



***LWDM. Warm Dark Matter Galaxy  
Theory in Agreement with  
Observations.***

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# **Basement- ground Zero**

**Dark matter is the dominant component of Galaxies and is an essential ingredient to understand Galaxy properties and Galaxy formation**

**Dark matter and Galaxy Formation must be treated in an cosmological context**

**The nature (the type) of Dark Matter and the cosmological model need to be explicitated when discussing galaxies and galaxy formation**

**All the building of galaxy formation depends on the nature of Dark Matter**

# CONTENTS

**(I) The Standard Model of the Universe Includes Inflation**

**(II) THE NATURE OF DARK MATTER IN GALAXIES**

**from Theory and Observations: Warm (keV scale) DM**

**(III) NEW: THE ESSENTIAL ROLE OF QUANTUM PHYSICS IN WDM GALAXIES:**

**Semiclassical framework: Analytical Results and Numerical (including analytical) Results**

**Observed Galaxy cores and structures from Fermionic WDM and more results.**

**(IV) NEW: The generic Galaxy types and properties from a same physical framework: From quantum (compact, dwarfs) to classical (dilute, large) galaxies. Equation of state**

# HIGHLIGHTS

**(I)** The Effective (Ginsburg-Landau) Theory of Inflation

## PREDICTIONS :

**The Primordial Cosmic Banana: non-zero amount of primordial gravitons.** And Forecasts for CMB exps.

**(II) : TURNING POINT IN THE DARK MATTER PROBLEM: DARK MATTER IN GALAXIES** from Theory and Observations: **Warm (keV scale) dark matter**

**Physical Clarification and Simplification**

**GALAXY FORMATION AND EVOLUTION IN AGREEMENT WITH OBSERVATIONS**

**naturally re-insert in COSMOLOGY (LWDM)**

**Analytical Results and Numerical**

# NEW RESULTS

## FERMIONIC QUANTUM WDM and GRAVITATION DETERMINE THE OBSERVED PHYSICAL GALAXY PROPERTIES

- > Dark matter (DM) is the main component of galaxies. Quantum mechanics is a cornerstone of physics from microscopic to macroscopic systems as quantum liquids  $\text{He}^3$ , white dwarf stars and neutron stars.
- > **NEW:** Quantum mechanics is also responsible of galaxy structures at the kpc scales and below: near the galaxy center, below 10 - 100 pc, the DM quantum effects are important for warm DM (WDM), that is for DM particles with masses in the keV scale. **dVS (New Astronomy 2013)**  
**dVS PRD 2013, dVSS MNRAS to appear, dVS 2014**
- > **A new approach to galaxy structure with results in remarkable agreement with observations:**

**(i) Dwarf galaxies turn to be quantum macroscopic objects for WDM supported against gravity by the WDM fermion pressure**

**(ii) Theoretical analytic framework based on Thomas-Fermi approach determine galaxy structure from the most compact dwarf galaxies to the largest dilute galaxies (spirals, ellipticals).**

**The obtained galaxy mass, halo radius, phase-space density, velocity dispersion, are fully consistent with observations.**

**(iii) Interestingly enough, a minimal galaxy mass and minimal velocity dispersion are found for DM dominated objects, which in turn imply an universal minimal mass  $m_{\min} = 1.9 \text{ keV}$  for the WDM particle.**

- OBSERVED GALAXY CORES vs CDM CUSPS and WDM CORES-

- Astronomical observations show that the **DM galaxy density profiles are cored**, that is, profiles which are flat at the center.

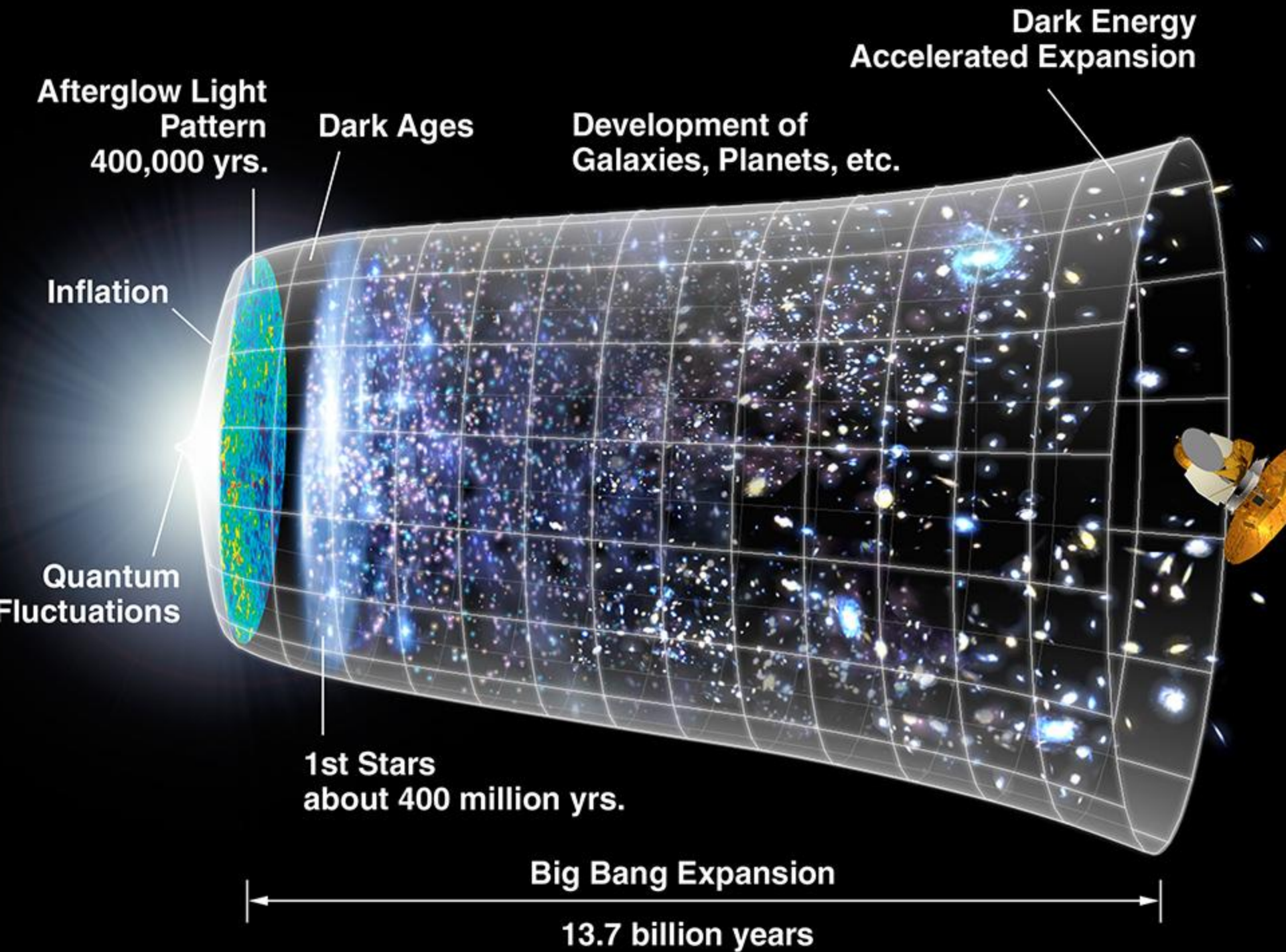
On the contrary, **N-body CDM simulations exhibit cusped density profiles**, with a typical  $1/r$  cusped behaviour near the galaxy center

$r = 0$ .

**Classical N-body WDM simulations** exhibit cores but with sizes much smaller than the observed cores.

We have recently developed a new approach to this problem thanks to **Quantum Mechanics**.

- **Fermions** always provide a non vanishing **pressure of quantum nature** due to the combined action of the Pauli exclusion principle and Heisenberg uncertainty principle.
- **Quantum effects for WDM fermions rule out the presence of galaxy cusps for WDM and enlarge the classical core sizes because their repulsive and non-local nature extend well beyond the small pc scales.**
- **Smoothing the density profile at the central regions has an effect on the whole galaxy halo.**





# From WMAP9 to Planck

Understanding the direction in which data are pointing:

- **PREDICTIONS for Planck**

- **Standard Model of the Universe**

- **Standard Single field Inflation**

- **NO RUNNING of the Primordial Spectral Index**

- **NO Primordial NON GAUSSIANTY**

- **$N_{\text{eff}}$  neutrinos : --> Besides meV active neutrinos:**

- **1 or 2 eV sterile neutrinos**

- **Would opens the sterile neutrino Family:**

- **keV sterile neutrino –WDM-**

## Sterile neutrinos and CMB fluctuations

CMB data give the **effective** number of neutrinos,  $N_{\text{eff}}$ .

$N_{\text{eff}}$  is related in a **subtle** way to the number of active neutrinos (3) plus the number of sterile neutrinos.

Planck result:  $N_{\text{eff}} = 3.5 \pm 0.5$  (95%; P+WP+highL+H<sub>0</sub>+BAO)

Entropy conservation determines the contributions to  $N_{\text{eff}}$ .

WDM sterile neutrino contribution at recombination

$$\Delta N^{WDM} = \left( \frac{T_d}{T_{rc}} \right)^4 = \left[ \frac{g_{rc}}{g(T_d)} \right]^{4/3}. \quad \text{At recombination } g_{rc} = 29/4.$$

WDM decouples early at  $T_d$  **beyond** the Fermi scale

The number of UR degrees of freedom at decoupling  $g(T_d)$  includes **all SM particles** and probably beyond.

$$g_{SM} = 427/4 \quad , \quad g_{MSSM} = 915/4,$$

$$\Delta N_{SM}^{WDM} = 0.02771 \dots \quad , \quad \Delta N_{MSSM}^{WDM} = 0.01003 \dots$$

**Too small** to be measurable at present !

**Conclusion:** Planck results say nothing about WDM.

Besides, Planck results are **compatible** with one or two eV sterile neutrinos (see e. g. G. Steigman, 1303.0049).

## Recent News on Cosmological Observables

**Before 2013:** Hubble constant  $H_0 = 73.8 \pm 2.4 \frac{\text{km}}{\text{s}} \frac{1}{\text{Mpc}}$  from direct observations of Cepheids by HST,  $\Omega_m = 0.27 \pm 0.03$ .  
A G Riess et al. ApJ 730, 119 (2011).

Planck 2013:  $H_0 = 67.3 \pm 1.2 \frac{\text{km}}{\text{s}} \frac{1}{\text{Mpc}}$ .  $\Omega_m = 0.32 \pm 0.02$ .

Planck **assumed** here only three massless neutrinos and **no sterile neutrinos**  $\nu_s$ .

There is today **strong evidence** for  $\nu_s$  with  $m_s \sim \text{eV}$  from short baseline experiments (reactors, MiniBoone, LSND).

Adding **one**  $\nu_s$  yields:

$H_0 = 70 \pm 1.2 \frac{\text{km}}{\text{s}} \frac{1}{\text{Mpc}}$ .  $\Omega_m = 0.30 \pm 0.01$  for  $m_s = 0.4 \text{ eV}$ .

These values for  $H_0$  and  $\Omega_m$  **are compatible** with the direct astronomical measurements.

M. Wyman et al. PRL. 112, 051302 (2014), J. Hamann & J. Hasekamp, JCAP,10,044H (2013) R. Battye & A. Moss, PRL. 112. 051303 (2014), S. Gariazzo et al. JHEP 1311

## Sterile Neutrinos $\nu$

Rhenium and Tritium **beta decay** (MARE, KATRIN).

Theoretical analysis: H J de V, O. Moreno, E. Moya de Guerra, M. Ramón Medrano, N. Sánchez, Nucl. Phys. B866, 177 (2013).

[Other possibility to detect a sterile  $\nu_s$ : a precise measure of nucleus recoil in tritium beta decay.]

**Conclusion: the empty slot** of right-handed neutrinos in the Standard Model of particle physics can be filled by **keV-scale sterile neutrinos** describing the DM.

An appealing **mass** neutrino hierarchy appears:

- Active neutrino:  $\sim$  mili eV
- Light sterile neutrino:  $\sim$  eV
- Dark Matter:  $\sim$  keV
- Unstable sterile neutrino:  $\sim$  MeV....

## Effective Theory of Inflation (ETI) confirmed by Planck

Quantity	ETI Prediction	Planck 2013
Spectral index $1 - n_s$	order $1/N = 0.02$	0.04
Running $dn_s/d\ln k$	order $1/N^2 = 0.0004$	$< 0.01$
Non-Gaussianity $f_{NL}$	order $1/N = 0.02$	$< 6$
	ETI + WMAP+LSS	
tensor/scalar ratio $r$	$r > 0.02$	$< 0.11$ see BICEP
inflaton potential curvature $V''(0)$	$V''(0) < 0$	$V''(0) < 0$

ETI + WMAP+LSS means the MCMC analysis combining the ETI with WMAP and LSS data. Such analysis calls for an inflaton potential with negative curvature at horizon exit. **The double well potential** is favoured (new inflation).

D. Boyanovsky, C. Destri, H. J. de Vega, N. G. Sanchez, arXiv:0901.0549, IJMPA 24, 3669-3864 (2009).

**Two key observable numbers :**  
**associated to the primordial density and**  
**primordial gravitons :**

$$n_s = 0.9608 , \quad r$$

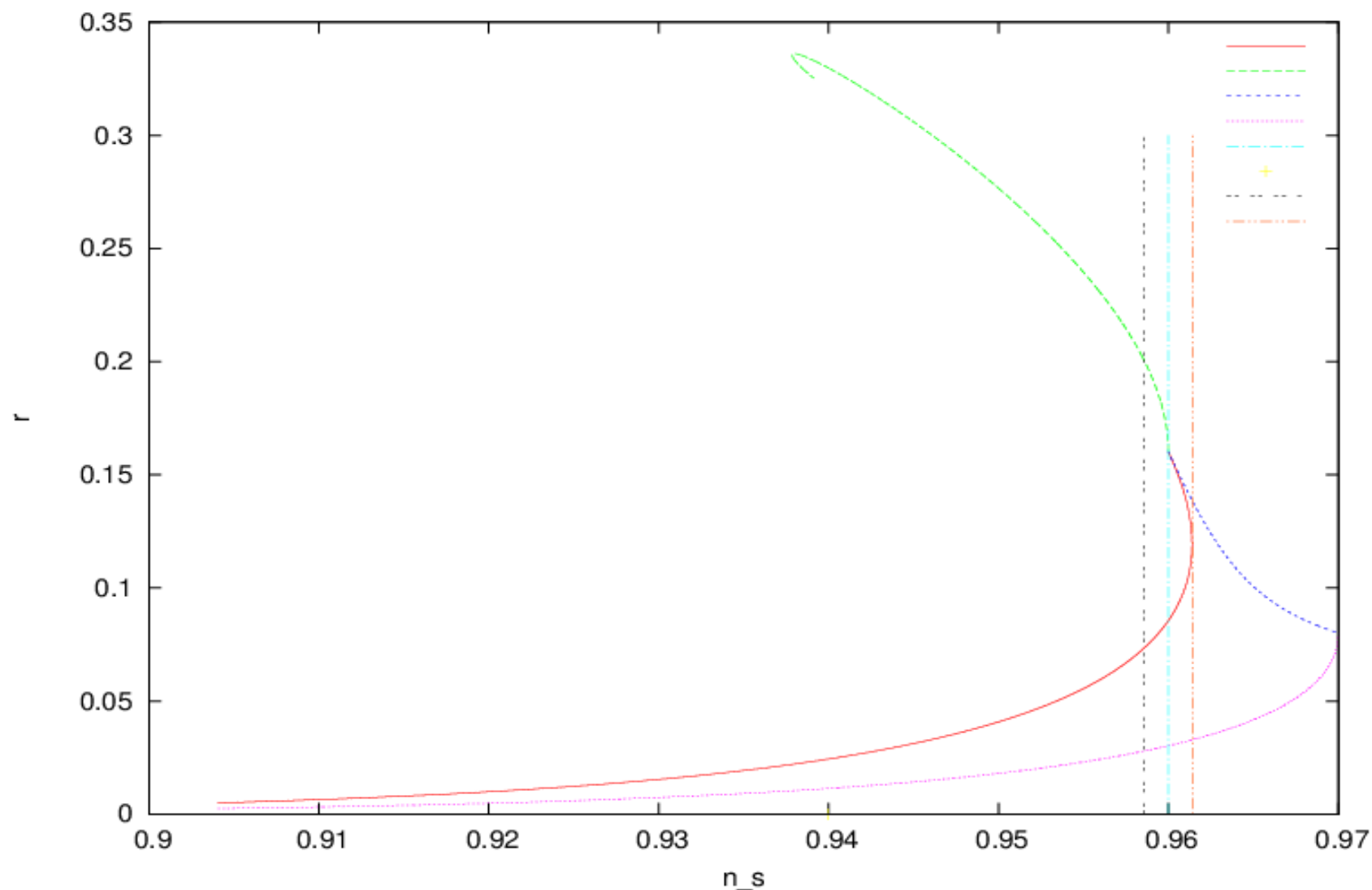
**PREDICTIONS**

$$r > 0.021$$

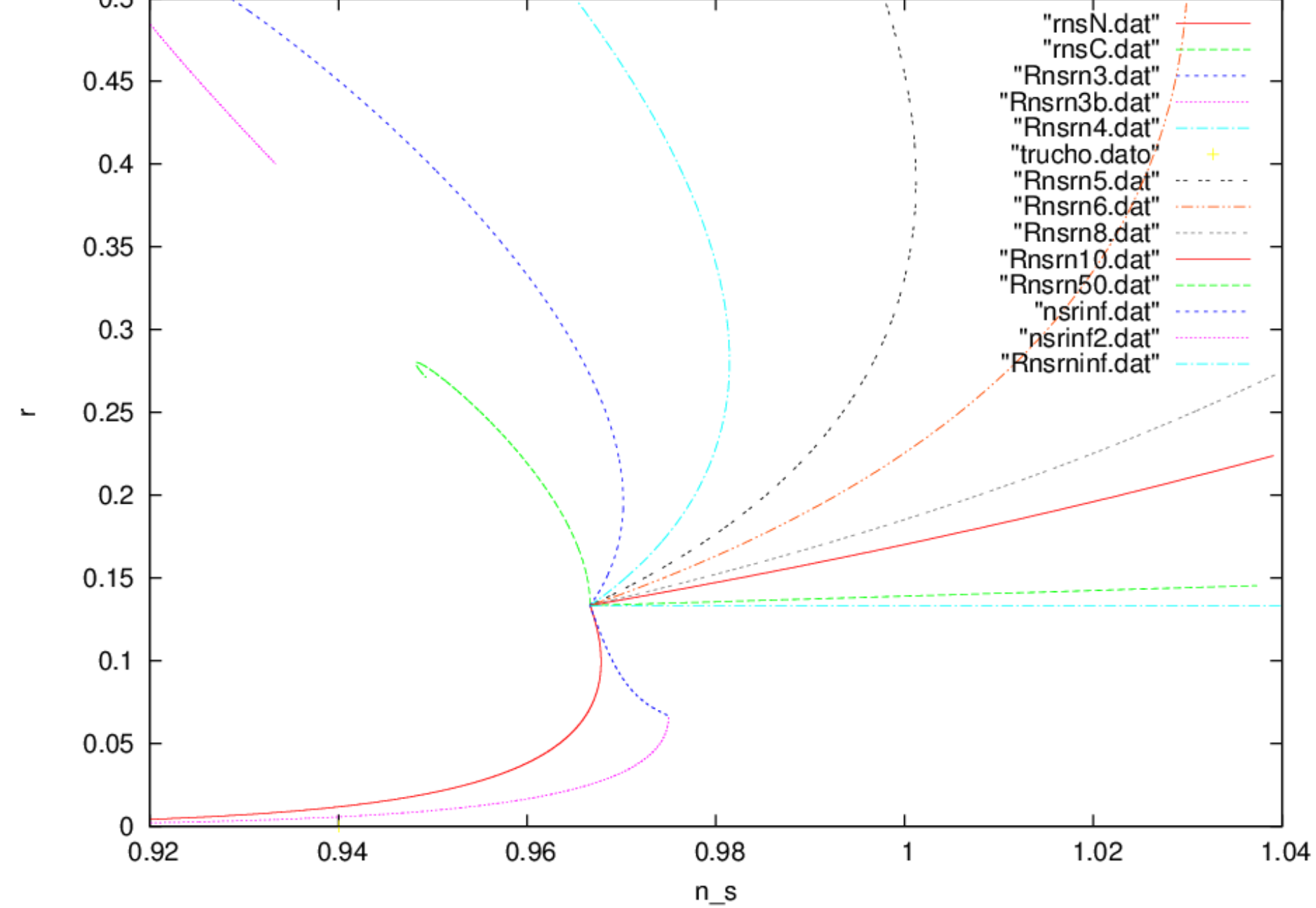
**DdS: Destri, de Vega, Sanchez & from WMAP data**  
**(PRD 2008)**

**BICEP2 result 2014:  $r$  about 0.20-0.16**

# Single and Double Well Inflaton Potentials



The **cosmic banana** for double well potentials ( $N=50$ ).  
 $n_s = 0.96 \pm 0.014$  Planck + BAO + sterile (Melchiorri et al.)





# The Energy Scale of Inflation

## Grand Unification Idea (GUT)

- Renormalization group running of electromagnetic, weak and strong couplings shows that they **all meet** at  $E_{GUT} \simeq 2 \times 10^{16}$  GeV
- Neutrino masses are explained by the **see-saw** mechanism:  $m_\nu \sim \frac{M_{\text{Fermi}}^2}{M_R}$  with  $M_R \sim 10^{16}$  GeV.
- Inflation energy scale:  $M \simeq 10^{16}$  GeV.

Conclusion: the GUT energy scale appears in at least **three** independent ways.

Moreover, moduli potentials:  $V_{\text{moduli}} = M_{\text{SUSY}}^4 v \left( \frac{\phi}{M_{\text{Pl}}} \right)$   
resemble inflation potentials provided  $M_{\text{SUSY}} \sim 10^{16}$  GeV.  
**First observation of SUSY in nature??**

# • Large Hadron Collider

- The first LHC results at 7-8 TeV, with the discovery of a candidate Higgs boson and **the non observation of new particles or exotic phenomena**, have made a big step towards completing **the experimental confirmation of the Standard Model of particle physics.**
- It is thus a good moment **to recall our scientific predictions made several years ago on this matter because they are of full actuality.**

# Large Hadron Collider - LHC-

The results are completely in line with  
the Standard Model.

**No evidence of SUSY at LHC**

*“Supersymmetry may not be dead but these latest results have certainly put it into hospital.”*

(Prof Chris Parkes, spokesperson for the UK Participation in the LHCb experiment)

**→ Does Not support wimps -CDM-**

*(In agreement with all dedicated wimp experiments at work from more than 20 years which have not found any*

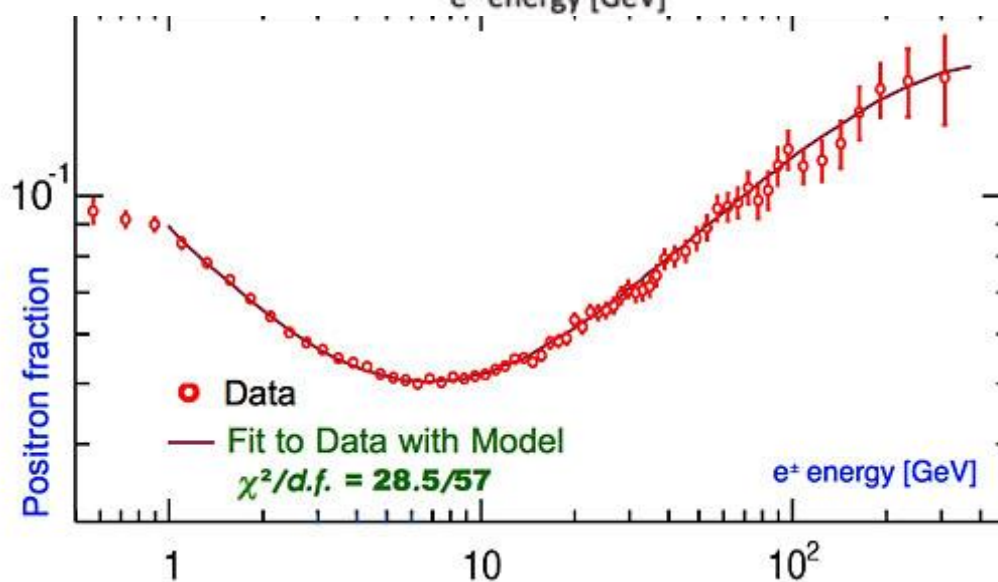
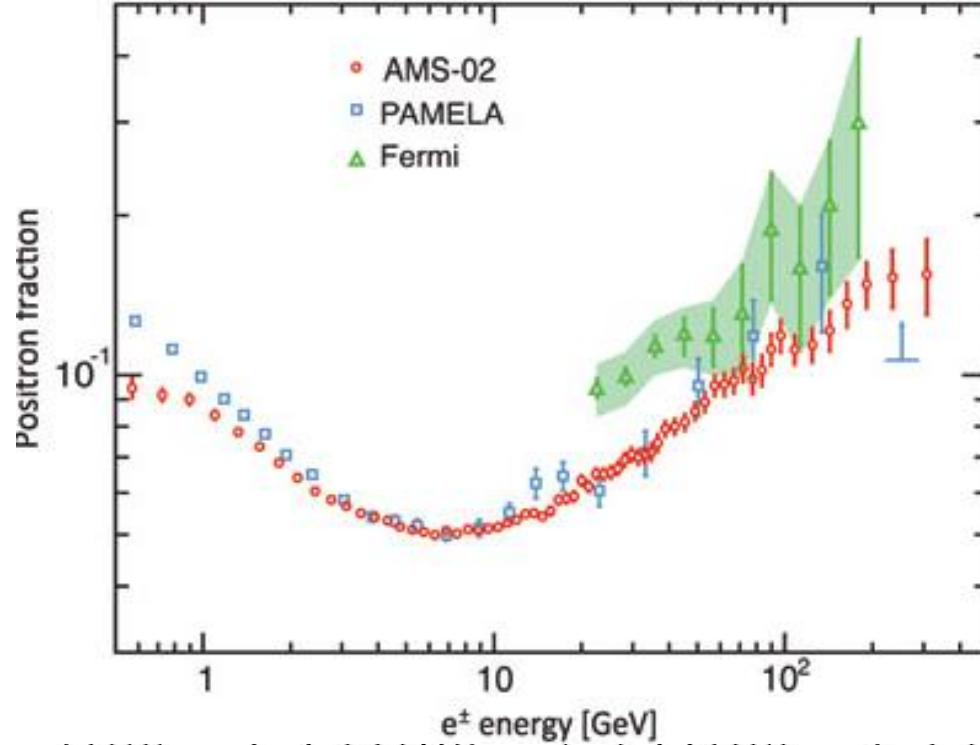
*wimp’s signal )* “So far researchers who are racing to find evidence of so called "new physics", ie non-standard models, have run into a series of dead ends”.

# ANTIMATTER IN SPACE - AMS on board ISS Alpha Magnet Spectrometer



NASA

NASA



**Positron excess in cosmic rays are not related to DM physics but to astrophysical sources and astrophysical mechanisms and can be explained by them**

- **Why No Experimental Detection of the DM particle has been reached so far ?**

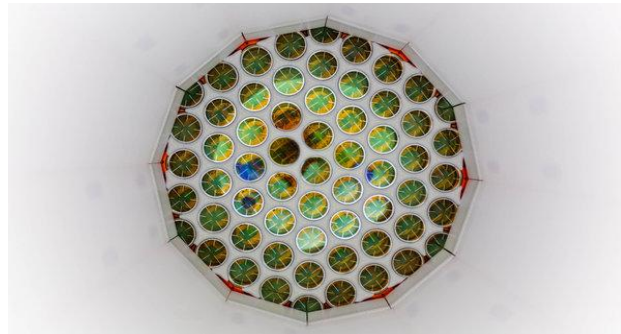
- **Because:**

- All experimental searches for DM particles are dedicated to CDM: wimps of  $m > 1 \text{ GeV}$ ,
- While the DM particle mass is in the keV scale .
- Moreover, past, present and future reports of signals of such CDM experiments **cannot be due to DM** because of the same reason.
- **The inconclusive signals in such experiments should be originated by phenomena of other kinds.**
- In addition, such signals contradict each other supporting the idea that they are **unrelated to any DM detection.**

# **LUX Large Underground Xenon Detector**

**30 October 2013**

**Dark Matter Experiment Has Detected Nothing,  
Researchers Say Proudly**



- **They found no sign of WIMPS signals.**  
beyond the expected background noise.
- The experiment did so at far better sensitivities than any such experiment before it.

## Direct searches of CDM particles

All direct searches of wimps look for  $m \gtrsim 1$  GeV.

Past, present and future reports of signals in such wimp experiments **cannot be due to DM detection** because the DM particle mass is in the keV scale.

The inconclusive signals in such experiments should be originated by **other kinds of phenomena**.

Contradictions between supposed detection signals in DAMA, CDMS-II, CoGeNT, CRESST, XENON100.

**CONCLUSION:** These signals are **unrelated to DM**.

$e^+$  and  $\bar{p}$  excess in cosmic rays reported by Pamela and Fermi may be explained by astrophysics: P. L. Biermann et al. PRL (2009), P. Blasi, P. D. Serpico PRL (2009).

AMS02: precise measure of the positron fraction in Galactic cosmic rays (CR) (PRL 2013) that increases with energy. Blum, Katz & Waxman (arXiv:1305.1324) show that this is consistent with positron production by the collision of high energy primary CR with the interstellar medium.



# Dark Matter Particles

DM particles decouple due to the universe expansion, their distribution function **freezes out** at decoupling.

The characteristic length scale is the **free streaming scale** (or Jeans' scale). For DM particles decoupling UR:

$$r_{Jeans} = 57.2 \text{ kpc} \frac{\text{keV}}{m} \left( \frac{100}{g_d} \right)^{\frac{1}{3}}, \text{ solving the linear Boltz-V eqs.}$$

$g_d$  = number of UR degrees of freedom at decoupling.

DM particles can **freely** propagate over distances of the order of the free streaming scale.

Therefore, structures at scales smaller or of the order of  $r_{Jeans}$  are **erased**.

The size of the DM galaxy cores is in the  $\sim 50$  kpc scale  $\Rightarrow m$  should be in the keV scale (WDM particles).

For neutrinos  $m \sim \text{eV}$  HDM particles

$r_{Jeans} \sim 60 \text{ Mpc} \Rightarrow$  **NO GALAXIES FORMED.**

## The Free Streaming Scale

The characteristic length scale is the **free streaming scale** (or Jeans' scale)

$$r_{lin} = 2 \sqrt{1 + z_{eq}} \left( \frac{3 M_{Pl}^2}{H_0 \sqrt{\Omega_{DM}} Q_{prim}} \right)^{\frac{1}{3}} = 21.1 q_p^{-\frac{1}{3}} \text{ kpc}$$

$q_p \equiv Q_{prim}/(\text{keV})^4$ . DM particles can **freely** propagate over distances of the order of the free streaming scale.

$$r_{lin} = 57.2 \text{ kpc} \frac{\text{keV}}{m} \left( \frac{100}{g_d} \right)^{\frac{1}{3}}$$

Therefore, structures at scales smaller or of the order  $r_{lin}$  are **erased**.

It is useful to introduce the dimensionless wavenumbers:

$$\gamma \equiv k r_{lin} / \sqrt{3} \quad \text{and} \quad \alpha \equiv \sqrt{3} \gamma / \sqrt{I_4}$$

where  $I_4$  is the second momentum of the DM zeroth order distribution.

## WDM properties

WDM is characterized by

- its initial power spectrum cutted off for scales below  $\sim 50$  kpc. Thus, structures are not formed in WDM for scales below  $\sim 50$  kpc.
- its initial velocity dispersion. However, this is negligible for  $z < 20$  where the non-linear regime starts.
- Classical  $N$ -body simulations **break down** at small distances ( $\sim$  pc). Need of **quantum** calculations to find WDM cores.

Structure formation is hierarchical in CDM.

WDM simulations show in addition top-hat structure formation at large scales and low densities but **hierarchical** structure formation remains **dominant**.

## Sterile neutrino models

- DW: Dodelson-Widrow model (1994) sterile neutrinos produced by non-resonant mixing from active neutrinos.
- Shi-Fuller model (1998) sterile neutrinos produced by resonant mixing from active neutrinos.
- $\nu$ -MSM model (1981)-(2006) sterile neutrinos produced by a Yukawa coupling from a real scalar  $\chi$ .
- DM models must reproduce  $\bar{\rho}_{DM}$ , galaxy and structure formation and be consistent with particle experiments.

WDM particles in different models behave just as if their masses were different (FD = thermal fermions):

$$\frac{m_{DW}}{\text{keV}} \simeq 2.85 \left(\frac{m_{FD}}{\text{keV}}\right)^{\frac{4}{3}}, \quad m_{SF} \simeq 2.55 m_{FD}, \quad m_{\nu\text{MSM}} \simeq 1.9 m_{FD}.$$

H J de Vega, N Sanchez,

Phys. Rev. D85, 043516 and 043517 (2012).

# Structure Formation in the Universe

Structures in the Universe as galaxies and cluster of galaxies form out of the **small primordial quantum fluctuations** originated by inflation just after the big-bang.

These linear small primordial fluctuations **grow** due to gravitational unstabilities (Jeans) and then classicalize.

Structures form through non-linear gravitational evolution.

Hierarchical formation starts from small scales first.

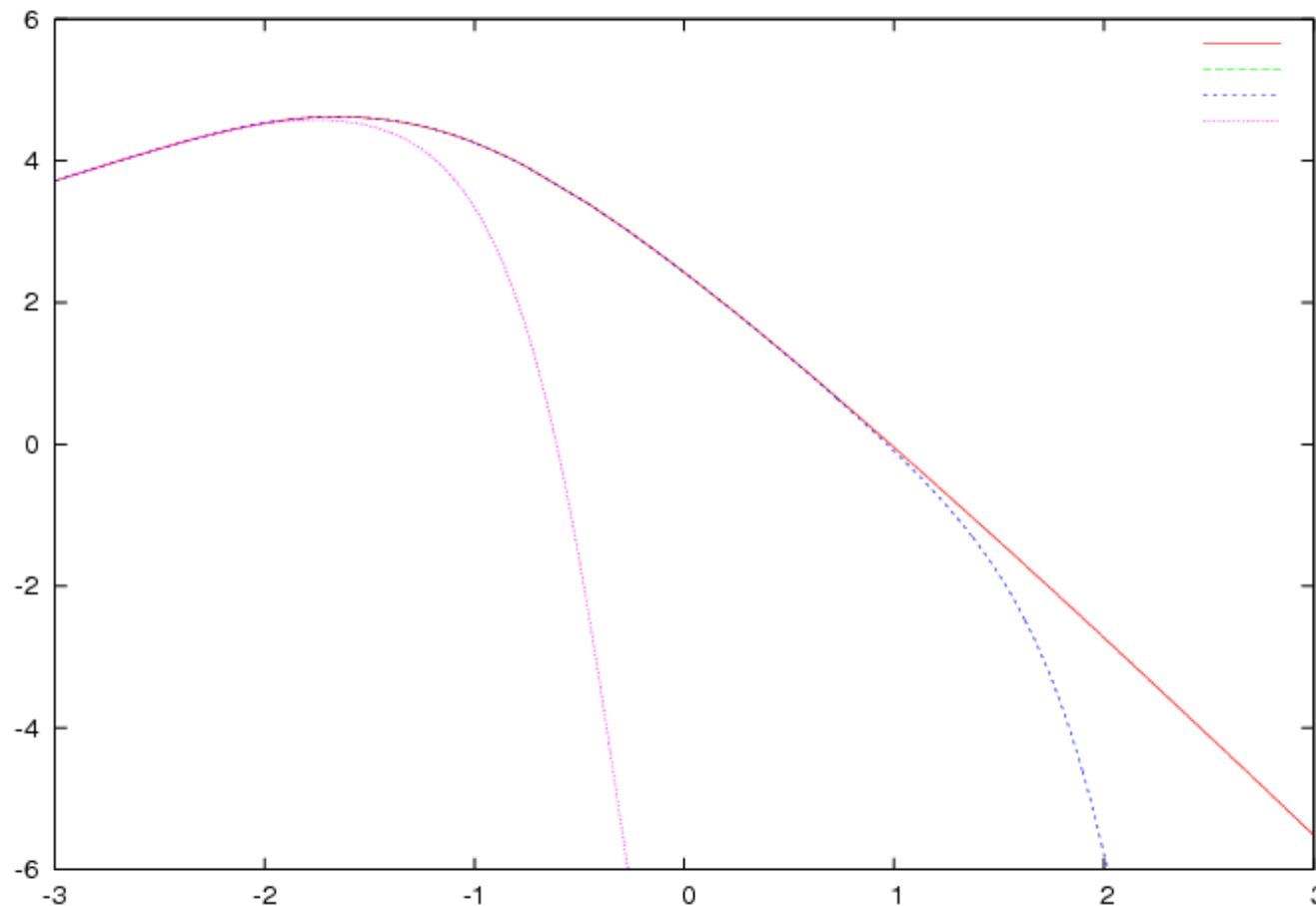
$N$ -body CDM simulations **fail** to produce the observed structures for **small** scales less than some kpc.

Both  $N$ -body WDM and CDM simulations yield **identical and correct** structures for scales larger than some kpc.

WDM predicts **correct structures for small scales** (below kpc) when its **quantum** nature is taken into account.

Primordial power  $P(k)$ : first ingredient in galaxy formation.

# Linear primordial power today $P(k)$ vs. $k$ Mpc $h$

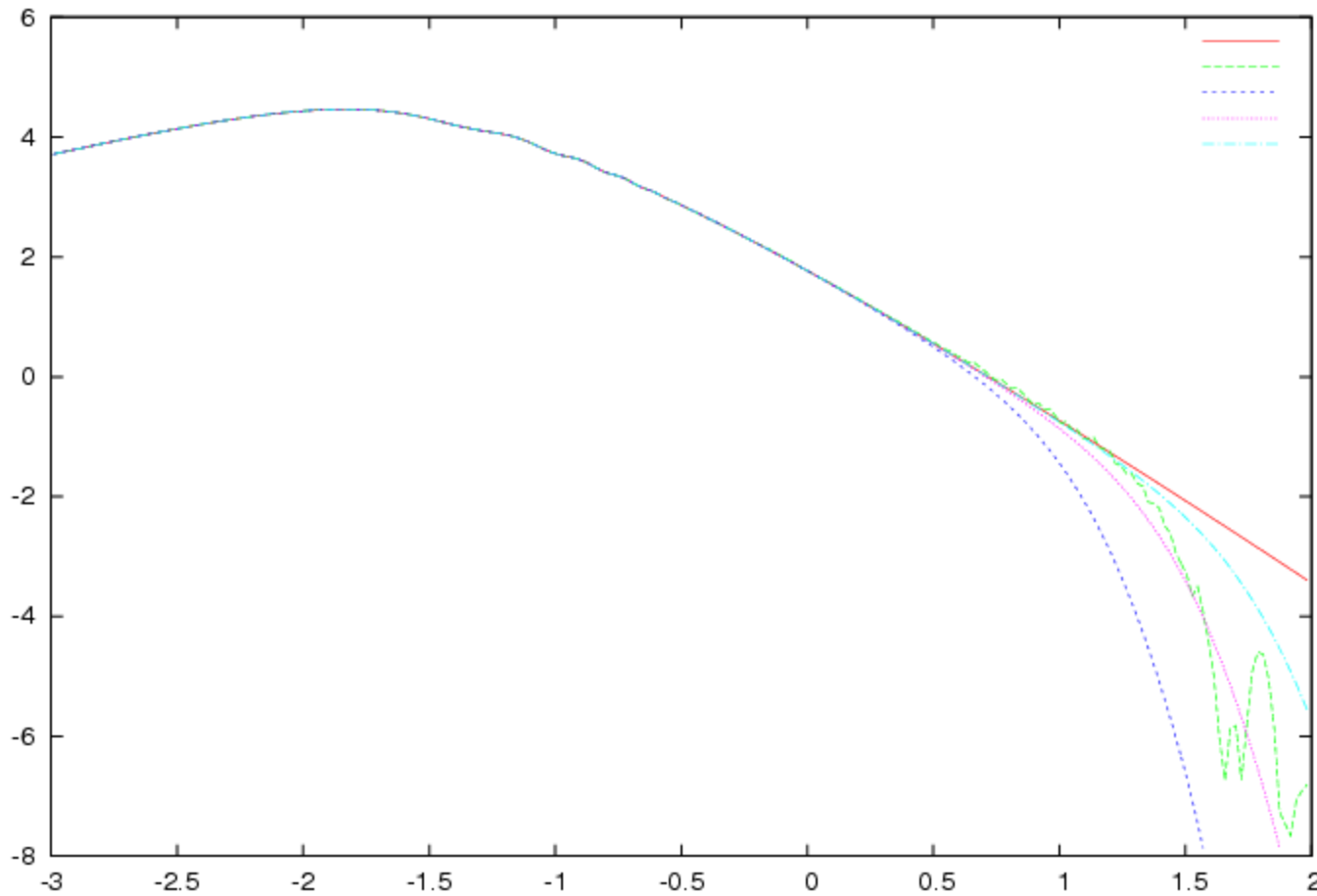


$\log_{10} P(k)$  vs.  $\log_{10}[k \text{ Mpc } h]$  for **WIMPS**, **1 keV** DM particles and **10 eV** DM particles.  $P(k) = P_0 k^{n_s} T^2(k)$ .

$P(k)$  cutted for **1 keV** DM particles on scales  $\lesssim 100$  kpc.

Transfer function in the MD era from Gilbert integral eq

# Linear primordial power today $P(k)$ vs. $k$ Mpc $h$



$\log_{10} P(k)$  vs.  $\log_{10}[k \text{ Mpc } h]$  for **CDM**, **1 keV**, **2 keV**,  
light-blue 4 keV DM particles decoupling in equil, and 1  
keV **sterile neutrinos**. WDM cuts  $P(k)$  on small scales  
 $r \lesssim 100 (\text{keV}/m)^{4/3} \text{ kpc}$ . CDM and WDM identical for CMB.

## WDM Primordial Power Spectrum

The WDM Primordial Power Spectrum is obtained solving the linear Boltzmann-Vlasov equations.

We define the transfer function ratio  $T^2(k) \equiv \frac{\Delta_{wdm}^2(k)}{\Delta_{cdm}^2(k)}$

Reproduced by the analytic formula  $T^2(k) = \left[1 + \left(\frac{k}{\kappa}\right)^a\right]^{-b}$

$a$  and  $b$  are independent of the WDM particle mass  $m$ .

$\kappa$  scales with  $m$ . In our best fit:

$$a = 2.304, \quad b = 4.478, \quad \kappa = 14.6 (m_{FD}/\text{keV})^{1.12} h/\text{Mpc}$$

At the wavenumber  $k_{1/2}$ :  $T^2(k_{1/2}) = 1/2$  and

$$k_{1/2} = 6.72 (m_{FD}/\text{keV})^{1.12} h/\text{Mpc}$$

The characteristic length scale is

$$l_{1/2} = 1/k_{1/2} = 207 \text{ kpc} (\text{keV}/m_{FD})^{1.12}$$

This scale reproduces the sizes of the DM galaxy cores when the WDM mass is in the **keV scale** !!



# The Mass function

The differential mass function gives the number of isolated bounded structures with mass between  $M$  and  $M + dM$ :  
(Press-Schechter)

$$\frac{dN}{dM} = -\frac{2 \delta_c}{\sqrt{2 \pi} \sigma^2(M, z)} \frac{\rho_M(z)}{M^2} \frac{d\sigma(M, z)}{d \ln M} e^{-\delta_c^2 / [2 \sigma^2(M, z)]},$$

$\delta_c = 1.686 \dots$ : linear estimate for collapse from the spherical model.

$\sigma(M, z)$  is **constant** for WDM for small scales: small objects (galaxies) formation is **suppressed** in WDM in comparison with CDM.

$$\sigma(M, z) = \frac{g(z)}{z+1} \sigma(M, 0)$$

$g(z)$ : takes into account the effect of the cosmological constant,  $g(0) = 0.76$ ,  $g(\infty) = 1$

## Relative overdensity $D(R)$ and Press-Schechter approach

The number of isolated bounded structures with mass between  $M$  and  $M + dM$ : (Press-Schechter)

$$\frac{dN}{dM} = -\frac{2 \delta_c}{\sqrt{2\pi} \sigma^2(M,z)} \frac{\rho_M(z)}{M^2} \frac{d\sigma(M,z)}{d \ln M} e^{-\delta_c^2/[2\sigma^2(M,z)]}, \quad \delta_c = 1.686 \dots$$

$\sigma(M, z)$  is **constant** for WDM for small scales: small objects formation is **suppressed** in WDM in comparison with CDM.

Computing  $dN/dM$  in WDM shows that small scale structure **suppression** with respect to CDM **increases** with  $z$ .  
H. J. de Vega, N. G. Sanchez, arXiv:1308.1109, Phys.Rev.D

It is therefore **important** to compare the observations at  $z > 1$  with the theoretical predictions:

Menci et al. ApJ 2013, Nierenberg et al. ApJ 2013,

**Conclusion:** WDM **reproduces** the observed small scale structures **better** than CDM for redshifts up to eight where observations are available.

## Redshift dependence and Relative overdensity $D(R)$

$\sigma(M, z) = \frac{g(z)}{z+1} \sigma(M, 0)$  during the MD/ $\Lambda$  dominated era.

$g(z)$ : the effect of the cosmological constant.  $g(z)$  is a hypergeometric function  ${}_2F_1$ ,  $g(0) = 0.76$ ,  $g(\infty) = 1$

We introduce the **relative overdensity**:  $D(R) \equiv \frac{\sigma_{WDM}^2(R, z)}{\sigma_{CDM}^2(R, z)}$   
( $z$  dependence cancels out).

Characteristic scale below which structures are suppressed in WDM compared with CDM:  $R_{1/2}$  where  $D(R_{1/2}) = 1/2$ ,

$$R_{1/2} = 73.1 \frac{\text{kpc}}{h} \left( \frac{\text{keV}}{m_{FD}} \right)^{1.45}$$

$D(R)$  can be reproduced by the simple formula:

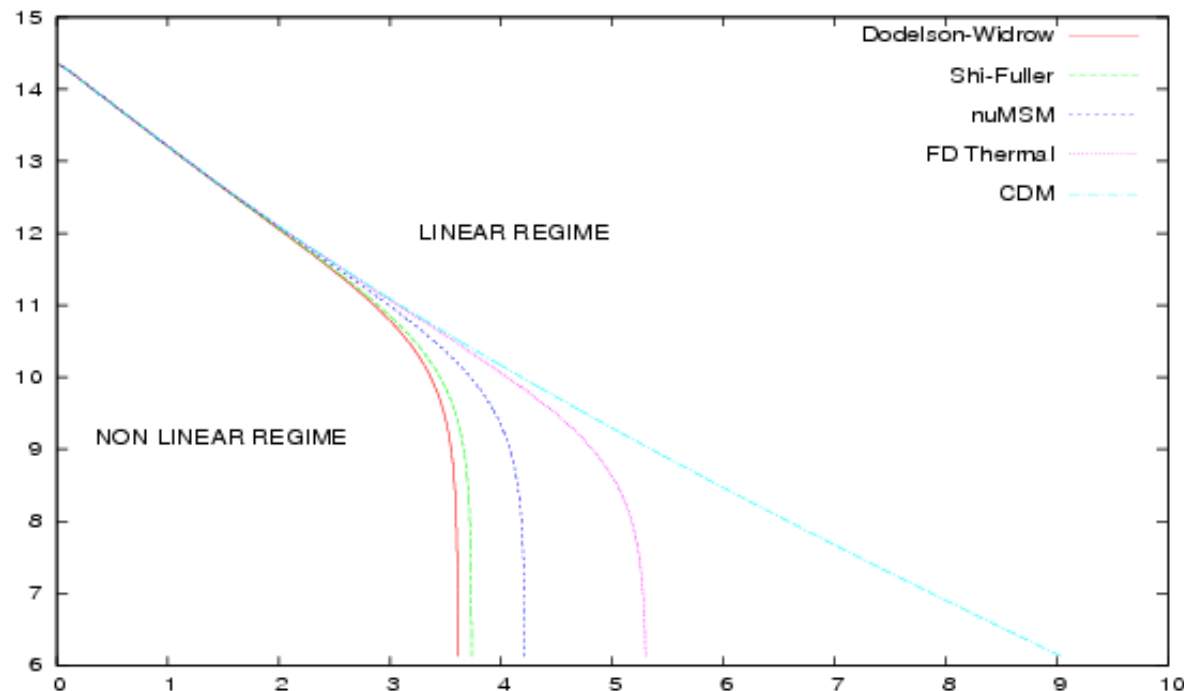
$$D(R) = \left[ 1 + \left( 2^{1/\beta} - 1 \right) \left( \frac{R_{1/2}}{R} \right)^\alpha \right]^{-\beta}$$

$$\alpha \simeq 2.2 \quad , \quad \beta \simeq 0.17 \quad , \quad 2^{1/\beta} - 1 \simeq 58$$

## Linear and non-linear regimes in $z$ and $R$

$\sigma^2(R, z) \sim 1$ : borderline between linear and non-linear regimes. Objects (galaxies) of scale  $R$  and mass  $\sim R^3$  start to form when this scale becomes non-linear.

**Smaller** objects can form **earlier**.



$\sigma^2(M, z) = 1$  in the  $z, \log[h M/M_\odot]$  plane for  $m = 2.5$  keV in four different WDM models and in CDM.

# The constant surface density in DM and luminous galaxy

The Surface density for dark matter (DM) halos and for luminous matter galaxies defined as:  $\mu_{0D} \equiv r_0 \rho_0$ ,

$r_0$  = halo core radius,  $\rho_0$  = central density for DM galaxies

$$\mu_{0D} \simeq 120 \frac{M_{\odot}}{\text{pc}^2} = 5500 (\text{MeV})^3 = (17.6 \text{ MeV})^3$$

5 kpc  $< r_0 < 100$  kpc. For luminous galaxies  $\rho_0 = \rho(r_0)$ .  
Donato et al. 09, Gentile et al. 09. [ $\mu_{0D} = g$  in the surface].

**Universal value** for  $\mu_{0D}$ : **independent** of galaxy luminosity for a large number of galactic systems (spirals, dwarf irregular and spheroidals, elliptics) spanning over 14 magnitudes in luminosity and of different Hubble types.

**Similar** values  $\mu_{0D} \simeq 80 \frac{M_{\odot}}{\text{pc}^2}$  in interstellar molecular clouds of size  $r_0$  of different type and composition over scales  $0.001 \text{ pc} < r_0 < 100 \text{ pc}$  (Larson laws, 1981).

## The Phase-space density $Q = \rho/\sigma^3$ and its decrease factor

The phase-space density **today**  $Q_{today}$  follows observing dwarf spheroidal satellite galaxies of the Milky Way (dSphs) as well as spiral galaxies. Its value is galaxy dependent.

For dSphs  $Q_{today} \sim 5000 (0.18 \text{ keV})^4$  Gilmore et al. 07/08.

During structure formation  $Q$  **decreases** by a factor that we call  $Z$ , ( $Z > 1$ ) :  $Q_{today} = \frac{1}{Z} Q_{prim}$

The spherical model gives  $Z \simeq 41000$  and  $N$ -body simulations indicate:  $10000 > Z > 1$ .  $Z$  is **galaxy dependent**.

As a consequence  $m$  is in the **keV scale**:  
 $1 \text{ keV} \lesssim m \lesssim 10 \text{ keV}$ .

This is true both for DM decoupling in or out of equilibrium, bosons or fermions.

It is **independent of the particle physics** model.

# WARM DARK MATTER REPRODUCE

→ OBSERVED GALAXY DENSITIES  
AND VELOCITY DISPERSIONS

→ SOLVES the OVERABUNDANCE (“satellite”) PROBLEM

-> OBSERVED SURFACE DENSITY VALUES OF DARK MATTER DOMINATED GALAXIES

→ OBSERVED GALAXY  
CORED DENSITY PROFILES : QUANTUM  
MECHANICS

# Galaxy Density Profiles: Cores vs. Cusps

Astronomical observations **always** find cored profiles for DM dominated galaxies. Selected references:

J. van Eymeren et al. A&A (2009), M. G. Walker, J. Peñarrubia, Ap J (2012). Reviews by de Blok (2010), Salucci & Frigerio Martins (2009).

Galaxy profiles in the **linear regime**: core size  $\sim$  free streaming length (de Vega, Salucci, Sanchez, 2010)=

$$\text{halo radius } r_0 = \begin{cases} 0.05 \text{ pc cusps for CDM (} m > \text{ GeV).} \\ 50 \text{ kpc cores for WDM (} m \sim \text{ keV).} \end{cases}$$

N-body simulations for CDM give **cusps** (NFW profile).

N-body simulations for WDM :

**quantum physics needed** for fermionic DM !!!

CDM simulations give a precise value for the concentration  $\equiv R_{\text{virial}}/r_0$ . CDM concentrations **disagree** with observed



# Quantum Bounds on Fermionic Dark Matter

The Pauli principle gives the **upper bound** to the phase space distribution function of spin- $\frac{1}{2}$  particles of mass  $m$ :

$$f(\vec{r}, \vec{p}) \leq 2$$

The DM mass density is given by:

$$\rho(\vec{r}) = m \int d^3 p \frac{f(\vec{r}, \vec{p})}{(2\pi\hbar)^3} = \frac{m^4}{2\hbar^3} \sigma^3(\vec{r}) \bar{f}(\vec{r}) K ,$$

where:

$\bar{f}(\vec{r})$  is the  $\vec{p}$ -average of  $f(\vec{r}, \vec{p})$  over a volume  $m^3 \sigma^3(\vec{r})$ ,

$\sigma(\vec{r})$  is the DM velocity dispersion,  $\sigma^2(\vec{r}) \equiv \langle v^2(\vec{r}) \rangle / 3$

$K \sim 1$  a pure number.

The Pauli bound  $\bar{f}(\vec{r}) \leq 2$  yields:  $Q(\vec{r}) \equiv \frac{\rho(\vec{r})}{\sigma^3(\vec{r})} \leq K \frac{m^4}{\hbar^3}$

This is an **absolute quantum upper bound** on  $Q(\vec{r})$  due to **quantum** physics, namely the Pauli principle.

$Q(\vec{r})$  can never take values larger than  $K m^4 / \hbar^3$ .

In the classical limit  $\hbar \rightarrow 0$  and the bound disappears.

# Classical physics breaks down near the galaxy center

$N$ -body simulations point to cuspy phase-space densities

$$Q(r) = Q_s \left( \frac{r}{r_s} \right)^{-\beta}, \quad \beta \simeq 1.9 - 2, \quad r_s = \text{halo radius},$$

$Q_s$  = mean phase space density in the halo.

$Q(r)$  derived within classical physics tends to infinity for  $r \rightarrow 0$  **violating** the Pauli principle bound.

Classical physics **breaks down** near the galaxy center.

For  $\beta = 2$  the quantum upper bound on  $Q(r)$  is valid for

$$r \geq r_q \equiv \frac{\hbar^{\frac{3}{2}}}{m^2} \sqrt{\frac{Q_s}{K}} r_s .$$

Observations yield:  $30 < \frac{r_s}{\text{pc}} < 5 \cdot 10^4$  ,  $2 \cdot 10^{-5} < \frac{\hbar^{\frac{3}{2}} \sqrt{Q_s}}{(\text{keV})^2} < 0.6$

The larger  $Q_s$  and the smaller  $r_s$  correspond to ultra compact dwarfs

The smaller  $Q_s$  and the larger  $r_s$  correspond to spirals.

# Dwarf galaxies as quantum objects

de Broglie wavelength of DM particles  $\lambda_{dB} = \frac{\hbar}{m \sigma}$

$d$  = mean distance between particles,

$\sigma$  = DM mean velocity

$$d = \left(\frac{m}{\rho}\right)^{\frac{1}{3}}, \quad Q = \rho/\sigma^3, \quad Q = \text{phase space density.}$$

ratio:  $\mathcal{R} = \frac{\lambda_{dB}}{d} = \hbar \left(\frac{Q}{m^4}\right)^{\frac{1}{3}}$

Observed values:  $2 \times 10^{-3} < \mathcal{R} \left(\frac{m}{\text{keV}}\right)^{\frac{1}{3}} < 1.4$

The **larger**  $\mathcal{R}$  is for ultracompact dwarfs.

The **smaller**  $\mathcal{R}$  is for big spirals.

$\mathcal{R}$  near unity (or above) means a **QUANTUM OBJECT**.

**Observations alone** show that compact dwarf galaxies are **quantum objects** (for WDM).

Galaxy	$\frac{r_h}{\text{pc}}$	$\frac{\sigma}{\frac{\text{km}}{\text{s}}}$	$\frac{h^{\frac{3}{2}} \sqrt{Q_h}}{(\text{keV})^2}$	$\rho(0) / \frac{M_{\odot}}{(\text{pc})^3}$	$\frac{M_h}{10^6 M_{\odot}}$
Willman 1	19	4	0.85	6.3	0.029
Segue 1	48	4	1.3	2.5	1.93
Leo IV	400	3.3	0.2	.19	200
Canis Venatici II	245	4.6	0.2	0.49	4.8
Coma-Berenices	123	4.6	0.42	2.09	0.14
Leo II	320	6.6	0.093	0.34	36.6
Leo T	170	7.8	0.12	0.79	12.9
Hercules	387	5.1	0.078	0.1	25.1
Carina	424	6.4	0.075	0.15	32.2
Ursa Major I	504	7.6	0.066	0.25	33.2
Draco	305	10.1	0.06	0.5	26.5
Leo I	518	9	0.048	0.22	96
Sculptor	480	9	0.05	0.25	78.8
Boötes I	362	9	0.058	0.38	43.2
Canis Venatici I	1220	7.6	0.037	0.08	344
Sextans	1290	7.1	0.021	0.02	116
Ursa Minor	750	11.5	0.028	0.16	193
Fornax	1730	10.7	0.016	0.053	1750
NGC 185	450	31	0.033	4.09	975
NGC 855	1063	58	0.01	2.64	8340
Small Spiral	5100	40.7	0.0018	0.029	6900
NGC 4478	1890	147	0.003	3.7	$6.55 \times 10^4$
Medium Spiral	$1.9 \times 10^4$	76.2	$3.7 \times 10^{-4}$	0.0076	$1.01 \times 10^5$
NGC 731	6160	163	$9.27 \times 10^{-4}$	0.47	$2.87 \times 10^5$
NGC 3853	5220	198	$8.8 \times 10^{-4}$	0.77	$2.87 \times 10^5$
NGC 499	7700	274	$5.9 \times 10^{-4}$	0.91	$1.09 \times 10^6$
Large Spiral	$5.9 \times 10^4$	125	$0.96 \times 10^{-4}$	$2.3 \times 10^{-3}$	$1. \times 10^6$

TABLE I: Observed values  $r_h$ ,  $\sigma$ ,  $\sqrt{Q_h}$ ,  $\rho(0)$  and  $M_h$  covering from ultracompact objects and

# Quantum pressure vs. gravitational pressure

**quantum** pressure:  $P_q = \text{flux of momentum} = n v p$ ,

$v = \text{mean velocity, momentum} = p \sim \hbar/\Delta x \sim \hbar n^{\frac{1}{3}}$ ,

particle number density  $= n = \frac{M_q}{\frac{4}{3} \pi R_q^3 m}$

galaxy mass  $= M_q$ , galaxy halo radius  $= R_q$

**gravitational** pressure:  $P_G = \frac{G M_q^2}{R_q^2} \times \frac{1}{4 \pi R_q^2}$

Equilibrium:  $P_q = P_G \implies$

$$R_q = \frac{3^{\frac{5}{3}}}{(4 \pi)^{\frac{2}{3}}} \frac{\hbar^2}{G m^{\frac{8}{3}} M_q^{\frac{1}{3}}} = 10.6 \dots \text{pc} \left( \frac{10^6 M_\odot}{M_q} \right)^{\frac{1}{3}} \left( \frac{\text{keV}}{m} \right)^{\frac{8}{3}}$$

$$v = \left( \frac{4 \pi}{81} \right)^{\frac{1}{3}} \frac{G}{\hbar} m^{\frac{4}{3}} M_q^{\frac{2}{3}} = 11.6 \frac{\text{km}}{\text{s}} \left( \frac{\text{keV}}{m} \right)^{\frac{4}{3}} \left( \frac{M_q}{10^6 M_\odot} \right)^{\frac{2}{3}}$$

for WDM the values of  $M_q$ ,  $R_q$  and  $v$  are **consistent with the dwarf galaxy observations !!**.

Dwarf spheroidal galaxies **can be supported** by the fermionic quantum pressure of WDM.

## In the presence of angular momentum $L$

**Adds** the centrifugal pressure:  $P_L = \frac{L^2}{M R^3} \frac{1}{4 \pi R^2}$

Equilibrium:  $P_q + P_L = P_G$ :

$$\left(\frac{3}{4 \pi}\right)^{5/3} \frac{\hbar^2 M^{5/3}}{m^{8/3} R^5} + \frac{L^2}{4 \pi M R^5} = \frac{G M^2}{4 \pi R^4}$$

$$\Rightarrow R = \frac{L^2}{G M^3} + \frac{3^{5/3}}{(4 \pi)^{2/3}} \frac{\hbar^2}{G m^{8/3} M^{1/3}} .$$

We estimate  $L^2$  as  $L^2 \sim \frac{1}{2} M^2 R^2 3 \sigma^2$ .

The  $\frac{1}{2}$  factor comes from averaging the  $\sin^2$  of the angle between the momentum  $\vec{p}$  and the particle position  $\vec{r}$ .

$$R = 10.6 \text{pc} \left(\frac{10^6 M_\odot}{M}\right)^{1/3} \left(\frac{\text{keV}}{m}\right)^{8/3} + 3.48 \text{pc} \frac{10^6 M_\odot}{M} \left(\frac{\sigma}{10 \frac{\text{km}}{\text{s}}}\right)^{1/2}$$

The angular momentum **increases** the size  $R$ .

For dwarf galaxies,  $R$  and  $\sigma$  have the **same** order of magnitude for  $L > 0$  and for  $L = 0$ .

# The quantum radius $r_q$ for different kinds of DM

DM type	DM particle mass	$r_q$	
$\Lambda$ CDM	1 – 100 GeV	$1 - 10^4$ meters	in practice zero
WDM	1 – 10 keV	0.1 – 1 pc	compatible with observed cores
HDM	1 – 10 eV	kpc - Mpc	too big !

## Self-gravitating Fermions in the Thomas-Fermi approach

WDM is non-relativistic in the MD era. A single DM halo in late stages of formation relaxes to a time-independent form especially in the interior.

Chemical potential:  $\mu(r) = \mu_0 - m \phi(r)$ ,  $\phi(r) = \text{grav. pot.}$

**Poisson's** equation:  $\frac{d^2 \mu}{dr^2} + \frac{2}{r} \frac{d\mu}{dr} = -4 \pi G m \rho(r)$

$\rho(0) = \text{finite for fermions} \implies \frac{d\mu}{dr}(0) = 0.$

Density  $\rho(r)$  and pressure  $P(r)$  in terms of the distribution function  $f(E)$ :

$$\rho(r) = \frac{m}{\pi^2 \hbar^3} \int_0^\infty p^2 dp f\left[\frac{p^2}{2m} - \mu(r)\right]$$

$$P(r) = \frac{1}{3 \pi^2 m \hbar^3} \int_0^\infty p^4 dp f\left[\frac{p^2}{2m} - \mu(r)\right]$$

These are **self-consistent** non-linear Thomas-Fermi equations that determine  $\mu(r)$ .



## WDM Thomas-Fermi equations

**Self-consistent** dimensionless Thomas-Fermi equation:

$$\frac{d^2 \nu}{d\xi^2} + \frac{2}{\xi} \frac{d\nu}{d\xi} + I_2(\nu) = 0 \quad , \quad \nu'(0) = 0$$

Core size  $r_h$  of the halo defined as for Burkert profile:

$$\frac{\rho(r_h)}{\rho_0} = \frac{1}{4} \quad , \quad r_h = l_0 \xi_h$$

Fermi-Dirac Phase-Space distribution function  $f(E/T_0)$ :

**Contrasting** the theoretical Thomas-Fermi solution with **galaxy data**,  $T_0$  turns to be  $10^{-3} \text{ }^\circ\text{K} < T_0 < 20 \text{ }^\circ\text{K}$

colder = **ultracompact**, warmer = **large spirals**.

$$T_0 \sim m \langle v^2 \rangle_{\text{observed}} \quad \text{for } m \sim 2 \text{ keV.}$$

All results are **independent** of any WDM particle physics model, they only follow from the **gravitational** interaction of the WDM particles and their **fermionic** nature.

# Thomas-Fermi approximation: solutions

$$M(R) = \frac{(3\pi)^2 \hbar^6}{256 G^3 m^8 R^3} \xi_0^5 |\nu'(\xi_0)|$$

$$P(r) = \frac{\pi^{4/3}}{3} \hbar^2 \left[ \frac{\rho(0)}{\beta(\xi_0) m^4} \right]^{5/3} \int_0^\infty y^4 dy \Psi(y^2 - \nu(\xi))$$

$L_0$  and  $M(R)$  turn to be of the order of the Jeans' length and the Jeans' mass, respectively.

The chemical potential at  $r = 0$  fixed by the value of  $Q(0)$ .

Using observed values of  $Q(0)$ , we obtain halo radius  $r_s \sim 0.1 - 10$  kpc, galaxy masses  $10^5 - 10^7 M_\odot$  and velocity dispersions, **all consistent** with the observations of dwarf galaxies.

The Thomas-Fermi approach gives **realistic halo radii**, larger than the quantum lower bound  $r_q$ , as expected.

Fermionic WDM **treated quantum mechanically is able to reproduce** the observed DM cores of galaxies.

we derive the local equation of state:

$$P(r) = \frac{1}{3} v^2(r) \rho(r) .$$

) the hydrostatic equilibrium equation

$$\frac{dP}{dr} + \rho(r) \frac{d\phi}{dr} = 0 .$$

ion of state generalizes the local perfect fluid equation of state for  $r$ -dependent velocity  $v(r)$ .  
 e perfect fluid equation of state is recovered both in the classical dilute limit and in the quan

$\rho(r)$  between eqs.(2.6) and (2.7) and integrating on  $r$  gives

$$\frac{\rho(r)}{\rho(0)} = \frac{v^2(0)}{v^2(r)} e^{-3 \int_0^r \frac{dr'}{v^2(r')} \frac{d\phi}{dr'}} .$$

) this relation reduces to the baryotropic equation. Inserting this expression for  $\rho(r)$  in the Poiss

$$\frac{d^2\phi}{dr^2} + \frac{2}{r} \frac{d\phi}{dr} = 4\pi G m \rho(0) \frac{v^2(0)}{v^2(r)} e^{-3 \int_0^r \frac{dr'}{v^2(r')} \frac{d\phi}{dr'}} .$$

equation generalizes the corresponding equation in the self-gravitating Boltzmann gas when  $v^2($

# Self-gravitating Fermions in the Thomas-Fermi approach

The Thomas-Fermi approach gives physical galaxy magnitudes: mass, halo radius, phase-space density and velocity dispersion **fully compatible** with observations from the largest spiral galaxies till the ultracompact dwarf galaxies for a WDM particle mass **around 2 keV**.

Compact dwarf galaxies are close to a degenerate WDM Fermi gas while large galaxies are classical WDM Boltzmann gases.

Fermionic WDM **treated quantum mechanically is able to reproduce** the observed galaxies.

C. Destri, H. J. de Vega, N. G. Sanchez,  
arXiv:1204.3090 to appear in New Astronomy.

'Quantum WDM fermions and gravitation determine the observed galaxy structures', arXiv:1301.1864.

# RESULTS

**All the obtained density profiles are cored.**

**The Core Sizes are in agreement with the observations**

**from the compact galaxies where  $r_h \sim 20$  pc till the spiral and elliptical galaxies where  $r_h \sim 0.2 - 60$  kpc.**

**The larger and positive is the chemical potential  $\nu(0)$ , the smaller is the core.**

**The minimal one arises in the degenerate case  $\nu(0) \rightarrow +\infty$   
(compact dwarf galaxies).**

**And**

**The Phase-space Density**

**The Galaxy halo Masses.**

**Agreement is found in all the range of galaxies  
for a DM particle mass  $m$  around 2 keV.**

**Error bars of the observational data are not shown but they are at least about 10-20 %.**

## Galaxy data vs. Thomas-Fermi

Mass, halo radius, velocity dispersion and central density from a broad variety of galaxies: ultracompact galaxies to giant spirals, Willman 1, Segue 1, Canis Venatici II, Coma-Berenices, Leo II, Leo T, Hercules, Carina, Ursa Major I, Draco, Leo I, Sculptor, Boötes, Canis Venatici I, Sextans, Ursa Minor, Fornax, NGC 185, NGC 855, NGC 4478, NGC 731, NGC 3853, NGC 499 and a large number of spiral galaxies.

Phase-Space distribution function  $f(E/E_0)$ : Fermi-Dirac ( $F(x) = \frac{1}{e^x + 1}$ ) and out of equilibrium sterile neutrinos give similar results.

$E_0$  = effective galaxy temperature (energy scale).

$E_0$  turns to be  $10^{-3} \text{ }^\circ\text{K} < E_0 < 50 \text{ }^\circ\text{K}$

colder = ultracompact, warmer = large spirals.

$E_0 \sim m \langle v^2 \rangle_{\text{observed}}$  for  $m \sim 2 \text{ keV}$ .

## Galaxy surface density

The surface density:  $\Sigma_0 \equiv r_h \rho_0 \simeq 120 M_\odot/\text{pc}^2$ ,

takes nearly the **same value** for galactic systems (spirals, dwarf irregular and spheroidals, elliptics) spanning over 14 magnitudes in luminosity and over different Hubble types.

We take  $\Sigma_0$  as physical scale to express the galaxy magnitudes in the Thomas-Fermi approach.

Dimensionless variables:  $\xi$ ,  $\nu(\xi)$ .

$$r = l_0 \xi \quad , \quad \mu(r) = T_0 \nu(\xi) \quad , \quad \rho_0 \equiv \rho(0).$$

$T_0$  = effective galaxy temperature,  $l_0$  characteristic length.

From the Thomas-Fermi equations:

$$l_0 \equiv \left(\frac{9\pi}{2^9}\right)^{\frac{1}{5}} \left(\frac{\hbar^6}{G^3 m^8}\right)^{\frac{1}{5}} \left[\frac{\xi_h I_2(\nu_0)}{\Sigma_0}\right]^{\frac{1}{5}} =$$
$$4.2557 [\xi_h I_2(\nu_0)]^{\frac{1}{5}} \left(\frac{2\text{keV}}{m}\right)^{\frac{8}{5}} \left(\frac{120 M_\odot}{\Sigma_0 \text{pc}^2}\right)^{\frac{1}{5}} \text{pc}$$

$$I_n(\nu) \equiv (n+1) \int_0^\infty y^n dy f(y^2 - \nu) \quad , \quad \nu_0 \equiv \nu(0)$$

## Lower bound on the particle mass $m$

In the **degenerate** quantum limit  $\nu_0 \rightarrow +\infty$ ,  $T_0 \rightarrow 0$  the galaxy mass and halo radius take their **minimum** values

$$r_h^{min} = 11.3794 \left(\frac{2 \text{ keV}}{m}\right)^{\frac{8}{5}} \left(\frac{120 M_\odot}{\Sigma_0 \text{ pc}^2}\right)^{\frac{1}{5}} \text{ pc}$$

$$M_h^{min} = 30998.7 \left(\frac{2 \text{ keV}}{m}\right)^{\frac{16}{5}} \left(\frac{\Sigma_0 \text{ pc}^2}{120 M_\odot}\right)^{\frac{3}{5}} M_\odot$$

Observed halo masses must be **larger or equal** than  $M_h^{min}$

From the minimum observed value of the halo mass  $M_h^{min}$  a **lower bound** for the WDM particle mass  $m$  follows

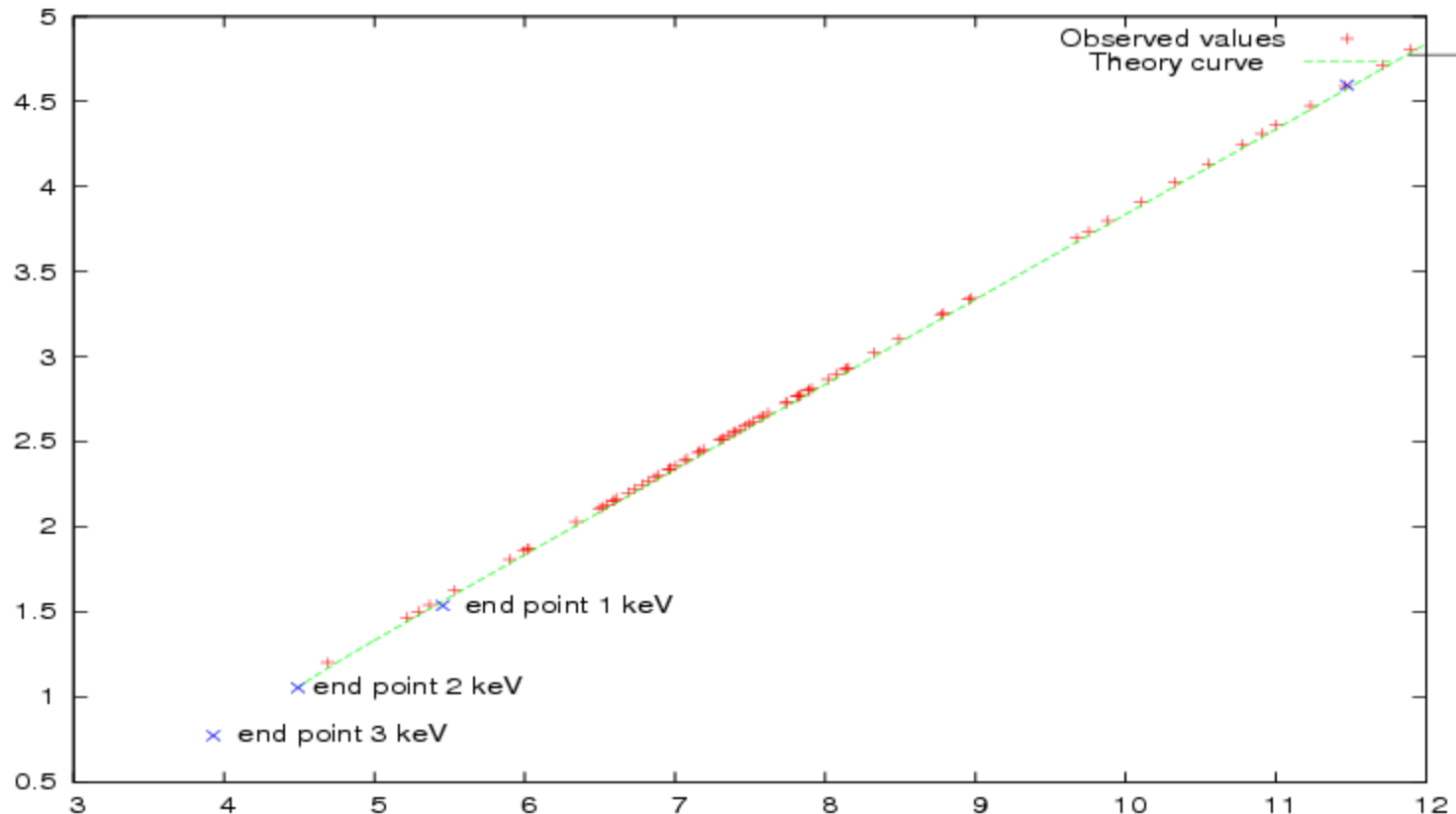
$$m \geq m_{min} \equiv 1.387 \text{ keV} \left(\frac{10^5 M_\odot}{M_h^{min}}\right)^{\frac{5}{16}} \left(\frac{\Sigma_0 \text{ pc}^2}{120 M_\odot}\right)^{\frac{3}{16}}$$

The minimal known halo mass is for Willman I:

$$M_{Willman I} = 3.9 \cdot 10^4 M_\odot \text{ which implies } m \geq 1.86 \text{ keV}$$

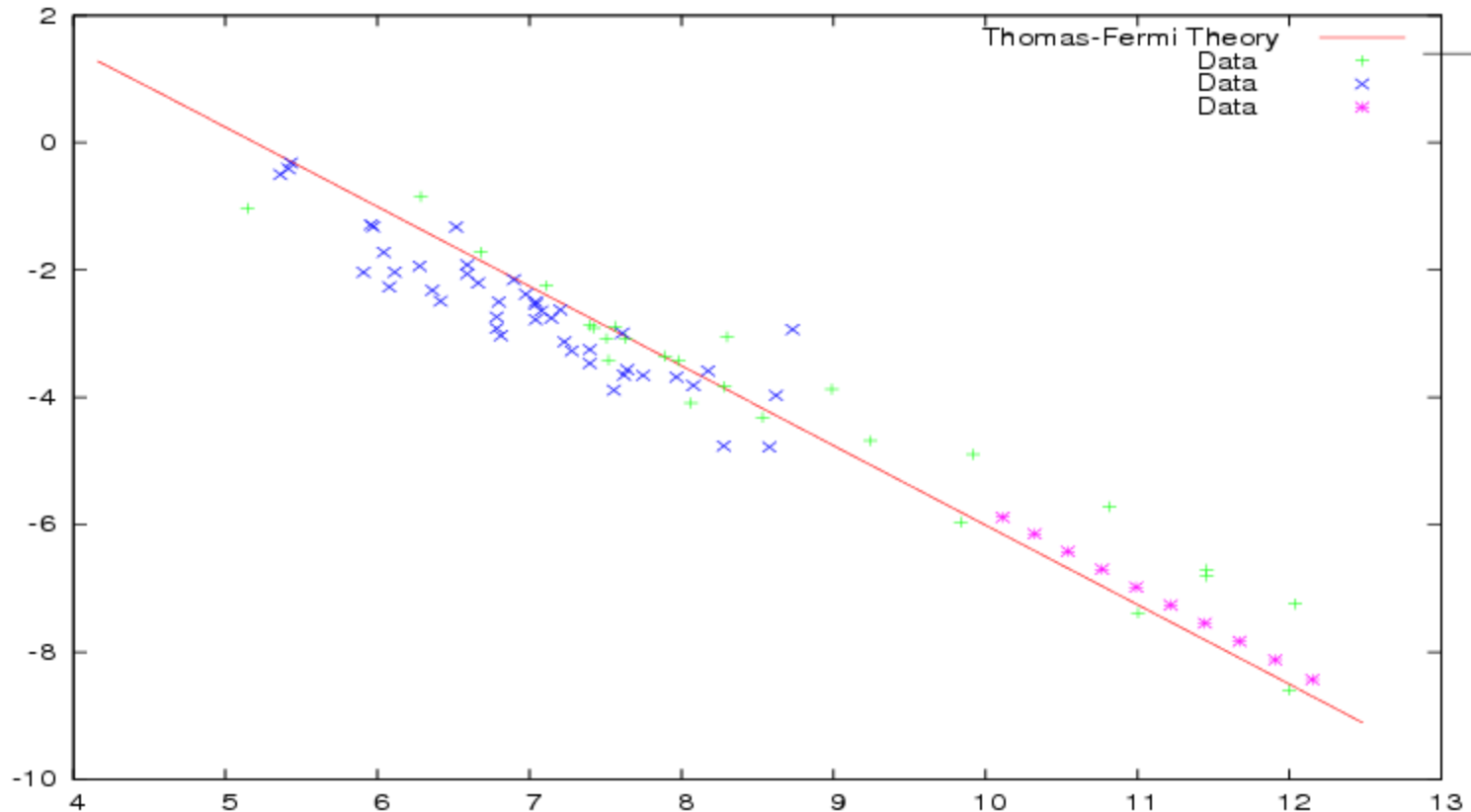


## Galaxy halo radius vs. Galaxy halo Mass



$\hat{r}_h = r_h (\Sigma_0 \text{ pc}^2 / [120 M_\odot])^{\frac{1}{5}}$  vs.  $\hat{M}_h = M_h (120 M_\odot / [\Sigma_0 \text{ pc}^2])^{\frac{3}{5}}$ .  
 $r_h$  follows **with precision** the square-root of  $M_h$  and the amplitude factor as predicted theoretically.

# Galaxy Phase-space density $Q$ vs. Galaxy halo Mass



$\log_{10} Q$  vs.  $\log_{10} \hat{M}_h$  theory and data.

$Q \equiv \rho(0)/\sigma^3(0)$ . Theoretical curve  $Q$  obtained from the Thomas-Fermi expression.

## Diluted regime of Galaxies

In the diluted regime of Galaxies

$$M_h \gtrsim 10^6 M_\odot, \quad \nu_0 \lesssim -5, \quad T_0 \gtrsim 0.017 \text{ K} = 17 \text{ mK.}$$

$r_h$ ,  $M_h$  and  $Q(0)$  **scale** as functions of each other.

$$M_h = 1.75572 \Sigma_0 r_h^2, \quad r_h = 68.894 \sqrt{\frac{M_h}{10^6 M_\odot}} \sqrt{\frac{120 M_\odot}{\Sigma_0 \text{ pc}^2}} \text{ pc}$$

$$Q(0) = 1.2319 \left(\frac{10^5 M_\odot}{M_h}\right)^{\frac{5}{4}} \left(\frac{\Sigma_0 \text{ pc}^2}{120 M_\odot}\right)^{\frac{3}{4}} \text{ keV}^4$$

These scaling behaviours are **very accurate** except near the degenerate limit.

C. Destri, H. J. de Vega, N. G. Sanchez, *New Astronomy* **22**, 39 (2013) and *Astroparticle Physics*, **46**, 14 (2013).

H. J. de Vega, P. Salucci, N. G. Sanchez,  
arXiv:1309.2290, to appear in *MNRAS*.

H. J. de Vega, N. G. Sanchez, arXiv:1310.6355.

# Classical and Quantum regimes of WDM Galaxies

I. Diluted and classical regime:

$$\hat{M}_h \gtrsim 10^6 M_\odot, \quad \nu_0 \lesssim -5, \quad T_0 \gtrsim 0.017 \text{ K.}$$

The density and the velocity profiles are **universal**.

**Exact** scaling laws for  $r_h$ ,  $M_h$  and  $Q(0)$ .

II. Quantum compact regime:

$$10^6 M_\odot \gtrsim \hat{M}_h \gtrsim \hat{M}_{h,min} = 3.1 \cdot 10^4 M_\odot,$$

$$\nu_0 \gtrsim -5, \quad 0 \leq T_0 \lesssim 0.017 \text{ K.}$$

The density and the velocity profiles are **non-universal**: the profiles **depend** on the galaxy mass  $M_h$ .

Small deviations from the scaling laws for  $r_h$ ,  $M_h$  and  $Q(0)$ .

III. Degenerate limit

$$\hat{M}_h = \hat{M}_{h,min} = 3.1 \cdot 10^4 M_\odot, \quad \nu_0 = +\infty, \quad T_0 = 0$$

## Circular Velocities and Density Profiles

The circular velocity  $v_c(r)$  follows from the virial theorem

$$v_c(r) = \sqrt{\frac{G M(r)}{r}} = \sqrt{-\frac{r}{m} \frac{d\mu}{dr}}$$

The circular velocity normalized at the core radius  $r_h$

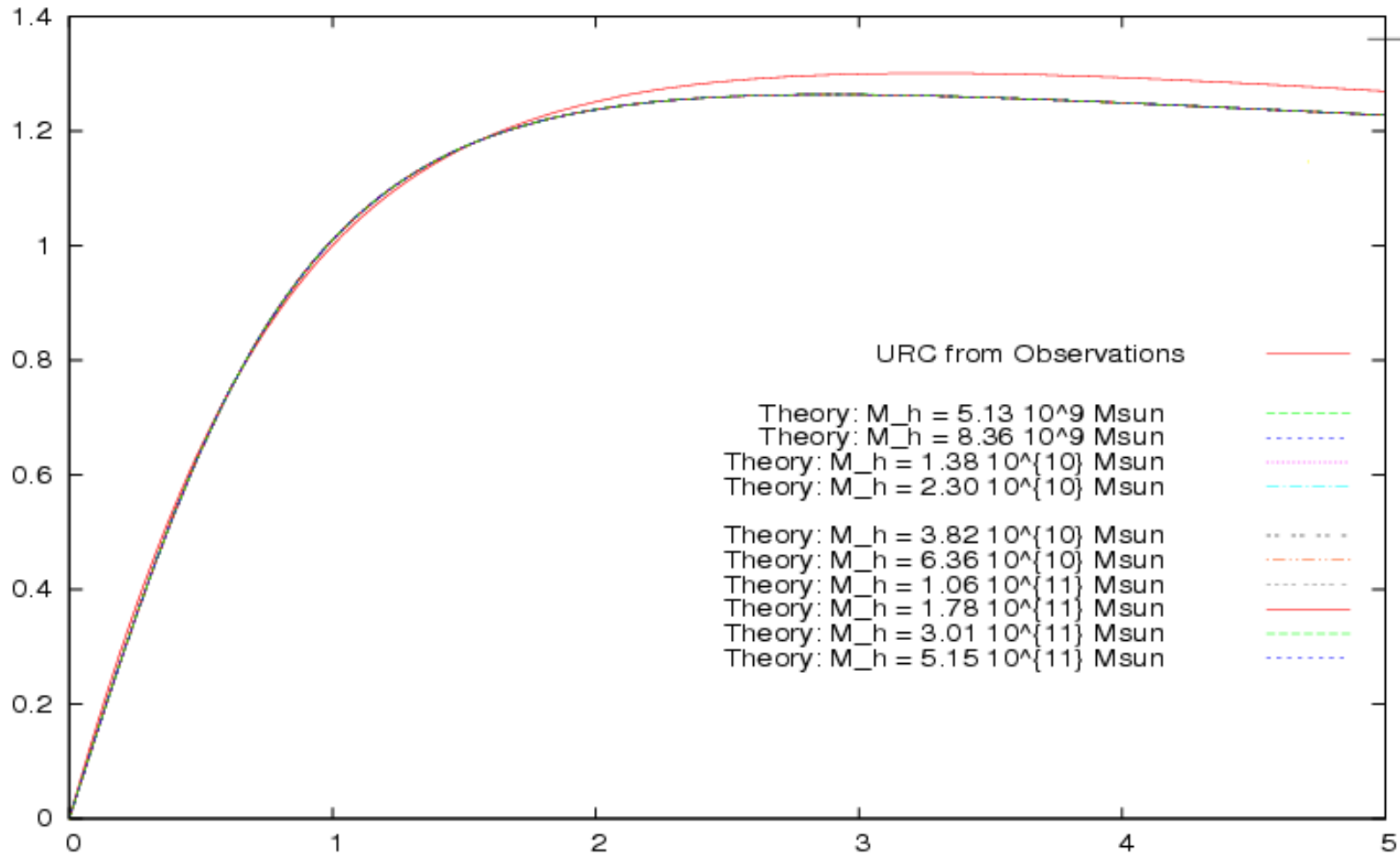
$$U(x) \equiv \frac{v_c(r)}{v_c(r_h)} \quad , \quad x = \frac{r}{r_h}$$

Solving the Thomas-Fermi equations we find:

- $U(x) = v_c(r)/v_c(r_h)$  is **only** function of  $x = r/r_h$ .
- $U(x)$  takes the **same** values for all galaxy halo masses in the range  $5.1 \cdot 10^9 M_\odot$  till  $5.1 \cdot 10^{11} M_\odot$ .
- $U(x)$  turns to be an **universal** function.
- The observational universal curves and the theoretical Thomas-Fermi curves **coincide** for  $r \lesssim 2 r_h$ ,  $x \lesssim 2$ .

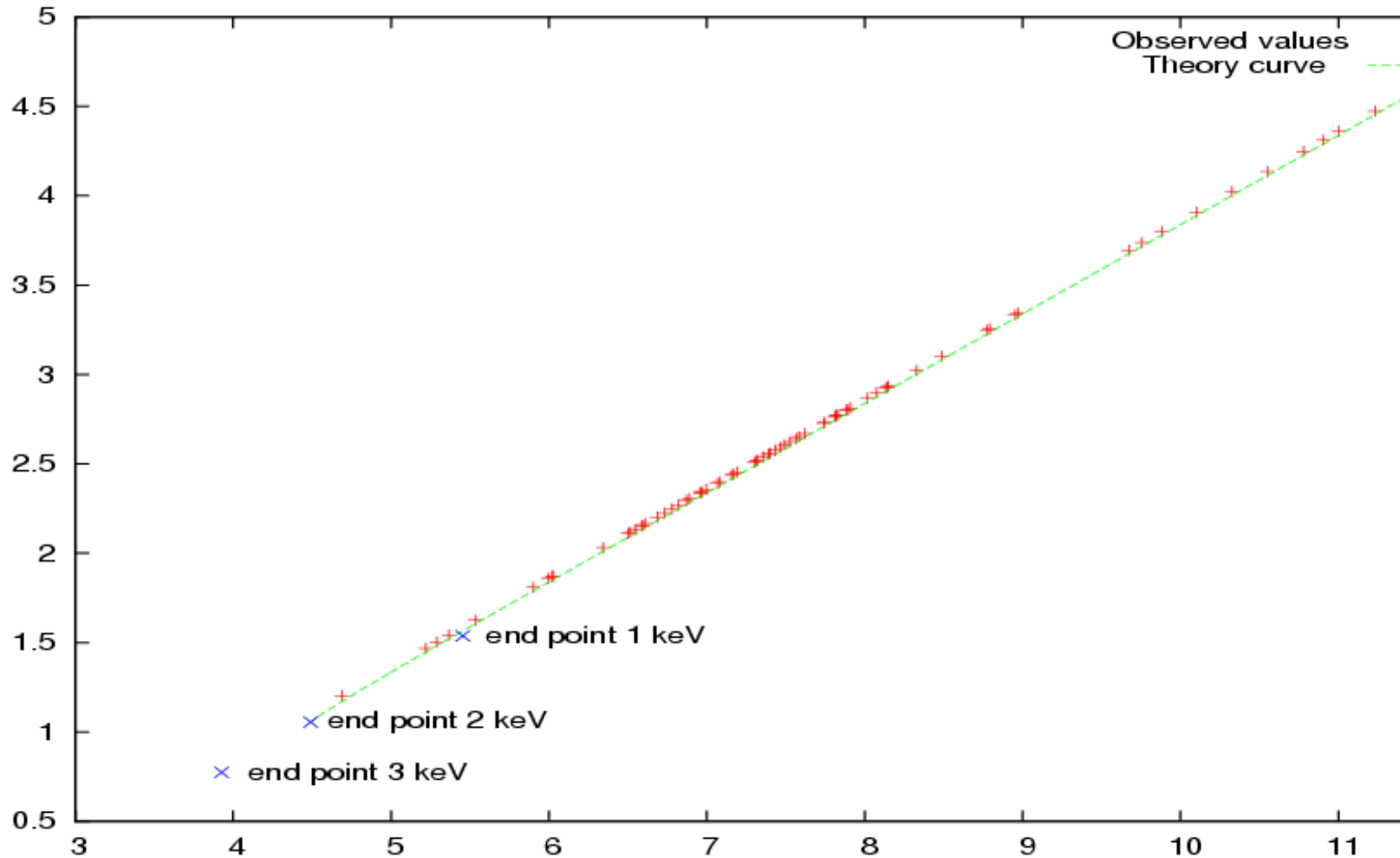
These are **remarkable** results !!

# Normalized circular velocities



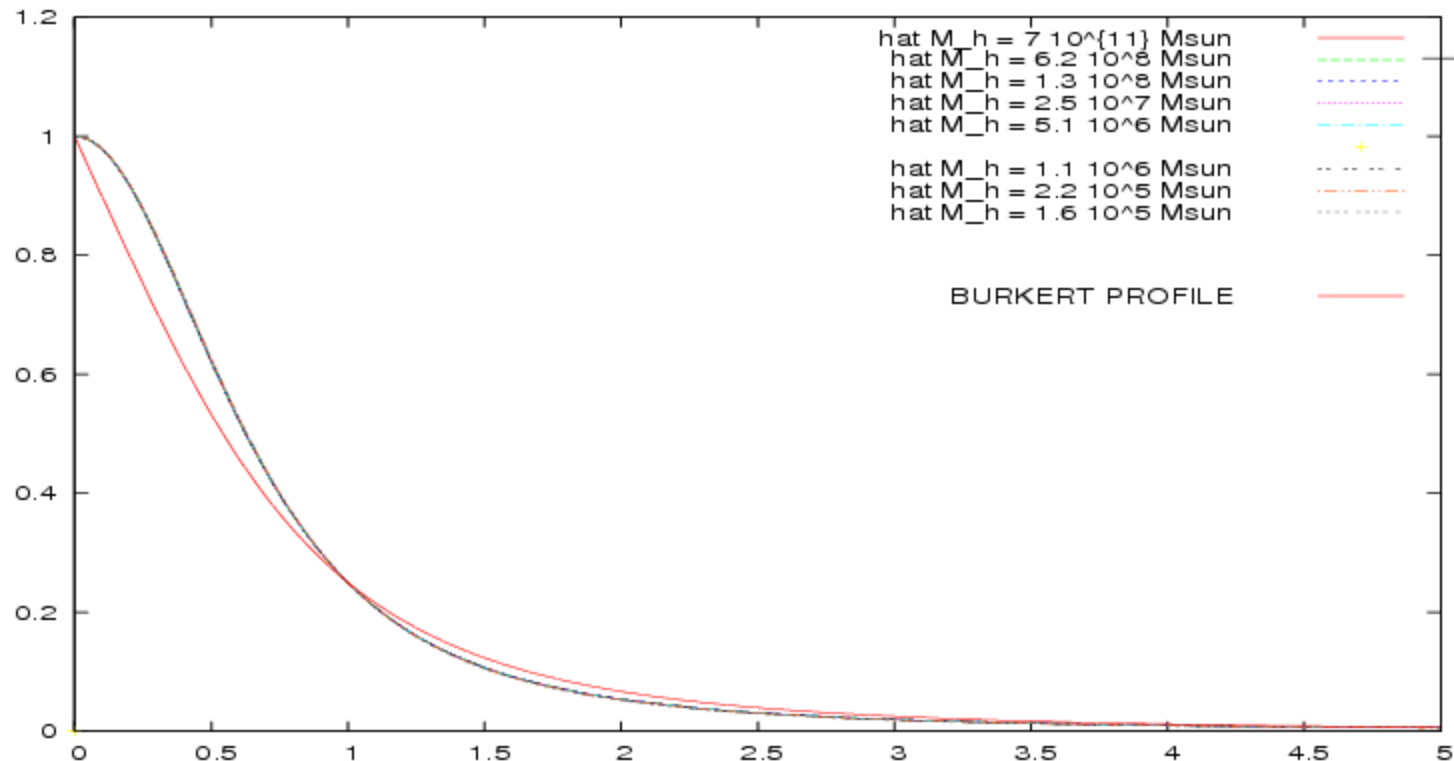
$$U(x) = v_c(r)/v_c(r_h) \text{ VS. } x = r/r_h.$$

# Galaxy halo radius vs. Galaxy halo Mass



$\hat{r}_h = r_h (\Sigma_0 \text{ pc}^2 / [120 M_\odot])^{\frac{1}{5}}$  vs.  $\hat{M}_h = M_h (120 M_\odot / [\Sigma_0 \text{ pc}^2])^{\frac{3}{5}}$   
 $r_h$  follows **with precision** the square-root of  $M_h$  and the amplitude factor as predicted theoretically.

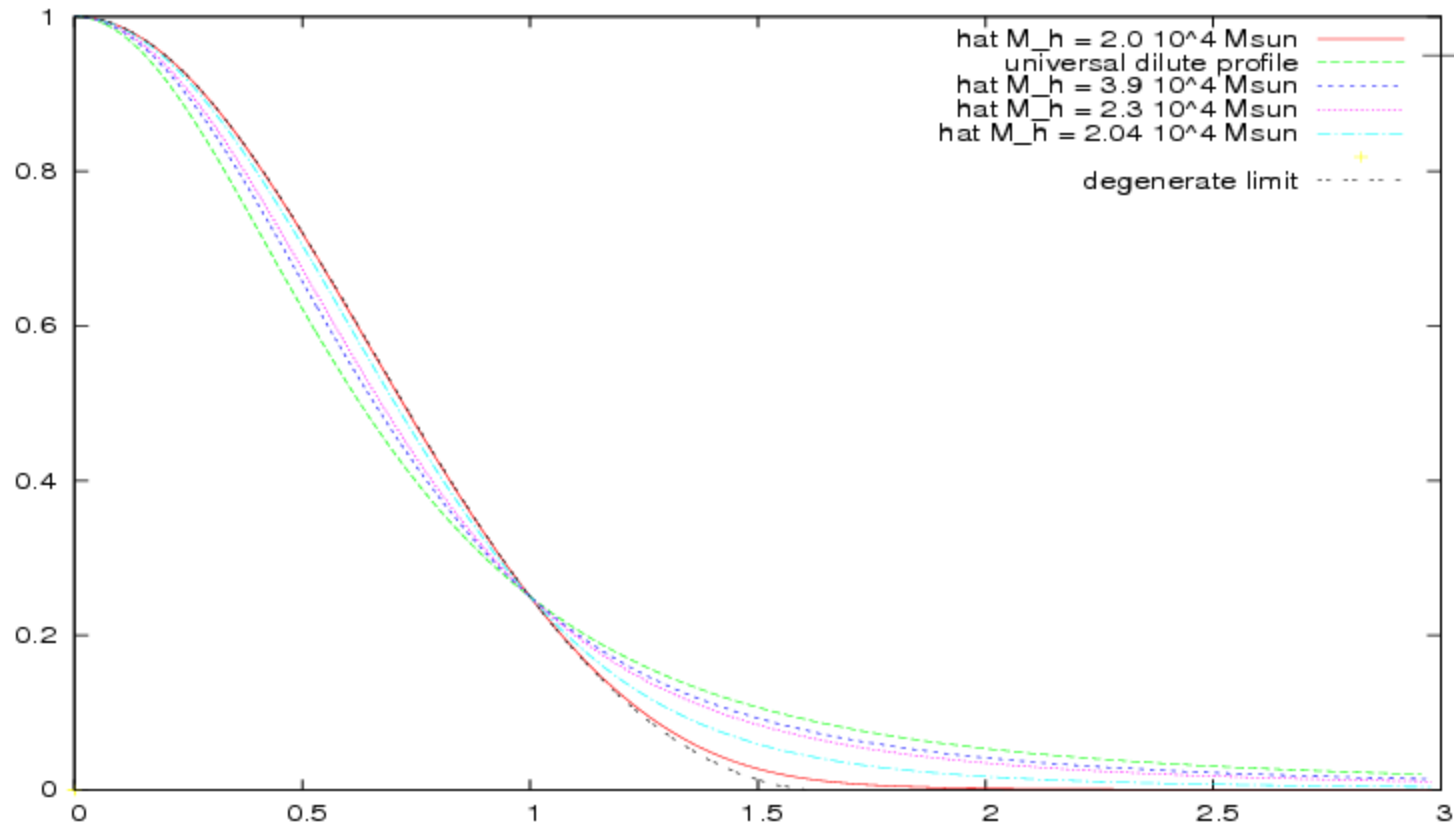
## Theoretical vs. observational density profiles



$\rho(r)/\rho(0)$  as functions of  $r/r_h$ . **ALL** the theoretical profiles in the diluted regime:  $1.4 \cdot 10^5 M_{\odot} < \hat{M}_h < 7.5 \cdot 10^{11} M_{\odot}$  fall into the **same and universal** density profile in very good agreement with the **empirical** Burkert profile.



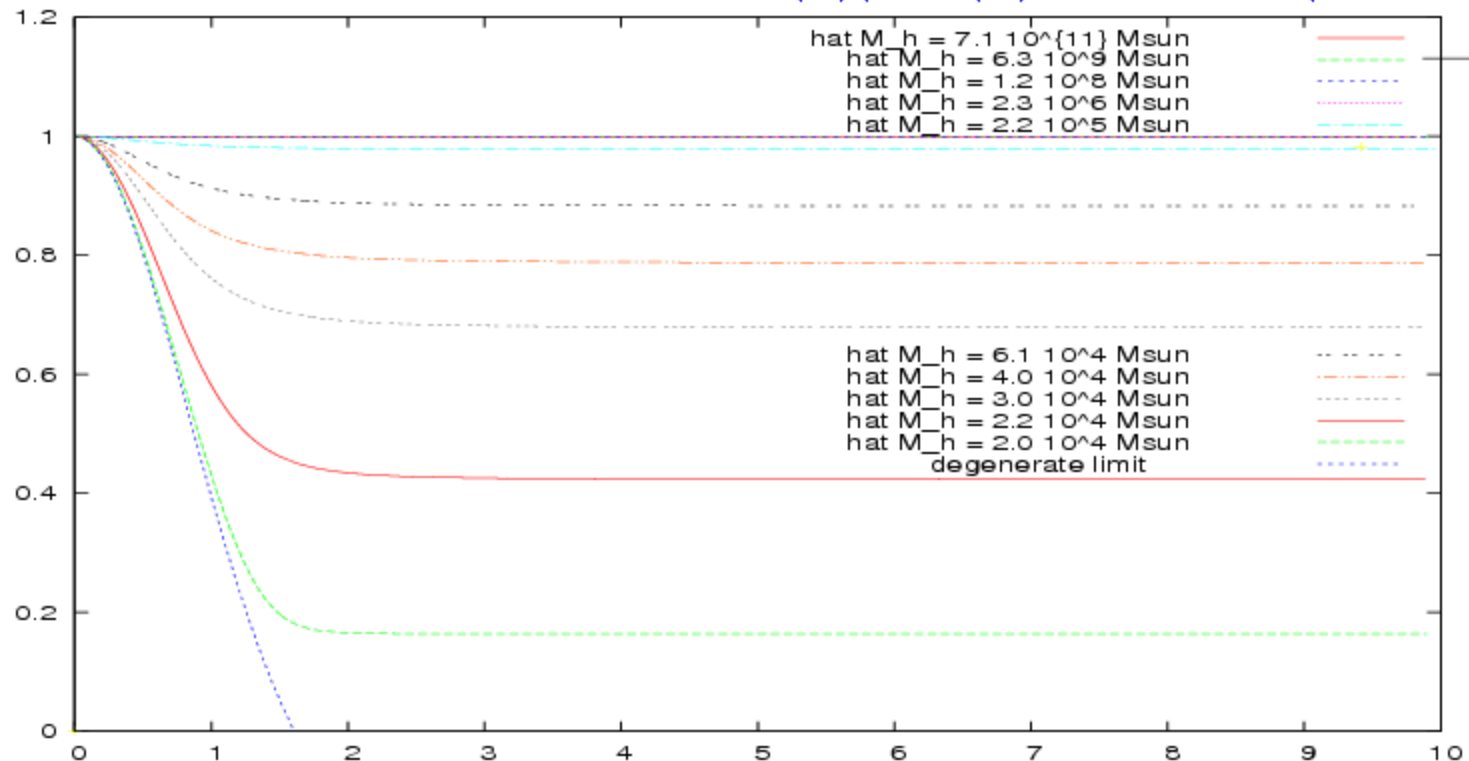
## Density profiles in the Quantum regime



$\rho(r)/\rho(0)$  as functions of  $r/r_h$ .

Galaxy halo masses  $M_h^{\text{min}} = 3.1 \cdot 10^4 M_{\odot} \leq \hat{M}_h < 3.9 \cdot 10^4 M_{\odot}$   
 in the **quantum** regime exhibit **shrinking** density profiles.

## Velocity dispersion profiles $\sigma^2(r)/\sigma^2(0)$ vs. $x = r/r_h$



**ALL** velocity profiles in the **classical diluted regime**

$\hat{M}_h > 2.3 \cdot 10^6 M_{\odot}$  fall into a **constant universal** value.

In the **quantum regime**:  $1.6 \cdot 10^6 M_{\odot} > \hat{M}_h > \hat{M}_{h,min}$  the profiles **are not universal** and do depend on  $\hat{M}_h$  and  $x$ .

## The local equation of state of WDM Galaxies

The pressure  $P(r)$  as a function of the density  $\rho(r)$

$$\rho = \frac{m^{\frac{5}{2}}}{3\pi^2 \hbar^3} (2T_0)^{\frac{3}{2}} I_2(\nu) \quad , \quad P = \frac{m^{\frac{3}{2}}}{15\pi^2 \hbar^3} (2T_0)^{\frac{5}{2}} I_4(\nu).$$

through the parameter  $\nu$  from the **Thomas-Fermi** equation.

$$P = \frac{T_0}{m} \rho \quad , \quad \nu \ll -1, \text{ WDM diluted galaxies.}$$

$$P = \frac{\hbar^2}{5} \left( \frac{3\pi^2}{m^4} \right)^{\frac{2}{3}} \rho^{\frac{5}{3}} \quad , \quad \nu \gg 1, \text{ WDM degenerate quantum limit.}$$

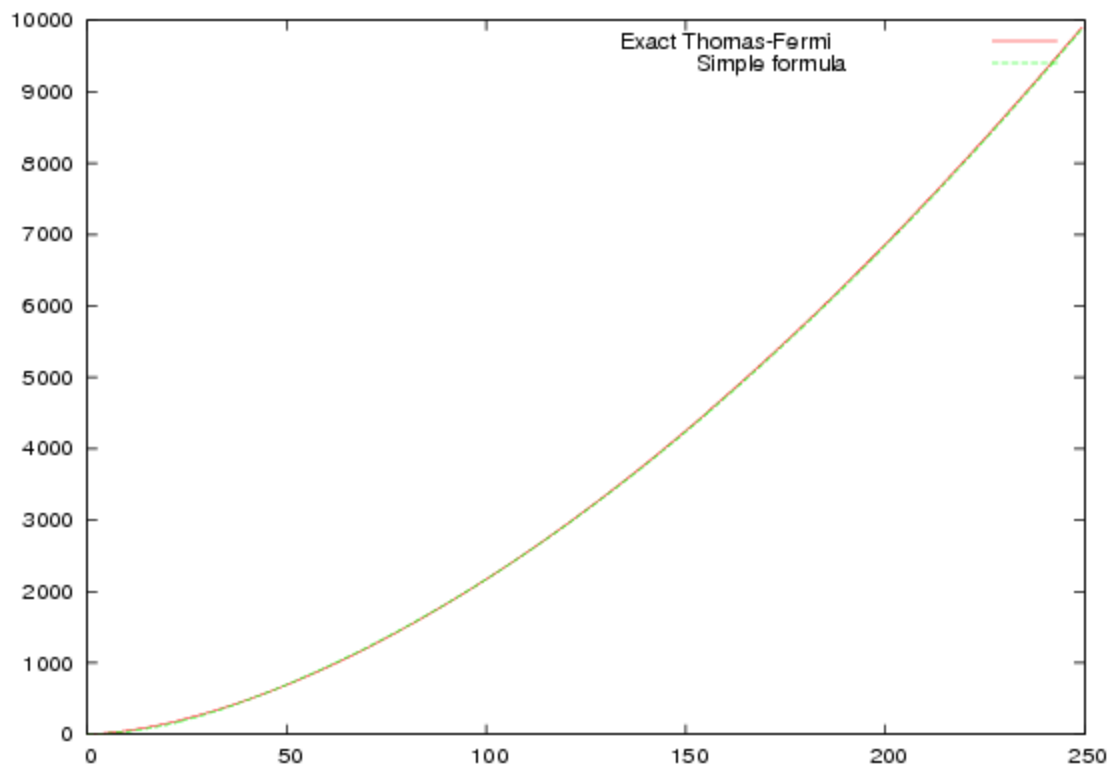
**Simple** formula accurately representing the exact equation of state obtained by solving the Thomas-Fermi equation:

$$P = \frac{m^{\frac{3}{2}} (2T_0)^{\frac{5}{2}}}{15\pi^2 \hbar^3} \left( 1 + \frac{3}{2} e^{-\beta_1 \tilde{\rho}} \right) \tilde{\rho}^{\frac{1}{3}} \left( 5 - 2 e^{-\beta_2 \tilde{\rho}} \right),$$
$$\tilde{\rho} \equiv \frac{3\pi^2 \hbar^3}{m^{\frac{5}{2}} (2T_0)^{\frac{3}{2}}} \rho = I_2(\nu),$$

best fit to the Thomas-Fermi equation of state for:

$$\beta_1 = 0.047098 \quad , \quad \beta_2 = 0.064492$$

# The equation of state of Galaxies: exact T-F and simple formula



The equation of state  $\tilde{P}$  vs.  $\tilde{\rho}$  obtained by solving the Thomas-Fermi equation and the simple formula.

$$\tilde{P} = \frac{15 \pi^2 \hbar^3}{m^{\frac{3}{2}} (2 T_0)^{\frac{5}{2}}} P = I_4(\nu) , \quad \tilde{\rho} \equiv \frac{3 \pi^2 \hbar^3}{m^{\frac{5}{2}} (2 T_0)^{\frac{3}{2}}} \rho = I_2(\nu)$$

## The Eddington equation for Dark Matter in Galaxies

$f(E)$  DM distribution function,  $E = p^2/(2m) - \mu$ ,

$m$  DM particle mass,  $\mu$  the chemical potential.

Equilibrium condition:  $\mu(r) = \mu_0 - m \phi(r)$ ,

$\phi(r)$  = gravitational potential.

The Poisson equation takes the **self-consistent** form:

$$\frac{d^2 \mu}{dr^2} + \frac{2}{r} \frac{d\mu}{dr} = -4\pi G m \rho(r) = -\frac{4 G m^2}{\pi \hbar^3} \int_0^\infty dp p^2 f \left[ \frac{p^2}{2m} - \mu(r) \right]$$

Dimensionless variables:  $q$ ,  $\nu(q)$ :

$$r = r_h q \quad , \quad \mu(r) = T_0 \nu(q) \quad , \quad f(E) = \Psi(E/T_0)$$

$T_0$  plays the role of the temperature and depends on the galaxy mass. The density profile is known from the observations:

$$\rho(r) = \rho_0 F \left( \frac{r}{r_h} \right) = \rho_0 F(q) \quad , \quad \rho_0 \equiv \rho(0) \quad , \quad F(1) = 1/4.$$

To be **determined**: the DM distribution function  $\Psi(E/T_0)$ .

## Abel's equation and its solution

Dimensionless Poisson's equation:

$$\frac{d^2 \nu}{dq^2} + \frac{2}{q} \frac{d\nu}{dq} = -b_0 F(q), \quad b_0 \equiv 4 \pi G \rho_0 r_h^2 \frac{m}{T_0}$$

$$\nu(q) = \nu(0) + b_0 \varepsilon(q), \quad \varepsilon(q) = \int_0^q \left(1 - \frac{q'}{q}\right) q' F(q') dq'$$

**Self-consistent** Poisson equation in dimensionless variables:

$$\rho(r) = \frac{\sqrt{2}}{\pi^2} m^{\frac{5}{2}} T_0^{\frac{3}{2}} \int_{\nu(\infty)}^{\nu} d\nu' \sqrt{\nu - \nu'} \Psi(-\nu'), \quad \nu' \equiv \nu - \frac{p^2}{2m T_0}$$

and in terms of the density profile  $F(q)$

$$F(\nu) = \frac{\sqrt{2}}{\pi^2} \frac{m^{\frac{5}{2}} T_0^{\frac{3}{2}}}{\rho_0} \int_{\nu(\infty)}^{\nu} d\nu' \sqrt{\nu - \nu'} \Psi(-\nu')$$

This is an **Abel integral** equation and its solution, the **Eddington formula**:

$$\Psi(-\nu) = \sqrt{2} \pi \frac{\rho_0}{m^{\frac{5}{2}} T_0^{\frac{3}{2}}} \int_{\nu(\infty)}^{\nu} \frac{d\nu'}{\sqrt{\nu - \nu'}} \frac{d^2 F}{d\nu'^2}$$

Boundary condition:  $\Psi$  and  $d\Psi/d\nu$  vanish at infinite distance.

## The Halo Dark Matter equation of state from the density profile

From the density profile we obtained the **pressure** and therefore the DM equation of state

$$\frac{P(r)}{\rho(r)} = \frac{1}{3} v^2(r) = G \Sigma_0 r_h \frac{\Pi(q)}{F(q)}$$

The local temperature  $T(r)$  is given by  $T(r) = \frac{1}{3} m v^2(r)$ .

Hence, the dark matter obeys **locally an ideal gas** equation of state

$$P(r) = \frac{T(r)}{m} \rho(r), \quad T(r) \equiv m G \Sigma_0 r_h t(q), \quad t(q) \equiv \frac{\Pi(q)}{F(q)}$$

The temperature  $T(r)$  turns to be **approximately constant** inside the halo radius  $r \lesssim r_h : t(q) \simeq 1.419$ .

$$T(r) = 8.238 t(q) \frac{m}{2 \text{ keV}} \sqrt{\frac{\Sigma_0 \text{ pc}^2}{120 M_\odot} \frac{M_h}{10^6 M_\odot}} \text{ mK}$$

The temperature **grows** as the square root of the galaxy halo mass.

## The Distribution Function in terms of the Density Profile

We explicitly find the distribution function  $\Psi(q)$  in terms of the density profile  $F(q)$  in H. J. de Vega, N. G. Sanchez, arXiv:1401.0726.

$$\Psi(q) = \frac{1}{G^{\frac{3}{2}} r_h^3 m^4 \sqrt{\rho_0}} \mathcal{D}(q), \quad \mathcal{D}(q) \equiv \frac{1}{\sqrt{32} \pi} \int_q^\infty \frac{\mathcal{J}(q') dq'}{\sqrt{\varepsilon(q) - \varepsilon(q')}}$$

$$\mathcal{J}(q) \equiv \frac{1}{\left(-\frac{d\varepsilon}{dq}\right)} \left[ \frac{\frac{d^2 F}{dq^2}}{\frac{d\varepsilon}{dq}} - \frac{\frac{dq^2}{d\varepsilon}}{\frac{d\varepsilon}{dq}} \frac{dF}{dq} \right]. \quad \text{Notice that } \left(-\frac{d\varepsilon}{dq} > 0\right).$$

We explicitly find the **velocity dispersion** and the **pressure** in terms of the density profile  $F(q)$ :

$$v^2(r) = 6 \pi G \rho_0 r_h^2 \frac{1}{F(q)} \int_q^\infty dq' [\varepsilon(q) - \varepsilon(q')]^2 \mathcal{J}(q')$$

$$P(r) = 2 \pi G \Sigma_0^2 \int_q^\infty dq' [\varepsilon(q) - \varepsilon(q')]^2 \mathcal{J}(q')$$



## Physical results from the Distribution Function

**Cored** density profiles behaving quadratically for small distances  $\rho(r) \stackrel{r \rightarrow 0}{\approx} \rho(0) - K r^2$  produce **finite and positive distribution functions** at the halo center while **cusped** density profiles always produce **divergent** distribution functions at the center.

We explicitly compute the phase-space distribution function and the equation of state for the **family** of  $\alpha$ -density profiles

$$\rho(r) = \frac{\rho_0}{\left[1 + \left(\frac{r}{r_h}\right)^2\right]^\alpha}, \quad 1 \leq \alpha \leq 2.5$$

This cored density profile generalizes the pseudo-thermal profile and with  $\alpha \sim 1.5$ , it is **perfectly appropriate** to fit galaxy observations.

For  $\alpha = 5/2$  this is the **Plummer** profile describing the density of stars in globular clusters.

## Halo Thermalization from the Distribution Function

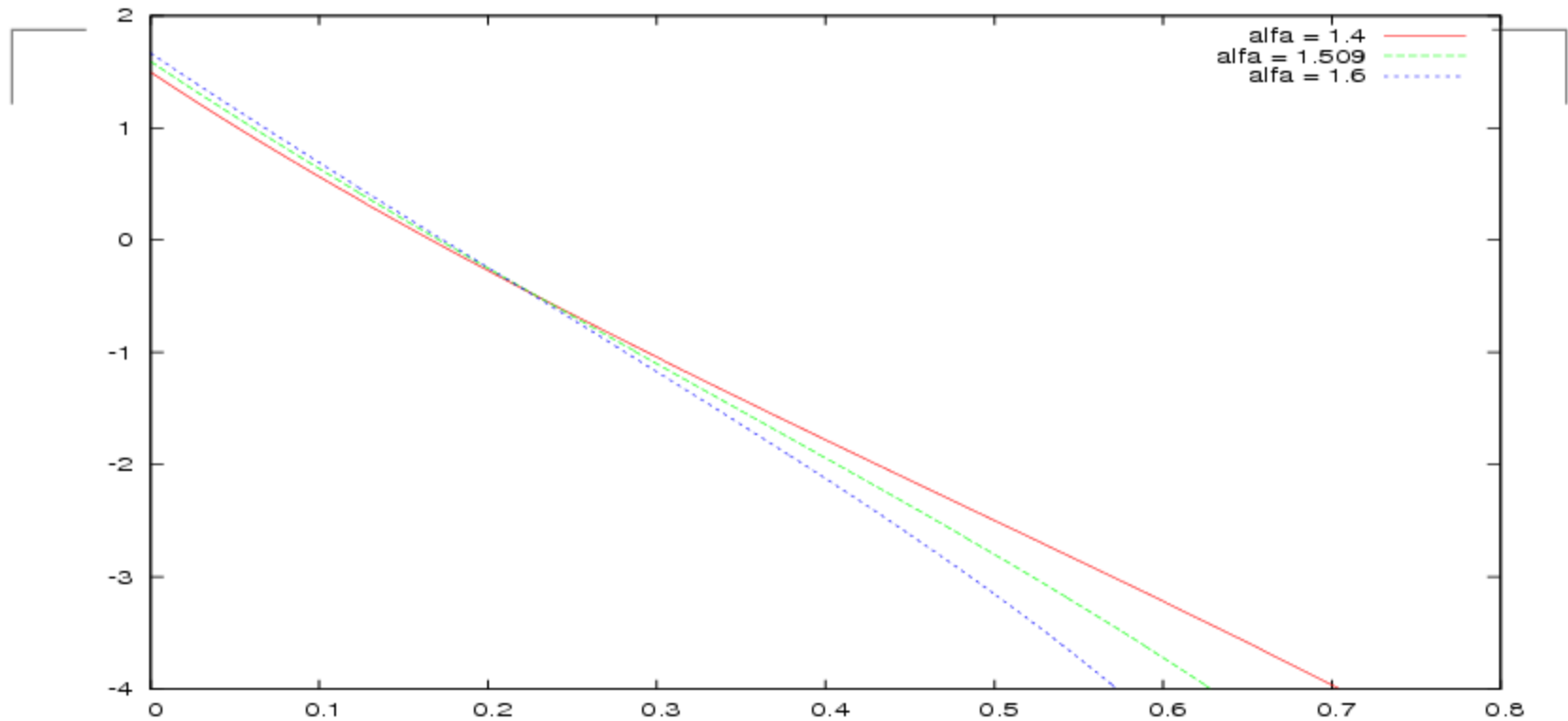
The obtained distribution function  $\Psi(q)$  is **positive** for all values of  $q$  in the whole range  $1 \leq \alpha \leq 2.5$ . Therefore, the  $\alpha$ -profiles are **physically meaningful**. [In general, there is no guarantee that  $\Psi(q)$  from the Eddington formula will be nowhere negative.]

$\ln \mathcal{D}(-\varepsilon)$  is approximately a **linear** function of the energy  $-\varepsilon$  for  $\alpha \sim 1.5$  and  $0 < -\varepsilon \lesssim 0.6$  which corresponds to  $0 < r \lesssim 7 r_h$ .

Therefore, the distribution function corresponding to  $\alpha$ -profiles for  $\alpha \sim 1.5$  is approximately a **thermal Boltzman** distribution in this interval. These are **realistic** halo galaxy density profiles.

The galaxy halos are therefore **thermalized, supporting and confirming** the Thomas-Fermi WDM approach.

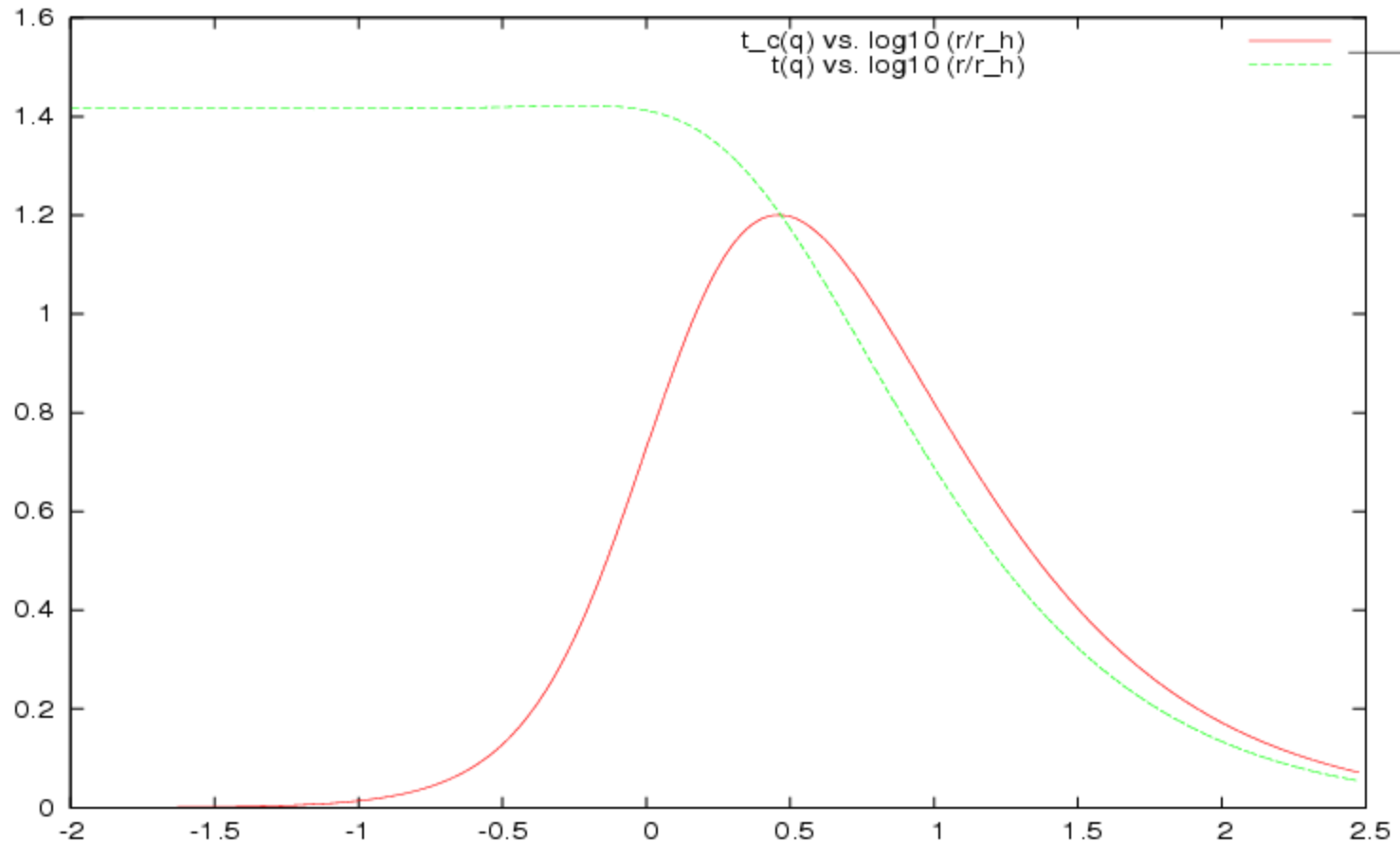
# Halo Thermalization



The distribution function  $\ln \mathcal{D}(-\epsilon)$  vs. the energy  $-\epsilon$ .

This **linear** behaviour of  $\ln \mathcal{D}(-\epsilon)$  indicates a **Boltzman** distribution function for  $0 \leq -\epsilon \lesssim 0.7$  and  $0 < r \lesssim 7 r_h$ . No assumption about the DM particle nature is made here.

## Thermalization and Virialization



The normalized temperature  $t(r/r_h)$  and the circular temperature  $t_c(r/r_h)$  vs.  $\log_{10}(r/r_h)$  for  $\alpha = 1.509$ .

For  $r \gtrsim r_h$ , the local temperature **decreases slowly** with  $r$ .

## Circular velocity and circular temperature

The circular velocity and the circular temperature are defined by the **virial theorem**:

$$v_c^2(r) \equiv \frac{G M(r)}{r}, \quad T_c(r) \equiv \frac{1}{3} m v_c^2(r) = \frac{G m M(r)}{3r}$$

$$T_c(r) = m G \rho_0 r_h^2 t_c(q)$$

The local temperature  $t(q)$  **turns to follow the decrease** of the circular temperature  $t_c(q)$  for  $r \gtrsim r_h$ .

### Conclusion:

- Halo thermalization for  $r < r_h$ .
- Halo virialization for  $r > r_h$ .

H. J. de Vega, N. G. Sanchez, arXiv:1401.0726

## X-ray detection of DM sterile neutrinos

Sterile neutrinos  $\nu_s$  decay into active neutrinos  $\nu_e$  plus **X-rays** with a lifetime  $\sim 10^{11} \times$  age of the universe.

These X-rays **may be seen** in the sky looking to galaxies !  
recent review: C. R. Watson et al. JCAP, (2012).

**Future** observations:

- Satellite projects: Xenia (NASA), ASTRO-H (Japan).
- **CMB**: WDM decay distorts the blackbody CMB spectrum. The projected PIXIE satellite mission (A. Kogut et al.) can measure WDM sterile neutrino mass.
- PTOLEMY experiment: Princeton Tritium Observatory. Aims to detect the cosmic neutrino background and WDM (keV scale) sterile neutrinos through the electron spectrum of the Tritium beta decay induced by the **capture** of a cosmic neutrino or a WDM sterile neutrino.
- HOLMES electron capture in  $^{163}\text{Ho}$  calorimeter G Sasso

Galaxy	$\frac{r_h}{\text{pc}}$	$\frac{\sigma}{\frac{\text{km}}{\text{s}}}$	$\frac{h^{\frac{3}{2}} \sqrt{Q_h}}{(\text{keV})^2}$	$\rho(0) / \frac{M_{\odot}}{(\text{pc})^3}$	$\frac{M_h}{10^6 M_{\odot}}$
Willman 1	19	4	0.85	6.3	0.029
Segue 1	48	4	1.3	2.5	1.93
Leo IV	400	3.3	0.2	.19	200
Canis Venatici II	245	4.6	0.2	0.49	4.8
Coma-Berenices	123	4.6	0.42	2.09	0.14
Leo II	320	6.6	0.093	0.34	36.6
Leo T	170	7.8	0.12	0.79	12.9
Hercules	387	5.1	0.078	0.1	25.1
Carina	424	6.4	0.075	0.15	32.2
Ursa Major I	504	7.6	0.066	0.25	33.2
Draco	305	10.1	0.06	0.5	26.5
Leo I	518	9	0.048	0.22	96
Sculptor	480	9	0.05	0.25	78.8
Boötes I	362	9	0.058	0.38	43.2
Canis Venatici I	1220	7.6	0.037	0.08	344
Sextans	1290	7.1	0.021	0.02	116
Ursa Minor	750	11.5	0.028	0.16	193
Fornax	1730	10.7	0.016	0.053	1750
NGC 185	450	31	0.033	4.09	975
NGC 855	1063	58	0.01	2.64	8340
Small Spiral	5100	40.7	0.0018	0.029	6900
NGC 4478	1890	147	0.003	3.7	$6.55 \times 10^4$
Medium Spiral	$1.9 \times 10^4$	76.2	$3.7 \times 10^{-4}$	0.0076	$1.01 \times 10^5$
NGC 731	6160	163	$9.27 \times 10^{-4}$	0.47	$2.87 \times 10^5$
NGC 3853	5220	198	$8.8 \times 10^{-4}$	0.77	$2.87 \times 10^5$
NGC 499	7700	274	$5.9 \times 10^{-4}$	0.91	$1.09 \times 10^6$
Large Spiral	$5.9 \times 10^4$	125	$0.96 \times 10^{-4}$	$2.3 \times 10^{-3}$	$1. \times 10^6$

TABLE I: Observed values  $r_h$ ,  $\sigma$ ,  $\sqrt{Q_h}$ ,  $\rho(0)$  and  $M_h$  covering from ultracompact objects and

## THE MINIMAL GALAXY MASS

A minimal galaxy mass and minimal velocity dispersion are found.

This in turn implies a **minimal mass  $m_{\min} = 1.91$  keV** for the WDM particle.

This **minimal WDM mass** is a **universal** value, independent of the WDM particle physics model because only relies on the **degenerate quantum fermion state**, which is universal whatever is the non-degenerate regime.

These results and the observed halo radius and mass of the compact galaxies also **provide further indication that the WDM particle mass  $m$  is approximately around 2 keV.**

More precise data will make this estimation more precise.



# Minimal galaxy mass from degenerate WDM

The halo radius, the velocity dispersion and the galaxy mass take their **minimum** values for degenerate WDM:

$$r_{h \min} = 24.51 \dots \text{ pc} \left( \frac{m}{\text{keV}} \right)^{\frac{4}{3}} \left[ \rho(0) \frac{\text{pc}^3}{M_{\odot}} \right]^{\frac{1}{6}}$$

$$M_{\min} = 2.939 \dots 10^5 M_{\odot} \left( \frac{\text{keV}}{m} \right)^4 \sqrt{\rho(0) \frac{\text{pc}^3}{M_{\odot}}}$$

$$\sigma_{\min}(0) = 2.751 \dots \frac{\text{km}}{\text{s}} \left( \frac{\text{keV}}{m} \right)^{\frac{4}{3}} \left[ \rho(0) \frac{\text{pc}^3}{M_{\odot}} \right]^{\frac{1}{3}} .$$

These **minimum** values **correspond** to the observations of compact dwarf galaxies.

Lightest known compact dwarf galaxy is Willman I:

$$M_{\text{Willman I}} = 2.9 \cdot 10^4 M_{\odot}$$

Imposing  $M_{\text{Willman I}} > M_{\min}$  yields the **lower bound** for the WDM particle mass:  $m > 1.91 \text{ keV}$ .

# WARM DARK MATTER REPRODUCE

→ OBSERVED GALAXY DENSITIES  
AND VELOCITY DISPERSIONS

→ OBSERVED GALAXY  
CORED DENSITY PROFILES

-> OBSERVED SURFACE DENSITY VALUES OF  
DARK MATTER DOMINATED GALAXIES

→ SOLVES the OVERABUNDANCE (“satellite)  
PROBLEM and the CUSPS vs CORES Problem

## Summary Warm Dark Matter, WDM: $m \sim \text{keV}$

- Large Scales, structures beyond  $\sim 100$  kpc: WDM and CDM yield **identical** results **which agree with observations**
  - Intermediate Scales: WDM give the **correct abundance** of substructures.
  - Inside galaxy cores, below  $\sim 100$  pc: N-body classical physics simulations are **incorrect** for WDM because of **important quantum effects**.
  - Quantum calculations (Thomas-Fermi) give galaxy cores, galaxy masses, velocity dispersions and densities in **agreement with the observations**.
  - Direct Detection of the main WDM candidate: the sterile neutrino. **Beta decay and electron capture**.  ${}^3\text{H}$ , Re, Ho.
- So far, **not a single valid** objection arose against WDM.
- Baryons (=16%DM) expected to give a correction to WDM

## • **WDM OVERALL CONCLUSION**

- **To conclude, we find it is highly remarkable that in the context of warm dark matter, the quantum description provided by this semiclassical framework, (quantum WDM and classical gravitation), is able to reproduce such broad variety of galaxies.**
- **The resulting galaxy, halo radius, galaxy masses and velocity dispersion are fully consistent with observations for all different types of galaxies. Fermionic WDM treated quantum mechanically, as it must be, is able to reproduce the observed galactic cores and their sizes. In addition, WDM simulations produce the right DM structures in agreement with observations for scales  $>$  kpc.**

# WDM + BARYONS

**Baryons have not been included in this study. This is fully justified because on one hand dwarf compact galaxies are composed today 99.99 % of DM, and on the other hand the baryon fraction in large galaxies can reach values up to 1 - 3 %.**

**Since Fermionic WDM by itself produces galaxies and structures in agreement with observations for all types of galaxies, masses and sizes, the effect of including baryons is expected to be a small correction to these pure WDM results, consistent with the fact that dark matter is in average six times more abundant than baryons.**

## Axions are ruled out as dark matter

Hot Dark Matter (eV particles or lighter) are ruled out because their free streaming length is **too large**  $\gtrsim$  Mpc and hence galaxies are not formed.

A Bose-Einstein condensate of light scalar particles **evades** this argument because of the quantum nature of the BE condensate.  $r_{\text{Jeans}} \sim 5$  kpc implies  $m_{\text{axion}} \sim 10^{-22}$  eV.

The phase-space density  $Q = \rho/\sigma^3$  **decreases** during structure formation:  $Q_{\text{today}} < Q_{\text{primordial}} \propto m^4$ .

Computing  $Q_{\text{primordial}}$  for a DM BE condensate we derived **lower bounds** on the DM particle mass  $m$  using the data for  $Q_{\text{today}}$  in dwarf galaxies:

$$\text{TE: } m \geq 0.155 \text{ MeV} \left(\frac{25}{g_d}\right)^{5/3}. \quad \text{Out of TE: } m \geq 14 \text{ eV} \left(\frac{25}{g_d}\right)^{5/3}$$

Axions with  $m \sim 10^{-22}$  eV **are ruled out as DM candidates.**

D. Boyanovsky, H. J. de Vega, N. G. Sanchez, PRD 77, 043518 (08). H. de Vega, N. Sanchez, arXiv:1401.1214

## Summary and Conclusions

- Combining **theoretical** evolution of fluctuations through the Boltzmann-Vlasov equation with **galaxy data** points to a DM particle mass 3 - 10 keV.  $T_d$  turns to be model dependent. The keV mass scale holds **independently** of the DM particle physics model.
- Universal Surface density in DM galaxies [ $\mu_{0D} \simeq (18 \text{ MeV})^3$ ] explained by keV mass scale DM. Density profile scales and decreases for intermediate scales with the **spectral index**  $n_s$  :  $\rho(r) \sim r^{-1-n_s/2}$  and  $\rho(r) \sim r^{-2}$  for  $r \gg r_0$ .

H. J. de Vega, P. Salucci, N. G. Sanchez, 'The mass of the dark matter particle from theory and observations', *New Astronomy*, 17, 653 (2012).

H. J. de Vega, N. Sanchez, 'Model independent analysis of dark matter points to a particle mass at the keV scale', *MNRAS* 404 885 (2010)

## Future Perspectives: Detection!

Sterile neutrino detection depends **upon** the particle physics model. There are sterile neutrino models where the keV sterile is **stable** and thus hard to detect.

Astronomical observation of steriles:  
X-ray data from galaxy halos.

**Direct** detection of steriles in Lab:

**Bounds** on mixing angles from  
Mare, Katrin, ECHo, Project 8 and PTOLEMY are expected.

For a **particle detection** a **dedicated** beta decay or electron capture experiment looks **necessary** to search sterile neutrinos with mass around 2 keV.

Calorimetric techniques seem **well suited**.

Best nuclei for study:

Electron capture in  $^{163}\text{Ho}$ , beta decay in  $^{187}\text{Re}$  and Tritium.



**END**

**THANK YOU FOR YOUR ATTENTION**

**UNDER COMPLETION NOW**

**H. J. de Vega, N. G. Sanchez:  
BLACK HOLES FORMED  
by WDM and BARYONS**

**(GALACTIC SUPERMASSIVE, STELLAR)**

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**Stars, globular clusters, galaxies,.... galaxy clusters  
And other results.....**

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**14 MARCH 2014:** Opening Session / Session ouverte de culture scientifique : "Présentation du programme 2014 et des dernières nouvelles scientifiques de l'univers" (Bâtiment Perrault, Observatoire de Paris)

**22 MAY 2014:** Spring Open Session of scientific culture / Session ouverte de printemps de culture scientifique interdisciplinaire : "L'homme et l'univers" (Bâtiment Perrault, Observatoire de Paris)

**4-7 JUNE 2014:** Chalonge Meudon workshop: "From large to small scale structures in agreement with observations: CMB, WDM, galaxies, black holes, neutrinos and sterile neutrinos" (Château de Meudon - CIAS, Meudon)

**22-25 JULY 2014:** The 18<sup>th</sup> Paris cosmology colloquium Chalonge 2014: "Latest news from the universe: A WDM, CMB, dark matter, A dark energy, neutrinos and sterile neutrinos" (Bâtiment Perrault, Observatoire de Paris)

**25 JULY 2014:** Summer Open Session of scientific culture / Session ouverte d'été de culture scientifique : A surprise session

**AUTOMNE 2014:** Cycle Les grandes questions posées aujourd'hui à la science : "Où va la science ?" (Cité Internationale Universitaire de Paris)

**17-18 OCTOBER 2014:** Chalonge Turin session: "Latest news from the universe: dark matter, galaxies and particle physics" (Palazzo de l'Università & Accademia delle Scienze, Piemonte region, Turin, Italy)

**27-28 NOVEMBER 2014:** Concluding session & Avant-première 2015

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Anthony LASENBY

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