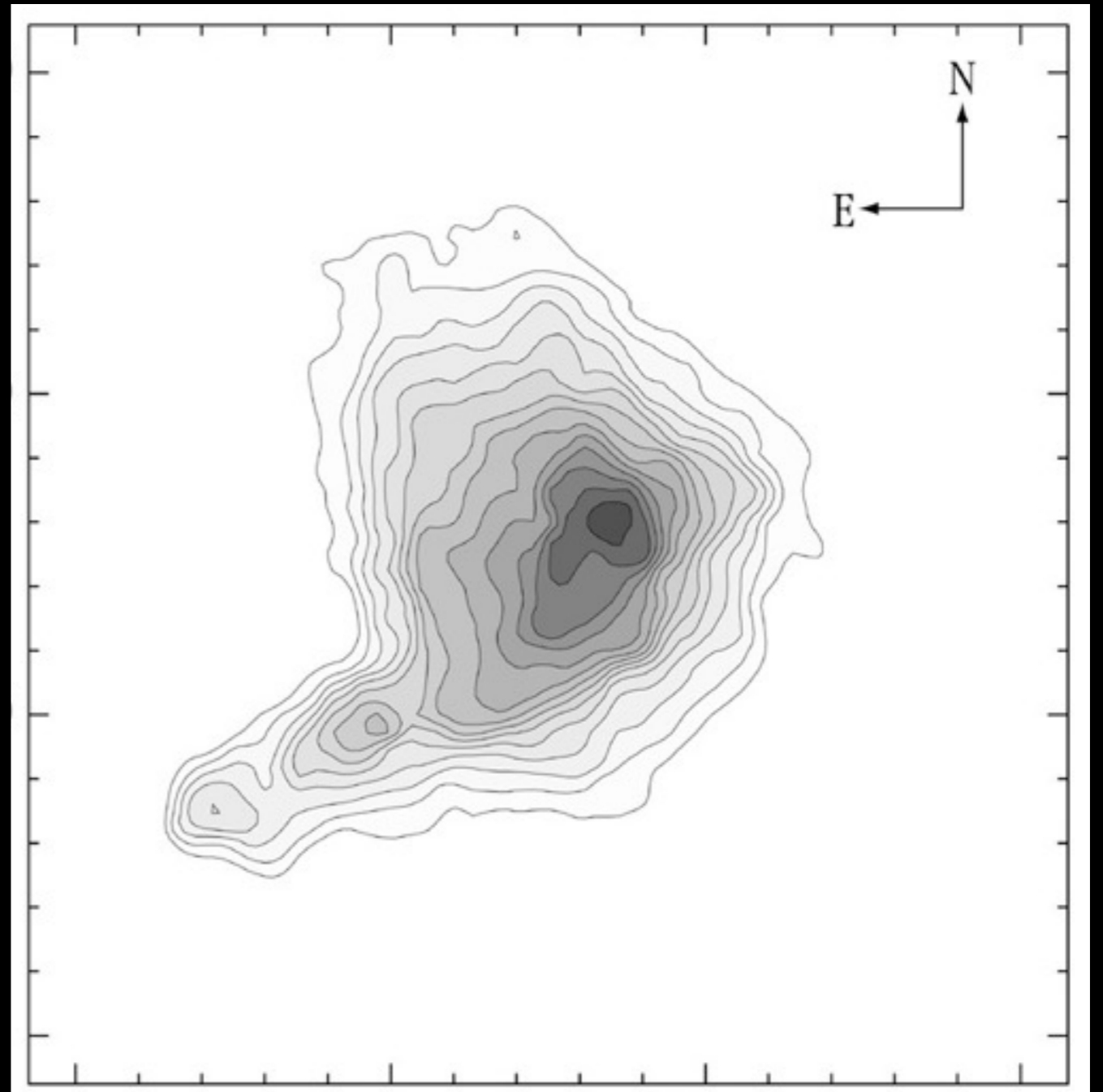
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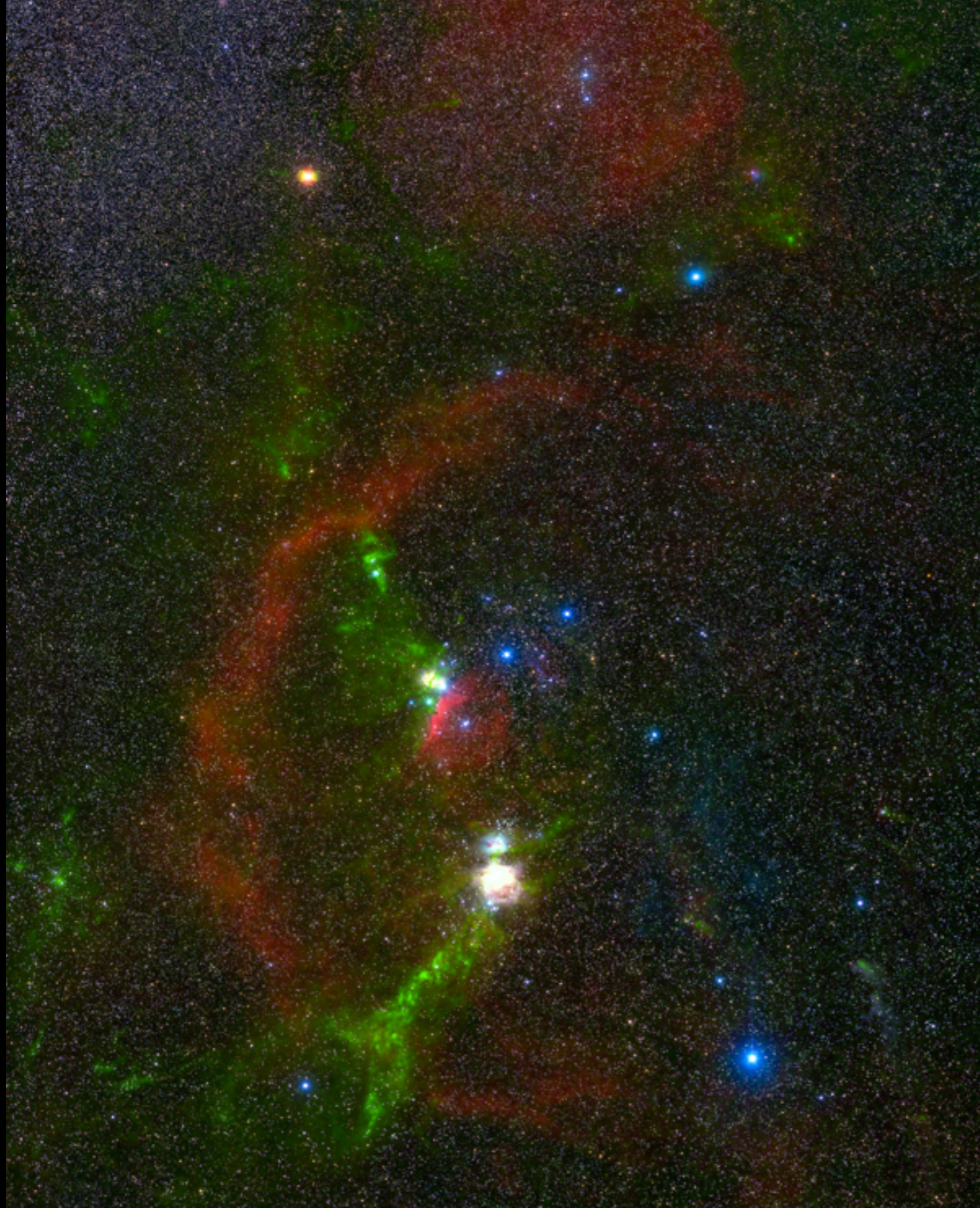
Making extinction maps

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- Make a smooth map
- Convert extinction into gas column density



Alves et al. (2014)

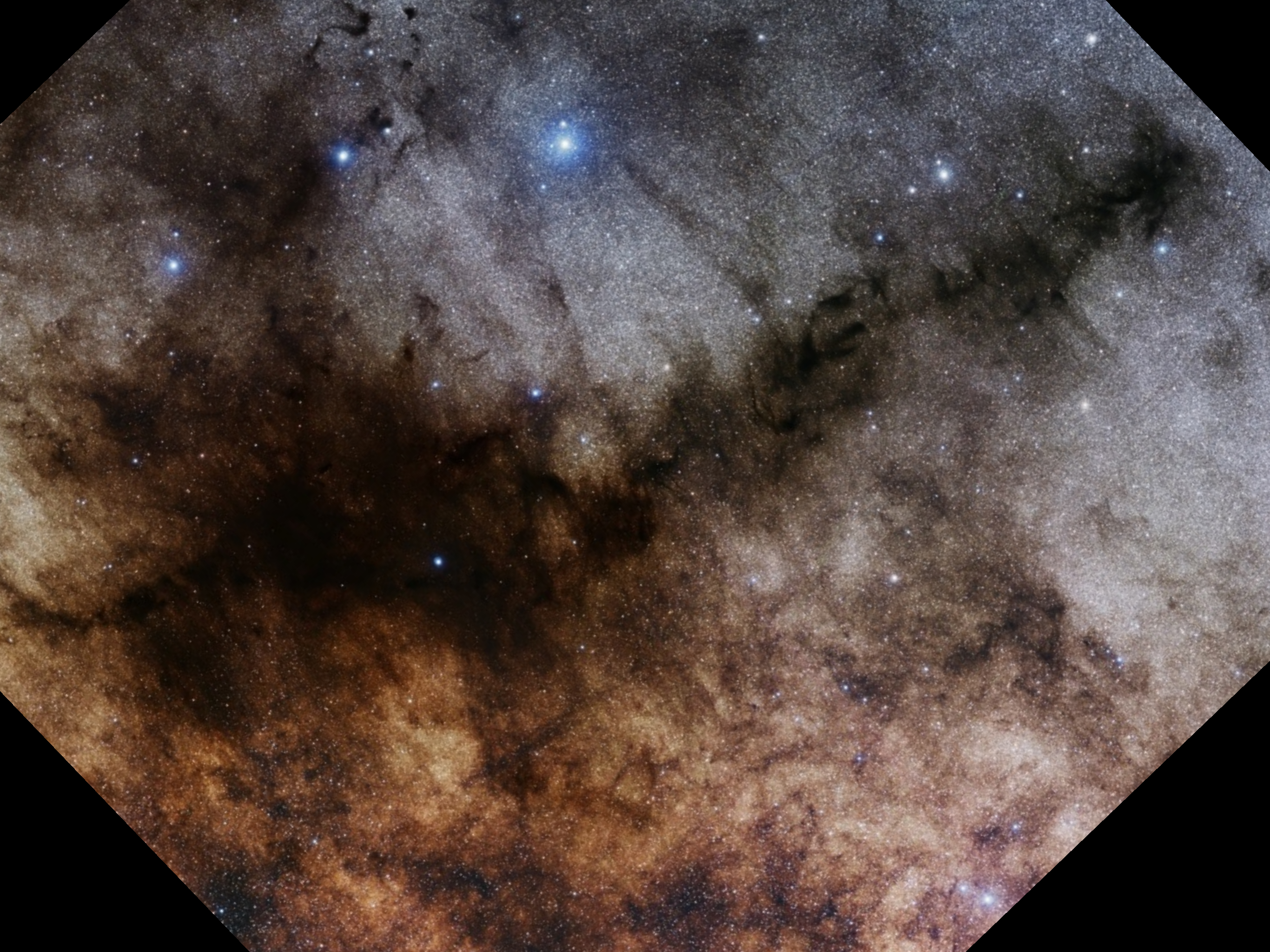


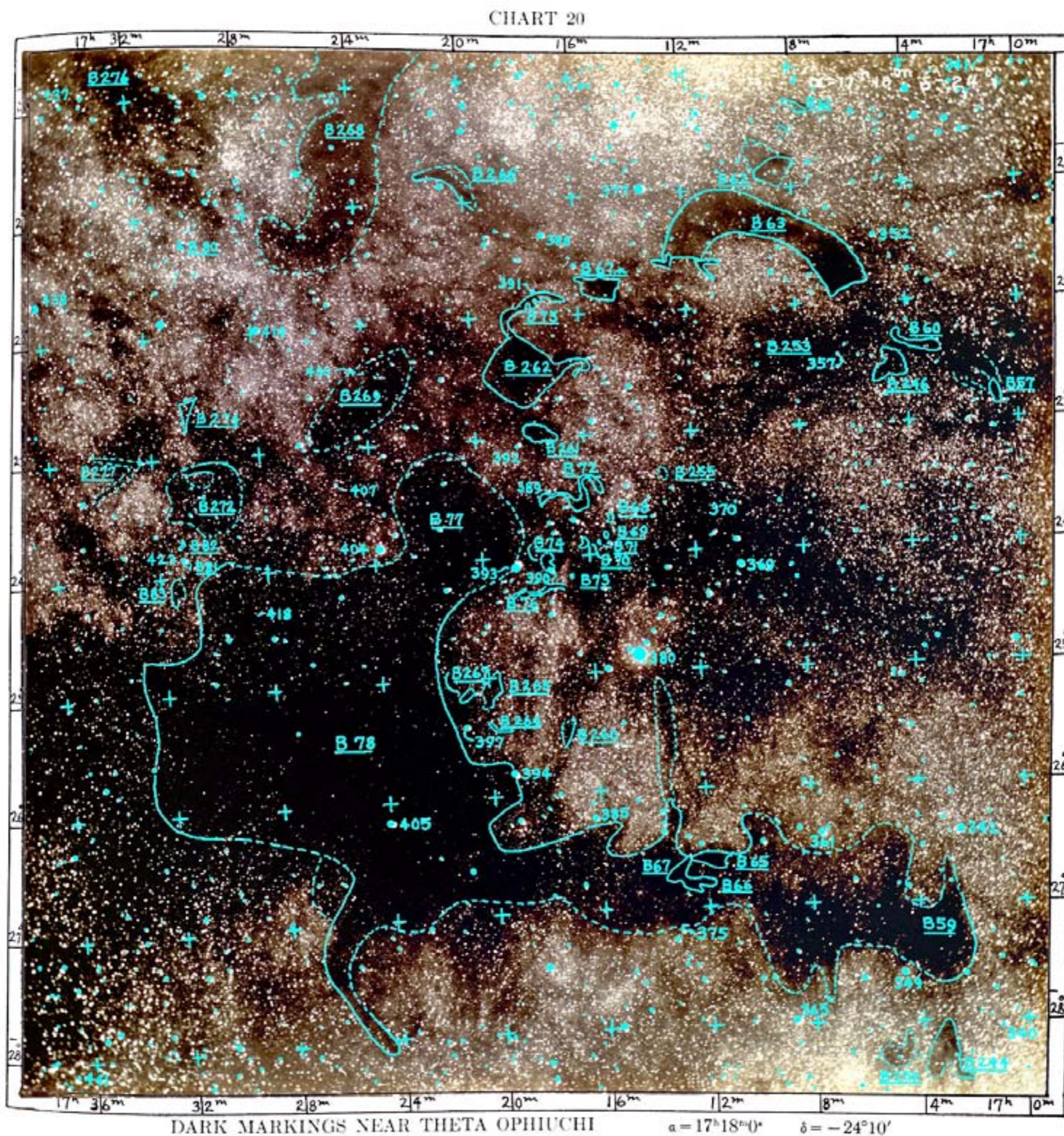


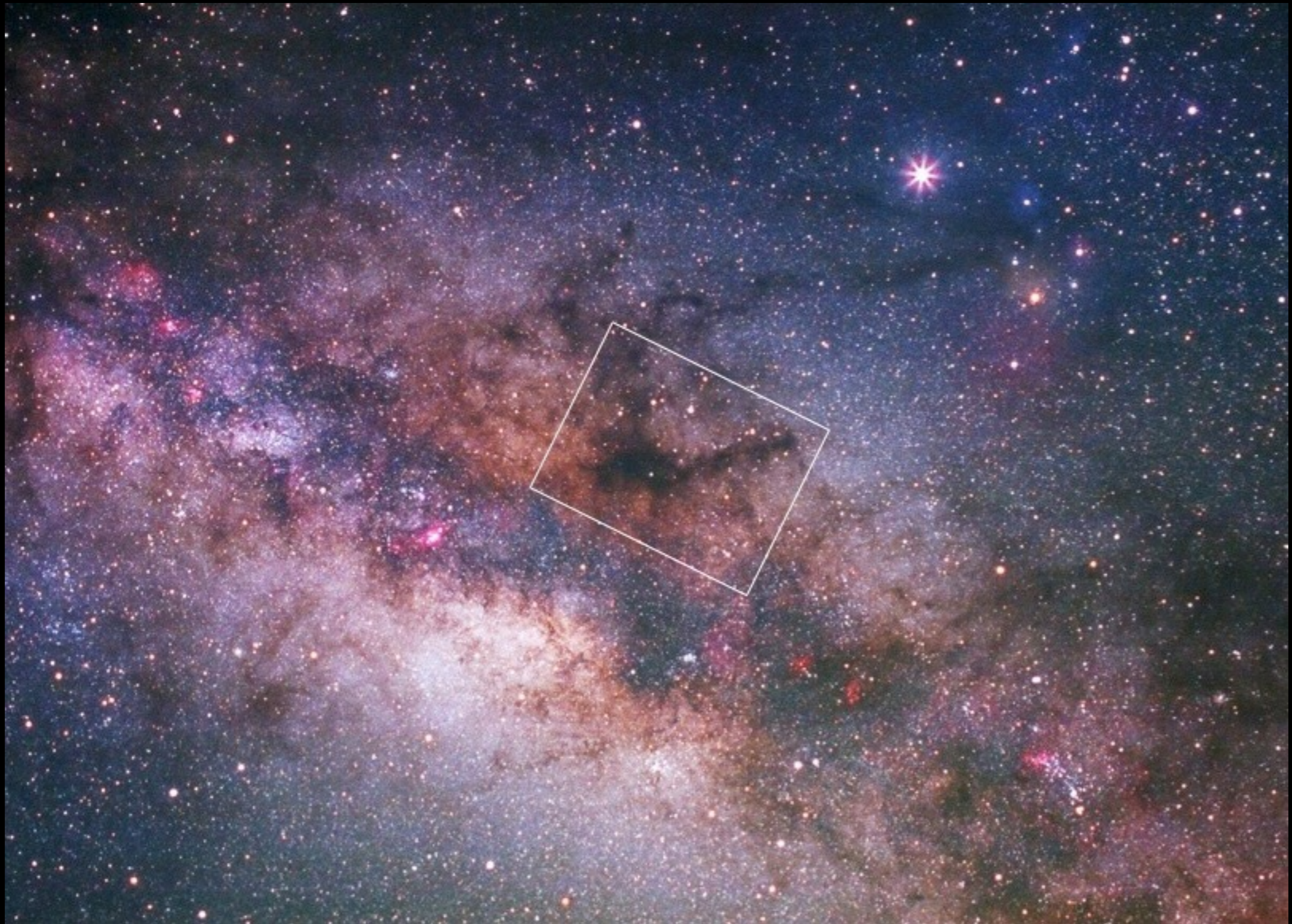


Ceci n'est pas une pipe.

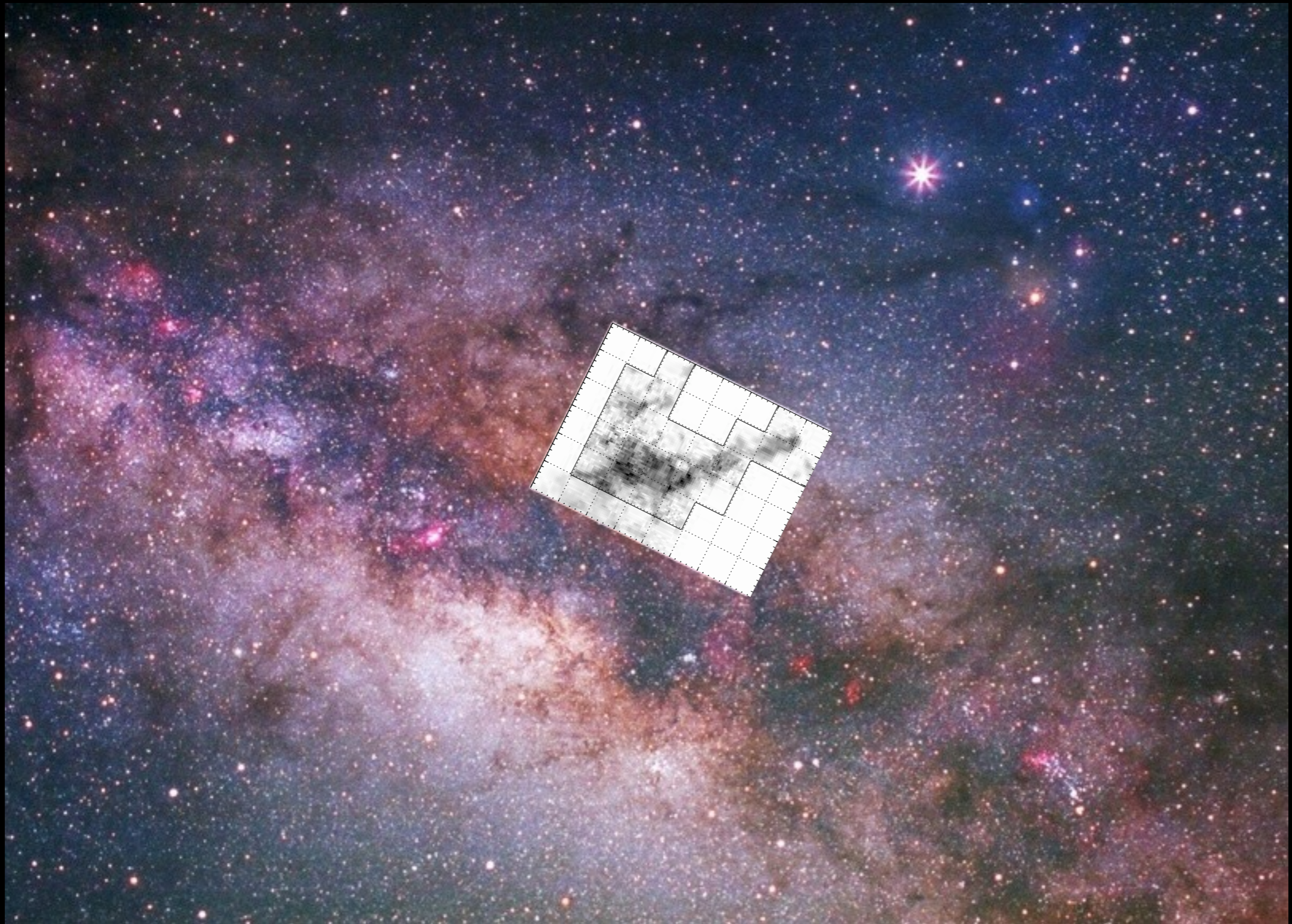






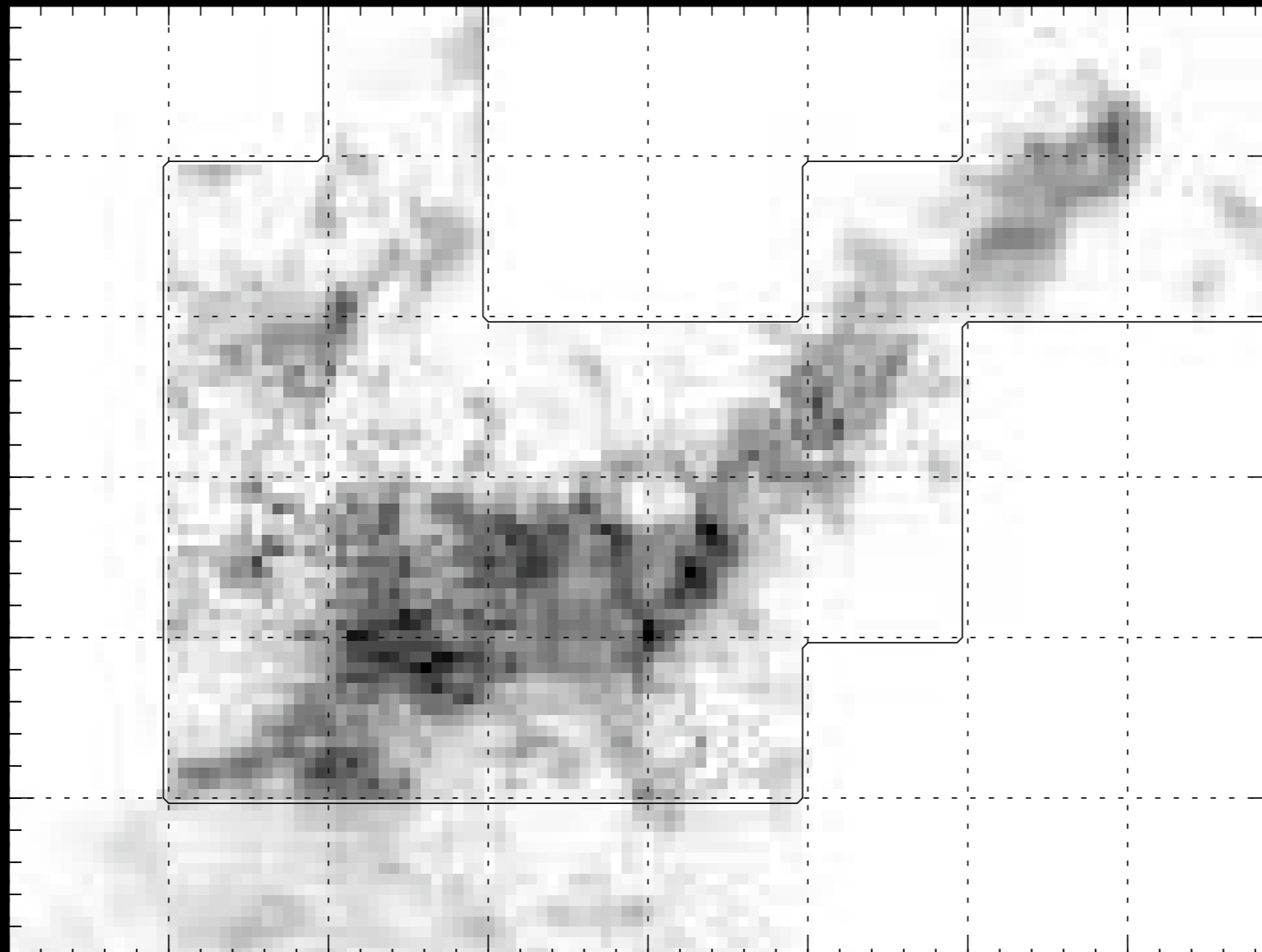


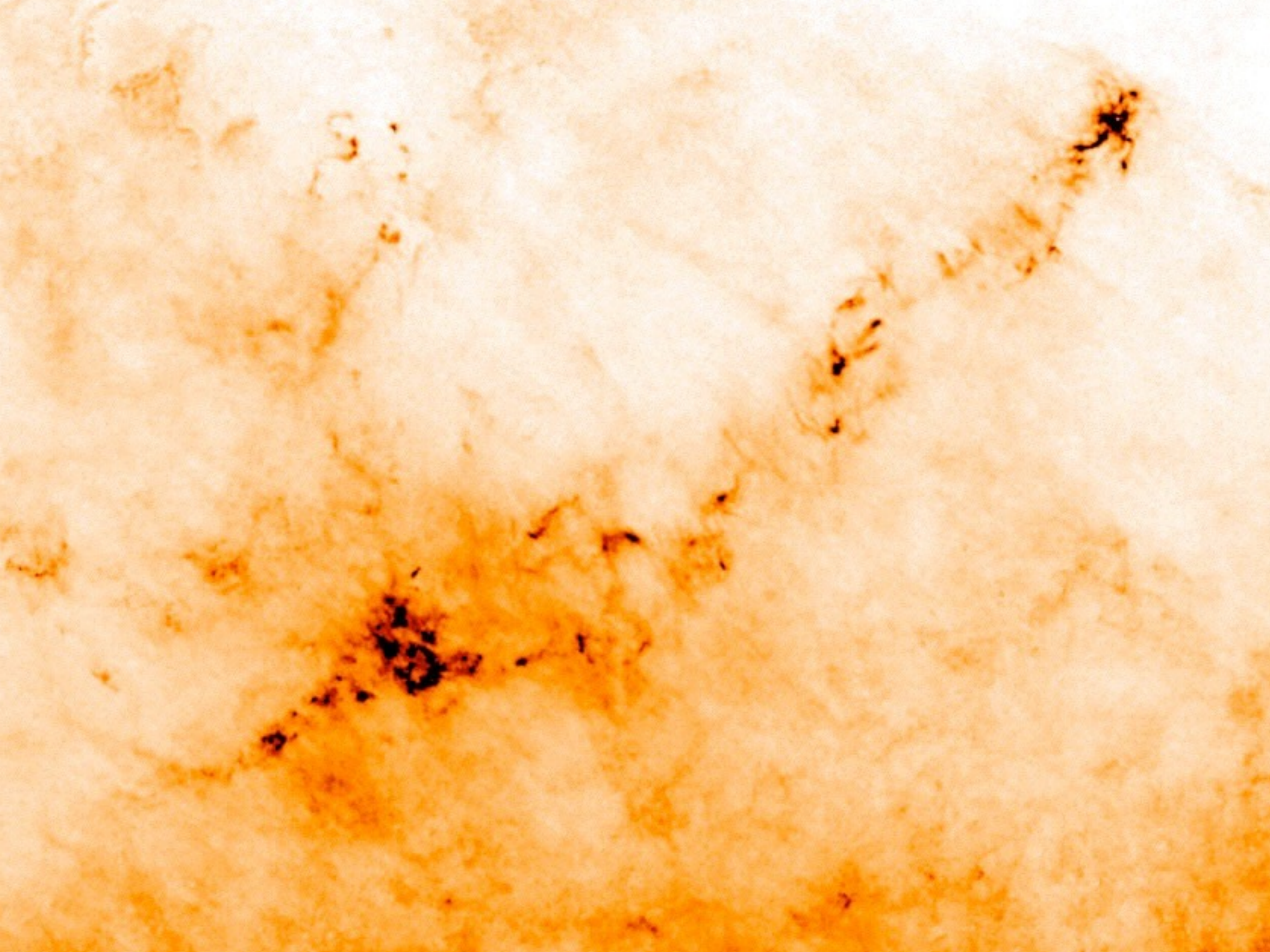
The Pipe Nebula

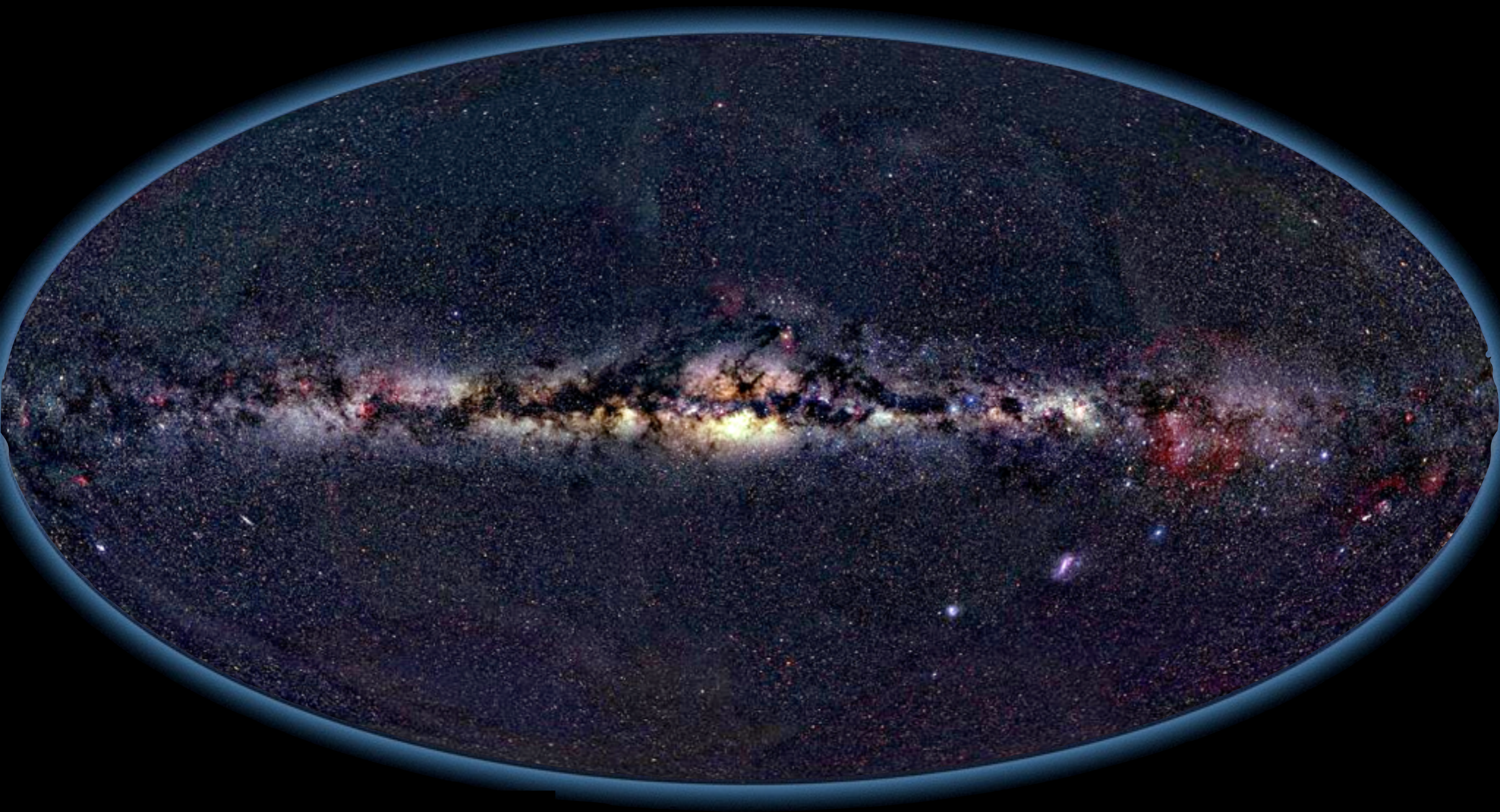


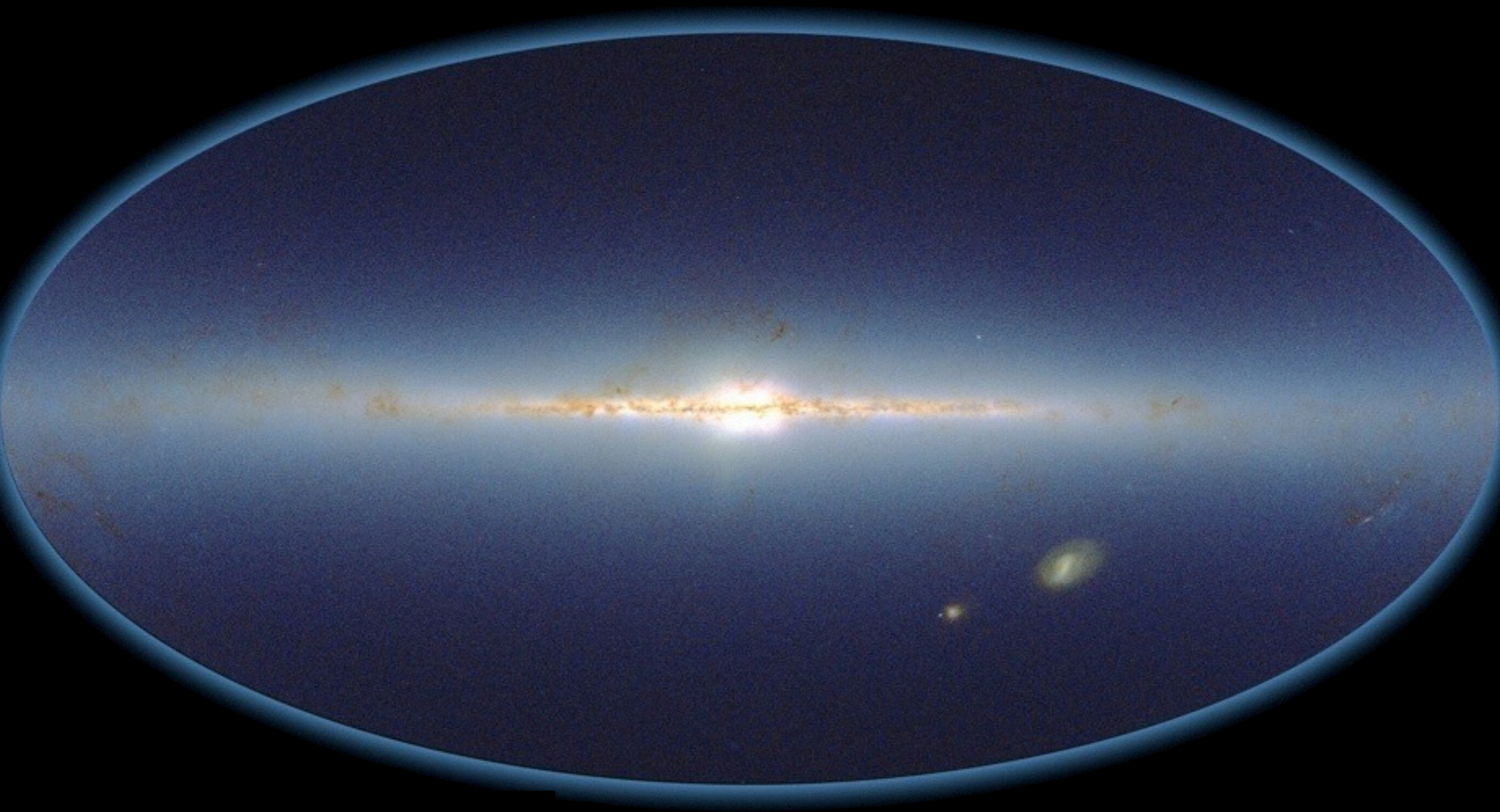
The Pipe Nebula

Extinction map



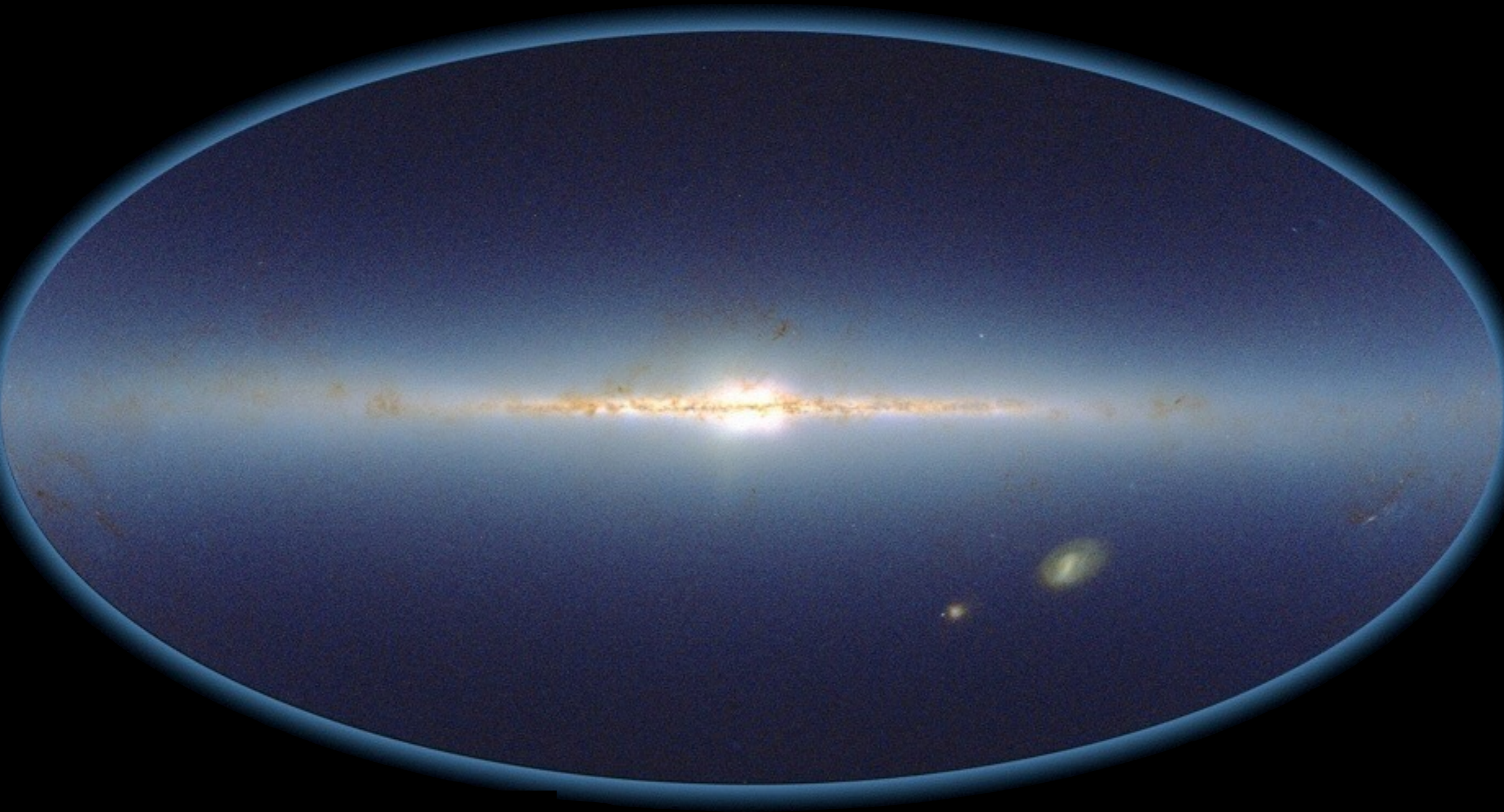




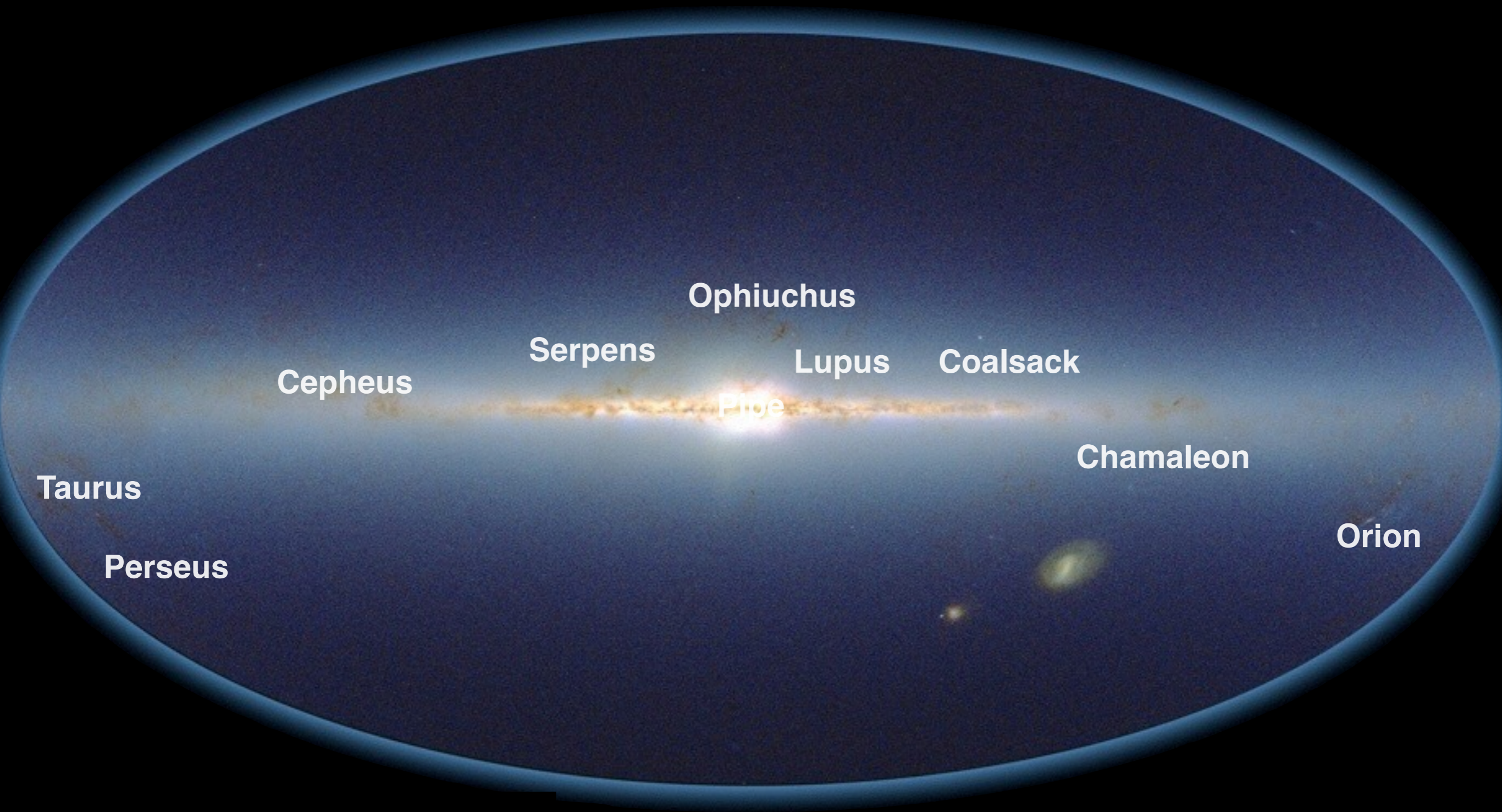


2MASS

Gould belt



Gould belt



Taurus

Perseus

Cepheus

Serpens

Ophiuchus

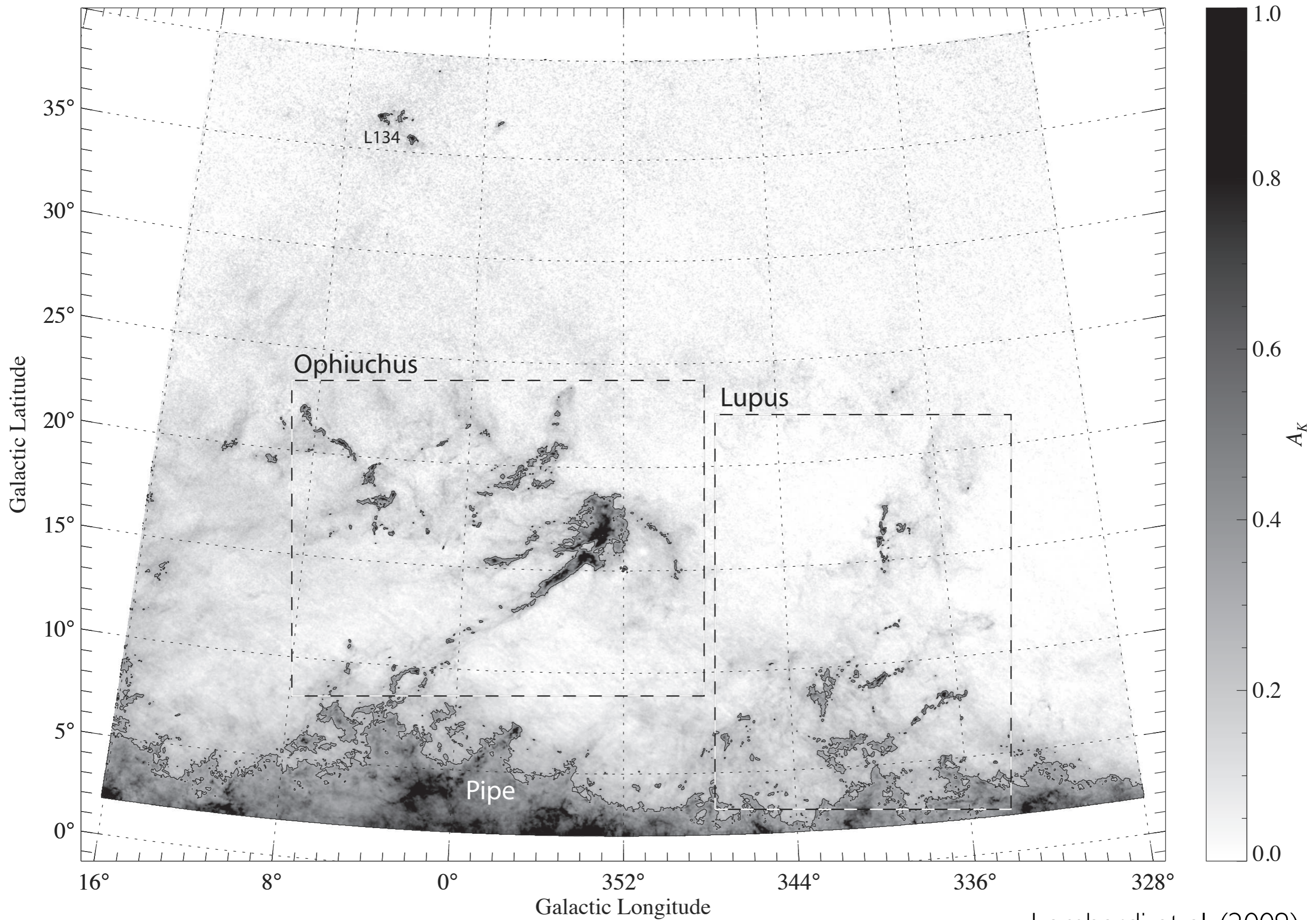
Pipe

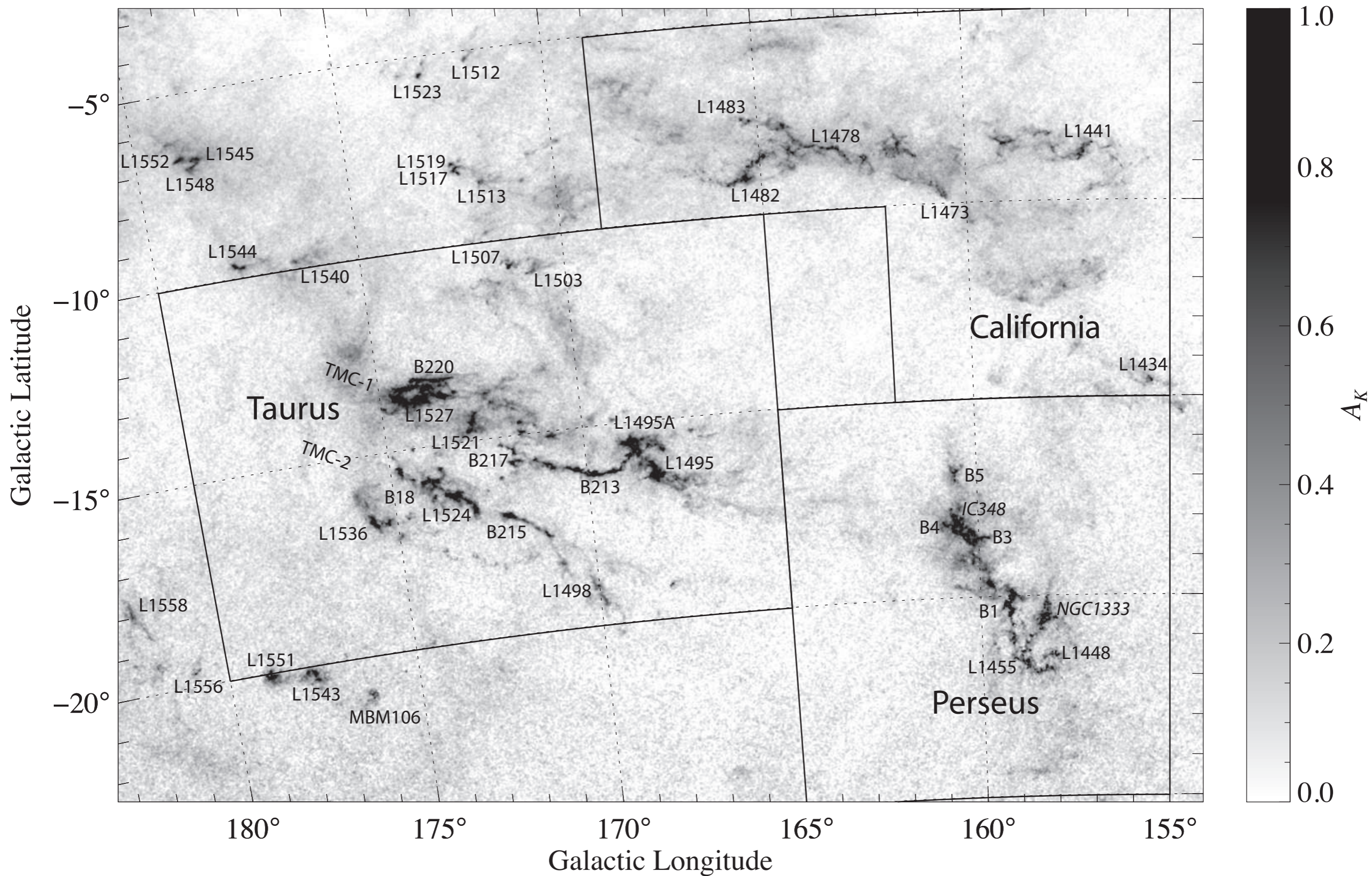
Lupus

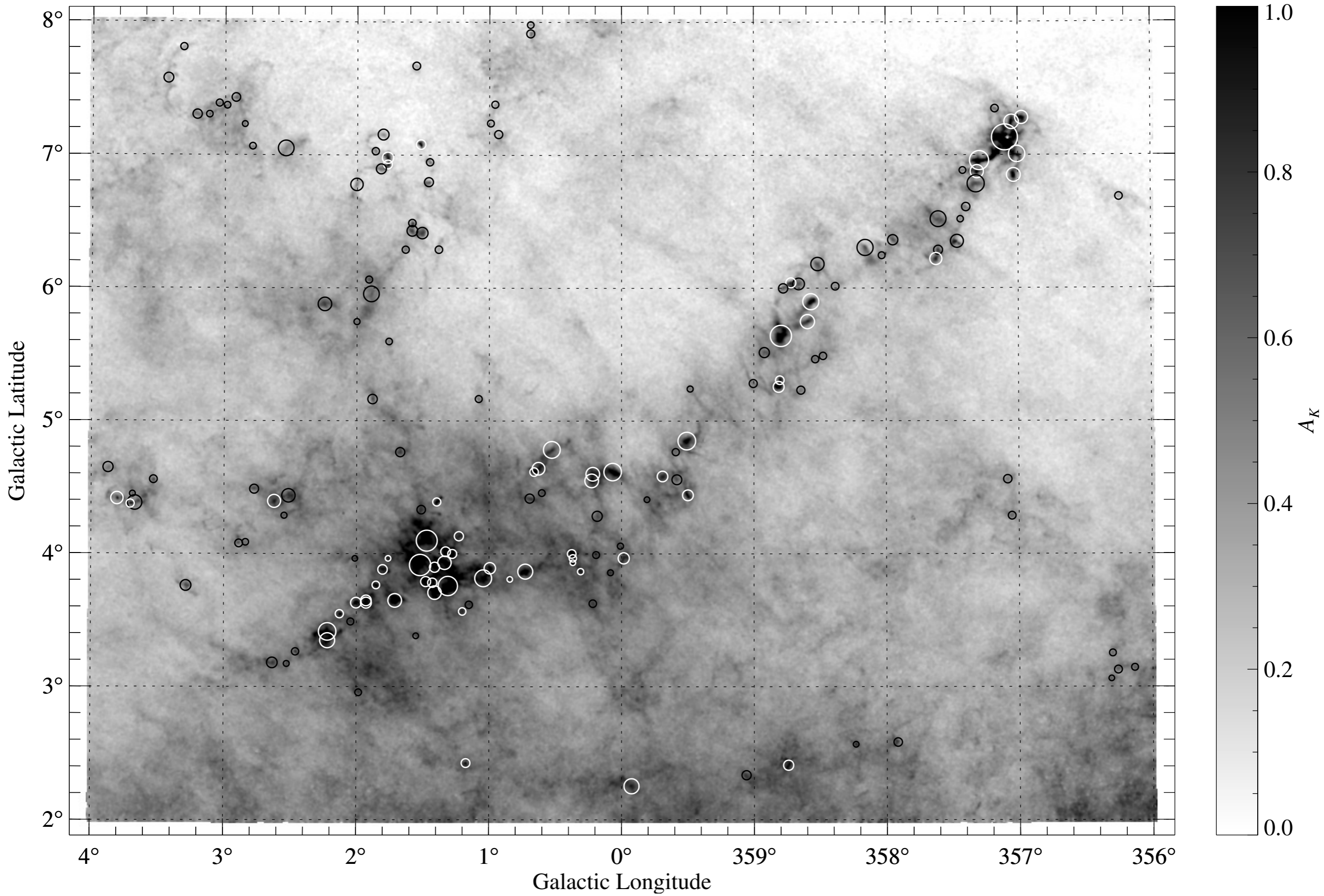
Coalsack

Chamaleon

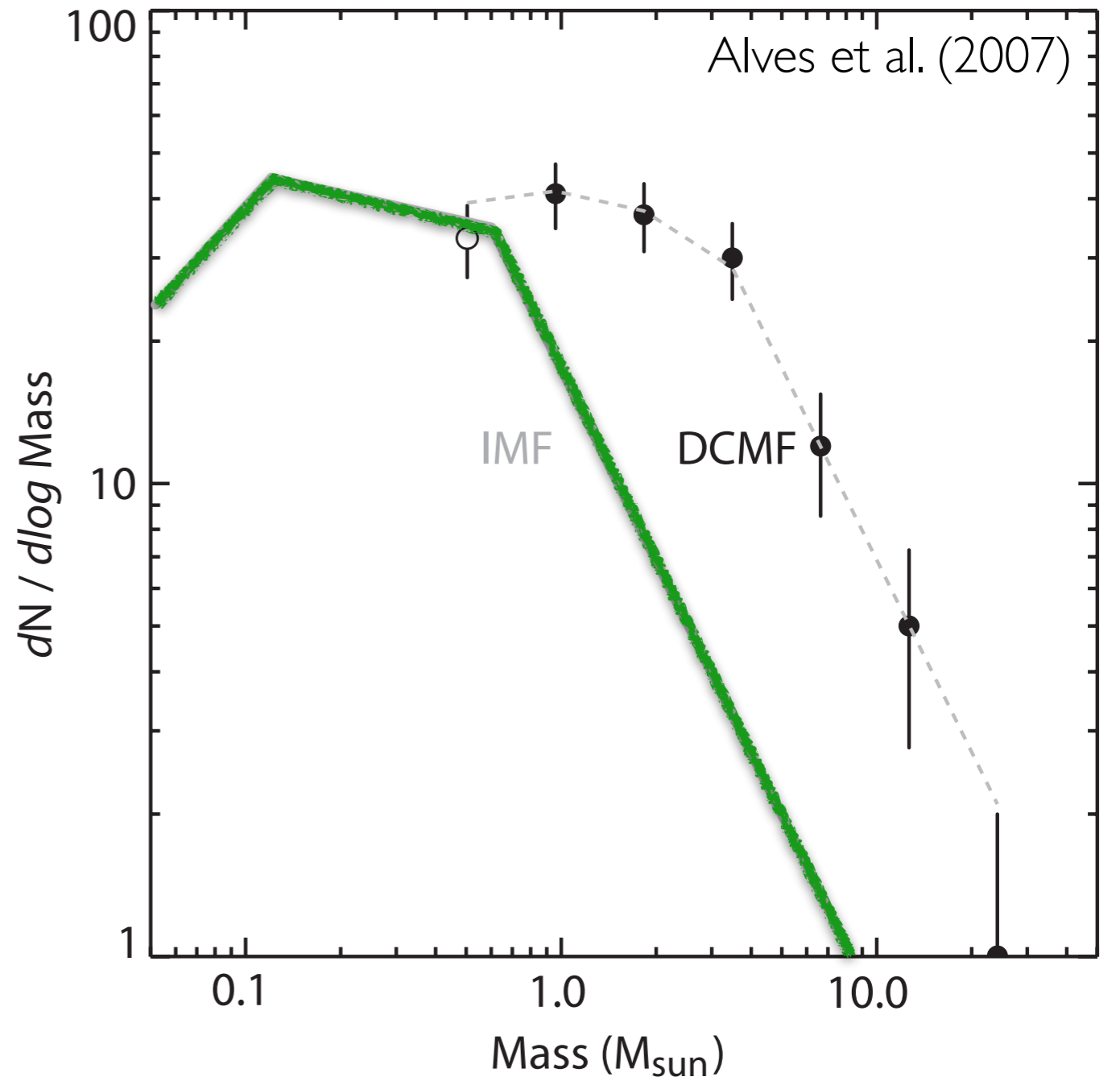
Orion



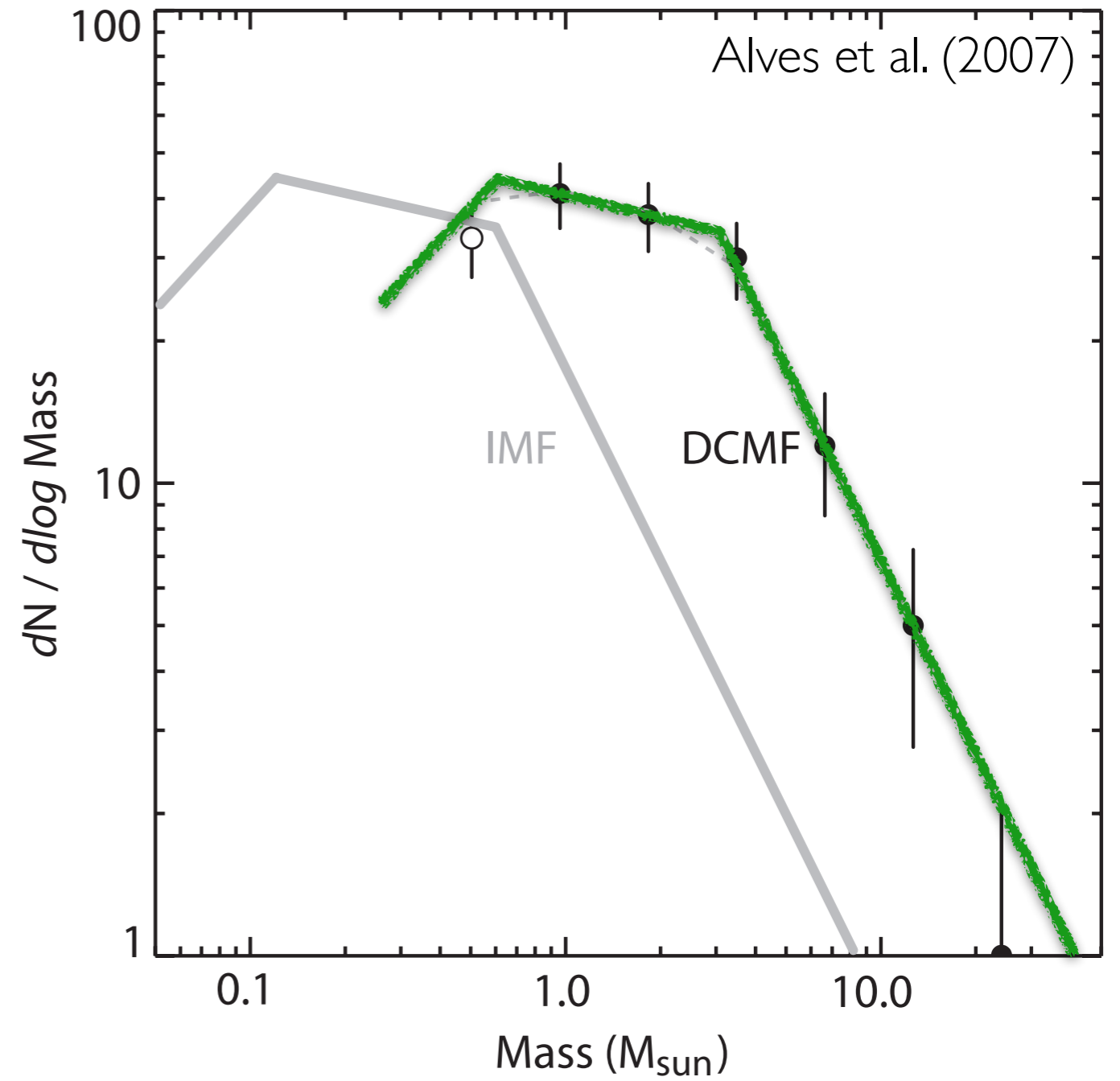




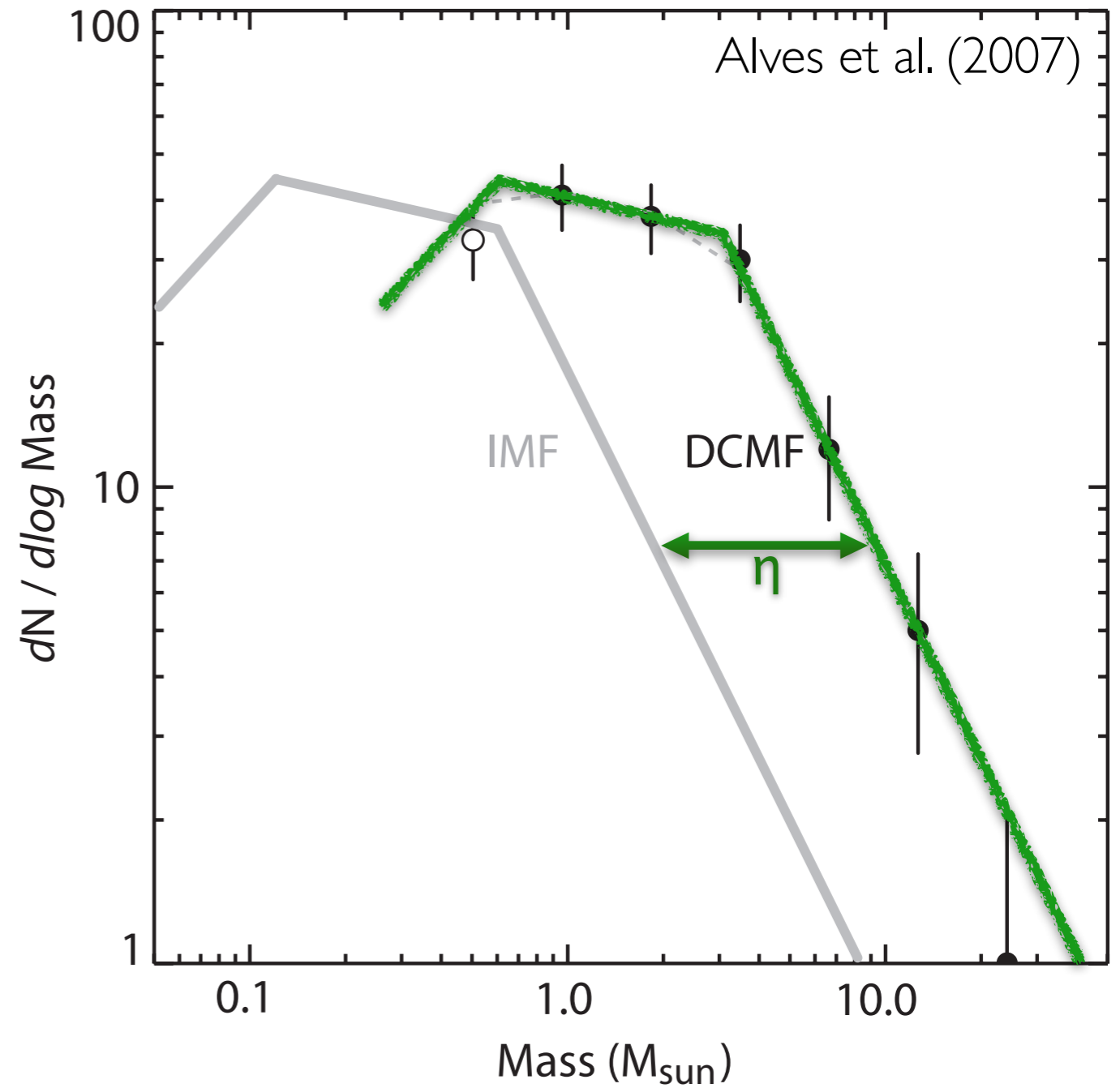
Alves et al. (2007)



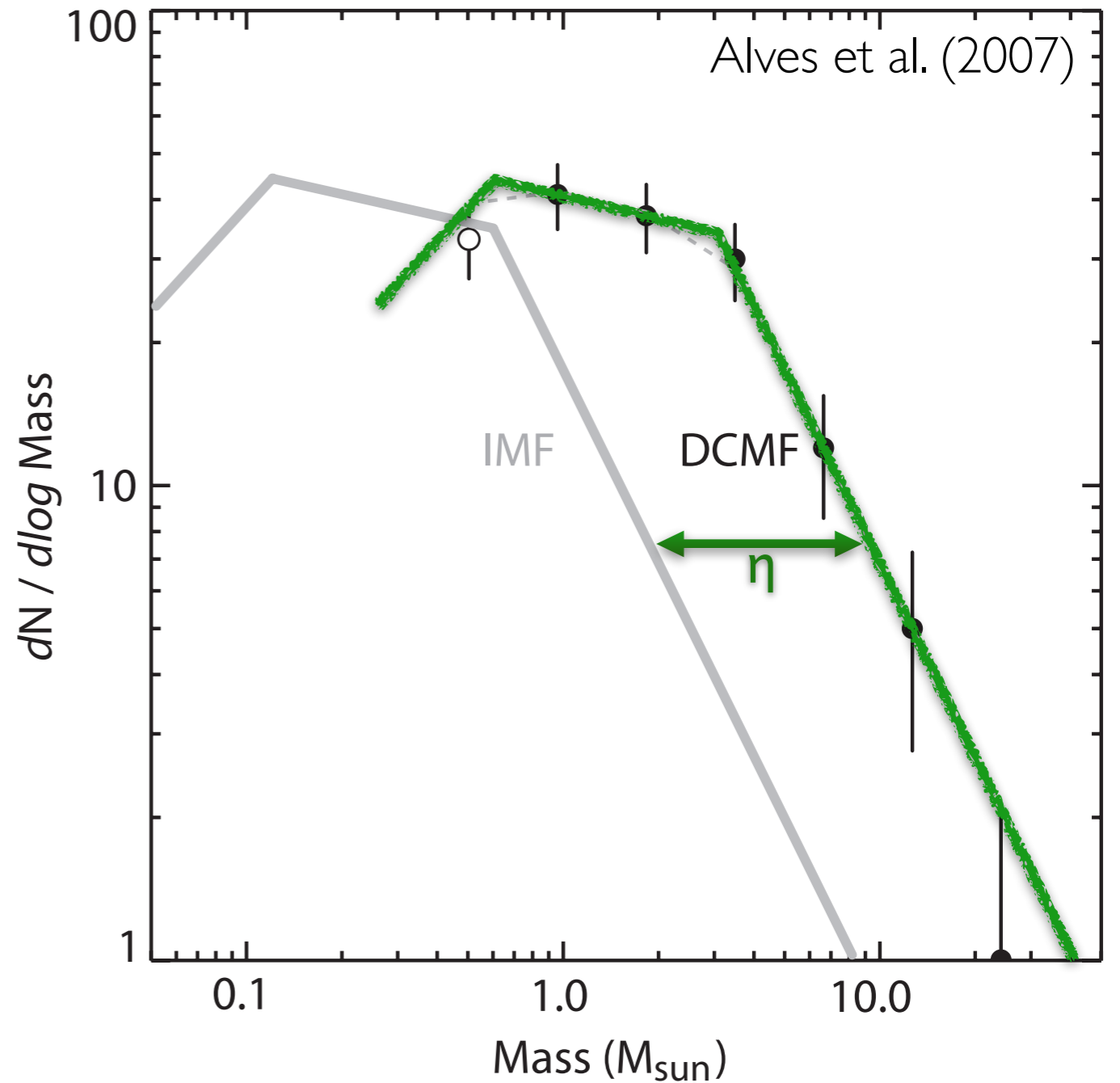
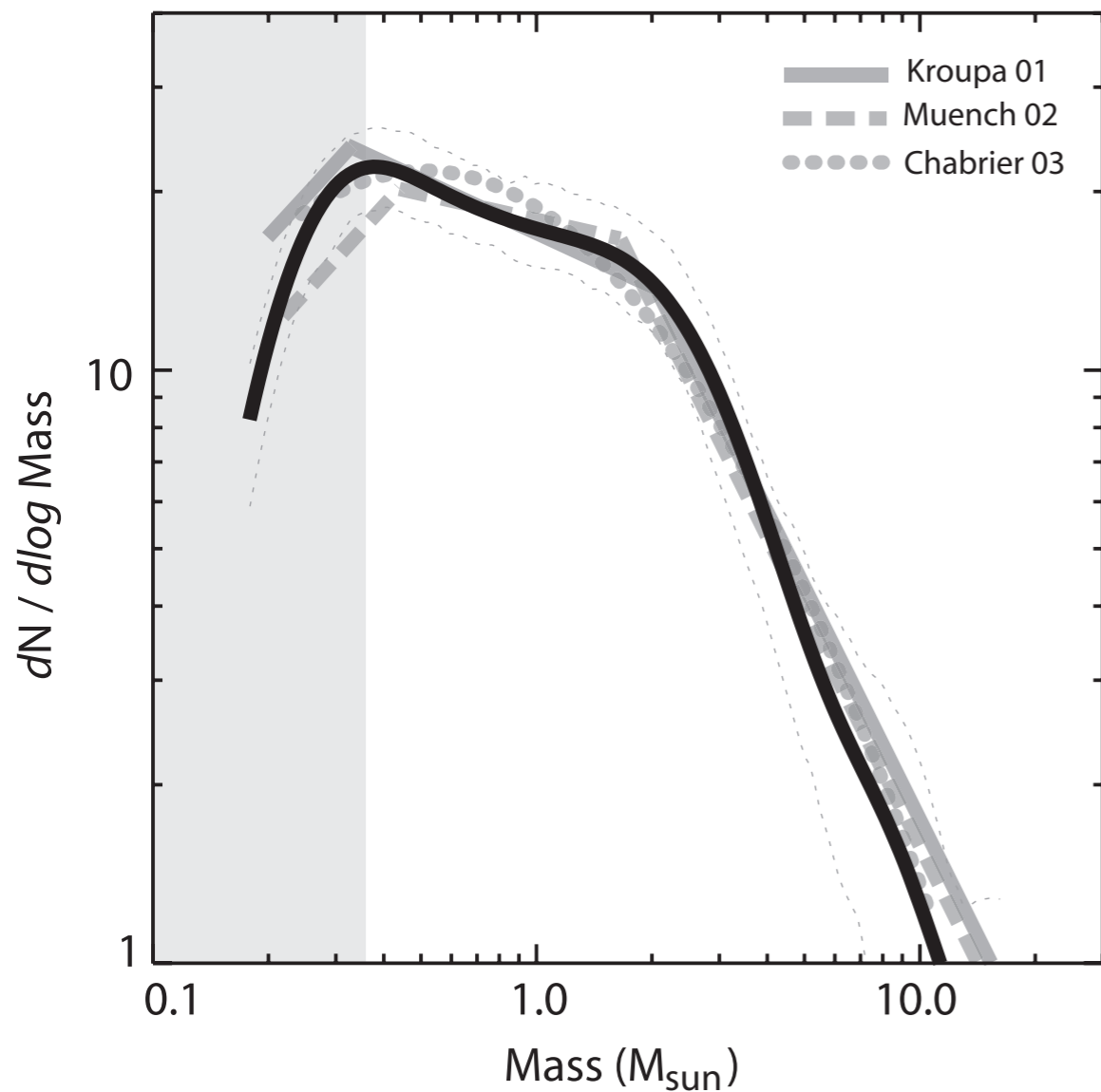
- The dense core mass function (DCMF) has the same shape as the IMF



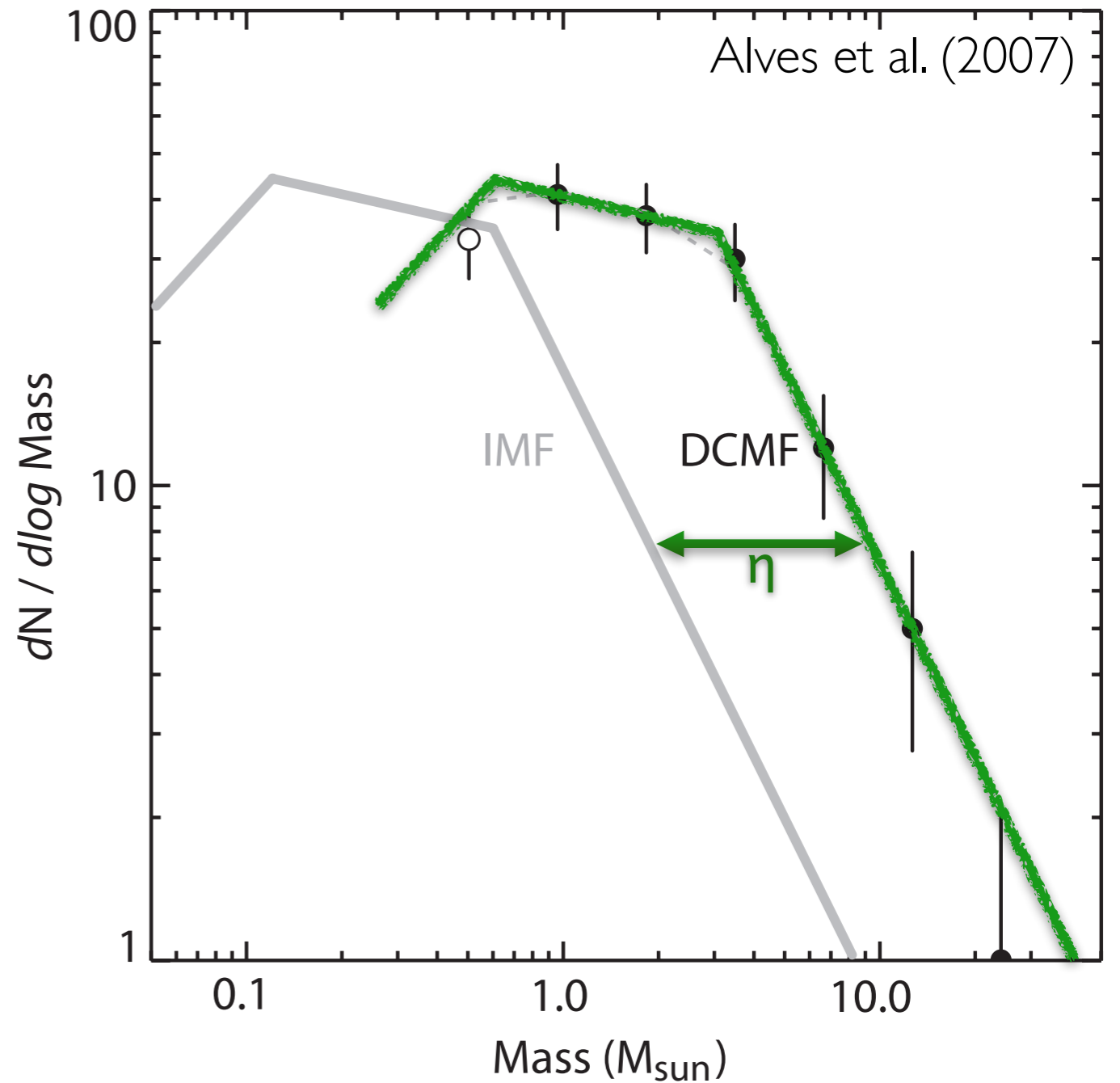
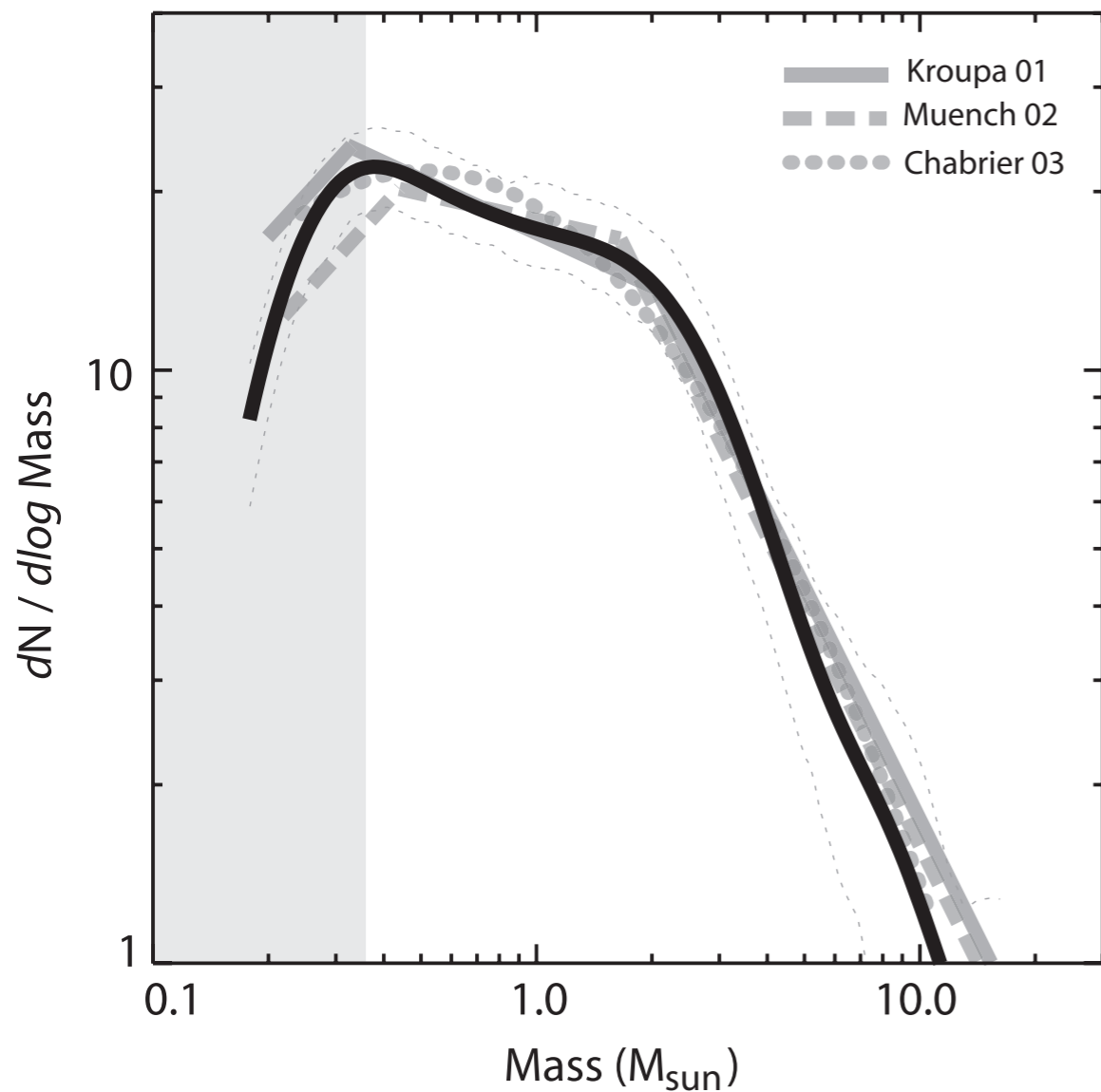
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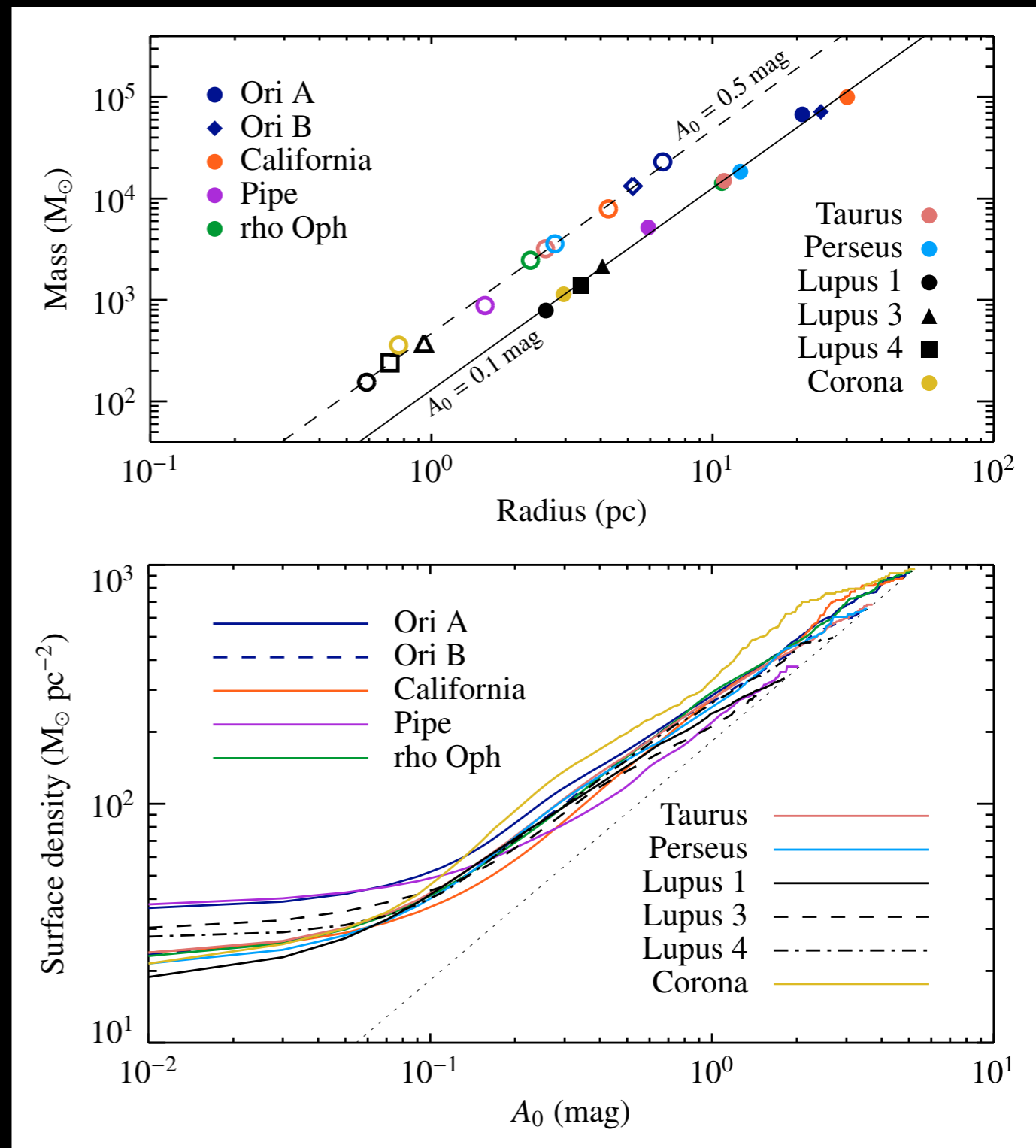


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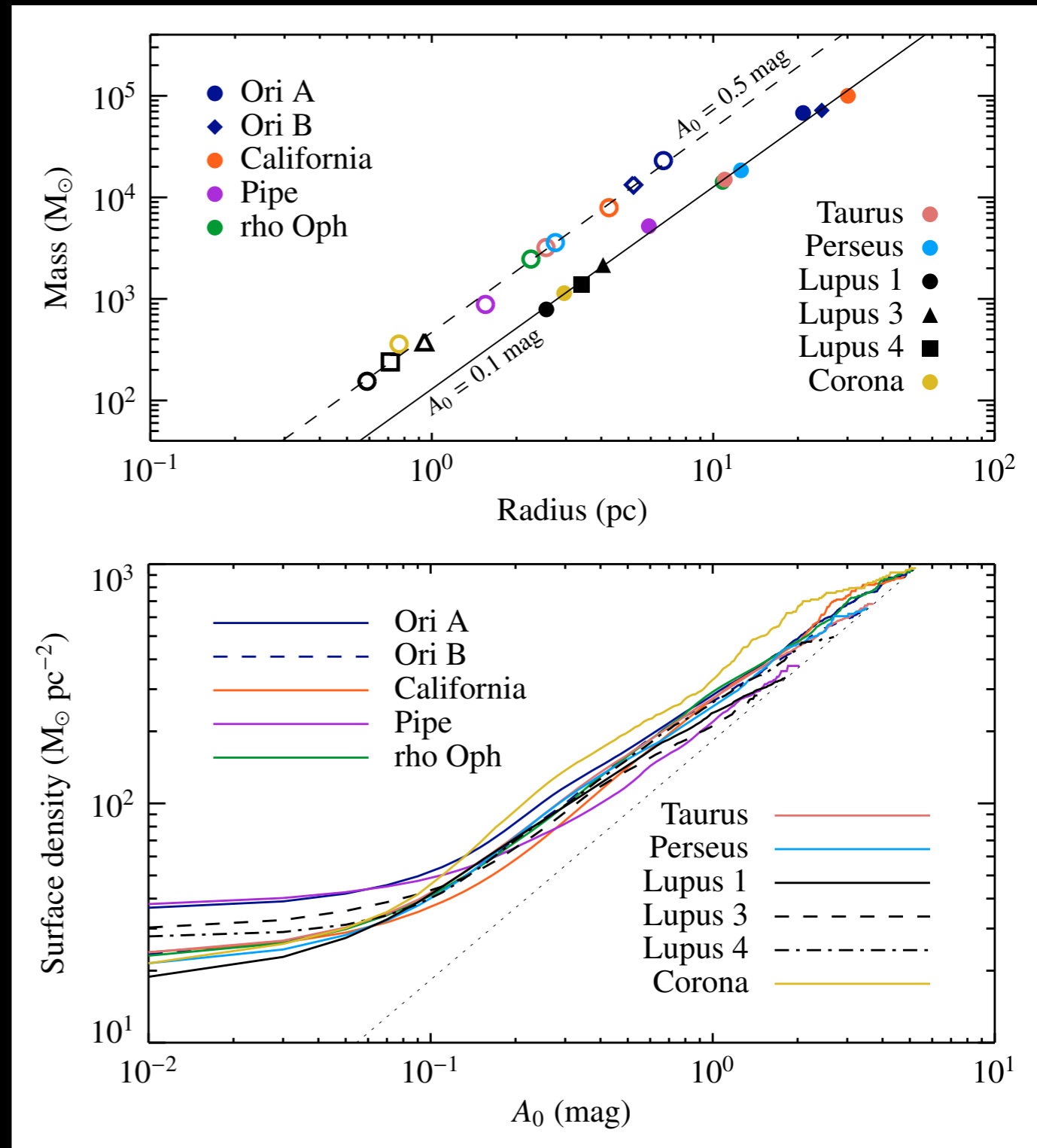
- Things might be more complicated (e.g., one core might fragment)

Larson's 3rd law



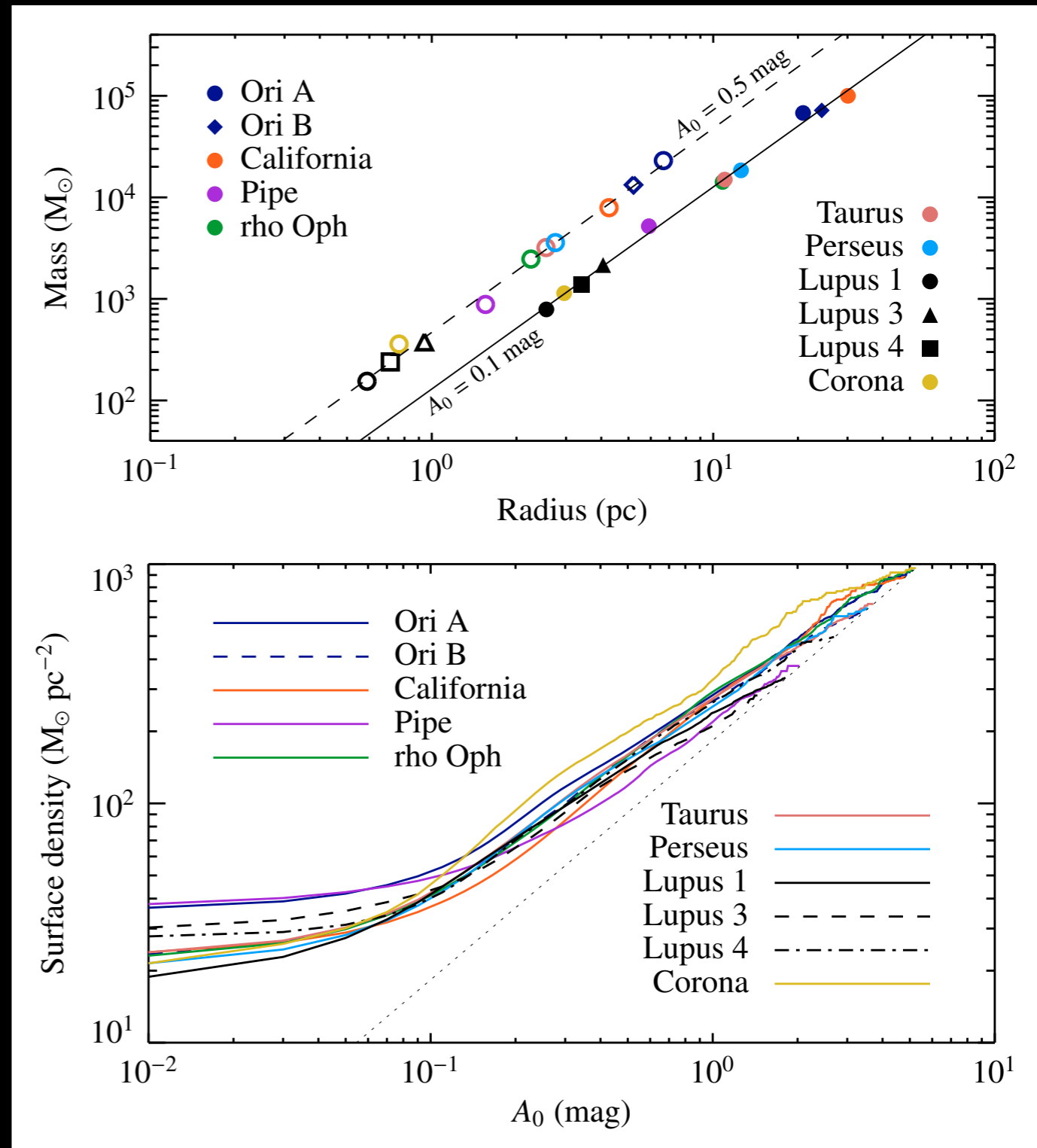
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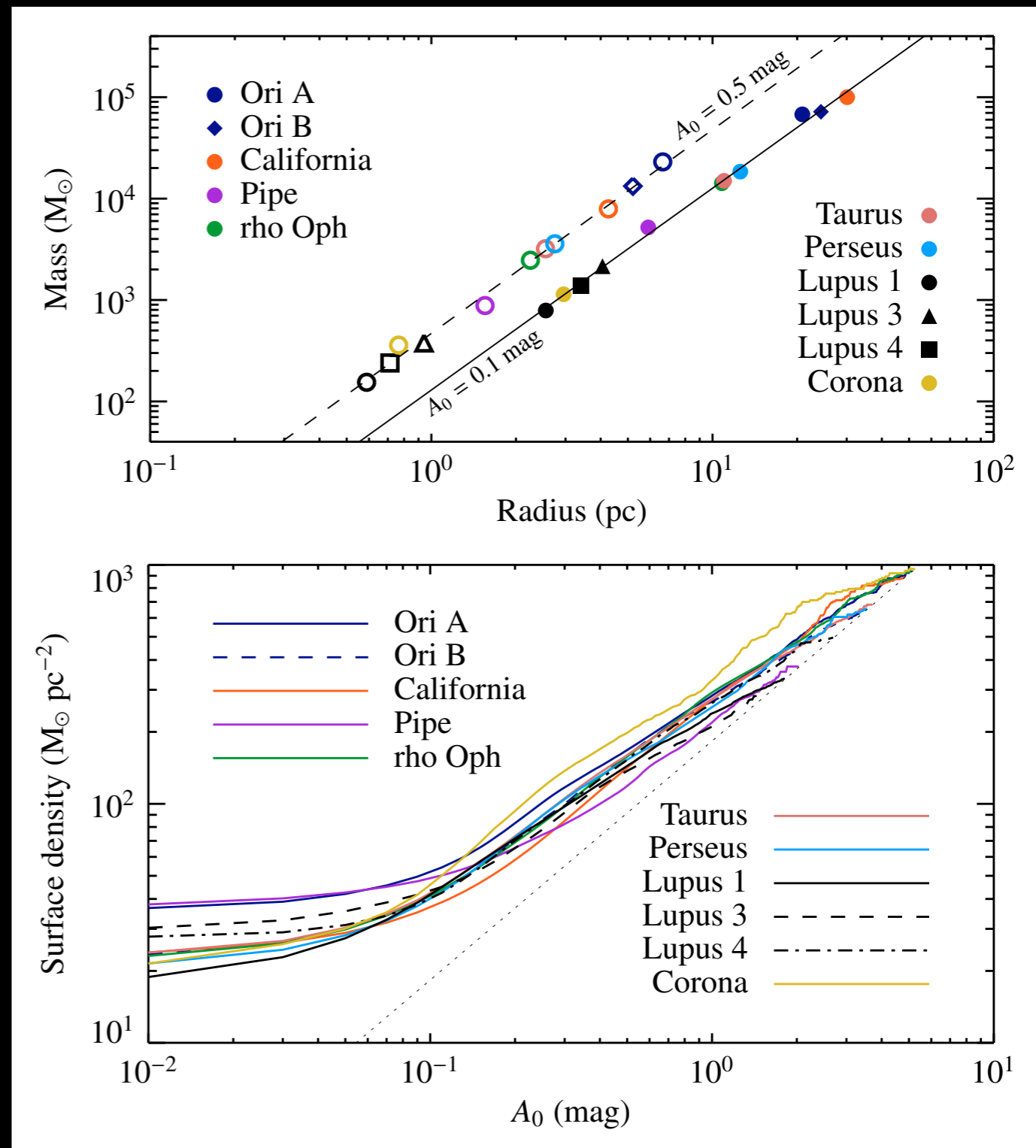


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- All this is related to the PDF for column densities

$$S(A_0) = S_{\text{tot}} \int_{A_0}^{\infty} p(A) dA$$

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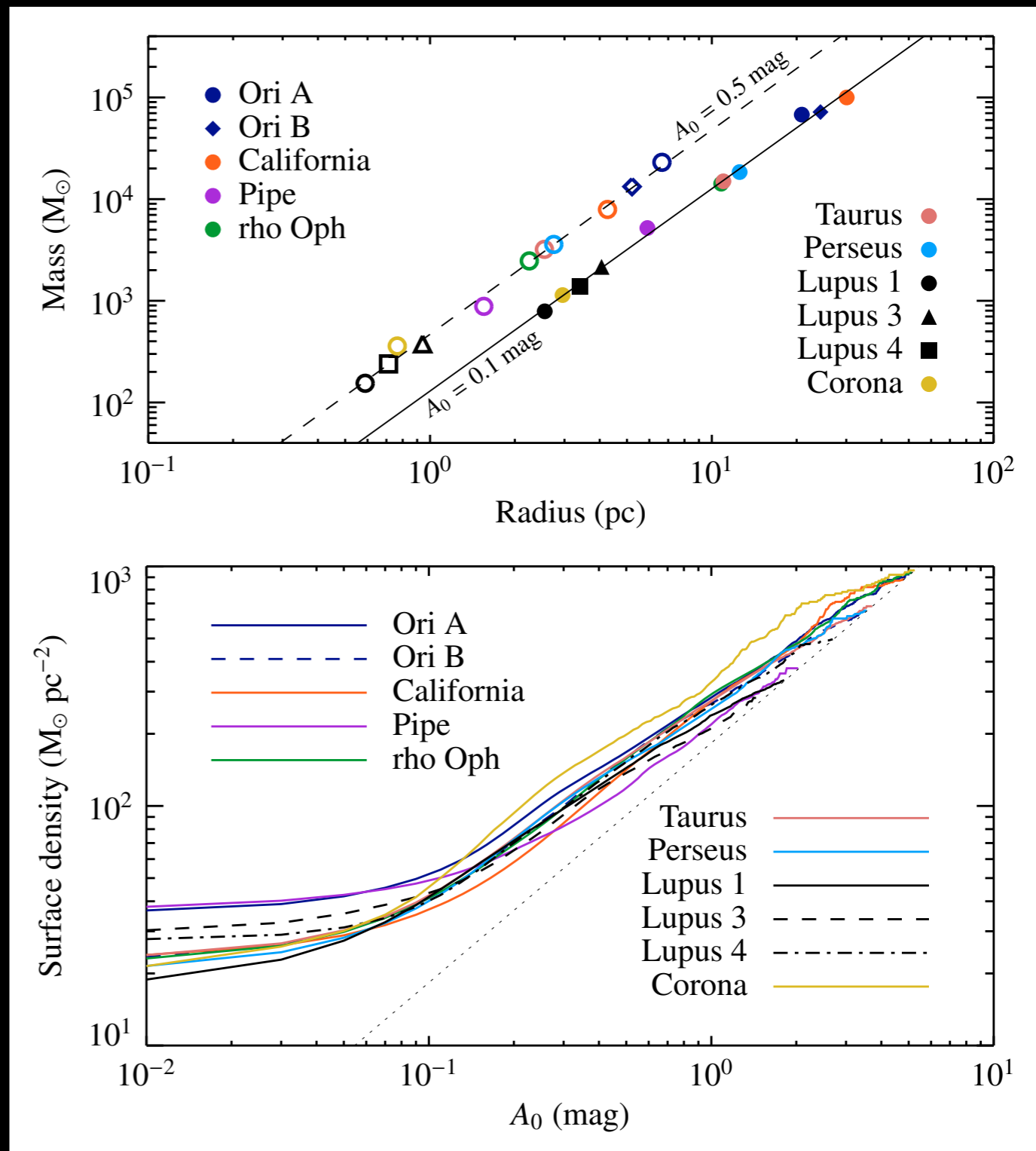
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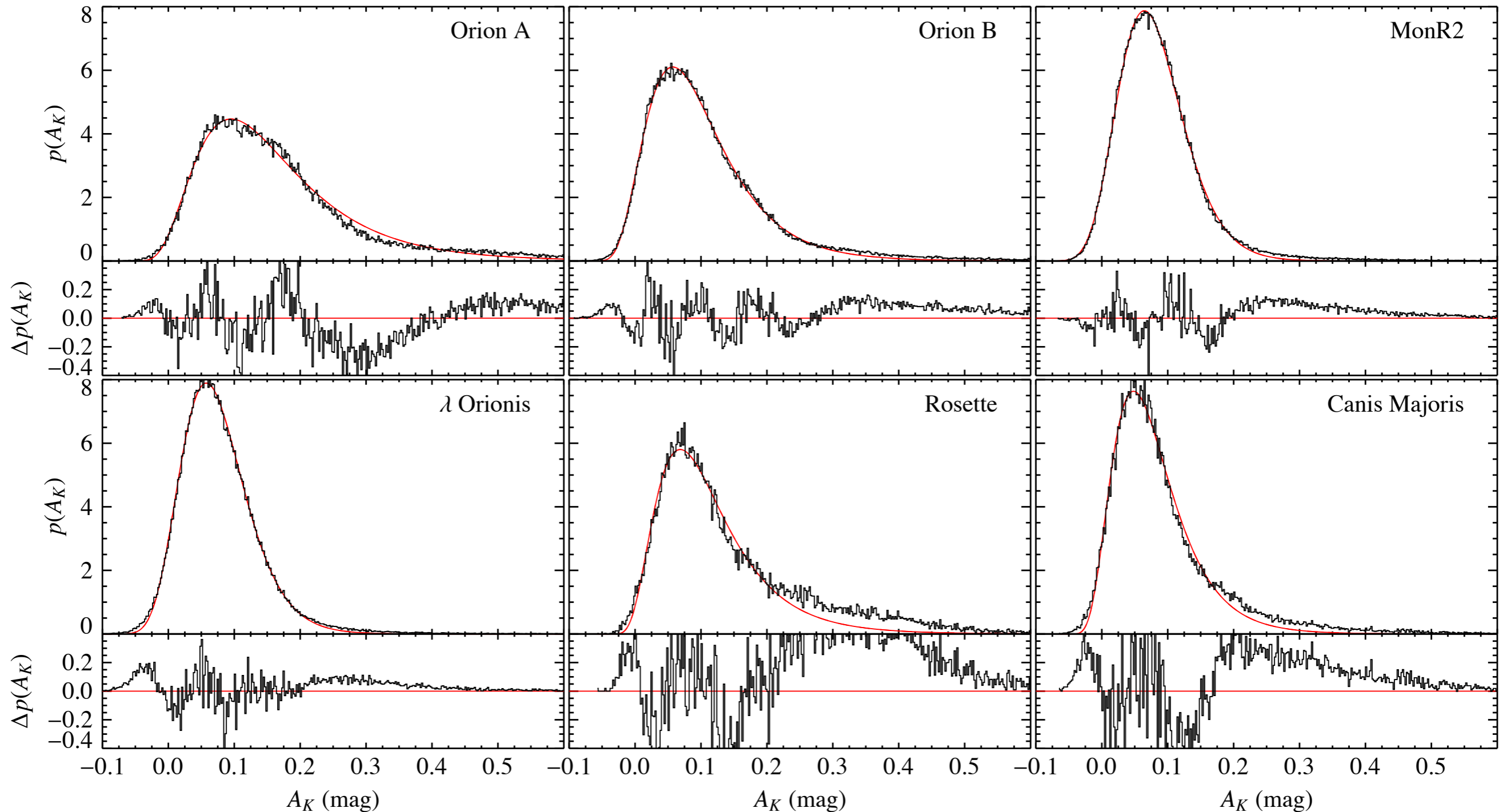
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- Makes sense to study the PDF of molecular clouds



Log-normal fits to cloud projected density distributions



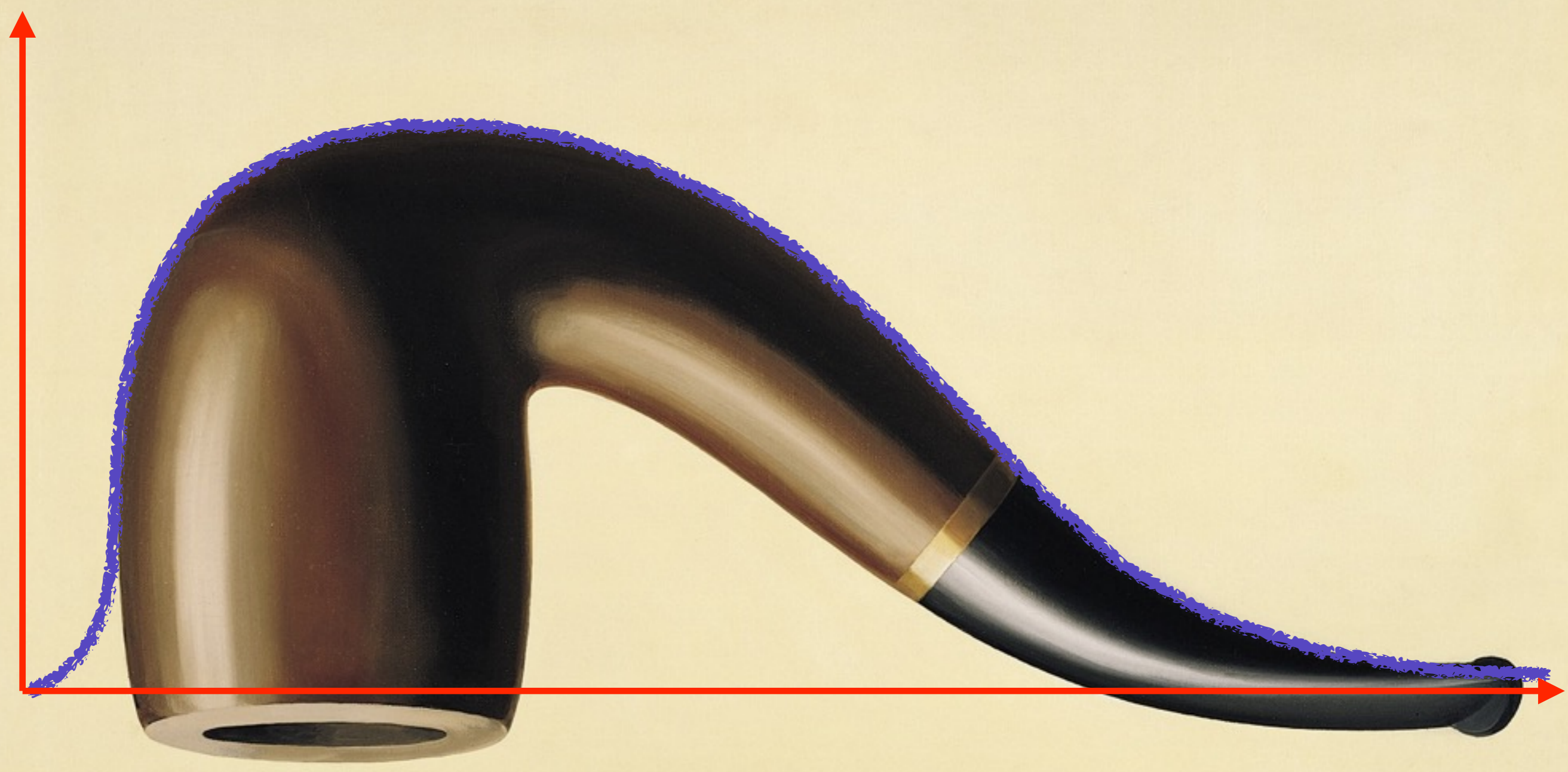


Ceci n'est pas une pipe.

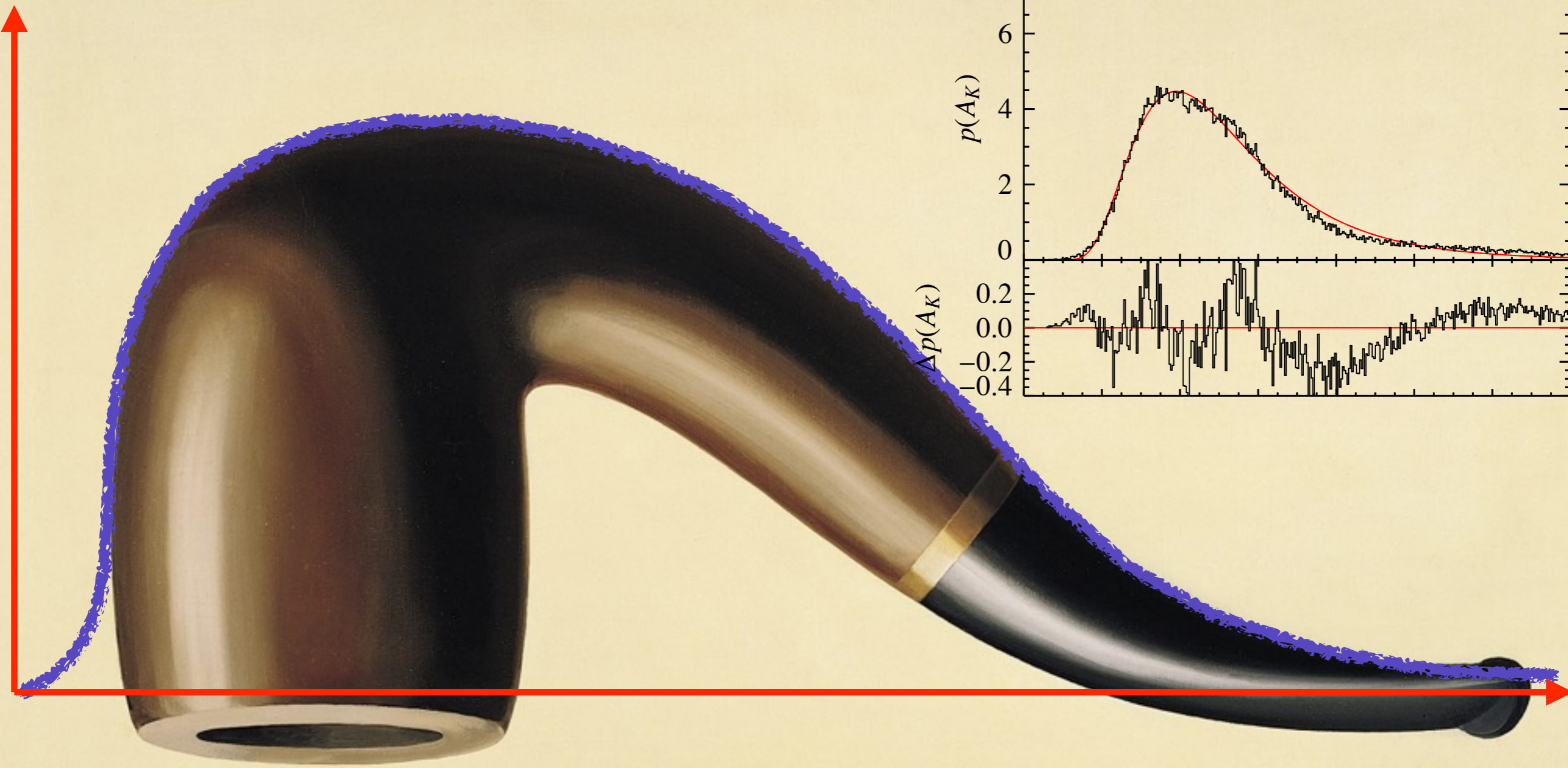
Ceci n'est pas une log-normale.



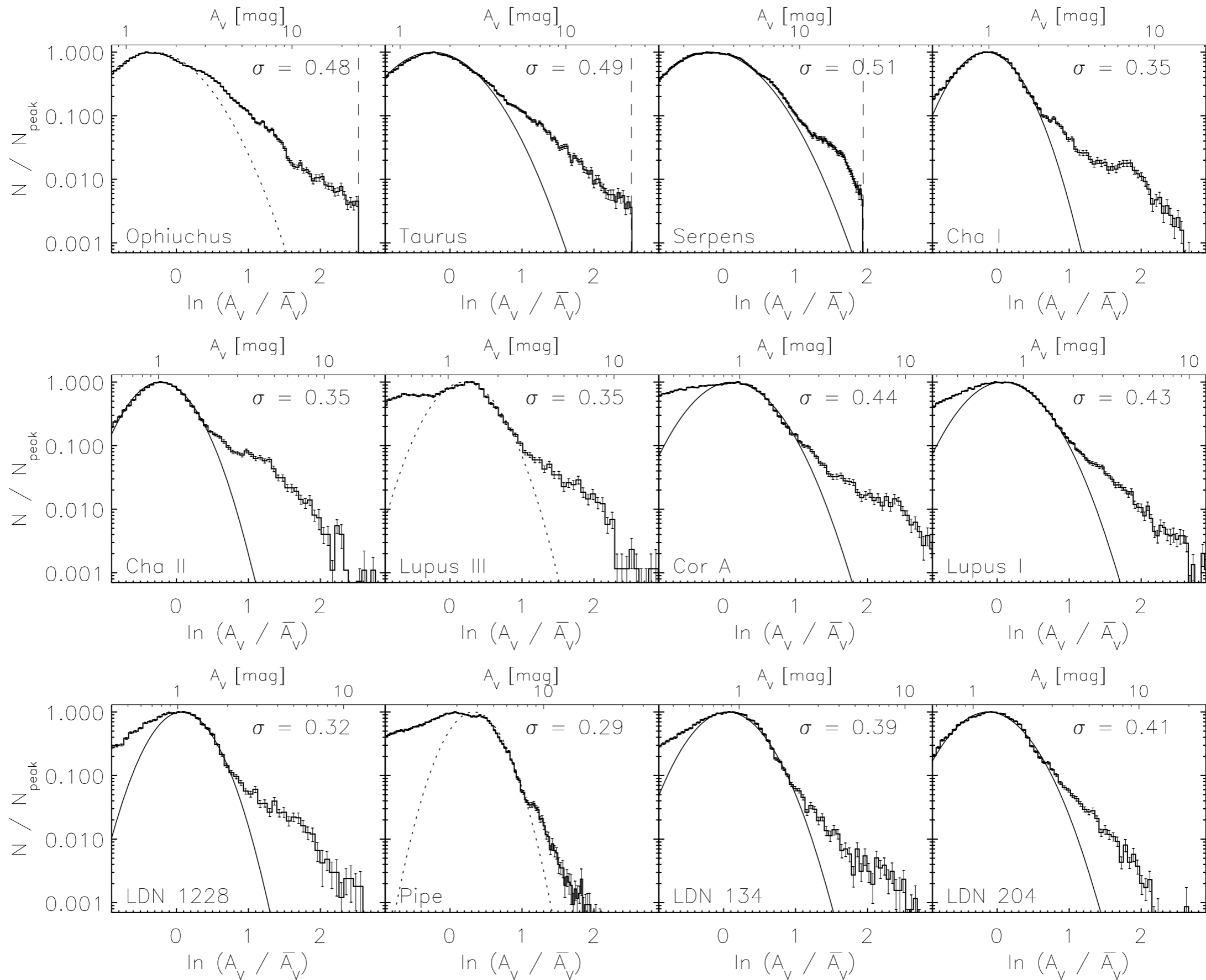
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Log-normals everywhere!



Kainulainen et al. (2009; see also 2014)

Why we like log-normals

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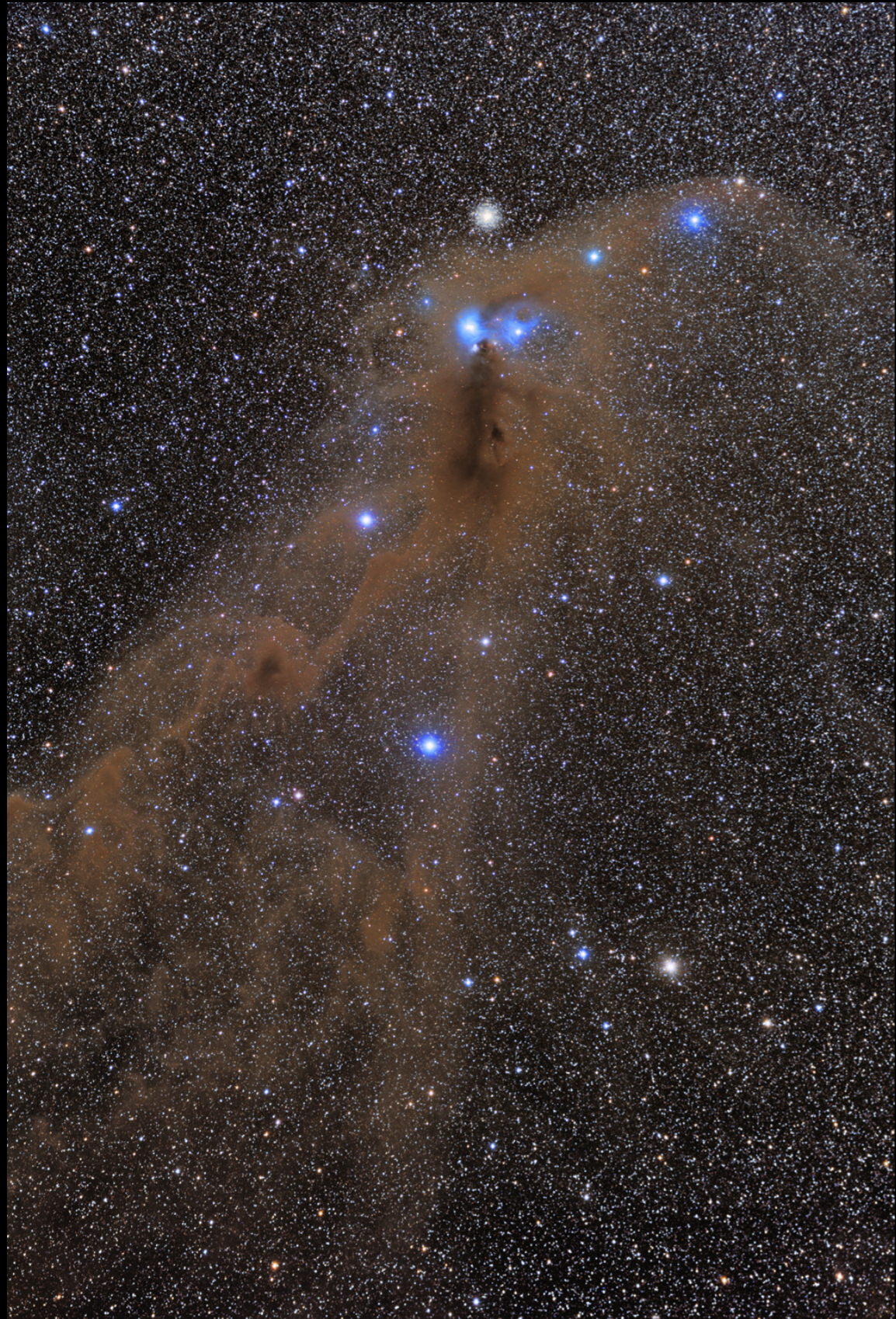
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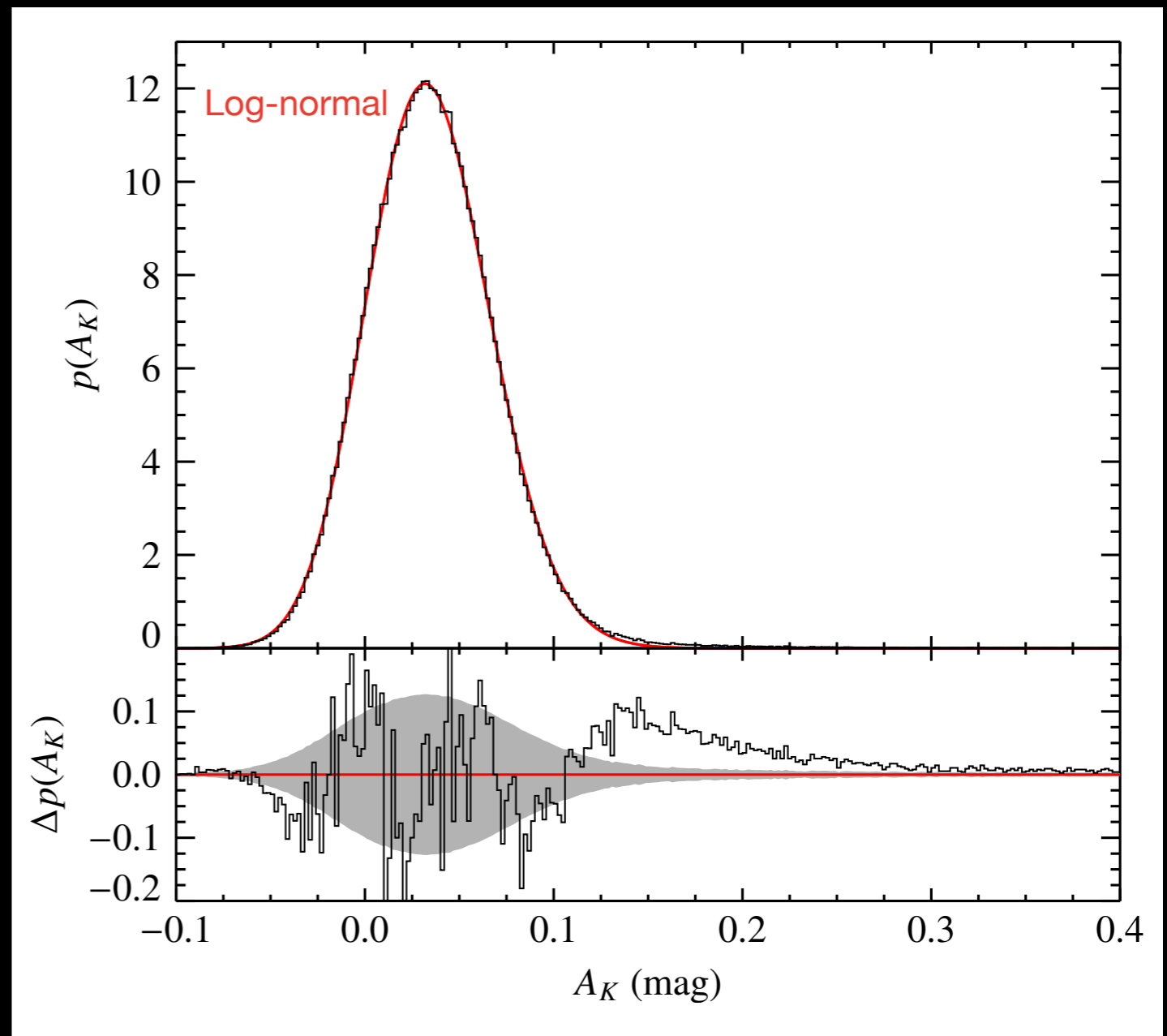
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- Projection effects (in most cases...) do not significantly alter this expectation (Vázquez-Semadeni & García 2001)



The end of a dream

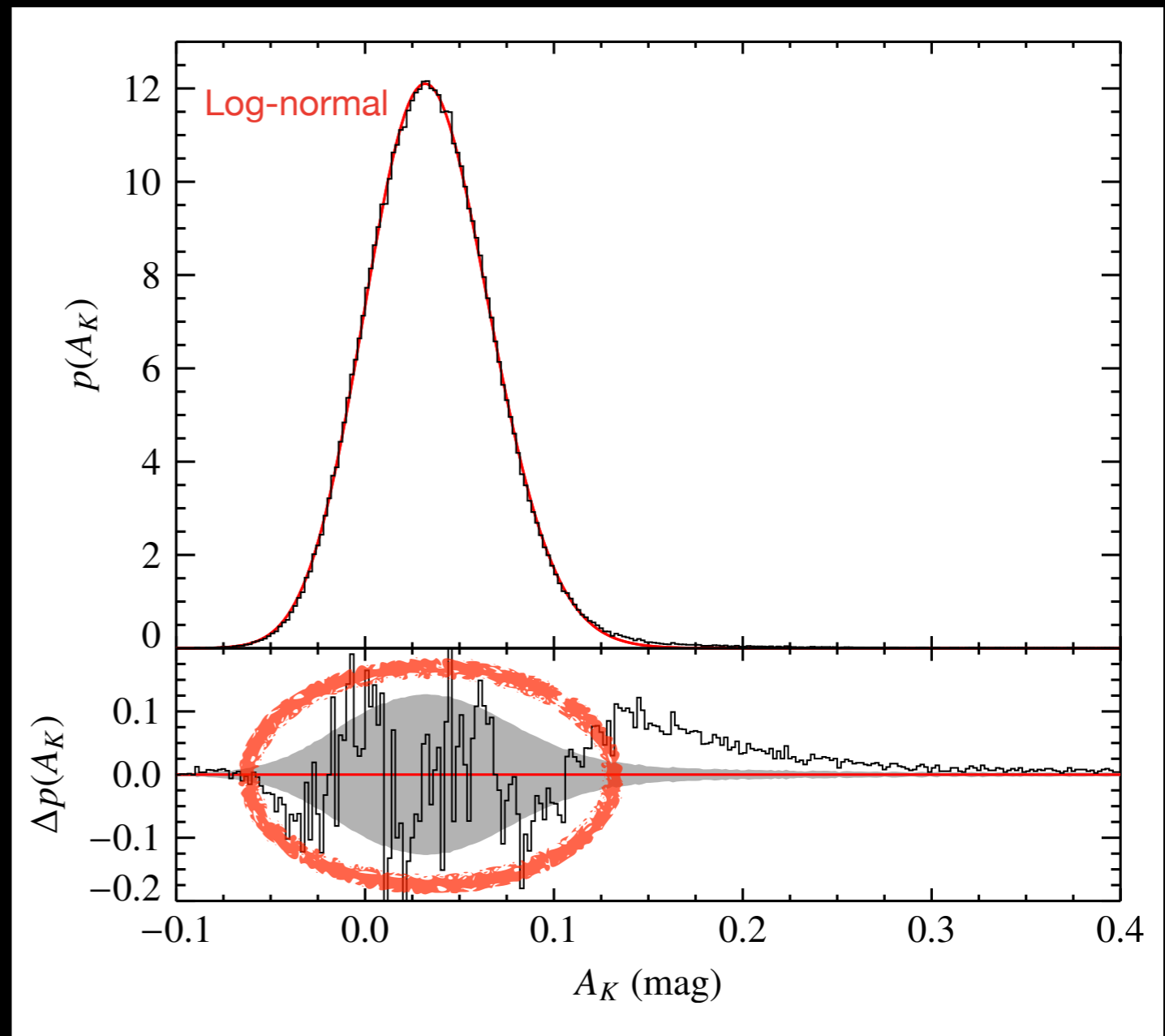


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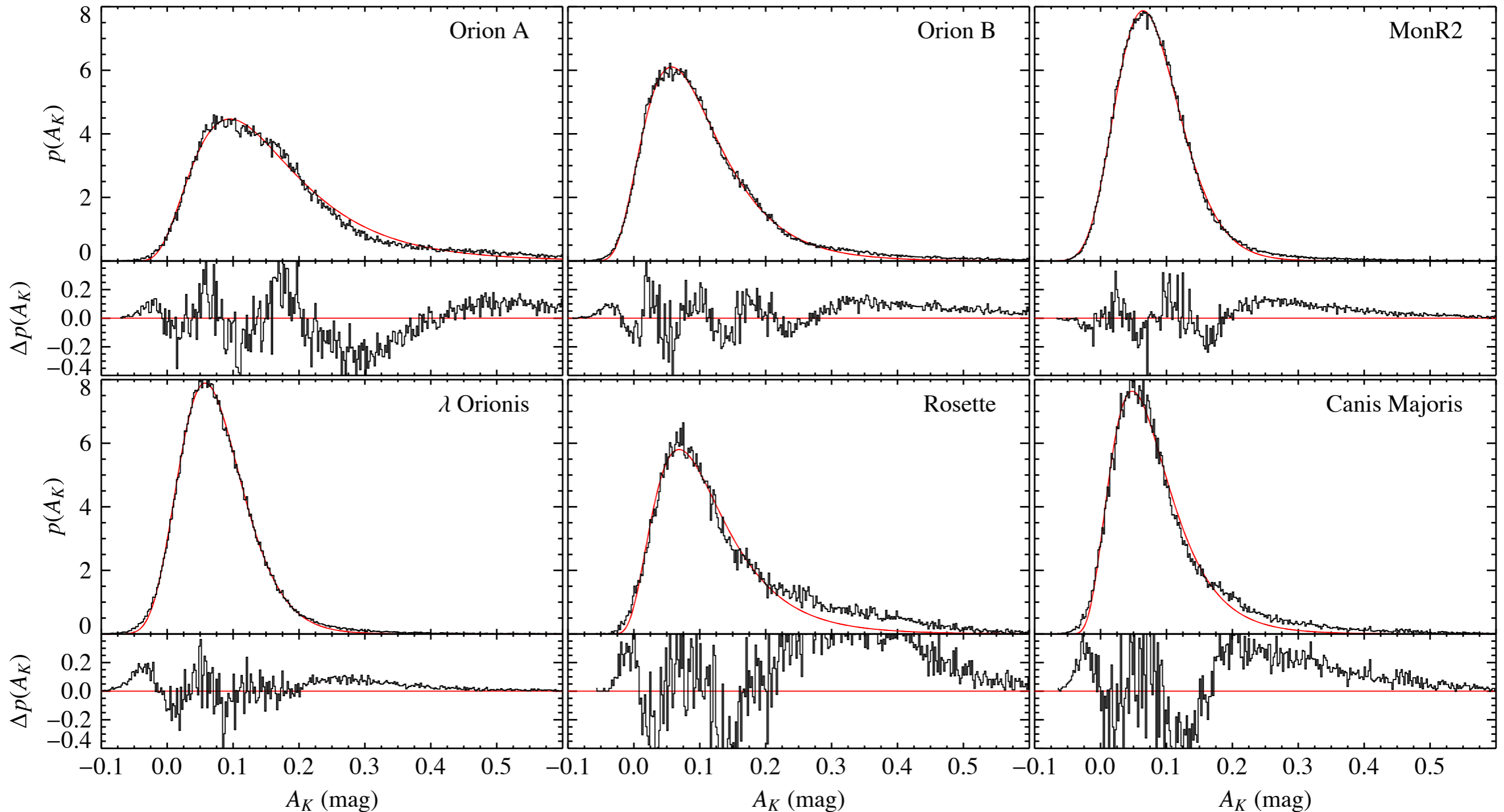
Systematic residuals in the entire fitting region!

The end of a dream

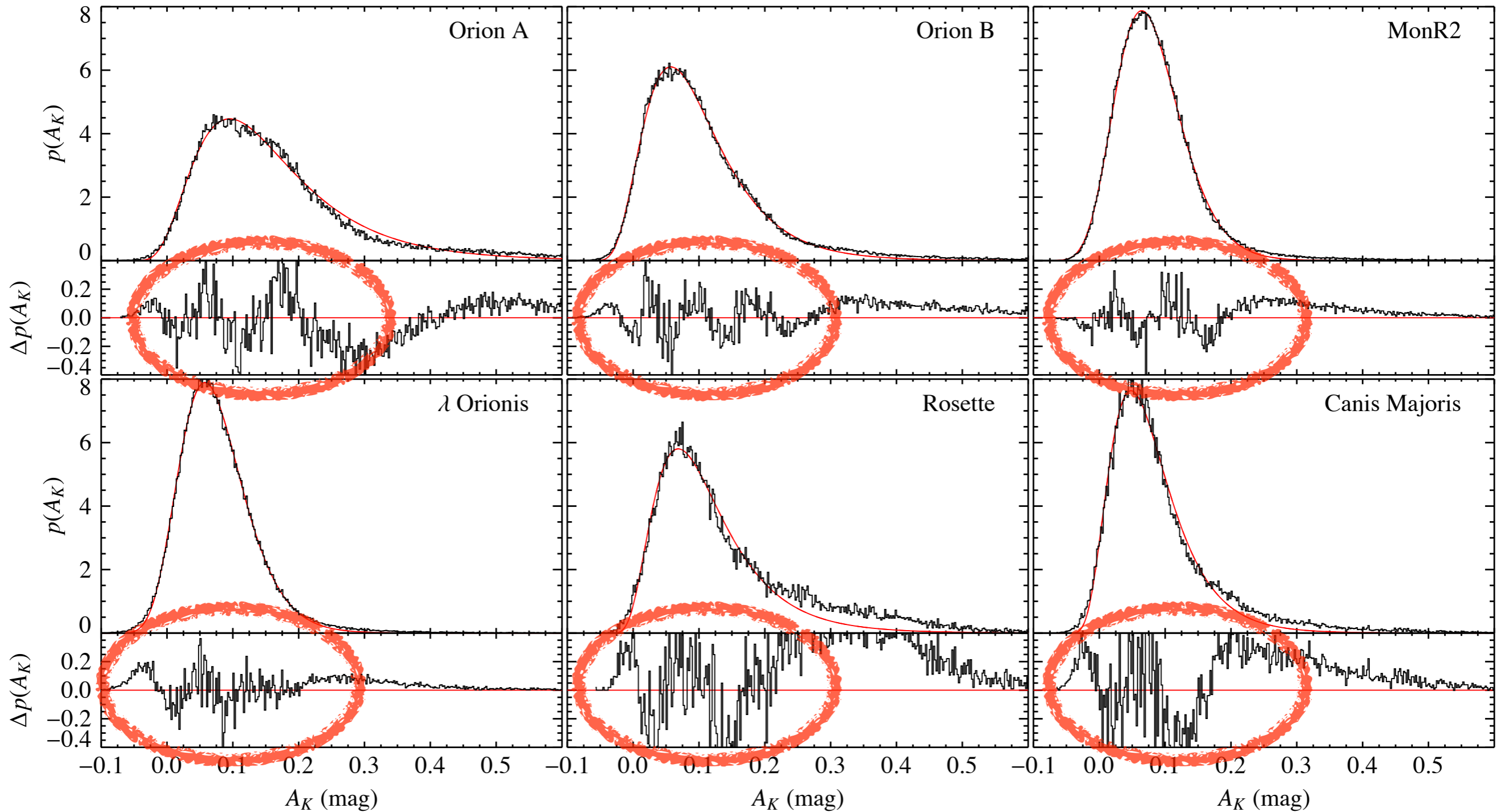


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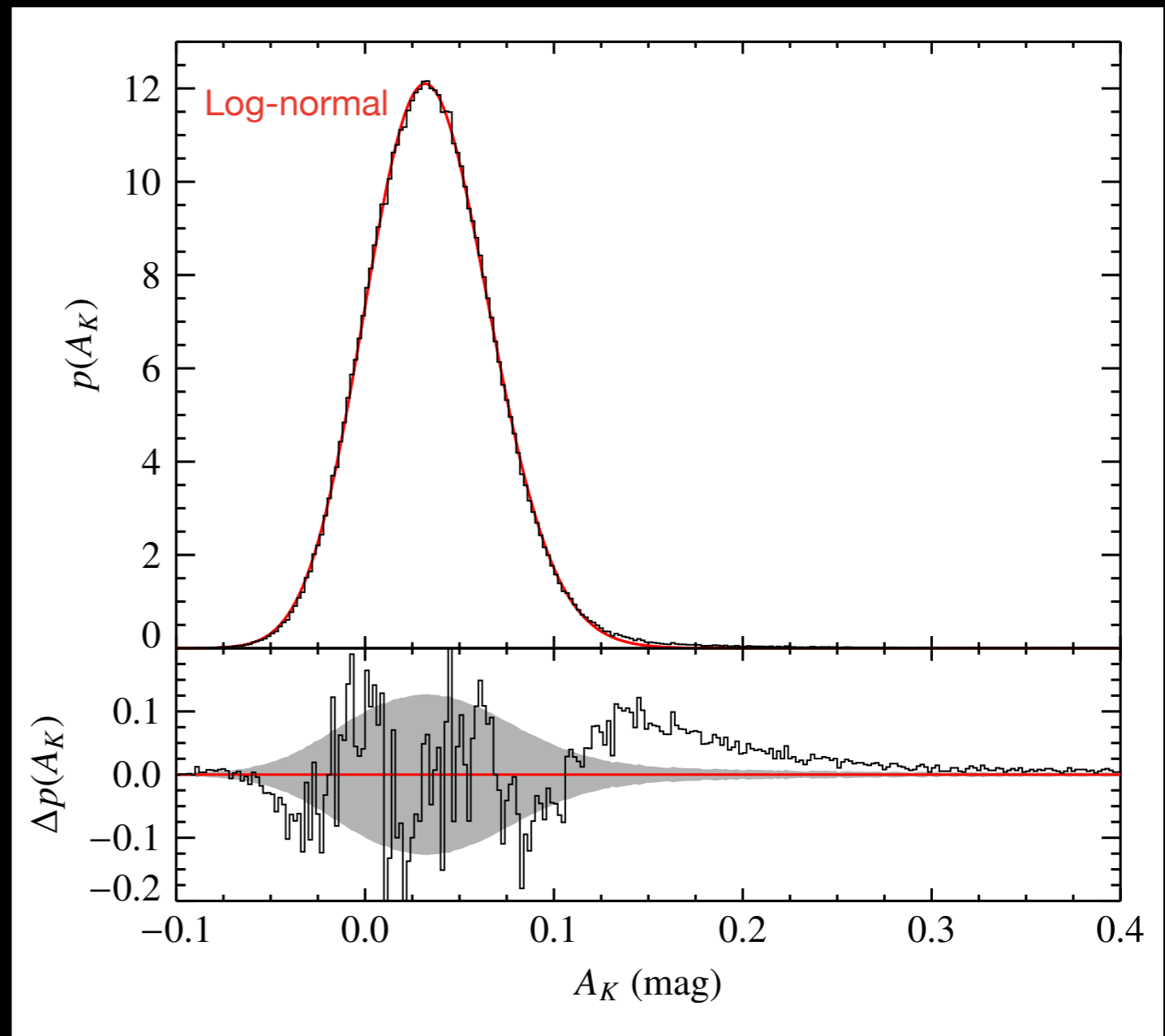
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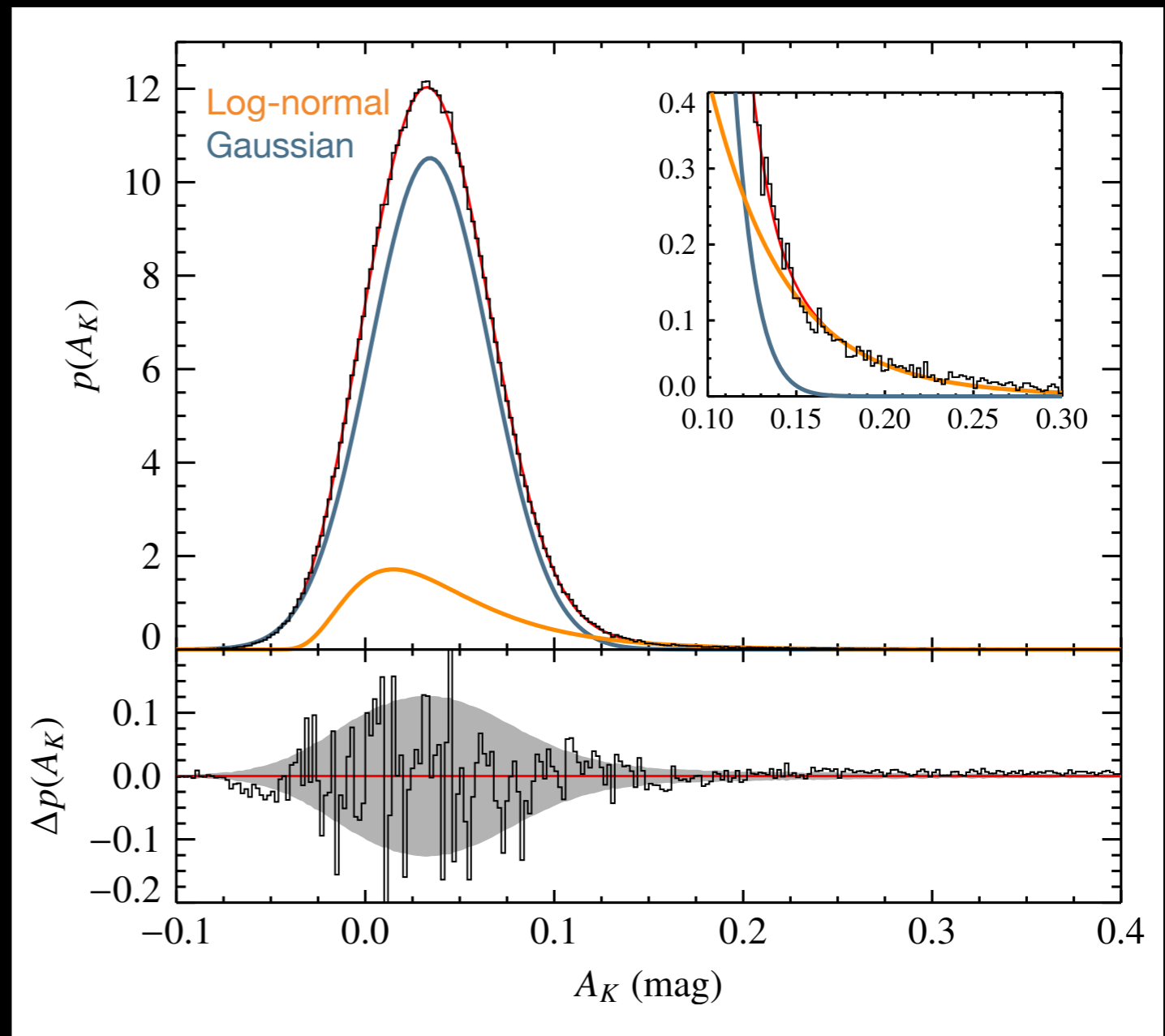
All log-normal fits show systematic residuals



The end of a dream

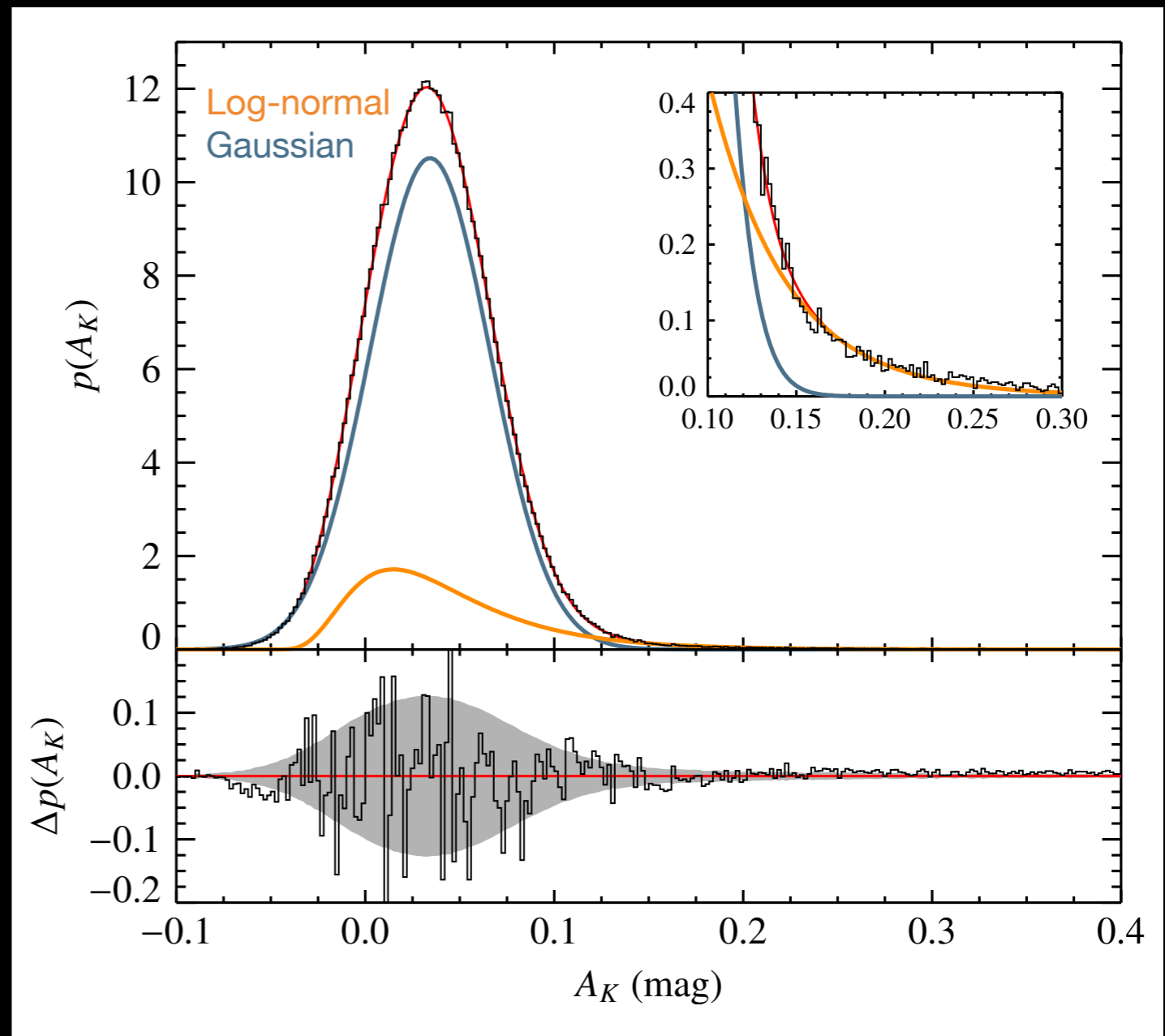


The end of a dream



Residuals disappear when fitting a
Gaussian + Log-normal.

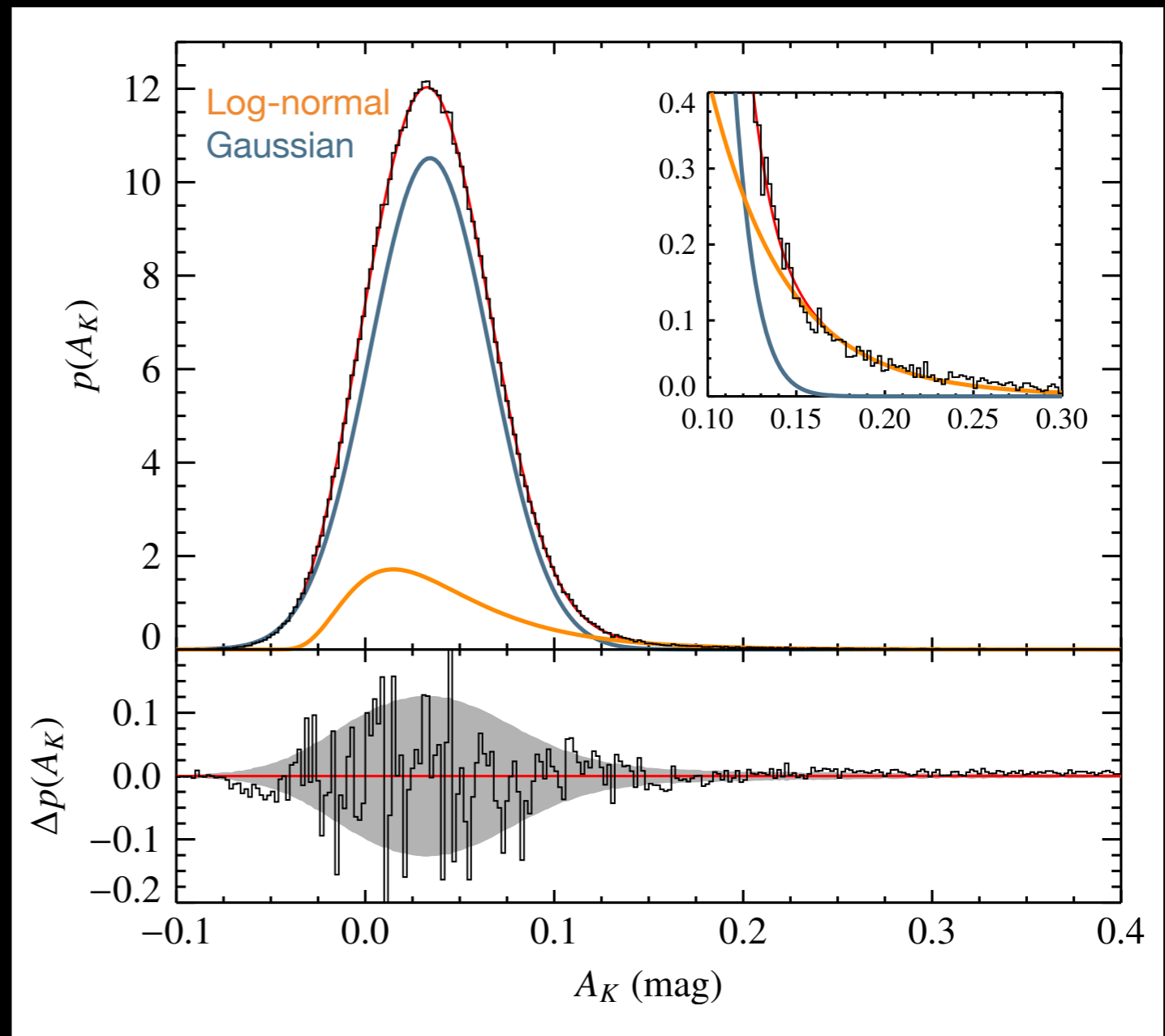
The end of a dream



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The end of a dream

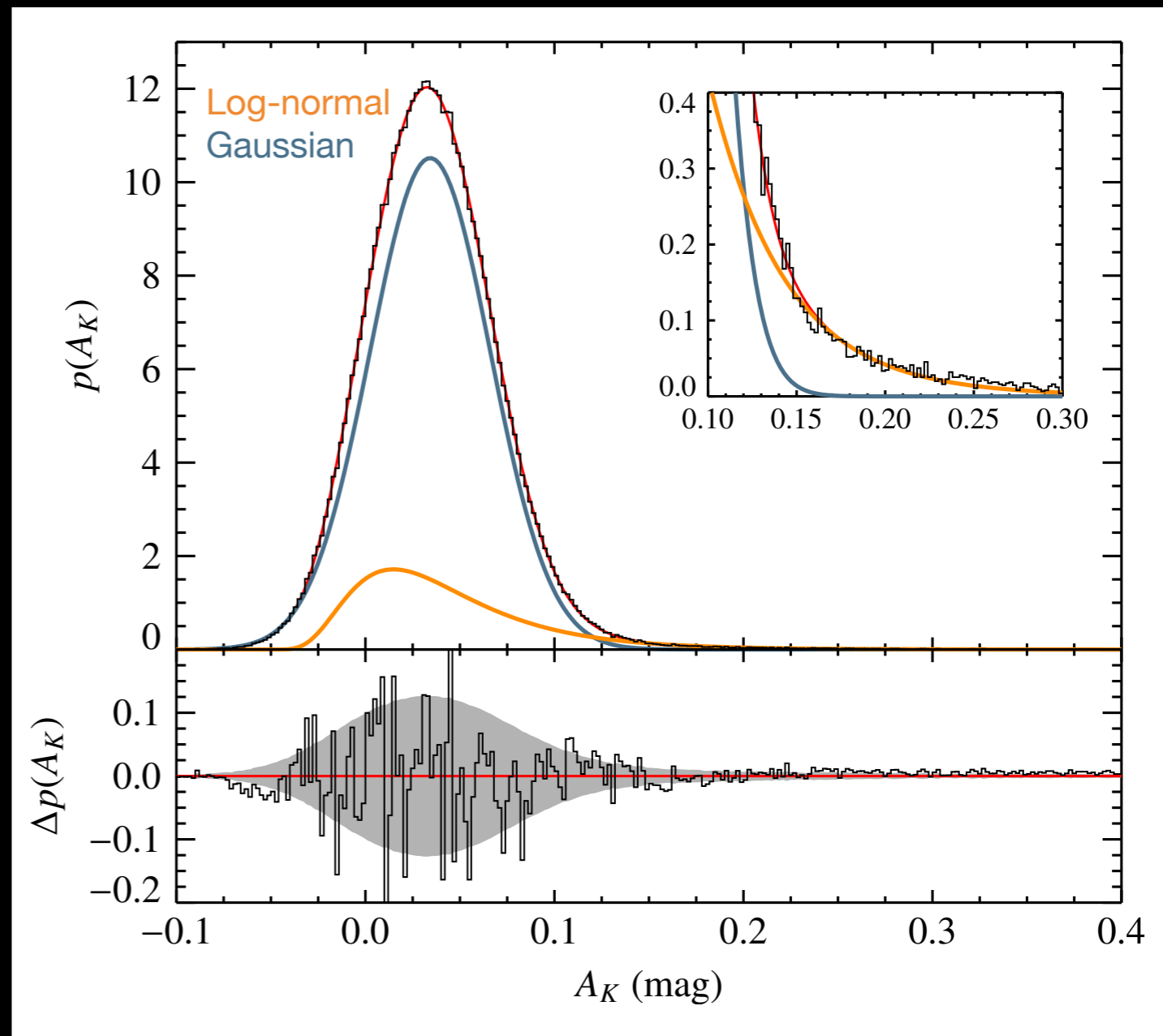
- What is the physical meaning?



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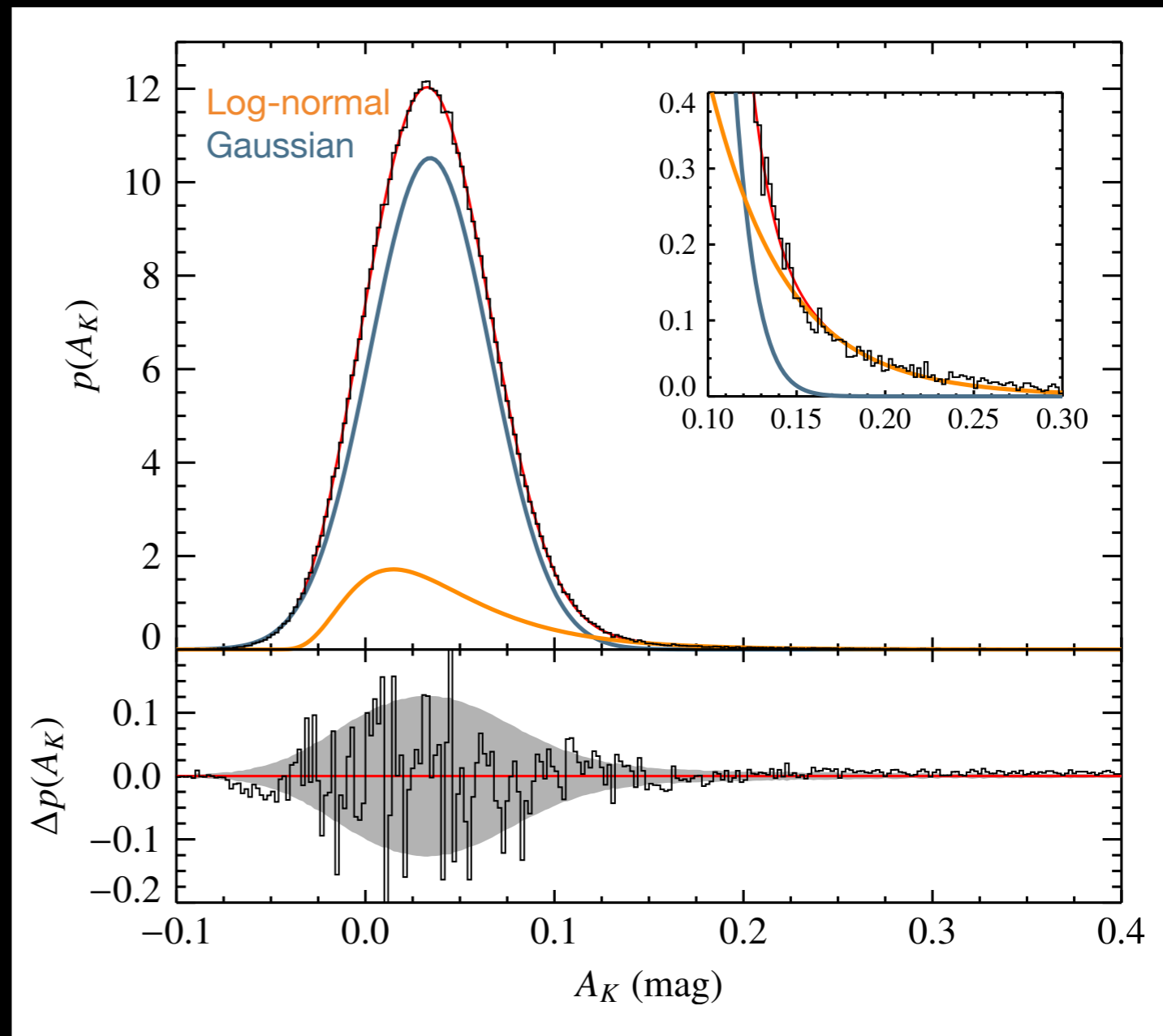
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- Gaussian: diffuse extended region + noise



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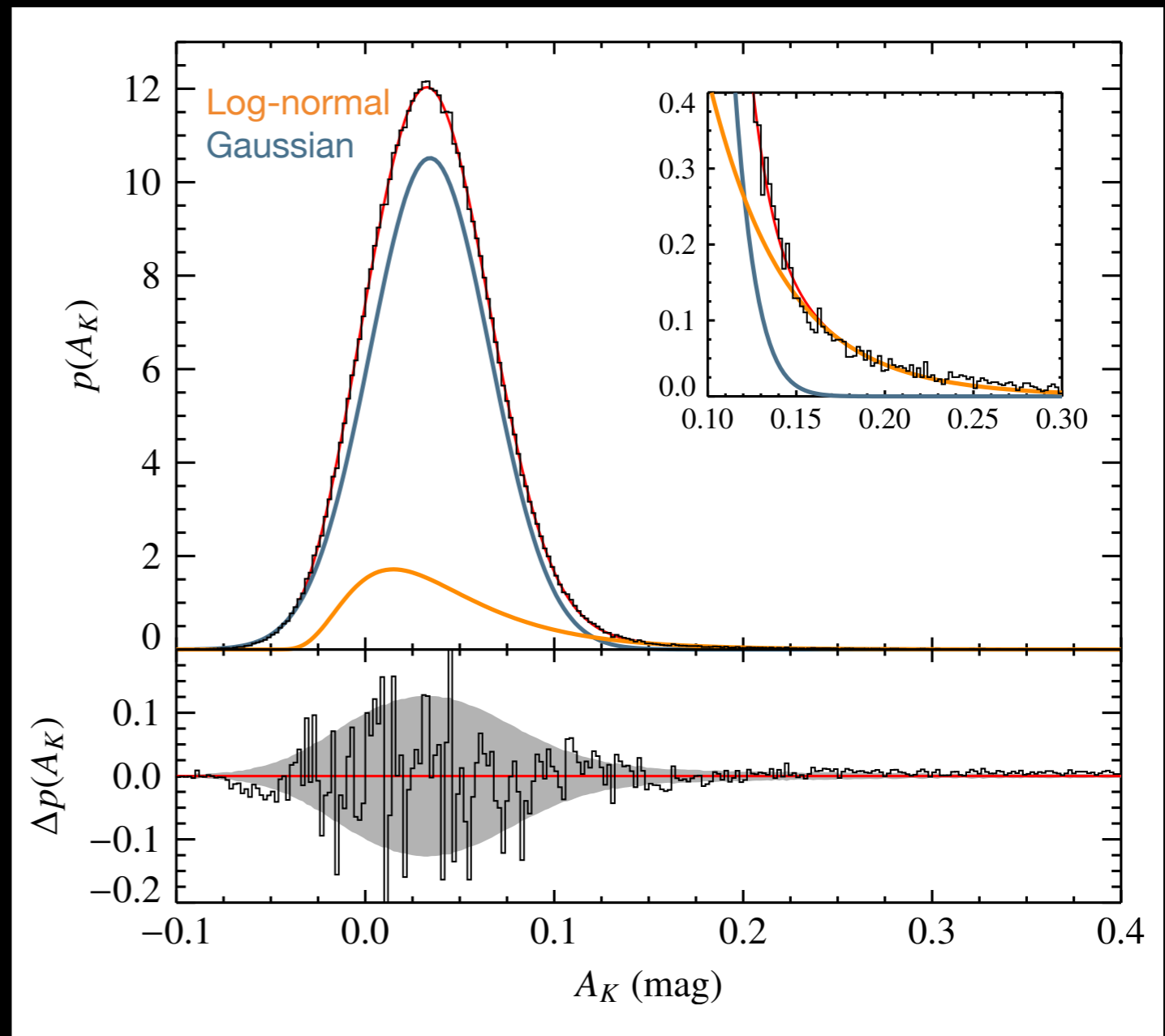
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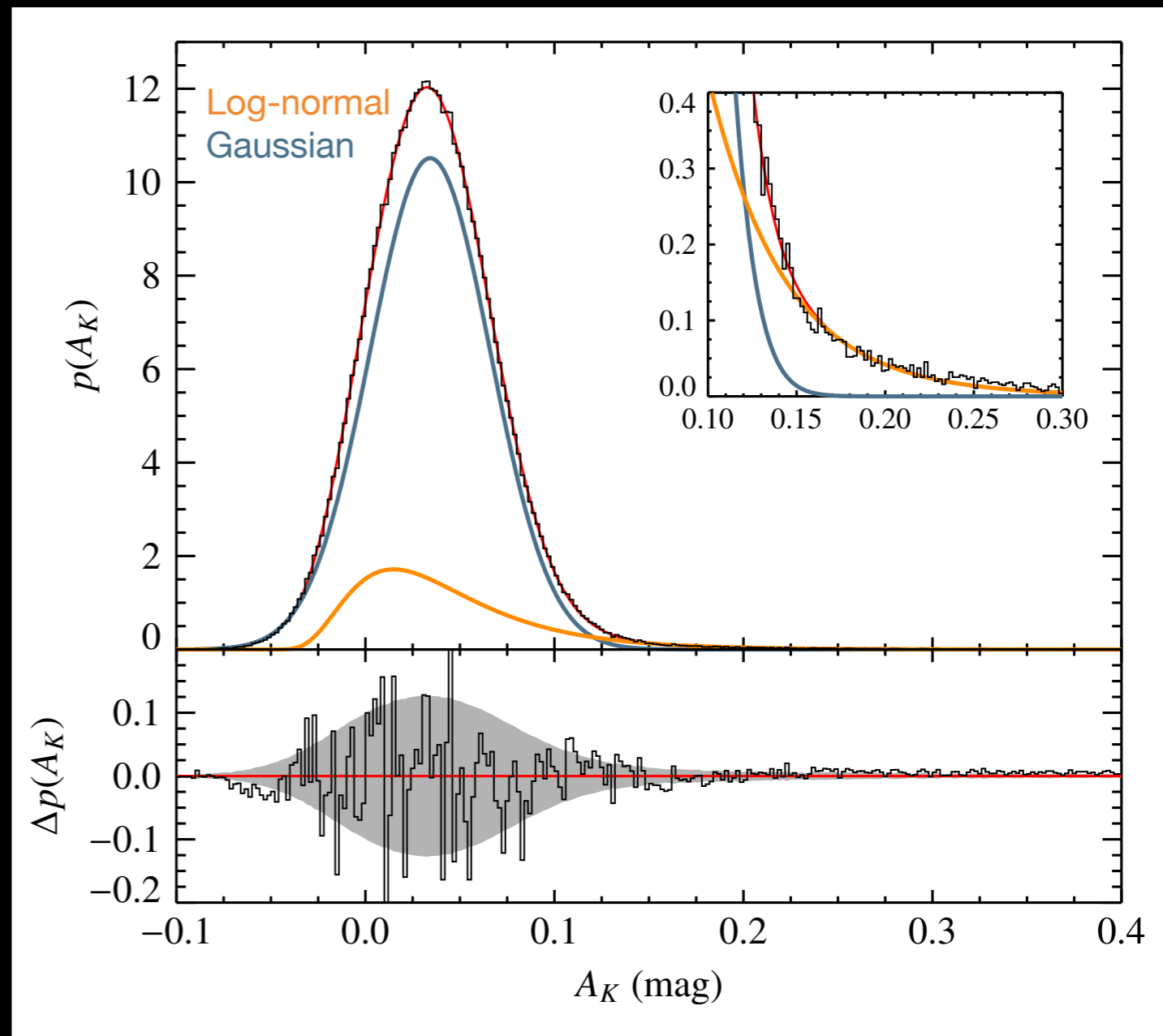
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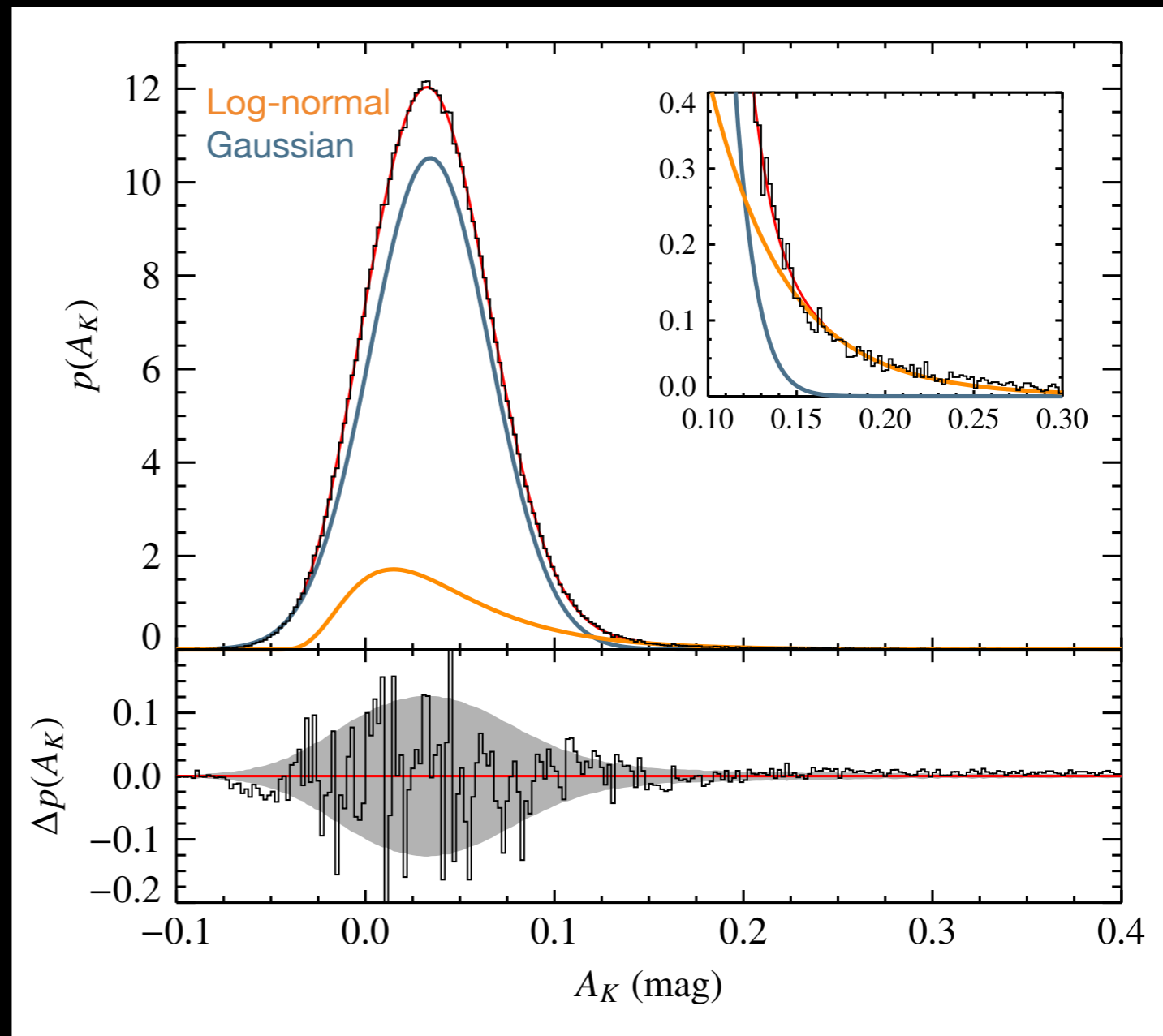
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- Dominates at low A_K !



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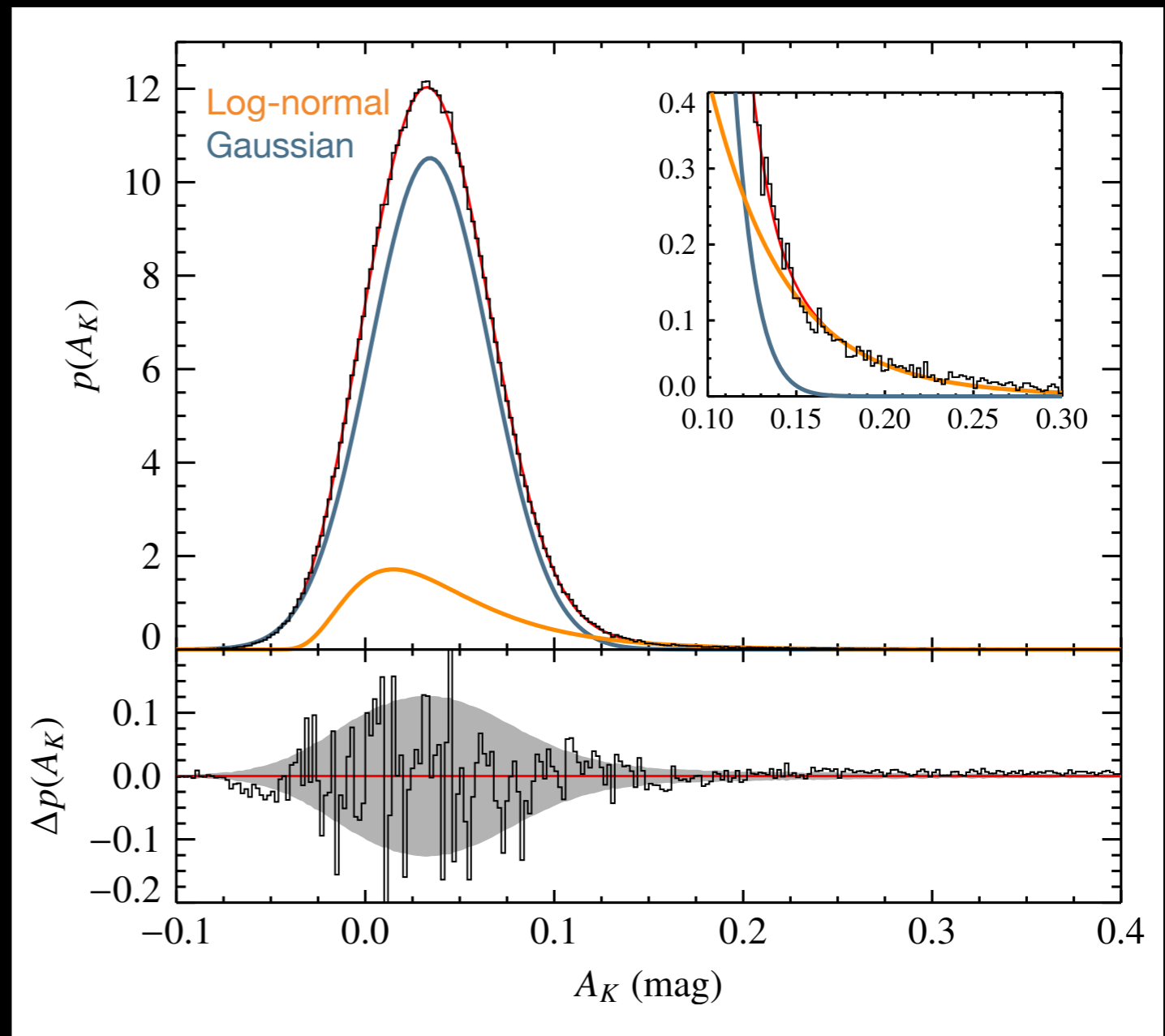
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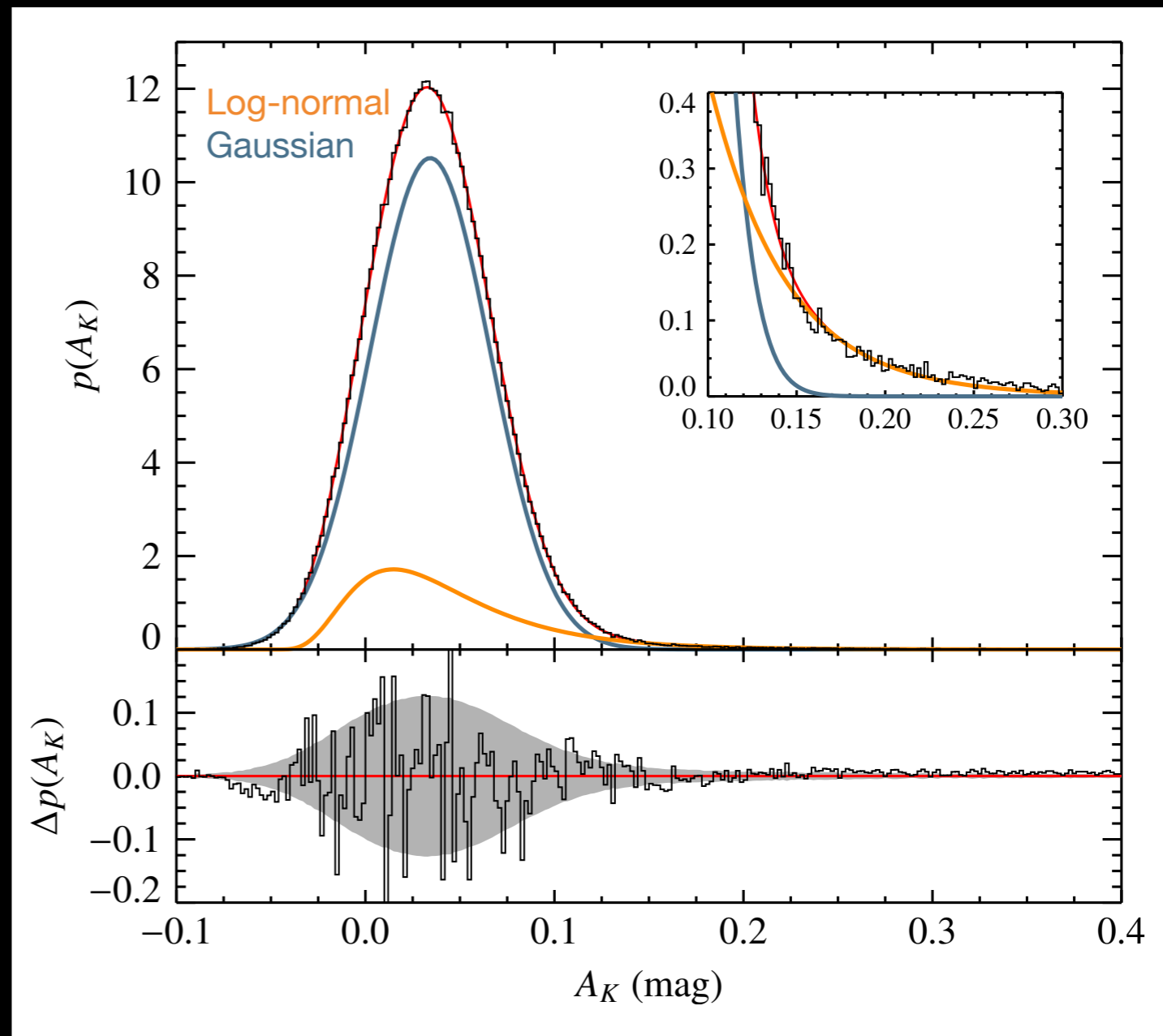
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- What is the physical meaning?
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 - Is still present at large A_K
- PDFs more difficult to measure than we expected...
- Log-normals: are they real?



Residuals disappear when fitting a Gaussian + Log-normal.

Do yourself your log-normal!

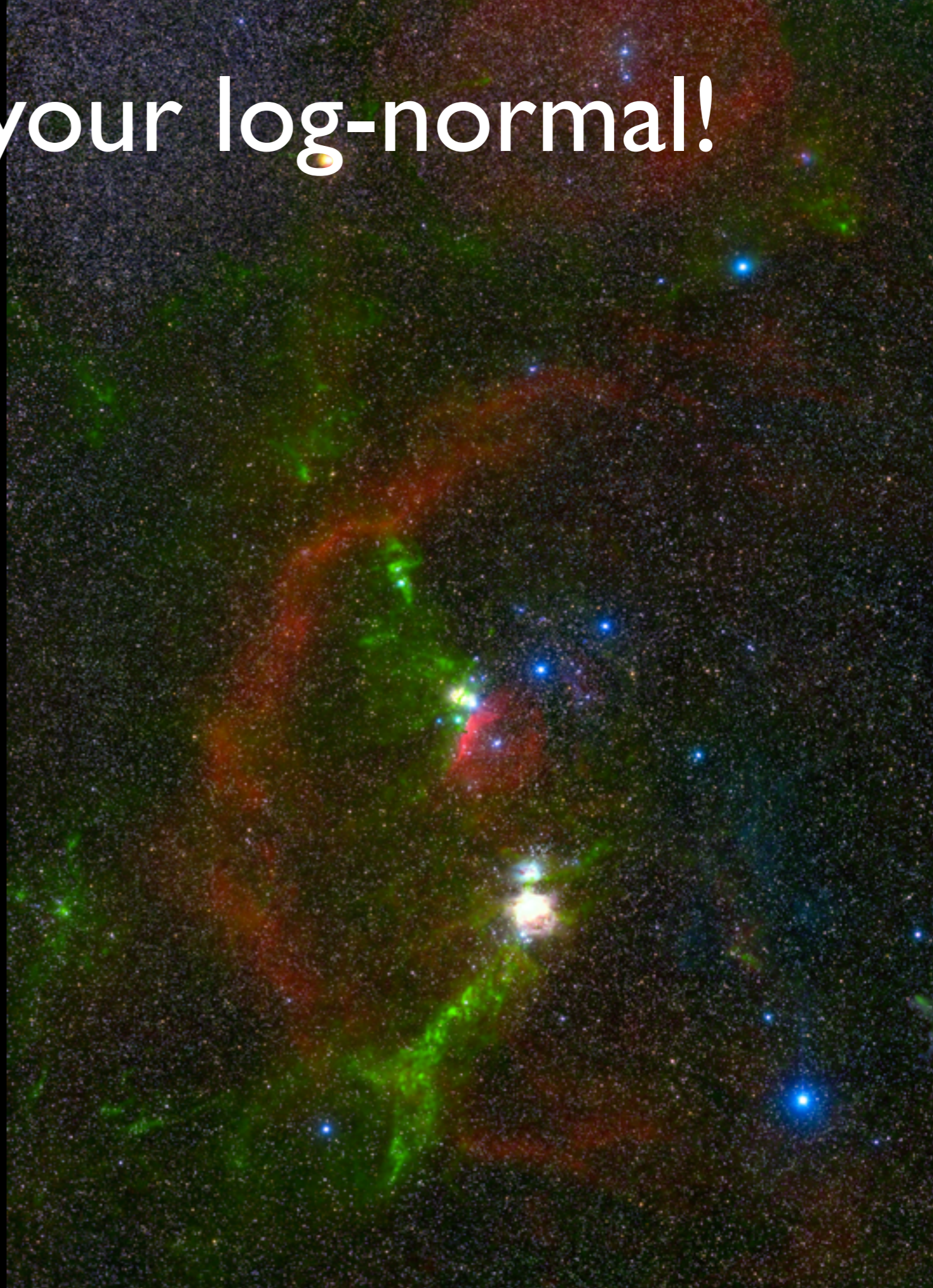
Do yourself your log-normal!

Recipe

Do yourself your log-normal!

Recipe

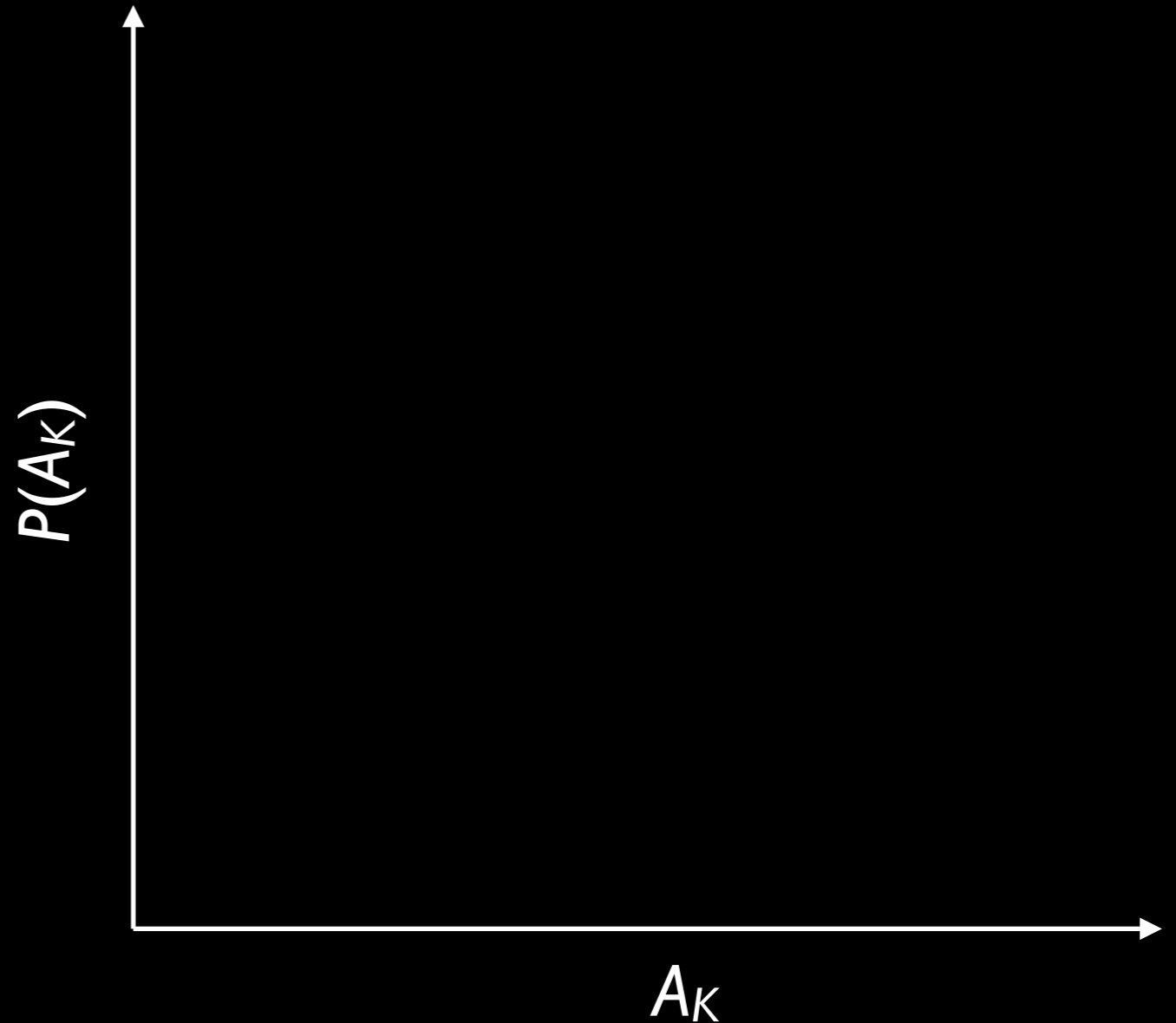
- Take any nice cloud



Do yourself your log-normal!

Recipe

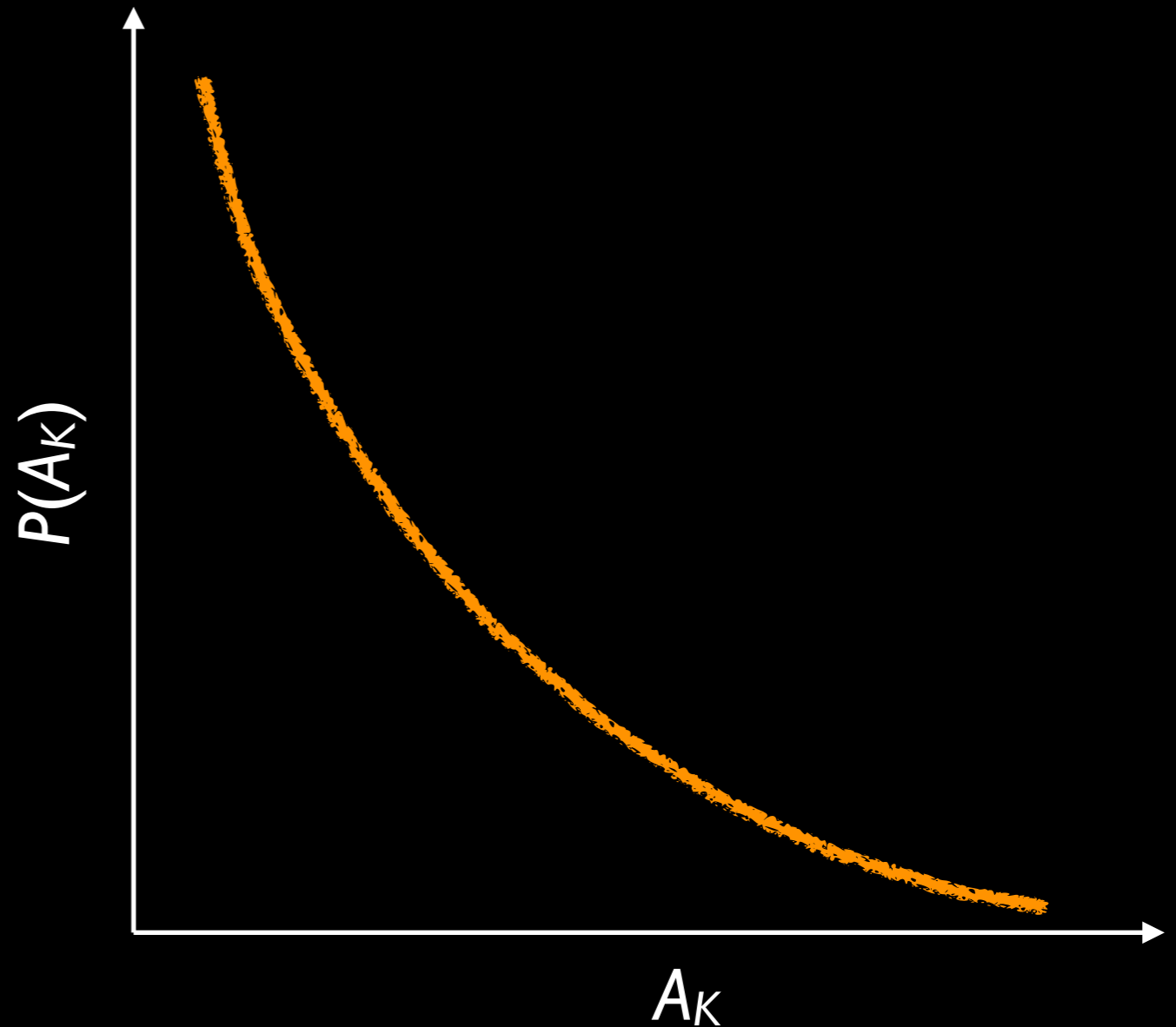
- Take any nice cloud
- For optimal results, make sure the *true* PDF is decreasing



Do yourself your log-normal!

Recipe

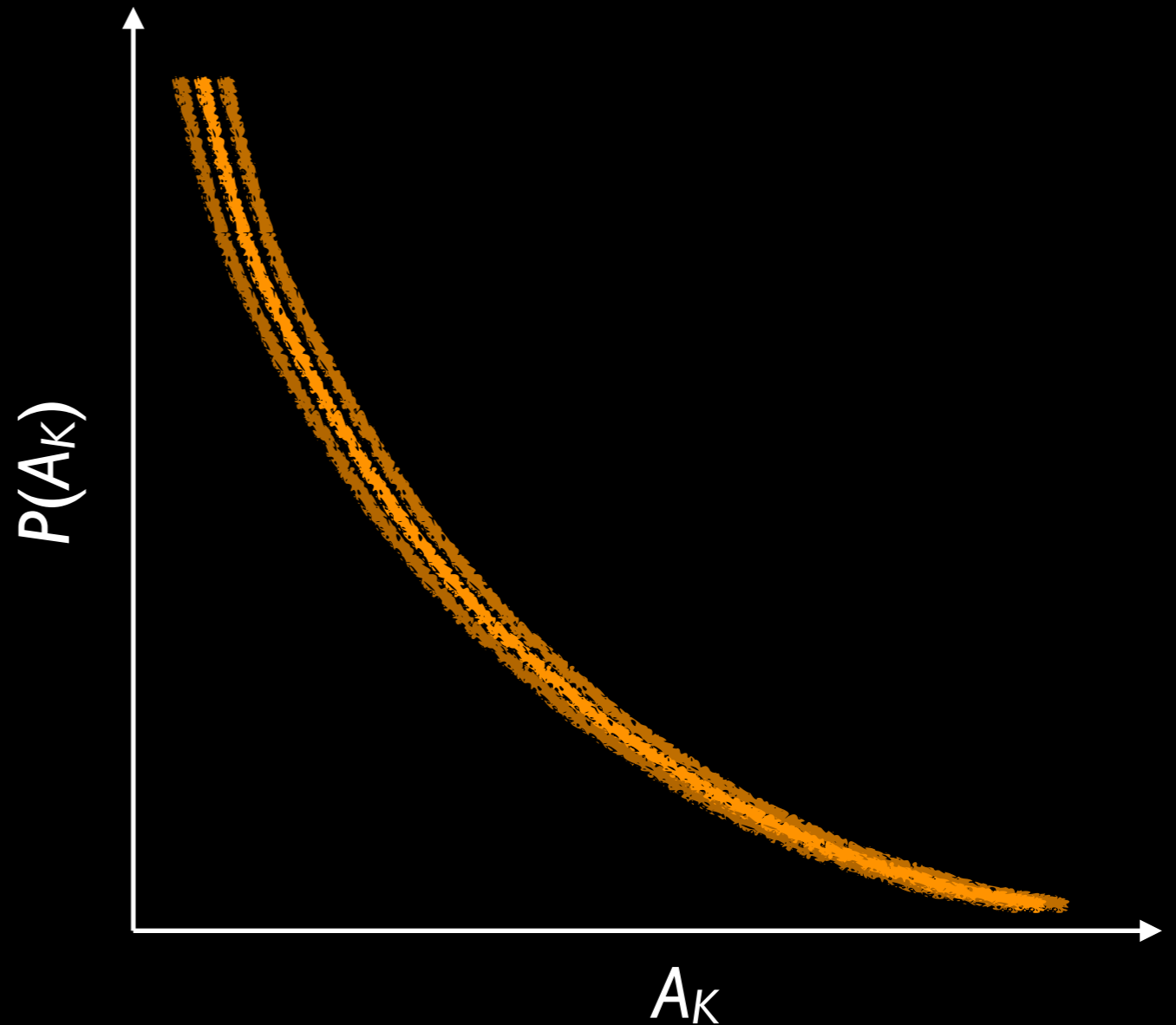
- Take any nice cloud
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- A nice $P(A_K) \sim A_K^{-n}$ will do



Do yourself your log-normal!

Recipe

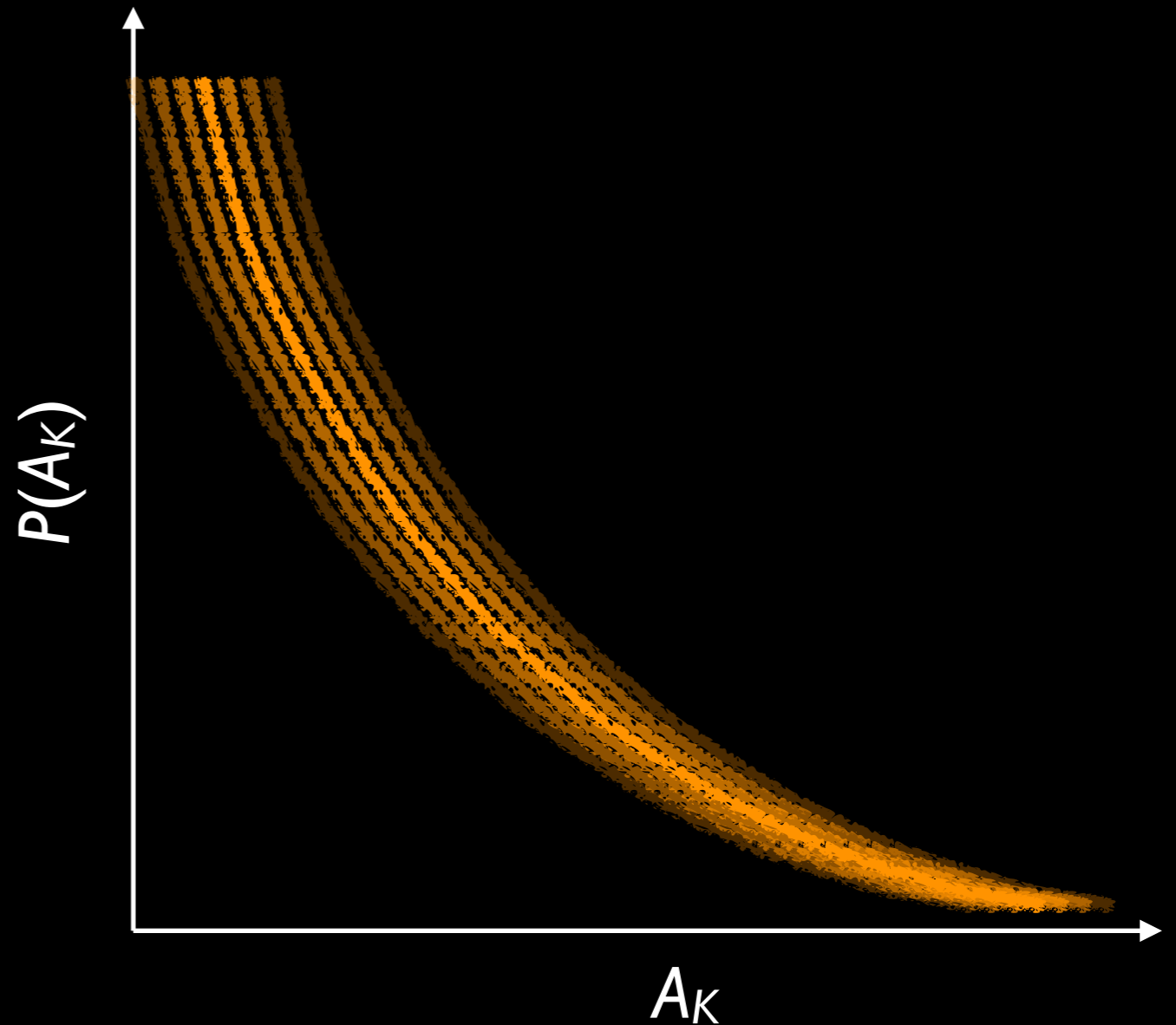
- Take any nice cloud
- For optimal results, make sure the *true* PDF is decreasing
- A nice $P(A_K) \sim A_K^{-n}$ will do
- Observe the cloud



Do yourself your log-normal!

Recipe

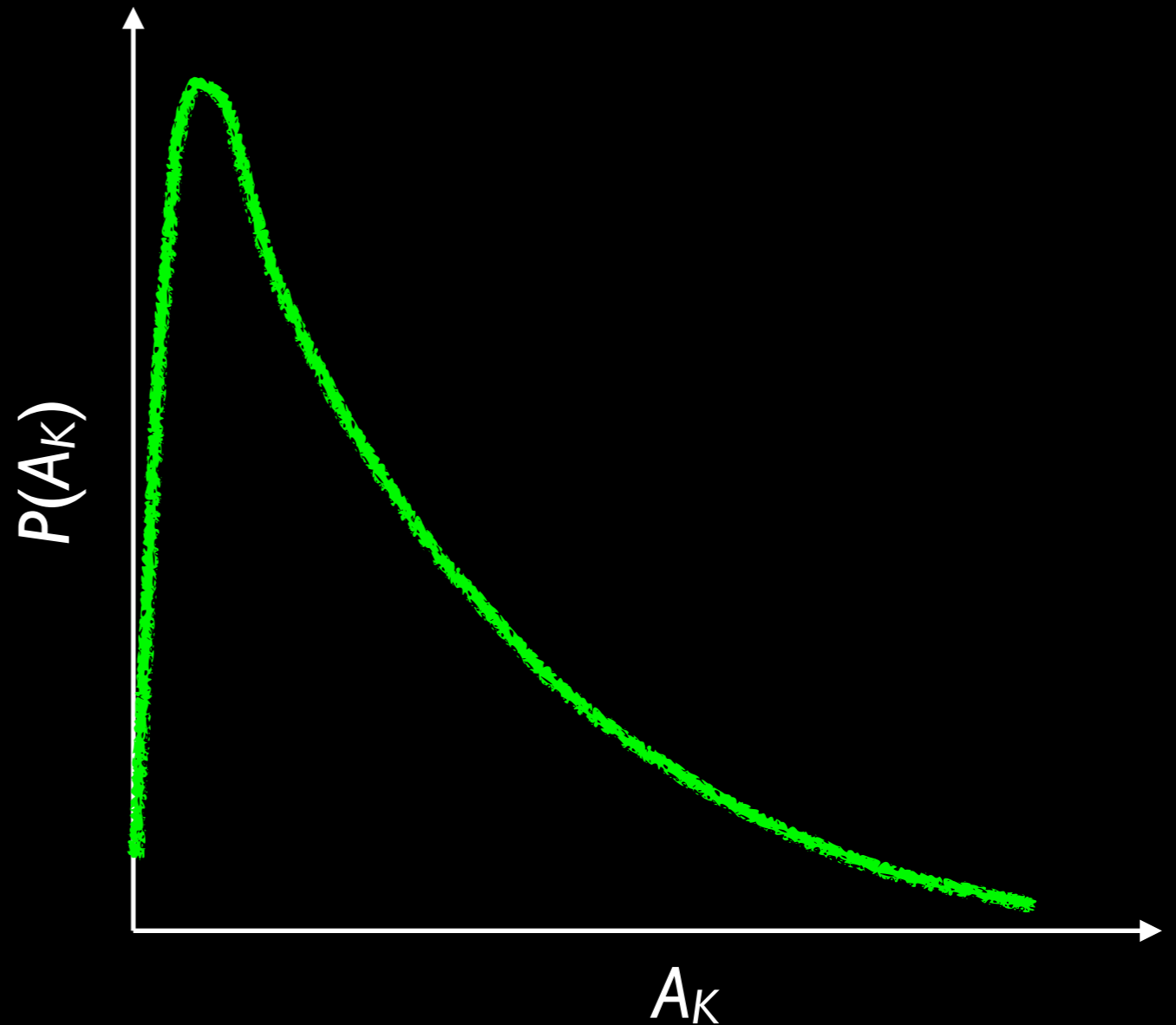
- Take any nice cloud
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- Make sure you make significant statistical errors



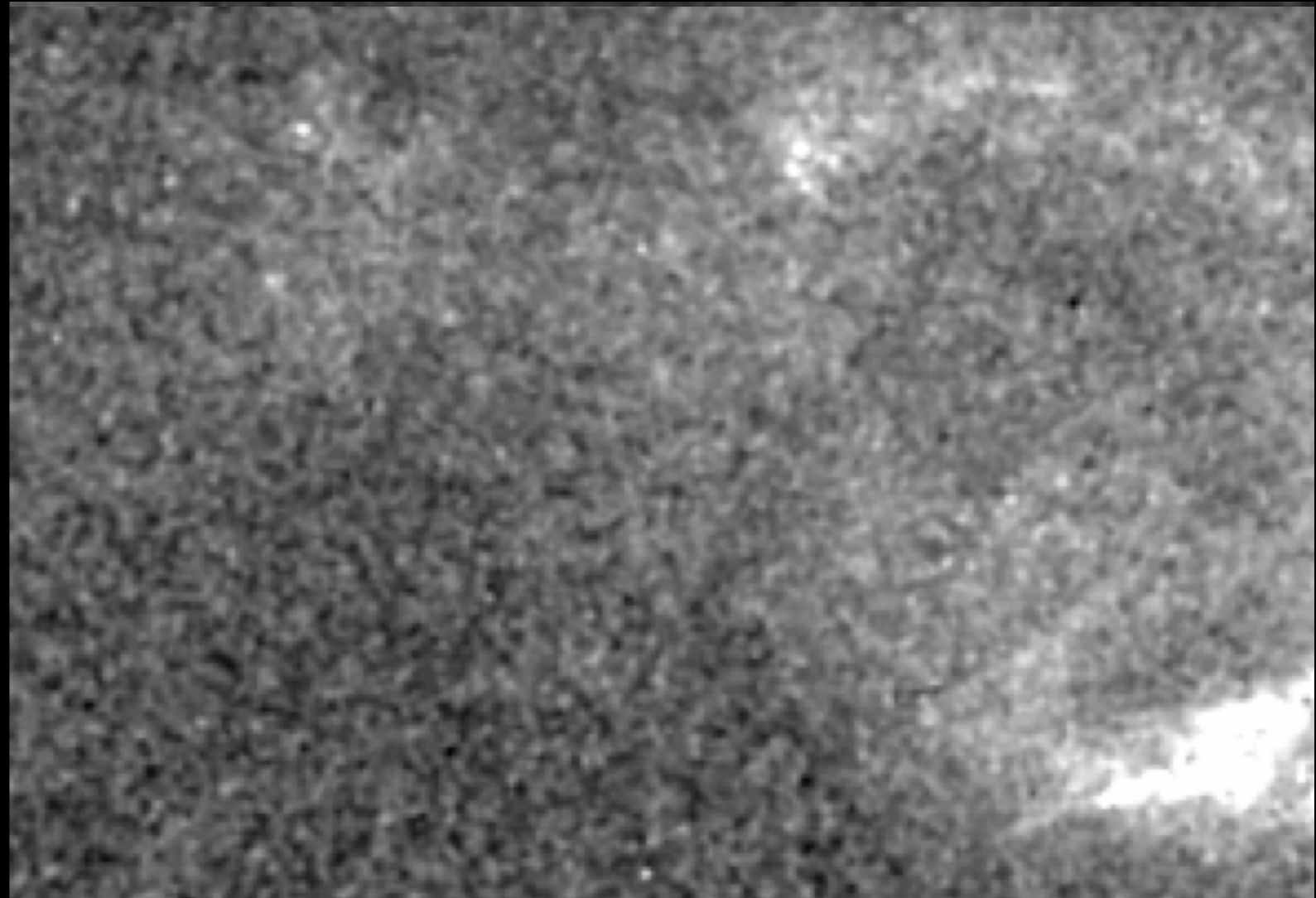
Do yourself your log-normal!

Recipe

- Take any nice cloud
- For optimal results, make sure the *true* PDF is decreasing
- A nice $P(A_K) \sim A_K^{-n}$ will do
- Observe the cloud
 - Make sure you make significant statistical errors
- You are done! The *observed* PDF looks like a log-normal!

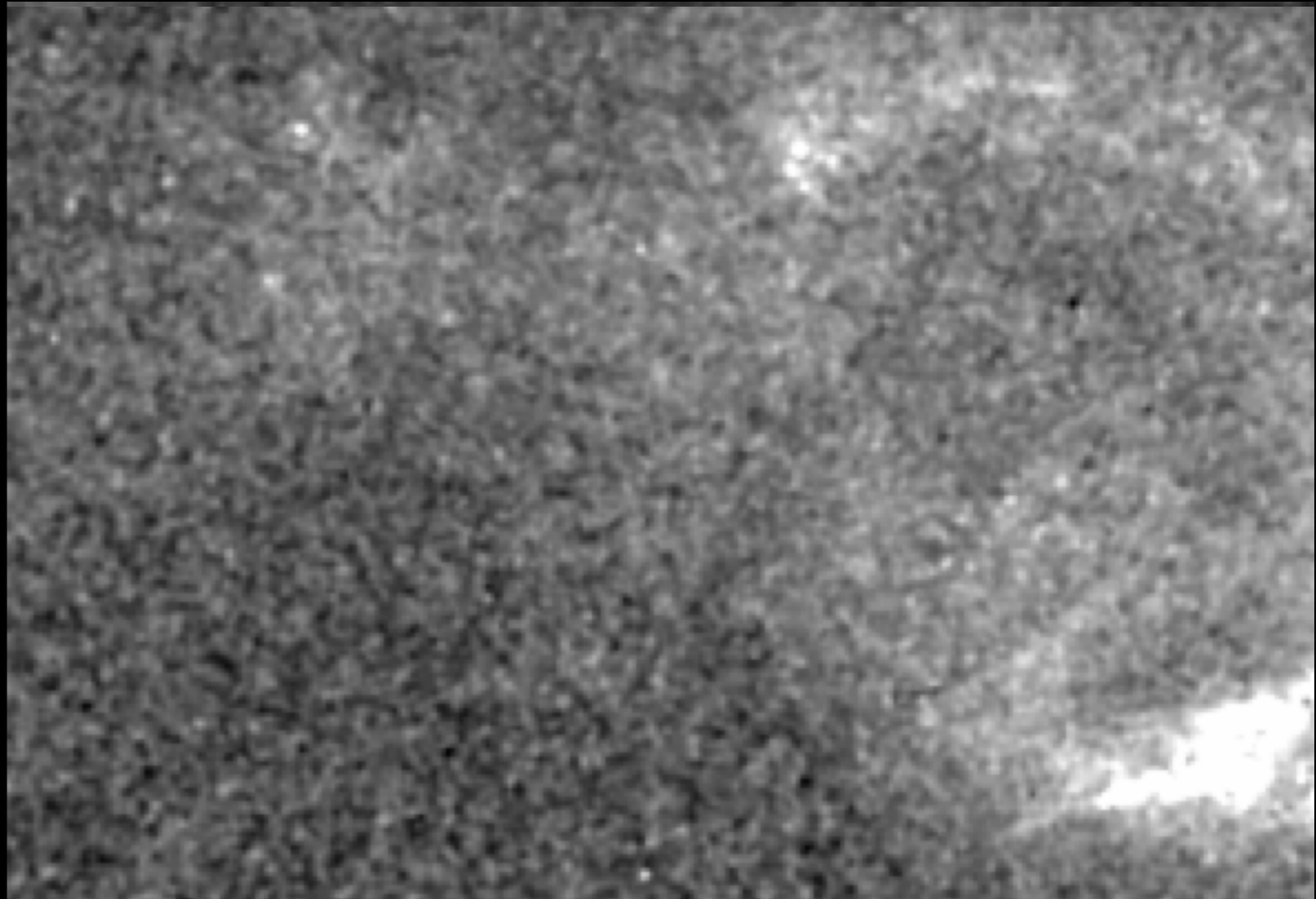


PDFs, noise, and resolution



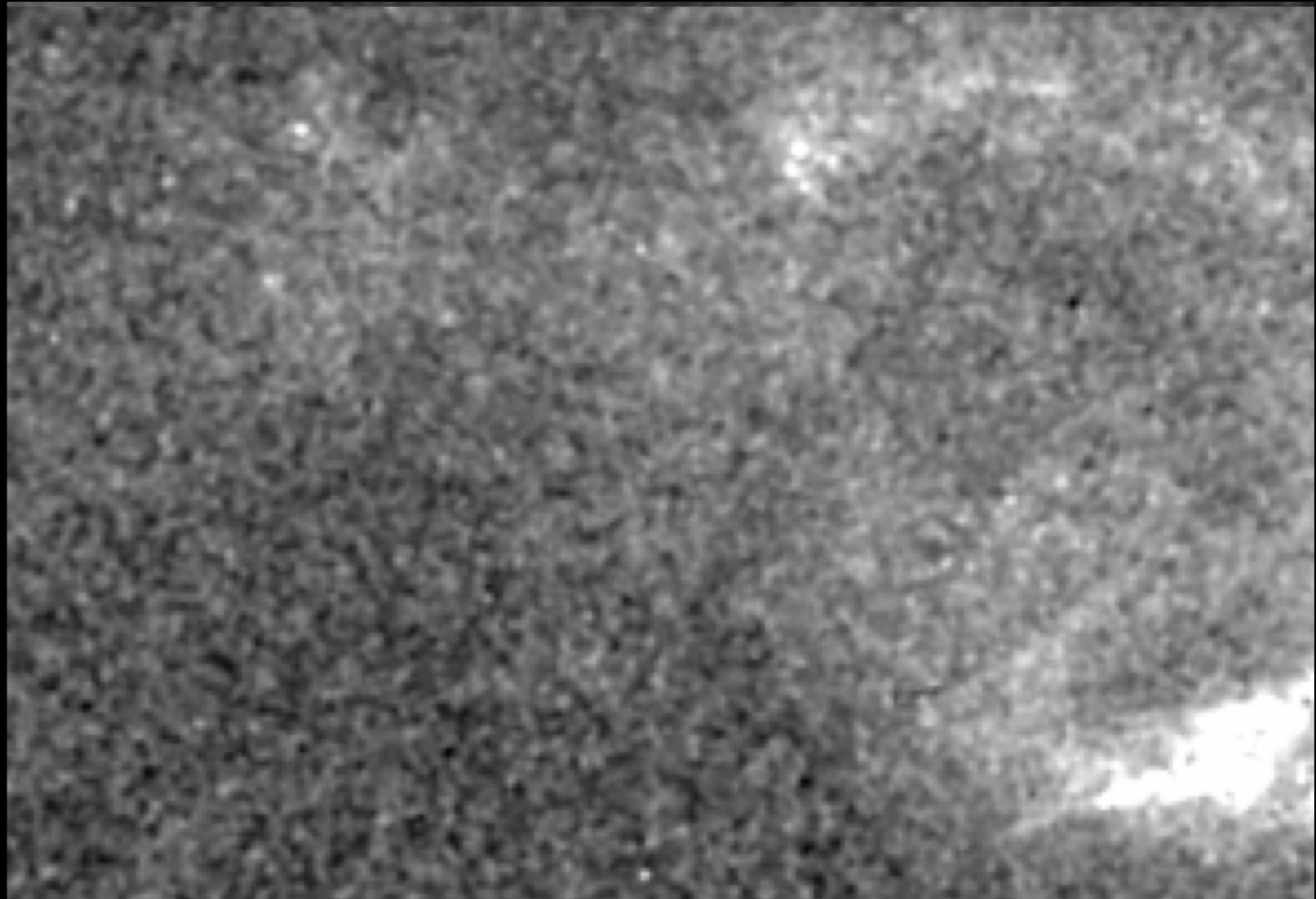
PDFs, noise, and resolution

- Noise can be significant at low column densities



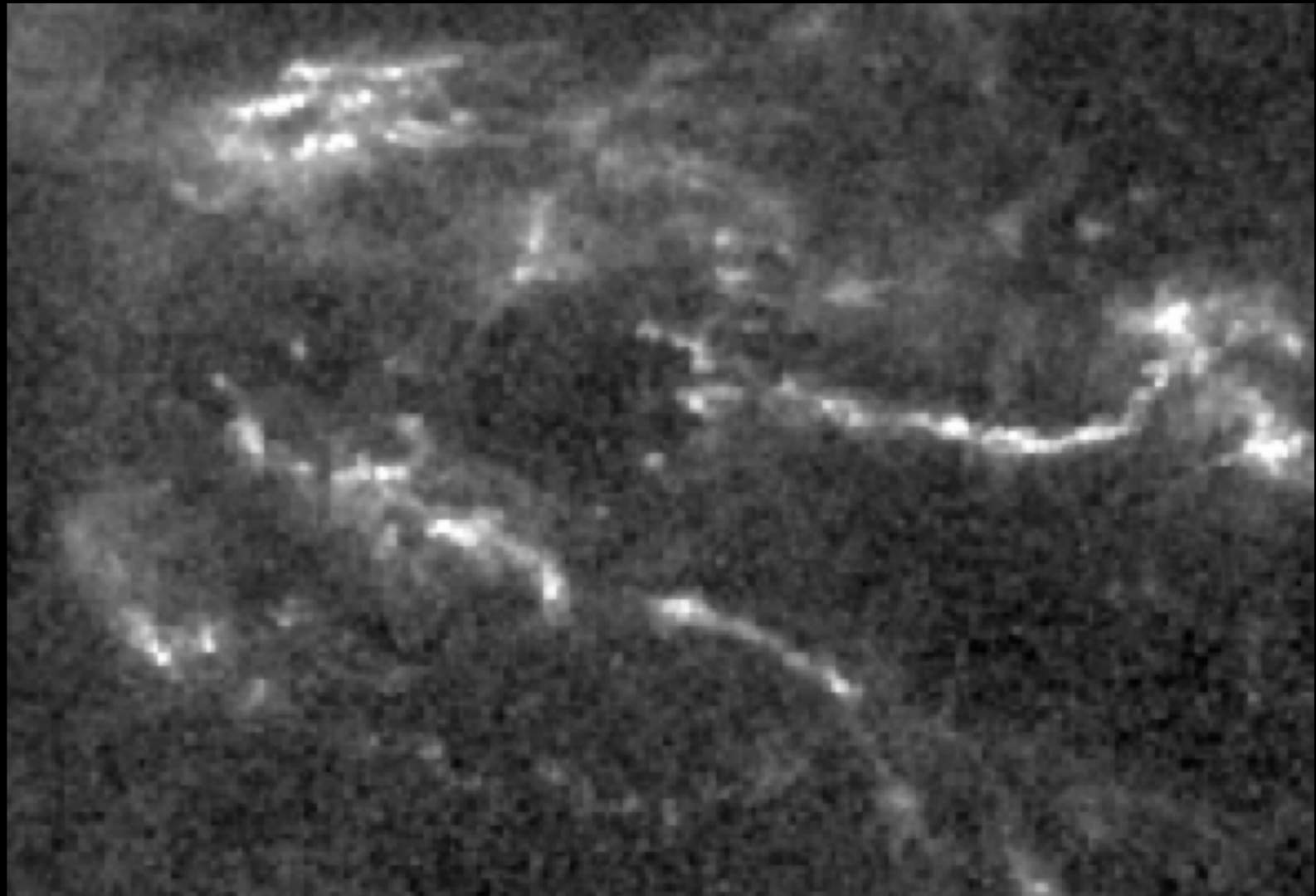
PDFs, noise, and resolution

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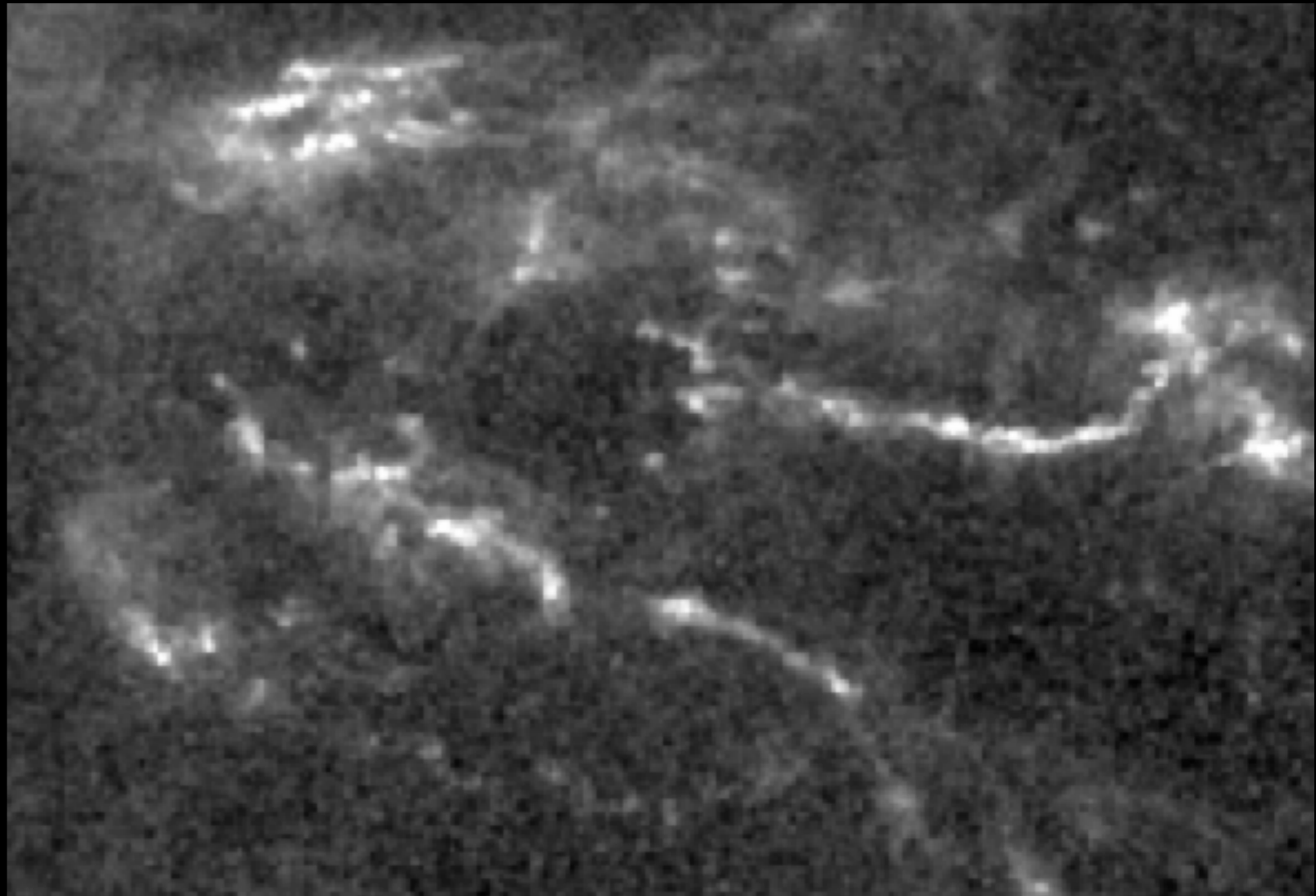
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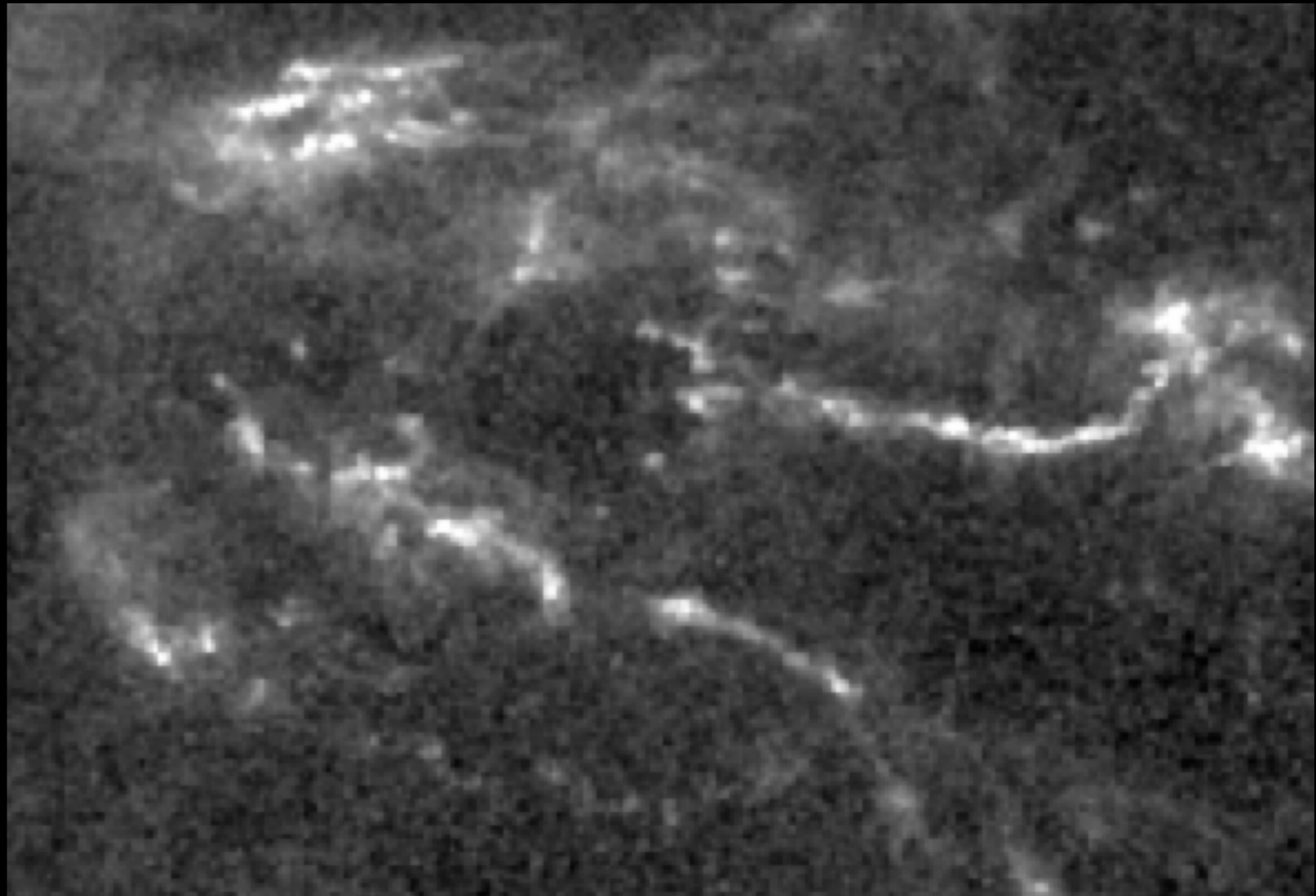
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PDFs, noise, and resolution

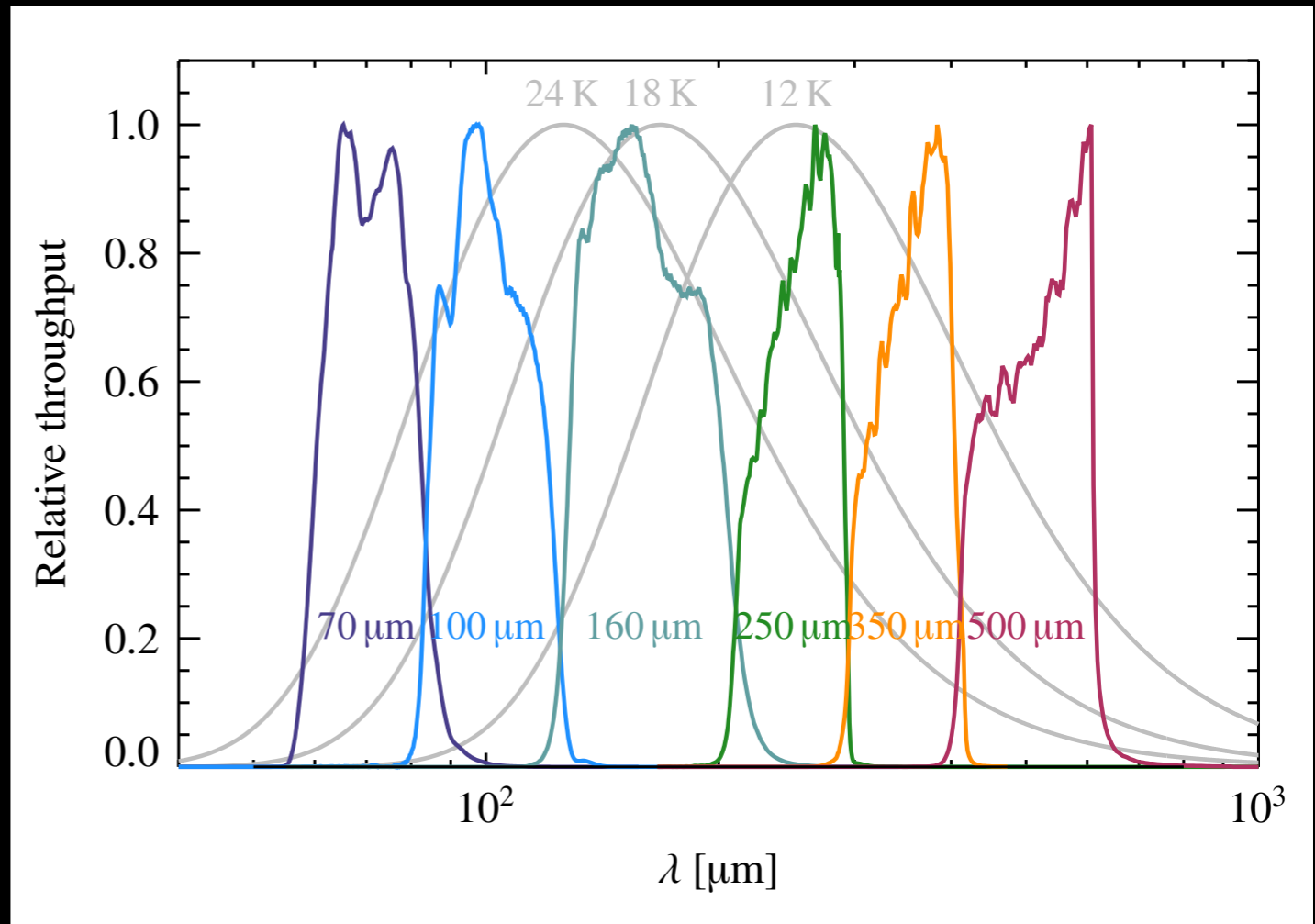
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Ideally we would like to have high-res, low-noise density maps of clouds

Beat the noise: Herschel maps!

Dust emission data

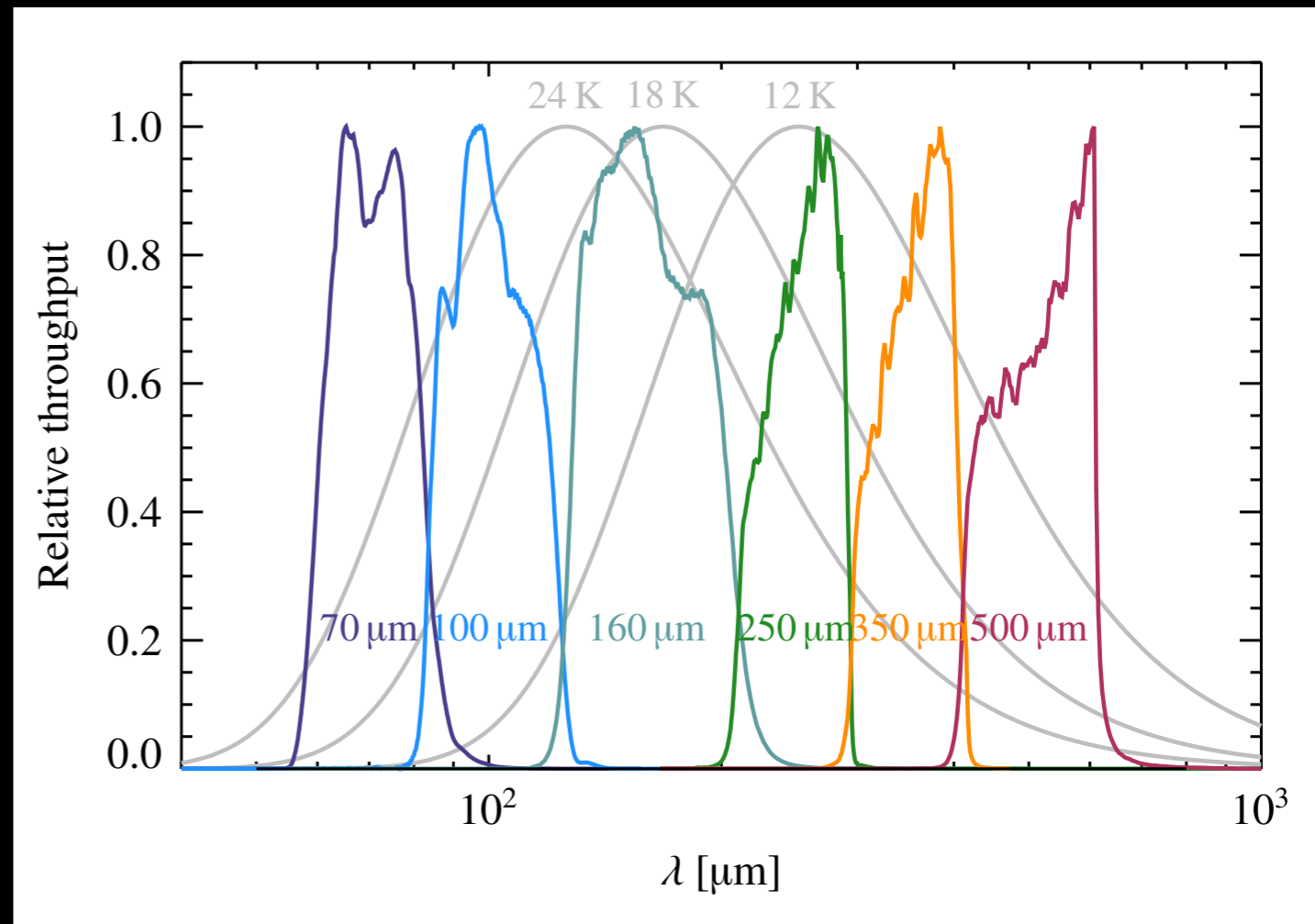


Dust emission data

- A cloud emits a (modified) black body spectrum

$$I_\nu = B_\nu(T) [1 - e^{-\tau_\nu}] \simeq B_\nu(T) \tau_\nu$$

$$\tau_\nu = \kappa_\nu \Sigma_{\text{dust}} \propto \nu^\beta$$



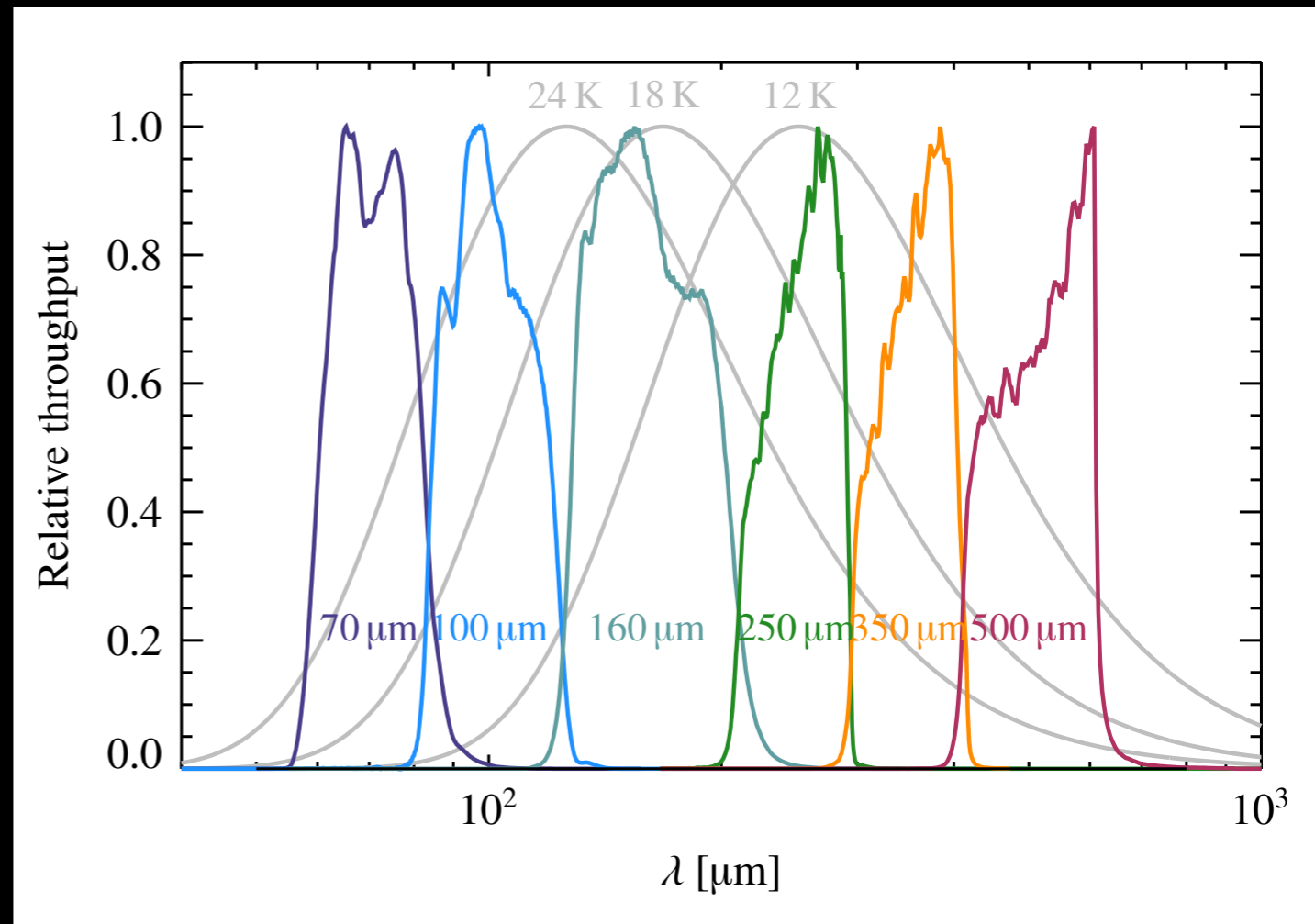
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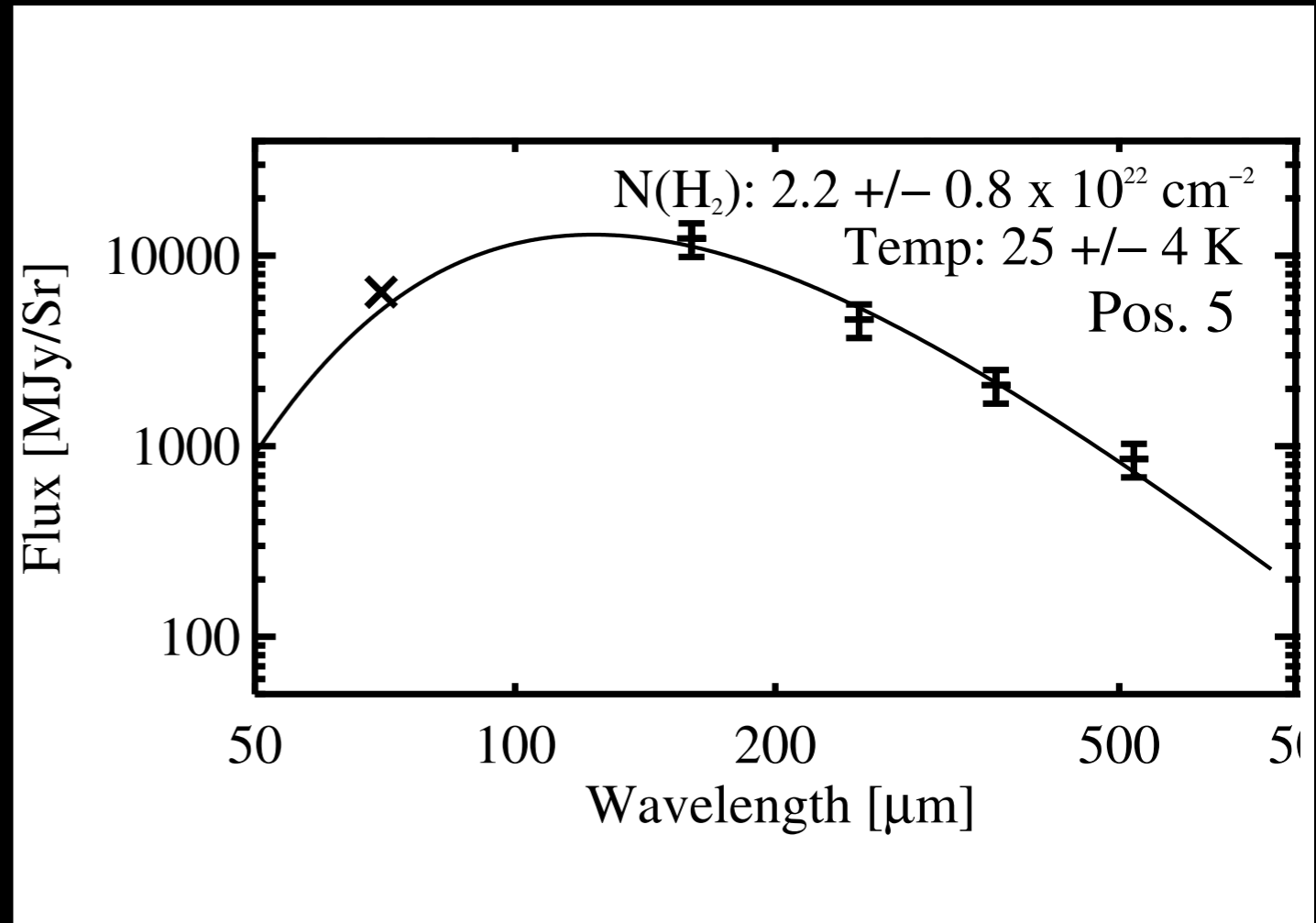
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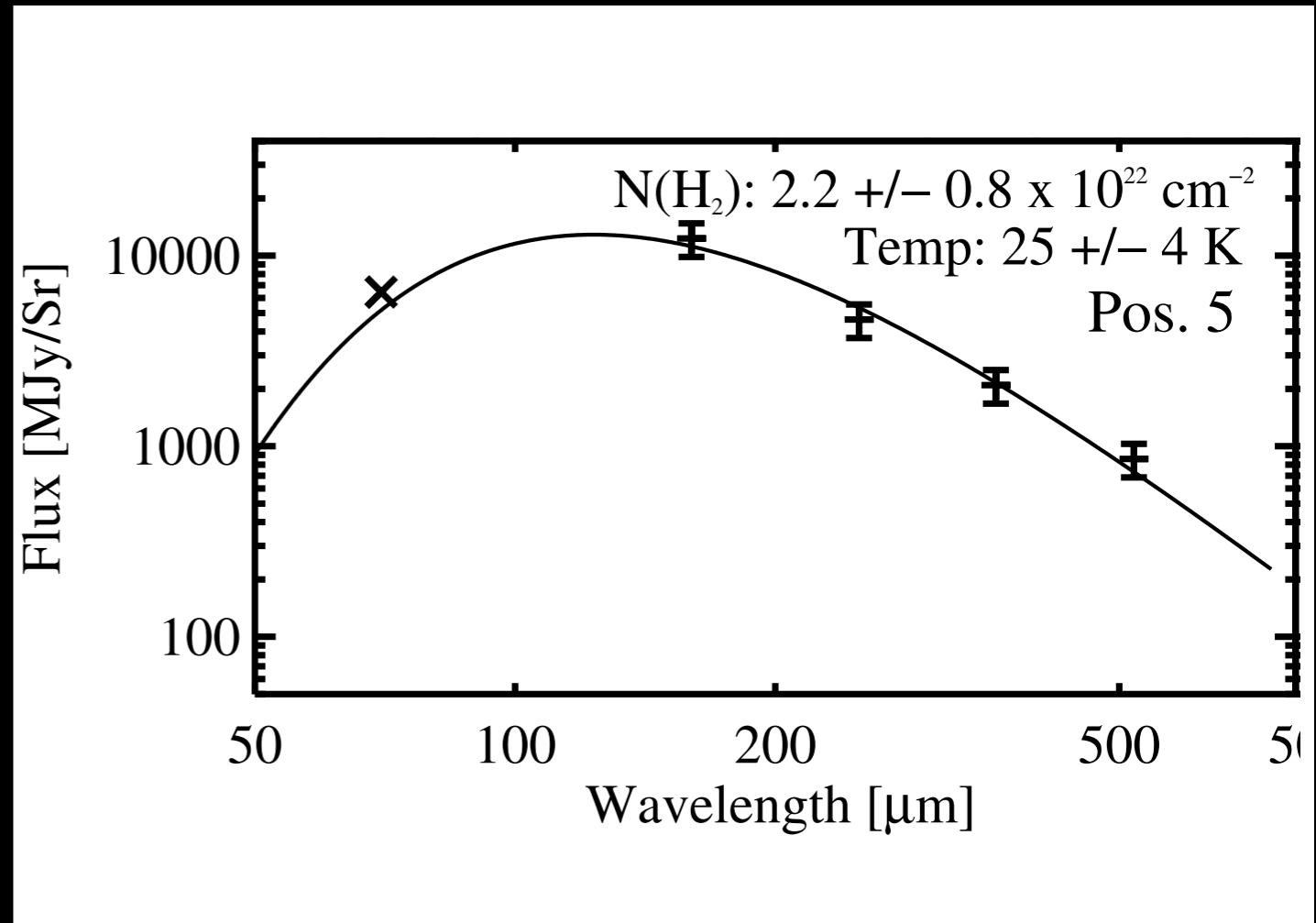
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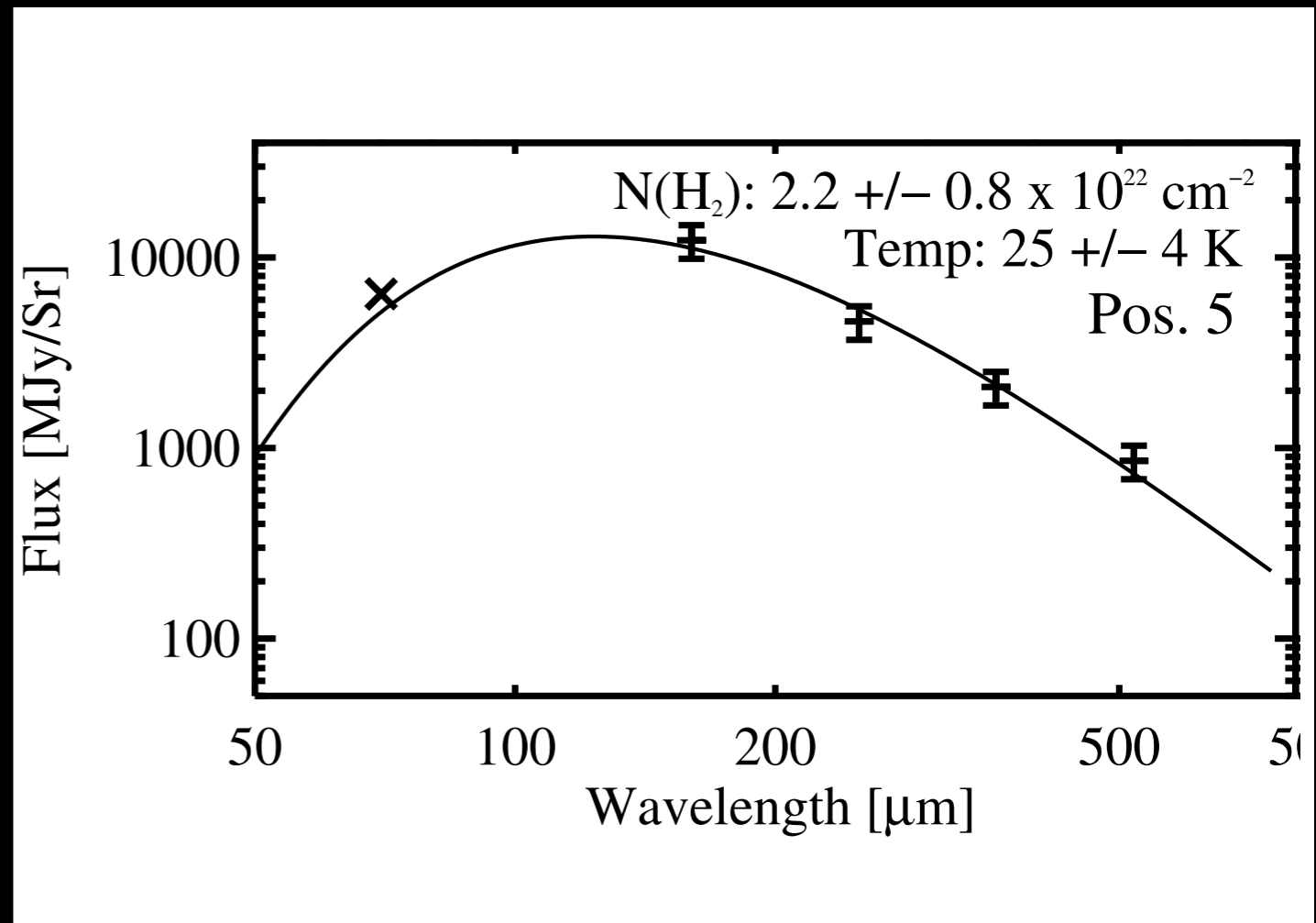
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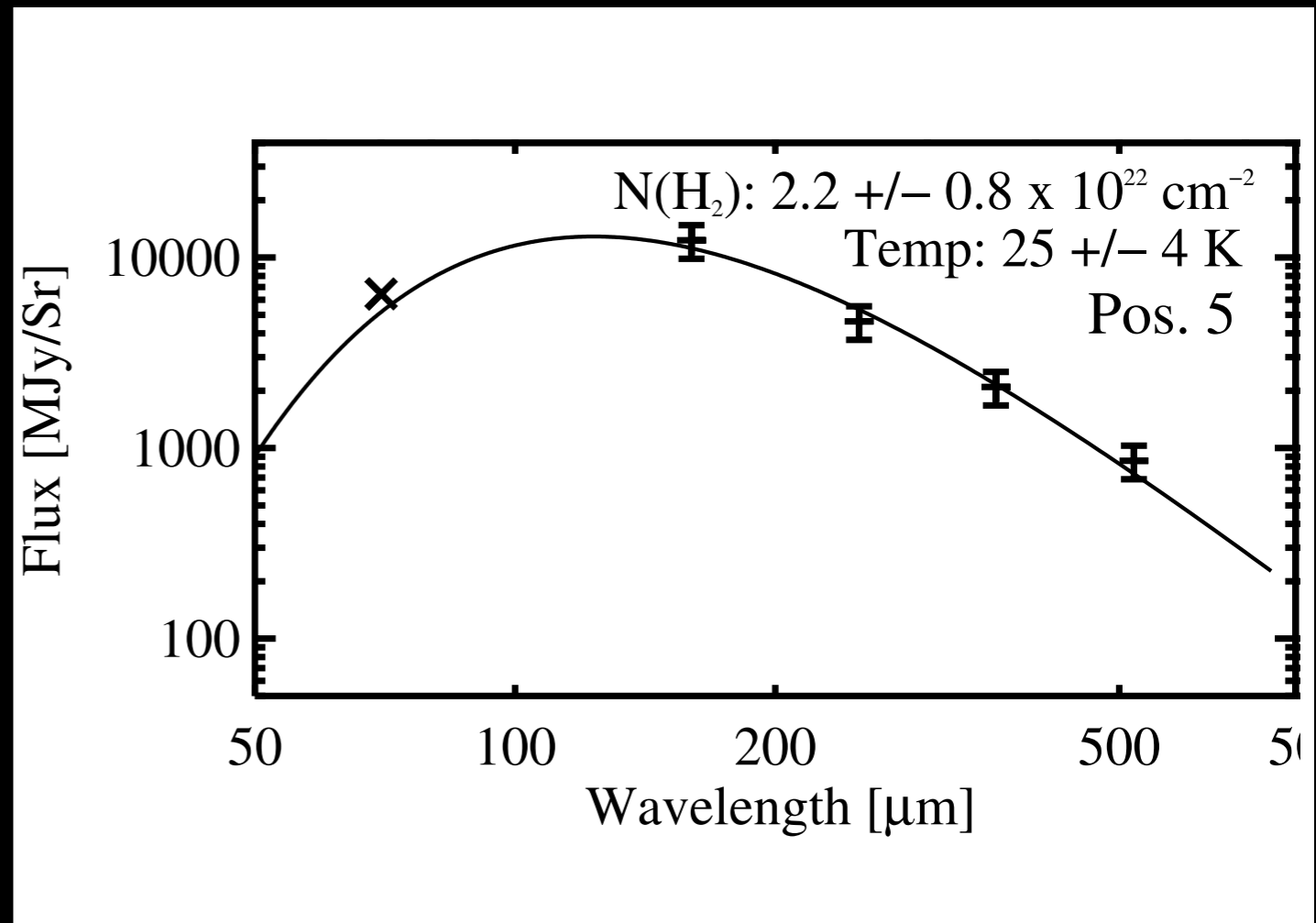
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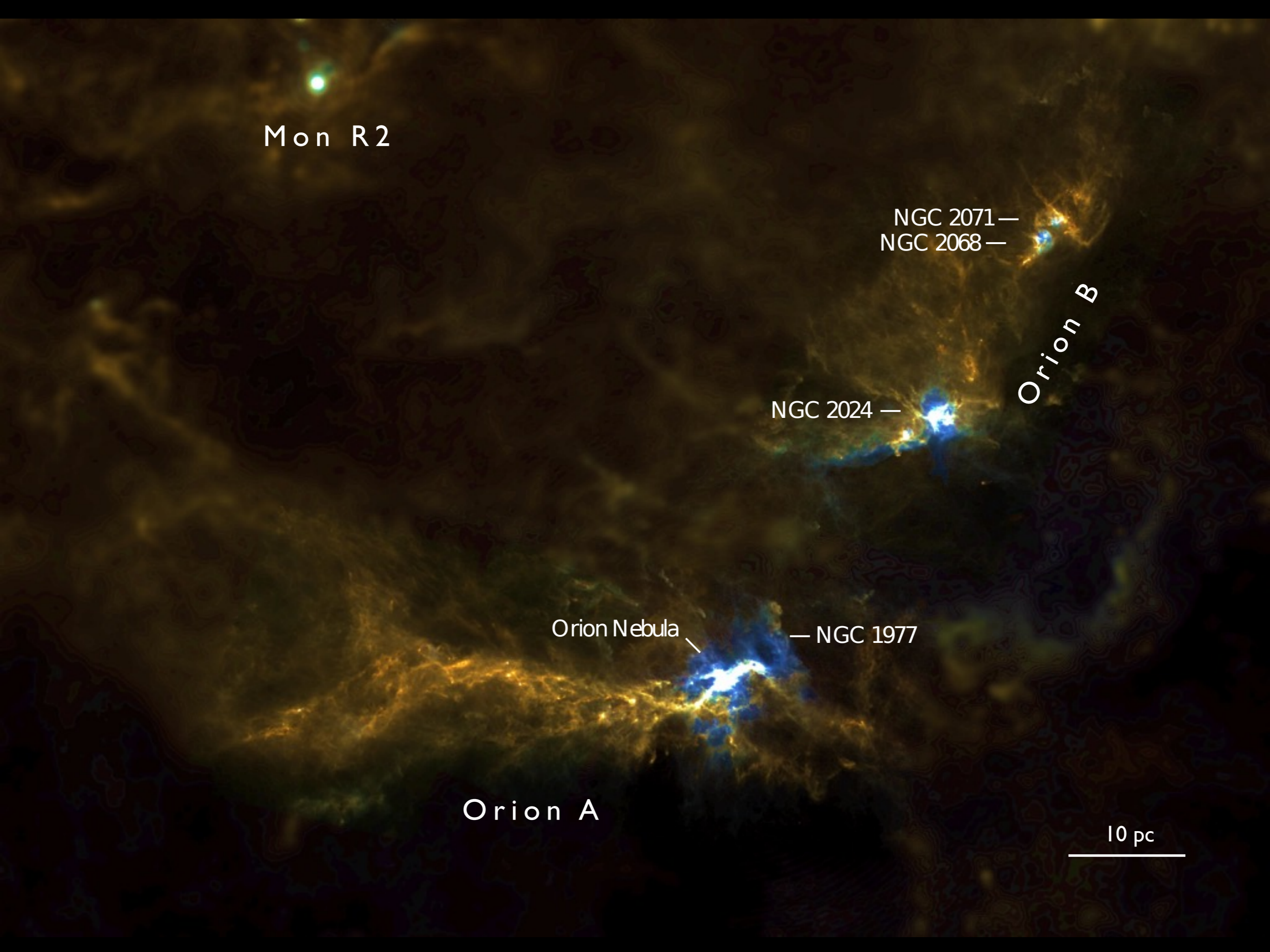
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- Temperature gradients along the l.o.s. bias τ low
- Things almost certainly go wrong near OB associations γ

Orion A & B

(Lombardi et al. 2014)



Mon R2

NGC 2071 —
NGC 2068 —

Orion B

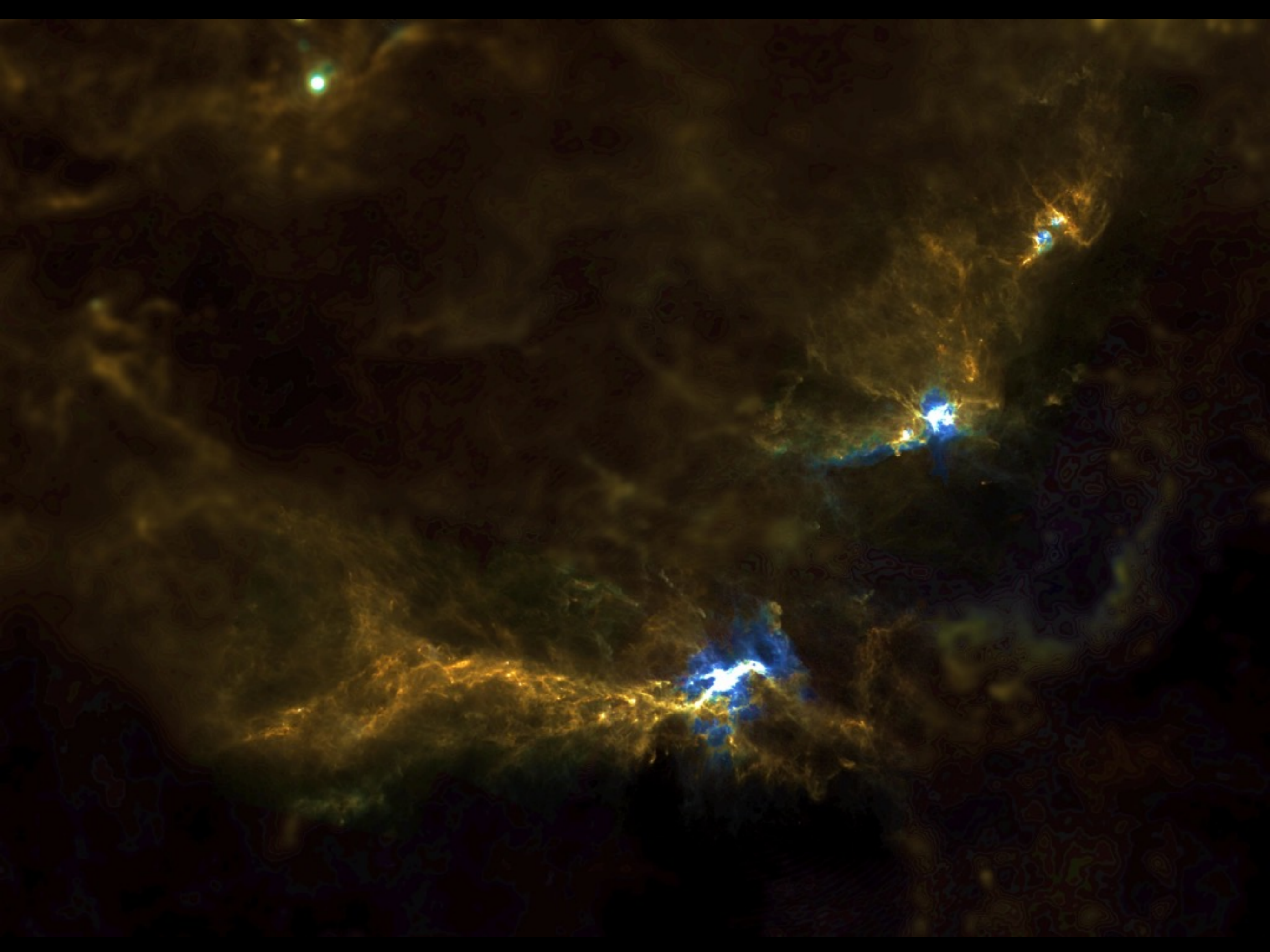
NGC 2024 —

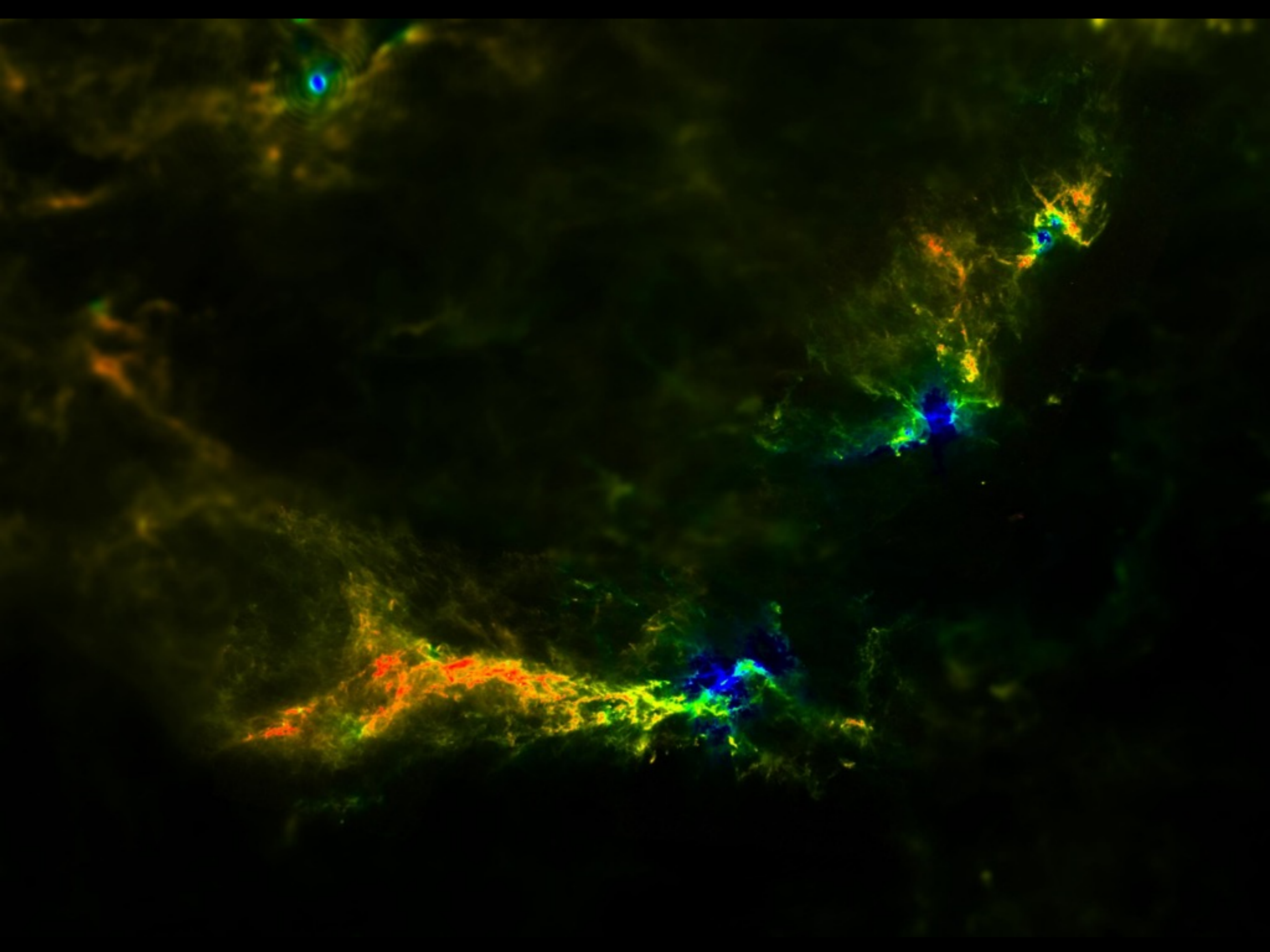
Orion Nebula

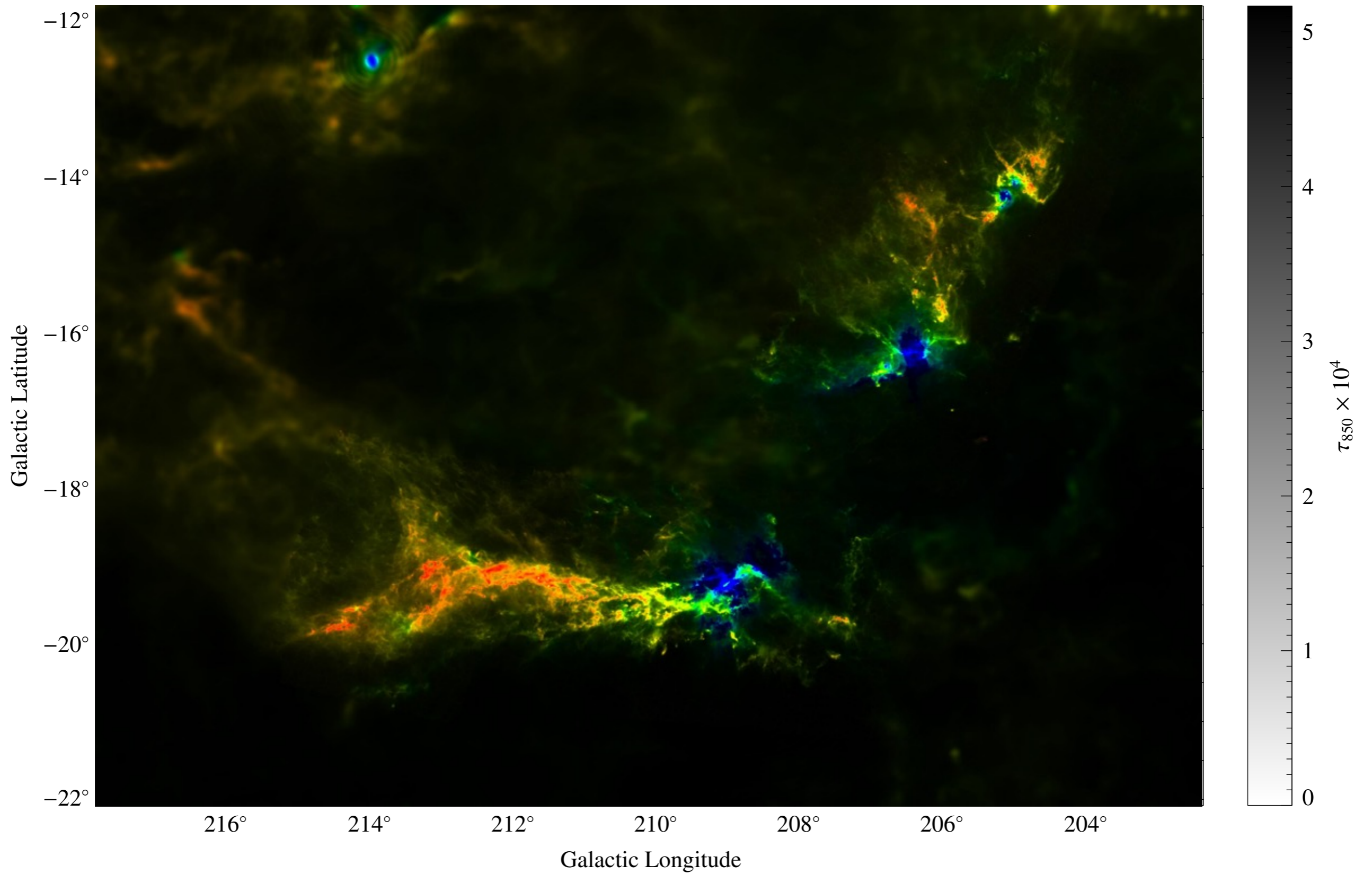
— NGC 1977

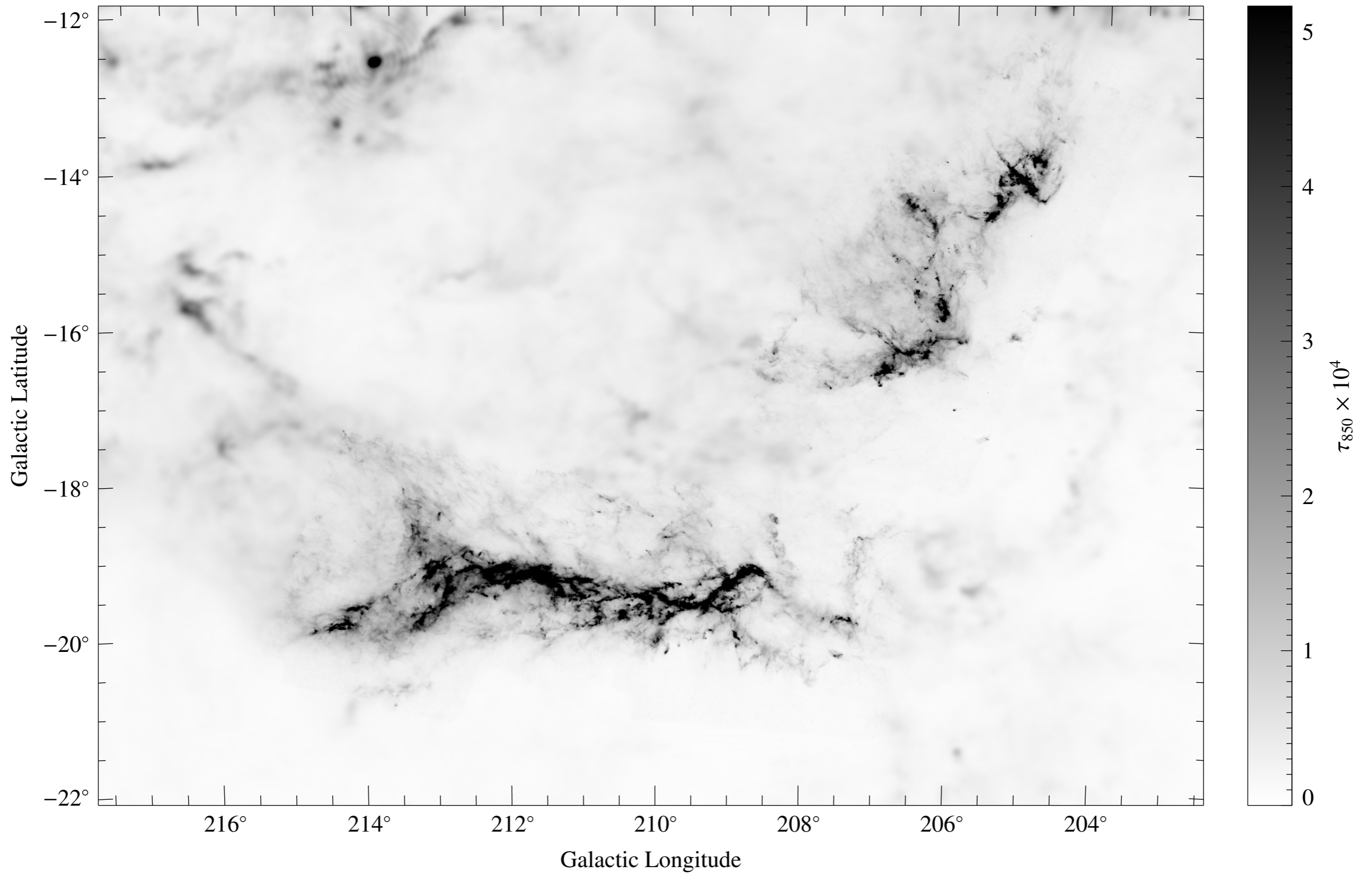
Orion A

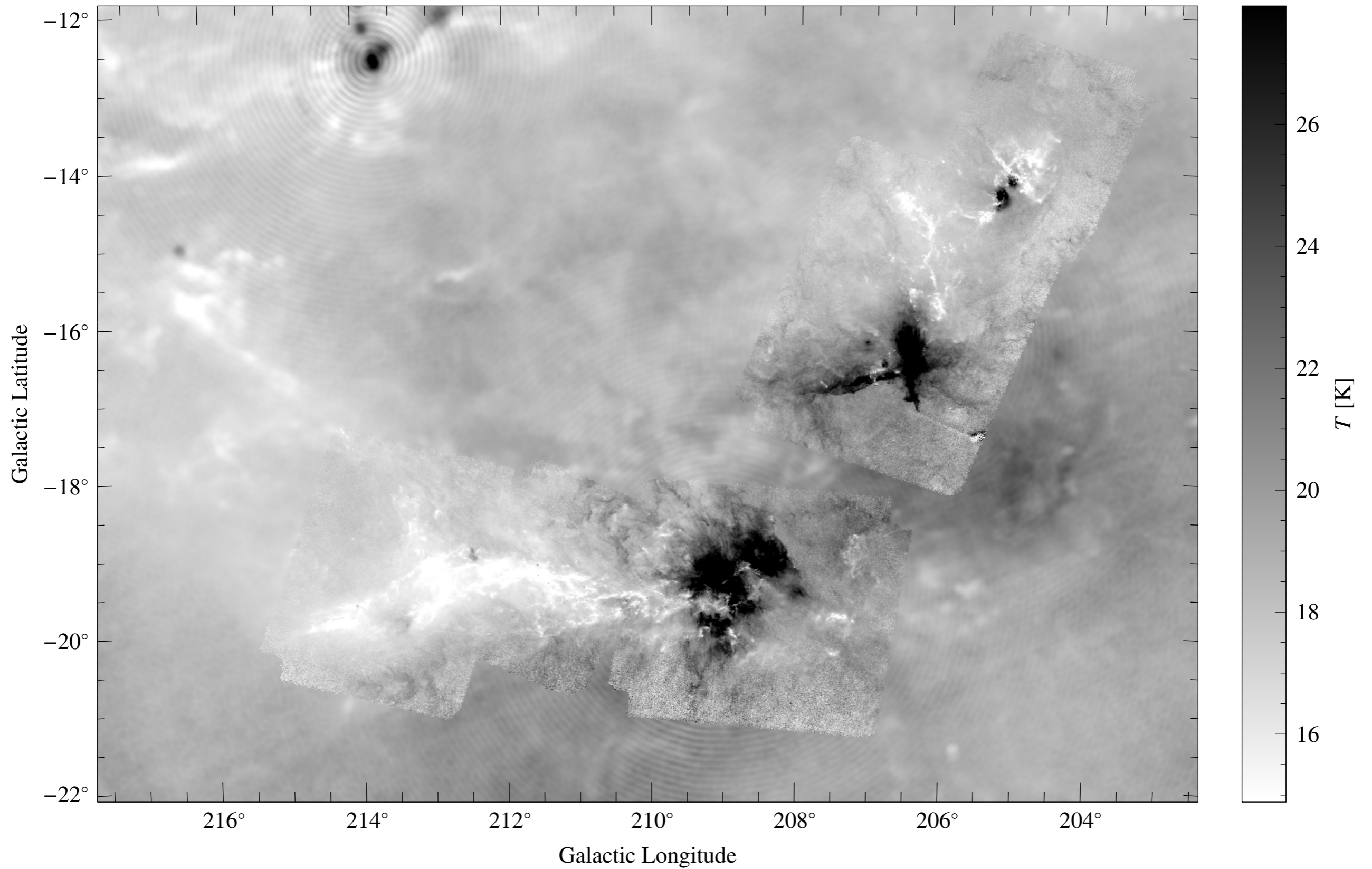
10 pc



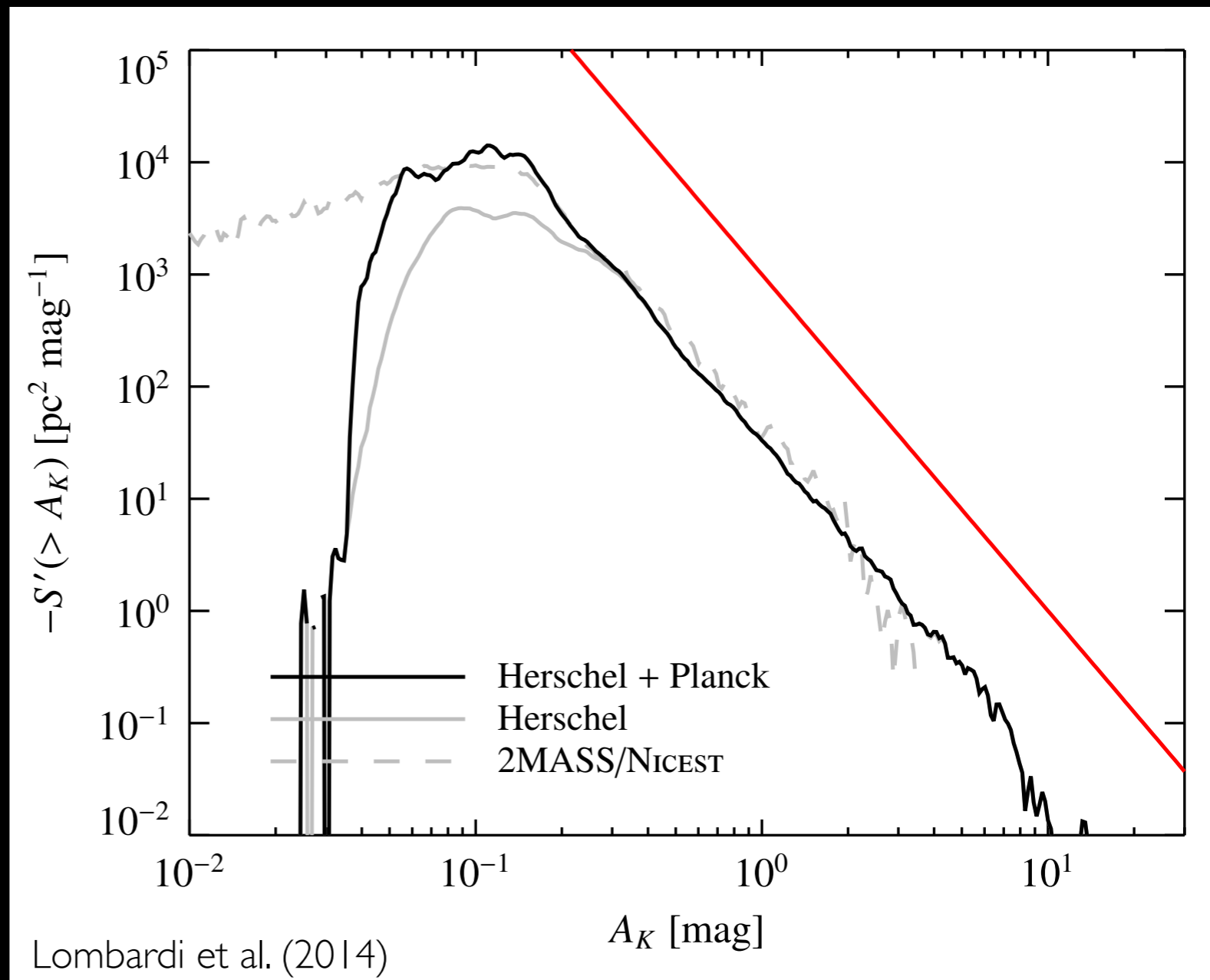






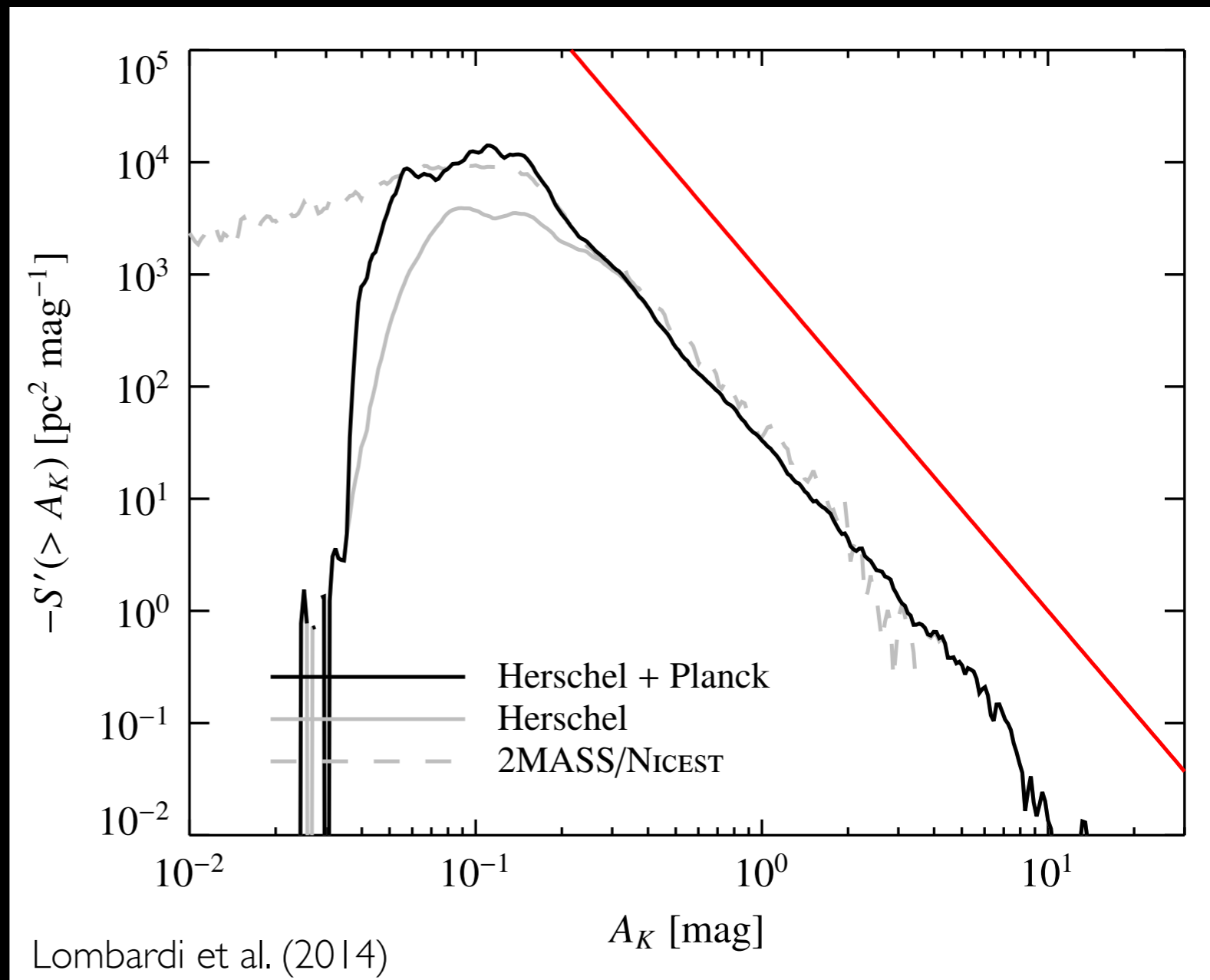


Herschel PDF for Orion B



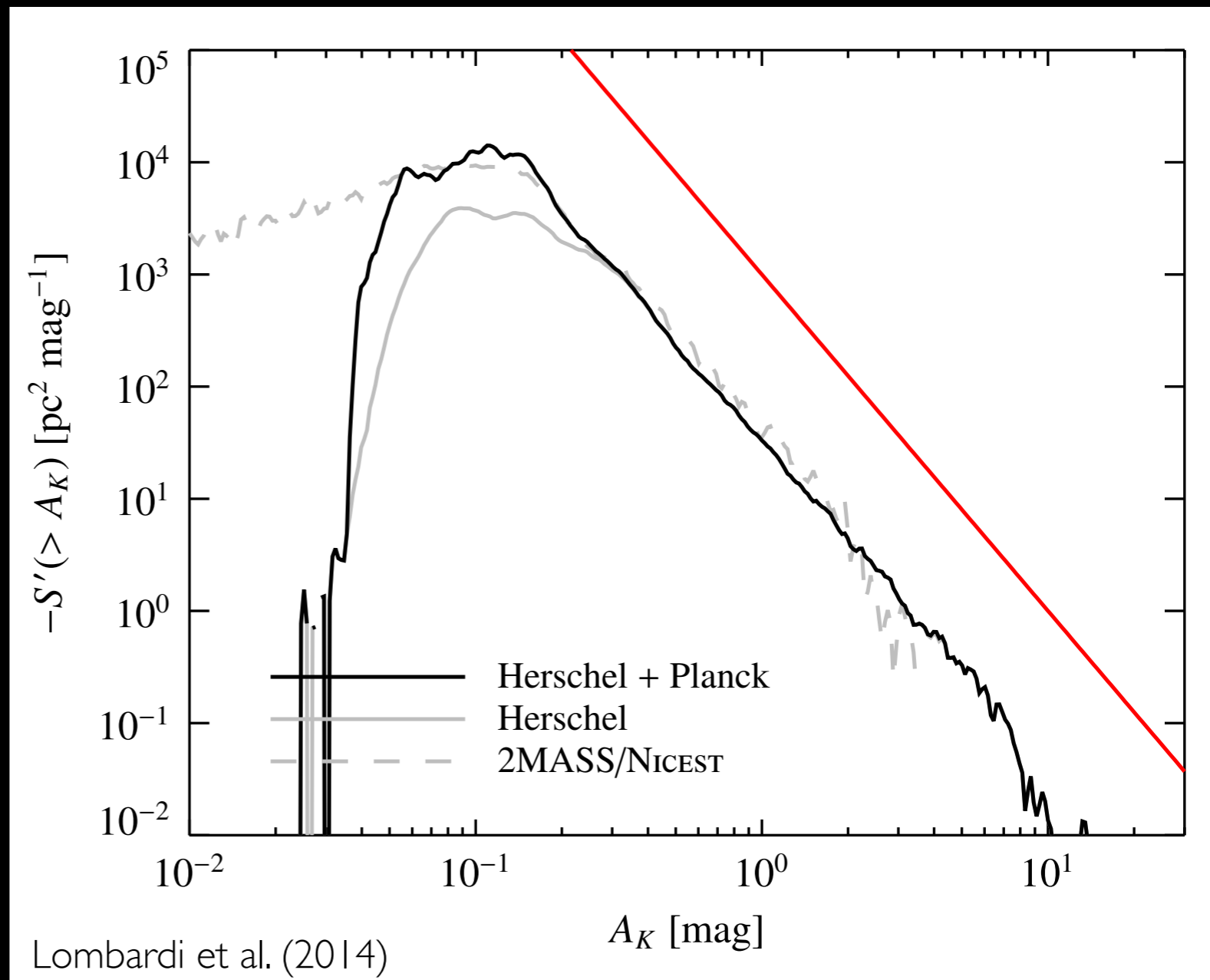
Herschel PDF for Orion B

- PDF is hardly symmetric in log-log



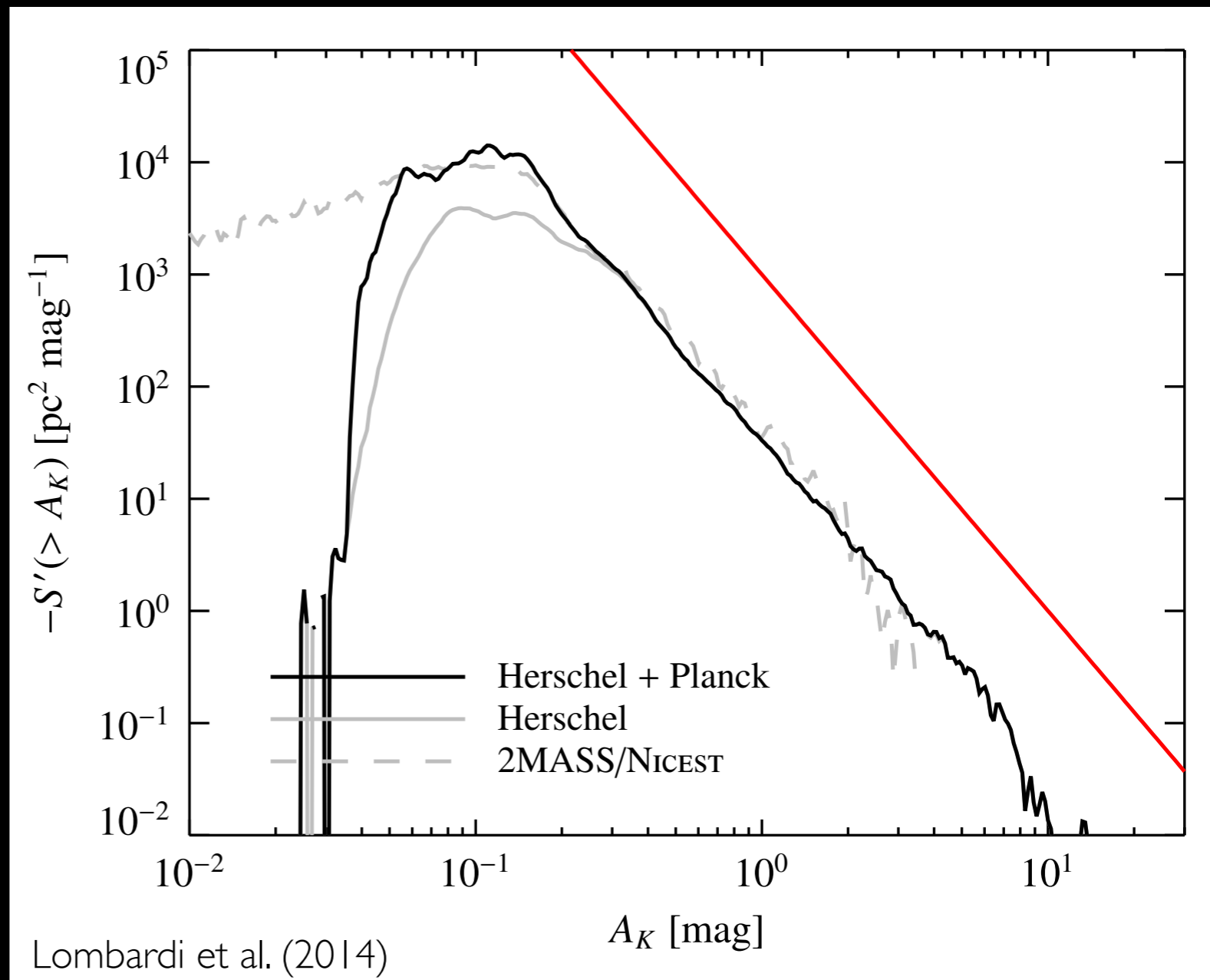
Herschel PDF for Orion B

- PDF is hardly symmetric in log-log
- Turn @ $A_K \sim 0.15$ mag



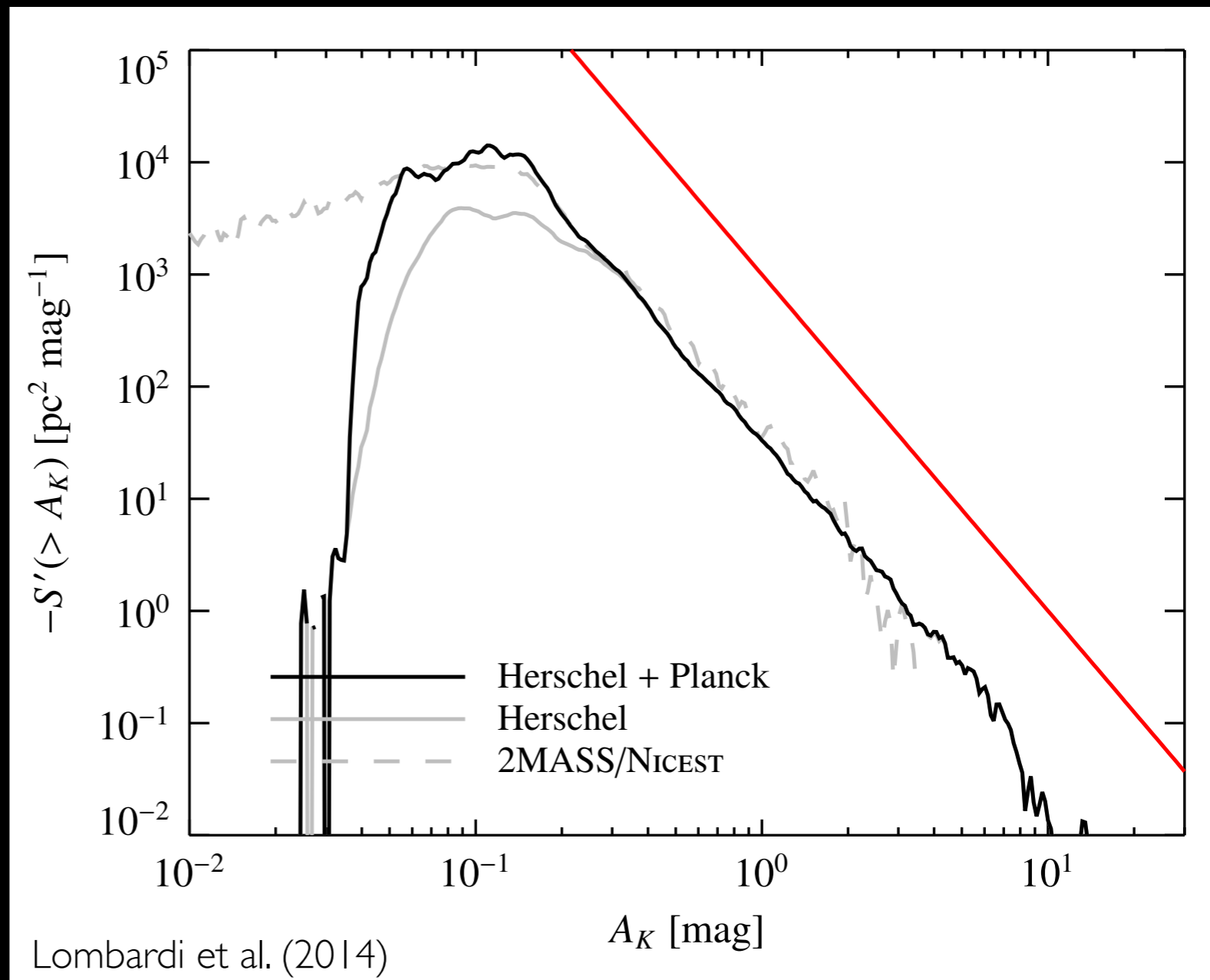
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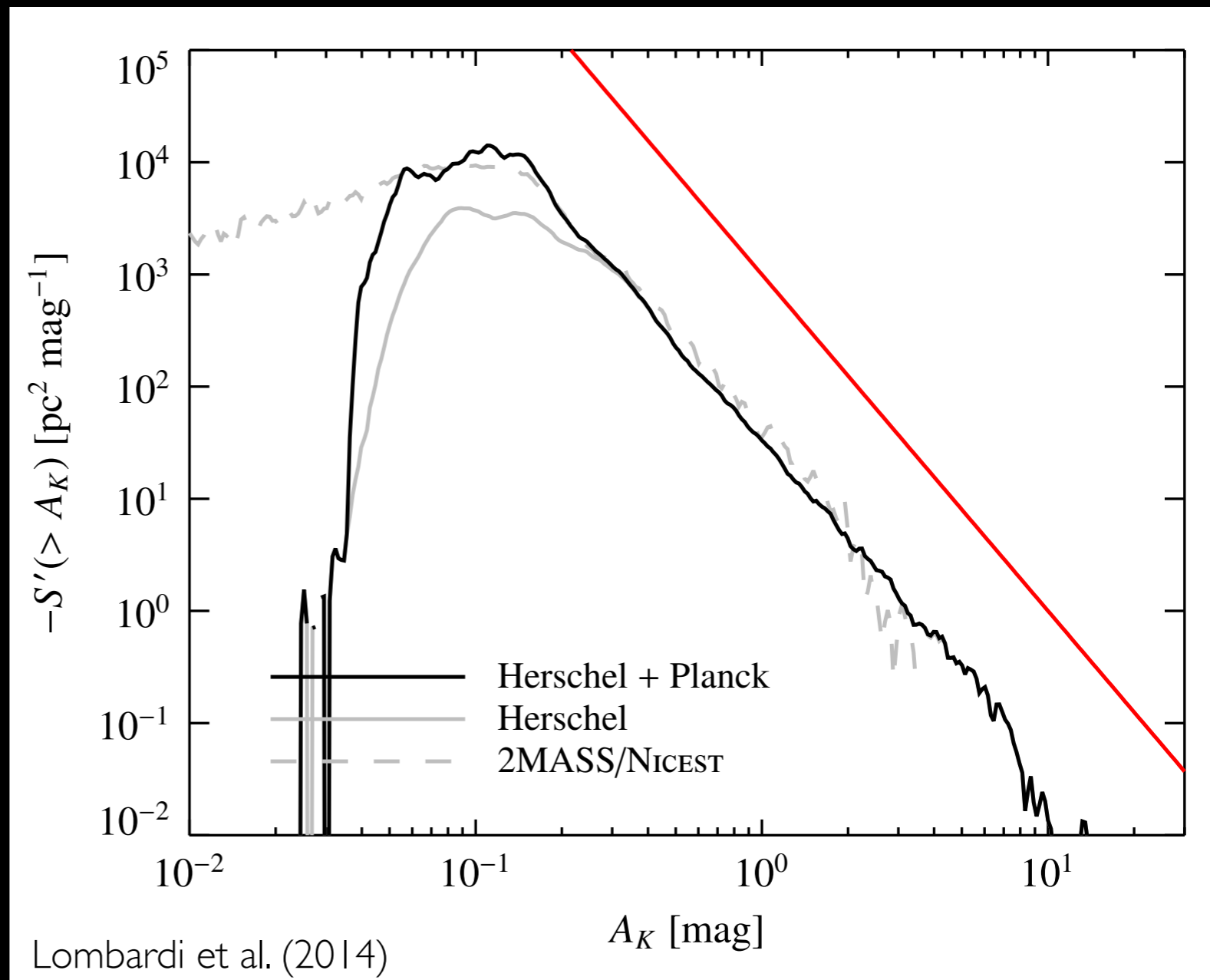
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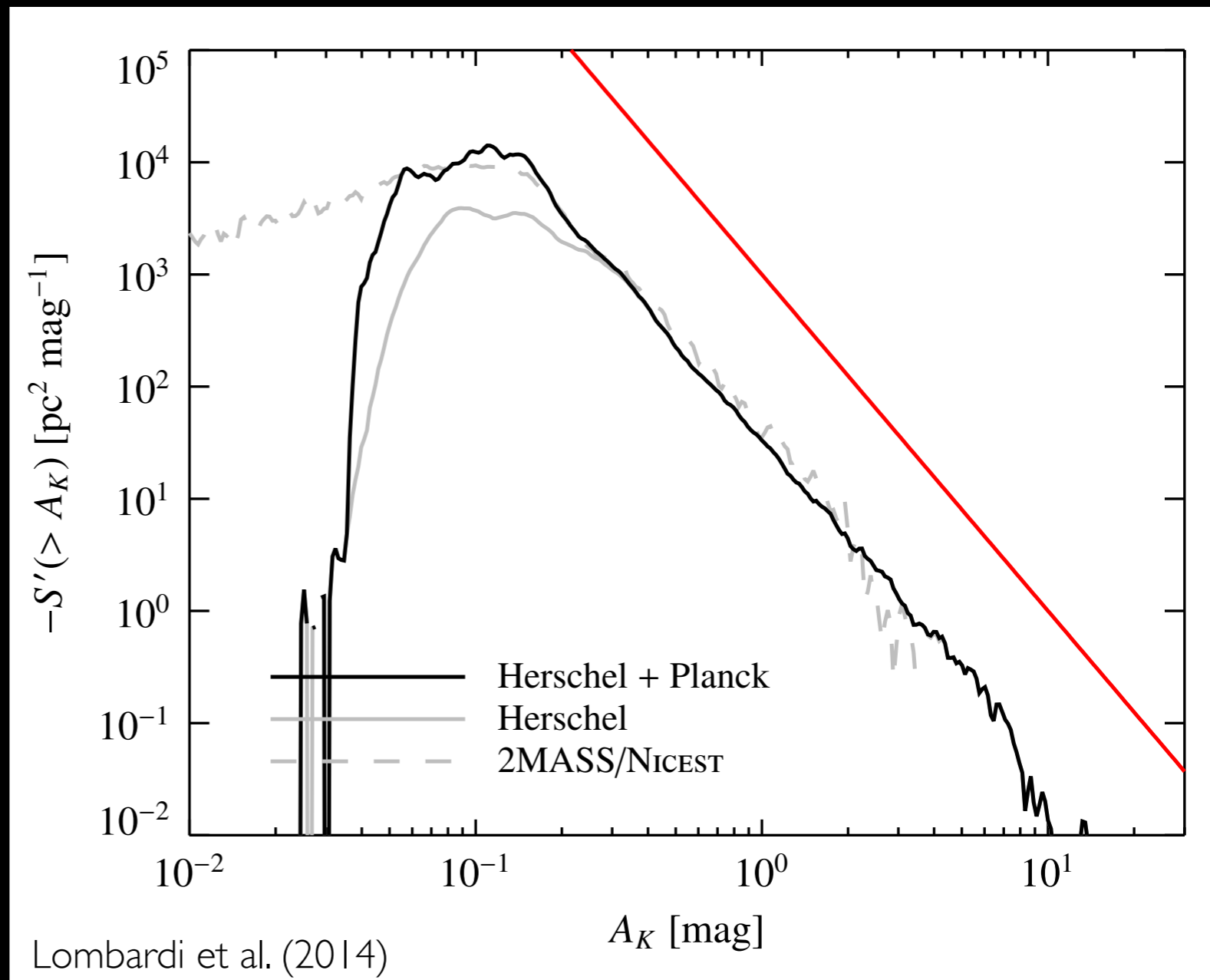
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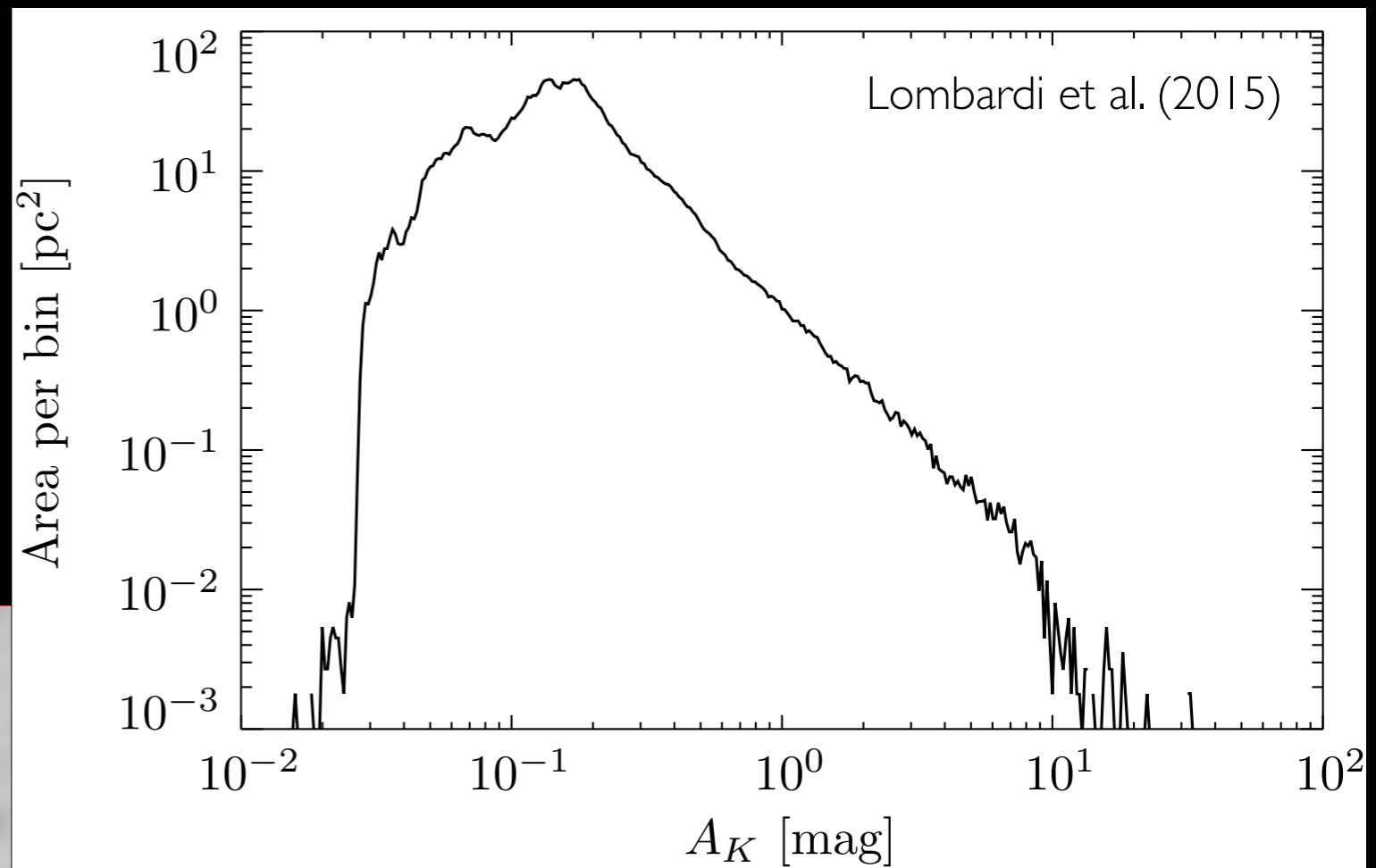
Log-normals, if present, confined to low A_K

Can we actually probe the low A_K ?

Lombardi et al. (2015)

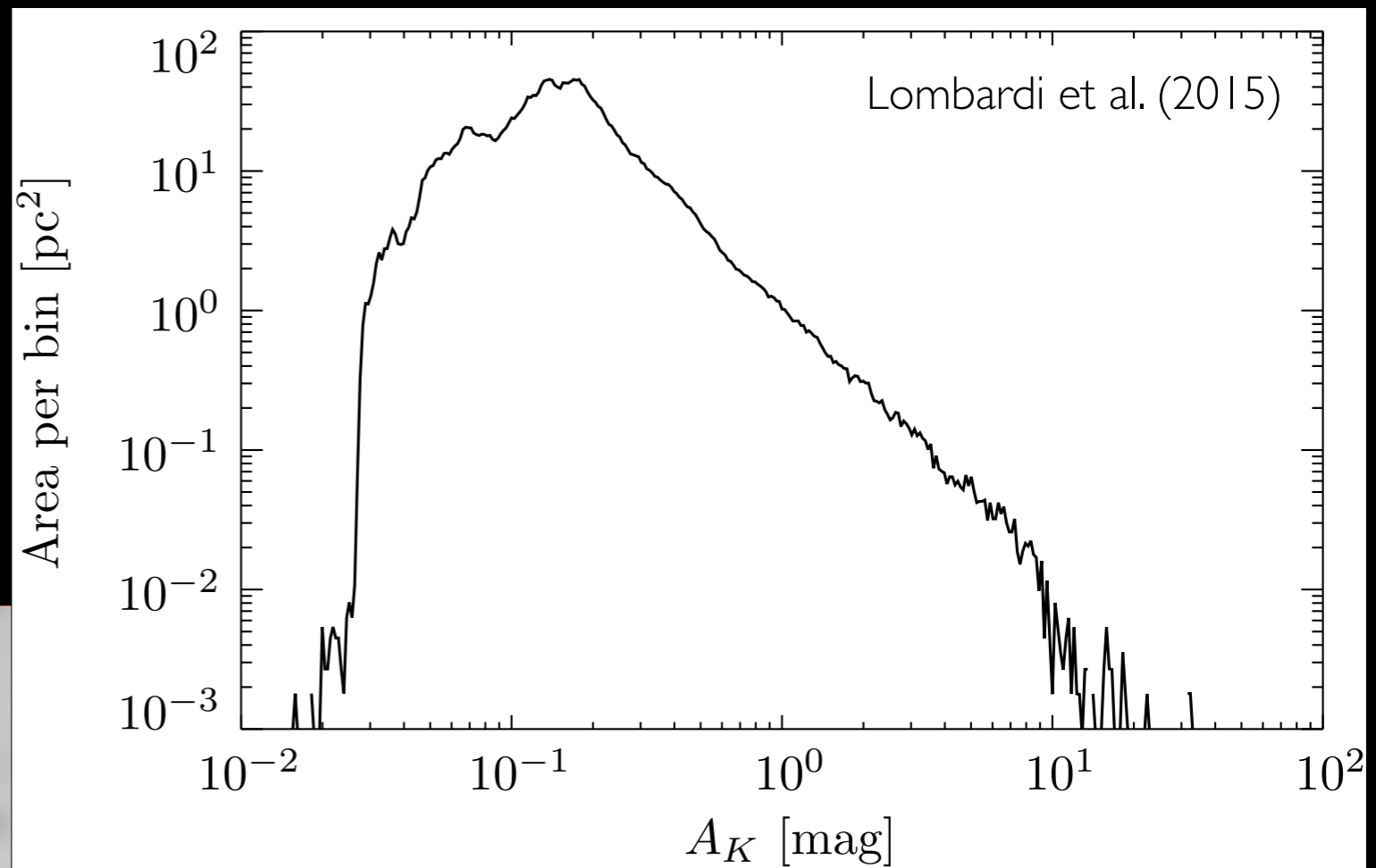
Can we actually probe the low A_K ?

- Cloud boundaries are not well defined!



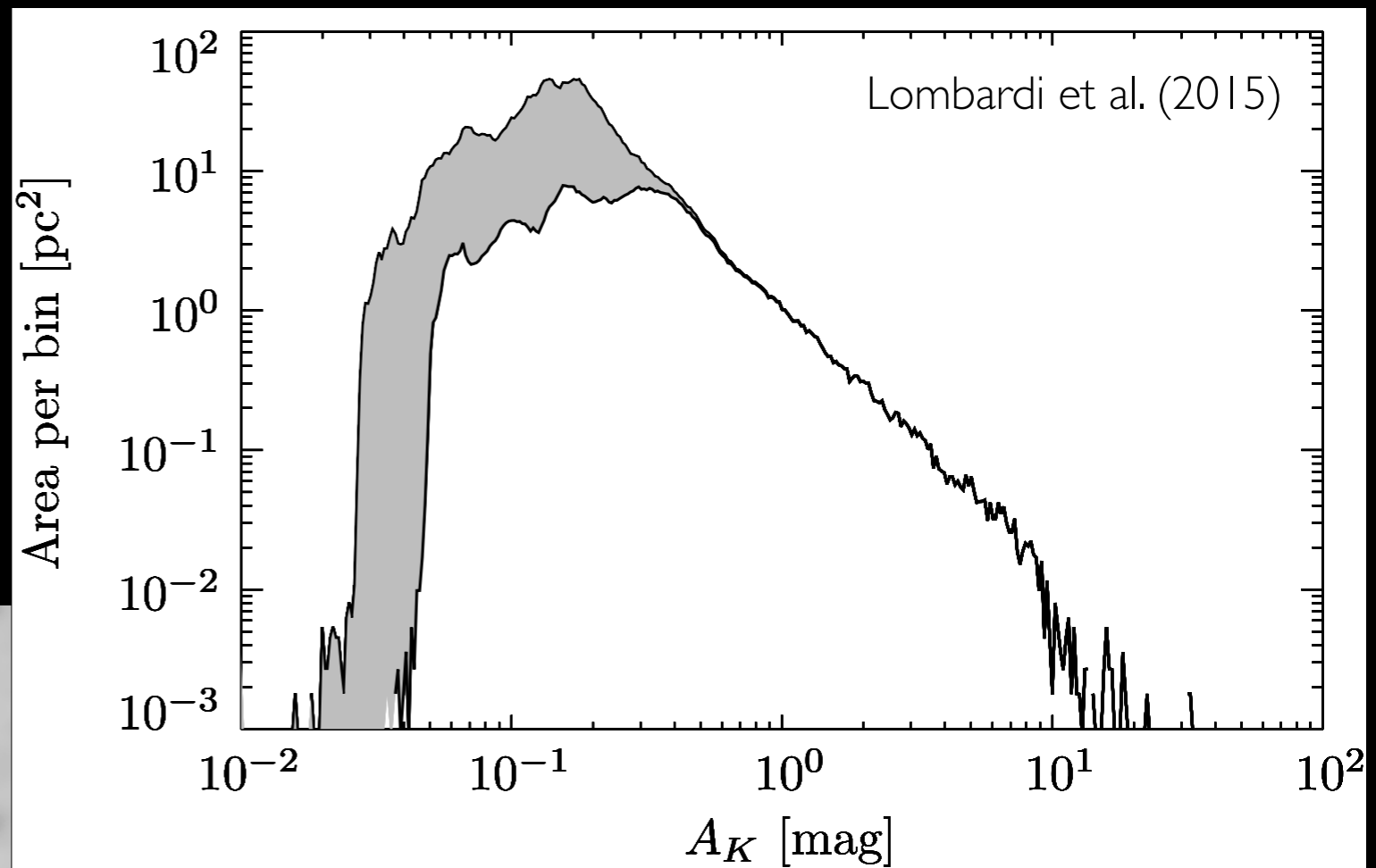
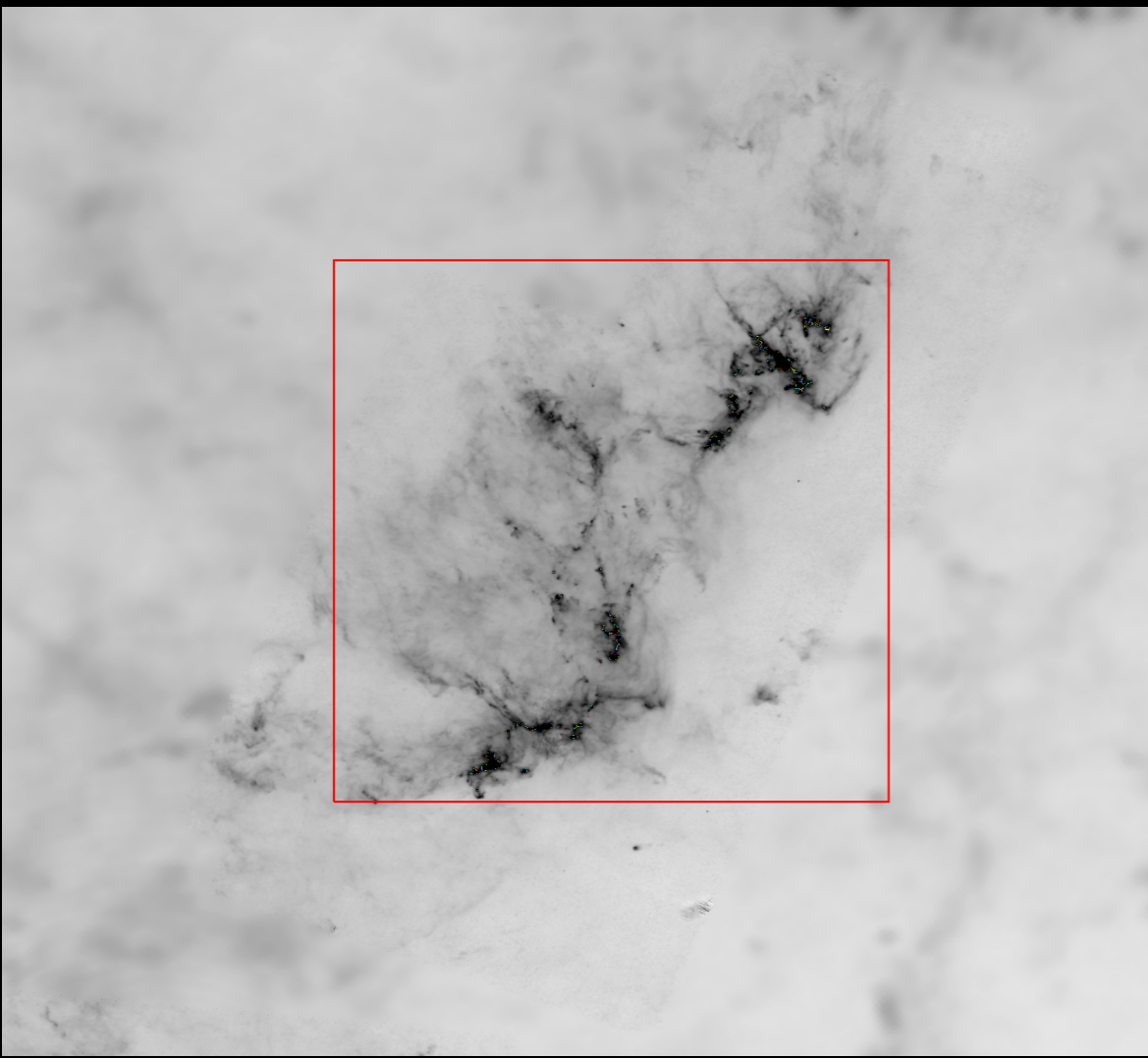
Can we actually probe the low A_K ?

- Cloud boundaries are not well defined!
- Different boundaries produce different PDFs at low A_K



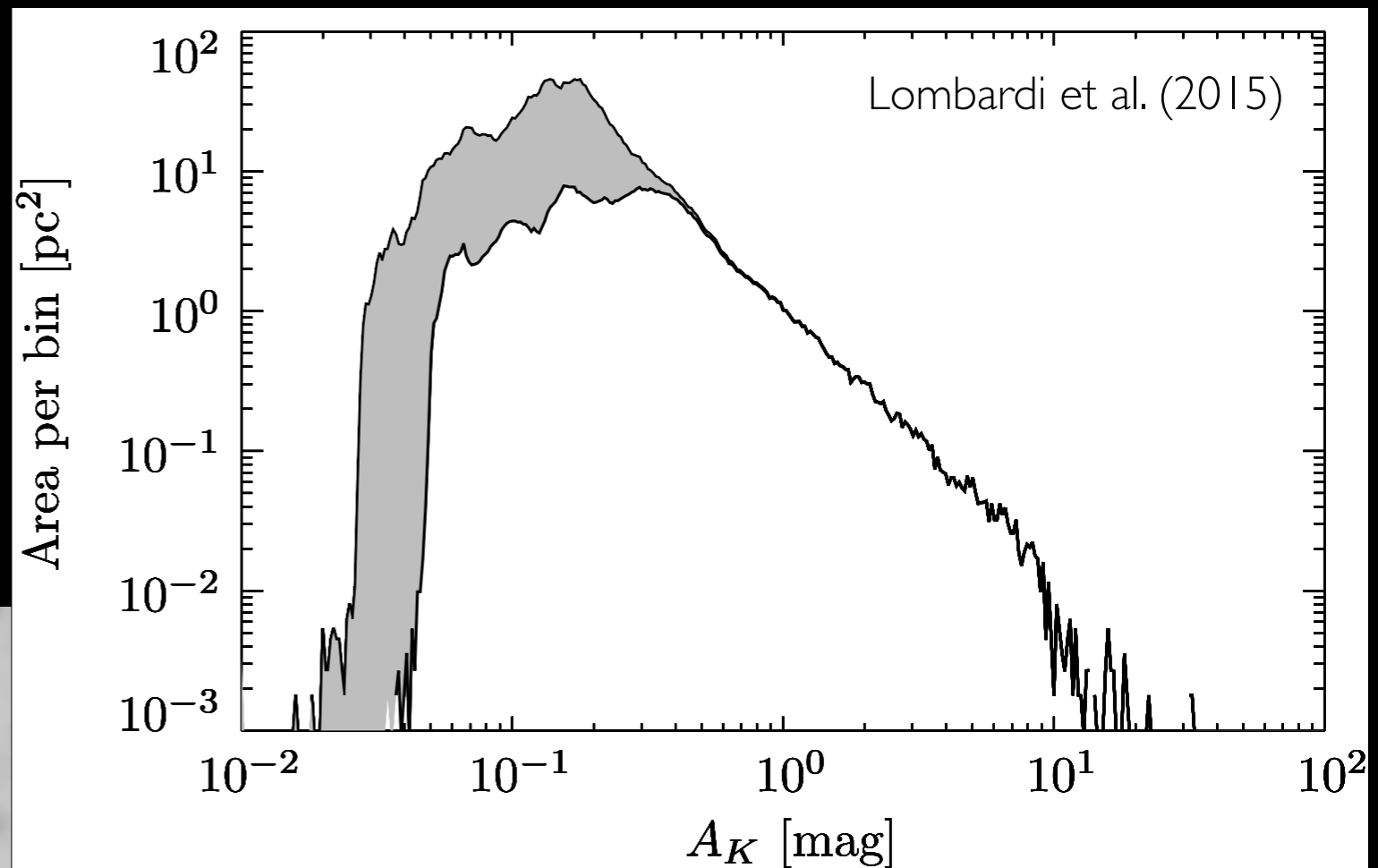
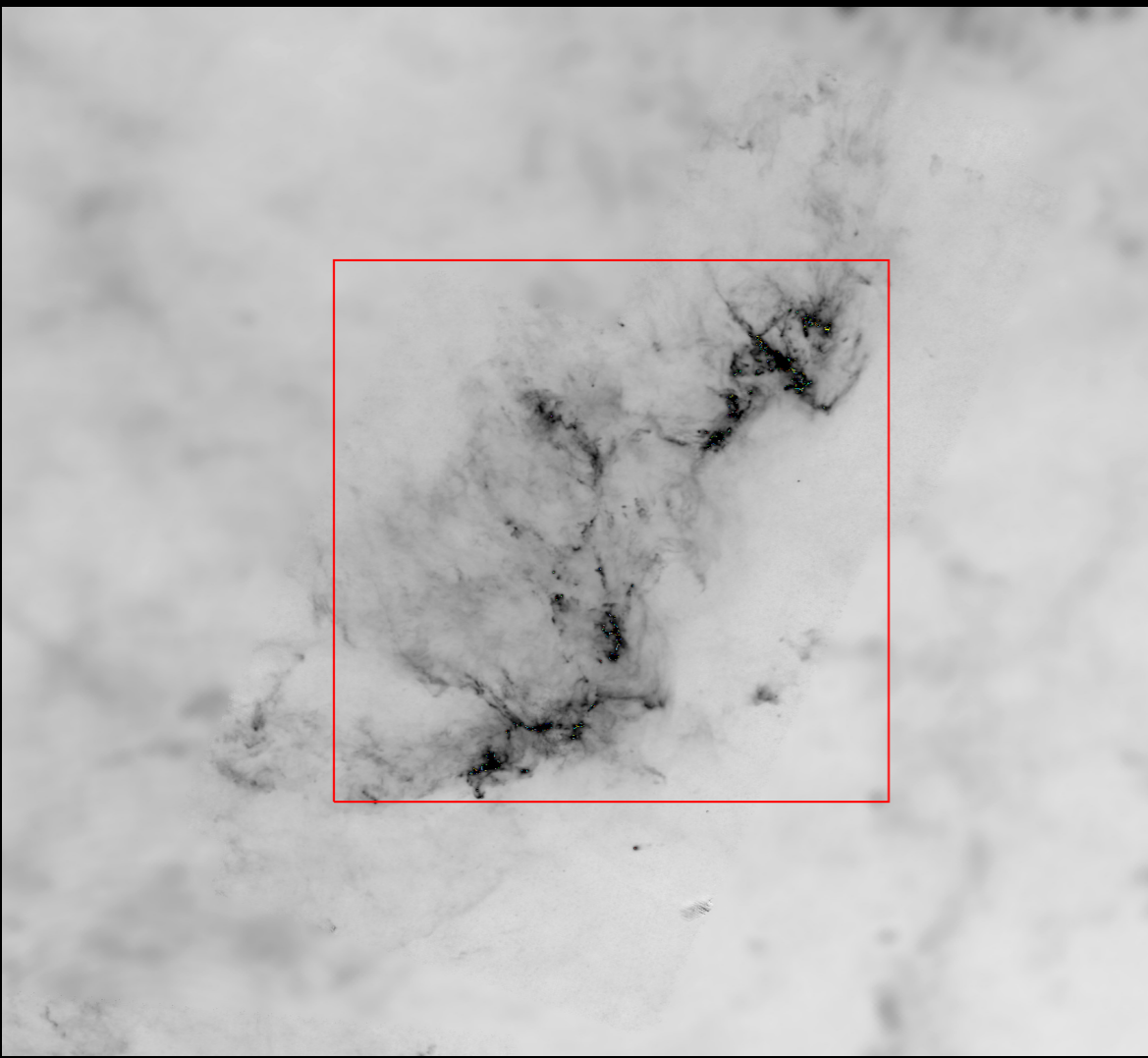
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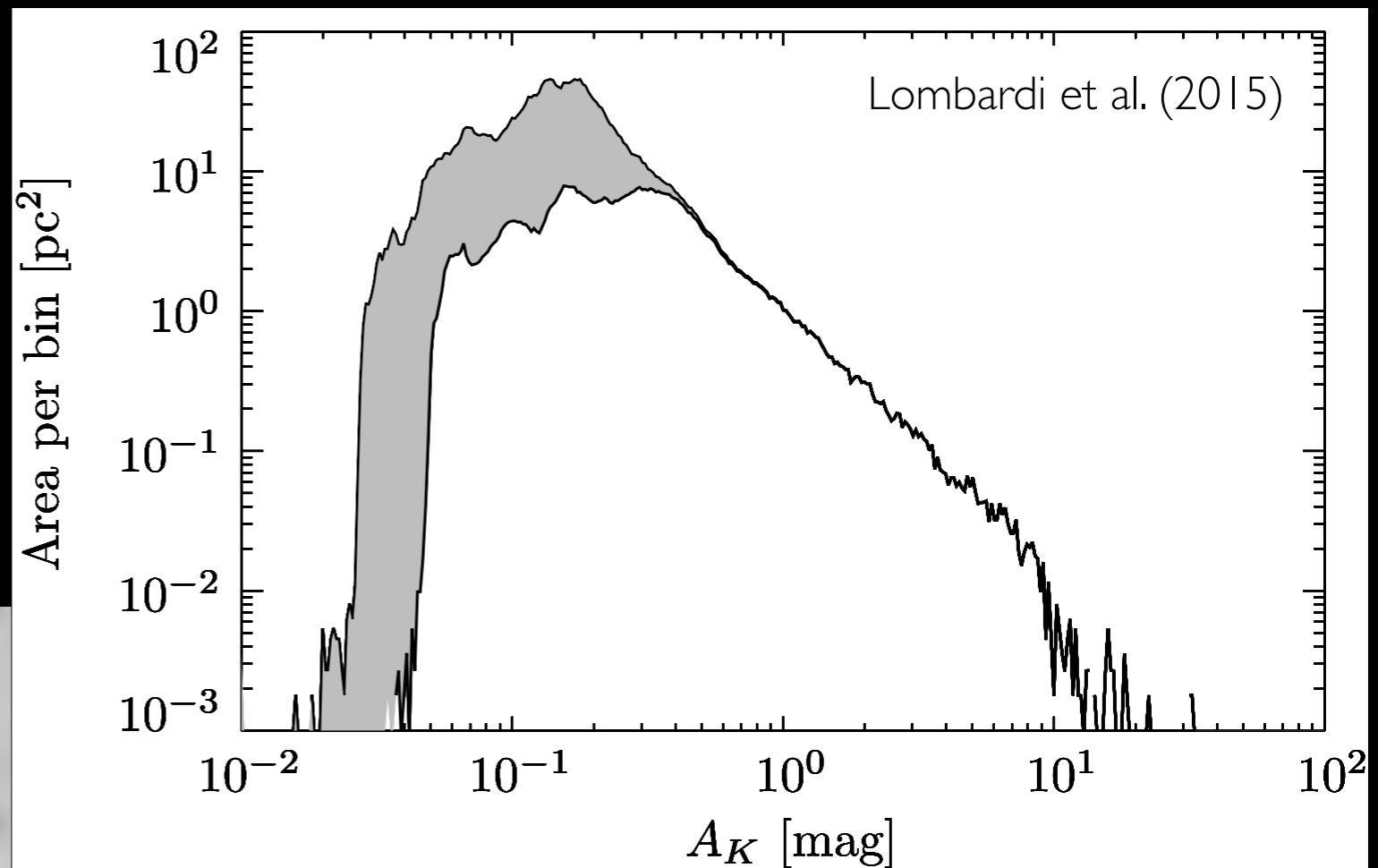
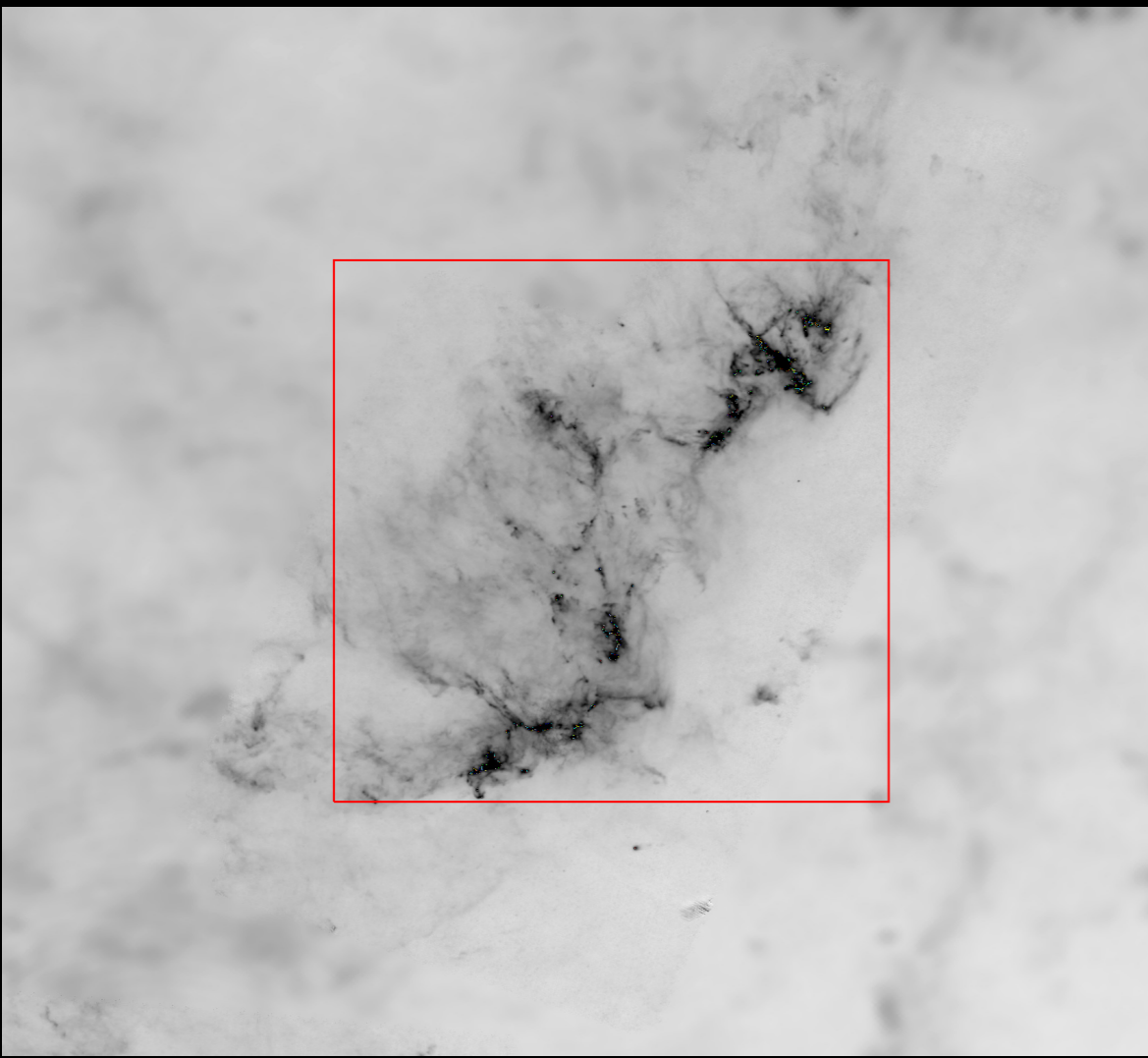
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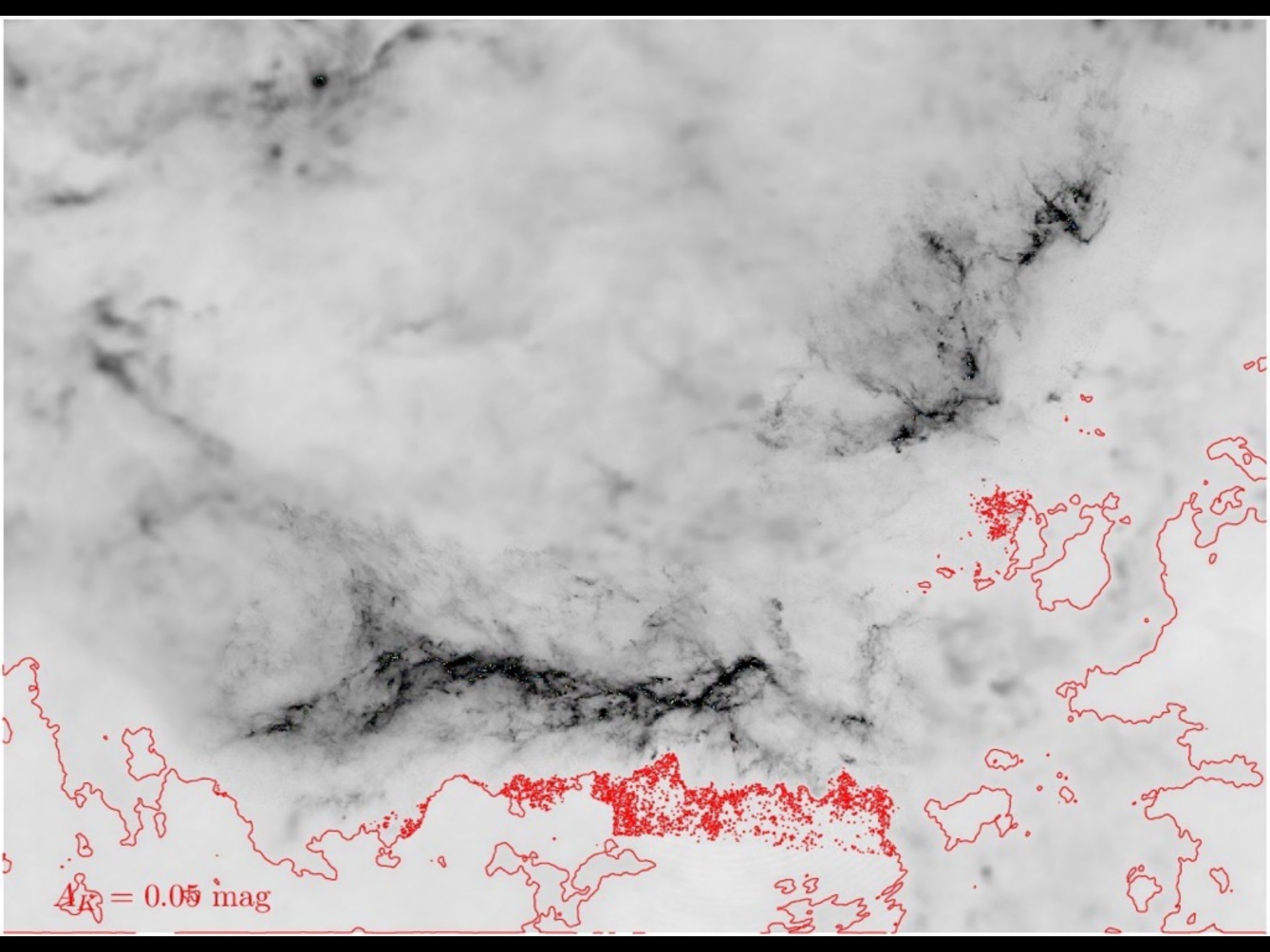
- The only sensible definition of a cloud boundary is using iso-density contours.

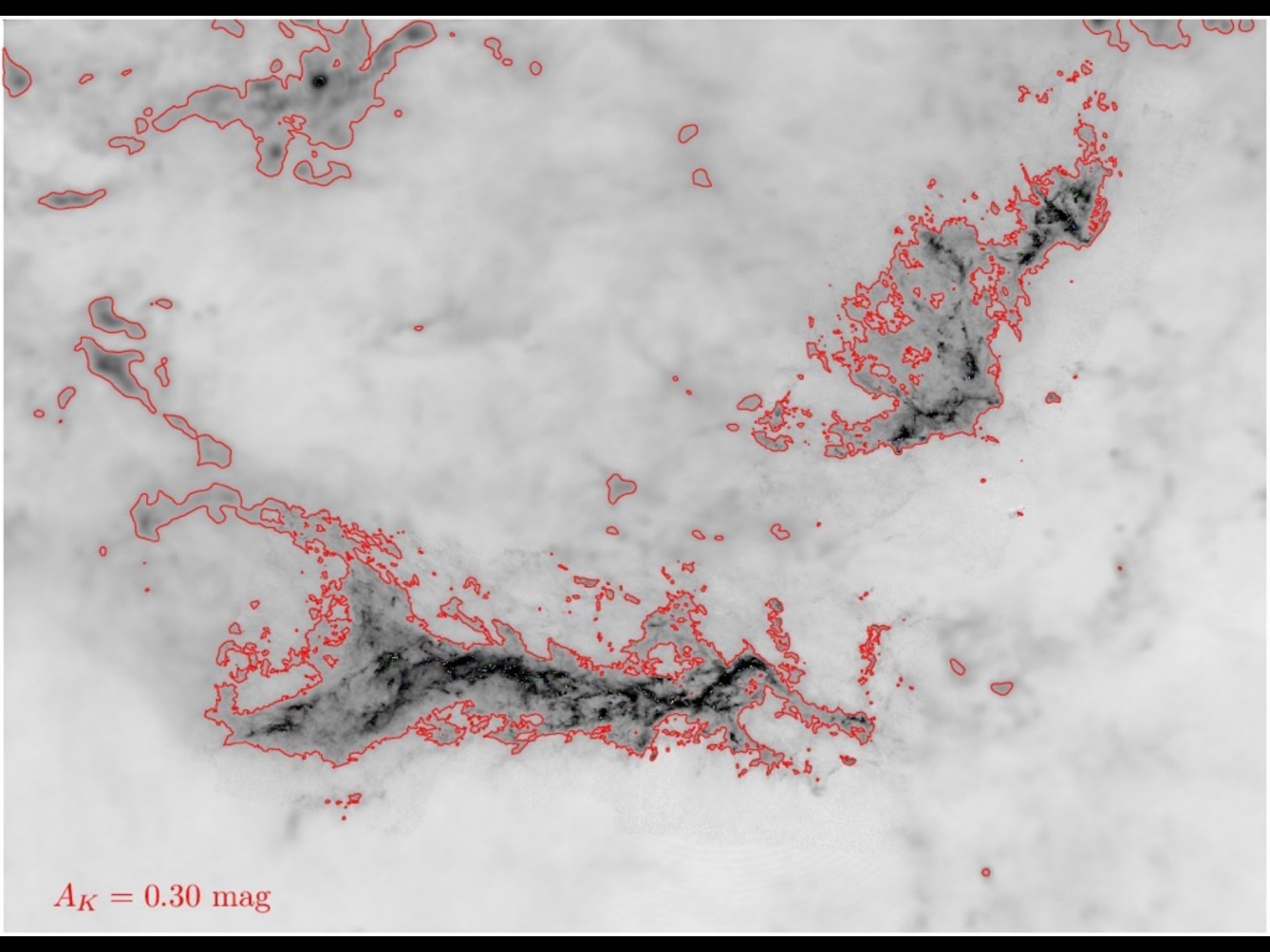
Can we actually probe the low A_K ?

- Cloud boundaries are not well defined!
- Different boundaries produce different PDFs at low A_K



- The only sensible definition of a cloud boundary is using iso-density contours.
- Which contour levels are we able to use securely?





$A_K = 0.30$ mag



Things are actually worse than
they appear



An aerial photograph of a volcanic eruption. A large, dark, billowing plume of ash and steam rises from a central crater, surrounded by a sea of white, fluffy clouds. The sky is a deep blue with wispy white clouds. The text "Things are actually worse than they appear" is overlaid in white, sans-serif font in the upper half of the image.

Things are actually worse than
they appear

If something can go wrong, it will.

An aerial photograph showing a vast, flat landscape, possibly a salt flat or a desert, under a clear blue sky. The ground is a mix of light and dark patches, suggesting different mineral compositions or perhaps a thin layer of water reflecting the sky. In the foreground, there is a large, dark, irregularly shaped cloud formation, possibly a volcanic plume or a large fire, which stands out against the lighter ground. The overall scene is desolate and expansive.

Things are actually worse than
they appear

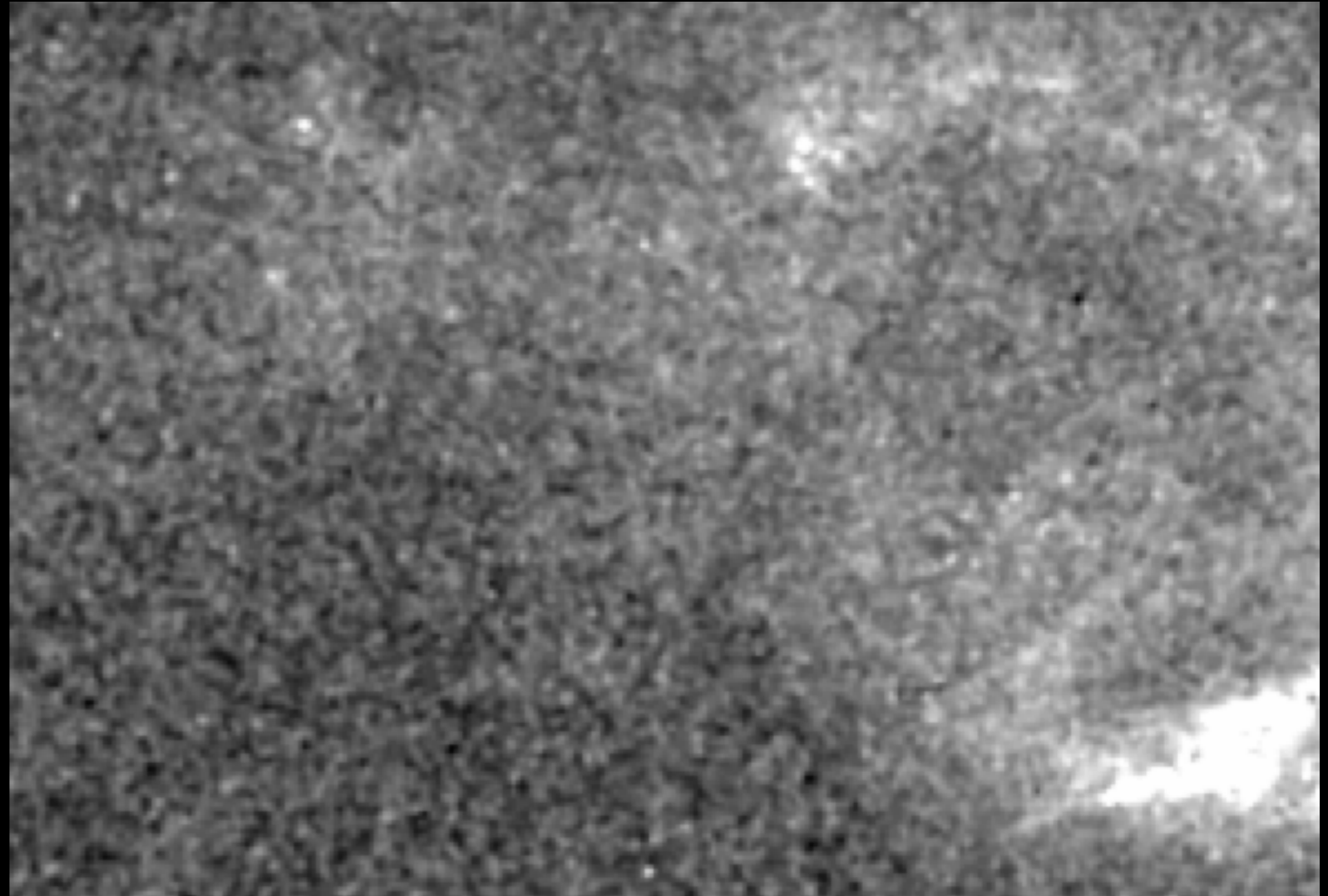
If something cannot go wrong, it will anyway.





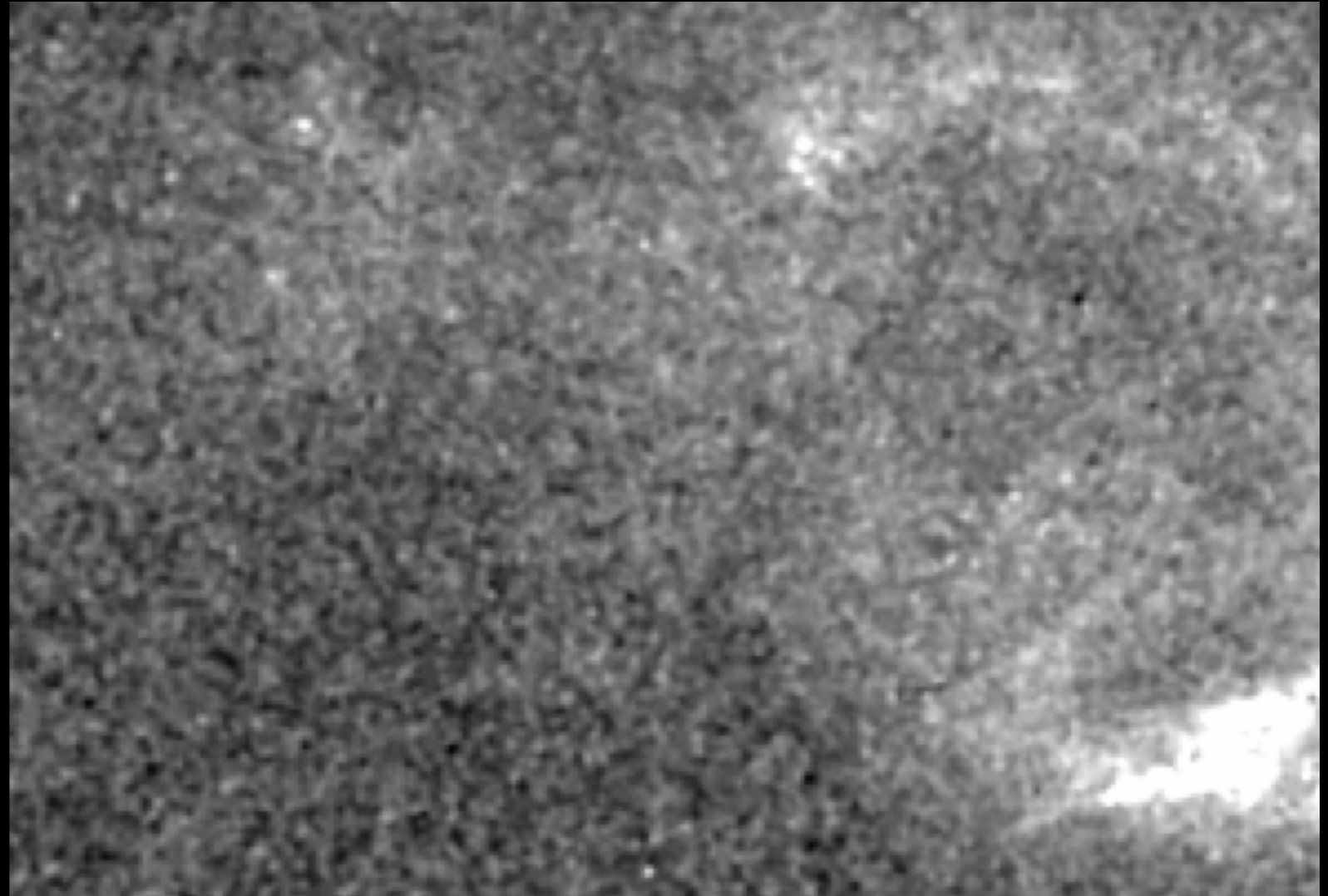


Low-column density part of PDFs



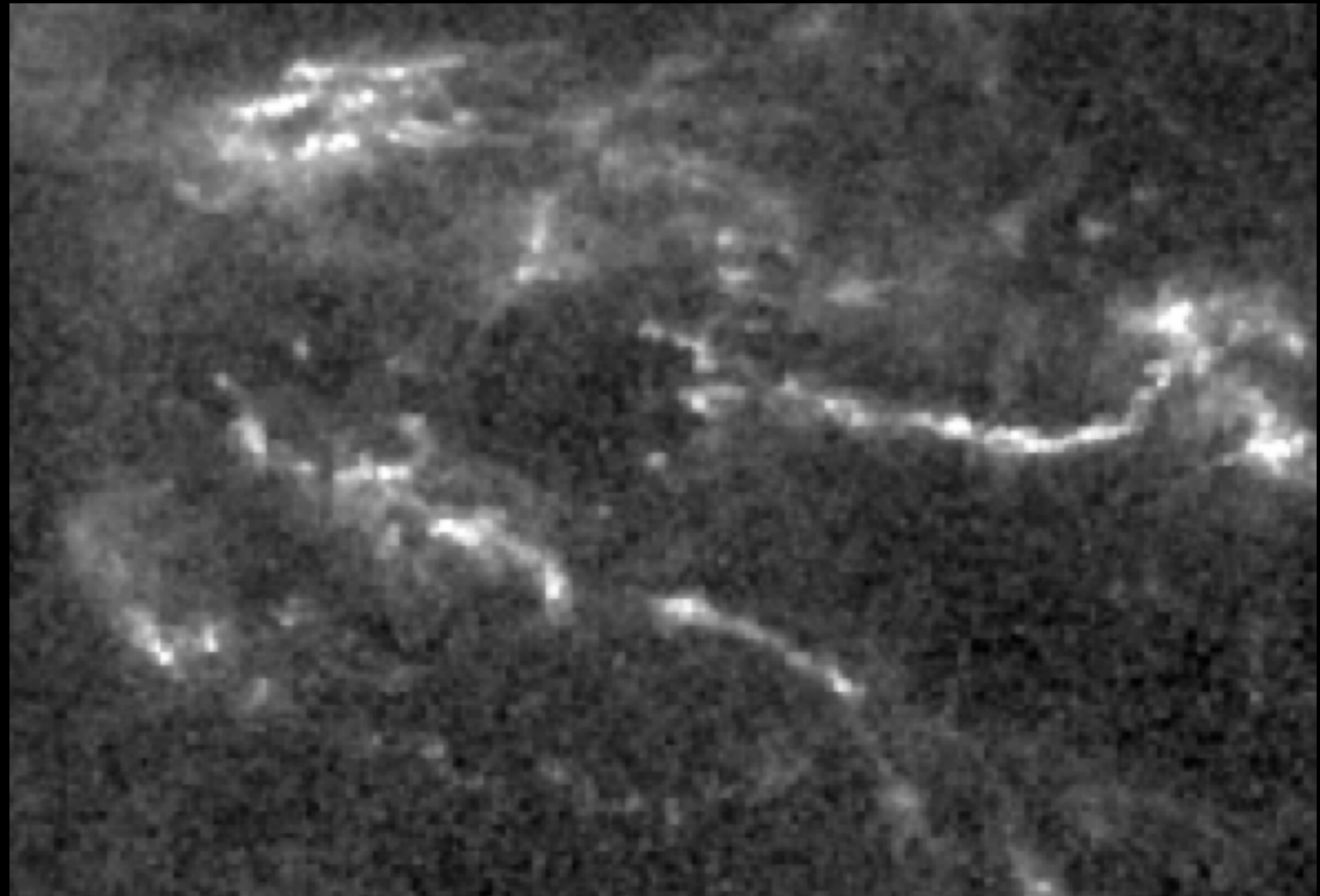
Low-column density part of PDFs

- Noise can be significant at low column densities



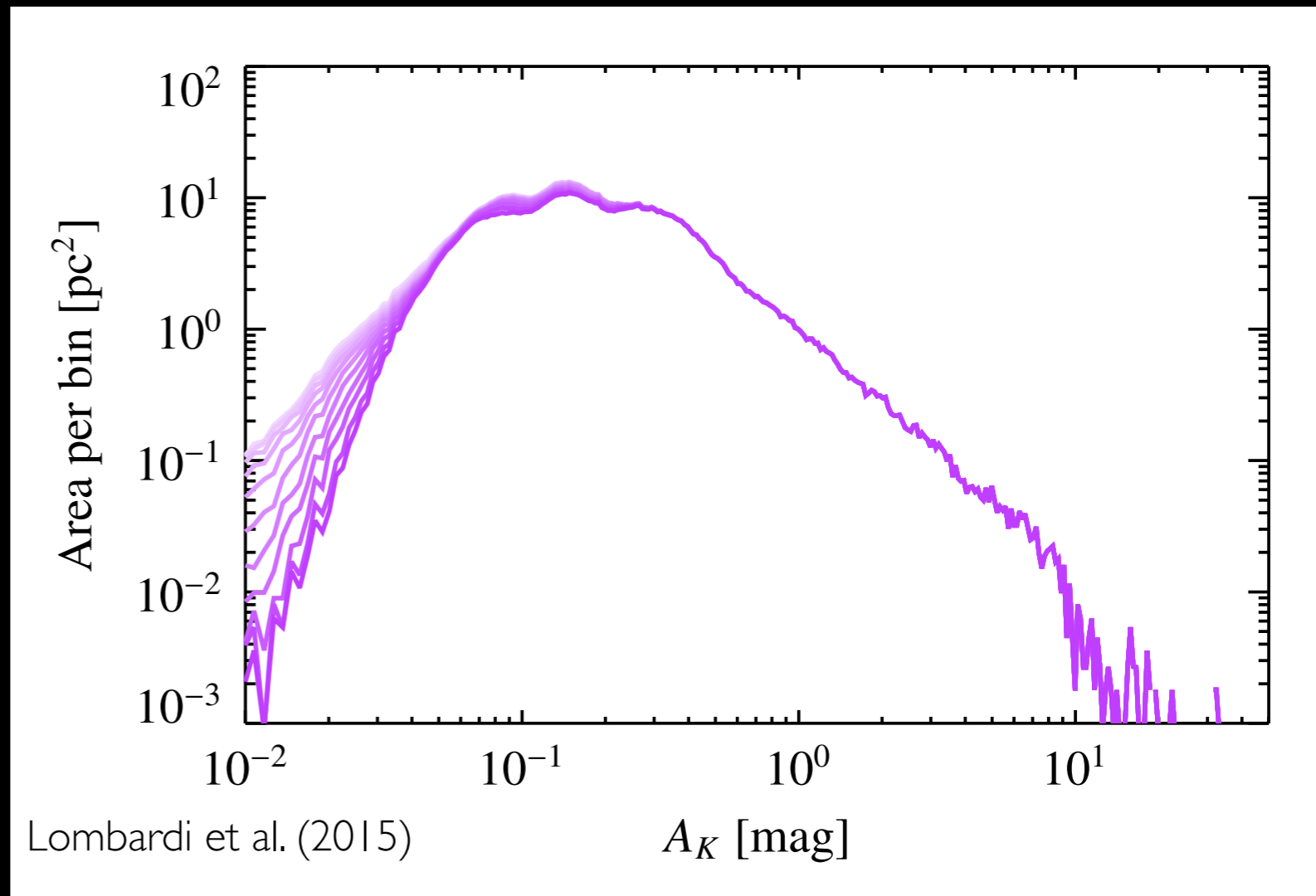
Low-column density part of PDFs

- Noise can be significant at low column densities
- Resolution effects (all bins): hard to model...



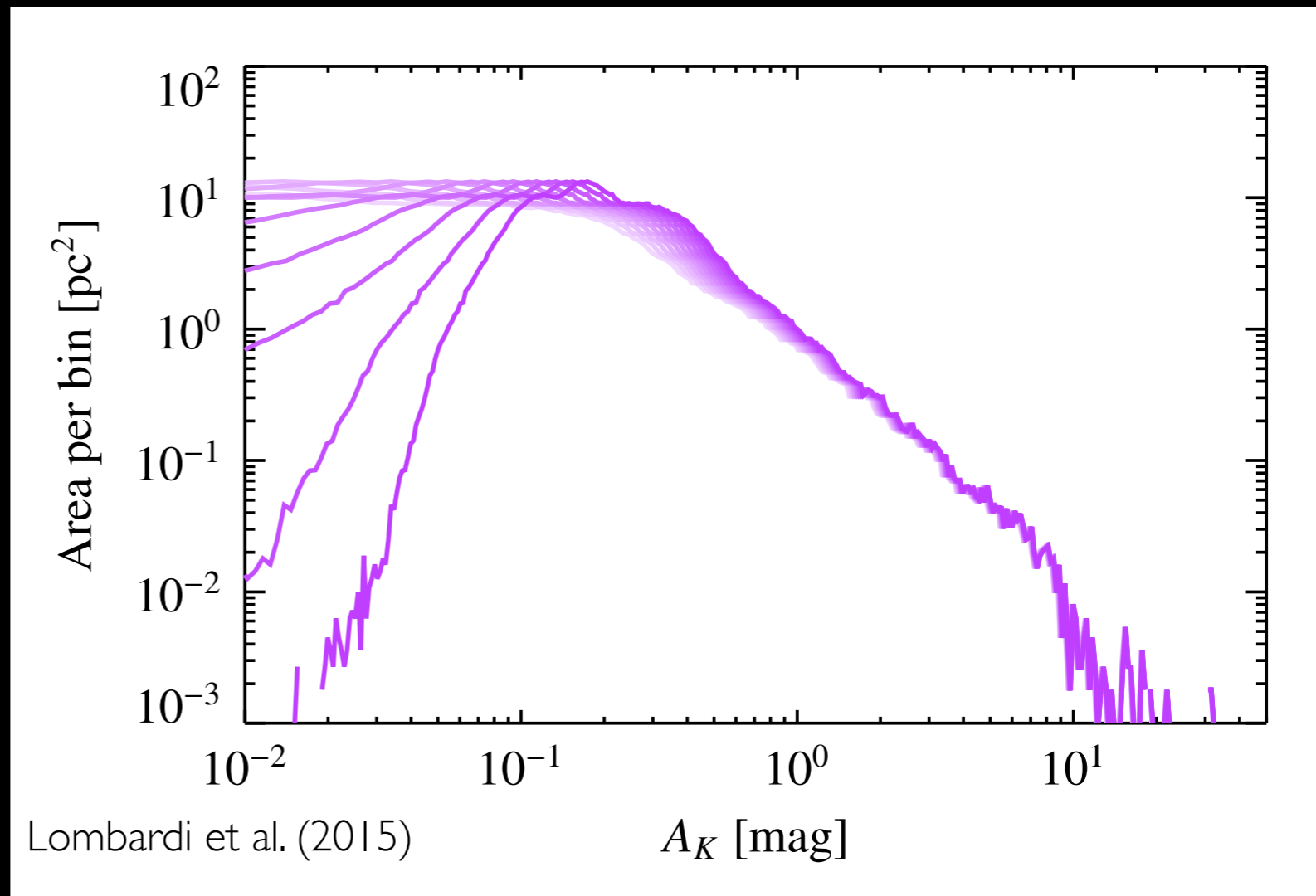
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- Cloud boundaries always (somewhat) arbitrary



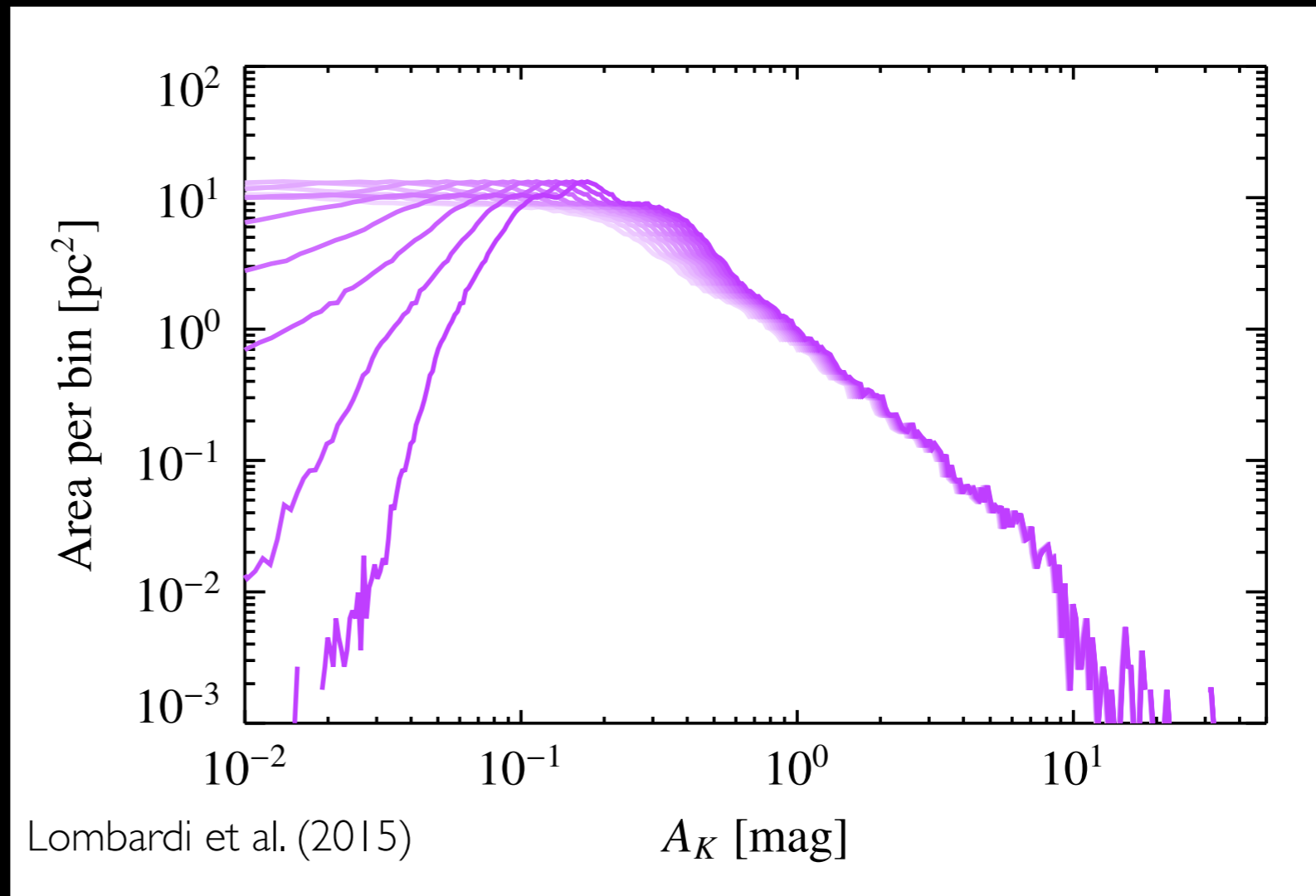
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- Superposition by unrelated material along the los



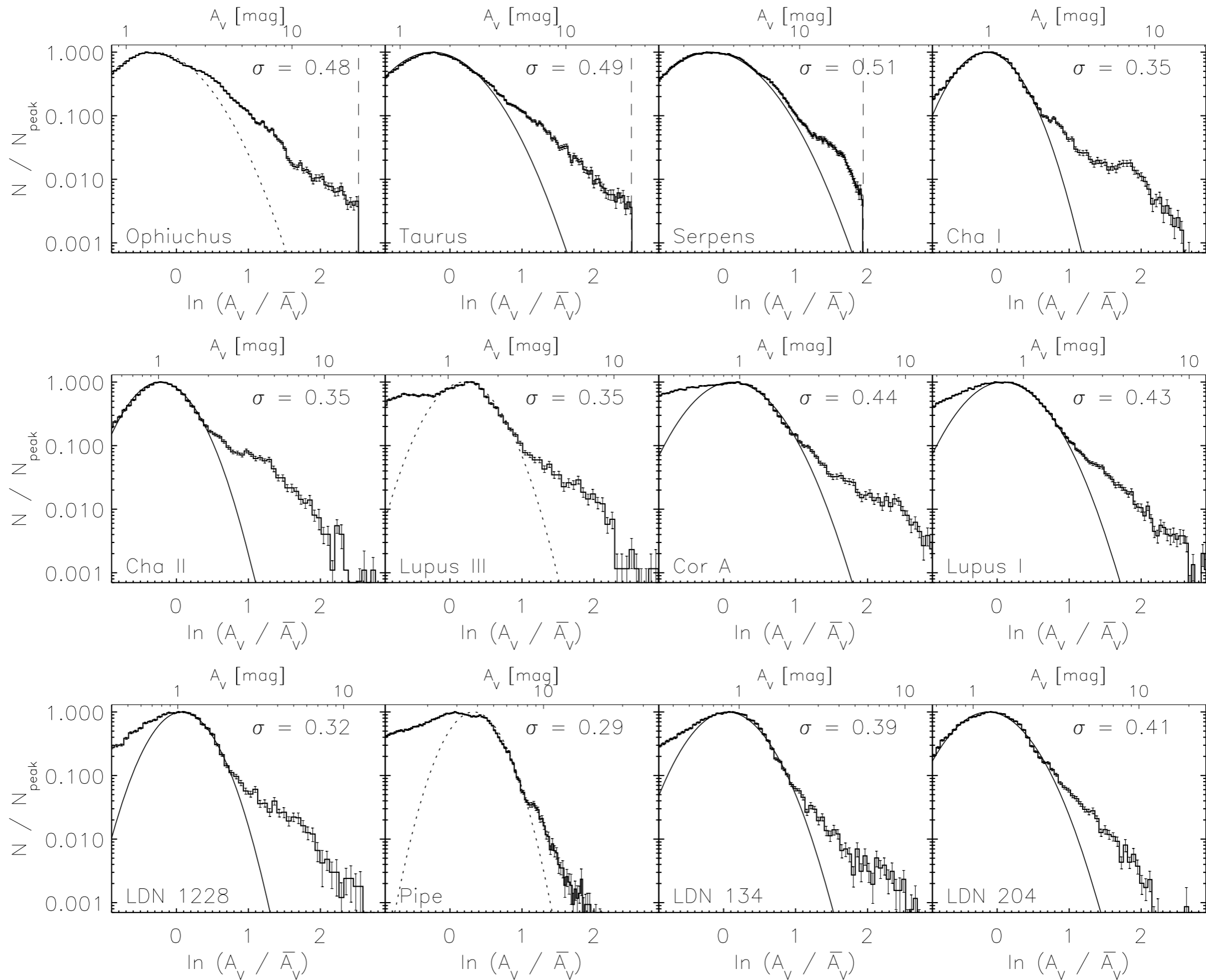
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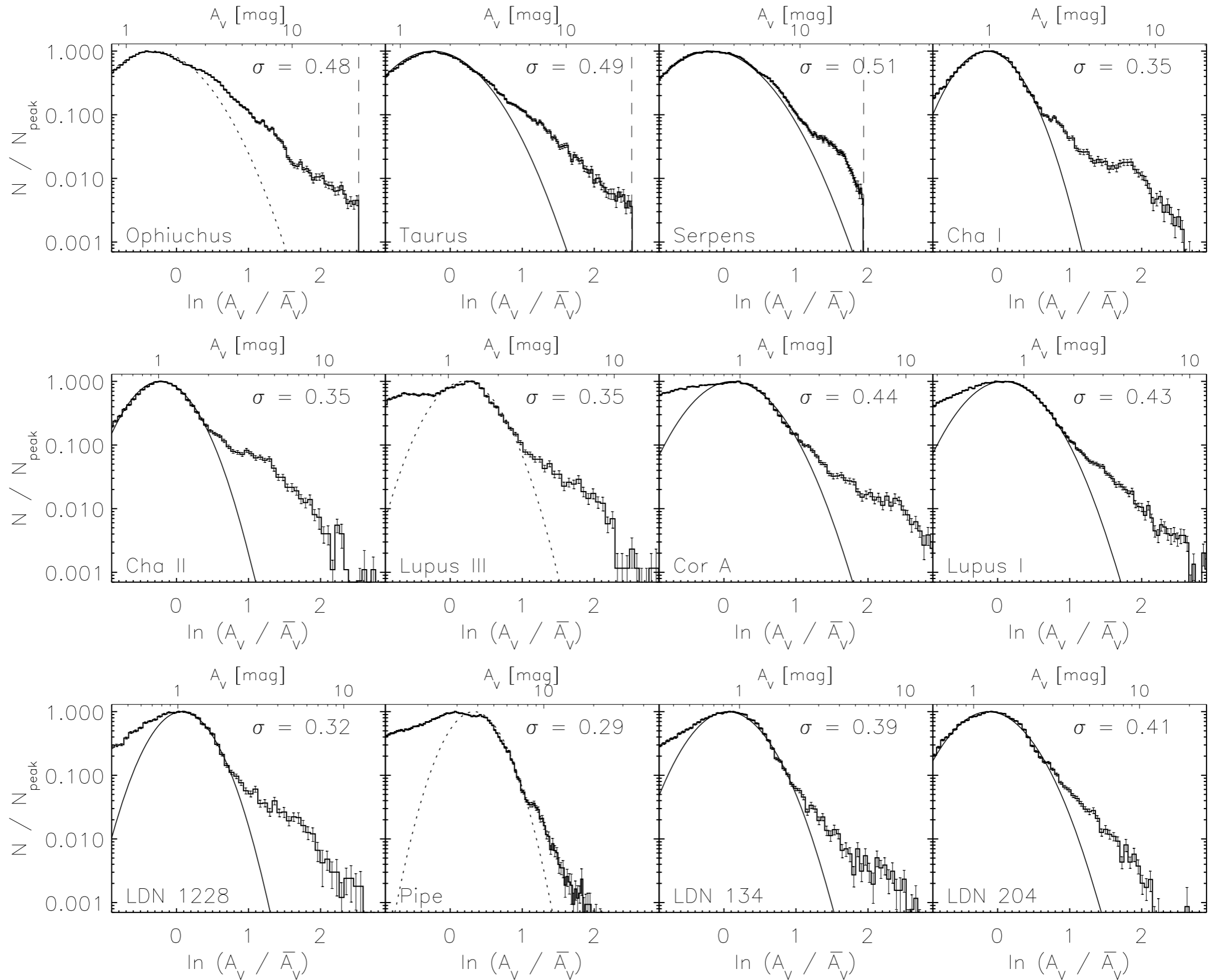
**We are virtually unable to study the PDF below
(at least) $A_K \sim 0.15$ mag**

Log-normals everywhere!



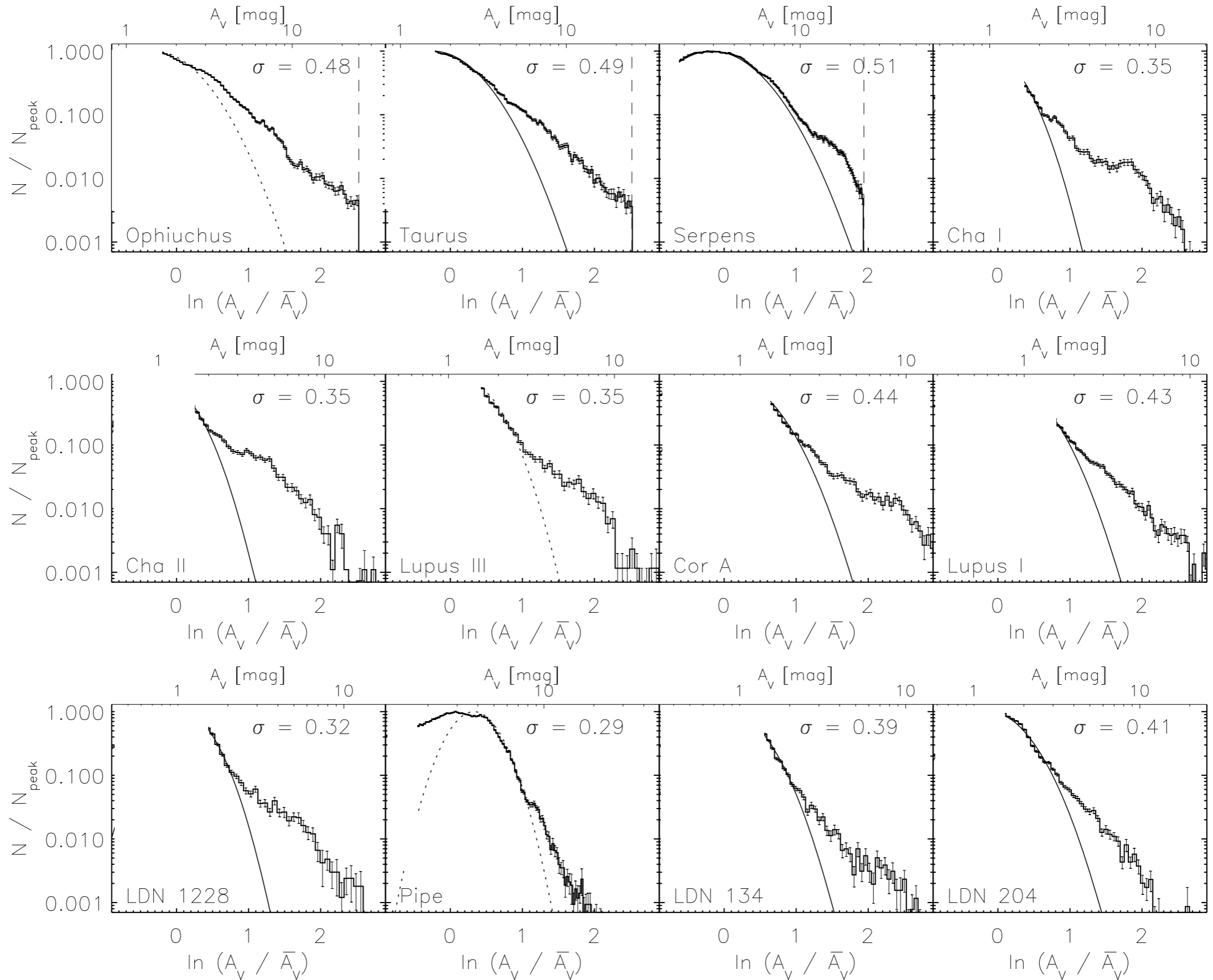
Kainulainen et al. (2009)

Log-normals everywhere?



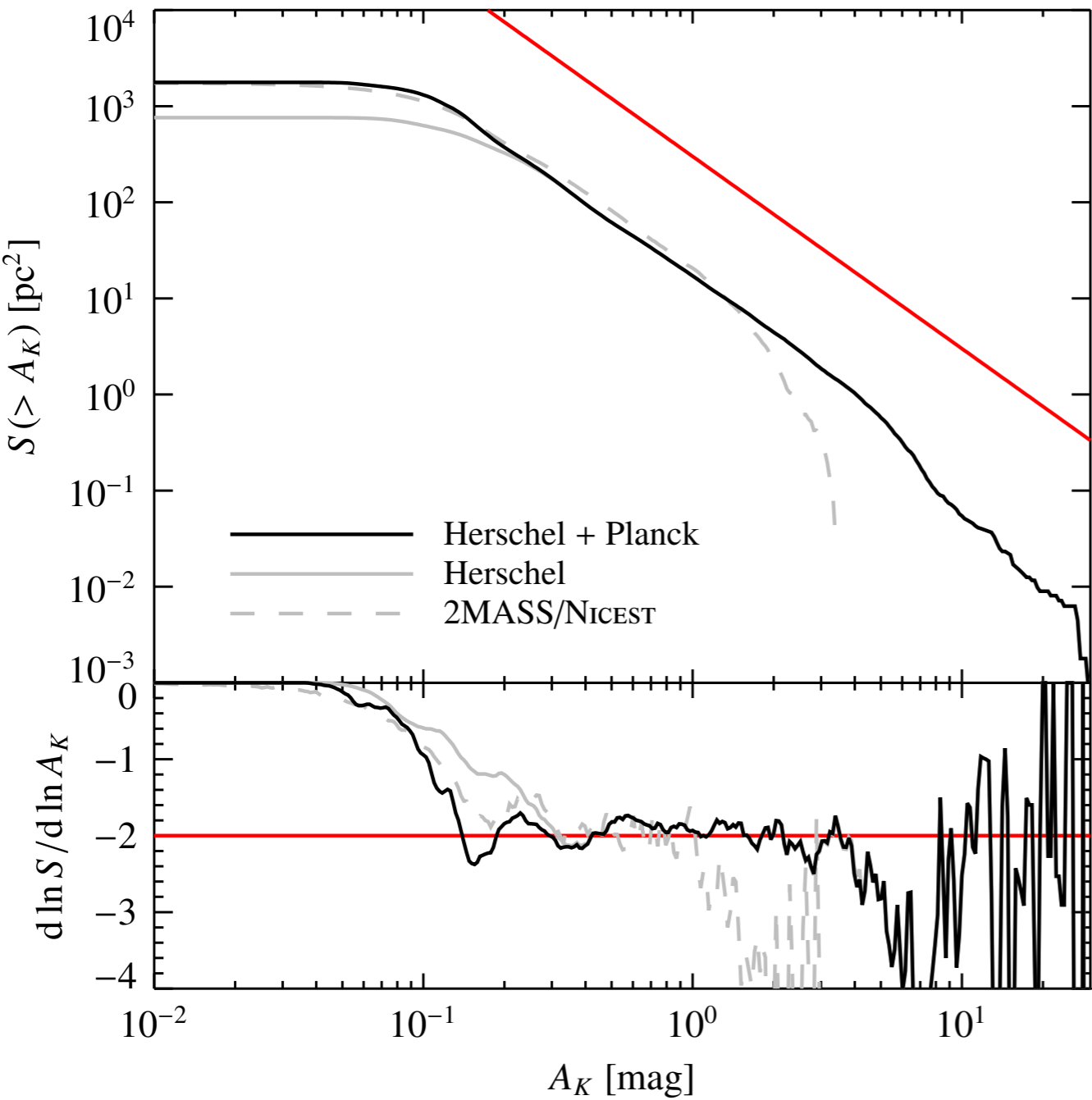
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Log-normals everywhere?

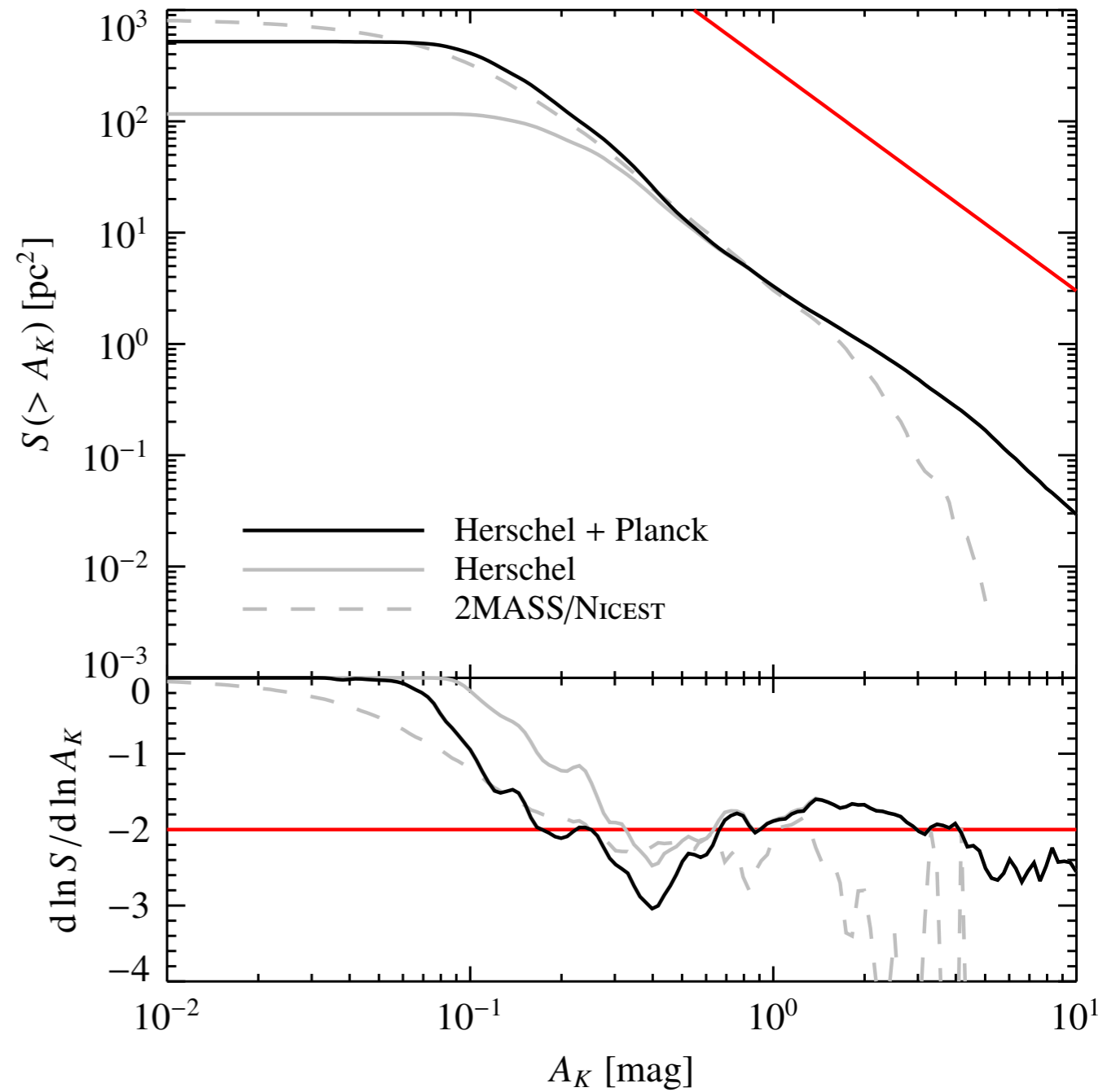


Kainulainen et al. (2009), censored

Area functions (integrals of PDFs)

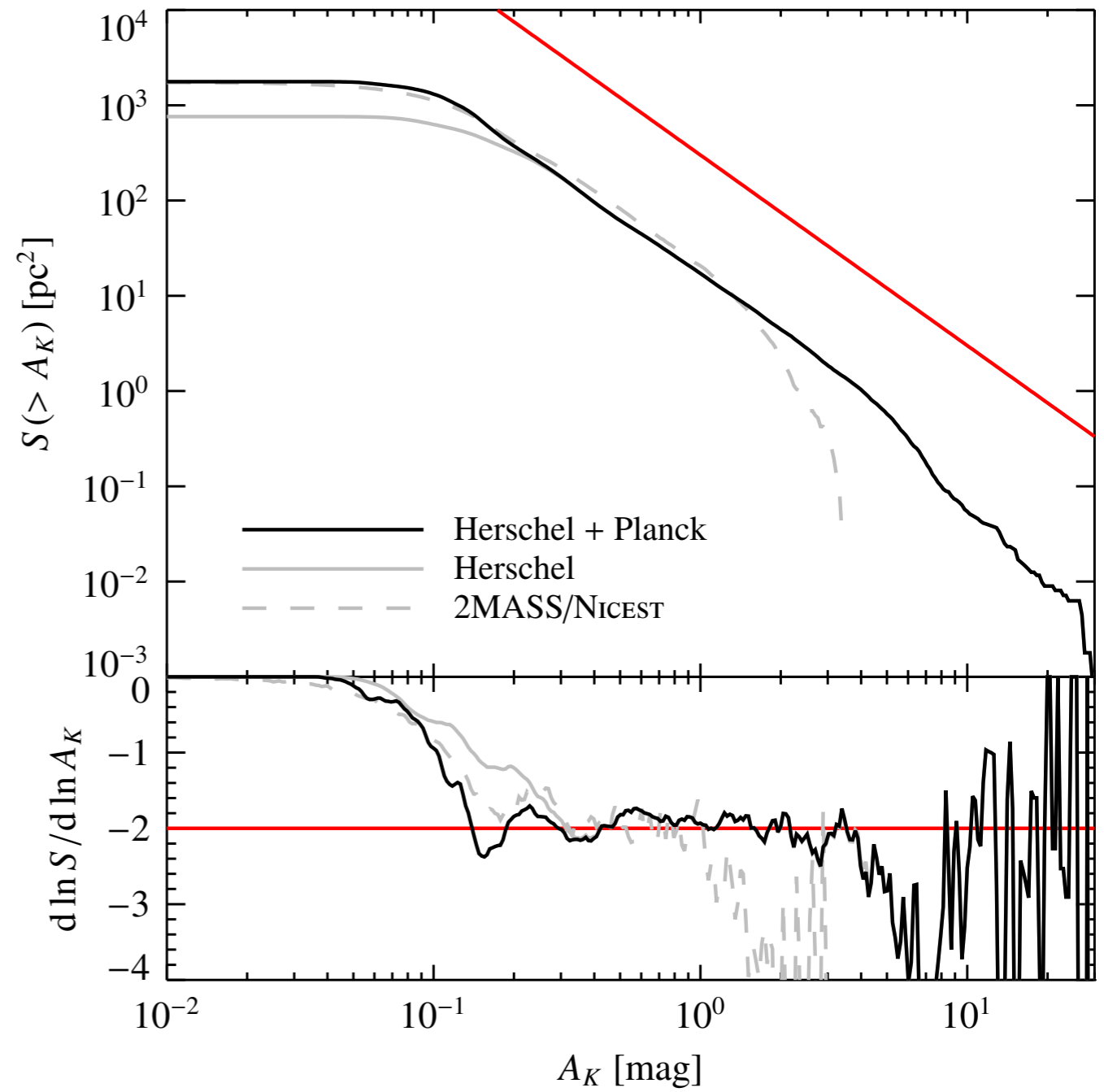


Lombardi et al. (2014)



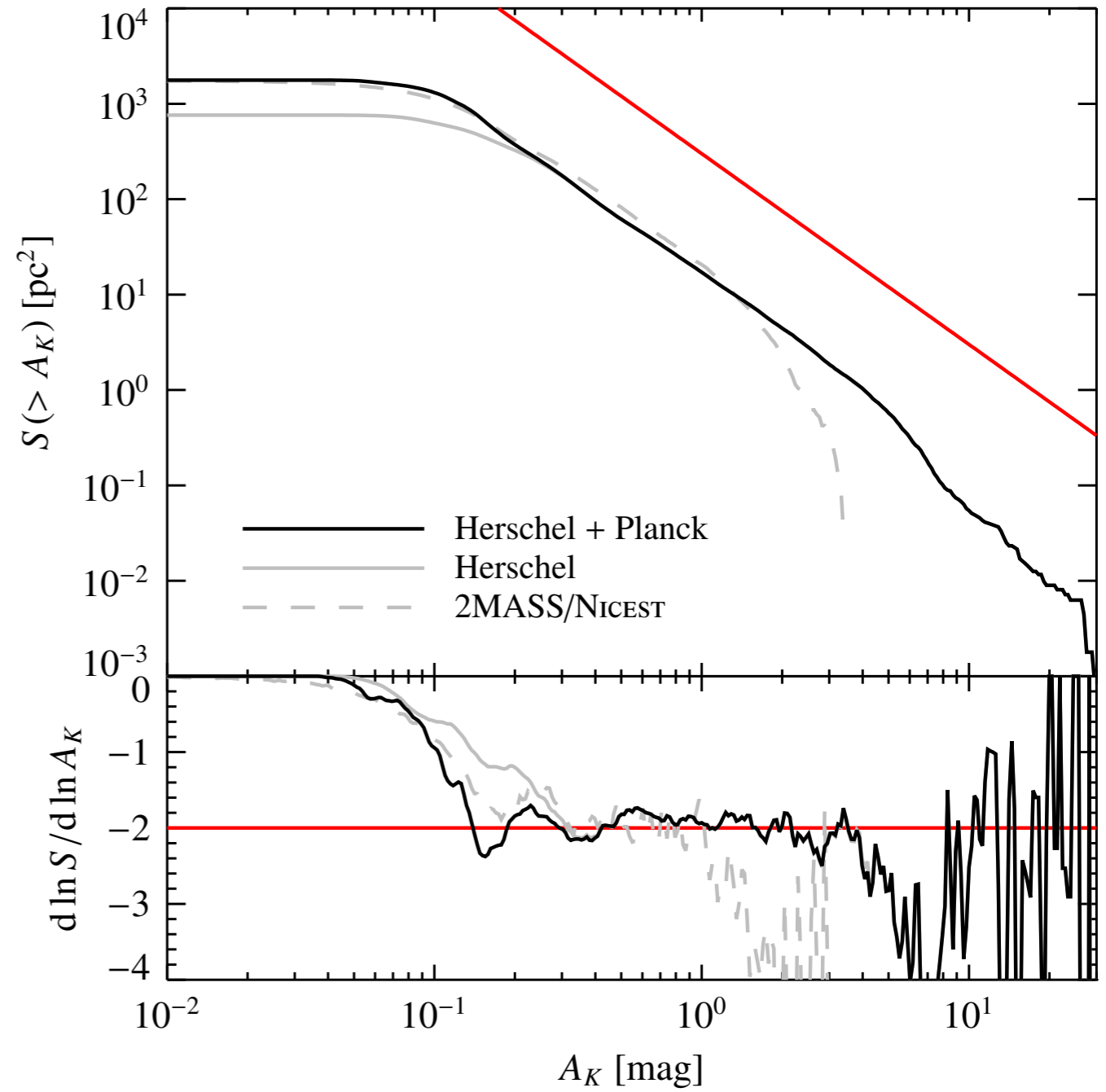
Alves et al. (2015)

Toy model



Toy model

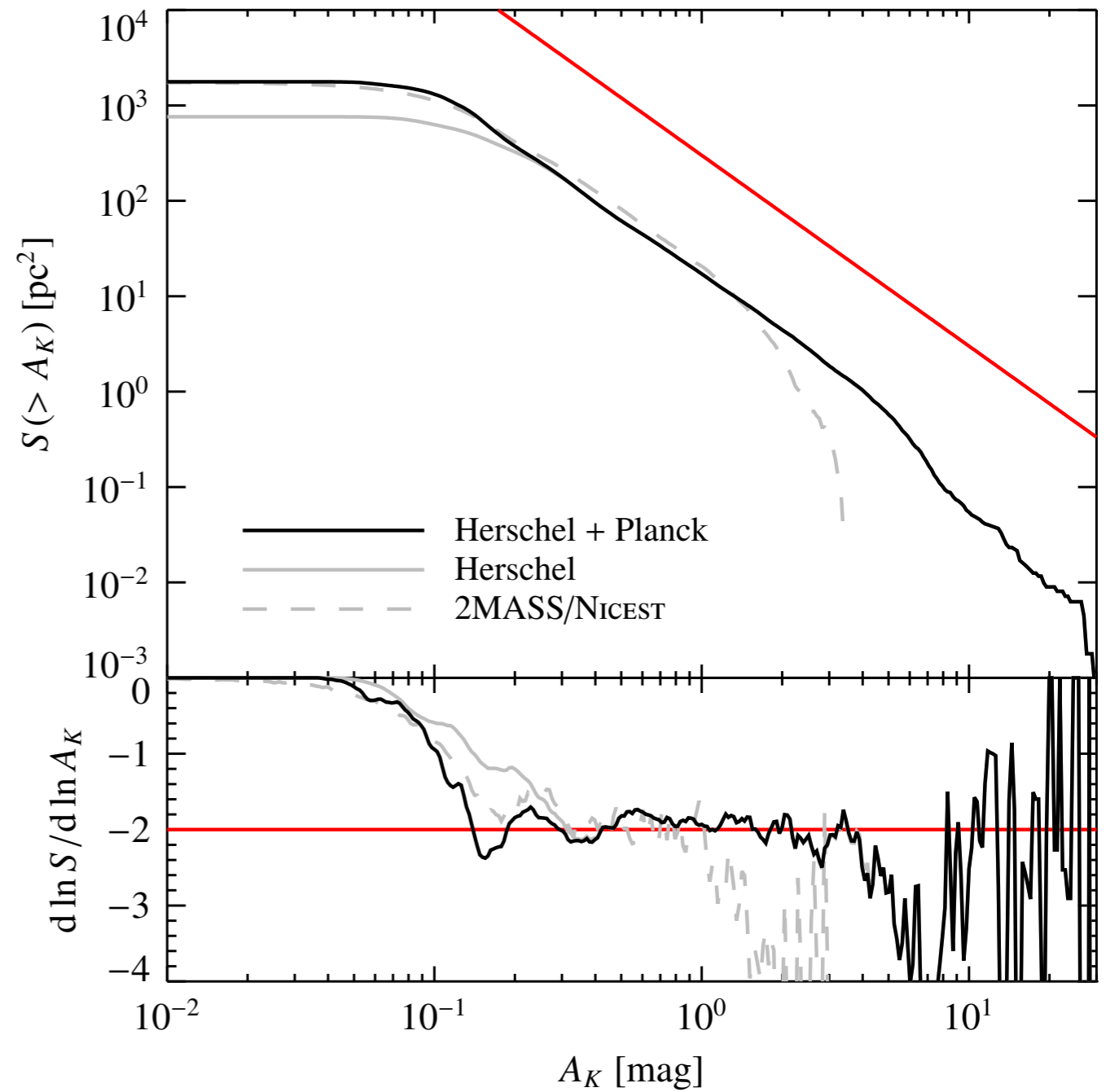
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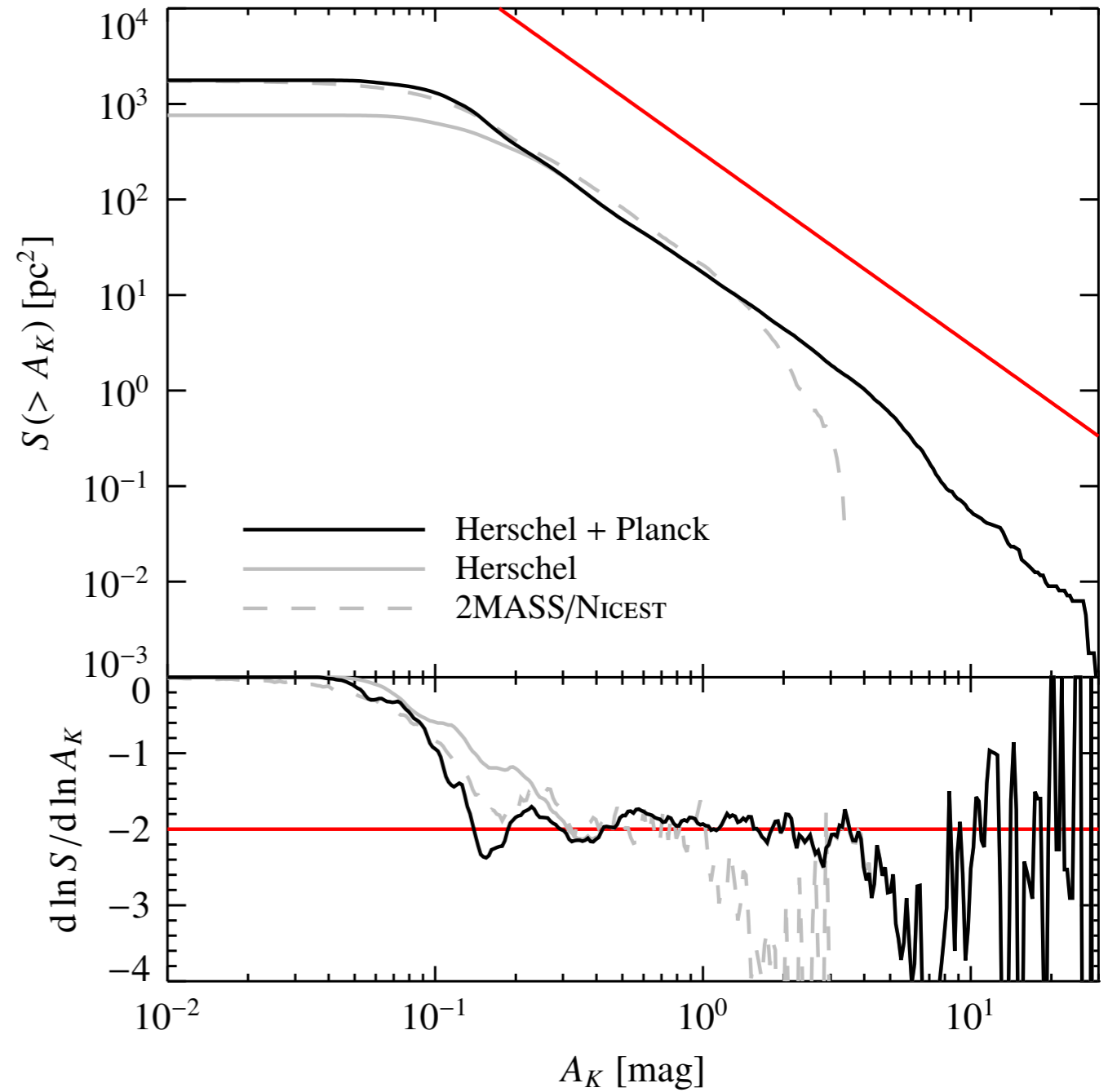


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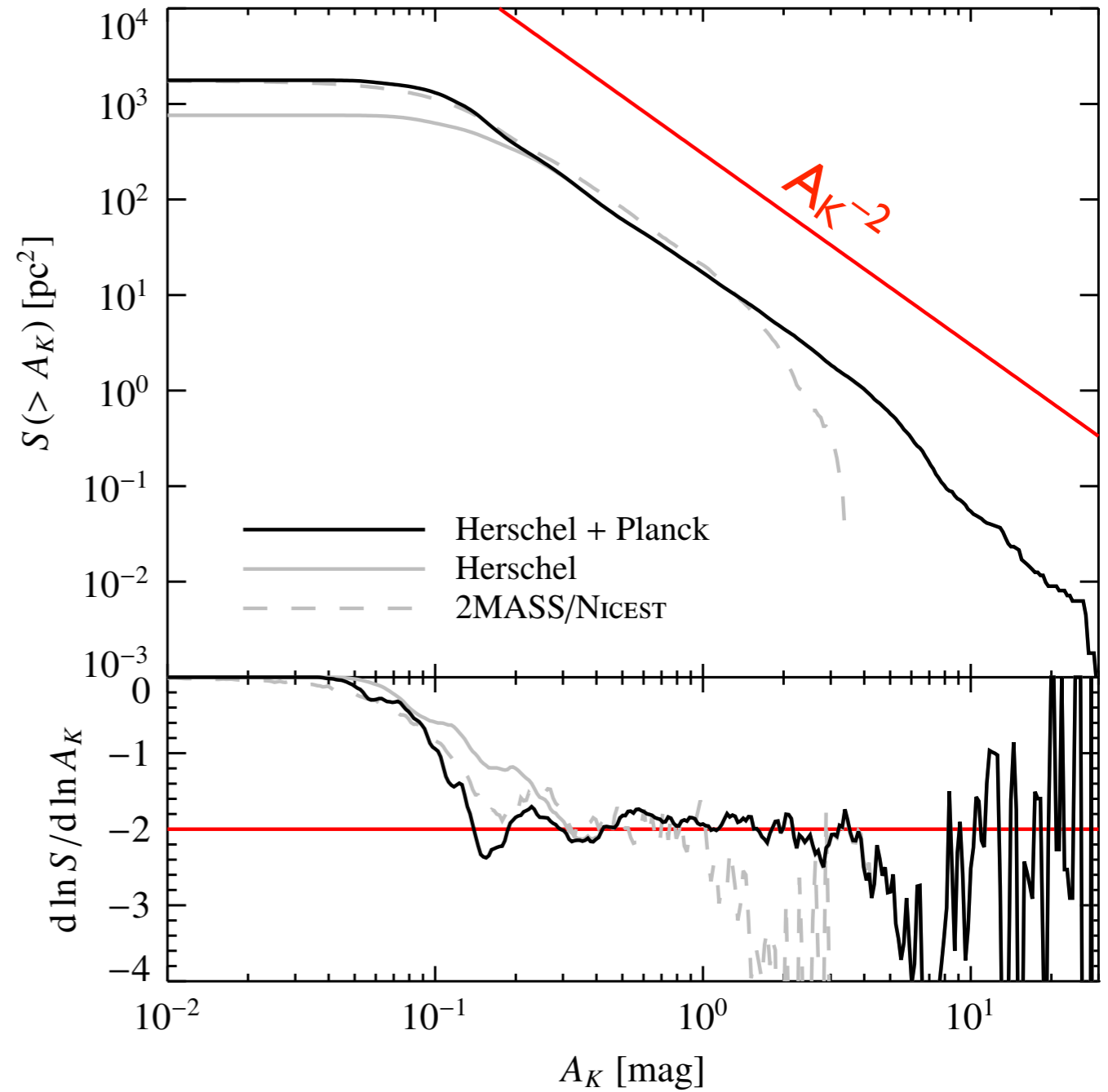
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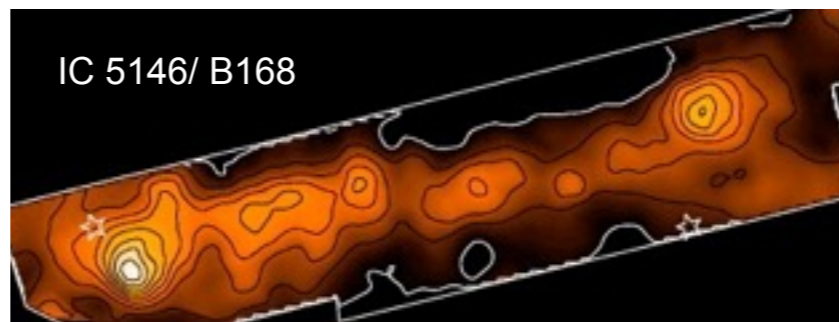
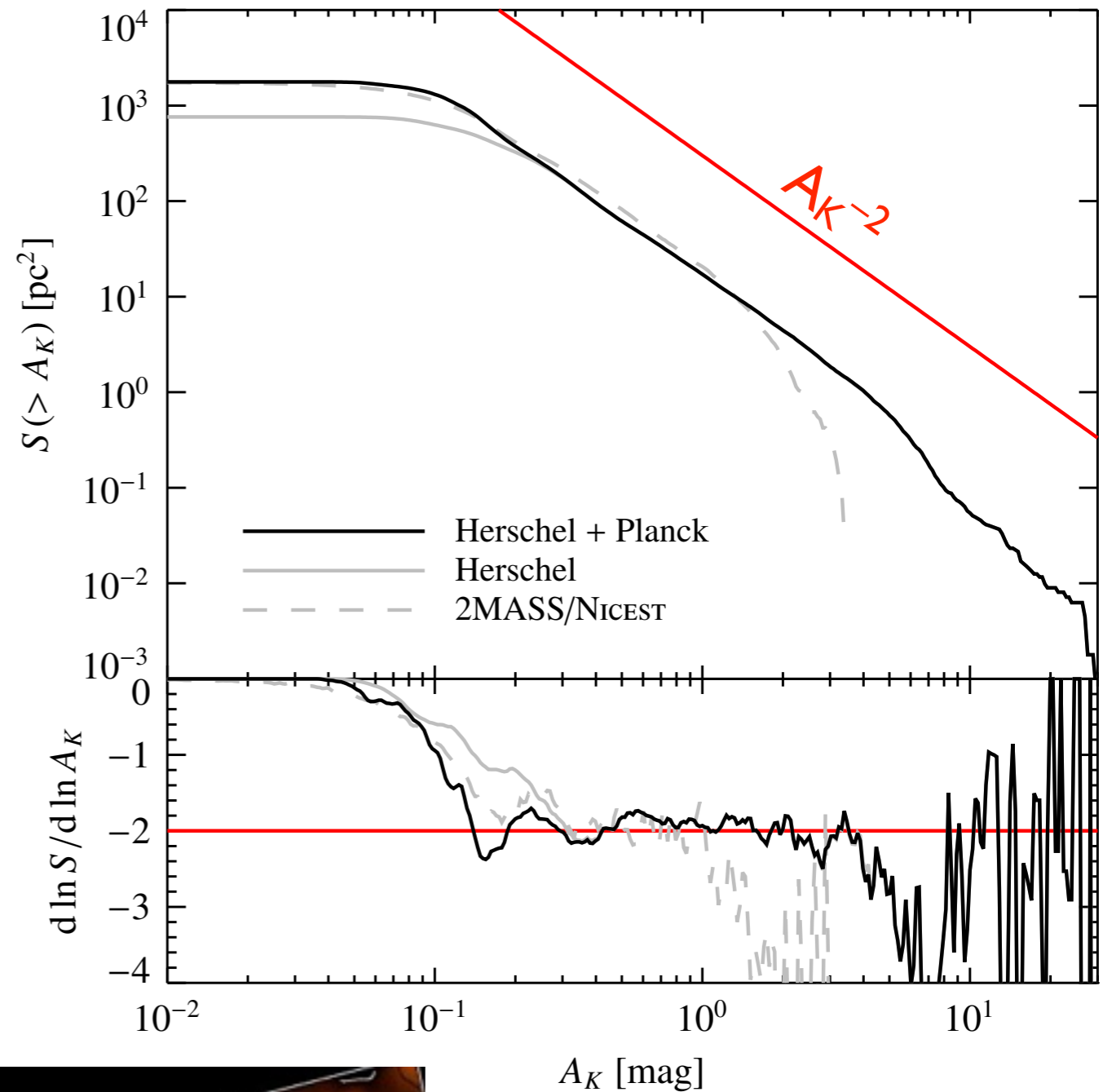
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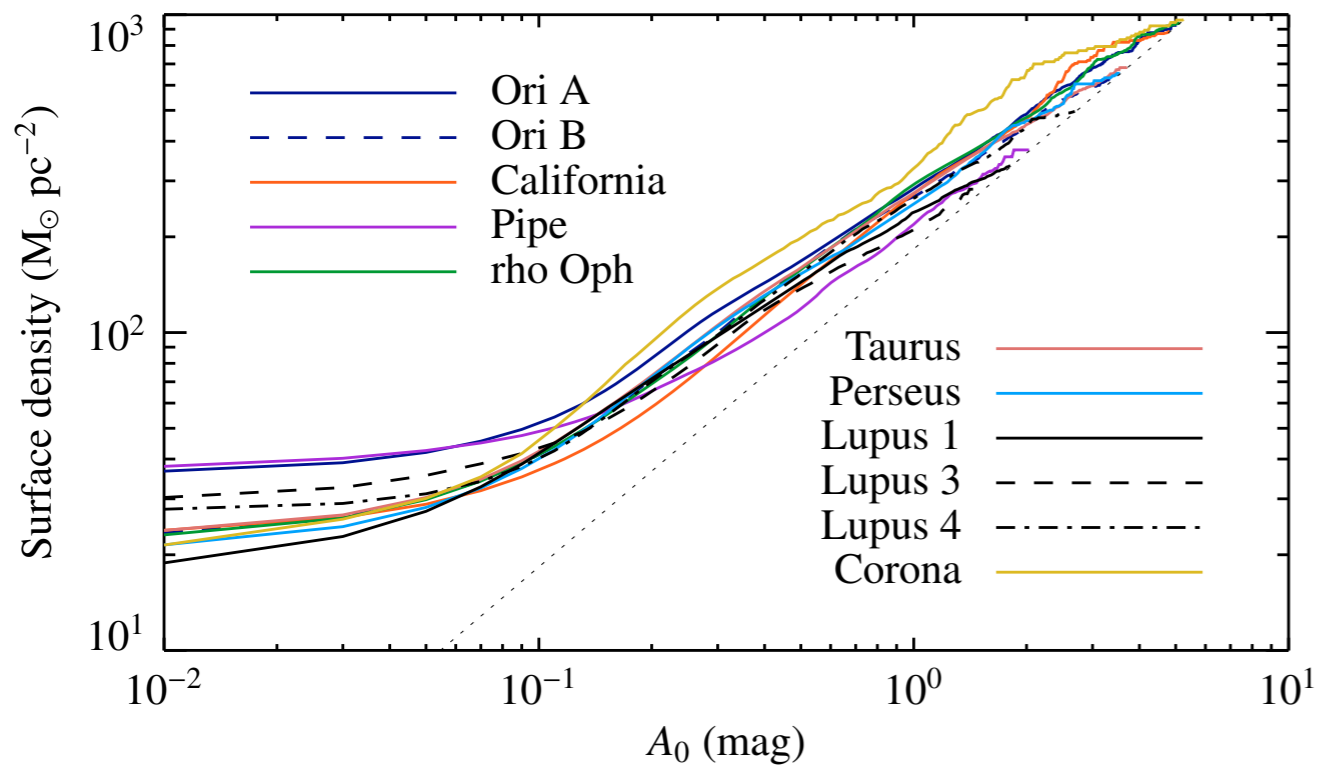
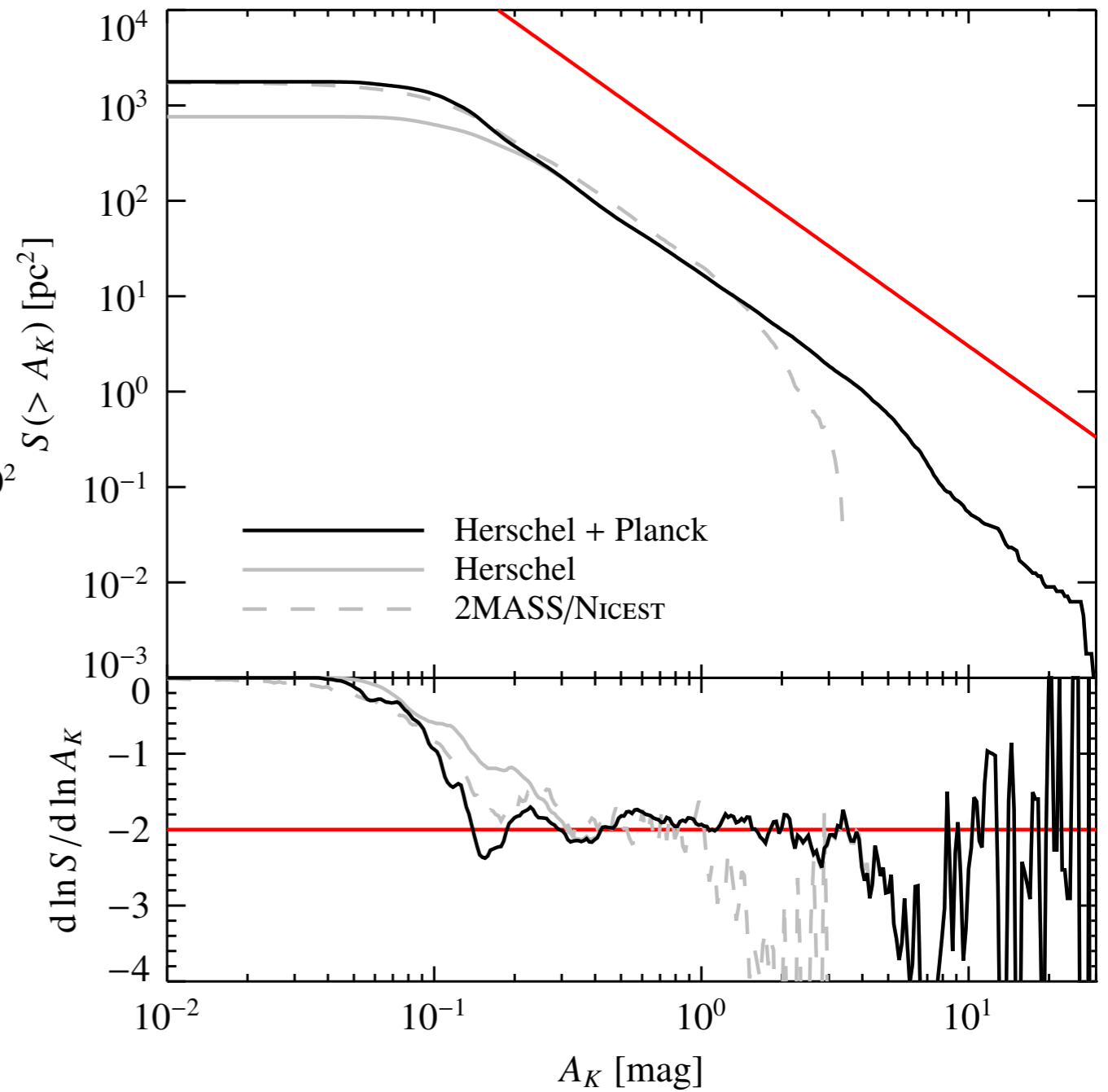
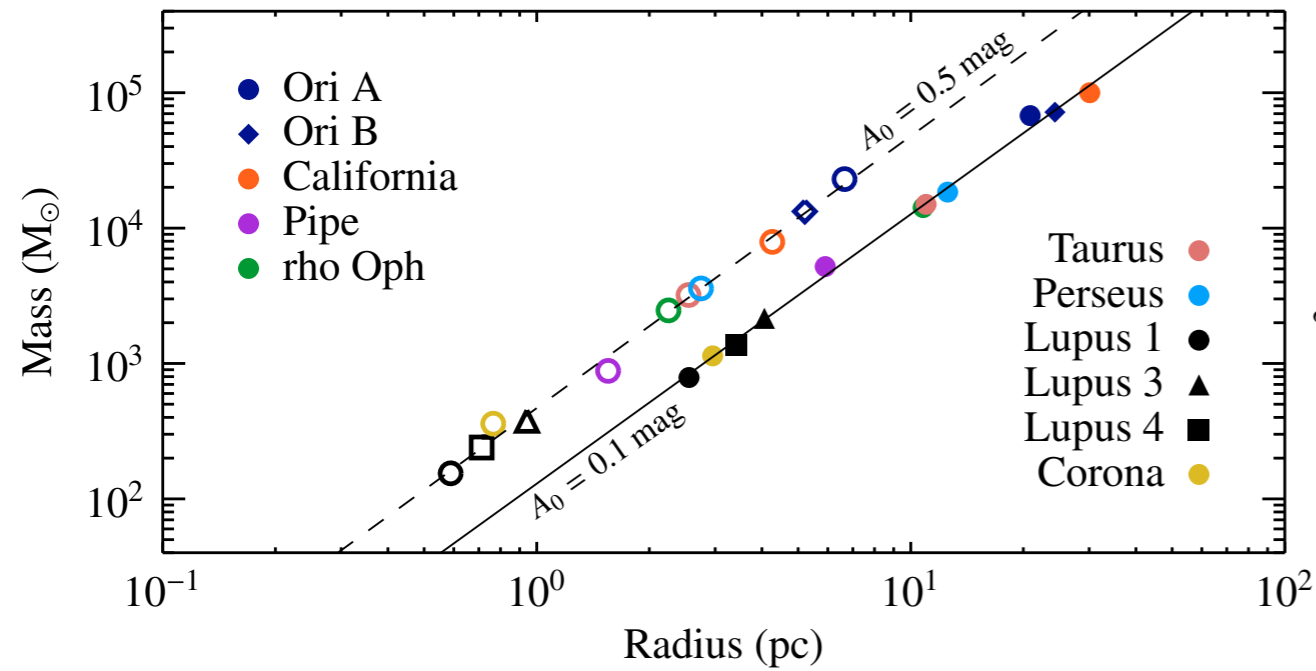
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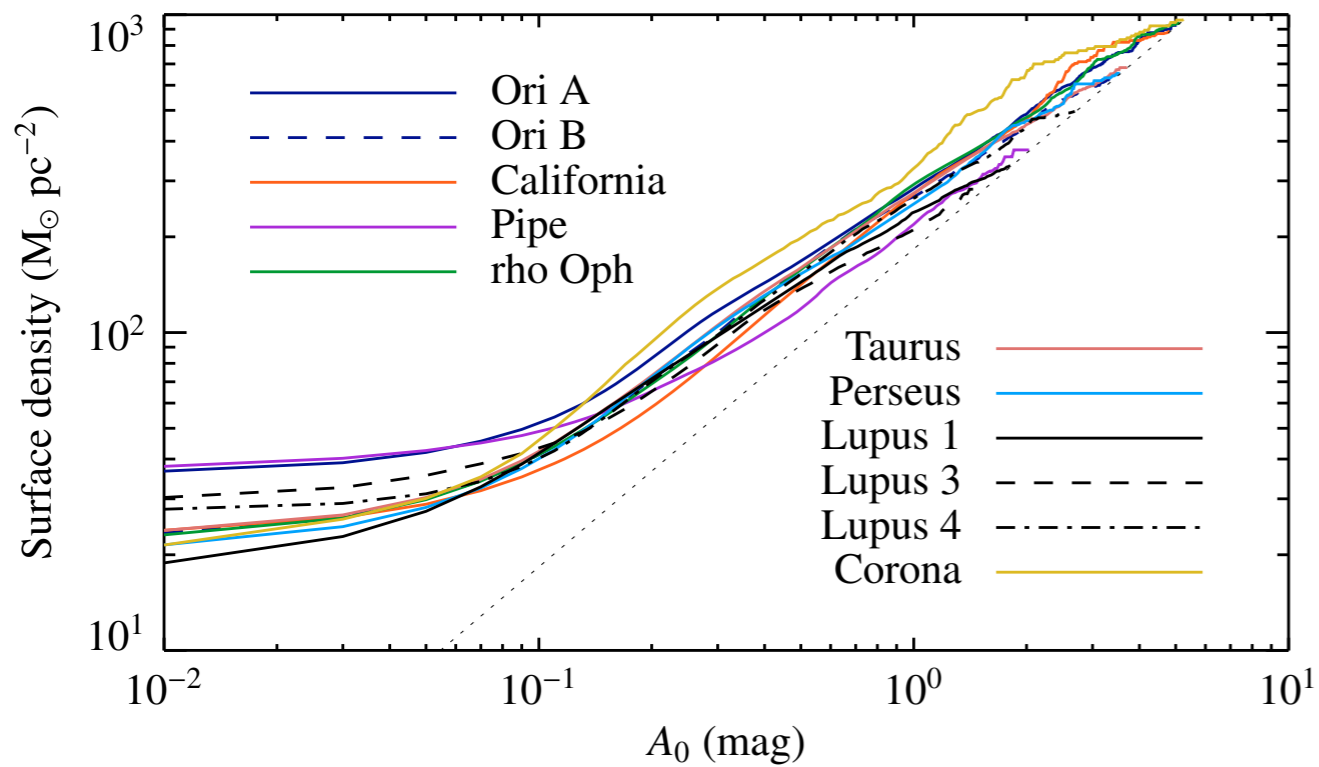
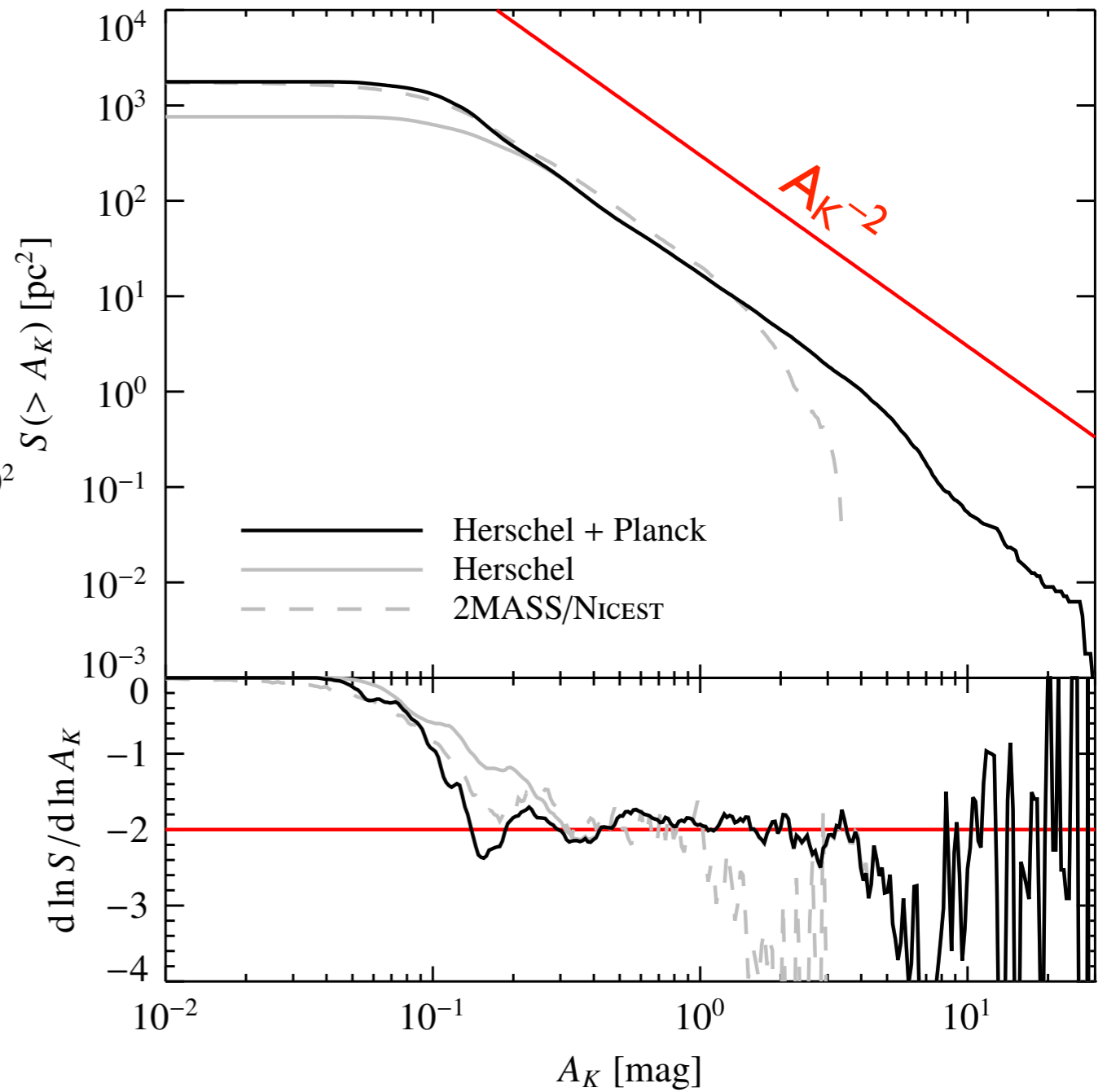
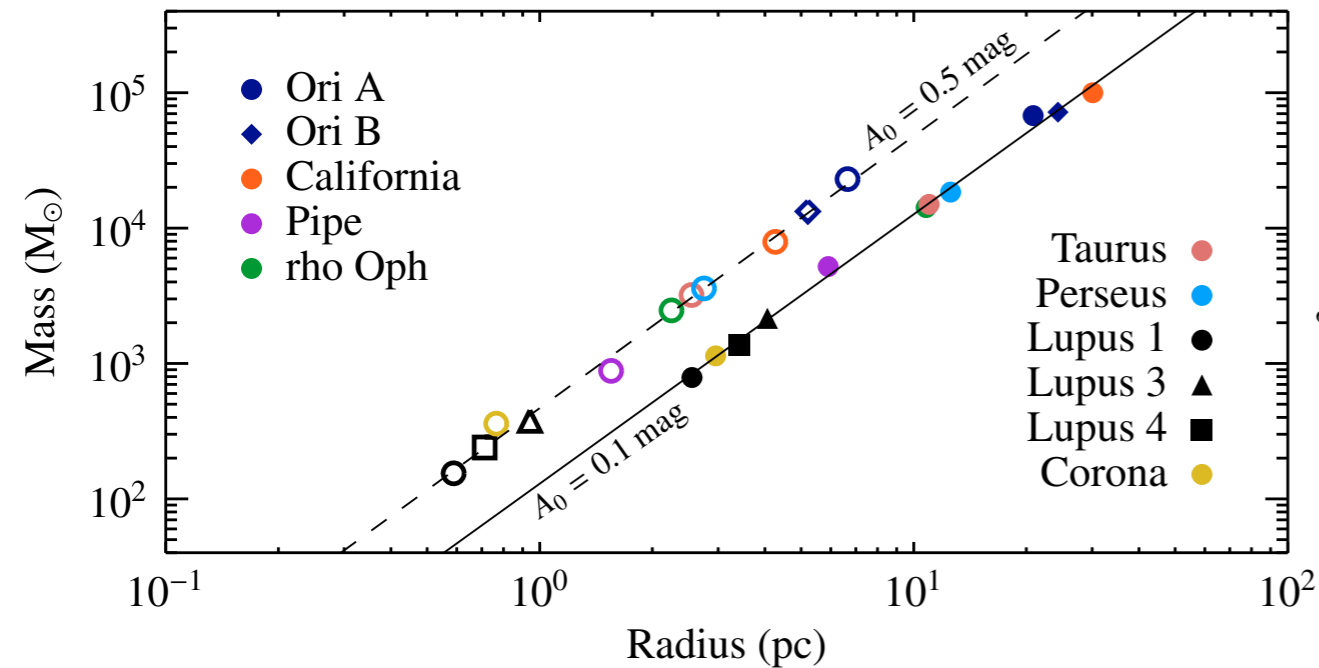


Lombardi et al. (2014)

3rd Larson's law

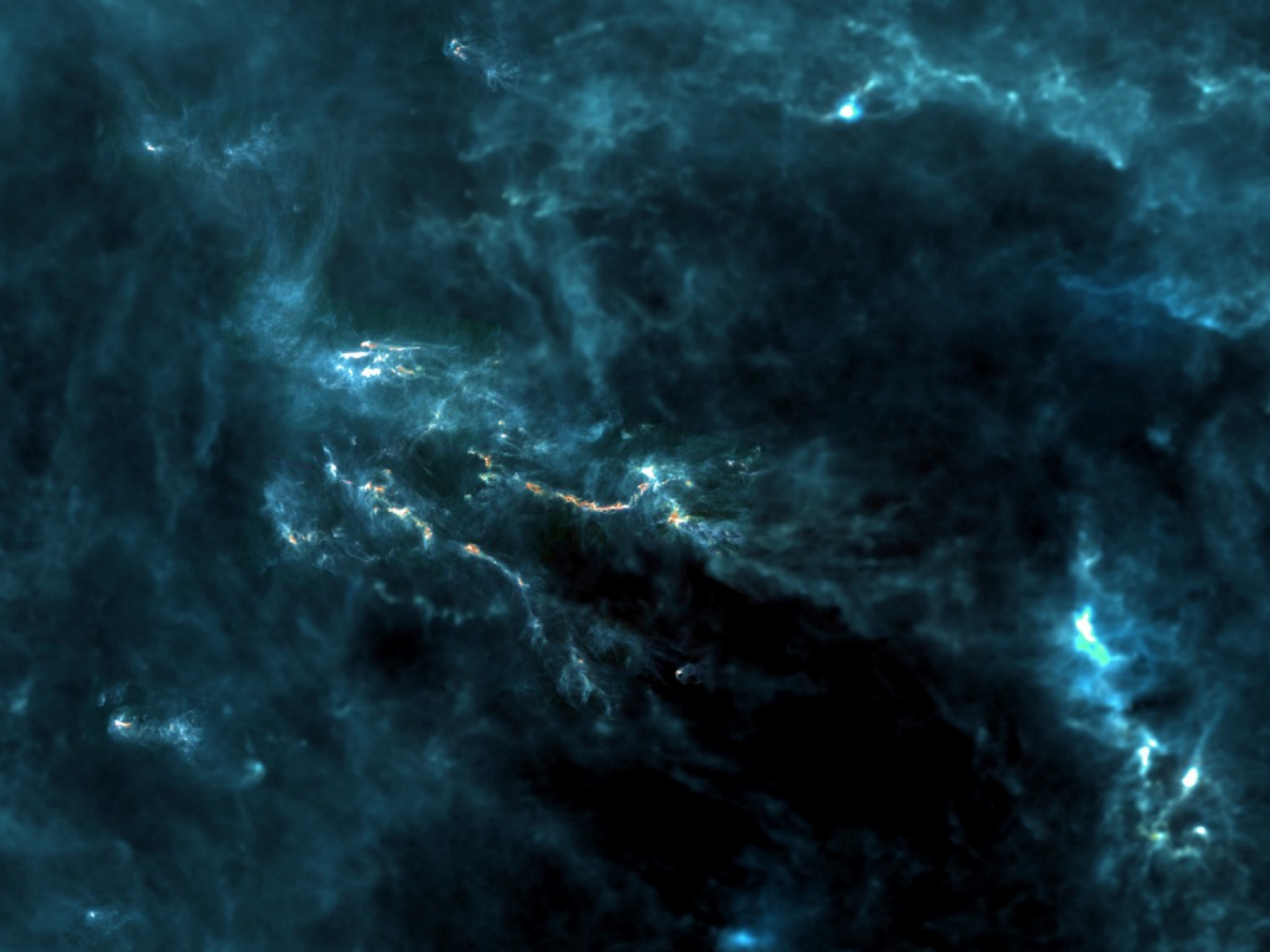


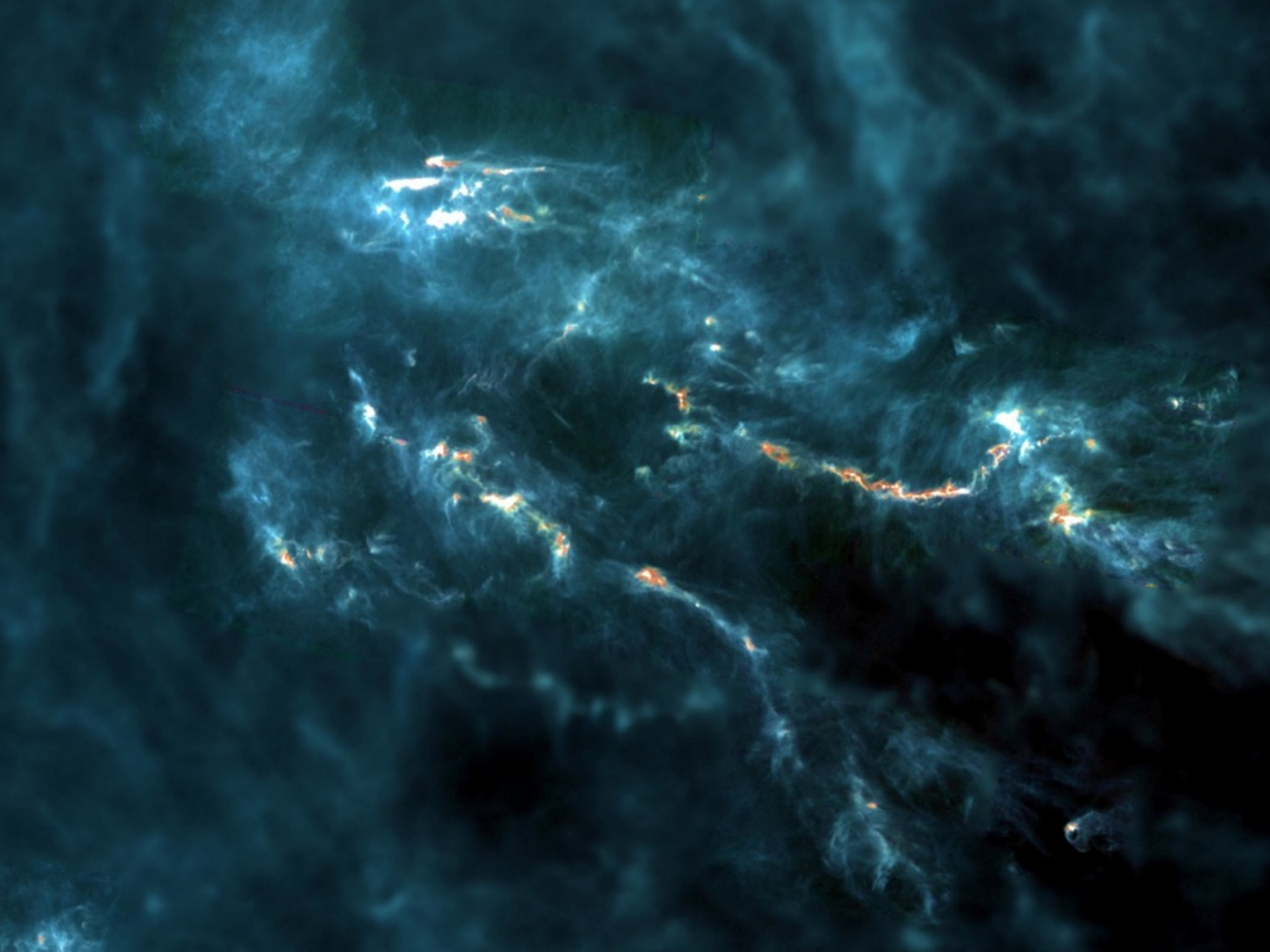
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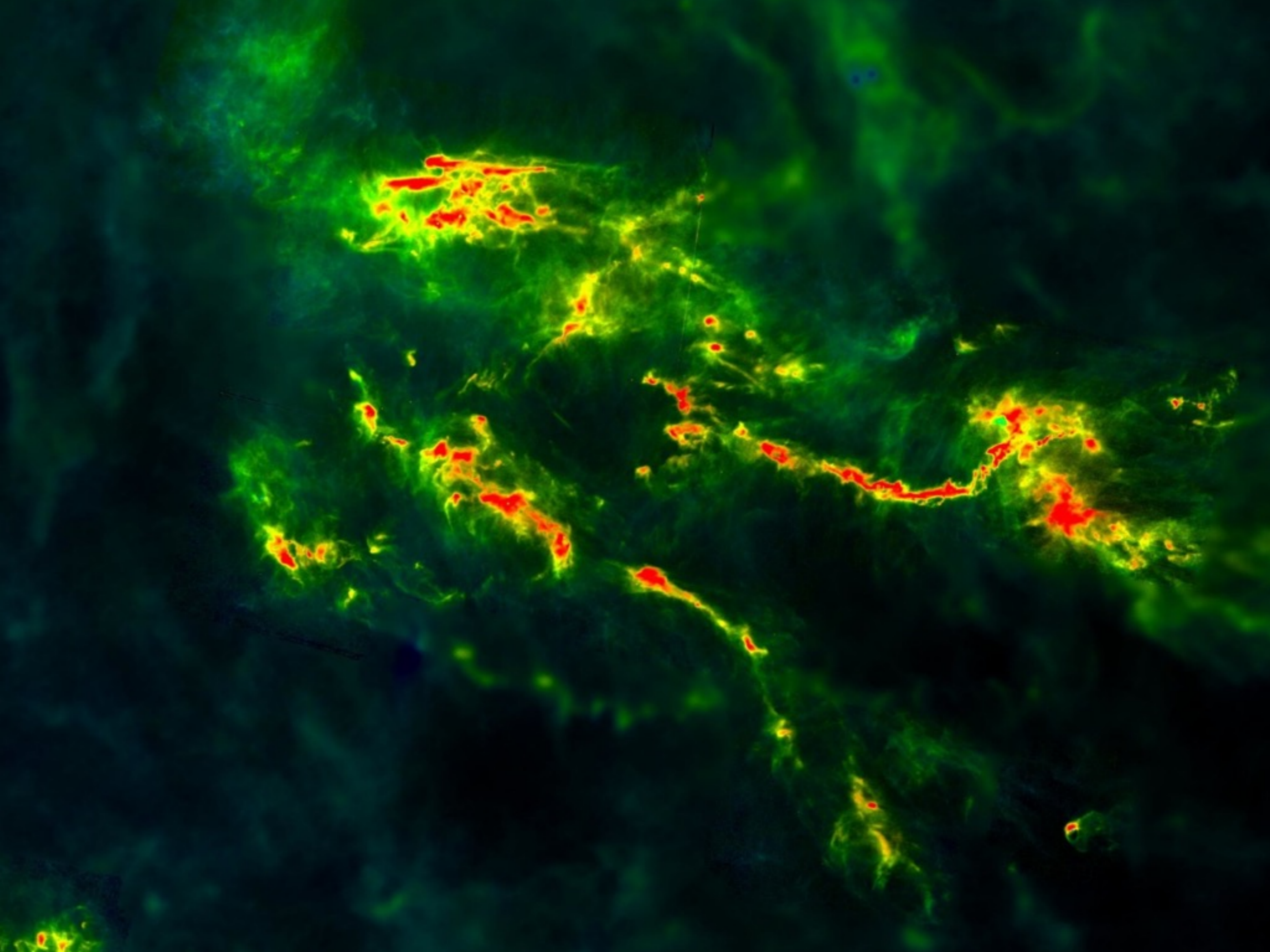


Taurus

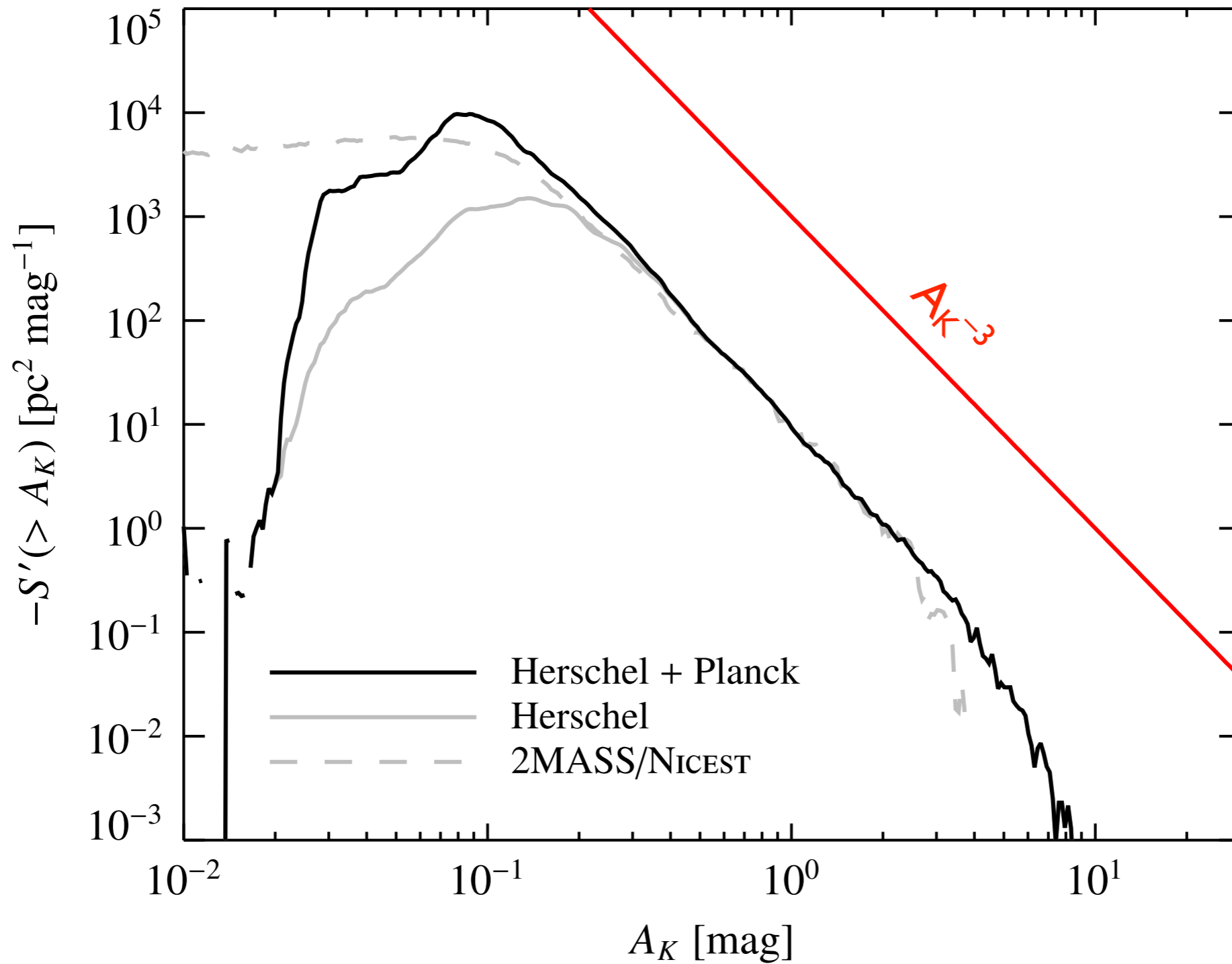
(Lombardi et al. 2015)





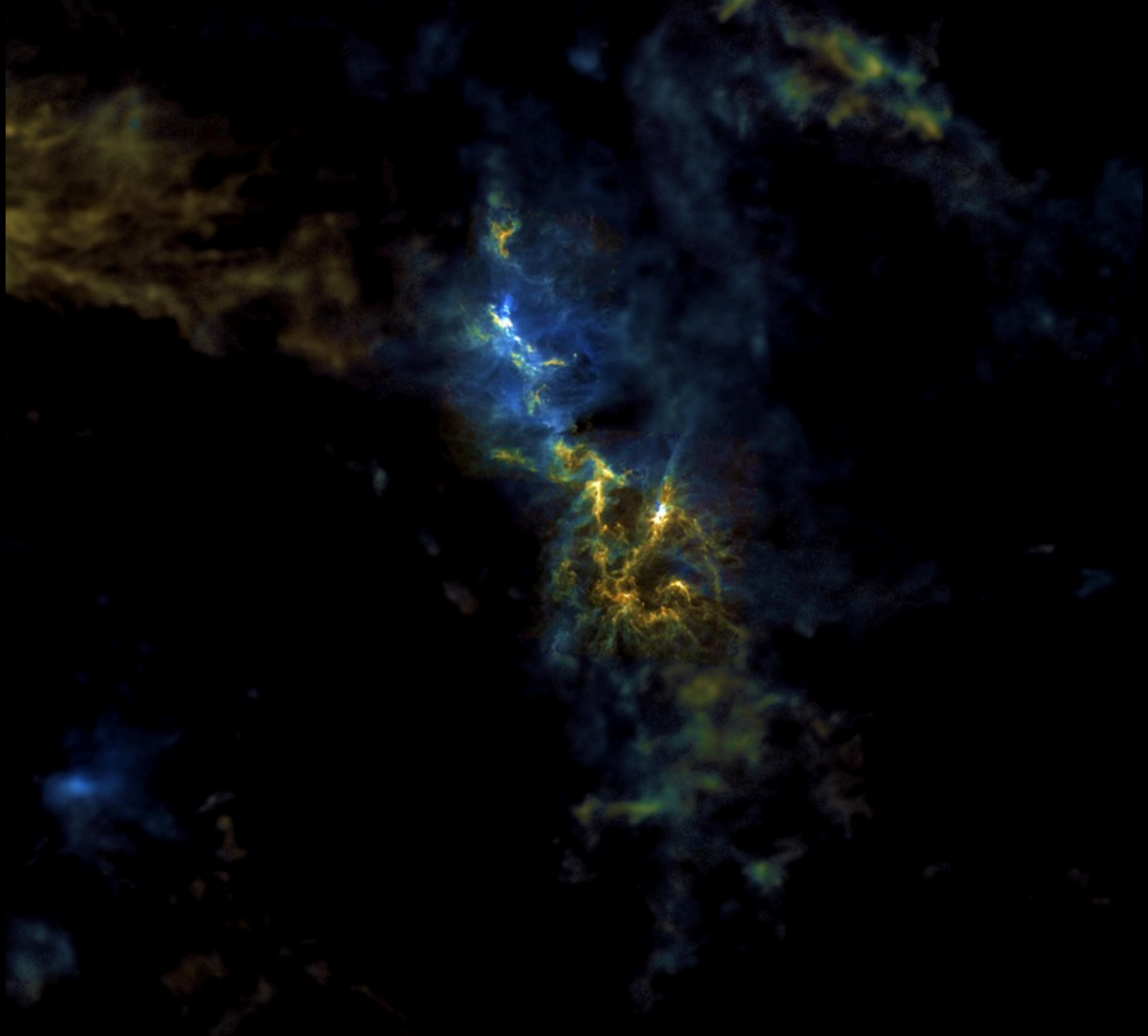


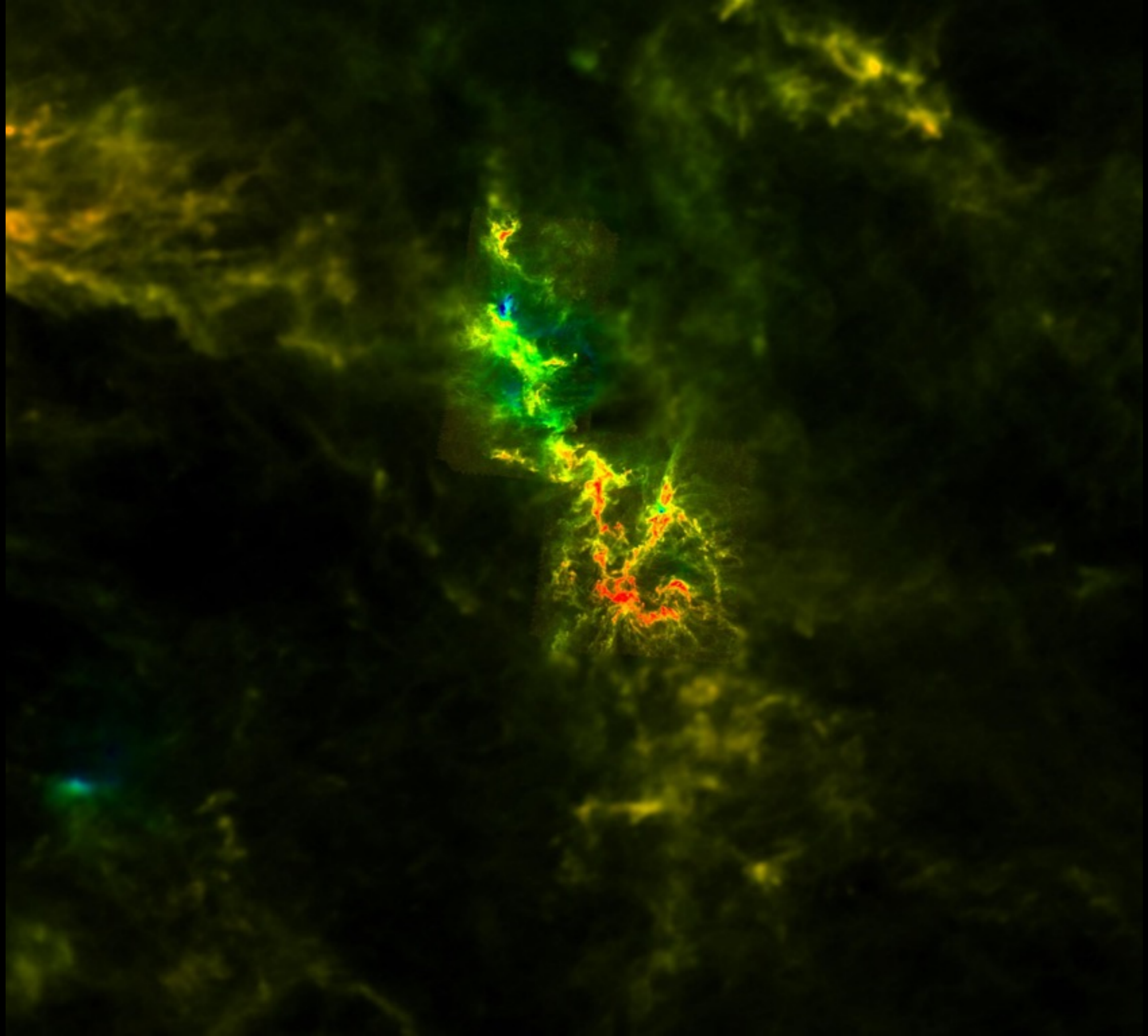
Herschel PDF for Taurus

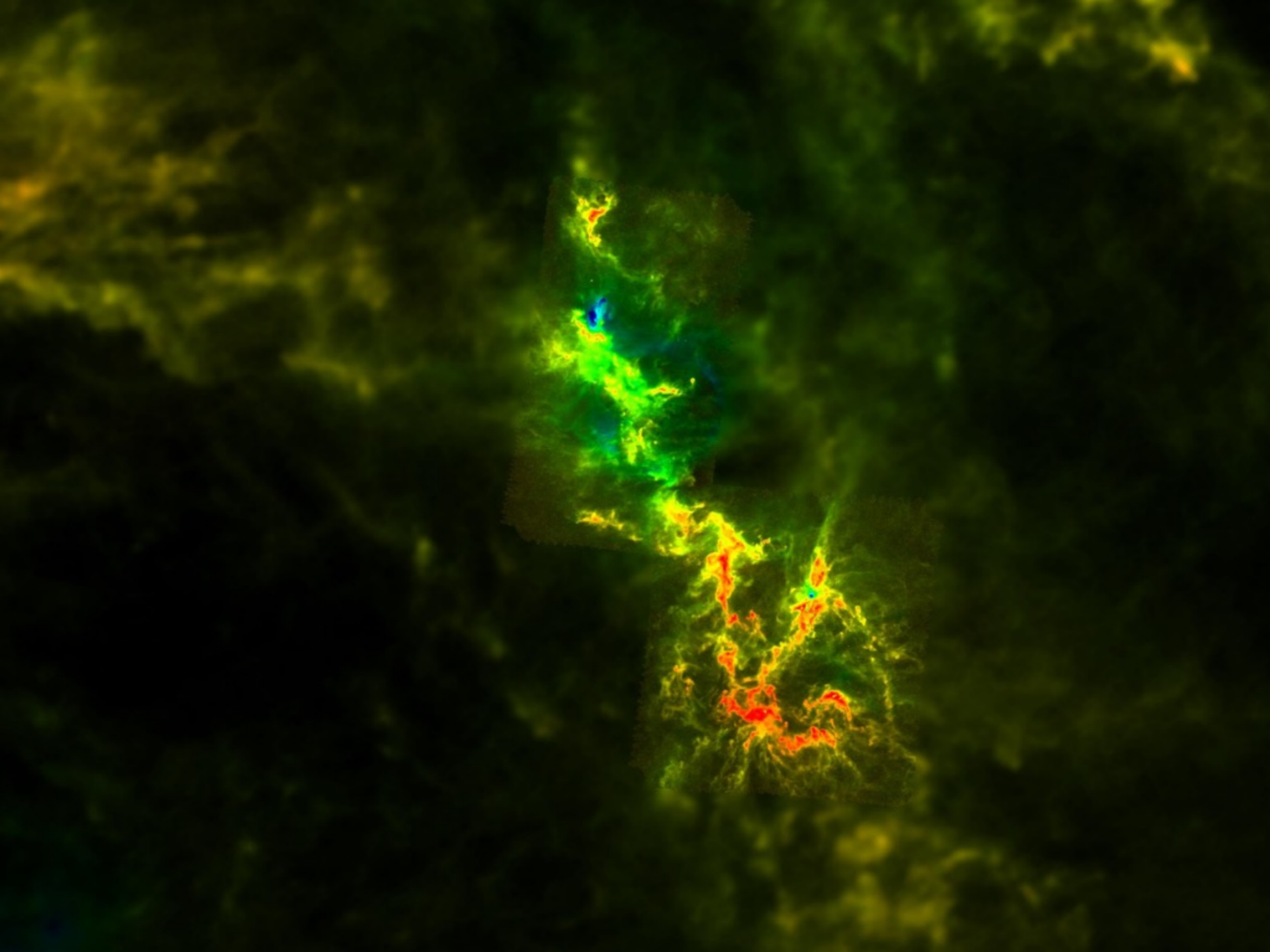


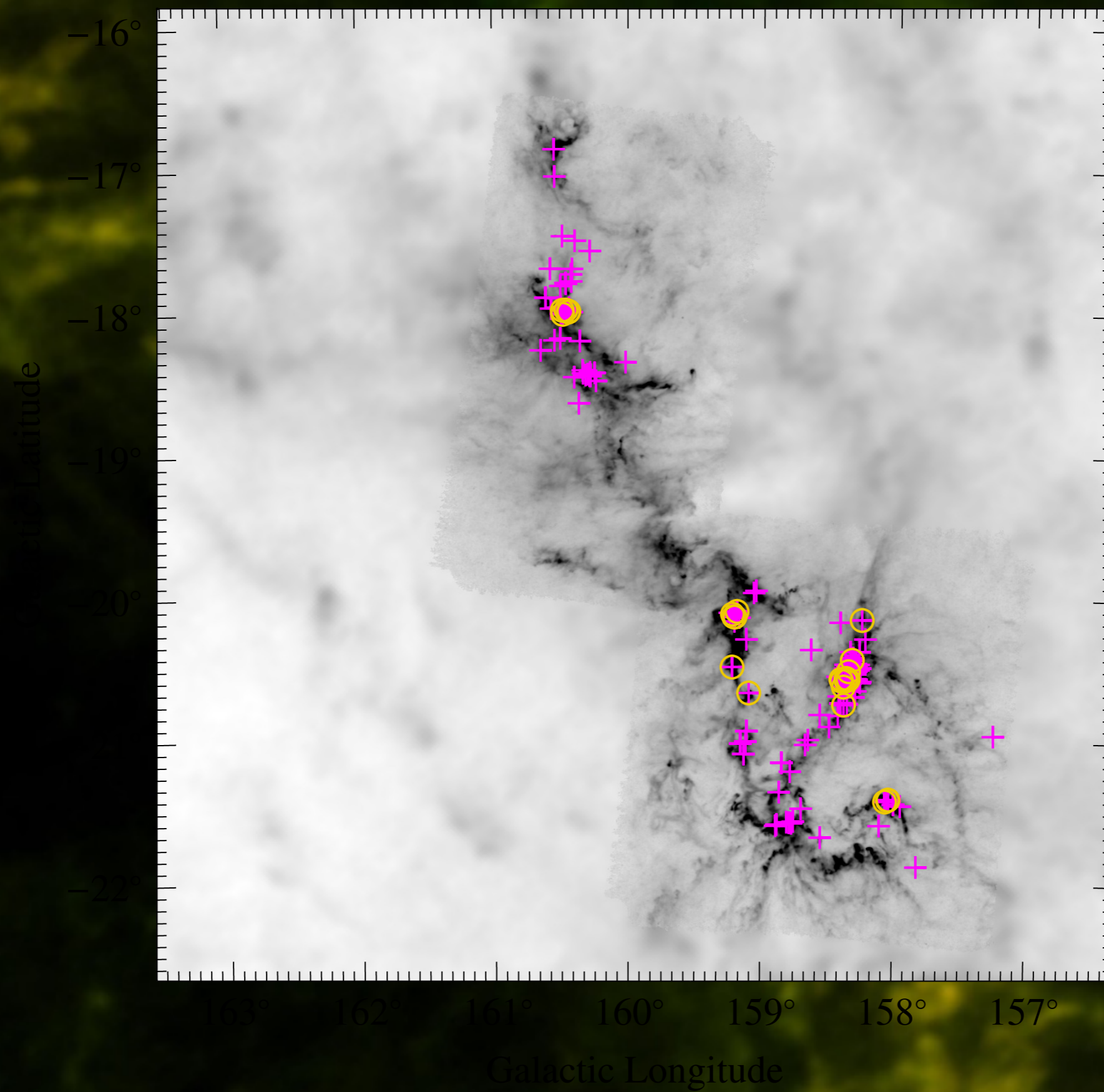
Perseus

(Zari et al. 2015)

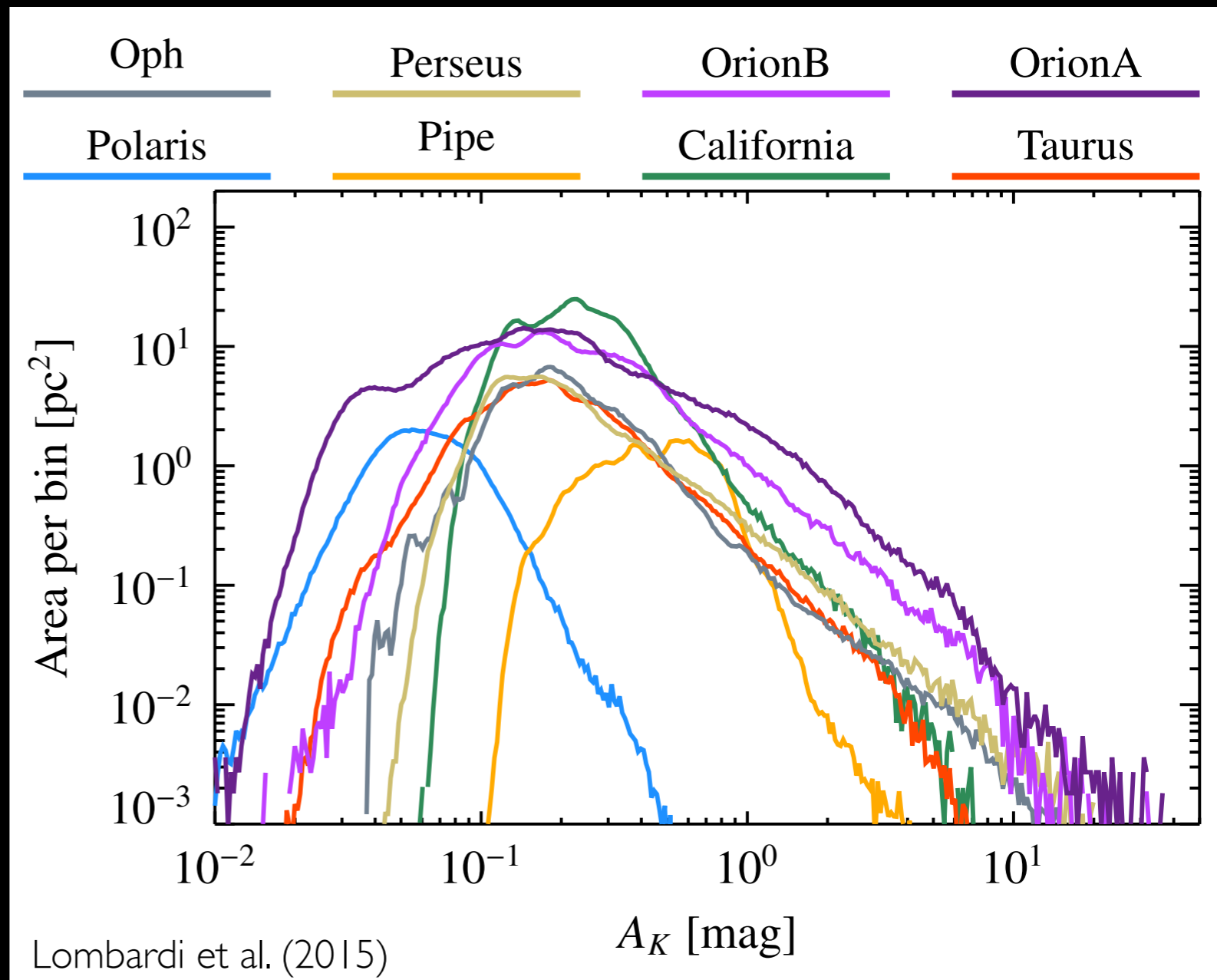






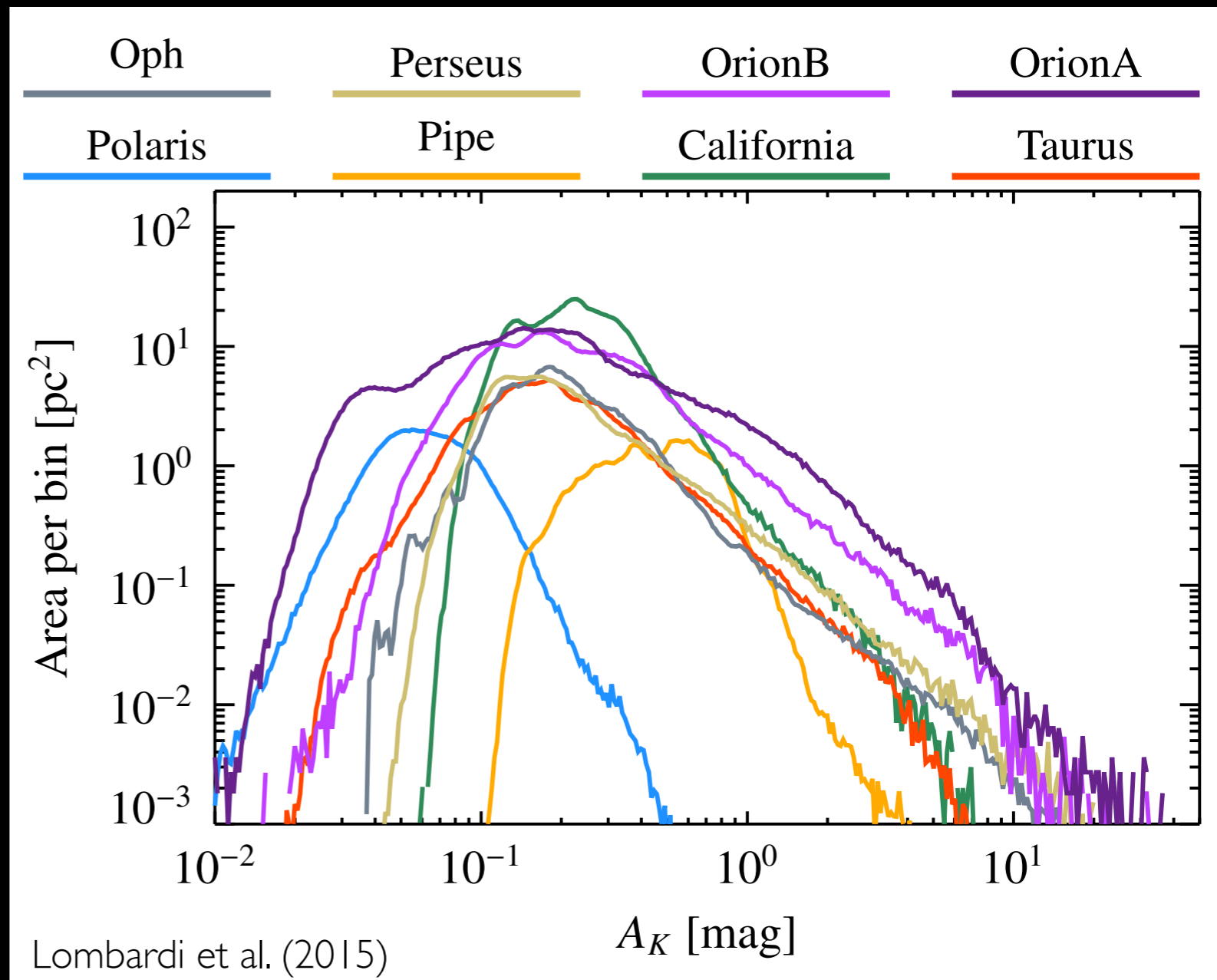


PDFs from Herschel



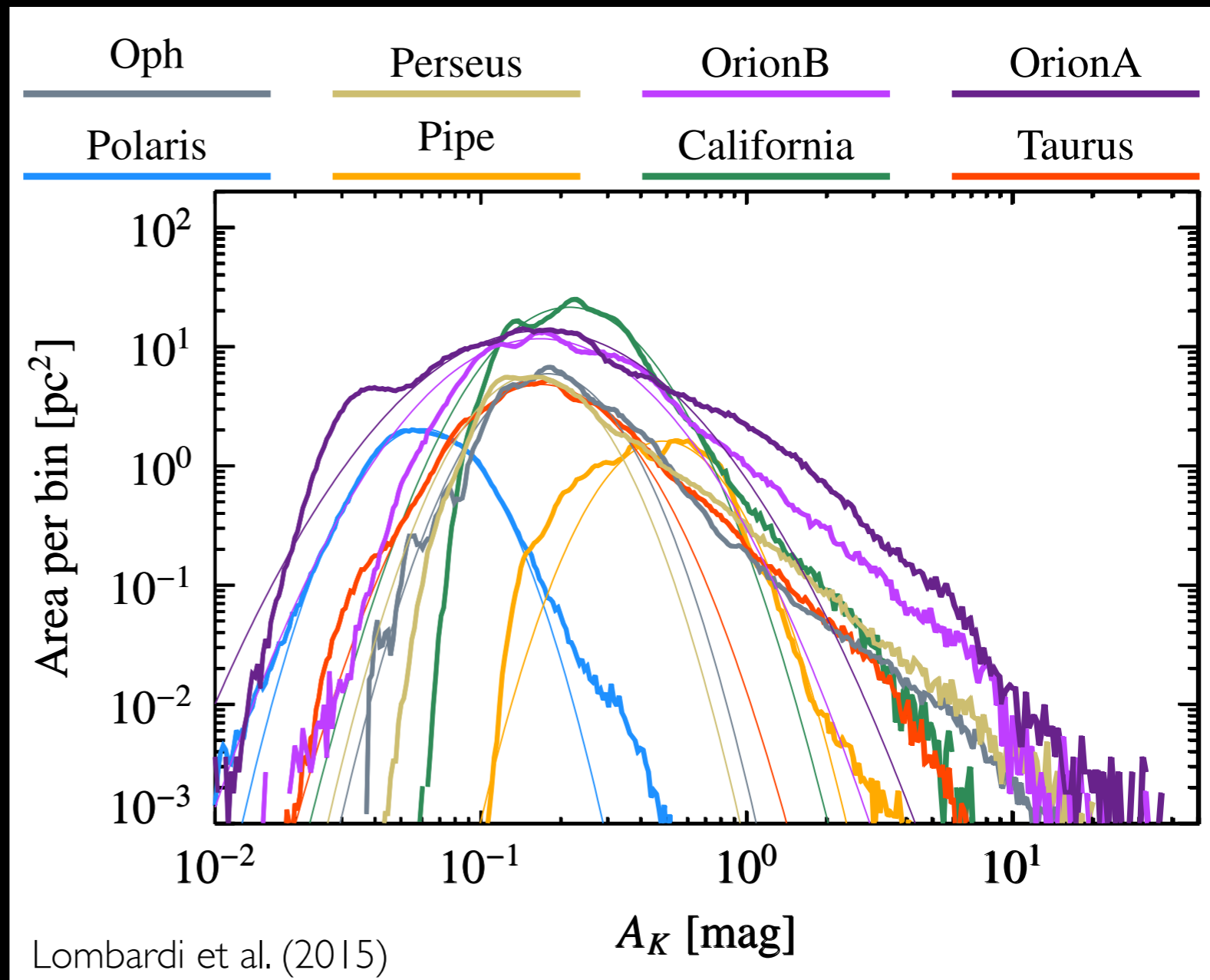
PDFs from Herschel

- PDFs are hardly symmetric in log-log



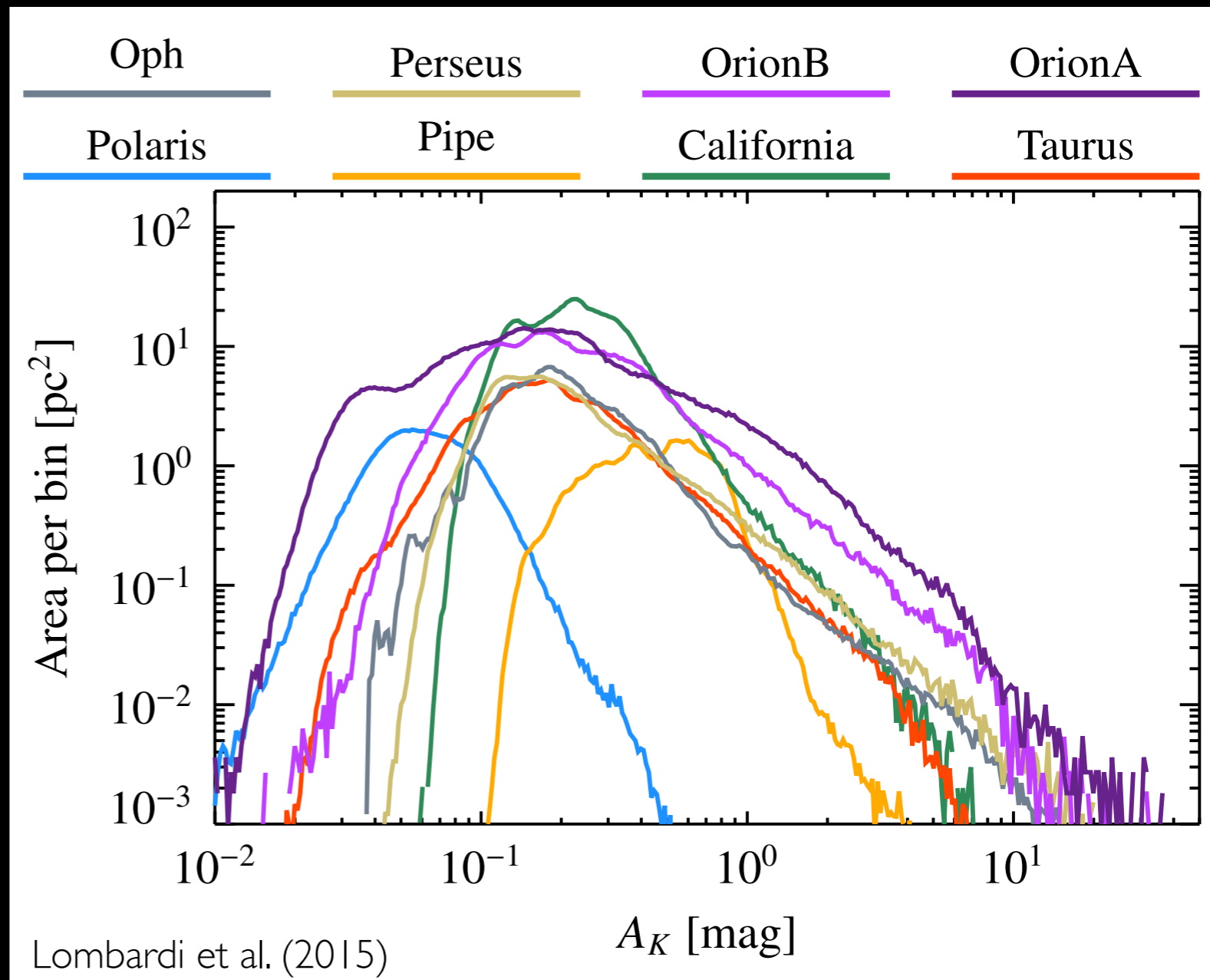
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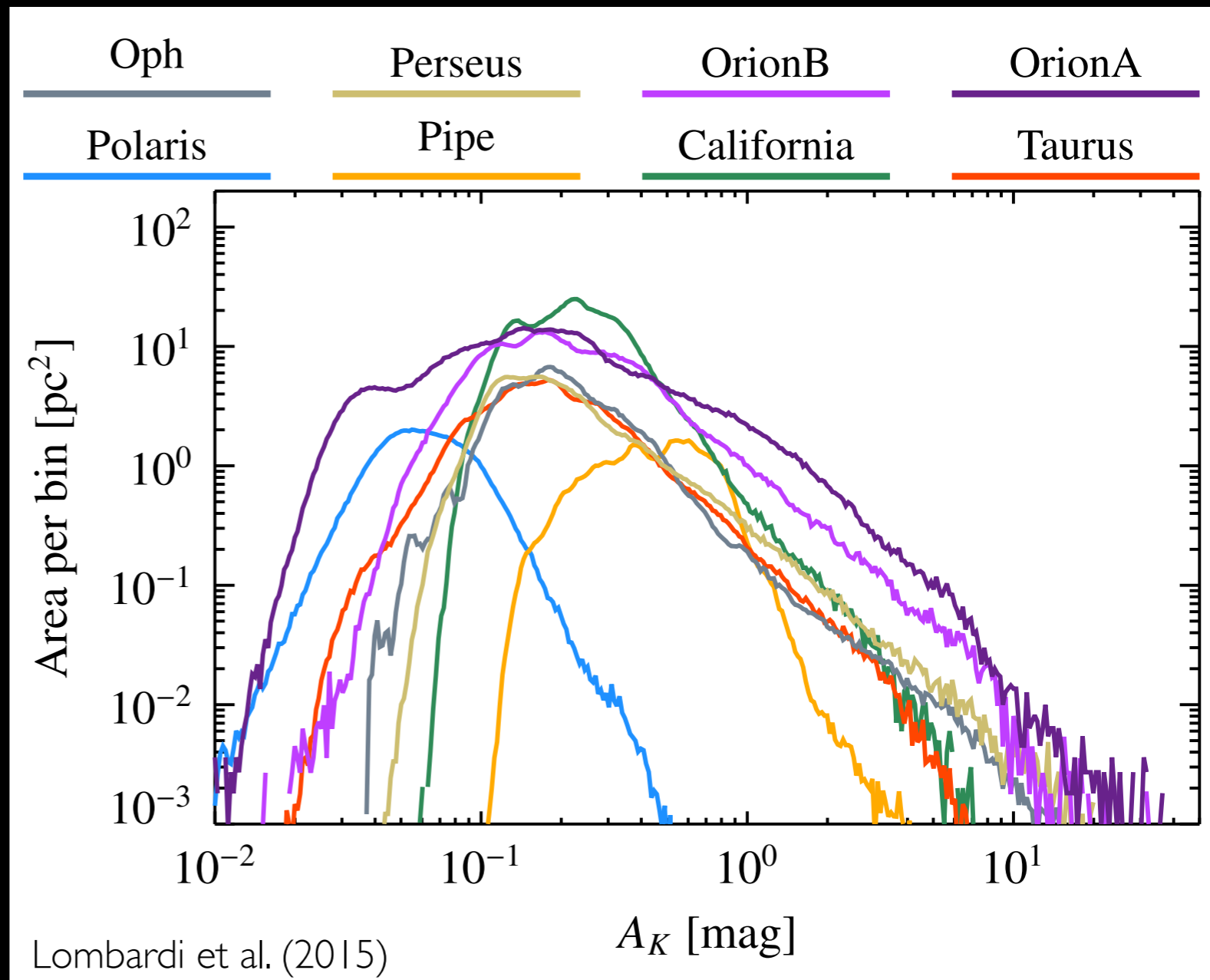
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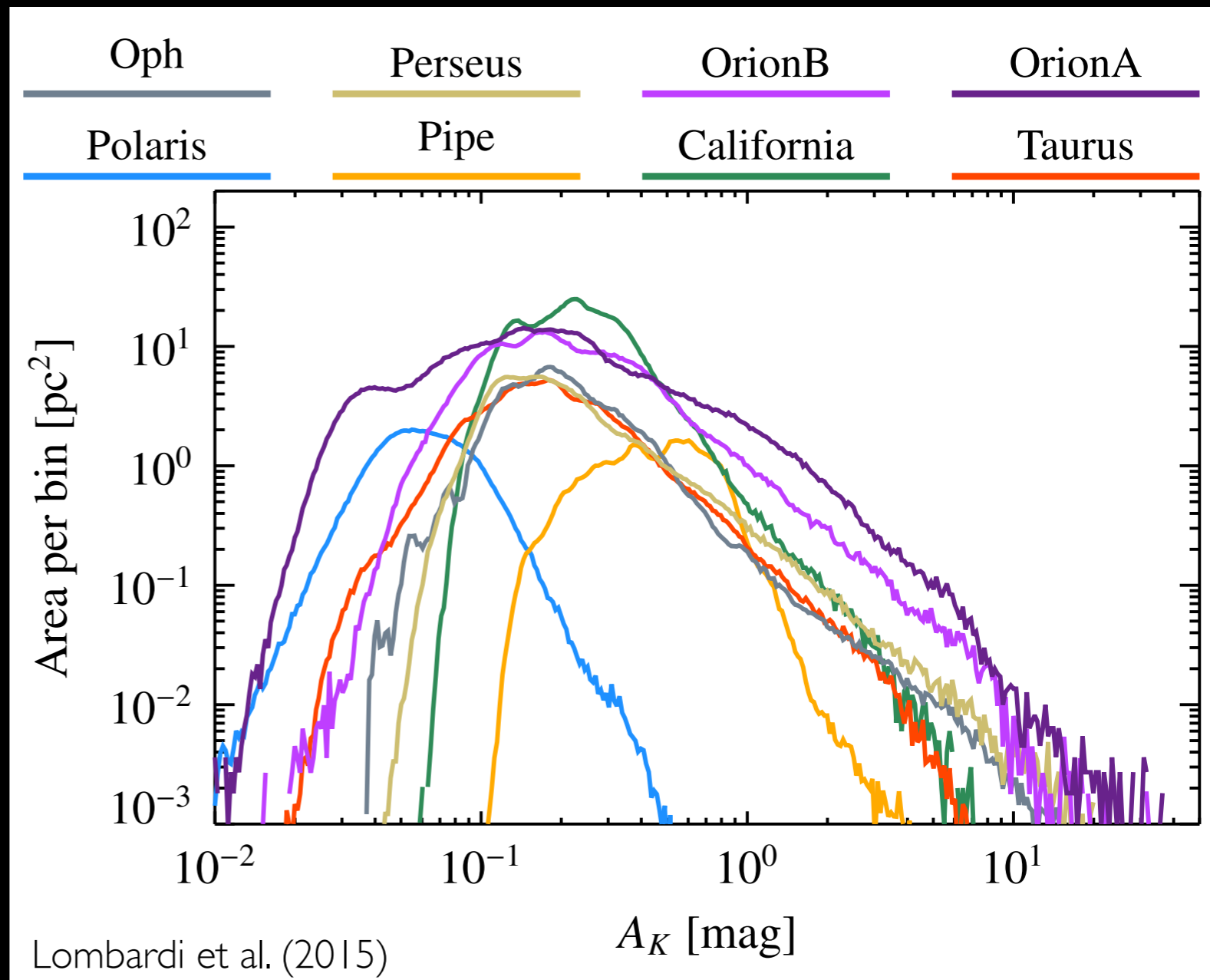
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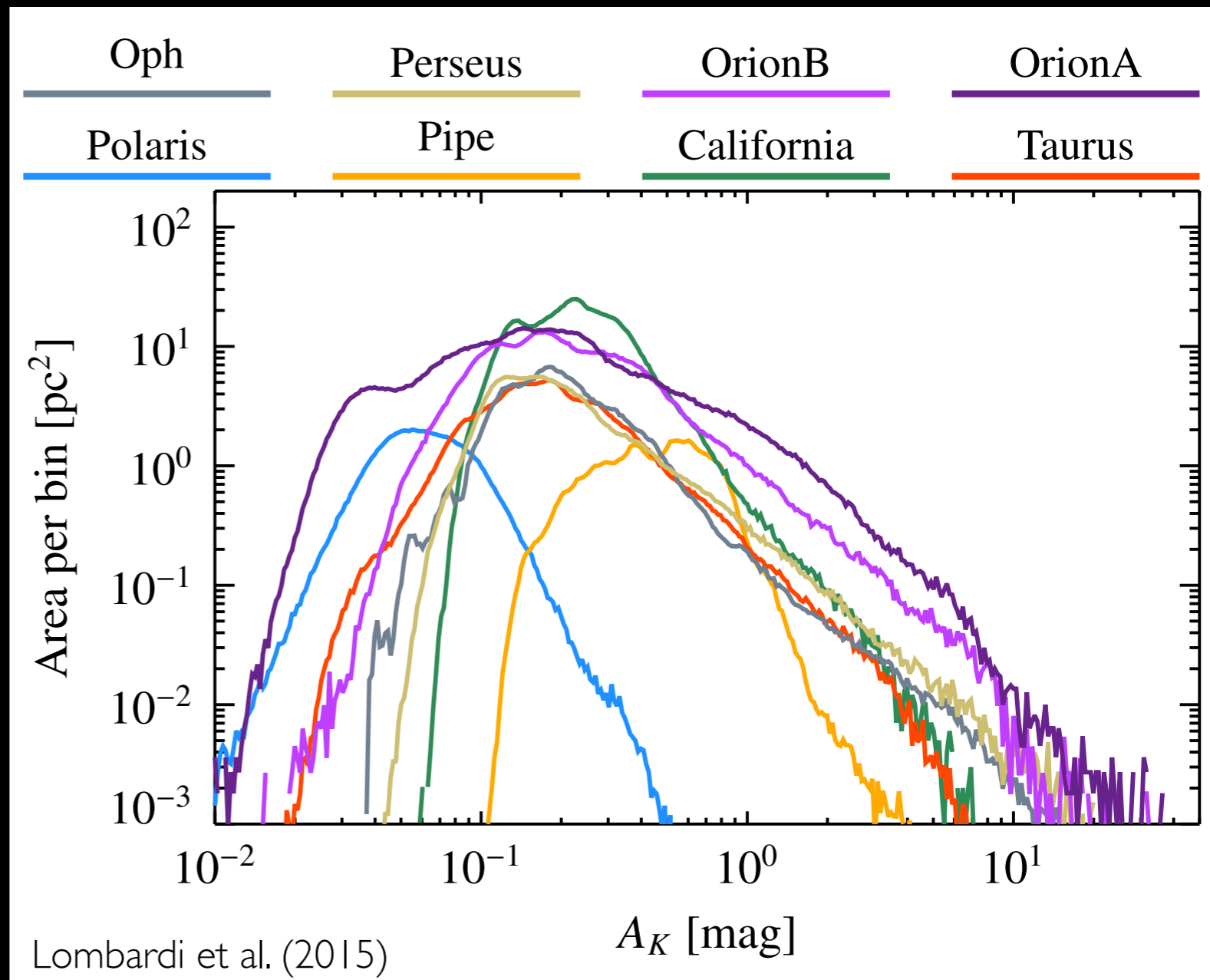
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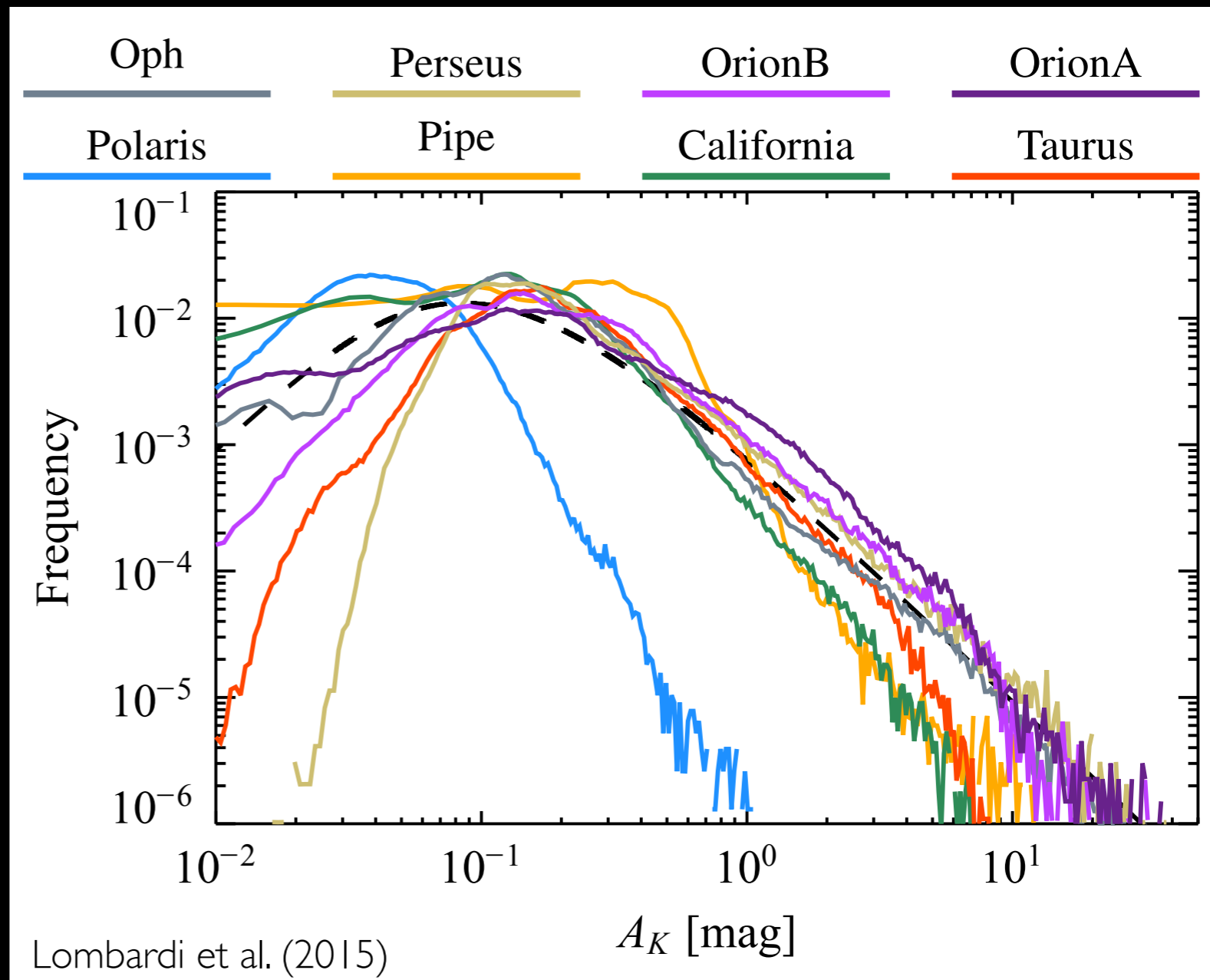
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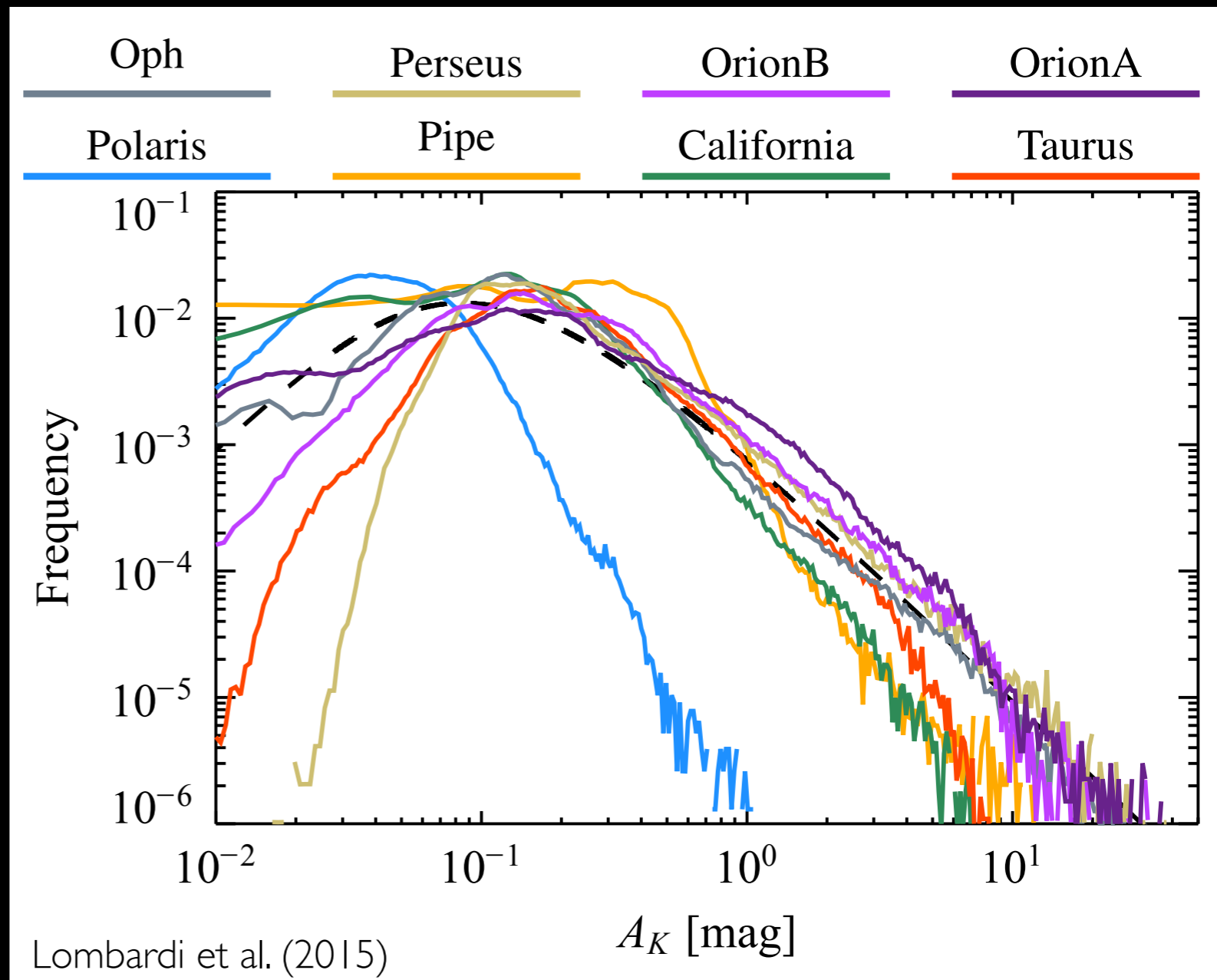
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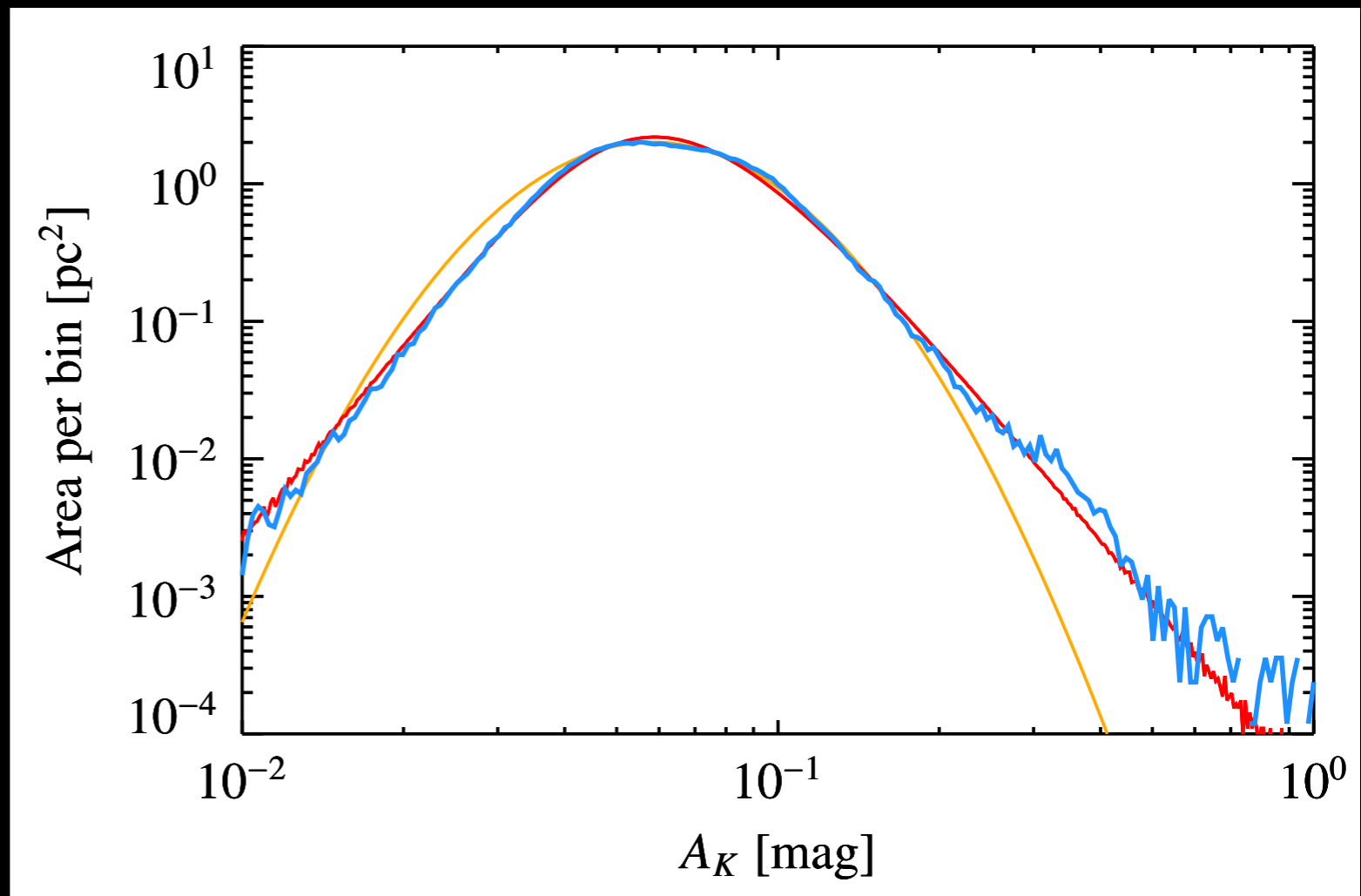
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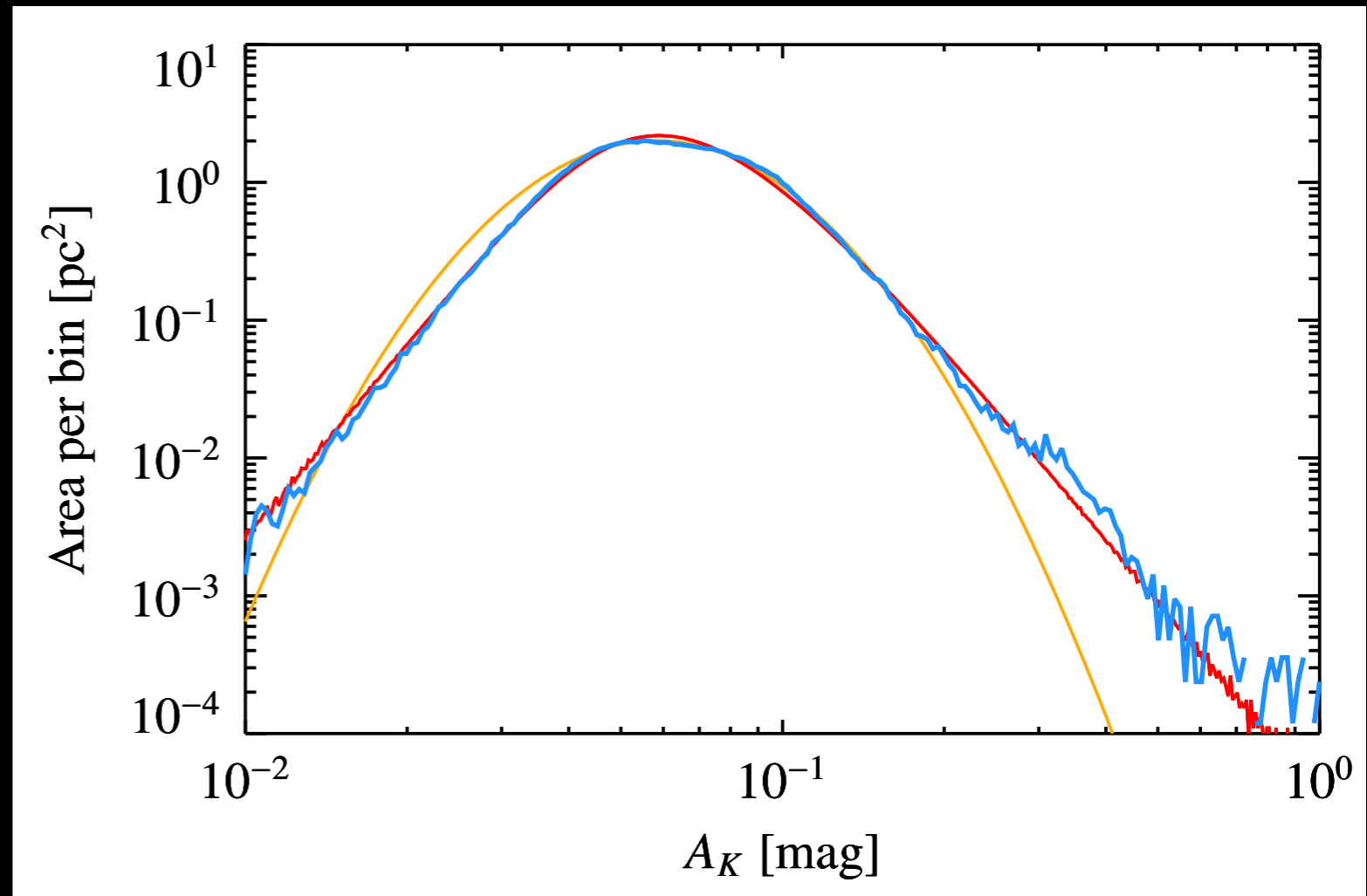
Can Polaris be described as log-normal?

Polaris log-normal fit



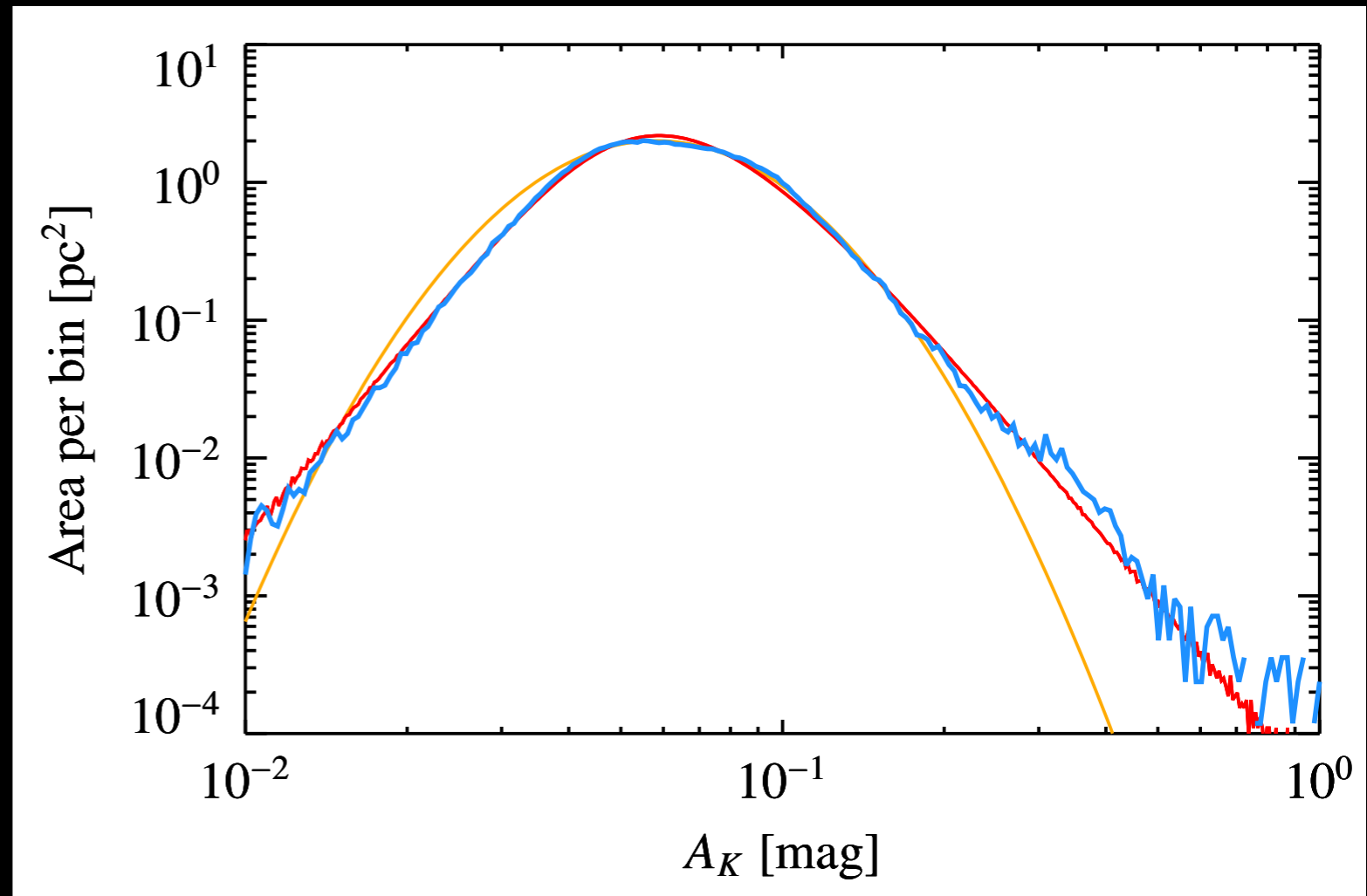
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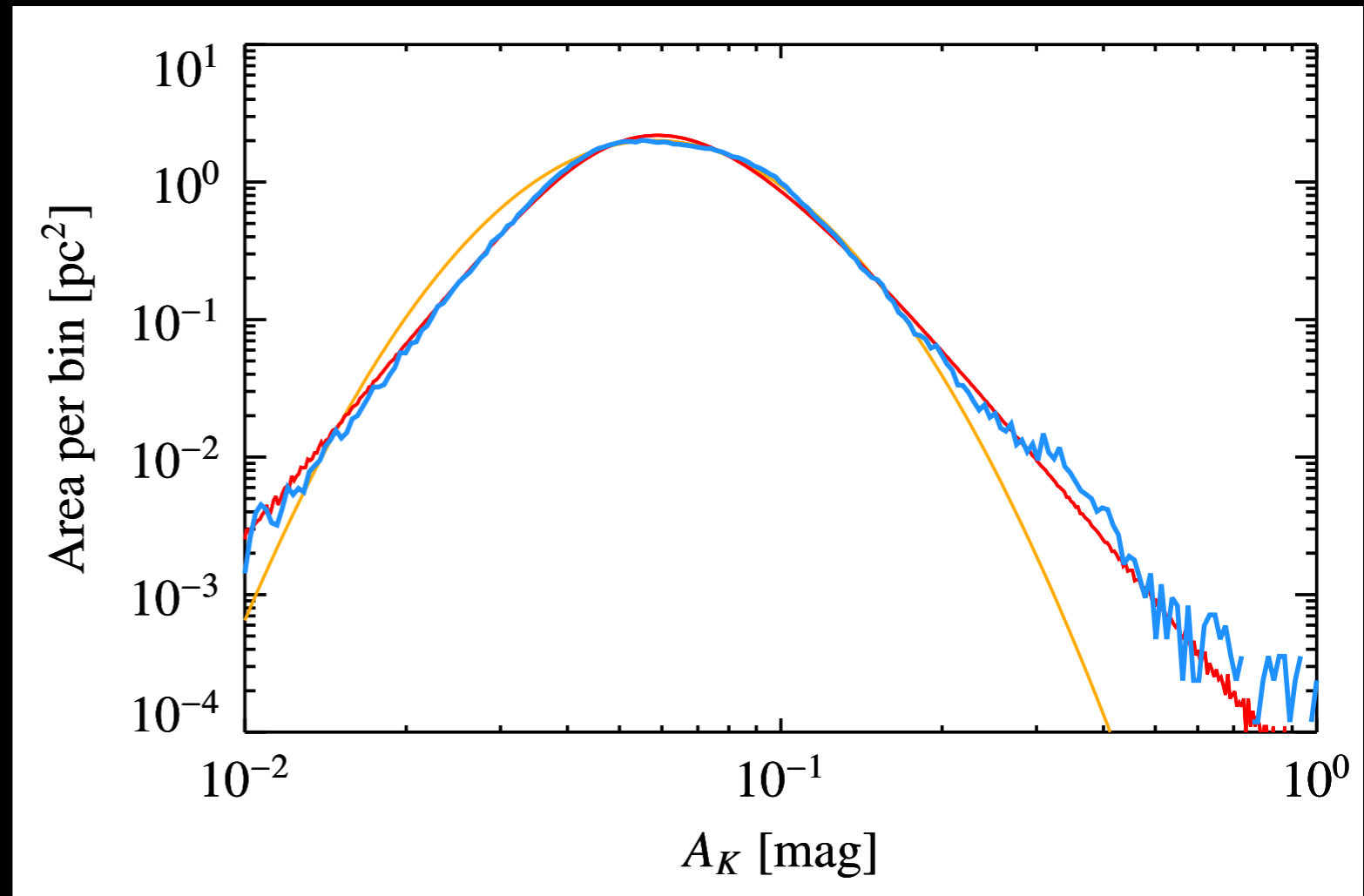
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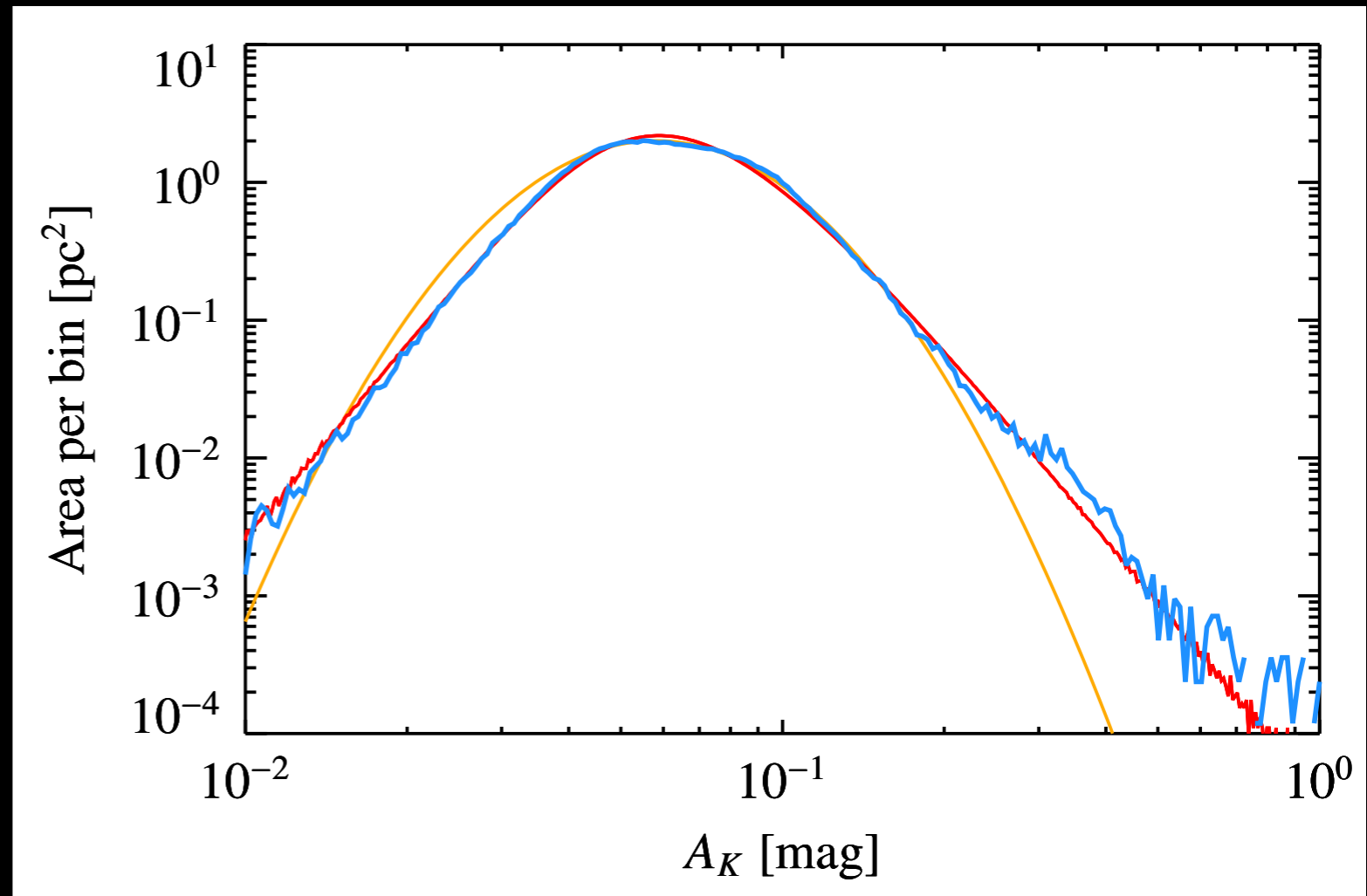
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- The associated PDF fits the measured one over 2 order of magnitudes!
- Caveat: ad-hoc model, but shows that log-normal is not that good



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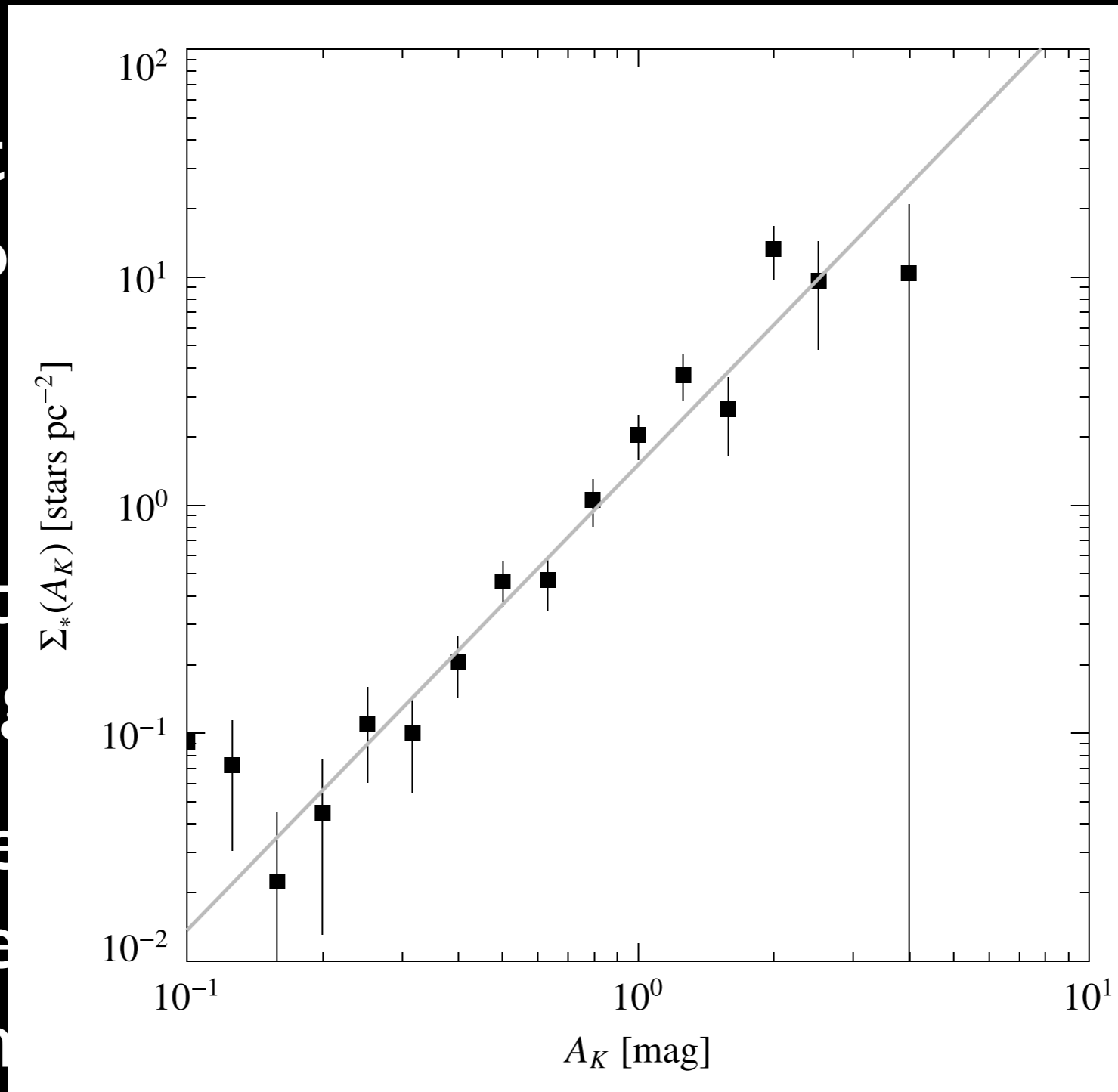
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$$\Sigma_{\star}(x) = \kappa [A_K(x)]^{\beta}$$

- Both coefficients seem to have a limited range of variation
- The SFE of a cloud is ultimately linked to its internal structure and PDF (amount of dense gas)

The local Schmidt law

- In the...
- Both...
- The...



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SUMMARY

1. For 20 years we have screwed up the simplest characterization of cloud structure, the PDF... but we now know PDFs are power laws
2. Various other scaling laws hold (Larson's 3rd law, the local Schmidt law)
3. Large differences in the SFRs of molecular clouds are to be linked to their internal structure (slope of the PDF)

