### Sterile neutrino dark matter and constraints on its properties from astrophysics and cosmology

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Warm Dark Matter Workshop. Meudon. June 9, 2011

#### Concordance model at cosmological scales







- ACDM: about 20% of total energy density is in the form of non-baryonic matter
- This dark matter is scale-free (noninteracting, "cold", ...)
- Standard Model neutrinos do not contribute significantly to the Universe mass balance at matter-dominated epoch (CMB, LSS, ...)

#### Dark matter - a fundamental physics problem



- Is evidence for DM convincing?
   yes
- Is DM made up of particles? most plausible assumption
- Is DM baryonic? no (MACHO searches; BBN constraints; structure formation problems)
- Is DM made from neutrinos? no (neutrino DM would contradict the observed LSS)

- Any DM candidate must be produced in the early Universe before matter-radiation equality and have correct relic abundance
- It should be stable or cosmologically long-lived
- Its non-gravitational interaction with ordinary matter or electromagnetic radiation should be feeble (to be "dark")
- Its clustering properties should allow to explain the observed large scale structure



- Phenomenologically we know little about the properties of dark matter particles
- Theoretical bias aside, dark matter particles should generically have "weaker-than-weak" interaction strength with the Standard Model sector (*super-weakly interacting* particles)
- Such DM candidates indeed appear in many extensions of the Standard Model (sterile neutrinos, gravitino, axion, axino, Majoron,...)
- For super-weakly interacting particles laboratory "direct detection" methods may be quite challenging =>

For Super-WIMPs astrophysics and cosmology may be our main tools to discover the true nature of dark matter particles

# Example of super-weakly interacting particles: sterile neutrinos

- Neutrino oscillations:  $m_{\nu} \sim \sqrt{\Delta m_{\rm atm}^2} \sim 10^{-2} \text{ eV}.$ See-saw mechanism  $m_{\nu} \sim v^2 / \Lambda$ , where  $v = \langle H \rangle = 174 \text{ GeV}$  and new scale  $\Lambda \sim 10^{15} \text{ GeV}$
- **Dark matter** (not a SM particle!)
  - particles with weak cross-section will have correct abundance  $\Omega_{\rm DM}$  ("WIMP miracle"). New scale  $\sim 1$  TeV
  - Axions. New scale  $10^{10} 10^{12}$  GeV.
- **Baryon asymmetry of the Universe**: what ensured that for each  $10^{10}$  anti-protons there was  $10^{10} + 1$  proton in the early Universe?
  - Sakharov conditions: CP-violation; B-number violation; out-ofequilibrium processes (leptogenesis, phase transitions, etc.)
- Fine-tuning problems: CP-problem, hierarchy problem, grand unification, cosmological constant problem

#### Standard Model



#### Standard Model neutrinos are strictly massless

#### Right-chiral neutrino counterparts?



The most natural explanation of neutrino experiments – adding rightchiral counterparts to the Standard Model

- Charges of right neutrinos?
  - SU(3) : singlets
  - SU(2) : singlets ( $\nu = L\tilde{H}$  singlet combination)
  - $U_Y(1)$  : singlets ( $Y(\nu) = Y(Higgs)$ )
- Right-chiral neutrinos carry no charge under the Standard Model interactions sterile neutrinos
- Can add for them a Majorana mass

$$\mathcal{L}_{ ext{see-saw}} = i ar{N}_{I} \not \! \partial N_{I} + \underbrace{egin{pmatrix} ar{
u}_{e} - N_{I} \ ar{
u}_{\mu} - N_{J} \ \dots \ egin{pmatrix} ar{
u}_{\mu} - N_{J} \ egin{pmatrix} egin{pmatr$$

Standard Model neutrino masses are given by **see-saw formula**:



Neutrino mass matrix – 9 parameters. Dirac+Majorana mass matrix – 11 (18) parameters for 2 (3) sterile neutrinos. Two sterile neutrinos are enough to fit the neutrino oscillations data.

### Scale of Dirac and Majorana masses is not fixed by neutrino oscillation data!

#### "Popular" choices of see-saw parameters

- Yukawa couplings  $F_{\alpha I} \sim 1$ , i.e. Dirac masses  $M_D \sim M_t$ . Majorana masses  $M_I \sim 10^{15}$  GeV.
- Attractive features:
  - Provides a mechanism of baryon asymmetry of the Universe
  - Scale of Majorana masses is possibly related to GUT scale
- This model does not provide the dark matter particle
- Alternative? Choose Majorana masses M<sub>I</sub> of the order of masses of other SM fermions and make Yukawa couplings small



#### Mass spectrum of the $\nu \text{MSM}$

#### Sterile neutrinos behave as **superweakly interacting** heavy neutrinos

| $M_I < 1 \; \mathrm{MeV}$   | $M_I\gtrsim 1~{ m MeV}$ | $M_I \gtrsim 140 \; {\rm MeV}$ |  |
|-----------------------------|-------------------------|--------------------------------|--|
| $N_I \to \nu \nu \bar{\nu}$ | $N_I \to \nu e^+ e^-$   | $N_I \to \pi^{\pm} e^{\mp}$    |  |
| $N_I  ightarrow  u \gamma$  |                         | $N_I \to \pi^0 \nu$            |  |

Mixing angle with usual neutrinos  $\theta_I$ :

$$\theta_I^2 = \sum_{\alpha=e,\mu,\tau} \frac{M_{\mathrm{Dirac},\alpha I}^2}{M_{\mathrm{Majorana},I}^2} \ll 1$$



**Fermi constant:**  $G_F \rightarrow \boldsymbol{\theta} G_F$ 

Lifetime  $\tau \propto \theta_I^{-2} M_I^{-5}$ . Can be cosmologically long

Mixing angle  $\theta \ll 1$  means that sterile neutrinos can be out of equilibrium in the early Universe

### Neutrino Minimal Standard Model (*v*MSM) solves several beyond the Standard Model problems

- $\checkmark$  ... explains neutrino oscillations
- $\checkmark$  ... matter-antimatter asymmetry of the Universe
- ✓ ... provides a viable dark matter candidate that can be cold, warm or mixed (cold+warm)
- The vMSM is self-consistent and does not require any other particles ⇒ we have a complete description of the Universe from the time of reheating
- Coupled with Higgs inflation the vMSM is a complete and self-consistent theory Bezrukov & up to the Planck scale
   Coupled with Higgs inflation the vMSM is a complete and self-consistent theory Bezrukov & Shaposhnikov (2008)

Asaka, Shaposhnikov Laine, **O.R.**, Boyarsky et al (2005-2011)

- Mass not restricted to the GeV range
- Can decay into the SM particles
- Produced in many different ways, non-thermally. Have nonuniversal spectrum of primordial velocities
- Can be warm or cold

Sterile neutrino DM is not completely dark. Its decay signal can

be searched for in the spectra of astrophysical objects.

#### Lifetime of sterile neutrino DM candidate

- Dominant decay channel for sterile neutrino (for  $M_s < 1$  MeV) is  $N \rightarrow 3\nu$ .
- Life-time  $\tau = 5 \times 10^{26} \text{sec} \times \left(\frac{\text{keV}}{M_s}\right)^5 \left(\frac{10^{-8}}{\theta^2}\right)^2$
- Subdominant radiative decay channel



- **Wolfenshtein** Pal (1982)
  - **Barger Phillips** Sarkar (1995)

Boyarsky, O.R

(2006-2009)

17

et al.

#### Search for dark matter particles

- DM may be decaying with a cosmologically long life-time (age of the Universe or even longer). Can we detect such decay?
- Yes! if you multiply a small number (probability of decay) with a large number (typical amount of DM particles in a galaxy  $\sim 10^{70}$ - $10^{100}$ )



Signal  $\propto \int \rho_{\rm DM}(r) dl$ line of sight

Expected signal from the galaxy at a particular energy

#### Search for dark matter particles

- DM may be decaying with a cosmologically long life-time (age of the Universe or even longer). Can we detect such decay?
- Yes! if you multiply a small number (probability of decay) with a large number (typical amount of DM particles in a galaxy  $\sim 10^{70}$ - $10^{100}$ )





Expected signal from a galaxy at a particular energy

In the case of decaying Dark Matter the signal, if detected, is easy to distinguish from astrophysical backgrounds



We have a lot of freedom in choosing observation targets and, therefore, can unambiguously check DM origin of a suspicious signal.



## For decaying DM "indirect" search becomes very promising!



MW (HEAO-1) Boyarsky, O.R et al. 2005

**Coma and** Virgo clusters Boyarsky, O.R et al.

**Bullet cluster** Boyarsky, O.R et al. 2006

LMC+MW(XM Boyarsky, O.R et al. 2006

**MW** Riemer-Sørensen et al.; Abazajian et al.

MW (XMM) Boyarsky, O.R et al. 2007

Results of almost 20 published works.

M31 Watson et al. 2006; 22Boyarsky et al 2007

Sterile neutrino DM and Lyman- $\alpha$ 

#### Window of parameters of sterile neutrino DM



#### Window of parameters of sterile neutrino DM



Asaka, Laine, Shaposhnikov

Laine, Shaposhnikov

**O.R.** and many others 2005-2010

#### Window of parameters of sterile neutrino DM



Laine,

Shaposhnikov

Asaka, Laine, Shaposhnikov

**O.R.** and many others 2005-2010

#### How sterile neutrino DM is produced?

Phenomenologically acceptable values of  $\theta_1$  are so small, that the rate of this interaction  $\Gamma$  of sterile neutrino with the primeval plasma is much slower than the expansion rate ( $\Gamma \ll H$ )

 $\Rightarrow$  Sterile neutrino are never in thermal equilibrium





How sterile neutrino DM is produced?



Sterile neutrinos have non-equilibrium spectrum of primordial velocities, roughly proportional to the spectrum of active neutrinos

$$f_s(p) \propto \frac{\theta^2}{\exp(\frac{p}{T_\nu(t)}) + 1} \qquad \Omega_s h^2 \sim \theta^2 M_s$$

(for this distribution  $\int dq \ q^2 f(q) \propto \theta^2 \ll 1$ )

• Average momentum  $\langle p \rangle \approx 3T_{max} \gg M_s$ 

#### Sterile neutrinos are produced highly relativistic

### Probing primordial velocities of dark matter particles

- Sterile neutrino DM is produced at temperatures  $T \sim 100$  MeV (for masses  $\sim \text{ keV}$  created relativistic  $\Rightarrow$  warm dark matter
- Relativistic particles free stream out of overdense regions and smooth primordial inhomogeneities

$$\lambda_{FS}^{co} = \int_0^t \frac{v(t')dt'}{a(t')}$$

Power spectrum of primordial density perturbations is suppressed at scales below free-streaming horizon





- Free-streaming horizon determines power spectrum suppression scale. (i.e. by the time of matter-radiation equality certain small scale primordial perturbations are suppressed/erased)
- For particle with Fermi-Dirac spectrum (thermal relics)

Bode et al. 2001

$$f(v) = \frac{1}{\exp\left\{\frac{M_{\mathsf{DM}}v}{T(t)}\right\} + 1}$$

this suppression is strong:

$$T(k) \equiv \sqrt{\frac{P(k)}{P_{\Lambda \text{CDM}(k)}}} \propto \left(\frac{k_{\text{FS}}}{k}\right)^{10} \qquad k_{\text{FS}} \sim 0.5 \frac{h}{\text{Mpc}} \frac{M_{\text{DM}}}{\text{keV}}$$

- Primordial velocities affect:
  - Power-spectrum of density fluctuations (suppress normalization at large scale)
  - Halo mass function (number of halos of small mass decreases)
  - Dark matter density profiles in individual objects
- Scales probed by CMB and LSS experiments (linear regime of perturbation growth)

$$k \simeq \ell \times \frac{H_0}{2} = \frac{\ell}{6000} \frac{h}{\text{Mpc}}$$

- Is sensitive up to scales  $k \leq 0.1 \ h/$  Mpc (See the next talk by Katarina Markovic about future sensitivity of LSS probes)
- Smaller scales? Non-linear stage of structure formation





### Is small number of observed substructures due to dark matter free-streaming?

#### WDM substructure suppression



Thermal relics with mass  $\sim 1~{\rm keV}$  would erase too many Maccio & substructures. Anything "colder" would produce enough structures  $^{\rm Fontanot}_{(2009);}$  to explain observed Milky Way structures

Polisensky & Ricotti (2010)




#### Lyman- $\alpha$ forest and cosmic web



Neutral hydrogen in intergalactic medium is a tracer of overall matter density. Scales  $0.3h/{
m Mpc} \lesssim k \lesssim 3h/{
m Mpc}$ 

#### Lyman- $\alpha$ forest and cosmic web



Image: Michael Murphy, Swinburne University of Technology, Melbourne, Australia

# Neutral hydrogen in intergalactic medium is a tracer of overall matter density. Scales $0.3h/{\rm Mpc} \lesssim k \lesssim 3h/{\rm Mpc}$

- Astronomical data analysis of quasar spectra
- Astrophysical modeling of hydrogen clouds
- N-body+hydrodynamical simulations of DM clustering at non-linear stage
- Simultaneous fit of cosmological parameters ( $\Omega_b, \Omega_M, n_s, h, \sigma_8 \dots$ ). Astrophysical parameters, describing IGM, are not known and should be fitted as well (another 20+ parameters)
- The data: Lyman-α+ CMB + maybe LSS . . . (thousands of data points, sometimes correlated)

0.1  $\Delta_{\rm F}^{\rm 2}({
m k})$ 0.01 0.001 0.01  $k [(km/s)^{-1}]$ 

#### Measured flux power spectrum is compared against CDM and non-CDM models

Seljak et al. '06



These bounds are for **non-resonantly produced** sterile neutrinos or **thermal relics** only!

#### Lyman- $\alpha$ forest and warm DM

- Previous works put bounds on free-streaming  $\lambda_{FS} \lesssim 150$  kpc Viel et al. ("WDM mass" > 8 keV)  $\gtrsim 150$  kpc Viel et al. 2005-2007; Seljak et
- The simplest WDM with such a free-streaming would not modify al.(2006) visible substructures:



Maccio & Fontanot (2009);

Polisensky & Ricotti (2010)

Thermal relic with exponential cut-off ~ 1 Mpc (= NRP sterile neutrino with the mass ~ 4.5 keV) would erase too many substructures. Anything "colder" would produce enough structures to explain observed Milky Way structures



Does this mean that sterile neutrino dark matter *ruled out*? – **NO**!

## Window of parameters of sterile neutrino DM

Once again:

Laine, Shaposhnikov



## Window of parameters of sterile neutrino DM



Asaka, Laine, Shaposhnikov

Laine, Shaposhnikov Quick reminded: necessary conditions for generation of baryon <sup>(1967)</sup> asymmetry of the Universe (Sakharov conditions): Kuzmin, Rubakov,

 $(\bullet)$  B-number violation  $\rightarrow$  sphalerons

(?) CP (and C) non-conservation  $\rightarrow$  phase of the CKM matrix

Out-of-equilibrium processes  $\rightarrow$  no phase transition in the SM for  $\frac{\text{Kajantie et al.}}{(1996)}$  $m_H > 72 \text{ GeV!}$ 

What changes in the  $\nu$ MSM?

Shaposhnikov

Shaposhnikov

(1985)

Farrar &

(1994)

Necessary conditions for generation of baryon asymmetry of the <sup>(1967)</sup> Universe (Sakharov conditions): Kuzmin,

(+) B-number violation  $\rightarrow$  sphalerons

? CP (and C) non-conservation → phase of the CKM matrix plus additional CP phases in the Dirac mass matrix of sterile neutrinos

Kajantie et al. (1996)

Rubakov,

(1985)

Farrar &

(1994)

Shaposhnikov

Shaposhnikov

 $\bigcirc$  Out-of-equilibrium processes  $\rightarrow$  no phase transition in the  $\nu$ MSM for  $m_H > 72$  GeV! but Yukawa couplings of sterile neutrinos are small enough to keep them out of thermal equilibrium at  $T \sim 100$  GeV

# Baryo- and lepto-genesis in the $\nu MSM$



At  $T > T_{sph}$  lepton asymmetry gets converted to baryon asymmetry by sphalerons — baryogenesis

• At  $T_{\rm sph} > T > T_+$  lepton asymmetry continues to be generated where  $|F|^2 T_+ = \frac{T_+^2}{M}$  (the Yukawa coupling  $|F|^2 \sim \frac{Mm_{\rm atm}}{v^2}$  from neutrino oscillations)

#### Resonant production



The presence of lepton asymmetry in primordial plasma makes active-sterile mixing much more effective – resonant production Shi Fuller'98

Shi Fuller'98 Laine, Shaposhnikov

Maximal amount of DM produced resonantly:

 $\Omega_{\rm RP}h^2 \propto M_s L_6$ 

#### - independent of the mixing angle!



Laine, Shaposhnikov'08; Boyarsky, O.R., Shaposhnikov'09

**Oleg Ruchayskiy** 



Velocity spectra of resonantly produce sterile neutrinos with the mass 2 keV, produced at different lepton asymmetries



**Transfer functions** of resonantly produce sterile neutrinos with the mass 2 keV, produced at different lepton asymmetries

Models with admixture of cold DM component (relevant for resonantly produced sterile neutrino DM, gravitino DM)



- *k*<sub>FSH</sub> depends on mass, does not depend on WDM fraction
- T(k) falls slower if more CDM
- For small WDM fraction T(k) cannot be distinguished from CDM within the precision of the data



Boyarsky, Lesgourgues, **O.R.**, Viel JCAP, PRL 2009;

Boyarsky, O.R., Shaposhnikov Ann. Rev. Nucl. Part. Sci. 2009

- Revised version of these bounds in CDM+WDM (mixed, CWDM) models demonstrates that
  - The primordial spectra are not described by free-streaming
  - There exist viable models with the masses as low as 2 keV



Boyarsky, O.R., Lesgourgues, Viel JCAP & PRL (2009)





#### Halo substructure with sterile neutrino DM



Lovell, Frenk, Theuns, **O.R** and others, 2011

work in progress

#### Halo substructure with CDM

Aq-A2 halo

# Halo substructure with sterile neutrino DM



Aq-A-2 CDM halo

**PRELIMINARY:** *Aq-A-2 halo* made of sterile neutrino DM (Gao, Theuns, Frenk, **O.R.**, ...)

Simulated sterile neutrino DM halo (right) is fully compatible with the Lyman-α forest data but provides a structure of Milky way-size halo different from CDM Large satellites



Lovell, Frenk, Eke, ..., **O.R.** 1104.2929 [astro-ph.CO]

- Neutrino Minimal Standard Model (vMSM) provides resolution of all major observational BSM problems and gives a complete history of the Universe from inflationary era till today.
- Sterile neutrino dark matter can leave its imprints on formation of structures and can be detected via its monochromatic decays to photons
- Thermal relics WDM with interesting astrophysical and cosmological applications are ruled out by Lyman-*α*
- Sterile neutrino dark matter (as a part of the  $\nu$ MSM model) is a viable dark matter candidate, consistent with the Lyman- $\alpha$  constraints within a wide range of the model parameters.







# Thank you for your attention!

# A couple of slides about dark matter surface density

# Observations vs. simulations



O.R., Macciò and others, 0911.1774



- More than half of all objects obey the derived relation between parameters of DM density profiles
- For most of them  $\rho_s r_s \propto \rho_c r_c$
- Observable not sensitive to the choice of dark matter density profile?
- Dark matter column density

$$\mathcal{S} = \int_{\text{l.o.s.}} \rho_{\text{DM}}(r) dl \propto \rho_{\star} r_{\star}$$

•  $r_{\star}$  is a characteristic scale ( $r_{\star} = r_s$  for NFW,  $r_{\star} = 6.1r_c$  for ISO).

 $\rho_{\star}$  – average density inside  $r_{\star}$ 



DM surface density for different types of galaxies.


Baryonic surface density for different types of galaxies.

- There exist many works on dark matter distribution in individual objects
- Going through the literature we collected a "catalog" of ~1000 DM 0911.1774 density profiles for ~300 individual objects, ranging from dwarf spheroidal satellites of the Milky Way to galaxy clusters
- Different groups of astronomers use different dark matter profiles to fit the mass distribution (ISO, NFW, BURK, ...)
- Often fits to different DM density profiles exist for the same object. How to relate their parameters?

Fitting the same (simulated) data with two different profiles



- one finds a relation between parameters of two DM density distribution, fitting the same data
   0911.1774
  - NFW vs. ISO :  $r_s \simeq 6.1 r_c$  ;  $\rho_s \simeq 0.11 \rho_c$
  - NFW vs. BURK :  $r_s \simeq 1.6 r_B$  ;  $\rho_s \simeq 0.37 \rho_B$
- Is this relation actually observed?

## About 60 objects with both NFW and ISO profiles



Number of profiles





- The data spans many orders of magnitude in halo masses ( $10^8 M_{\odot}$   $10^{15} M_{\odot}$ )
- The relation between S and  $M_{halo}$  is observed for halos of all scales
- Actual observed halos reproduce concentration-mass relation known in simulations for decades but never probed before over such a large mass scale
- Its median value and scatter coincide remarkably well with pure dark matter numerical simulations
- Separately the slope of subhalos is reproduced
- No visible features universal (scale-free) dark matter down to the lowest observed scales and masses?

Dark Matter Search Using Chandra Observations of Willman 1, and Loewenstein 8 a Spectral Feature Consistent with a Decay Line of a 5 keV Sterile Kusenko (Dec'2009) Neutrino



Can the excess in the FeXXVI Ly gamma line from the Galactic Prokhorov & Center provide evidence for 17 keV sterile neutrinos?
Silk (Jan'2010

## Do we see this line anywhere else? Objects with comparable $S_{\rm MW}$ Msun/pc<sup>2</sup> expected signal for which 600 archival data is available 500 Fornax dSph (XMM) $\mathcal{S}_F = 54.4 M_{\odot} \mathrm{pc}^{-2}$ 400 M31 Sculptor dSph 300 (Chandra) $S_{Sc} = 140 M_{\odot} \, \mathrm{pc}^{-2}$ Willman 1 200 Sculptor 100 Andromeda galaxy Fornax • (M31): 0 $S_{M31} \sim 100 - 600 M_{\odot} / \mathrm{pc}^2$ 150 50 100 0

# Do we see this 2.5 keV line?

## DM in Andromeda galaxy (2008)



## DM in Andromeda galaxy (2010)





## Checking for DM line in M31

Willman 1 spectral feature excluded with high significance from archival observations of M31 and Fornax and Sculptor dSphs

- Many DM-dominated objects would provide comparable decay signal. Freedom in choosing observation targets that optimize the signal-to-noise ratio (with well-controlled astrophysical backgrounds).
- Candidate line can be distinguish from astrophysical backgrounds by studying its surface density and sky distribution.

# For decaying dark matter indirect search becomes direct!

- CWDM Ly- $\alpha$  bounds: about 20% of DM can be rather warm
- Primordial velocities at MD epoch can be significant ( $\sim 10$  km/sec)
- Numerical simulations with velocities? Require high resolution



- CWDM Ly- $\alpha$  bounds: about 20% of DM can be rather warm
- Primordial velocities at MD epoch can be significant ( $\sim 10$  km/sec)
- Numerical simulations with velocities?

Effect of velocities is negligible at scales of interest:

Work in progress

$$\frac{\Delta P(k,z)}{P(k,z)} \simeq -3.2 \times 10^{-6} \left(\frac{k}{h \,\mathrm{Mpc}^{-1}}\right)^2 \left(\frac{\mathrm{keV}}{M_s}\right)^2 \left(\frac{0.27}{\Omega_M}\right) (1+z_i)$$

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