

# Testing cosmological models with dwarf spheroidals

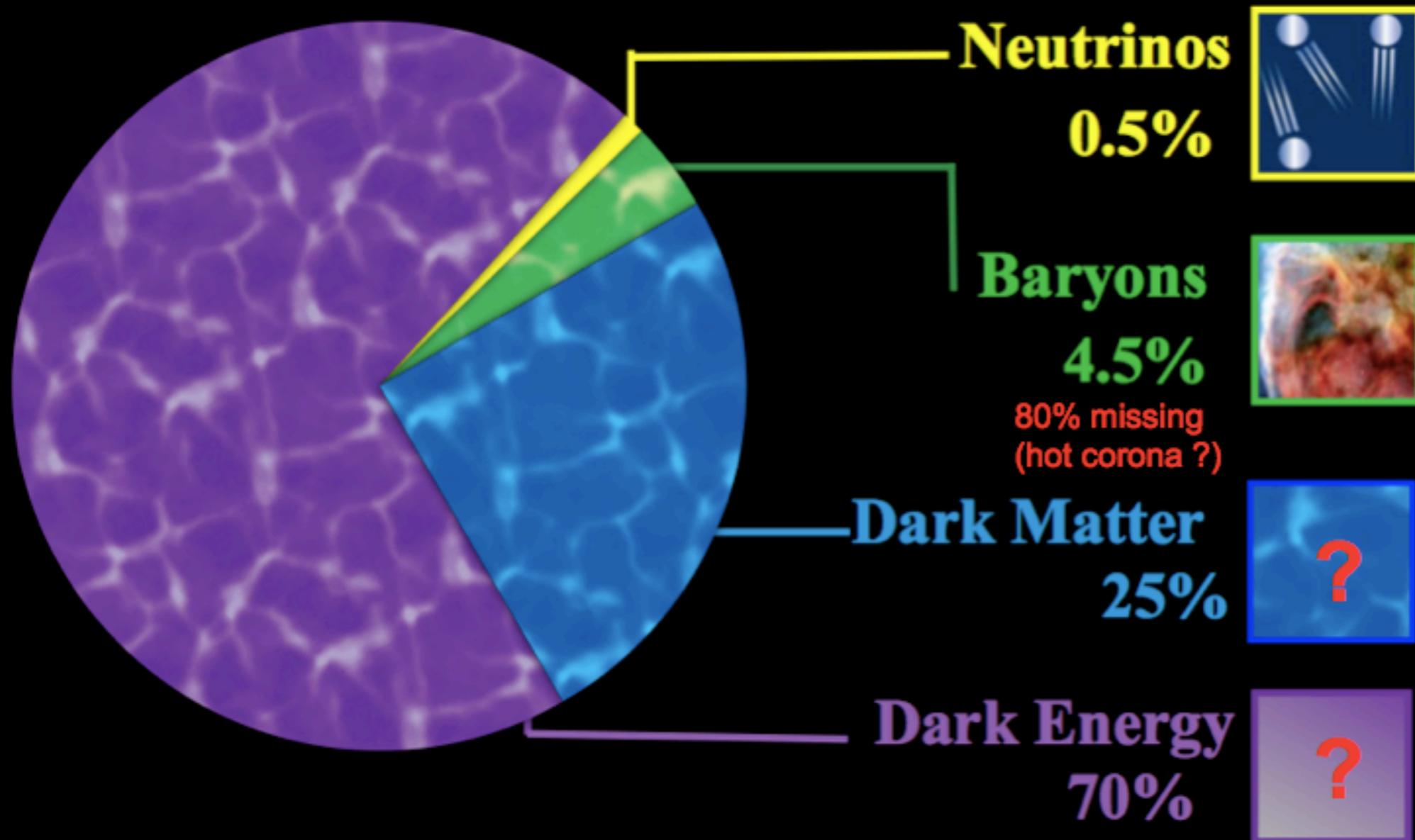
Jorge Peñarrubia



UNIVERSITY OF  
CAMBRIDGE

Paris  
7th of June 2012

# Universe Composition



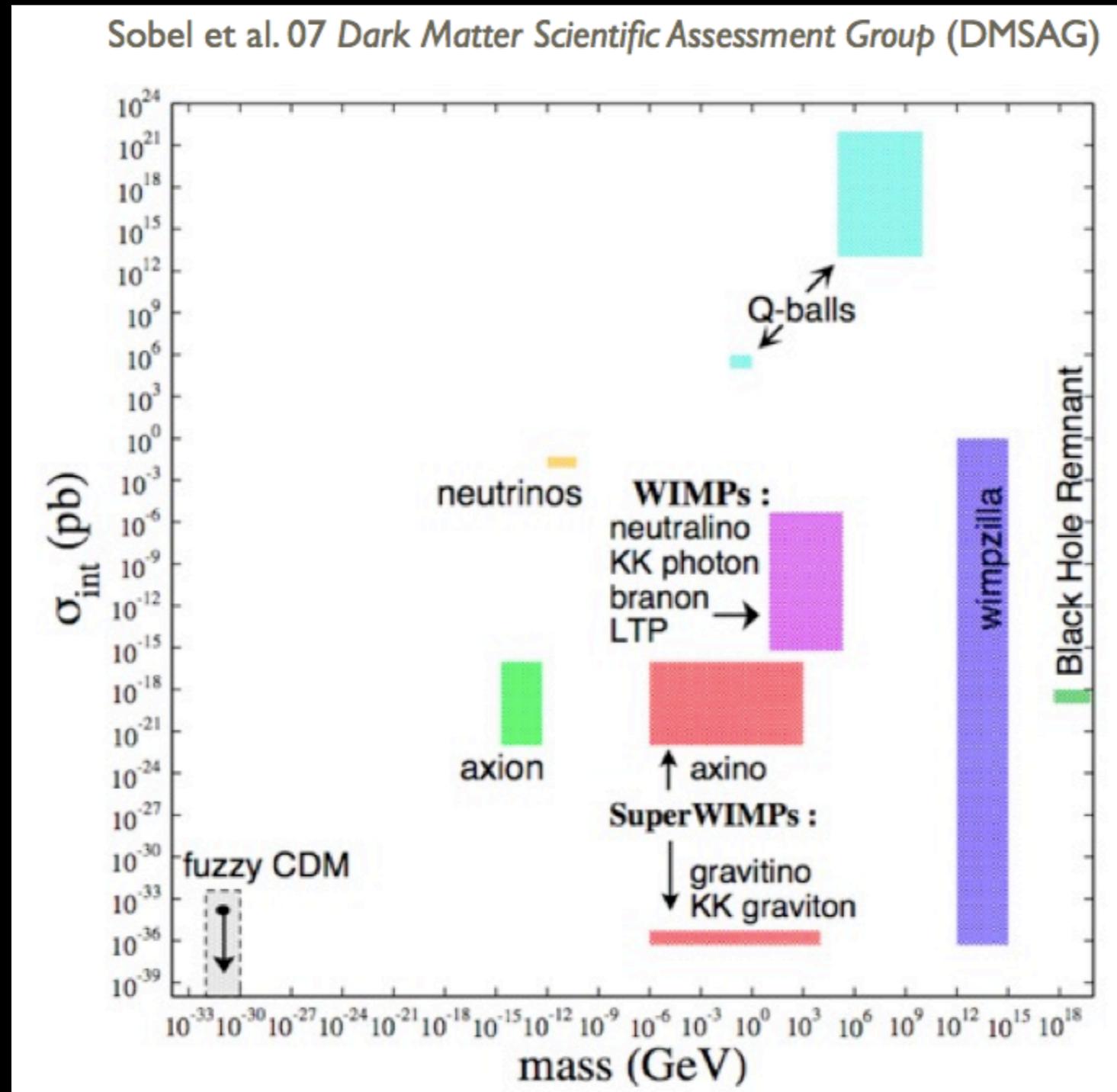
WMAP7

# DM particle models: **Constraints**

**Assumption:** dark matter is composed of “exotic” particles (i.e. beyond the current standard model of particle physics) that were created after the Big Bang

1. Relic density (CMB)
2. Electrically Neutral
3. Consistent with the Big Bang Nucleosynthesis
4. Leave stellar evolution unchanged
5. Compatible with constraints on self-interactions
6. Compatible with direct-searches constraints
7. It can be manufactured in the laboratory

# DM particle models: Constraints



63 orders

51 orders

# DM particle models: **Classification**

**HOT**  
 $< 10^2$  eV

**WARM**  
 $10^3 - 10^5$  eV

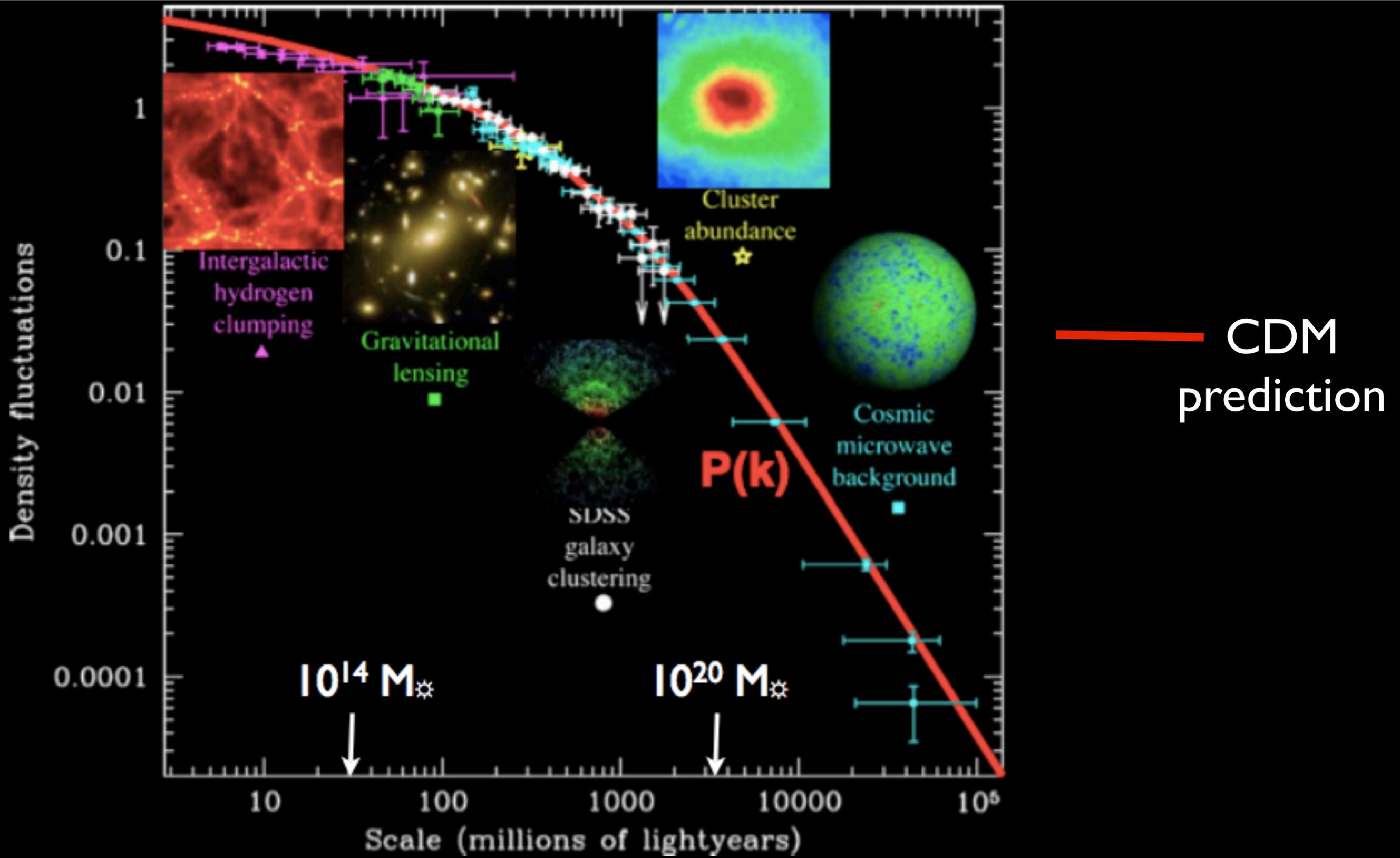
**COLD**  
 $10^9 - 10^{12}$  eV

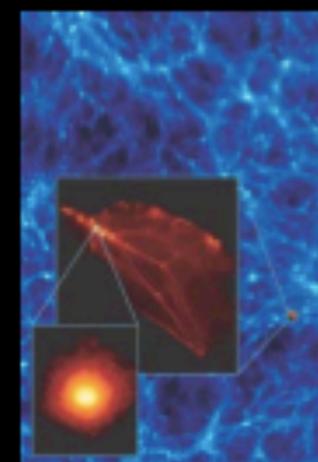
$\lambda_{\text{FS}} \equiv$  “average distance travelled by a DM particle before it falls in a potential well”

$$\lambda_{\text{FS}} \sim 20 \text{ Mpc} (30 \text{ eV} / m_\nu)$$

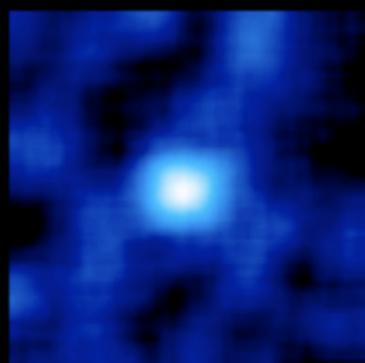
$$\lambda_{\text{FS}} \sim 1 \text{ Mpc} (1 \text{ keV} / m_\nu)$$

$$\lambda_{\text{FS}} \sim 3.7 \text{ pc} (100 \text{ GeV} / m_\nu)^{1/2}$$

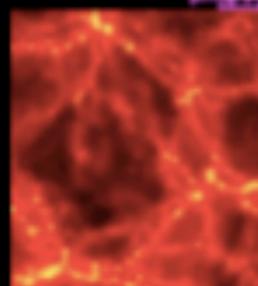




Gravitational  
milli lensing?



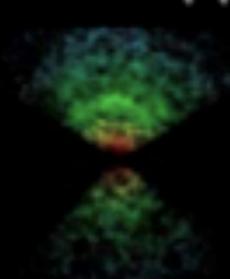
Dwarf galaxies



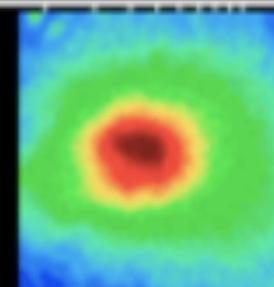
Intergalactic  
hydrogen  
clumping



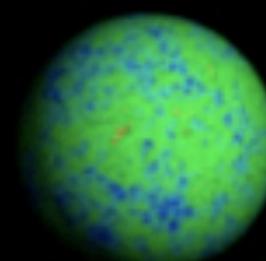
Gravitational  
lensing



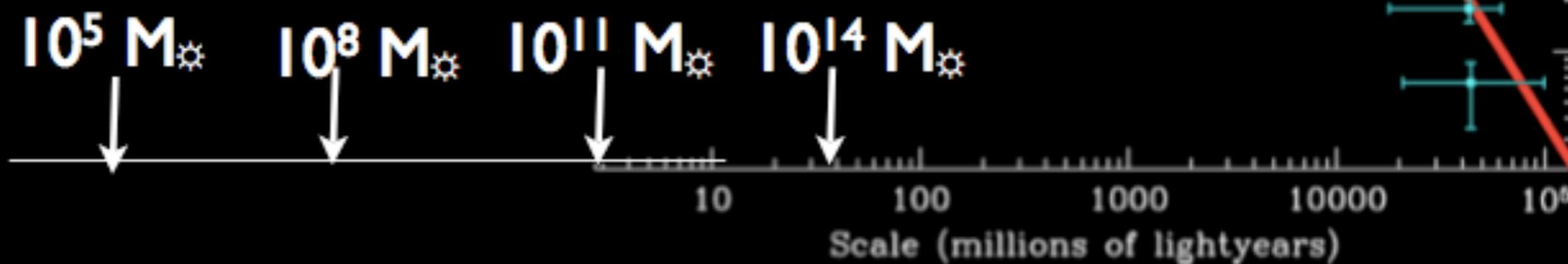
SDSS  
galaxy  
clustering

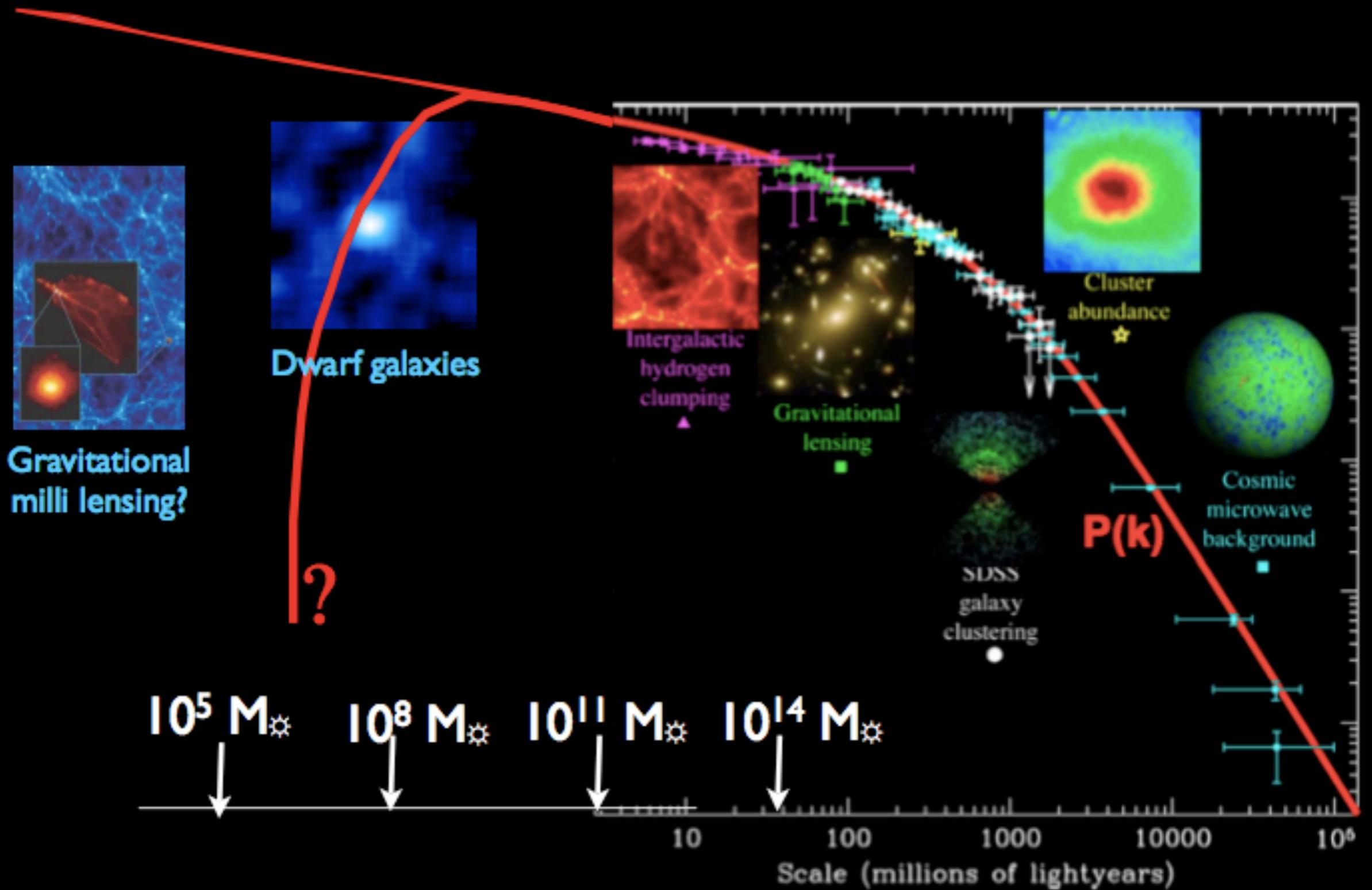


Cluster  
abundance

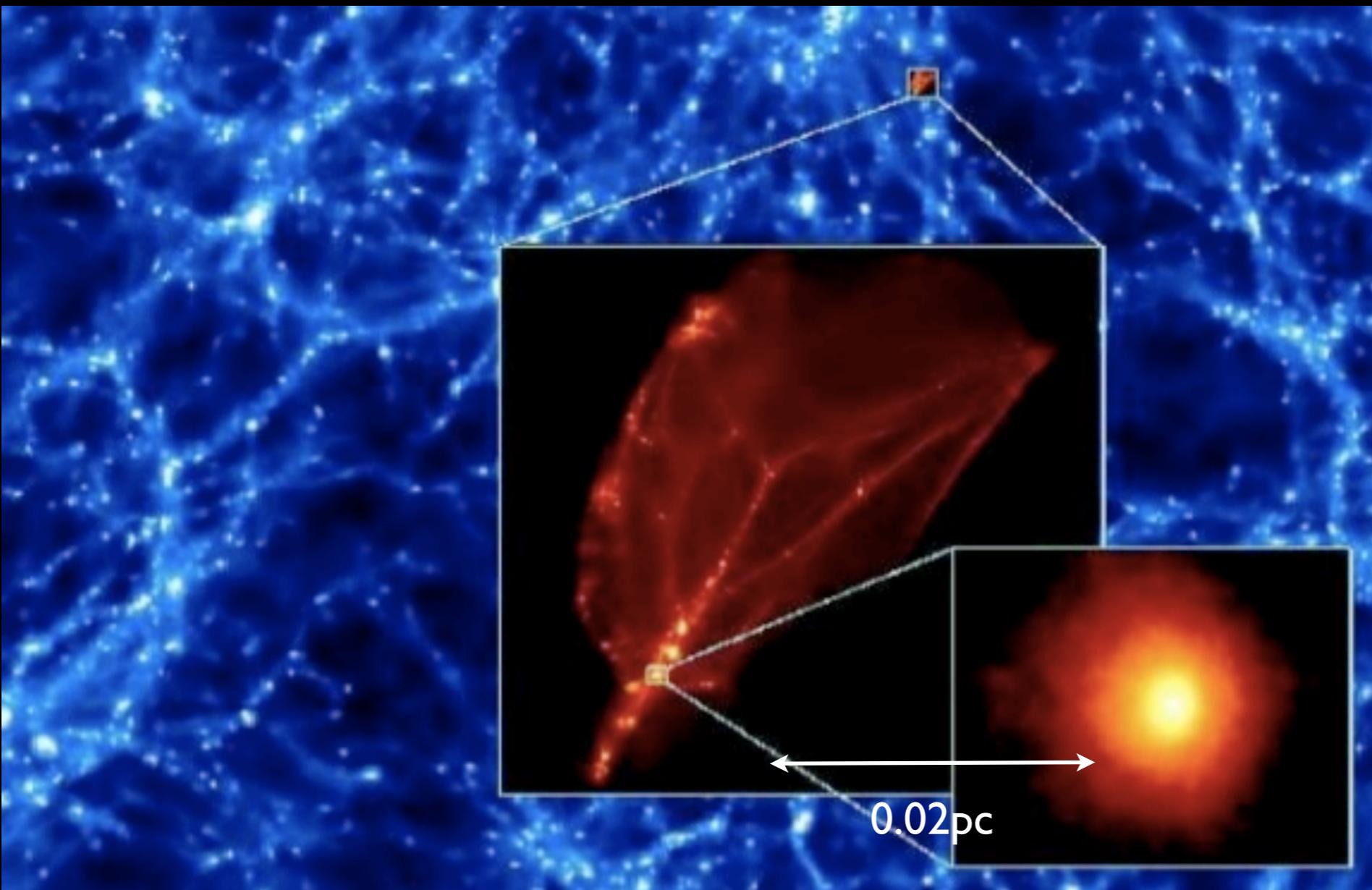


Cosmic  
microwave  
background





**Clues on the nature of DM must be searched on small scales**



Diemand+05

## DM particle mass $\sim 100$ Gev

- $M_{\text{subhalo,MW}} > 10^{-5} M_{\text{sol}}$
- $N_{\text{subhalo,MW}} > 10^{14}$  (!)

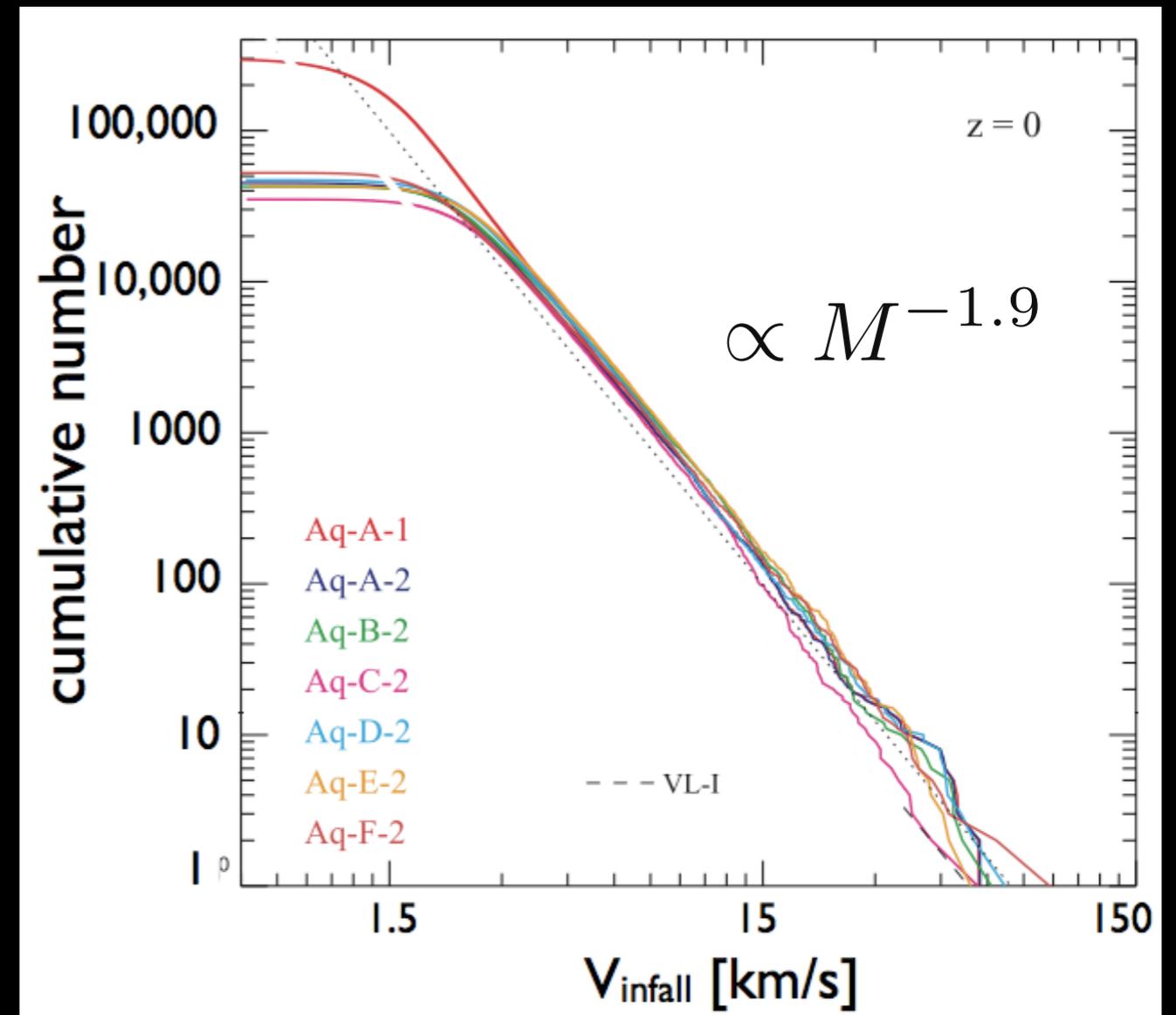


all of them galaxies?

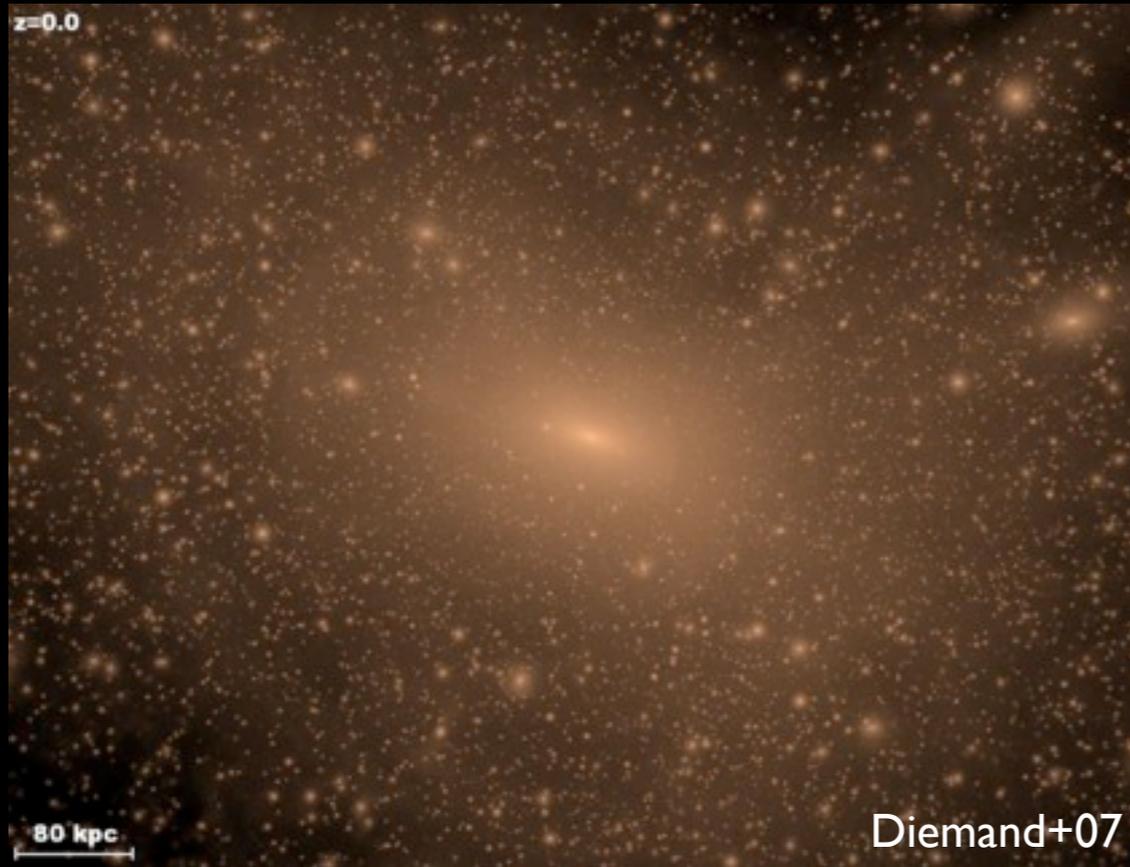
# The “missing satellite” problem



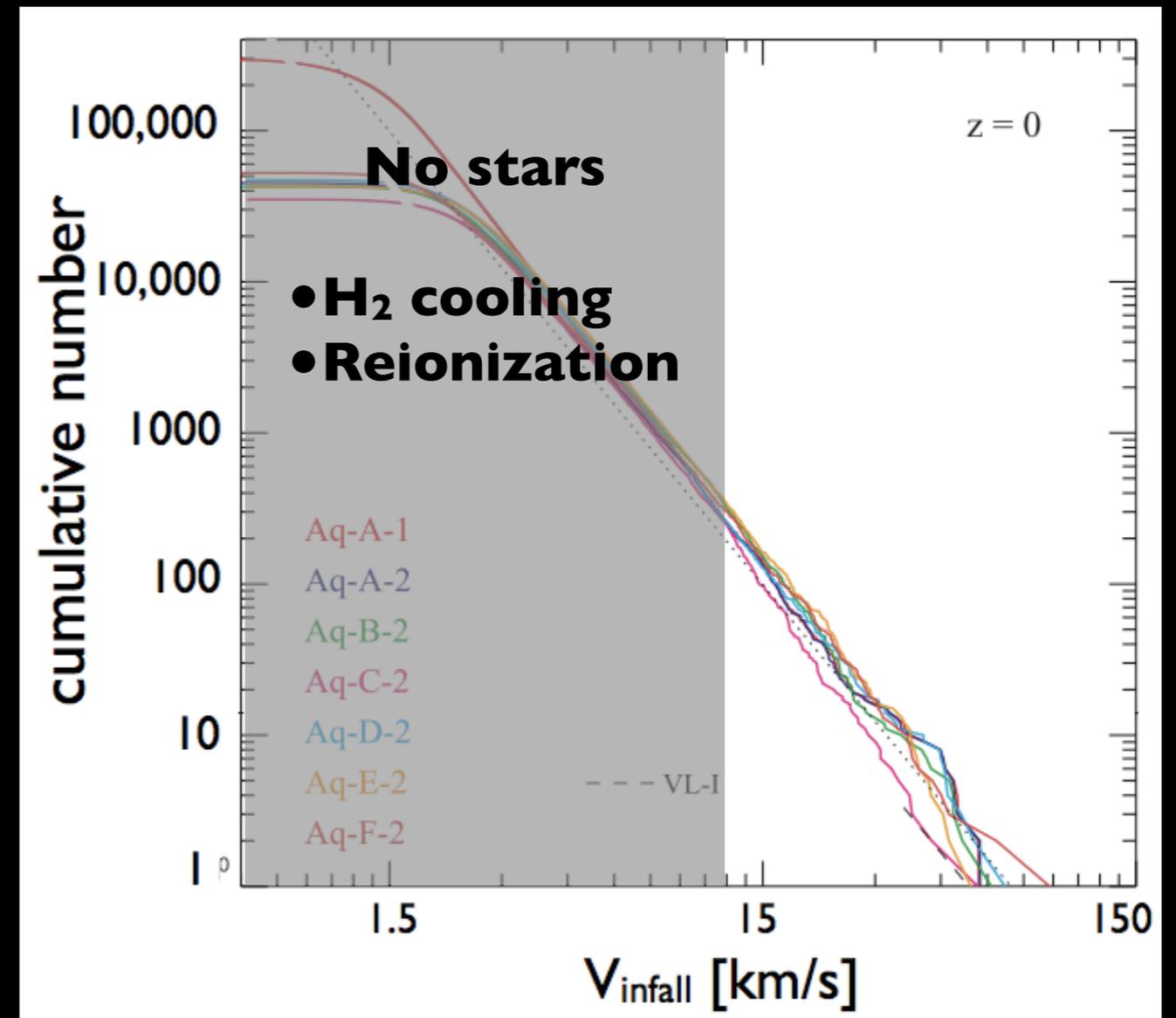
MW: ~25 dSph satellites  
M31: ~23 dSph sats.



# The “missing satellite” problem



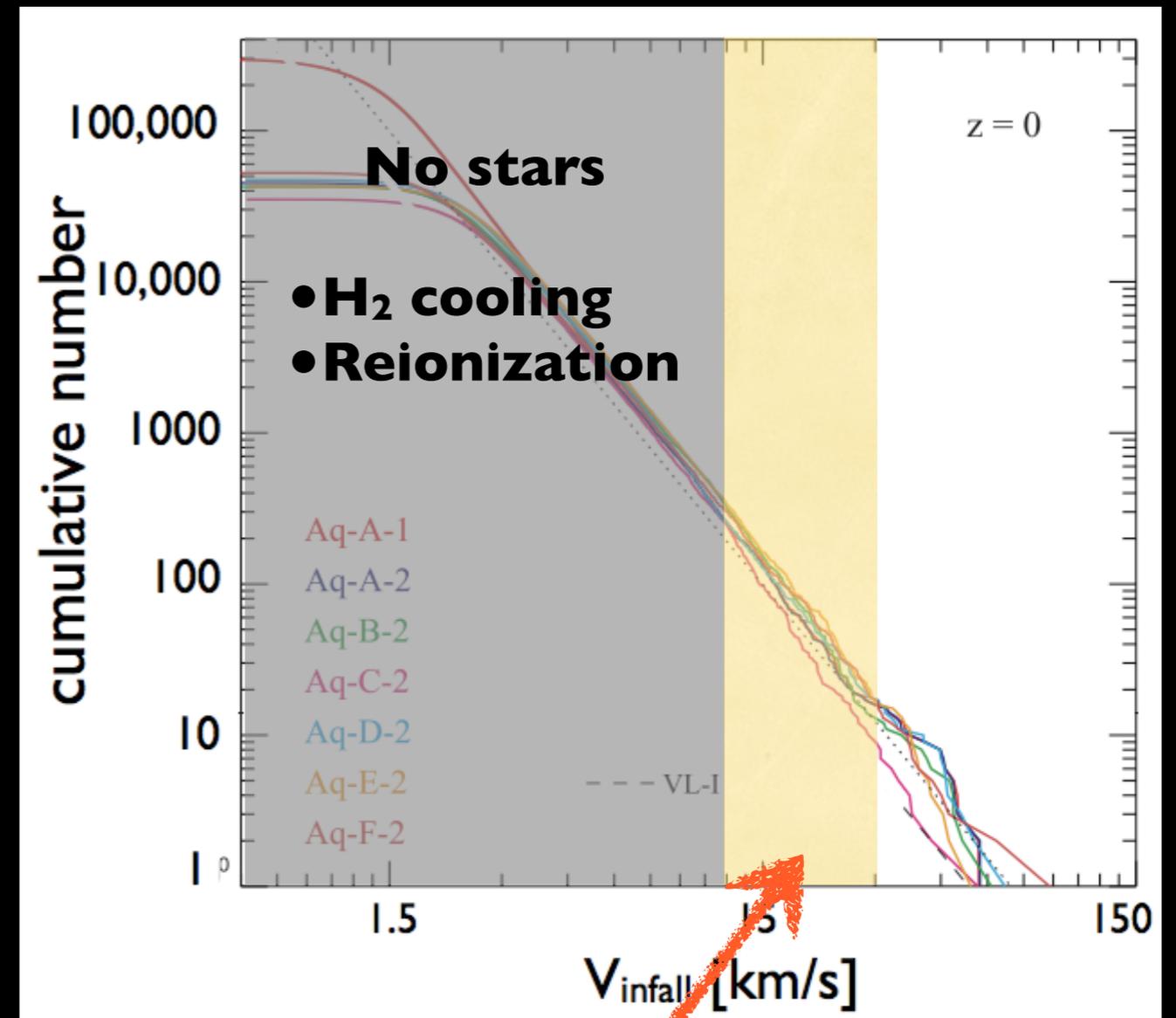
MW: ~25 dSph satellites  
M31: ~23 dSph sats.



# The “missing satellite” problem



MW: ~25 dSph satellites  
M31: ~23 dSph sats.

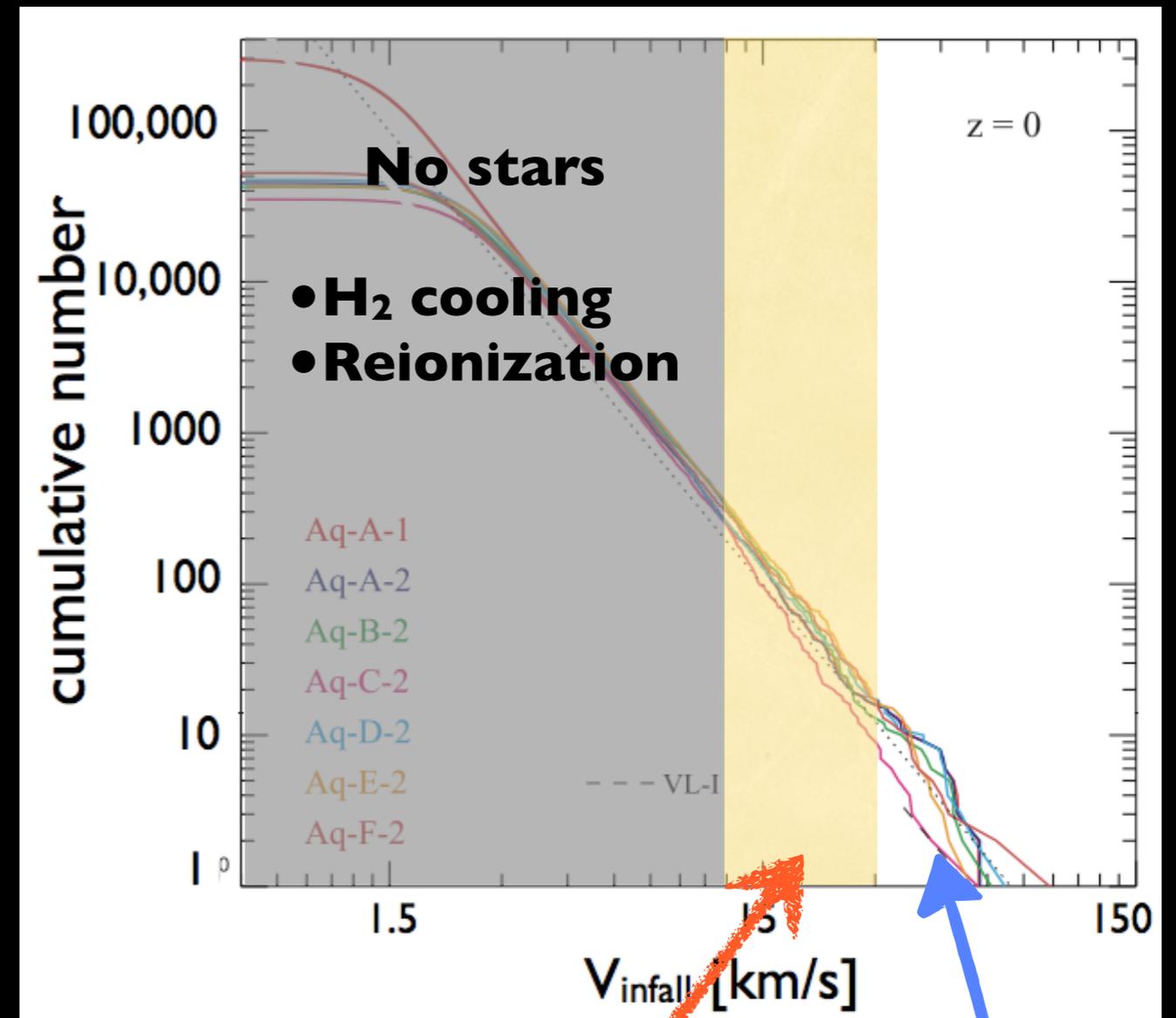


faint dSphs: incomplete sample  
Koposov+08; Tollerud+08

# The “missing satellite” problem



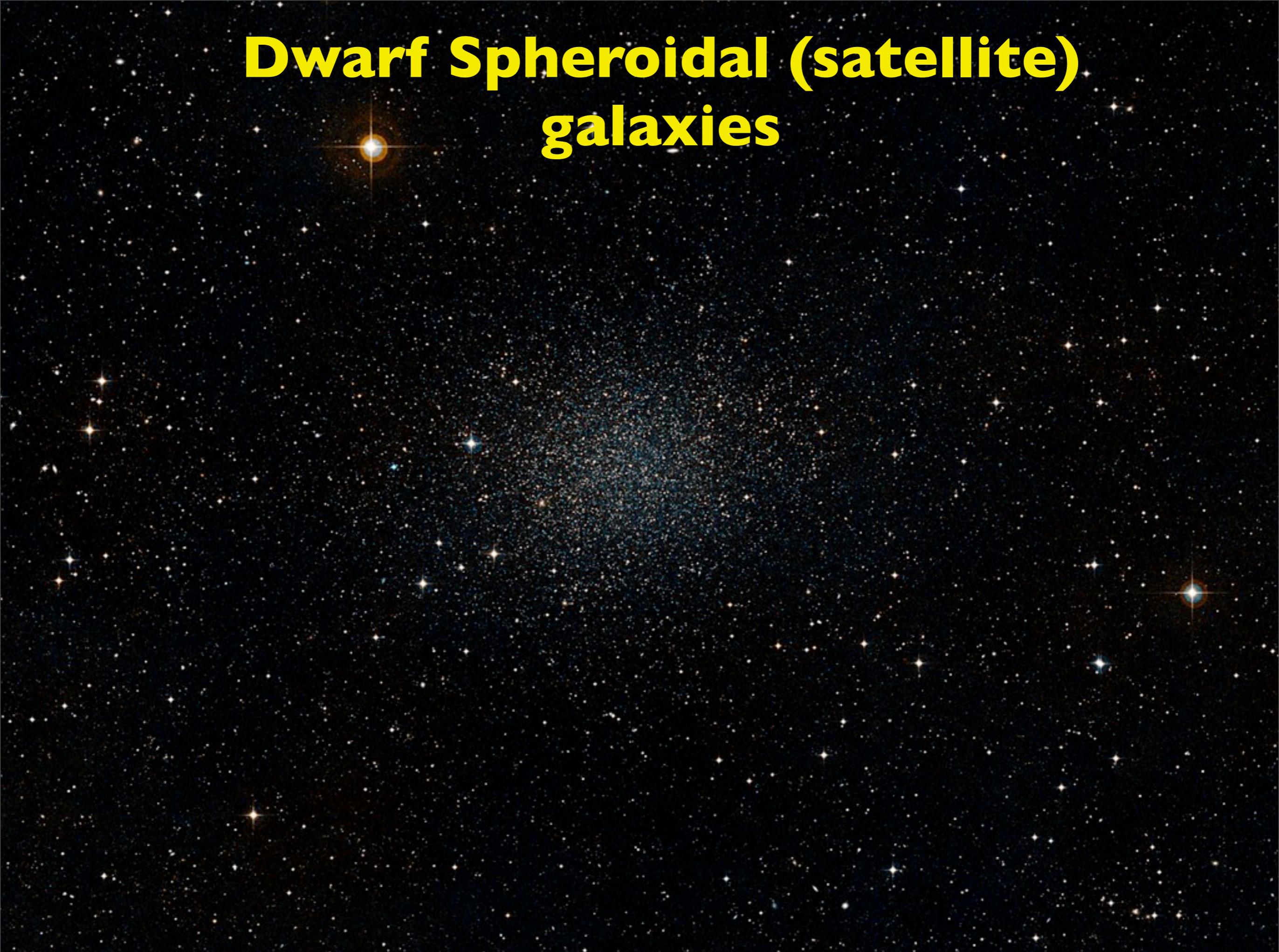
Inconclusive  
results ...



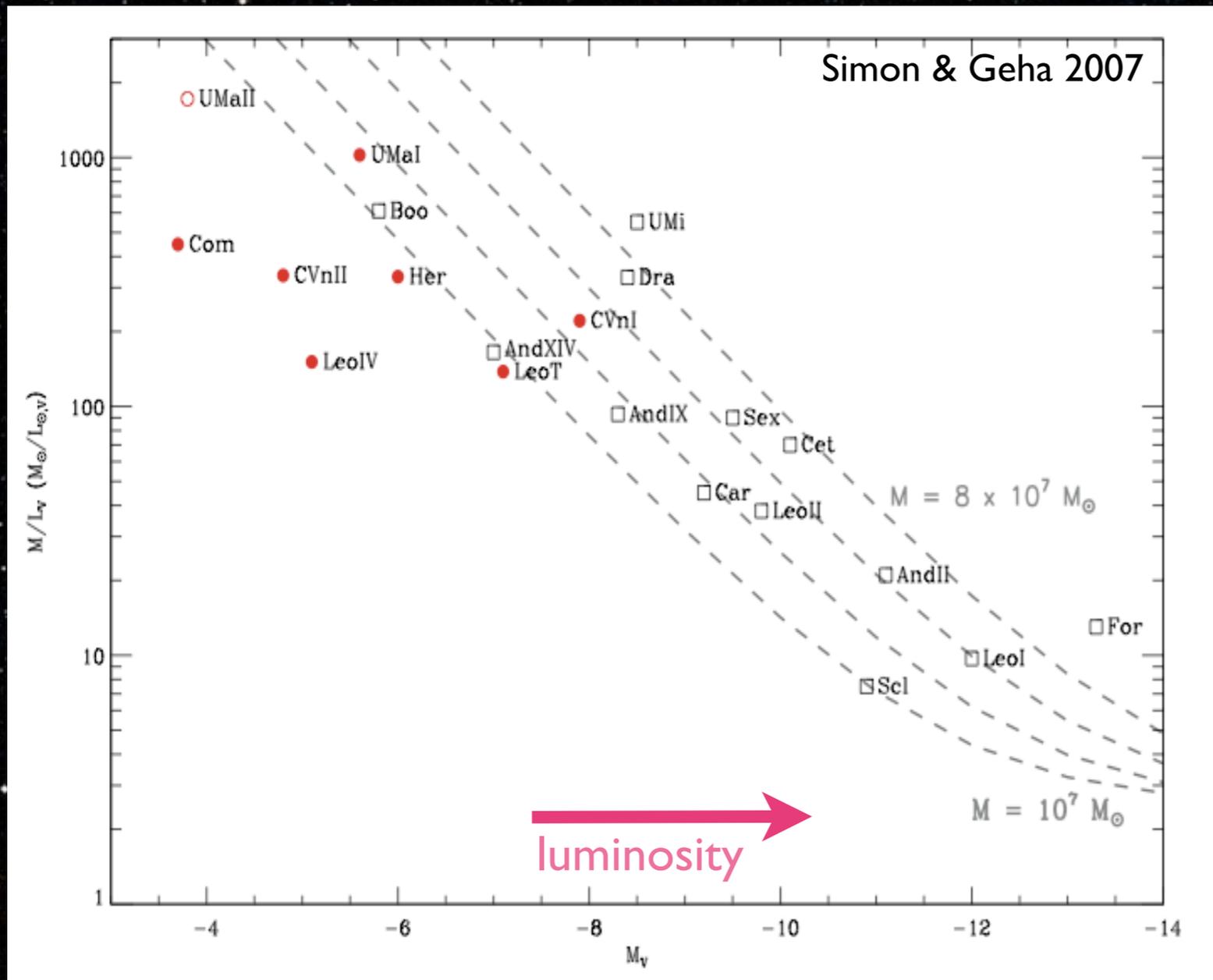
faint dSphs: incomplete sample  
Koposov+08; Tollerud+08

8 bright dSphs

# Dwarf Spheroidal (satellite) galaxies



# Dwarf Spheroidal (satellite) galaxies



★ Faintest galaxies in the known Universe:

$$10^3 < L/L_{\text{sol}} < 10^7$$

★ High mass-to-light ratios:

$$10 < M/L < 1000$$

(Potential dominated by DM)

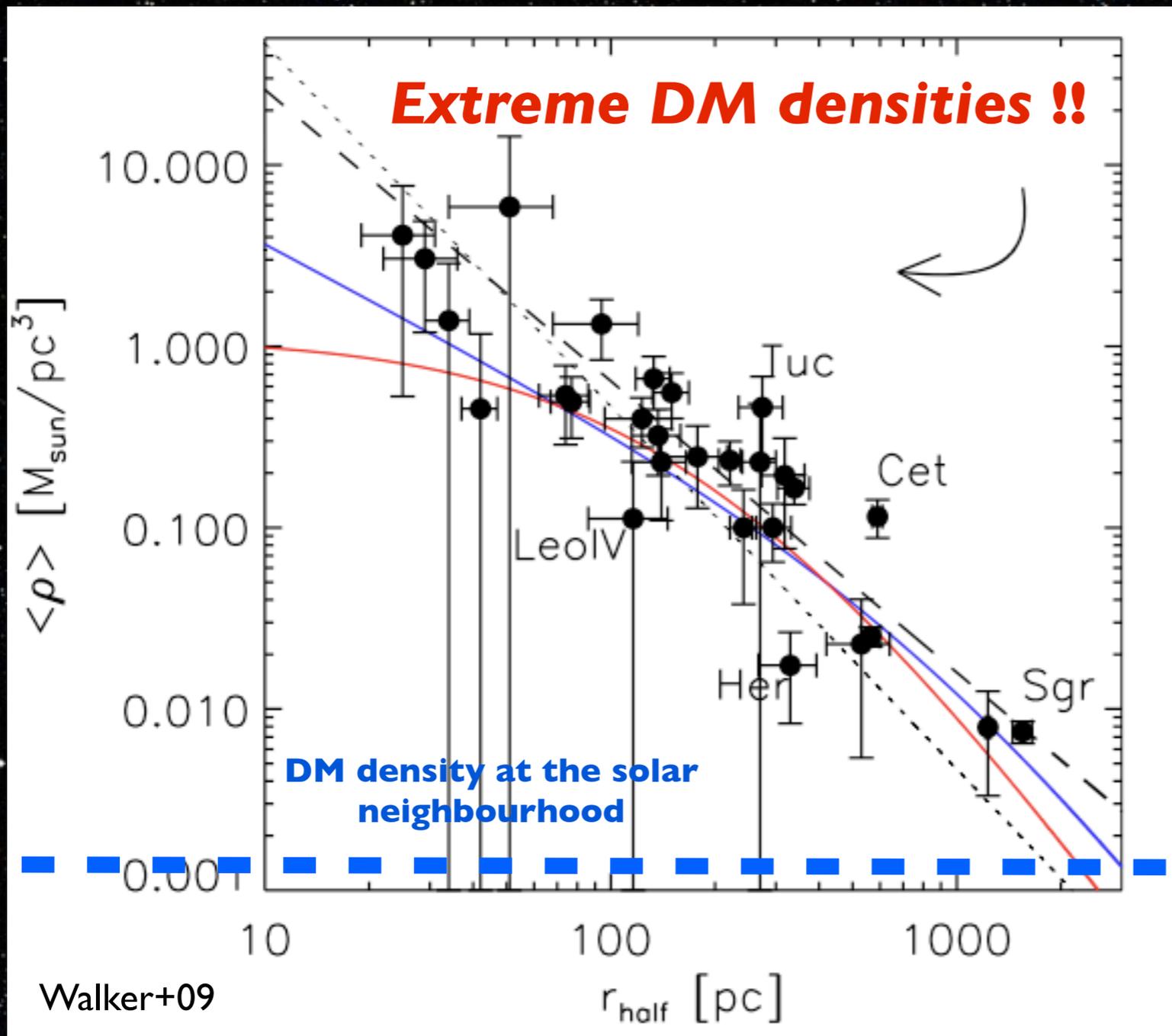
★ Old, metal poor stellar populations

$$0.1 < \text{age/Gyr} < 12$$

★ No gas

★ No rotation (pressure-supported)

# Dwarf Spheroidal (satellite) galaxies



★ Faintest galaxies in the known Universe:

$$10^3 < L/L_{\text{sol}} < 10^7$$

★ High mass-to-light ratios:

$$10 < M/L < 1000$$

(Potential dominated by DM)

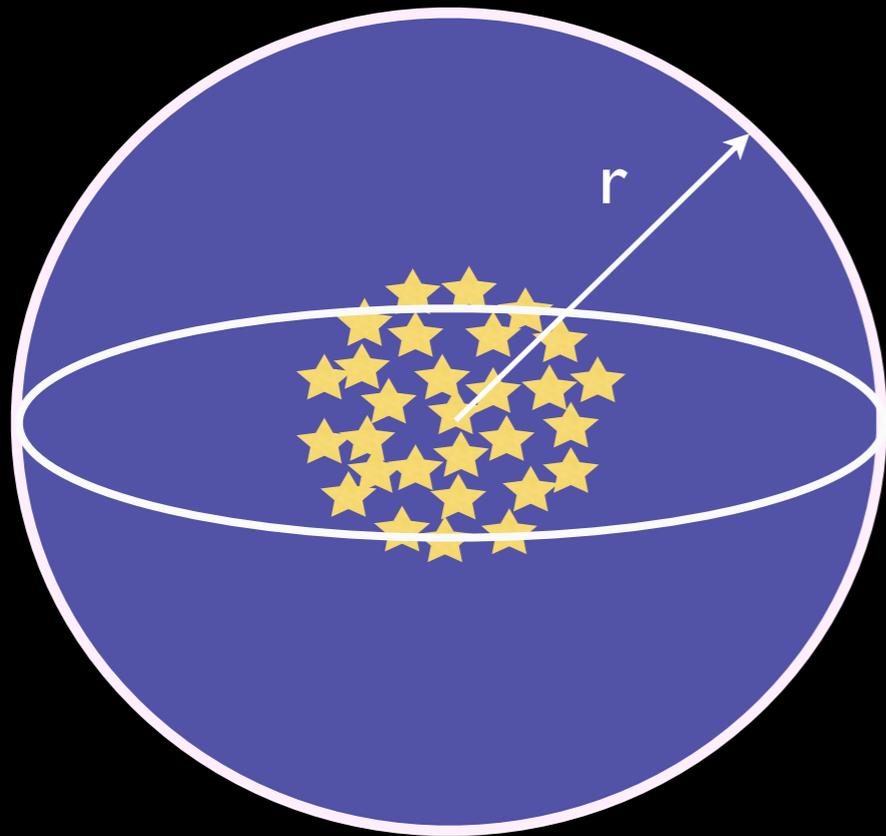
★ Old, metal poor stellar populations

$$0.1 < \text{age}/\text{Gyr} < 12$$

★ No gas

★ No rotation (pressure-supported)

# Talk overview



**stars**  $\equiv$  mass-loss tracers of the  
**DM potential**

## dwarf spheroidal galaxies

1- Existence of “dark” substructures  
*missing sat. problem*

2- DM distribution in galactic haloes  
*core/cusp problem*

# “dark” substructures in dSphs

- \* dSphs have virial masses  
 $M_{\text{vir}} \approx 10^9 M_{\text{sol}}$

Strigari+07; Peñarrubia+08; Walker+09; Wolf+09

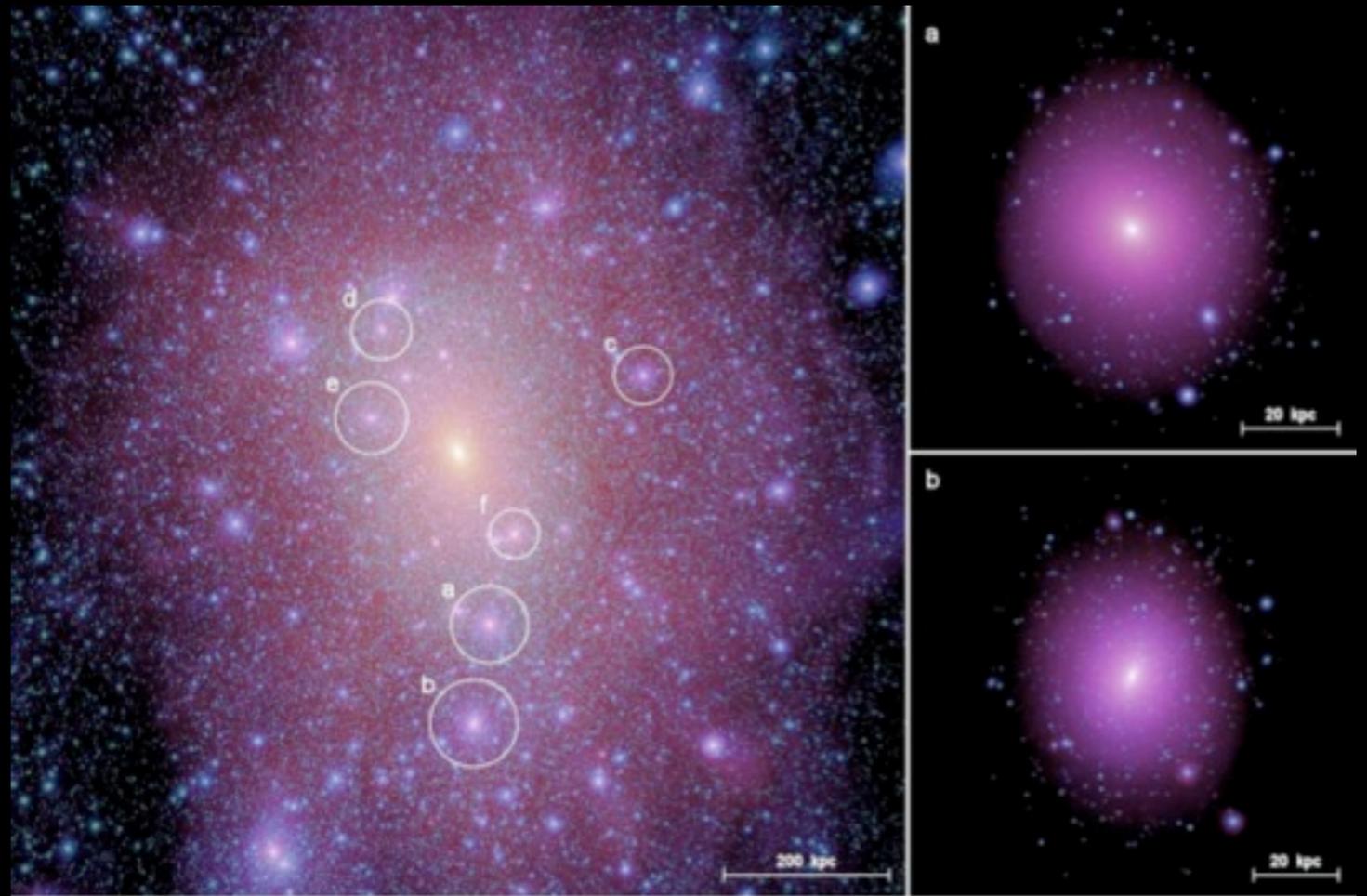
- \* CDM mass function:

$$dN/dm \propto m^{-1.9}$$

NFW97; Diemand+07; Springel+08



- DM **substructures** in dSphs  
have  $m \approx 0.01 M_{\text{vir}} \sim 10^7 M_{\text{sol}}$   
i.e. they are “**dark**”



sub-sub haloes in CDM simulations (Springel+08)

# “dark” substructures in dSphs

- \* dSphs have virial masses  $M_{\text{vir}} \lesssim 10^9 M_{\text{sol}}$

Strigari+07; Peñarrubia+08; Walker+09; Wolf+09

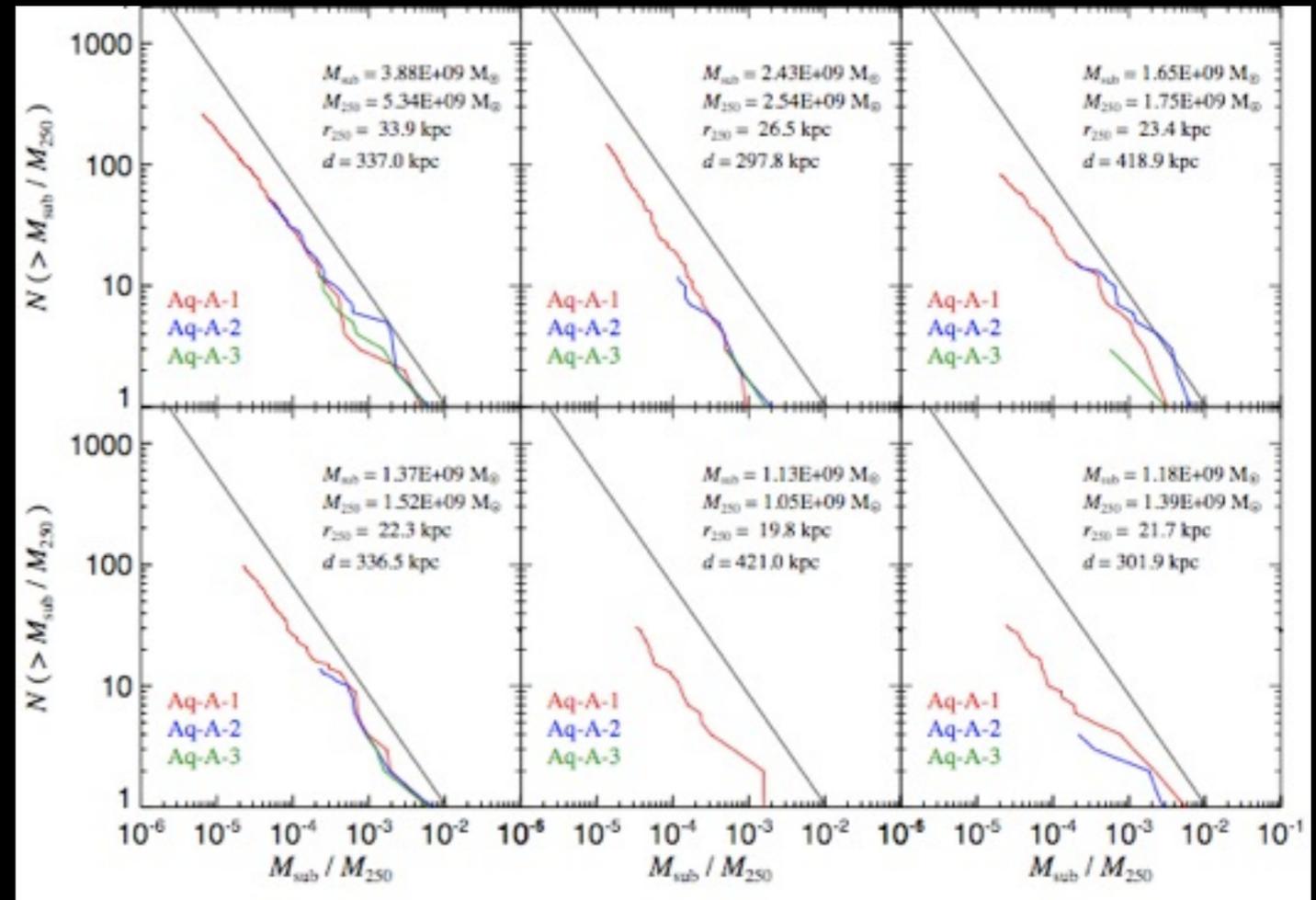
- \* CDM mass function:

$$dN/dm \propto m^{-1.9}$$

NFW97; Diemand+07; Springel+08

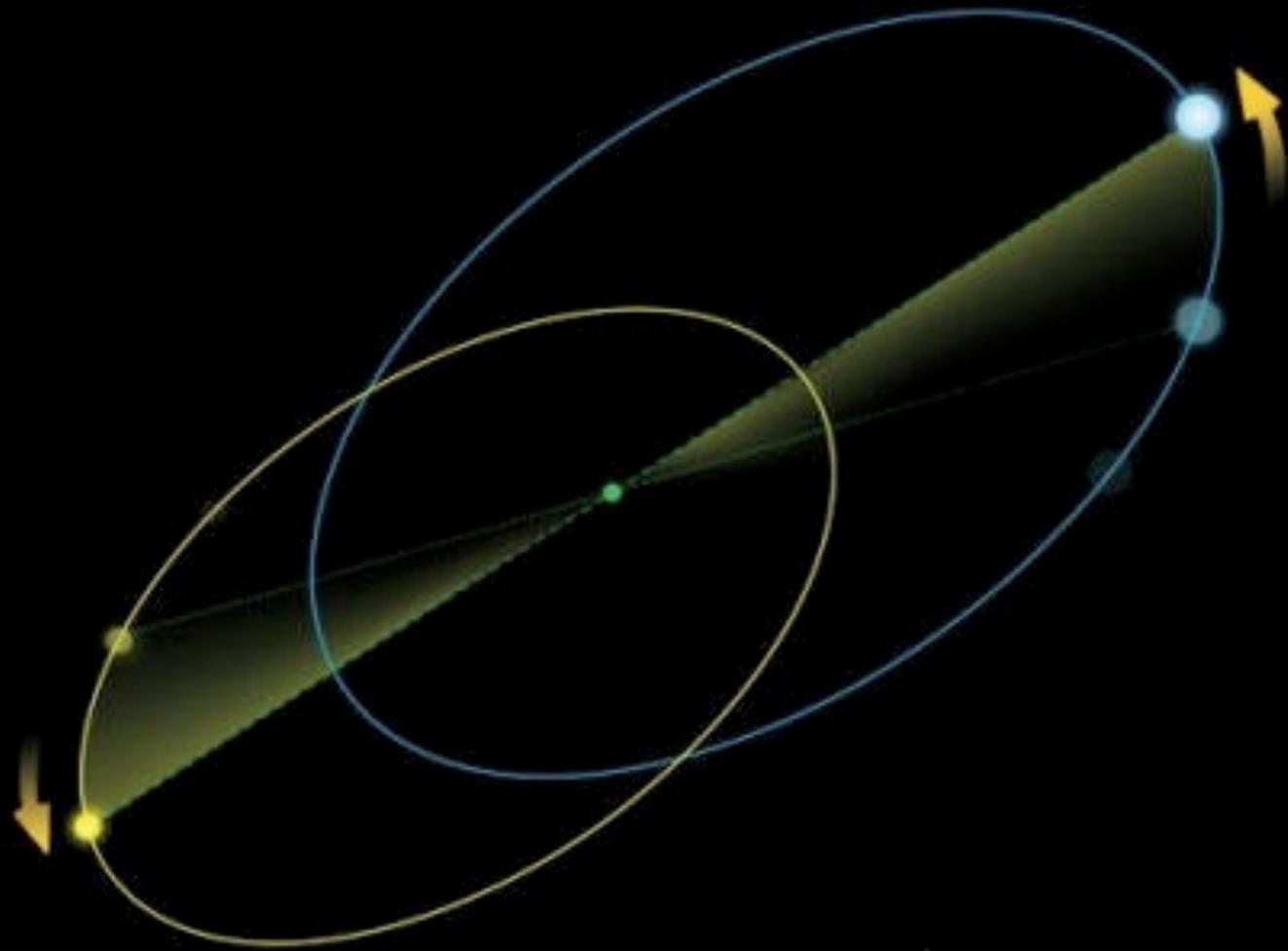


- DM **substructures** in dSphs have  $m \lesssim 0.01 M_{\text{vir}} \sim 10^7 M_{\text{sol}}$   
i.e. they are “**dark**”



sub-sub haloes in CDM simulations (Springel+08)

# Disruption of binary stars by “dark” substructures



Wide binaries have very  
low binding energies

$$E = - G M_b / 2a$$

small tidal perturbations can  
disrupt these systems



Probes of **clumpiness**  
in the galaxy potential

e.g MACHOS in the MW halo: Carr & Sakellariadou (1999);  
Chaname & Gould (2004)

# Disruption of binary stars by “dark” substructures

$$\langle \Delta E \rangle = \frac{7G^2 M_p^2 a^2}{3V_{\text{rel}}^2 b^4} U(b/r_h);$$

mean change of energy after  
encounter with DM sub-subhalo

$$U(b/r_h) \approx 1 \quad \text{non-penetrating encounters}$$

stellar halo of the MW:  $V_{\text{rel}} \sim \sqrt{2} \times 160 \text{ km/s}$   
dSphs  $V_{\text{rel}} \sim \sqrt{2} \times 10 \text{ km/s}$

“**Catastrophic**” encounters:  $\frac{\langle \Delta E \rangle}{E_b} > 1 \rightarrow M_p > M_{p,\text{crit}}$

$$M_{p,\text{crit}} \approx 2M_{\odot} \frac{V_{\text{rel}}}{\sqrt{2} \cdot 10\text{kms}^{-1}} \left( \frac{M_b}{1M_{\odot}} \frac{a}{0.1\text{pc}} \right)^{1/2};$$

# Disruption of binary stars by “dark” substructures

Analytically we expect binaries with  $a > a_{\max}$  to be disrupted

$$a_{\max} \equiv \left( \frac{k_{\text{cat}}}{G \rho_p \Delta t} \right)^{2/3} (GM_b)^{1/3};$$

$$\left\{ \begin{array}{l} k_{\text{cat}} \simeq 0.07 \quad (\text{Bahcall+85}) \\ \Delta t \equiv t_{\text{now}} - t_{\text{form}} \\ \rho_p = \frac{f_{\text{sub}} M_{\text{vir}}}{4\pi/3 R_b^3} \quad \text{Density of sub-sub haloes} \end{array} \right.$$

CDM field haloes:  $f_{\text{sub}} \sim 10^{-2}$

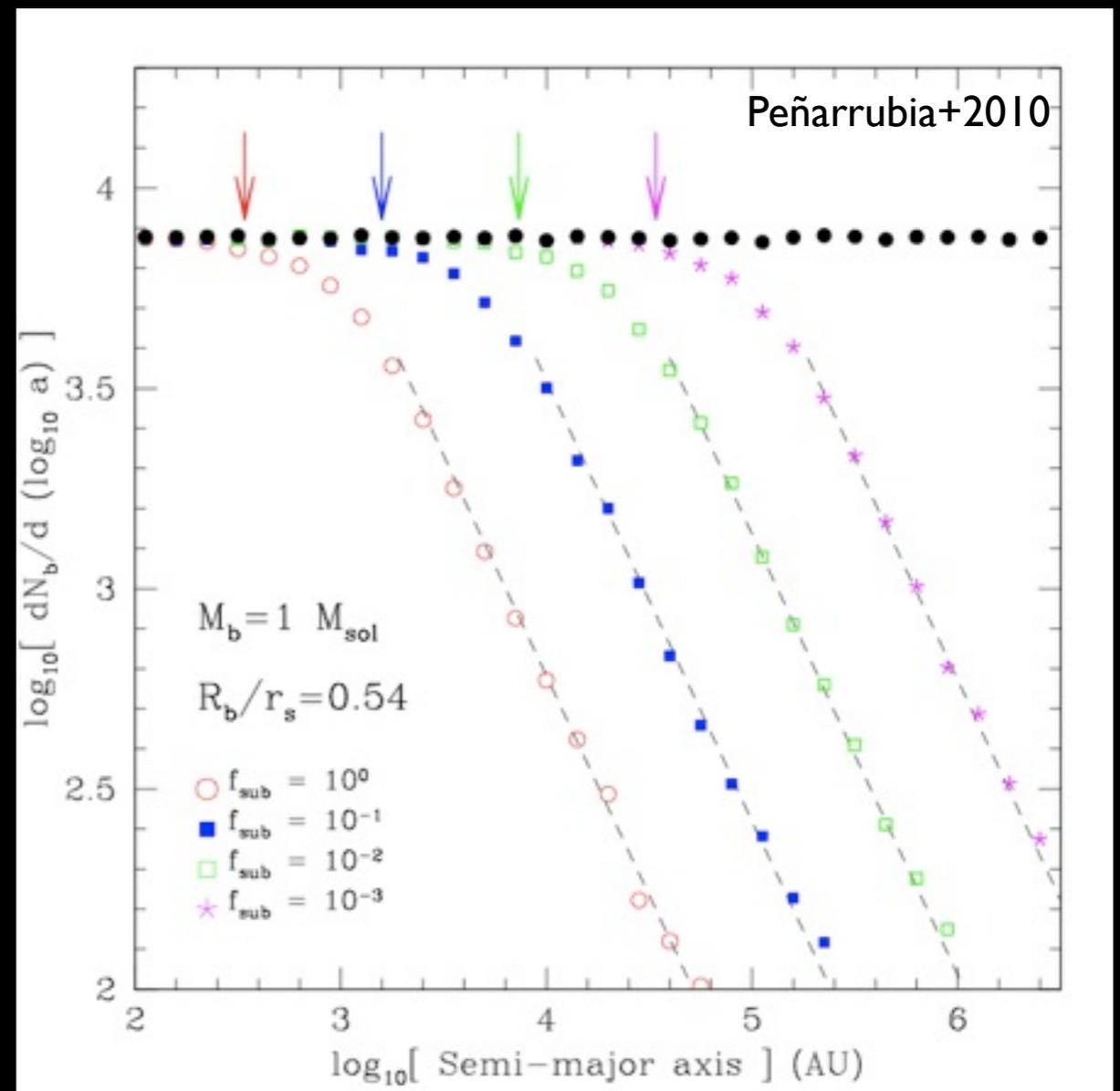
\*We expect a truncation in the binary separation function at

$$a_{\max} \sim 10^4 \text{ AU} \simeq 0.05 \text{ pc}$$

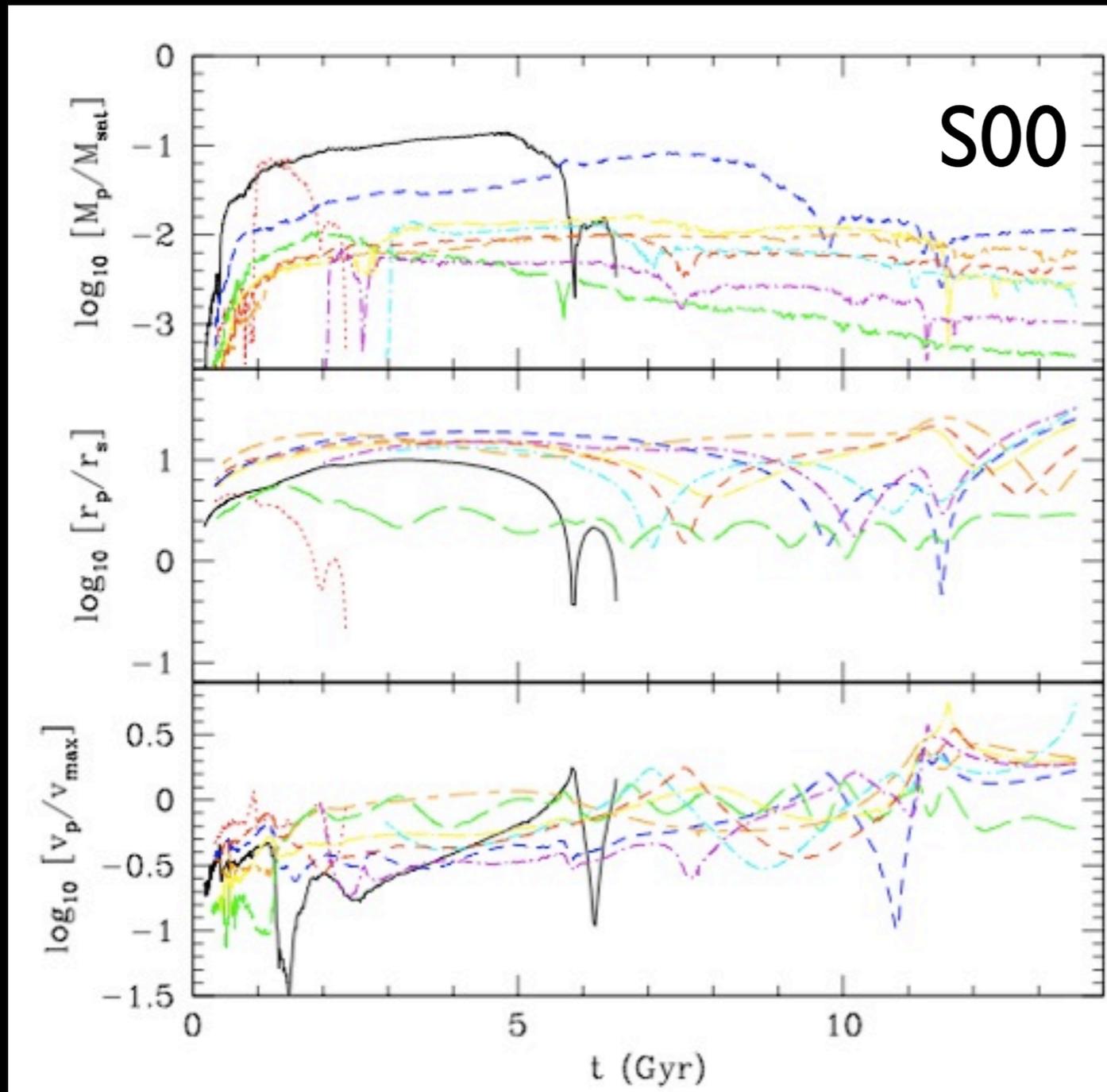
\*The perturbed separation function scales as

$$dN_b/da \propto a^{-2.1} \quad \text{for } a \gtrsim a_{\max}$$

Monte-Carlo/N-body simulations



# The Aquarius satellites



**Aquarius sims:** Assembly of a MW-like galaxy halo with  $5 \times 10^9$  particles (particle mass =  $10^4 M_{\text{sol}}$ )

Springel et al. (2008)



Position, velocity & mass of sub-subhaloes in satellite haloes



Generate samples of binary stars in the host satellites

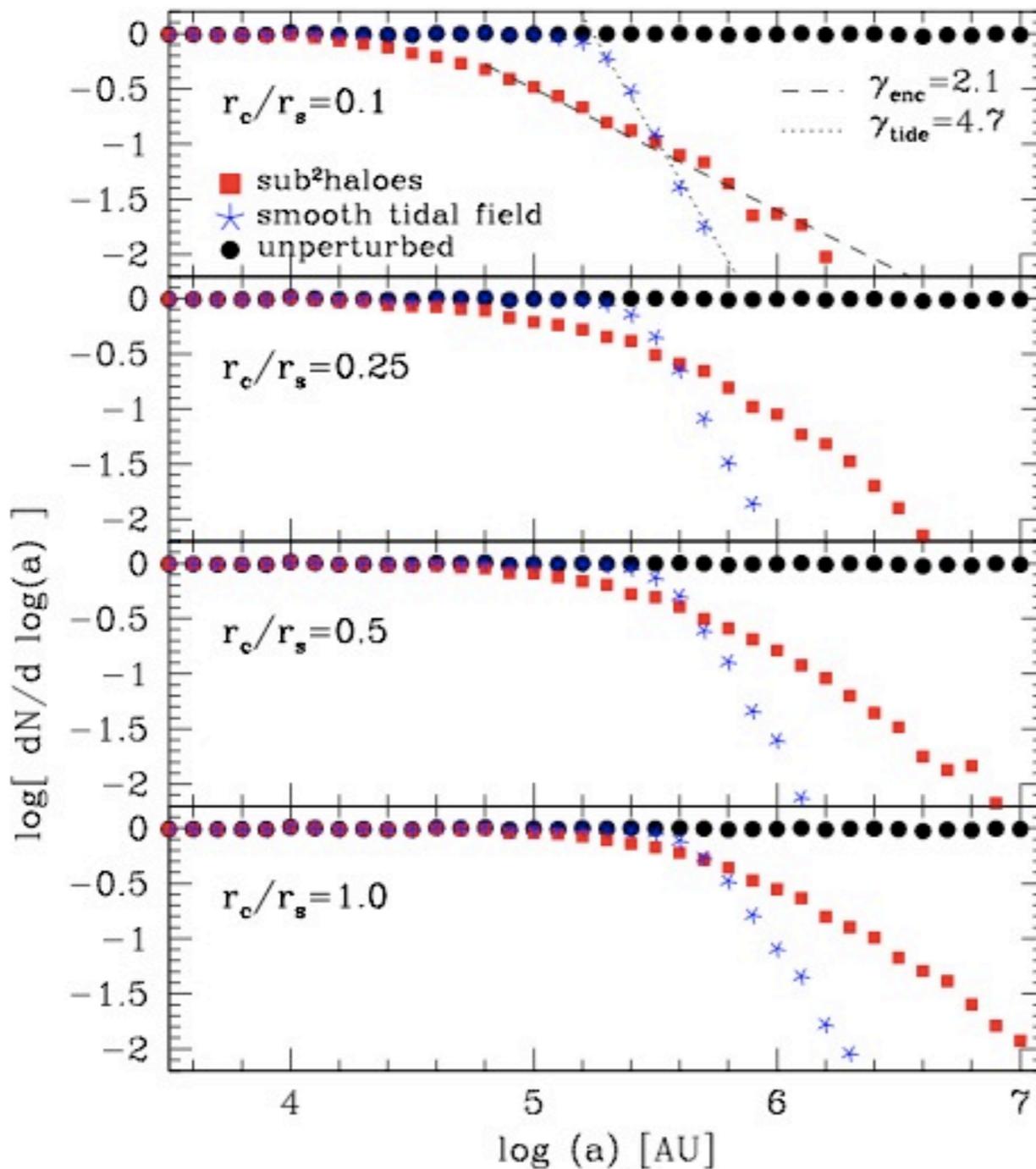
**Substructures:**  $\langle \Delta E \rangle = \frac{7G^2 M_p^2 a^2}{3V_{\text{rel}}^2 b^4} U(b/r_h);$

**Smooth field:**  $r_J(r) = \left[ \frac{M_b}{3M_{\text{sat}}(< r)} \right]^{1/3} r$

# The Aquarius satellites

**Aquarius sims:** Assembly of a MW-like galaxy halo with  $5 \times 10^9$  particles (particle mass =  $10^4 M_{\text{sol}}$ )

Springel et al. (2008)



Position, velocity & mass of sub-subhaloes in satellite haloes

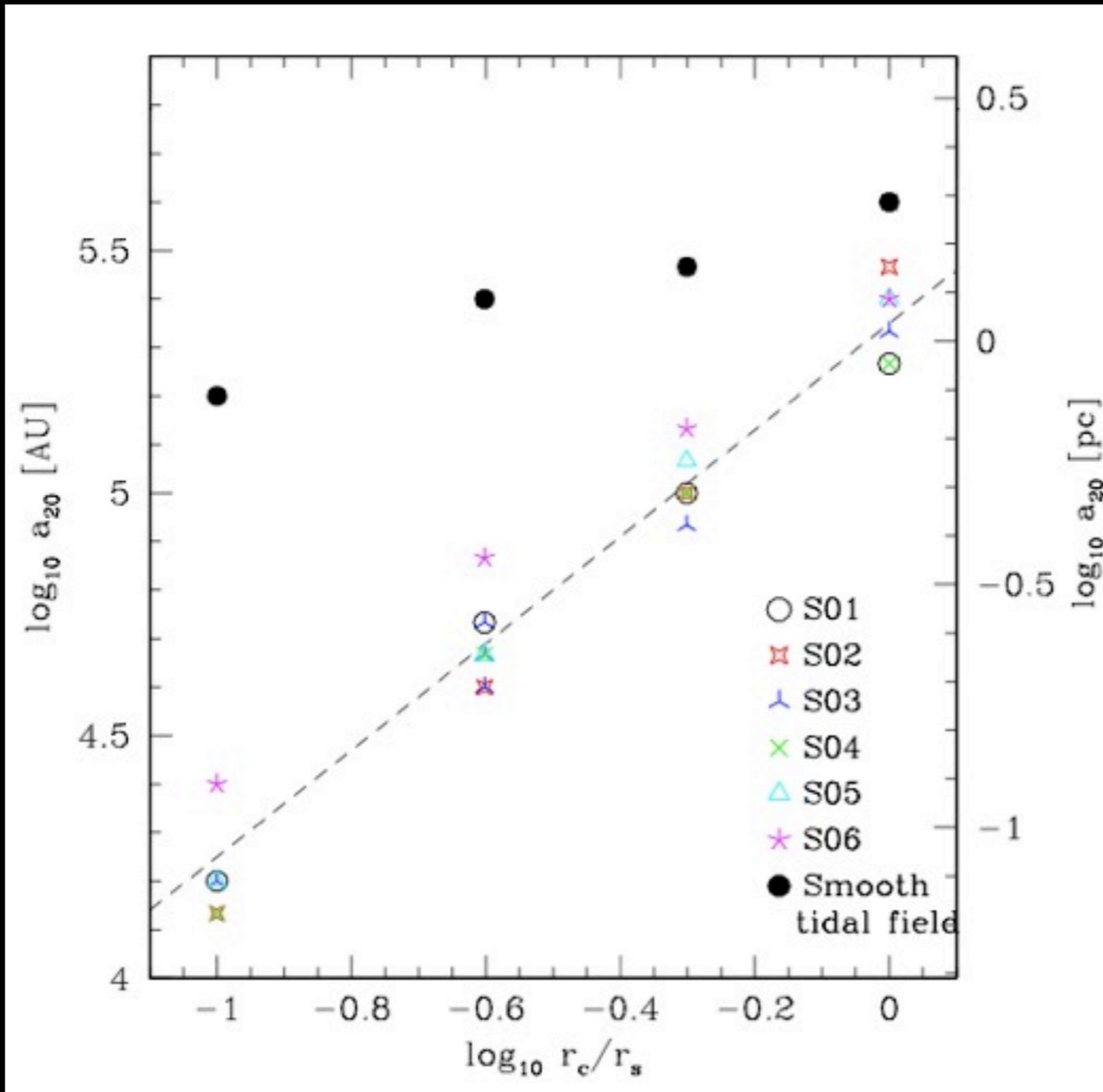


Generate samples of binary stars in the host satellites

**Substructures:**  $\langle \Delta E \rangle = \frac{7G^2 M_p^2 a^2}{3V_{\text{rel}}^2 b^4} U(b/r_h);$

**Smooth field:**  $r_J(r) = \left[ \frac{M_b}{3M_{\text{sat}}(< r)} \right]^{1/3} r$

# The Aquarius satellites



**Aquarius sims:** Assembly of a MW-like galaxy halo with  $5 \times 10^9$  particles (particle mass =  $10^4 M_{\text{sol}}$ )

Springel et al. (2008)



Position, velocity & mass of sub-subhaloes in satellite haloes



Generate samples of binary stars in the host satellites

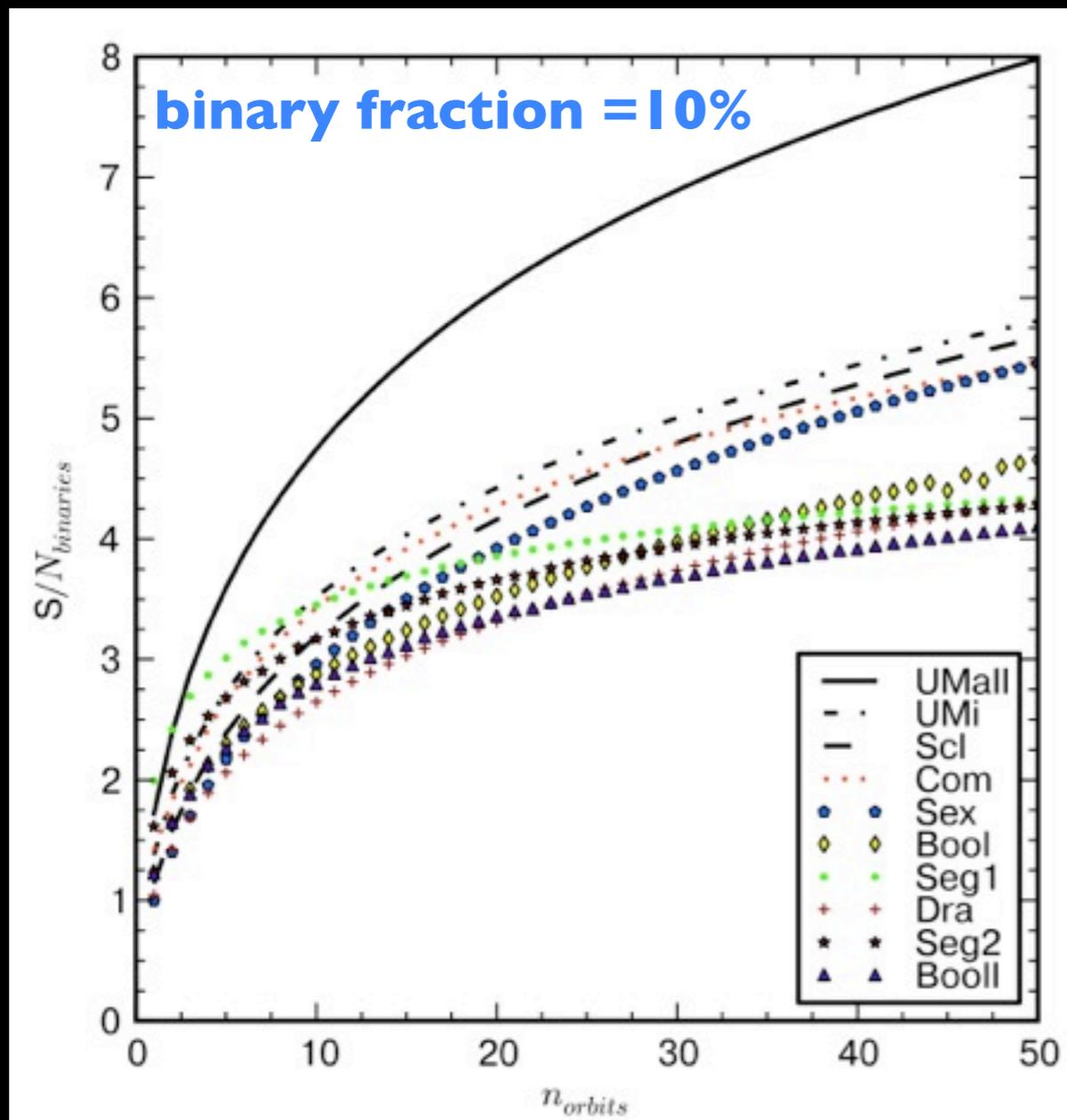
**Substructures:**  $\langle \Delta E \rangle = \frac{7G^2 M_p^2 a^2}{3V_{\text{rel}}^2 b^4} U(b/r_h);$

**Smooth field:**  $r_J(r) = \left[ \frac{M_b}{3M_{\text{sat}}(< r)} \right]^{1/3} r$

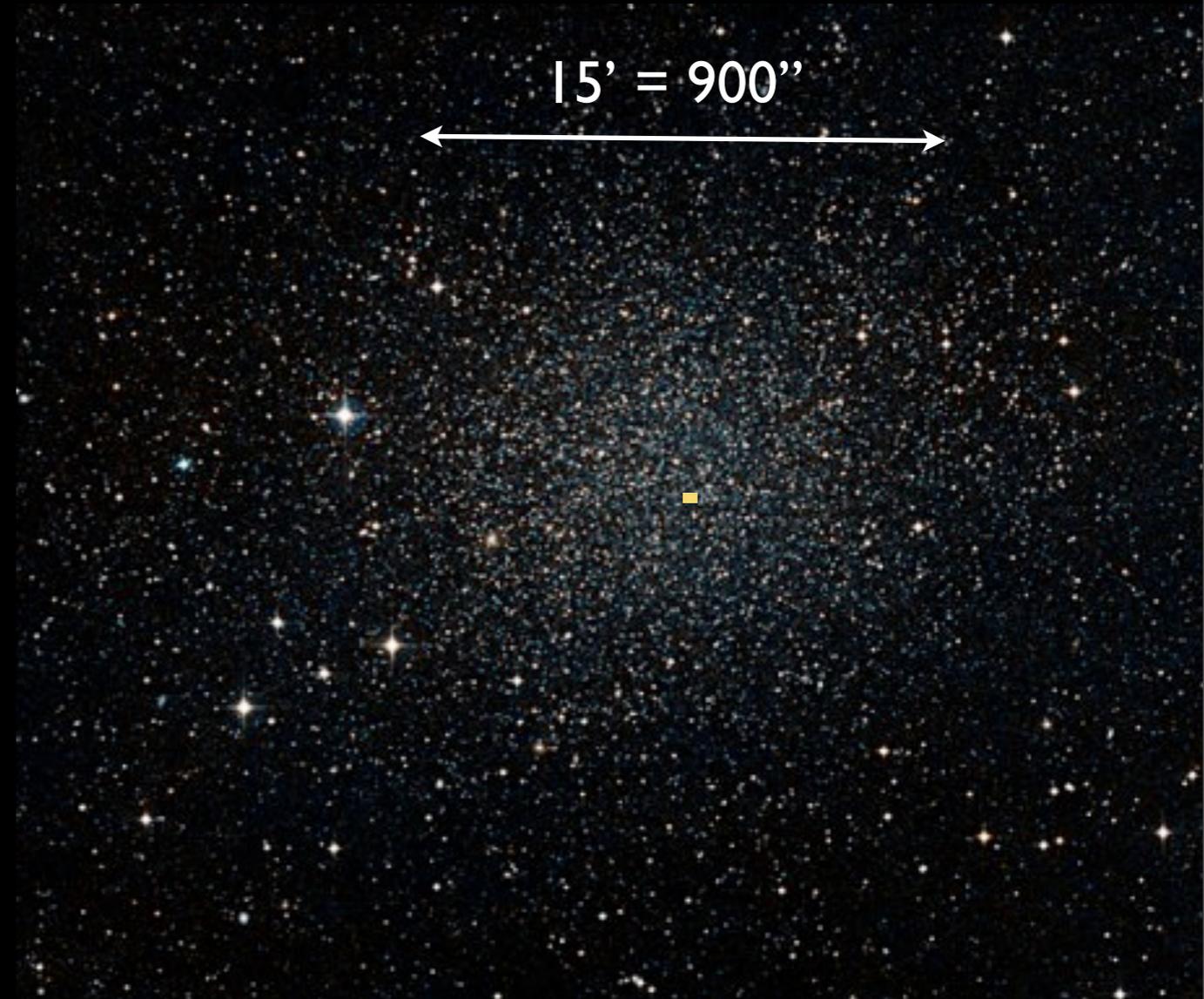
# Detection of binary stars in dSphs

challenging owing to their large heliocentric distance

- ACS camera on Hubble:
- resolution =  $4 \times 0.05''$  pixels
  - f.o.v =  $25'' \times 25''$
  - limiting magnitude =  $29^{\text{mag}}$



Peñarrubia+2010



# The inner structure of **Cold (?)** DM haloes

# The inner structure of **Cold (?)** DM haloes

Collision-less N-body sims. of  
structure formation

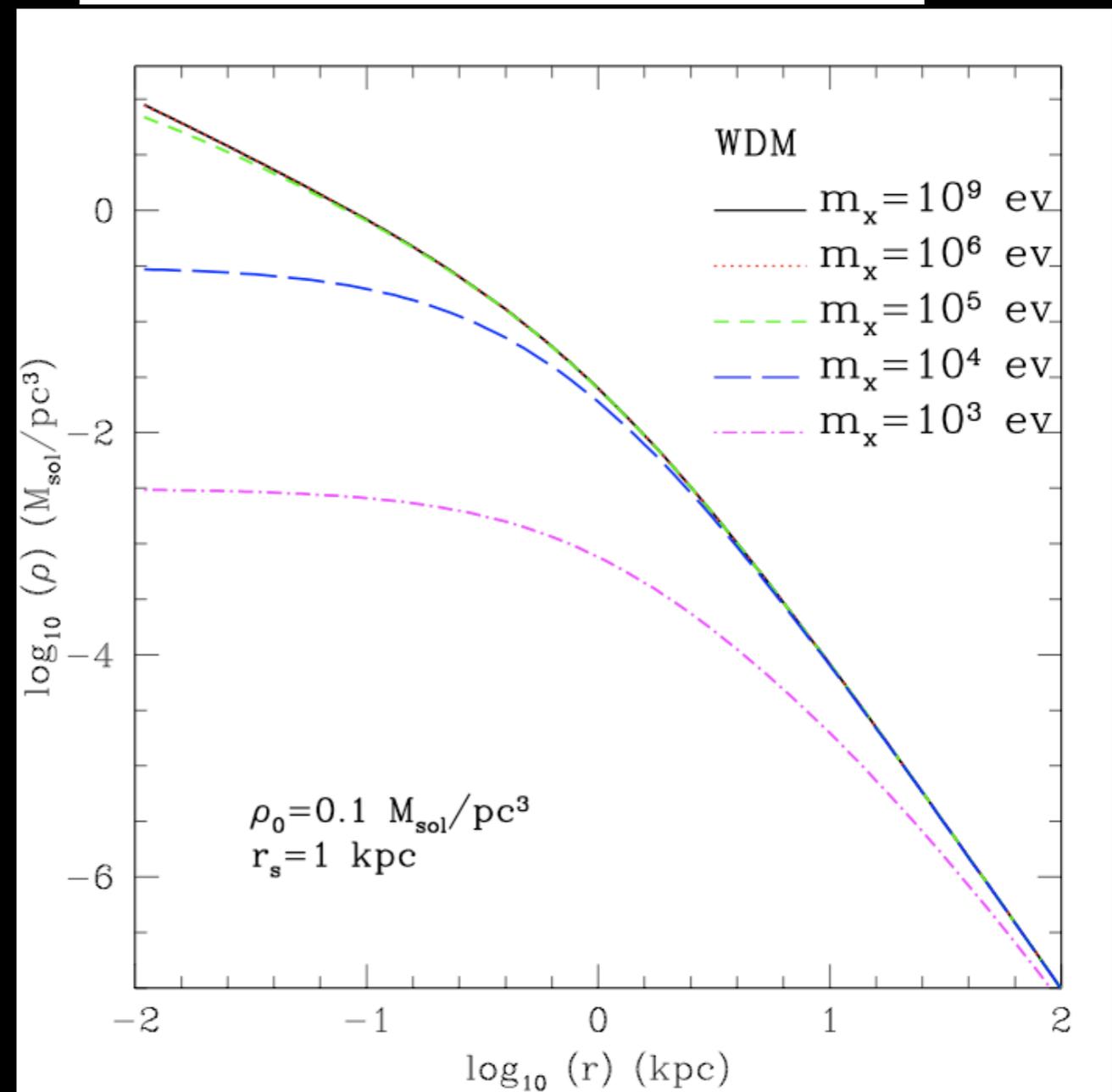


**CDM** haloes follow a universal  
density profile that **diverges** at  
 $r=0$  (**cusp**)

Dubinsky & Carlberg 91, NFW97,  
Moore+98, Diemand+ 05)

$$r_c > 32 \left( \frac{10 \text{ km s}^{-1}}{\sigma} \right)^{1/2} \left( \frac{\text{keV}}{m_X} \right)^2 \text{ pc} .$$

Bode+01



# Baryonic feedback

Baryons may alter the inner  
DM profile:

\*SNe-driven gas outflows

(Navarro+1996; Gnedin & Zhao 1992; Read & Gilmore 2005; Governato+2008, 2010)

\*SNe-induced resonant  
motion of bulk gas

(Mashchenko+2006, 2008)

\*Orbital decay of dense  
clusters

(El-Zant+2001; Goerdt+2008)

## THE FORMATION OF A BULGELESS GALAXY WITH A SHALLOW DARK MATTER CORE

Fabio Governato (University of Washington)  
Chris Brook (University of Central Lancashire)  
Lucio Mayer (ETH and University of Zurich)  
and the N-Body Shop

KEY: Blue: gas density map. The brighter regions represent gas that is actively forming stars. The clock shows the time from the Big Bang. The frame is 50,000 light years across.

Simulations were run on Columbia (NASA Advanced Supercomputing Center) and at ARSC

$L \sim 10^9 L_{\text{sol}}$ ;  $M \sim 10^{10} M_{\text{sol}}$

# Baryonic feedback

Baryons may alter the inner  
DM profile:

\*SNe-driven gas outflows

(Navarro+1996; Gnedin & Zhao 1992; Read & Gilmore 2005; Governato+2008, 2010)

\*SNe-induced resonant  
motion of bulk gas

(Mashchenko+2006, 2008)

\*Orbital decay of dense  
clusters

(El-Zant+2001; Goerdt+2008)

## THE FORMATION OF A BULGELESS GALAXY WITH A SHALLOW DARK MATTER CORE

Fabio Governato (University of Washington)  
Chris Brook (University of Central Lancashire)  
Lucio Mayer (ETH and University of Zurich)  
and the N-Body Shop

KEY: Blue: gas density map. The brighter regions represent gas that is actively forming stars. The clock shows the time from the Big Bang. The frame is 50,000 light years across.

Simulations were run on Columbia (NASA Advanced Supercomputing Center) and at ARSC

$L \sim 10^9 L_{\text{sol}}$ ;  $M \sim 10^{10} M_{\text{sol}}$

**Do those process affect dSphs?  
(100-1000 less luminous)**

# Baryonic feedback in CDM dSphs

## The baryons in the Milky Way satellites

O. H. Parry,<sup>1★</sup> V. R. Eke,<sup>1</sup> C. S. Frenk<sup>1</sup> and T. Okamoto<sup>1,2</sup>

<sup>1</sup>*Institute for Computational Cosmology, Department of Physics, University of Durham, Science Laboratories, South Road, Durham DH1 3LE*

<sup>2</sup>*Center for Computational Sciences, University of Tsukuba, 1-1-1 Tennodai, Tsukuba, 305-8577 Ibaraki, Japan*

Accepted 2011 October 9. Received 2011 September 29; in original form 2011 May 18

### ABSTRACT

We investigate the formation and evolution of satellite galaxies using smoothed particle hydrodynamics (SPH) simulations of a Milky Way (MW) like system, focusing on the best resolved examples, analogous to the classical MW satellites. Comparing with a pure dark matter simulation, we find that the condensation of baryons has had a relatively minor effect on the structure of the satellites' dark matter haloes. The stellar mass that forms in each satellite agrees relatively well over three levels of resolution (a factor of  $\sim 64$  in particle mass) and scales with (sub)halo mass in a similar way in an independent semi-analytical model. Our model provides a relatively good match to the average luminosity function of the MW and M31. To establish whether the potential wells of our satellites are realistic, we measure their masses within observationally determined half-light radii, finding that they have somewhat higher mass-to-light ratios than those derived for the MW dSphs from stellar kinematic data; the most massive examples are most discrepant. A statistical test yields an  $\sim 6$  per cent probability that the simulated and observationally derived distributions of masses are consistent. If the satellite population of the MW is typical, our results could imply that feedback processes not properly captured by our simulations have reduced the central densities of subhaloes, or that they initially formed with lower concentrations, as would be the case, for example, if the dark matter were made of warm, rather than cold particles.

Same results found independently by  
Sawala, Scannapieco, Maio & White (2010)

# The inner structure of Cold (?) DM haloes



## Jeans equations

$$\frac{1}{v} \frac{d}{dr} (v \bar{v}_r^2) + 2 \frac{\beta \bar{v}_r^2}{r} = - \frac{GM(r)}{r^2},$$

- \* Halo mass profile
- \* stellar density profile

**stars**  $\equiv$  mass-loss tracers of the  
**DM potential**

# The inner structure of Cold (?) DM haloes



**stars**  $\equiv$  mass-loss tracers of the  
**DM potential**

## Jeans equations

$$\frac{1}{v} \frac{d}{dr} (\overline{v v_r^2}) + 2 \frac{\beta \overline{v_r^2}}{r} = - \frac{GM(r)}{r^2},$$

- \* Halo mass profile
- \* stellar density profile
- \* radial component of the velocity dispersion

# The inner structure of Cold (?) DM haloes



**stars**  $\equiv$  mass-loss tracers of the  
**DM potential**

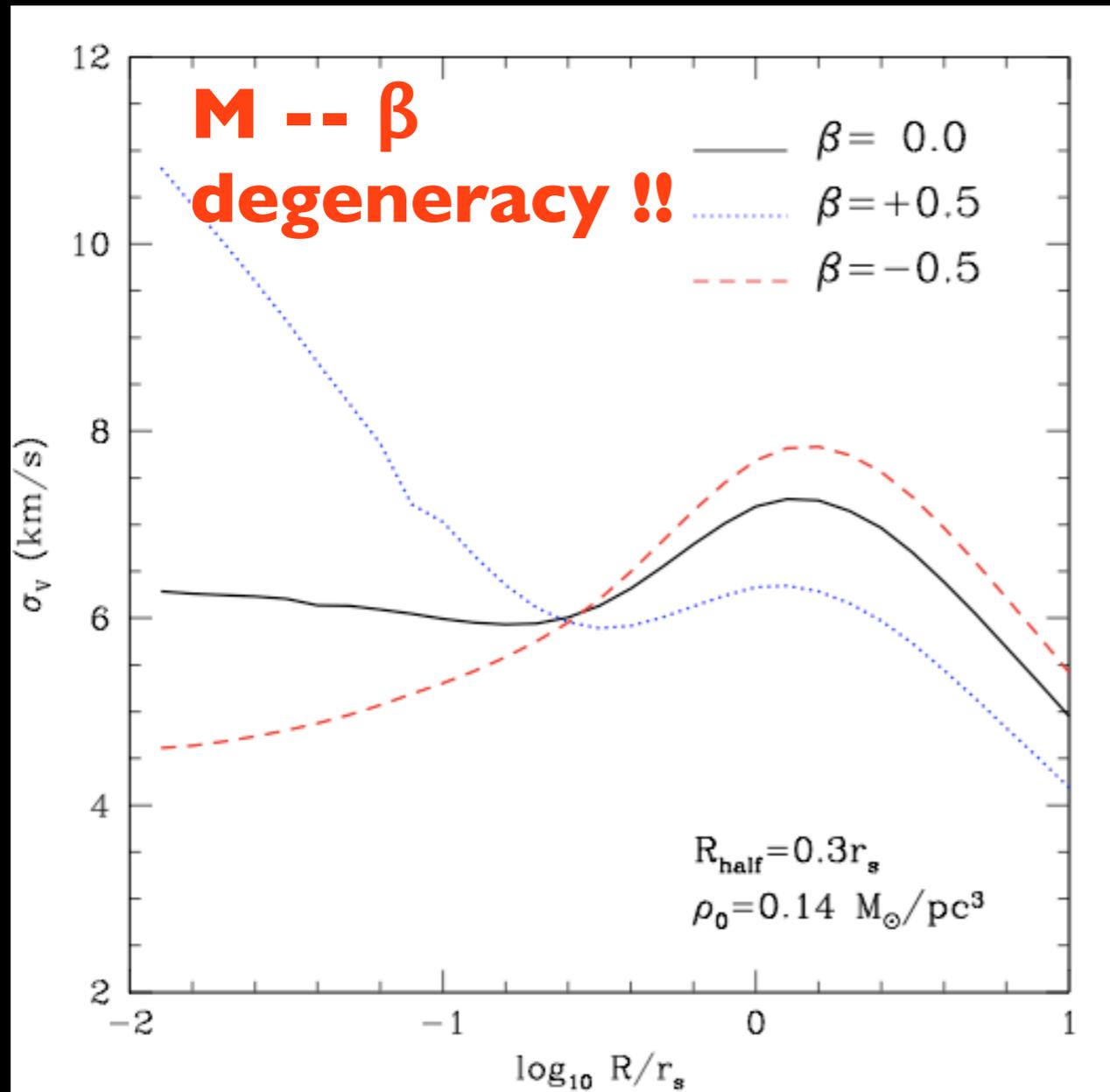
## Jeans equations

$$\frac{1}{v} \frac{d}{dr} (v \bar{v}_r^2) + 2 \frac{\beta v^2}{r} = - \frac{GM(r)}{r^2},$$

- \* Halo mass profile
- \* stellar density profile
- \* radial component of the velocity dispersion
- \* velocity anisotropy  $\beta \equiv 1 - \sigma_t^2 / \sigma_r^2$

# The inner structure of Cold (?) DM haloes

## Jeans equations



$$\frac{1}{v} \frac{d}{dr} (v \bar{v}_r^2) + 2 \frac{\beta v^2}{r} = - \frac{GM(r)}{r^2},$$

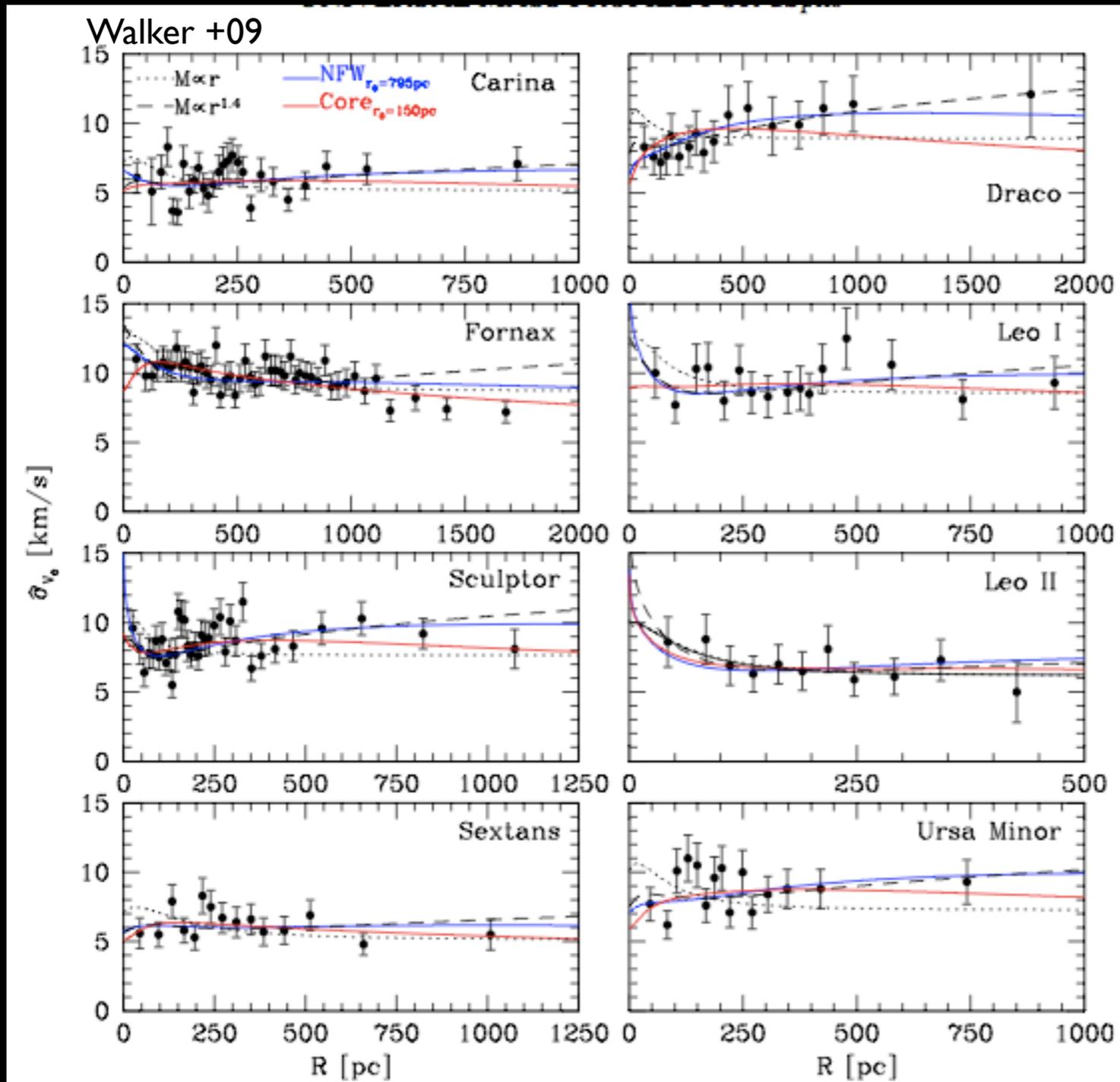
- \* Halo mass profile
- \* stellar density profile
- \* radial component of the velocity dispersion
- \* velocity anisotropy  $\beta \equiv 1 - \sigma_t^2 / \sigma_r^2$

## Projected velocity dispersion

$$\sigma_p^2(R) = \frac{2}{I(R)} \int_R^{\infty} \left( 1 - \beta \frac{R^2}{r^2} \right) \frac{v \bar{v}_r^2 r}{\sqrt{r^2 - R^2}} dr.$$

# DM cusps?

— NFW profile  
— cored profile



Unknown  $\beta(r)$



Unknown  $M(r)$

e.g. Battaglia+08; Walker+09

**Can we break  
the degeneracy?**

# THE IDEA

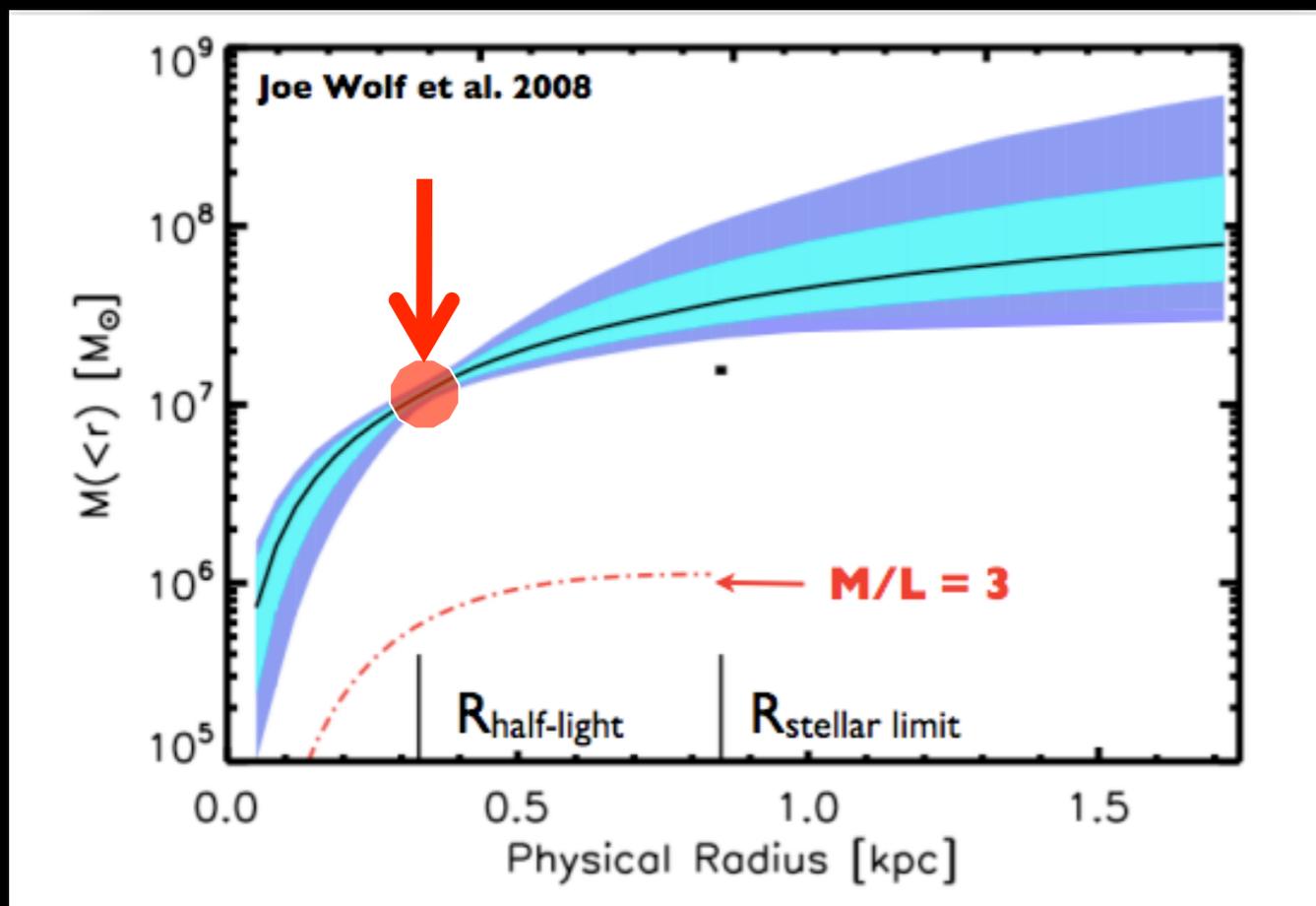
Walker & Peñarrubia (2011)

# THE IDEA

Walker & Peñarrubia (2011)

**M --  $\beta$  degeneracy breaks at  $R \approx R_{\text{half}}$**

Peñarrubia+08; Walker+09; Wolf+10; Amorisco & Evans 2010



$$M(R_{\text{half}}) \approx \mu R_{\text{half}} \langle \sigma_V \rangle^2$$

$$\mu \approx 480 M_{\odot} \text{pc}^{-1} \text{km}^{-2} \text{s}^{-2} \quad (\text{Walker+09})$$

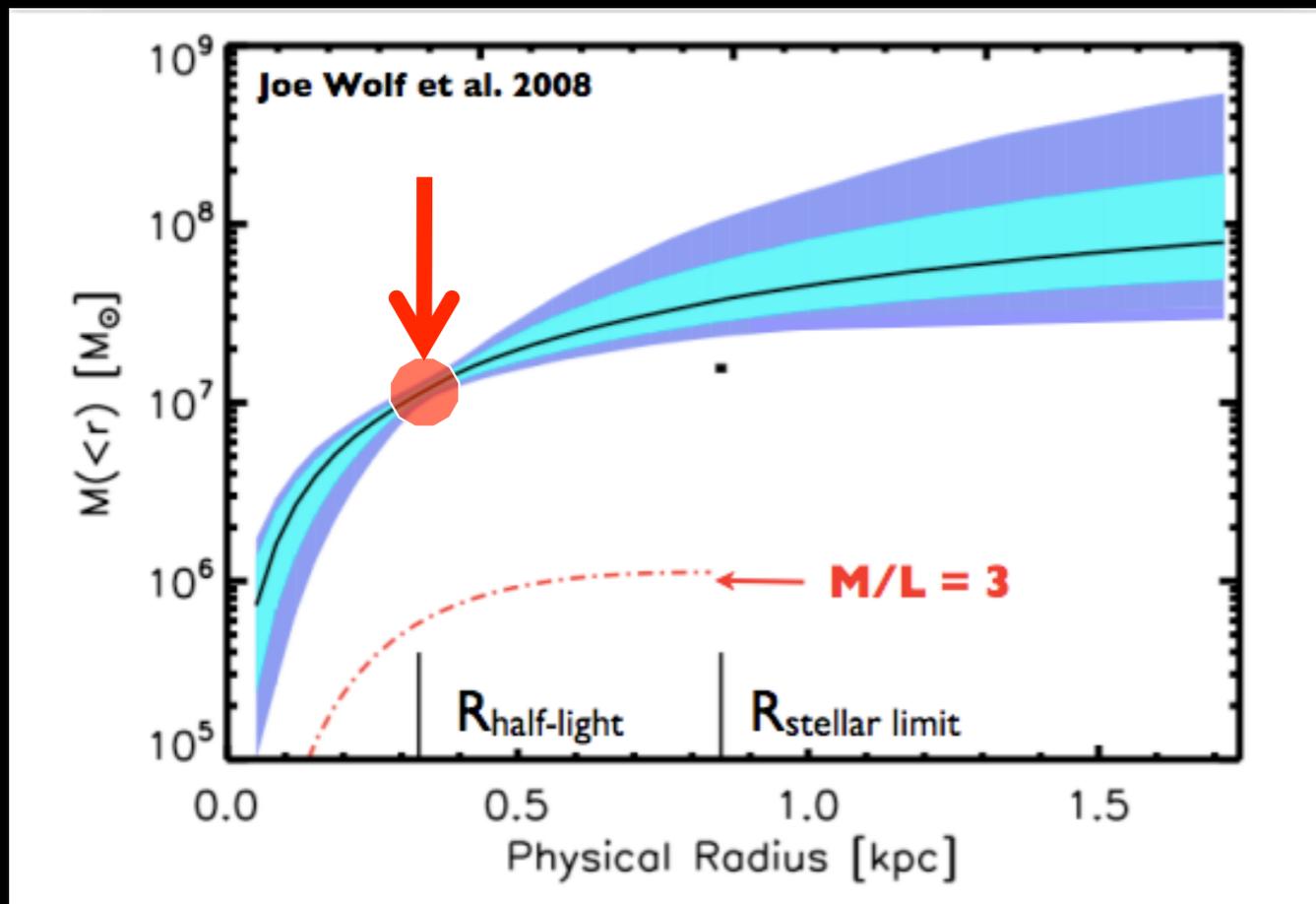
# THE IDEA

Walker & Peñarrubia (2011)

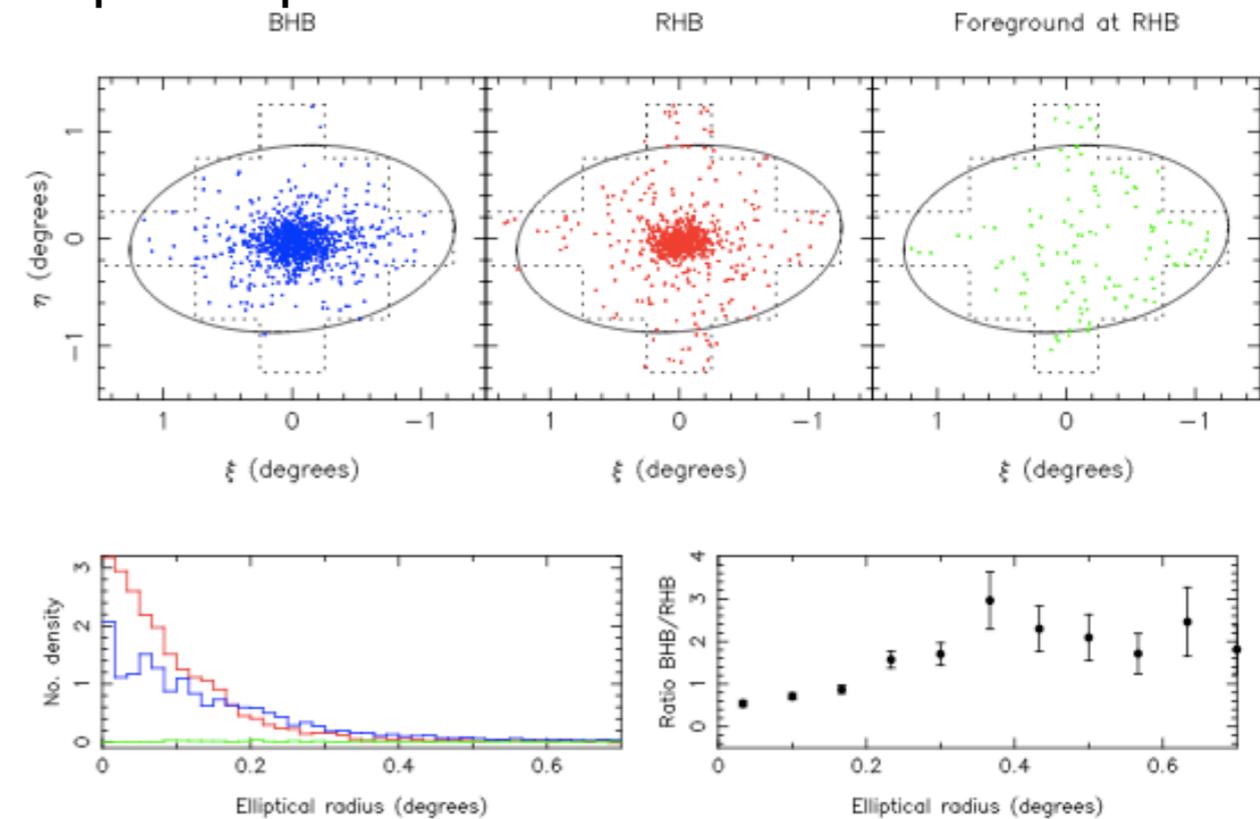
**M --  $\beta$  degeneracy breaks at  $R \approx R_{\text{half}}$**

Peñarrubia+08; Walker+09; Wolf+10; Amorisco & Evans 2010

Some dSphs show spatially + kinematically distinct stellar components



Sculptor dSph



$$M(R_{\text{half}}) \approx \mu R_{\text{half}} \langle \sigma_V \rangle^2$$

Tolstoy + 04 (see also Battaglia+08)

$$\mu \approx 480 M_{\odot} \text{pc}^{-1} \text{km}^{-2} \text{s}^{-2} \quad (\text{Walker+09})$$

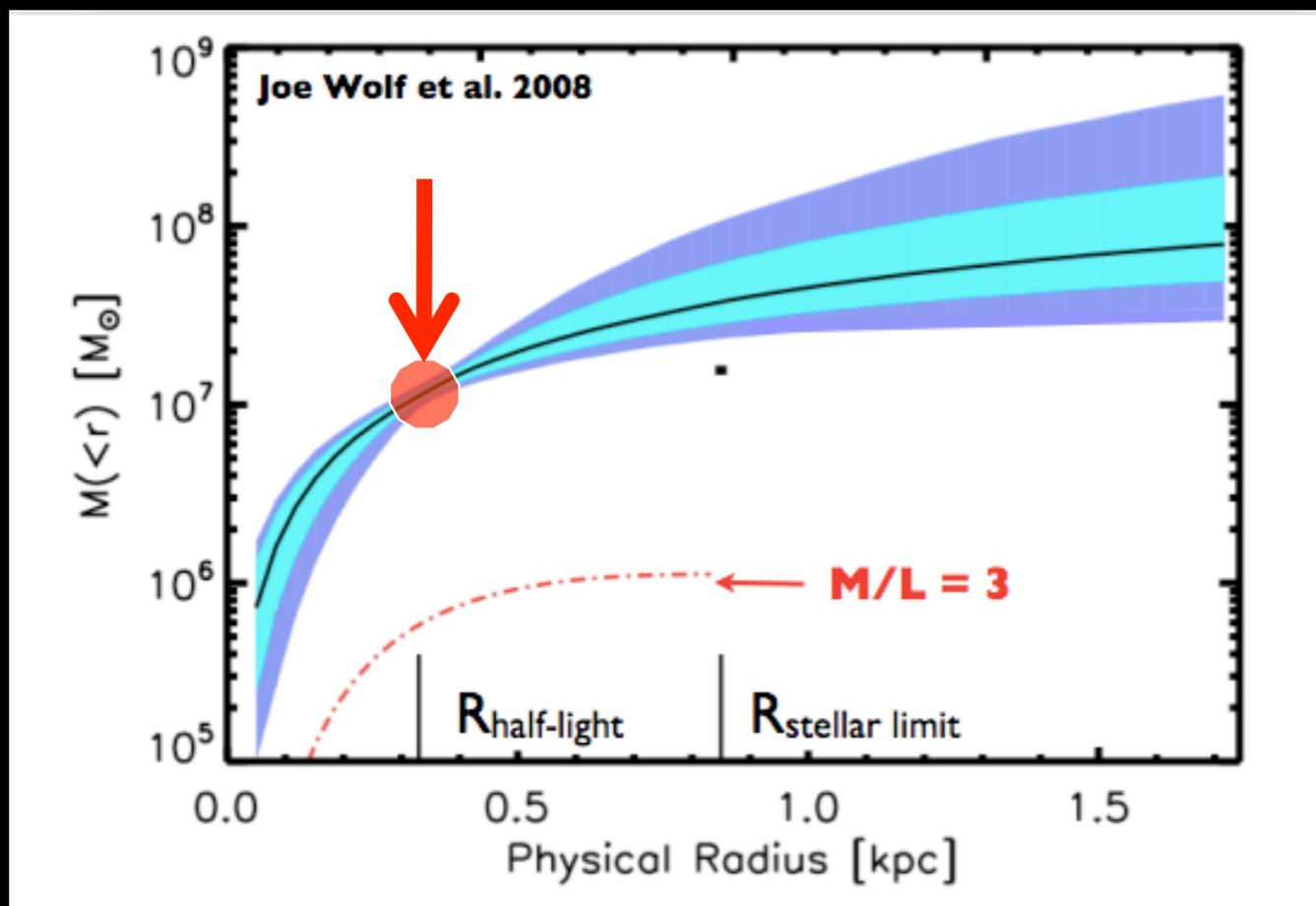
# THE IDEA

Walker & Peñarrubia (2011)

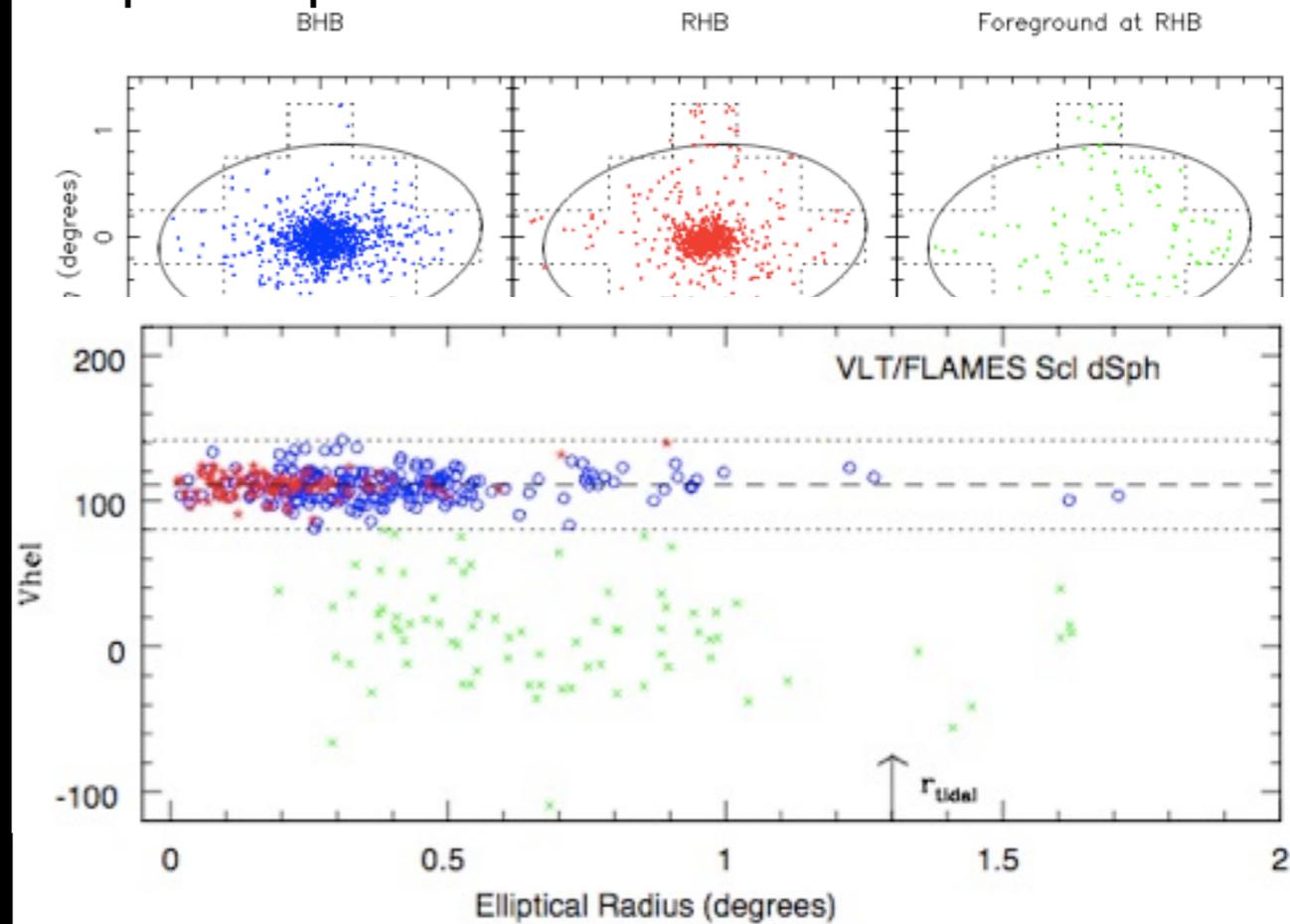
**M --  $\beta$  degeneracy breaks at  $R \approx R_{\text{half}}$**

Peñarrubia+08; Walker+09; Wolf+10; Amorisco & Evans 2010

Some dSphs show spatially + kinematically distinct stellar components



Sculptor dSph



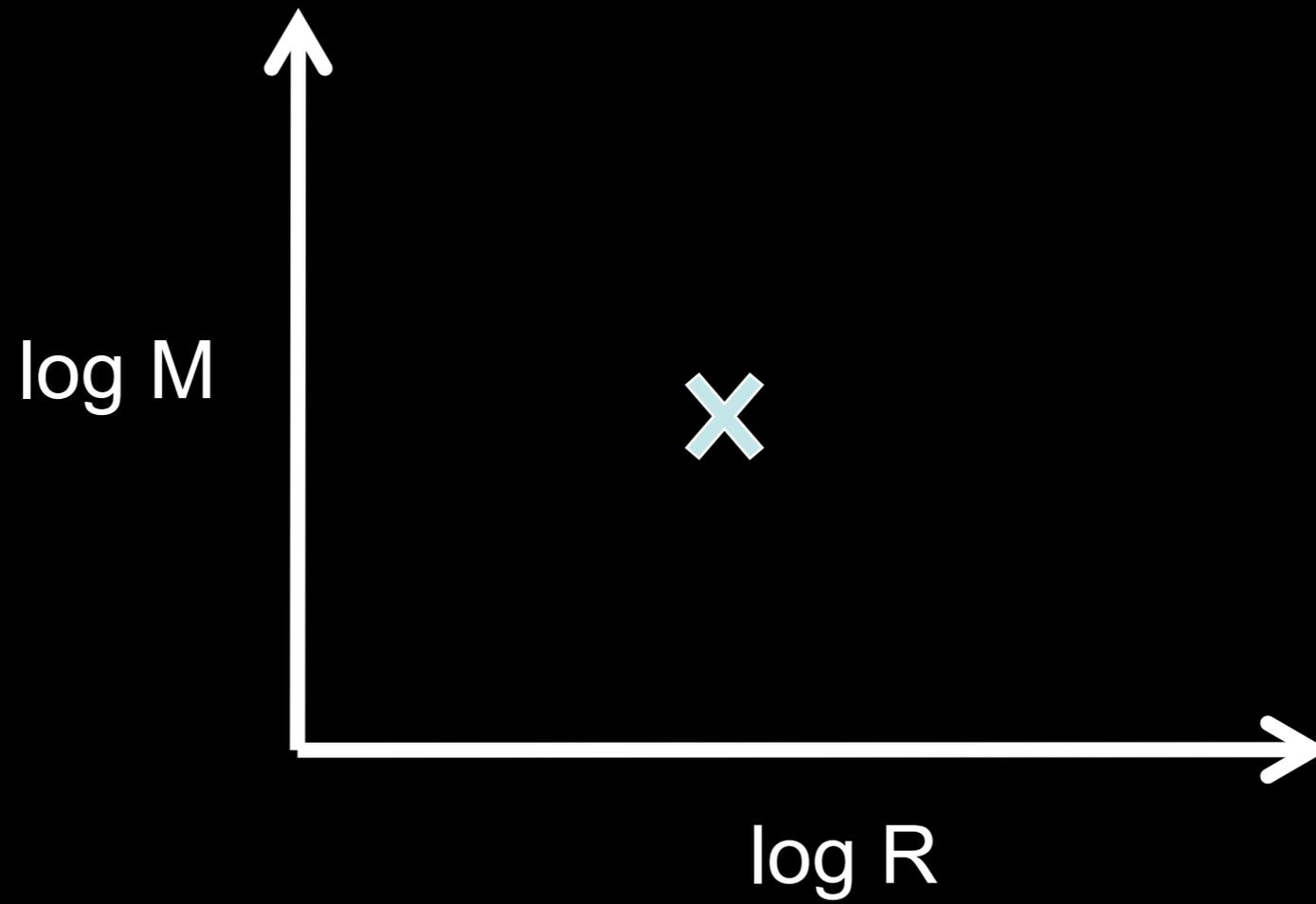
Tolstoy + 04 (see also Battaglia+08)

$$M(R_{\text{half}}) \approx \mu R_{\text{half}} \langle \sigma_V \rangle^2$$

$$\mu \approx 480 M_{\odot} \text{pc}^{-1} \text{km}^{-2} \text{s}^{-2} \quad (\text{Walker+09})$$

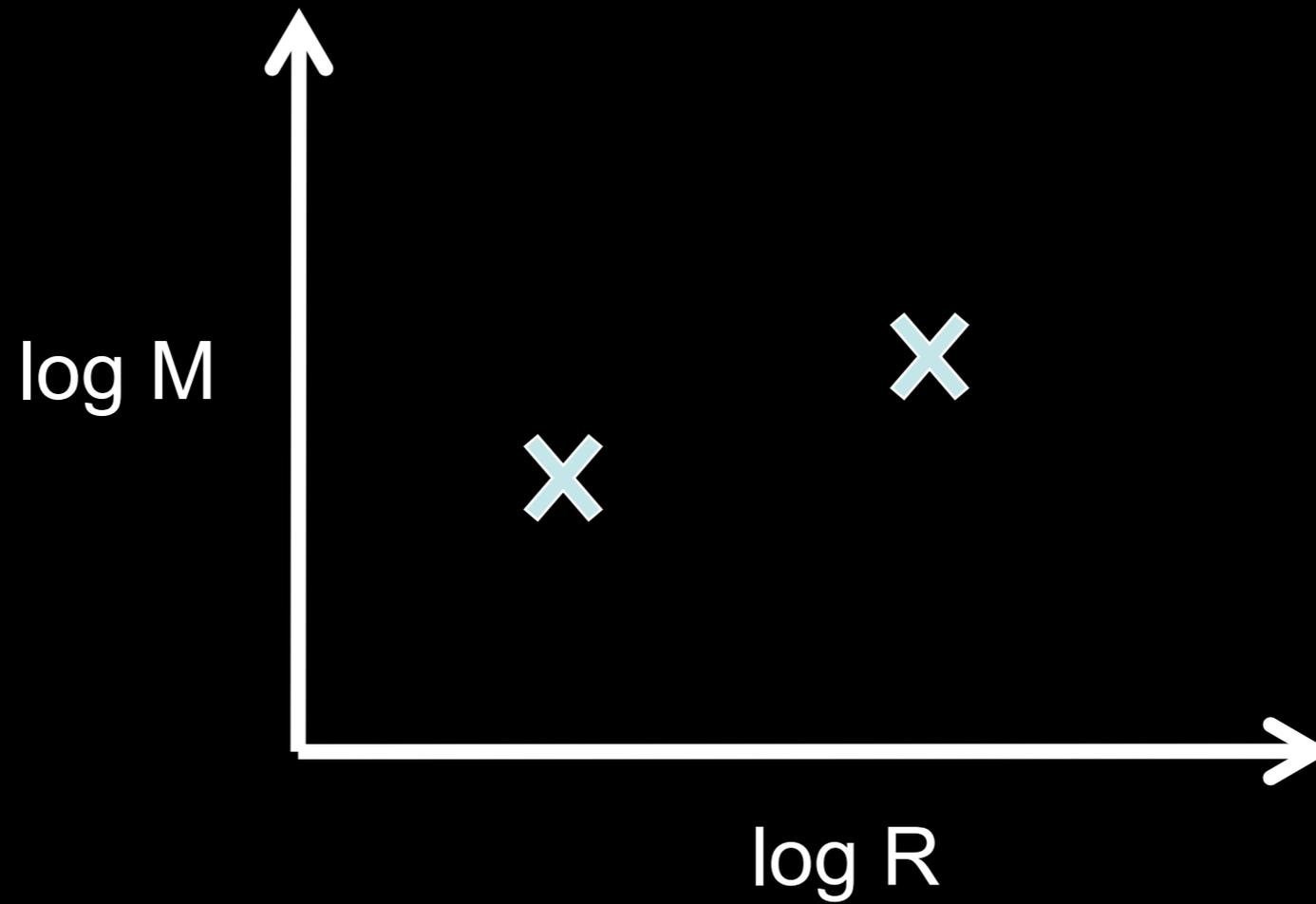
# THE IDEA

Walker & Peñarrubia (2011)



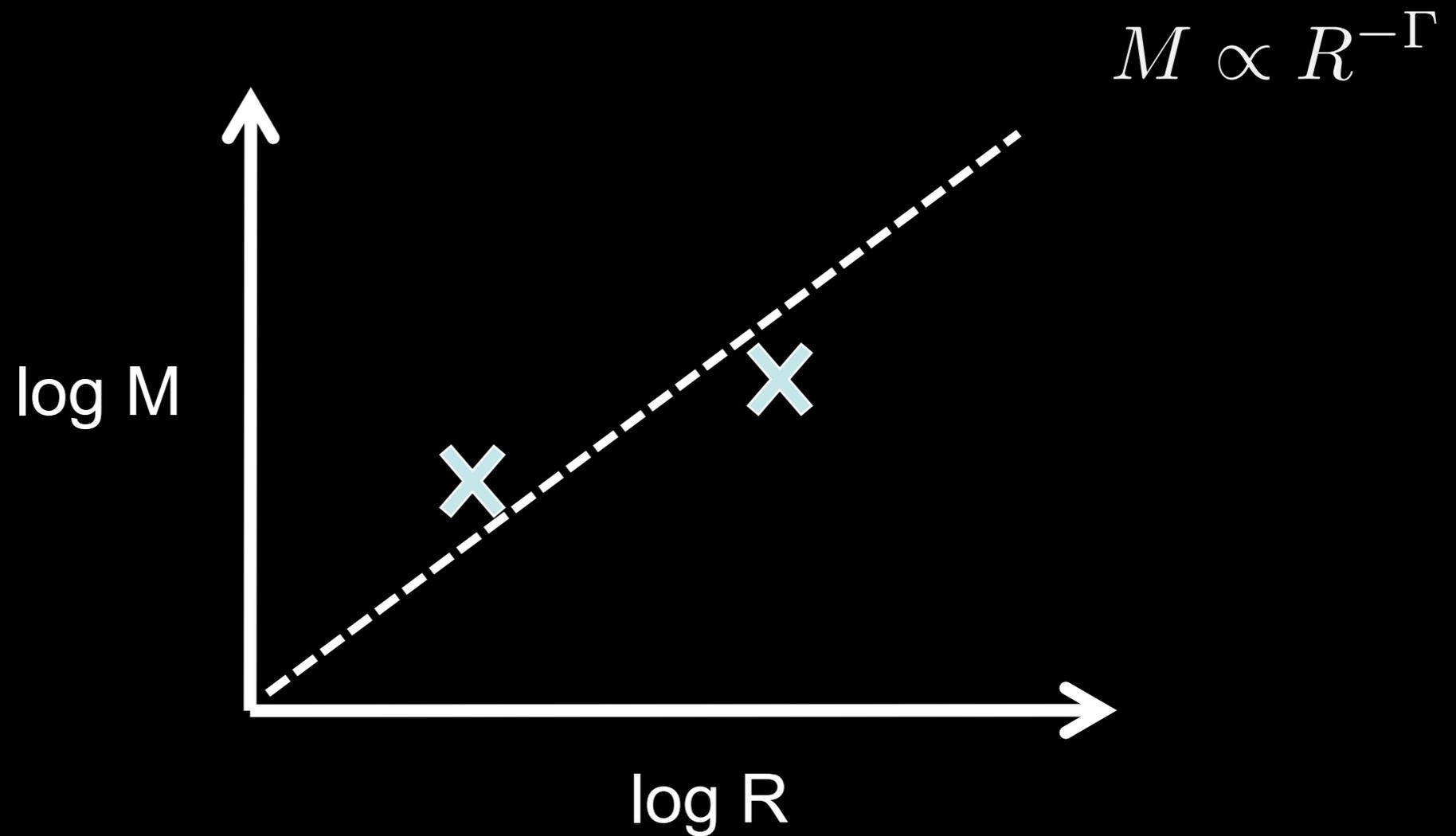
# THE IDEA

Walker & Peñarrubia (2011)



# THE IDEA

Walker & Peñarrubia (2011)



$$dM = 4\pi\rho_{\text{DM}}r^2dr$$

$$\rho_{\text{DM}} \propto r^{-1} \quad \longrightarrow \quad \Gamma \approx 2$$

$$\rho_{\text{DM}} \propto \text{const.} \quad \longrightarrow \quad \Gamma \approx 3$$

# Method

Walker & Peñarrubia (2011)

$$L(\{R_i, V_i, W'_i\}_{i=1}^{N_{\text{sample}}} | \vec{S}) = \prod_{i=1}^{N_{\text{sample}}} \left[ f_1 \frac{w(R_i) p_{R,1}(R_i) p_{V,1}(V_i) p_{W',1}(W'_i)}{\int_0^\infty w(R) p_{R,1}(R) dR} + f_2 \frac{w(R_i) p_{R,2}(R_i) p_{V,2}(V_i) p_{W',2}(W'_i)}{\int_0^\infty w(R) p_{R,2}(R) dR} + (1 - f_1 - f_2) \hat{p}_{\text{MW},R}(R_i) \hat{p}_{\text{MW},V}(V_i) \hat{p}_{\text{MW},W'}(W'_i) \right].$$

**MCMC algorithm:**

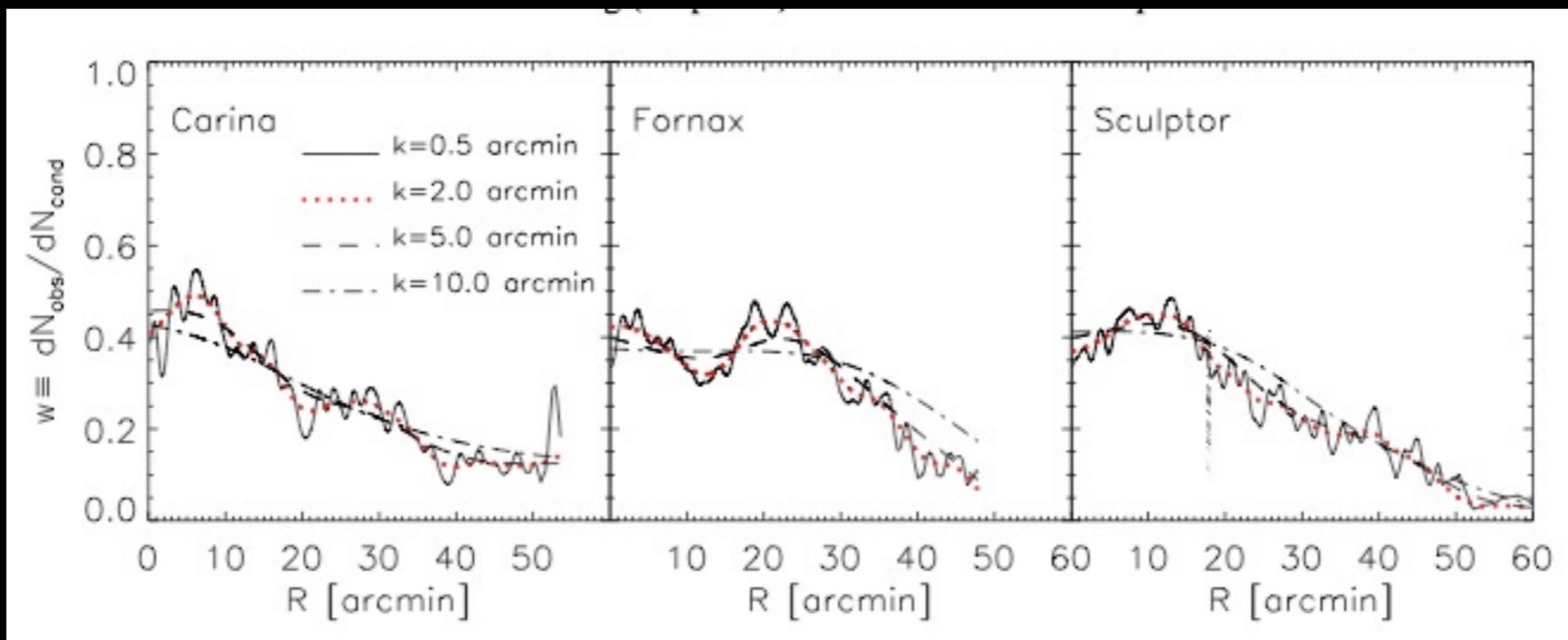
**2 stellar components + MW  
foreground contamination**

# Method

Walker & Peñarrubia (2011)

**MCMC algorithm:**  
**2 stellar components + MW**  
**foreground contamination**

$$L(\{R_i, V_i, W'_i\}_{i=1}^{N_{\text{sample}}} | \vec{S}) = \prod_{i=1}^{N_{\text{sample}}} \left[ f_1 \frac{w(R_i) p_{R,1}(R_i) p_{V,1}(V_i) p_{W',1}(W'_i)}{\int_0^\infty w(R) p_{R,1}(R) dR} + f_2 \frac{w(R_i) p_{R,2}(R_i) p_{V,2}(V_i) p_{W',2}(W'_i)}{\int_0^\infty w(R) p_{R,2}(R) dR} + (1 - f_1 - f_2) \hat{p}_{\text{MW},R}(R_i) \hat{p}_{\text{MW},V}(V_i) \hat{p}_{\text{MW},W'}(W'_i) \right]$$



# Method

Walker & Peñarrubia (2011)

$$L(\{R_i, V_i, W'_i\}_{i=1}^{N_{\text{sample}}} | \vec{S}) =$$

$$\prod_{i=1}^{N_{\text{sample}}} \left[ f_1 \frac{w(R_i) p_{R,1}(R_i) p_{V,1}(V_i) p_{W',1}(W'_i)}{\int_0^\infty w(R) p_{R,1}(R) dR} \right.$$

$$+ f_2 \frac{w(R_i) p_{R,2}(R_i) p_{V,2}(V_i) p_{W',2}(W'_i)}{\int_0^\infty w(R) p_{R,2}(R) dR}$$

$$\left. + (1 - f_1 - f_2) \hat{p}_{\text{MW},R}(R_i) \hat{p}_{\text{MW},V}(V_i) \hat{p}_{\text{MW},W'}(W'_i) \right].$$

## MCMC algorithm:

2 stellar components + MW  
foreground contamination

## Priors (14 free parameters)

$$p_i(R, V, W) = p_{R,i}(R) p_{V,i}(V) p_{W,i}(W);$$

Plummer prof. 
$$p_{R,i}(R) = \frac{2R/r_i^2}{(1 + R^2/r_i^2)^2}$$

Gaussian  $p_{V,i}$  and  $p_{W,i}$

- $f_{\text{mem}} = (N_1 + N_2) / (N_1 + N_2 + N_{\text{MW}})$  Fraction of dwarf members
- $f_{\text{sub},2} = N_2 / (N_1 + N_2)$  Fraction of stars in comp. 2
- $r_{\text{half},2}$  Half-light radius of comp. 2
- $r_{\text{half},1} / r_{\text{half},2}$  Ratio of Half-light radii
- $\langle W_1 \rangle$  Mean spectral index of comp. 1
- $\langle W_1 \rangle - \langle W_2 \rangle$  Spectral index difference
- $\sigma_{W1}$  Spectral index dispersion of comp. 1
- $\sigma_{W2}$  Spectral index dispersion of comp. 2
- $\sigma_{V1}$  Velocity dispersion of comp. 1
- $\sigma_{V2}$  Velocity dispersion of comp. 2
- $\mu_\alpha$  Proper motion in R.A.
- $\mu_\delta$  Proper motion in Declination

# Tests

Walker & Peñarrubia (2011)

## Synthetic data sets:

$$\nu_*(r) = \nu_0 \left( \frac{r}{r_*} \right)^{-\gamma_*} \left[ 1 + \left( \frac{r}{r_*} \right)^{\alpha_*} \right]^{(\gamma_* - \beta_*) / \alpha_*}$$

**Plummer:**  
 $(\alpha, \beta, \gamma)_* = (2, 5, 0)$

$$\rho_{\text{DM}}(r) = \rho_0 \left( \frac{r}{r_{\text{DM}}} \right)^{-\gamma_{\text{DM}}} \left[ 1 + \left( \frac{r}{r_{\text{DM}}} \right)^{\alpha_{\text{DM}}} \right]^{(\gamma_{\text{DM}} - \beta_{\text{DM}}) / \alpha_{\text{DM}}}$$

**NFW:**  
 $(\alpha, \beta, \gamma)_{\text{DM}} = (1, 3, 1)$

## Opsikov-Merritt DFs

$$Q \equiv E + \frac{L^2}{2r_a^2} = \frac{1}{2} [v_r^2 + (1 + r^2/r_a^2)v_t^2] + U(r)$$

$$f(Q) = \frac{1}{\sqrt{8\pi^2}} \int_Q^0 \frac{d^2 \rho_Q}{dU^2} \frac{dU}{\sqrt{U - Q}}$$

where  $\rho_Q(r) \equiv (1 + r^2/r_a^2)\rho(r)$

**DM potential**

**stellar density**

$$\beta \equiv 1 - \frac{\sigma_t^2}{\sigma_r^2} = \frac{r^2}{r_a^2 + r^2}$$

$r \ll r_a$   $\beta = 0$  (isotropic)

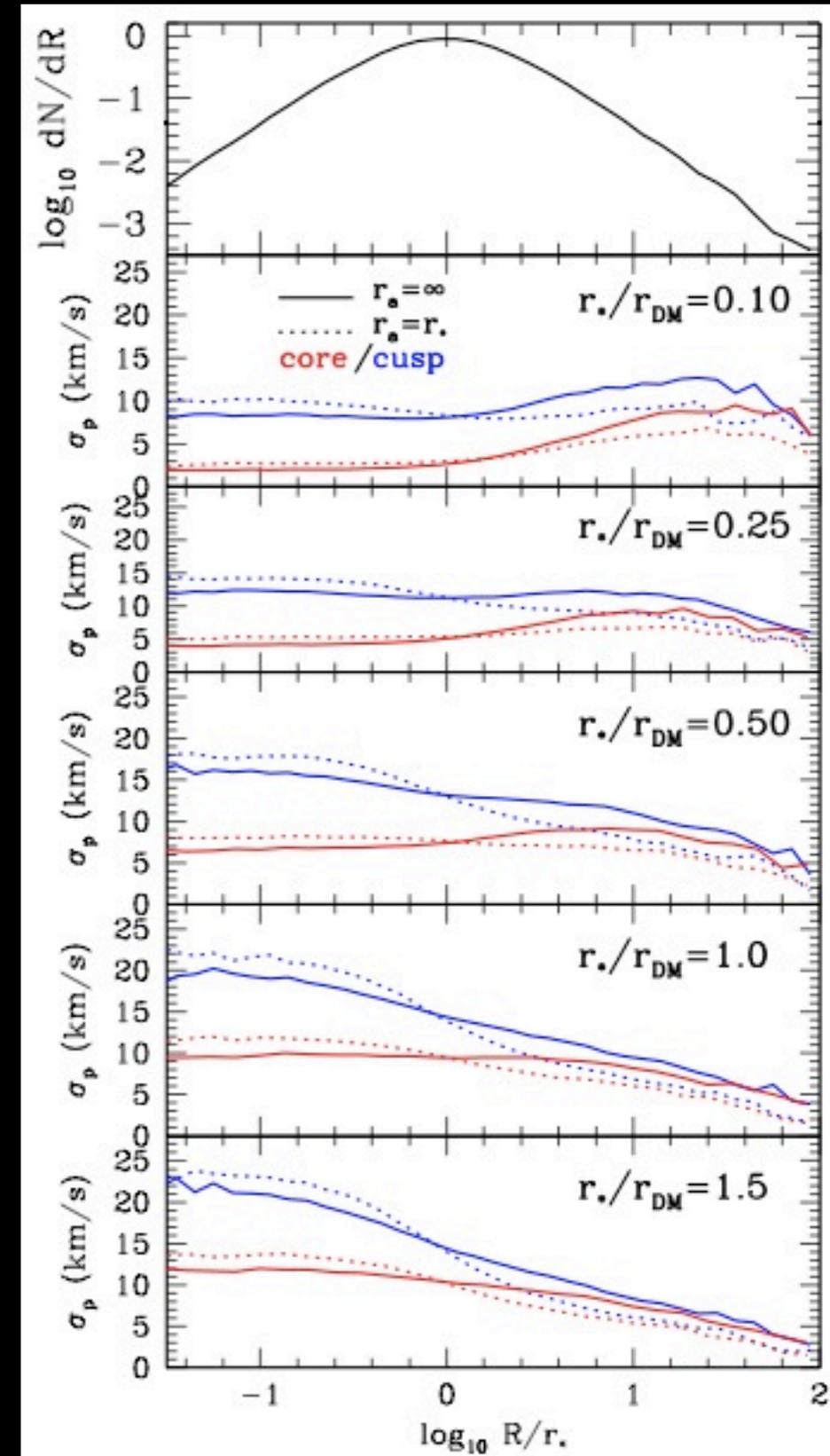
$r \gg r_a$   $\beta = 1$  (radially anisotropic)

# Tests

Walker & Peñarrubia (2011)

TABLE 3  
TESTS ON SYNTHETIC DATA: INPUT PARAMETERS FOR DYNAMICAL TEST MODELS

Stellar Profile (Equation 15)				Dark Matter Profile (Equation 16)				
$r_*$	$\alpha_*$	$\beta_*$	$\gamma_*$	$\rho_0$	$r_{DM}$	$\alpha_{DM}$	$\beta_{DM}$	$\gamma_{DM}$
[pc]				$[M_\odot \text{pc}^{-3}]$	[pc]			
<b>Cored Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
<b>Cusped Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1



# Tests

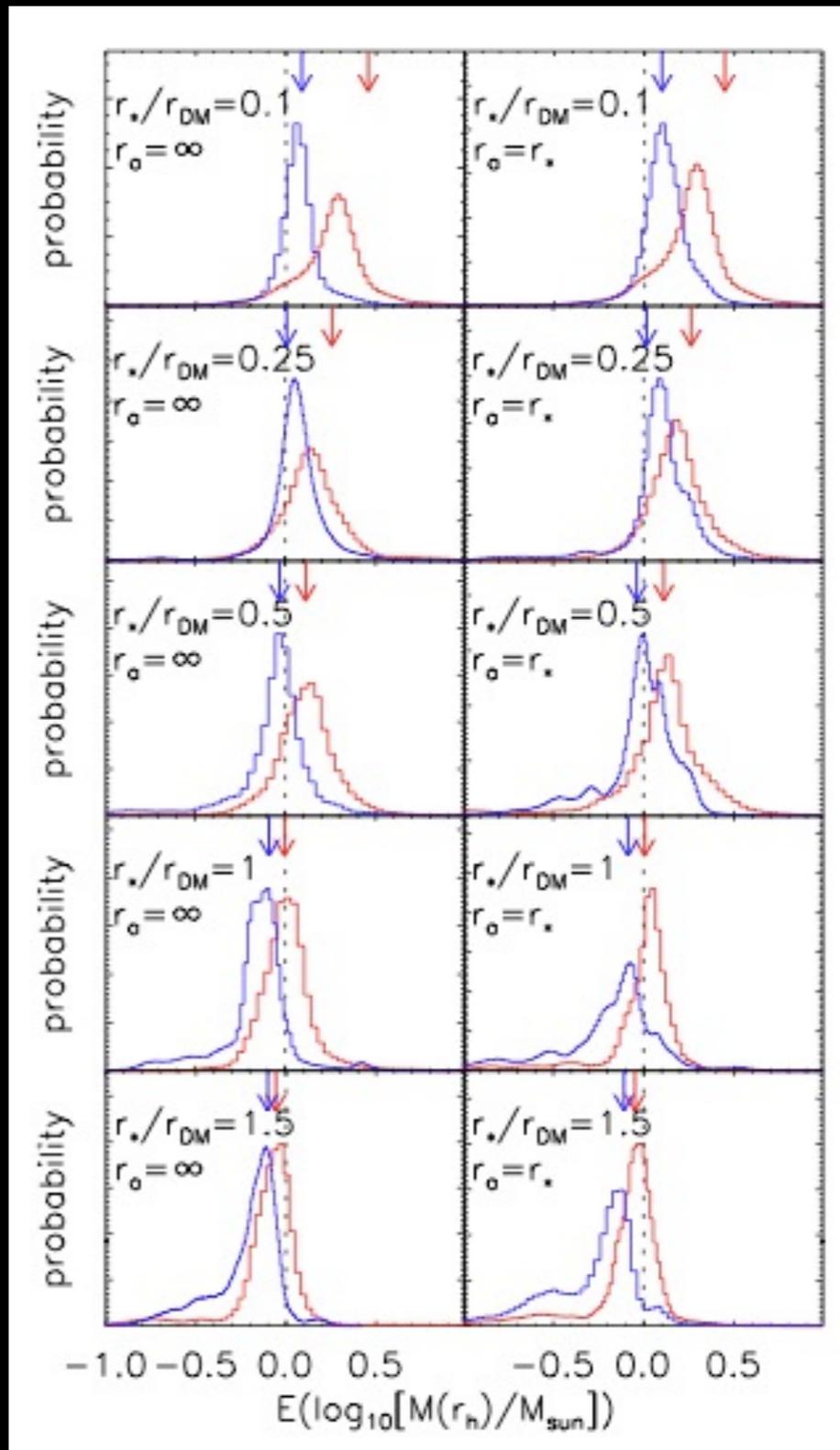
Walker & Peñarrubia (2011)

TABLE 3  
TESTS ON SYNTHETIC DATA: INPUT PARAMETERS FOR DYNAMICAL TEST MODELS

Stellar Profile (Equation 15)				Dark Matter Profile (Equation 16)				
$r_*$ [pc]	$\alpha_*$	$\beta_*$	$\gamma_*$	$\rho_0$ [ $M_\odot \text{pc}^{-3}$ ]	$r_{\text{DM}}$ [pc]	$\alpha_{\text{DM}}$	$\beta_{\text{DM}}$	$\gamma_{\text{DM}}$
<b>Cored Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
<b>Cusped Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1

isotropic

anisotropic

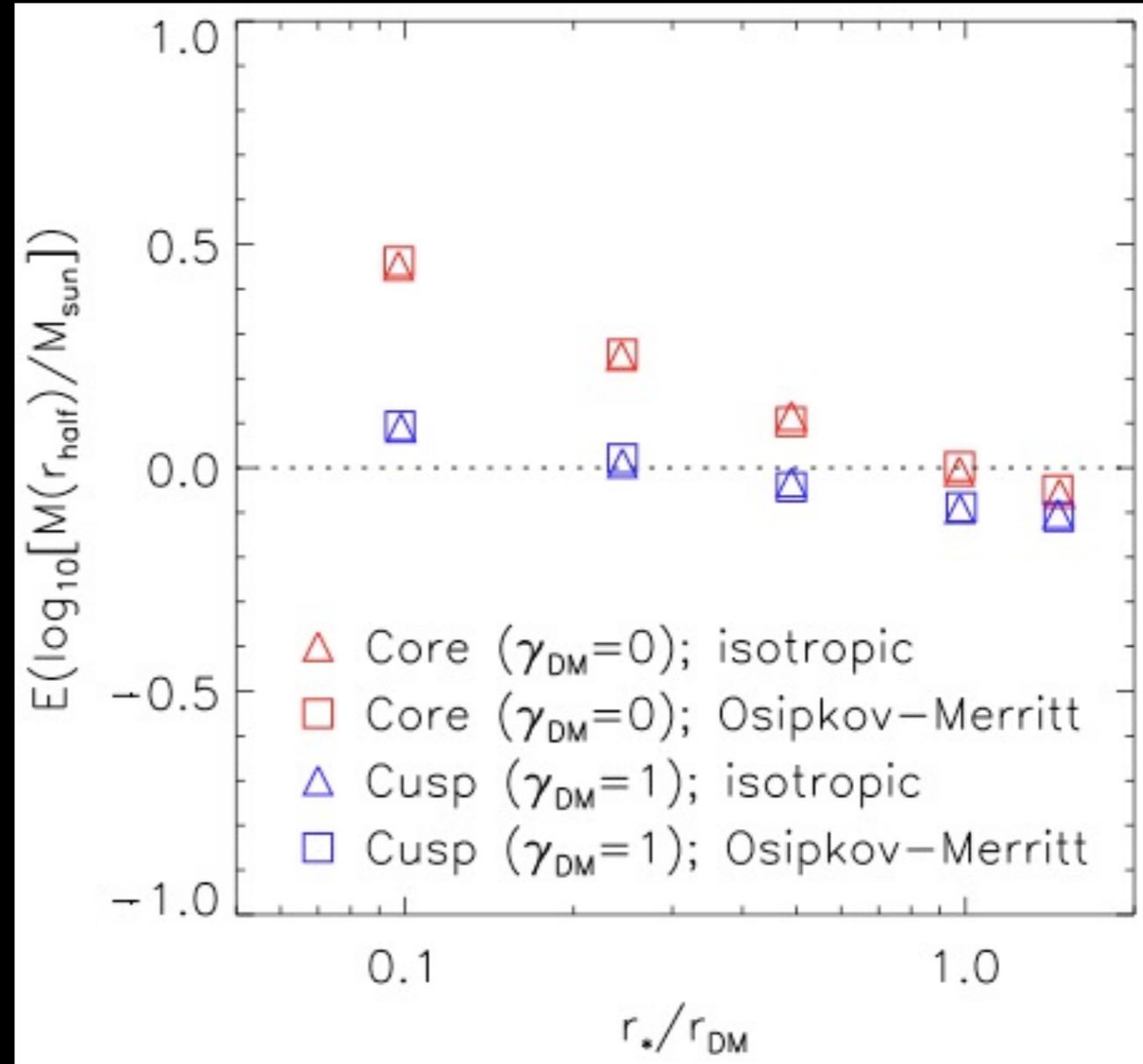


# Tests

Walker & Peñarrubia (2011)

TABLE 3  
TESTS ON SYNTHETIC DATA: INPUT PARAMETERS FOR DYNAMICAL TEST MODELS

Stellar Profile (Equation 15)				Dark Matter Profile (Equation 16)				
$r_*$ [pc]	$\alpha_*$	$\beta_*$	$\gamma_*$	$\rho_0$ [ $M_\odot \text{pc}^{-3}$ ]	$r_{\text{DM}}$ [pc]	$\alpha_{\text{DM}}$	$\beta_{\text{DM}}$	$\gamma_{\text{DM}}$
<b>Cored Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
<b>Cusped Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1



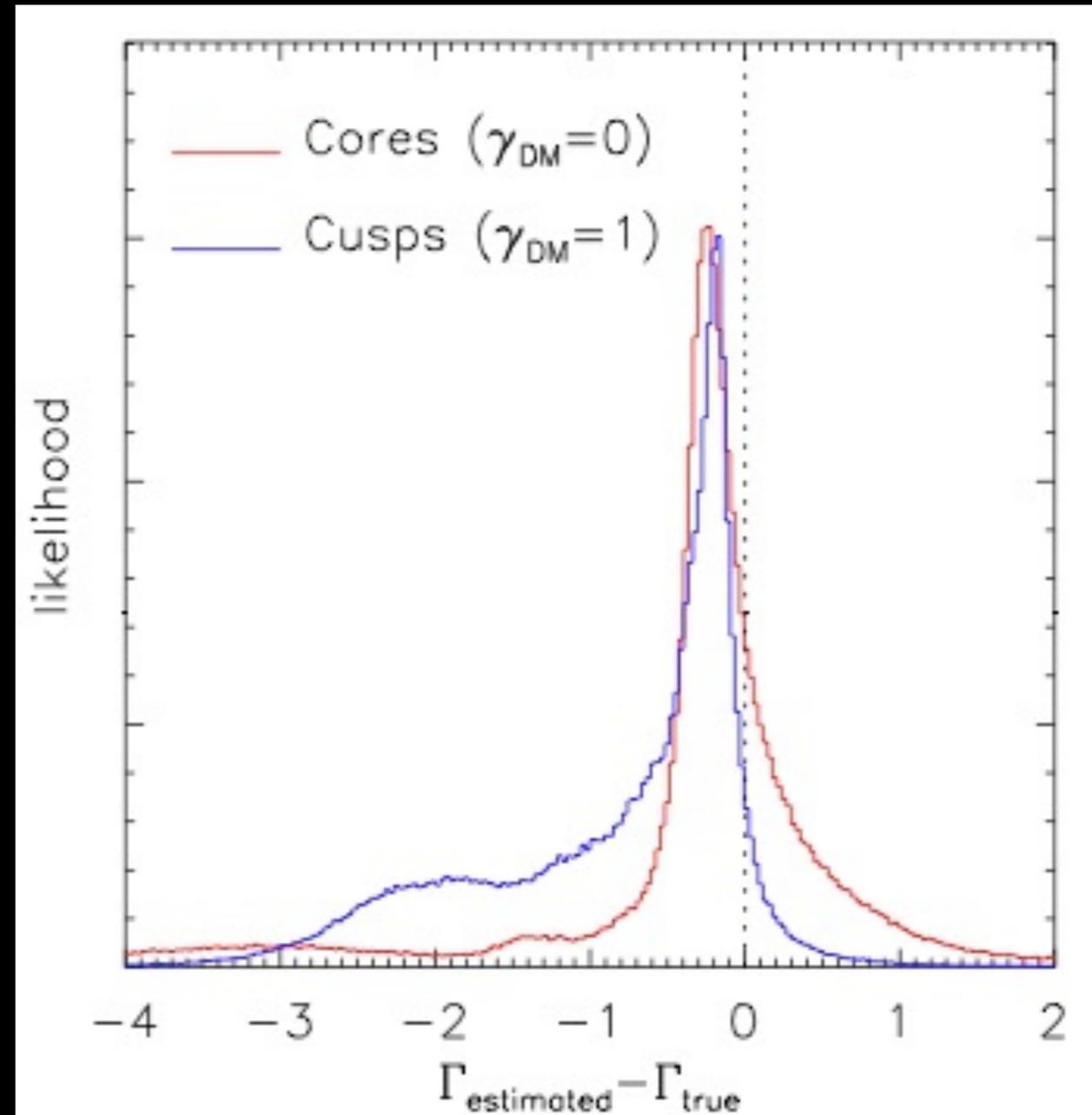
$$M(R_{\text{half}}) \approx \mu R_{\text{half}} \langle \sigma_V \rangle^2$$

# Tests

Walker & Peñarrubia (2011)

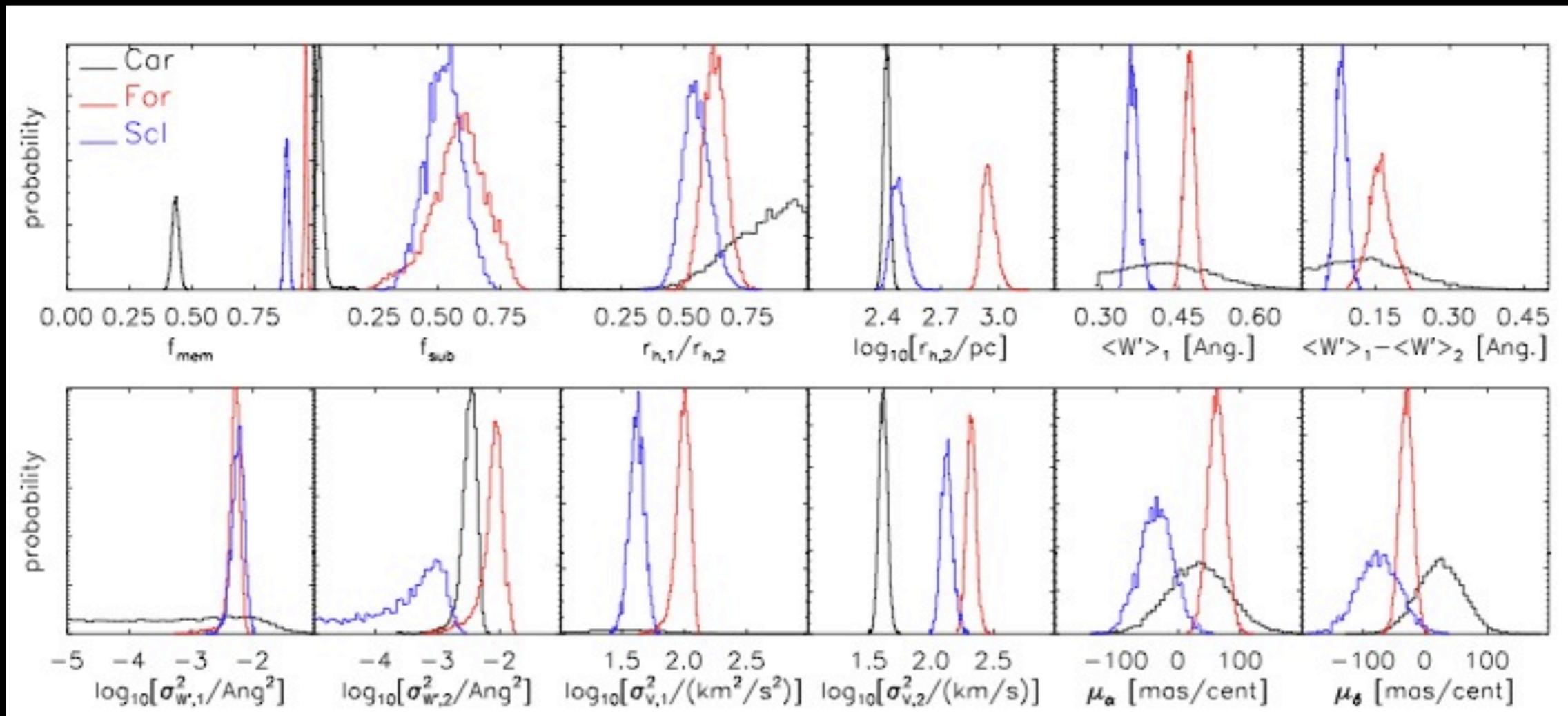
TABLE 3  
TESTS ON SYNTHETIC DATA: INPUT PARAMETERS FOR DYNAMICAL TEST MODELS

Stellar Profile (Equation 15)				Dark Matter Profile (Equation 16)				
$r_*$ [pc]	$\alpha_*$	$\beta_*$	$\gamma_*$	$\rho_0$ [ $M_\odot \text{pc}^{-3}$ ]	$r_{\text{DM}}$ [pc]	$\alpha_{\text{DM}}$	$\beta_{\text{DM}}$	$\gamma_{\text{DM}}$
<b>Cored Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	0
250	2	5	0.1	0.064	1000	1	3	0
500	2	5	0.1	0.064	1000	1	3	0
1000	2	5	0.1	0.064	1000	1	3	0
1500	2	5	0.1	0.064	1000	1	3	0
<b>Cusped Halos</b>								
Isotropic ( $r_a = \infty$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1
Anisotropic ( $r_a = r_*$ )								
100	2	5	0.1	0.064	1000	1	3	1
250	2	5	0.1	0.064	1000	1	3	1
500	2	5	0.1	0.064	1000	1	3	1
1000	2	5	0.1	0.064	1000	1	3	1
1500	2	5	0.1	0.064	1000	1	3	1



# Results

Walker & Peñarrubia (2011)



## MCMC posteriors

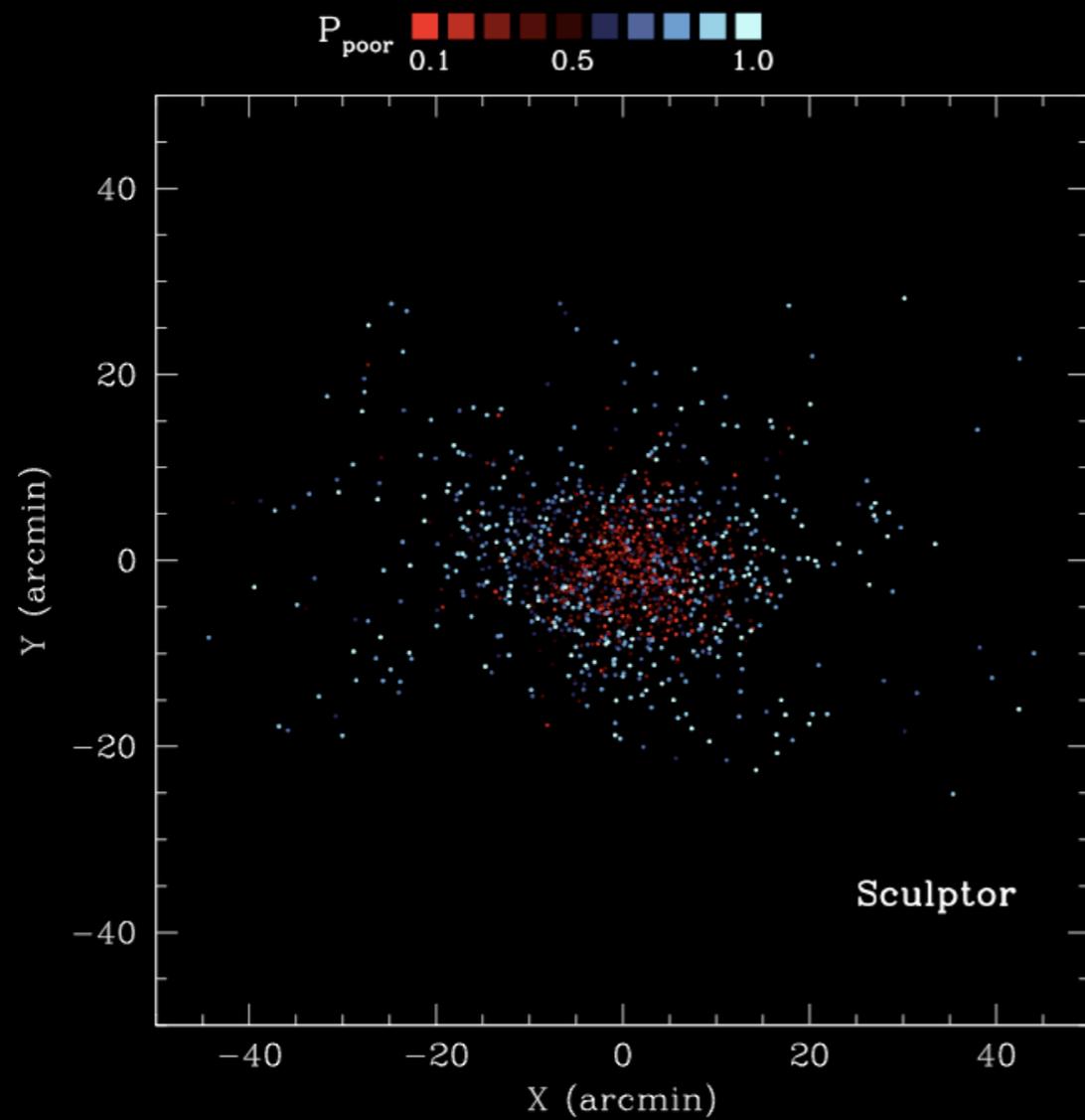
Two components detected  
in **Sculptor** and **Fornax**

We recover published data on:

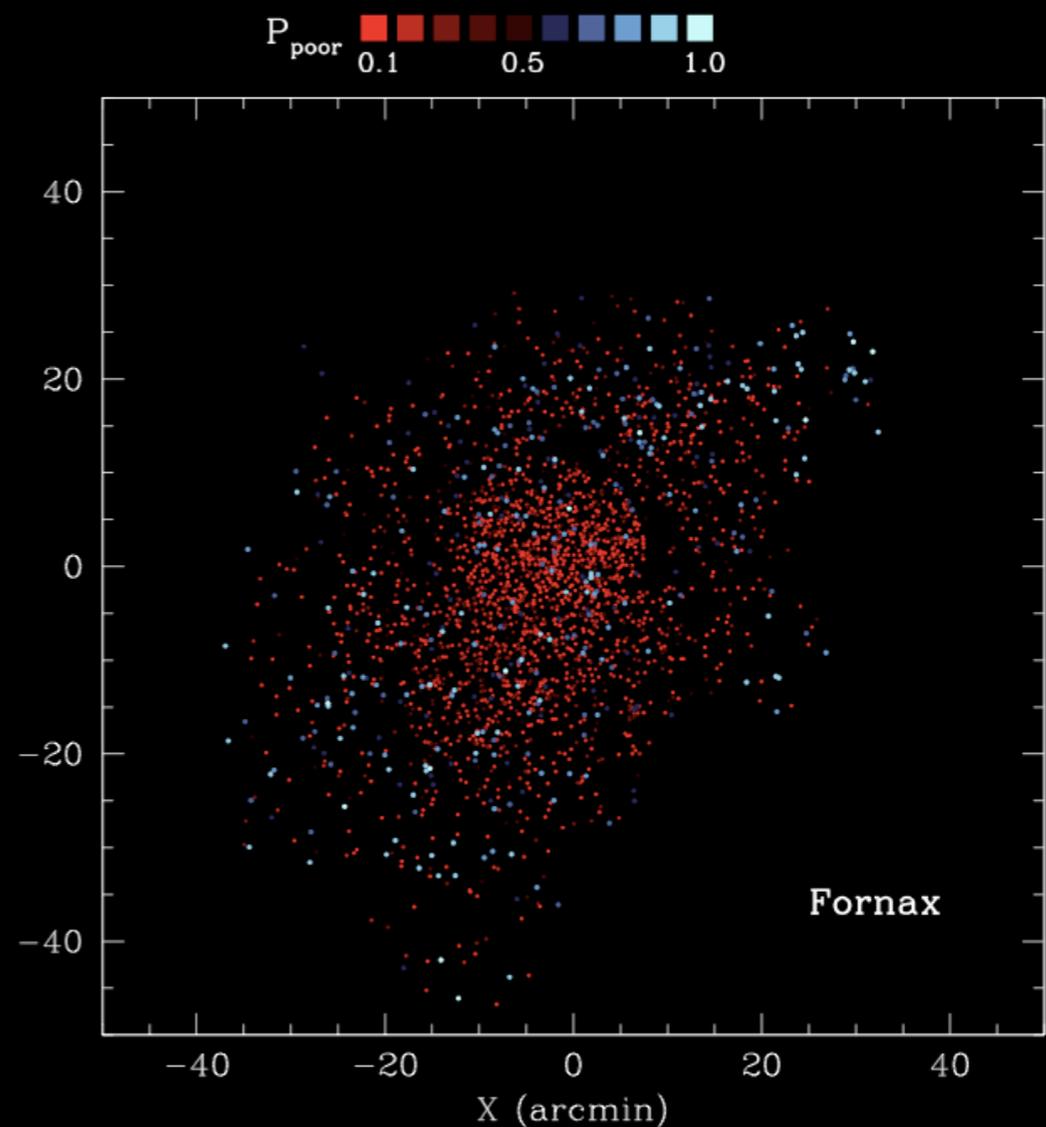
1. proper motions
2. mean velocity dispersion
3. averaged  $R_{\text{half}}$
4. mean metallicity

# Results

Walker & Peñarrubia (2011)



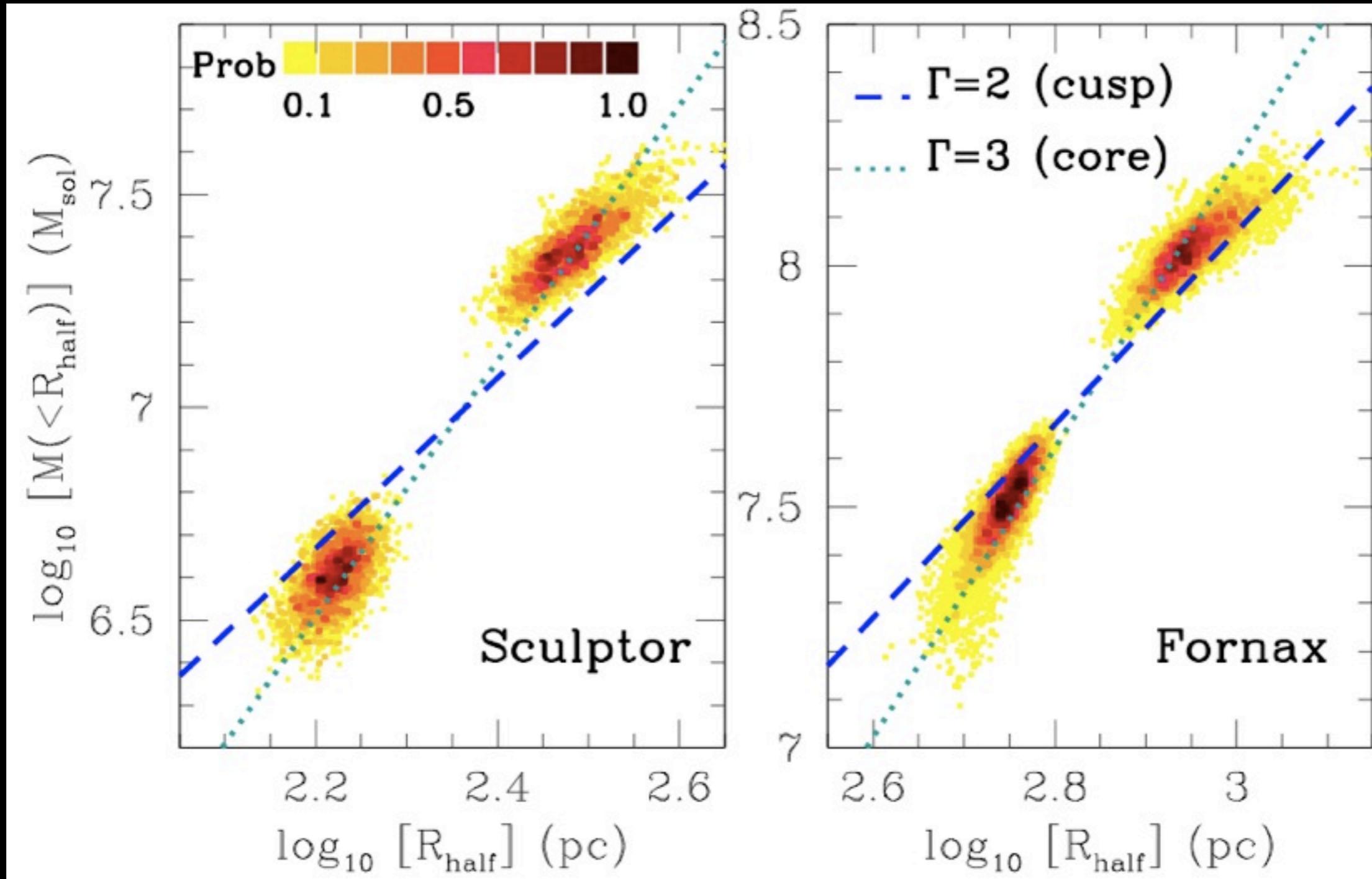
$N_{\text{sample}} = 1497$  spectra



$N_{\text{sample}} = 2603$  spectra

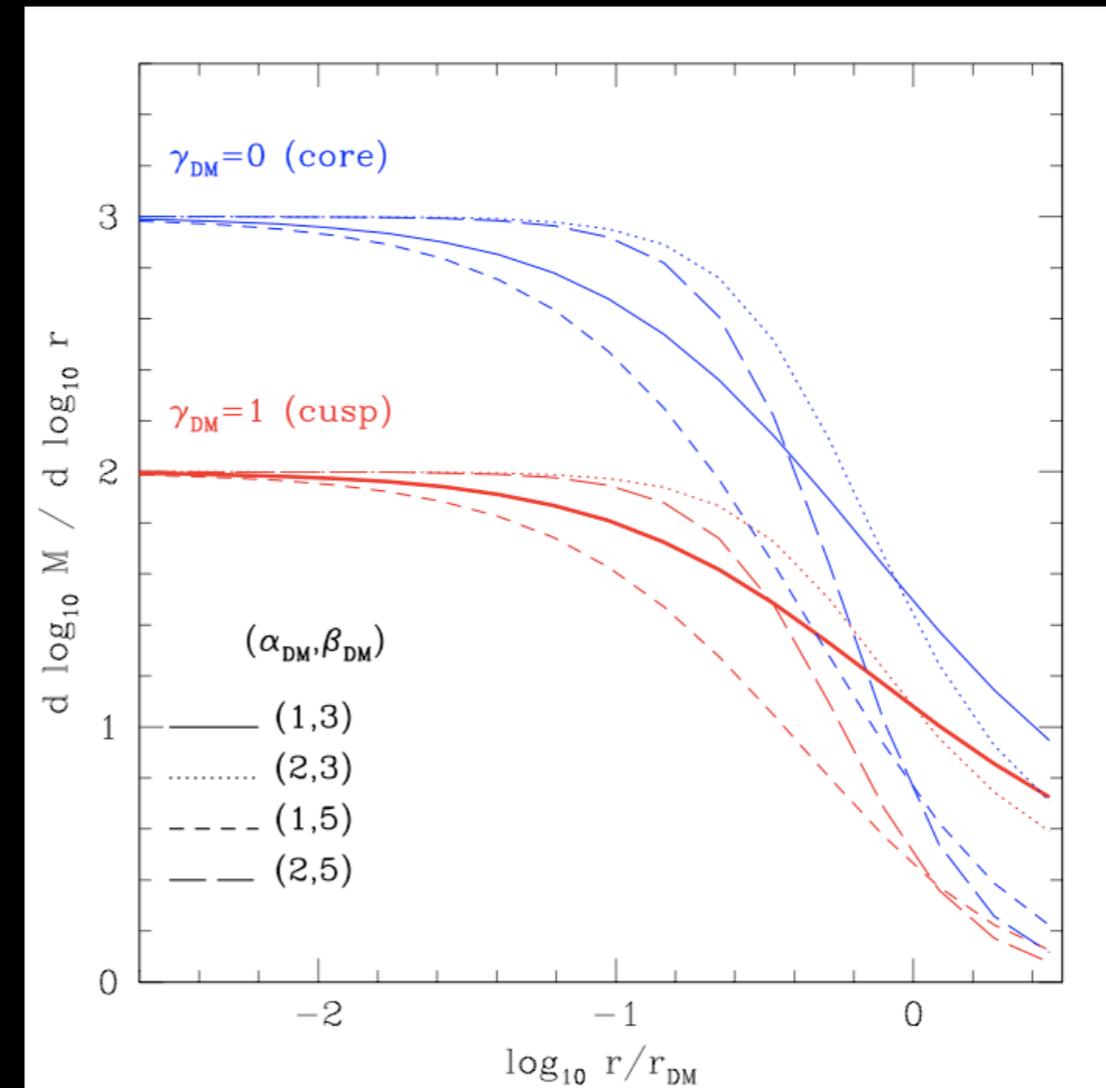
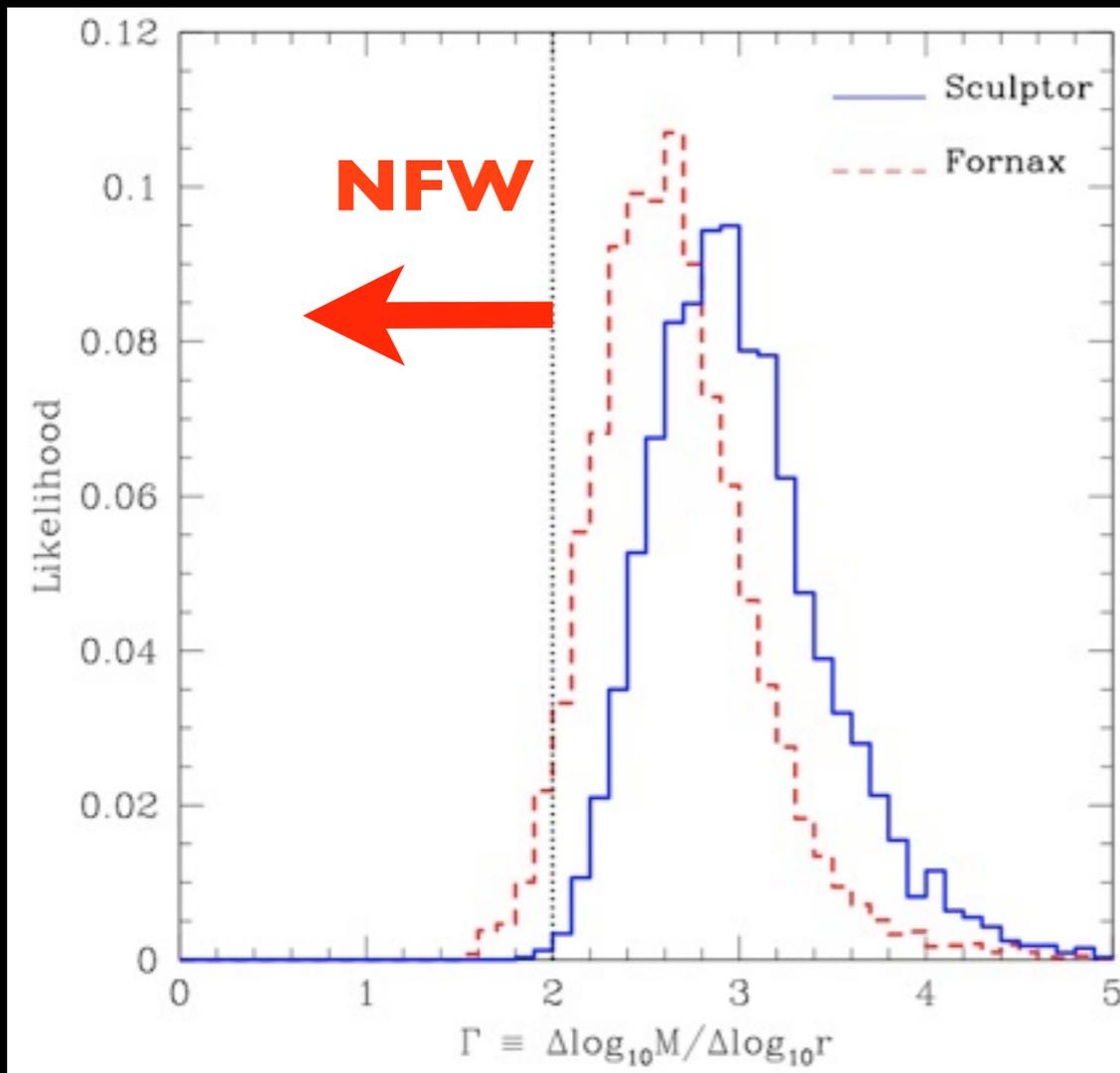
# Results

Walker & Peñarrubia (2011)



# Results

Walker & Peñarrubia (2011)



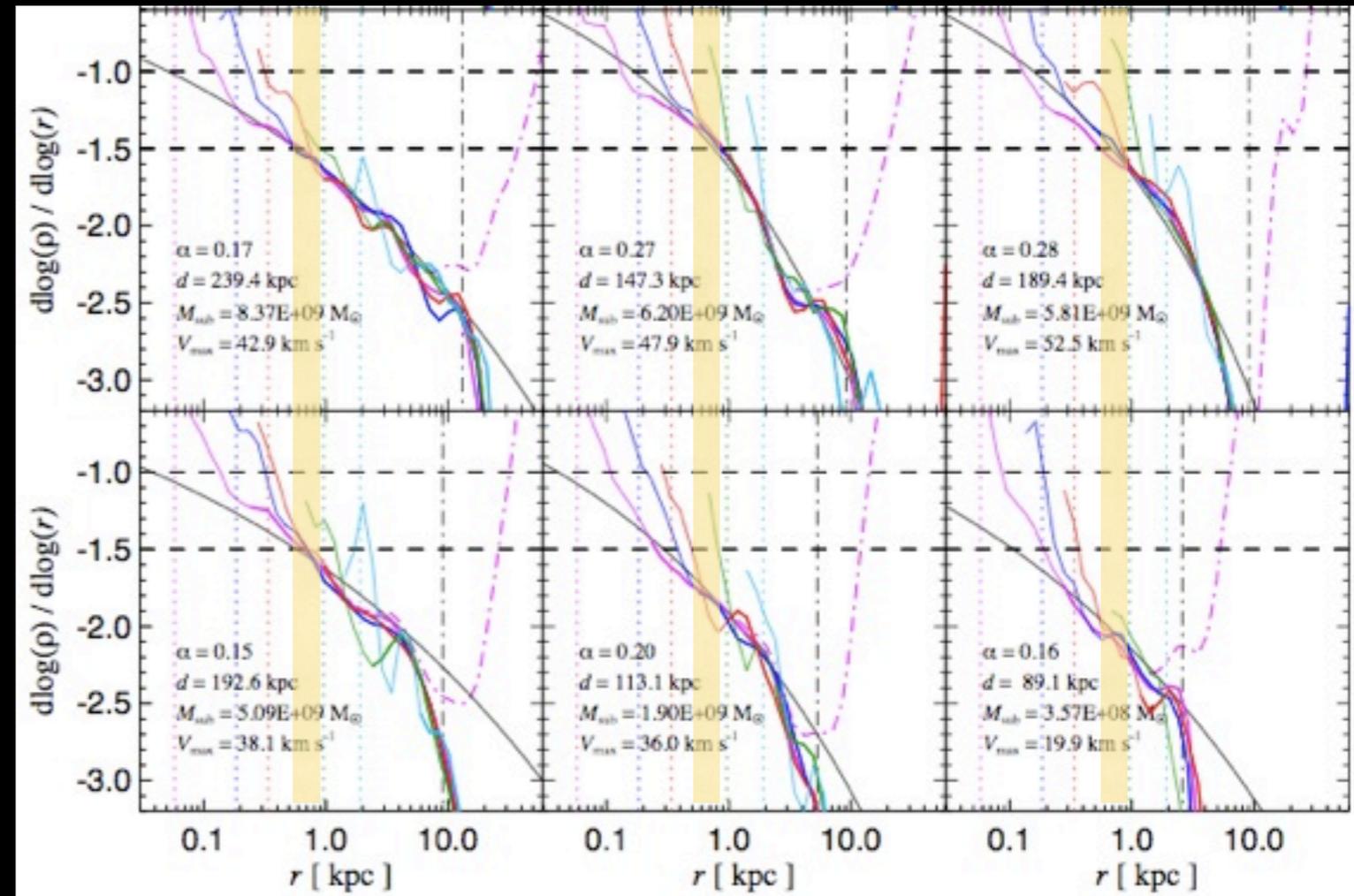
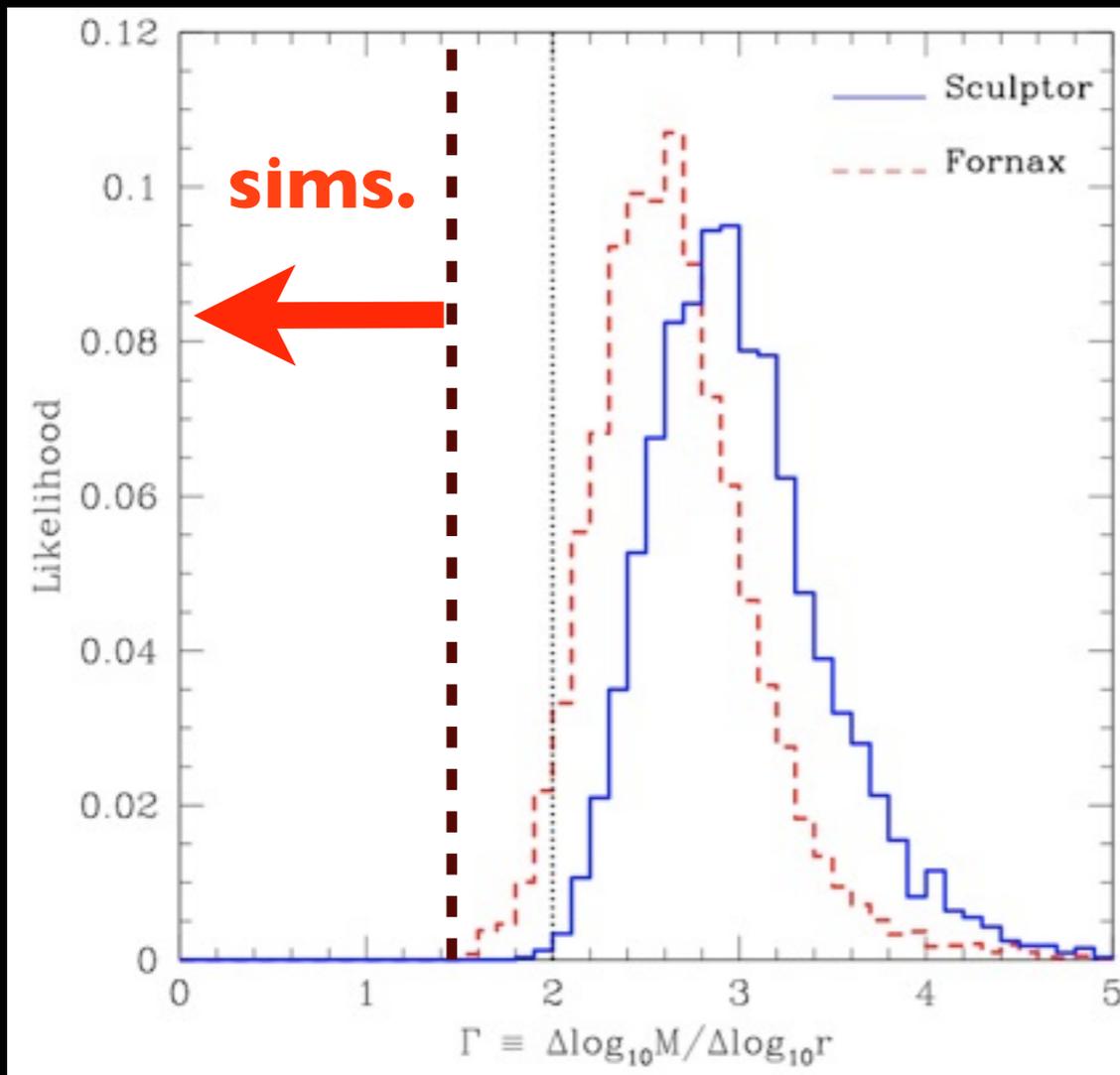
$$\rho_{DM} = \frac{\rho_0}{\left( r / r_{DM} \right)^{\gamma_{DM}} \left[ 1 + \left( r / r_{DM} \right)^{\alpha_{DM}} \right]^{(\beta_{DM} - \gamma_{DM}) / \alpha_{DM}}}$$

**NFW** ruled out in Fornax and Sculptor at a **96%** and **99%** confidence level

# Results

Walker & Peñarrubia (2011)

Springel+08



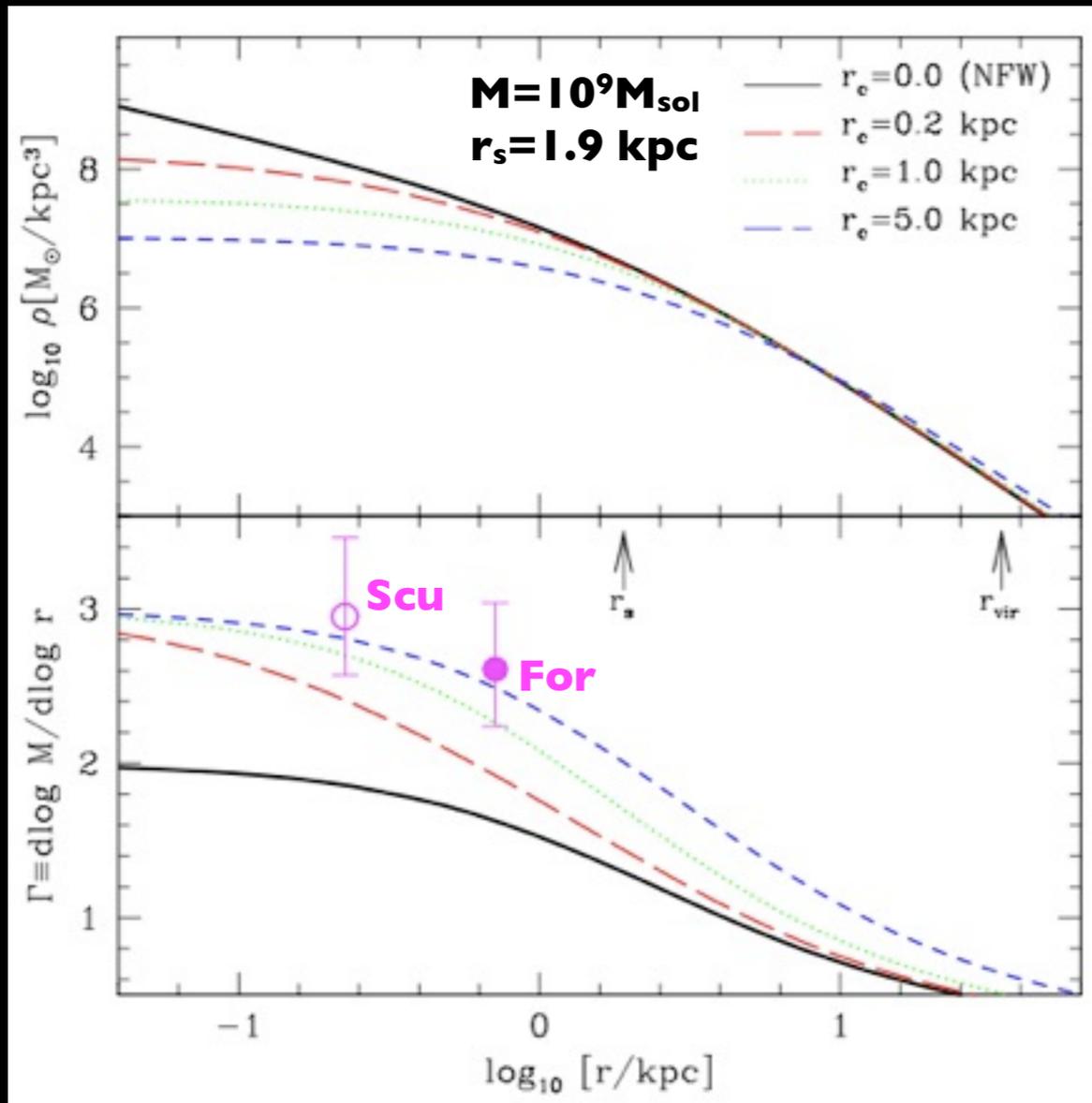
$$\rho_{\text{DM}} = \frac{\rho_0}{\left( r / r_{\text{DM}} \right)^{\gamma_{\text{DM}}} \left[ 1 + \left( r / r_{\text{DM}} \right)^{\alpha_{\text{DM}}} \right]^{(\beta_{\text{DM}} - \gamma_{\text{DM}}) / \alpha_{\text{DM}}}}$$

**Profiles from collision-less cosmological simulations of satellites ruled out in Fornax and Sculptor at a 99.98% and 99.999% confidence level**

# Core size

Only slope mass profile is known

$$\rho = \frac{\rho_0}{(r + r_c)(r + r_s)^2}$$



for  $r_h \ll r_s$

$$\Gamma(r_h) \approx 3 - \frac{3 + 2x}{4x} \left( \frac{r_h}{r_s} \right); \quad x \equiv r_c/r_s$$

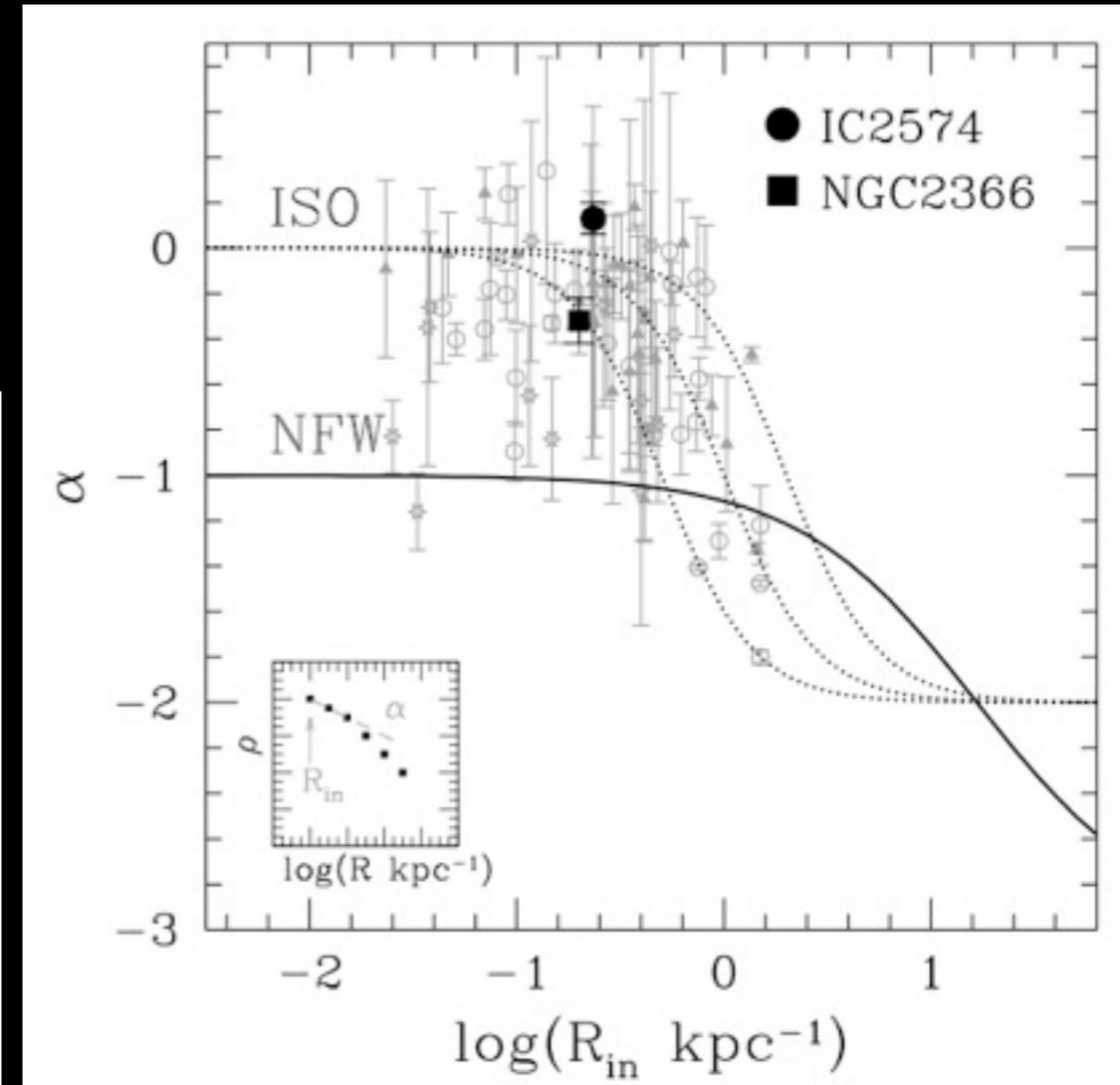
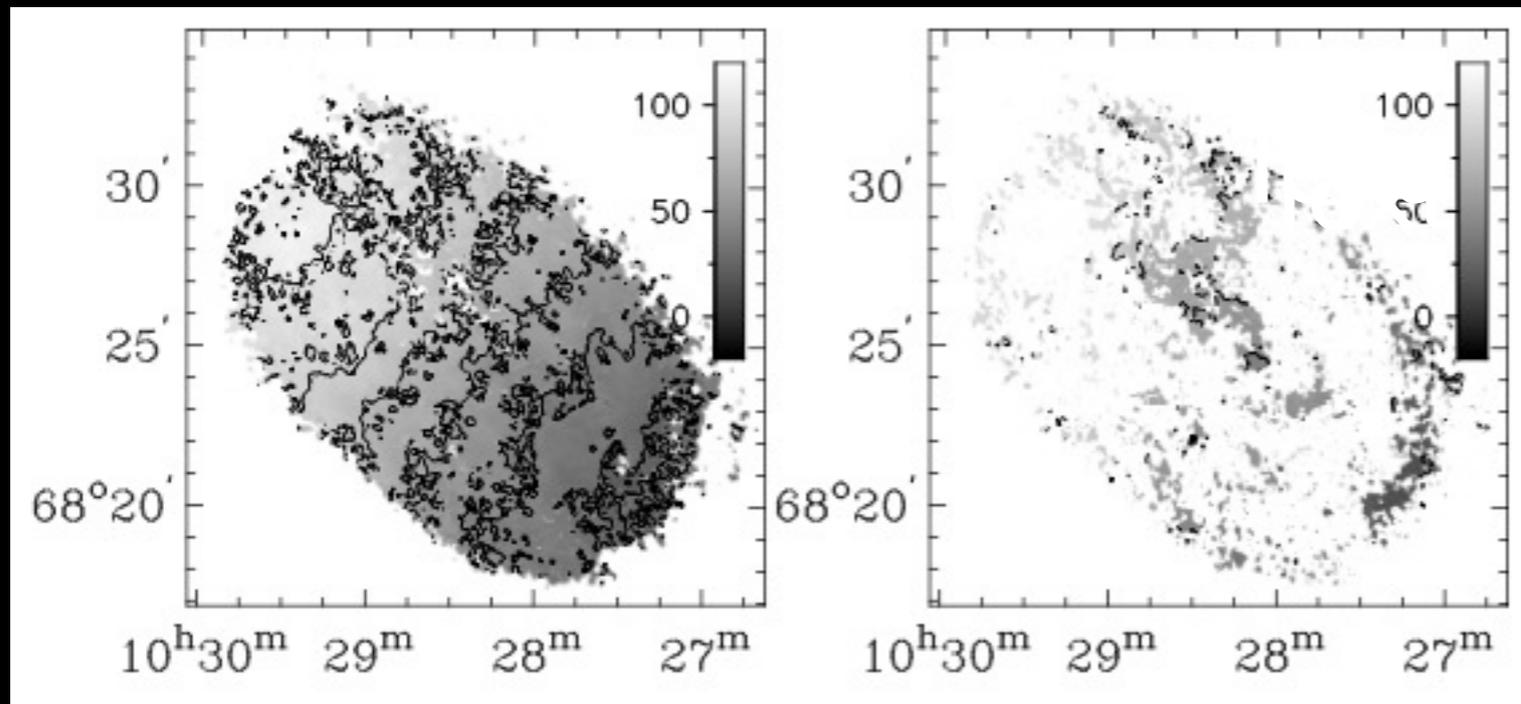
Only lower limits on  $r_c$  can be derived

$r_c \gg r_h \sim 0.5 - 1.0$  kpc

# The core/cusp problem

Most **LSB** and **late-type** galaxies  
( $10^{10}$ – $10^{11} M_{\text{sol}}$ ) show rotation curves  
indicative of **cored** DM profiles

de Blok+ 2001; de Blok & Bosma 2002; Swaters+2003

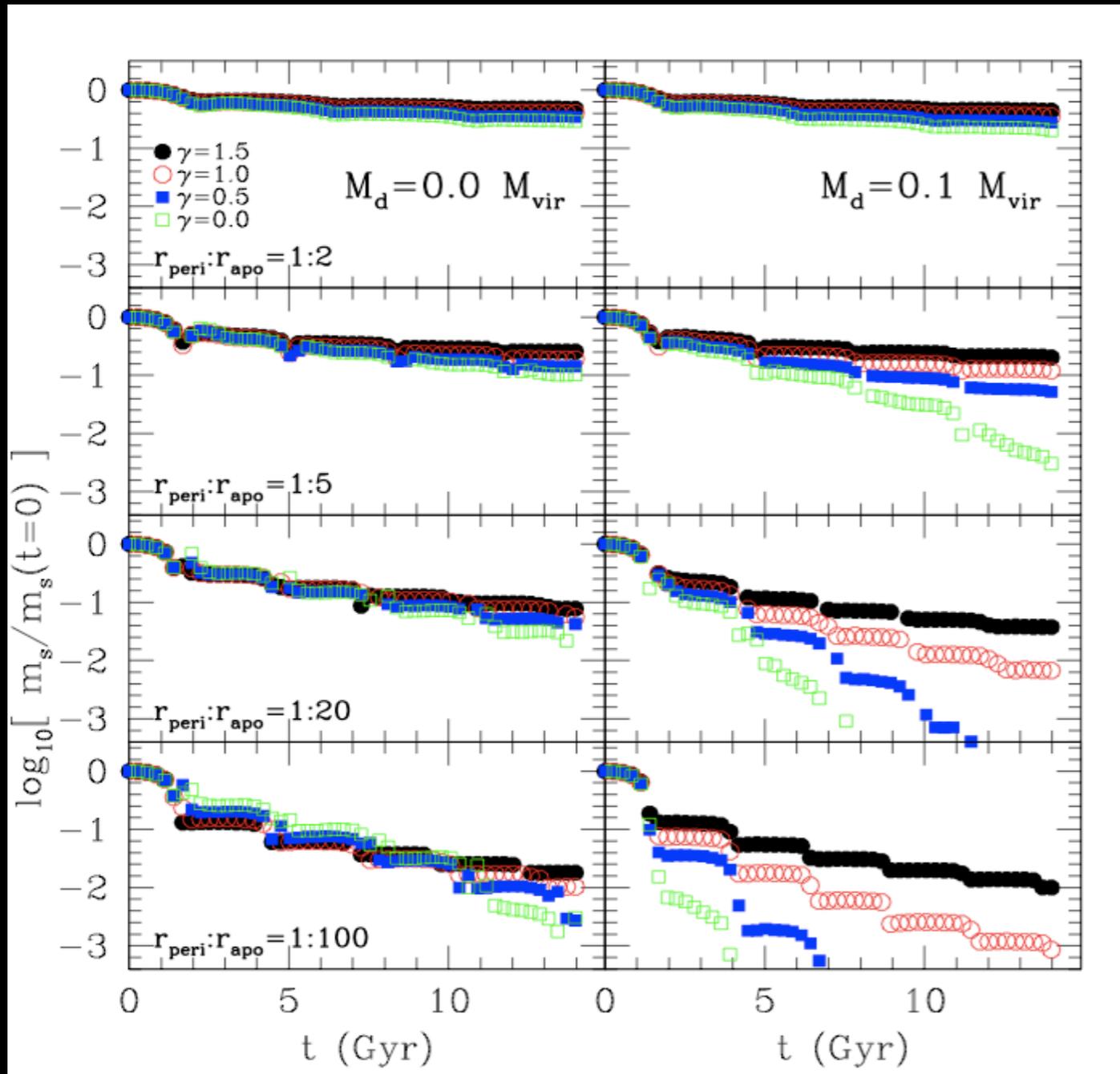


Oh+08

2D velocities from the THINGS survey  
confirm the result

Oh+2008; Kuzio de Naray 2008, 2009; de Blok+2010

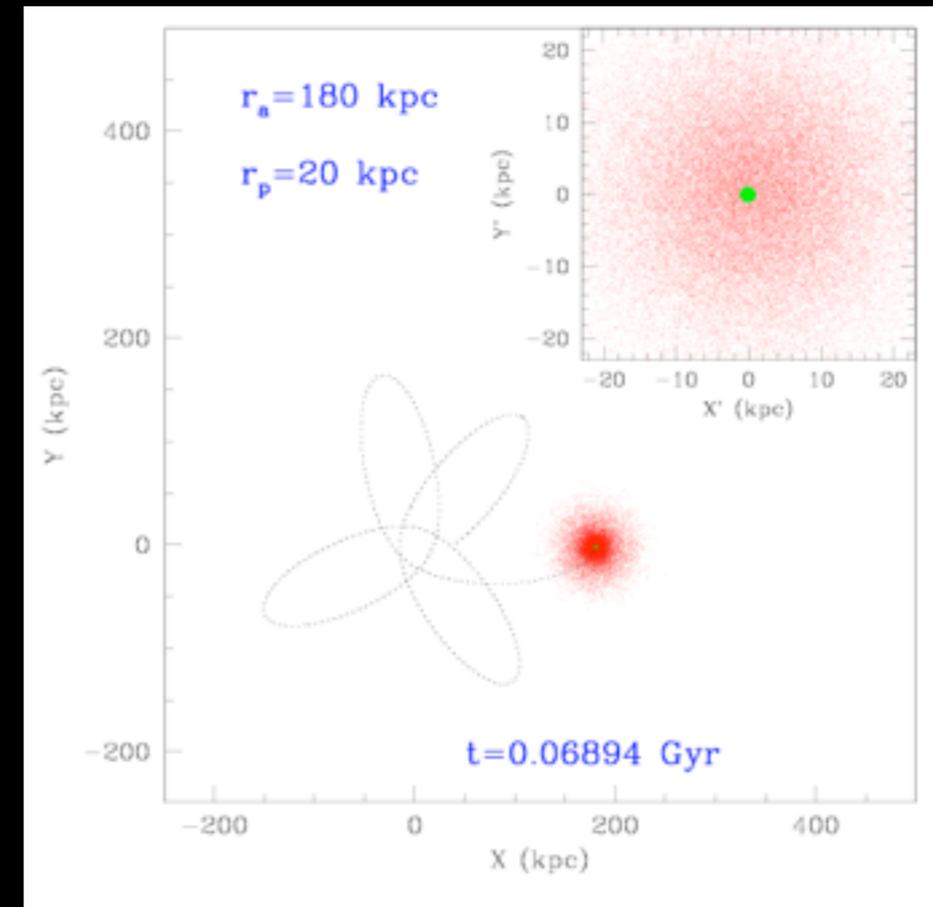
# Impact of cored DM profiles on Galaxy formation



Peñarrubia+2010

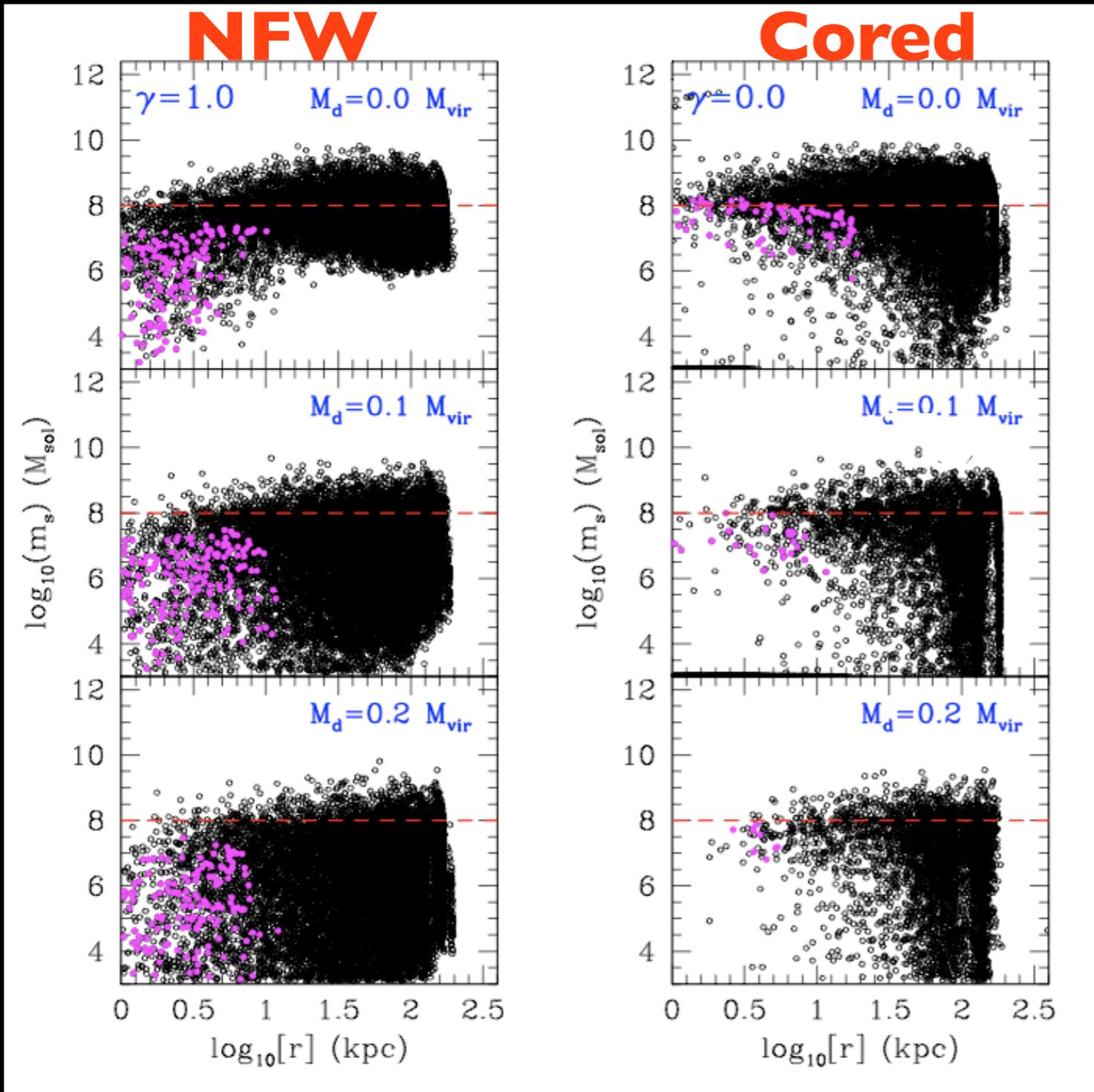
## N-body simulations:

- \*  $6 \times 10^5$  particles,
- \* resolution = 10 pc



**Cuspy haloes ( $\gamma \geq 1$ ) cannot be disrupted by the host tidal field**

# Impact of cored DM profiles on Galaxy formation



$$M_{\text{sat}}(\tau_{\text{acc}}) \geq 10^8 M_{\text{sol}}$$

(possibly luminous)

**Galactic discs deplete inner regions from satellites**



- \* number of tidal streams?
- \* stellar halo profile?

Peñarrubia+2010

## Summary

- 1) Wide binaries in dSphs probe the existence of **dark** substructures
- 2) We have introduced a robust method to measure the mass profiles of pressure-supported galaxies with multiple stellar components
- 3) Applied to dSphs it **rules out NFW profiles** (Fornax~96%; Sculptor~99%)
- 4) This is in tension with CDM hydrodynamical simulations that follow the formation of (field) dSphs (Sawala+10; Parry+12)
- 5) The presence of DM cores in satellite galaxies has a strong impact on their **mass evolution** in the MW tidal field, as well as on the formation of **stellar halo**

## Future work

- 1) Increase the sample of stars with measured radial velocities in MW dSphs
- 2) N-body simulations of the Milky Way formation where satellites are embedded in a cored DM profile



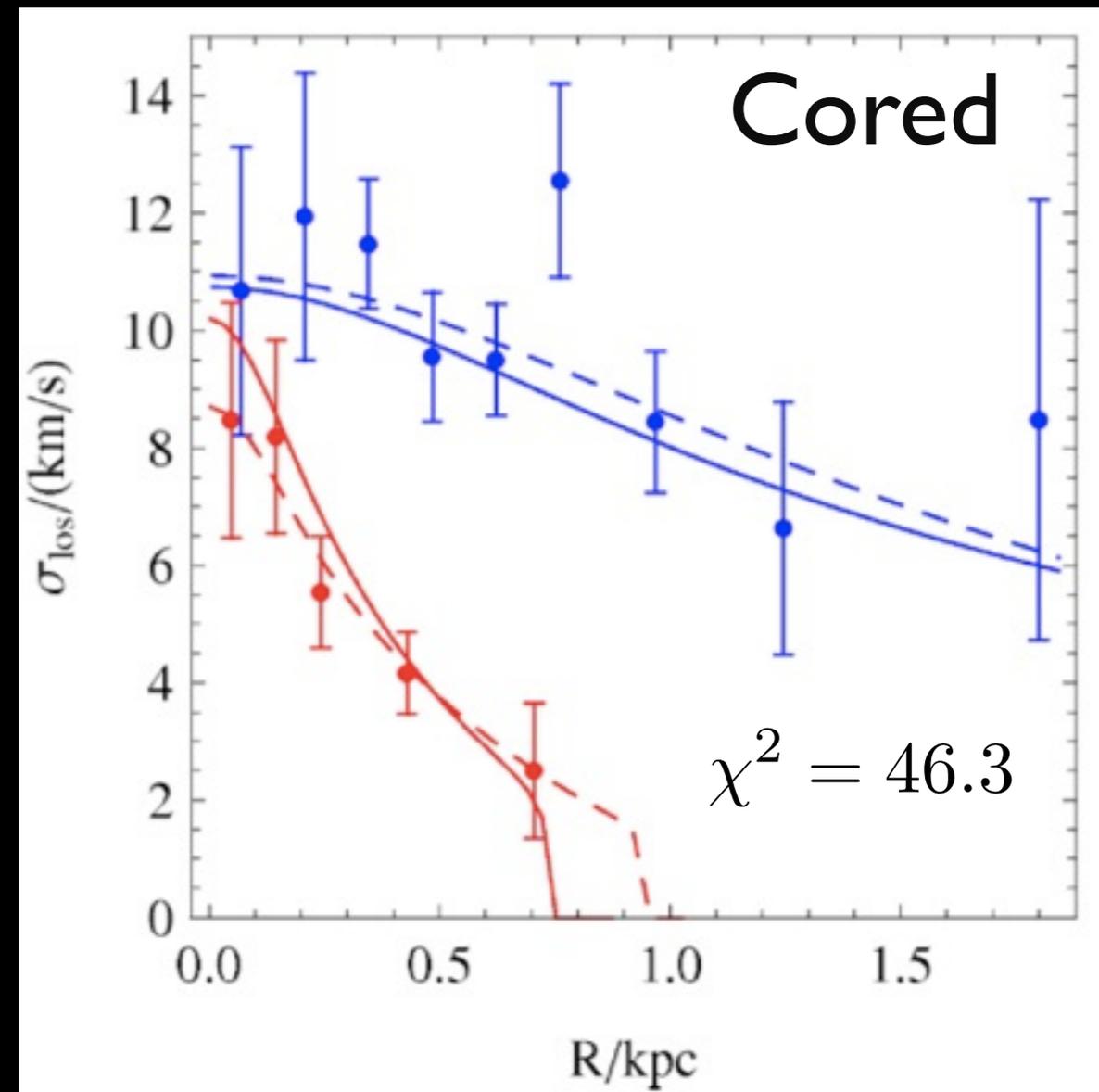
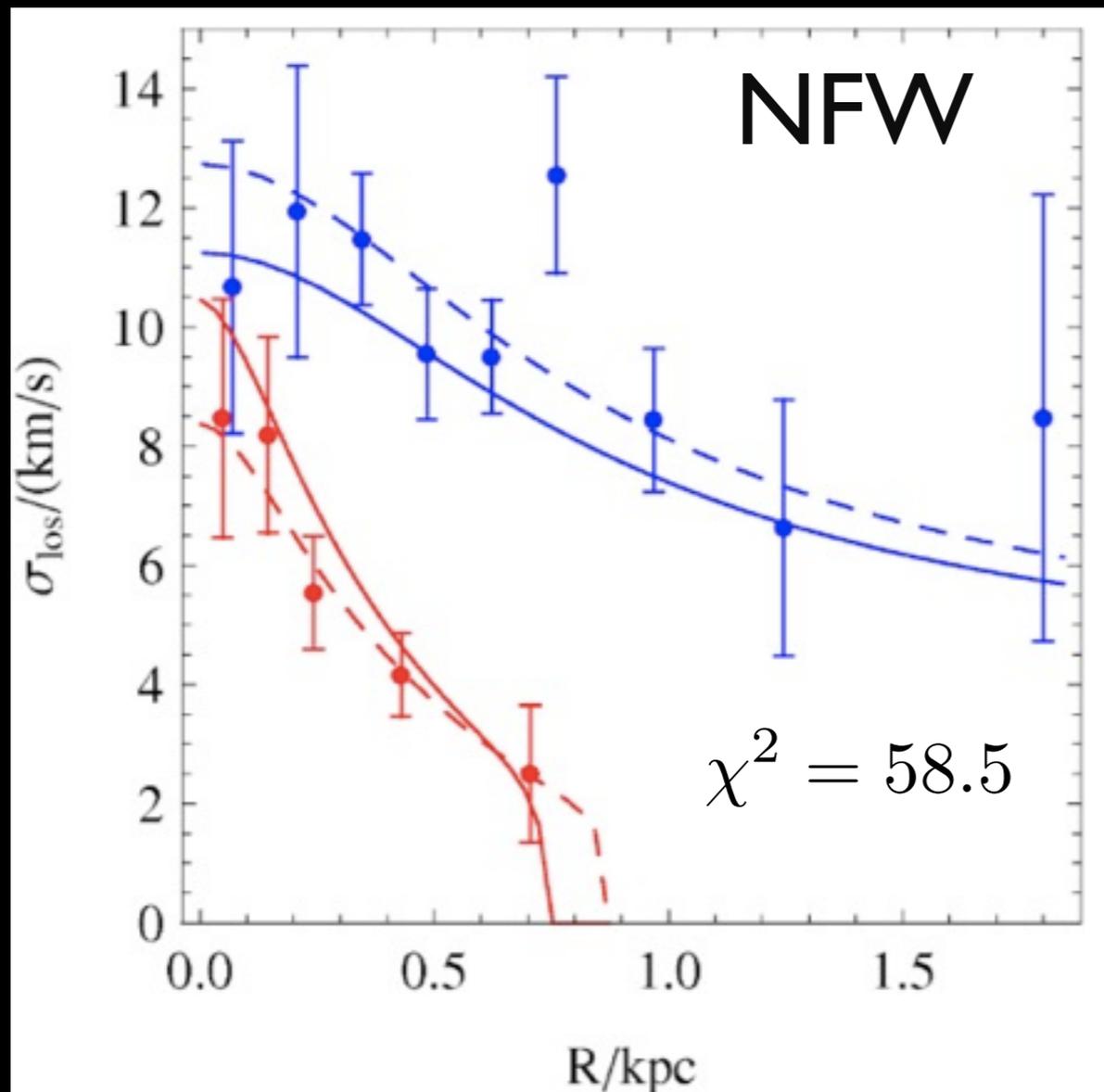
# Dynamical models

Amorisco & Evans (2012) bin projected velocities  
and fit Michie-King DFs to **Sculptor**\*

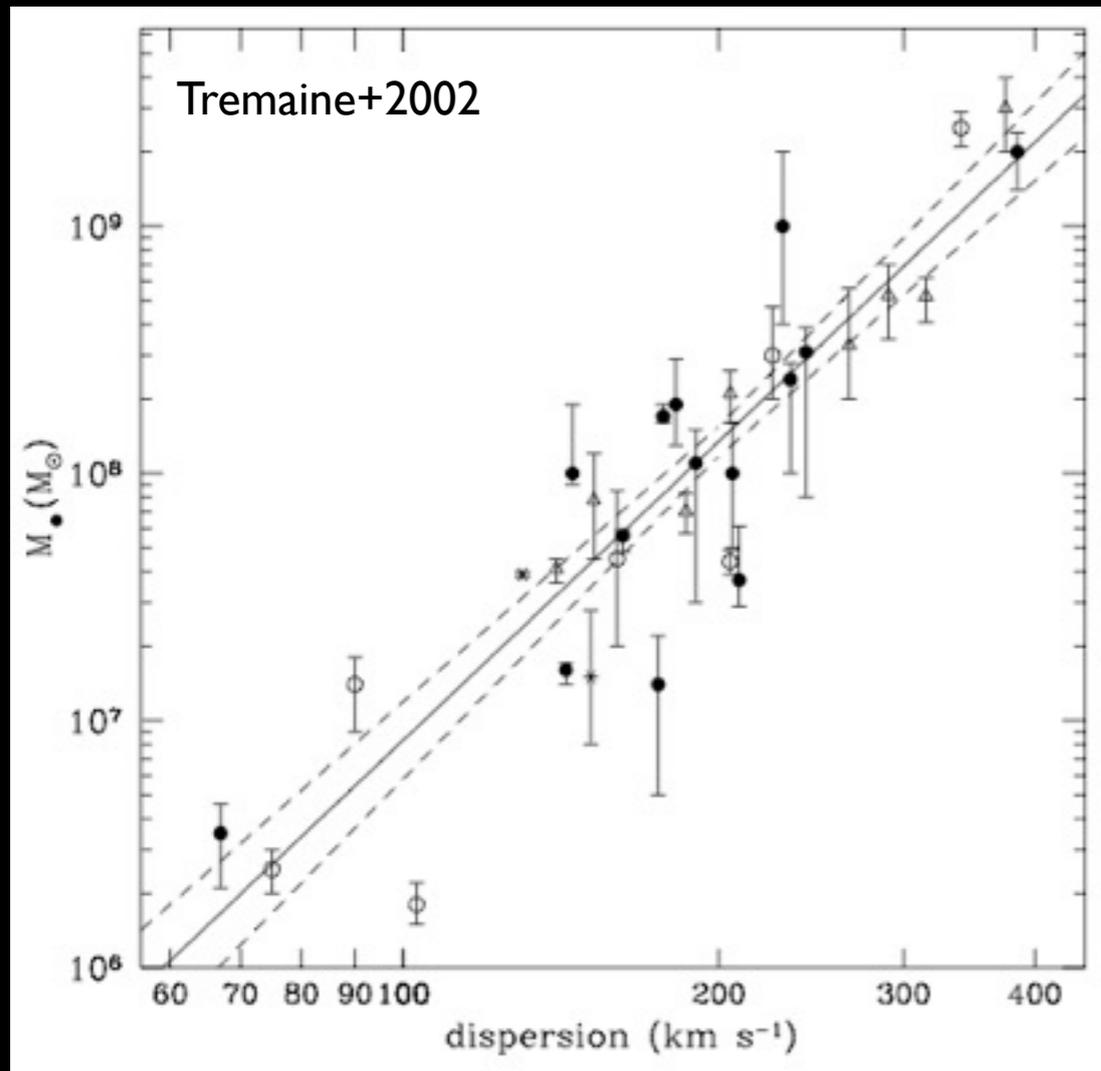
\***metallicity cut**  
\***model dependent**



uncertainties?



# Black Holes in dSphs?



tight correlation between the mass of the central BH and the galaxy luminosity in pressure-supported galaxies

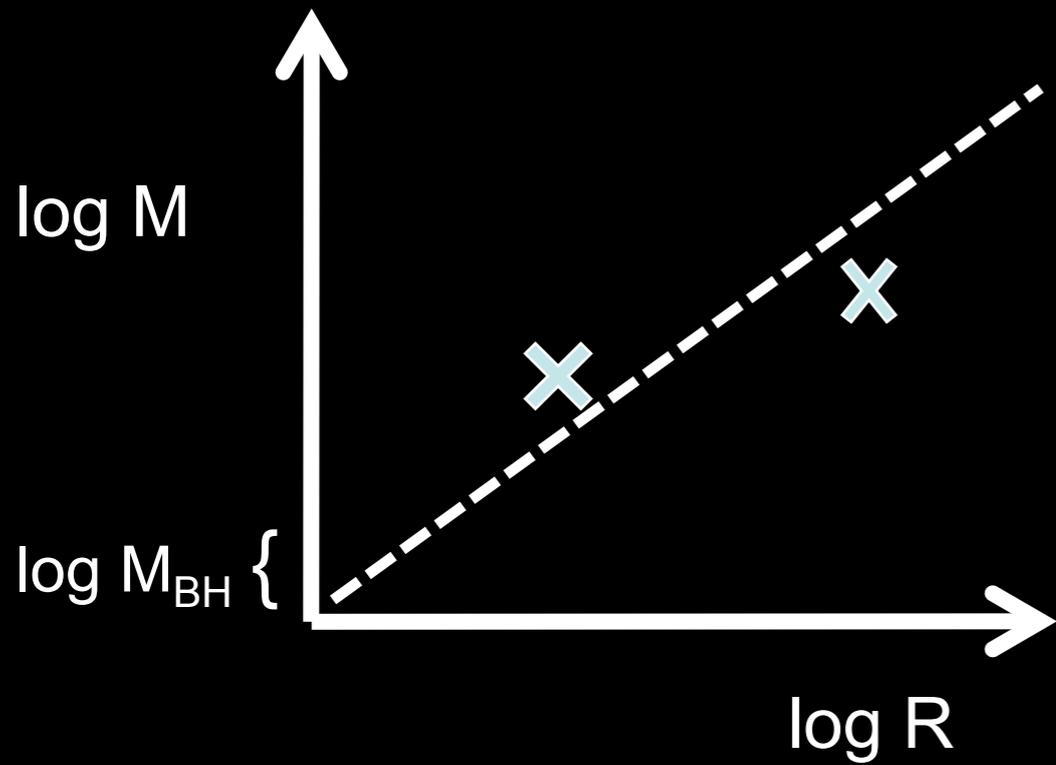
Gebhardt+ 2000; Tremaine+2002; Ferrarese & Ford 2005; Hu 2008; Gadotti & Kauffmann 2009

$$M_{\text{BH}} \sim 10^8 M_{\odot} \left( \frac{\sigma_{\star}}{200 \text{ km s}^{-1}} \right)^{3.75}$$

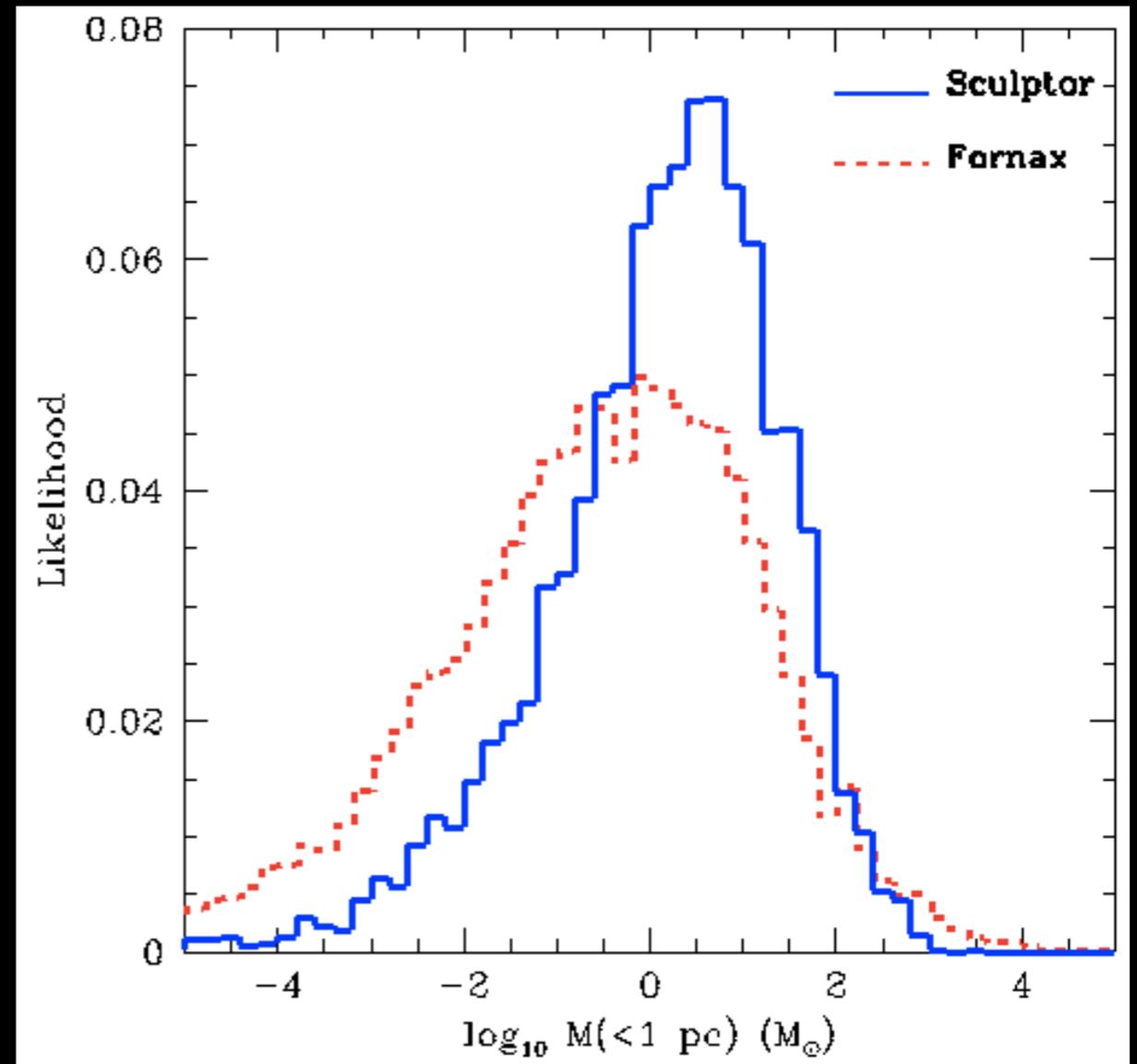


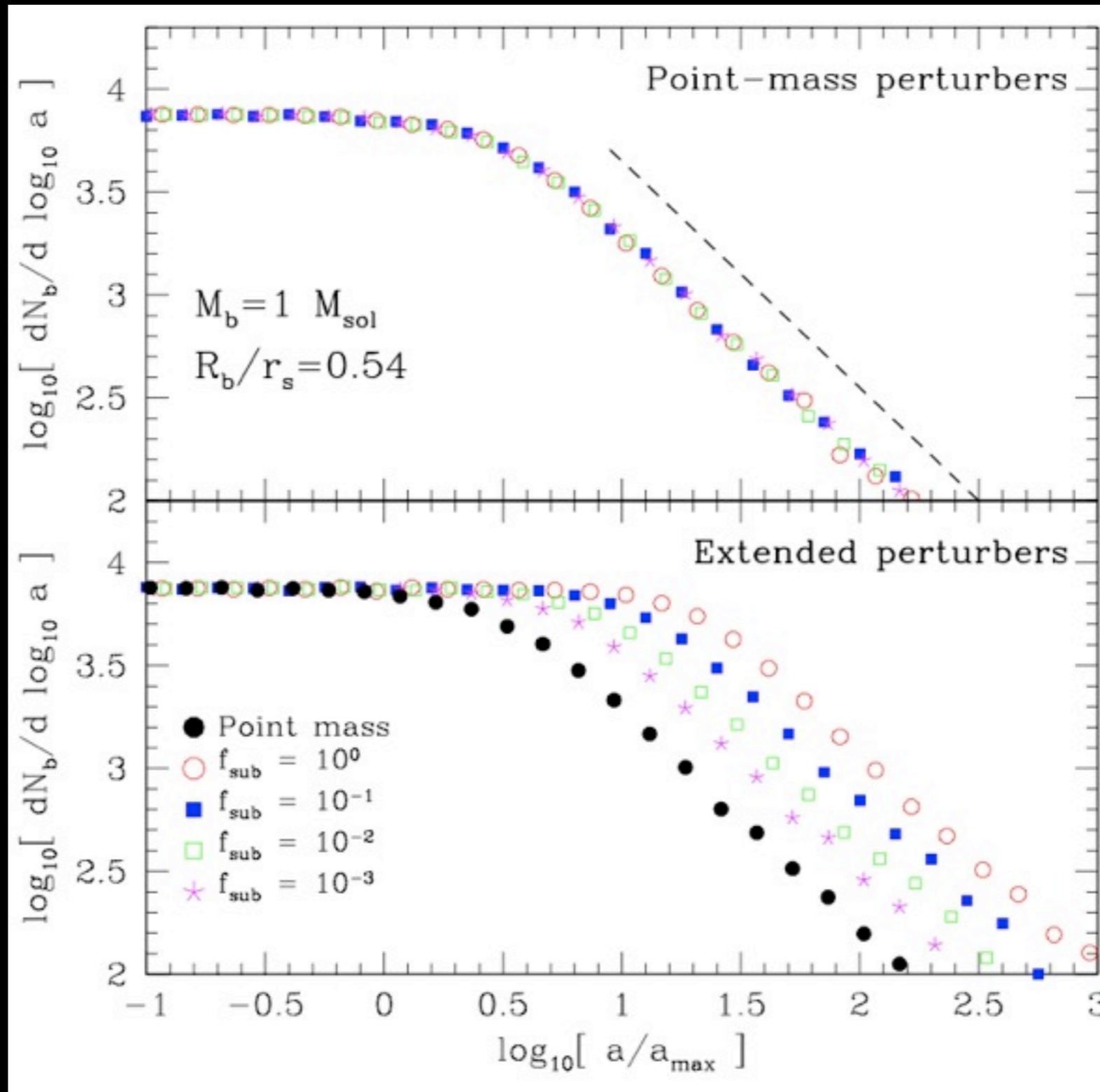
$$M_{\text{BH,dSph}} \sim 10^3 M_{\text{sol}}$$

# Black Holes in dSphs?



**No clear evidence for  
BHs**

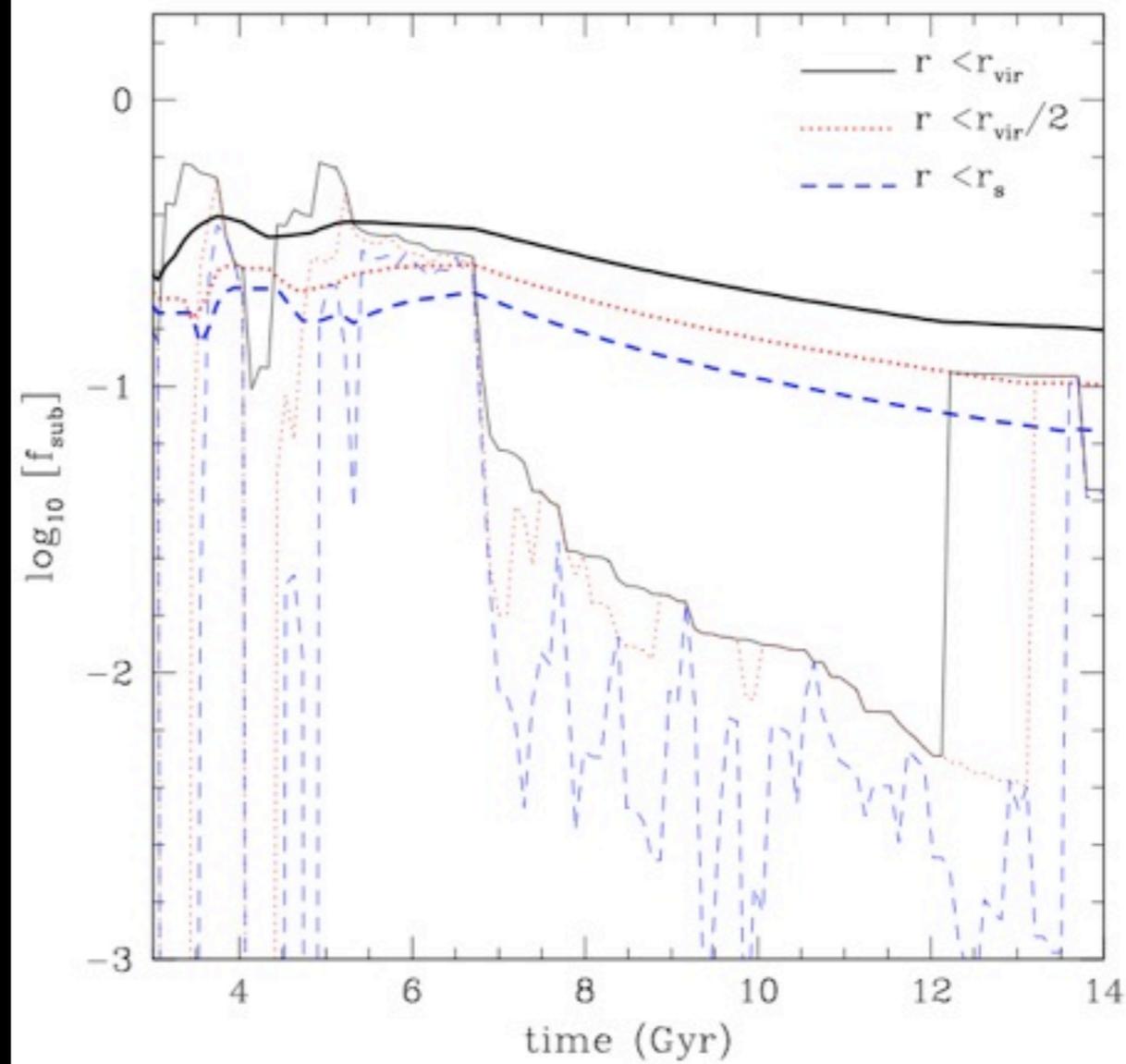




$z = 48.4$

$T = 0.05 \text{ Gyr}$

500 kpc



# TESTS

## Synthetic data sets

(self-consistently calculated *by M. Wilkinson* from distribution functions)

### 1- stellar distribution

$$\nu_*(r) = \nu_0 \left( \frac{r}{r_*} \right)^{-\gamma_*} \left[ 1 + \left( \frac{r}{r_*} \right)^{\alpha_*} \right]^{(\gamma_* - \beta_*) / \alpha_*}$$

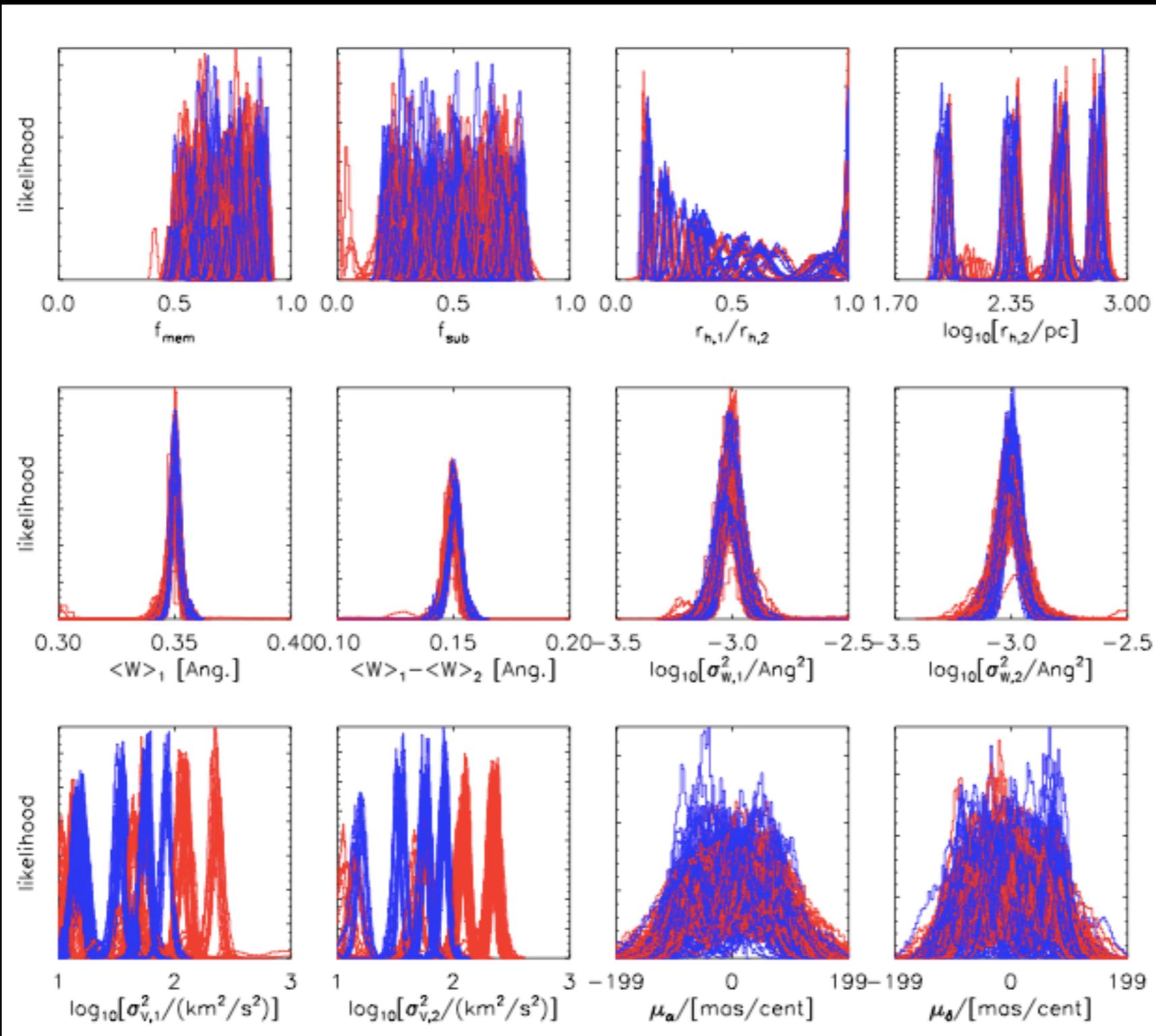
### 2- stellar kinematics

$$\rho_{\text{DM}}(r) = \rho_0 \left( \frac{r}{r_{\text{DM}}} \right)^{\gamma_{\text{DM}}} \left[ 1 + \left( \frac{r}{r_{\text{DM}}} \right)^{\alpha_{\text{DM}}} \right]^{(\gamma_{\text{DM}} - \beta_{\text{DM}}) / \alpha_{\text{DM}}}$$

TABLE 3  
TESTS ON SYNTHETIC DATA: INPUT PARAMETERS FOR DYNAMICAL TEST MODELS

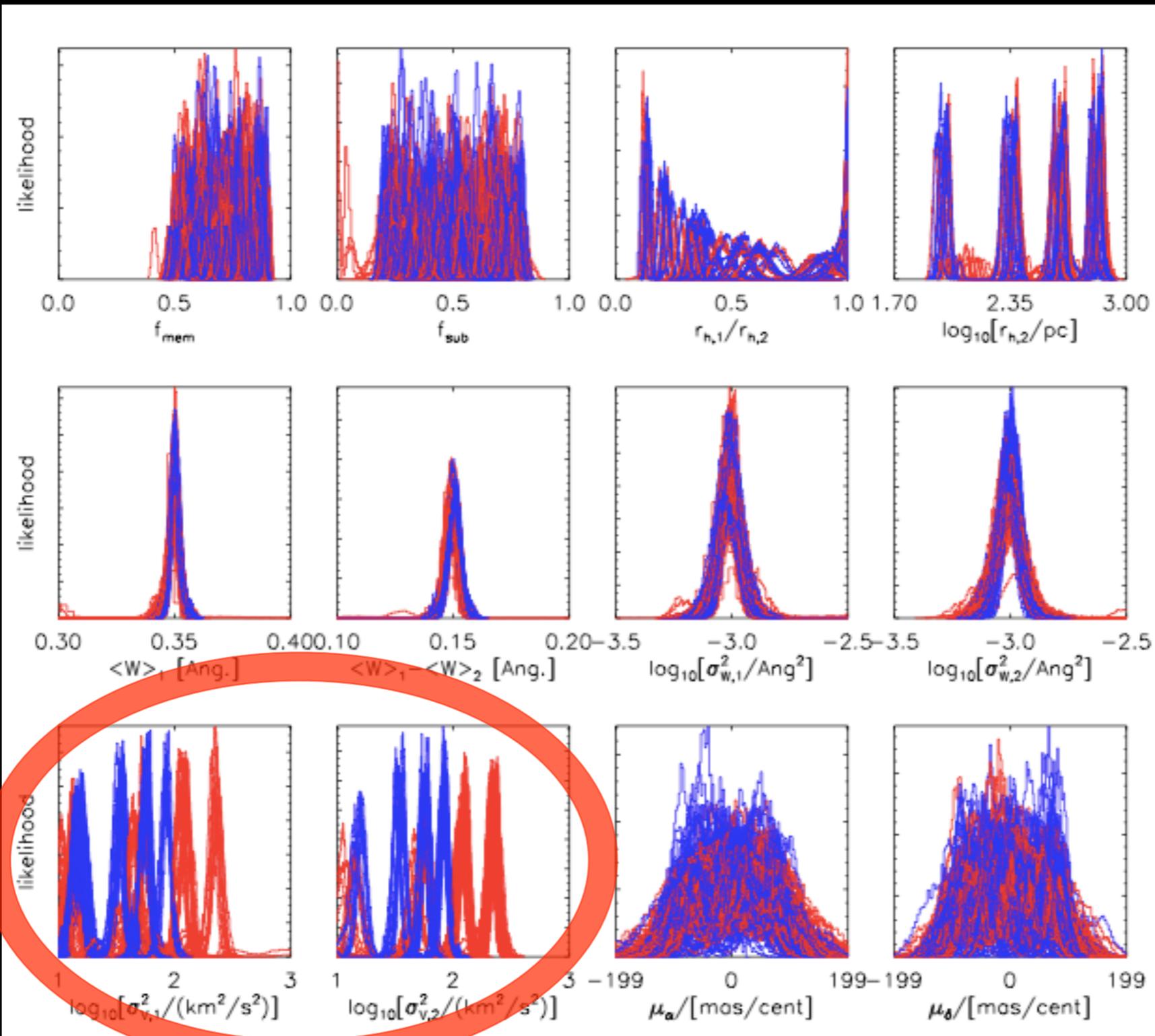
Stellar Profile (Equation 14)					Dark Matter Profile (Equation 15)				
$\beta_{\text{ani}}$	$r_*$ [pc]	$\alpha_*$	$\beta_*$	$\gamma_*$	$\rho_0$ [ $M_{\odot} \text{pc}^{-3}$ ]	$r_{\text{DM}}$ [pc]	$\alpha_{\text{DM}}$	$\beta_{\text{DM}}$	$\gamma_{\text{DM}}$
Cored Halos									
Isotropic									
0.00	100	2	5	0.0	0.064	1000	2	3.1	0.0
0.00	250	2	5	0.0	0.064	1000	2	3.1	0.0
0.00	500	2	5	0.0	0.064	1000	2	3.1	0.0
0.00	1000	2	5	0.0	0.064	1000	2	3.1	0.0
Radially Anisotropic									
+0.25	100	2	5	0.6	0.064	1000	2	3.1	0.0
+0.25	250	2	5	0.6	0.064	1000	2	3.1	0.0
+0.25	500	2	5	0.6	0.064	1000	2	3.1	0.0
+0.25	1000	2	5	0.6	0.064	1000	2	3.1	0.0
Tangentially Anisotropic									
-0.45	100	2	5	0.0	0.064	1000	2	3.1	0.0
-0.45	250	2	5	0.0	0.064	1000	2	3.1	0.0
-0.45	500	2	5	0.0	0.064	1000	2	3.1	0.0
-0.45	1000	2	5	0.0	0.064	1000	2	3.1	0.0
Cusped Halos									
Isotropic									
0.00	100	2	5	0.1	0.014	1000	2	3.1	0.9
0.00	250	2	5	0.1	0.014	1000	2	3.1	0.9
0.00	500	2	5	0.1	0.014	1000	2	3.1	0.9
0.00	1000	2	5	0.1	0.014	1000	2	3.1	0.9
Radially Anisotropic									
+0.25	100	2	5	0.6	0.014	1000	2	3.1	0.9
+0.25	250	2	5	0.6	0.014	1000	2	3.1	0.9
+0.25	500	2	5	0.6	0.014	1000	2	3.1	0.9
+0.25	1000	2	5	0.6	0.014	1000	2	3.1	0.9
Tangentially Anisotropic									
-0.45	100	2	5	0.1	0.014	1000	2	3.1	0.9
-0.45	250	2	5	0.1	0.014	1000	2	3.1	0.9
-0.45	500	2	5	0.1	0.014	1000	2	3.1	0.9
-0.45	1000	2	5	0.1	0.014	1000	2	3.1	0.9

# TESTS



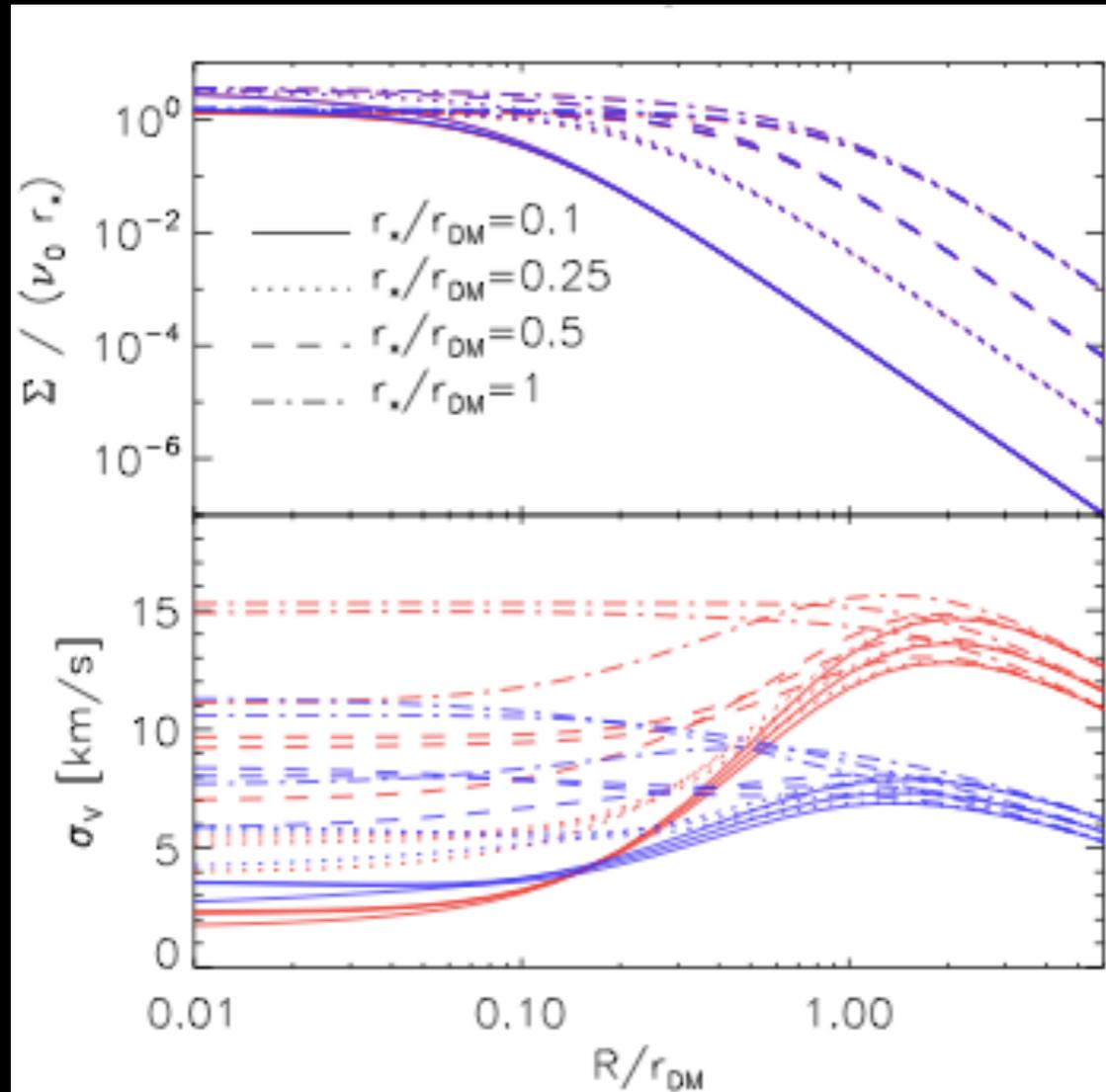
**CUSP**  
**CORE**

# TESTS

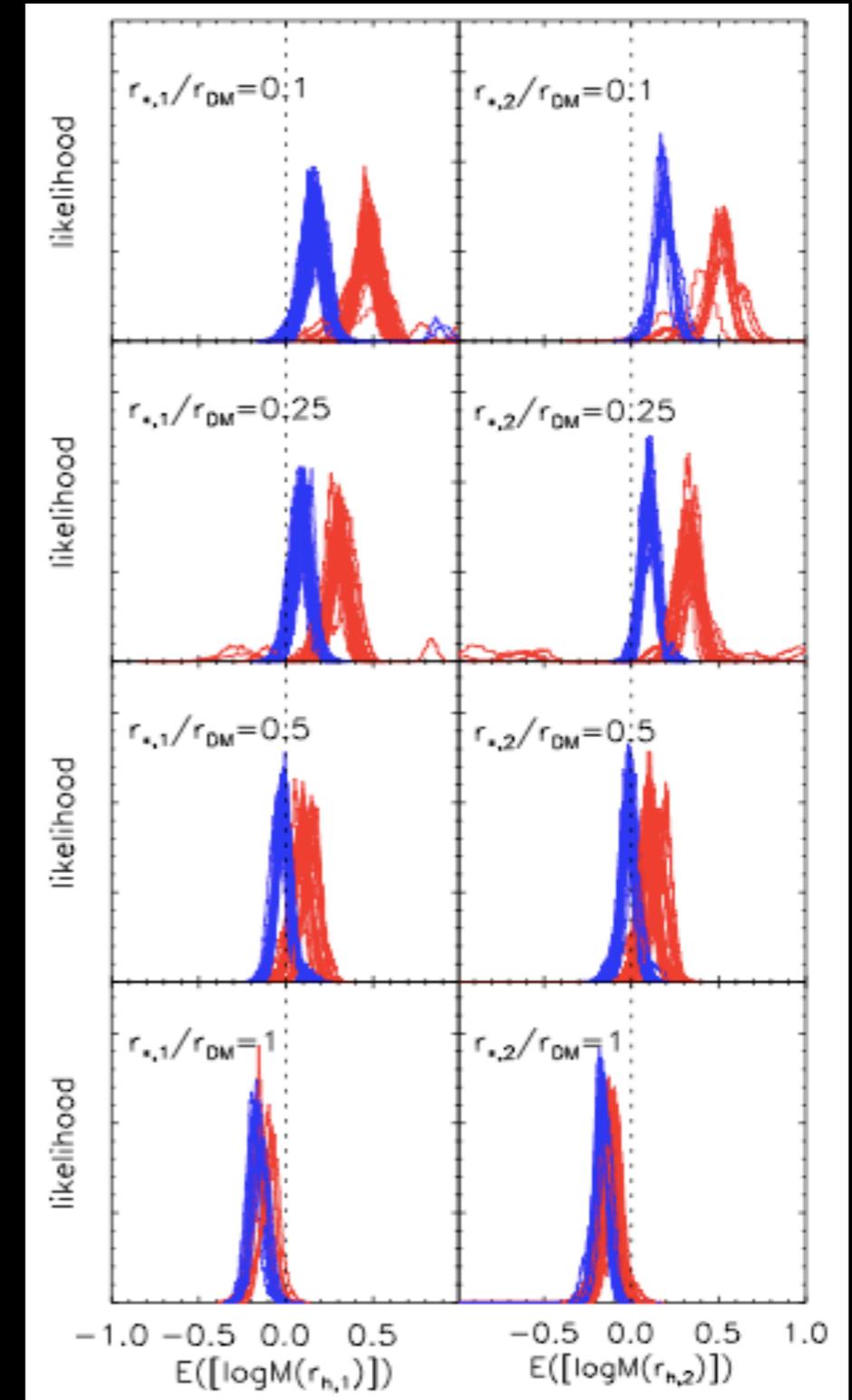


CUSP  
CORE

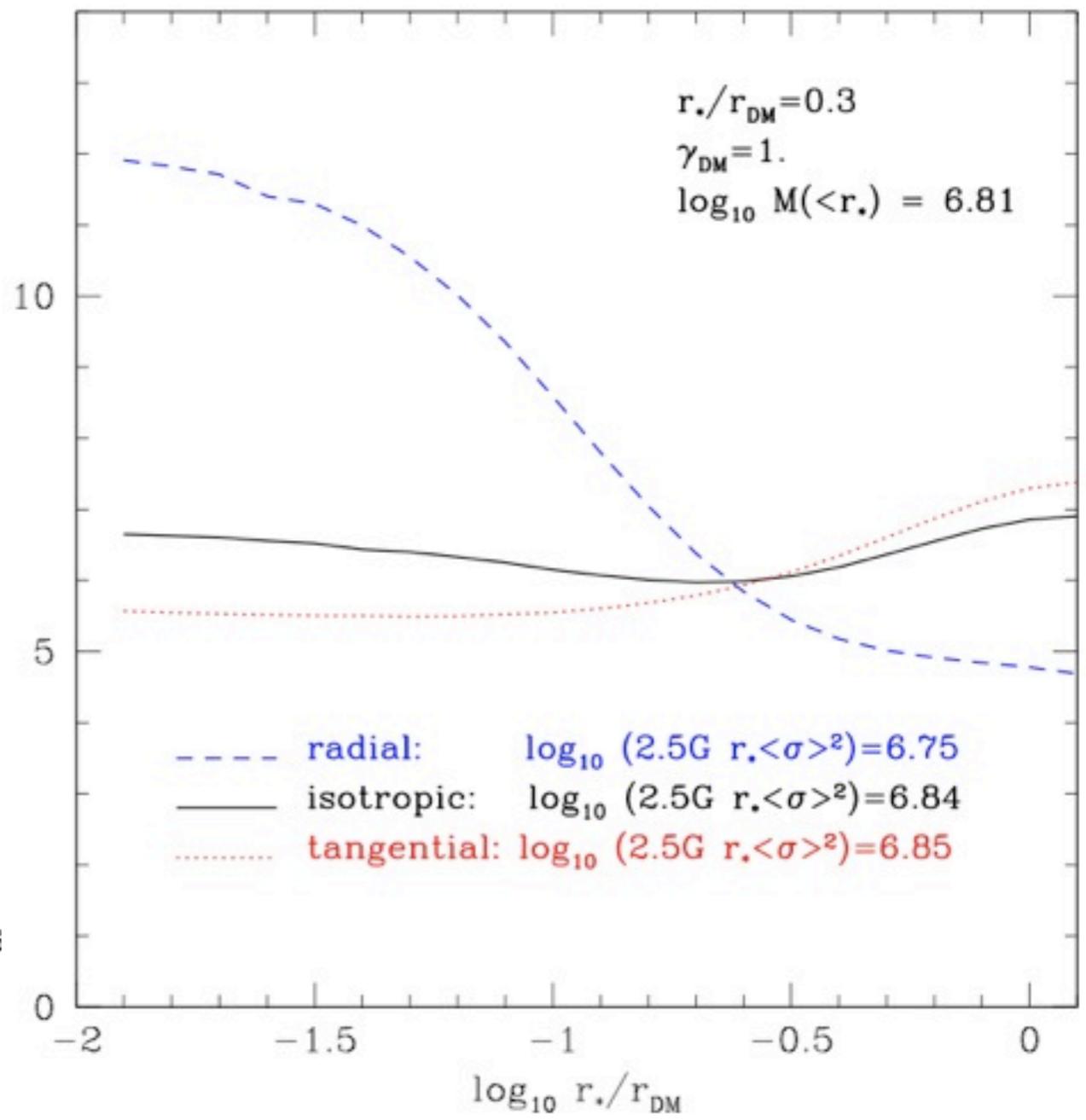
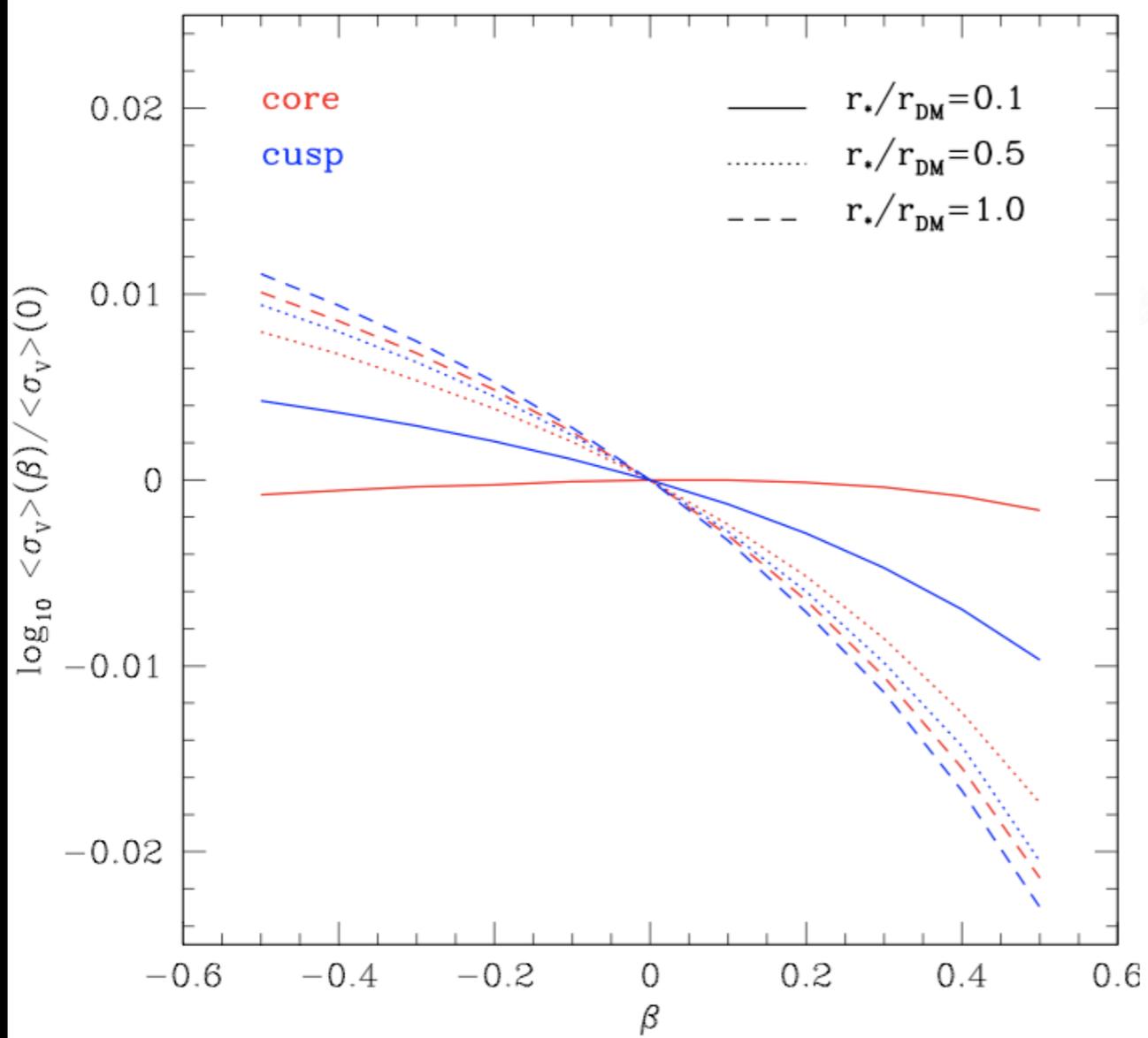
# TESTS



DM halo mass slope  
**underestimated**



$M(<R_{half})$  over-estimated as  
 $R_{half}/r_{DM} \rightarrow 0$



dSph	Distance [kpc]	$r_{\text{half}}$ [pc]	$\sigma_*$ [km s <sup>-1</sup> ]
Segue I	28 ± 2	29 ± 7	4.3 ± 1.2
Ursa Major II	36 ± 5	140 ± 25	6.7 ± 1.4
Bootes II	40 ± 8	51 ± 17	10.5 ± 7.4
Segue II	41 ± 5	34 ± 5	3.4 ± 1.8
Wilman I	43 ± 7	25 ± 6	4.3 ± 1.8
Coma	45 ± 4	77 ± 10	4.6 ± 0.8
Bootes I	64 ± 3	242 ± 21	6.5 ± 2.0
Ursa Minor	67 ± 3	280 ± 15	9.5 ± 1.2
Sculptor	79 ± 4	260 ± 39	9.2 ± 1.1
Draco	81 ± 6	196 ± 12	9.1 ± 1.2
Sextans	88 ± 4	682 ± 117	7.9 ± 1.3
Ursa Major I	100 ± 8	318 ± 45	11.9 ± 3.5
Carina	102 ± 5	241 ± 23	6.6 ± 1.2
Hercules	126 ± 12	330 ± 63	3.7 ± 0.9
Fornax	140 ± 8	668 ± 34	11.7 ± 0.9
Leo IV	160 ± 15	116 ± 30	3.3 ± 1.7
Canis Venatici II	160 ± 5	74 ± 12	4.6 ± 1.0
Leo V	180 ± 15	42 ± 5	2.4 ± 1.9
Leo II	207 ± 12	151 ± 17	6.6 ± 0.7
Canis Venatici I	217 ± 10	564 ± 36	7.6 ± 0.4
Leo I	253 ± 30	246 ± 19	9.2 ± 1.4
Leo T	411 ± 38	178 ± 39	7.5 ± 1.6

