#### Star Formation Rates in Molecular Gas and the Nature of the Extragalactic Scaling Relations

Marco Lombardi, University of Milan

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with: Charles Lada, CfA Joao Alves et al., University of Vienna z = 0.1 - 10





### Local Universe

"It would seem most probable that the rate of star formation depends on the gas density and we shall assume that the number formed per unit interval of time varies with a power of the gas density ..."

(Schmidt 1959)







The Milky Way



#### Pipe Nebula

#### ρ Ophiuchi Cloud



$$\sum_{Pipe} = 50 M_{\odot} pc^{-2}$$

$$\sum_{Oph} = 40 M_{\odot} pc^{-2}$$



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$$\sum_{Oph} = 40 M_{\odot} pc^{-2}$$

#### 316YSOs

14000 M<sub>☉</sub>

#### 8000 M<sub>☉</sub>

21 YSOs

$$\sum_{Pipe} = 50 M_{\odot} pc^{-2}$$

$$\sum_{Oph} = 40 M_{\odot} pc^{-2}$$

#### $SFR_{Oph} = I5 \times SFR_{Pipe}$

$$\sum_{Pipe} = 50 M_{\odot} pc^{-2}$$

 $\sum_{Oph} = 40 M_{\odot} pc^{-2}$ 







 $SFR_{Orion} = I0 \times SFR_{California}$ 



 $SFR_{Orion} = I0 \times SFR_{California}$ 

#### Clouds identical in mass & size

#### Inventory of Local Star Formation Activity

Infrared extinction and cloud masses

### **Extinction Primer**





Extinction

 $m_{\rm obs} - m_{\star} = A_{\rm V} = 1.086 \,\tau$ 

### **Extinction Primer**

Color  $\Delta m = m_{\lambda_1} - m_{\lambda_2}$ **Color Excess**  $E(\lambda_1 - \lambda_2) = \Delta m_{\rm obs} - \Delta m_{\star}$  $= A_{\lambda_1} - A_{\lambda_2} = R_{1,2}^{-1} A_{\lambda_1}$  $F_{\star}\mathrm{e}^{- au}$ 

 $R_{1,2}$  parametrizes our knowledge (or ignorance) on the dust properties at the two frequencies  $\lambda_1$  and  $\lambda_2$ 

T '

H - K

 Un-reddened stars occupy a small region in the color-color plane

I

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- Reddened stars are shifted in this plane

- Un-reddened stars occupy a small region in the color-color plane
- Reddened stars are shifted in this plane
- Optimal extinction obtained from colors and errors of each star



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Single star measurement

- Un-reddened stars occupy a small region in the color-color plane
- Reddened stars are shifted in this plane
- Optimal extinction obtained from colors and errors of each star



- Un-reddened stars occupy a small region in the color-color plane
- Reddened stars are shifted in this plane
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## CO vs. dust



<sup>12</sup>CO: Onishi et al. (1999), M=6500

## CO vs. dust



NICER: Lombardi et al. (2006), M=11000

## CO vs. dust



#### NICER: full resolution (1 arcmin)

## Extinction



VLT (BVI)

#### VLT (BVI)



VLT + NTT (BIK)

Extinction
### Extinction



VLT (BVI)

VLT + NTT (BIK)

### Extinction



VLT (BVI)

VLT + NTT (BIK)

### Milky Way & Gould belt (optical)



### Milky Way & Gould belt (optical)





### Milky Way & Gould belt (optical)



### Milky Way & Gould belt (NIR)

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### The Pipe Nebula (Lombardi et al. 2006)



The Pipe Nebula (Lombardi et al. 2006)













### Inventory of Star Formation Activity: Molecular Clouds

#### Cloud sample: wide field 2MASS/NICER extinction survey of 21 local modelcular clouds



Cloud	Mass (10 <sup>4</sup> $M_{\odot}$ )
Orion A	6.77
Orion B	7.18
California	9.99
Perseus	I.84
Taurus	1.49
Ophiuchus	1.41
RCrA	0.11
Pipe	0.79
Lupus I	0.22
Lupus 3	0.14
Lupus 4	0.08

### Inventory of Star Formation Activity: Young Stellar Objects (YSOs)

#### Mining the literature: mostly IR data (SPITZER)



Cloud	YSOs
Orion A	2862
Orion B	635
California	279
Perseus	598
Taurus	335
Ophiuchus	316
RCrA	100
Pipe	21
Lupus I	3
Lupus 3	69
Lupus 4	12

### Variation of specific star formation rate

## Variations of efficiencies and star formation rates in local molecular clouds



 $SFR = \langle m_{\star} \rangle N_{\rm YSOs} / t_{\rm sf} \simeq 0.25 \times 10^{-6} N_{\rm YSOs} \, \mathrm{M}_{\odot} \, \mathrm{yr}^{-1}$ 

## Variations of efficiencies and star formation rates in local molecular clouds



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## Variations of efficiencies and star formation rates in local molecular clouds



Greather than one order of magnitude and independent of the cloud mass!



 $SFR = \langle m_{\star} \rangle N_{\rm YSOs} / t_{\rm sf} \simeq 0.25 \times 10^{-6} N_{\rm YSOs} \, \mathrm{M}_{\odot} \, \mathrm{yr}^{-1}$ 

#### What determines the star formation rate?





Nearly identical shapes & sizes, but YSOs(Orion) > 10 x YSOs(California)



Nearly identical shapes & sizes, but YSOs(Orion) > 10 x YSOs(California) SFR(Orion) > 10 x SFR(California)





Nearly identical shapes & sizes, but

YSOs(Orion) > 10 x YSOs(California)

 $SFR(Orion) > 10 \times SFR(California)$ 

#### Orion has 10 x as much material at A<sub>K</sub> > 1 mag as California



### Normalized cloud mass profiles



Kainulainen et al. (2009)







$$\left(\frac{SFR}{M_{\odot} \text{ yr}^{-1}}\right) = 4.6 \times 10^{-8} \left(\frac{M_{0.8}}{M_{\odot}}\right)$$







What is the meaning of the slope of this relation?





What is the meaning of the slope of this relation?

$$SFR = \varepsilon M_{0.8} / \tau_{sf}$$
  
 $\tau_{sf} \simeq 2 \times 10^6 \text{ yr}$   
 $\varepsilon = SFE \simeq 0.10$ 

### The physical process

- Stars form in dense regions of molecular clouds
  - "proctected" environment: cold gas, no UV radiation, Jeans/Bonnor-Ebert instability
- We find that the SFR correlates with the amount of mass above a projected density threshold
- The projected mass density is unphysical (depends on the line of sight); we should have instead a volume density threshold!
# A $\Sigma$ - $\rho$ relation for molecular clouds

- Different Molecular clouds show consistent structure
  - Same average density a above threshold value (as predicted by WDM)
  - Same probability distribution for Σ (lognormal)
  - Similar stratification of surface density contours



#### Lombardi et al. (2010)

# Log-normal fits to cloud projected density distributions



Lombardi et al. (2011)

# A $\Sigma$ - $\rho$ relation for molecular clouds

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# SFR directly proportional to mass above $A_K > 0.8 \text{ mag} (\Sigma > 116 \text{ M}_{\odot} \text{ pc}^{-2})$

$$\left(\frac{SFR}{M_{\odot} \text{ yr}^{-1}}\right) = 4.6 \times 10^{-8} \left(\frac{M_{0.8}}{M_{\odot}}\right)$$

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$$M_{0.8} = \int_D \rho(x) \,\mathrm{d}^3 x$$

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$$M_{0.8} = \int_D \rho(x) \, \mathrm{d}^3 x$$
$$D = \{ x \, | \, \rho(x) > 400 \, \mathrm{M}_\odot \, \mathrm{pc}^{-3} \}$$

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$$M_{0.8} = \int_D \rho(x) \, \mathrm{d}^3 x$$
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### Star formation scaling laws for low density gas



### <sup>12</sup>CO observations (Dame et al 2001)



$$M(CO) \sim M(A_K > 0.1 \text{ mag})$$









SFR =  $4.6 \times 10^{-8} M_{dense} = 4.6 \times 10^{-8} f_{dense} M_{tot}$ 

# From local clouds to galaxies

# Extragalactic scaling law



Local clouds SF law:  $SFR_{MC} = 4.6 \times 10^{-8} M_{0.8}$ Extragalactic SF law:  $SFR_{XGAL} = 1.8 \times 10^{-8} M_{HCN}$ 

# Extragalactic scaling law

- Does M<sub>0.8</sub> ~ M<sub>HCN</sub> ?
  - $M_{HCN} = X_{HCN} I_{HCN}$
  - $\rho_{HCN} > 2-3 \times 10^4 \text{ cm}^{-3}$
  - $\rho_{0.8} > 1-2 \times 10^4 \text{ cm}^{-3}$
- Probably!



Local clouds SF law:  $SFR_{MC} = 4.6 \times 10^{-8} M_{0.8}$ Extragalactic SF law:  $SFR_{XGAL} = 1.8 \times 10^{-8} M_{HCN}$ 

# Extragalactic scaling law

- Does SFR<sub>MC</sub> ~ SFR<sub>XGAL</sub> ?
  - SFR<sub>XGAL</sub> derived from SB99 code
  - SFR<sub>MC</sub> =  $N_* < M_* > / t_{sf}$
  - SB99 code often used as a "black box" with default parameters



Local clouds SF law:  $SFR_{MC} = 4.6 \times 10^{-8} M_{0.8}$ Extragalactic SF law:  $SFR_{XGAL} = 1.8 \times 10^{-8} M_{HCN}$ 



Standard parameters:

 $SFR_{99} = 2.0 \times 10^{-10} L_{IR}/L_{\odot} M_{\odot} yr^{-1}$ 

#### $SFR_{obs} = 8.7 \times 10^{-4} M_{\odot} yr^{-1}$



Standard parameters:

 $SFR_{99} = 2.0 \times 10^{-10} L_{IR}/L_{\odot} M_{\odot} yr^{-1}$ 

 $L_{IR}(obs) = 5.4 \times 10^5 L_{\odot}$ 

 $SFR_{obs} = 8.7 \times 10^{-4} M_{\odot} yr^{-1}$ 



Standard parameters:

 $SFR_{99} = 2.0 \times 10^{-10} L_{IR}/L_{\odot} M_{\odot} yr^{-1}$ 

 $L_{IR}(obs) = 5.4 \times 10^5 L_{\odot}$ 

 $SFR_{99} = 1.1 \times 10^{-4} M_{\odot} yr^{-1}$ 

 $SFR_{obs} = 8.7 \times 10^{-4} M_{\odot} yr^{-1}$ 



For  $t_{sf} = 2$  Myr:  $SFR_{99} = 3.2 \times 10^{-10} L_{IR}/L_{\odot} M_{\odot} \text{ yr}^{-1}$   $_{\pi}L_{IR}(obs) = 5.4 \times 10^5 L_{\odot}$   $SFR_{99} = 1.6 \times 10^{-4} M_{\odot} \text{ yr}^{-1}$  $SFR_{obs} = 8.7 \times 10^{-4} M_{\odot} \text{ yr}^{-1}$ 



For  $t_{sf} = 2$  Myr &  $M_{max} = 30$  M $_{\odot}$  $SFR_{99} = 10 \times 10^{-10} L_{IR}/L_{\odot} M_{\odot} yr^{-1}$  $L_{IR}(obs) = 5.4 \times 10^5 L_{\odot}$  $SFR_{99} = 5.6 \times 10^{-4} M_{\odot} \text{ yr}^{-1}$  $SFR_{obs} = 8.7 \times 10^{-4} M_{\odot} yr^{-1}$ 



For  $t_{sf} = 2 \text{ Myr } \& \text{ M}_{max} = 30 \text{ M}_{\odot}$ SFR<sub>99</sub> = 10 × 10<sup>-10</sup> L<sub>IR</sub>/L<sub> $\odot$ </sub> M<sub> $\odot$ </sub> yr<sup>-1</sup> L<sub>IR</sub>(obs) = 5.4 × 10<sup>5</sup> L<sub> $\odot$ </sub> SFR<sub>99</sub> = 5.6 × 10<sup>-4</sup> M<sub> $\odot$ </sub> yr<sup>-1</sup> SFR<sub>obs</sub> = 8.7 × 10<sup>-4</sup> M<sub> $\odot$ </sub> yr<sup>-1</sup>

Similar results obtained by Chomiuk & Povich (2011):

 $SFR_{GMCs} = 2.7 SFR_{SB99}$ 

Star Formation Scaling Laws from Local Clouds to Galaxies



Star Formation Scaling Laws from Local Clouds to Galaxies



Star Formation Scaling Laws from Local Clouds to Galaxies



#### Star Formation Scaling Laws from Local Clouds to Galaxies



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#### Star Formation Scaling Laws from Local Clouds to Galaxies



#### A Linear Scaling Law for Galaxies

Young & Scoville 1991, ARAA 32, 581



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Young & Scoville 1991, ARAA 32, 581



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Young & Scoville 1991, ARAA 32, 581



The nature of the Schmidt-Kennicutt scaling relation
# Physical interpretation

• Standard interpretation:

 $ho_{
m SF} \propto rac{
ho_{
m gas}}{ au_{
m ff}} \propto \sqrt{G} 
ho^{1.5}$ 

- We do not observe collapsing gas forming stars
- A CO beam (~kpc) includes several clouds: higher CO intensity implies more clouds, not densier gas
- A shallower relation should hold

## Physical interpretation

- Standard interpretation:  $\rho_{\rm SF} \propto \frac{\rho_{\rm gas}}{\tau_{\rm ff}} \propto \sqrt{G} \rho^{1.5}$ 
  - We do not observe collapsing gas forming stars
  - A CO beam (~kpc) includes several clouds: higher CO intensity implies more clouds, not densier gas
  - A shallower relation should hold



Star Formation Scaling Laws from Local Clouds to Galaxies



Star Formation Scaling Laws from Local Clouds to Galaxies



### Sample of 17 nearby galaxies

Biegel et al. 2008



- HI does not correlate at all with the SFR
- H<sub>2</sub> correlates with slope I (Gao-Solomon law)
- $HI + H_2$  correlates with slope ~1.5 (Schmidt-Kennicutt law) Smidth-Kennicutt law seems to be just the result of gas dilution!

B)

**Observational Implications and Test:** 

		N	
F	=\		

**Observational Implications and Test:** 





Mass(A) = Mass(B)



Mass(A) = Mass(B)



Schmidt Scaling Laws

n= 1.5

 $SFR \thicksim \rho^n$ 

 $\rho_{SFR} \thicksim (\rho_g)^n$ 

 $\Sigma_{\rm SFR} \sim (\Sigma_g)^n$ 



Mass(A) = Mass(B)

Schmidt Scaling Laws		n= 1.5	
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SFR ~  $\rho^n$  SFR(B) =  $(\rho_{g(B)} / \rho_{g(A)})^n$  SFR(A)

 $\rho_{SFR} \sim (\rho_g)^n$ 

 $\Sigma_{\rm SFR} \sim (\Sigma_g)^n$ 



Mass(A) = Mass(B)

SFR ~  $\rho^n$  SFR(B) =  $(\rho_{g(B)} / \rho_{g(A)})^n$  SFR(A) SFR(B) = 1600 SFR(A)

 $\rho_{SFR} \sim (\rho_g)^n$ 

 $\Sigma_{\rm SFR} \sim (\Sigma_{\rm g})^{\rm n}$ 



Mass(A) = Mass(B)

SFR ~  $\rho^n$ SFR(B) =  $(\rho_{g(B)} / \rho_{g(A)})^n$  SFR(A)SFR(B) = 1600 SFR(A) $\rho_{SFR} ~ (\rho_g)^n$ SFR(B) =  $(\rho_{g(B)} / \rho_{g(A)})^{n-1}$  SFR(A) $\nabla_{SFR} ~ (\nabla_g)^n$ SFR(B) =  $(\rho_{g(B)} / \rho_{g(A)})^{n-1}$  SFR(A)

 $\Sigma_{\rm SFR} \sim (\Sigma_{\rm g})^{\rm n}$ 



Schmidt Scaling Laws		n= 1.5	
SFR ~ $\rho^n$	SFR(B) = $(\rho_{g(B)} / \rho_{g(A)})^n$ SFR(A)	SFR(B) = 1600 SFR(A)	
$\rho_{SFR} \sim (\rho_g)^n$	SFR(B) = $(\rho_{g(B)} / \rho_{g(A)})^{n-1}$ SFR(A)	SFR(B) = 10 SFR(A)	
$\Sigma_{\rm SFR} \sim (\Sigma_{\rm g})^{\rm n}$			

A)  $\rho = \rho_t$ SFR(B) = SFR(A) Density Scaling Law

Mass(A) = Mass(B)

Schmidt Scaling Laws		n= 1.5	
SFR ~ ρ <sup>n</sup>	SFR(B) = $(\rho_{g(B)} / \rho_{g(A)})^n$ SFR(A)	SFR(B) = 1600 SFR(A)	
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$\Sigma_{\rm SFR} \sim (\Sigma_{\rm g})^{\rm n}$	$SFR(B) = (\Sigma_{g(B)} / \Sigma_{g(A)})^{n-1} SFR(A)$		

A)  $\rho = \rho_t$   $P = 10^2 \rho_t$  $P = 10^2 \rho_t$ 

Mass(A) = Mass(B)

Schmidt Scaling Laws		n= 1.5	
SFR ~ $\rho^n$	SFR(B) = $(\rho_{g(B)} / \rho_{g(A)})^n$ SFR(A)	SFR(B) = 1600 SFR(A)	
$\rho_{SFR} \sim (\rho_g)^n$	SFR(B) = $(\rho_{g(B)} / \rho_{g(A)})^{n-1}$ SFR(A)	SFR(B) = 10 SFR(A)	
$\Sigma_{\rm SFR} \sim (\Sigma_{\rm g})^{\rm n}$	$SFR(B) = (\Sigma_{g(B)} / \Sigma_{g(A)})^{n-1} SFR(A)$	SFR(B) = (1-5) SFR(A)	

### SUMMARY

- I. Specific star formation rates in molecular clouds vary considerably
- 2. The SFR correlates most directly with total mass of dense gas above a threshold column density of  $A_V \approx 7$  mag, corresponding to  $n \approx 10^4$  cm<sup>-3</sup>
- 3. A single, linear, star formation law connects galactic clouds to external galaxies: SFR =  $4.6 \pm 2.6 \times 10^{-8} M_{dense} (M_{\odot} \text{ yr}^{-1})$