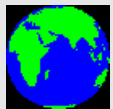


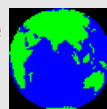
Structural properties of Galaxies and Cored Density Profiles from Galaxy Observations

PAOLO SALUCCI

SISSA

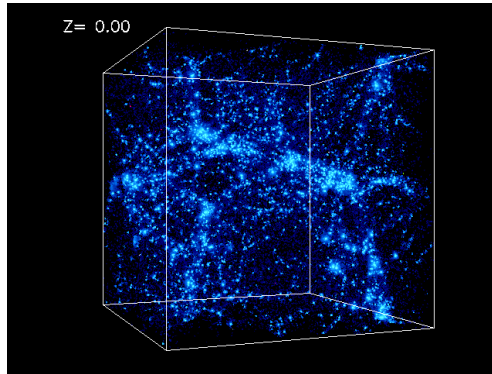
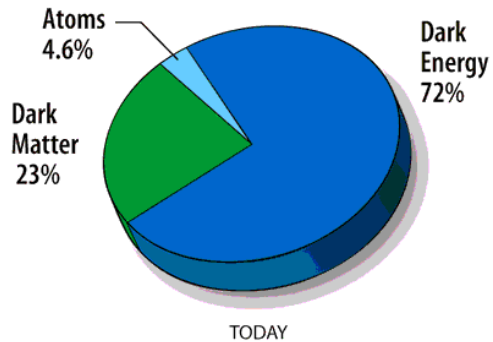


Ecole Internationale Daniel Chalonge
Workshop CIAS Meudon 8-10/6/2011



Outline

Dark Matter: main protagonist in Cosmology, change of paradigm?



This lecture focus: Dark Matter distribution in Galaxies

The concept of Dark Matter in virialized objects

Dark Matter in Spirals, Ellipticals, dSph

Phenomenology of the mass distribution in Galaxies and theoretical predictions

spiral



elliptical



**3 MAJOR TYPES
OF GALAXIES**

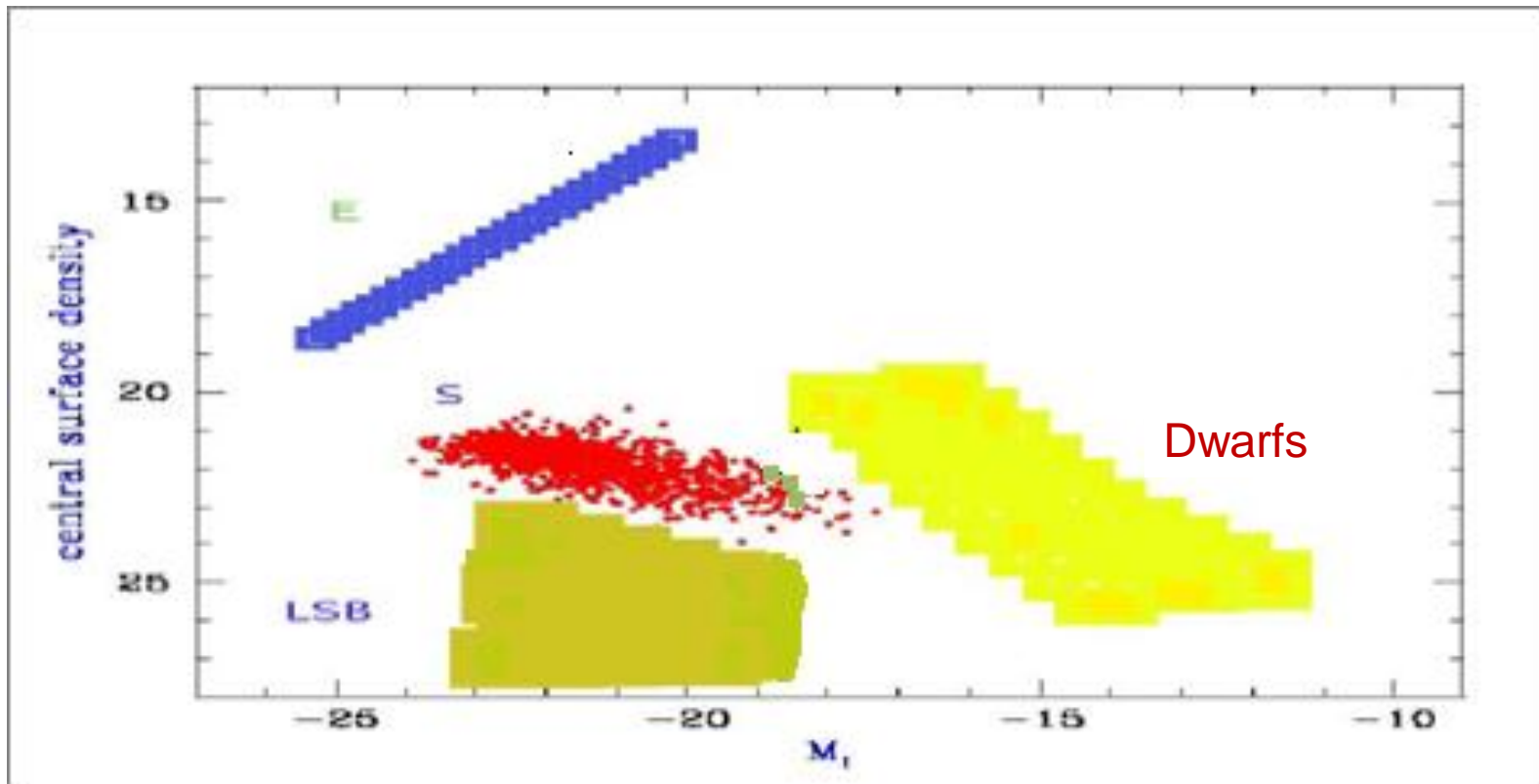
dwarfs



The Realm of Galaxies

The range of galaxies in magnitudes, types and central surface densities : 15 mag, 4 types, 16 mag arsec⁻²

Central surface brightness vs galaxy magnitude



Spirals : stellar disk +bulge +HI disk

The distribution of luminous matter :

Ellipticals & dwarfs E: stellar spheroid

What is Dark Matter ?

In a galaxy, the radial profile of the gravitating matter $M(r)$ does not match that of the luminous component $M_L(r)$.

A **MASSIVE DARK COMPONENT** is then introduced to account for the disagreement:

Its profile $M_H(r)$ must obey:

$$\frac{d \log M(r)}{d \log r} = \frac{M_L(r)}{M(r)} \frac{d \log M_L(r)}{d \log r} + \frac{M_H(r)}{M(r)} \frac{d \log M_H(r)}{d \log r}$$

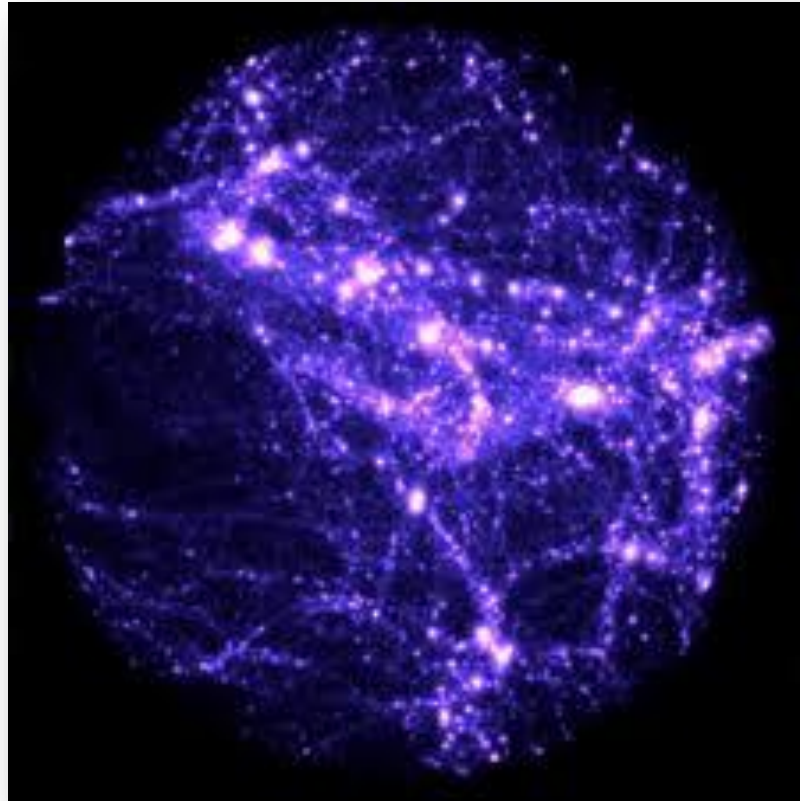
$M(r)$, $M_L(r)$, $d \log M_L(r)/d \log r$ **observed**

The DM phenomenon can be investigated only if we **accurately** measure the distribution of:

Luminous matter $M_L(r)$.

Gravitating matter $M(r)$

THEORY AND SIMULATIONS



Λ CDM Dark Matter Density Profiles from N-body simulations

The density of virialized DM halos of any mass is empirically described at all times by an Universal profile (Navarro+96, 97, NFW).

$$\rho_{NFW}(r) = \delta\rho_c \frac{r_s}{r} \frac{1}{(1+r/r_s)^2}$$

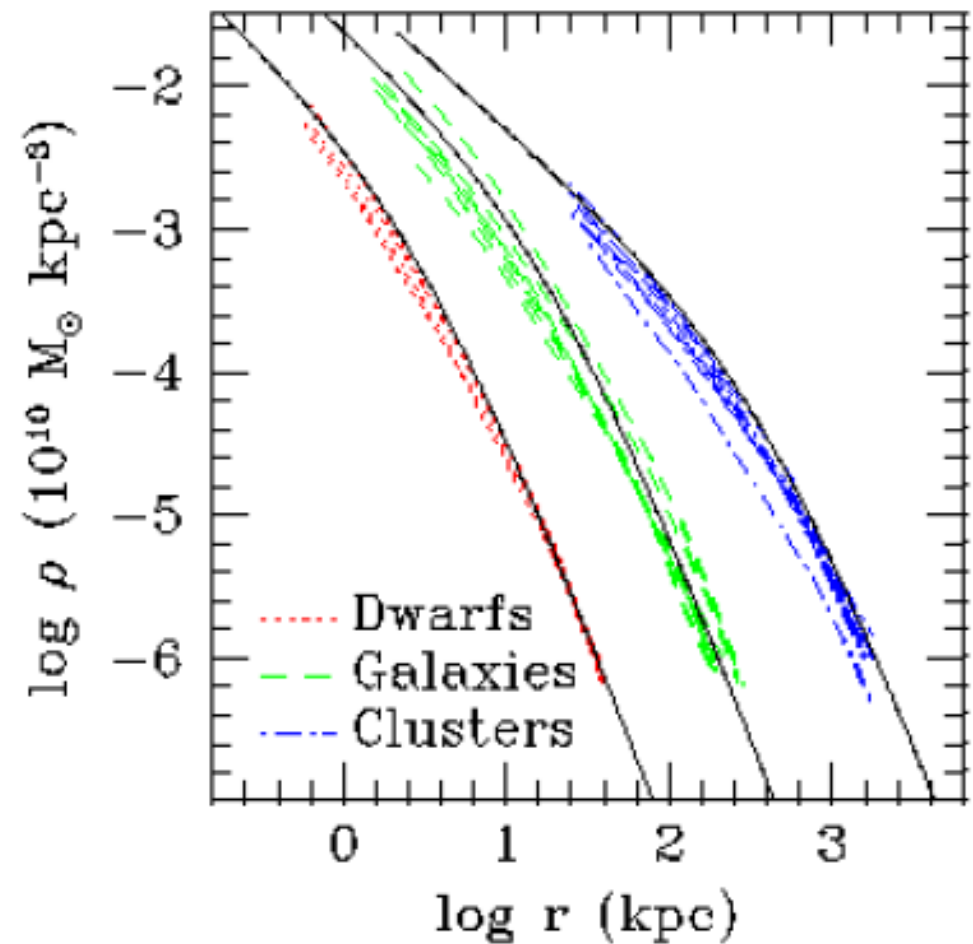
$$c = \frac{R_{vir}}{r_s} \quad R_{vir} = 260 \left(\frac{M_{vir}}{10^{12} M_\odot} \right)^{1/3} \text{ kpc}$$

More massive halos and those formed earlier have larger overdensities

Today mean halo density inside

$$R_{vir} = 100 \rho_c$$

$$c(M_{vir}) = 9.35 \left(\frac{M_{vir}}{10^{12} M_\odot} \right)^{-0.09} \quad \text{Klypin, 2010}$$

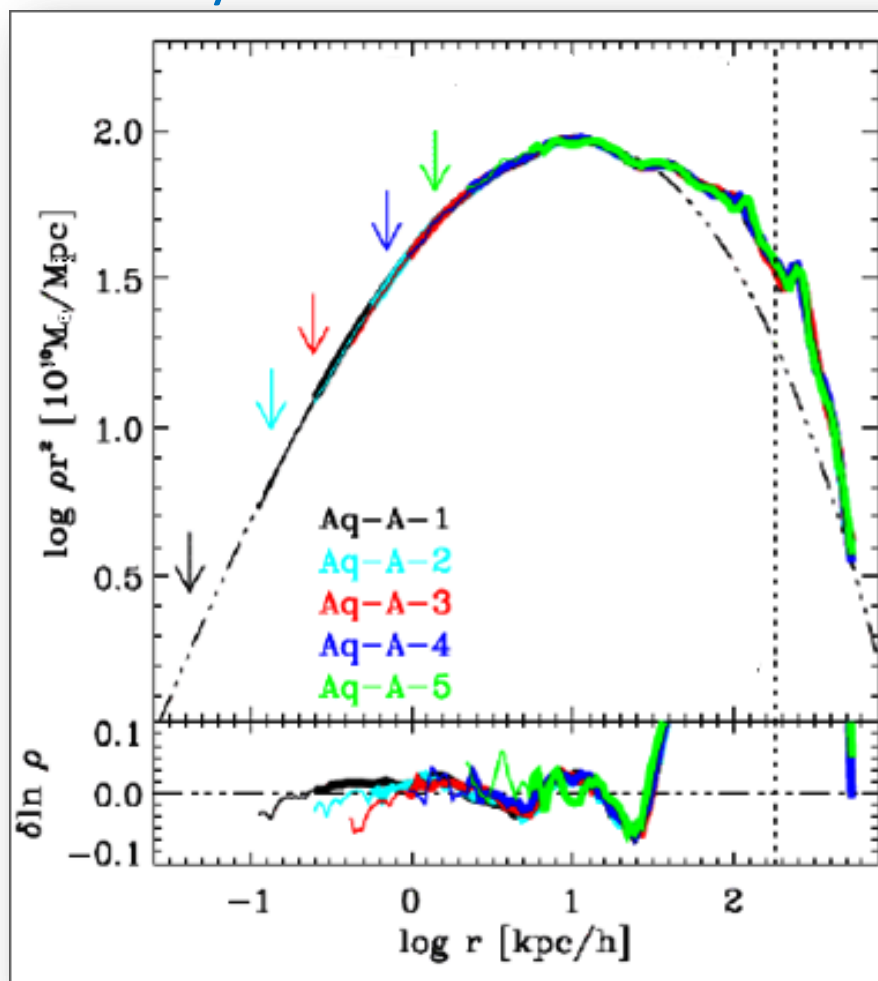


Aquarius N-Body simulations, highest mass resolution to date.

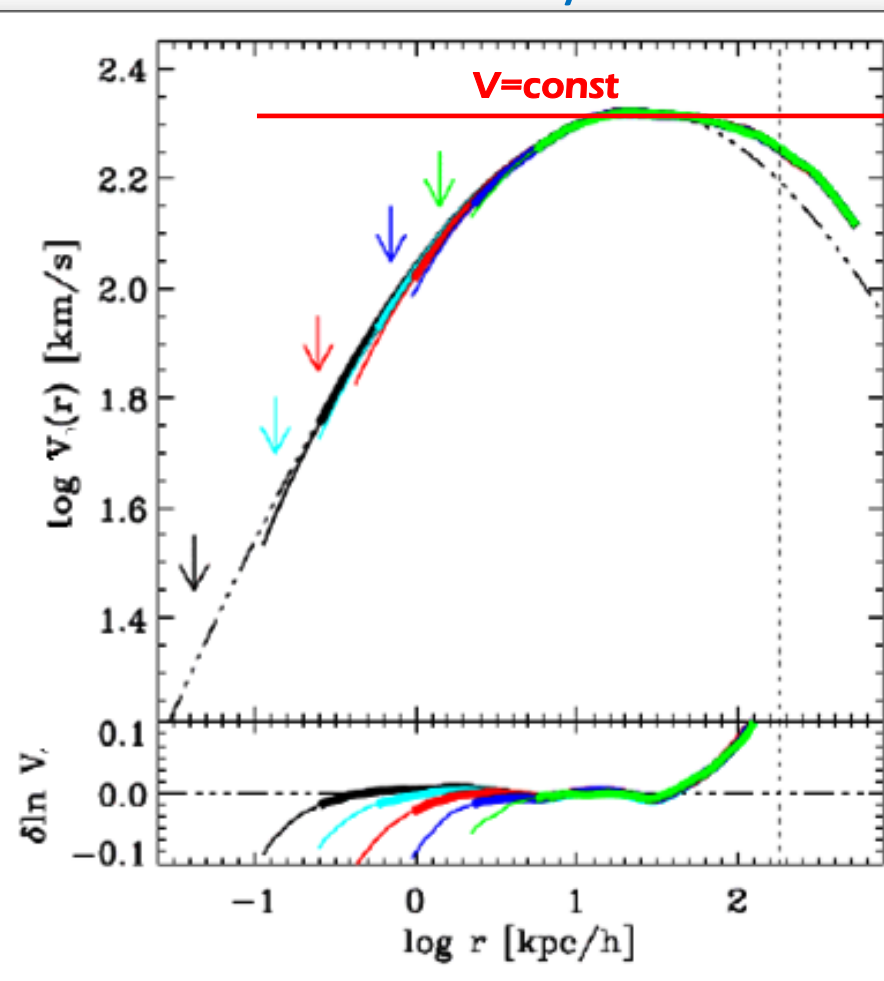
Density: central cusp $\rho \approx r^{-1}$, asymptotically: $\rho \approx r^{-2.5}$

Navarro et al +10

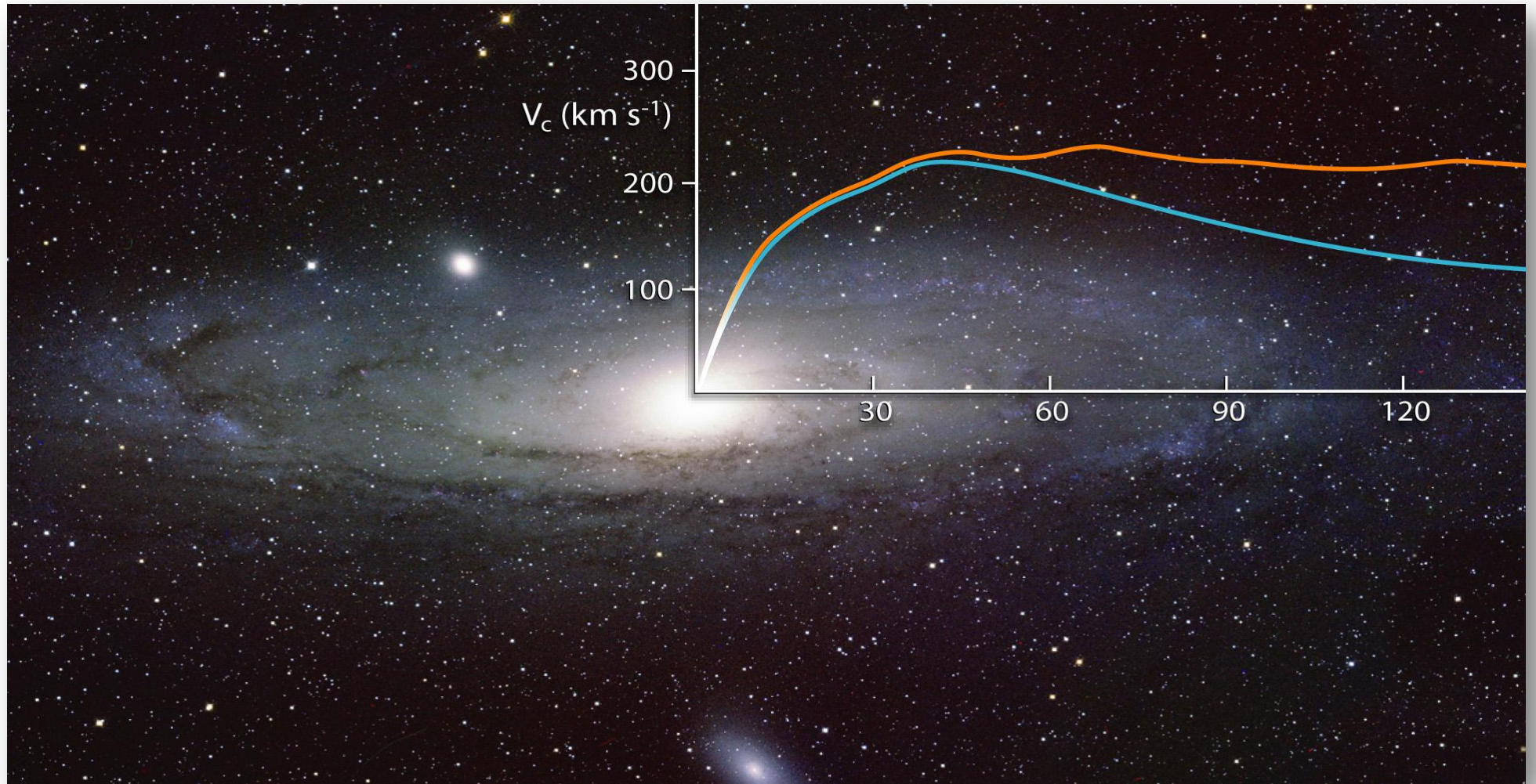
density



circular velocity



SPIRALS





Stellar Disks

M33 disk very smooth,
truncated at 4 scale-lengths

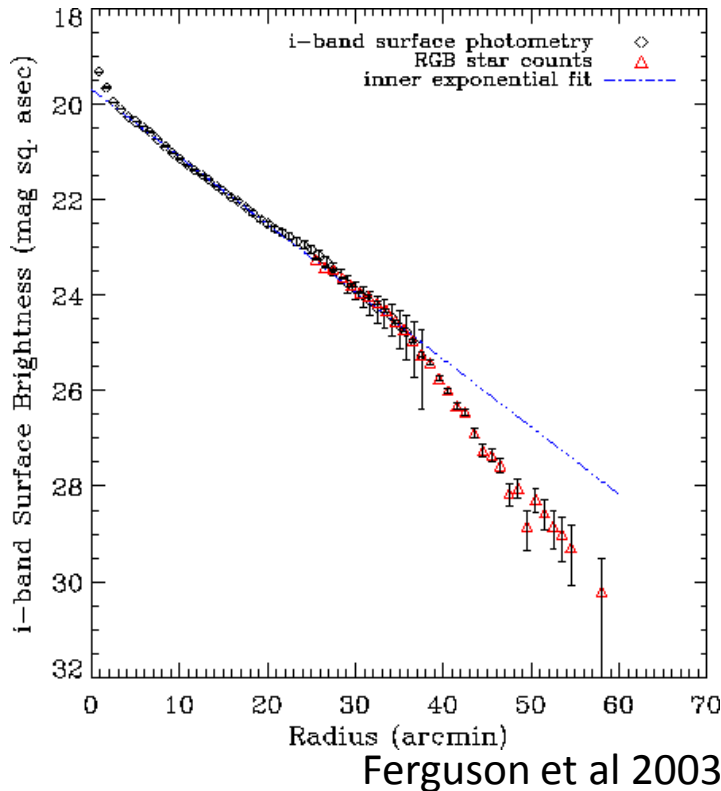
NGC 300 exponential disk
for at least 10 scale-lengths



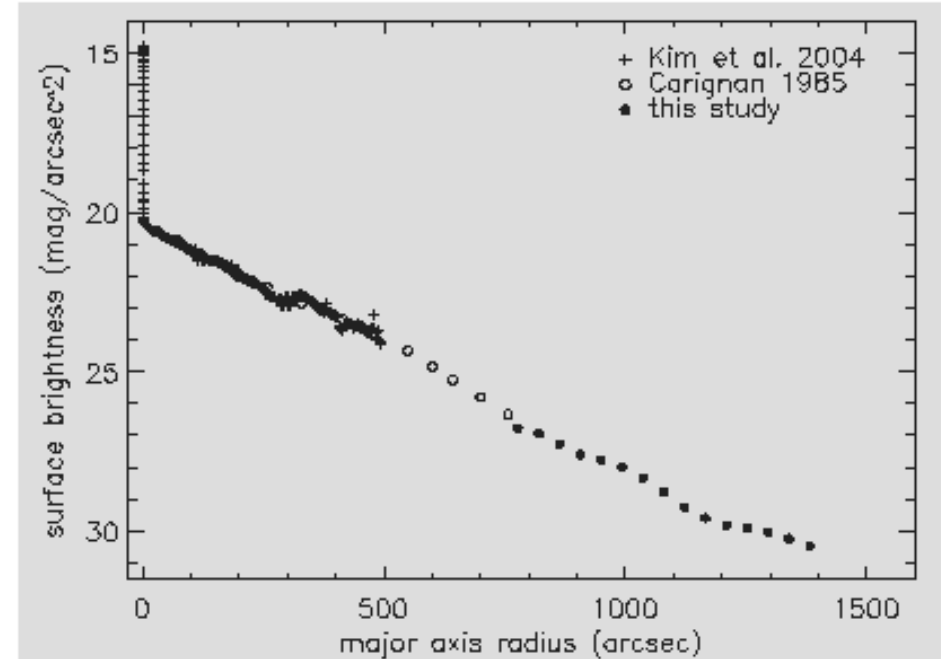
Spiral Galaxy NGC 300
(MPG/ESO 2.2-m + WFI)
ESO PR Photo 18a/02 (7 August 2002) © European Southern Observatory

$$I(r) = I_0 e^{-r/R_D}$$

R_D length scale of the disk



Freeman, 1970



Bland-Hawthorn et al 2005

Gas surface densities

HI

Flattish radial distribution

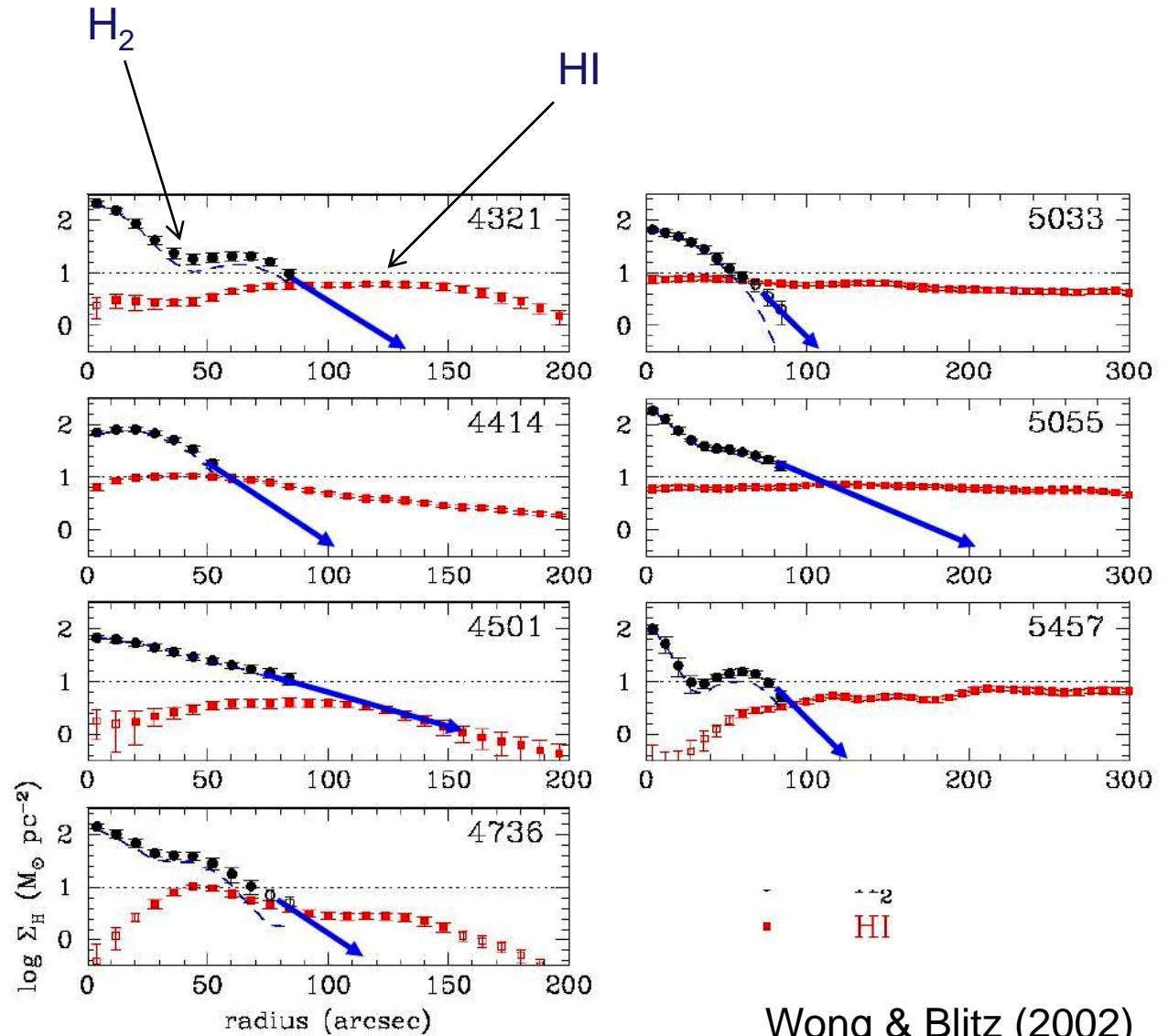
Deficiency in the centre

Extended to $(8 - 40) R_D$

H₂

Follows the stellar disk

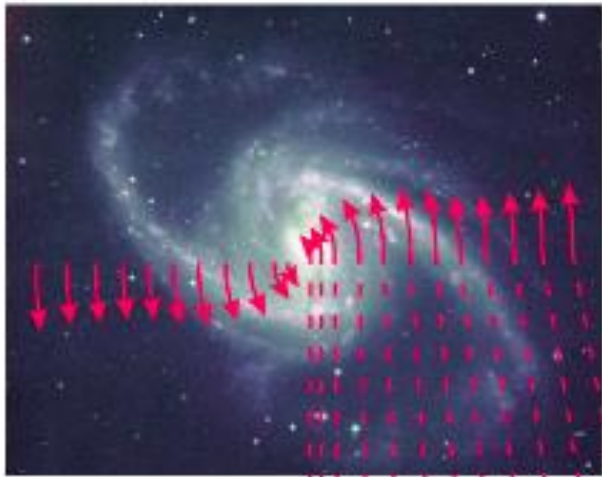
Negligible



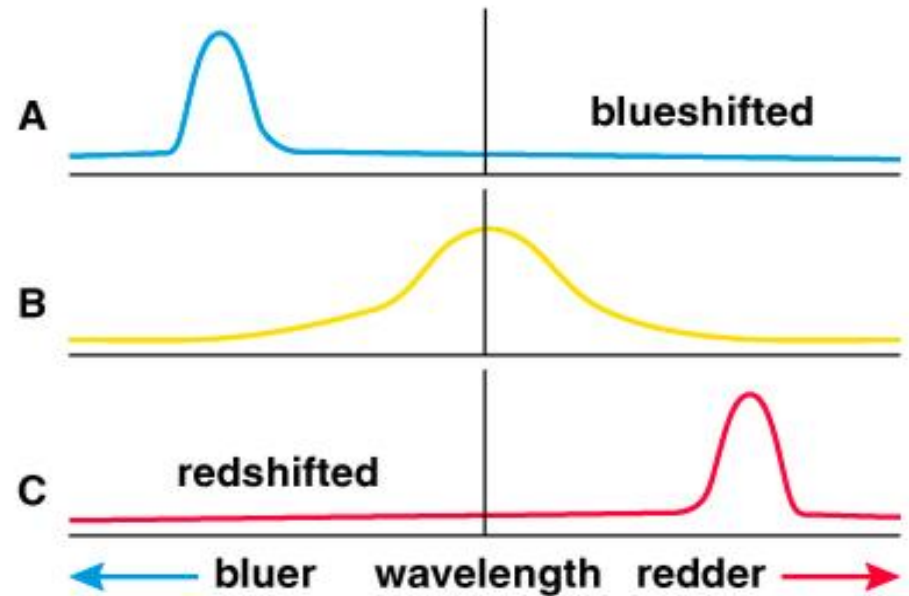
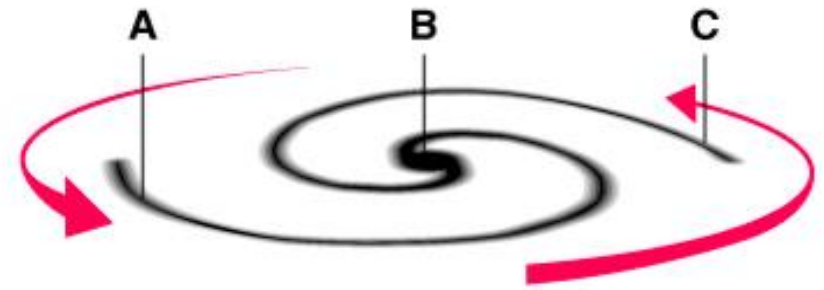
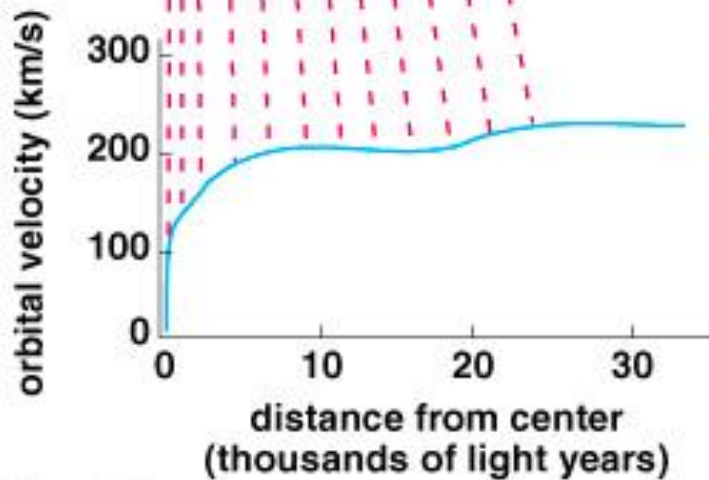
Wong & Blitz (2002)

ROTATION CURVES

artist impression



Longer arrows represent larger orbital velocities.



Copyright © Addison Wesley.

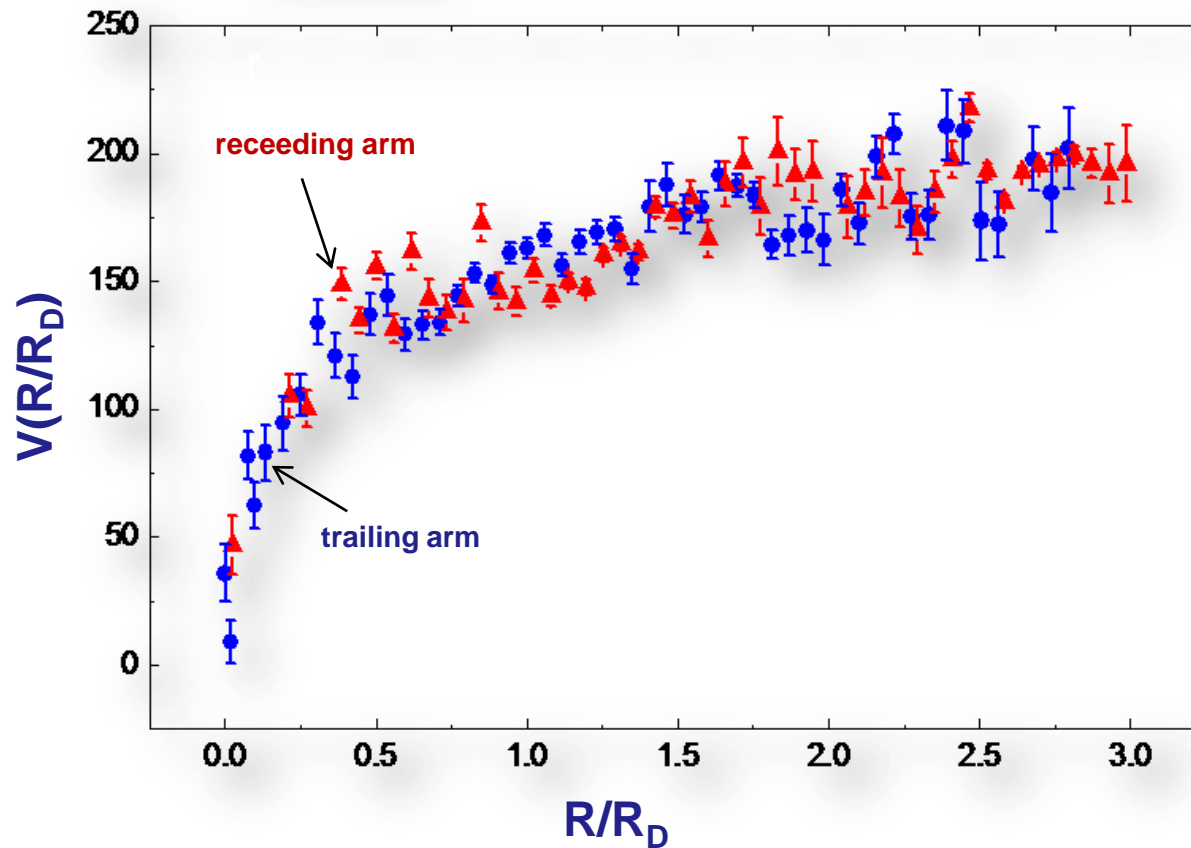
Copyright © Addison Wesley.

artist impression

Symmetric circular rotation of a disk characterized by

- Sky coordinates of the galaxy centre
- Systemic velocity V_{sys}
- Circular velocity $V(R)$
- Inclination angle

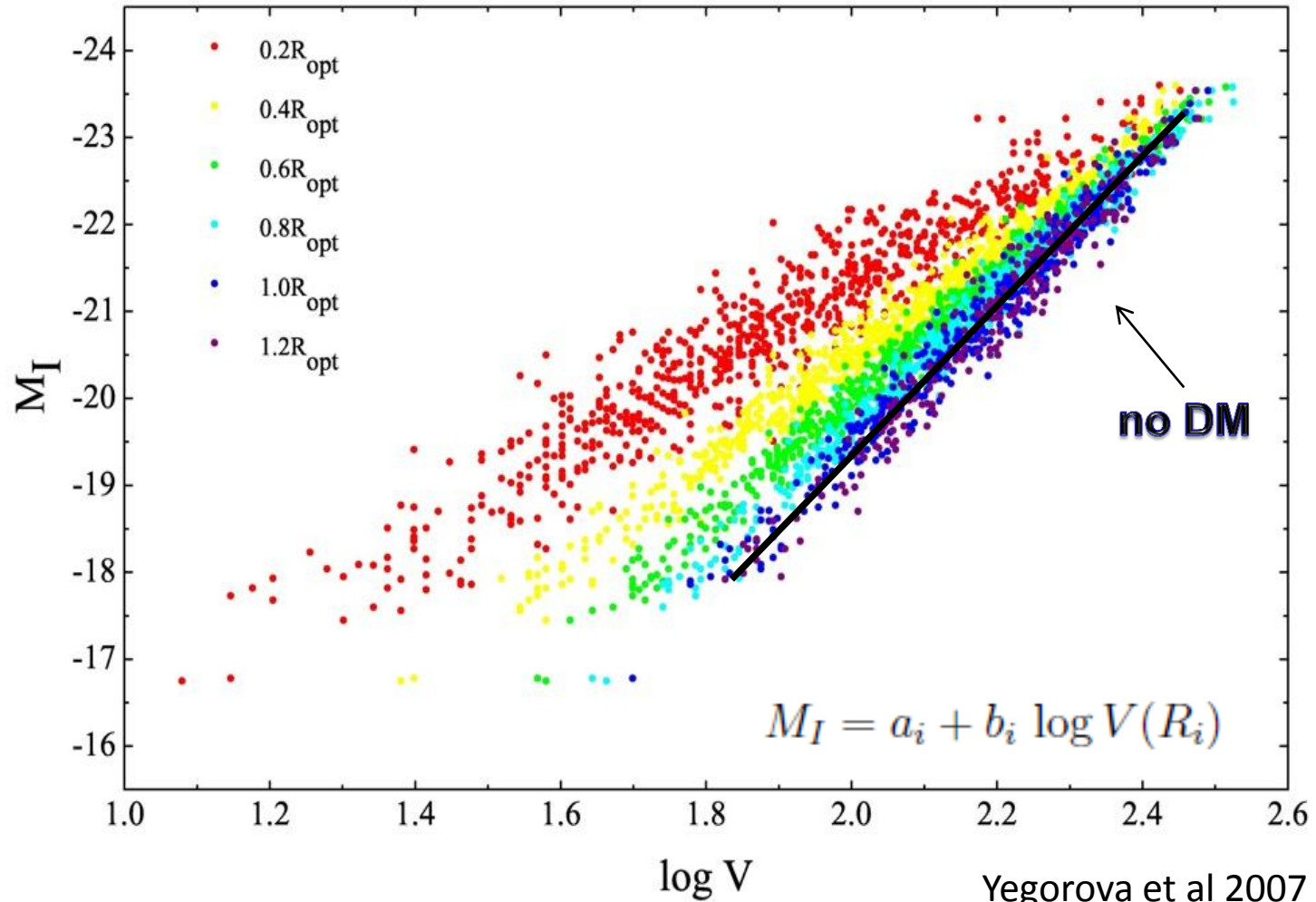
UGC2405 HIGH QUALITY ROTATION CURVE



Evidence for a Mass Discrepancy in Galaxies

The distribution of gravitating matter, unlike the luminous one, is luminosity dependent.

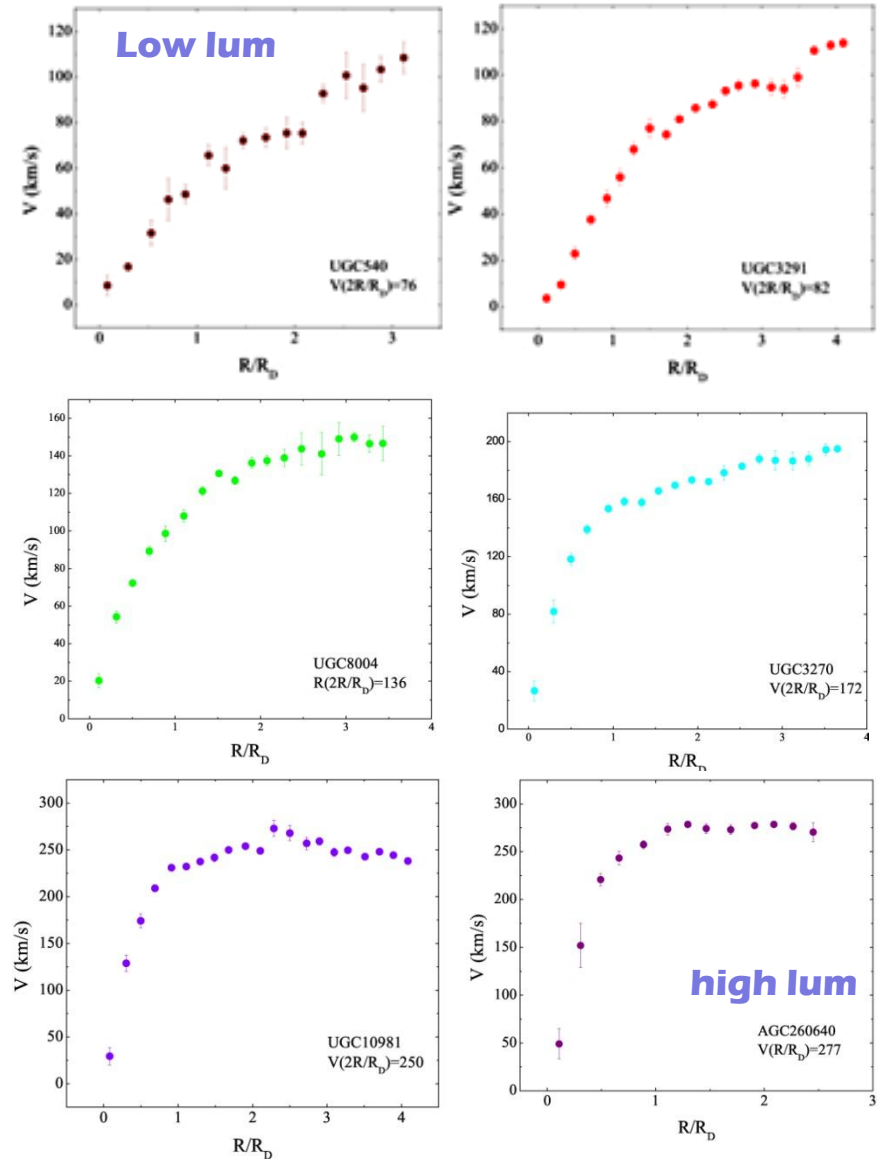
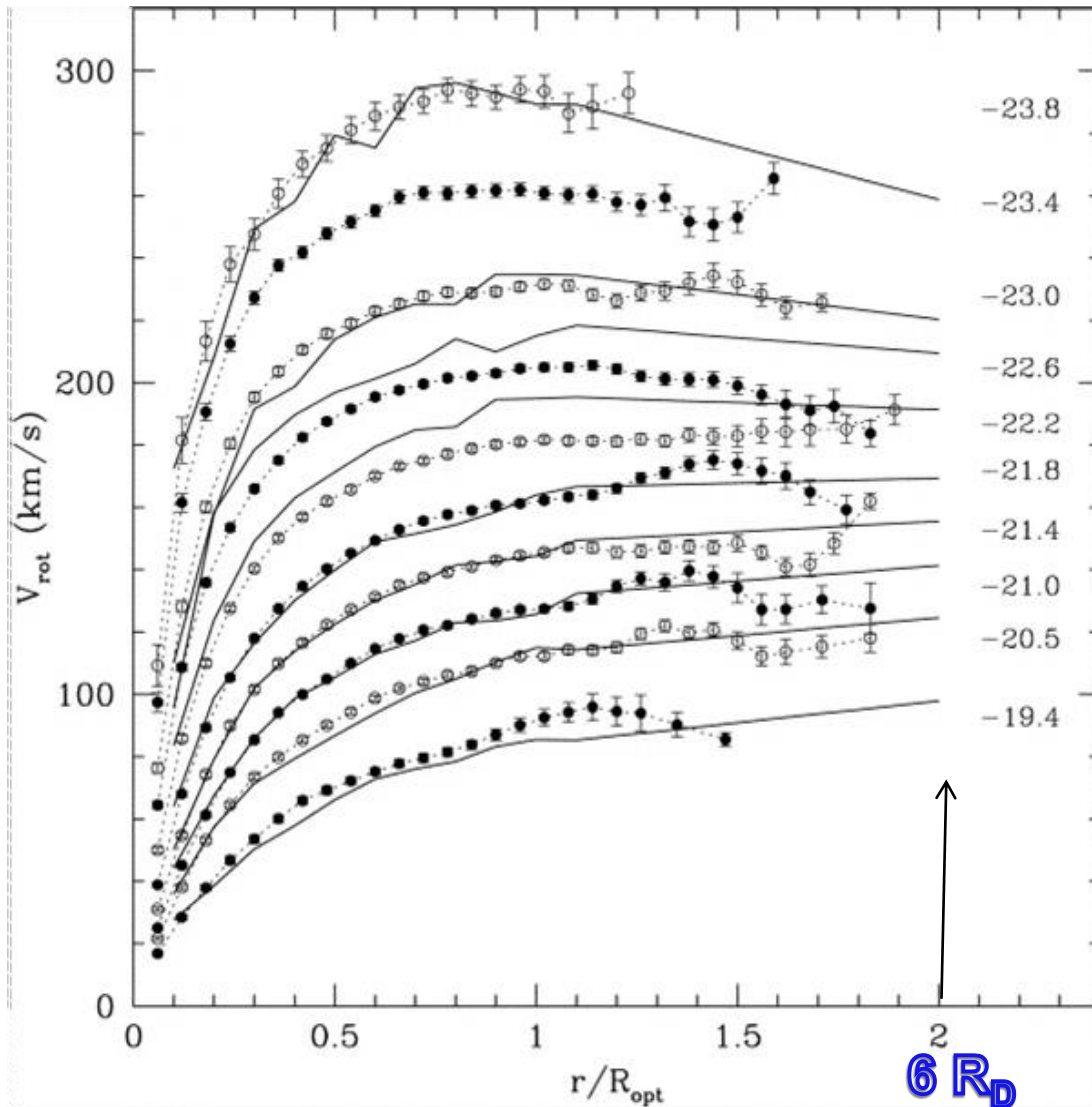
Tully-Fisher relation exists at local level (radii R_i)



Rotation Curves

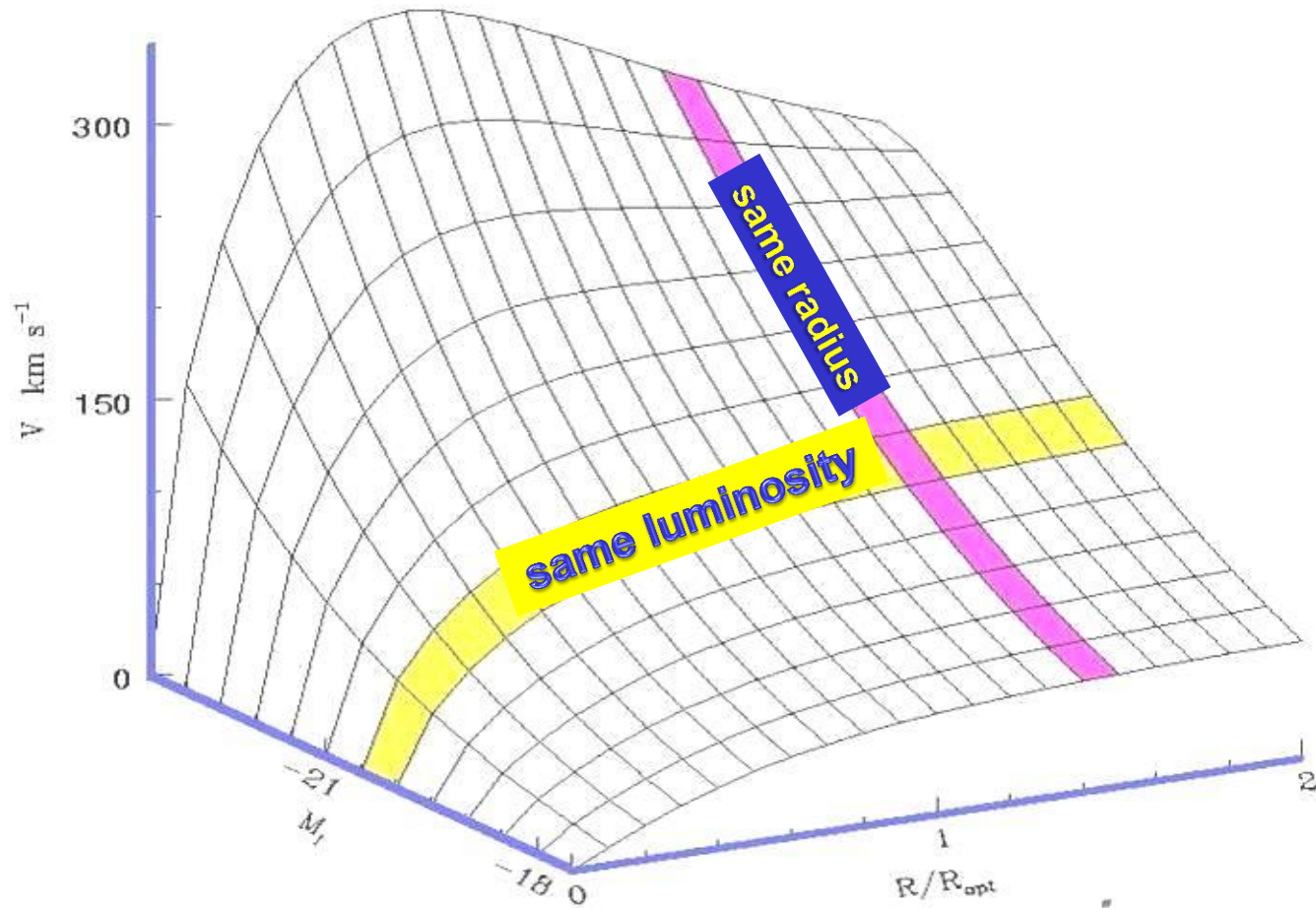
TYPICAL INDIVIDUAL RCs SHOWN BY INCREASING LUMINOSITY

Coadded from 3200 individual RCs



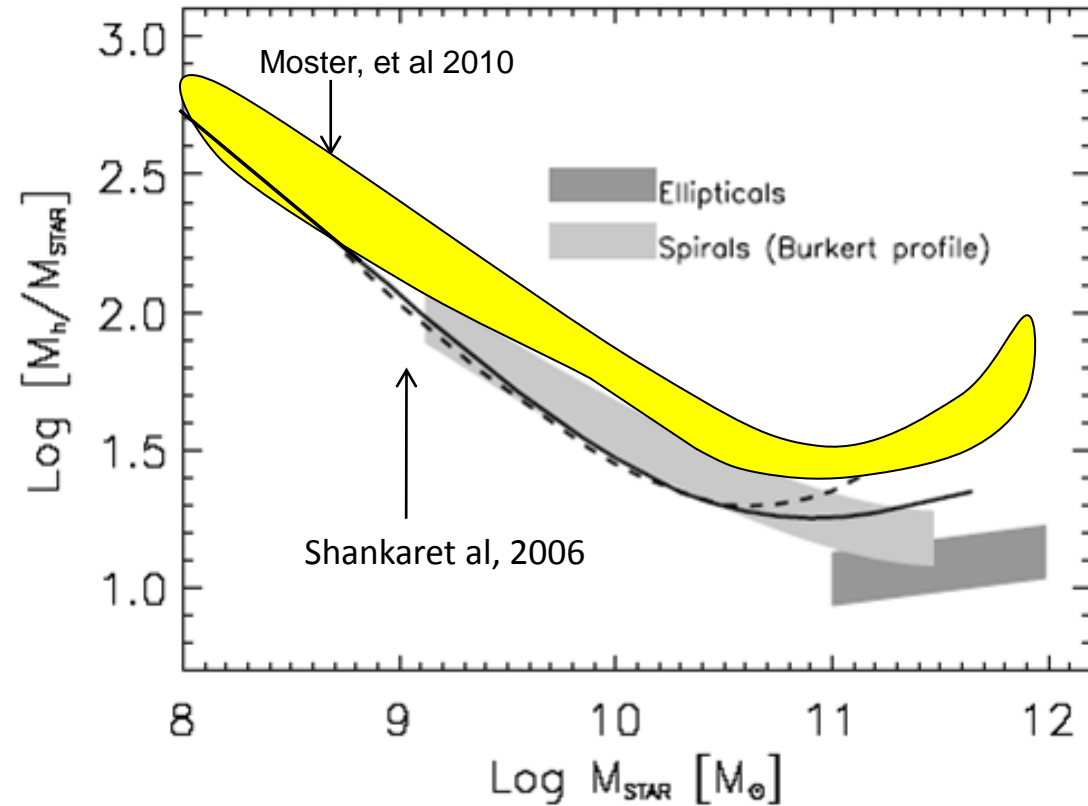
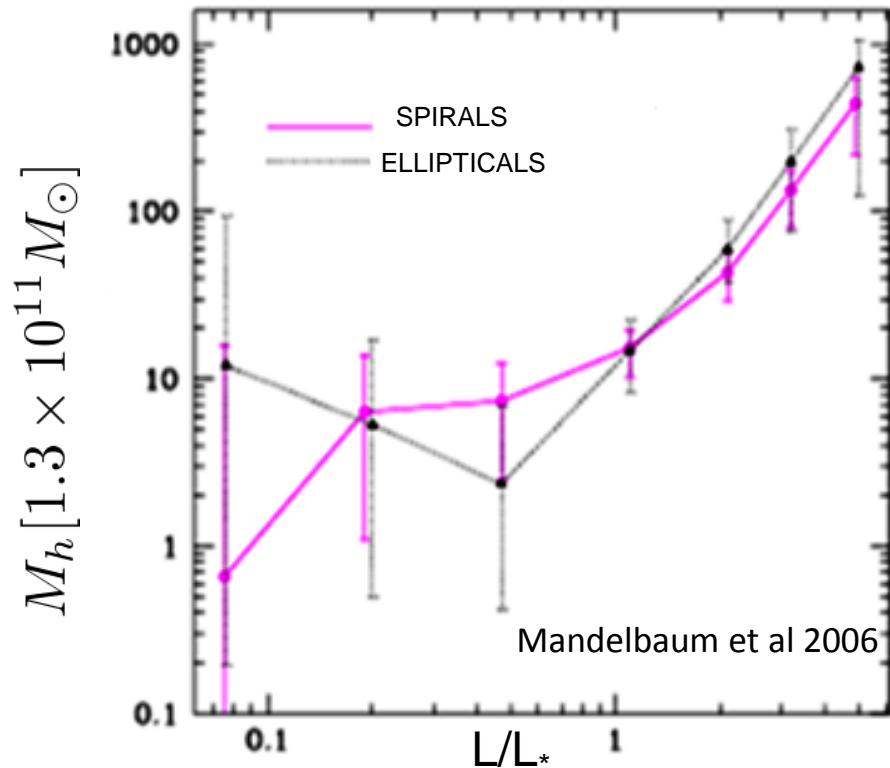
The Cosmic Variance of V measured in galaxies of **same** luminosity L at the **same** radius $x=R/R_D$ is negligible compared to the variations that V shows as x and L varies.

The Universal Rotation Curve



Universal Rotation Curve out to the Virial Radius

Method: inner kinematics + independent determinations of halo virial masses

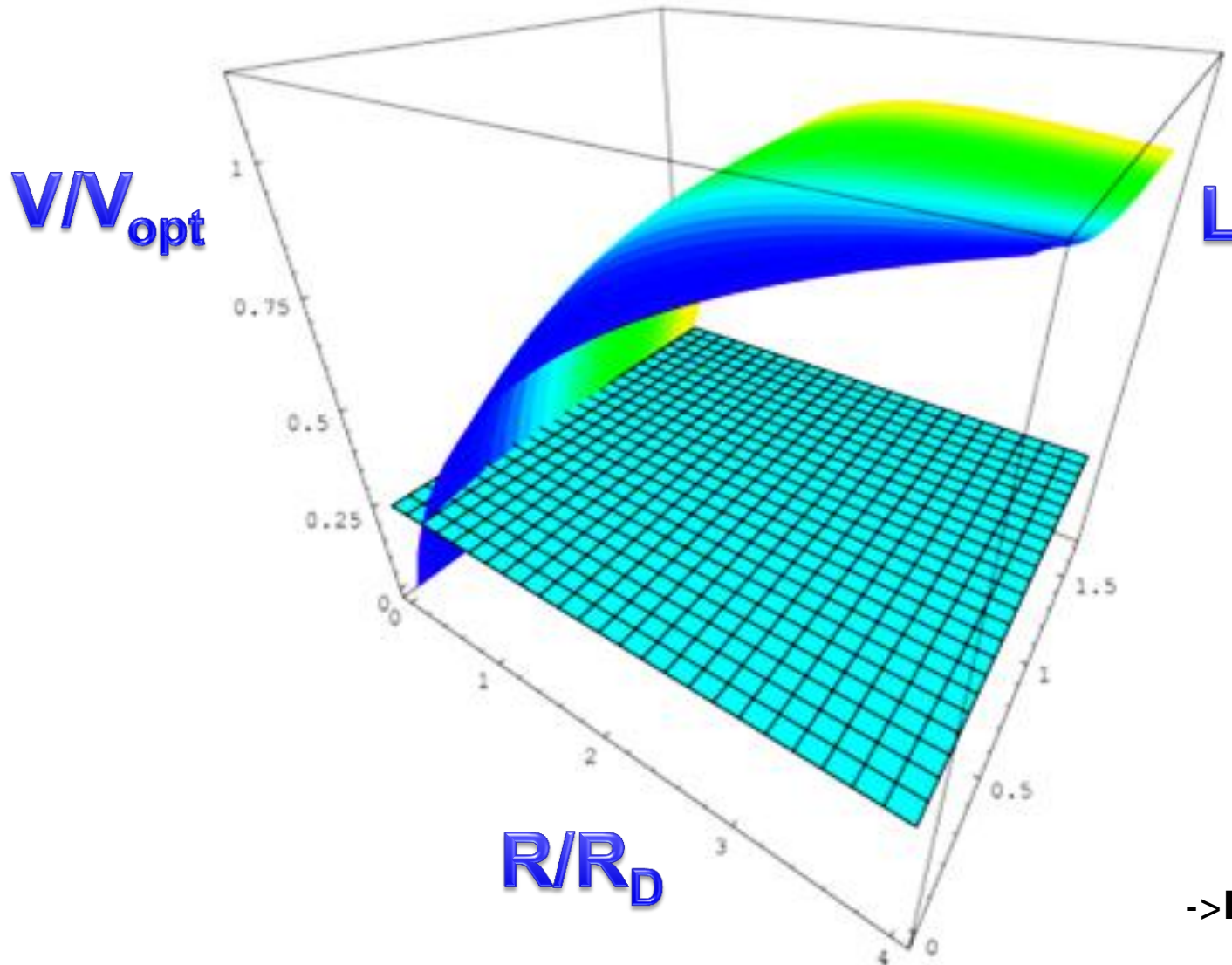


Virial masses M_h of halos around galaxies with stellar mass M_{STAR} (or luminosity L) are obtained

- **directly** by weak-lensing analysis (*left*)
- **indirectly** by correlating dN/dL with theoretical DM halo dN/dM (*right*)

The Concept of the Universal Rotation Curve (URC)

Every RC can be represented by: $V(x,L)$ $x=R/R_D$



->Link to Movie 2

The URC out to $6 R_D$ is derived directly from observations
Extrapolation of URC out to virial radius by using $V(R_{vir})$

Rotation curve analysis

From data to mass models

$$V^2(R) = V_{halo}^2(R) + V_{HI}^2(R) + V_{disk}^2(R)$$

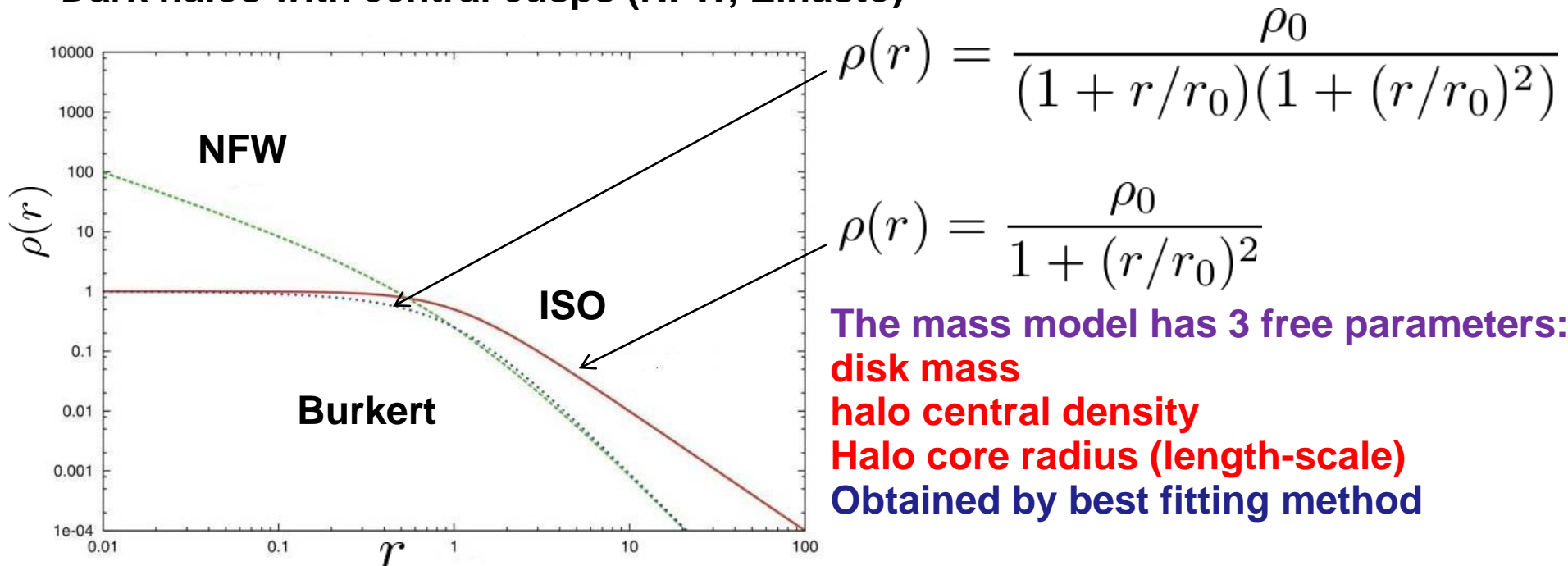
observations =

model

- V_{disk}^2 from I-band photometry
- V_{HI}^2 from HI observations
- V_{halo}^2 different choices for the DM halo density

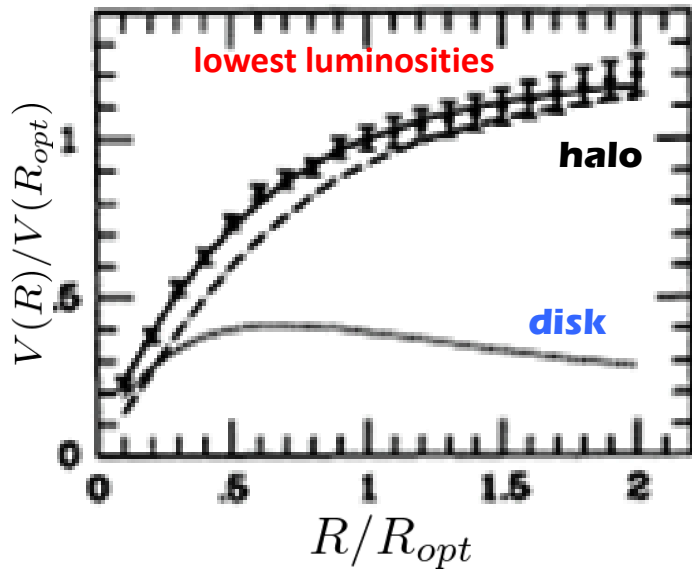
Dark halos with central constant density (Burkert, Isothermal)

Dark halos with central cusps (NFW, Einasto)

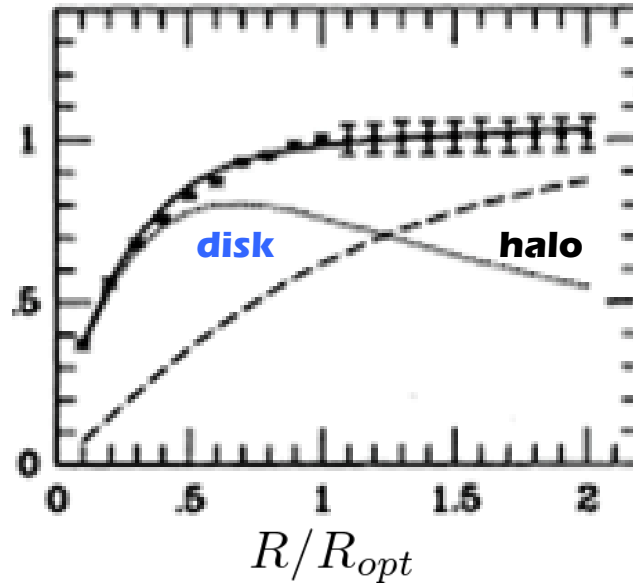


MASS MODELLING RESULTS

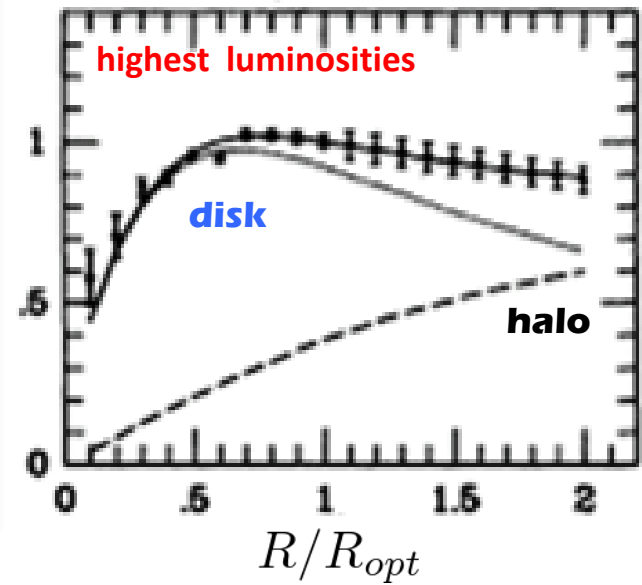
$M_i = -18$



$M_i = -21$

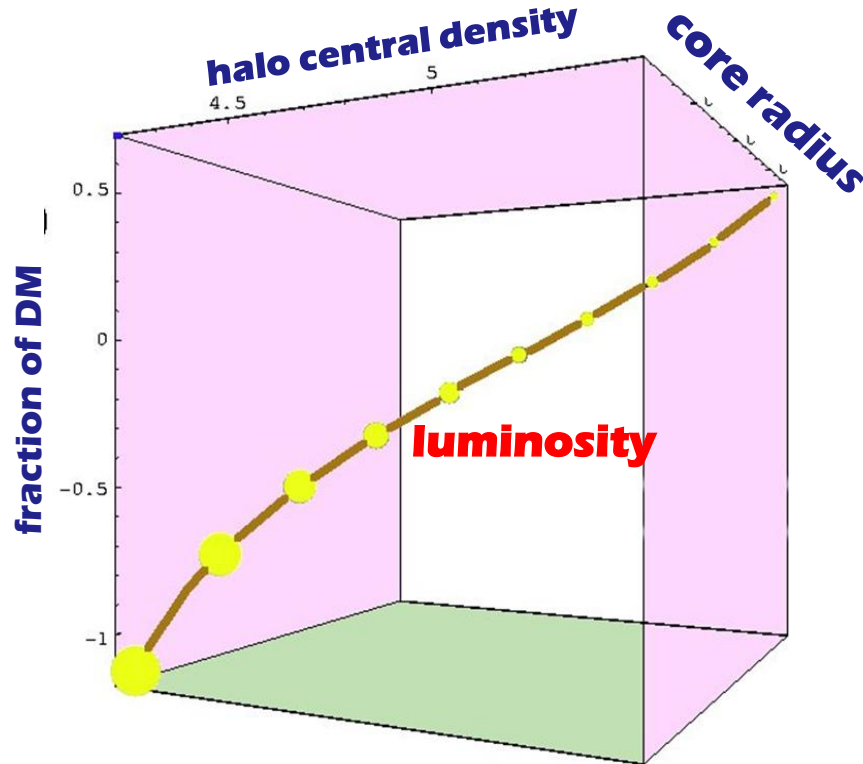


$M_i = -23$



All structural DM and LM parameters are related with luminosity.

Smaller galaxies are denser and have a higher proportion of dark matter.

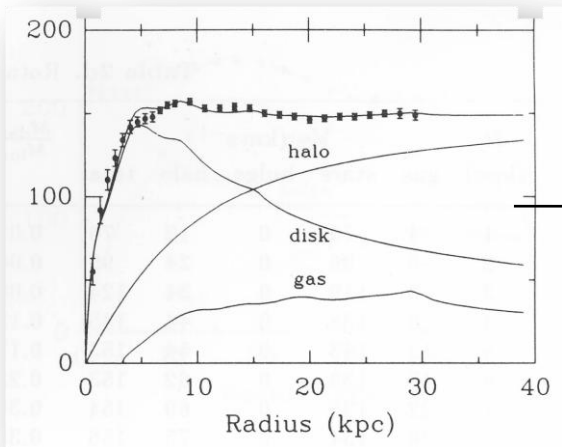


MASS MODELLING INDIVIDUAL OBJECTS

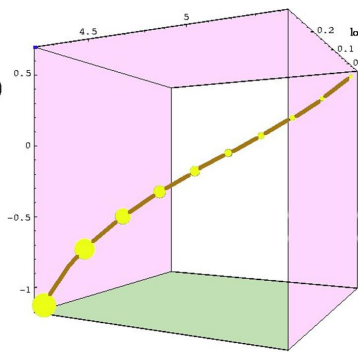
Dark Halo Scaling Laws in Spirals

Careful derivation of halo structural parameters (ρ_0, r_0)

- Assumption: Maximum Disk
- the slope of the halo contribution gives the halo central density
- extended RC provides the estimate of halo core radius r_0



URC

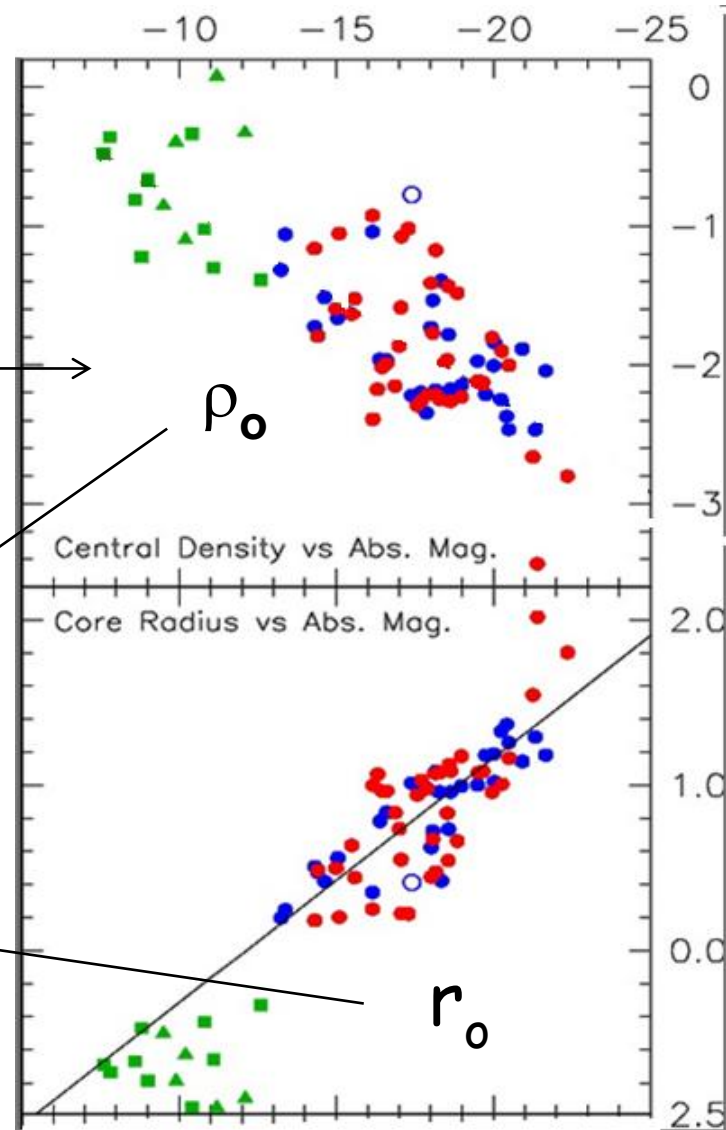


$$\rho_0 \sim L_I^{-0.7}$$

$$r_0 \sim L_I^{0.7}$$

$$\rho_0 \sim L_B^{-0.6}$$

$$r_0 \sim L_B^{0.6}$$



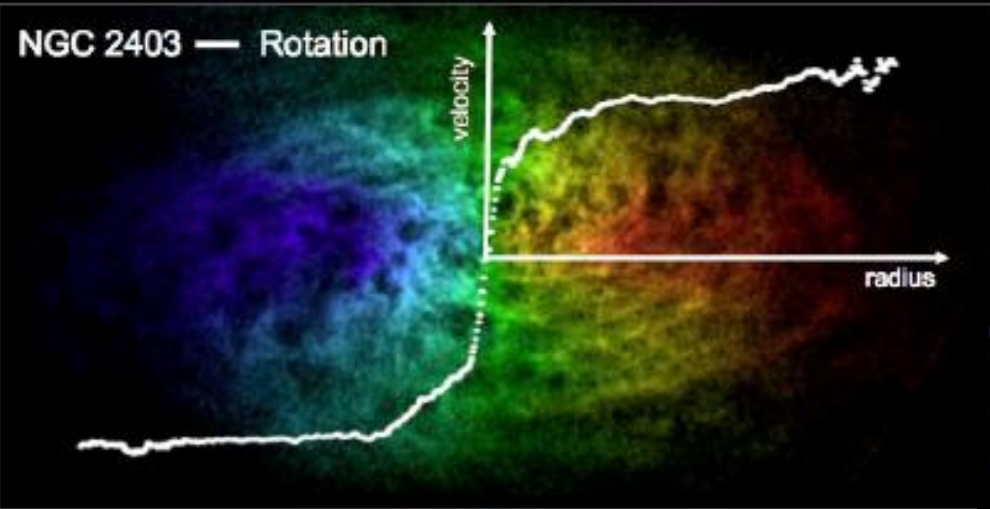
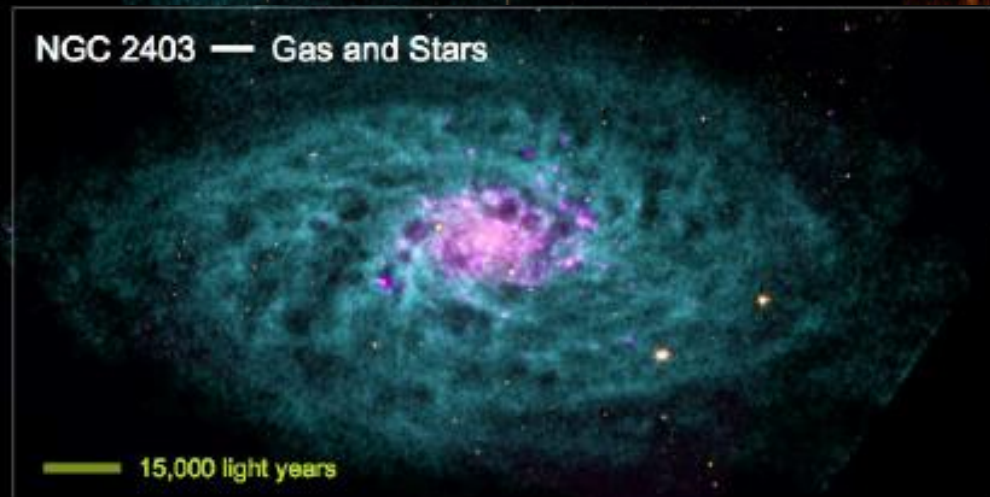
Kormendy & Freeman (2004)

The distribution of DM around spirals

Individual objects **Gentile+ 2004, de Blok+ 2008 Kuzio de Naray+ 2008, Oh+ 2008, Spano+ 2008, Trachternach+ 2008, Donato+,2009**

A detailed investigation: high quality data and model independent analysis

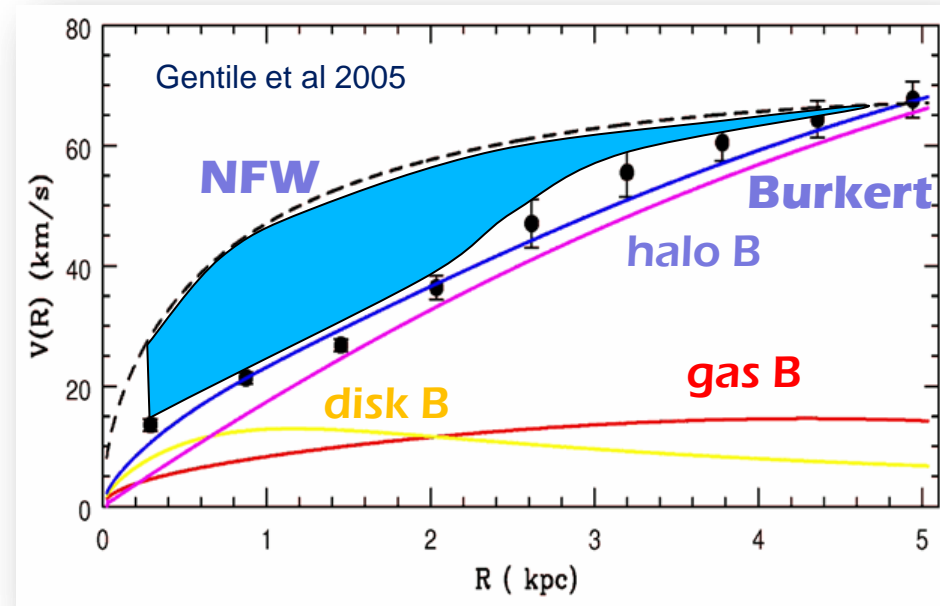
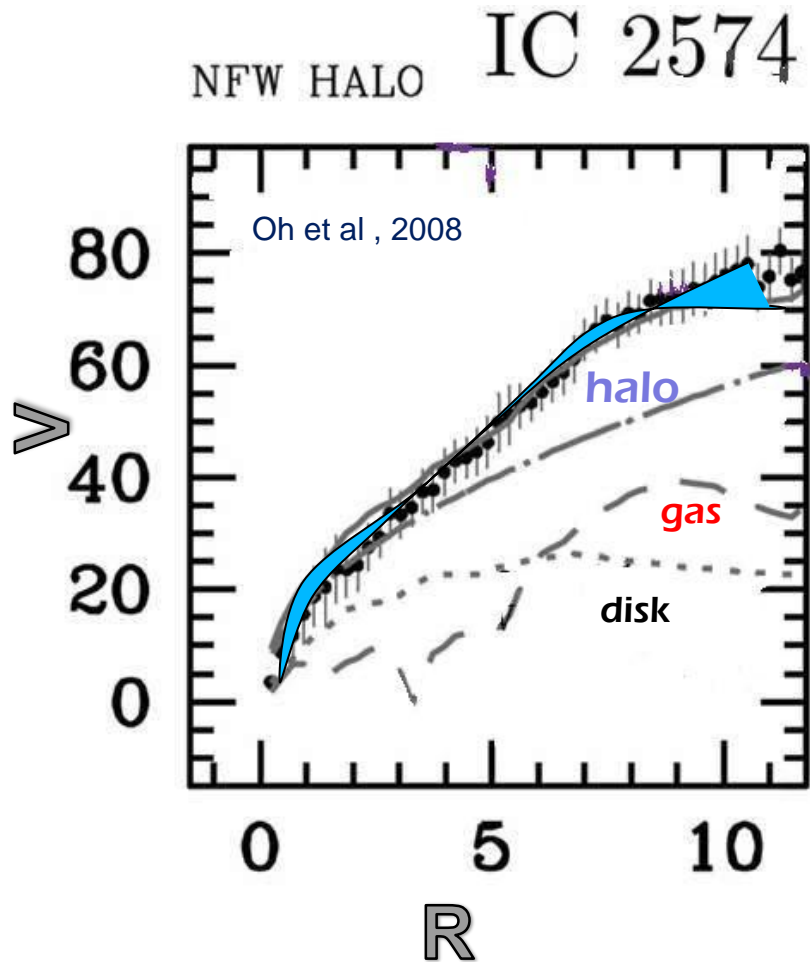
Galaxy Dynamics in THINGS — The HI Nearby Galaxy Survey



THINGS Data: Walter et al 2008
Milky Way HI mass: Gent et al 1998
Milky Way HI: NASA/IPAC Extragalactic Database

COUNTEREXAMPLES FOR NFW

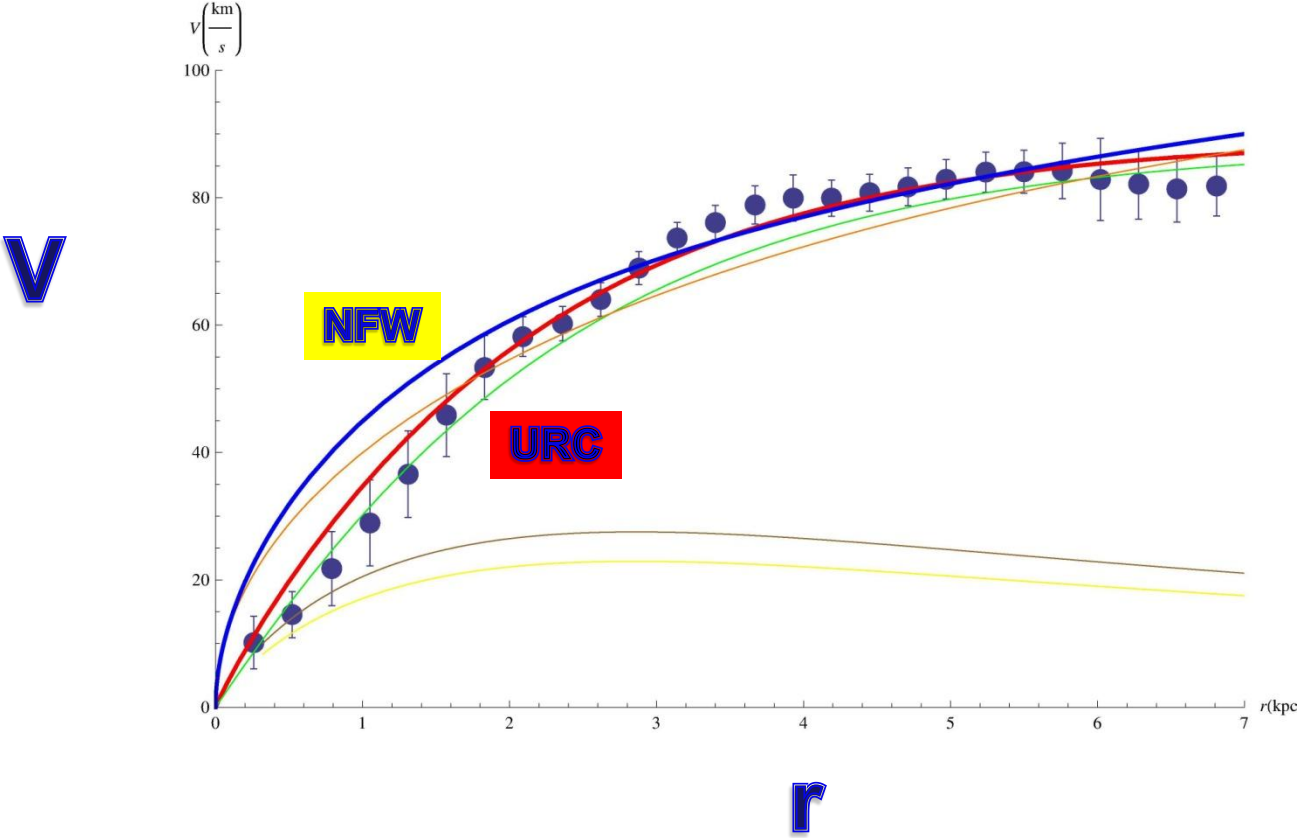
DDO 47



General results from several samples e.g. THINGS

- **Non-circular motions are small.**
- **DM halo spherical**
- **ISO/Burkert halos much more preferred over NFW**
- **Tri-axiality and non-circular motions cannot explain the CDM/NFW cusp/core discrepancy**

ORION DWARF



SPIRALS: WHAT WE KNOW

**AN UNIVERSAL CURVE REPRESENTS ALL INDIVIDUAL RCs
MORE PROPORTION OF DARK MATTER IN SMALLER SYSTEMS
THE RADIUS IN WHICH THE DM SETS IN IS A FUNCTION OF LUMINOSITY
THE MASS PROFILE AT LARGER RADII IS COMPATIBLE WITH NFW
DARK HALO DENSITY SHOWS A CENTRAL CORE OF SIZE $2 R_D$**

ELLIPTICALS



The Stellar Spheroid

Surface brightness of ellipticals follows a Sersic

$$I(R) = I_e \operatorname{dex}\left[-b_n \left(\frac{R}{R_e}\right)^{1/n} - 1\right]$$

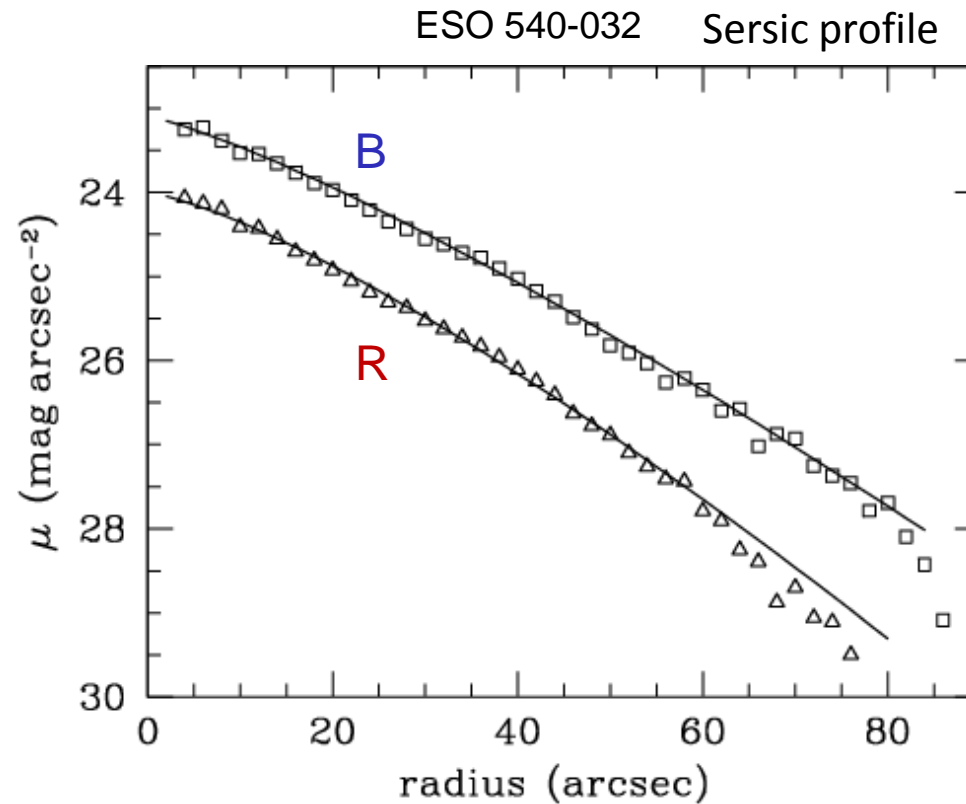
R_e the radius enclosing half of the projected light.

$$b_n = 0.868 n - 0.142$$

By deprojecting $I(R)$ we obtain the luminosity density $j(r)$:

$$I(R) = \int_{-\infty}^{+\infty} j(r) dz = 2 \int_R^{+\infty} \frac{j(r) r dr}{\sqrt{r^2 - R^2}}$$

$$\rho_{sph}(r) = (M/L)_\star j(r)$$



Modelling Ellipticals

Measure the light profile = stellar mass profile $(M_*/L)^{-1}$

Derive the total mass profile $M(r)$

Dispersion velocities of stars or of Planetary Nebulae

X-ray properties of the emitting hot gas

Weak and/or strong lensing data

Disentangle $M(r)$ into its dark and the stellar components

In ellipticals gravity is balanced by pressure gradients -> Jeans Equation

$$\frac{d}{dr}(j\sigma_r^2) + \frac{2\beta}{r}j\sigma_r^2 = -j\frac{d\Phi}{dr}$$

Diagram illustrating the Jeans Equation for elliptical galaxies:

- The term $\frac{d}{dr}(j\sigma_r^2)$ is associated with **anisotropy of the orbits**.
- The term $\frac{2\beta}{r}j\sigma_r^2$ is associated with **dispersion velocities**.
- The right-hand side term $-j\frac{d\Phi}{dr}$ is associated with **grav. potential**.

Kinematics of ellipticals: **Isotropic** Jeans modelling of velocity dispersions

$$M(r) = M_{sph}(r) + M_h(r).$$

$$\sigma_r^2(r) = \frac{G}{\rho_{sph}(r)} \int_r^\infty \frac{\rho_{sph}(r') M(r')}{r'^2} dr' \quad \text{radial not observable}$$

$$\sigma_P^2(R) = \frac{2}{I(R)} \int_R^\infty \frac{\rho_{sph}(r) \sigma_r^2(r) r}{\sqrt{r^2 - R^2}} dr \quad \text{projected}$$

$$\sigma_A^2(R_A) = \frac{2\pi}{L(R_A)} \int_0^{R_A} \sigma_P^2(R) I(R) R dR \quad \text{aperture}$$

$$L(R) = 2\pi \int I(R) R dR$$

measure $I(R)$, $\sigma_P(R)$
 derive $M_h(r)$, $M_{sph}(r)$

Anisotropic Jeans equations

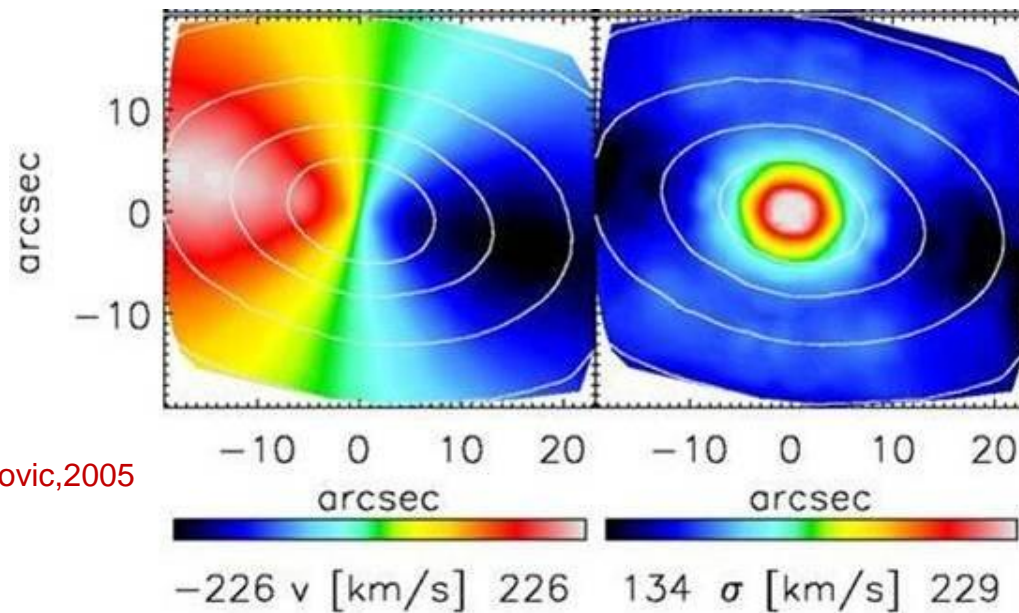
~~$$\frac{\partial(\nu \overline{v_R^2})}{\partial R} + \frac{\partial(\nu \overline{v_R v_z})}{\partial z} + \nu \left(\frac{\overline{v_R^2} - \overline{v_\phi^2}}{R} + \frac{\partial \Phi}{\partial R} \right) = 0,$$~~

~~$$\frac{\partial(\nu \overline{v_R v_z})}{\partial R} + \frac{\partial(\nu \overline{v_z^2})}{\partial z} + \frac{\nu \overline{v_z^2}}{R} + \nu \frac{\partial \Phi}{\partial z} = 0.$$~~

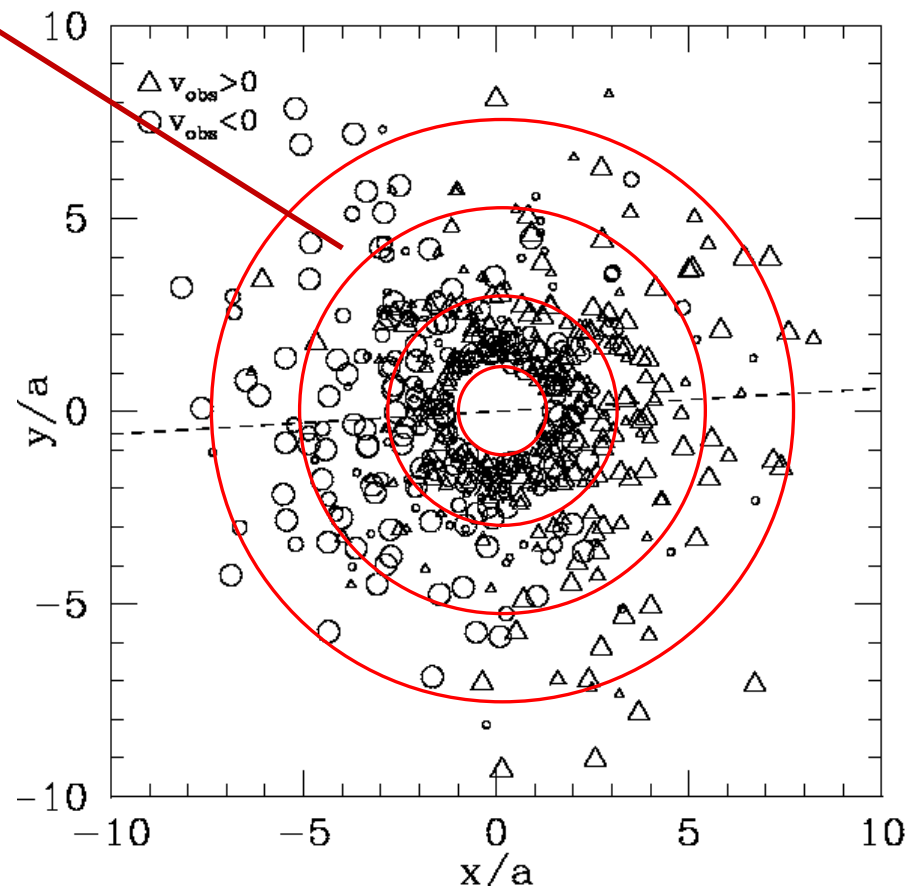
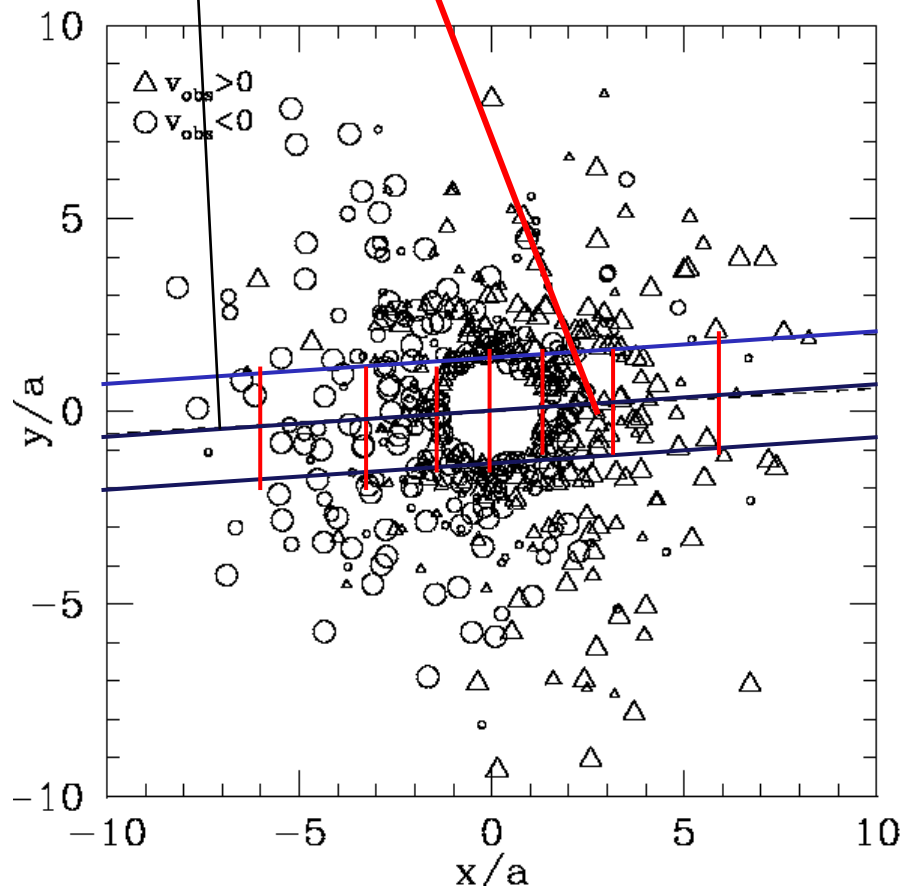
Cappellari, 2008

Krajnovic, 2005

V SAURON data of N 2974 σ_P

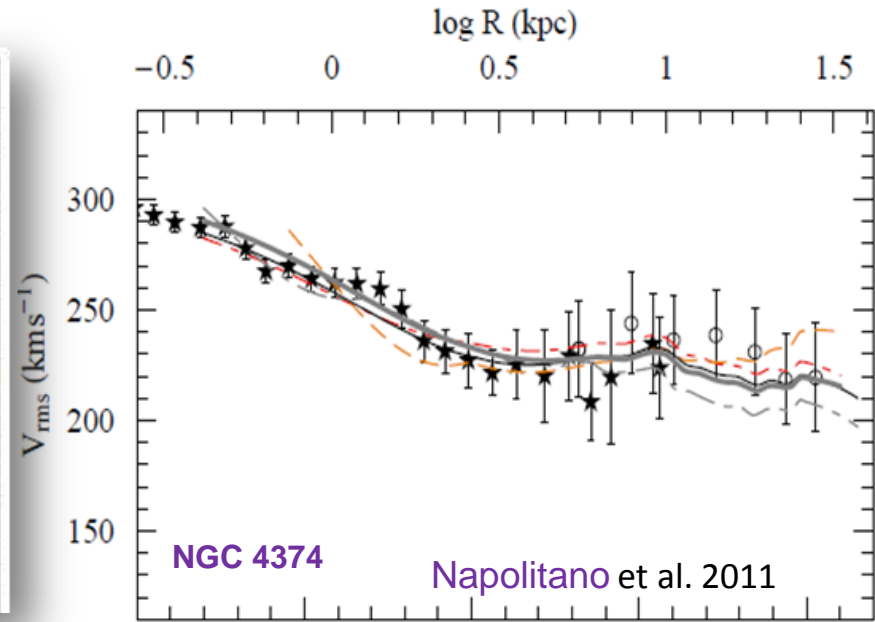
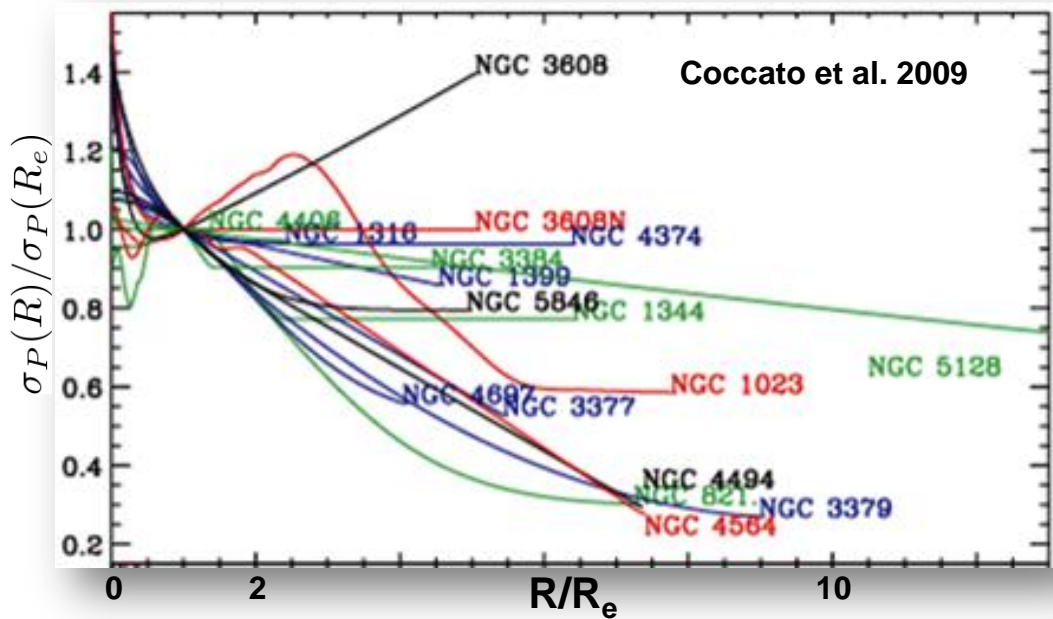


PN : Major/minor axis or radial binning of the data



PN data

Jeans modelling of PN data with a stellar spheroid + NFW dark halo



Velocity dispersion are flat or strongly decreasing outside $\sim 2R_e$

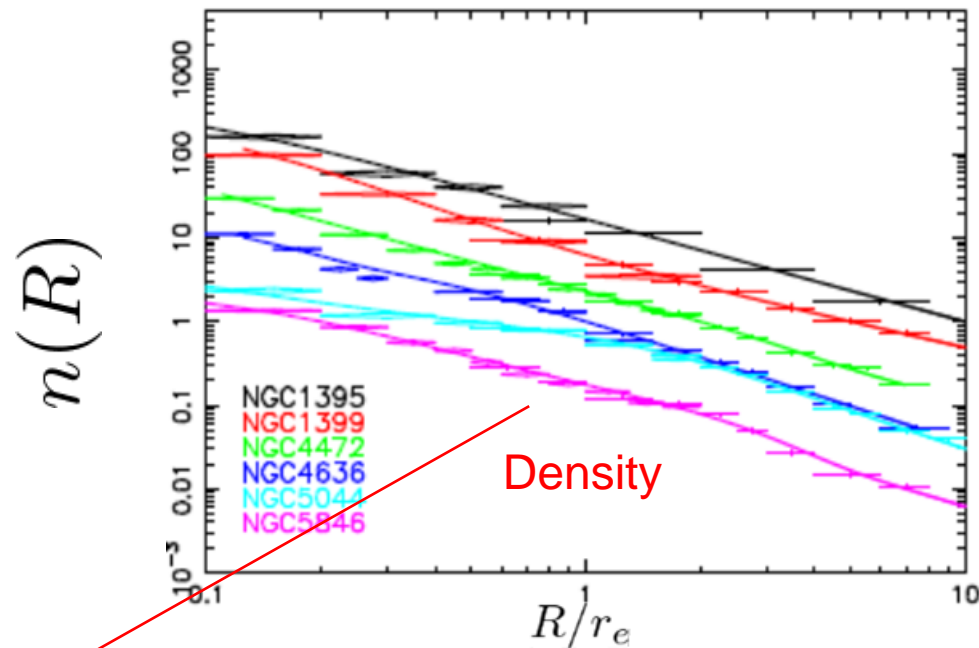
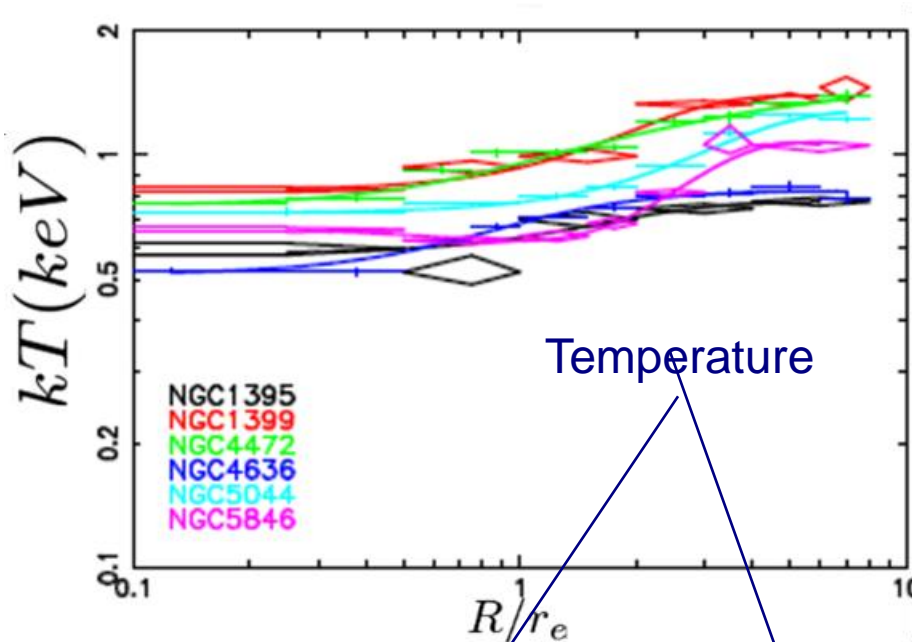
$$M(r) = -\frac{\sigma_r^2 r}{G} \left(\frac{d \ln j_*}{d \ln r} + \frac{d \ln \sigma_r^2}{d \ln r} + 2\beta \right)$$

JEANS ANALYSIS

There exist big DM halos around Ellipticals,
Cored and cuspy DM profiles are both possible.

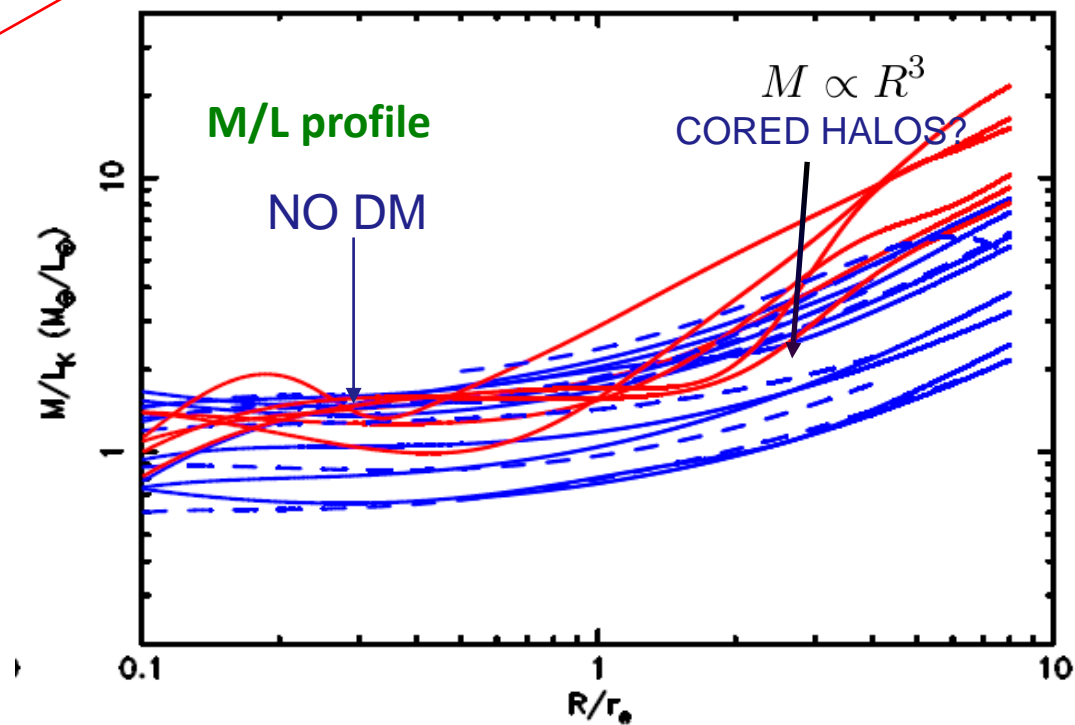
Mass Profiles from X-ray

Nigishita et al 2009



$$M(R) = -\frac{kT(R) \cdot R}{G\mu m_p} \left(\frac{d \ln n(R)}{d \ln R} + \frac{d \ln T(R)}{d \ln R} \right)$$

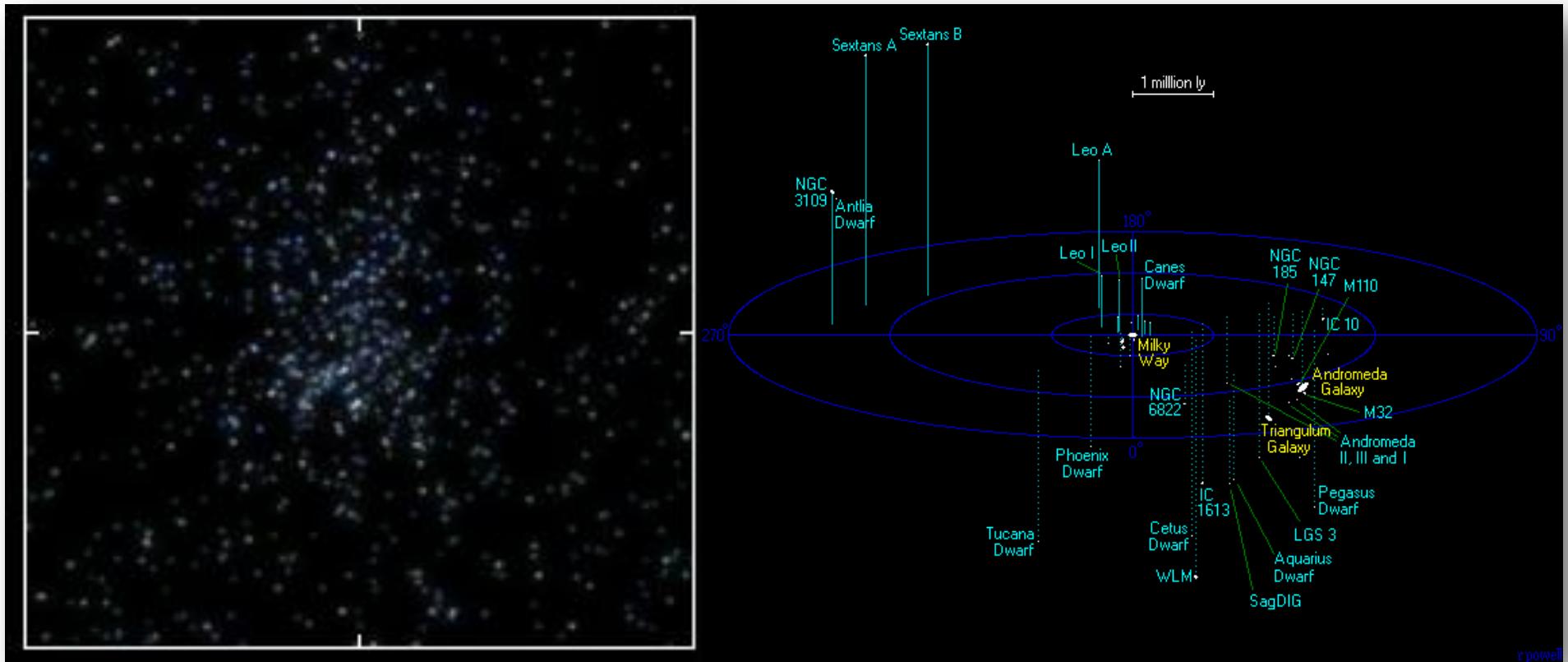
Hydrostatic Equilibrium



ELLIPTICALS: WHAT WE KNOW

A LINK AMONG THE STRUCTURAL PROPERTIES OF STELLAR SPHEROID
SMALL AMOUNT OF DM INSIDE R_E
MASS PROFILE COMPATIBLE WITH NFW AND BURKERT
DARK MATTER DIRECTLY TRACED OUT TO R_{VIR}

dSphs



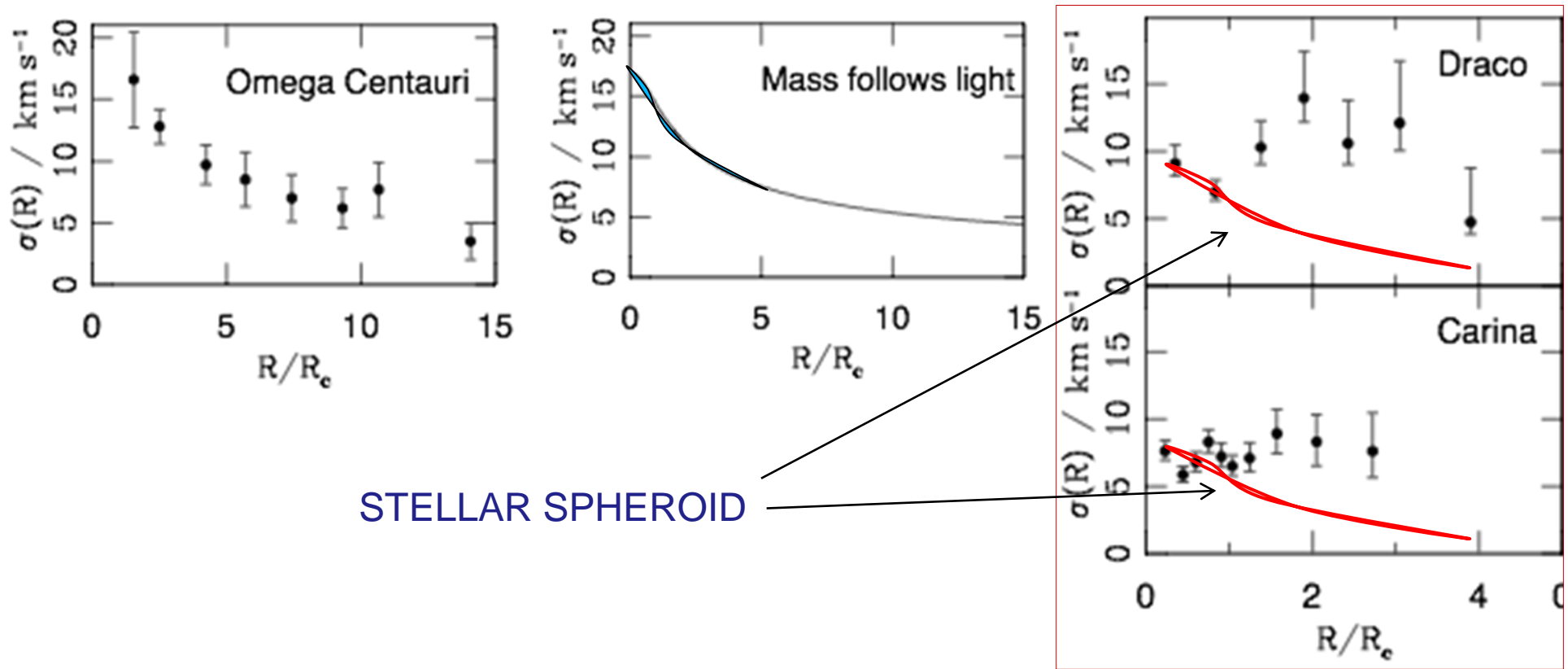
Kinematics of dSph

1983: Aaronson measured velocity dispersion of Draco based on observations of 3 carbon stars - $M/L \sim 30$

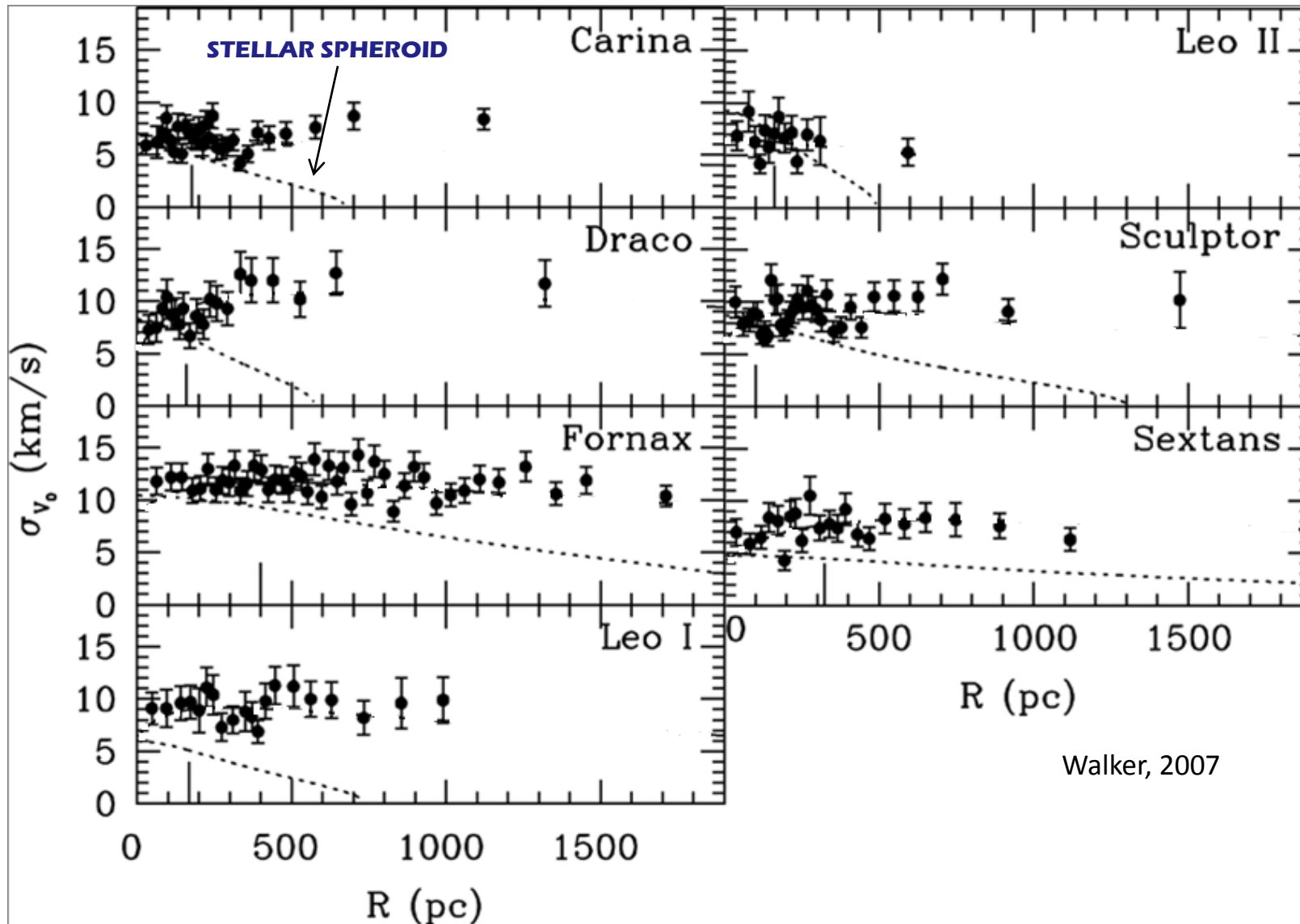
1997: First dispersion velocity profile of Fornax (Mateo)

2000+: Dispersion profiles of all dSphs measured using multi-object spectrographs

2010: full radial coverage in each dSph, with 1000 stars per galaxy



Dispersion velocity profiles



dSph dispersion profiles generally remain flat to large radii
Huge model-independent evidence of mass-to-light discrepancy

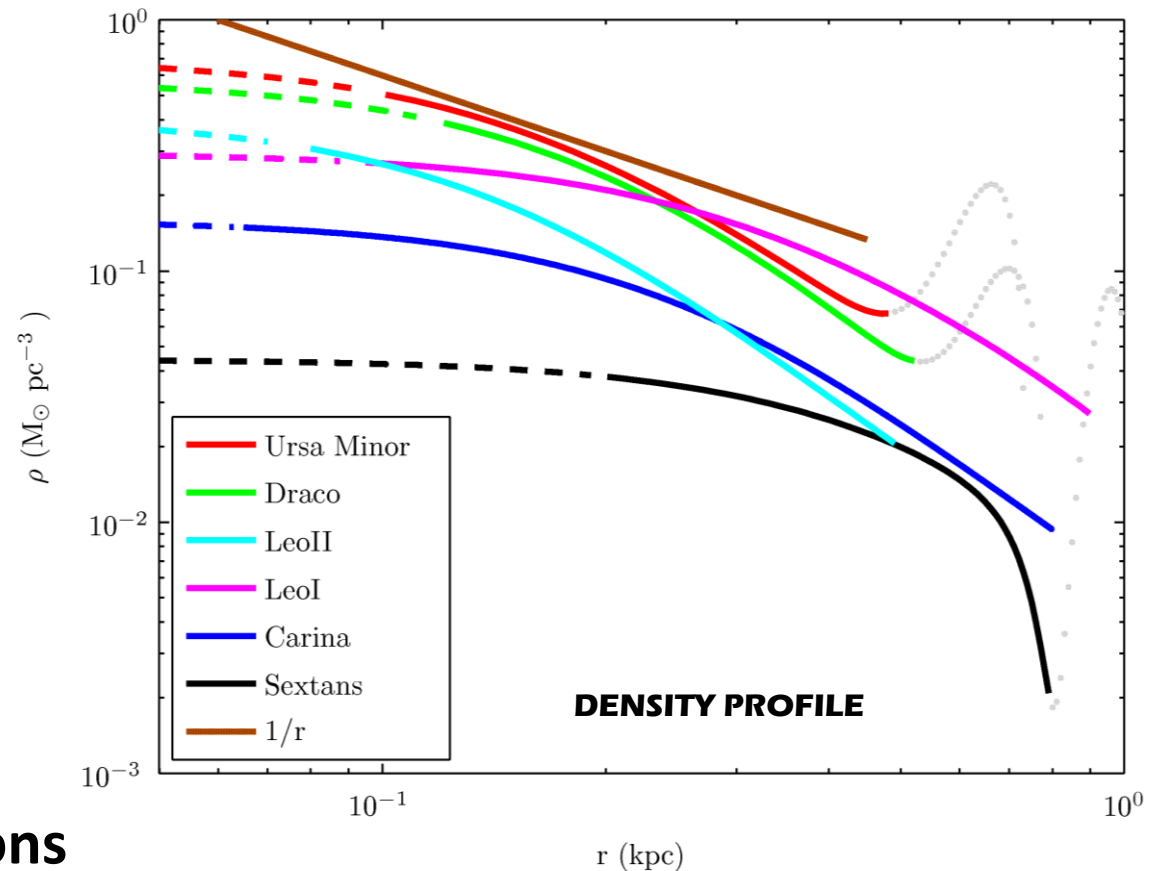
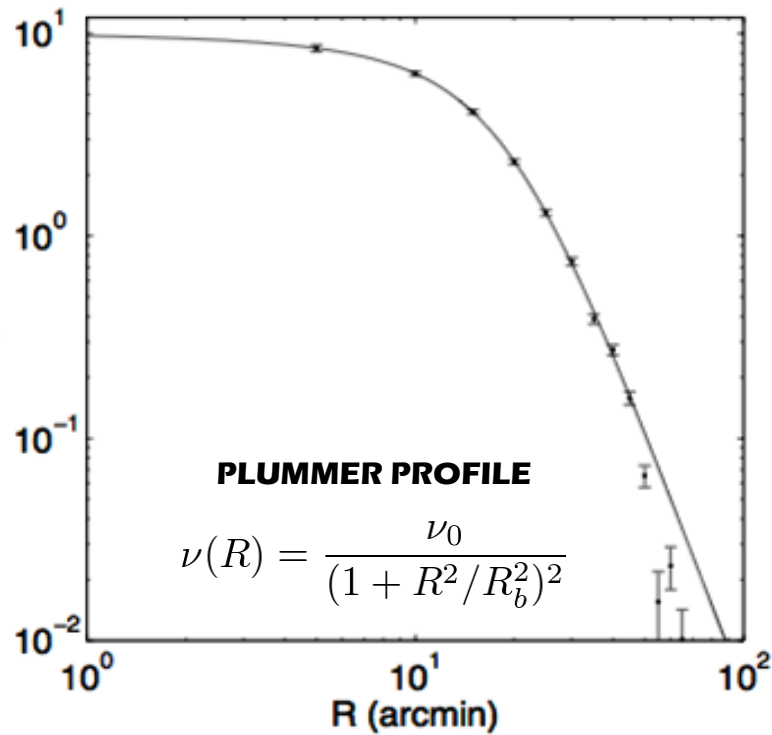
Mass profiles of dSphs

$$M(r) = -\frac{r^2}{G} \left(\frac{1}{\nu} \frac{d\nu\sigma_r^2}{dr} + 2 \frac{\beta\sigma_r^2}{r} \right)$$

Jeans' models provide the most objective sample comparison

Jeans equation relates kinematics, light and underlying mass distribution

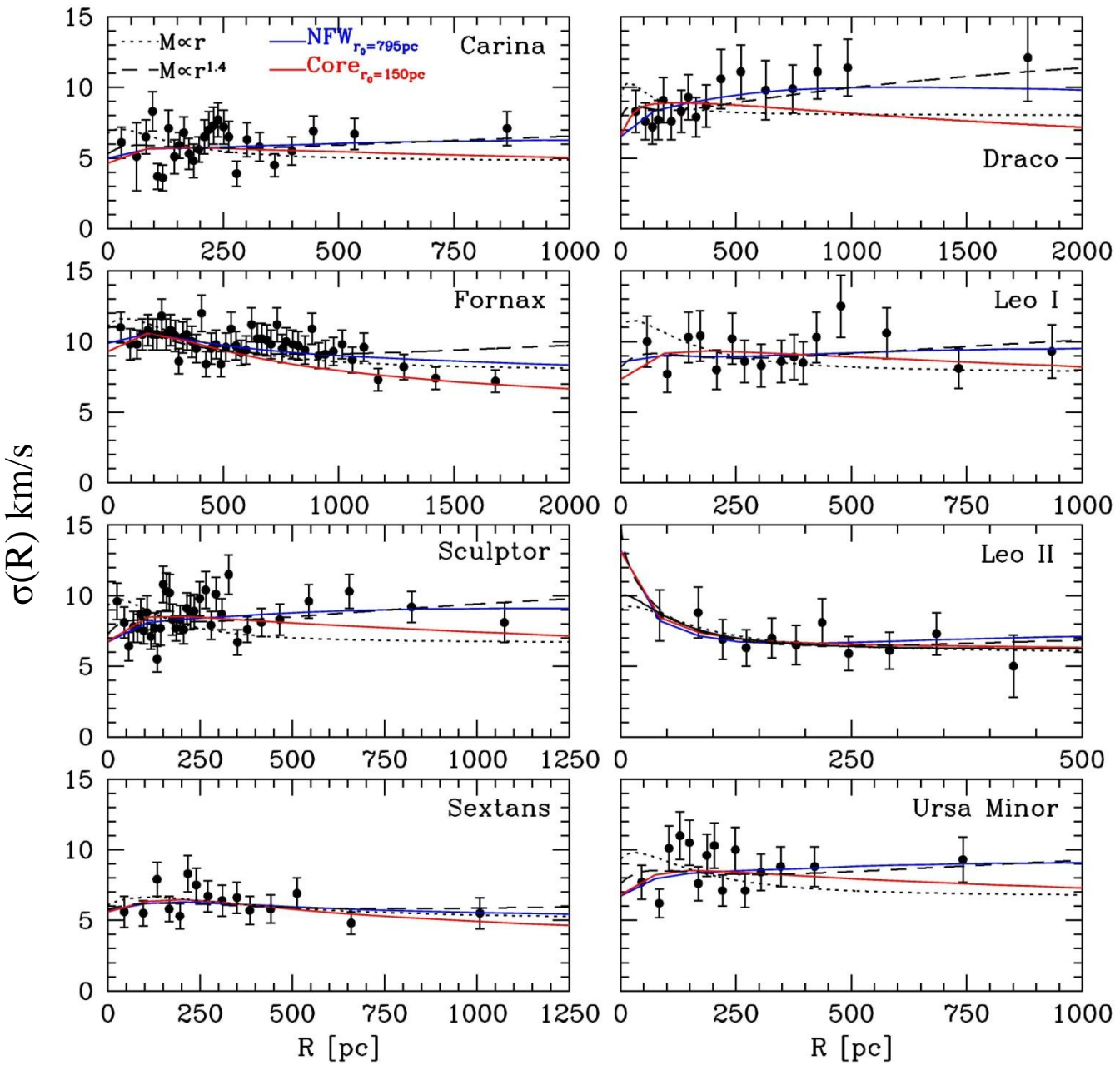
Make assumptions on the velocity anisotropy and then fit the dispersion profile



Results point to cored distributions

Gilmore et al 2007

Cored and (lesser cusped halos) fit dispersion velocity profiles

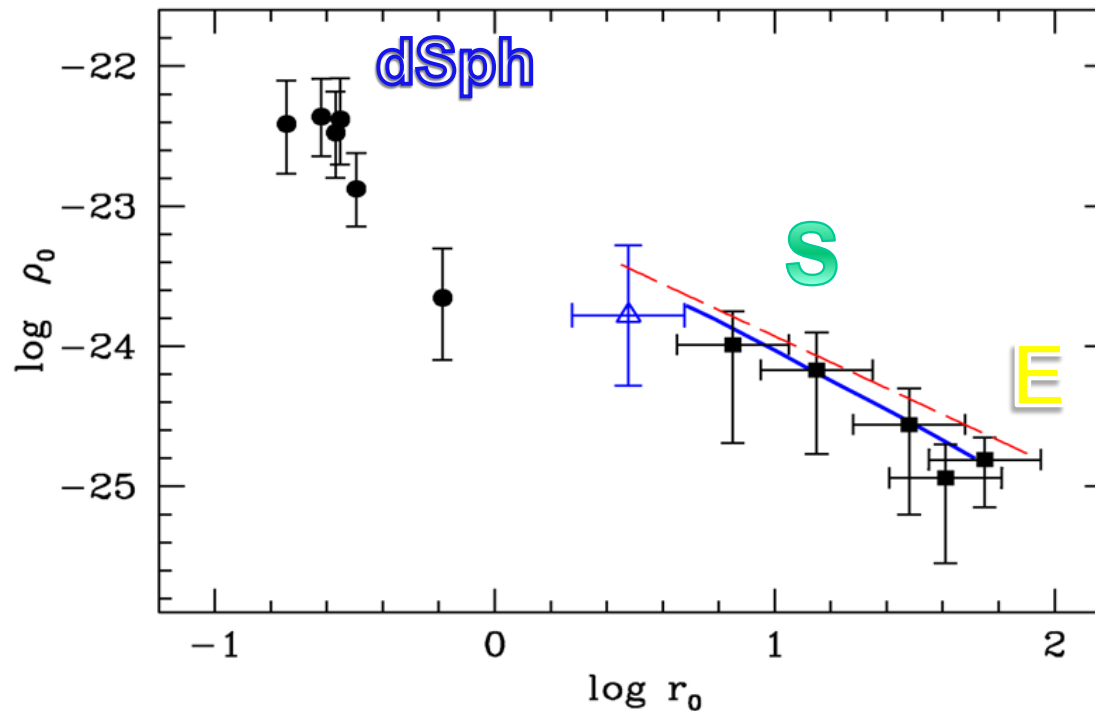


Walker et al 2009
 Donato et al 2009

dSphs cored halo model

halo central densities correlate with core radius in the same way as Spirals and Ellipticals

$$\rho_0 = 10^{-23} \left(\frac{r_0}{1 \text{ kpc}} \right)^{-1} \text{ g/cm}^3$$



Donato et al 2009

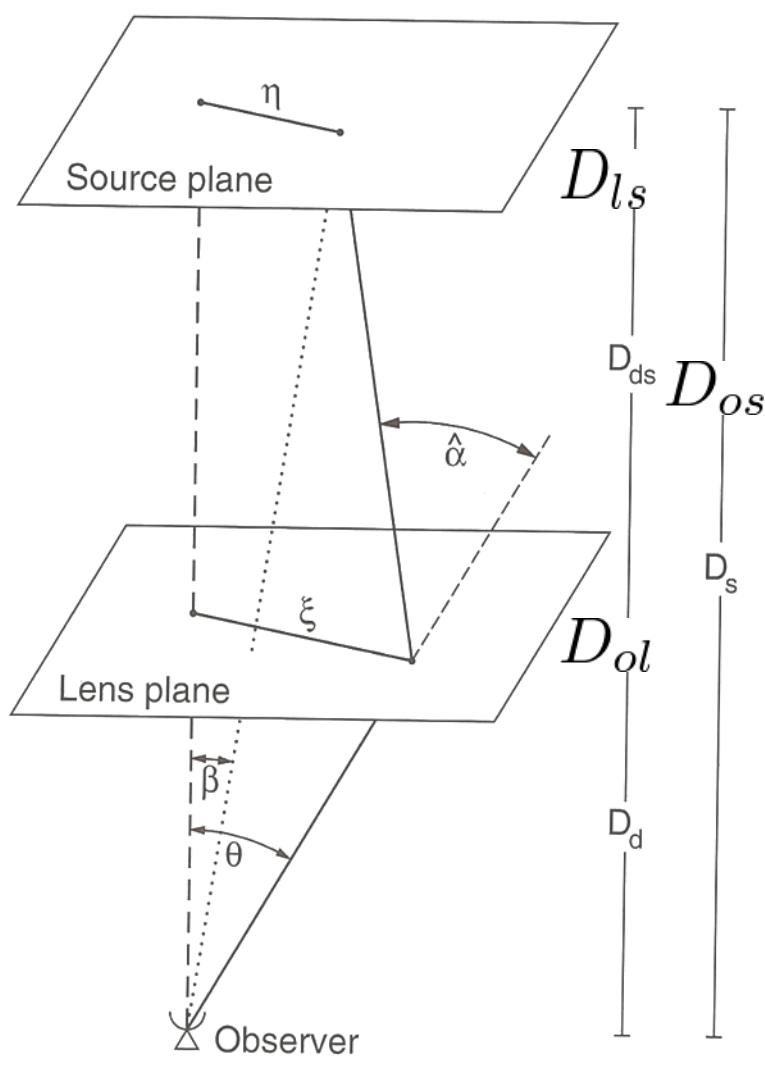
DSPH: WHAT WE KNOW

**PROVE THE EXISTENCE OF DM HALOS OF $10^{10} M_{\text{SUN}}$ AND $\rho_0 = 10^{-21} \text{ g/cm}^3$
DOMINATED BY DARK MATTER AT ANY RADIUS
MASS PROFILE CONSISTENT WITH THE EXTRAPOLATION OF THE URC
HINTS FOR THE PRESENCE OF A DENSITY CORE**

Mass profiles from weak lensing

Lensing equation for the observed tangential shear

e.g. Schneider, 1996



$$\langle \gamma_t \rangle \equiv \frac{\bar{\Sigma}(R) - \Sigma(R)}{\Sigma_c(R)}$$

$$\bar{\Sigma} = \frac{M(R)}{4\pi R^2}$$

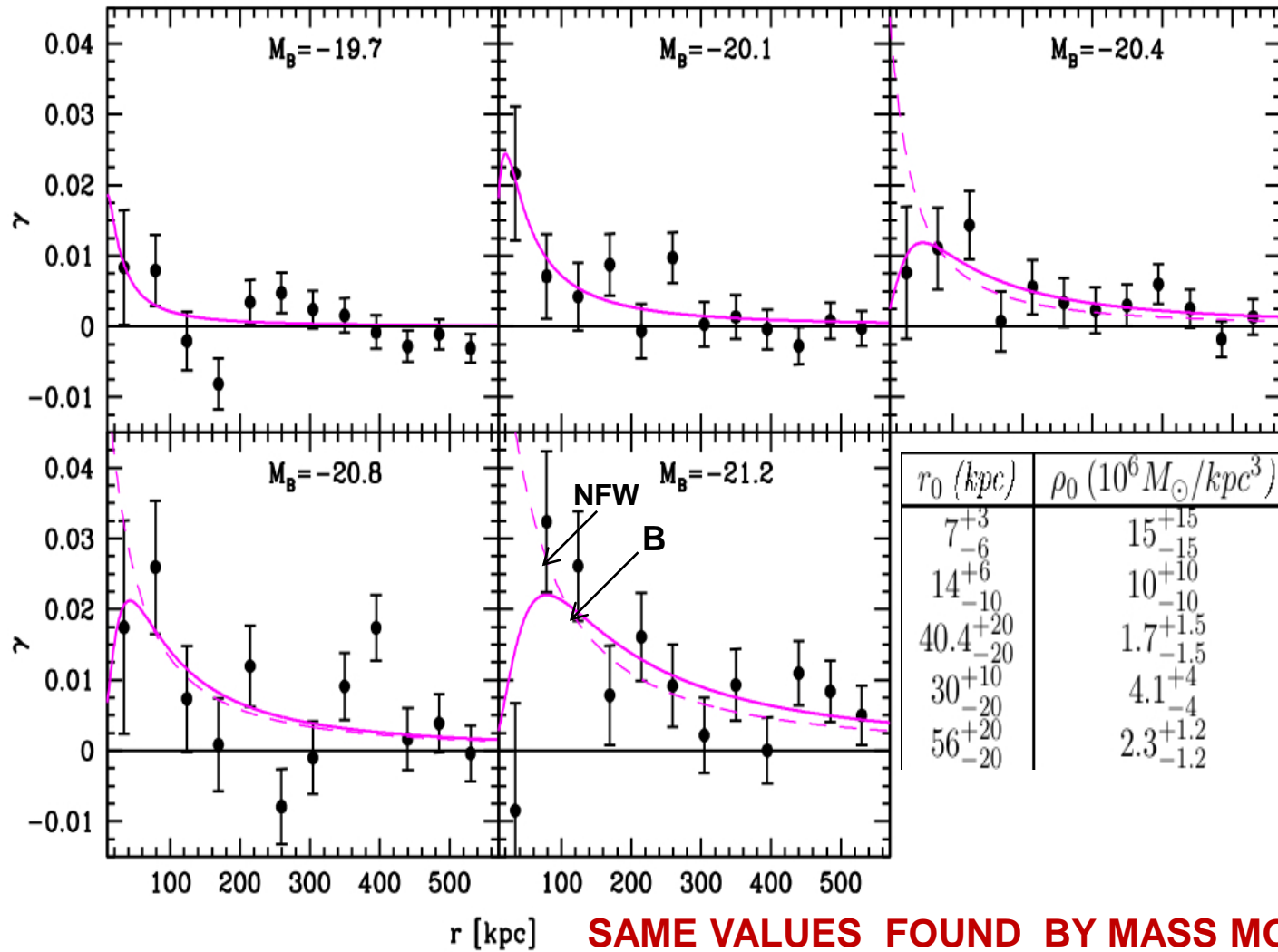
$$R = \theta D_{ol}$$

$$\Sigma_c = \frac{c^2}{4\pi G} \frac{D_{os}}{D_{ol} D_{ls}}$$

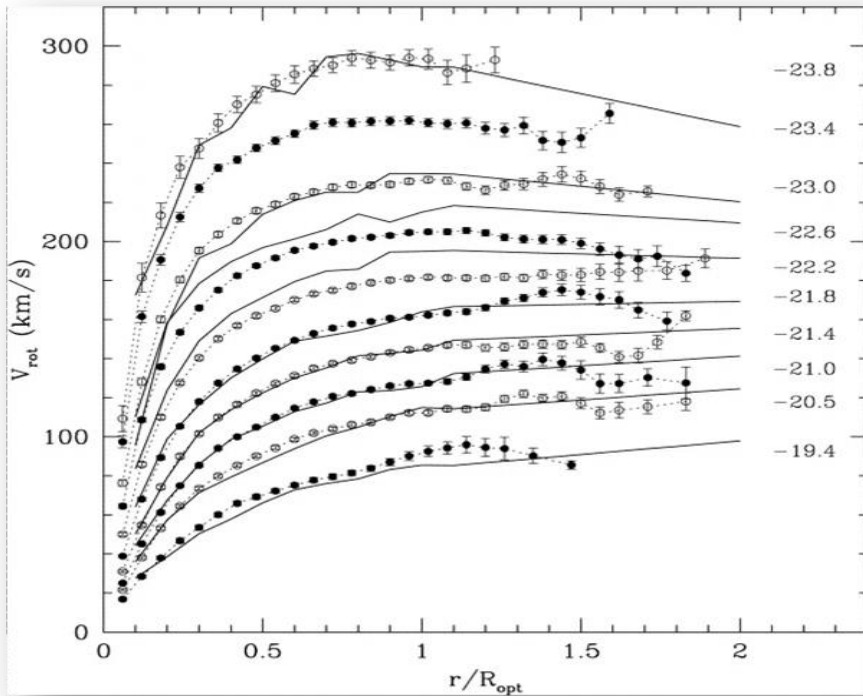
OUTER DM HALOS: NFW/BURKERT PROFILE

Lenses: 170 000 isolated galaxies, sources: 3×10^7 SDSS galaxies

Donato et al 2009

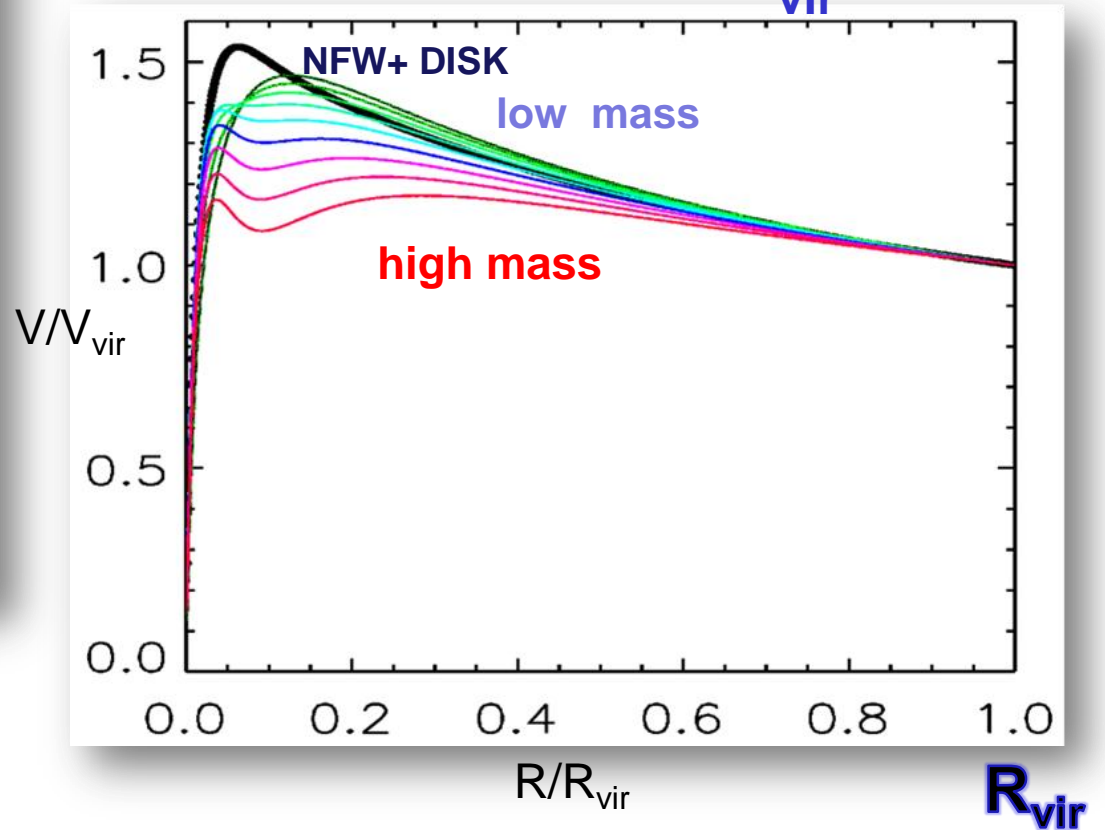


URC



$$V = F(R/R_D, M_I)$$

URC out to R_{vir}



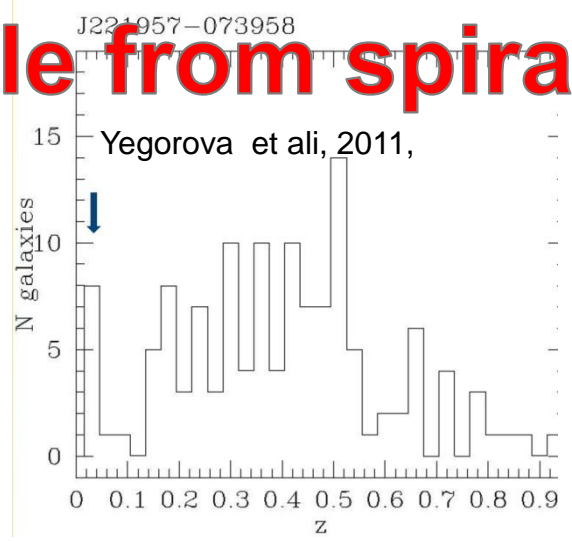
$$V = G(R/R_{\text{vir}}, M_{\text{vir}})$$

primaries - satellites

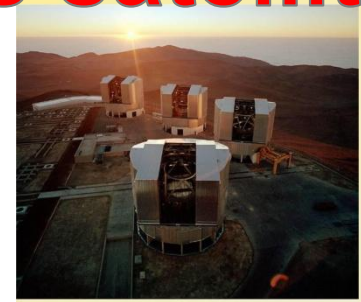
1.5 - 2 satellites per host galaxy

- Zaritsky (1993): 45 primaries – 69 satellites
Kitt Peak 2.3 m
- Sales & Lambas (2004): 1498 primaries – 3079 satellites
2dFGRS 3.9 m
- Breinerd (2004) 3 samples: 1351 primaries – 2084 satellites
SDSS 2.5 m
948 primaries – 1294 satellites
400 primaries – 658 satellites
- Bailin et al. (2008): 273 primaries – 321 satellites
SDSS 2.5 m

DM profile from spiral's satellites



We are studying 8 isolated spiral galaxies at $z = 0.03 - 0.09$



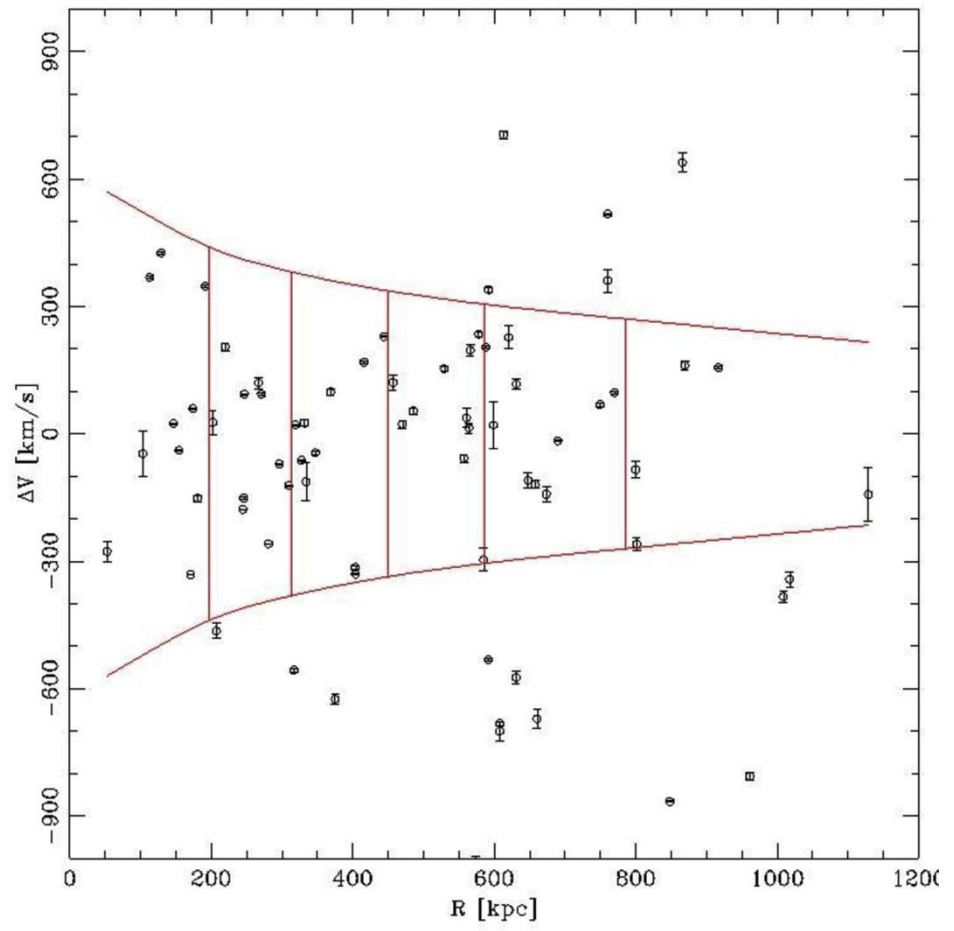
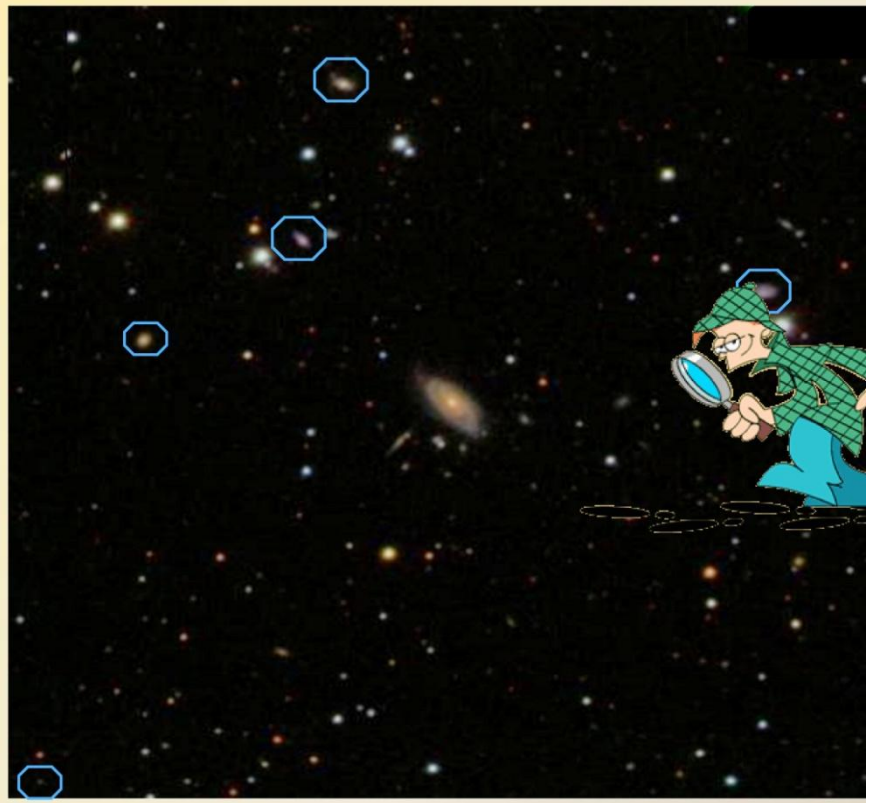
VIMOS



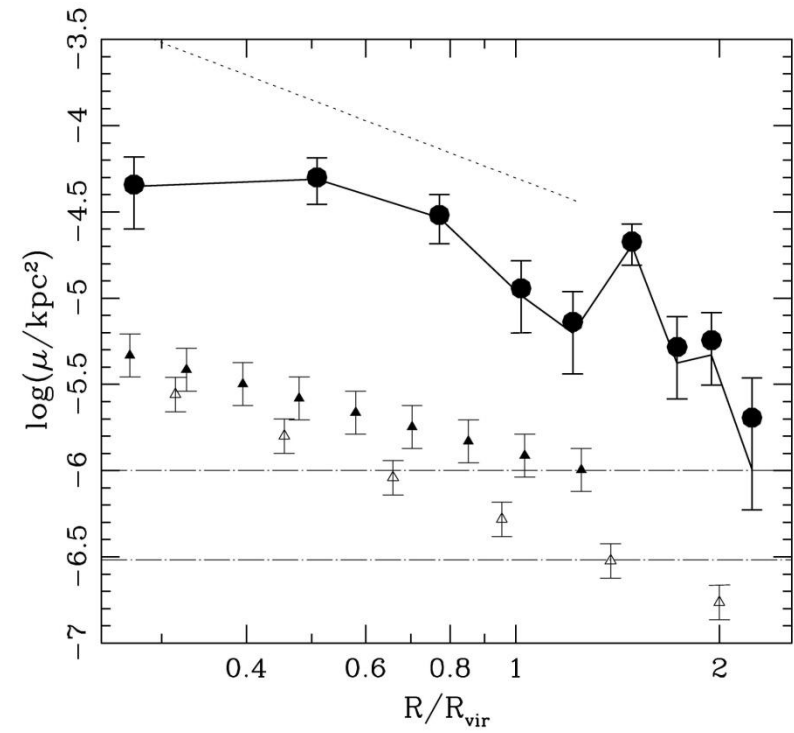
EMMI

Satellites + Rotation curves

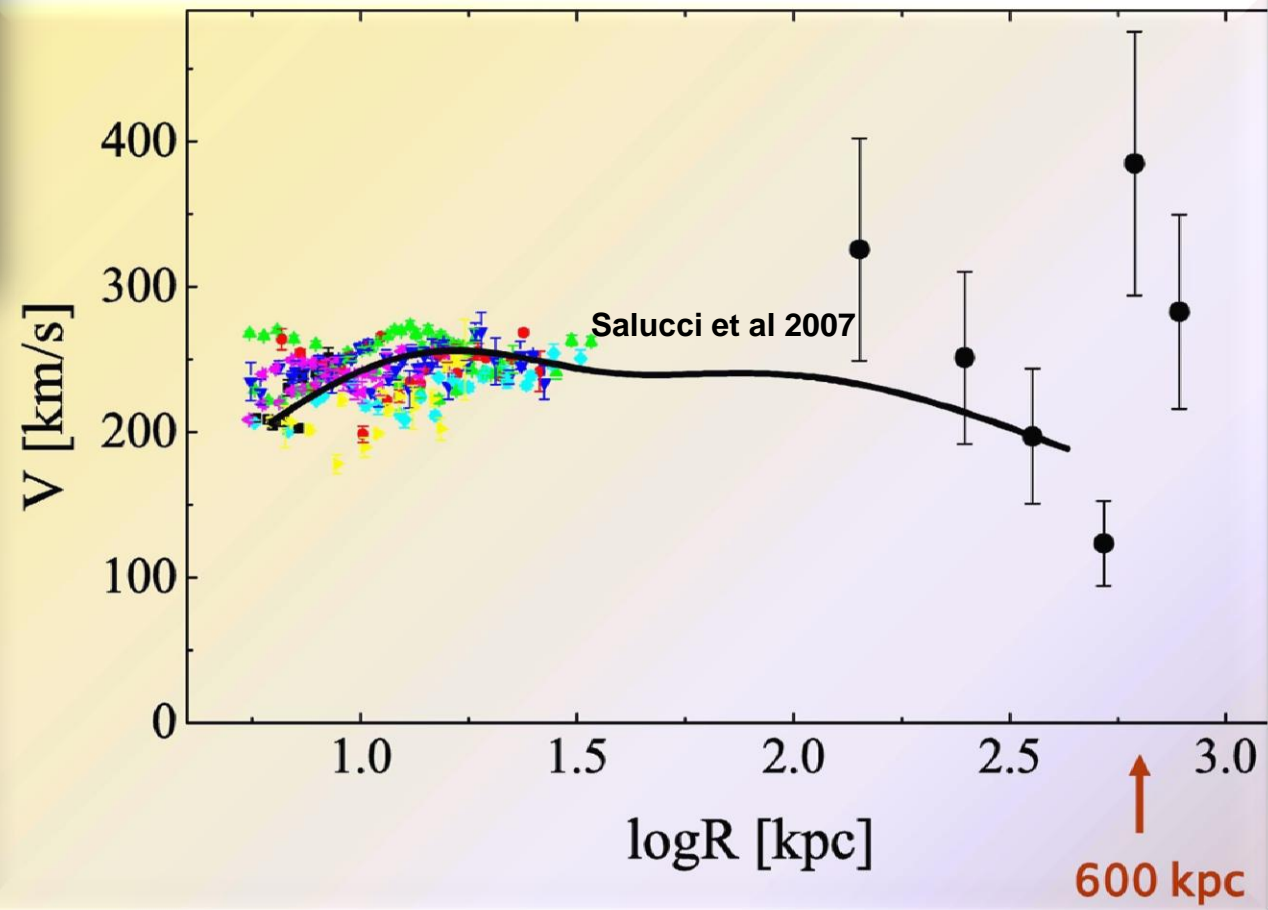
SDSS J154040.56-000933.5
 $z=0.078$



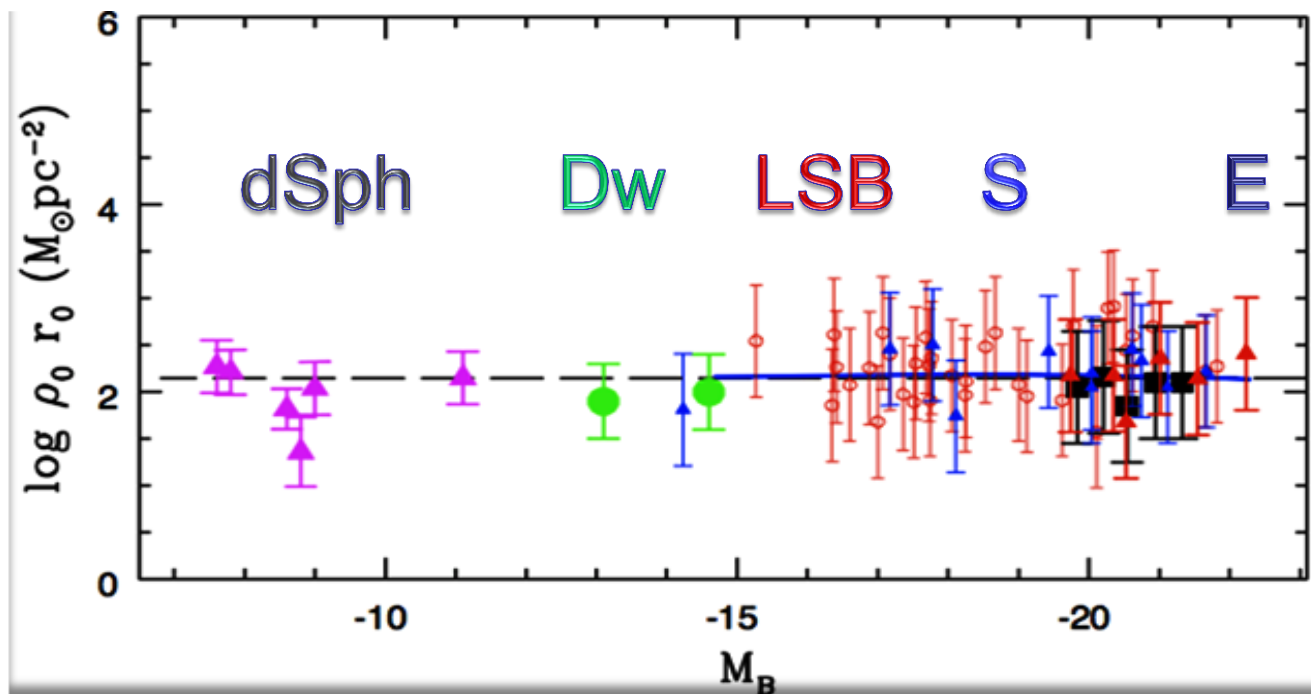
Surface density of satellites around 8 primaries



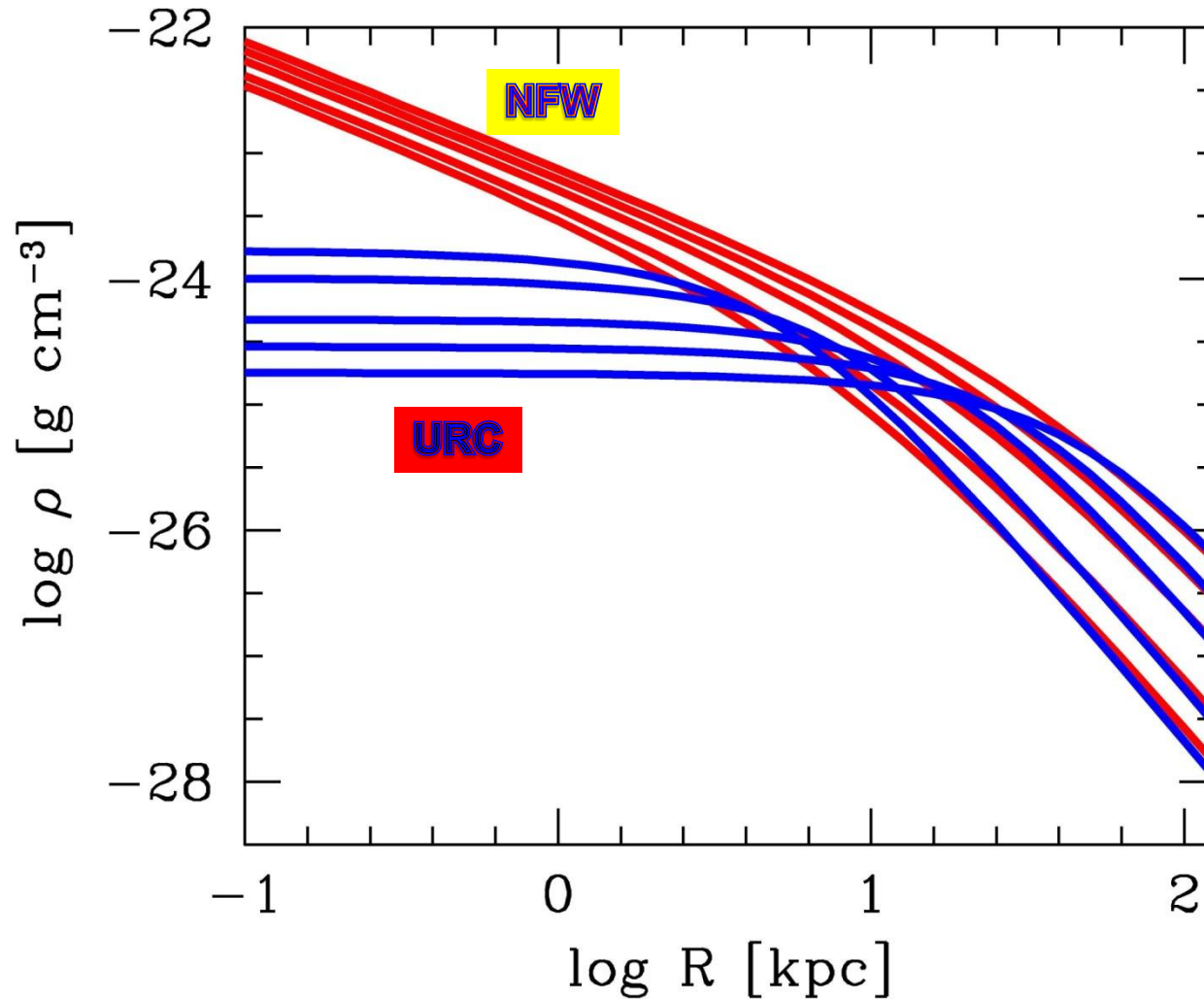
averaged circular velocity



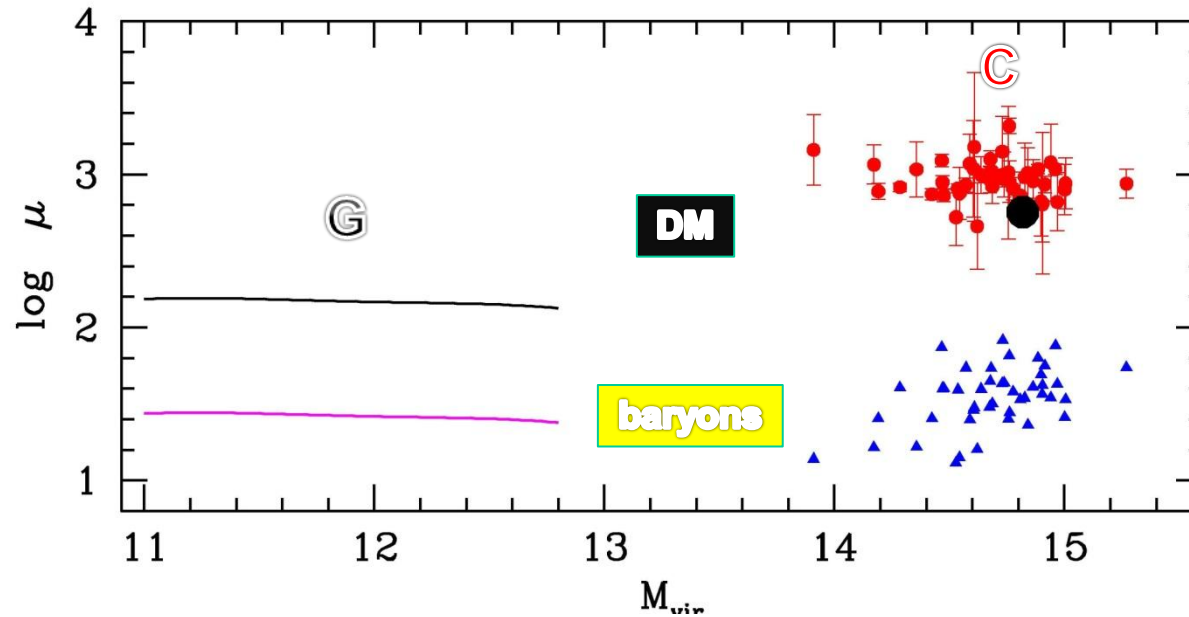
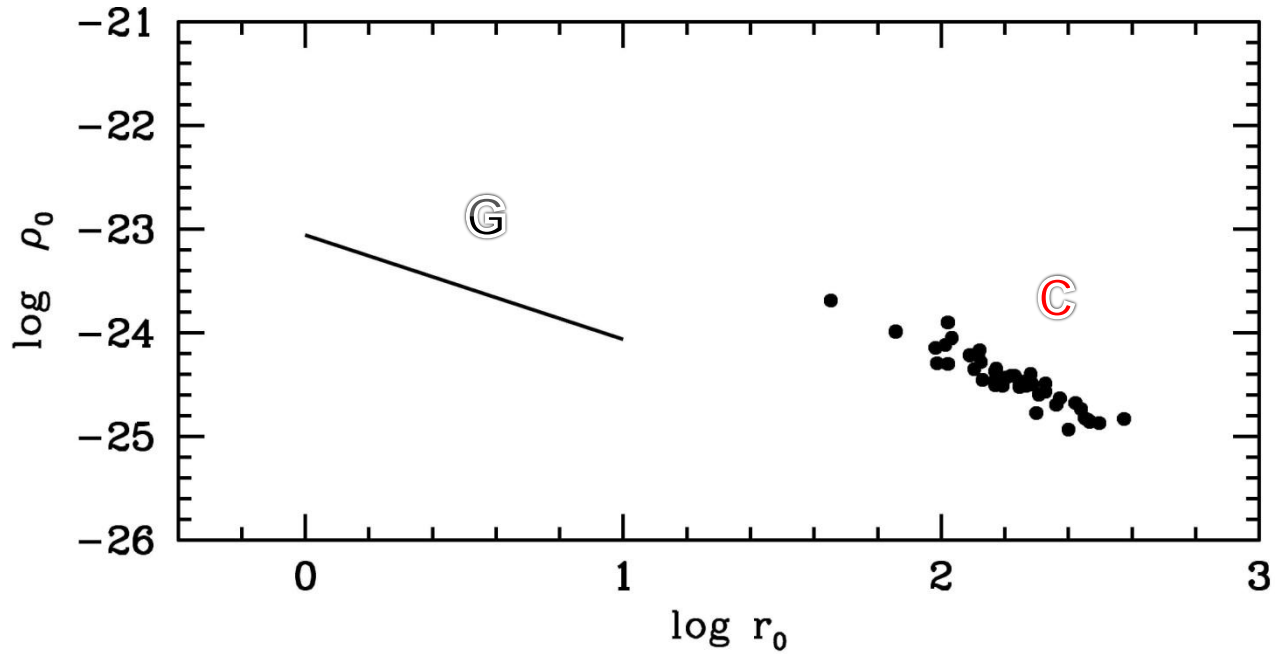
GALAXY HALOS: UDP



Universal Density Profile



CLUSTERS:
$$M(R) = -\frac{kT(R) \cdot R}{G\mu m_p} \left(\frac{d \ln n(R)}{d \ln R} + \frac{d \ln T(R)}{d \ln R} \right)$$



CONCLUSIONS

The distribution of DM in halos around galaxies shows a **striking** and **complex** phenomenology

At play: the nature of dark matter and the galaxy formation process

We find a centrally shallow, Universal DM density profile.

Unlikely that all this masks a new law of Gravity, rather it points to a warm particle with a characteristic scale

Innovative review on DM in galaxies

<http://people.sissa.it/~salucci/DMAW2010>

DMAW20101.pptx