

Scaling laws in Star & Structure formation:
Density Models fitted to Observational Data

Marco Lombardi, University of Milan

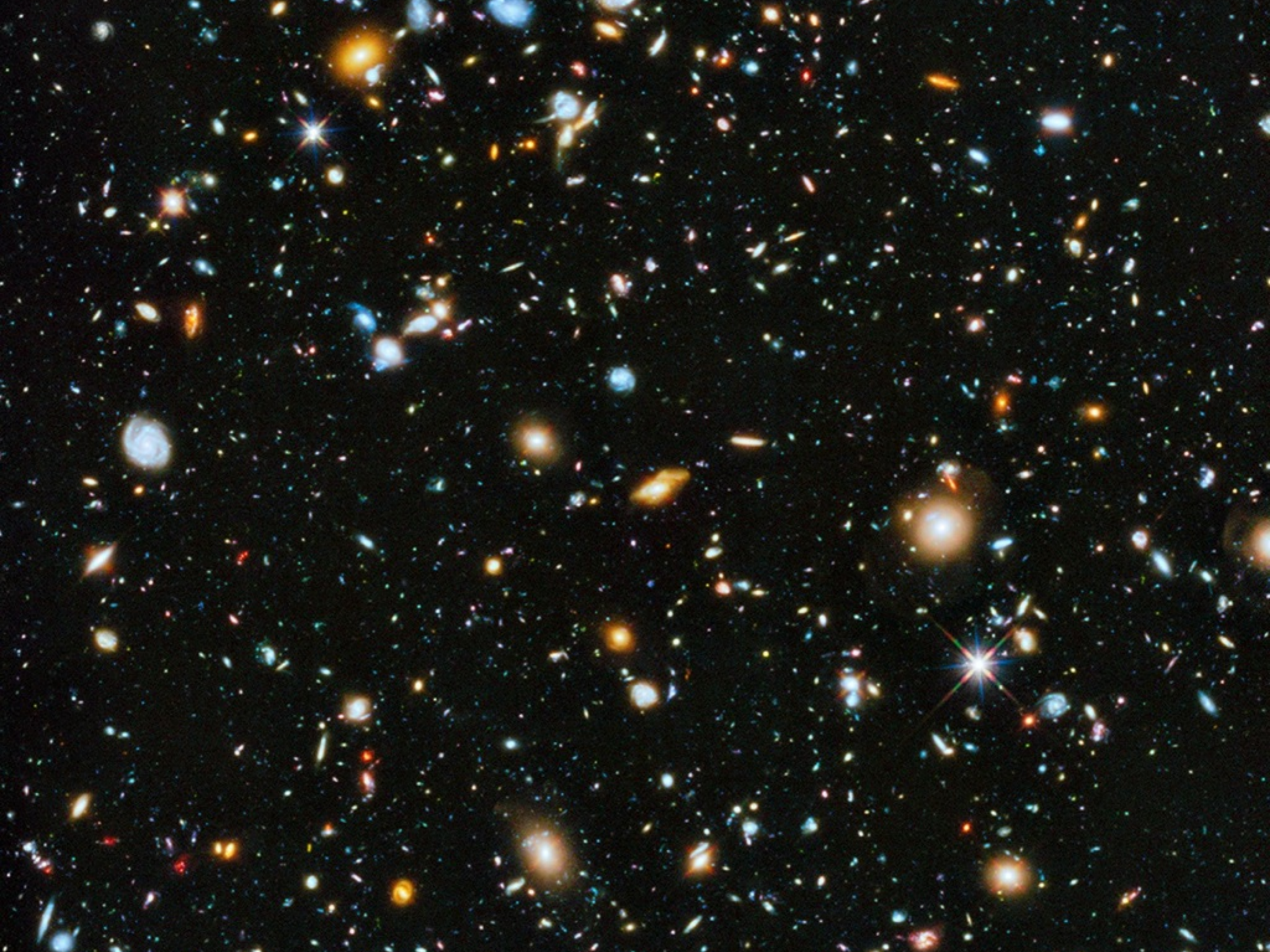
Scaling laws in Star & Structure formation:
Density Models fitted to Observational Data

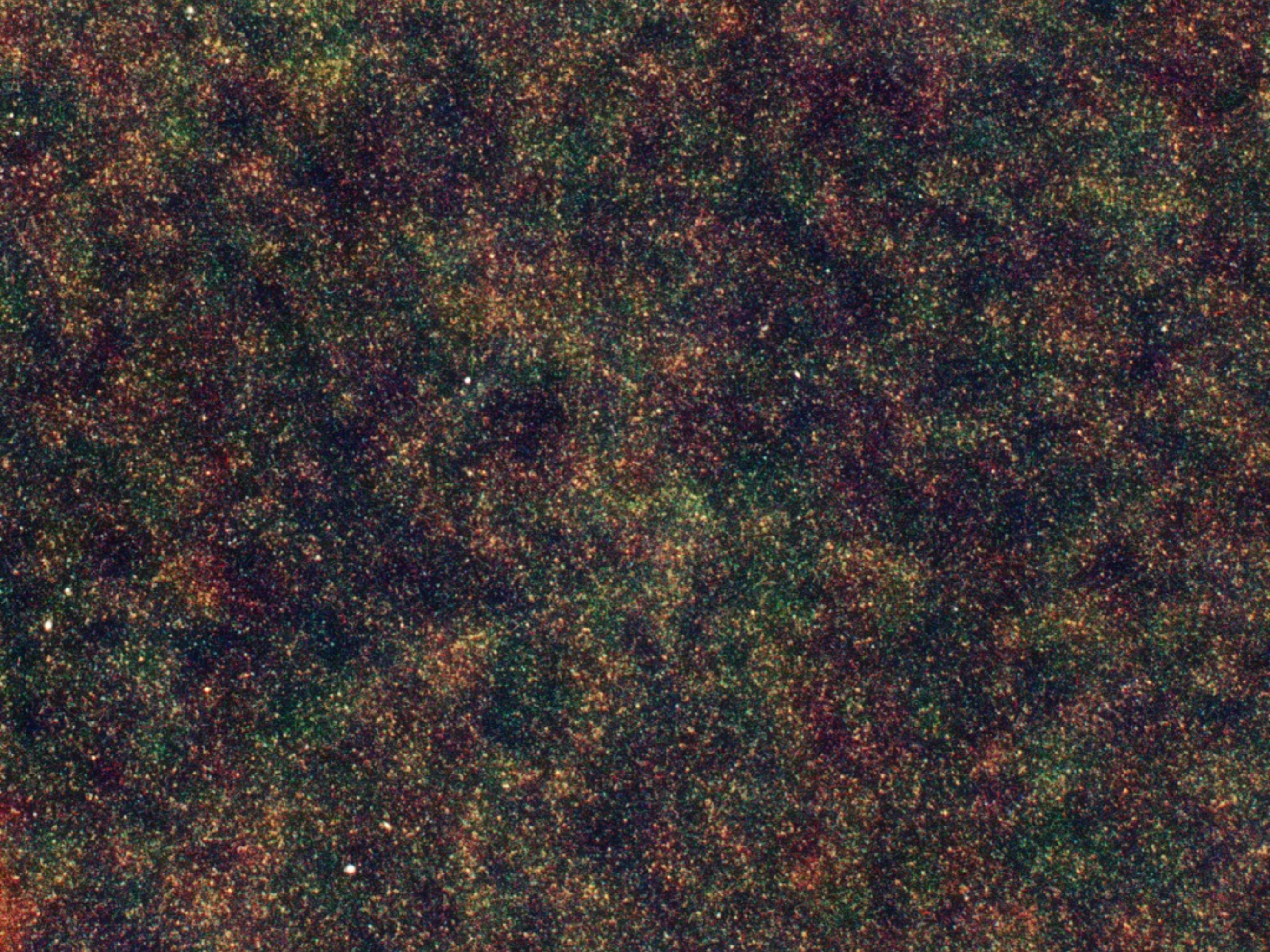
Marco Lombardi, University of Milan

with:

Charles Lada, CfA, Harvard

Joao Alves et al., University of Vienna







Pillars of star formation

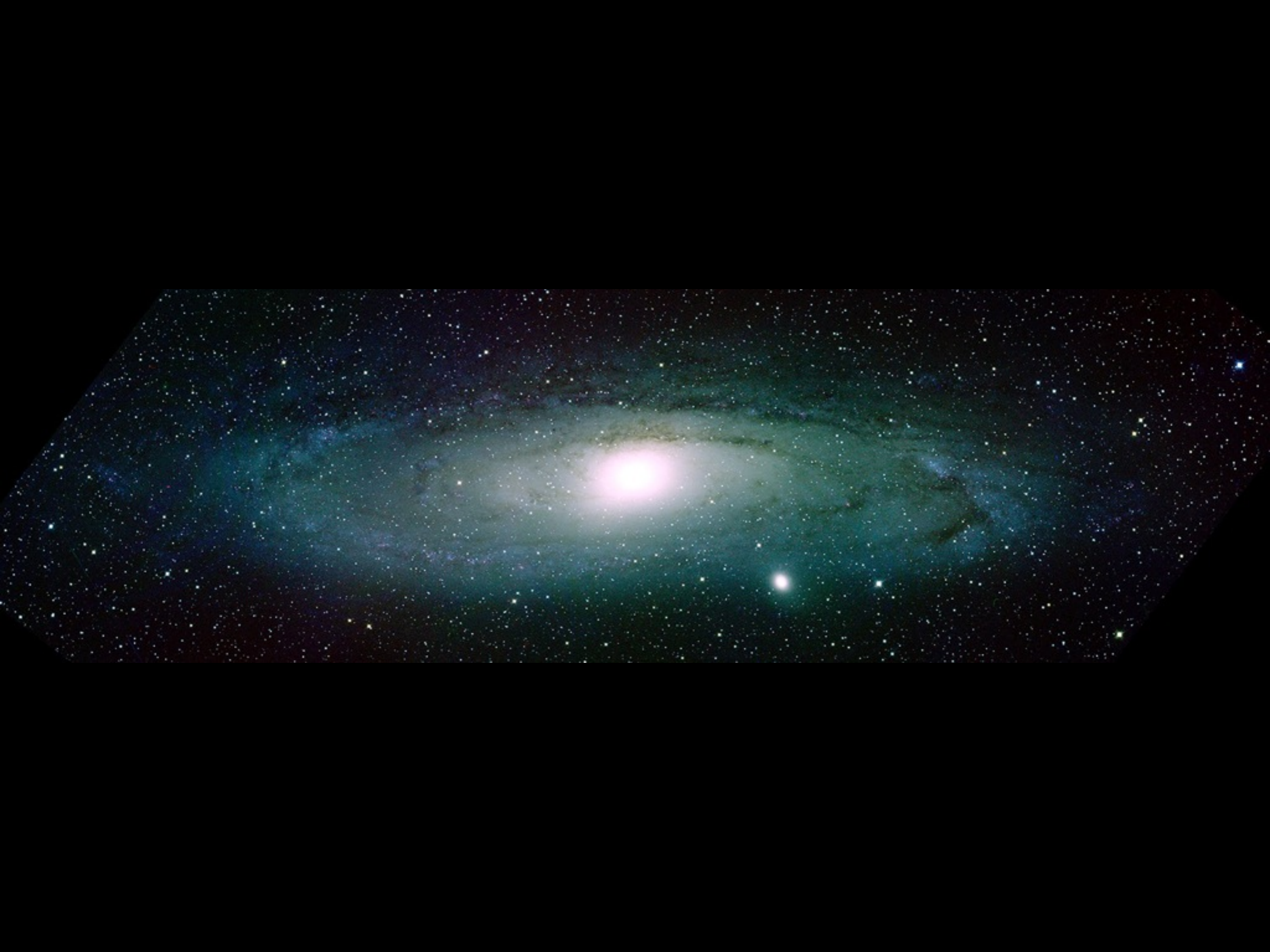
1. Stars form within dense molecular clouds
2. Star formation is a complex process
3. Different clouds have different star formation efficiencies
4. Molecular clouds have peculiar structures
5. Scaling laws play a fundamental role in SF

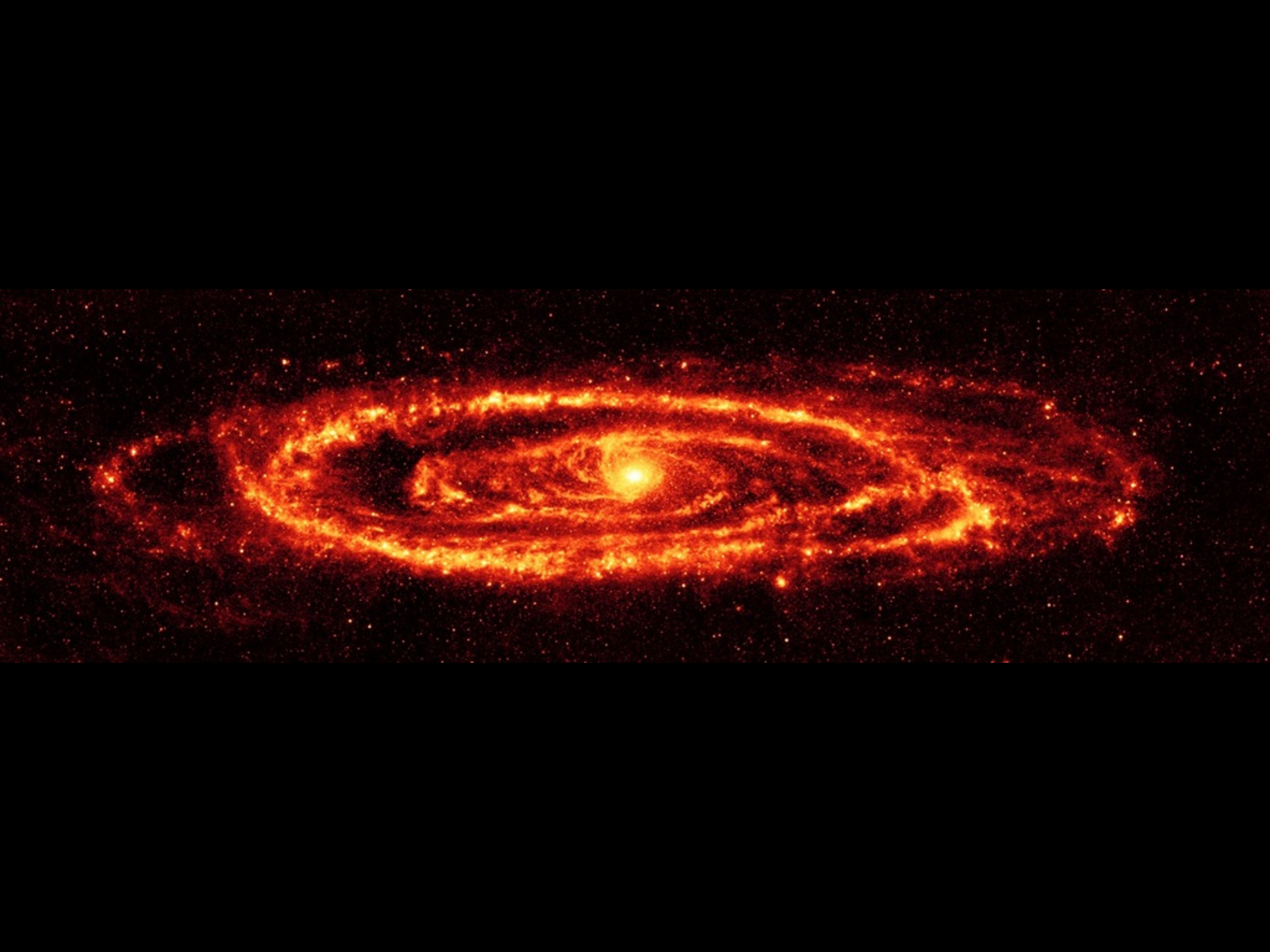
Fact I

Stars form within dense
molecular clouds













Fact 2

Star formation is a
complex process



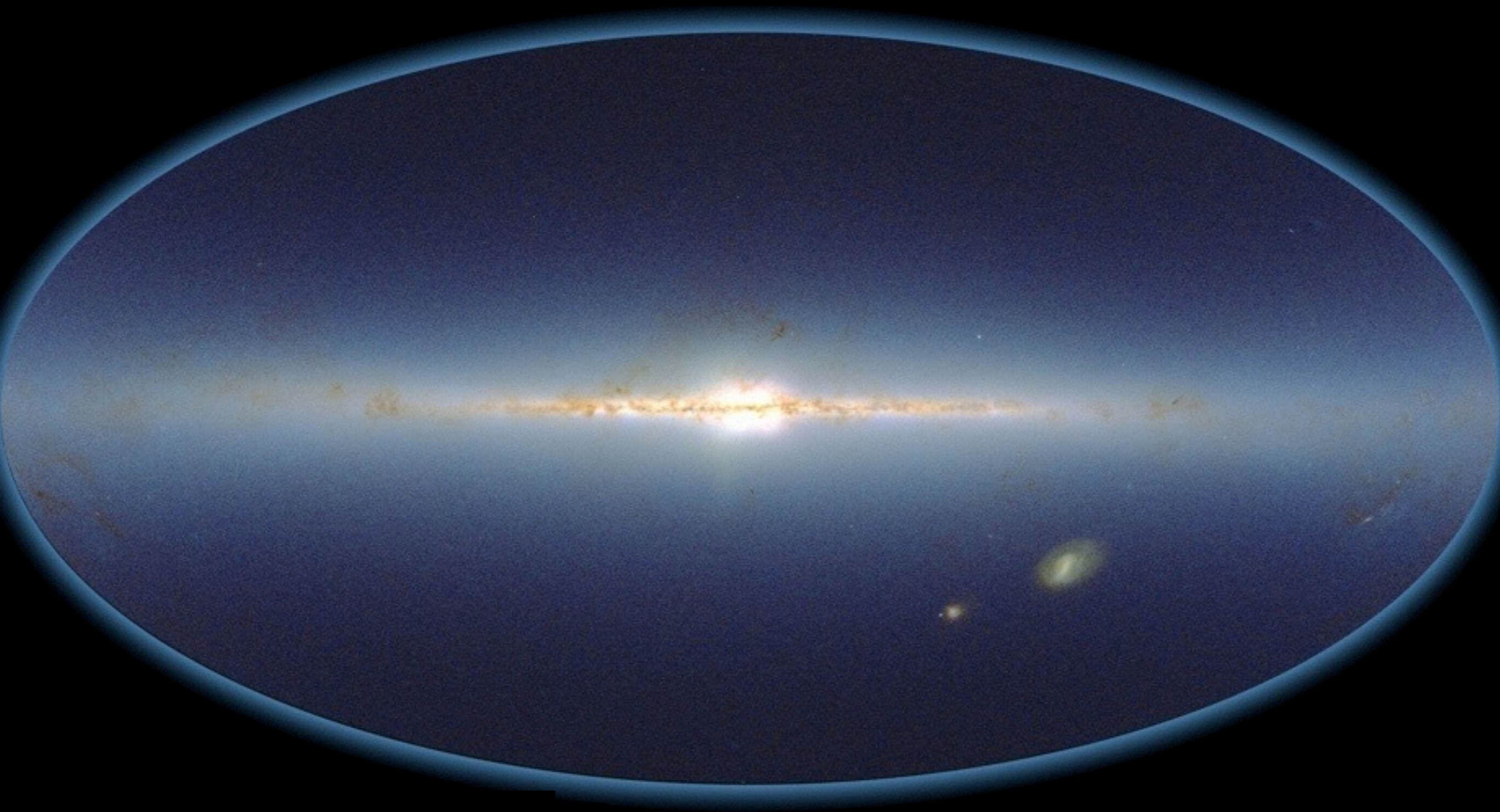




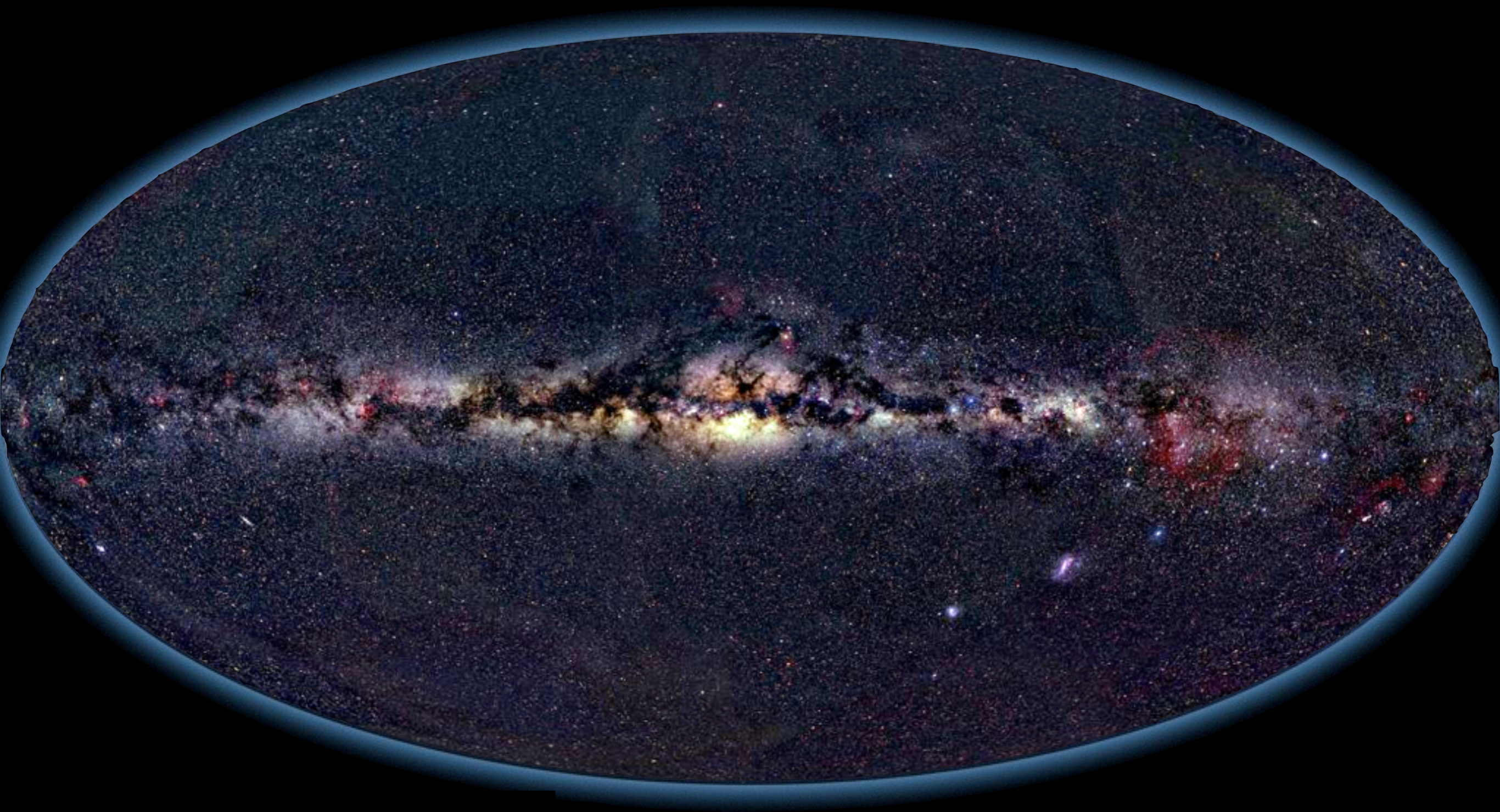




Molecular clouds in the Milky Way

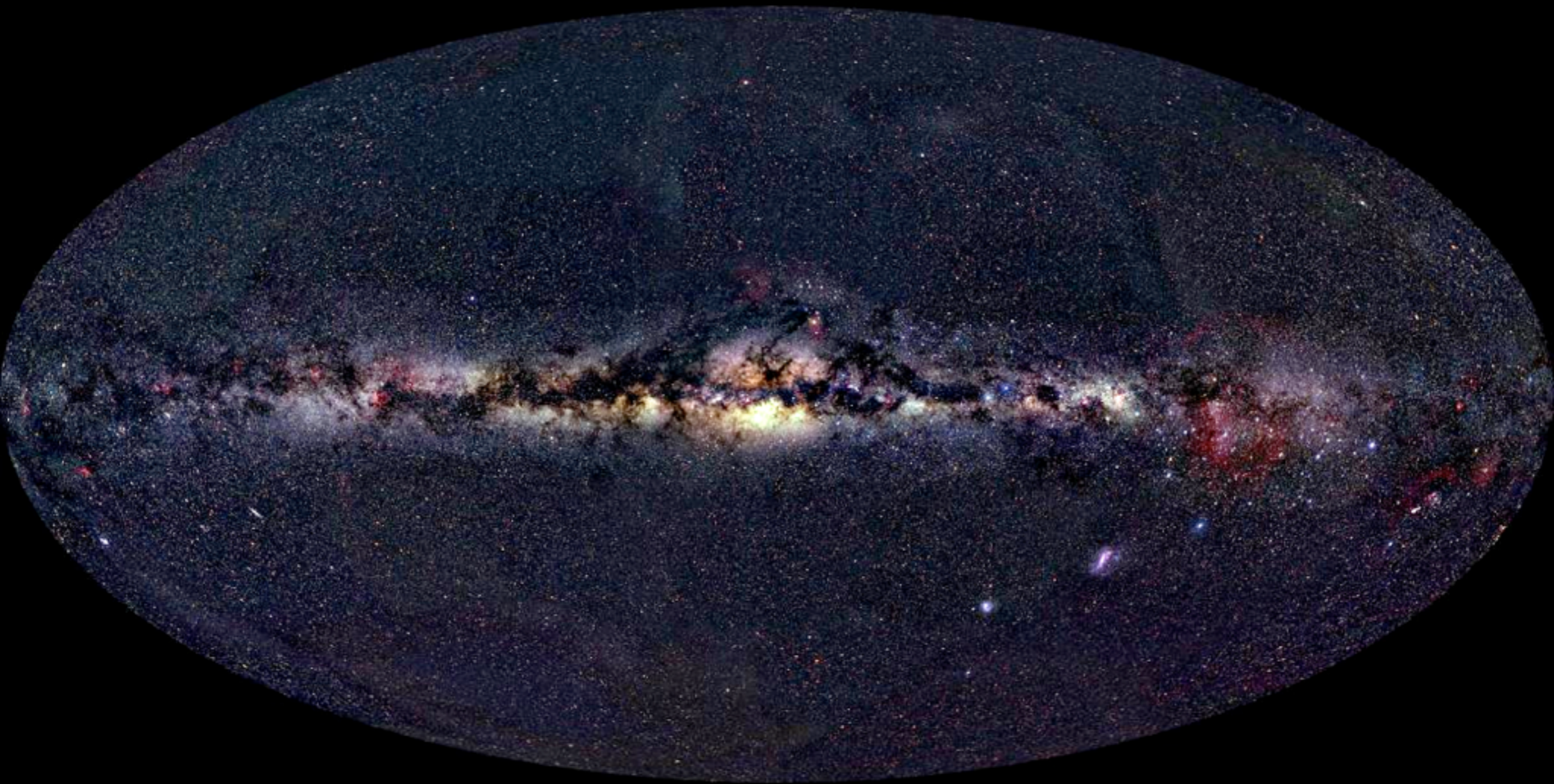


2MASS

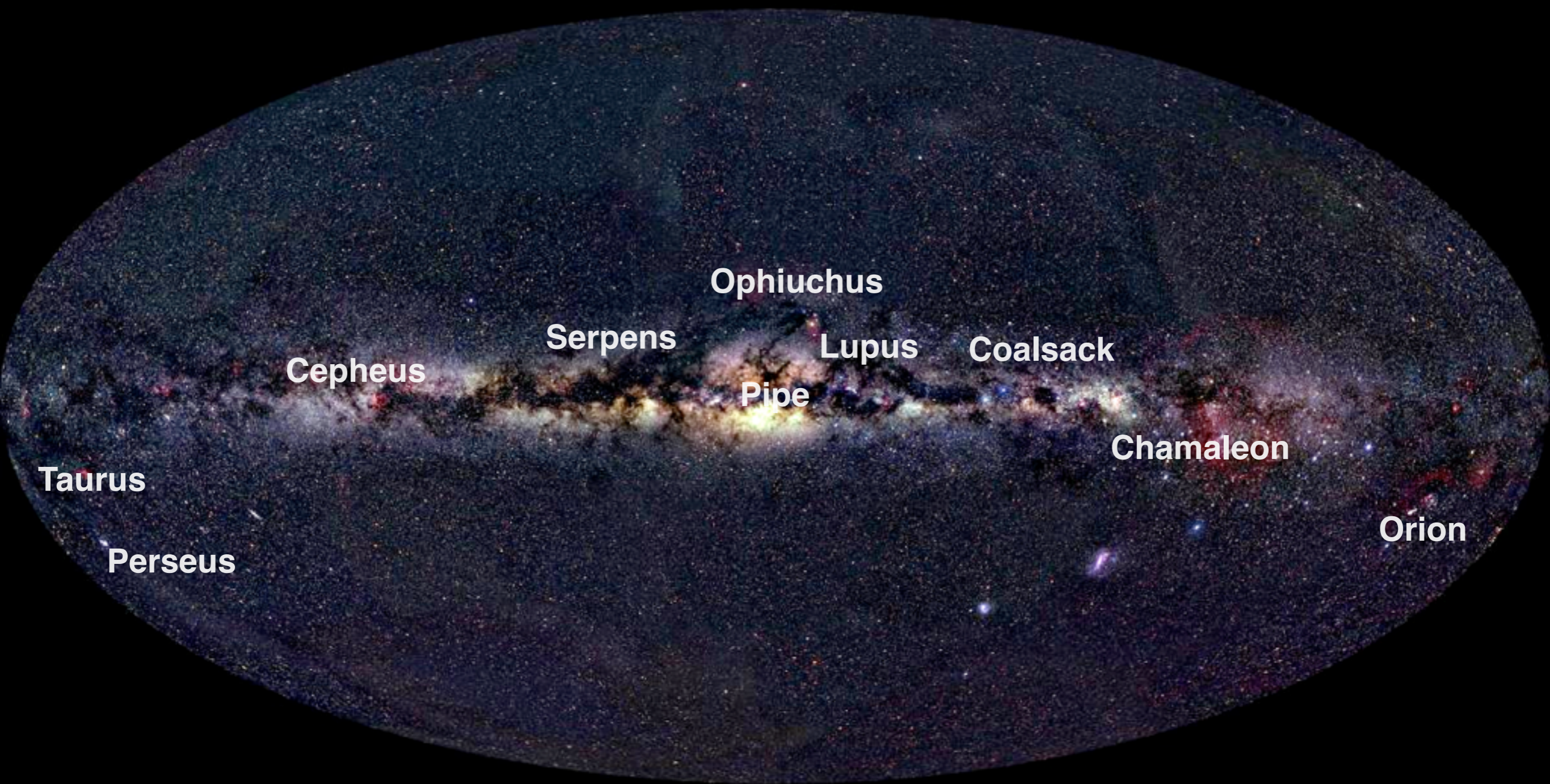


A. Mellinger

Gould belt



Gould belt



Extinction

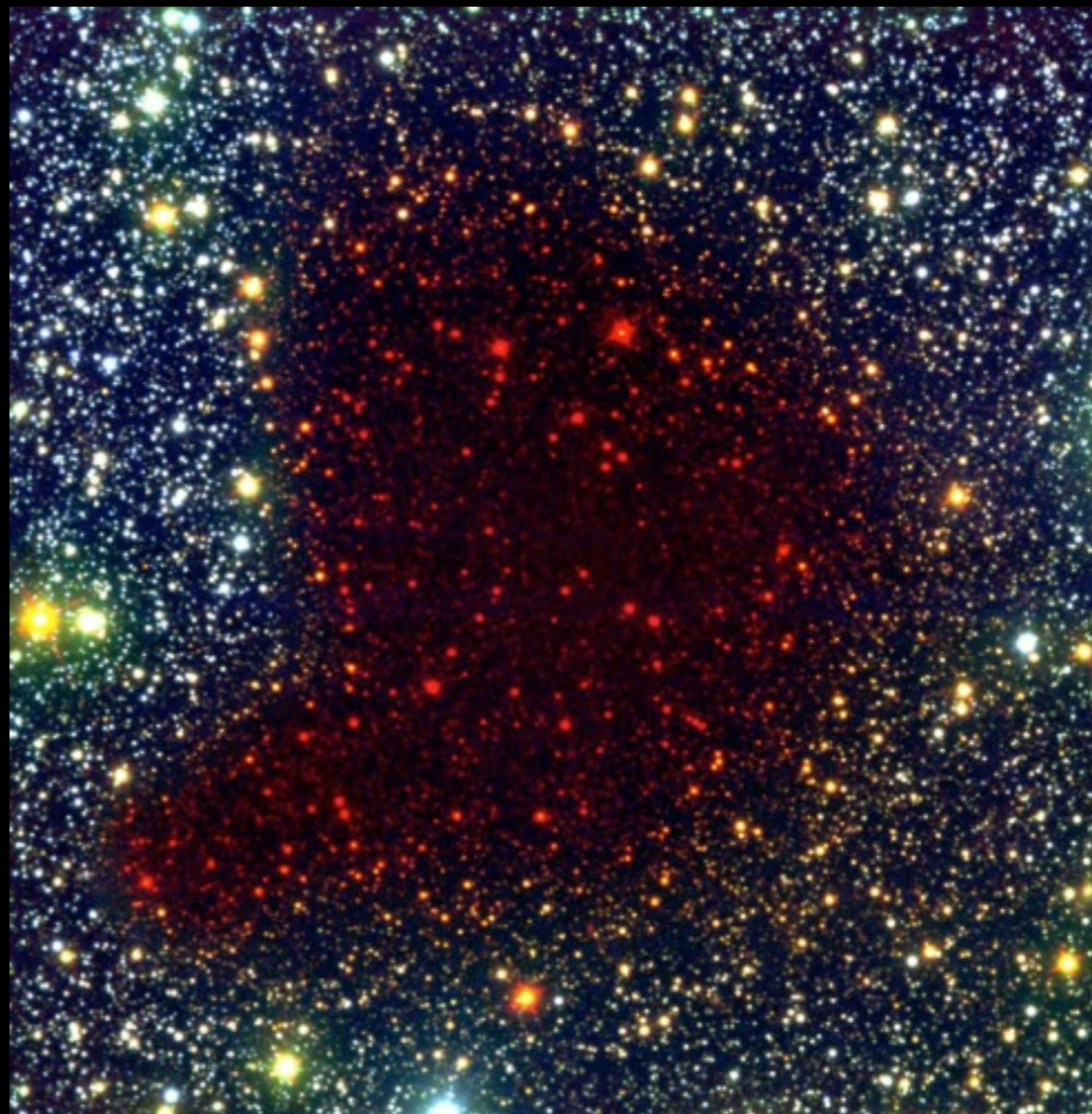
Extinction



Extinction



VLT (BVI)



VLT + NTT (BIK)

NICE(R)



VLT (BVI)

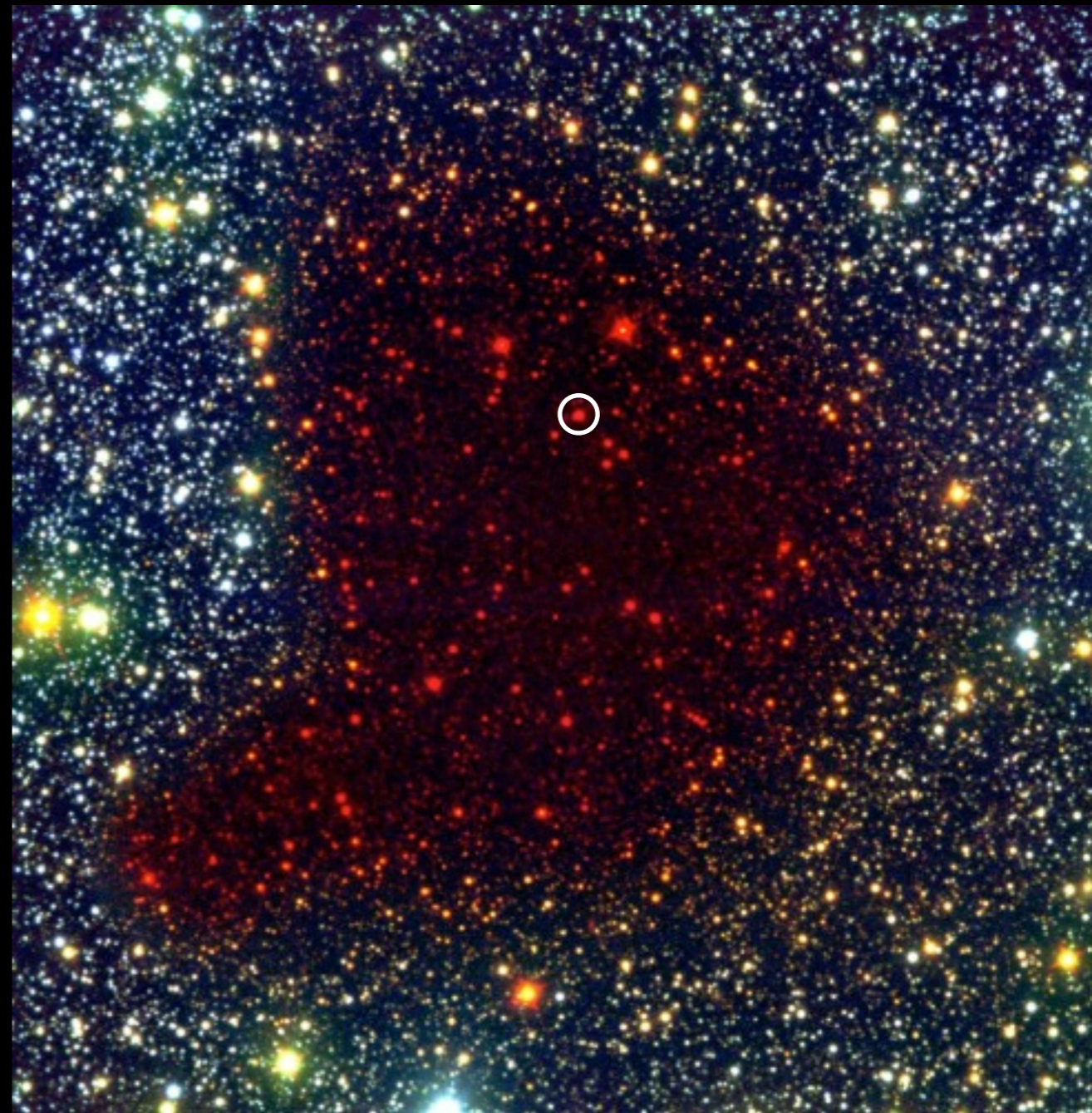


VLT + NTT (BIK)

NICE(R)



VLT (BVI)

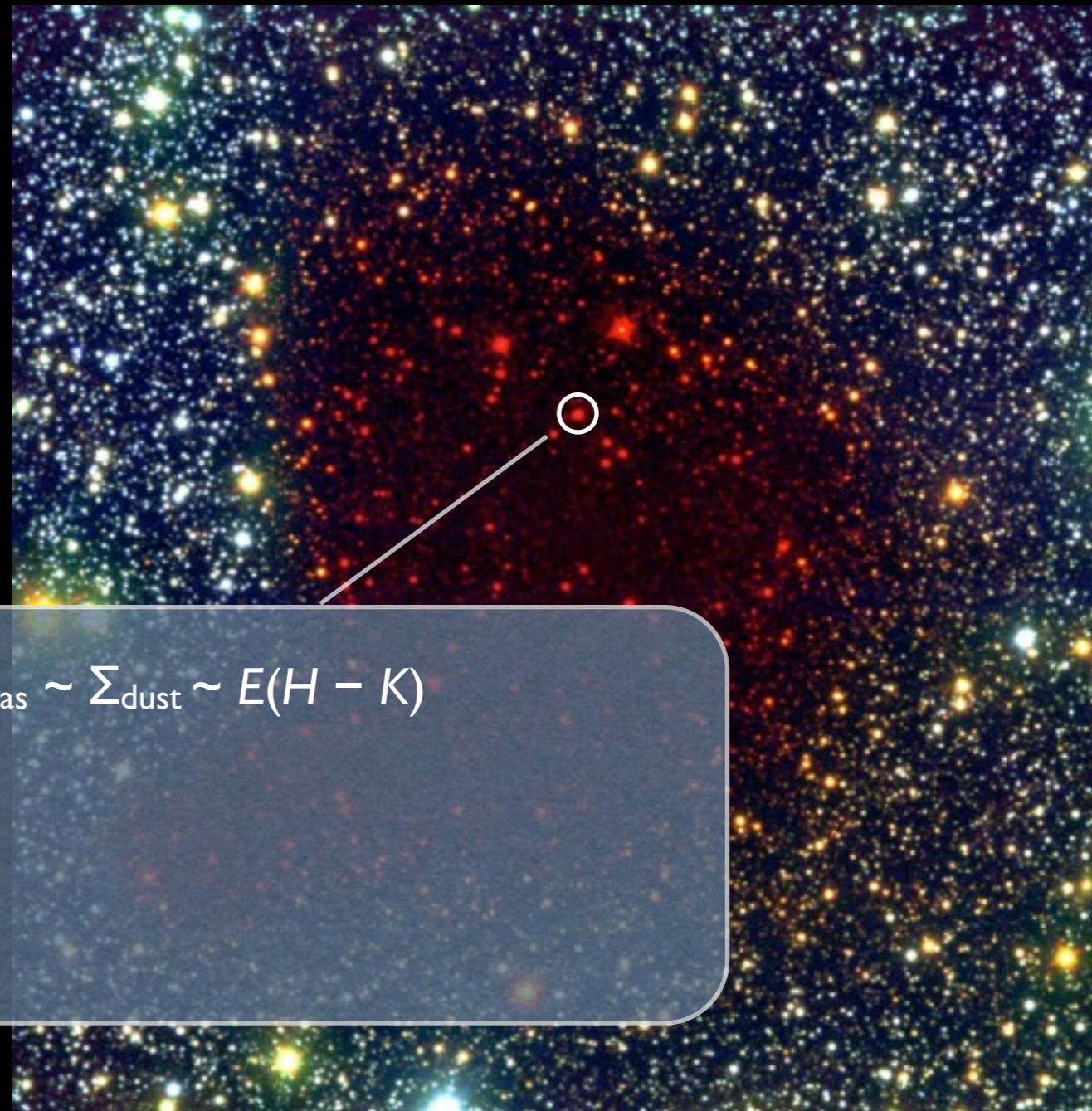


VLT + NTT (BIK)

NICE(R)



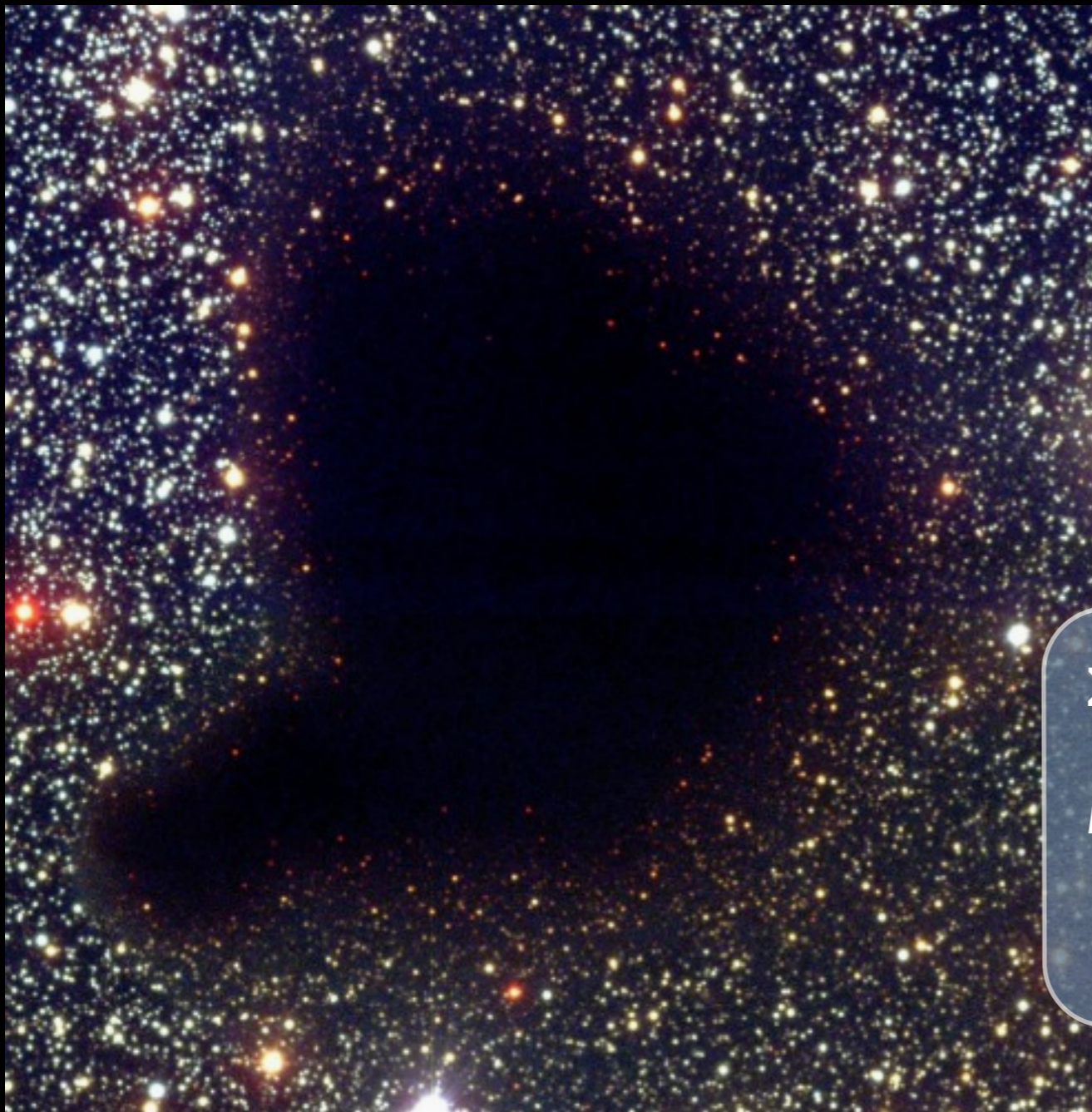
VLT (BVI)



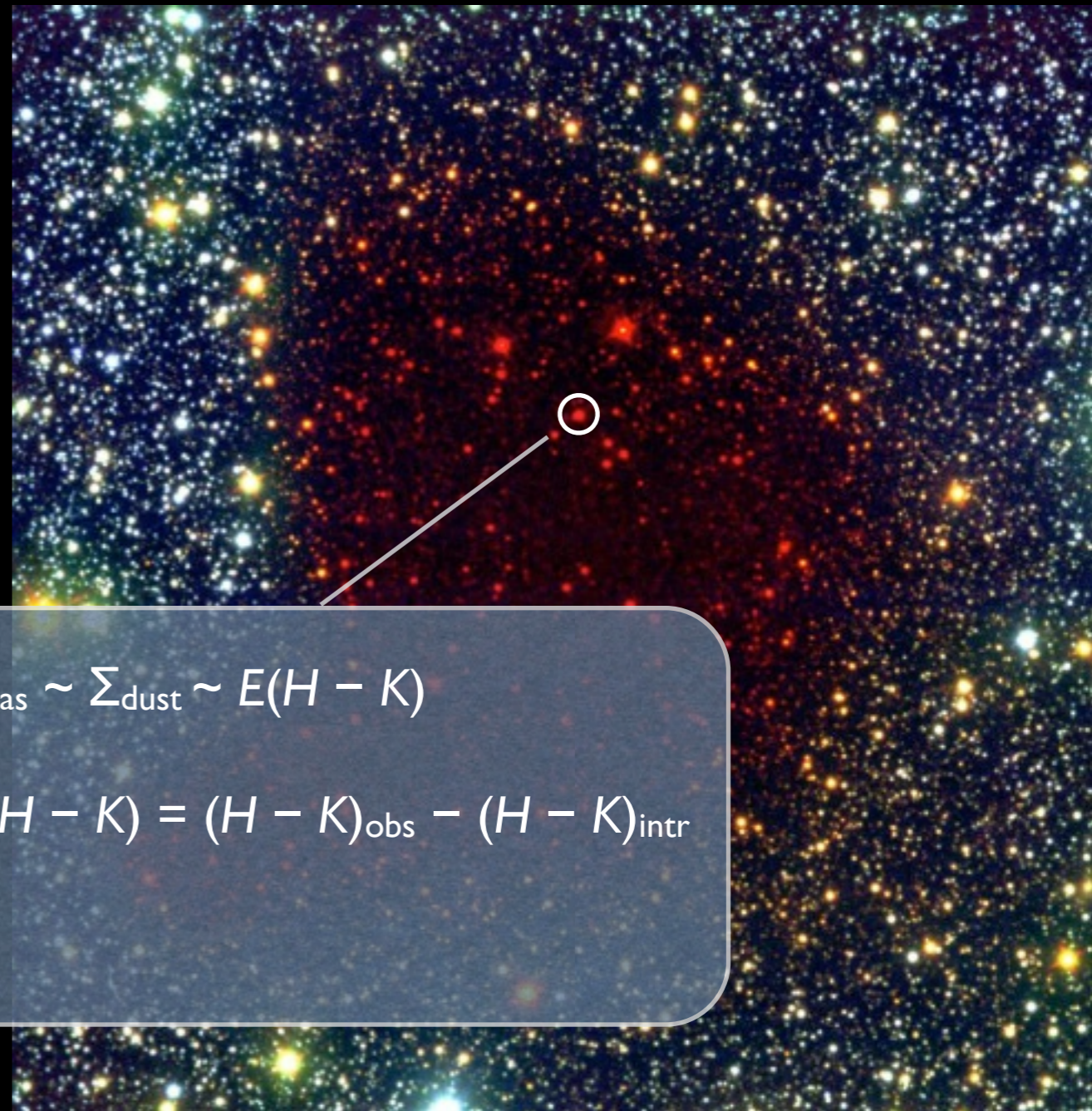
VLT + NTT (BIK)

$$\Sigma_{\text{gas}} \sim \Sigma_{\text{dust}} \sim E(H - K)$$

NICE(R)



VLT (BVI)

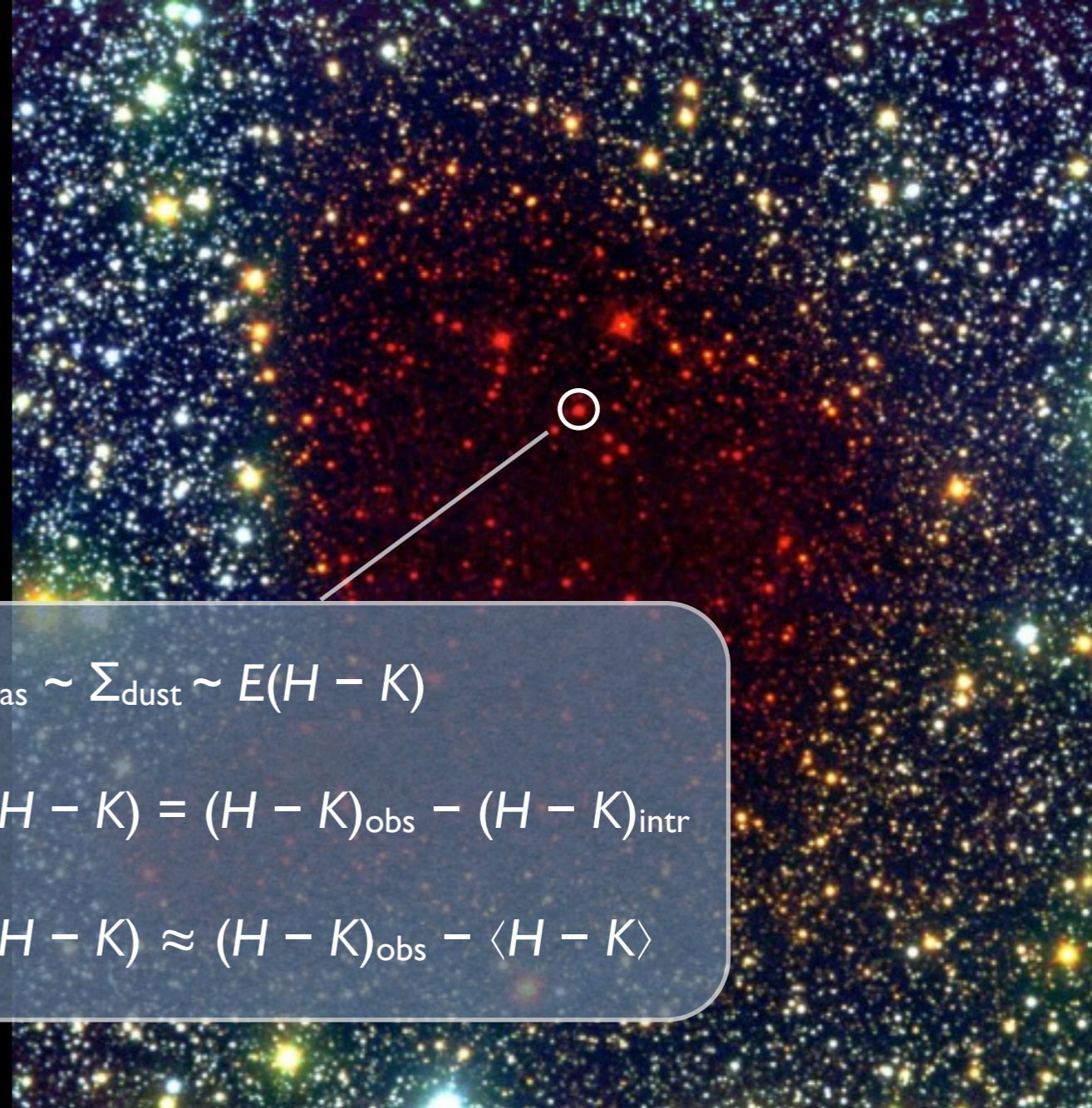


VLT + NTT (BIK)

$$\Sigma_{\text{gas}} \sim \Sigma_{\text{dust}} \sim E(H - K)$$

$$E(H - K) = (H - K)_{\text{obs}} - (H - K)_{\text{intr}}$$

NICE(R)



$$\Sigma_{\text{gas}} \sim \Sigma_{\text{dust}} \sim E(H - K)$$

$$E(H - K) = (H - K)_{\text{obs}} - (H - K)_{\text{intr}}$$

$$E(H - K) \approx (H - K)_{\text{obs}} - \langle H - K \rangle$$

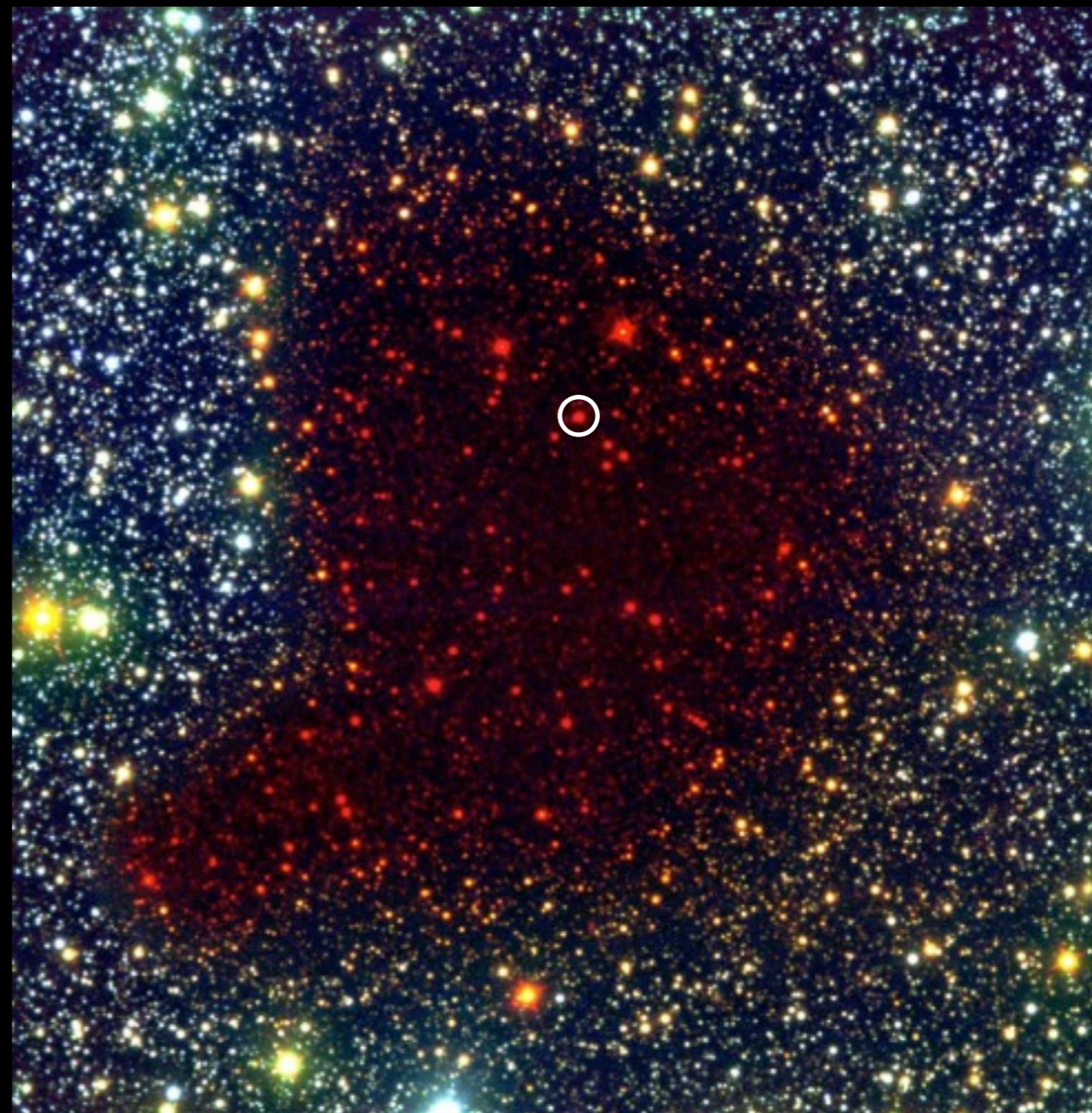
VLT (BVI)

VLT + NTT (BIK)

NICE(R)

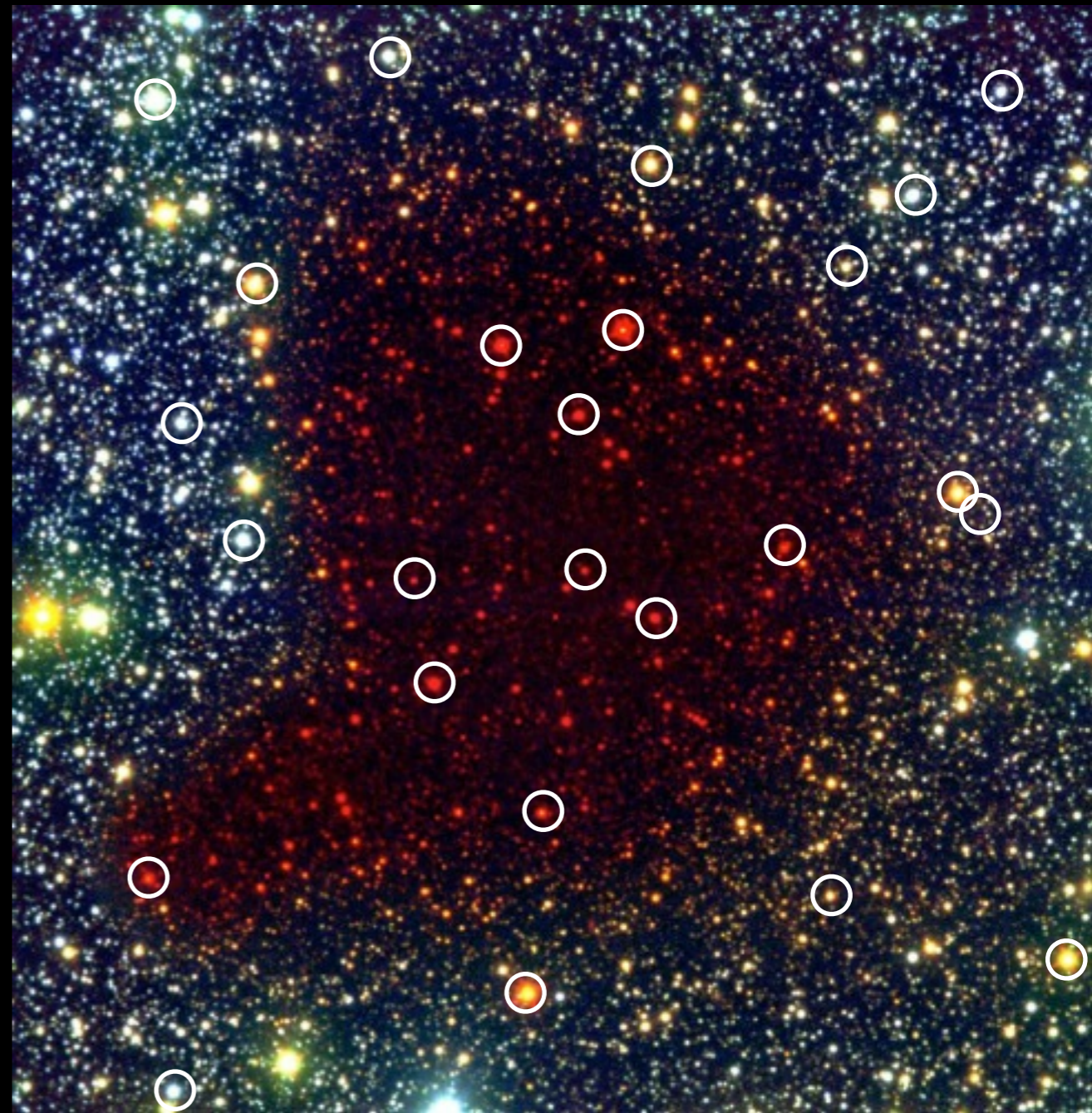


VLT (BVI)

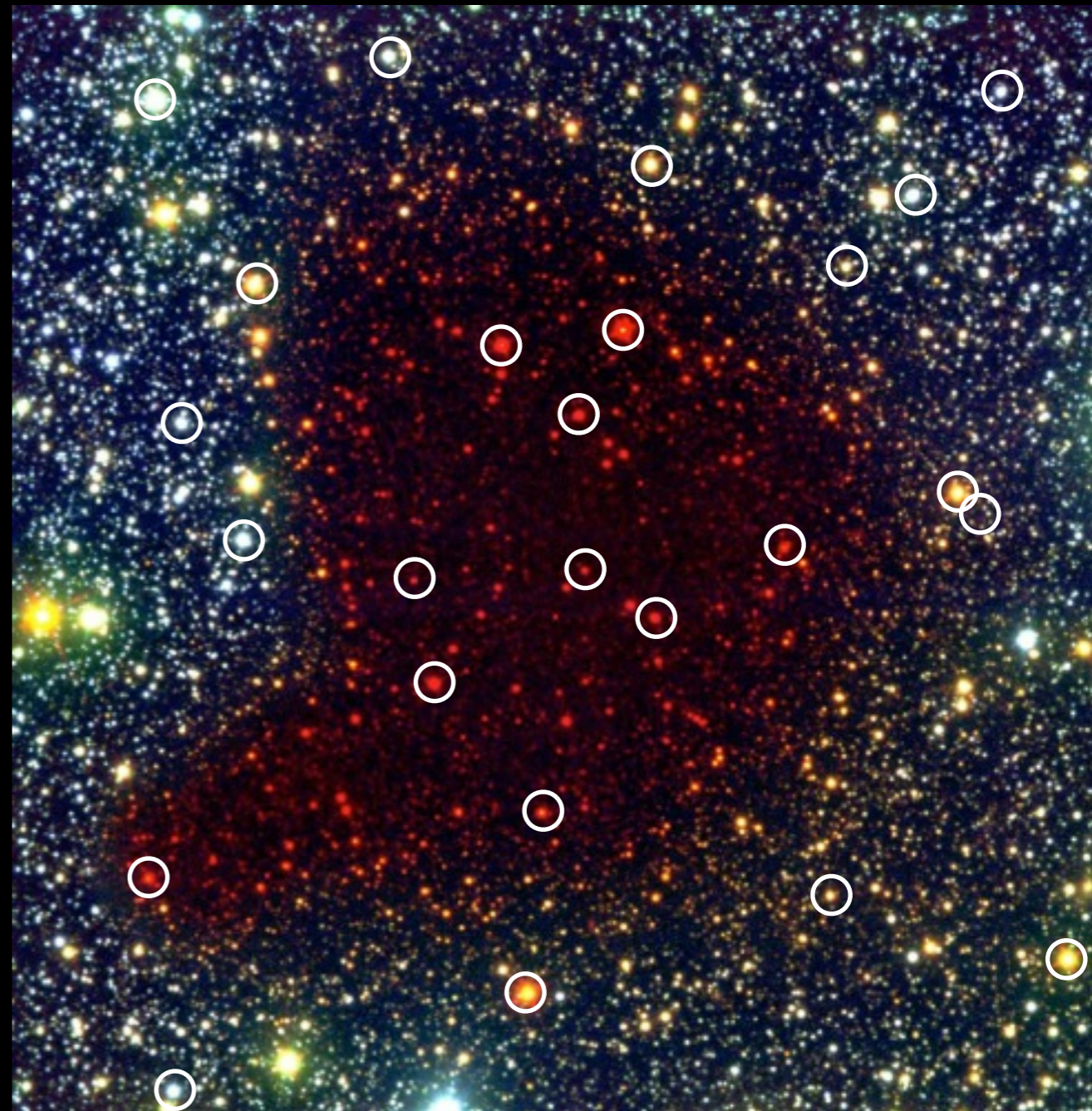
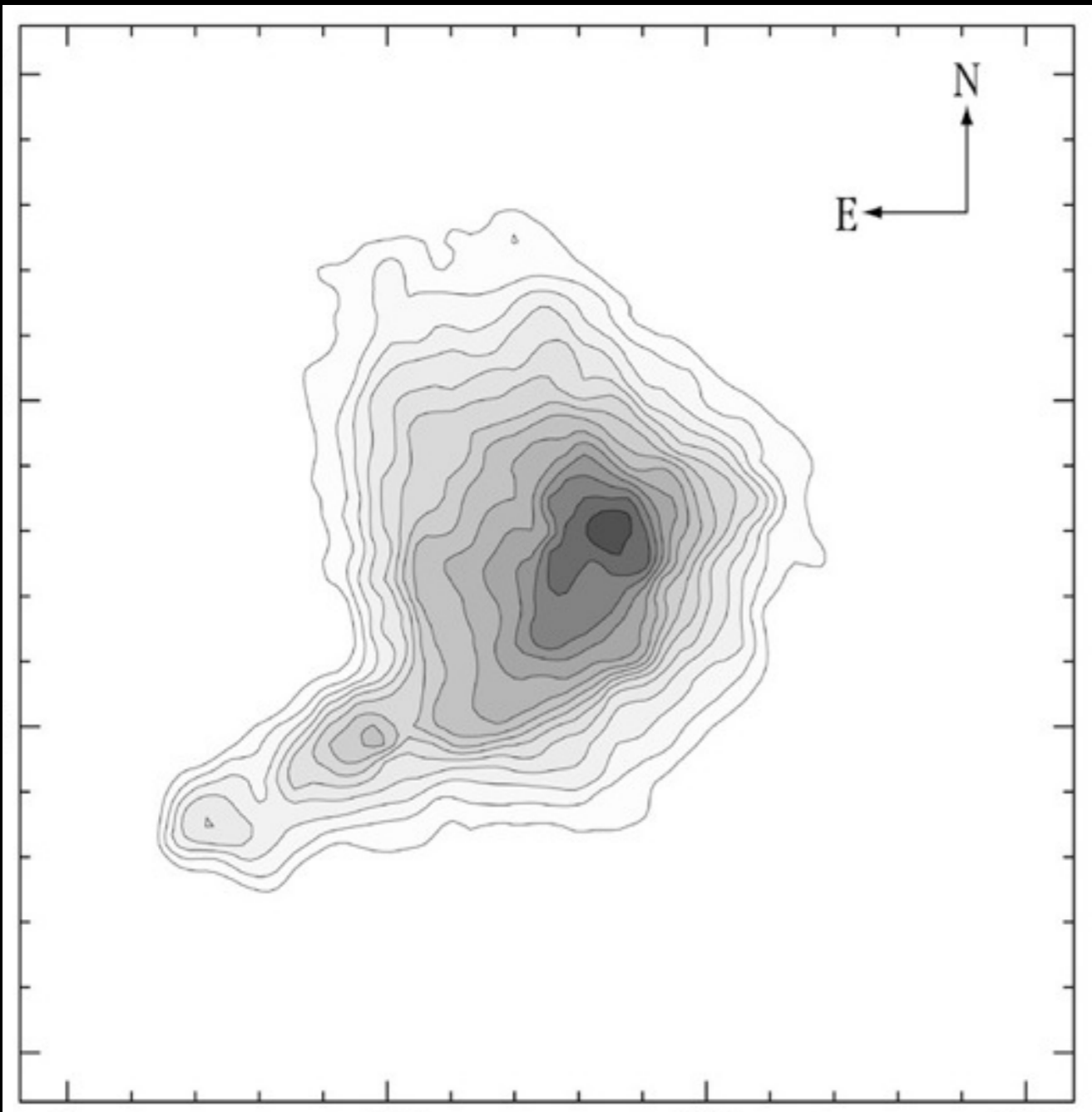


VLT + NTT (BIK)

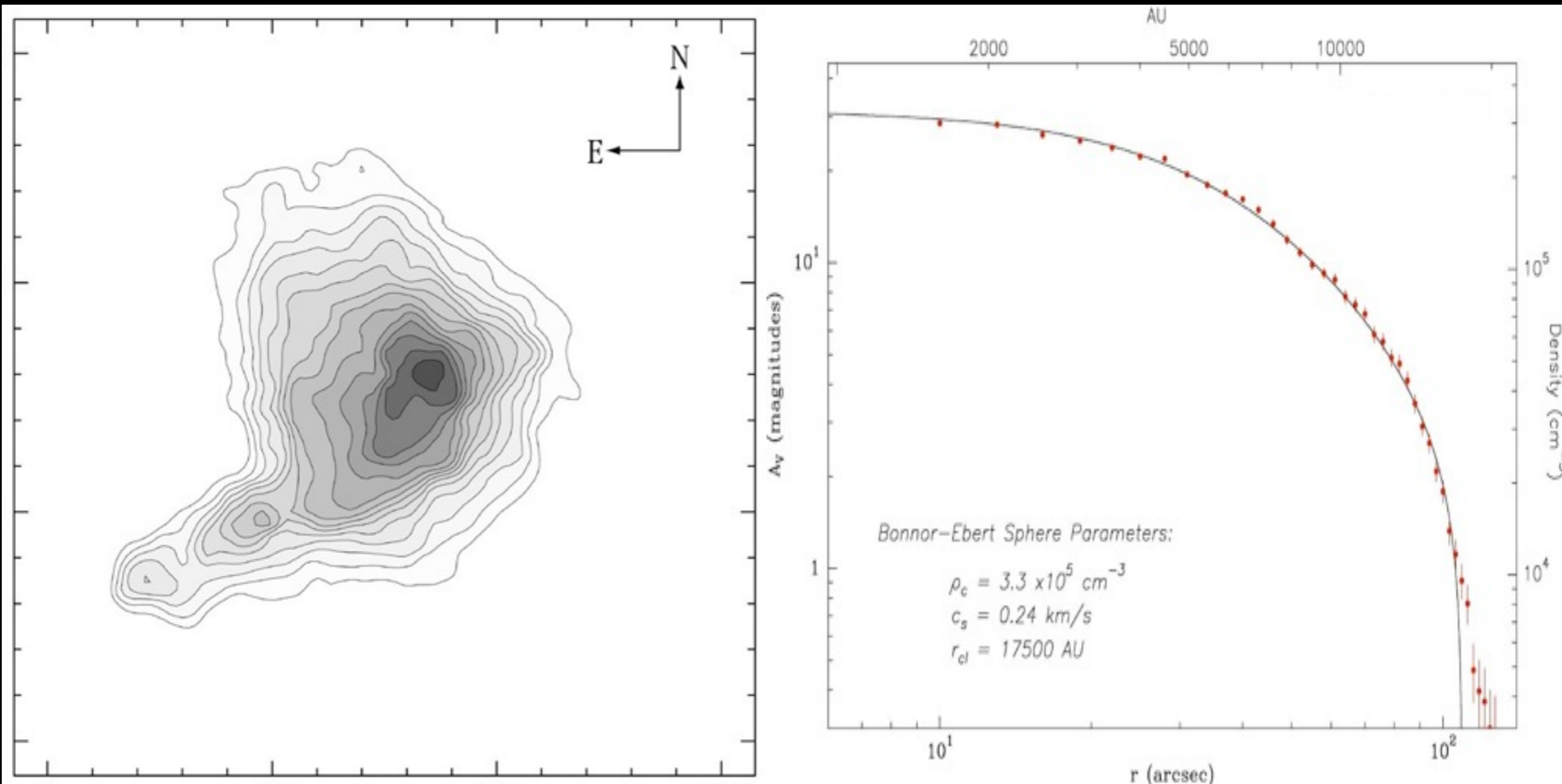
NICE(R)



NICE(R)



NICE(R)



Barnard 68



Barnard 68

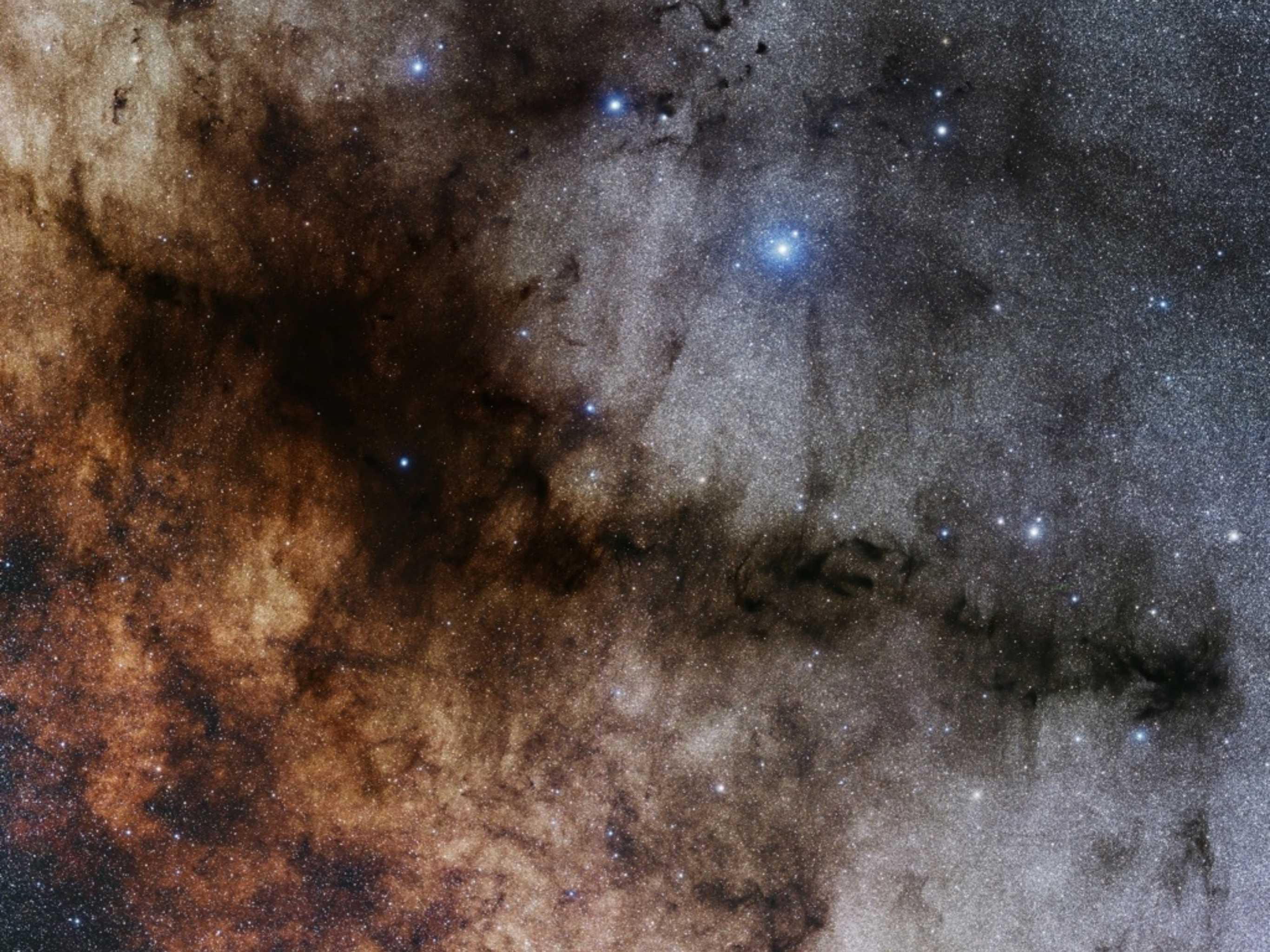


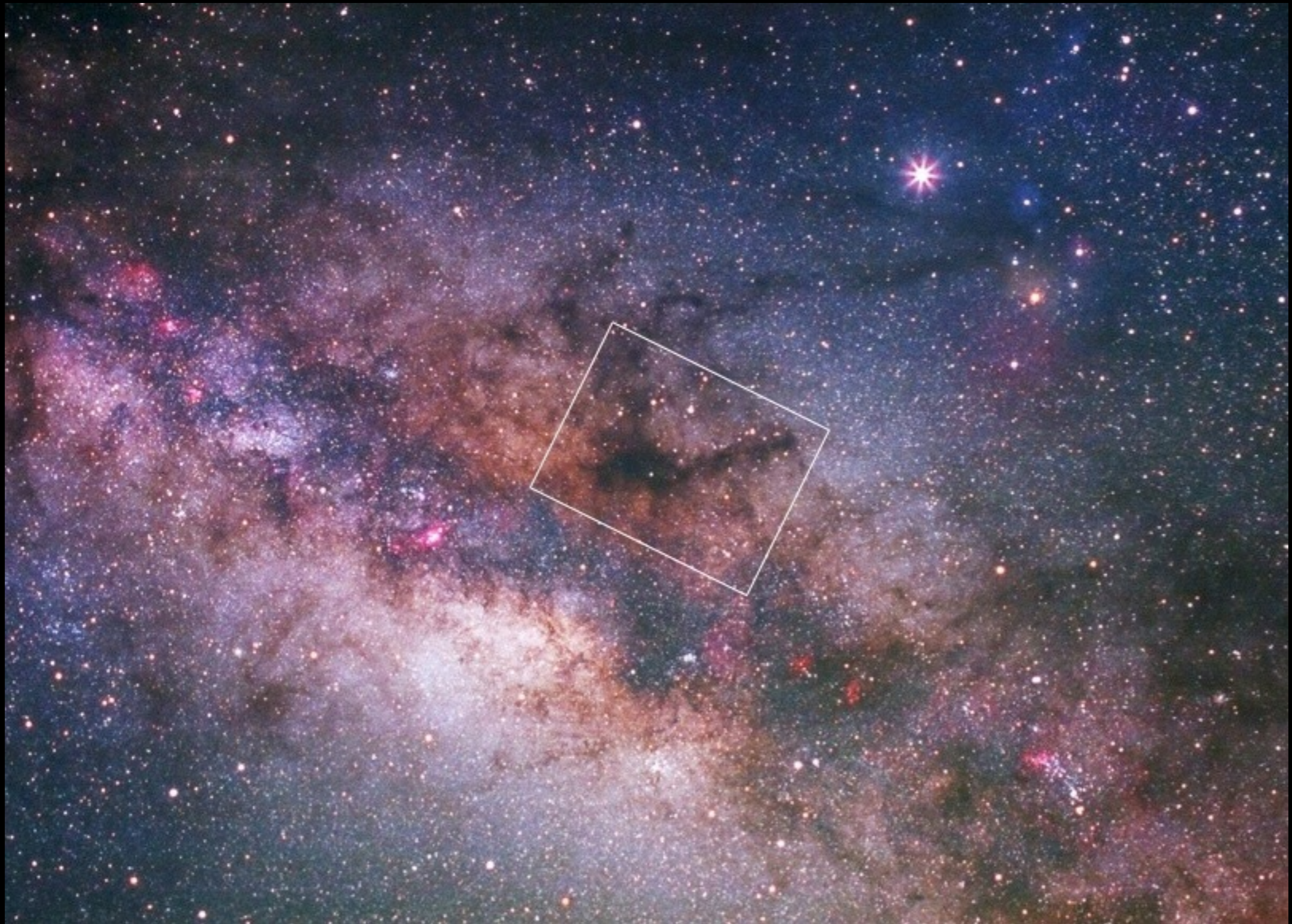


Ceci n'est pas une pipe.

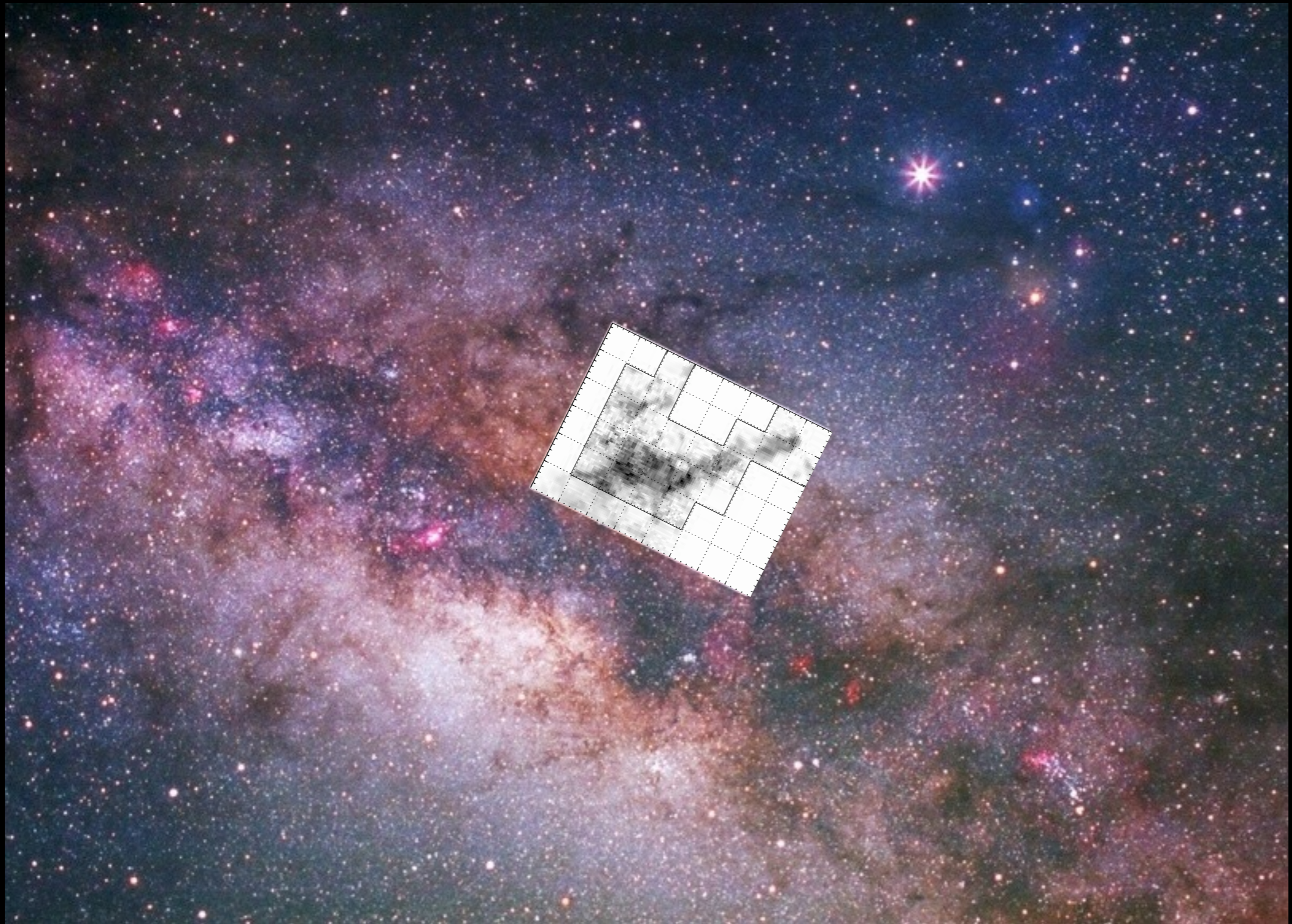






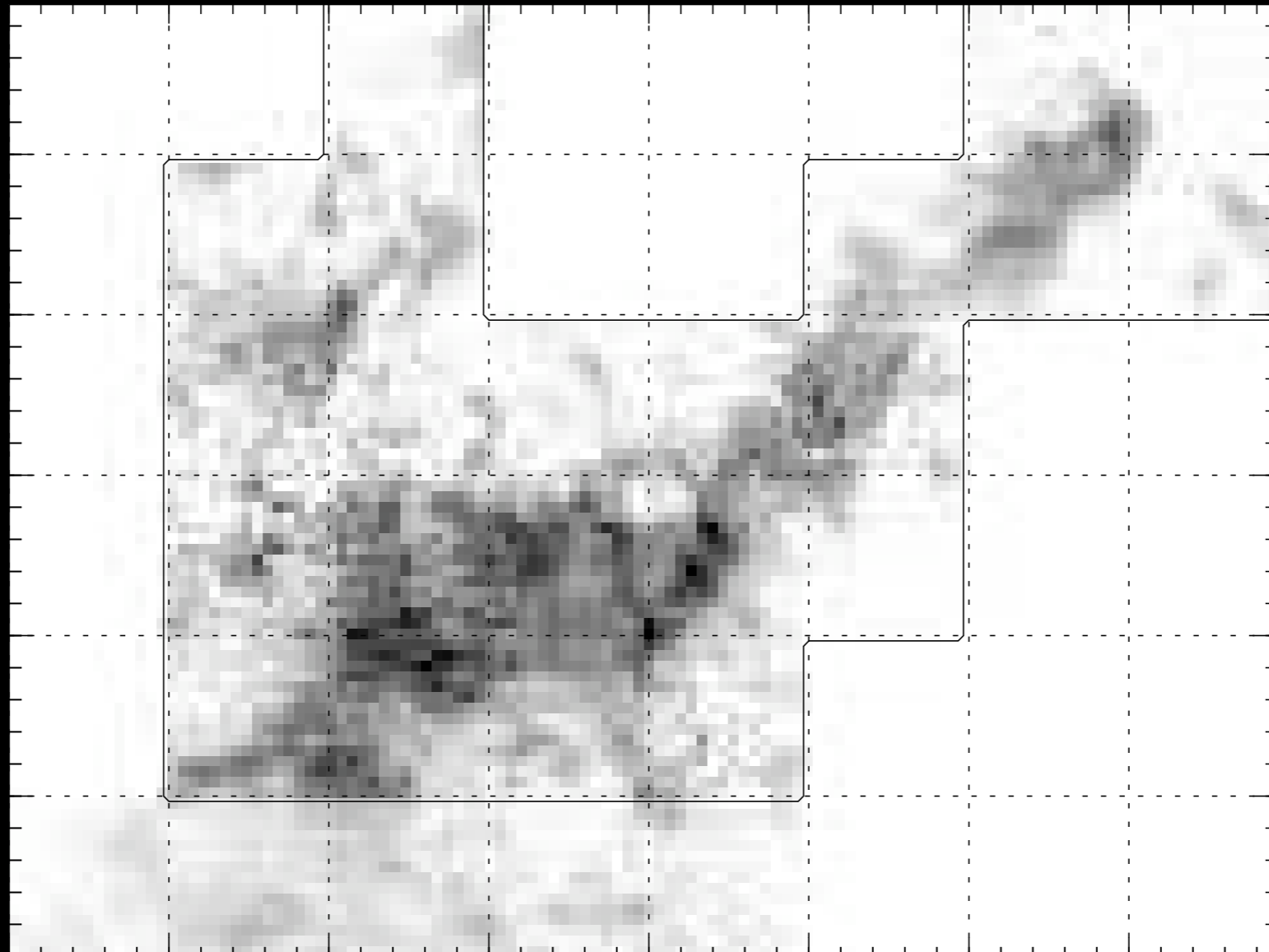


The Pipe Nebula



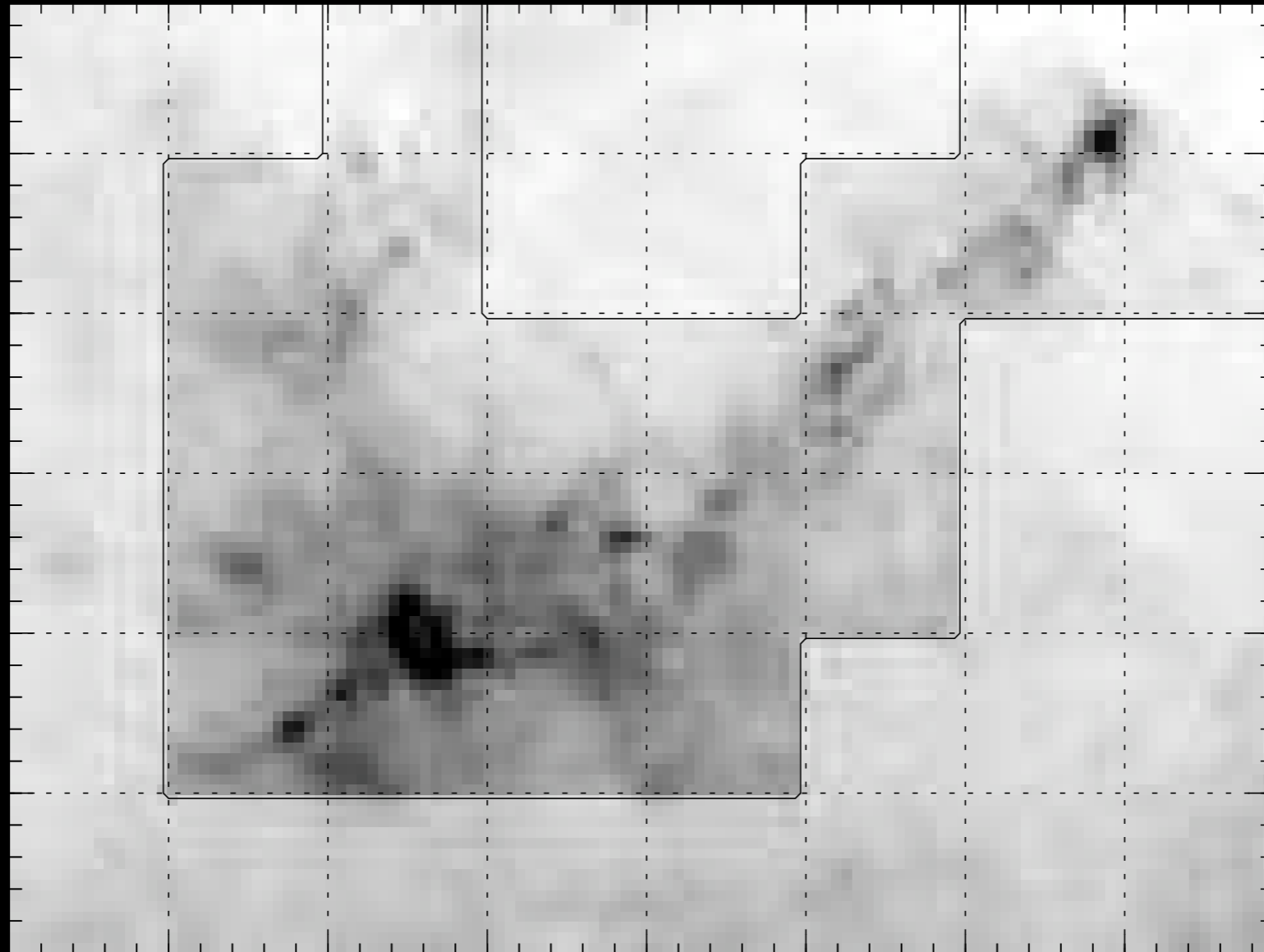
The Pipe Nebula

CO vs. dust



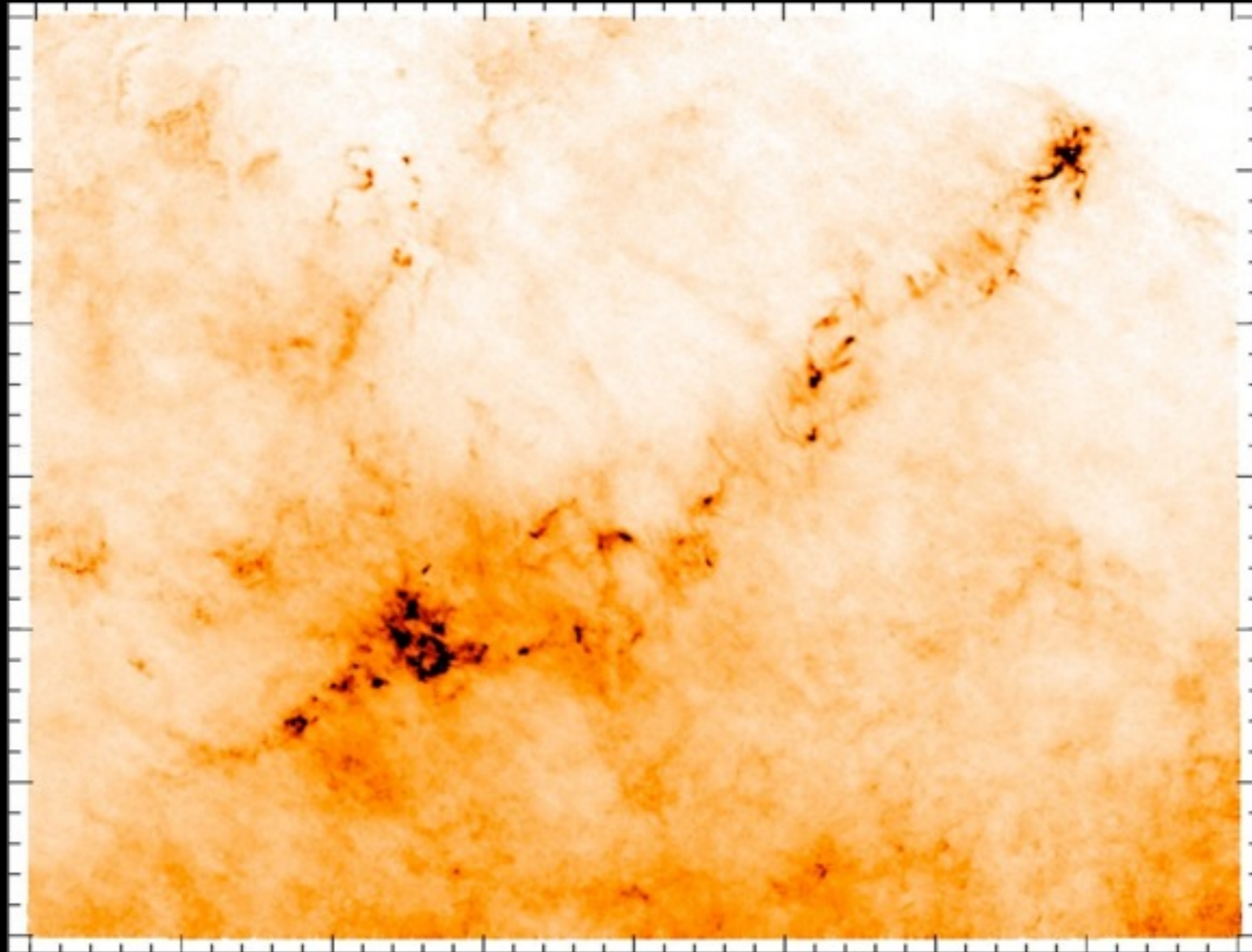
^{12}CO : Onishi et al. (1999), $M=6500 M_{\odot}$

CO vs. dust

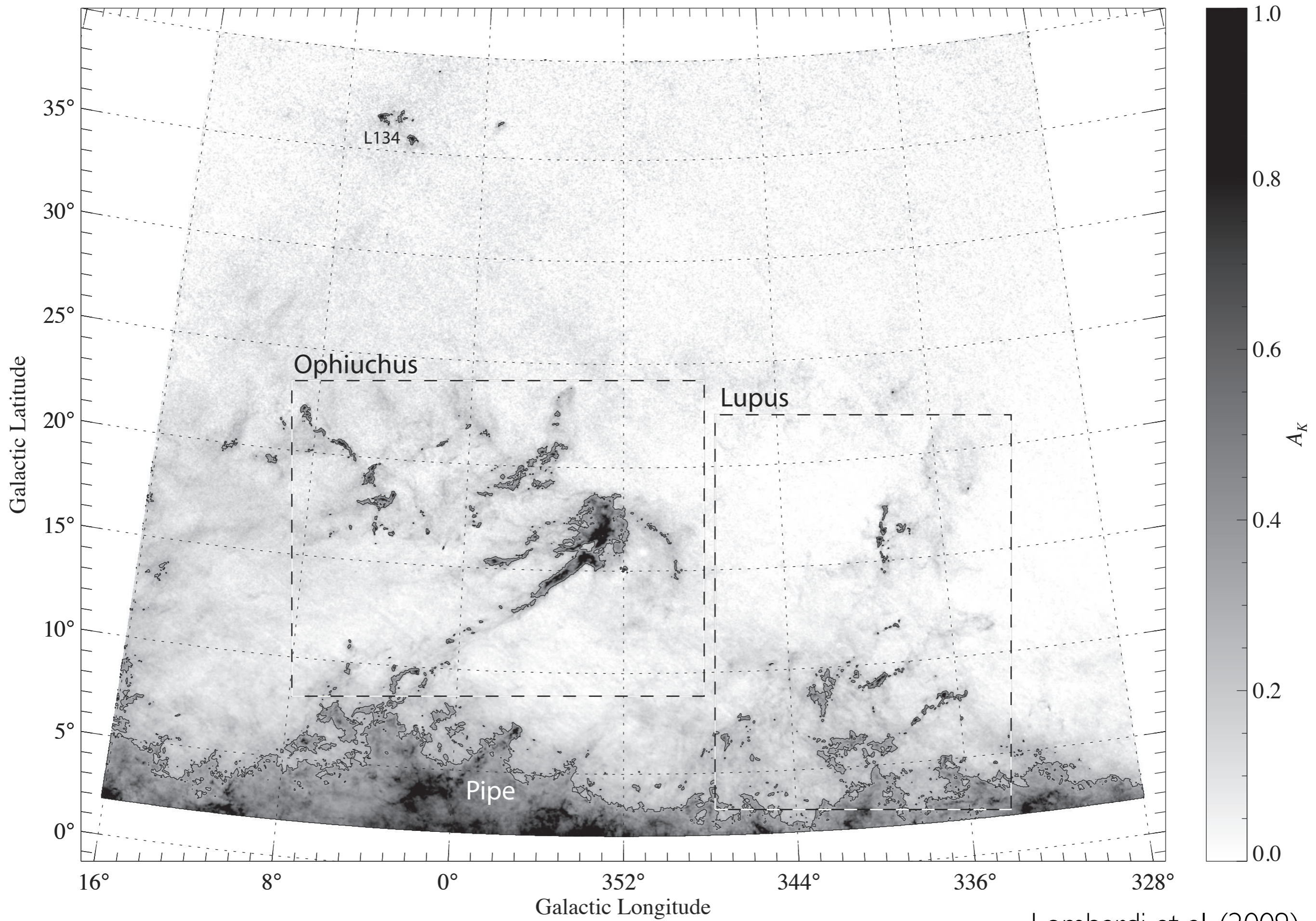


NICER: Lombardi et al. (2006), $M=11000 M_{\odot}$

CO vs. dust



NICER: full resolution (1 arcmin)



Fact 3

Different molecular clouds
have different SFRs



S. Guisard (ESO)

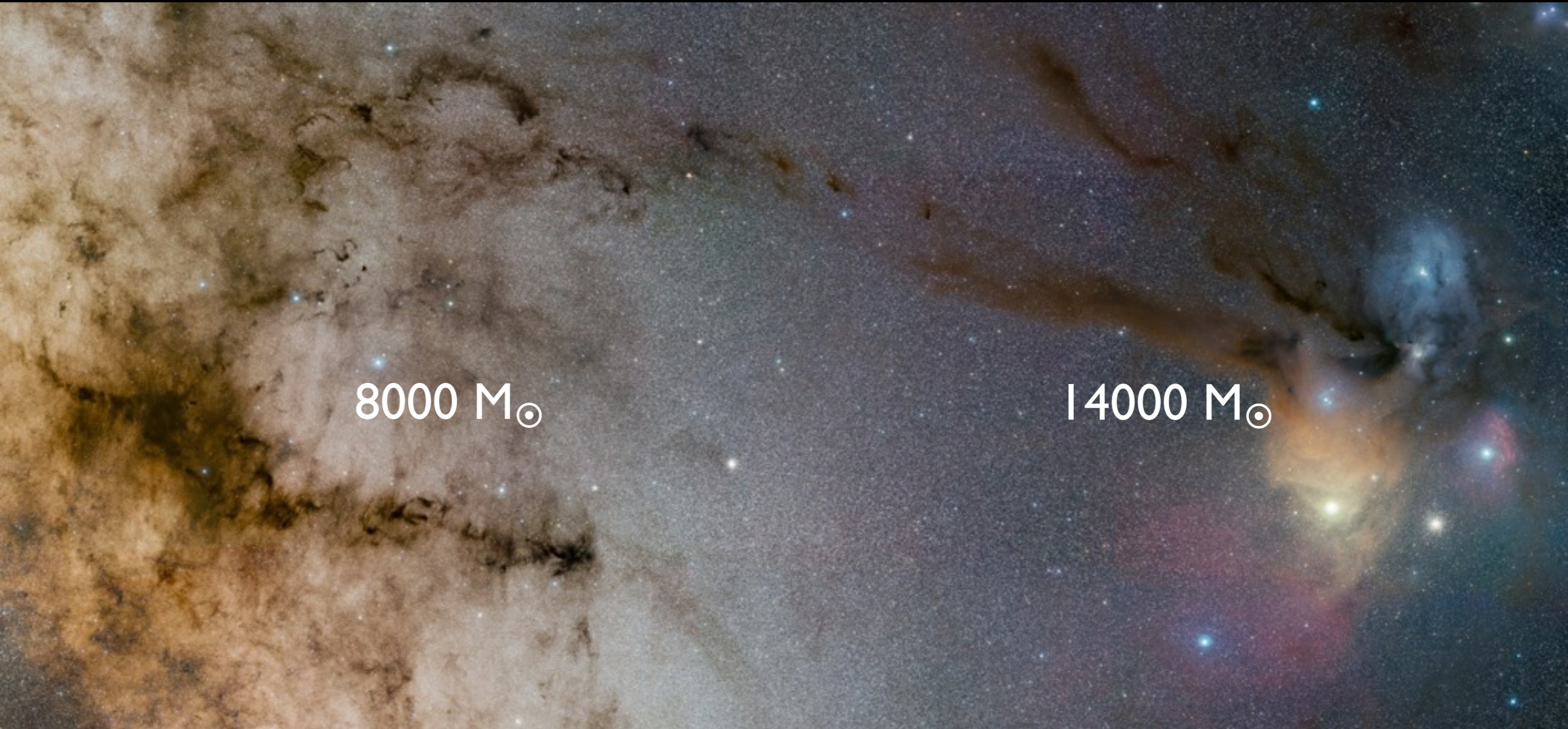
Pipe nebula

ρ Ophiuchi cloud



$$\Sigma_{\text{Pipe}} = 50 M_{\odot} \text{ pc}^{-2}$$

$$\Sigma_{\text{Oph}} = 40 M_{\odot} \text{ pc}^{-2}$$



8000 M_⊙

14000 M_⊙

$$\Sigma_{\text{Pipe}} = 50 \text{ M}_{\odot} \text{ pc}^{-2}$$

$$\Sigma_{\text{Oph}} = 40 \text{ M}_{\odot} \text{ pc}^{-2}$$



8000 M_{\odot}

21 YSOs

14000 M_{\odot}

316 YSOs

$$\Sigma_{\text{Pipe}} = 50 M_{\odot} \text{ pc}^{-2}$$

$$\Sigma_{\text{Oph}} = 40 M_{\odot} \text{ pc}^{-2}$$



8000 M_{\odot}

21 YSOs

14000 M_{\odot}

316 YSOs

$$\text{SFR}_{\text{Oph}} = 15 \times \text{SFR}_{\text{Pipe}}$$

$$\Sigma_{\text{Pipe}} = 50 M_{\odot} \text{ pc}^{-2}$$

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8000 M_{\odot}

21 YSOs

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316 YSOs

8000 M_{\odot}

10000 M_{\odot}

You need to restart your computer. Hold down the Power button for several seconds or press the Restart button.

Vous devez redémarrer votre ordinateur. Maintenez la touche de démarrage enfoncée pendant plusieurs secondes ou bien appuyez sur le bouton de réinitialisation.

Sie müssen Ihren Computer neu starten. Halten Sie dazu die Einschalttaste einige Sekunden gedrückt oder drücken Sie die Neustart-Taste.

コンピュータを再起動する必要があります。パワーボタンを数秒間押し続けるか、リセットボタンを押してください。

$$\text{SFR}_{\text{Oph}} = 15 \times \text{SFR}_{\text{Pipe}}$$

$$\Sigma_{\text{Pipe}} = 50 M_{\odot} \text{ pc}^{-2}$$

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$$\text{SFR}_{\text{Oph}} = 15 \times \text{SFR}_{\text{Pipe}}$$

Ceci n'est pas une exception.

$$\Sigma_{\text{Pipe}} = 50 M_{\odot} \text{ pc}^{-2}$$

$$\Sigma_{\text{Oph}} = 40 M_{\odot} \text{ pc}^{-2}$$

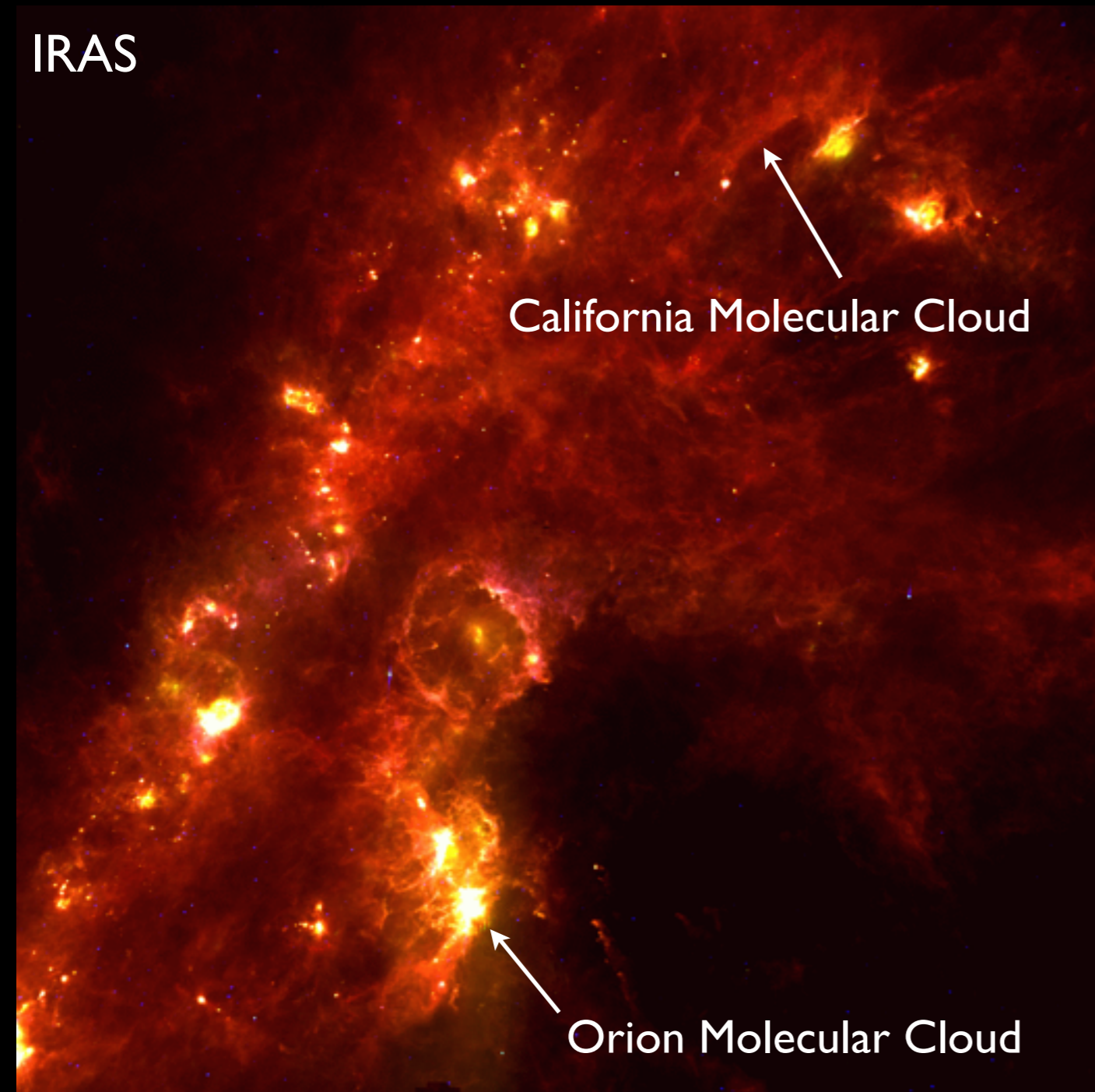
Ceci n'est pas une exception.

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IRAS

California Molecular Cloud

Orion Molecular Cloud

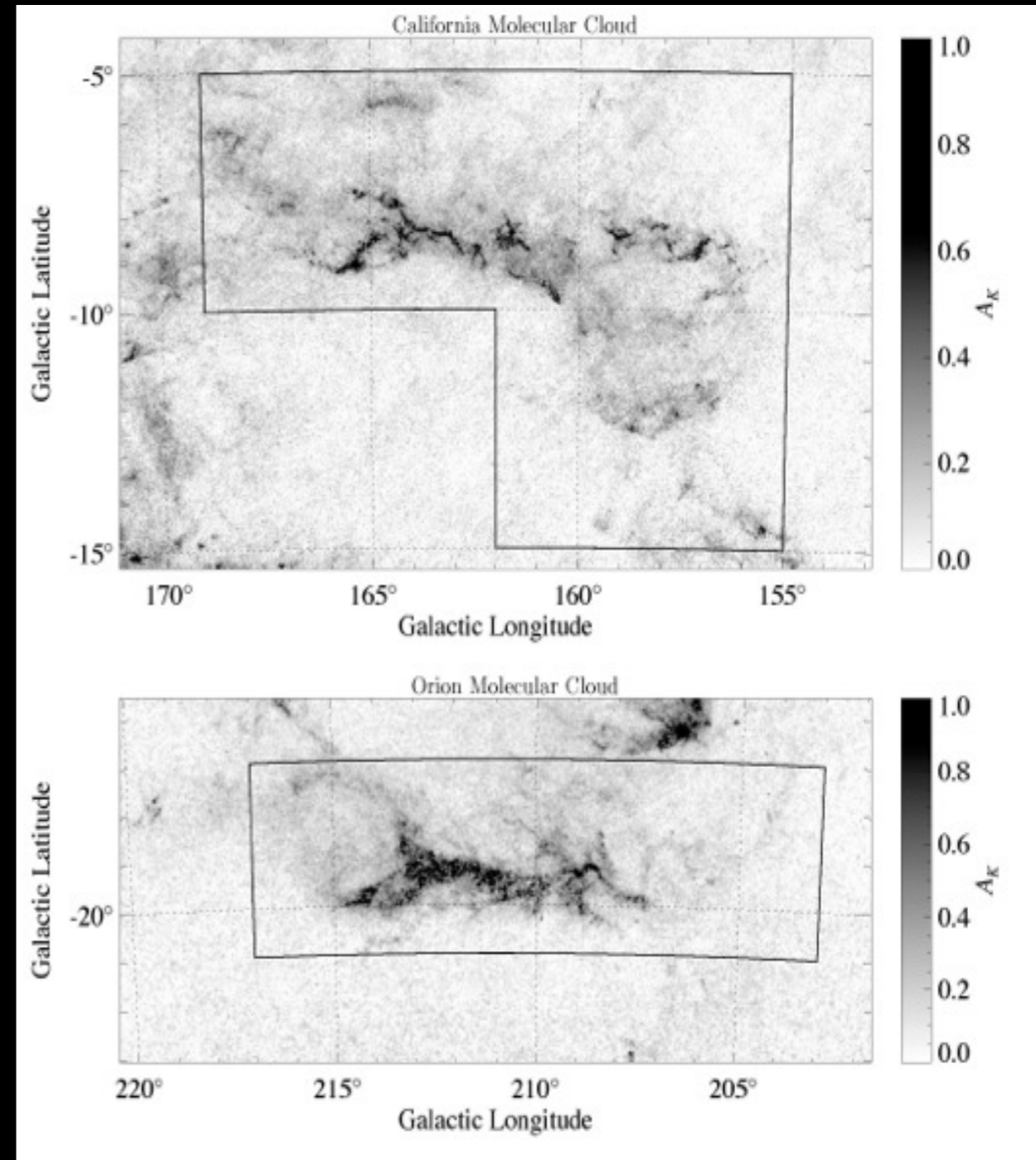


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IRAS

California Molecular Cloud

Orion Molecular Cloud

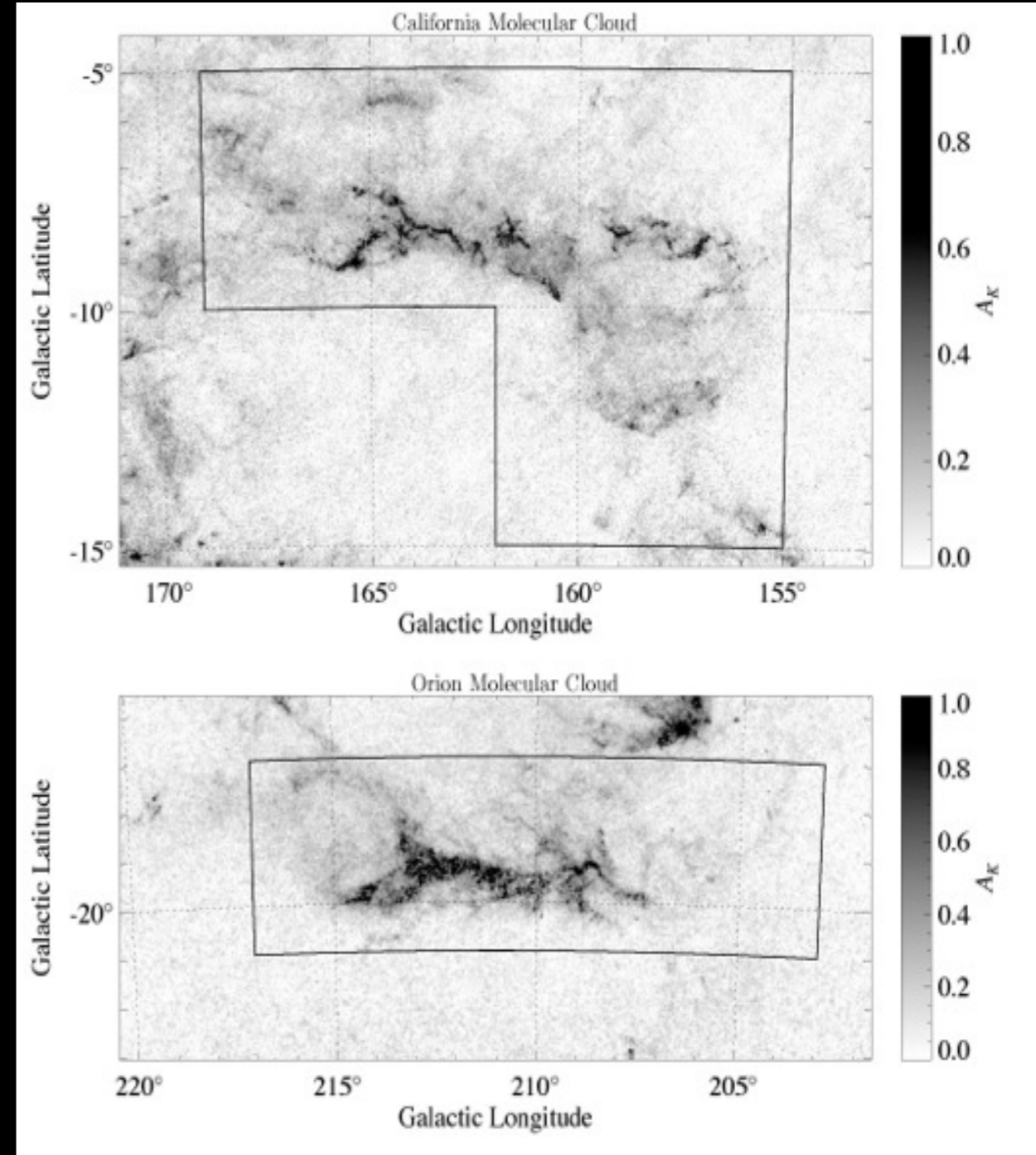


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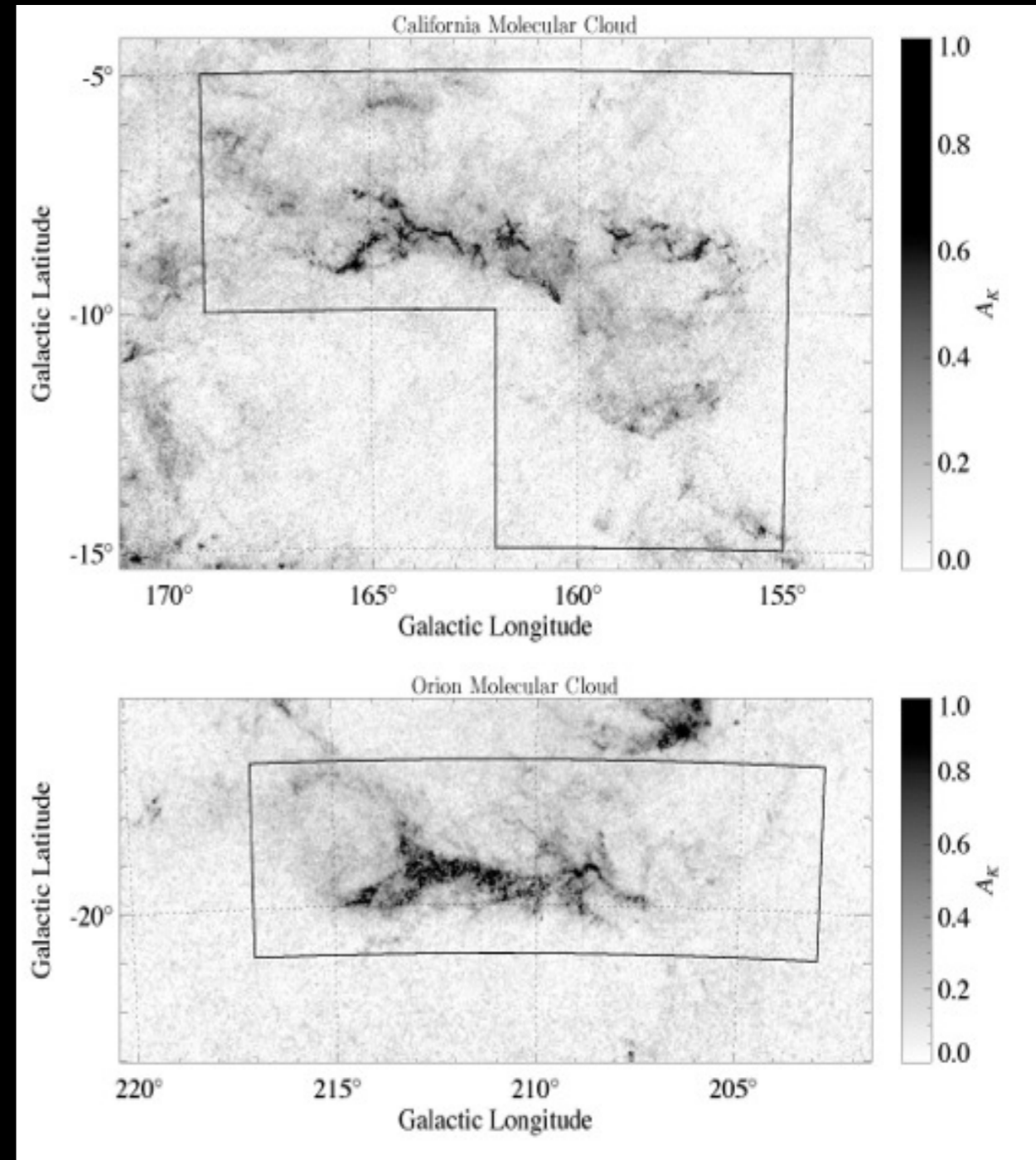
$$\text{SFR}_{\text{Orion}} = 10 \times \text{SFR}_{\text{California}}$$

Ceci n'est pas une exception.

IRAS

California Molecular Cloud

Orion Molecular Cloud



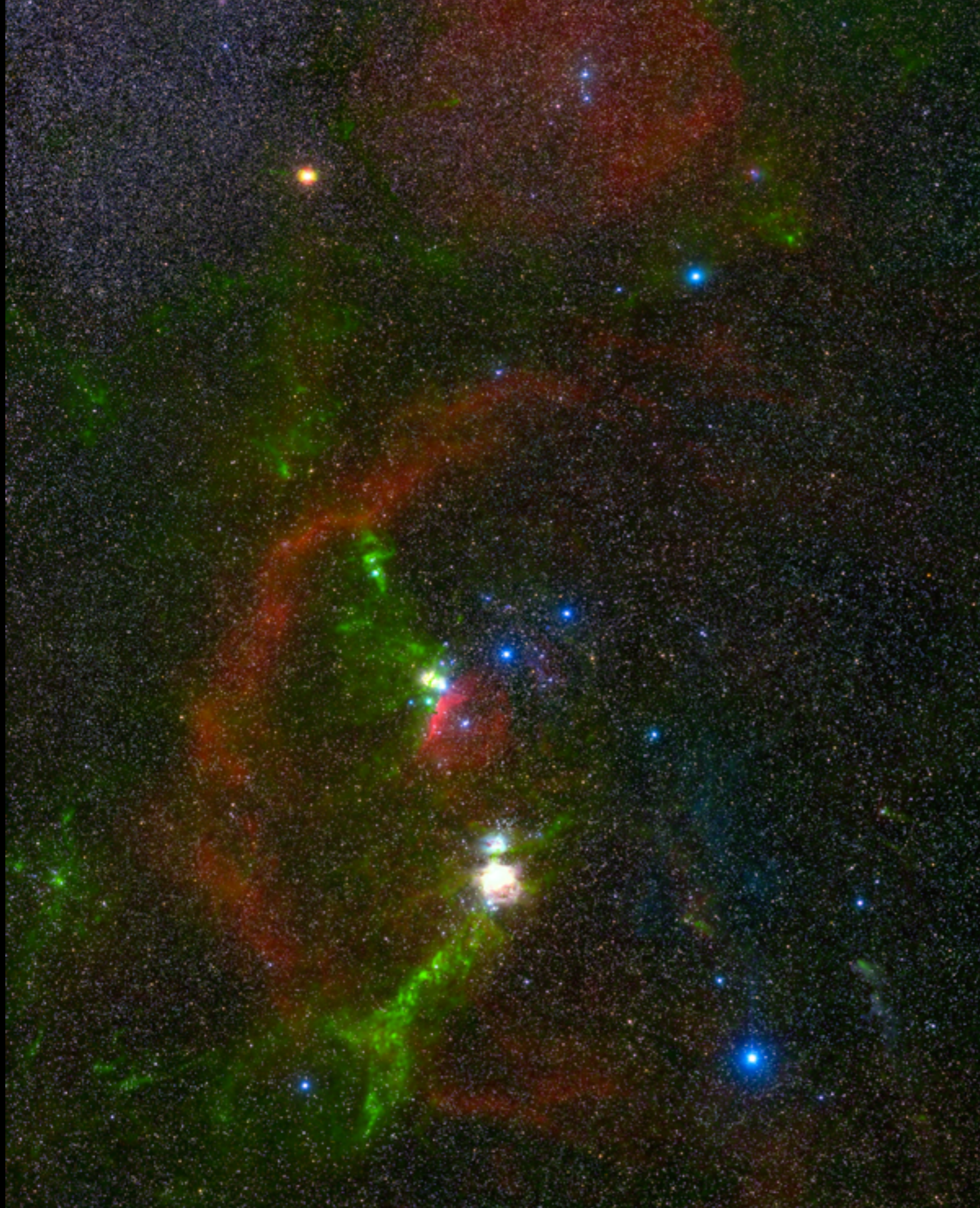
$$\text{SFR}_{\text{Orion}} = 10 \times \text{SFR}_{\text{California}}$$

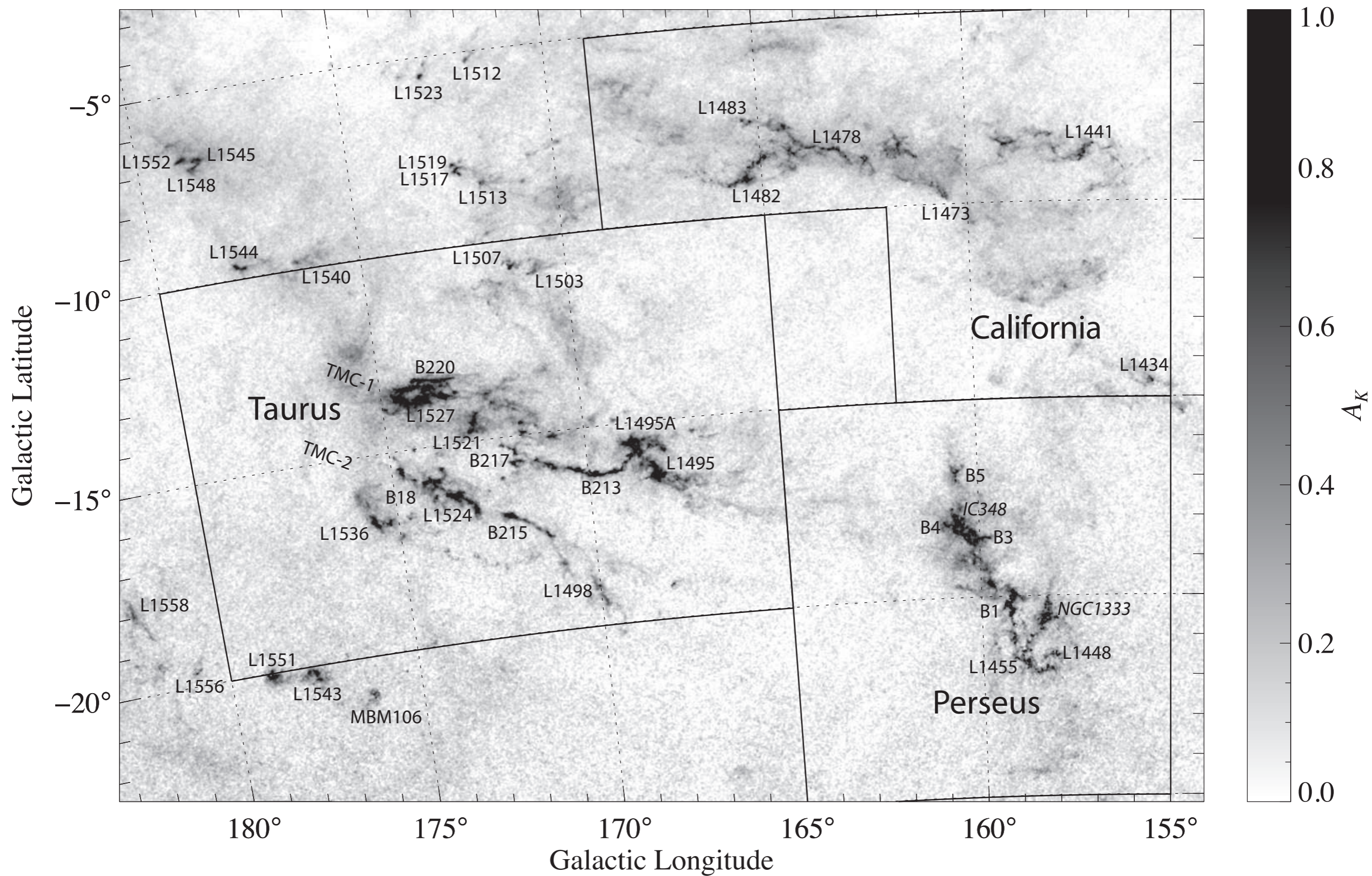
Clouds identical in mass & size

Inventory of Local Star Formation Activity

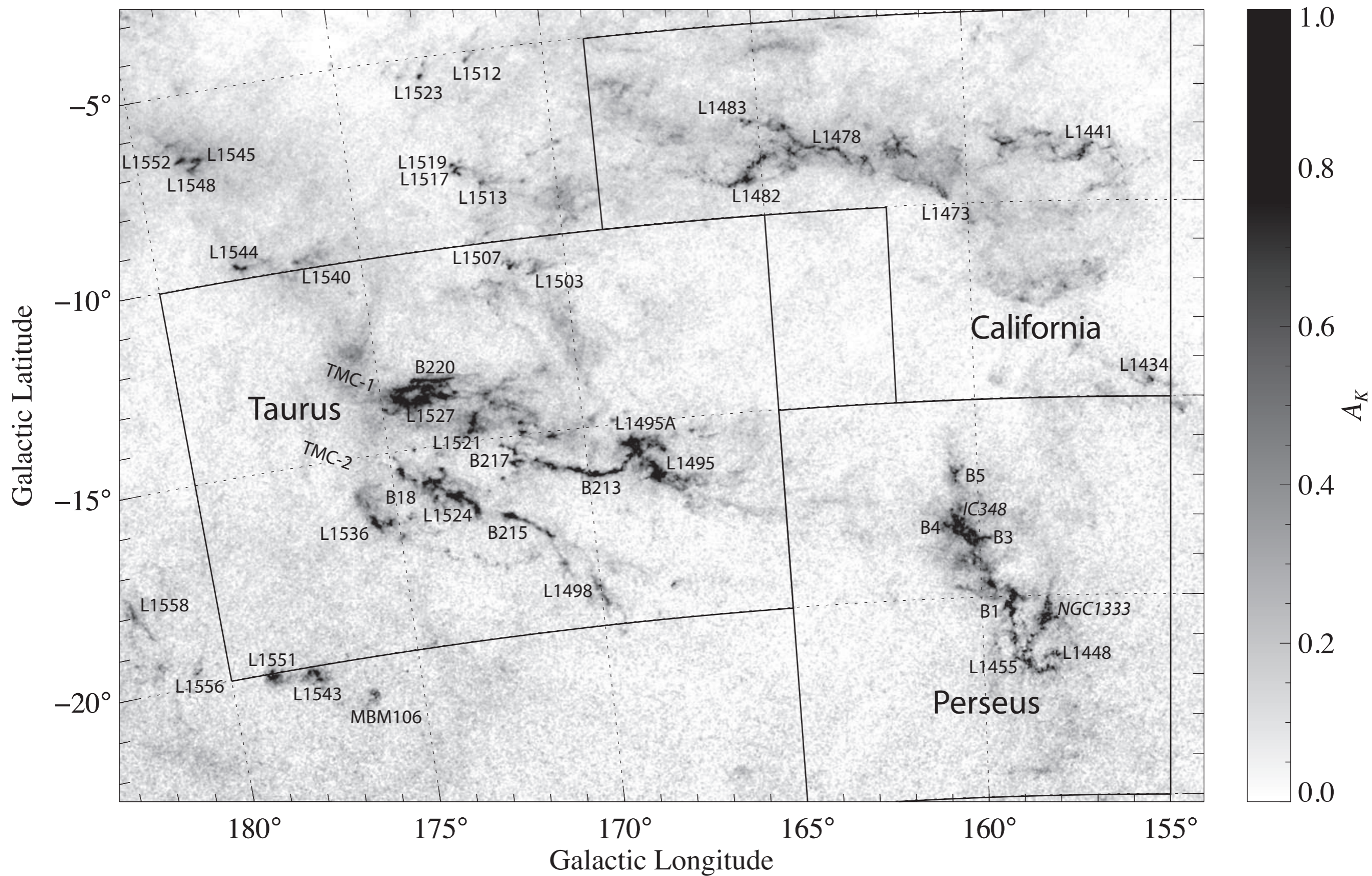
Infrared extinction and cloud masses





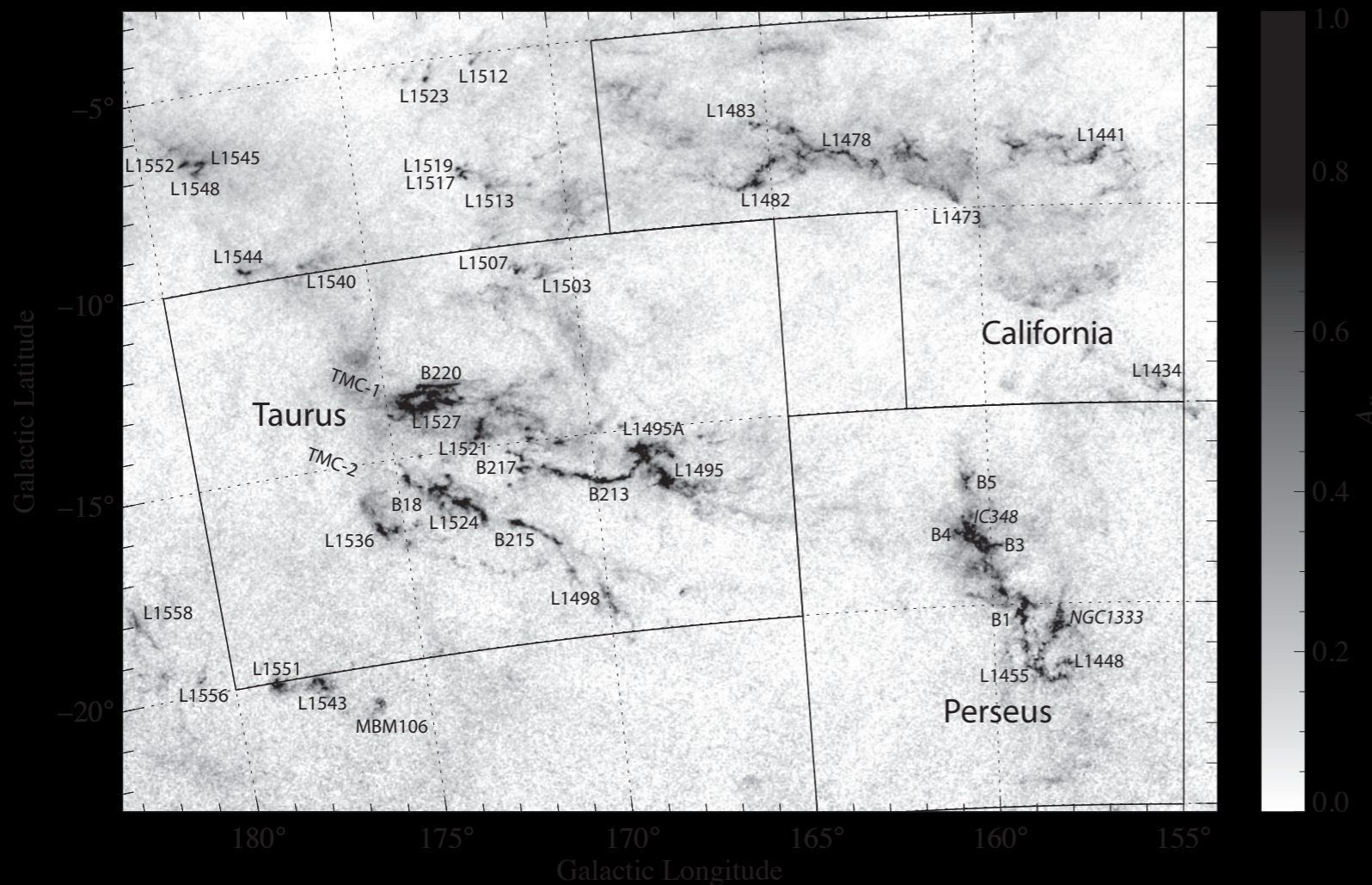


Lombardi et al. (2010)



Inventory of Star Formation Activity: Molecular Clouds

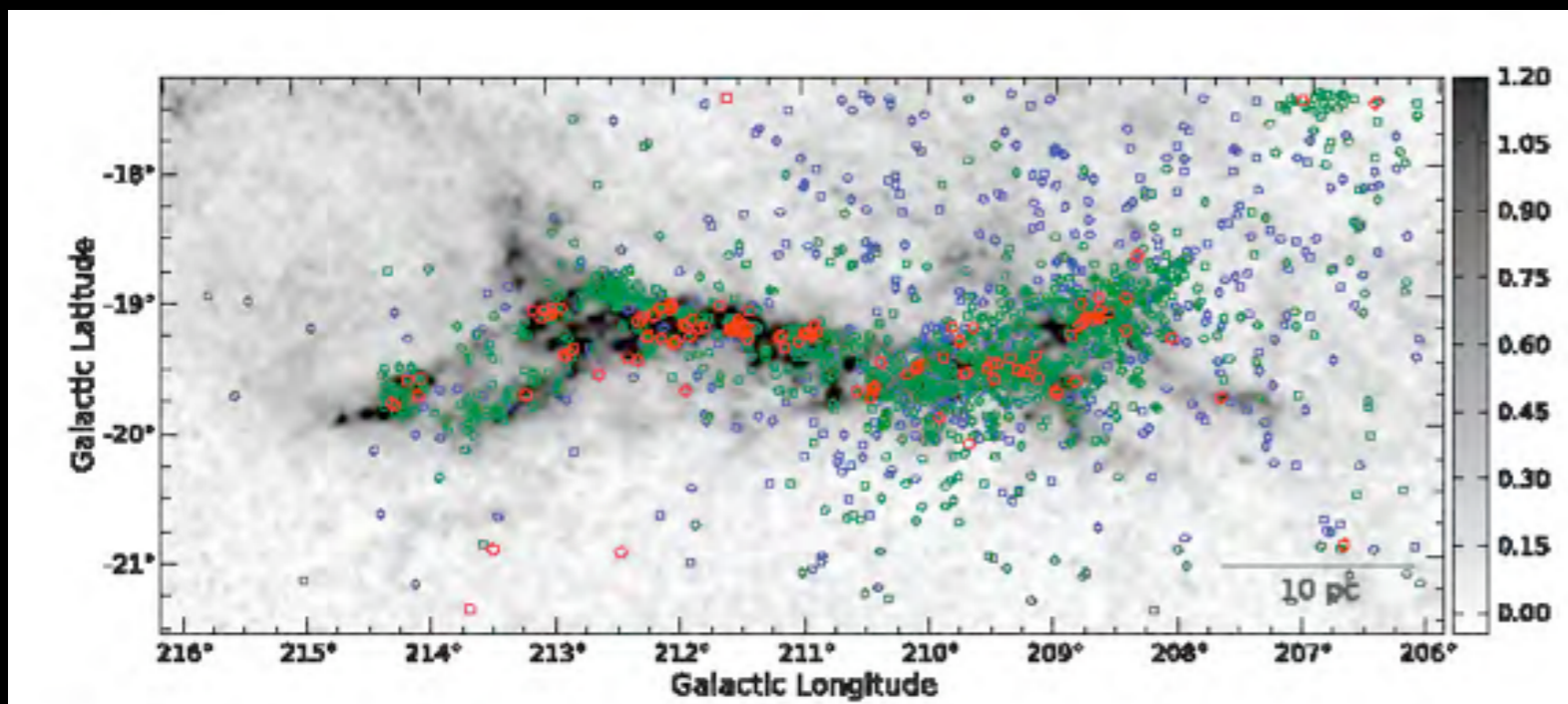
Cloud sample: wide field 2MASS/NICER
extinction survey of 21 local molecular clouds



Cloud	Mass (10^4)
Orion A	6.77
Orion B	7.18
California	9.99
Perseus	1.84
Taurus	1.49
Ophiuchus	1.41
RCrA	0.11
Pipe	0.79
Lupus 1	0.22
Lupus 3	0.14
Lupus 4	0.08

Inventory of Star Formation Activity: Young Stellar Objects (YSOs)

Mining the literature: mostly IR data (SPITZER)

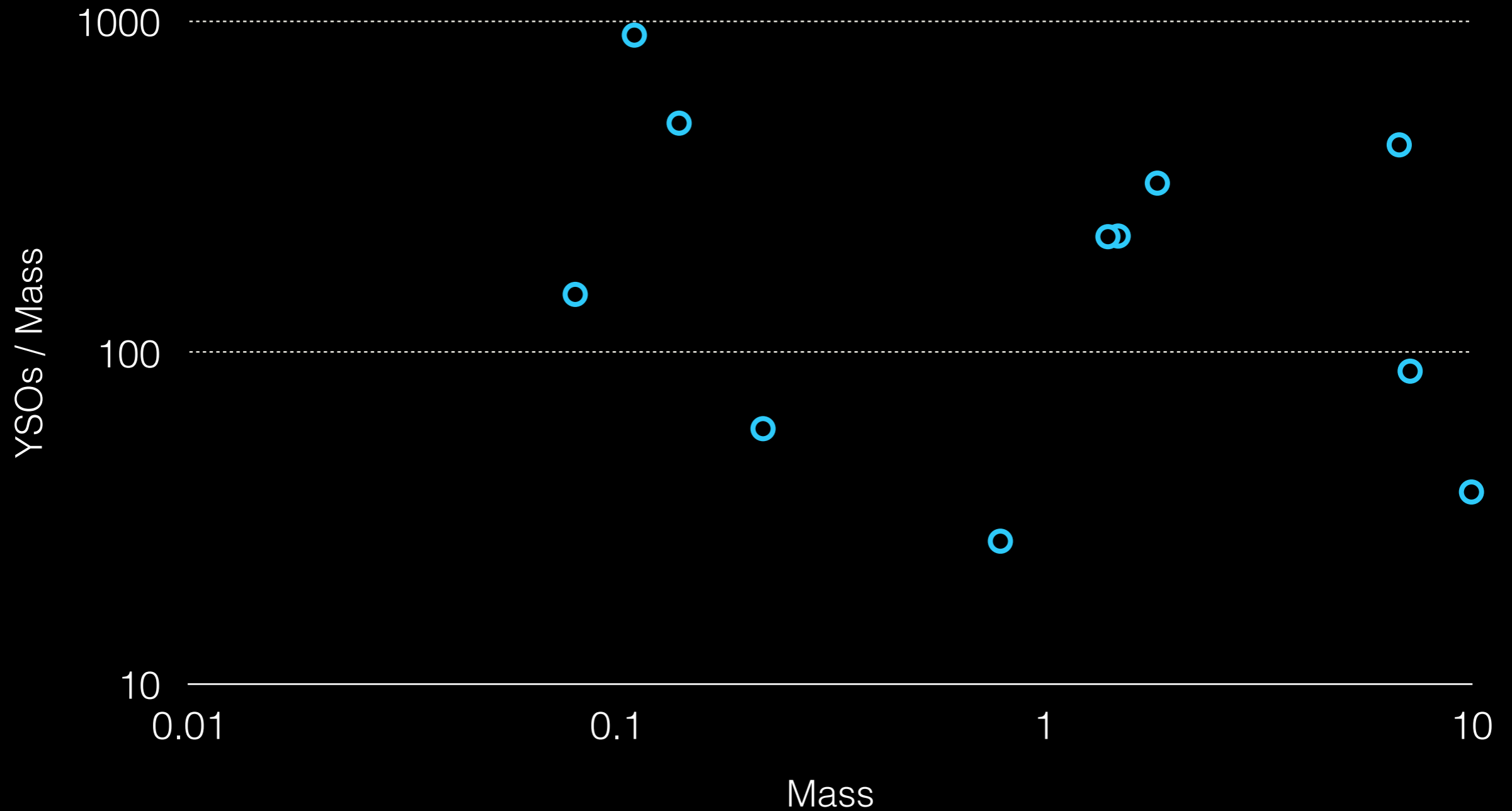


Cloud	YSOs
Orion A	2862
Orion B	635
California	279
Perseus	598
Taurus	335
Ophiuchus	316
RCrA	100
Pipe	21
Lupus 1	13
Lupus 3	69
Lupus 4	12

Inventory of Star Formation Activity: Young Stellar Objects (YSOs)

Cloud	Mass (10	YSOs	YSOs / Mass
Orion A	6.77	2862	424
Orion B	7.18	635	88
California	9.99	279	38
Perseus	1.84	598	325
Taurus	1.49	335	225
Ophiuchus	1.41	316	224
RCrA	0.11	100	909
Pipe	0.79	21	27
Lupus 1	0.22	13	59
Lupus 3	0.14	69	493
Lupus 4	0.08	12	150

Inventory of Star Formation Activity: Young Stellar Objects (YSOs)



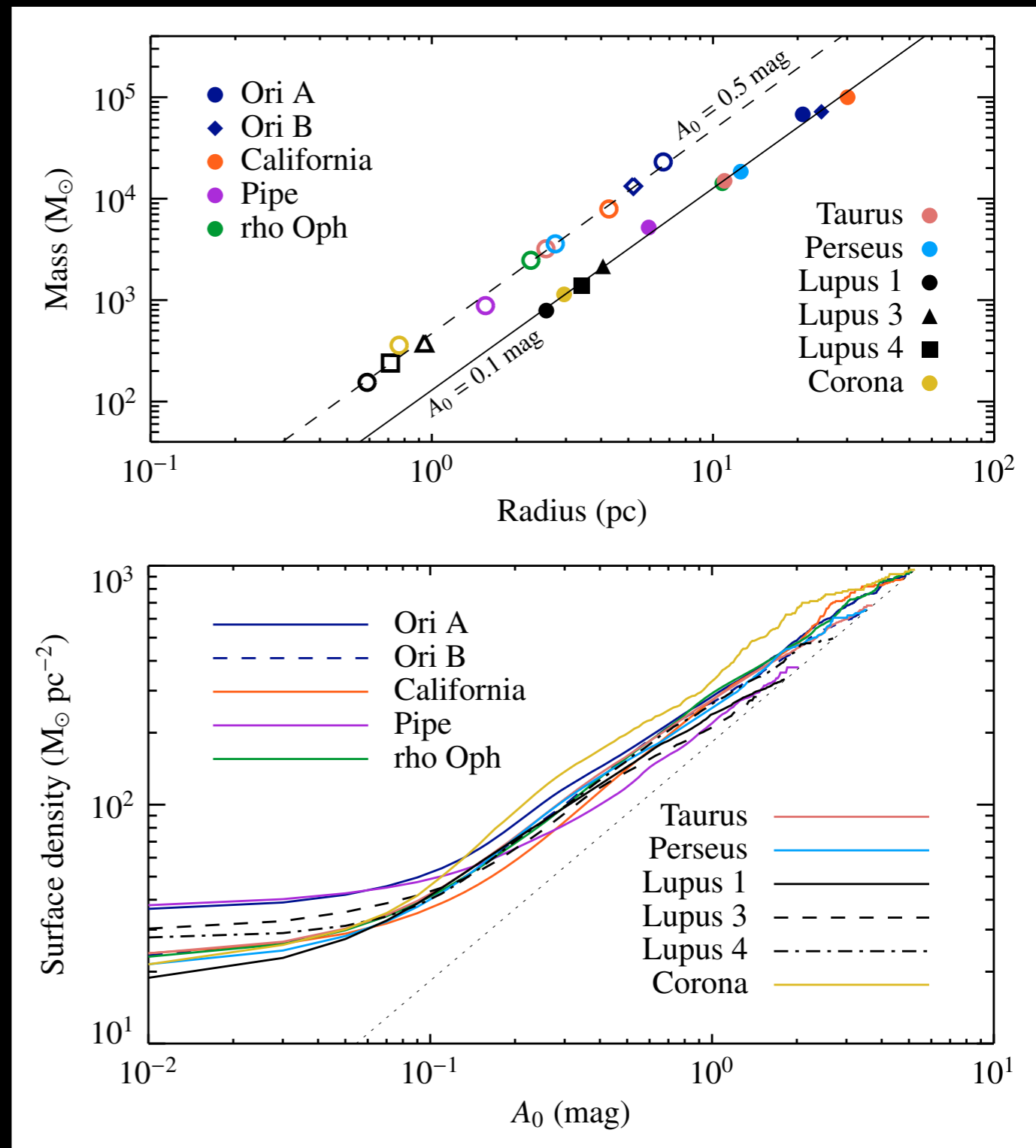
Inventory of Star Formation Activity: Young Stellar Objects (YSOs)



Fact 4

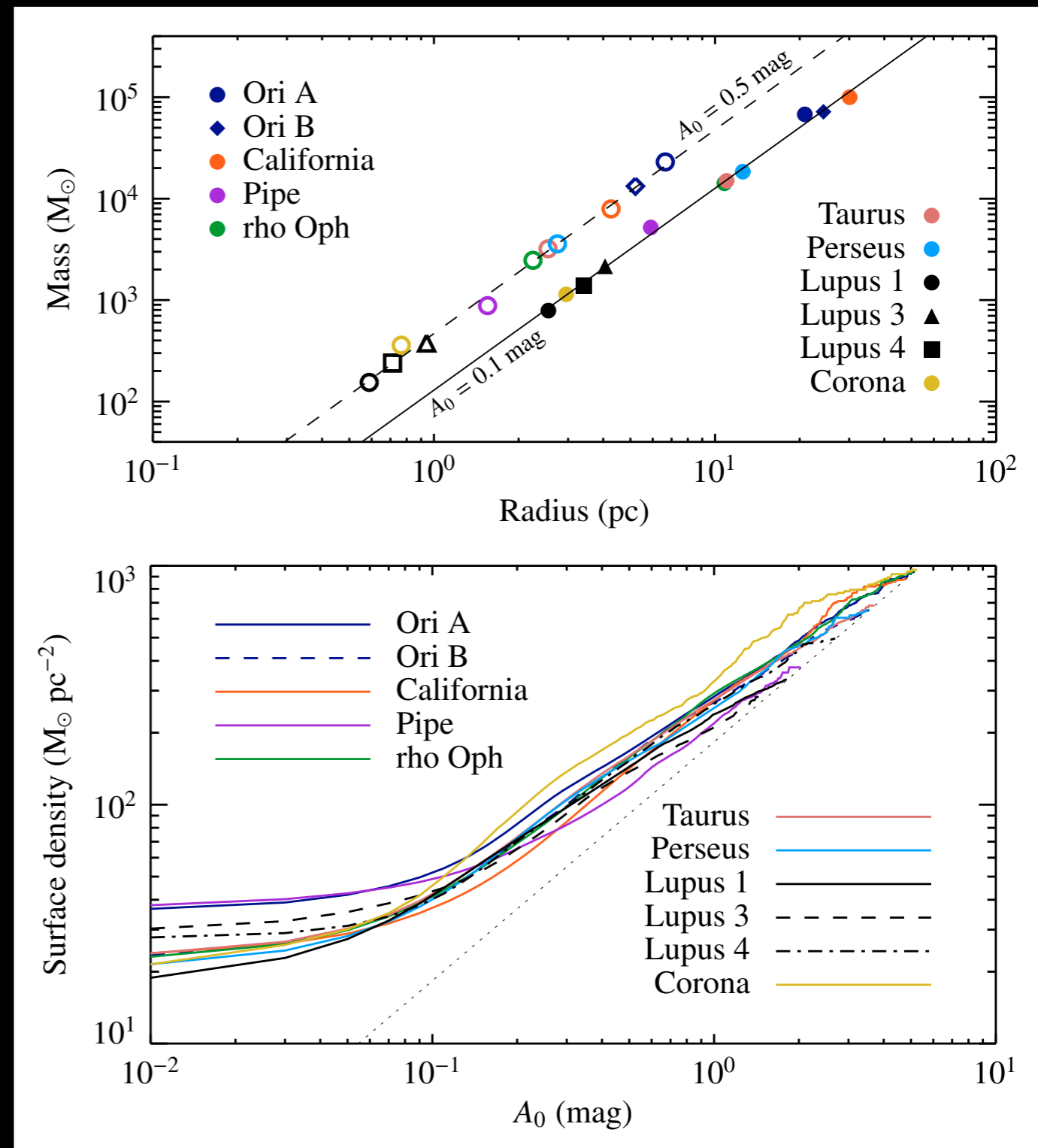
Molecular clouds have a
peculiar structure

The structure of molecular clouds



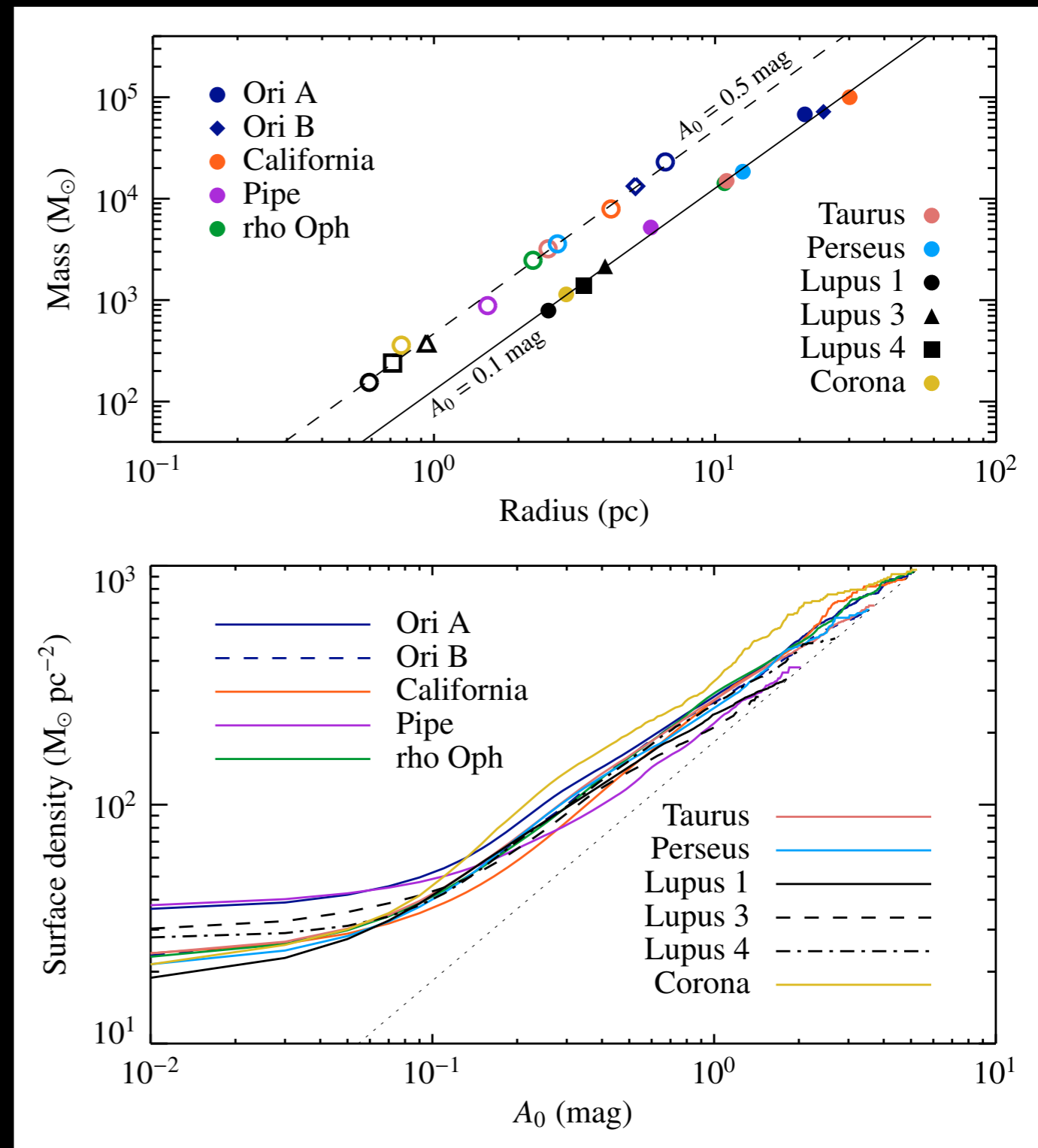
The structure of molecular clouds

- Different molecular clouds show **consistent structure**



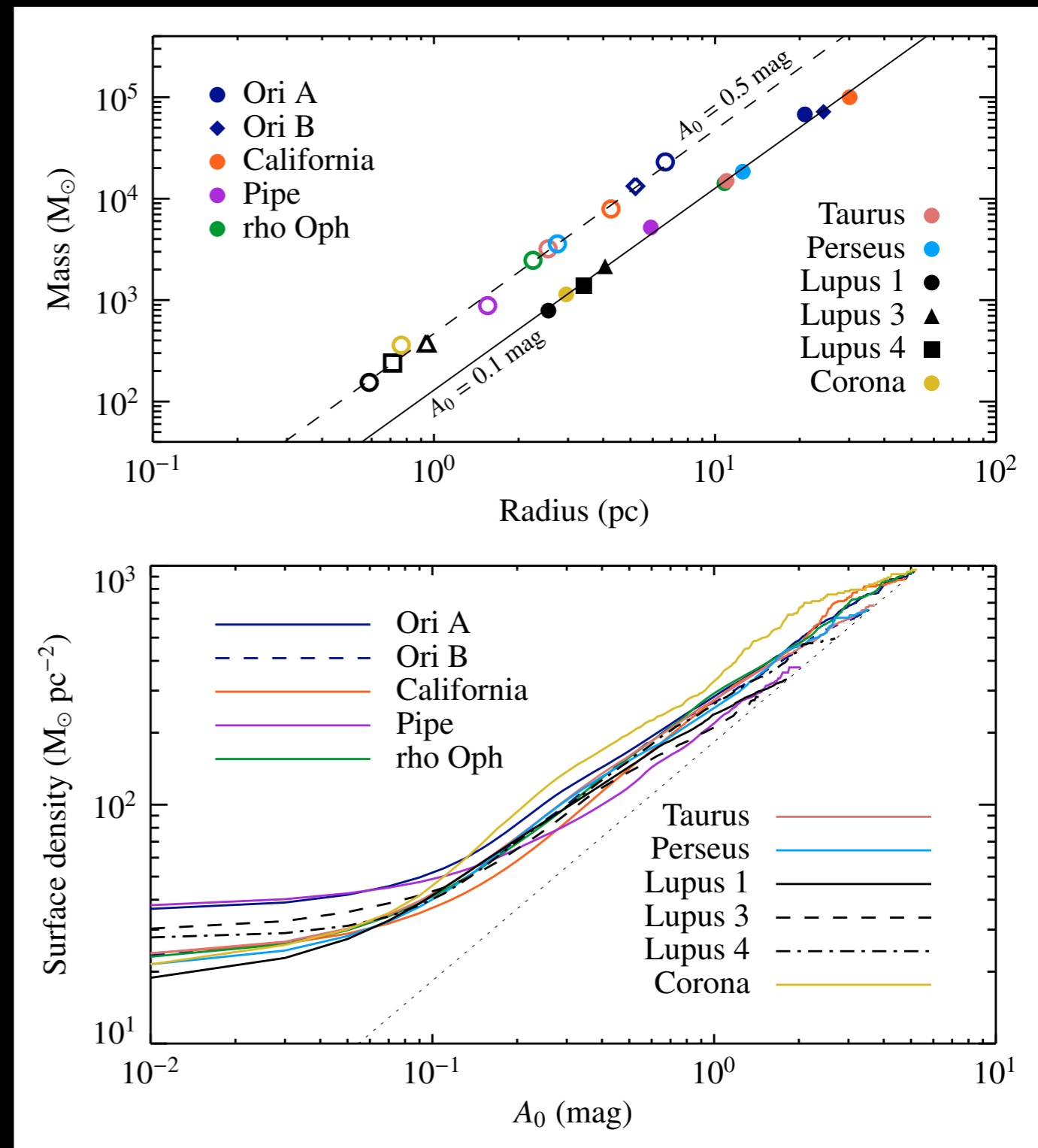
The structure of molecular clouds

- Different molecular clouds show **consistent structure**
- **Same average density** above threshold value (as predicted by WDM)



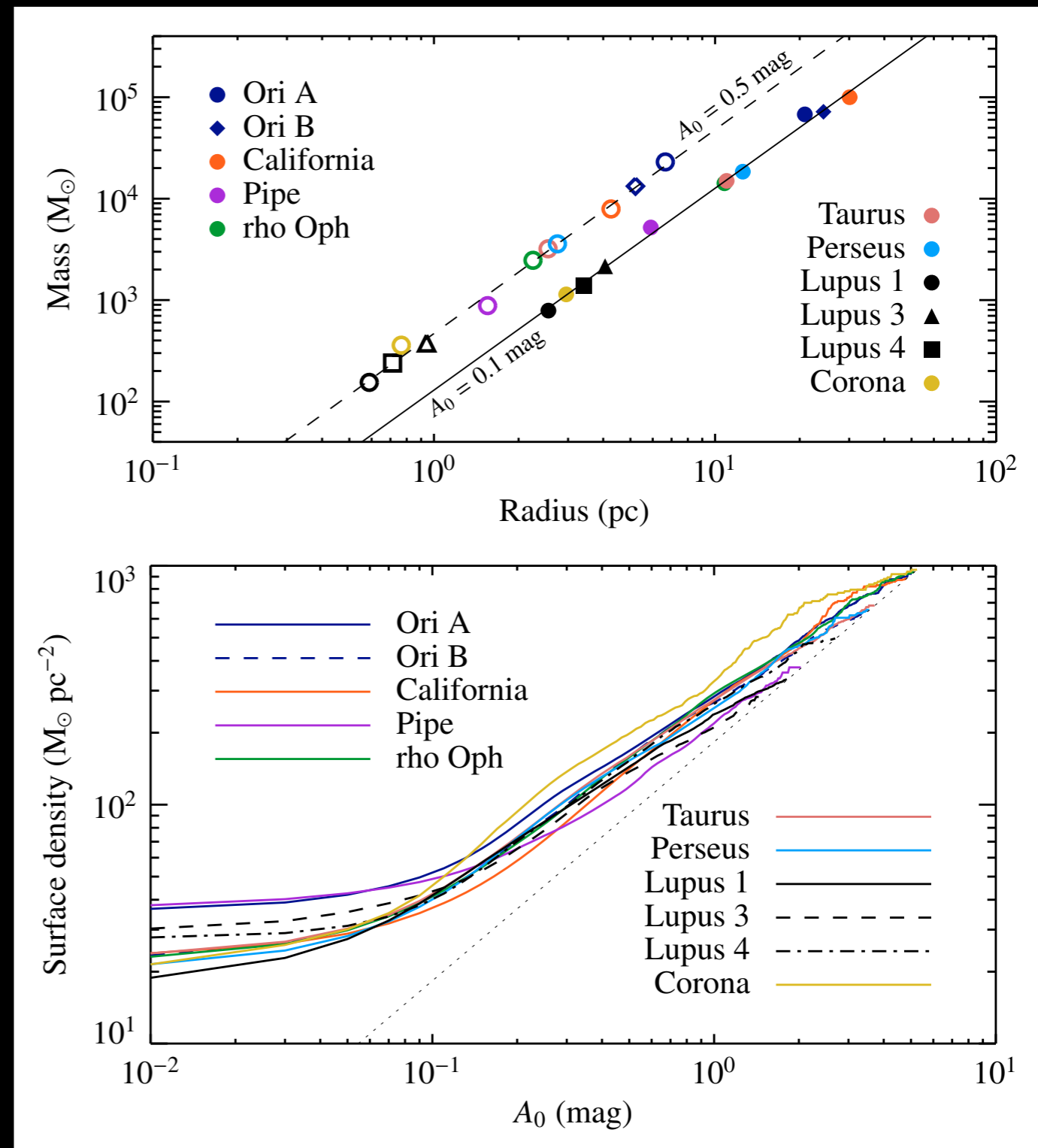
The structure of molecular clouds

- Different molecular clouds show **consistent structure**
- **Same average density** above threshold value (as predicted by WDM)
- **Same probability distribution** for Σ (log-normal)

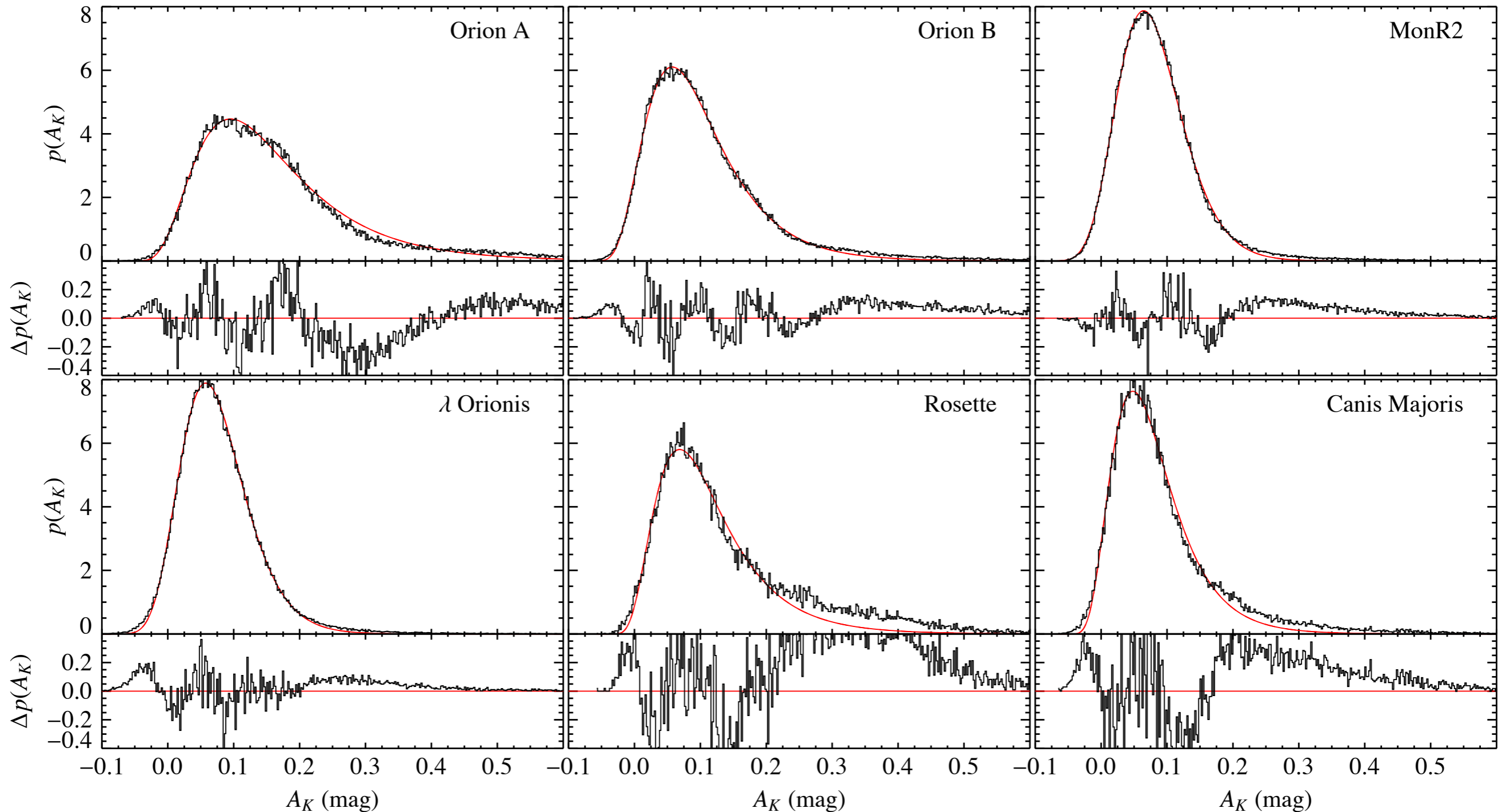


The structure of molecular clouds

- Different molecular clouds show **consistent structure**
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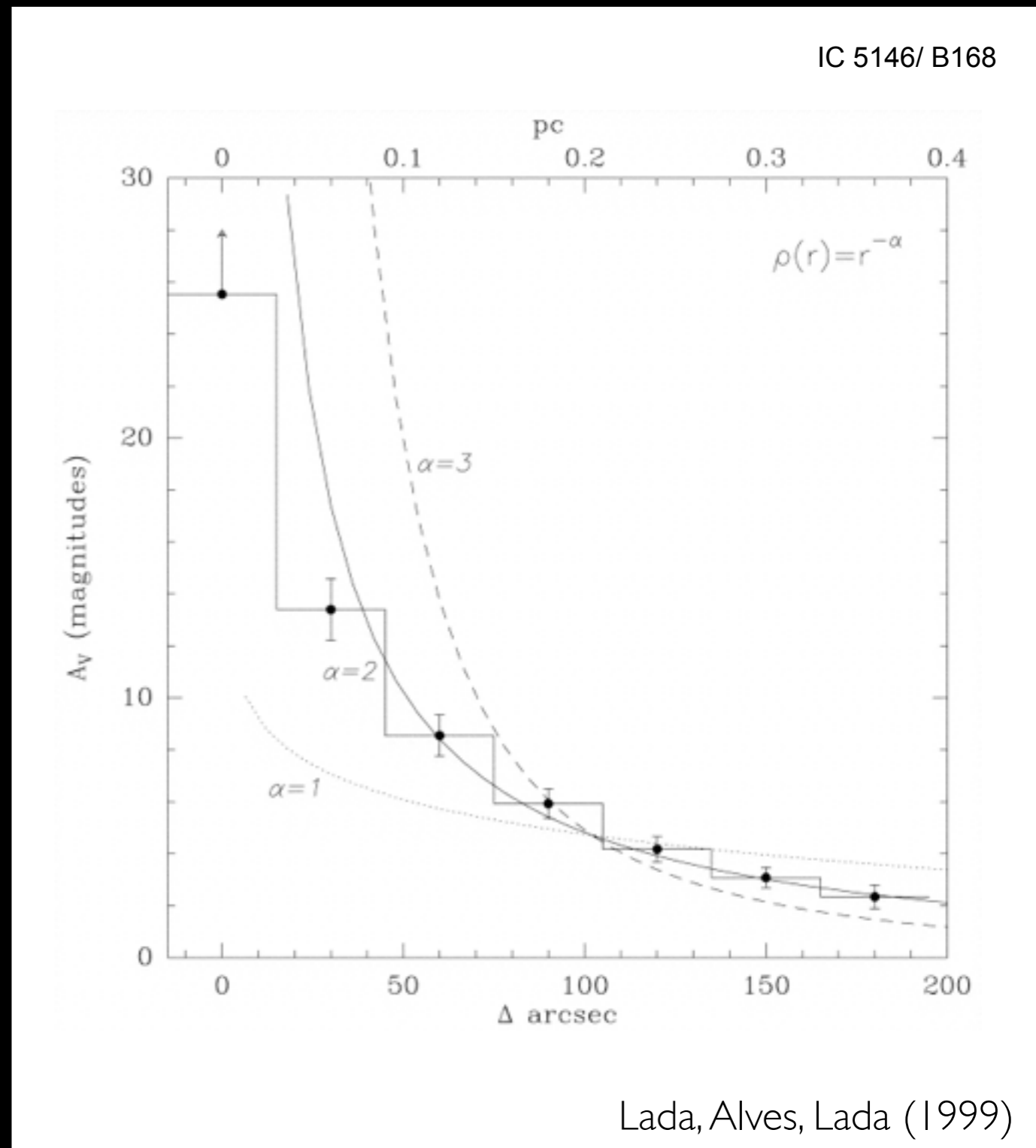
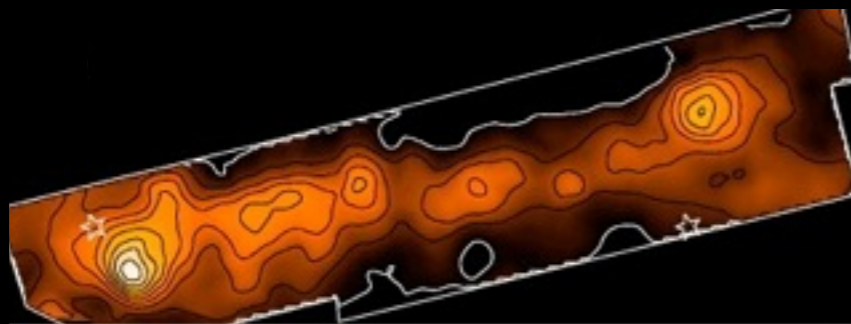


Log-normal fits to cloud projected density distributions

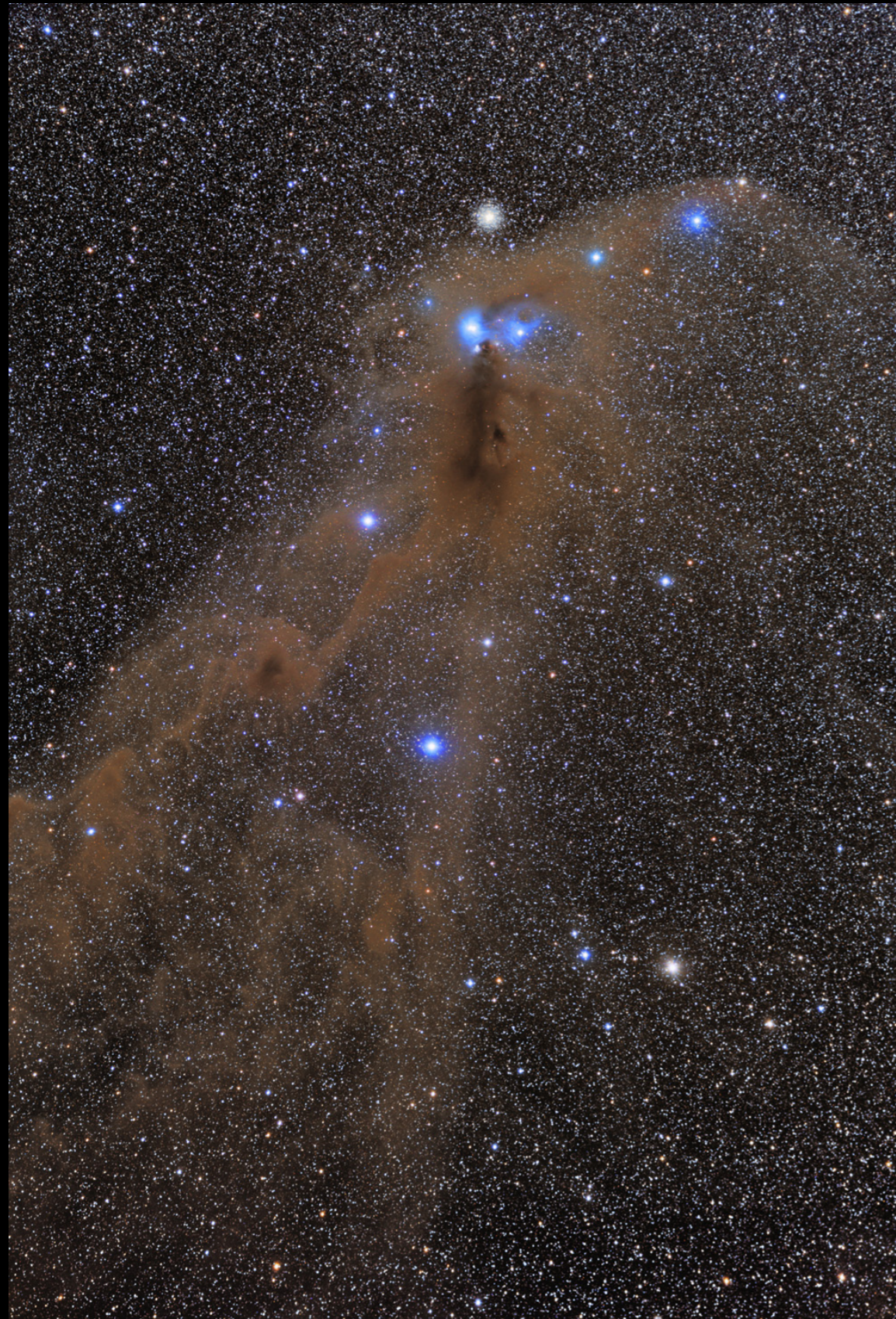


A Σ - ρ relation for molecular clouds

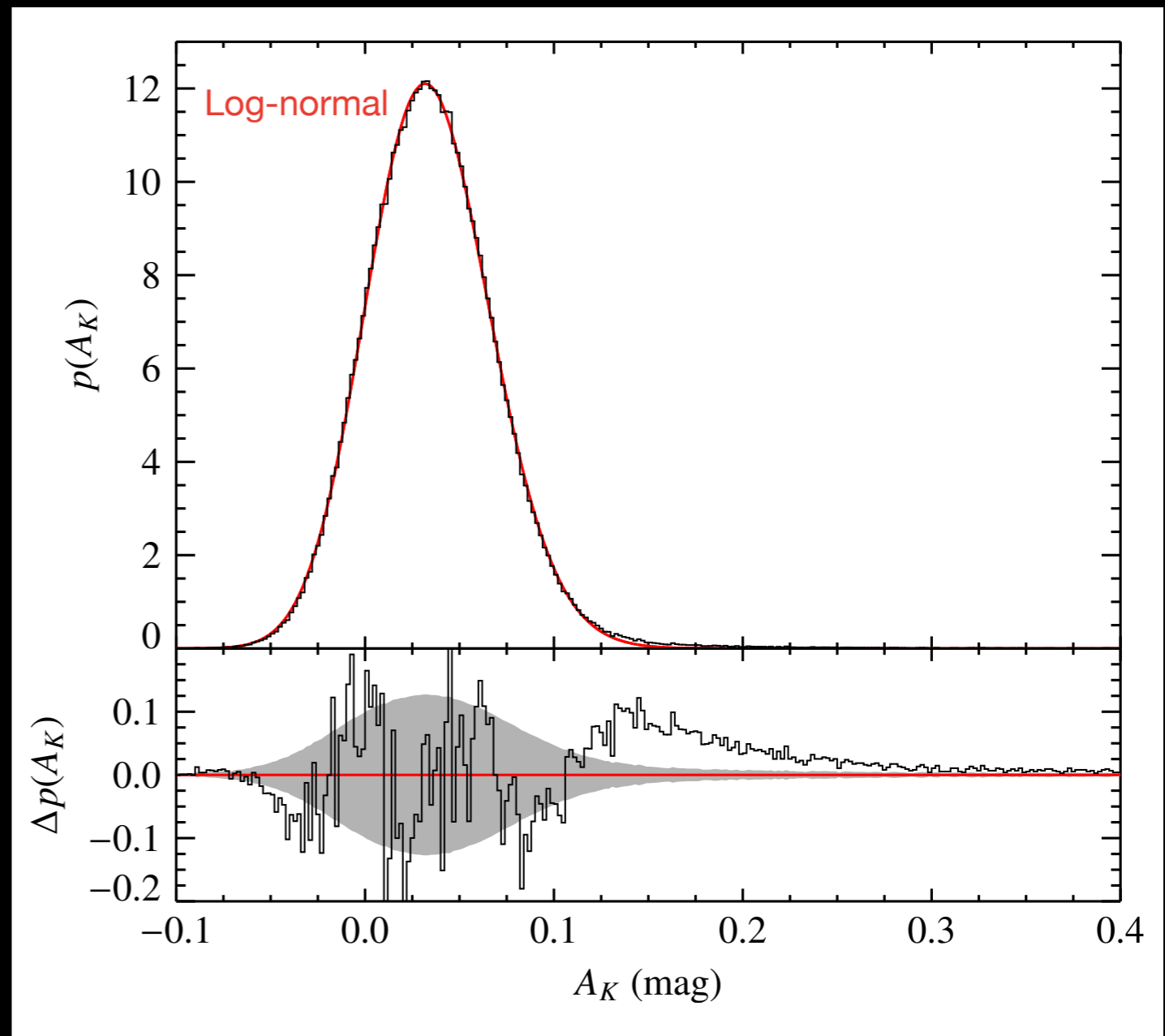
- Different Molecular clouds show **consistent structure**
- **Same average density** above threshold value (as predicted by WDM)
- **Same probability distribution** for Σ (log-normal)
- Similar stratification of surface density contours



Log-normals? Think it twice

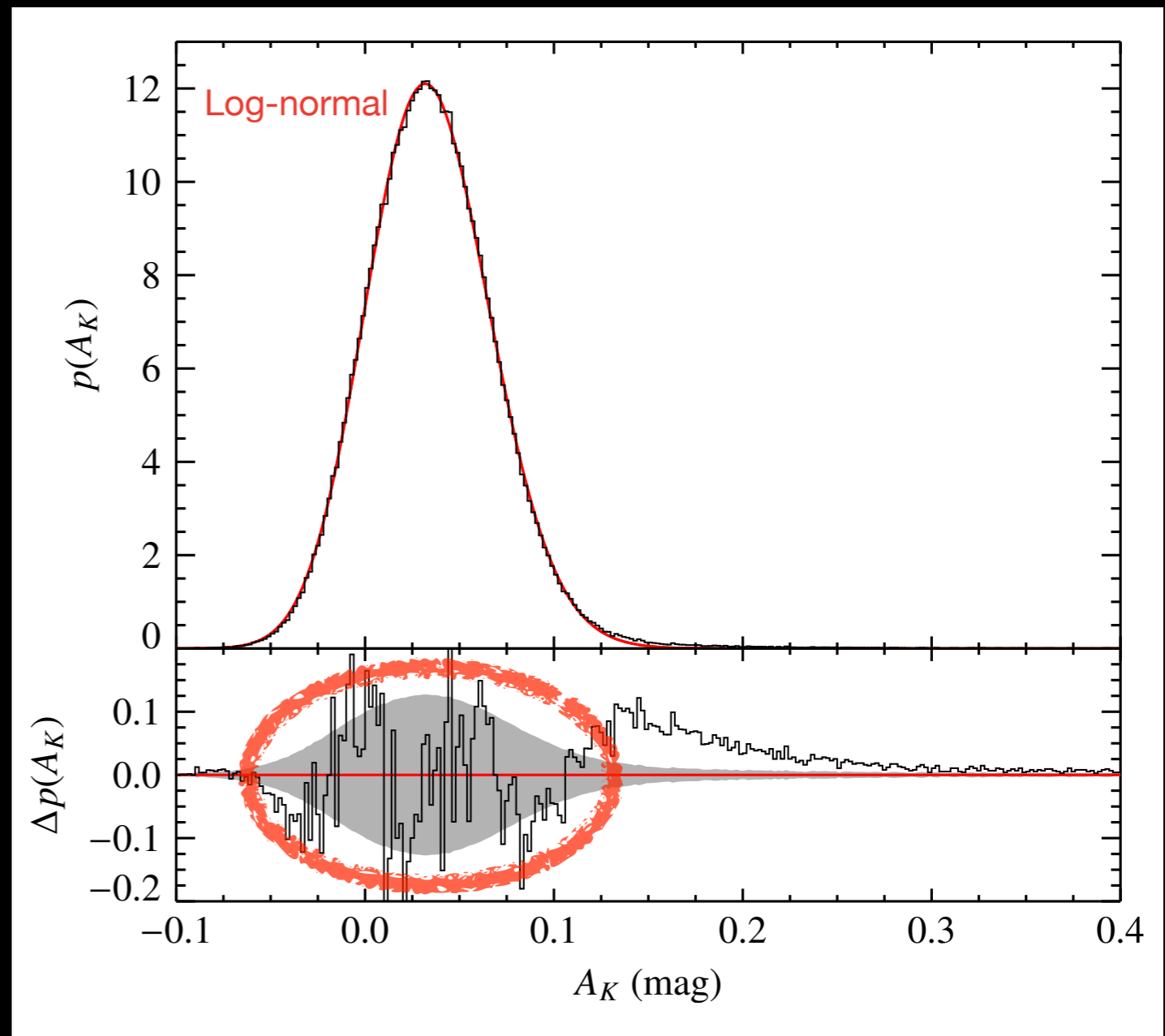


Log-normals? Think it twice



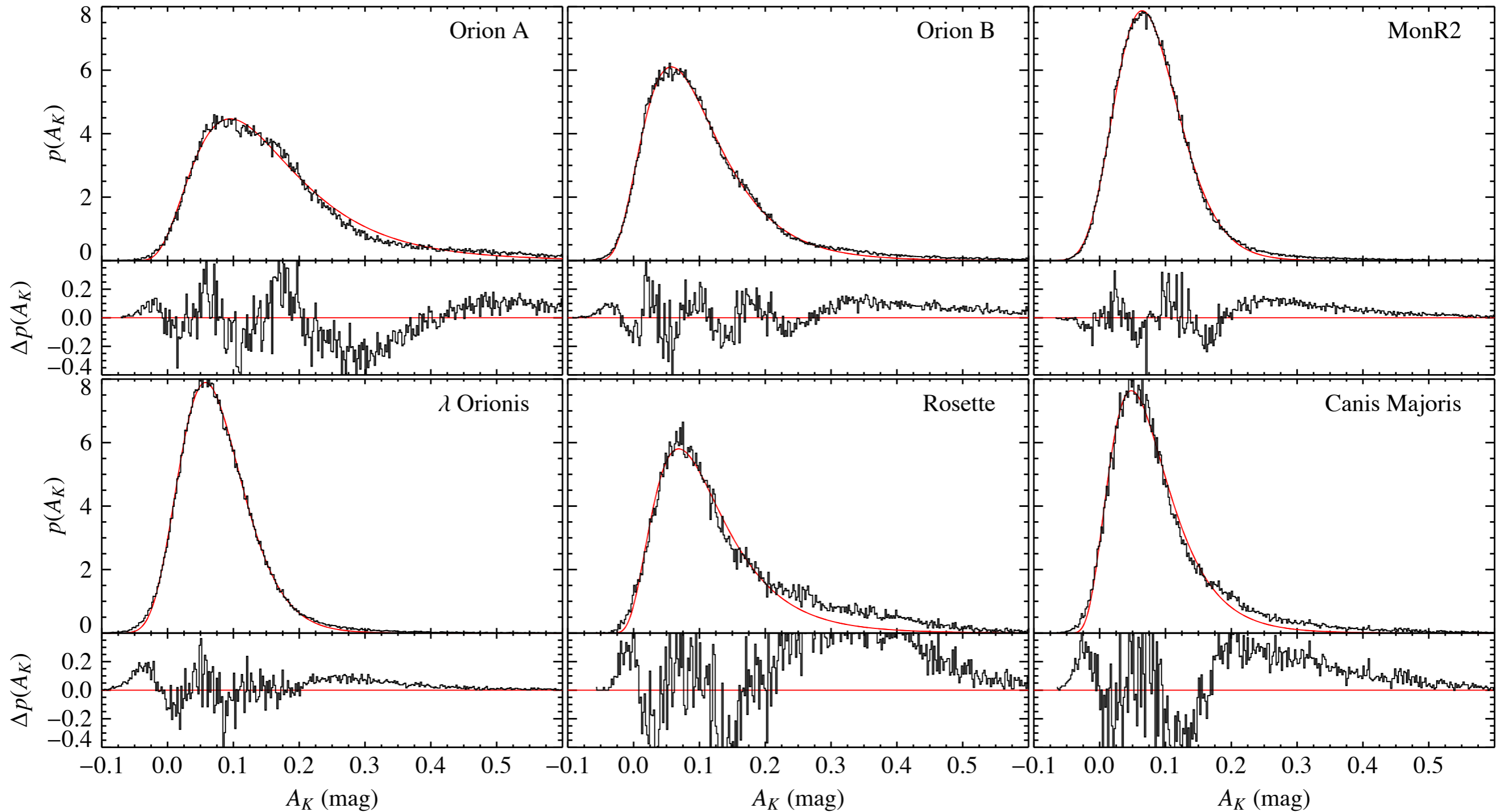
Systematic residuals in the entire fitting region!

Log-normals? Think it twice

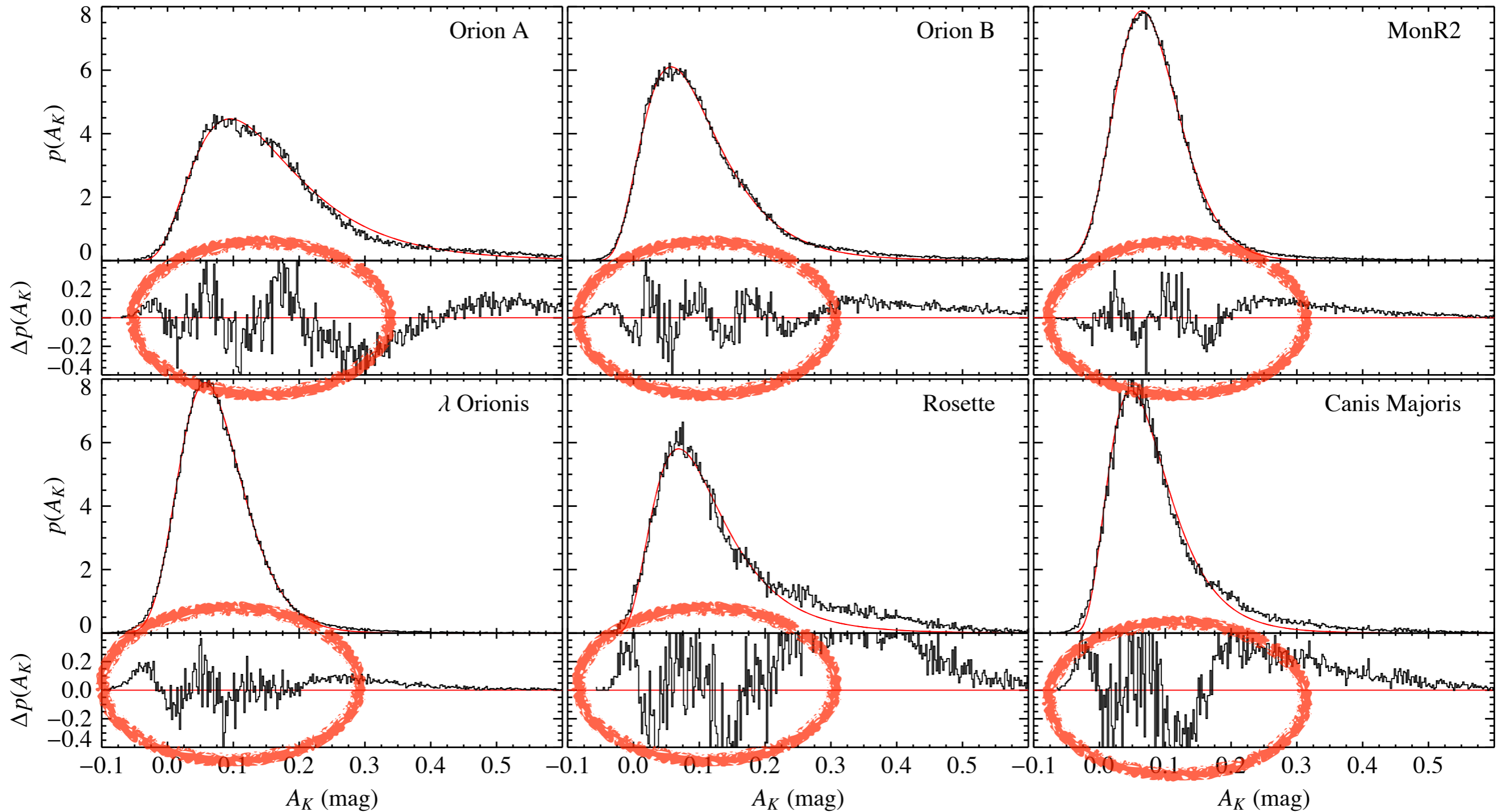


Systematic residuals in the entire fitting region!

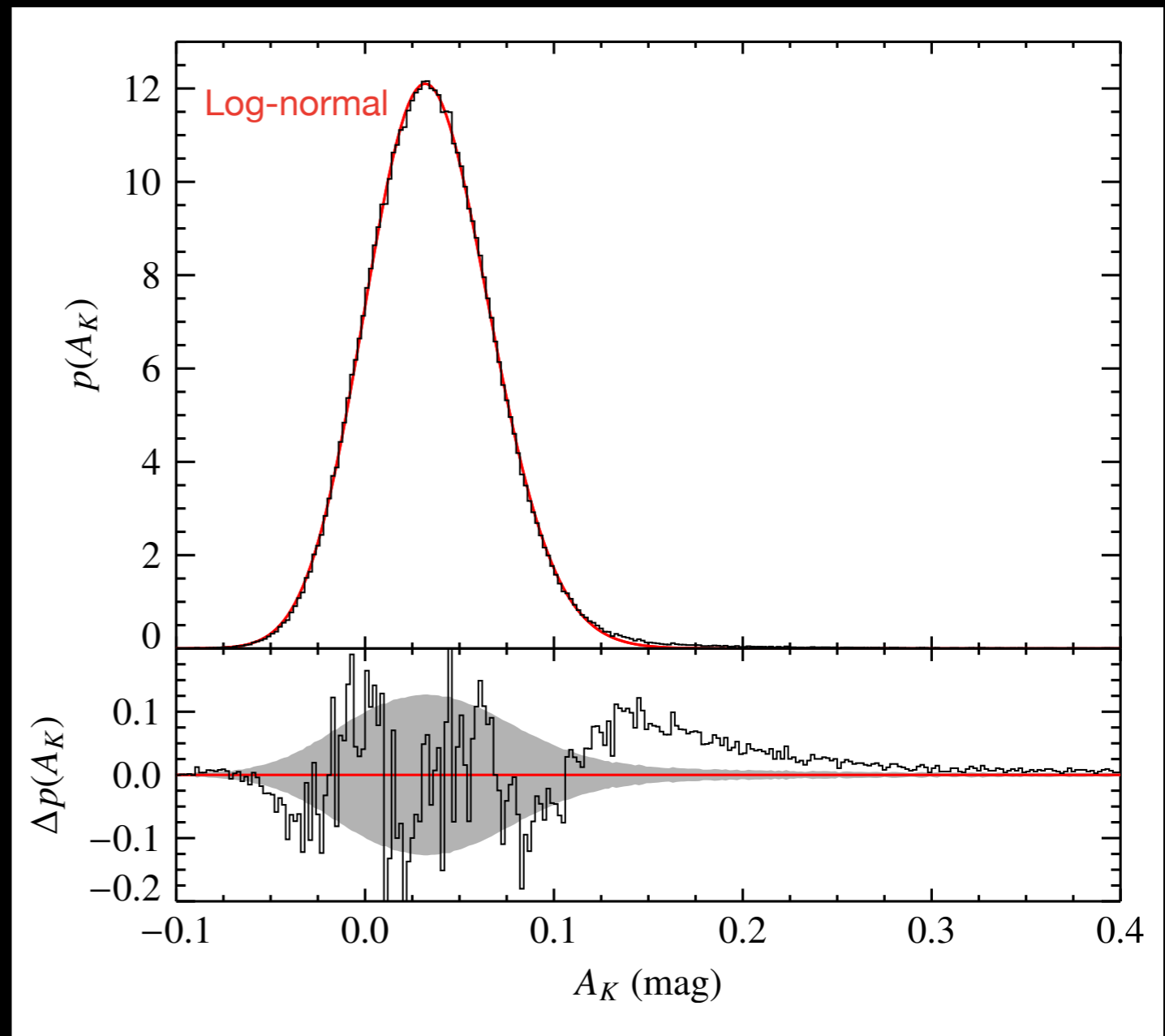
All log-normal fits show systematic residuals



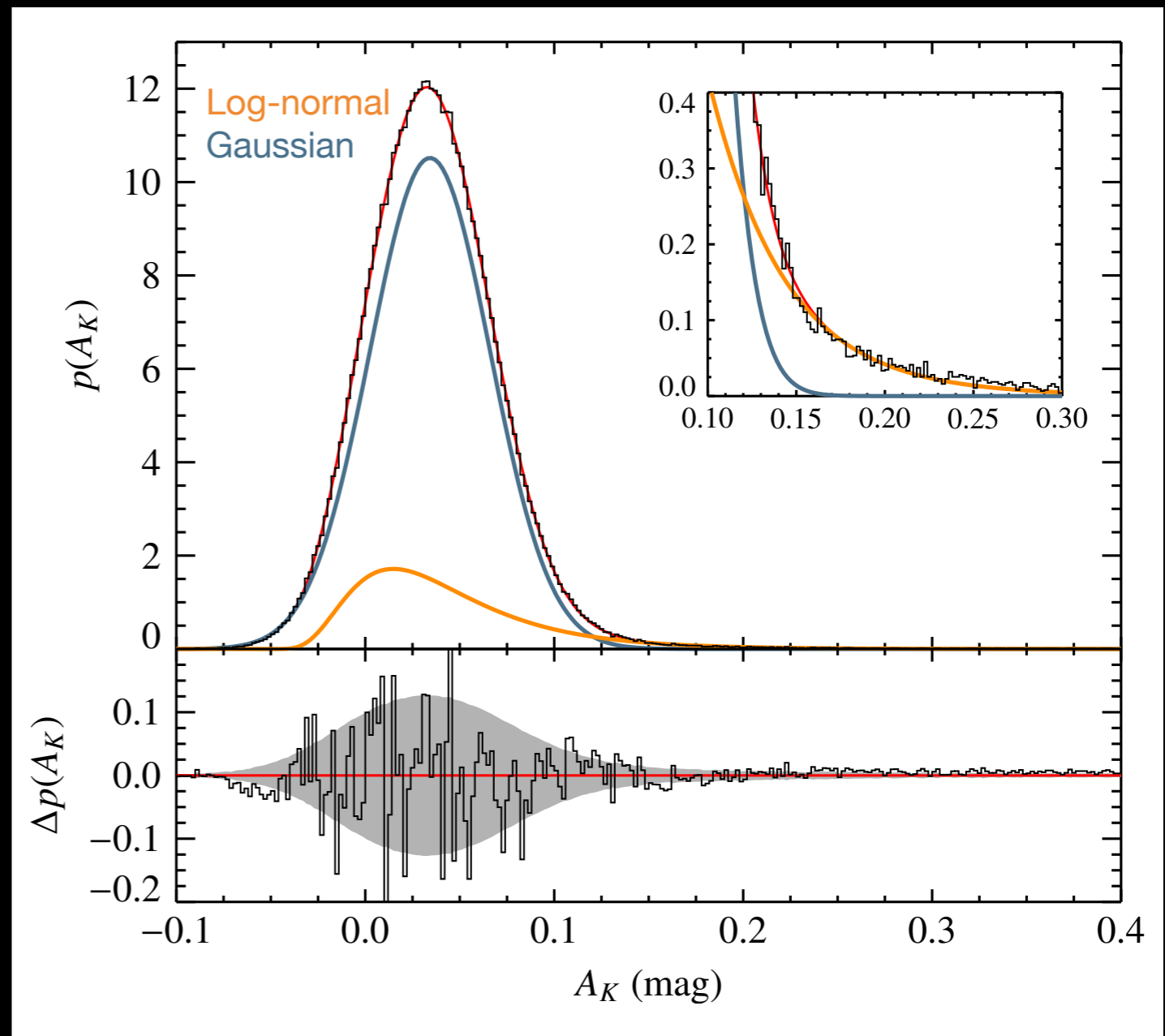
All log-normal fits show systematic residuals



Log-normals? Think it twice

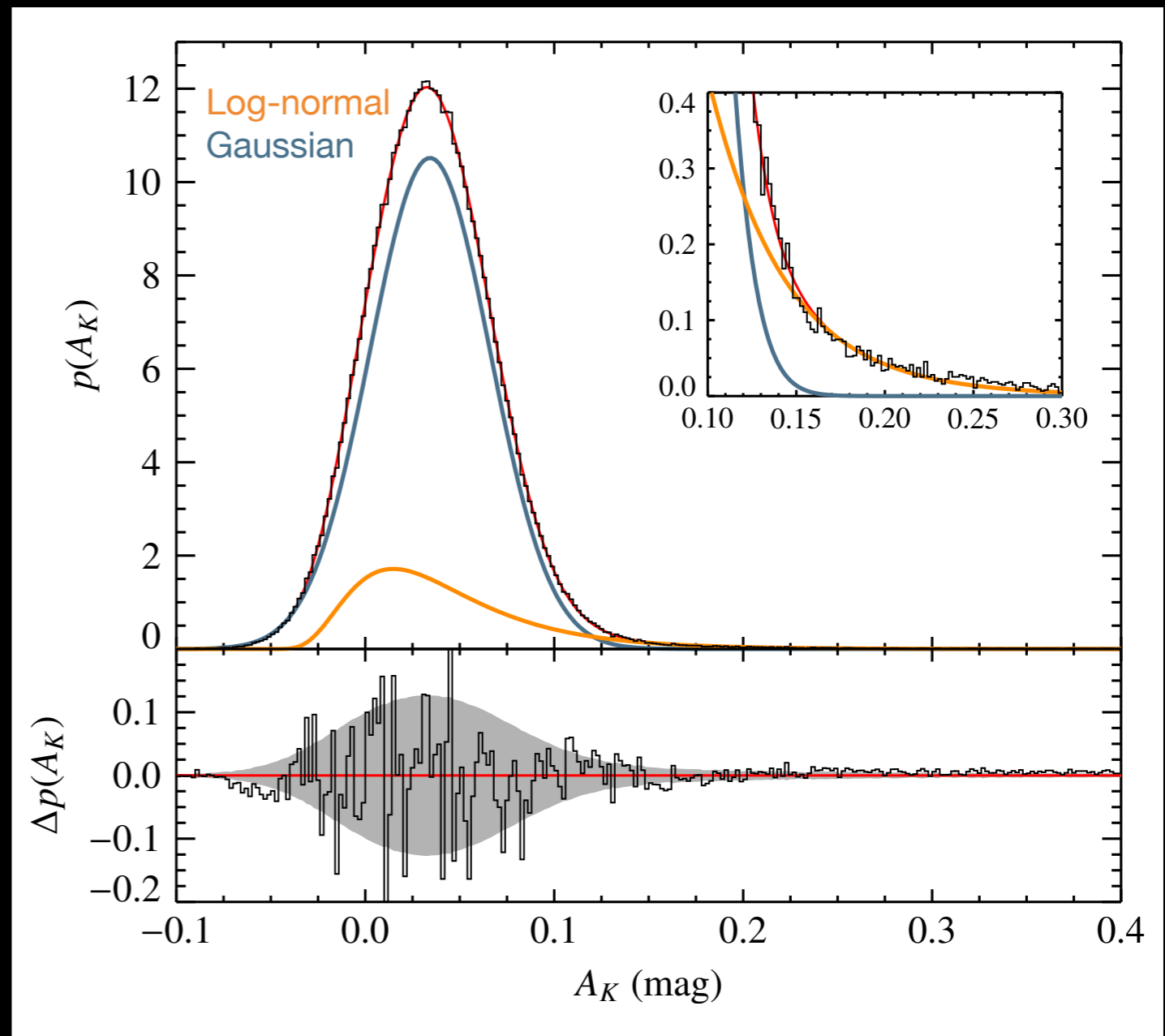


Log-normals? Think it twice



Residuals disappear when fitting a
Gaussian + Log-normal.

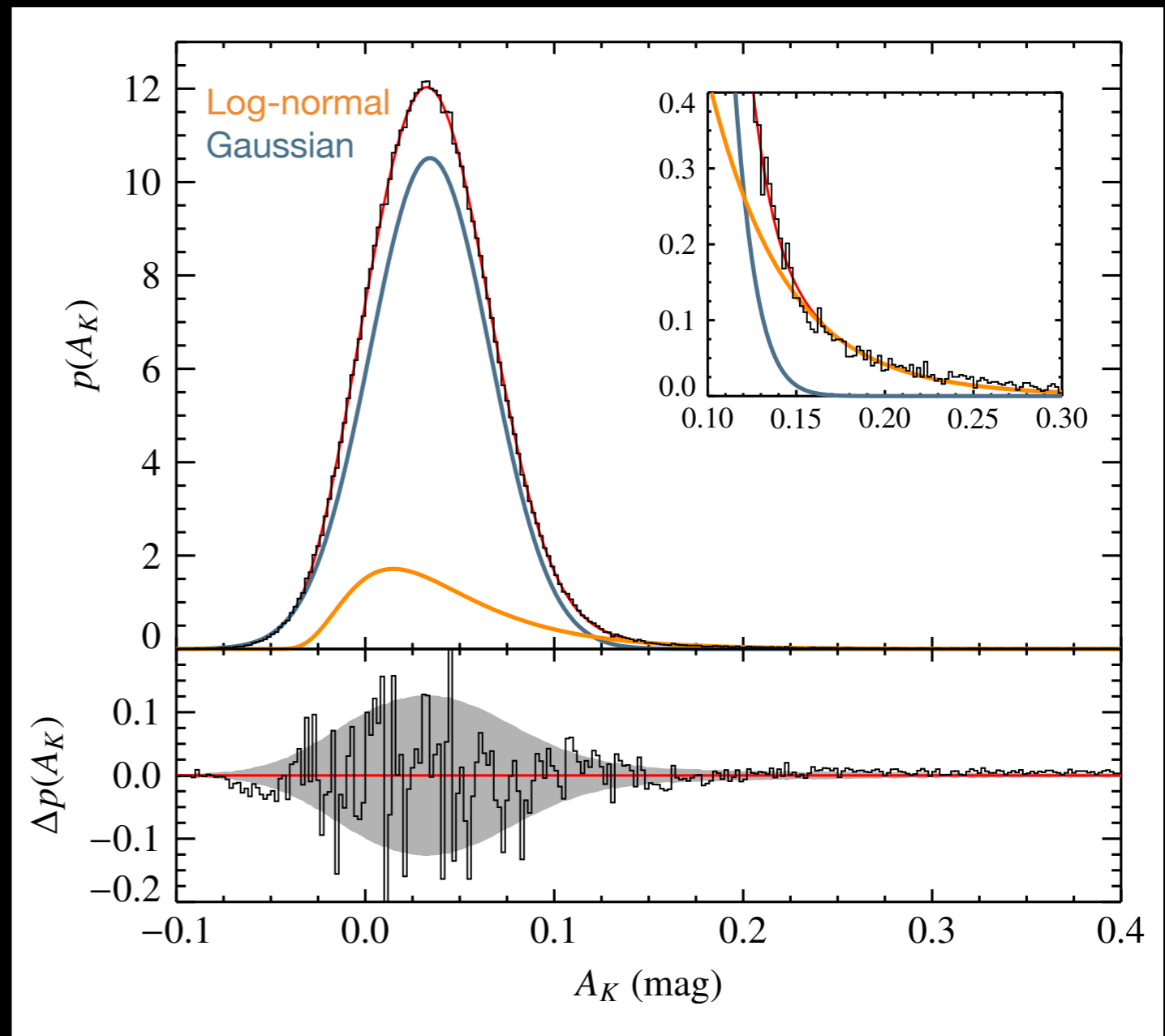
Log-normals? Think it twice



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Log-normals? Think it twice

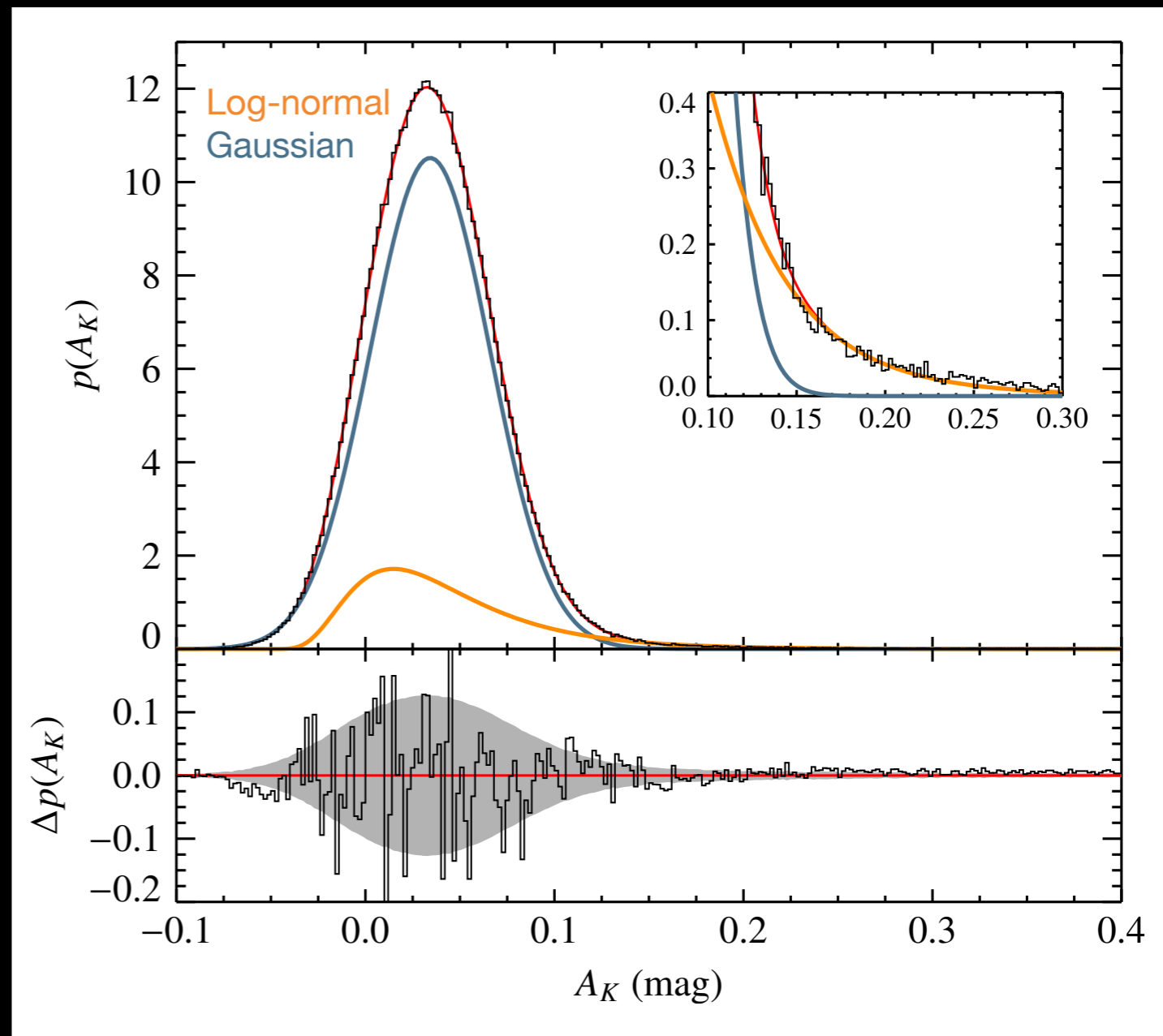
- What is the physical meaning?



Residuals disappear when fitting a
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Log-normals? Think it twice

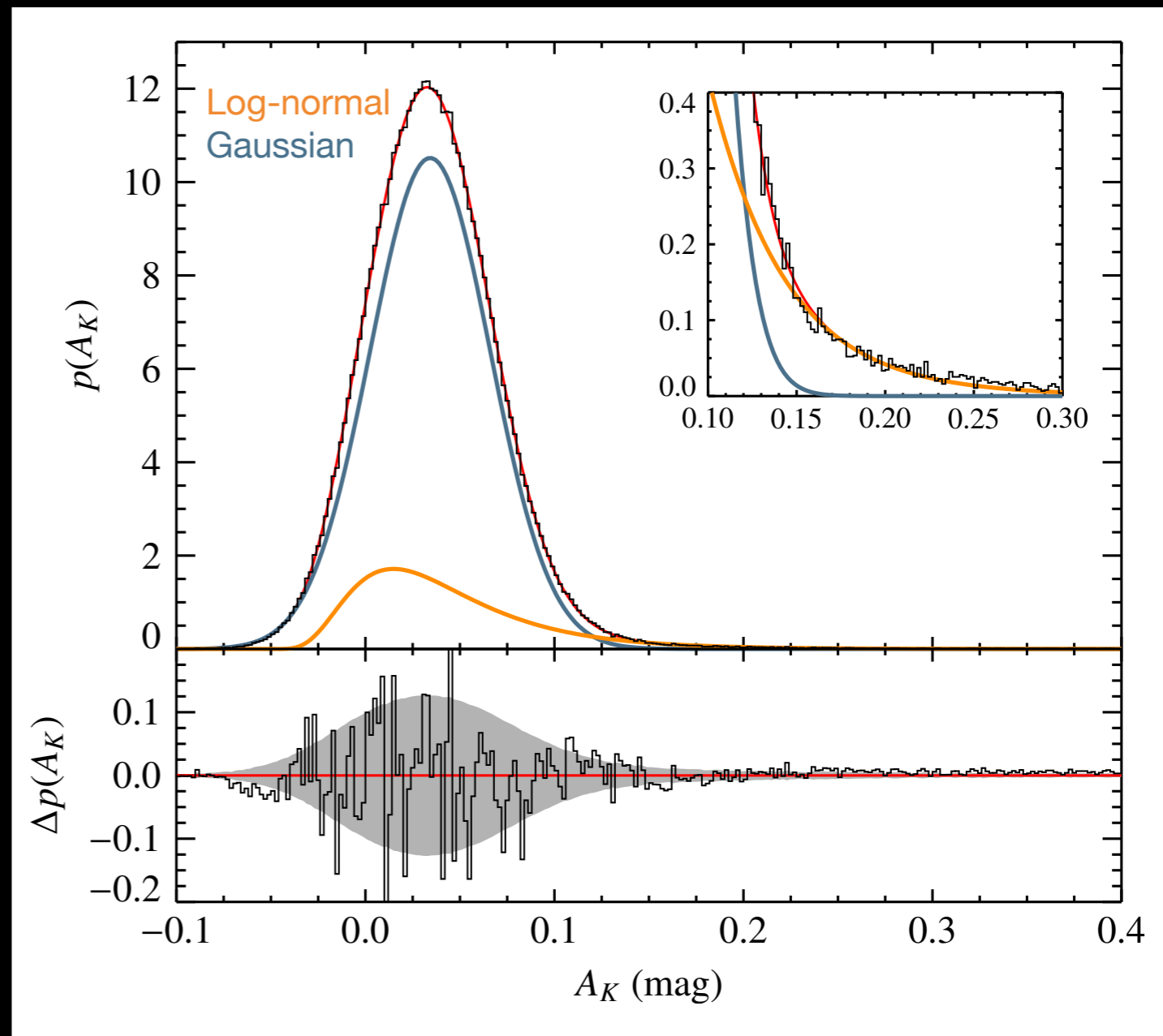
- What is the physical meaning?
- **Gaussian**: diffuse extended region + noise



Residuals disappear when fitting a Gaussian + Log-normal.

Log-normals? Think it twice

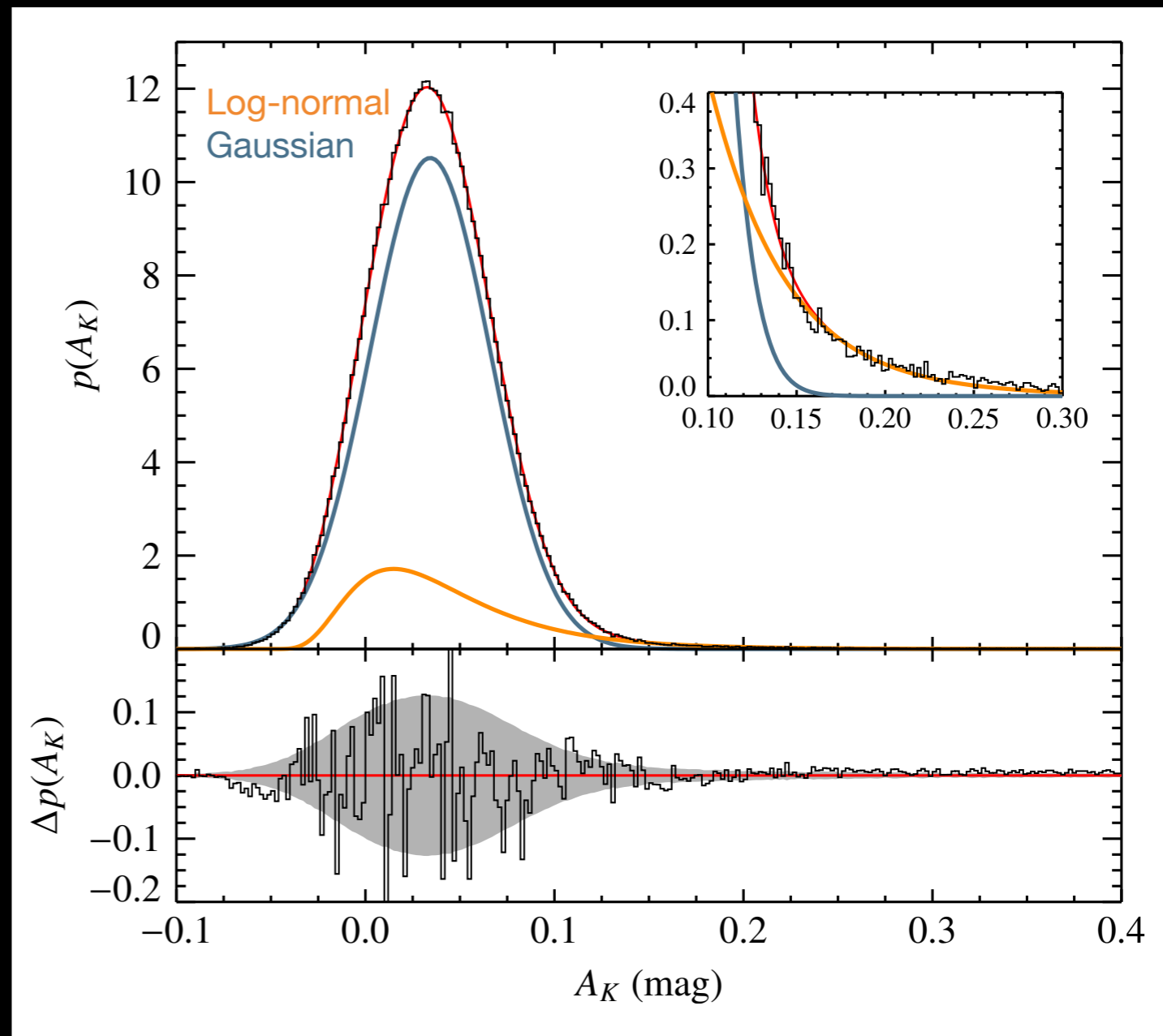
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Log-normals? Think it twice

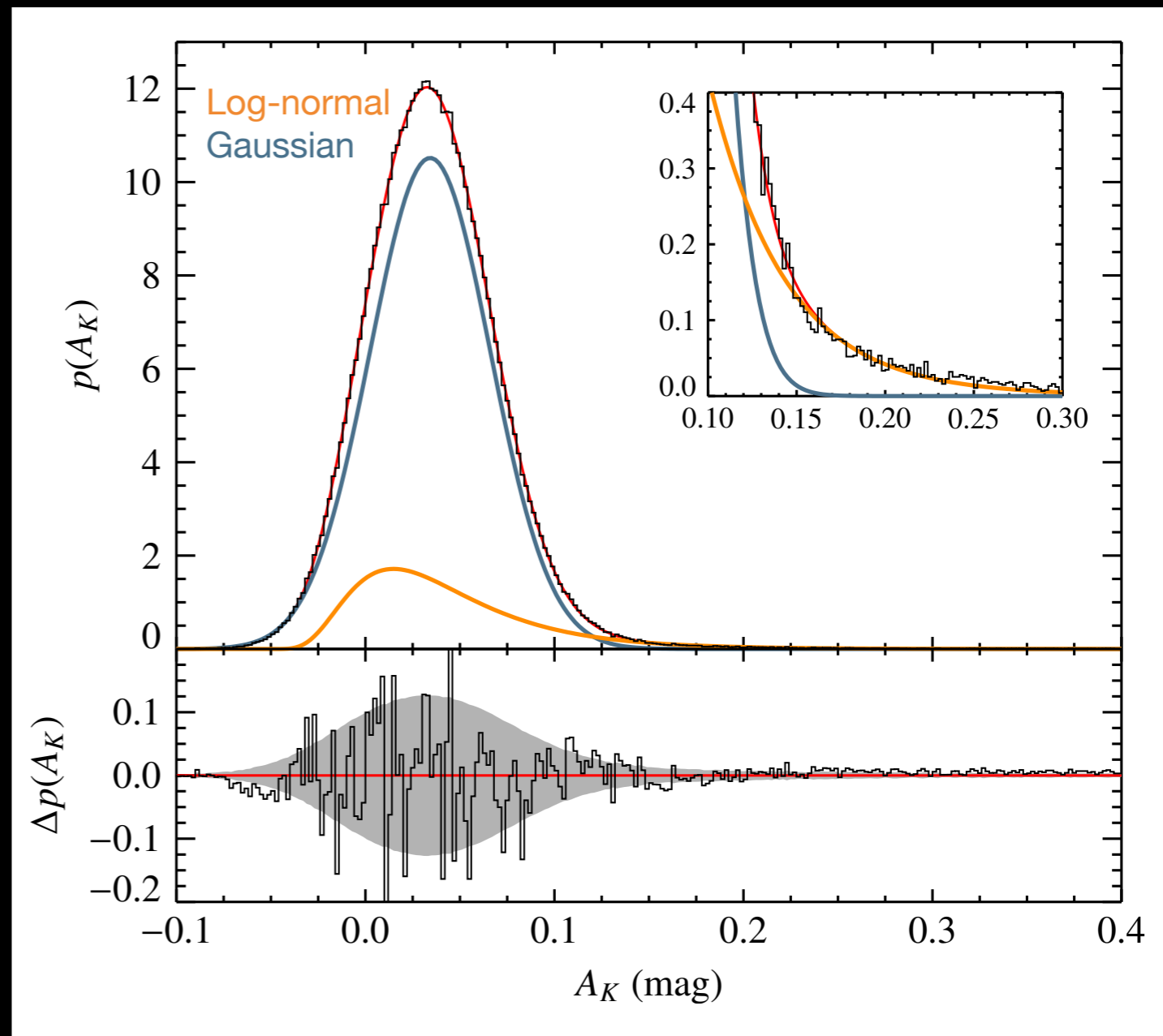
- What is the physical meaning?
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- **Log-normal**: denser parts
- What is the role of noise?



Residuals disappear when fitting a Gaussian + Log-normal.

Log-normals? Think it twice

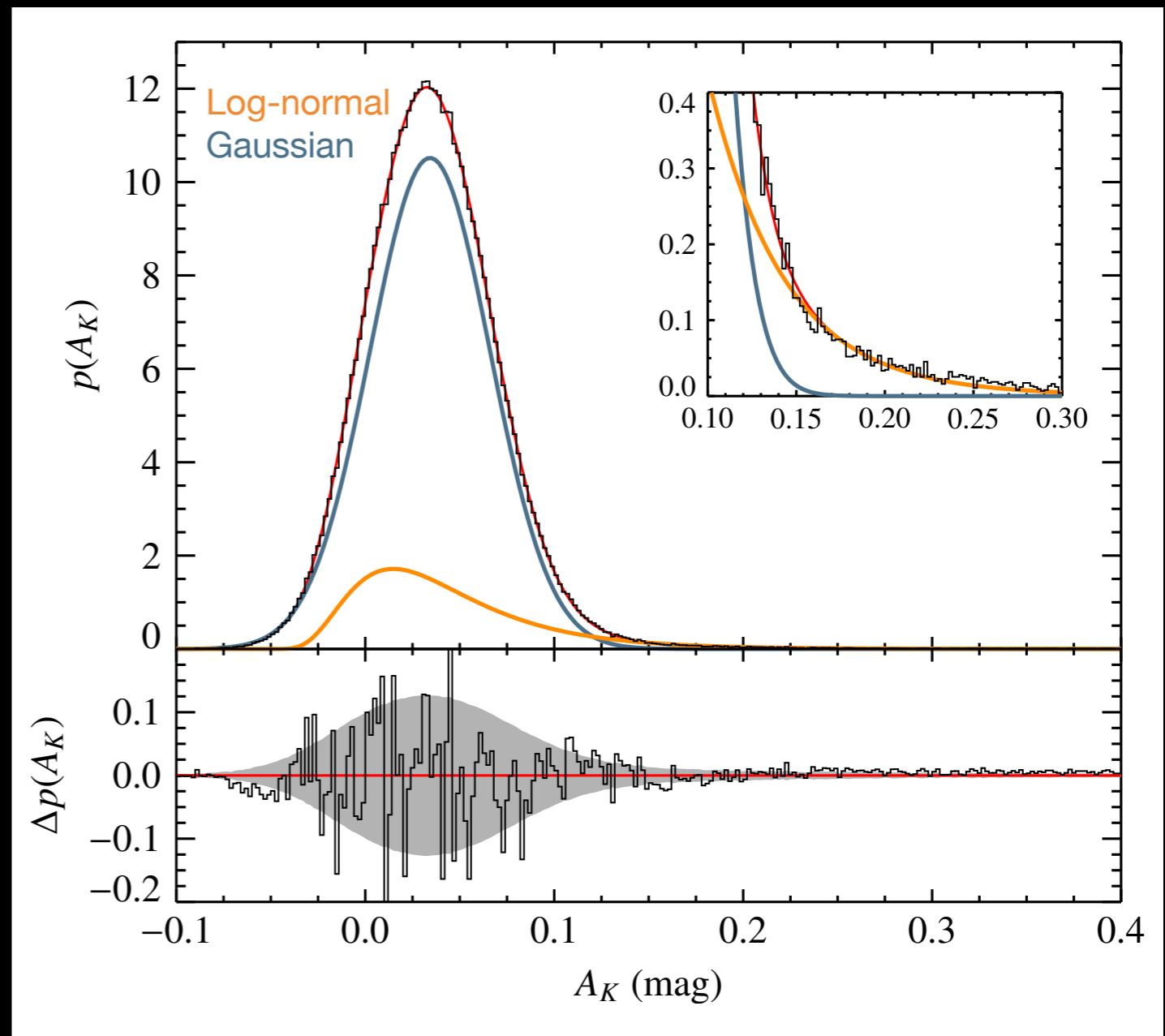
- What is the physical meaning?
- **Gaussian**: diffuse extended region + noise
- **Log-normal**: denser parts
- What is the role of noise?
- Dominates at low A_K !



Residuals disappear when fitting a Gaussian + Log-normal.

Log-normals? Think it twice

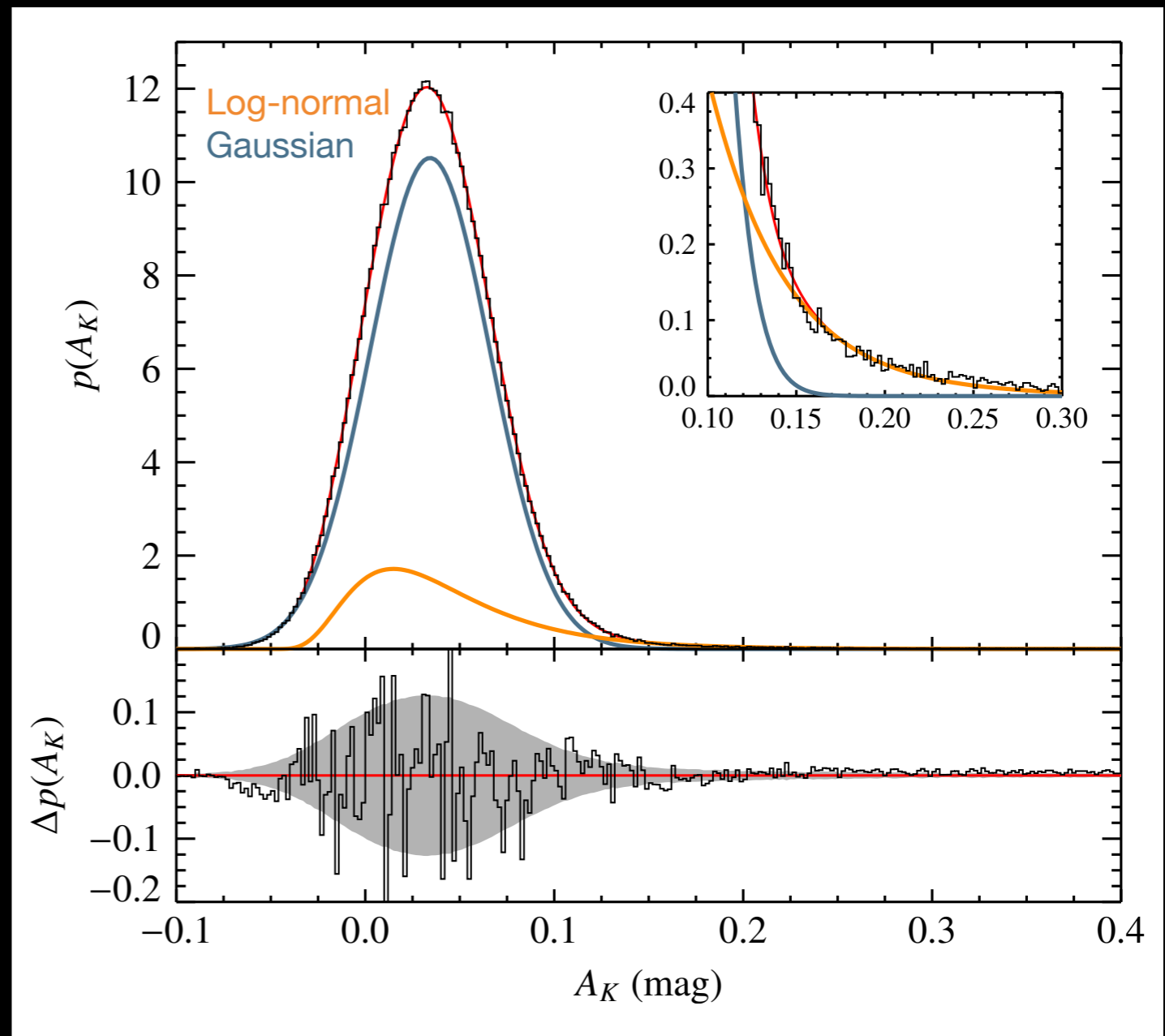
- What is the physical meaning?
 - **Gaussian**: diffuse extended region + noise
 - **Log-normal**: denser parts
- What is the role of noise?
 - Dominates at low A_K !
 - Is still present at large A_K



Residuals disappear when fitting a Gaussian + Log-normal.

Log-normals? Think it twice

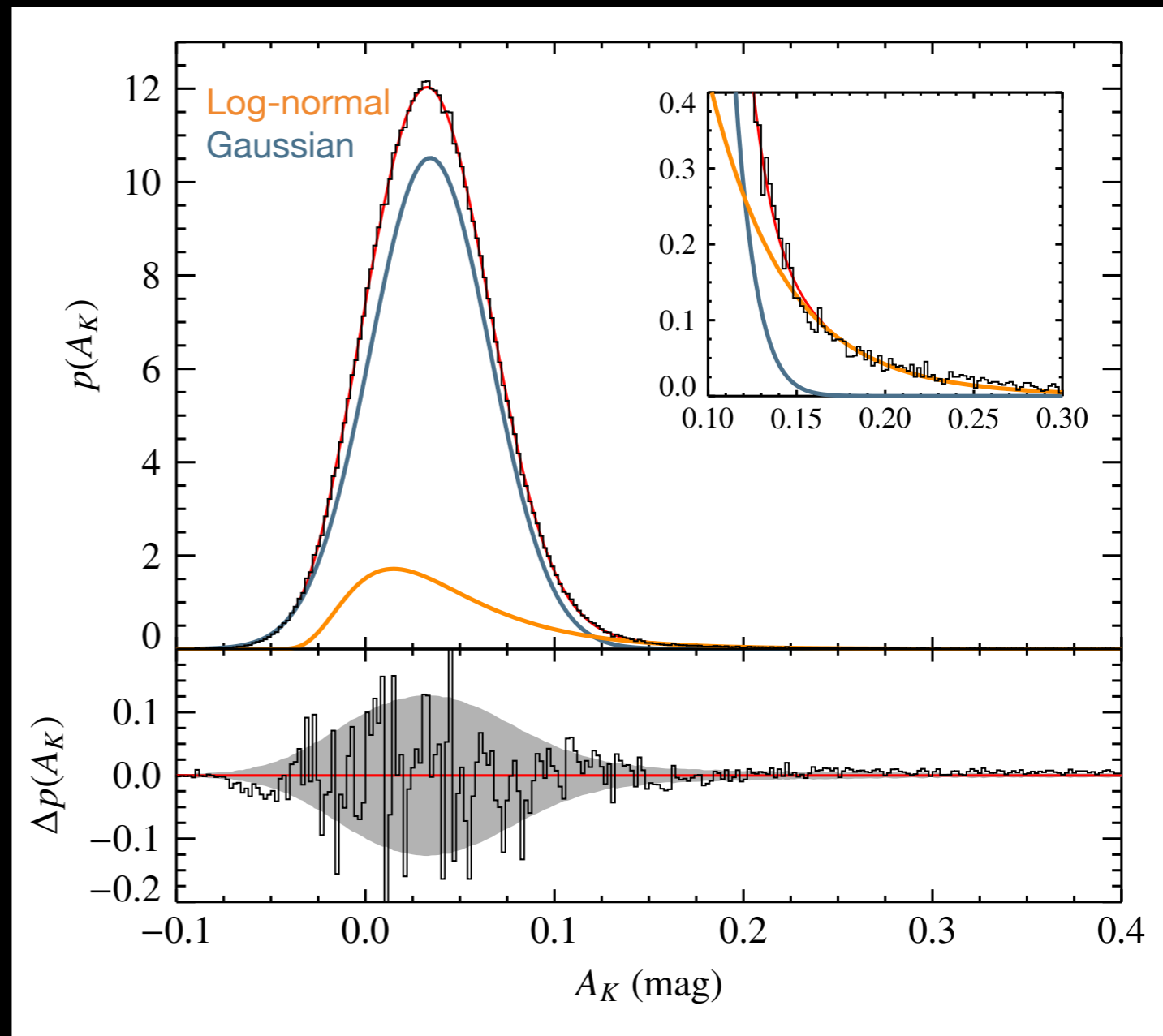
- What is the physical meaning?
 - **Gaussian**: diffuse extended region + noise
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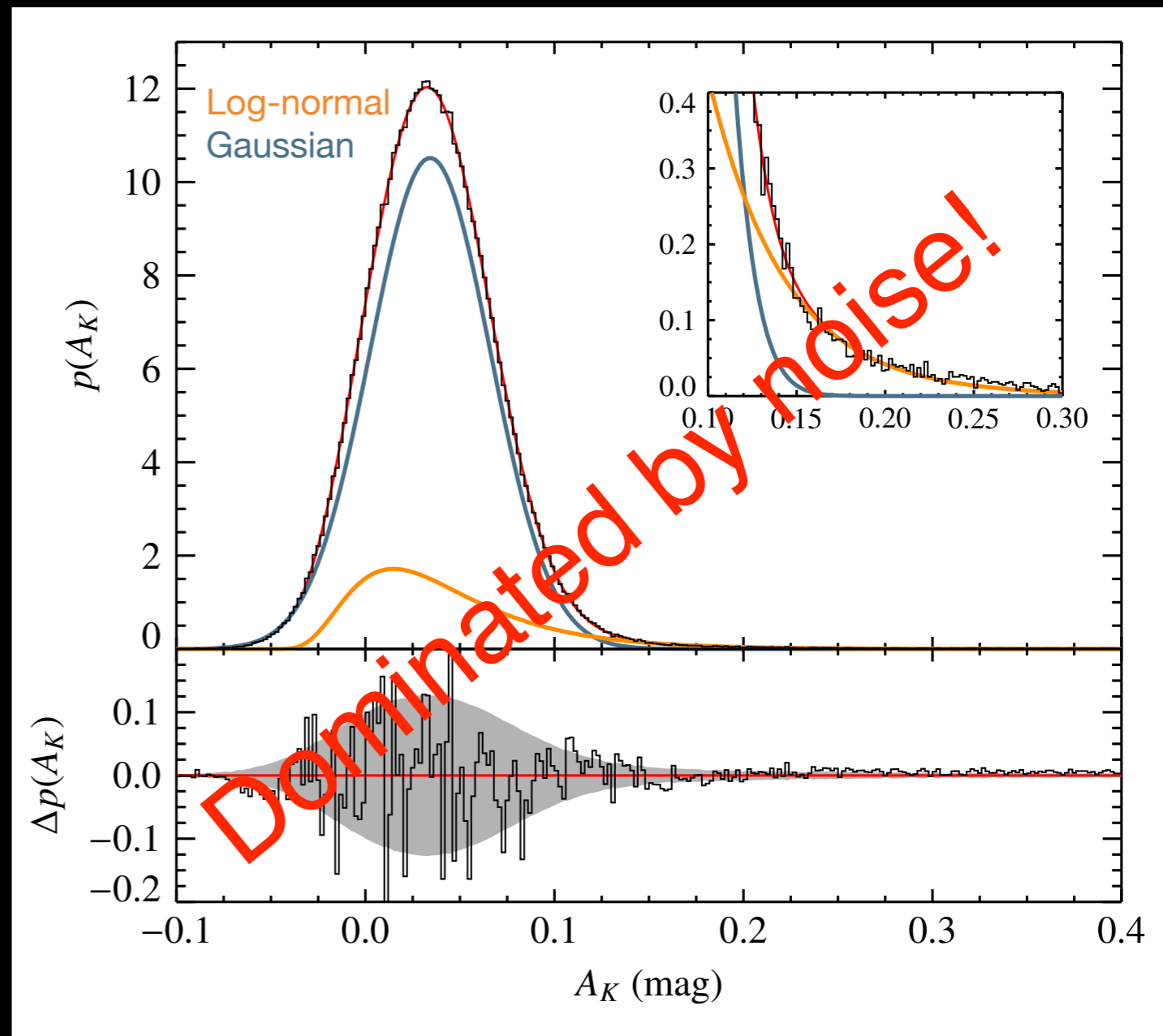
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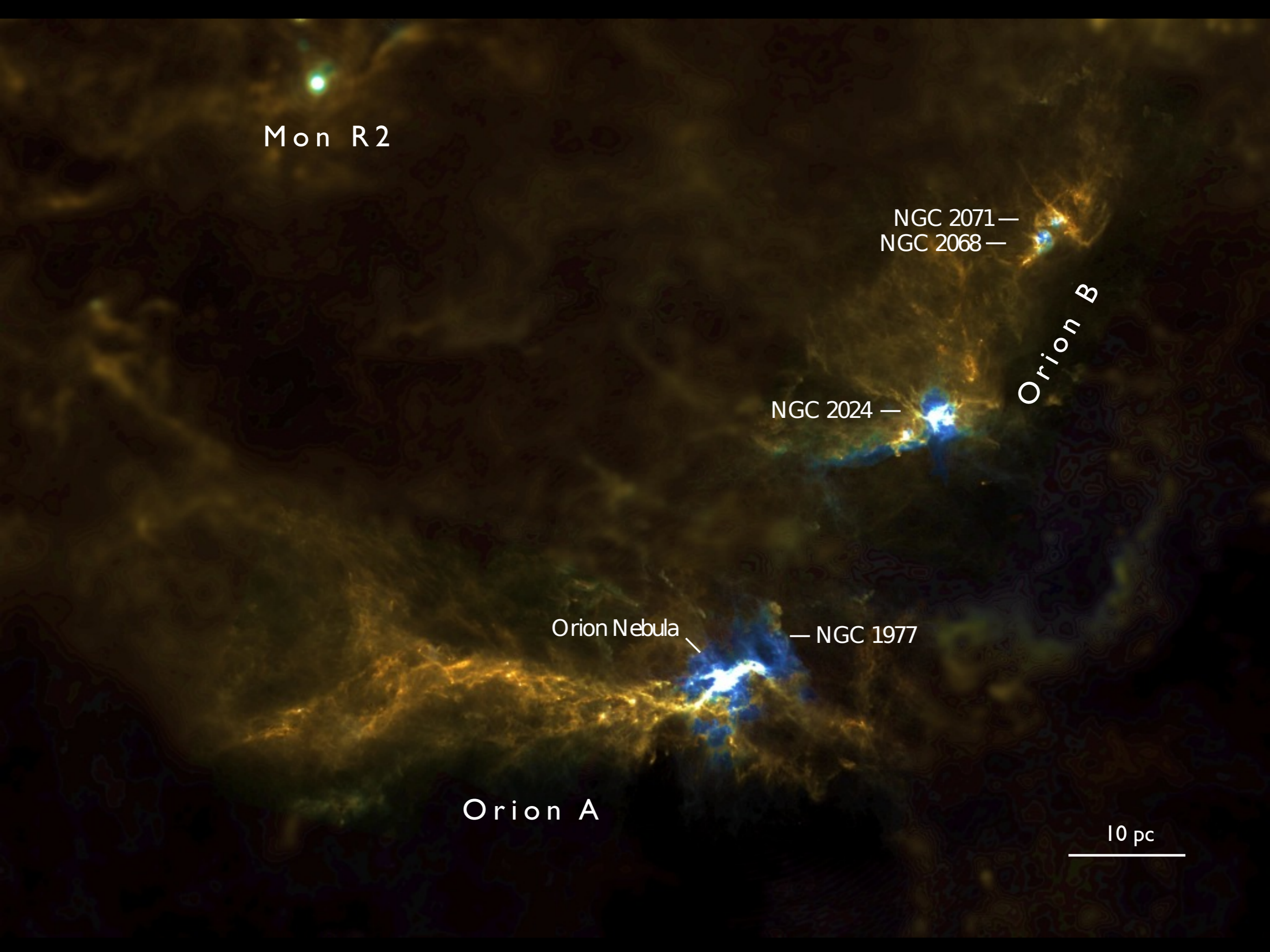
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Residuals disappear when fitting a Gaussian + Log-normal.

We need high-resolution, low-noise density
maps of molecular clouds

i.e., Herschel data...



Mon R2

NGC 2071 —
NGC 2068 —

Orion B

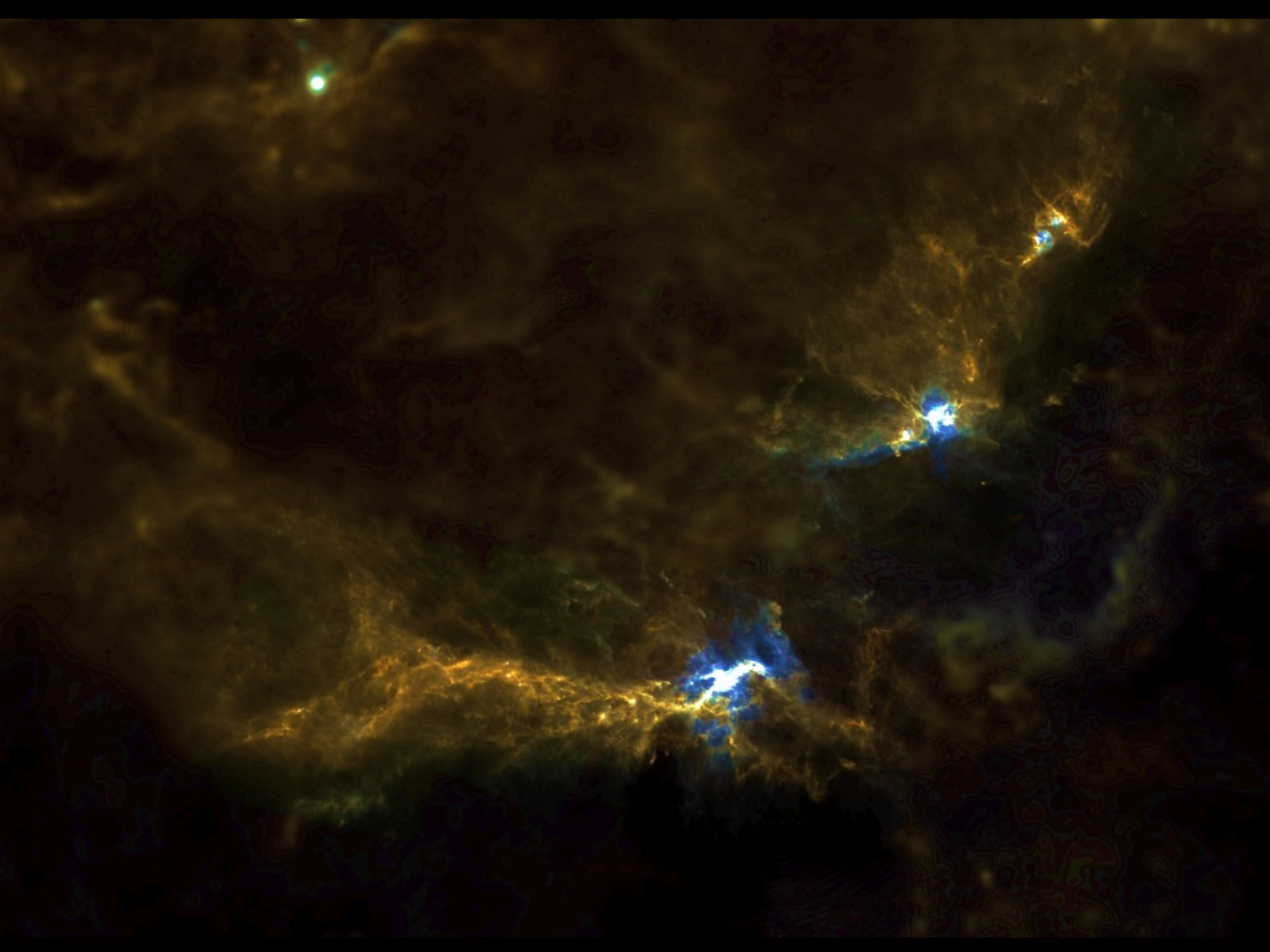
NGC 2024 —

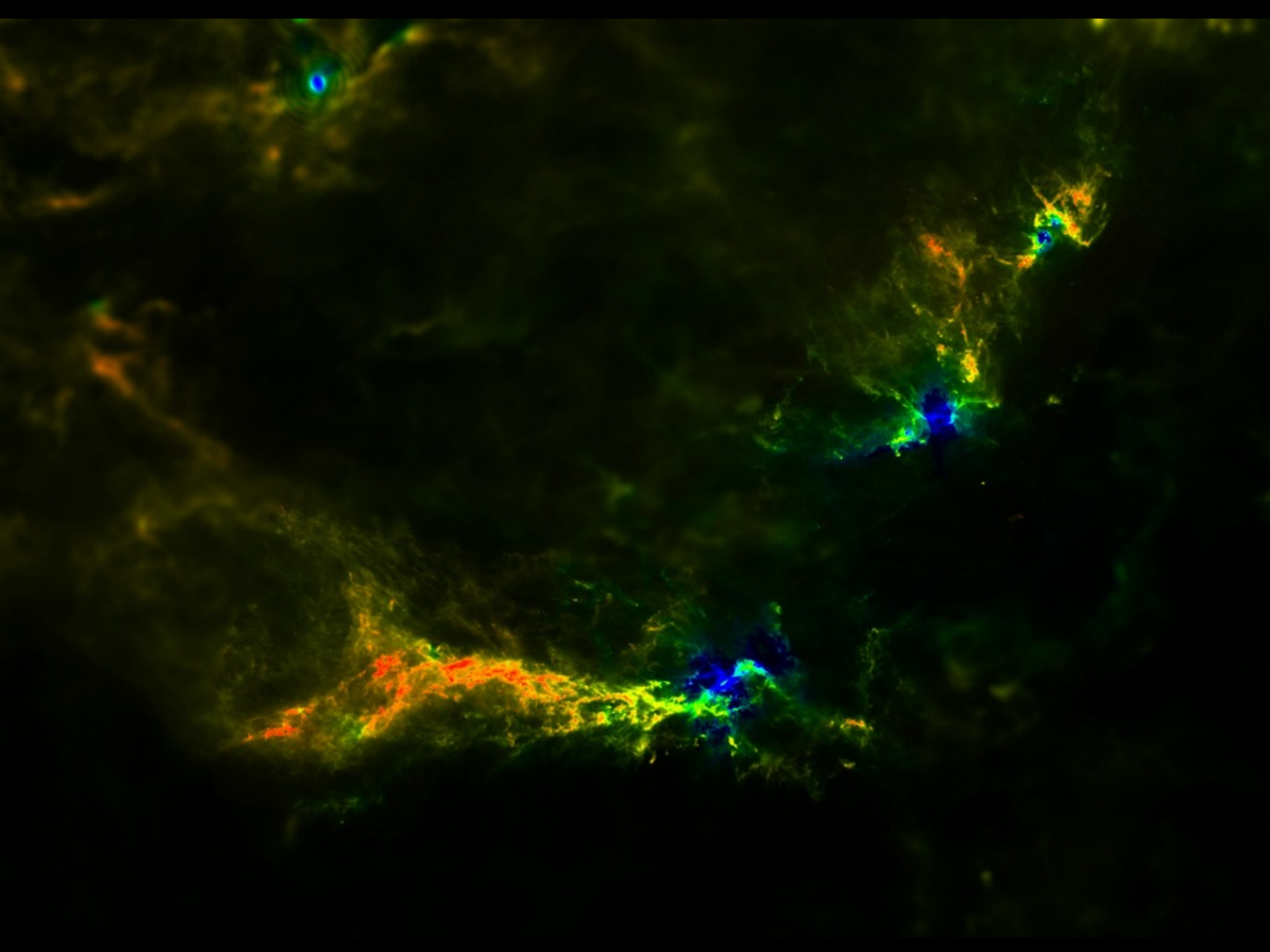
Orion Nebula —

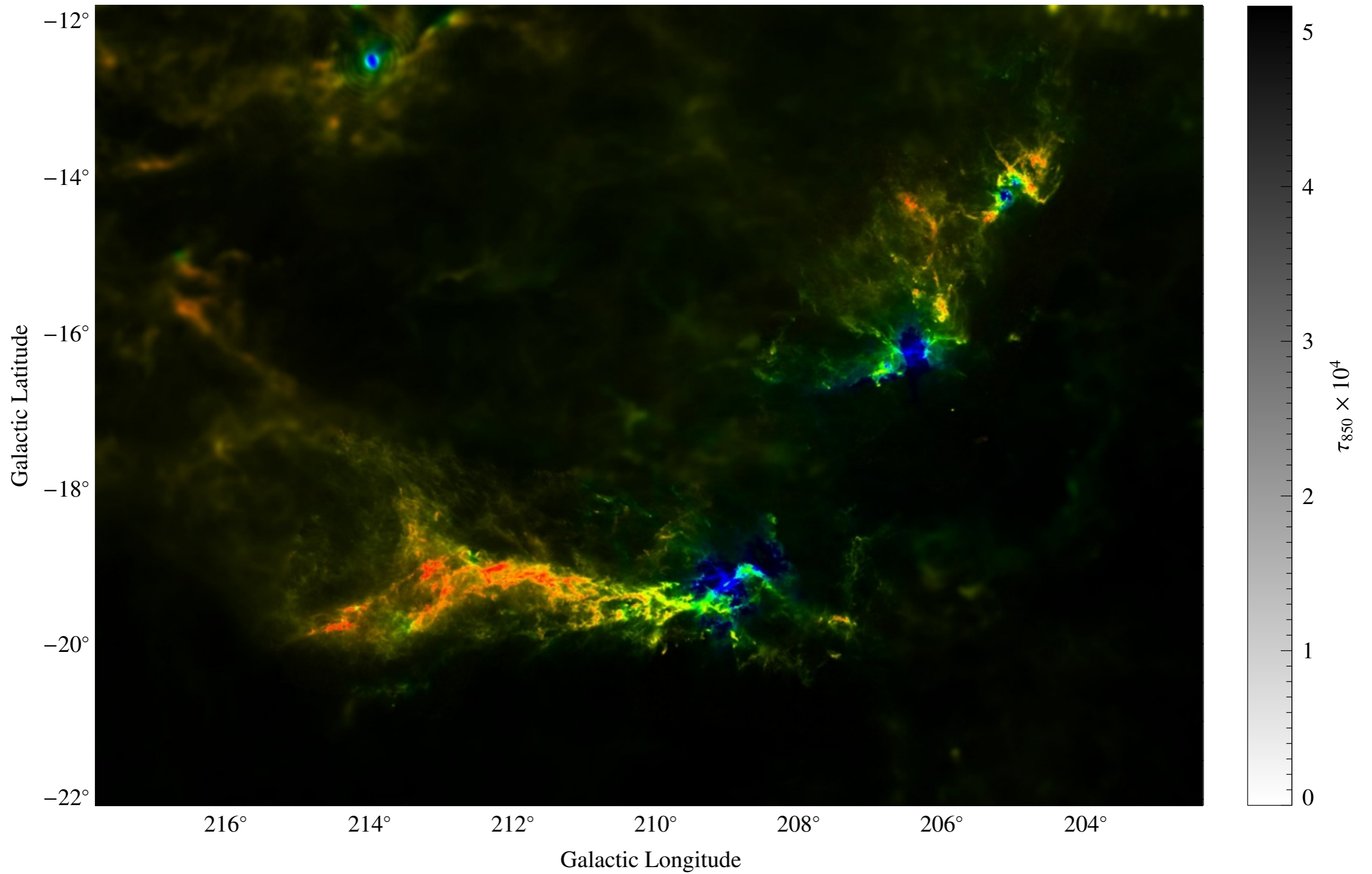
— NGC 1977

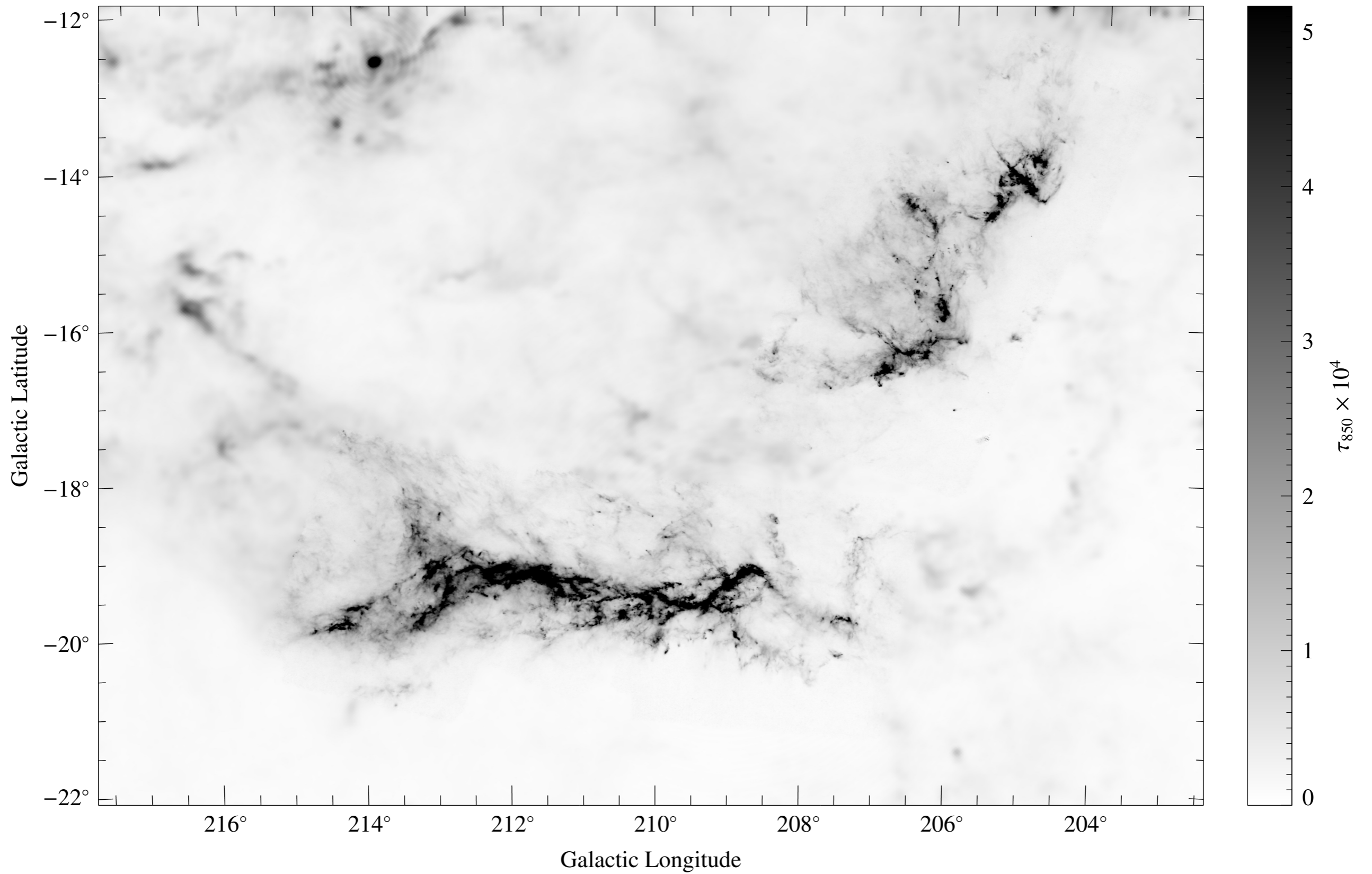
Orion A

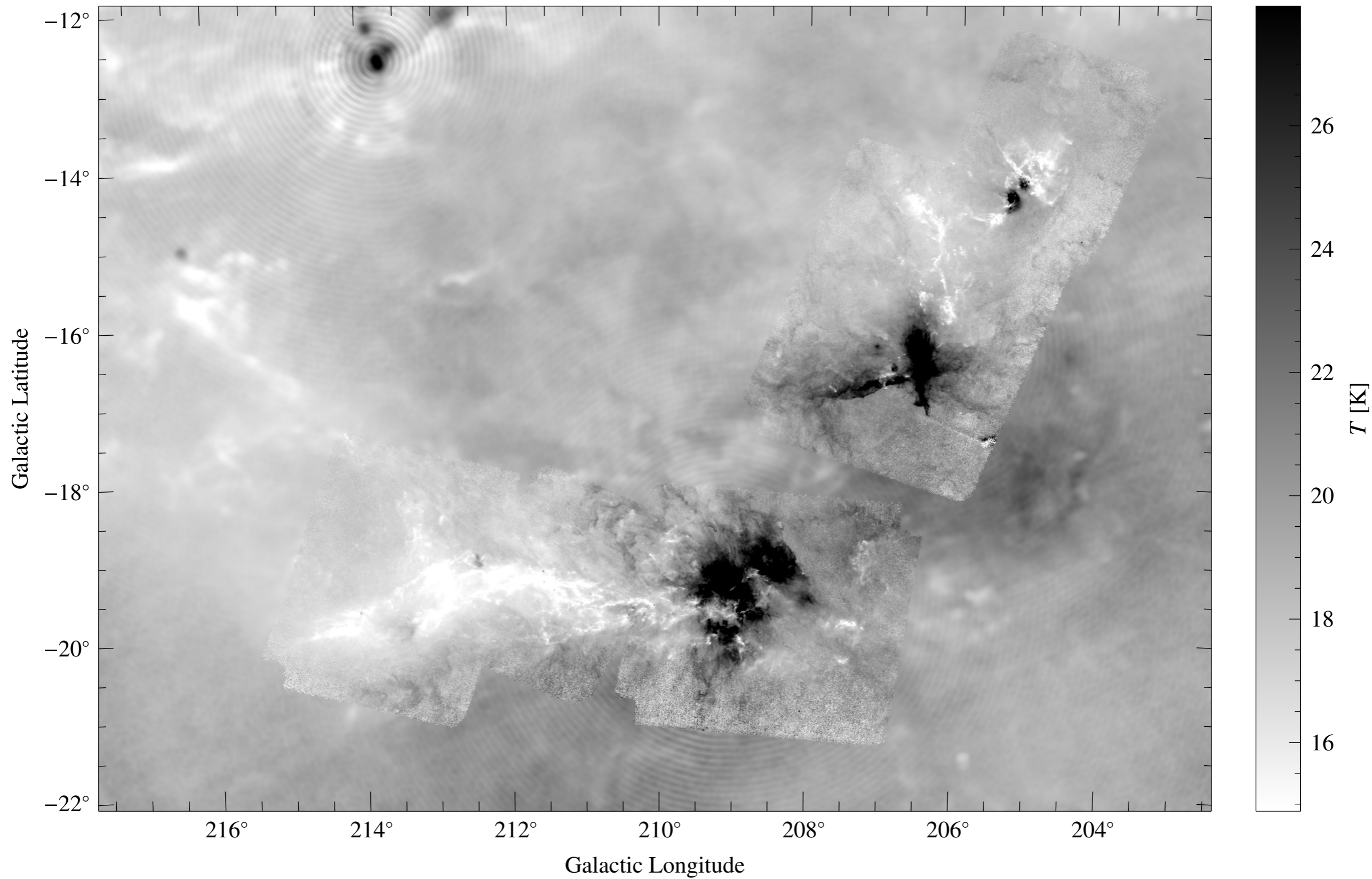
10 pc



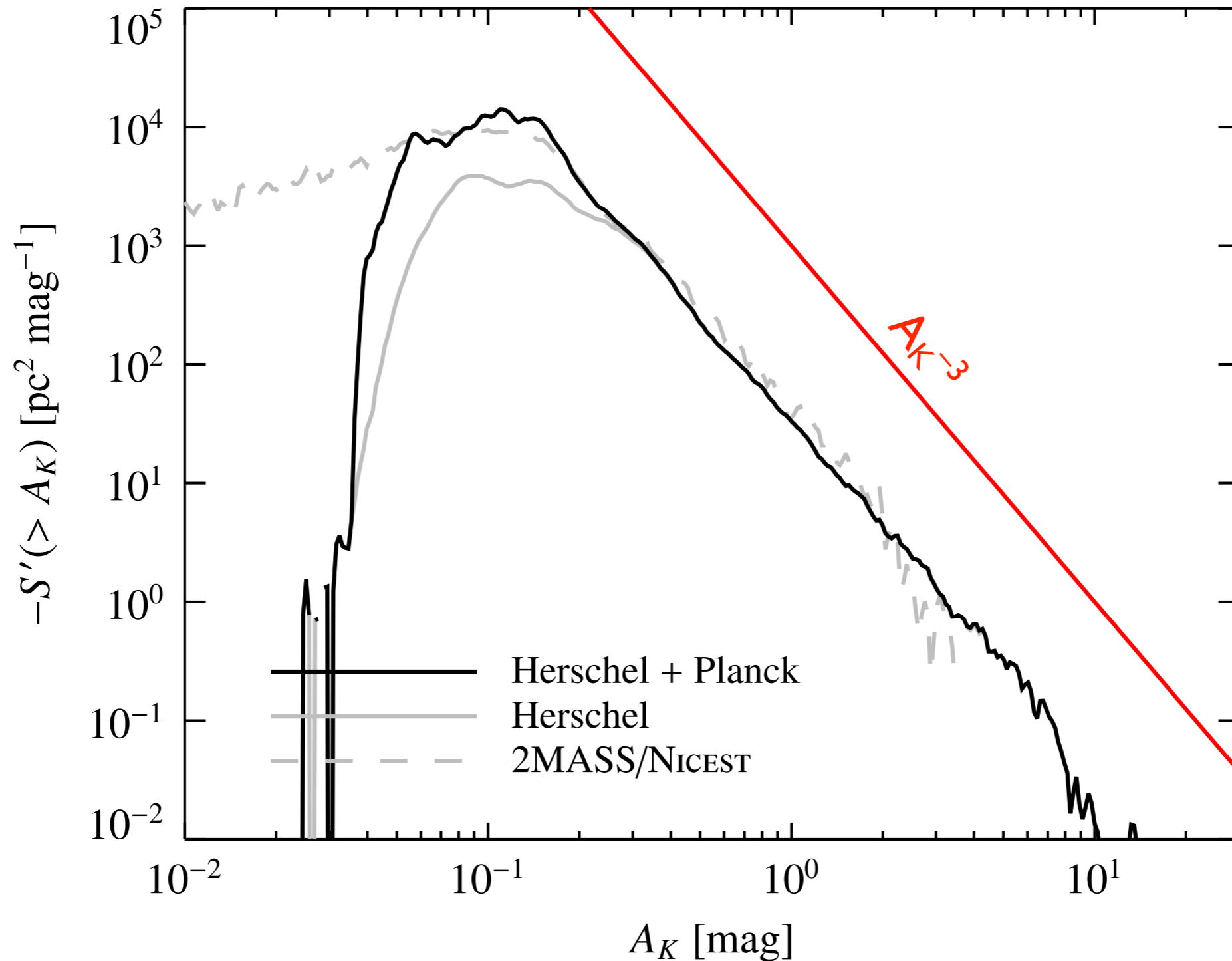








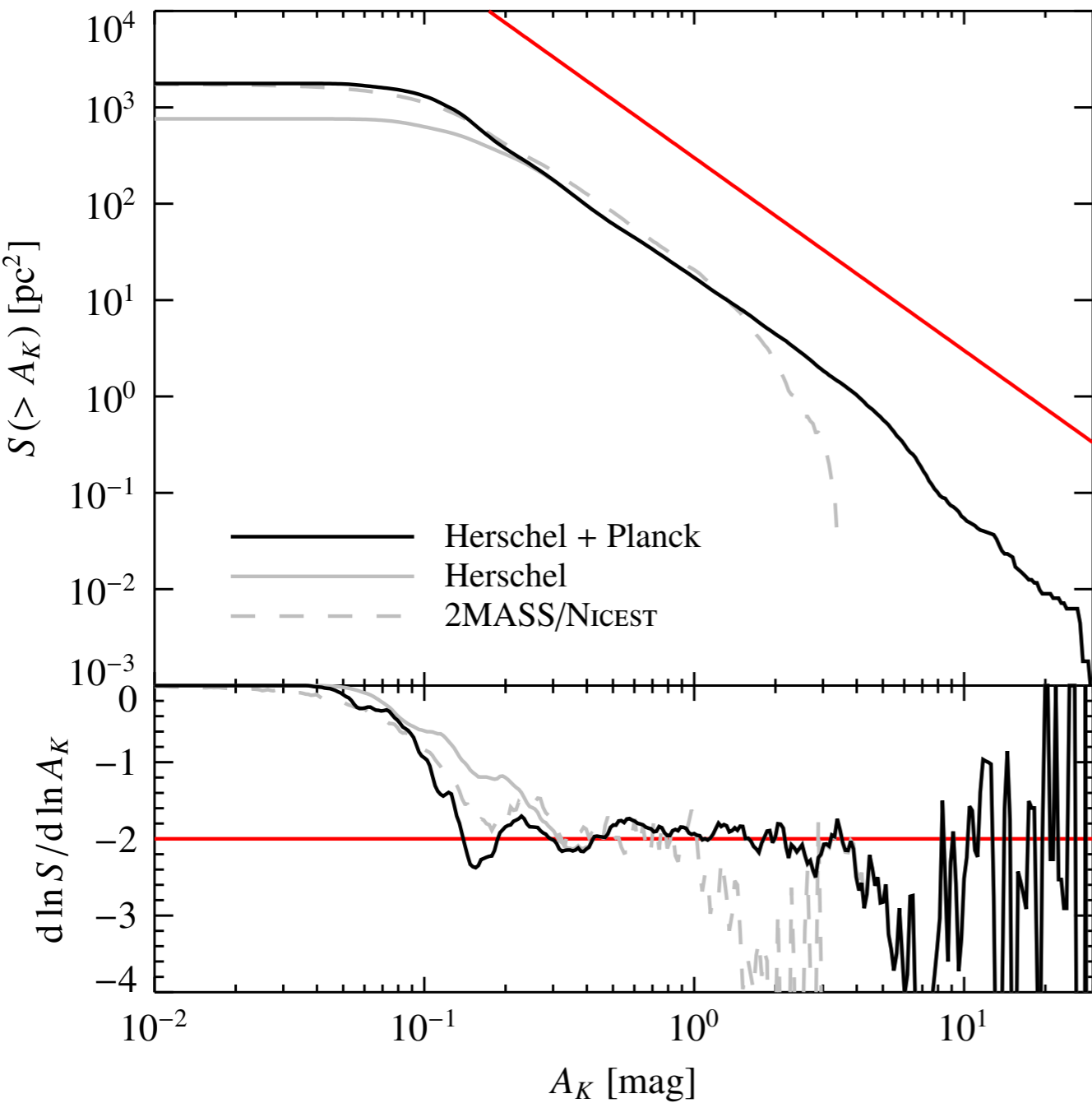
Herschel PDF for Orion B



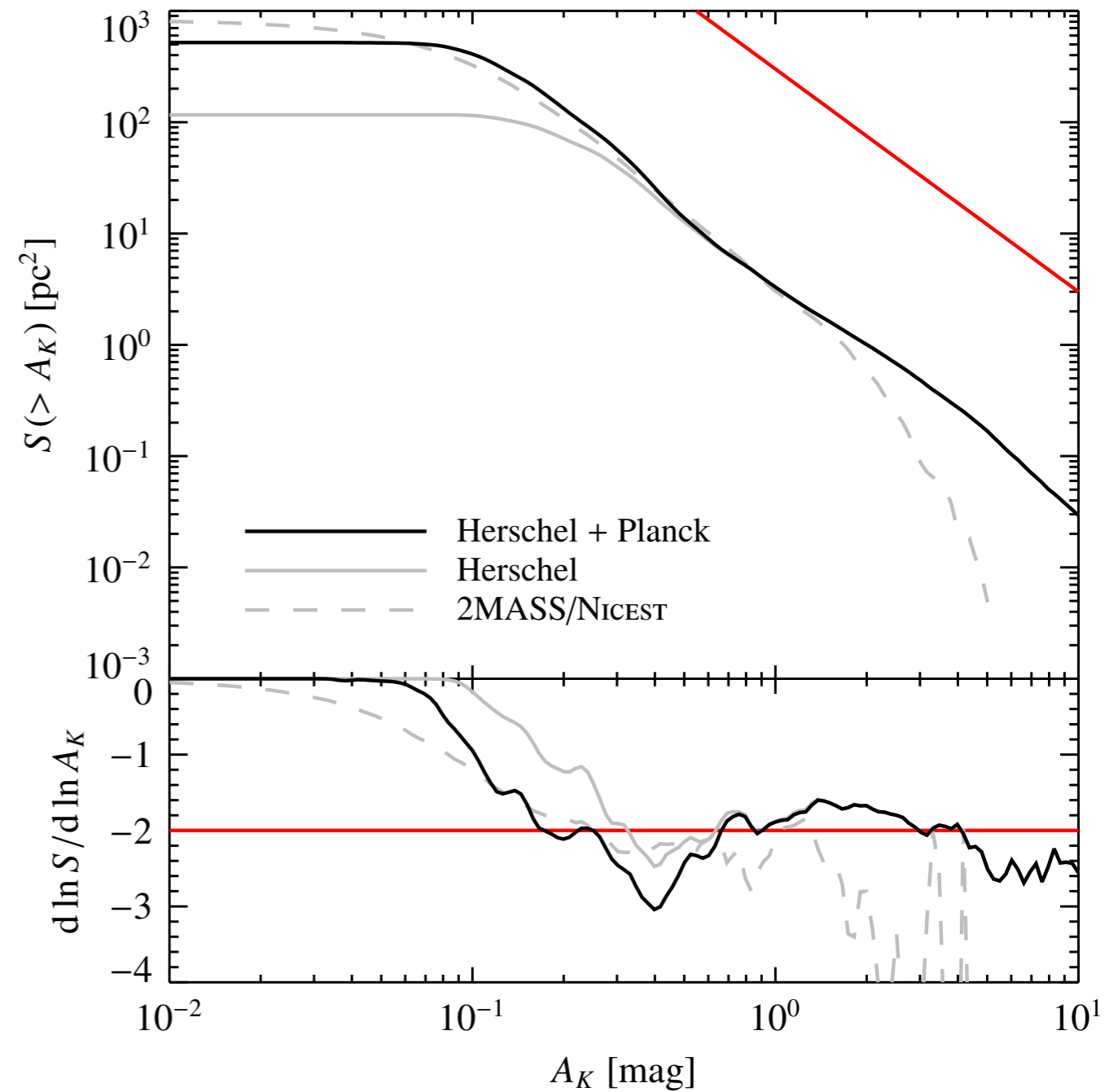
Fact 5

Scaling laws play a
fundamental role in SF

Area functions (integrals of PDFs)

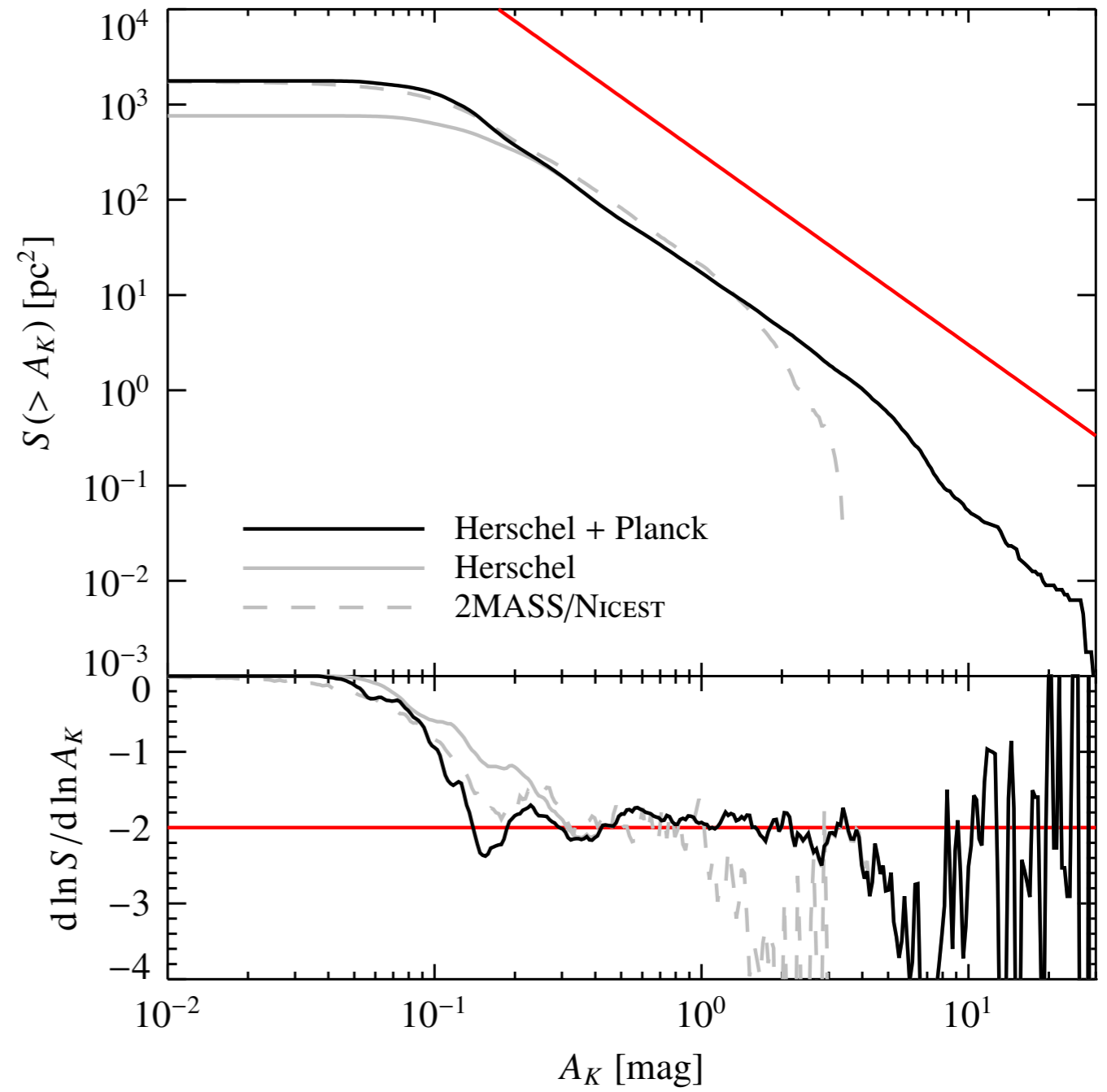


Lombardi et al. (2014)



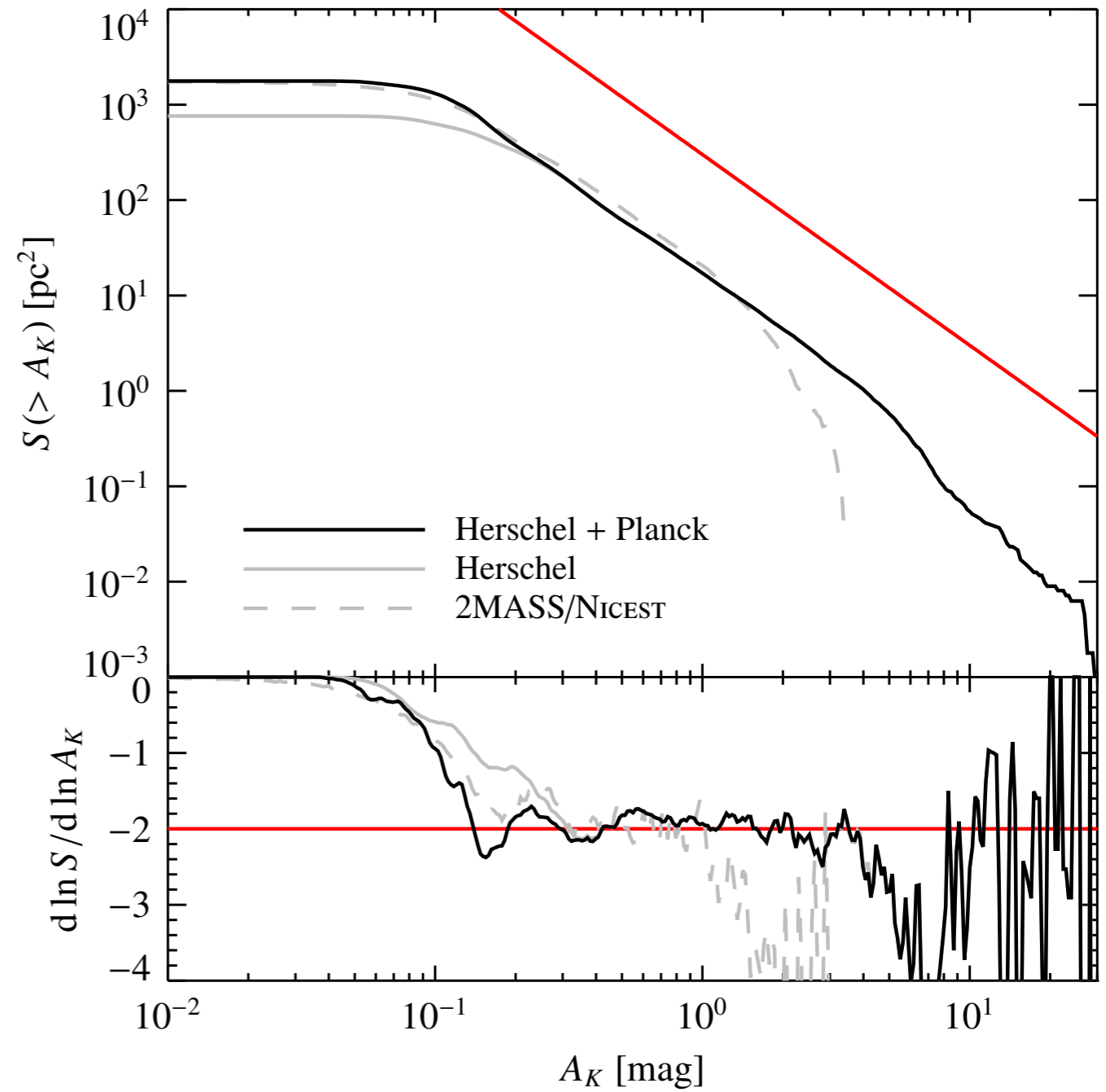
Alves et al. (2014)

Toy model



Toy model

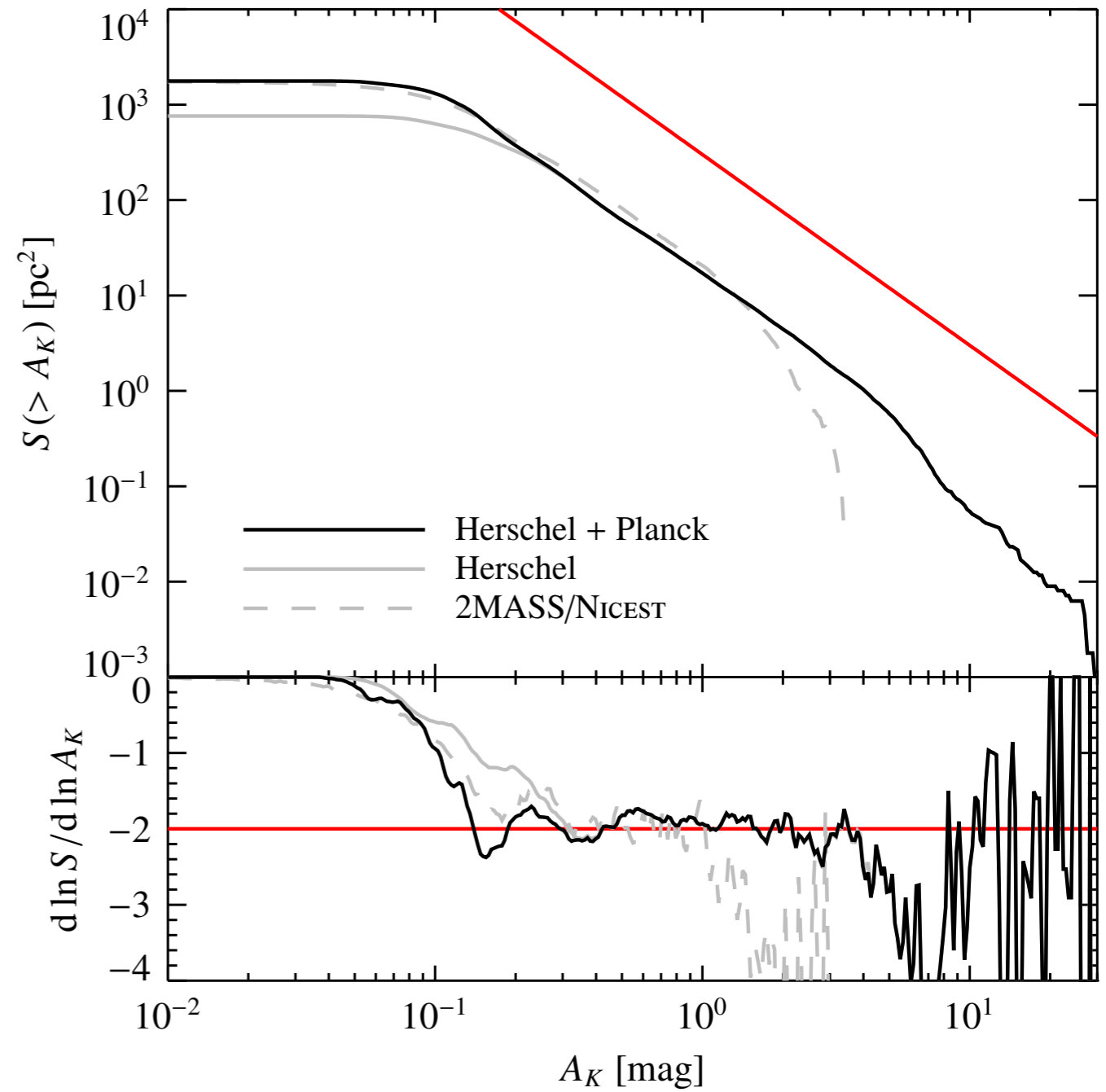
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Toy model

Consider an isothermal sphere:

$$\rho \sim R^{-2}$$

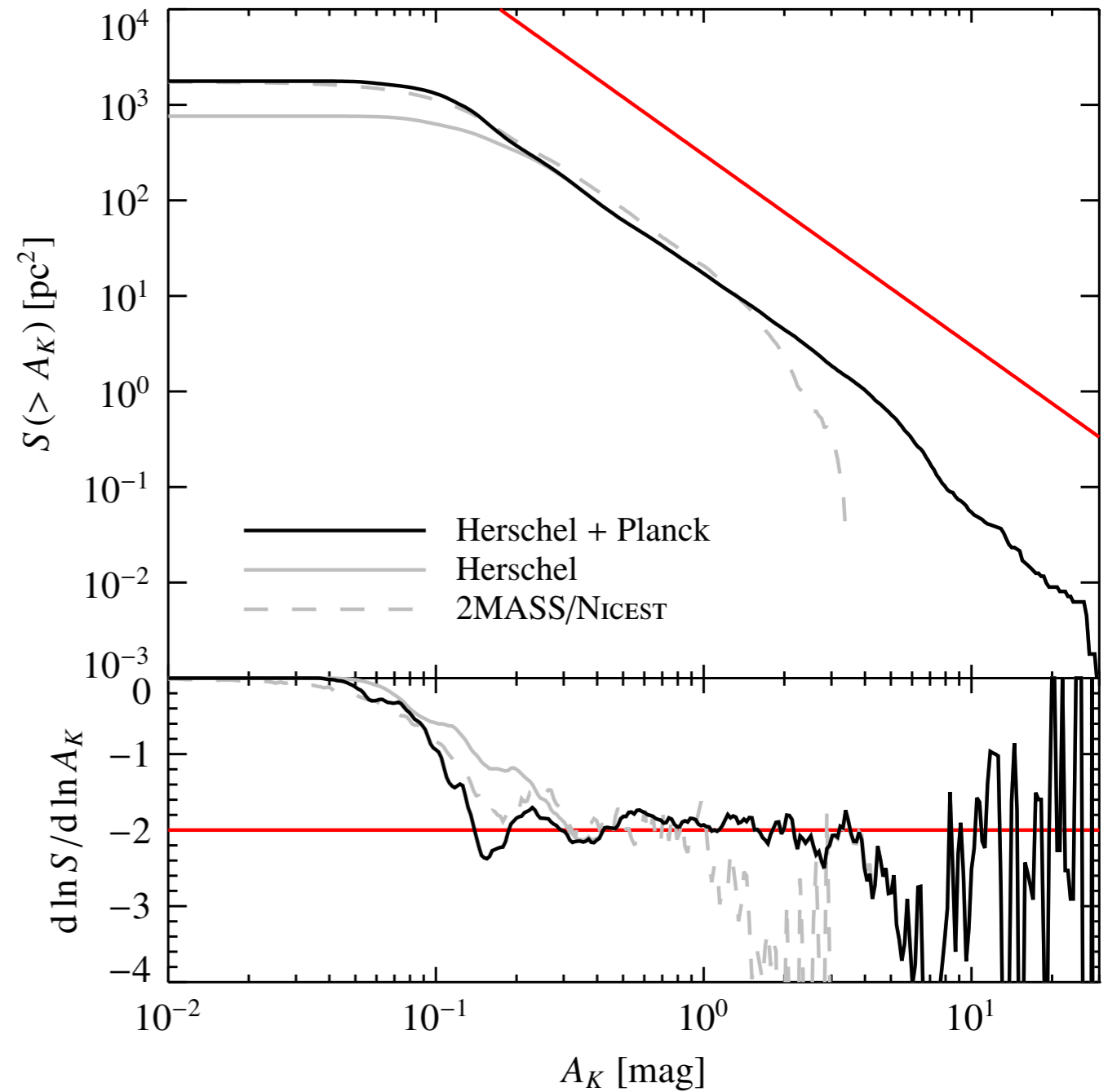


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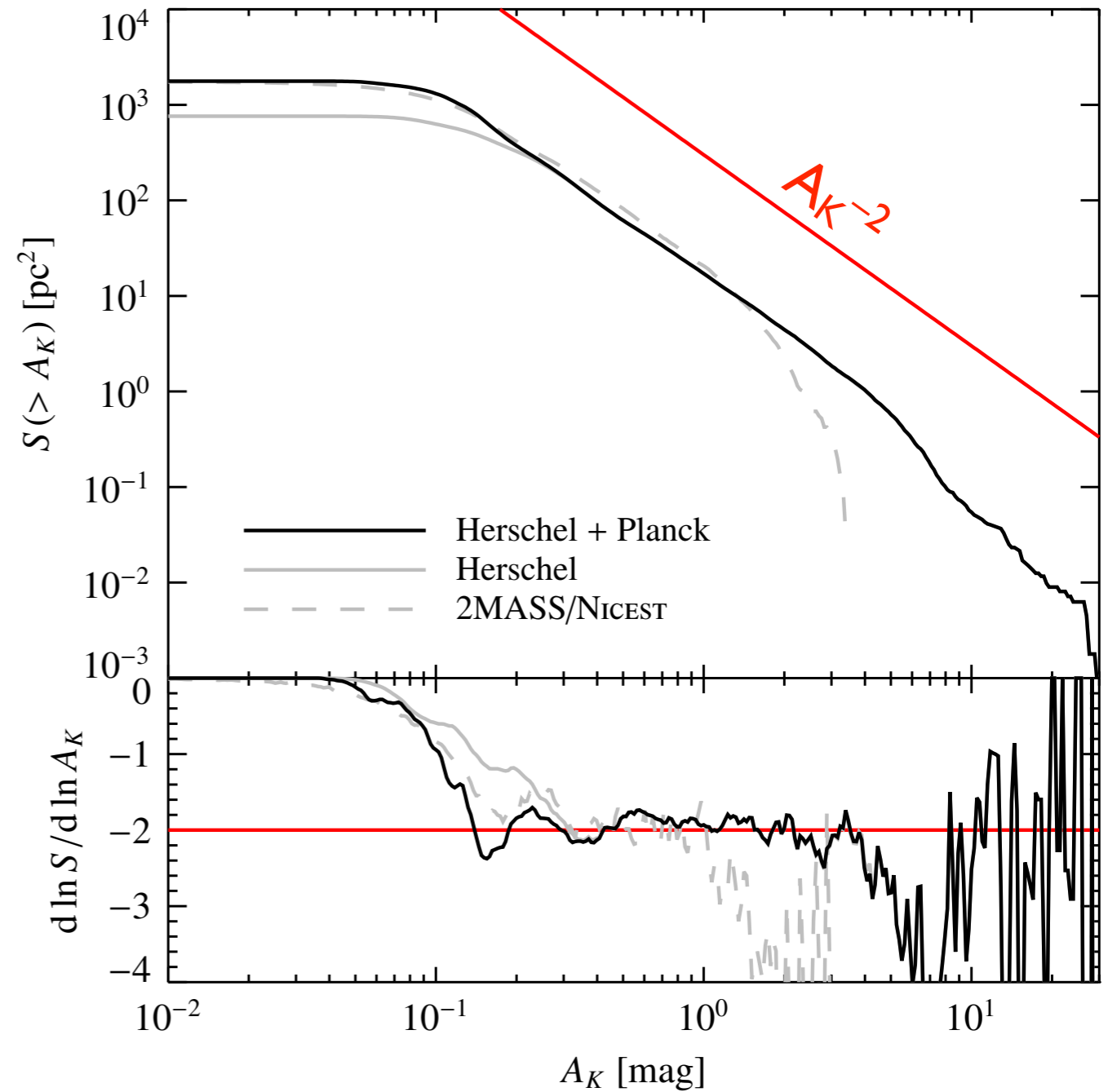
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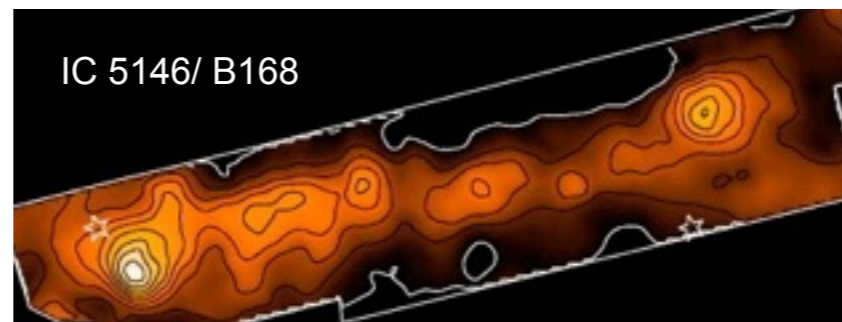
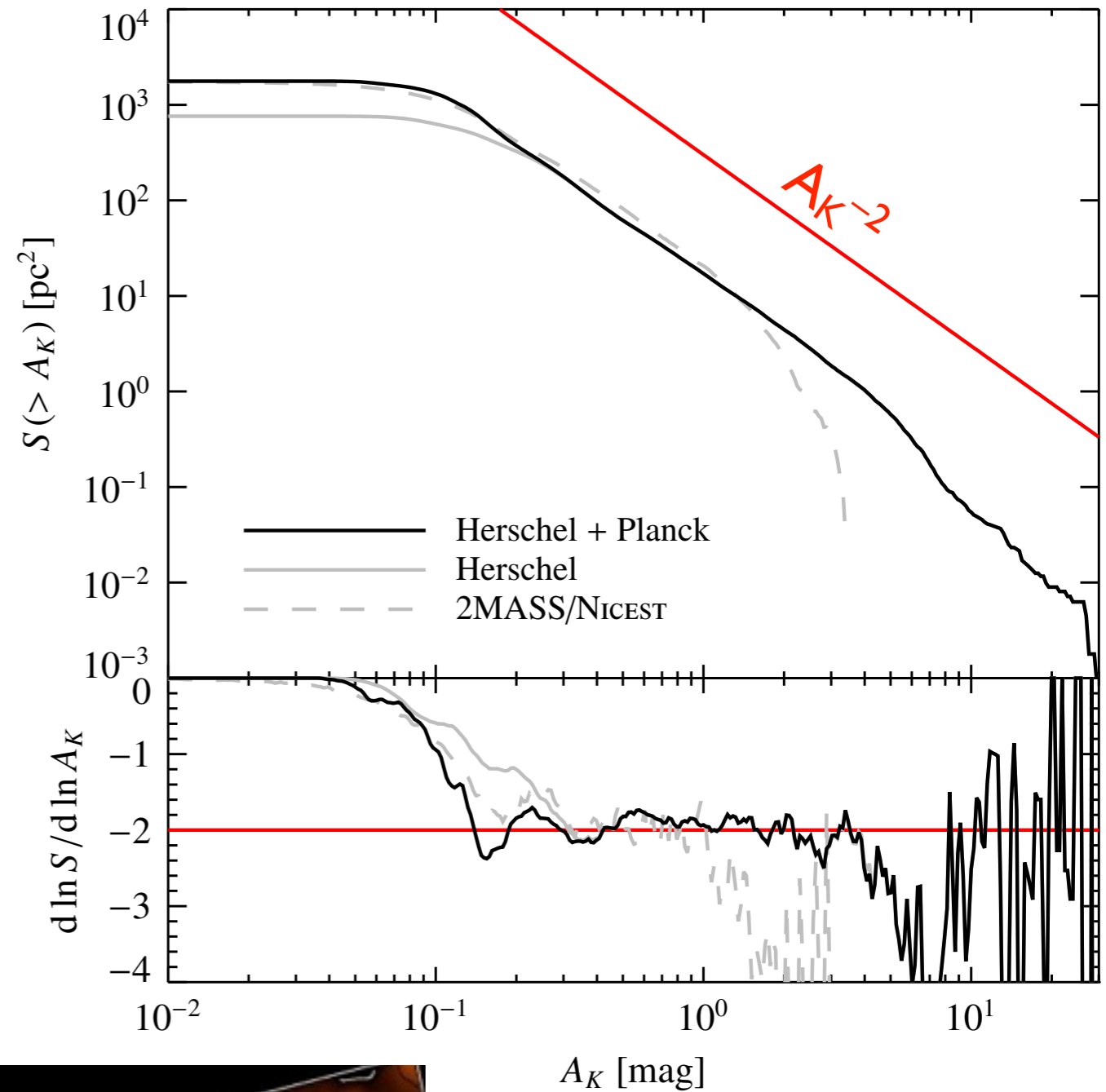
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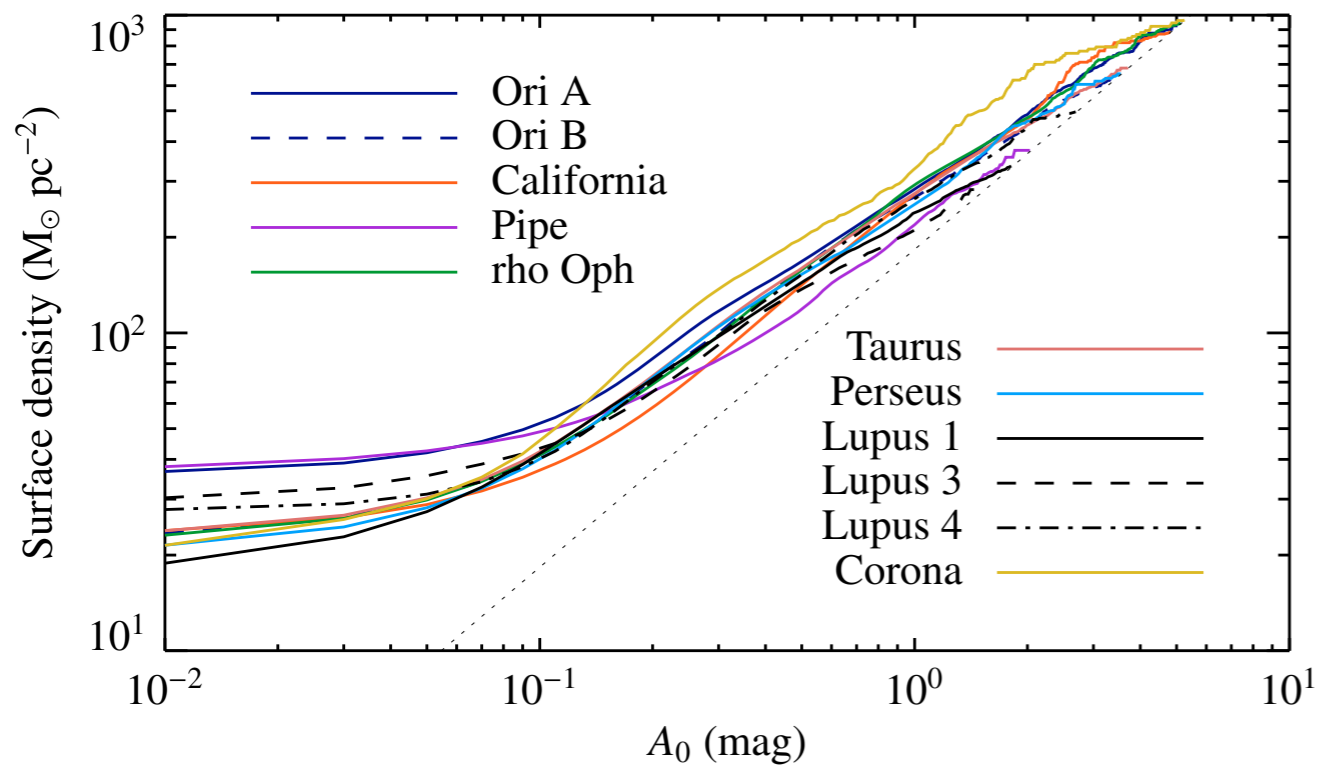
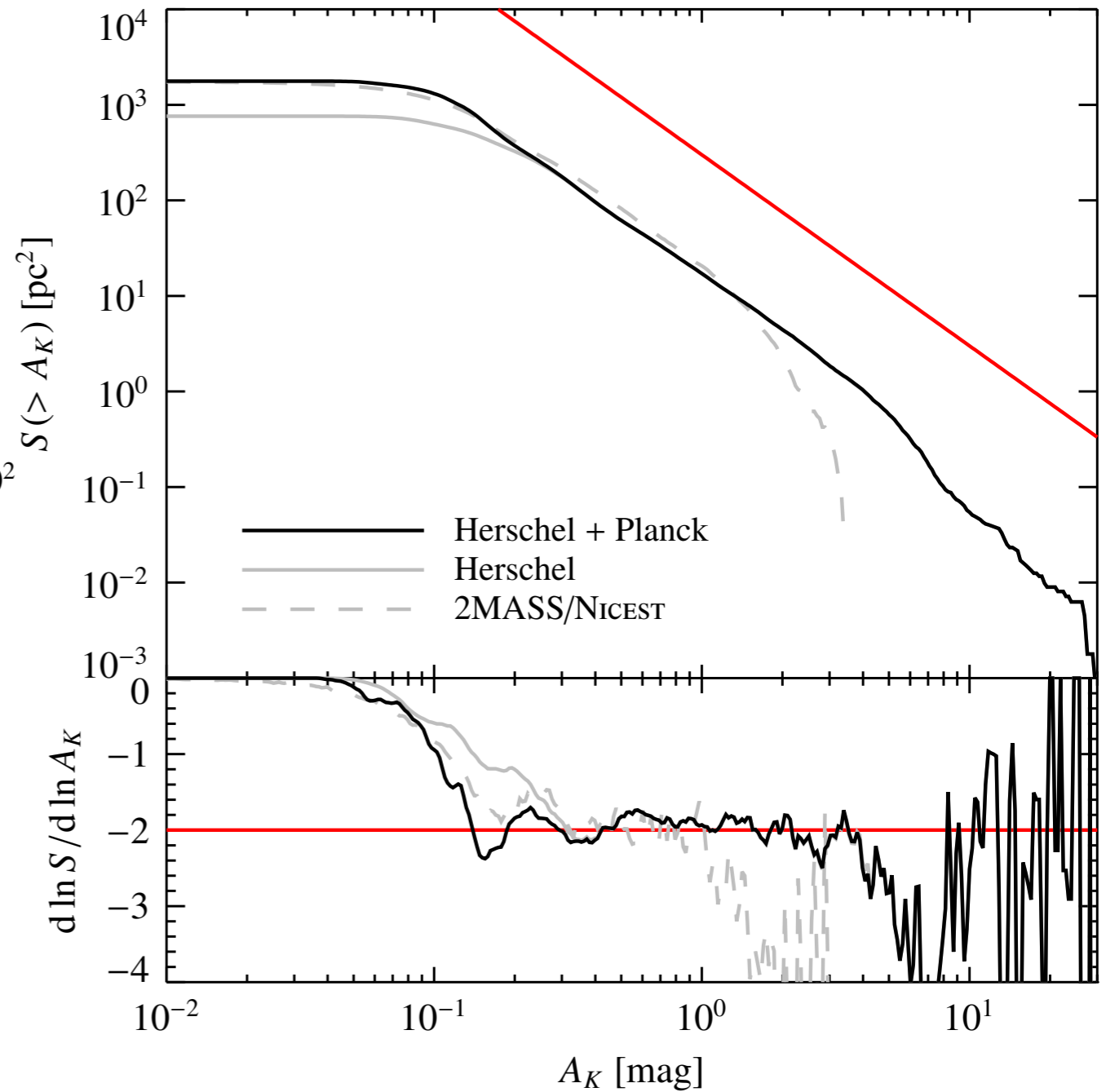
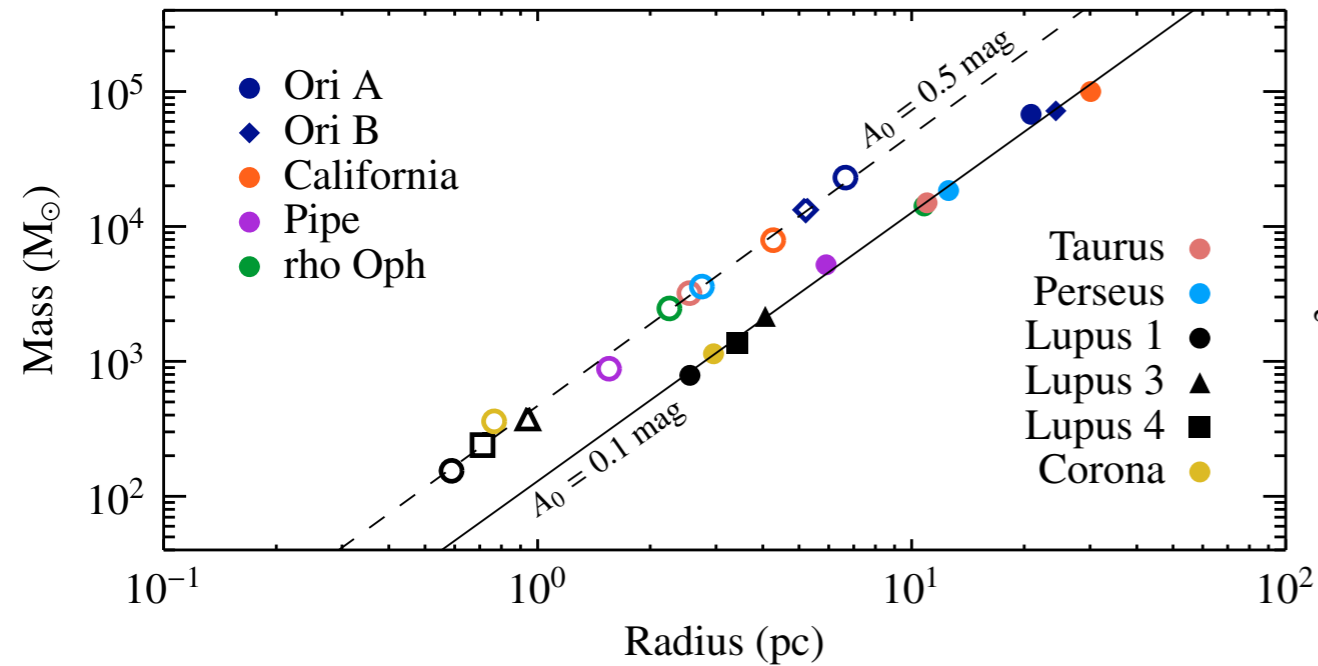
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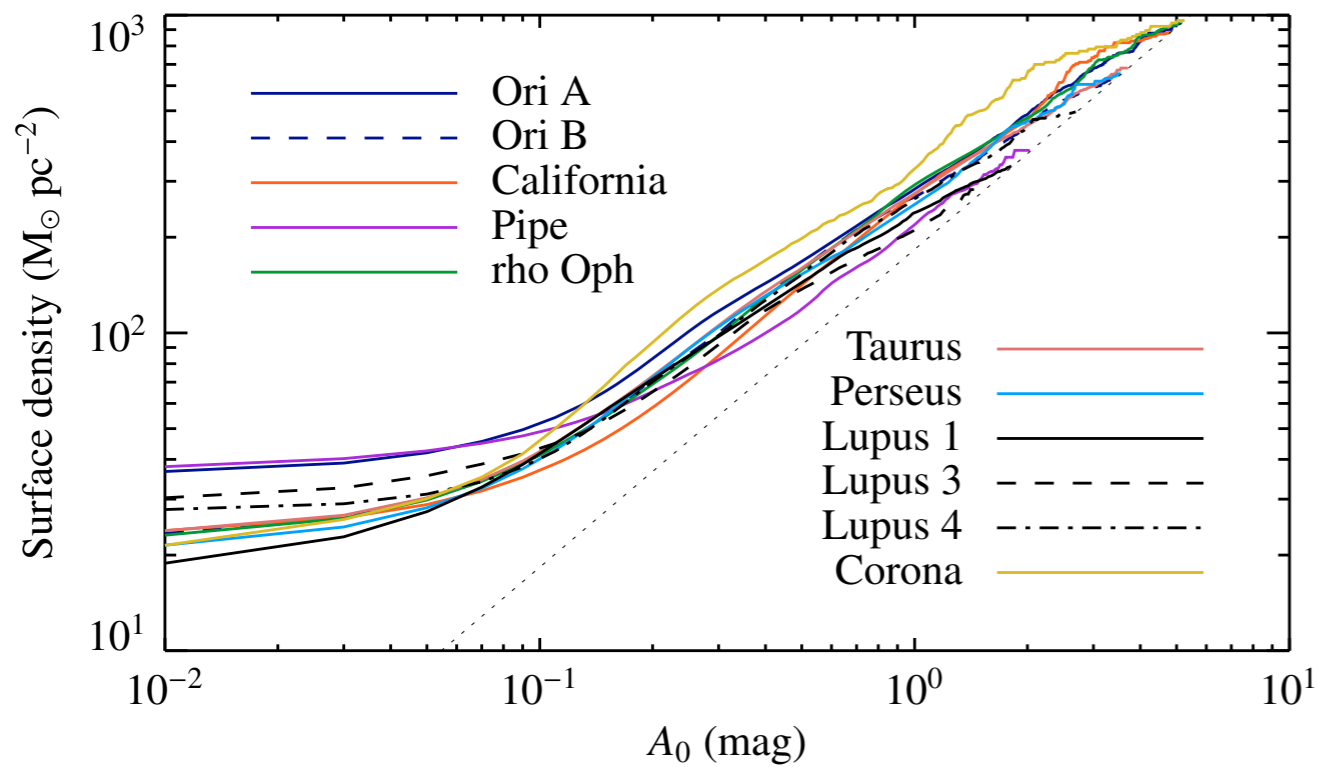
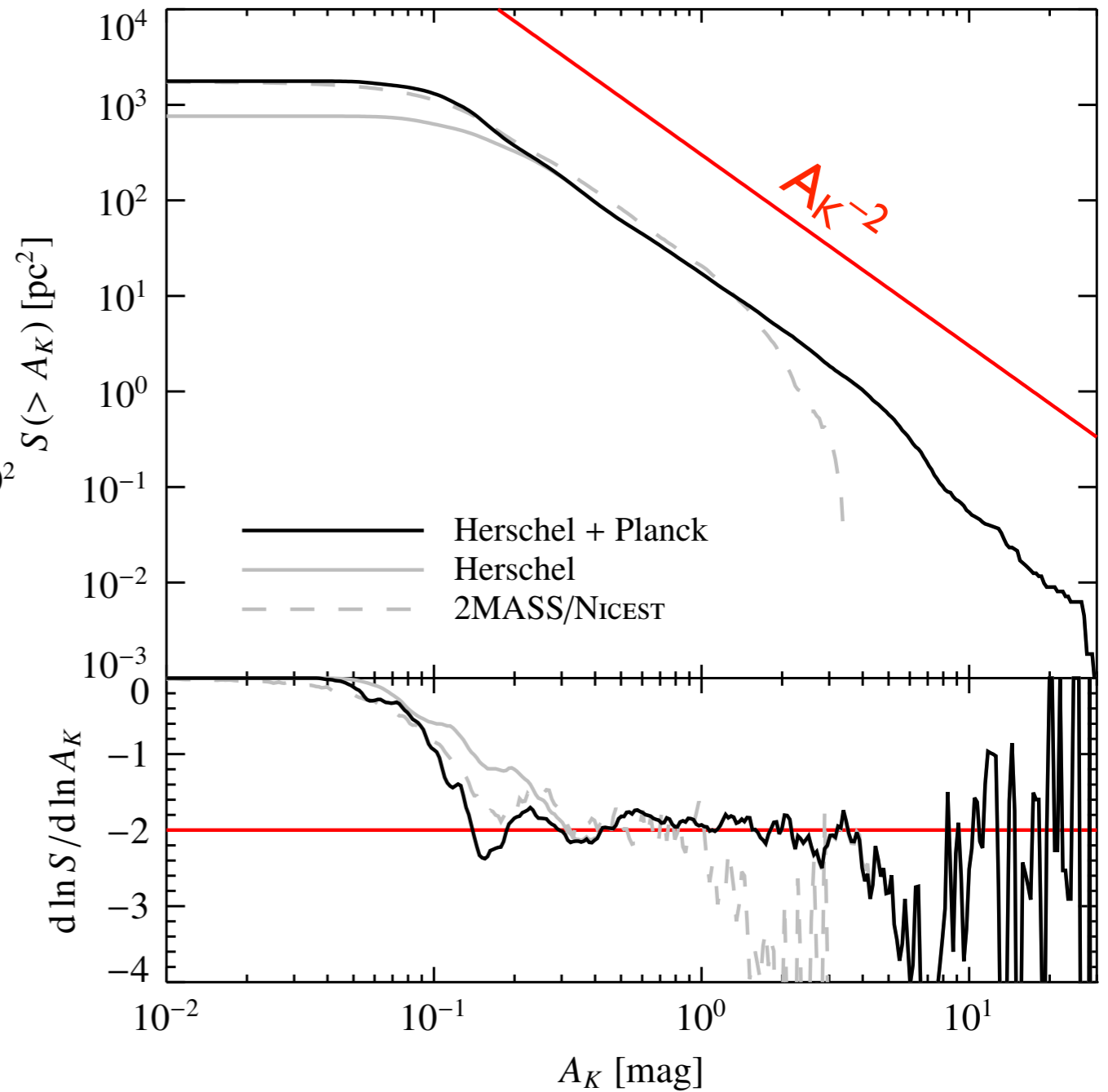
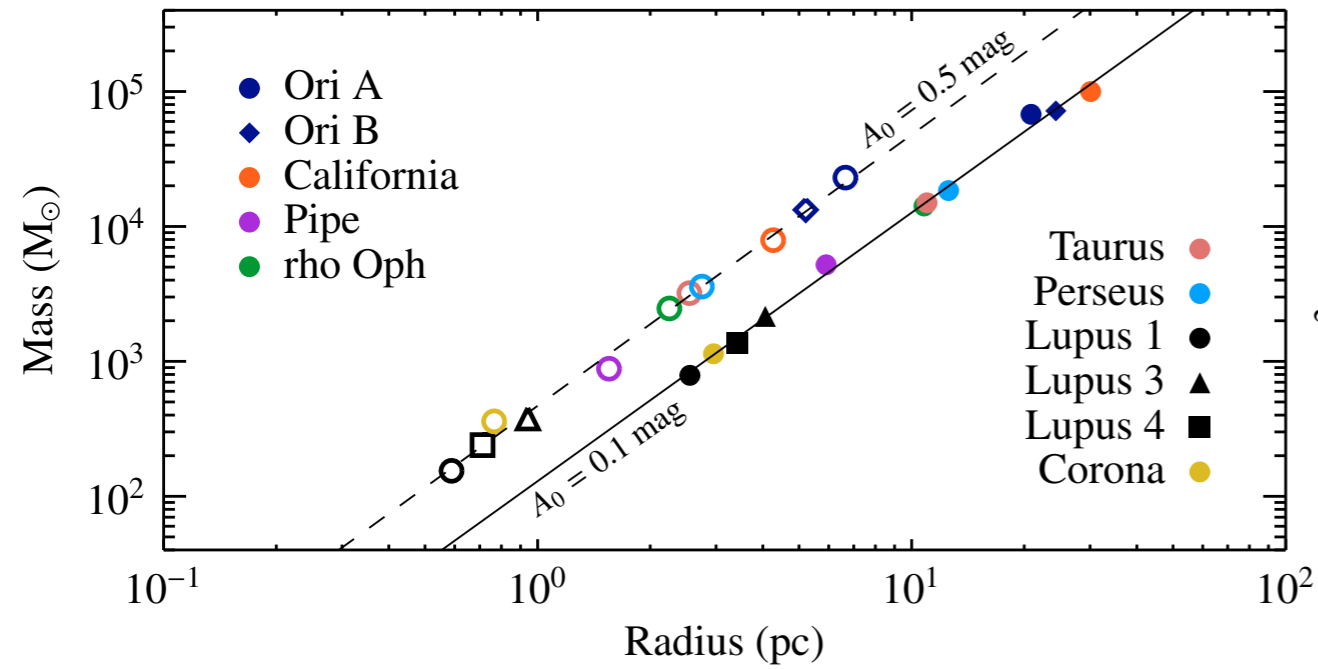


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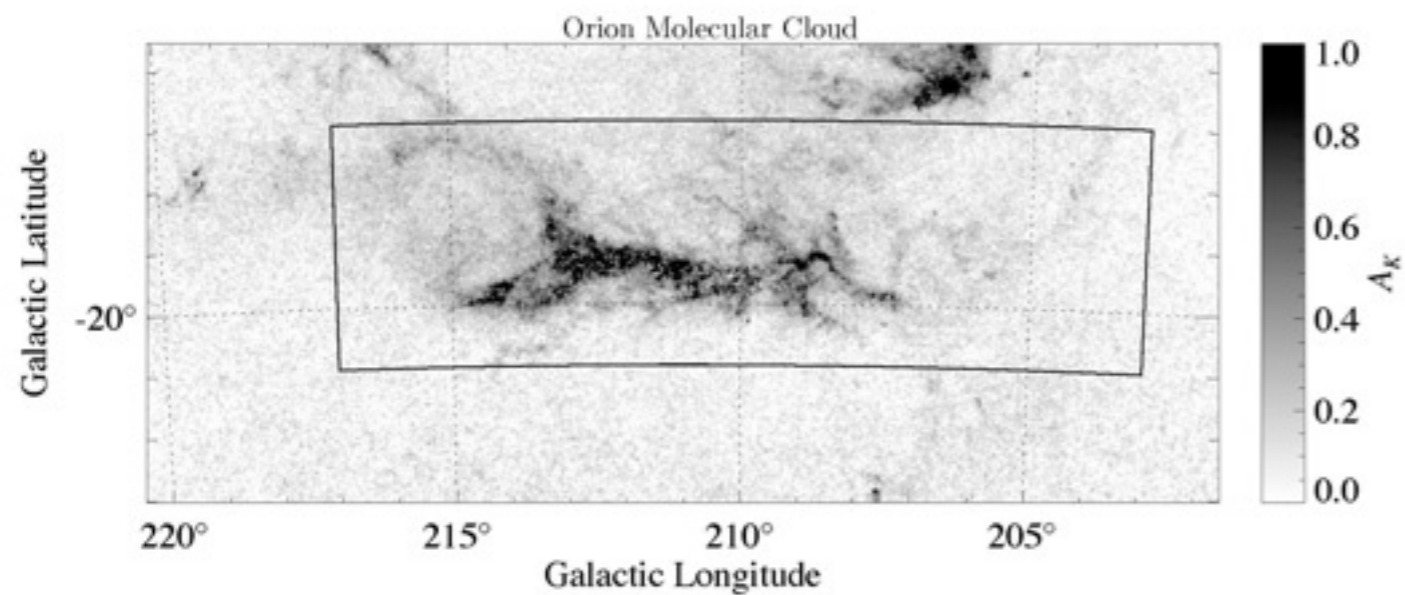
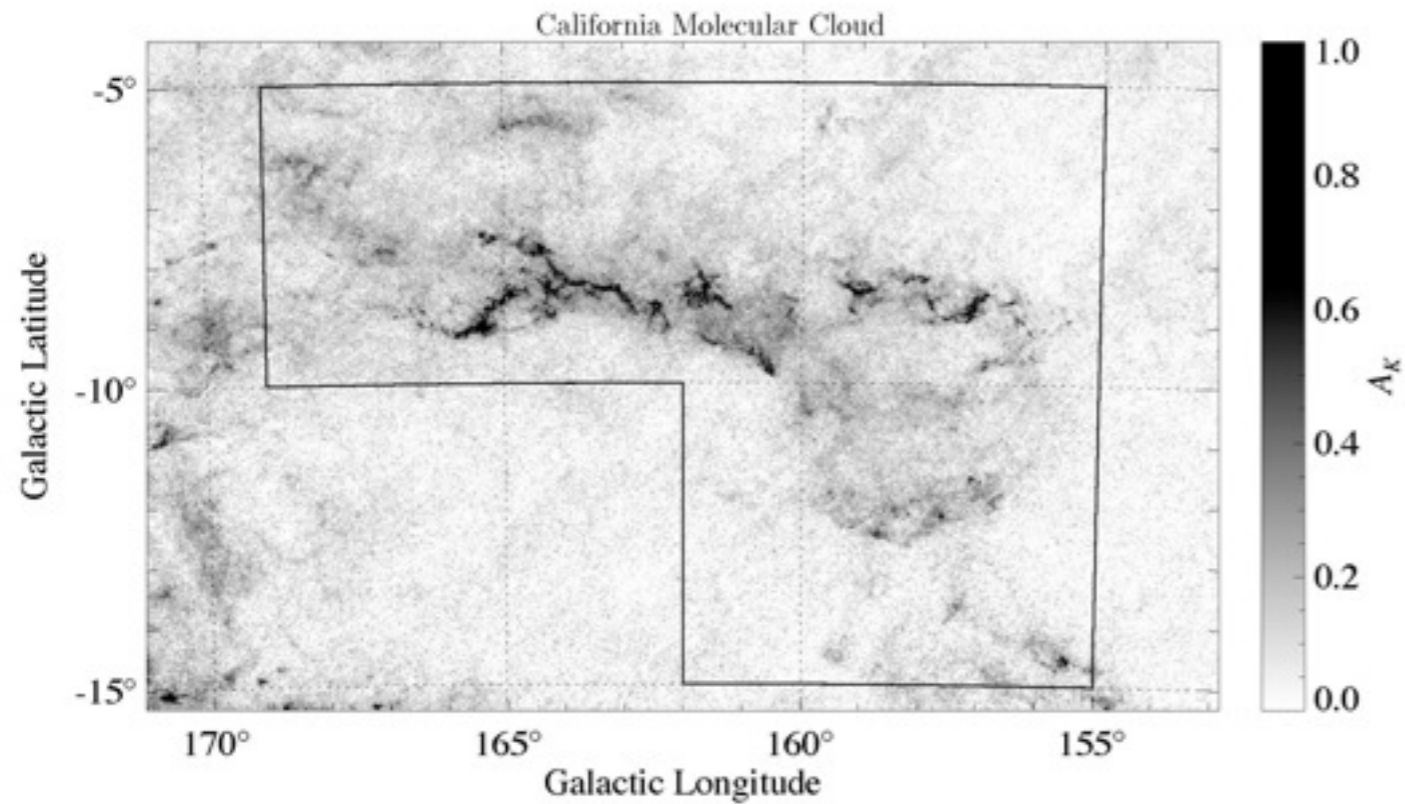
3rd Larson's law



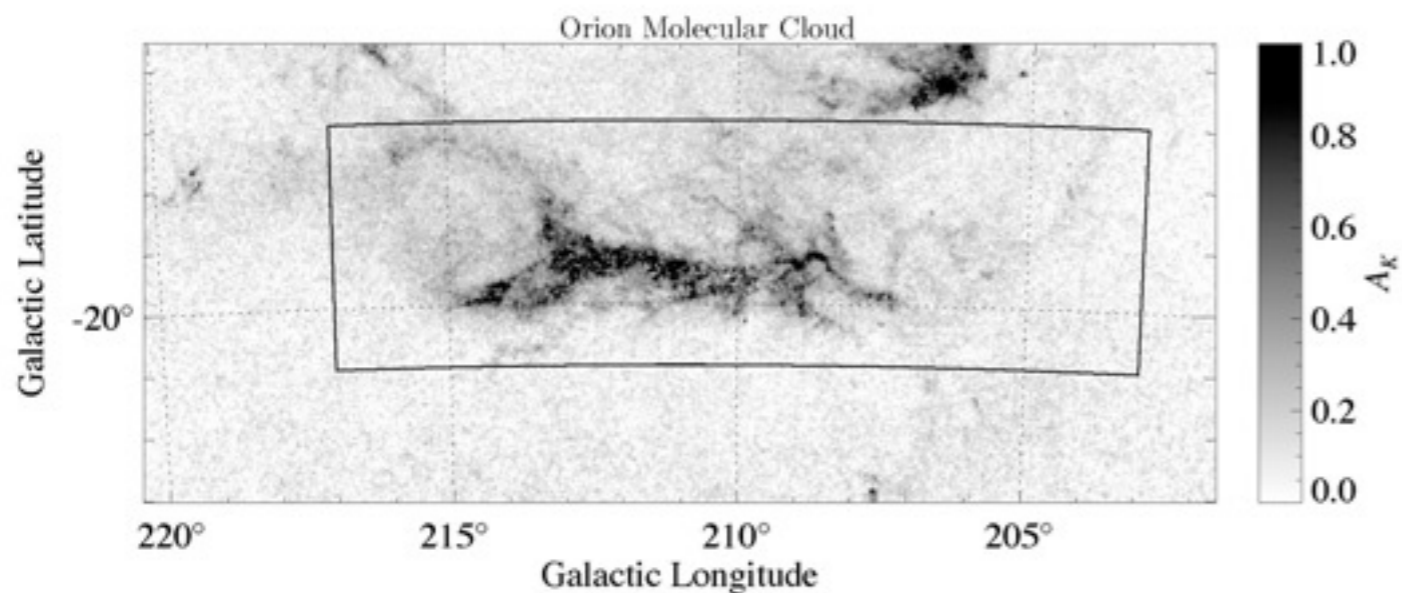
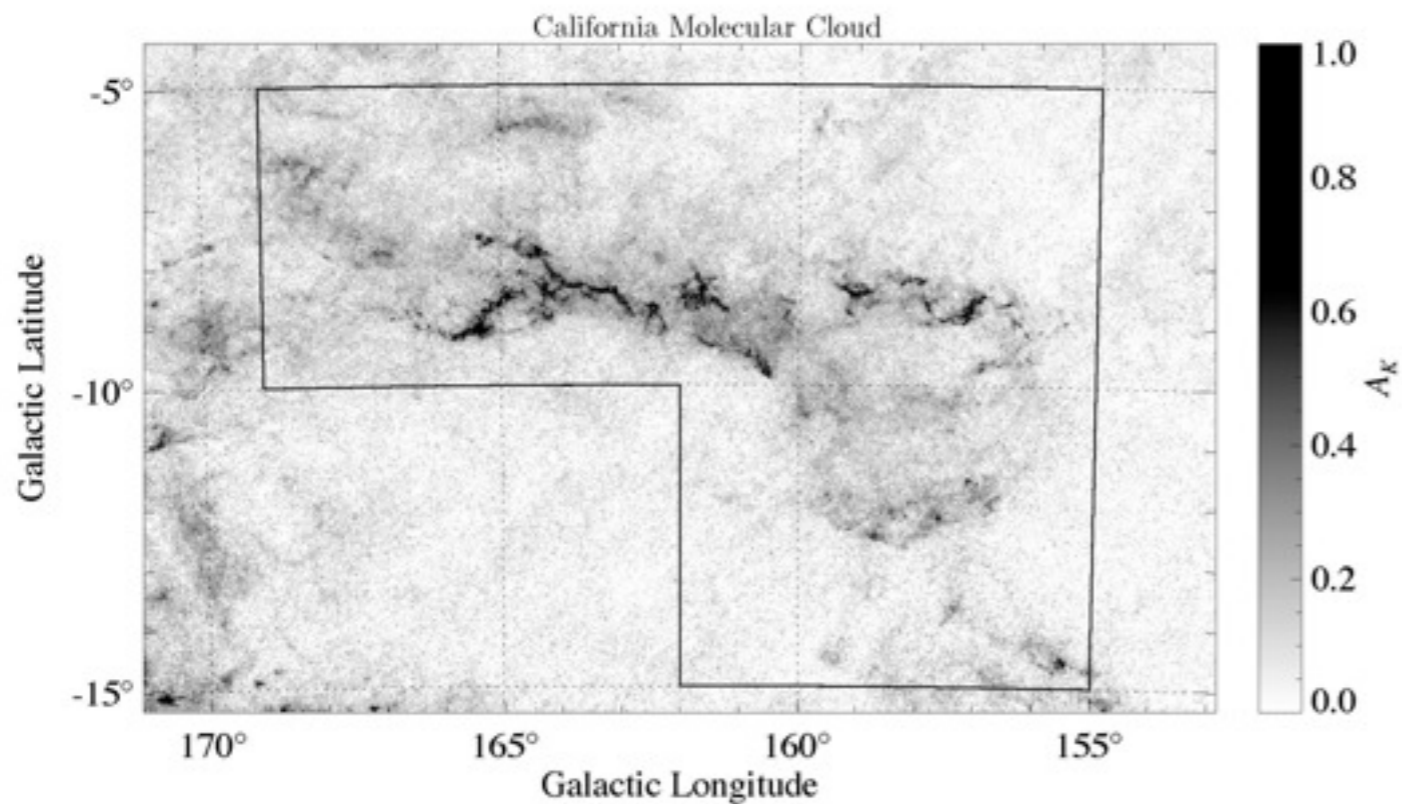
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SFRs in the California and Orion molecular clouds

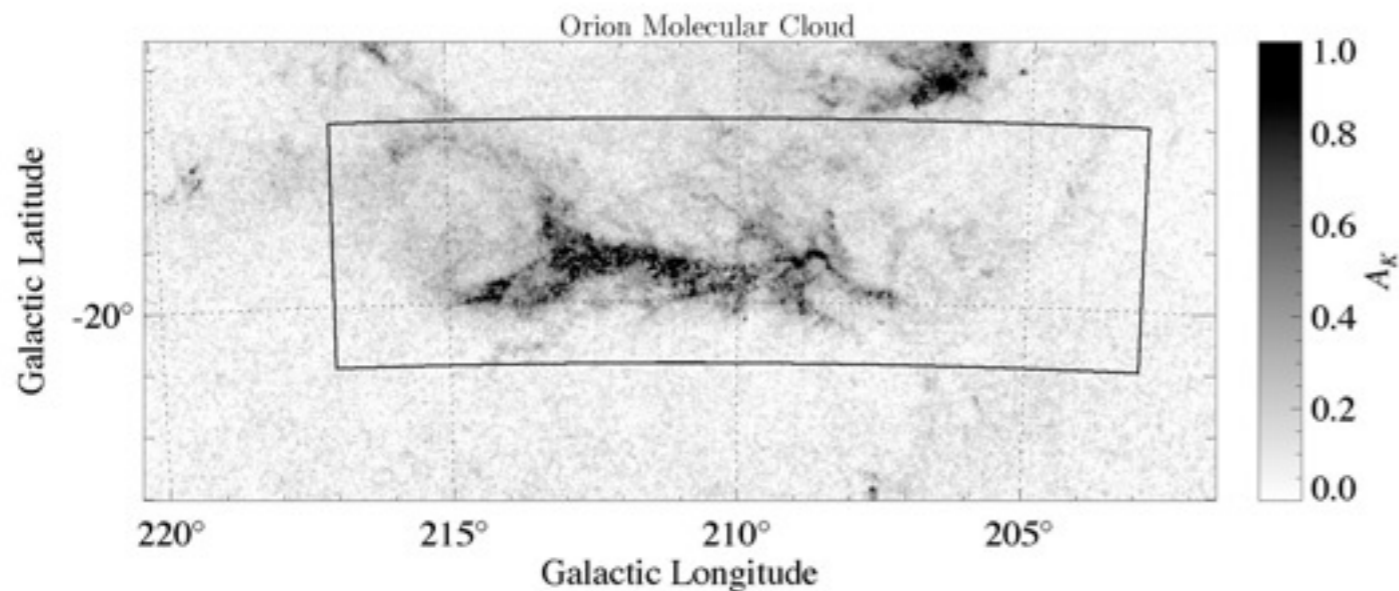
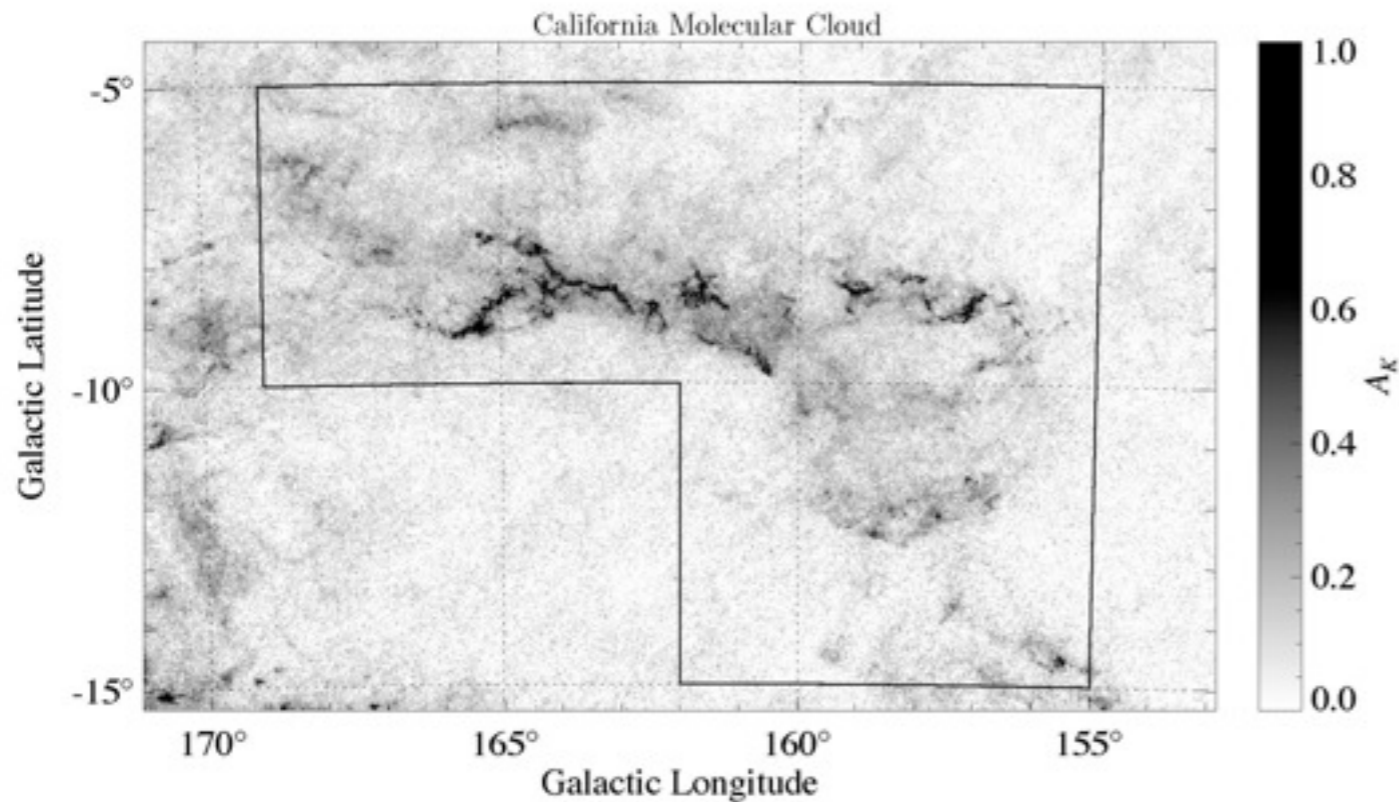


SFRs in the California and Orion molecular clouds



Nearly identical shapes & sizes, but
 $YSOs(Orion) > 10 \times YSOs(California)$

SFRs in the California and Orion molecular clouds

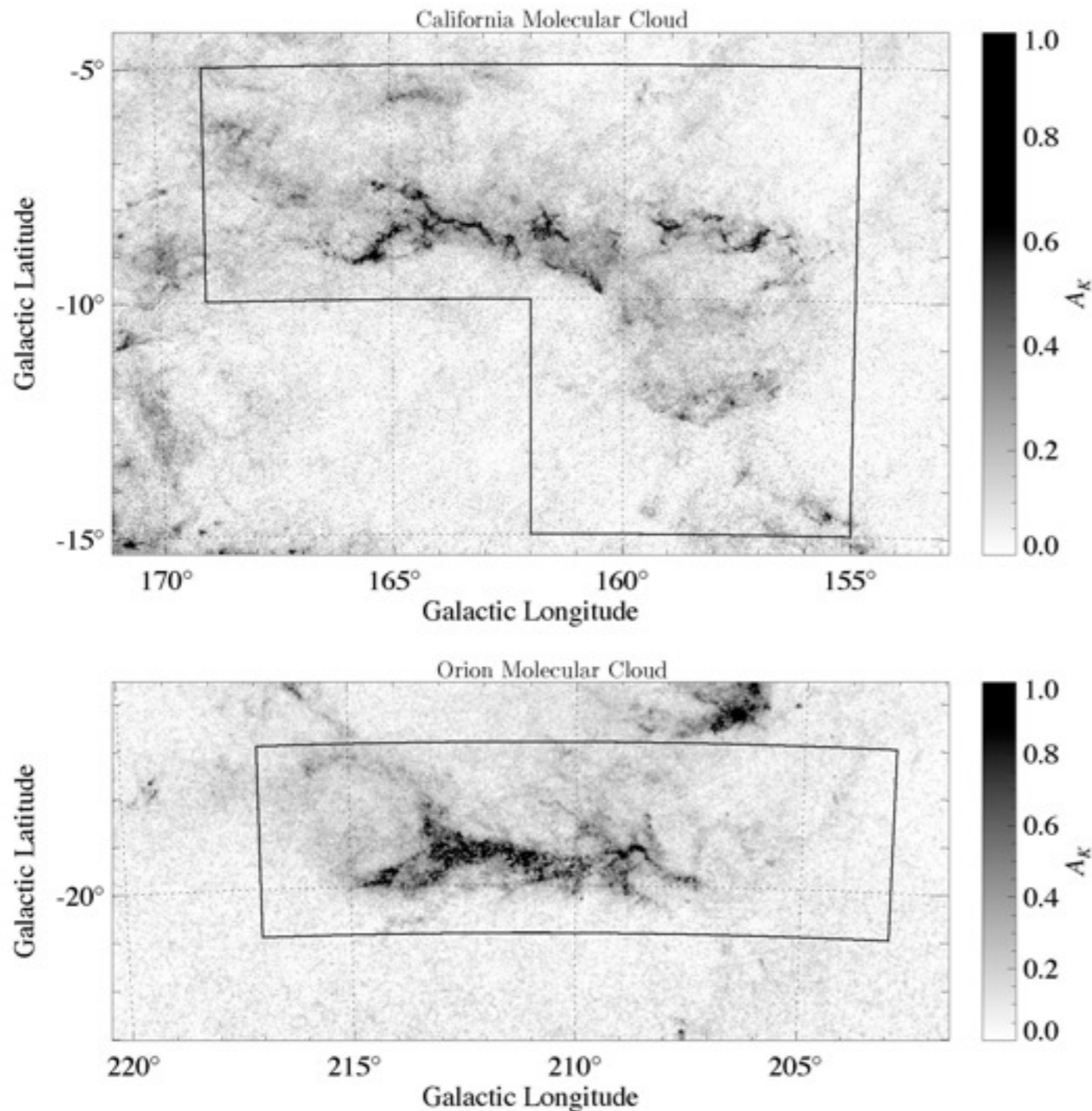


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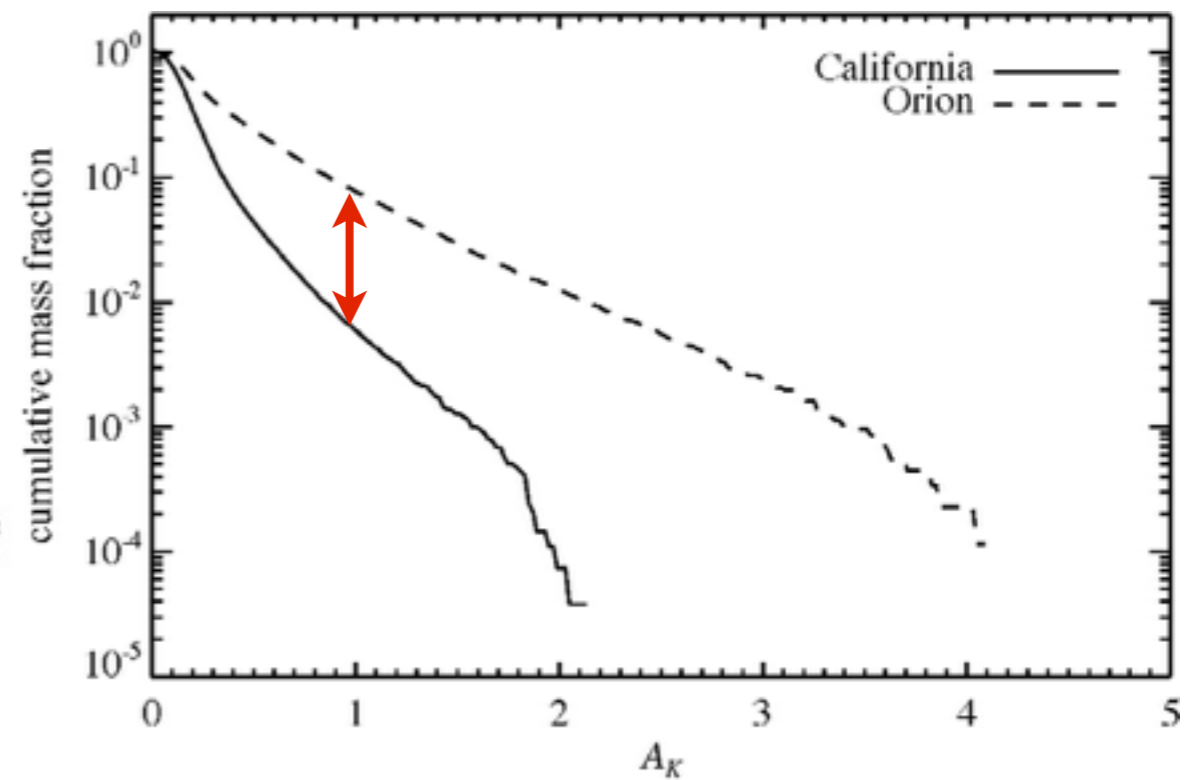
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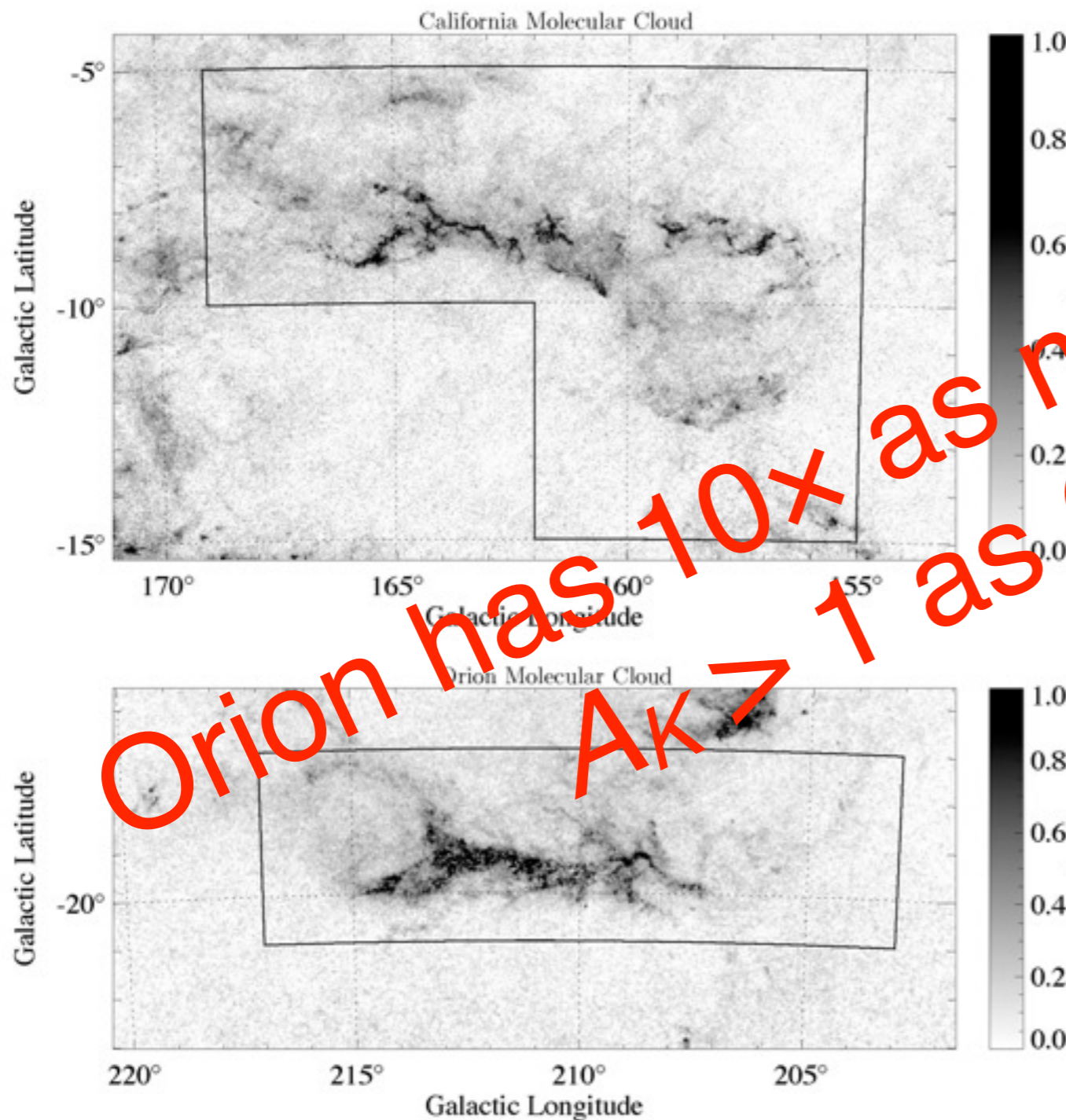
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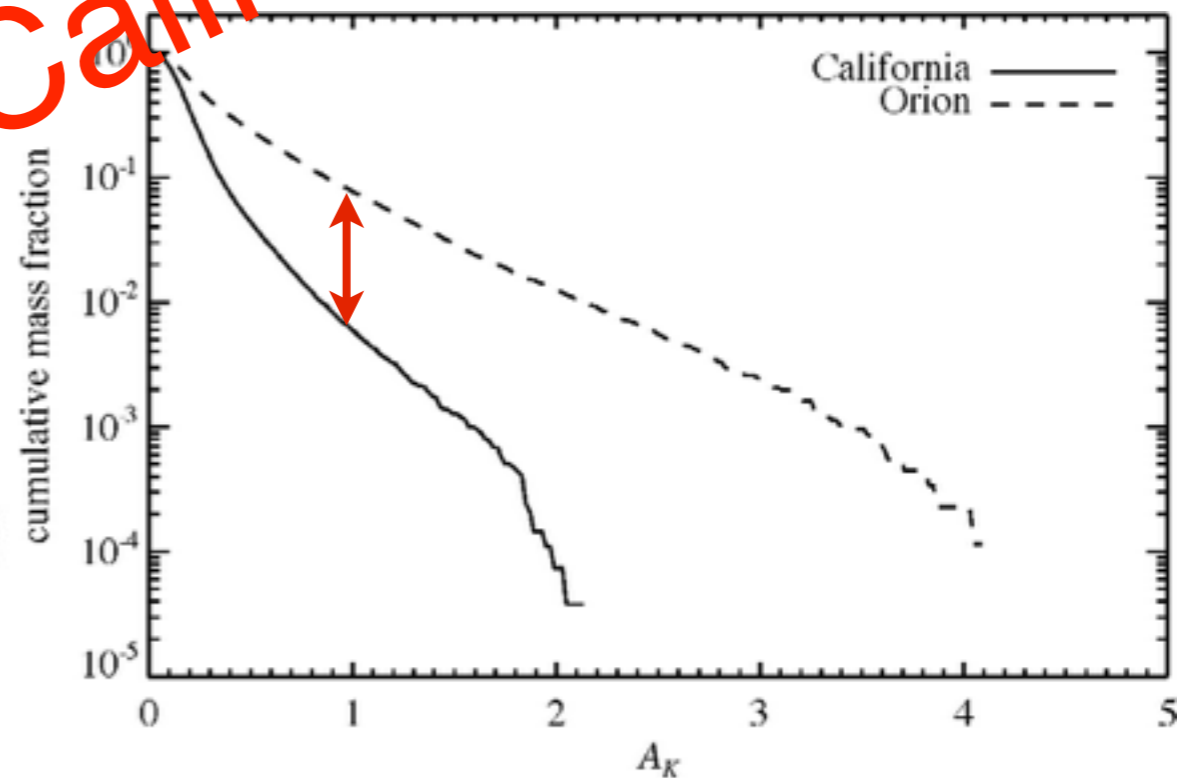
SFRs in the California and Orion molecular clouds



Nearly identical shapes & sizes, but

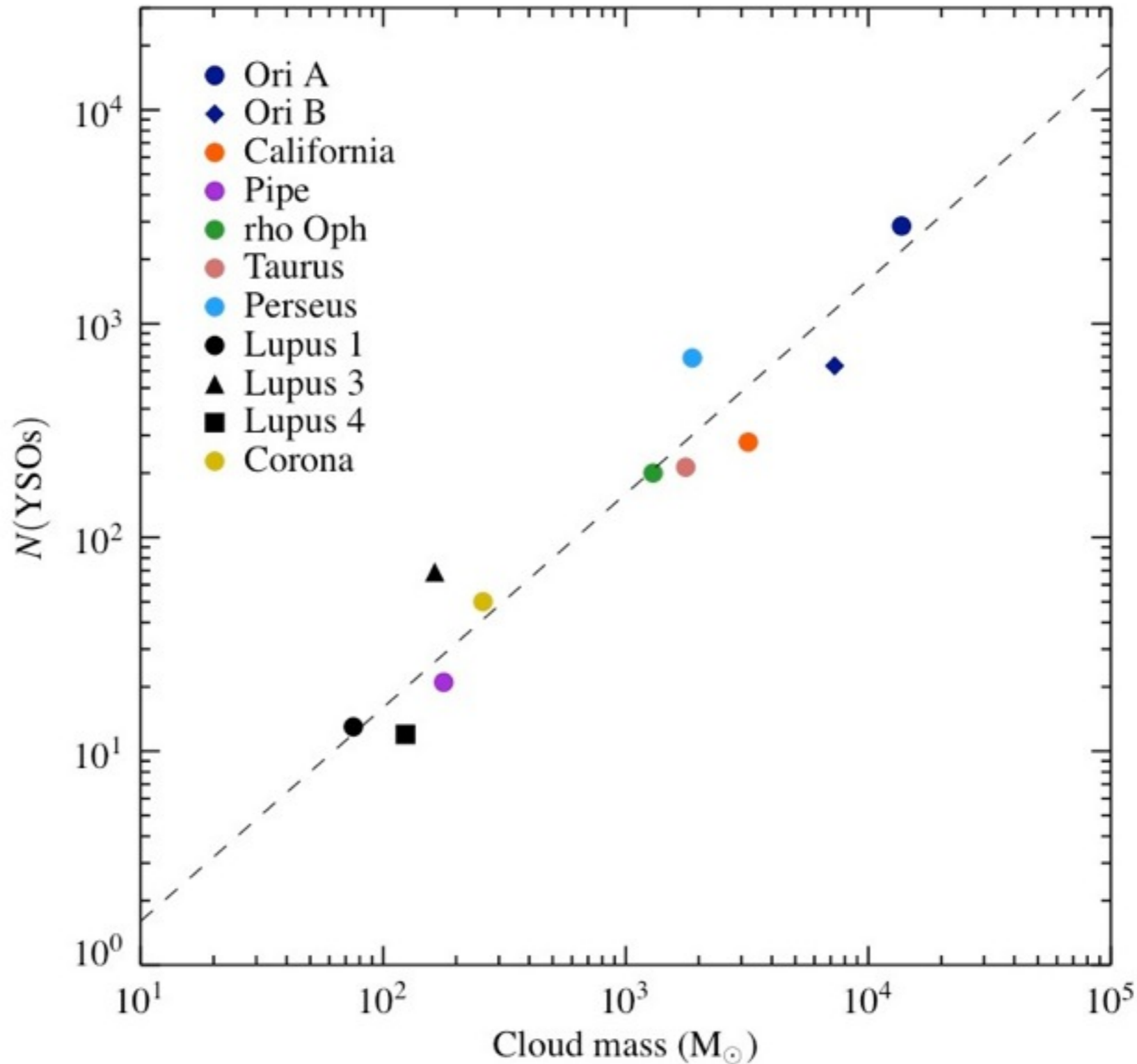
$\text{YSOs}(\text{Orion}) \geq 10 \times \text{YSOs}(\text{California})$

$\text{SFR}(\text{Orion}) \geq 10 \times \text{SFR}(\text{California})$

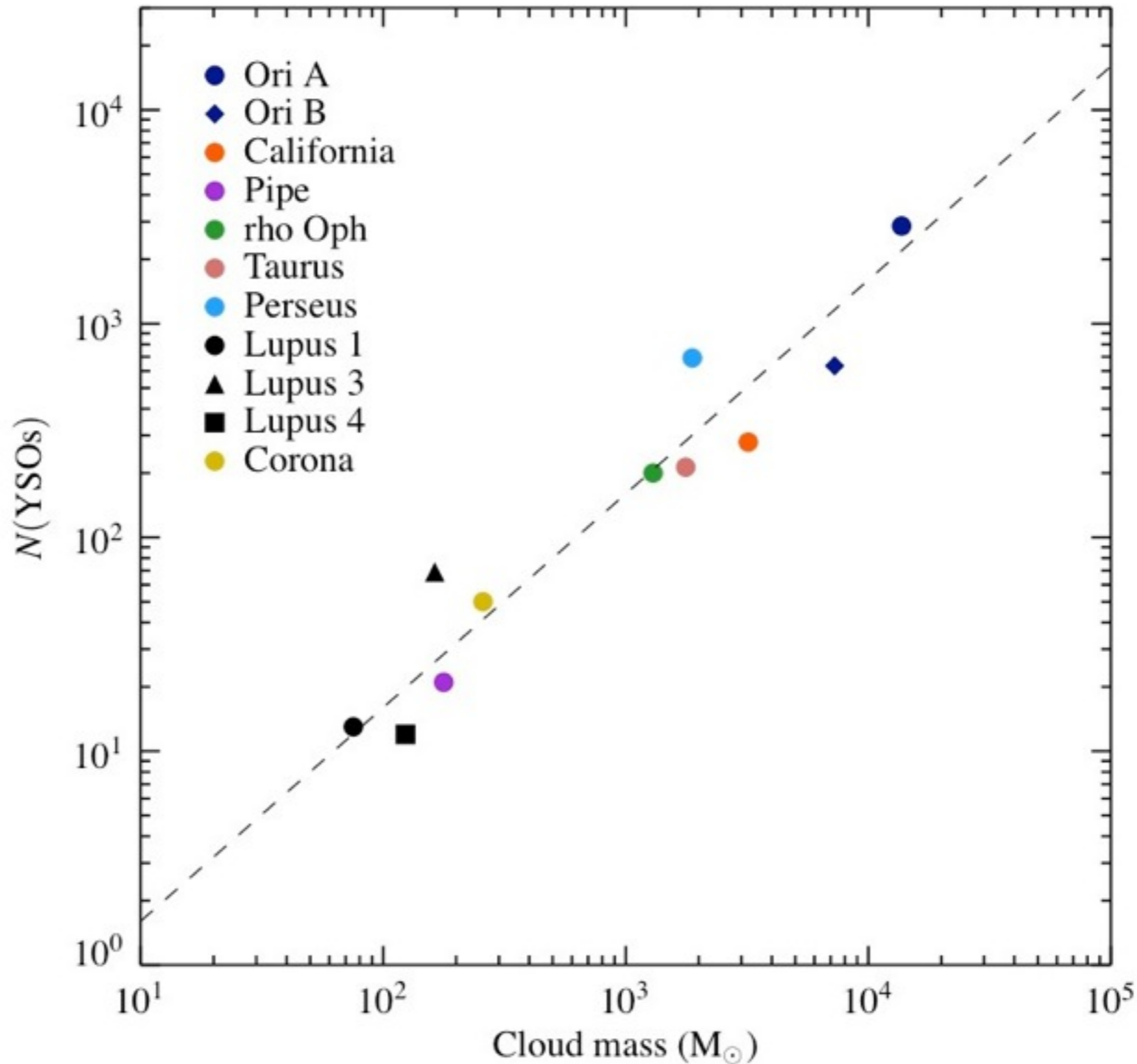


Orion has $10 \times$ as much material at $A_K > 1$ as California

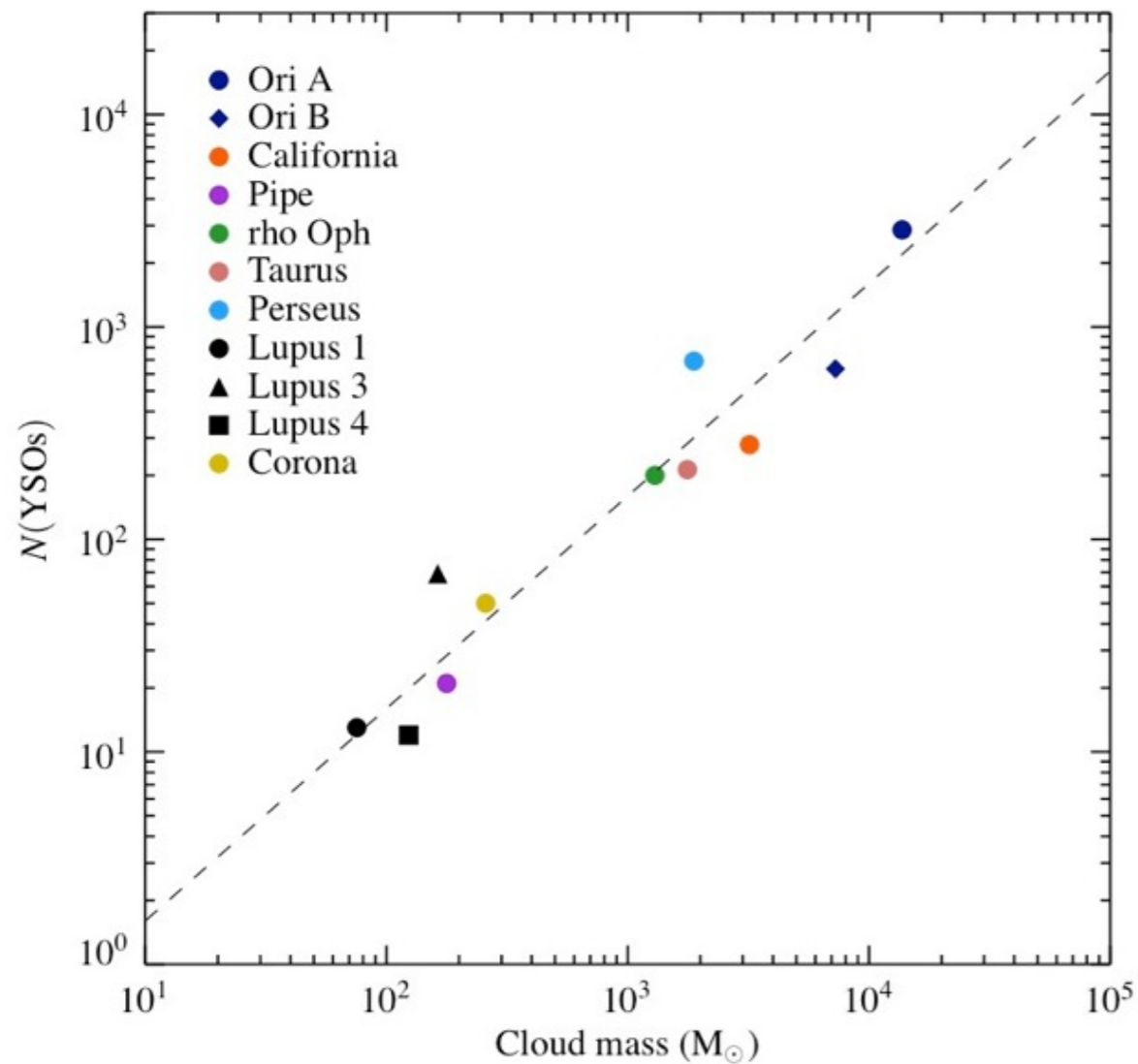
SFR directly proportional to mass
above $A_K > 0.8$ mag ($\Sigma > 116 M_\odot \text{pc}^{-2}$)



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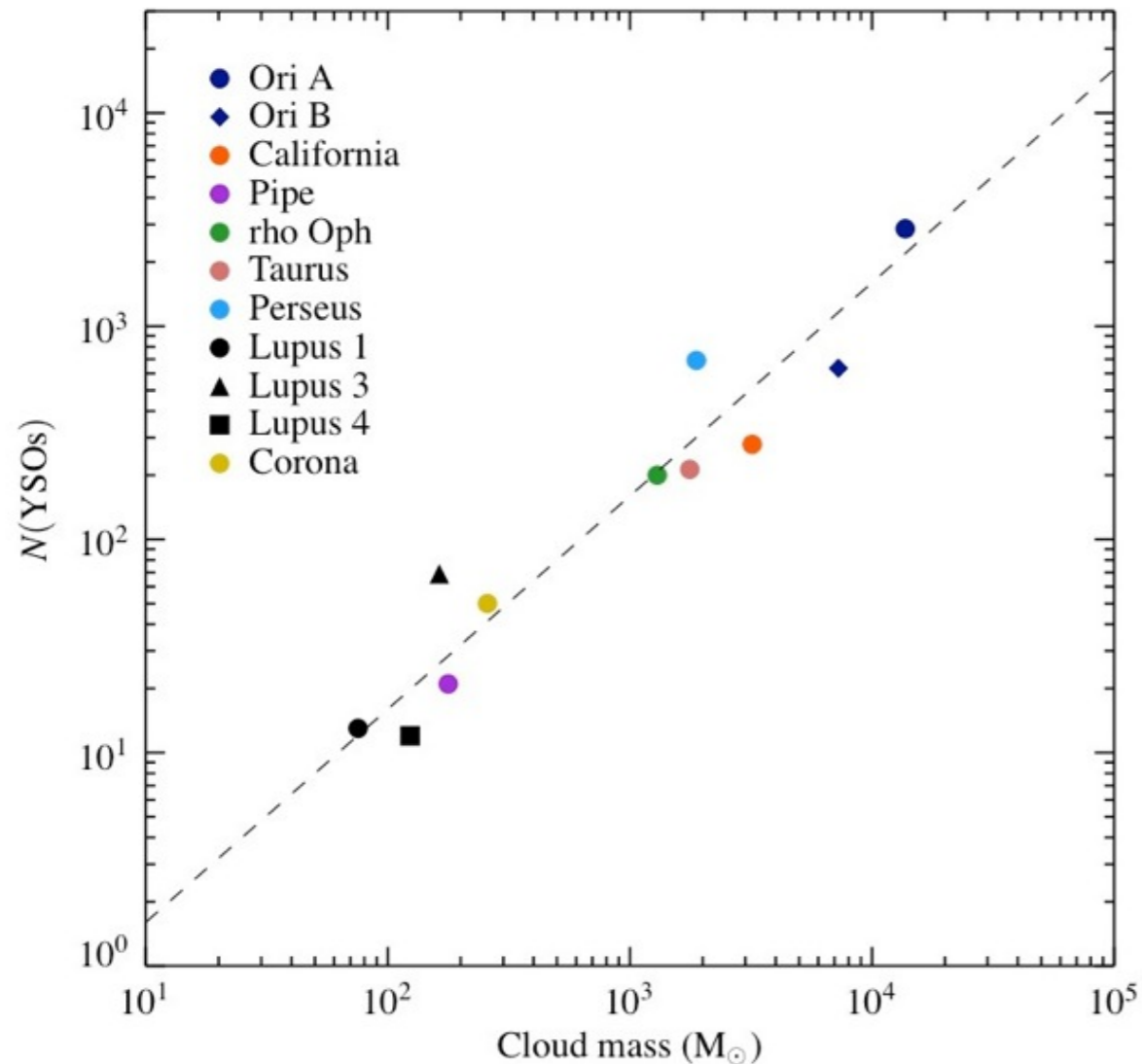


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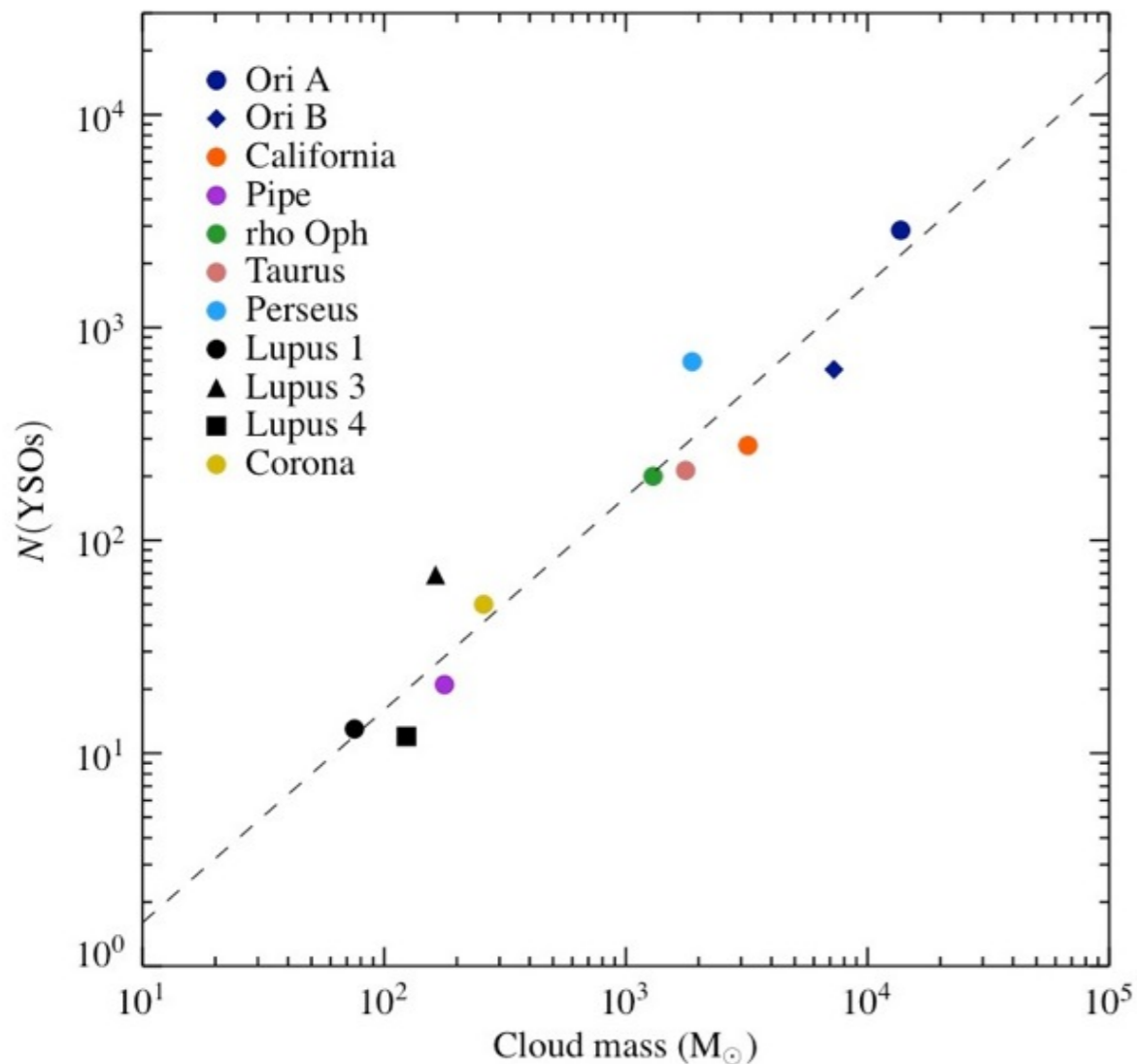
SFR directly proportional to mass
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$$\left(\frac{SFR}{M_\odot \text{ yr}^{-1}} \right) = 4.6 \times 10^{-8} \left(\frac{M_{0.8}}{M_\odot} \right)$$



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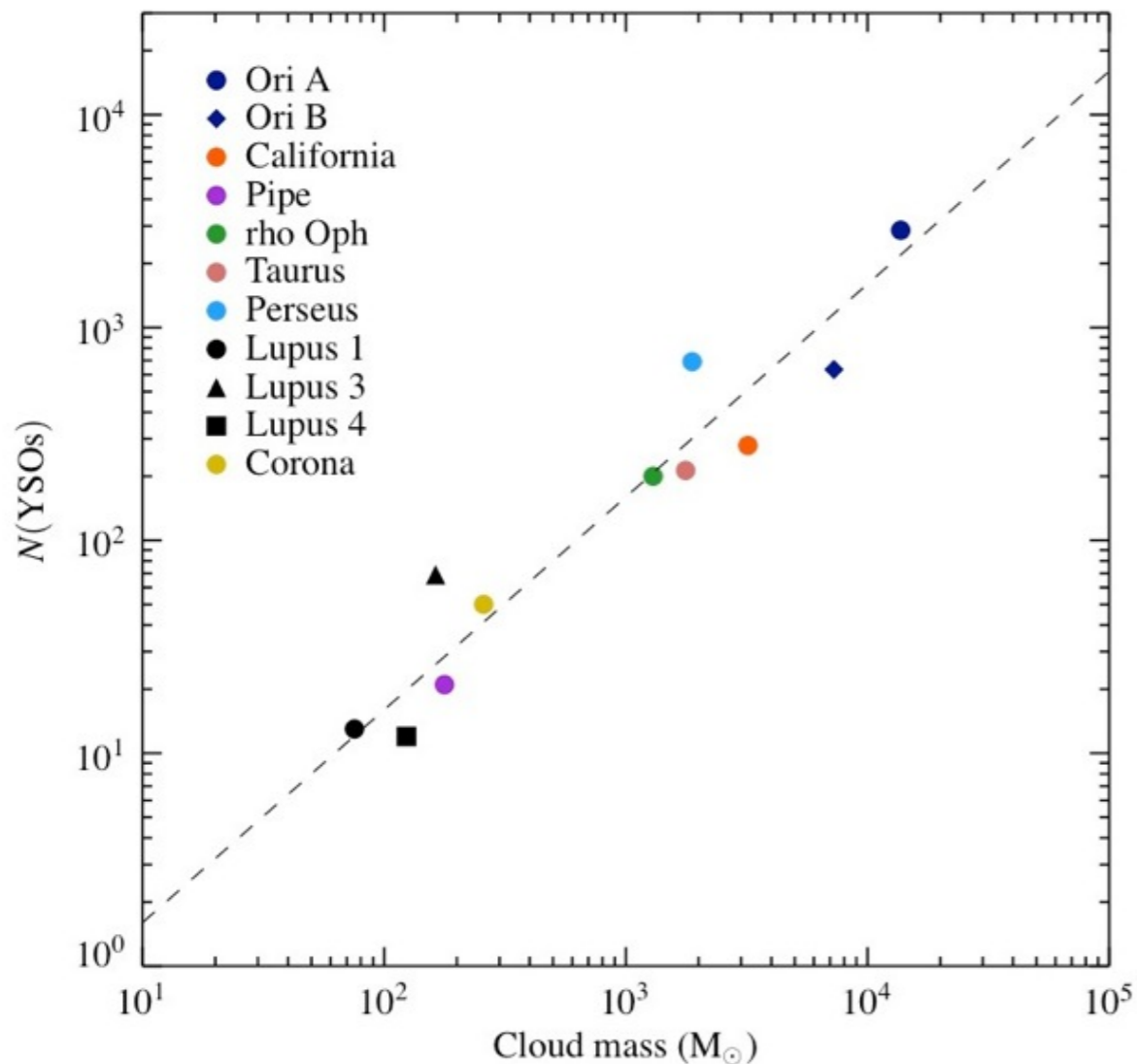
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What is the meaning of the slope of this relation?

SFR directly proportional to mass
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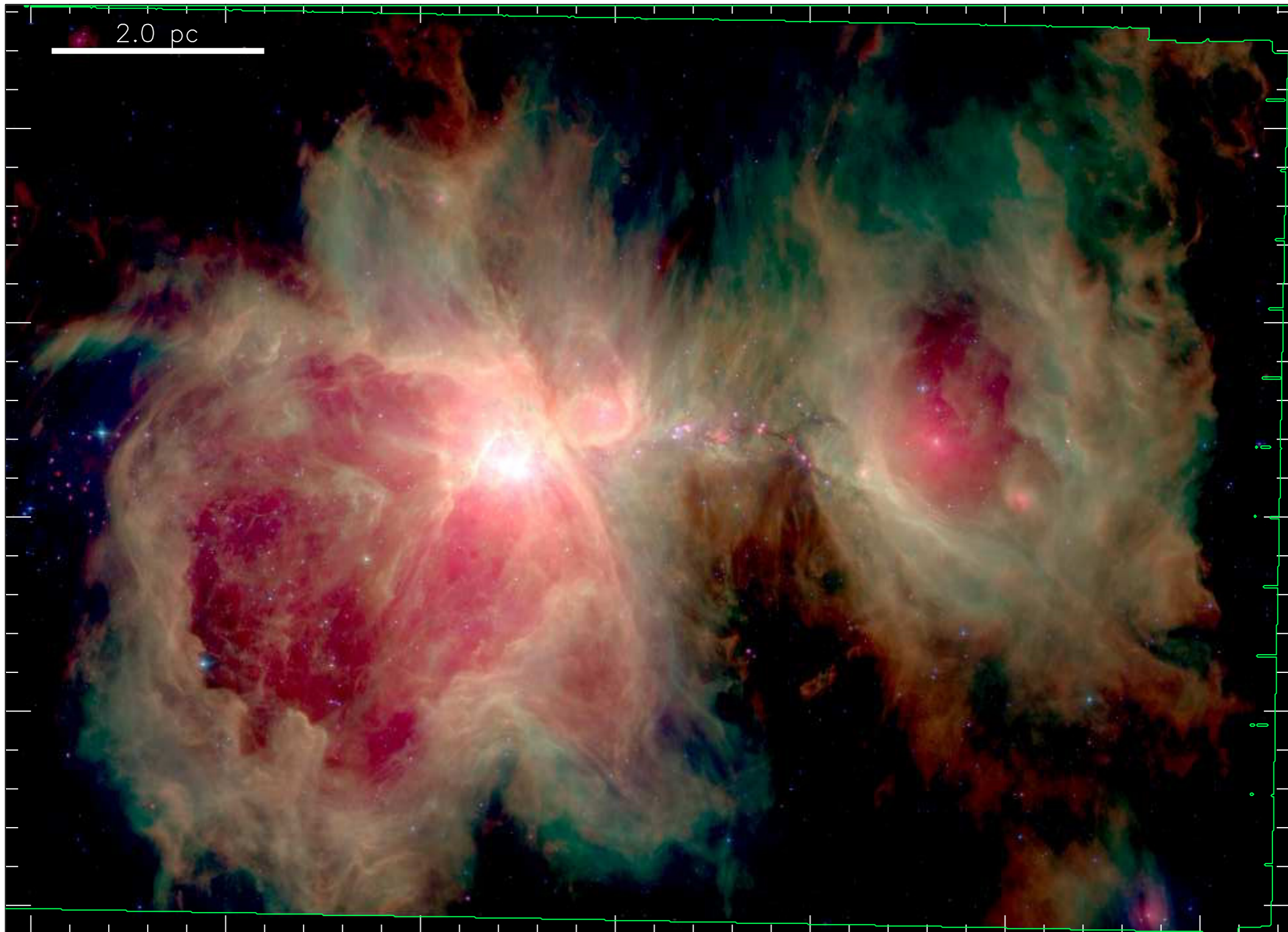
What is the meaning of the slope of this relation?

$$SFR = \varepsilon M_{0.8} / \tau_{\text{sf}}$$

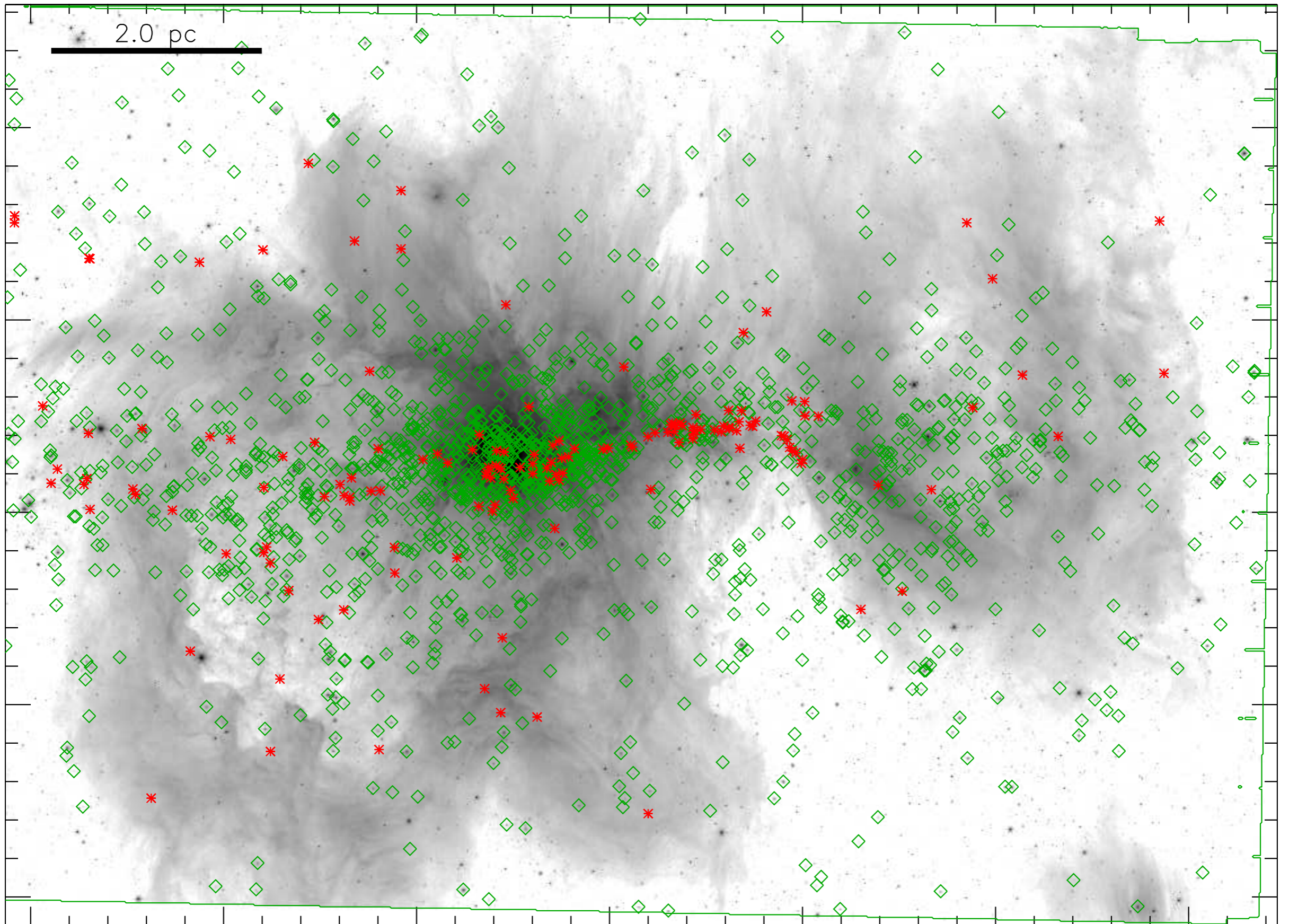
$$\tau_{\text{sf}} \simeq 2 \times 10^6 \text{ yr}$$

$$\varepsilon = SFE \simeq 0.10$$

One step further:
the *local* Schmidt law



Megeath et al. (2012)

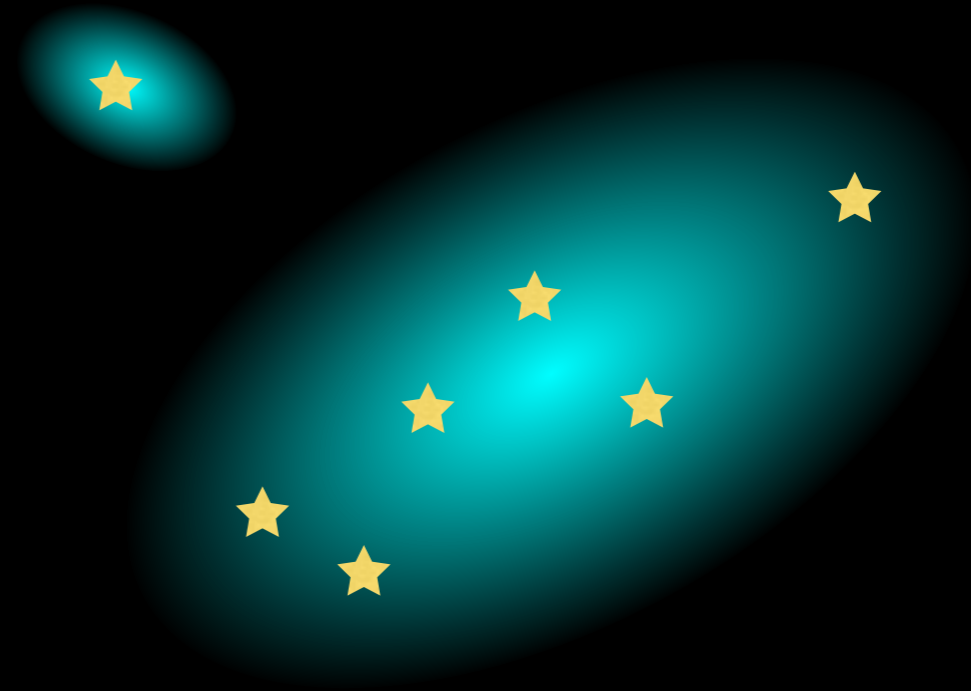




Fitting random spatial data



Fitting random spatial data



(Sarazin 1980, Lombardi et al. 2013)

Fitting random spatial data

Problem 1: check if a set of points is a likely realization of a 2D density



(Sarazin 1980, Lombardi et al. 2013)

Fitting random spatial data

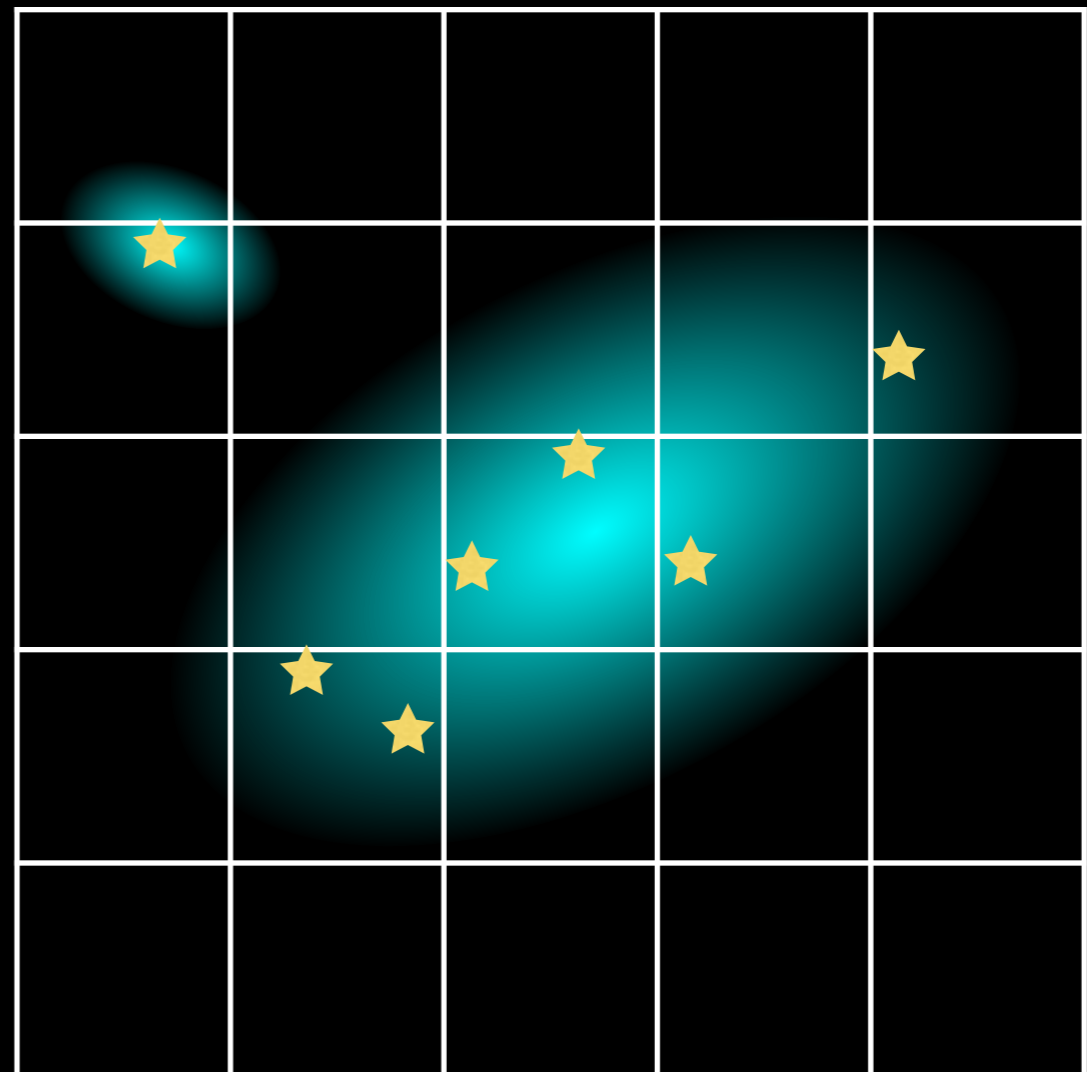
Problem 1: check if a set of points is a likely realization of a 2D density

Solution: bin the data and apply a Poisson statistics

$$P(N_i) = e^{-\mu_i} \frac{\mu_i^{N_i}}{N_i!}$$

$$\mu_i = \int_{\square_i} \Sigma(x) d^2x$$

$$P_{\text{tot}} = \prod_i P(N_i)$$



(Sarazin 1980, Lombardi et al. 2013)

Fitting random spatial data

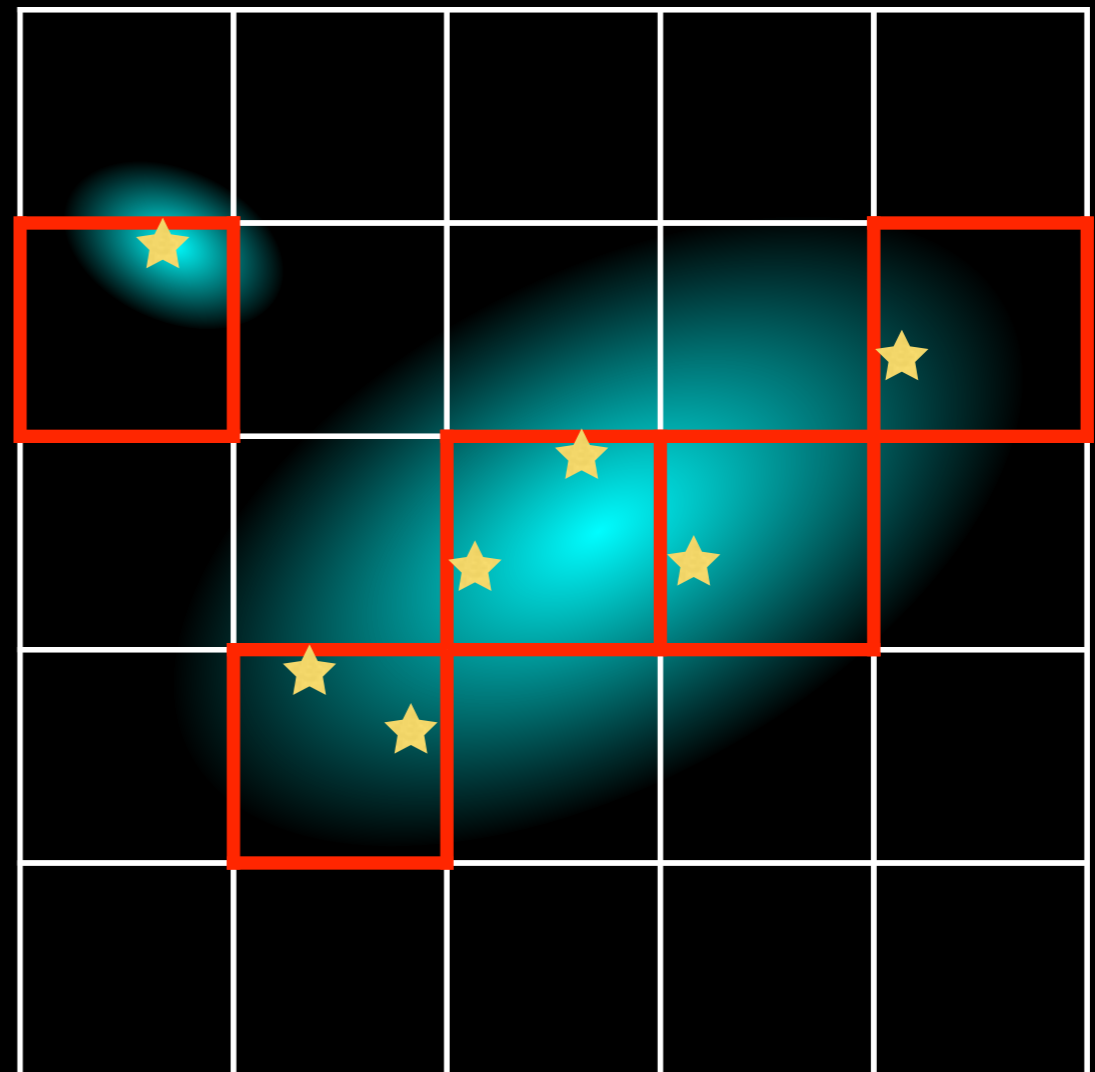
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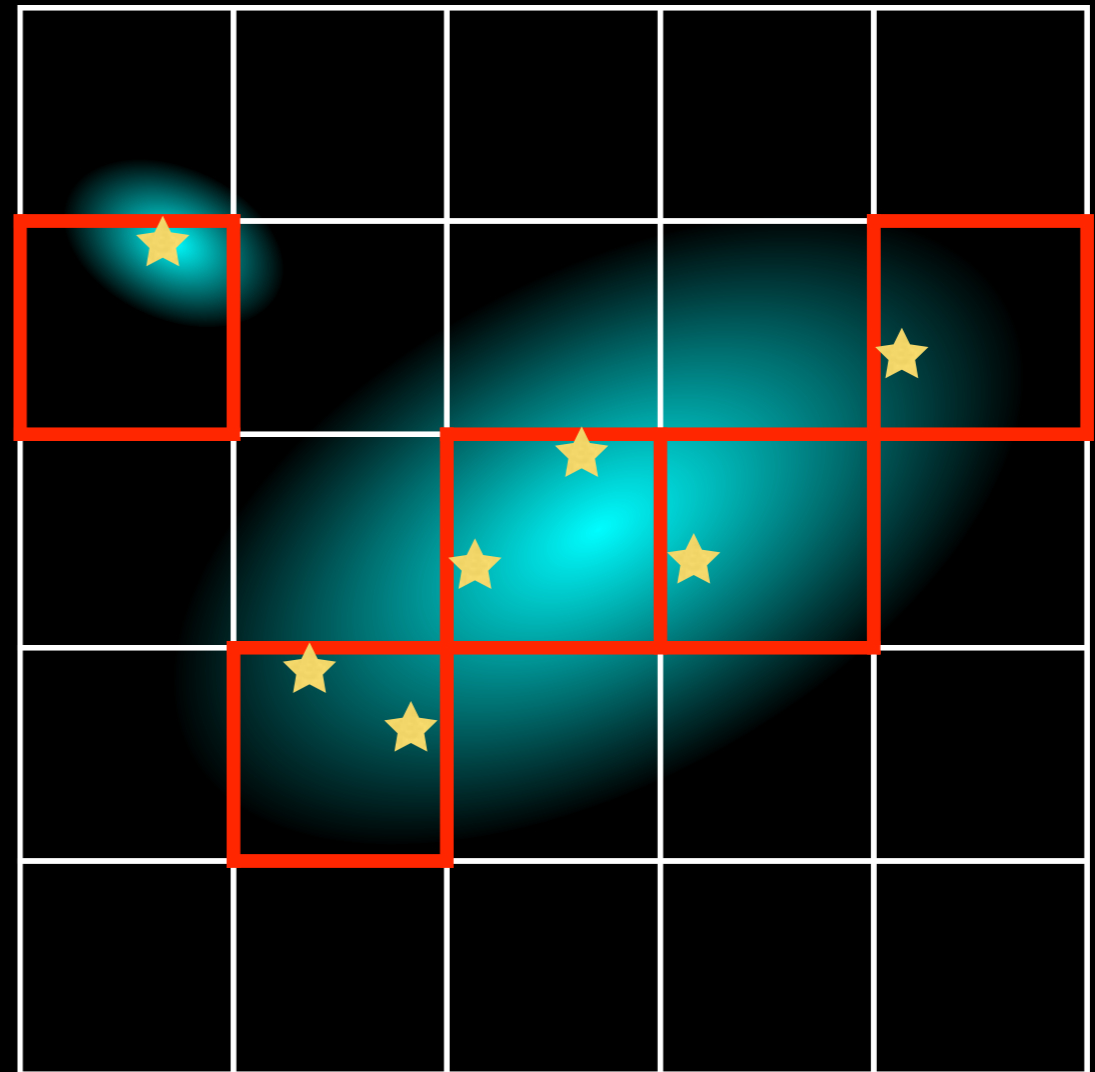
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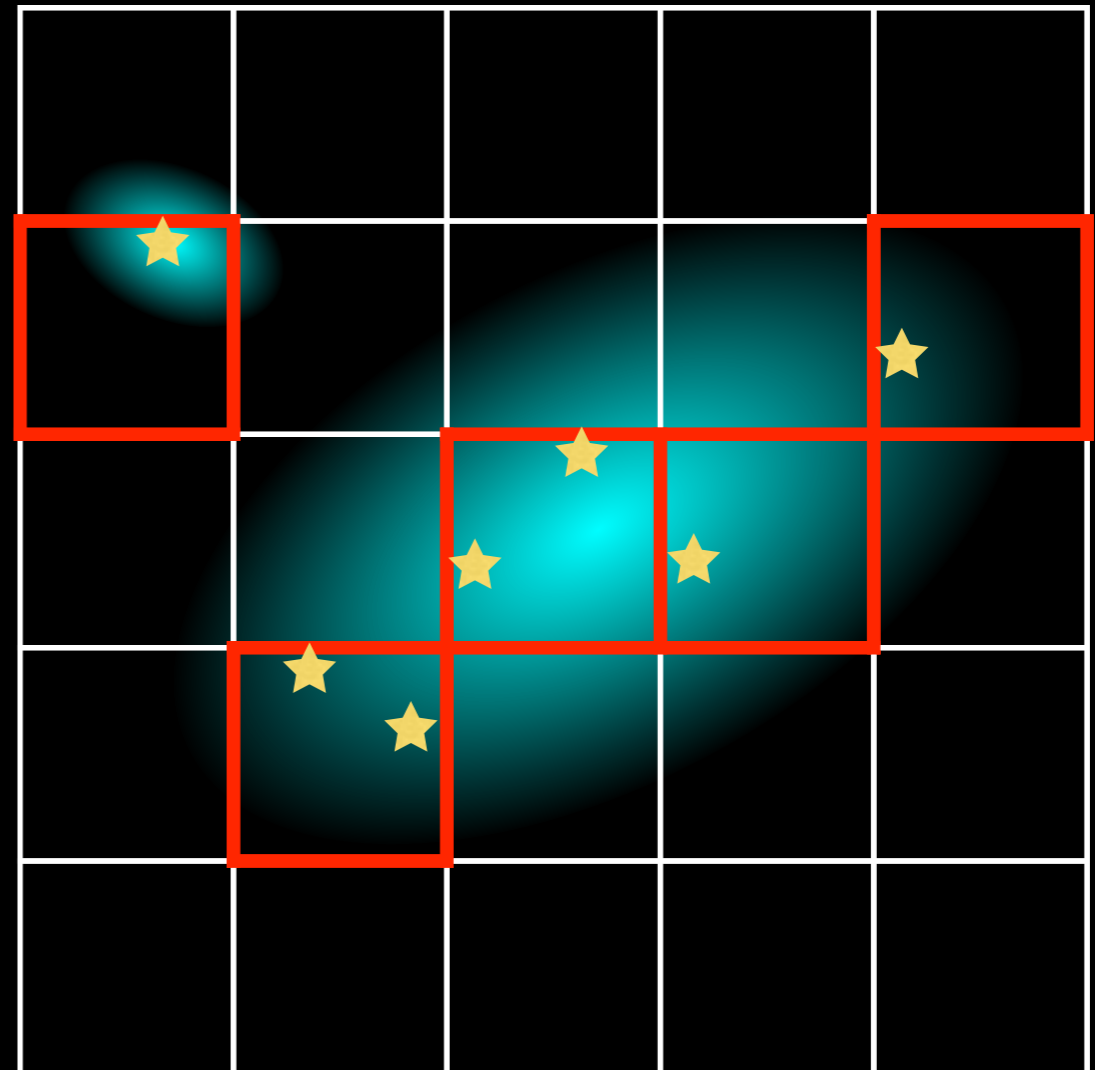
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Fitting random spatial data



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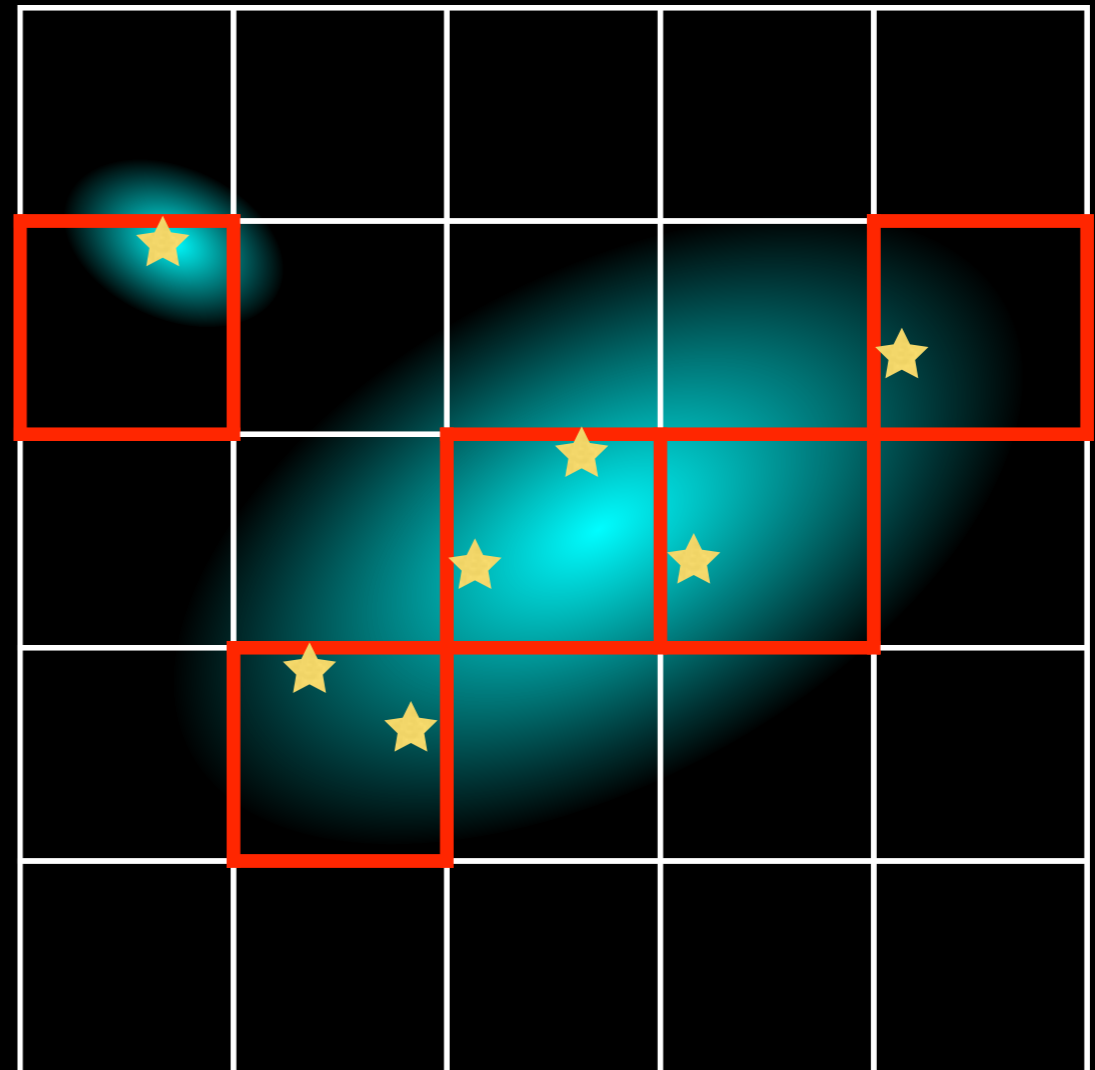
Problem II: how should we bin the data?



Fitting random spatial data

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Solution: use infinitesimal bins (easier math, optimal test)

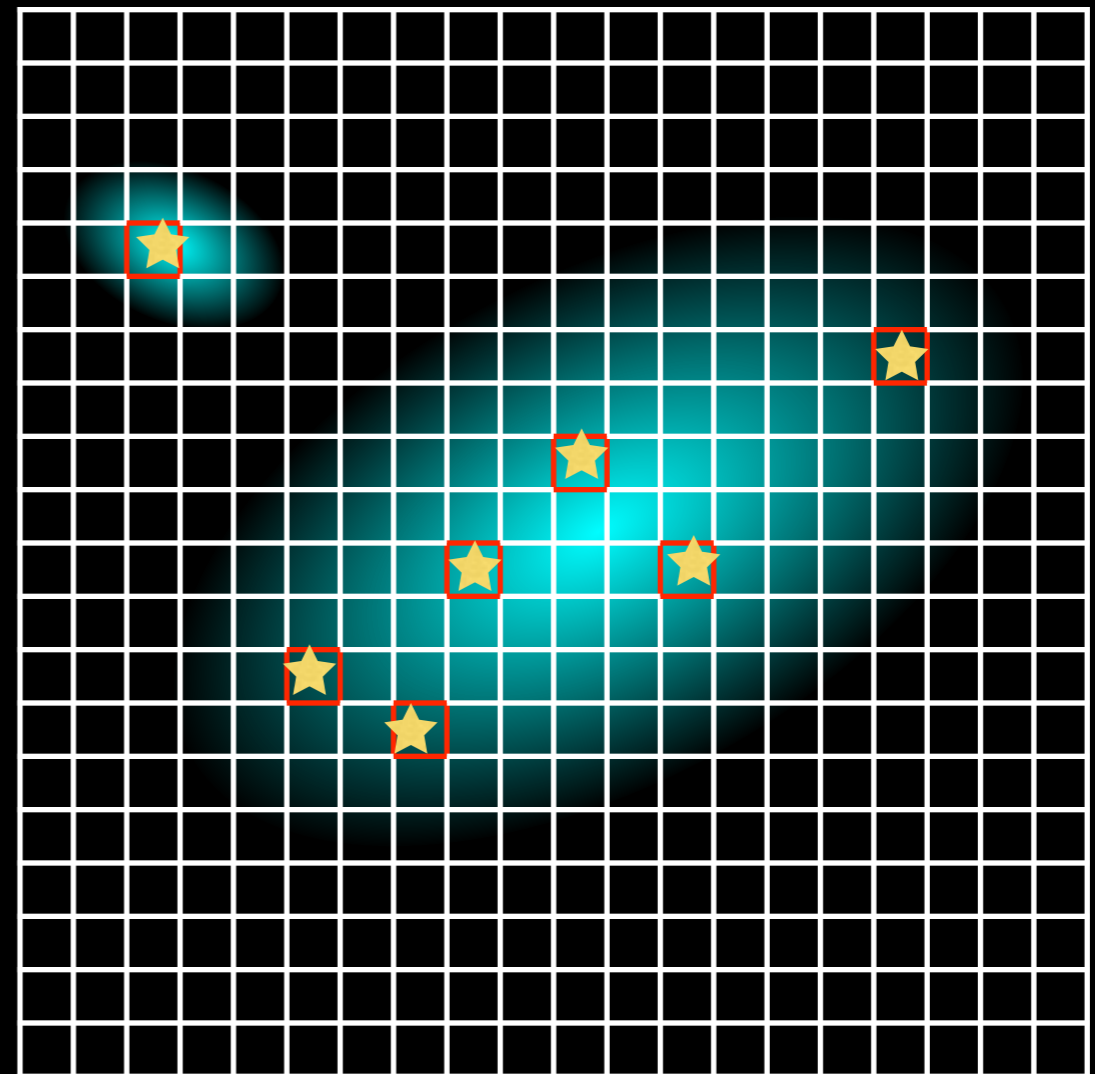


Fitting random spatial data

Problem II: how should we bin the data?

Solution: use infinitesimal bins (easier math, optimal test)

$$P(N_i) = \begin{cases} 1 - a\Sigma(x_i) \\ a\Sigma(x_i) \end{cases}$$



Fitting random spatial data

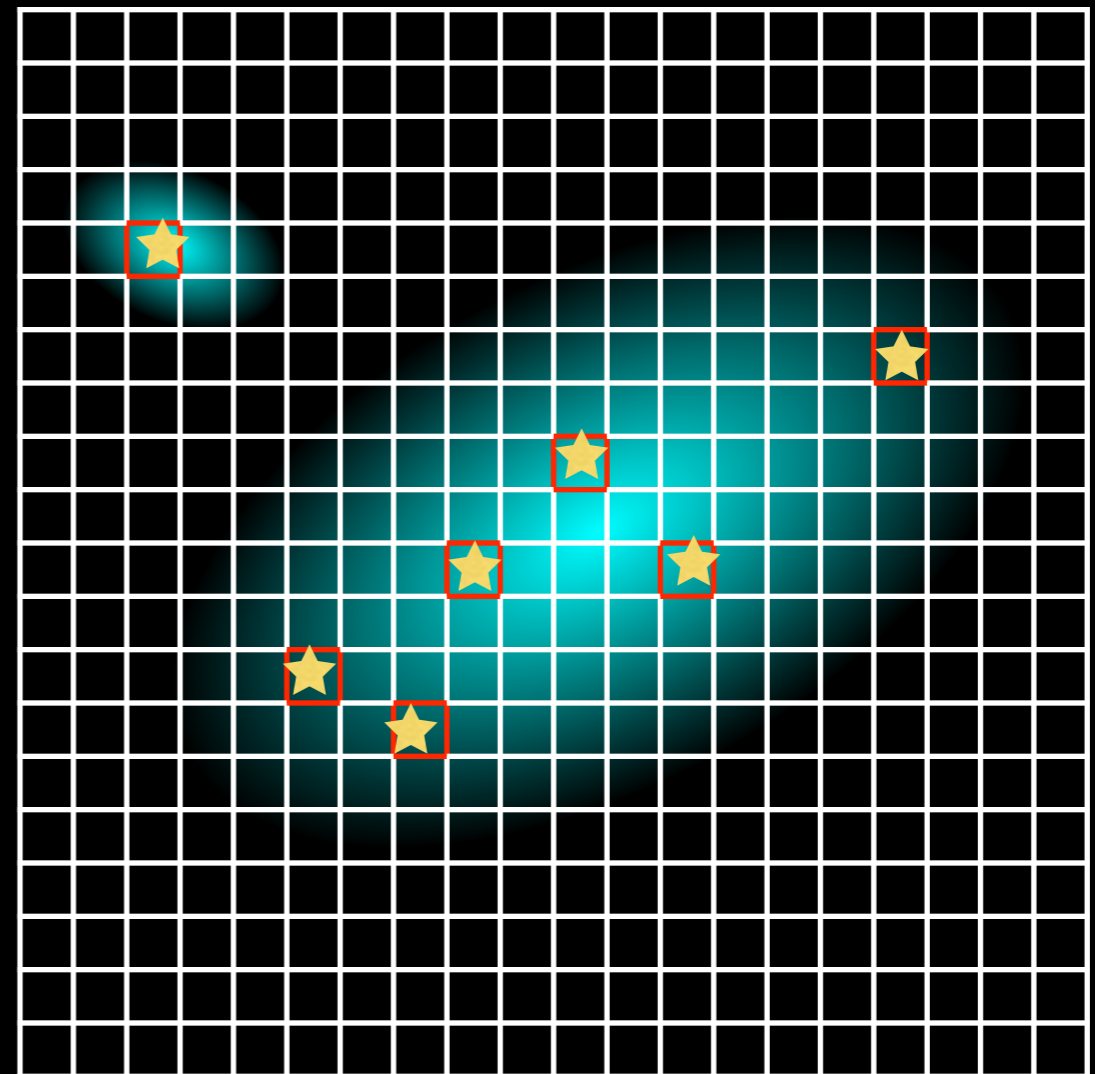
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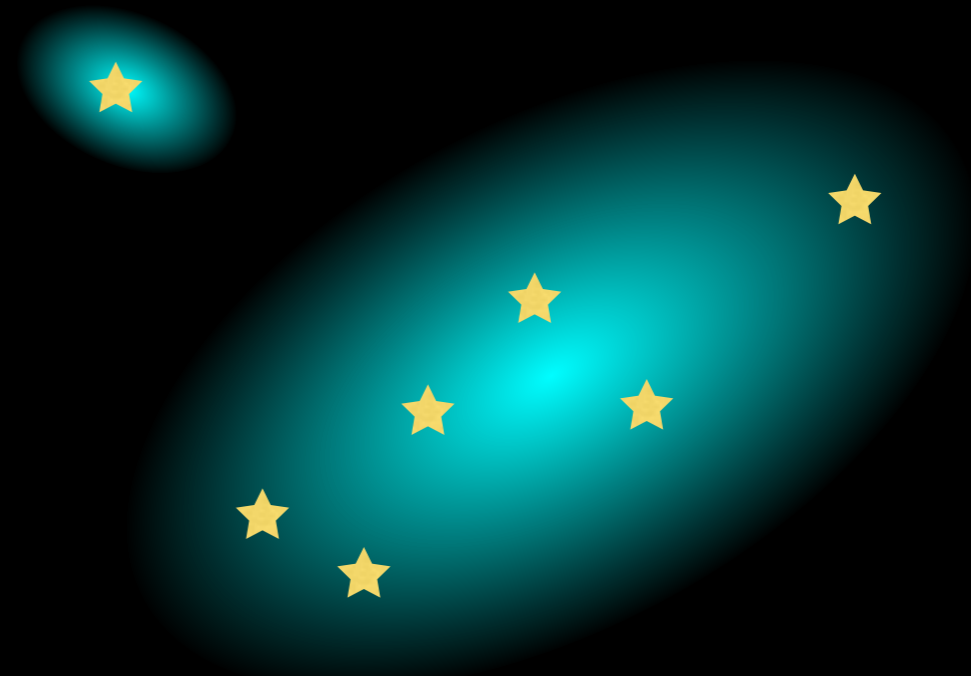
$$P(N_i) = \begin{cases} 1 - a\Sigma(x_i) \\ a\Sigma(x_i) \end{cases}$$

The final solution is best expressed using logarithms

$$\ln P_{\text{tot}} \equiv L = \sum_i \ln \Sigma(x_i) - \int \Sigma(x) d^2x$$

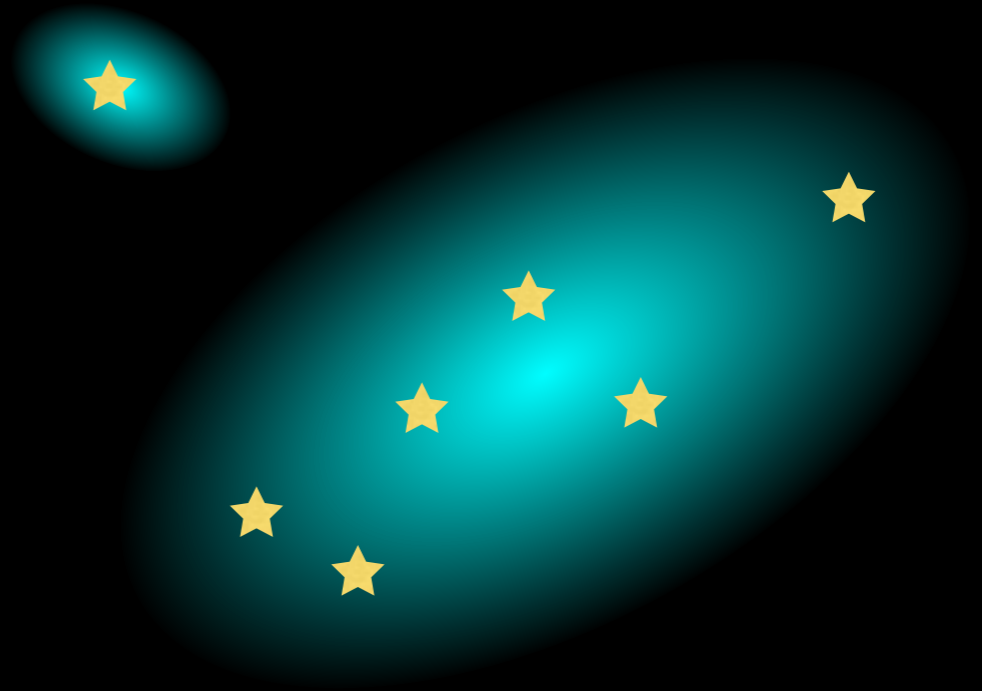


Fitting random spatial data



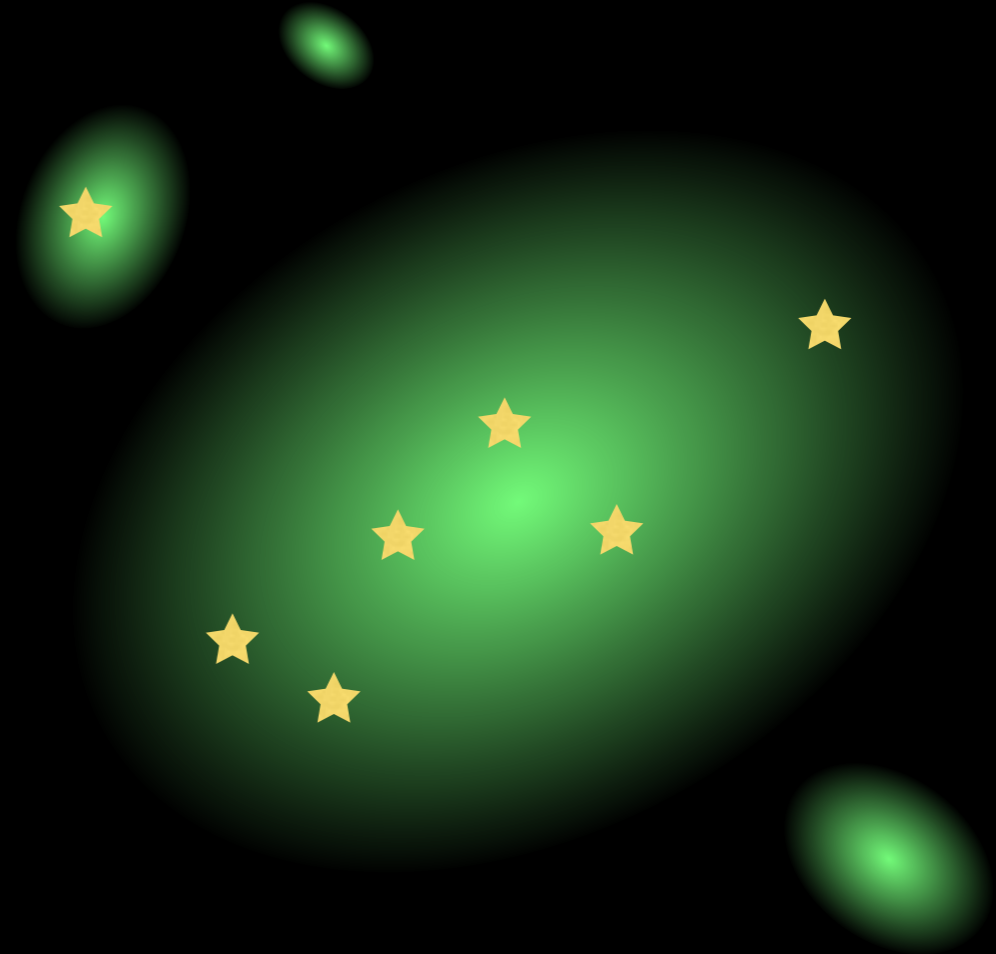
Fitting random spatial data

Problem III: which density fits best the data?



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Solution: this is an inverse problem, and therefore we use...



Fitting random spatial data

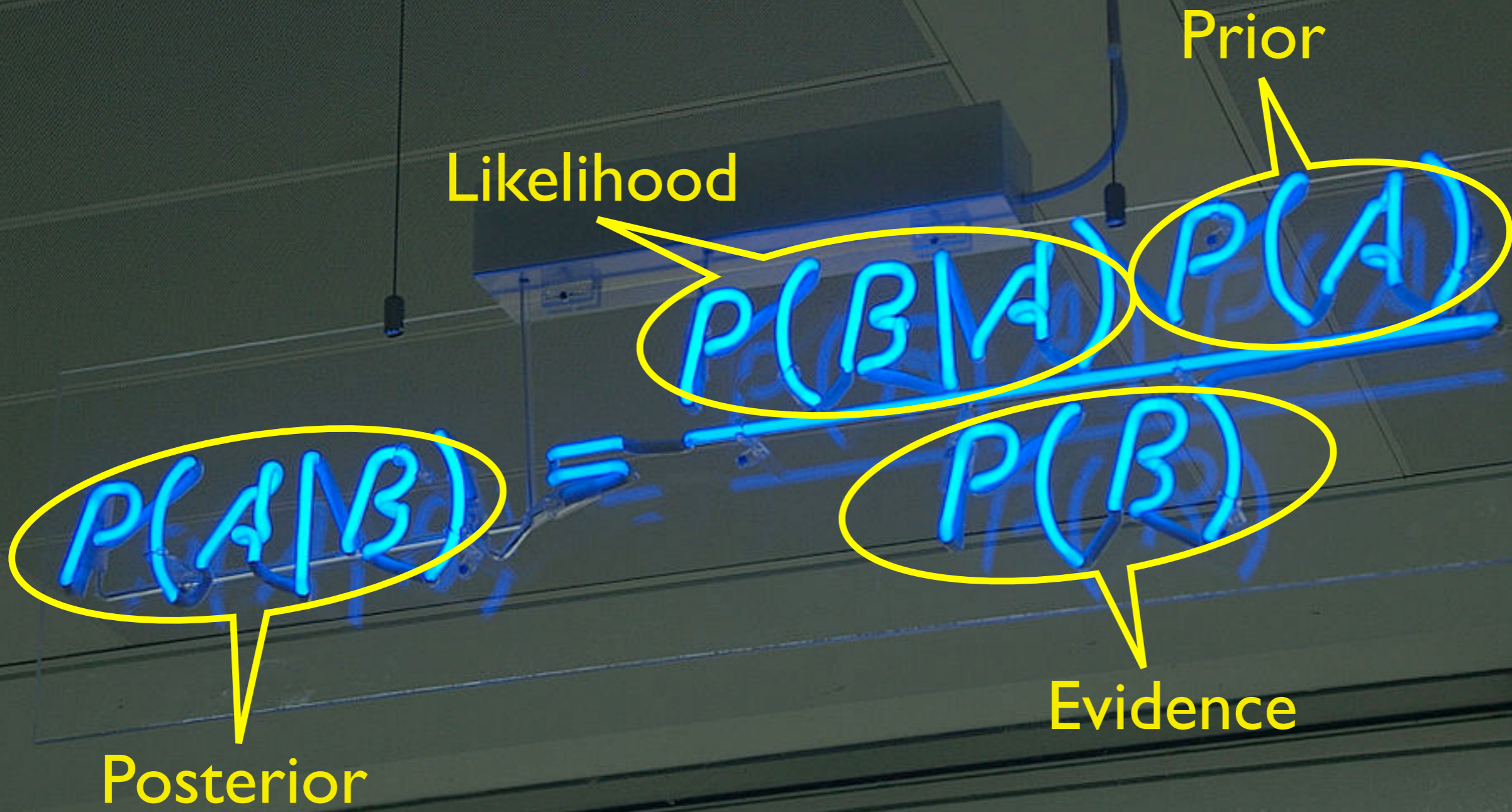
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$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

T. Bayes.



T. Bayes.

Trombe

Handwritten musical notation for Trombe (Trumpets). The staff begins with a treble clef, a key signature of one sharp (F#), and a common time signature (C). The music consists of several measures of notes, including quarter notes, eighth notes, and half notes, with some rests.

Oboe

Handwritten musical notation for Oboe. The staff begins with a treble clef, a key signature of one sharp (F#), and a common time signature (C). The music consists of several measures of notes, including quarter notes, eighth notes, and half notes, with some rests. A dynamic marking *W:* is visible in the middle of the staff.

Violini

Handwritten musical notation for Violini (Violins). The staff begins with a treble clef, a key signature of one sharp (F#), and a common time signature (C). The music consists of several measures of notes, including quarter notes, eighth notes, and sixteenth notes, with some rests.

Viola

Handwritten musical notation for Viola. The staff begins with a treble clef, a key signature of one sharp (F#), and a common time signature (C). The music consists of several measures of notes, including quarter notes and half notes, with some rests.

Spirito
11

Handwritten musical notation for Spirito. The staff begins with a treble clef, a key signature of one sharp (F#), and a common time signature (C). The music consists of several measures of notes, including quarter notes, eighth notes, and sixteenth notes, with some rests.

The local Schmidt law

The local Schmidt law

The local Schmidt law

- Density of protostars: $\Sigma_{\star}(x) = \kappa [A_K(x)]^{\beta}$

The local Schmidt law

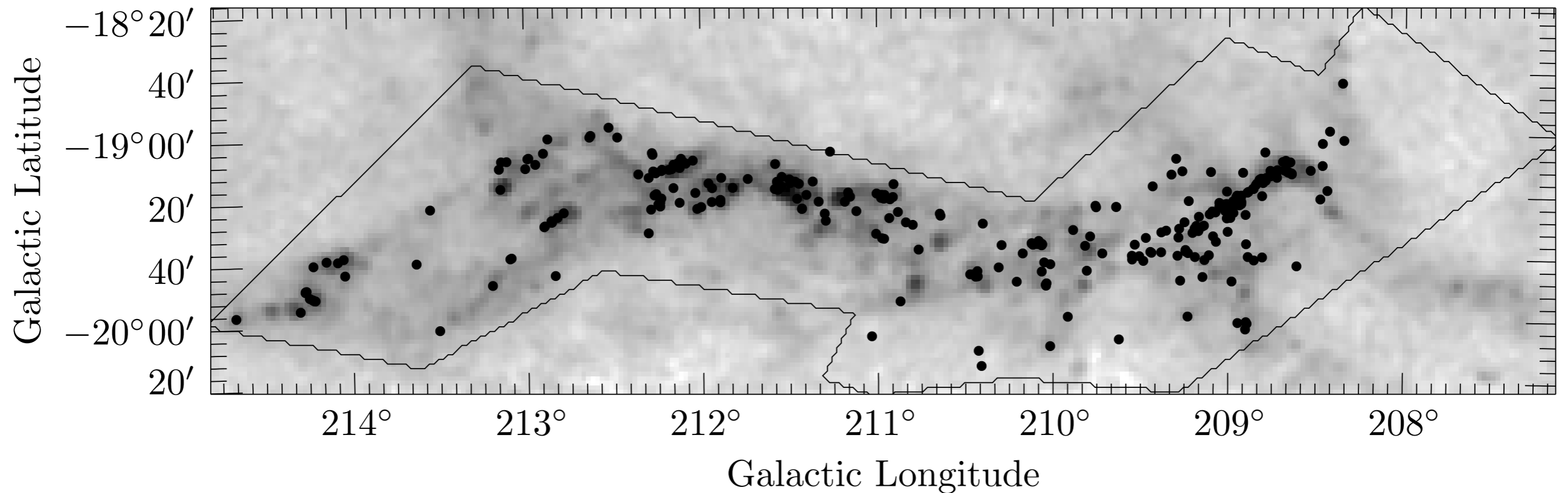
- Density of protostars: $\Sigma_{\star}(x) = \kappa [A_K(x)]^{\beta}$
- Include other possible effects:
 - A **threshold**: $\Sigma_{\star}(x) = 0$ if $A_K(x) < A_0$
 - The **diffusion** of the stars from the cloud (σ)
 - [**Contamination** by spurious sources...]

The local Schmidt law

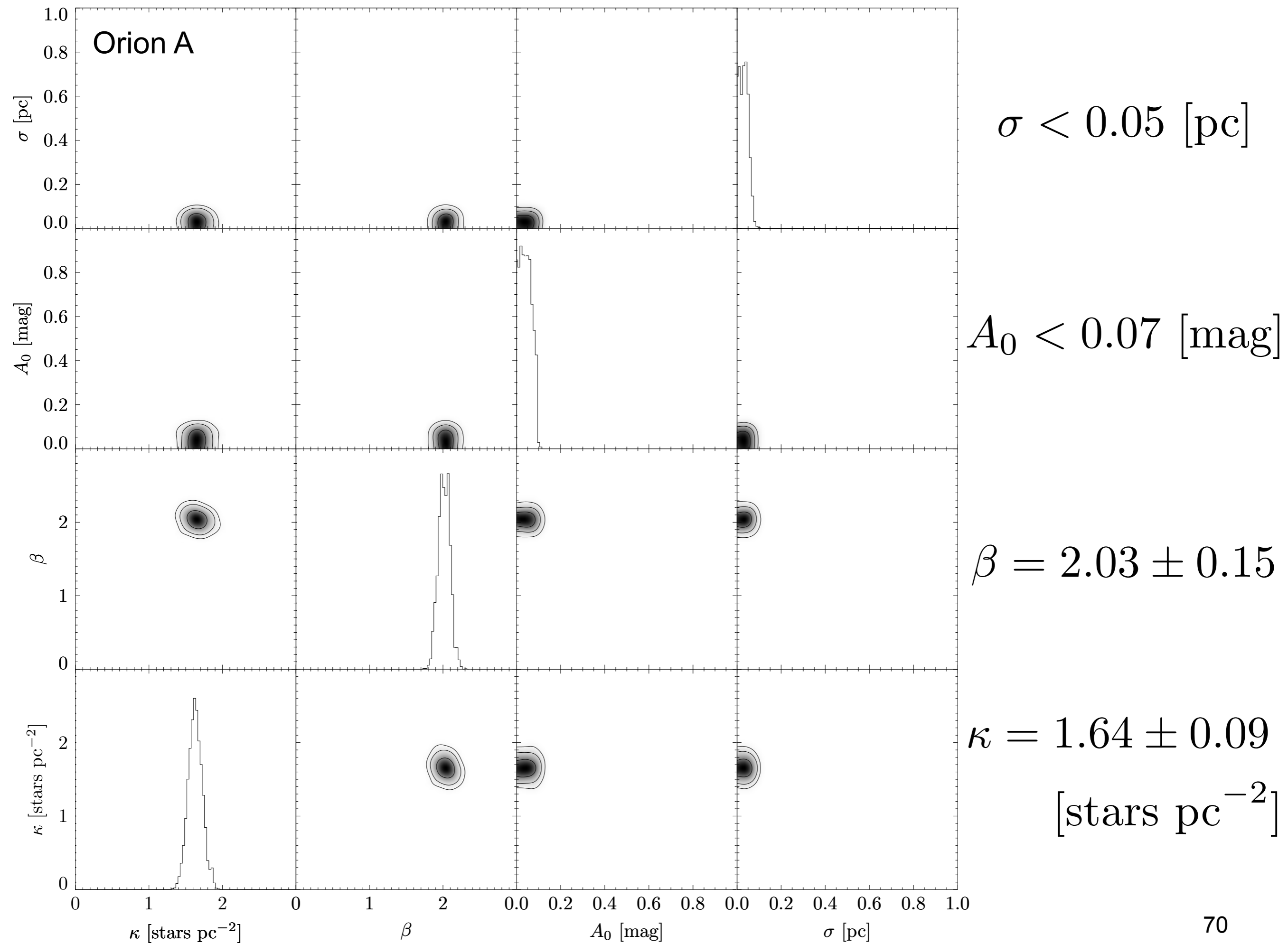
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- Data: **2MASS/Nicer** extinction maps and **Spitzer** catalogues of YSOs

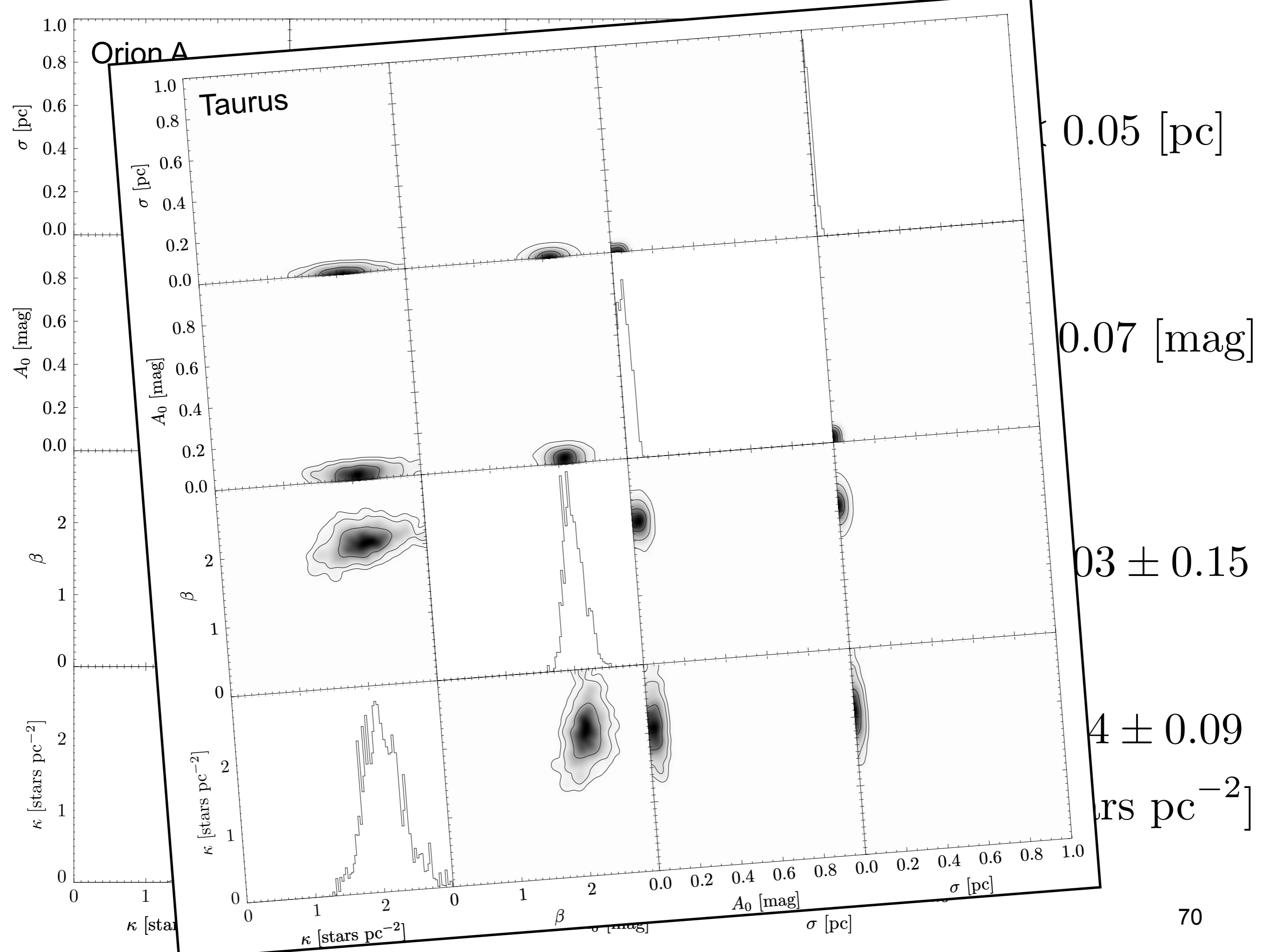
Orion A

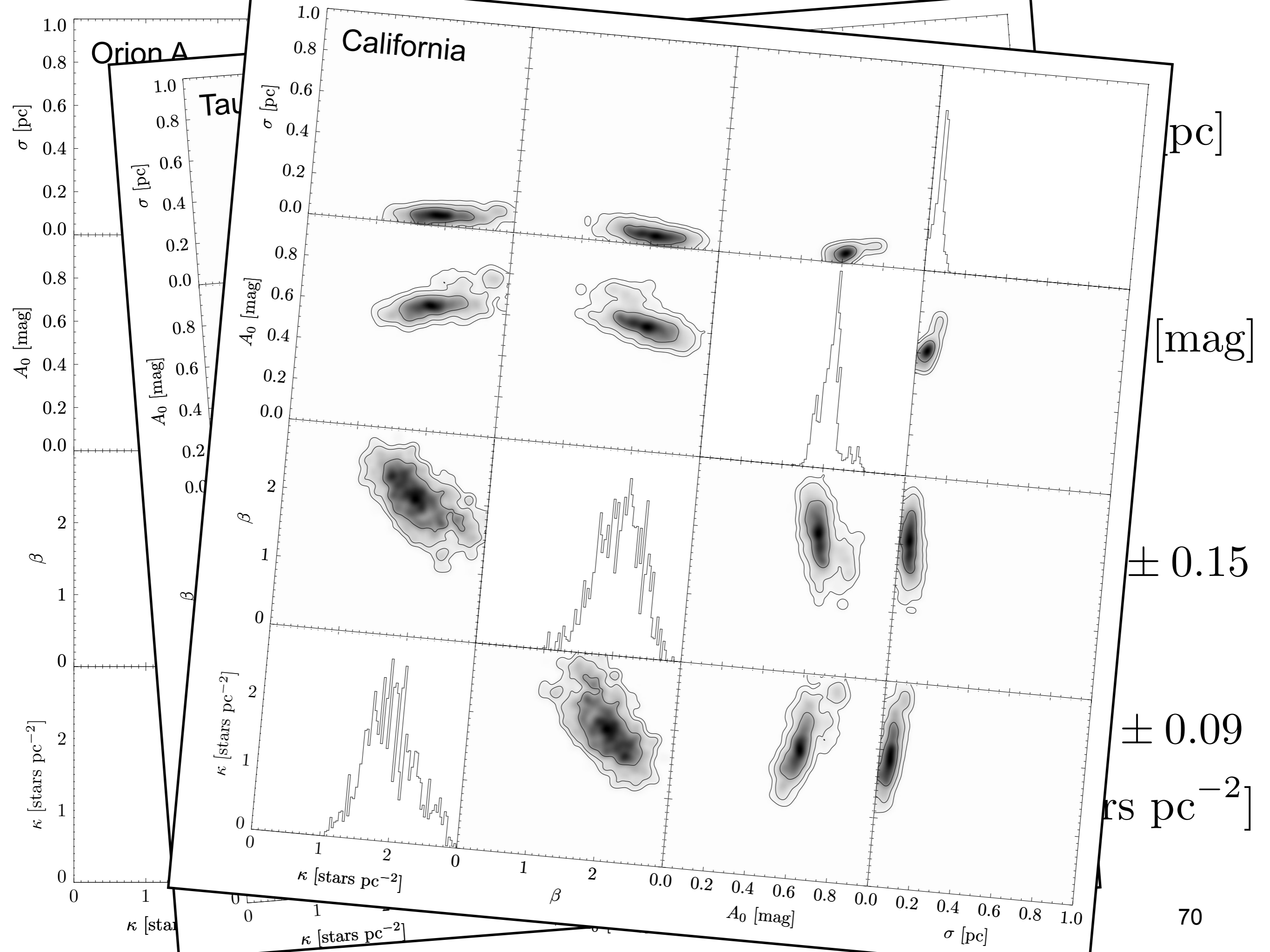
(Lombardi et al. 2011, Megeath et al. 2012)



- 329 Class I protostars in Orion A
- Posterior distribution sampled with MCMC
- Credible intervals inferred for 4 parameters







A consistent picture

- The local Schmidt law holds: $SFR \sim \Sigma^2$
- Clouds are self-similar **above a threshold**, with isothermal profiles $S(> \Sigma) \sim \Sigma^{-2}$
 - 3rd Larson's law holds: identical Σ above threshold
- Stars form in **dense regions** of molecular clouds
 - “protected” environment: cold gas, no UV radiation, Jeans/Bonnor-Ebert instability
 - SFR proportional to the amount of mass **above a (projected) density threshold**, $SFR \sim M_{\text{dense}}$





SUMMARY

1. Scaling laws are ubiquitous in molecular cloud physics (local Schmidt law, Larson's law, power-laws for PDFs)
2. Large differences in the properties of molecular clouds might be confined to the low-density, peripheral areas
3. Current observations show that clouds have self-similar structures