

# Filaments, surface density and scaling laws in star and structure formation

Marco Lombardi, University of Milan

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with

Joao Alves, University of Vienna &  
Charles Lada, CfA, Harvard

# Penitenziagite

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M42/M43

1 pc



$z=z_{\odot}$

134606 yr



Matthew Bate  
University of Exeter

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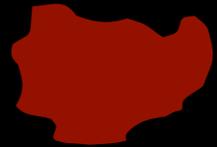
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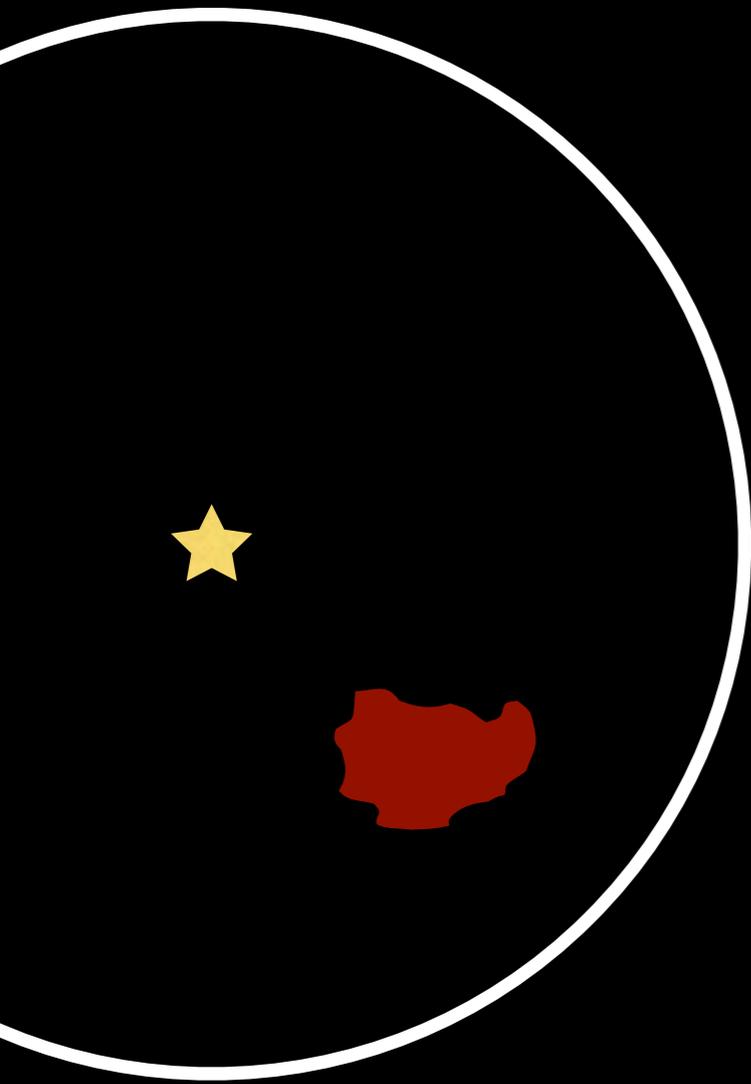
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- Each tracer has its own benefits and limitations!

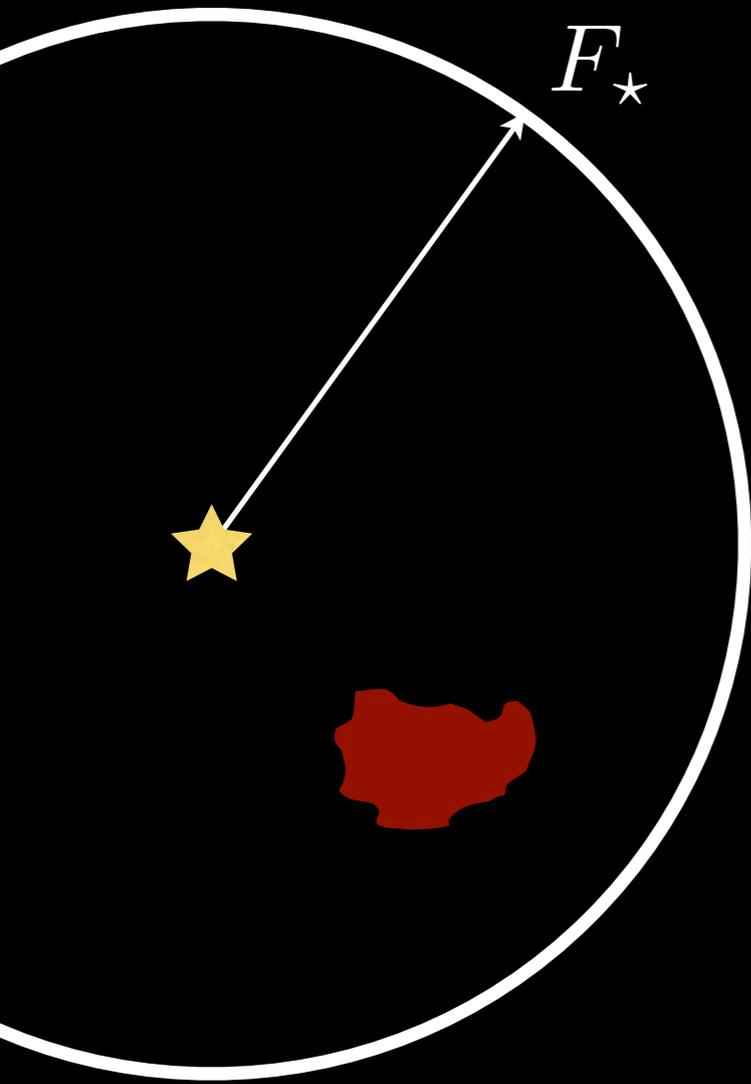
# Extinction Primer



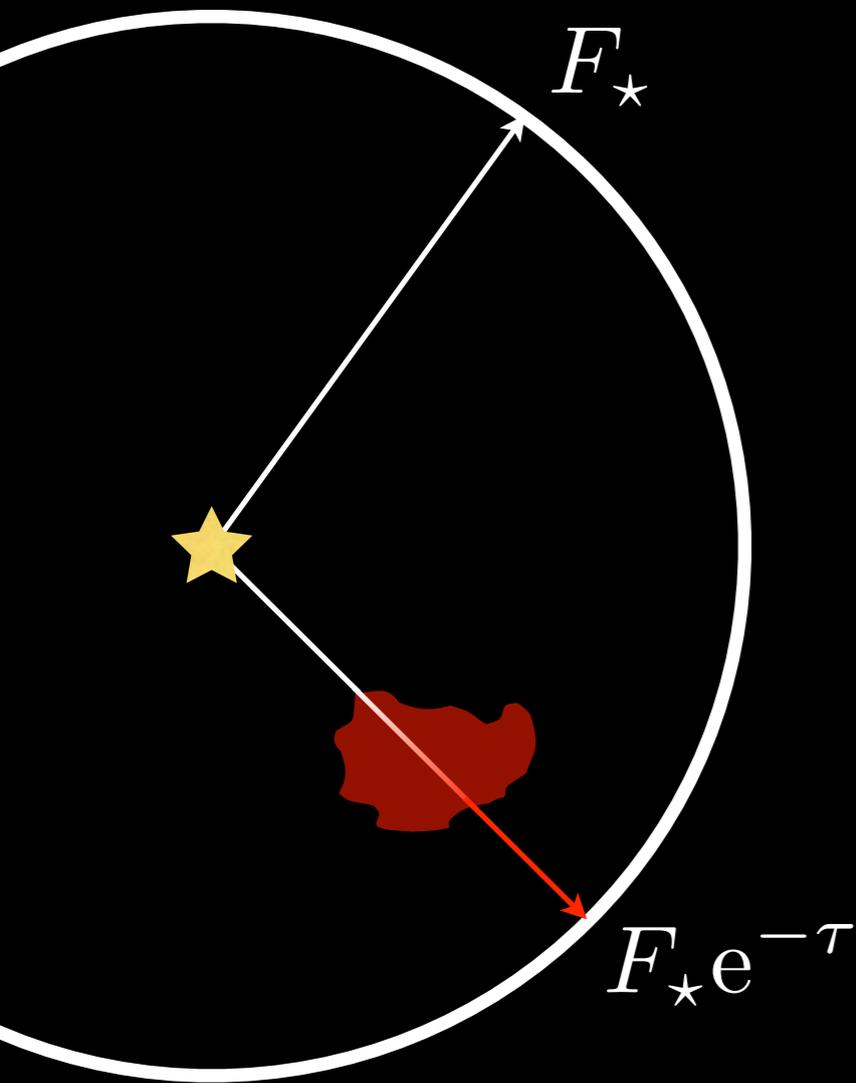
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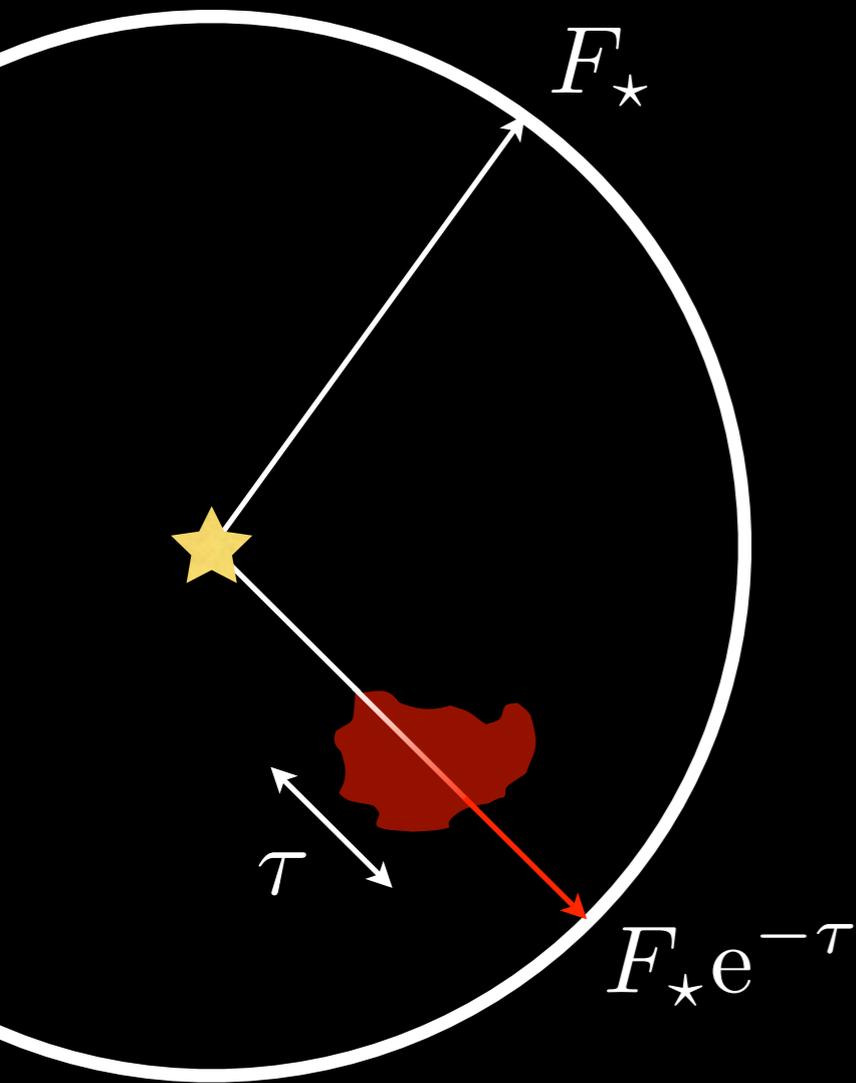
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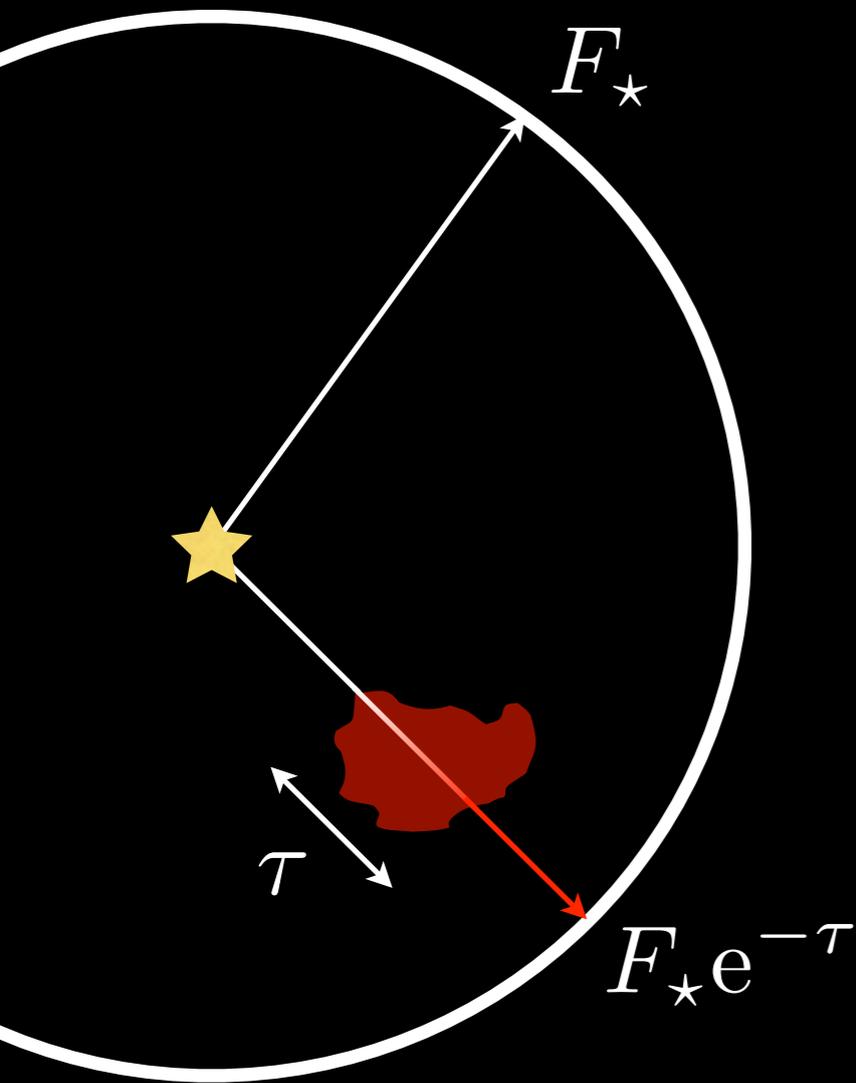
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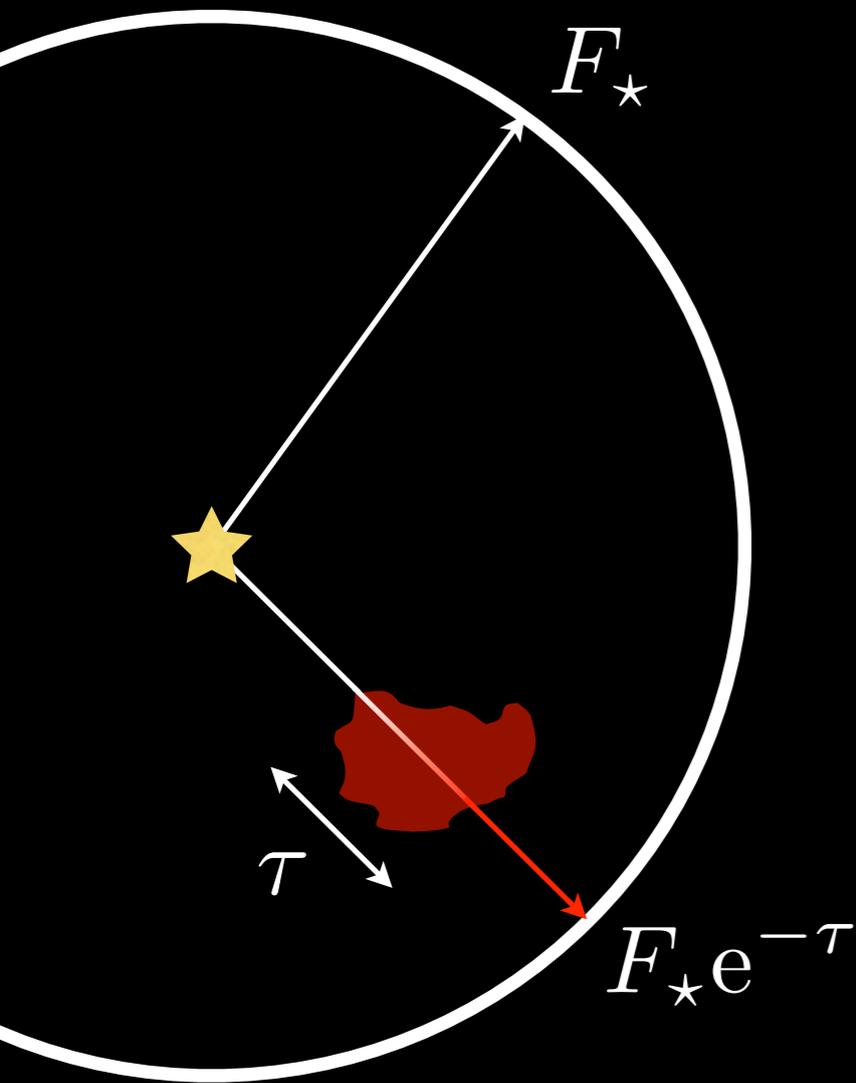
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## Brightness

$$\begin{aligned} m_{\text{obs}} &= -2.5 \log (F_{\star} e^{-\tau}) \\ &= -\underbrace{2.5 \log F_{\star}}_{m_{\star}} + \underbrace{2.5 \tau \log e}_{A_V} \end{aligned}$$

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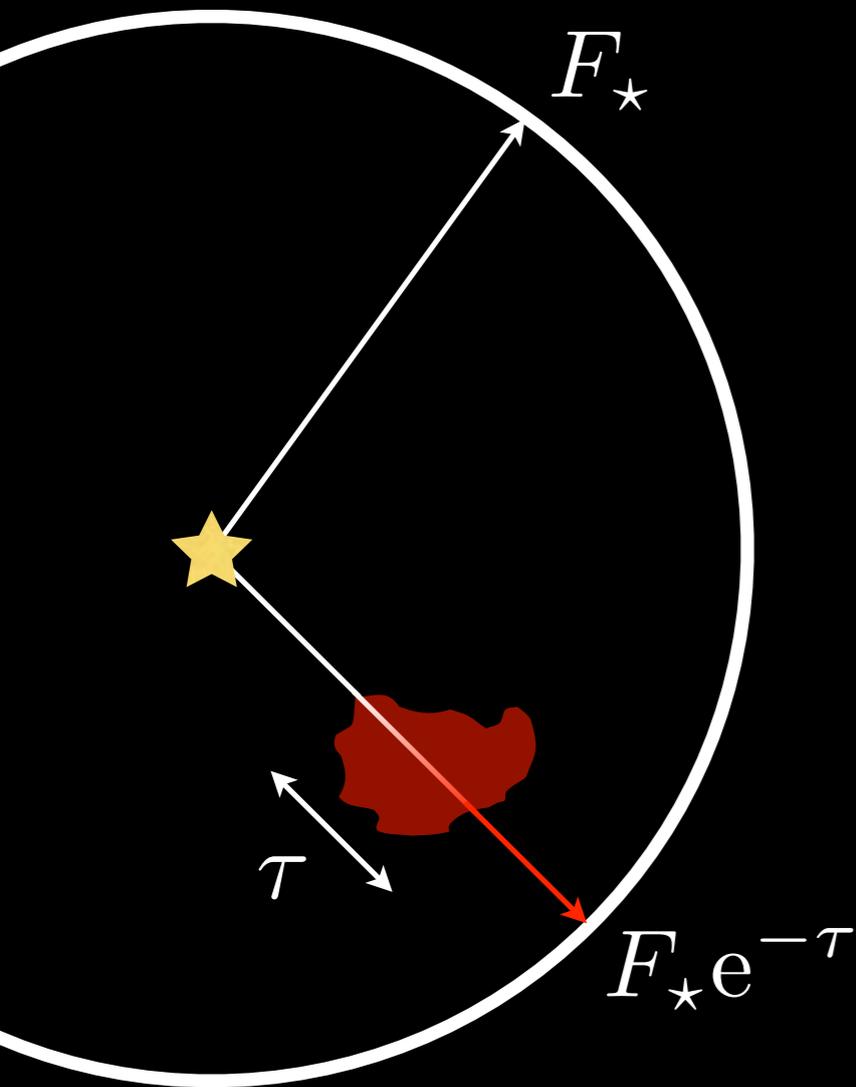
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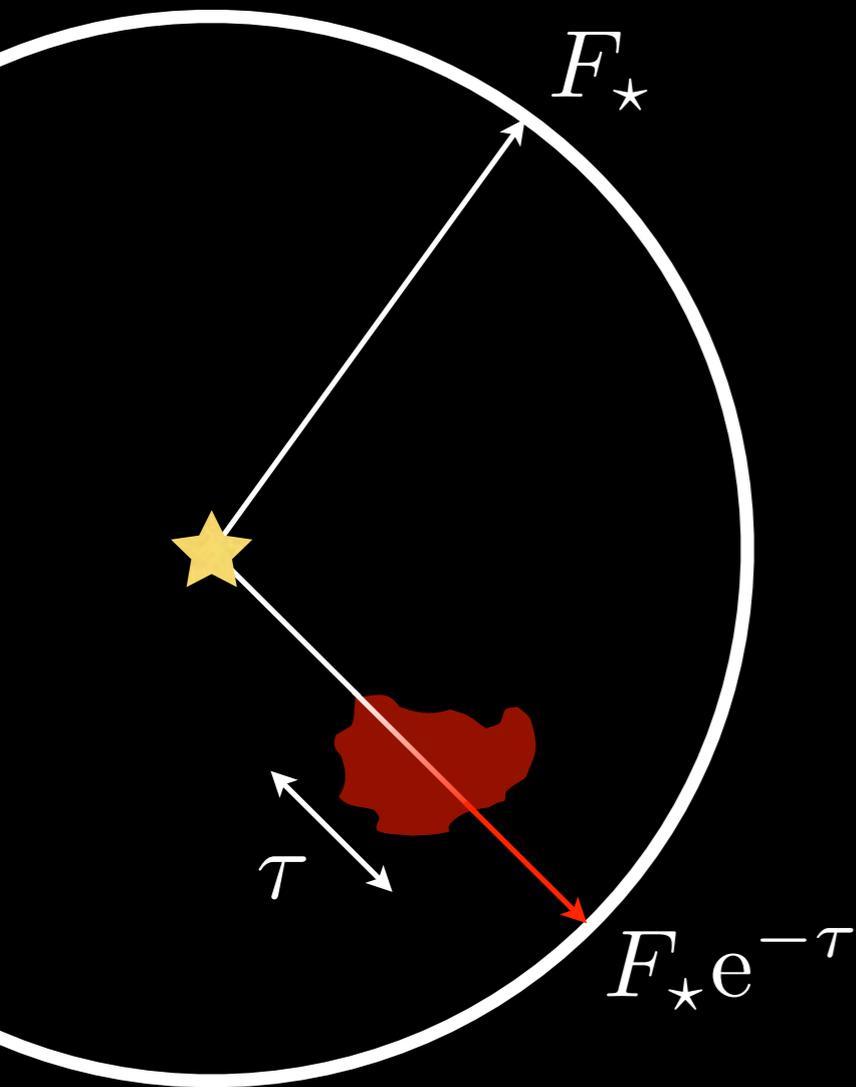


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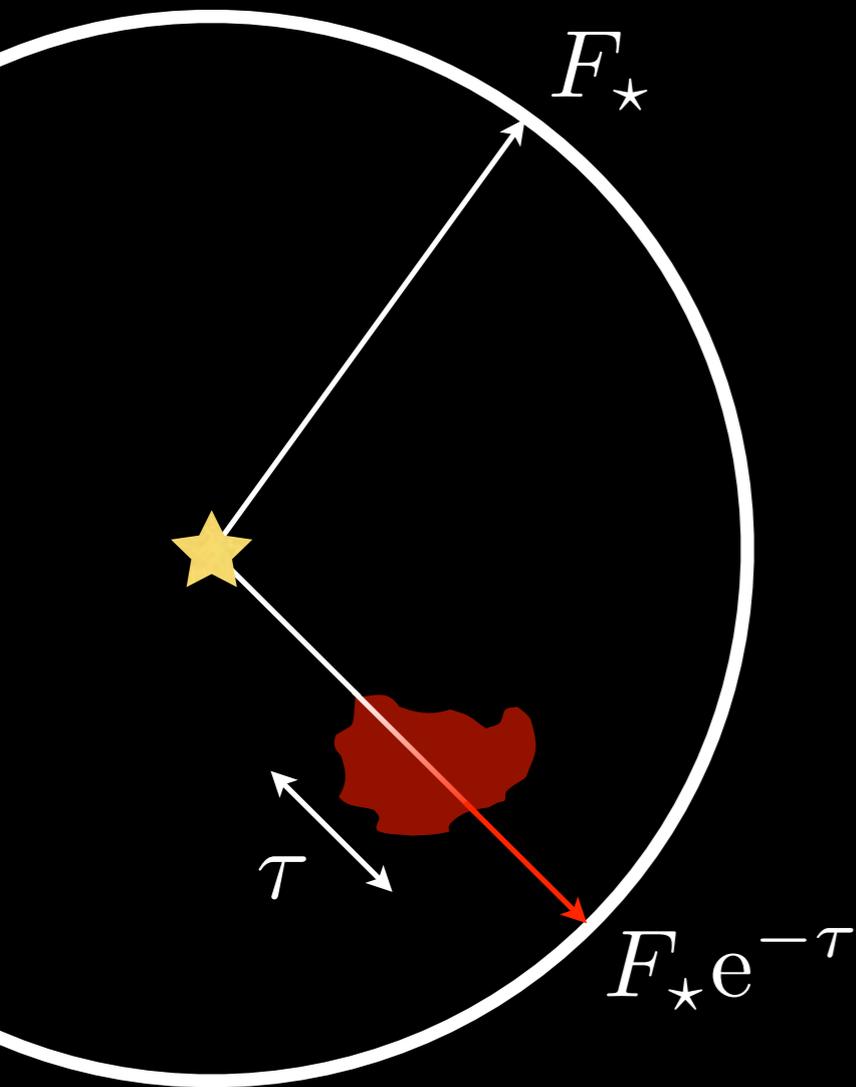
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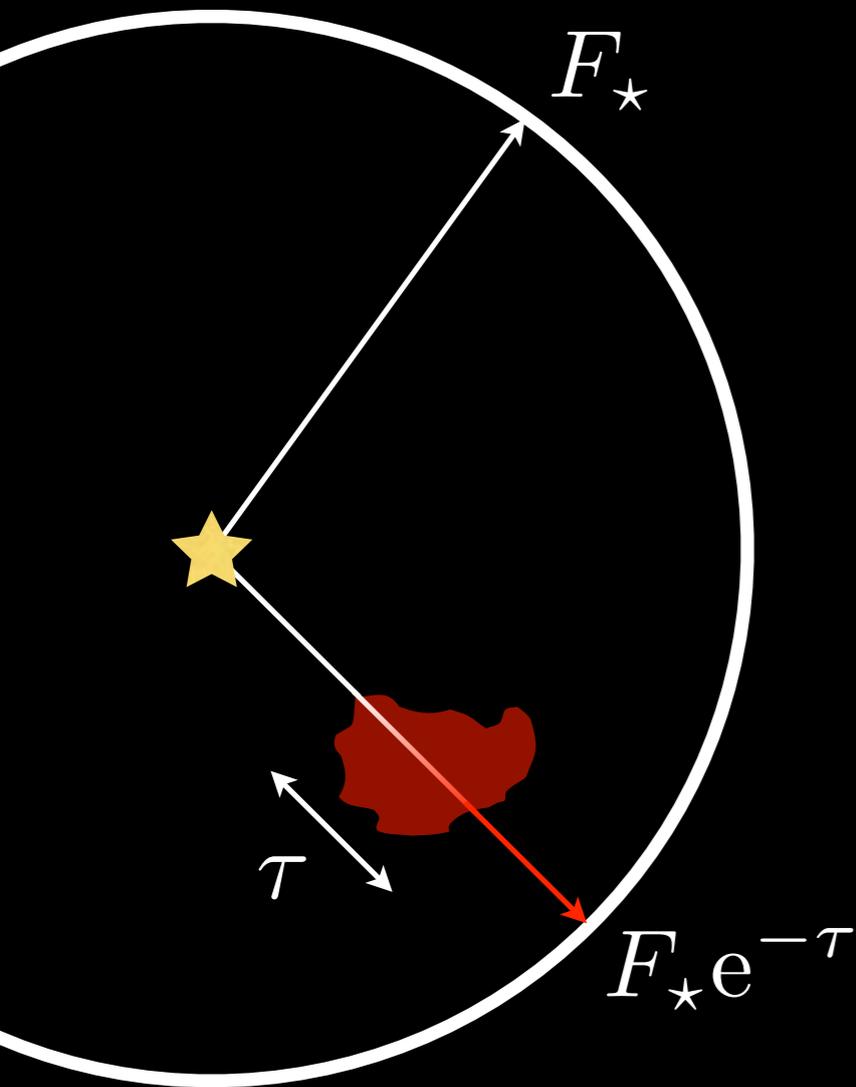
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$R_{1,2}$  parametrizes our knowledge (or ignorance) on the dust properties at the two frequencies  $\lambda_1$  and  $\lambda_2$

# Making extinction maps



Alves et al. (2014)

# Making extinction maps

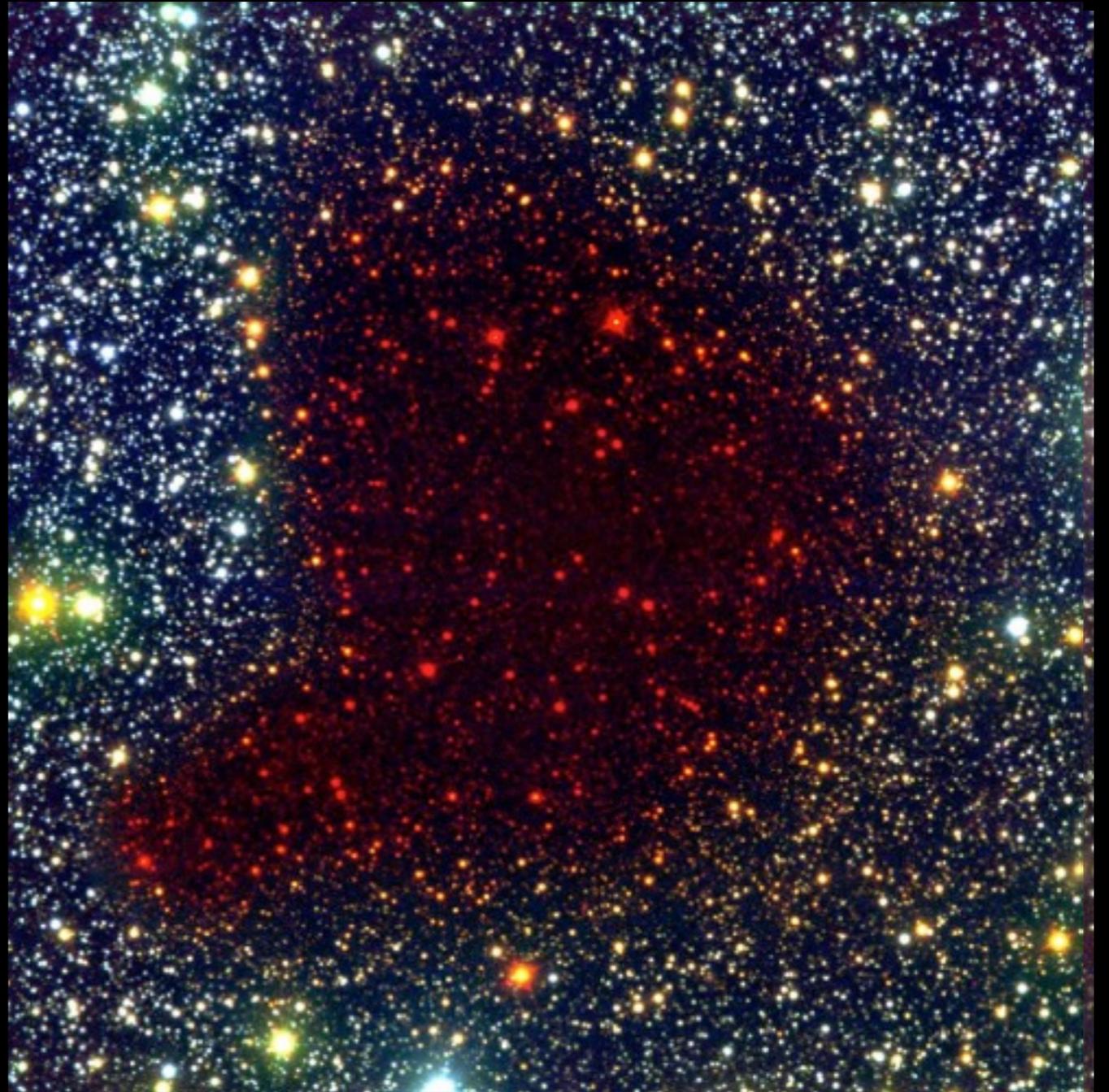
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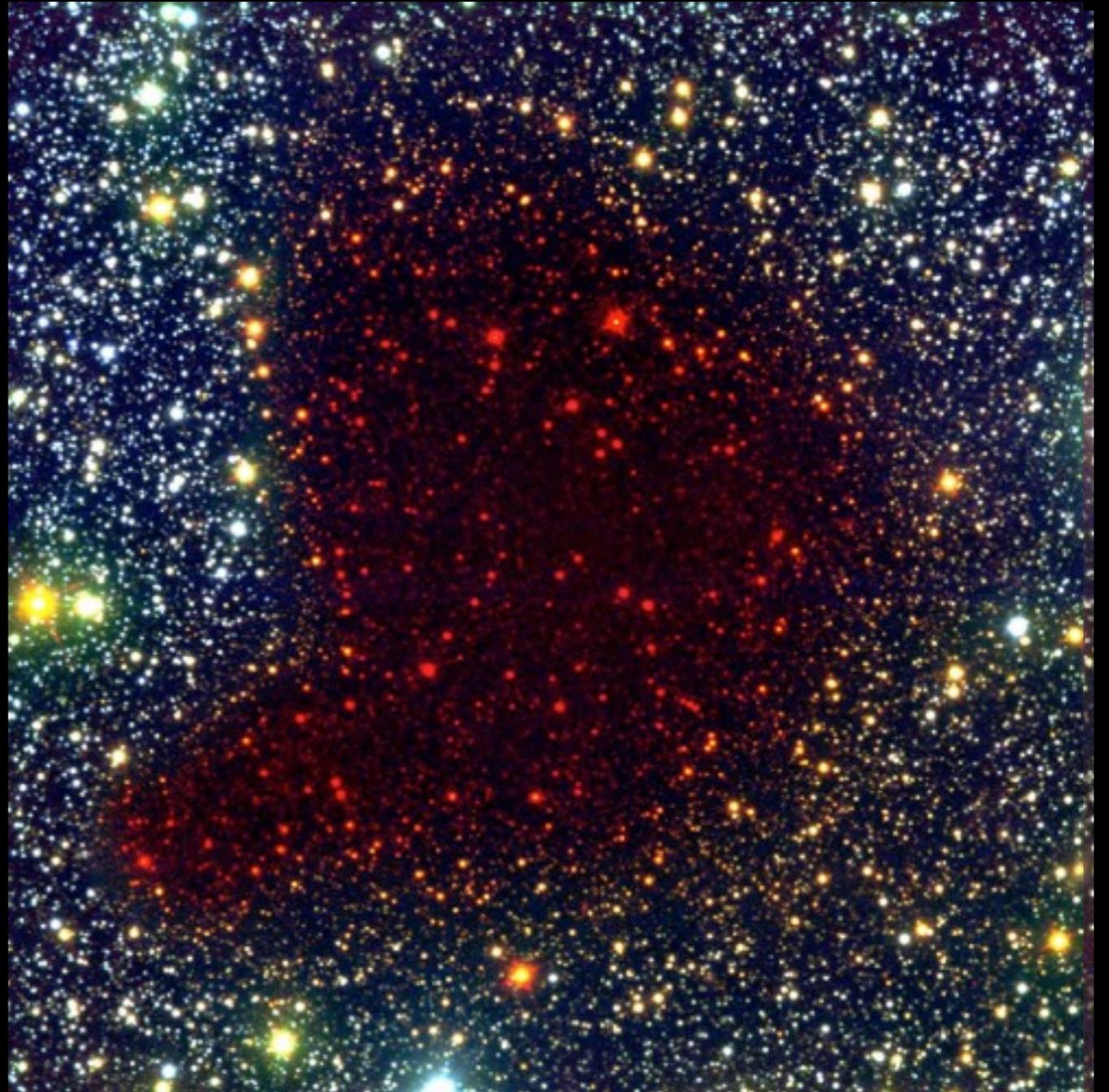
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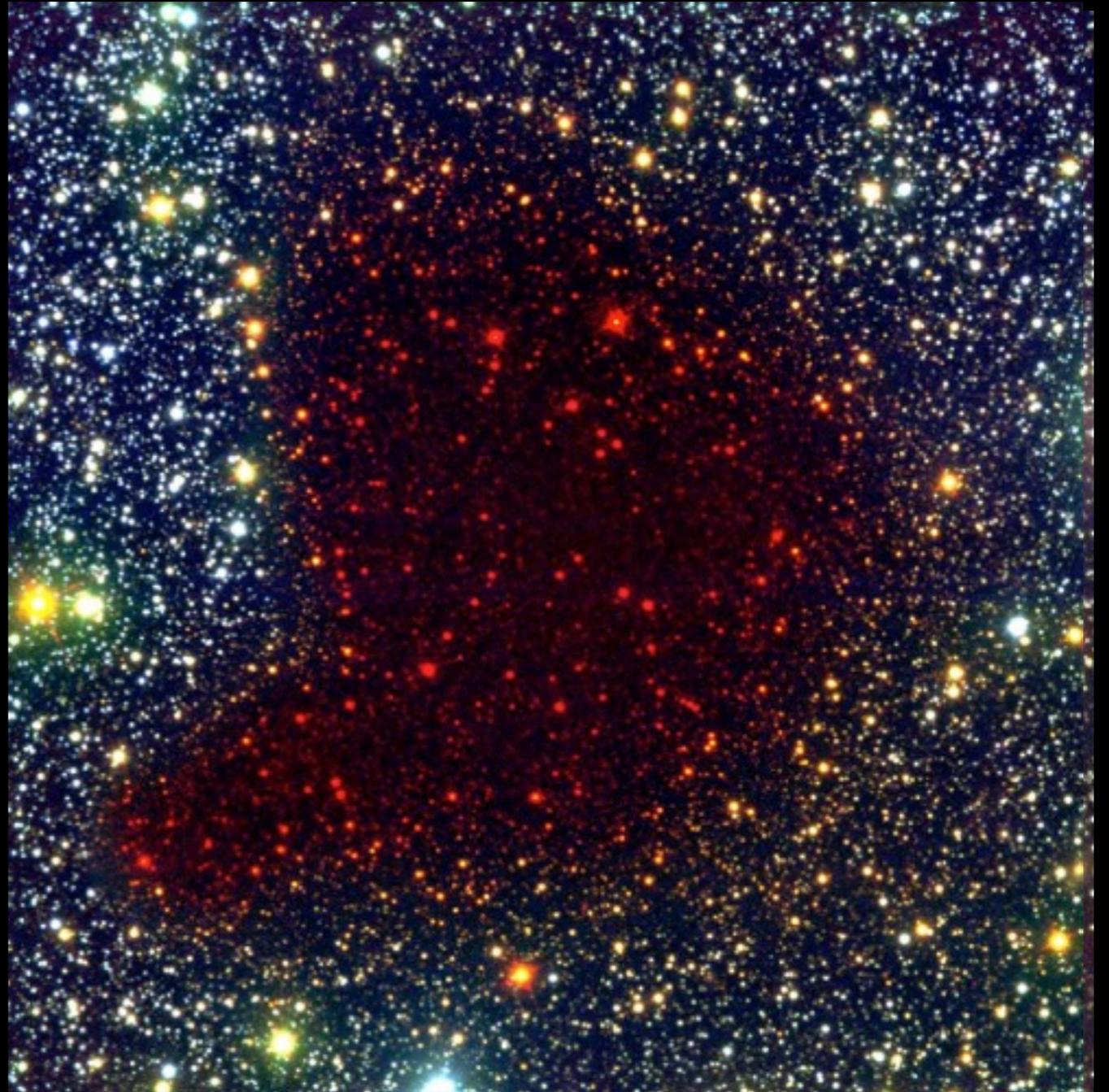
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$$\Sigma_{\text{gas}} \sim \Sigma_{\text{dust}} \sim E(H - K)$$



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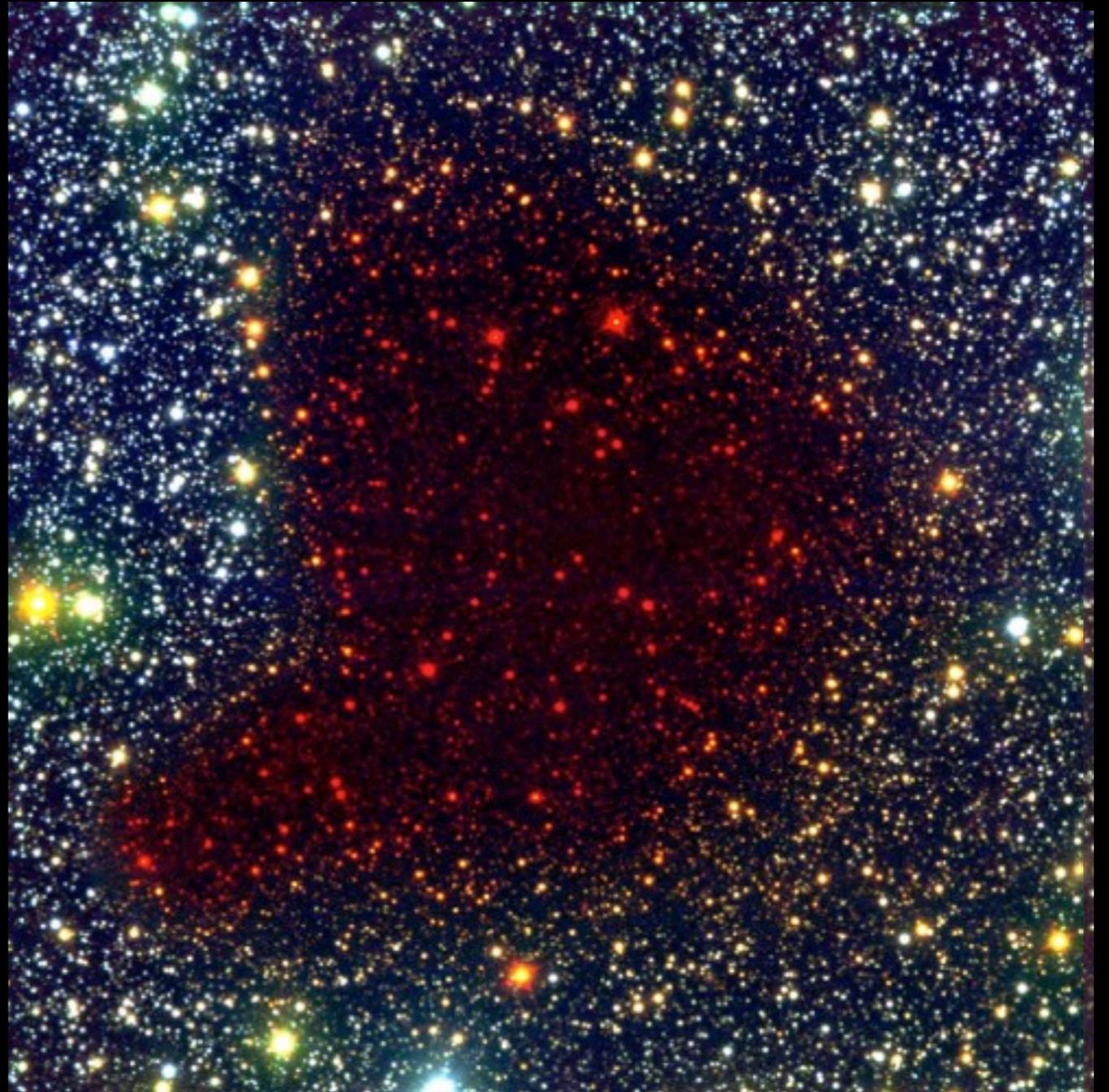
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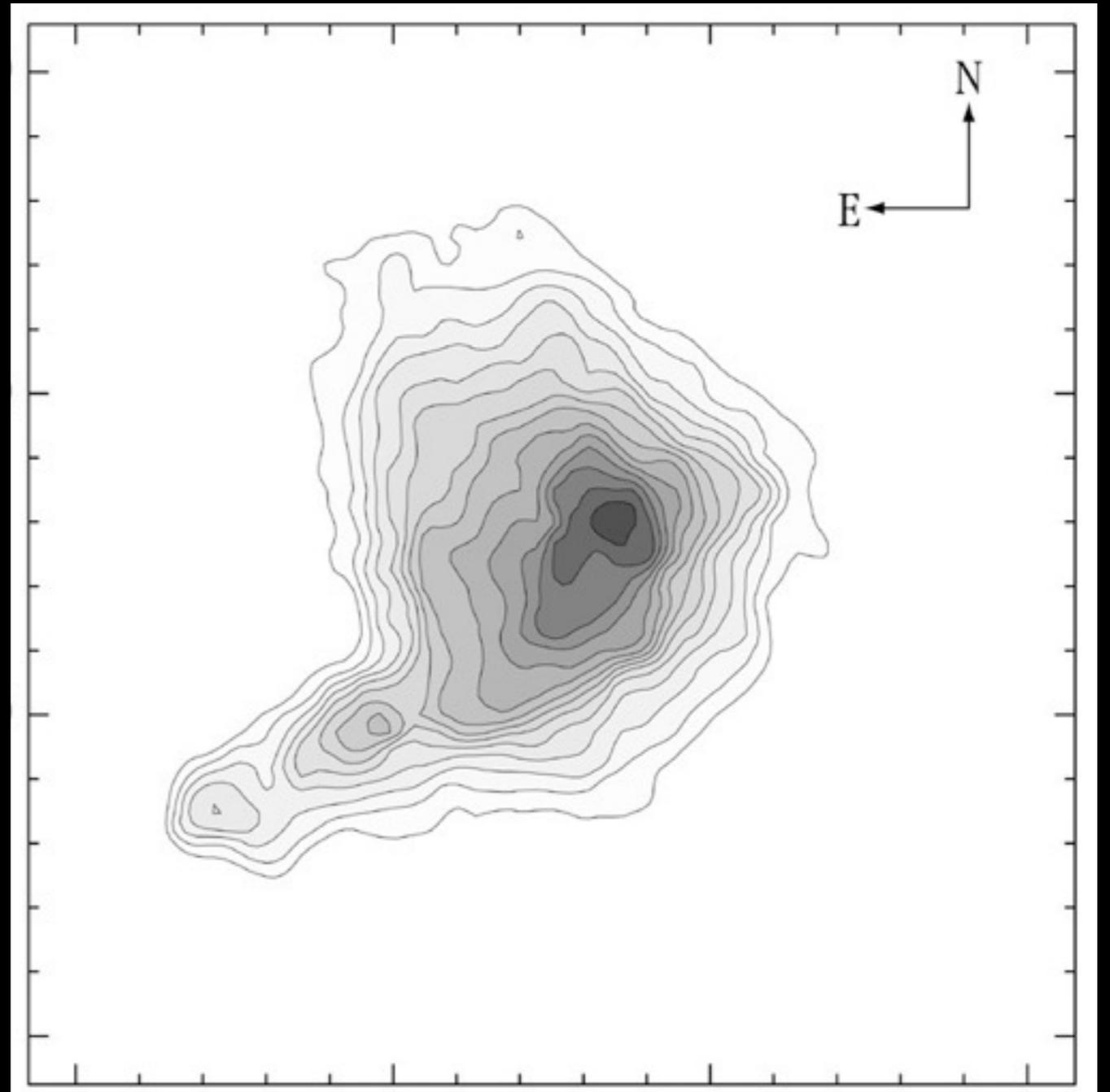
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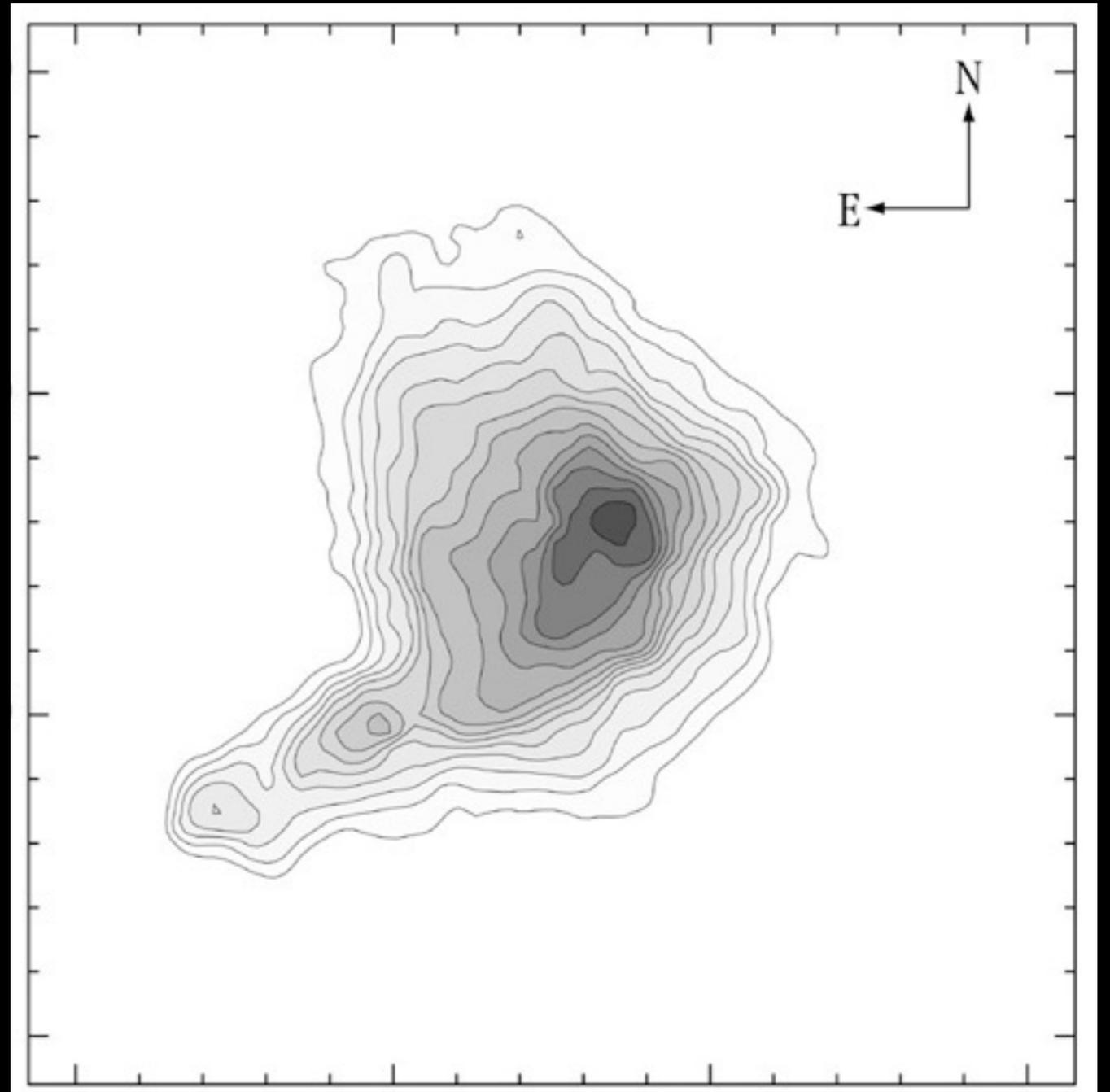
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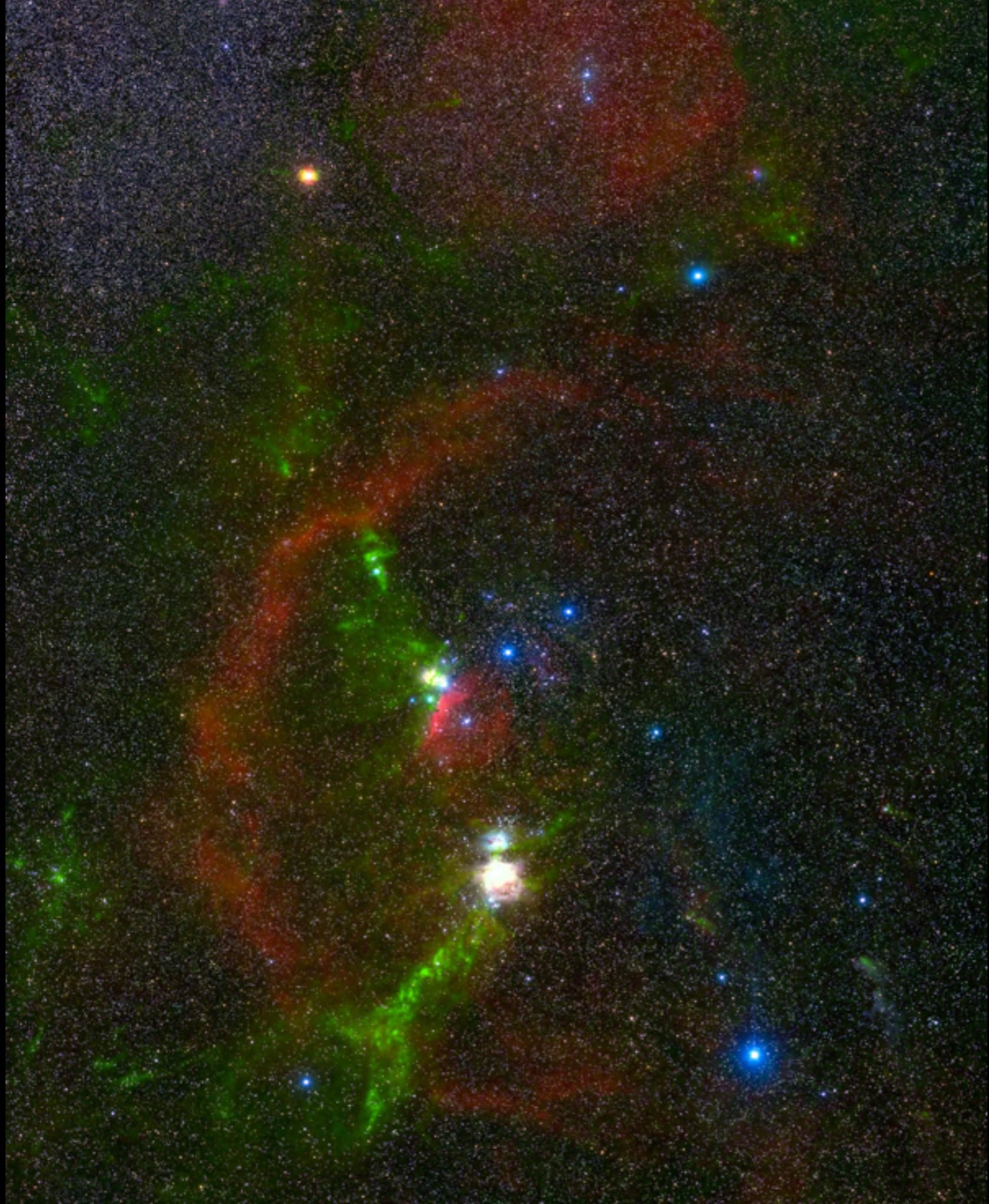
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- Convert extinction into gas column density



Alves et al. (2014)

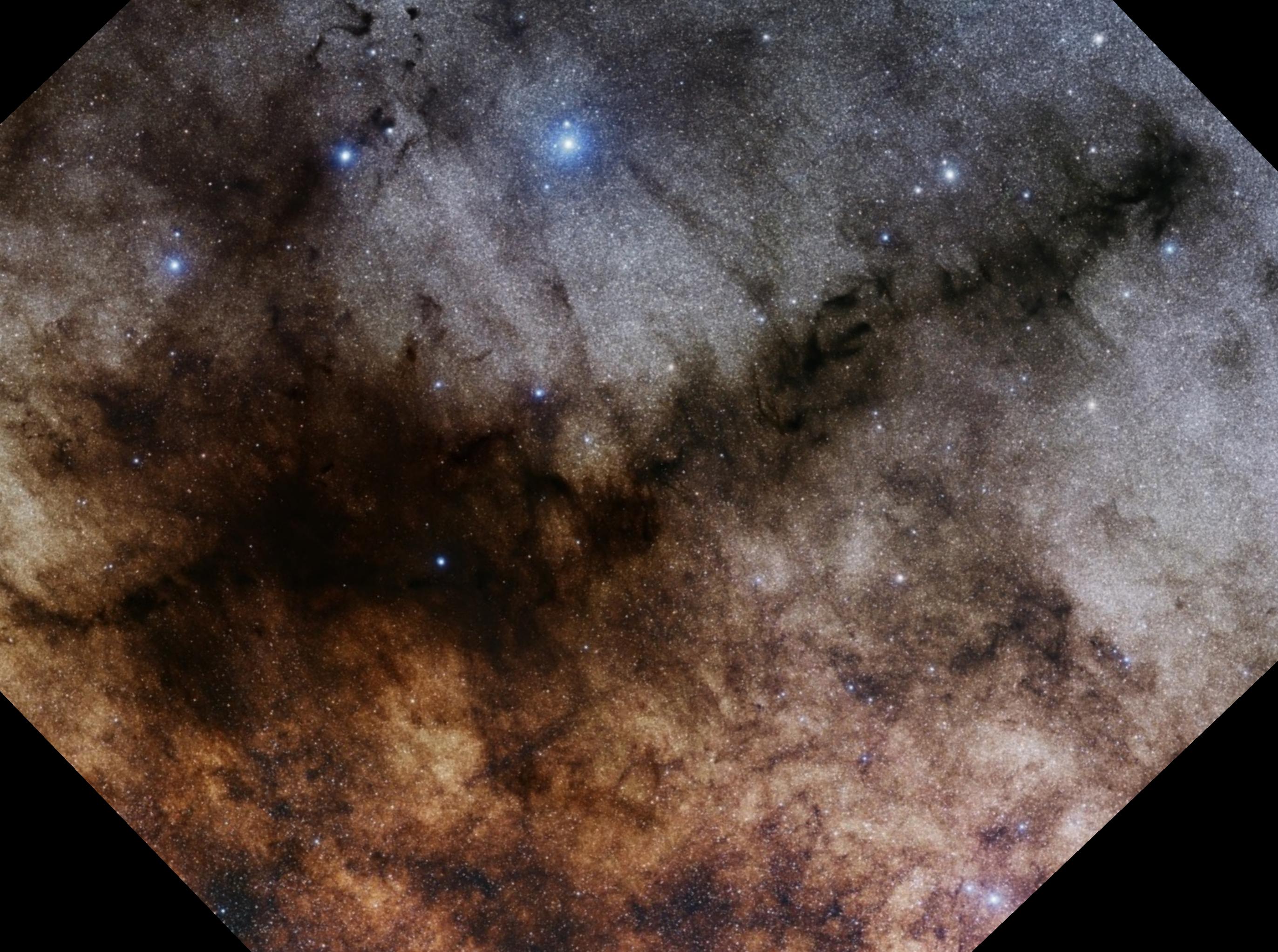


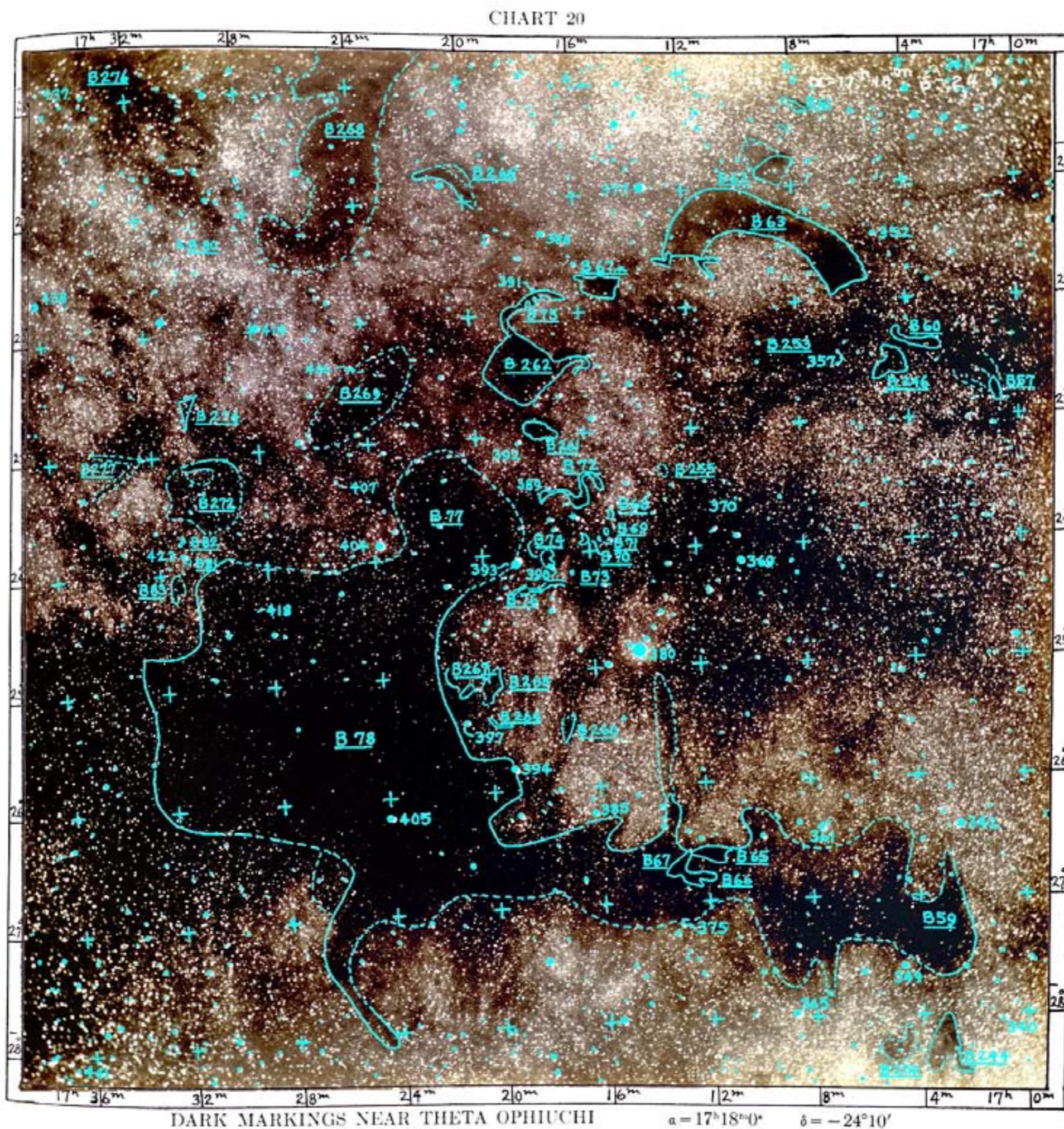


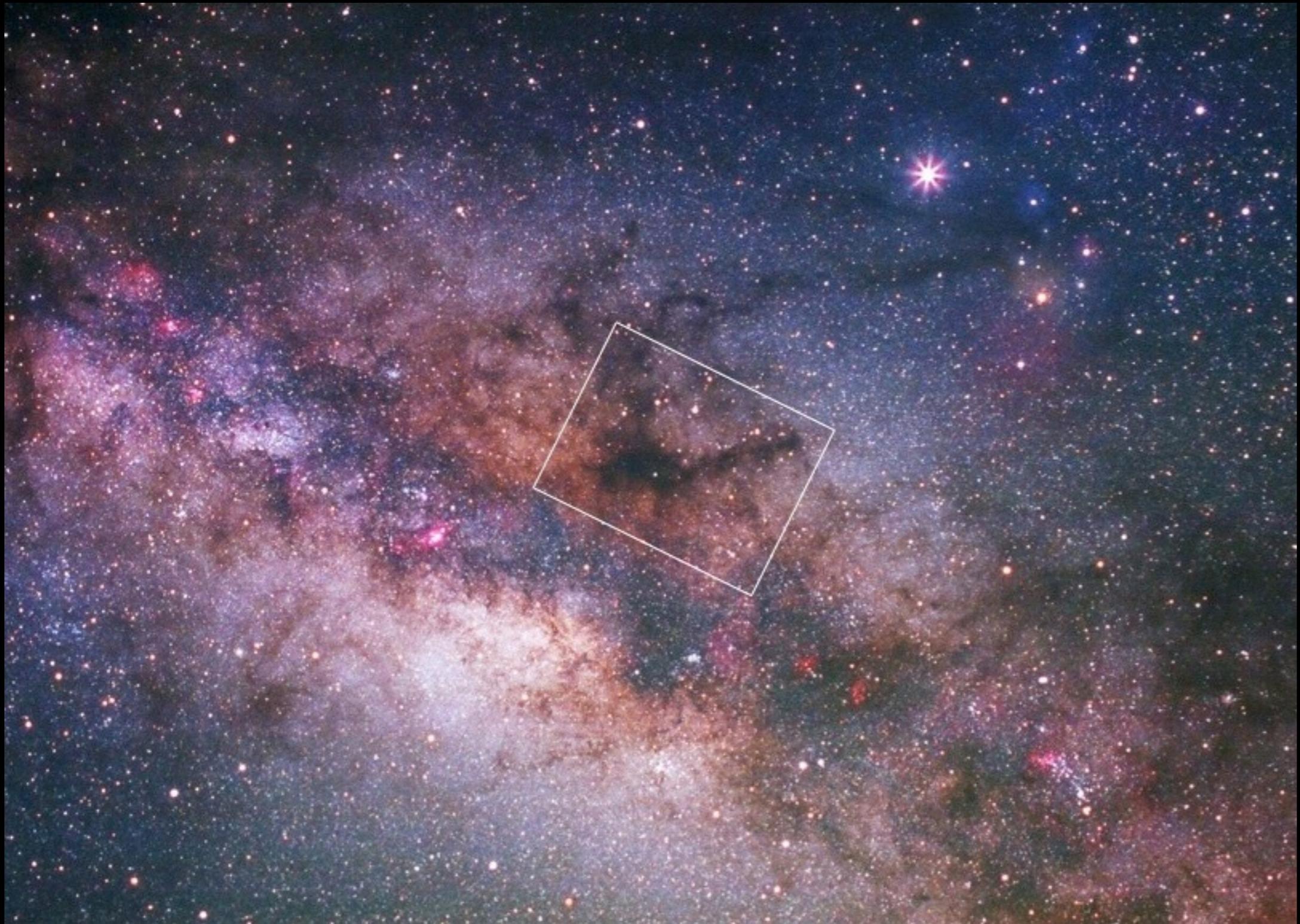


*Ceci n'est pas une pipe.*

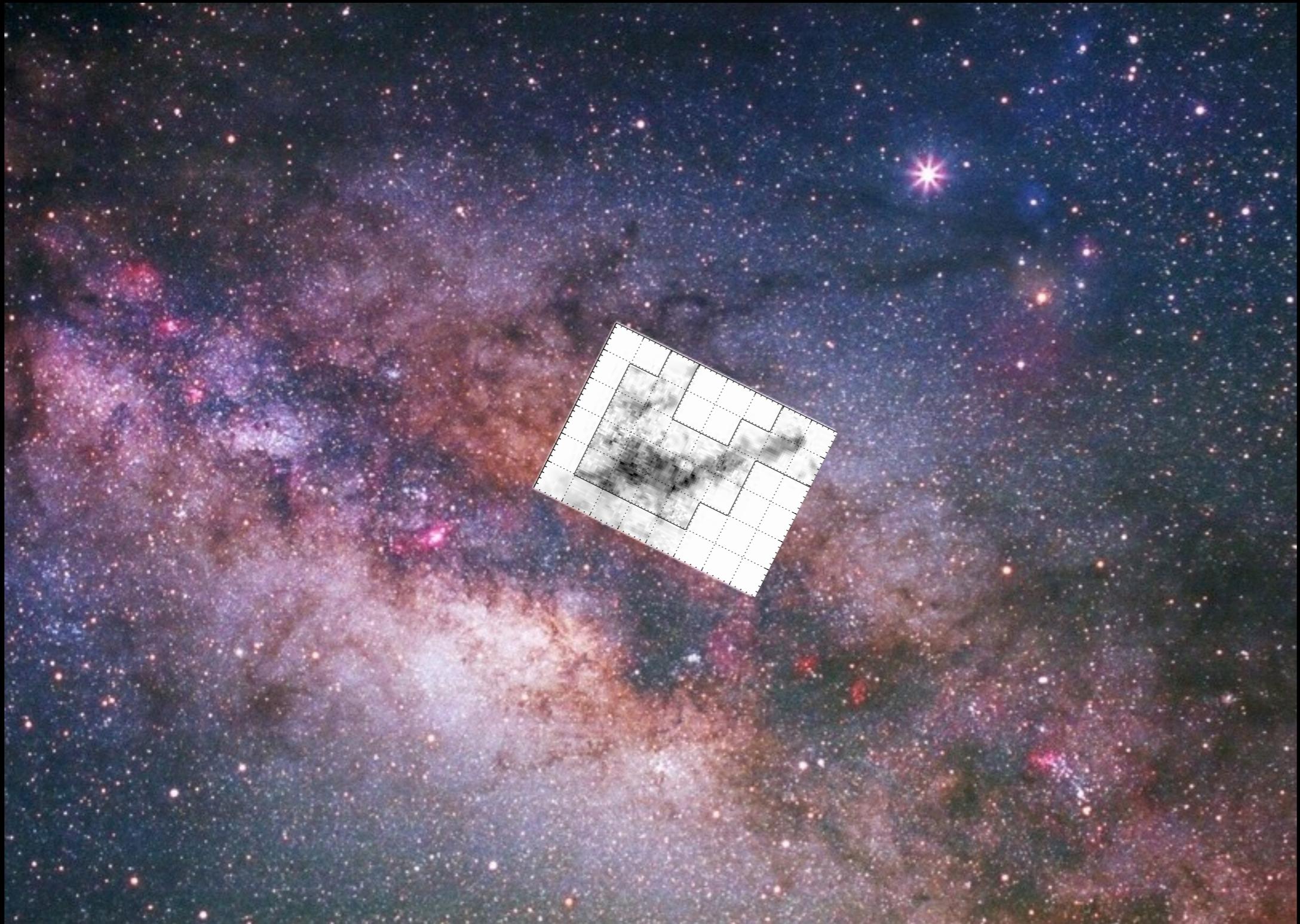






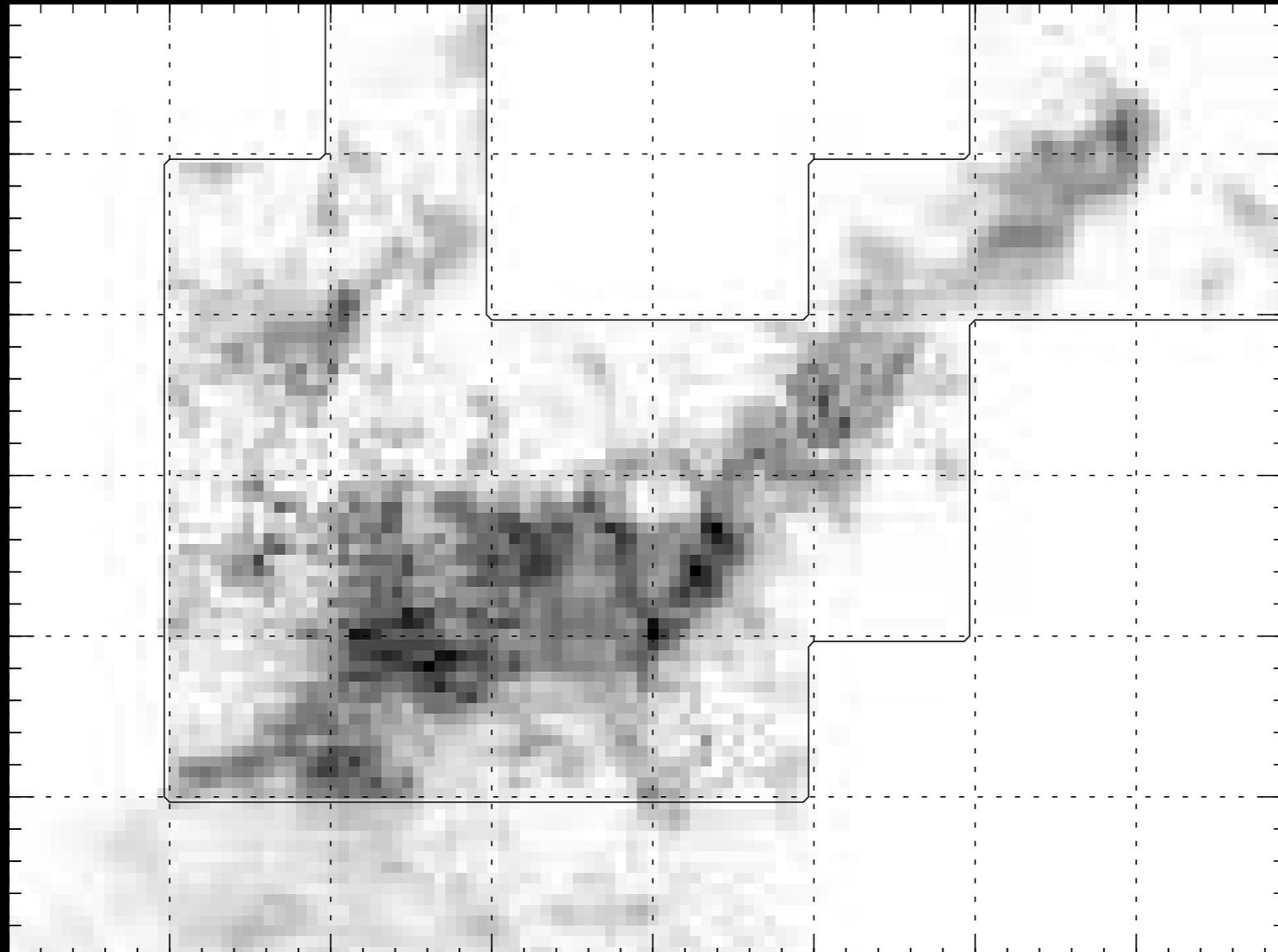


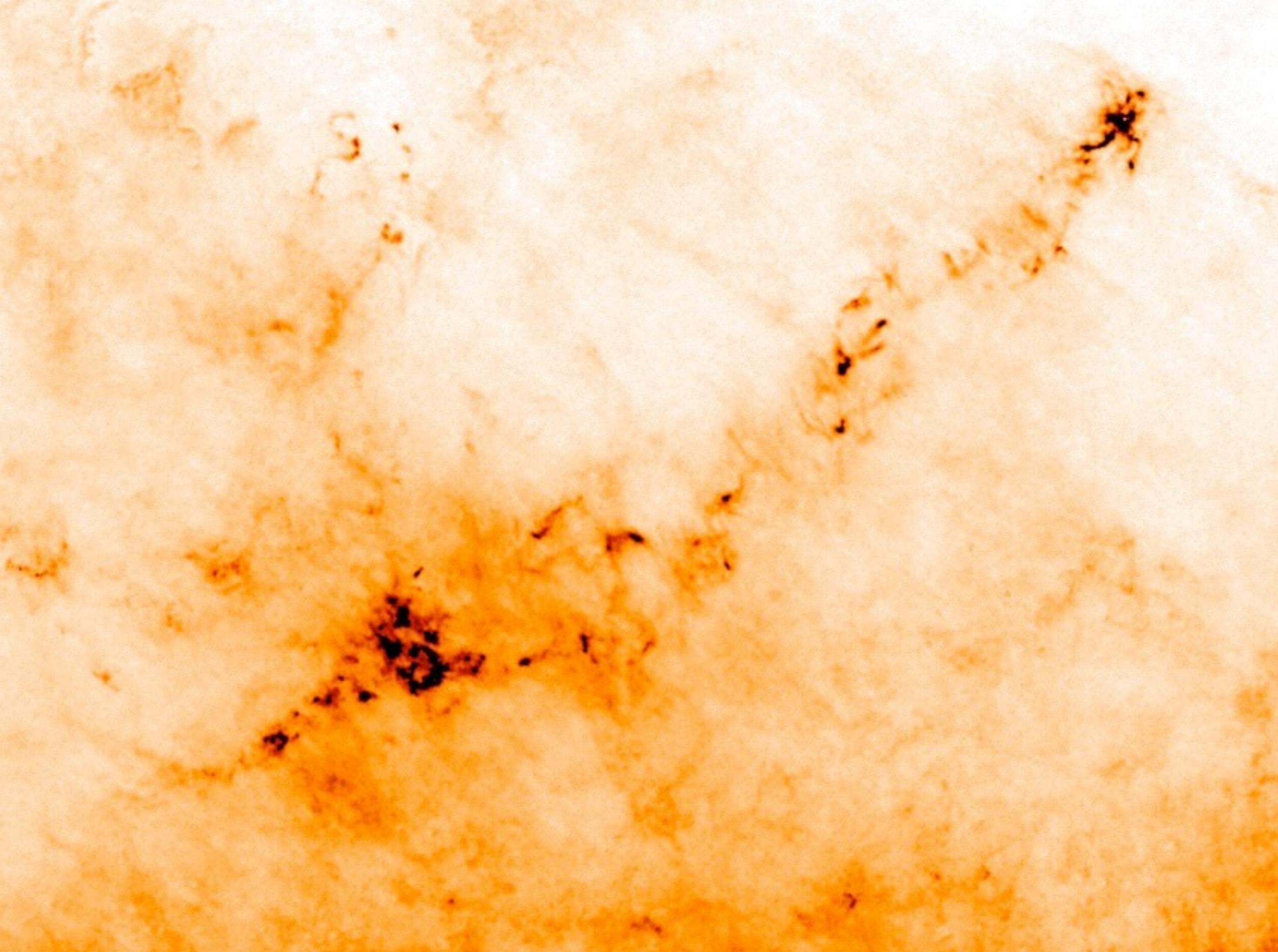
# The Pipe Nebula

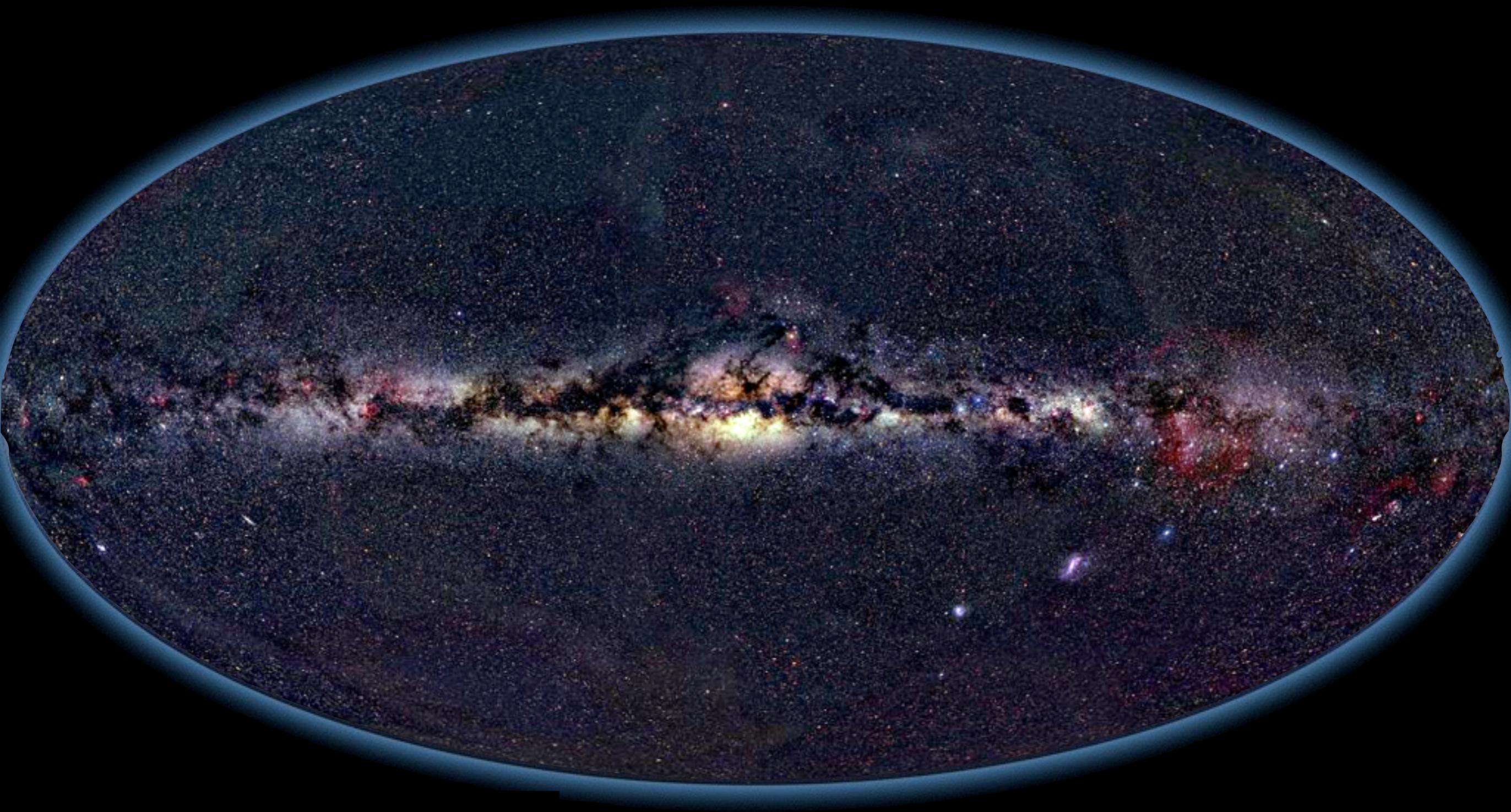


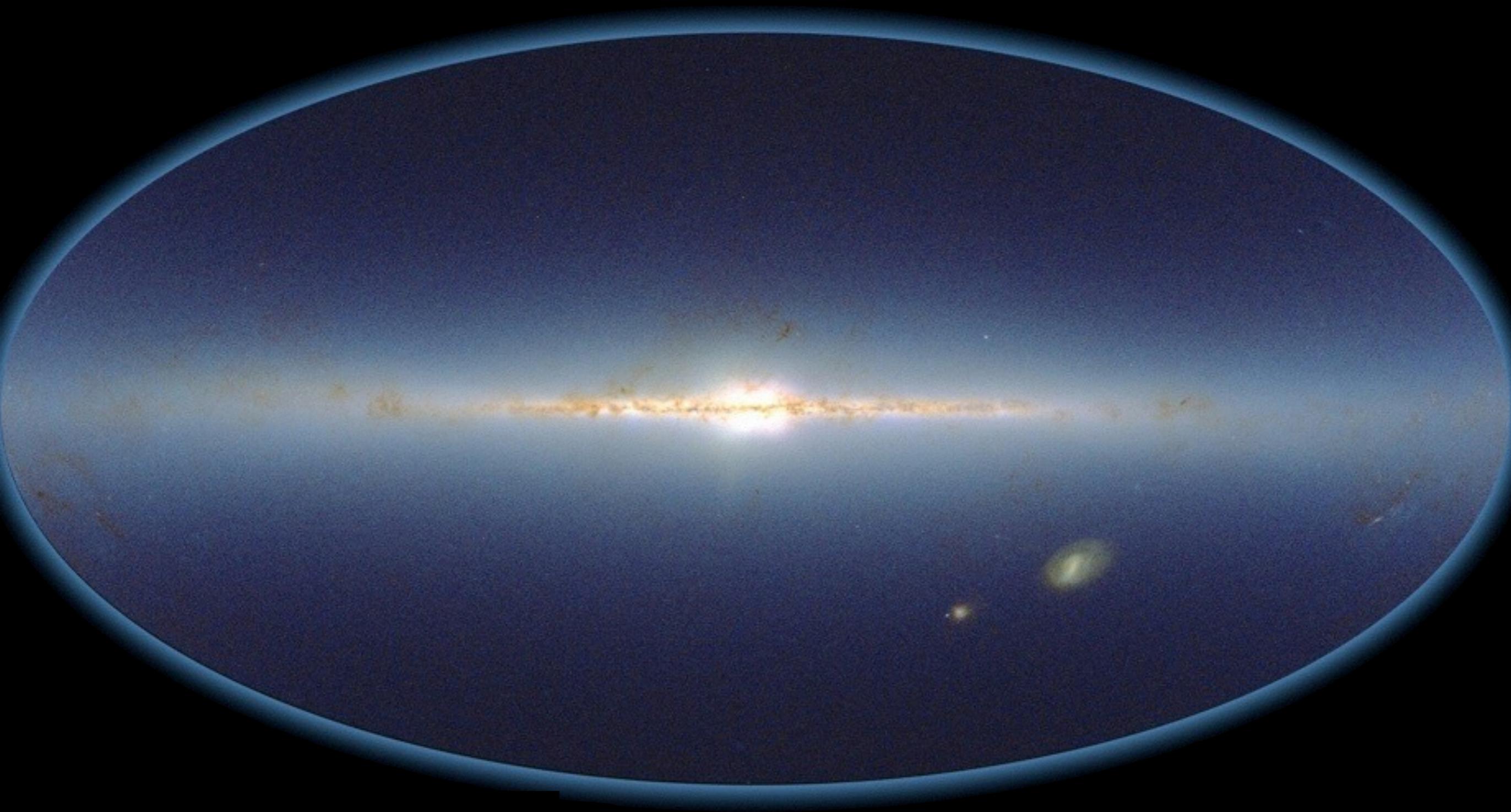
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# Extinction map



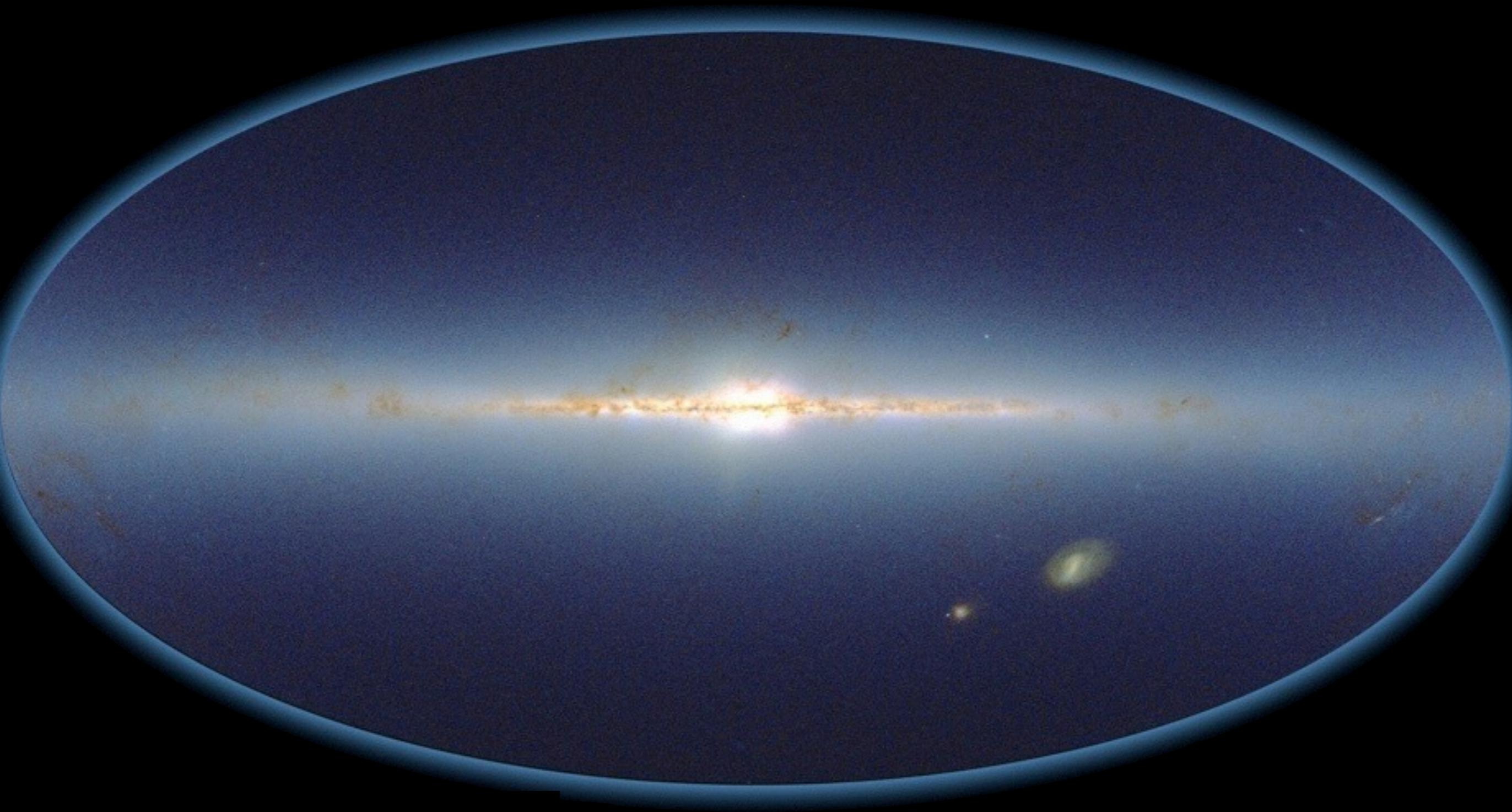




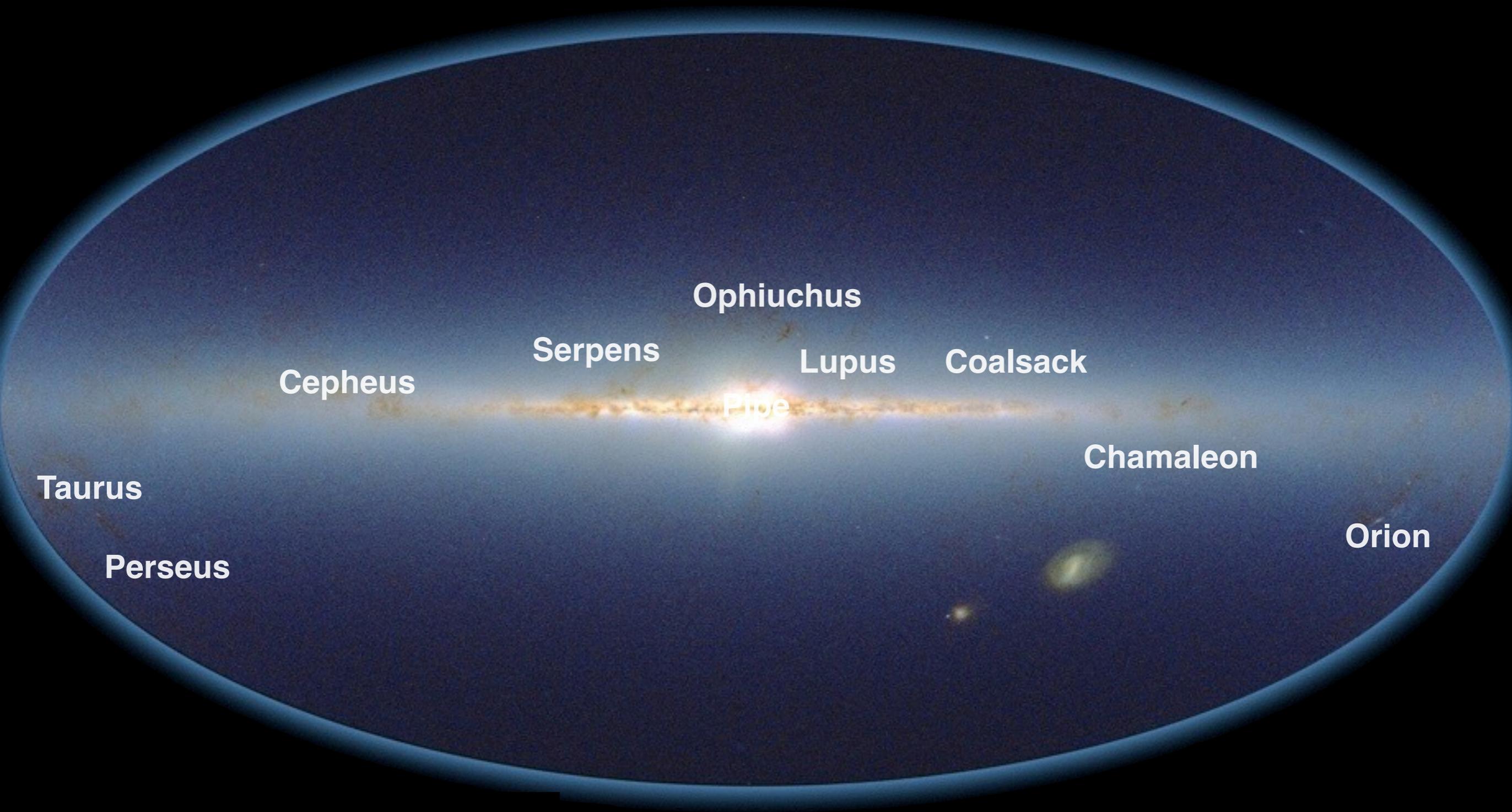


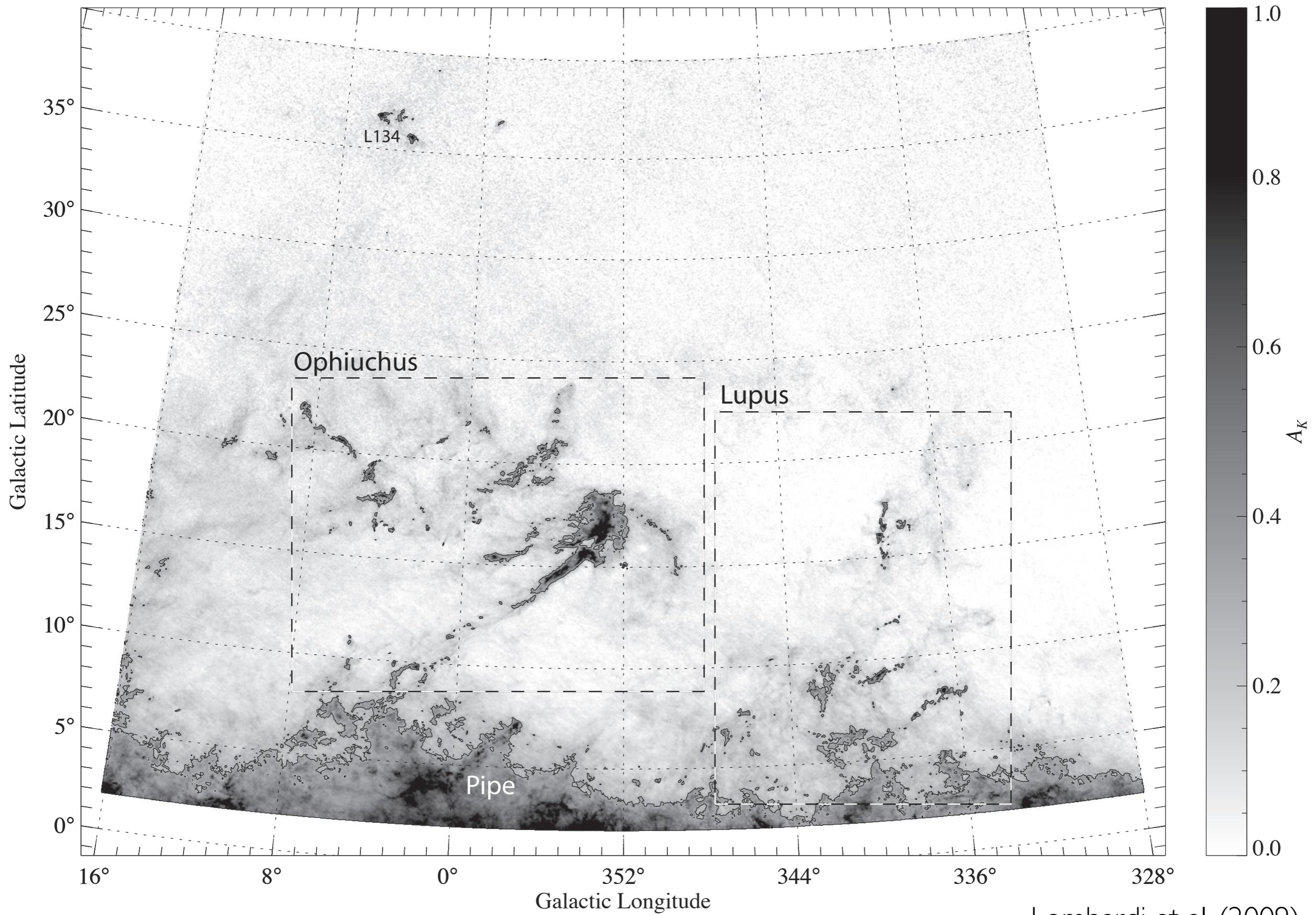
2MASS

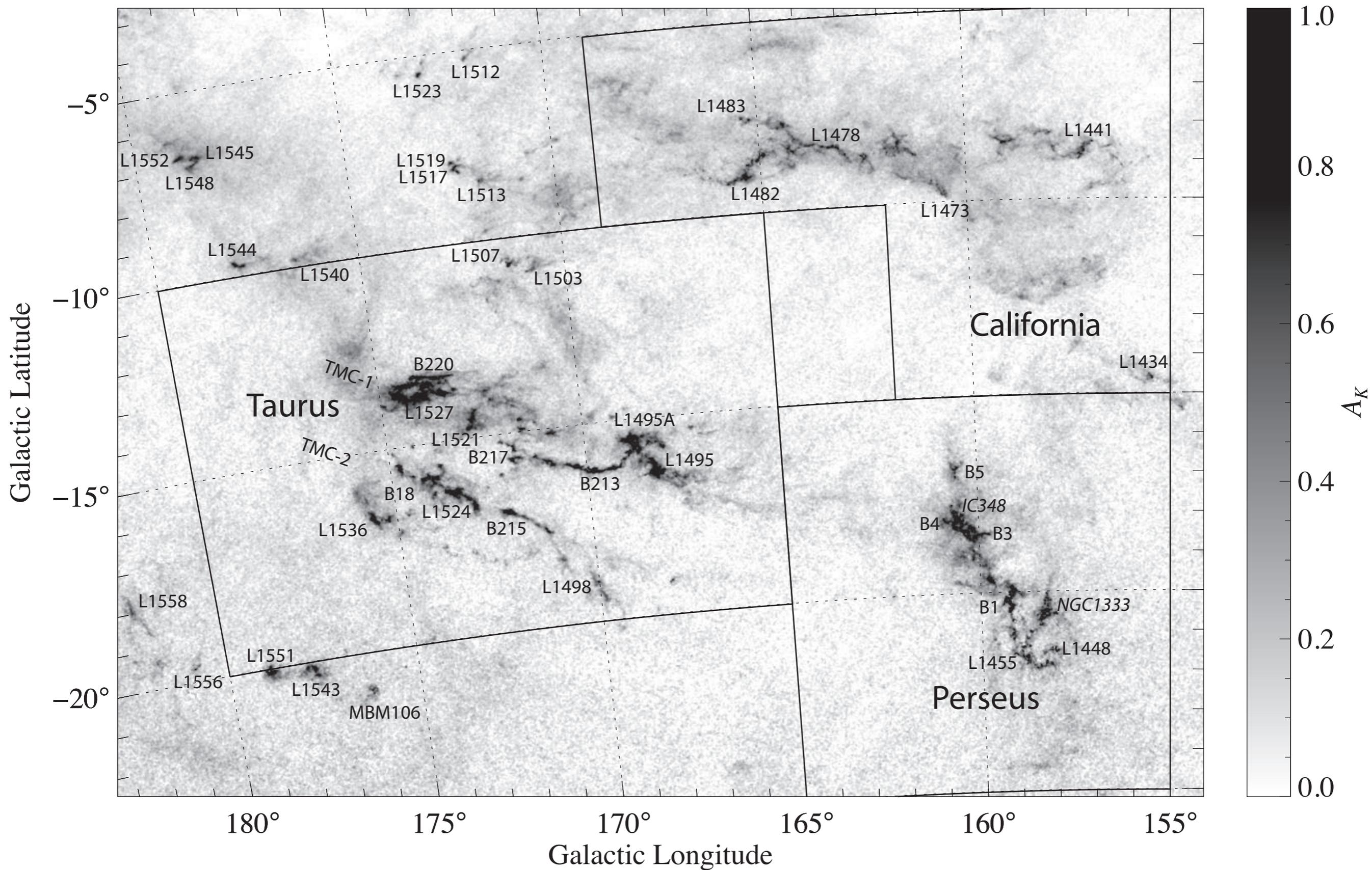
# Gould belt

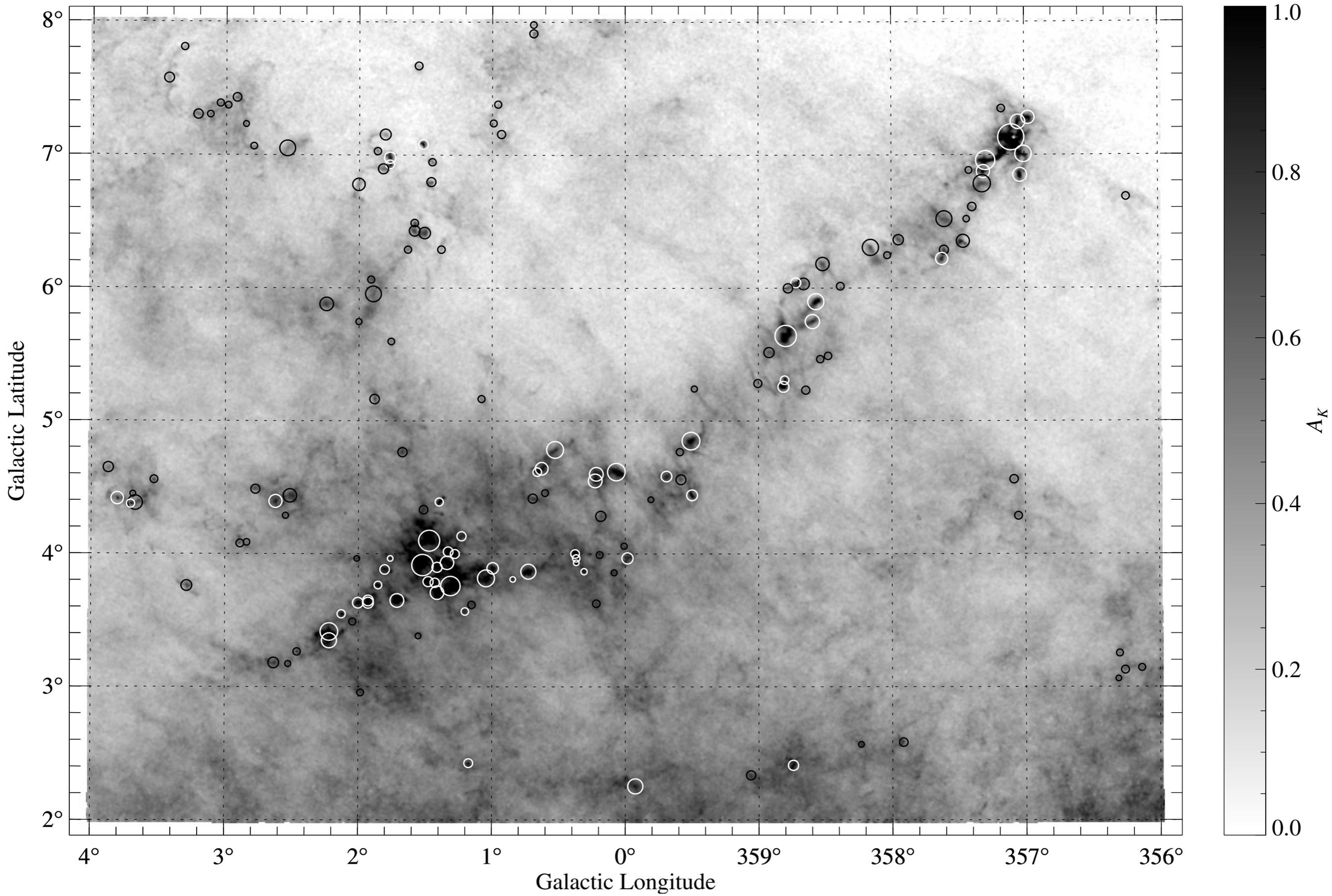


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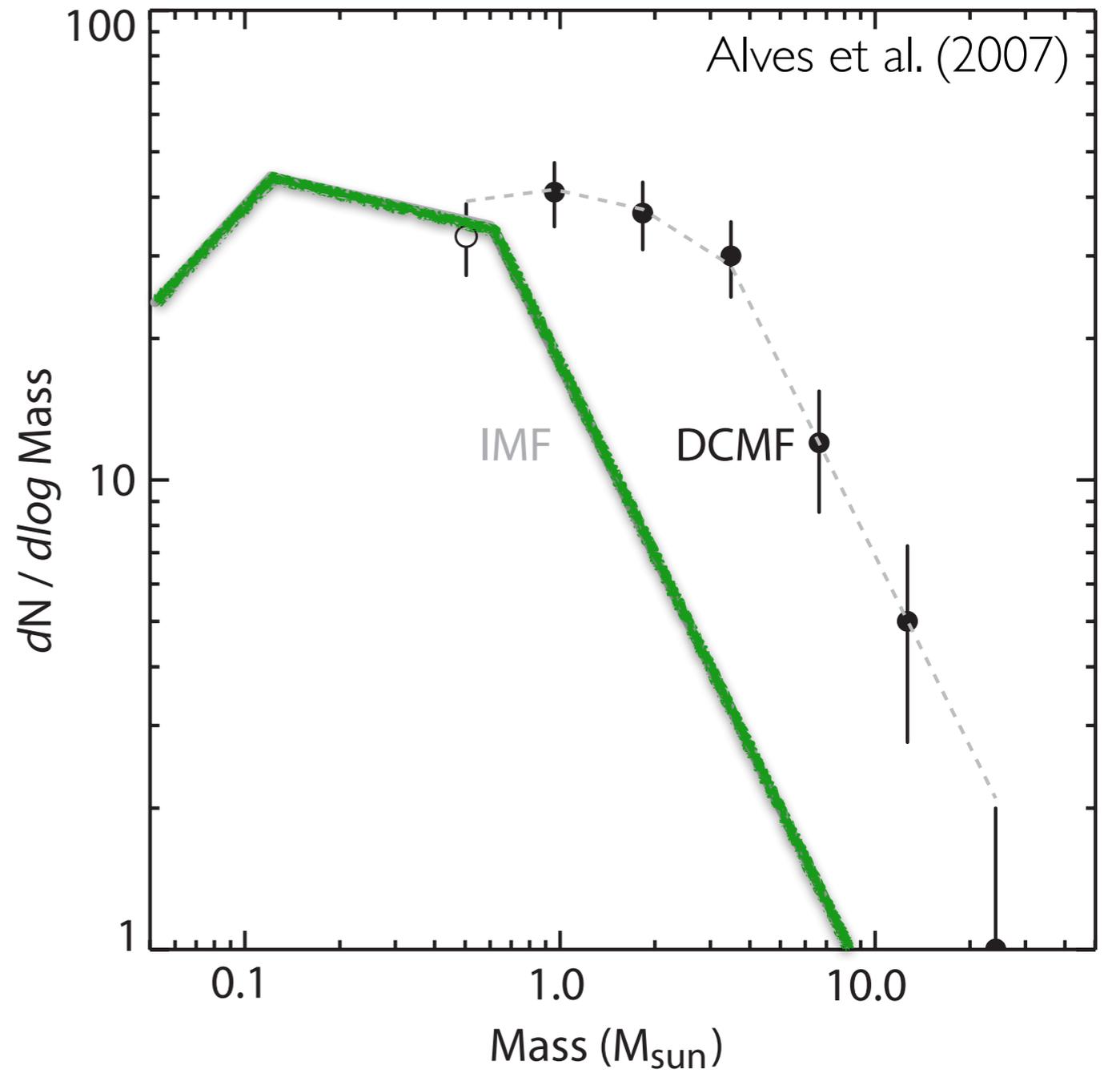




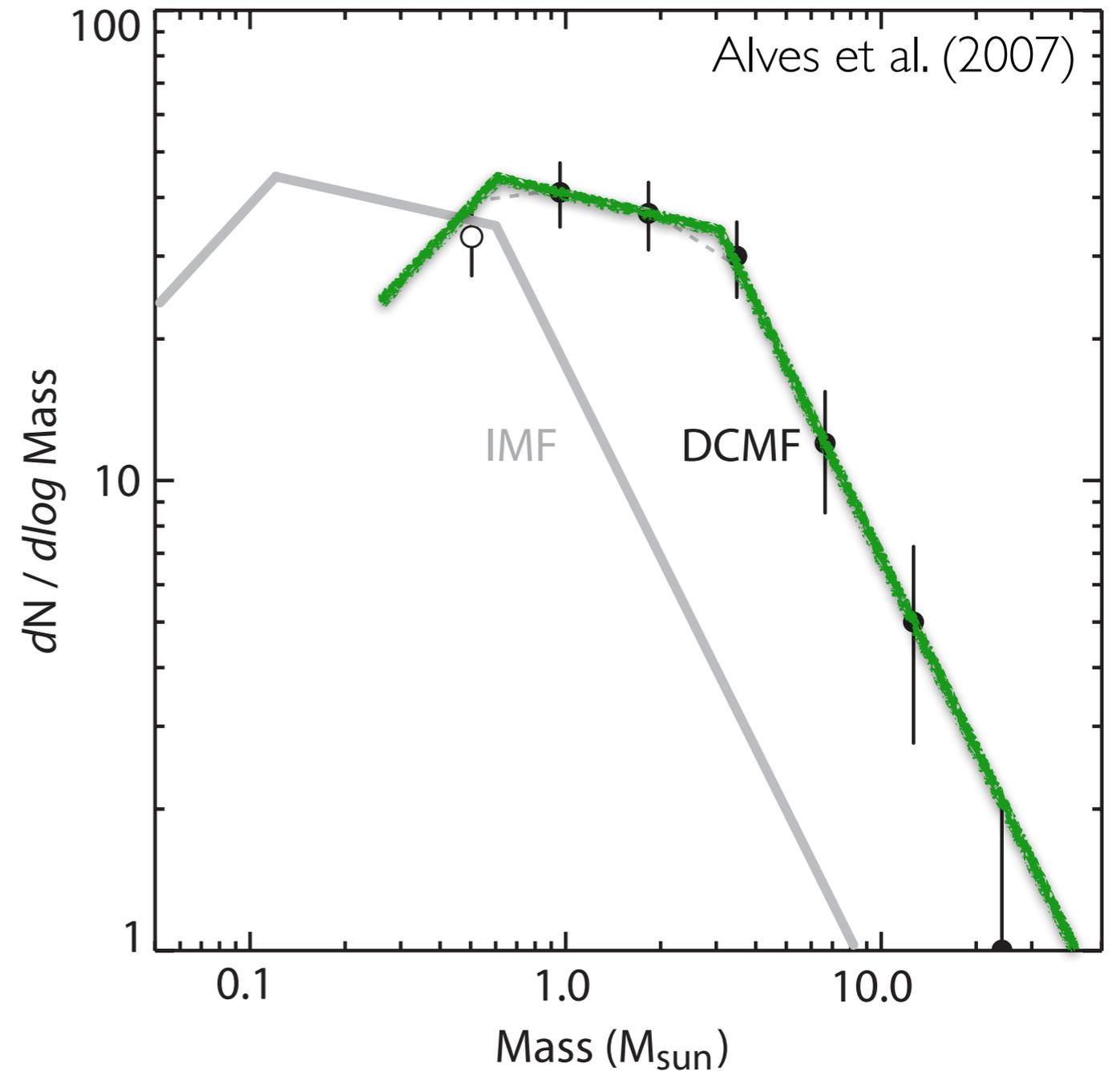




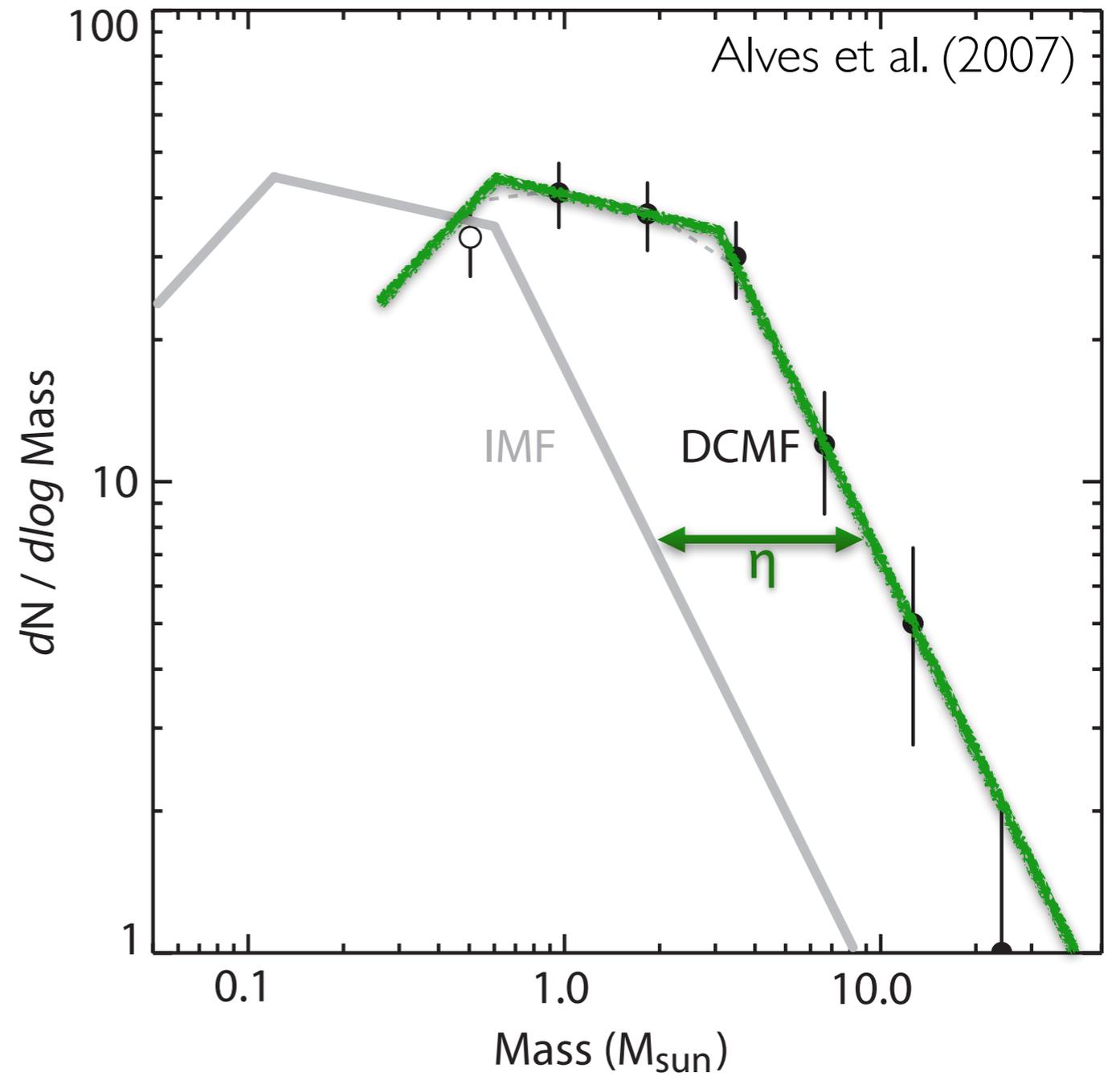
Alves et al. (2007)



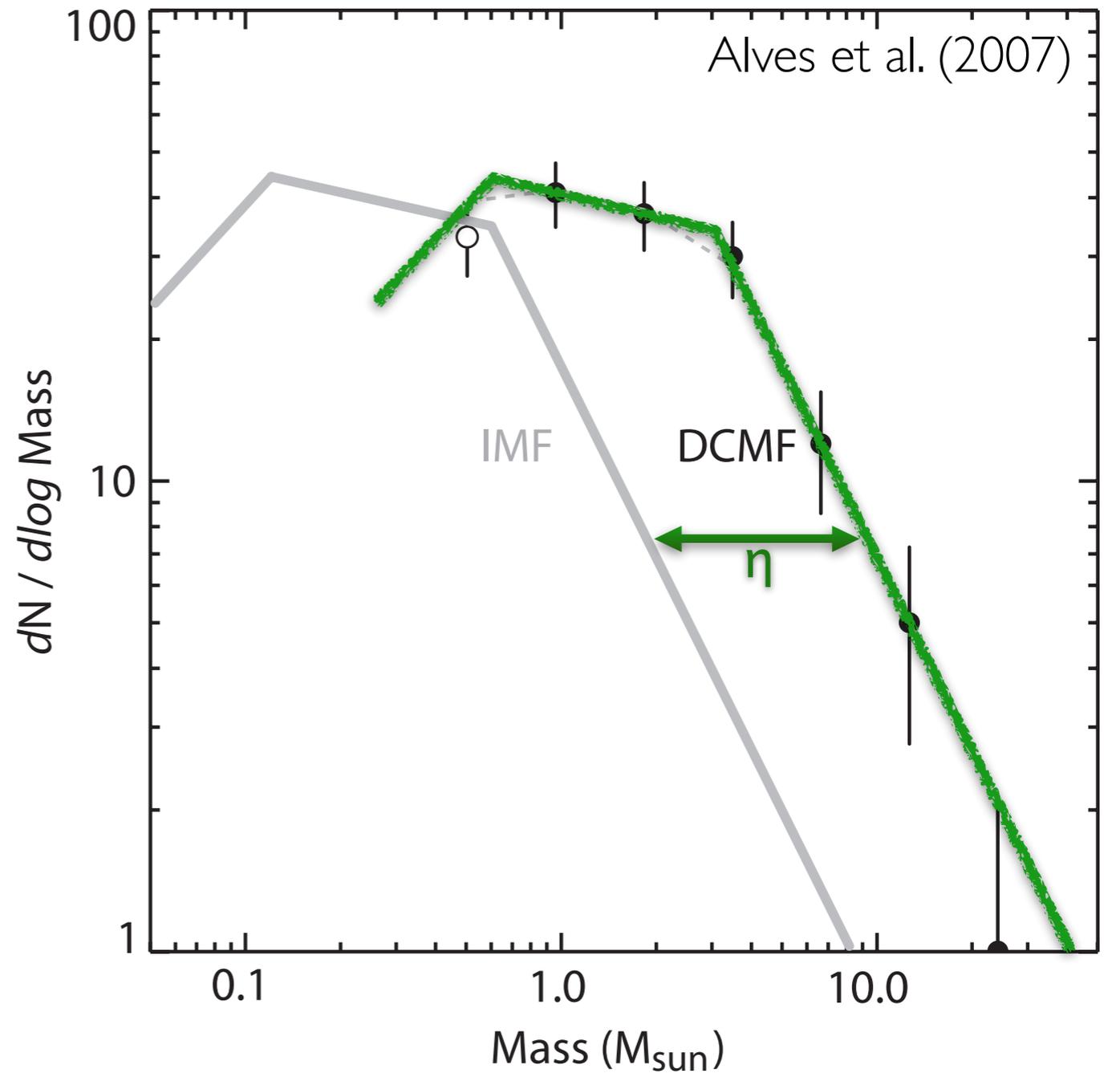
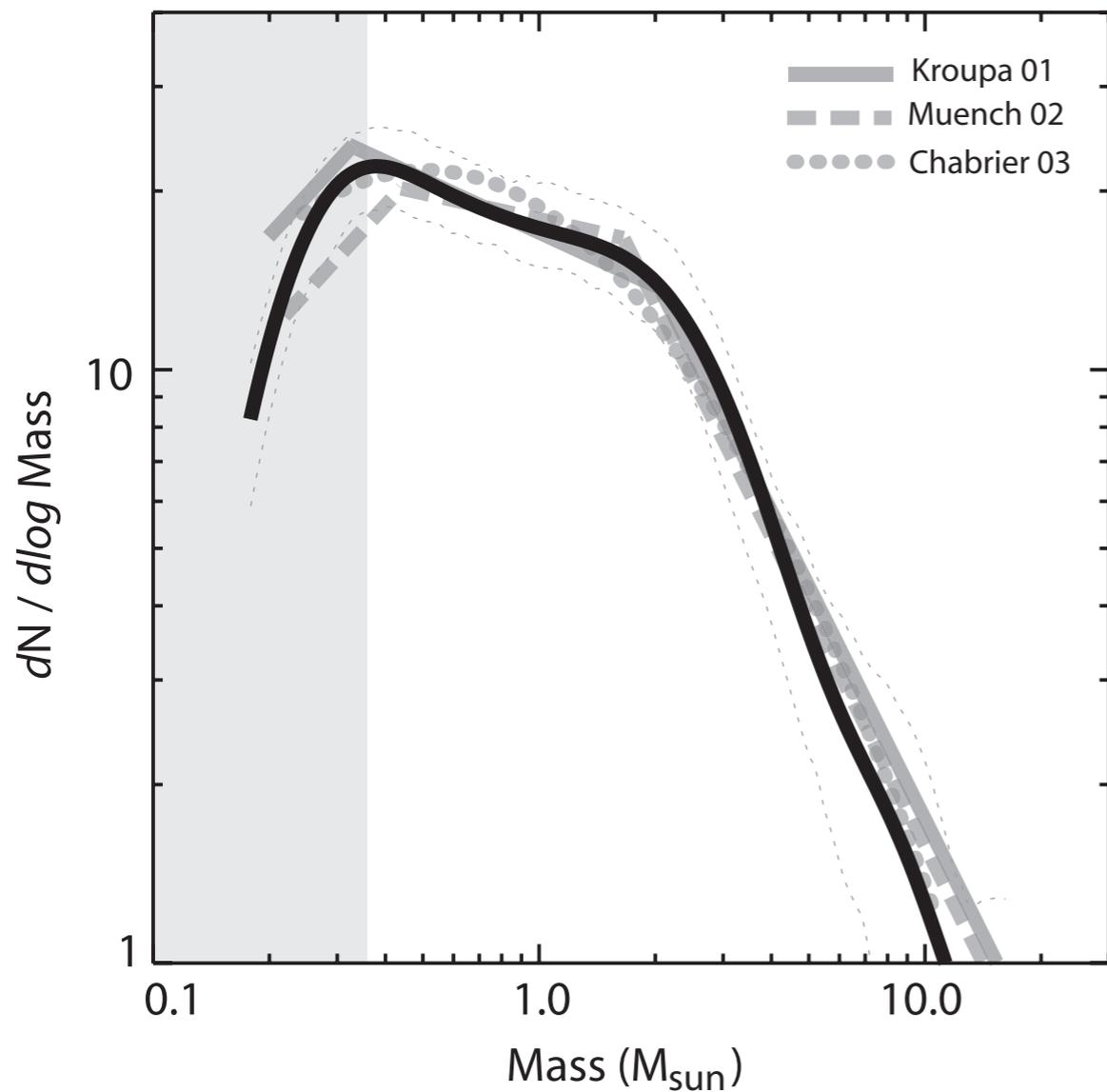
- The dense core mass function (DCMF) has the same shape as the IMF



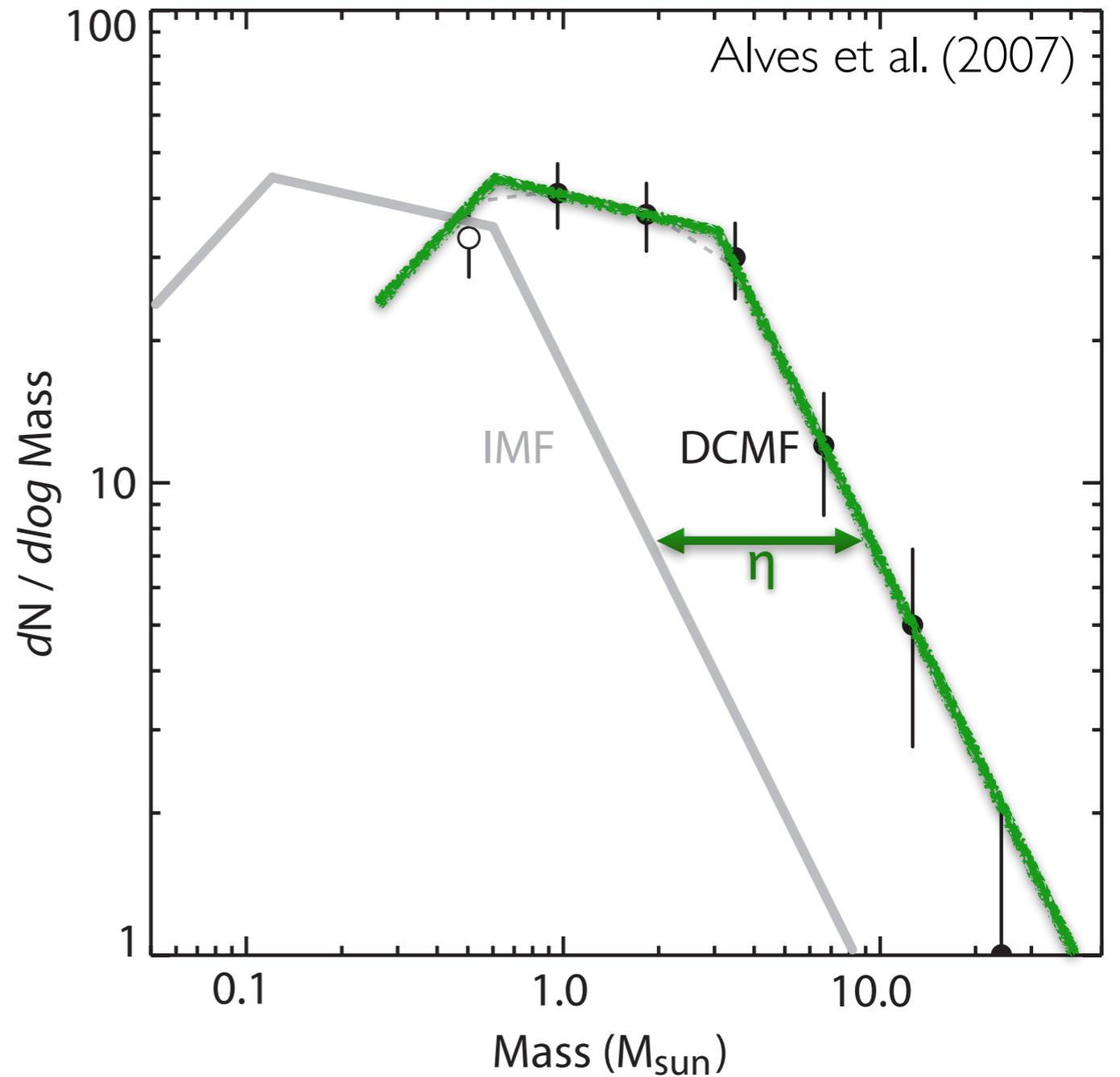
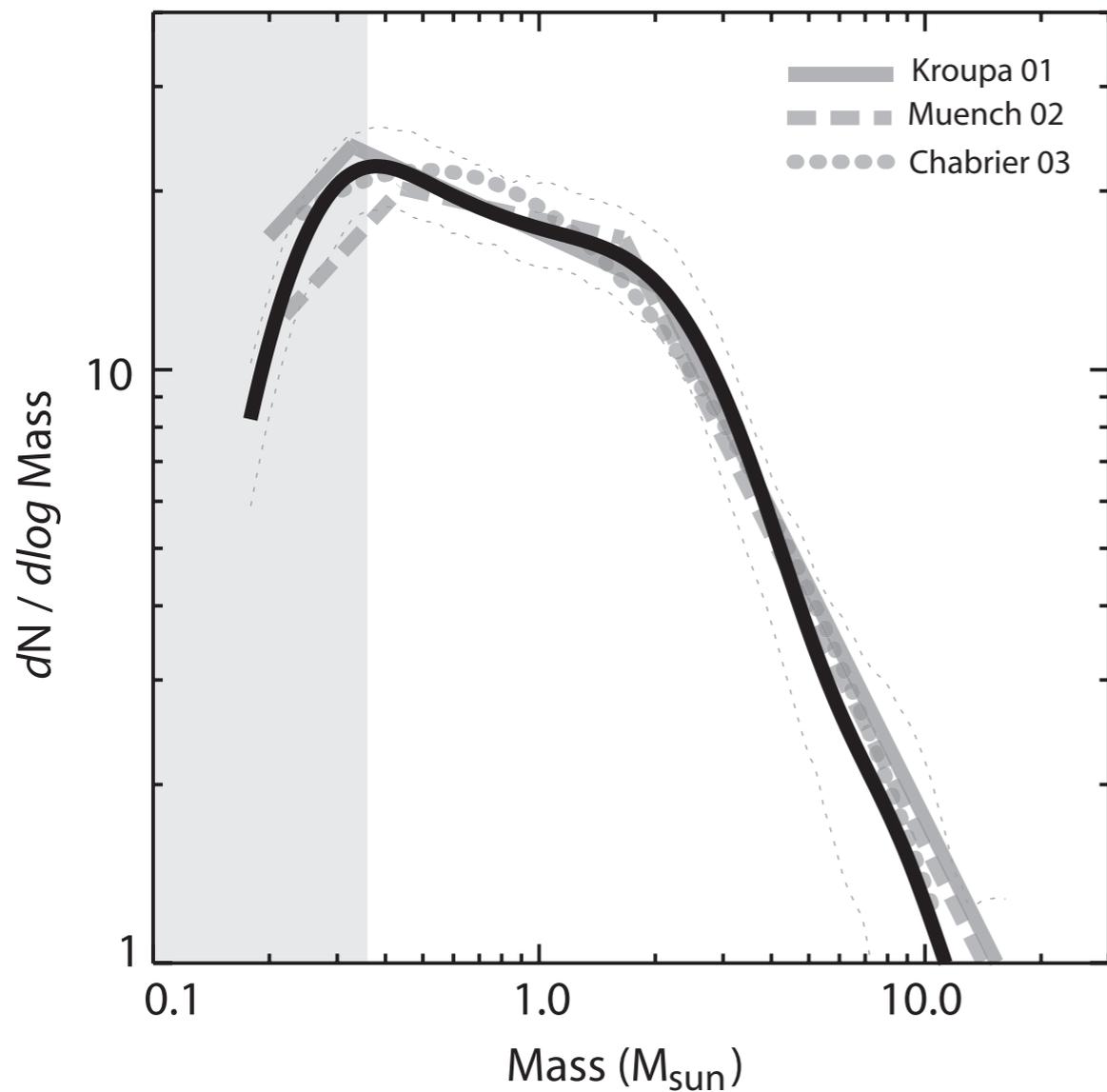
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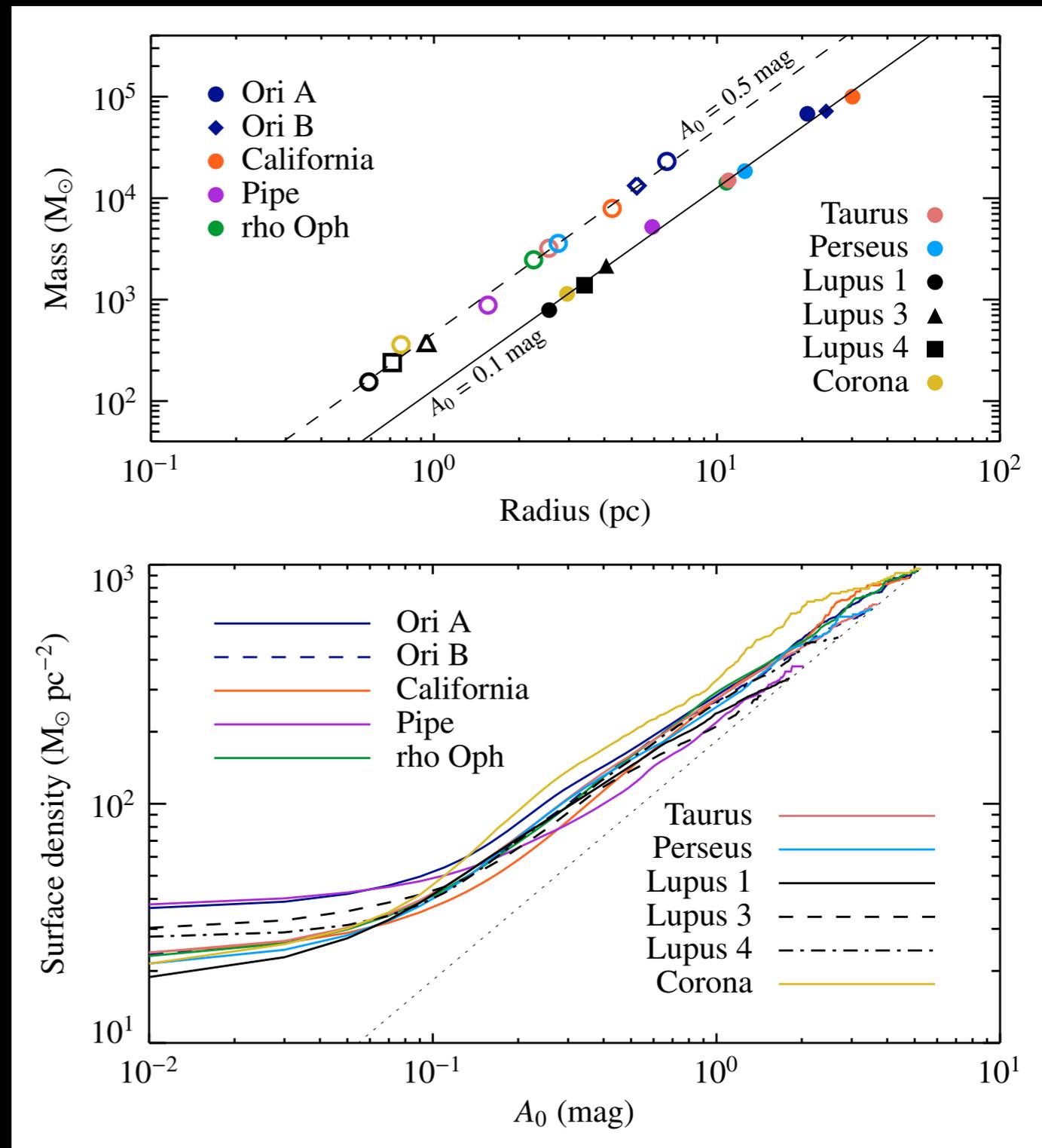


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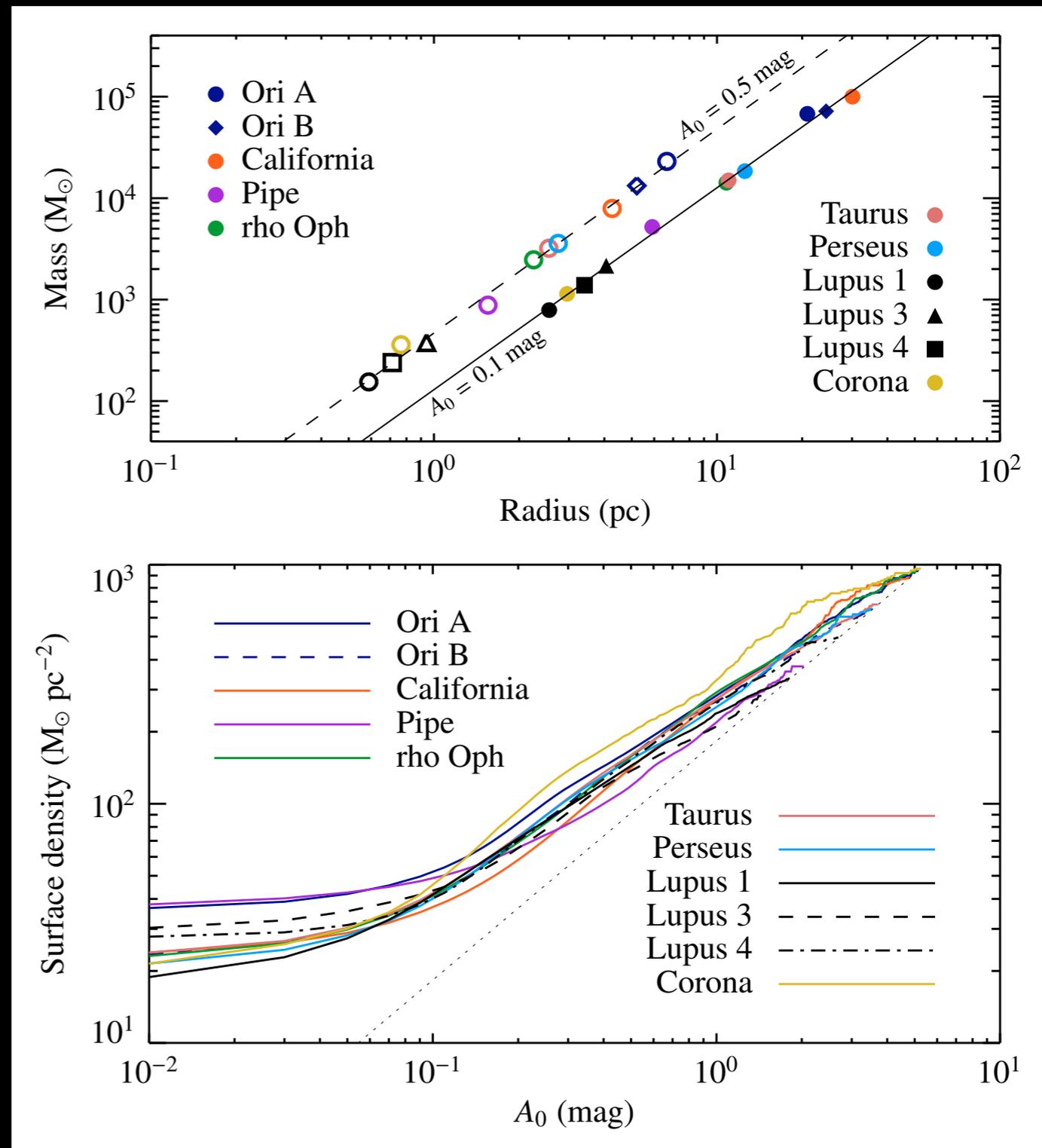
- Things might be more complicated (e.g., one core might fragment)

# Larson's 3rd law



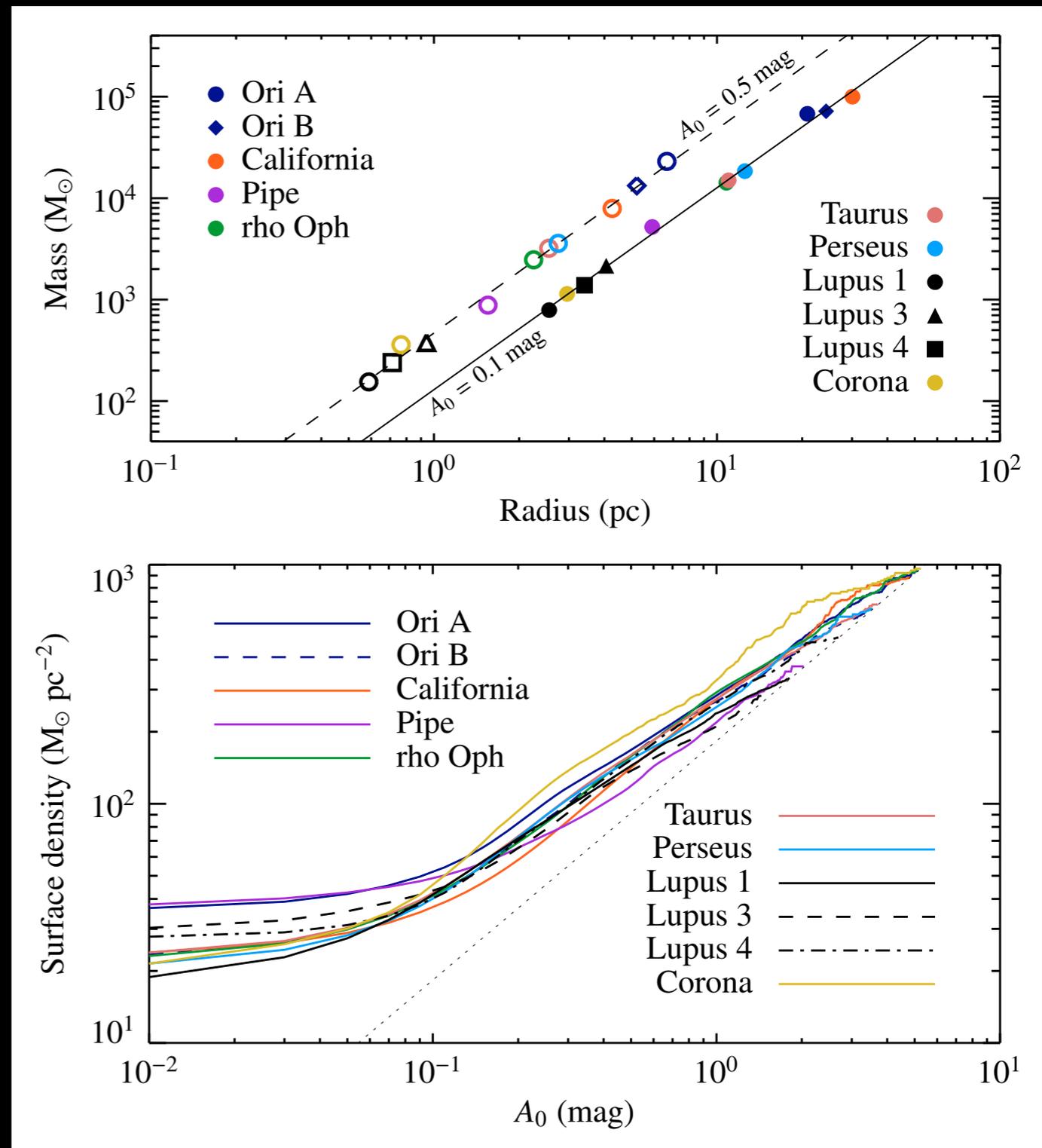
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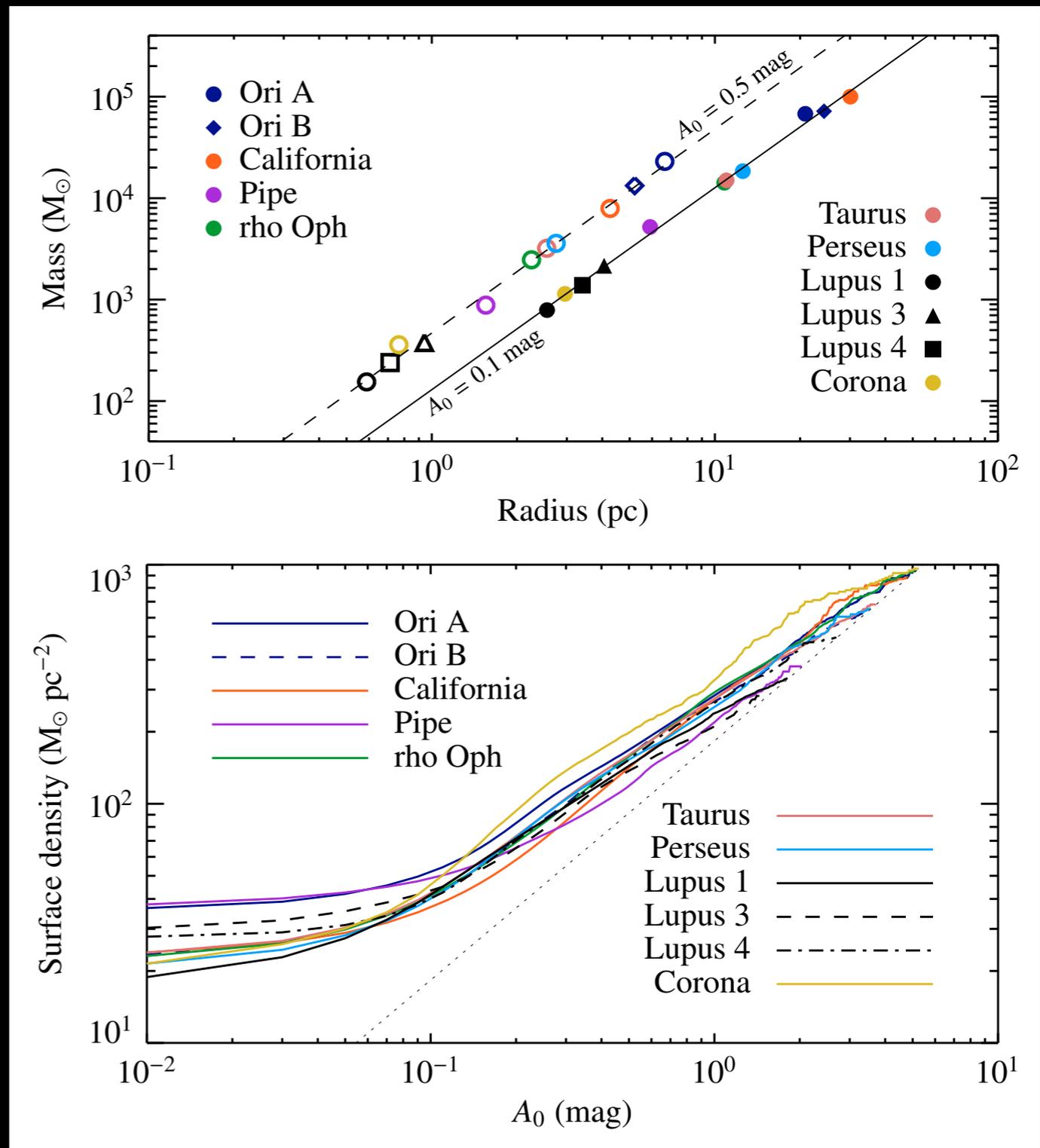


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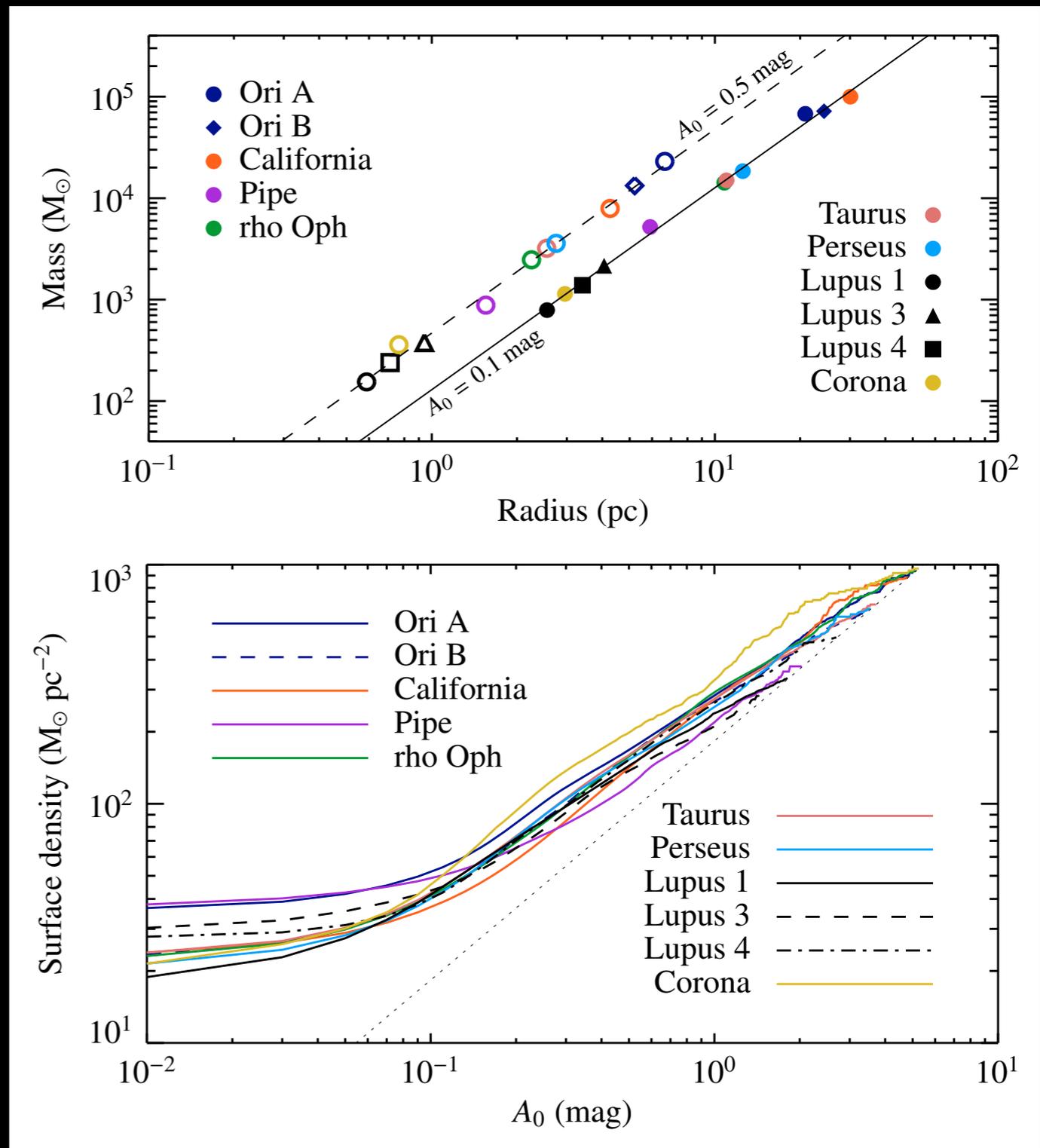
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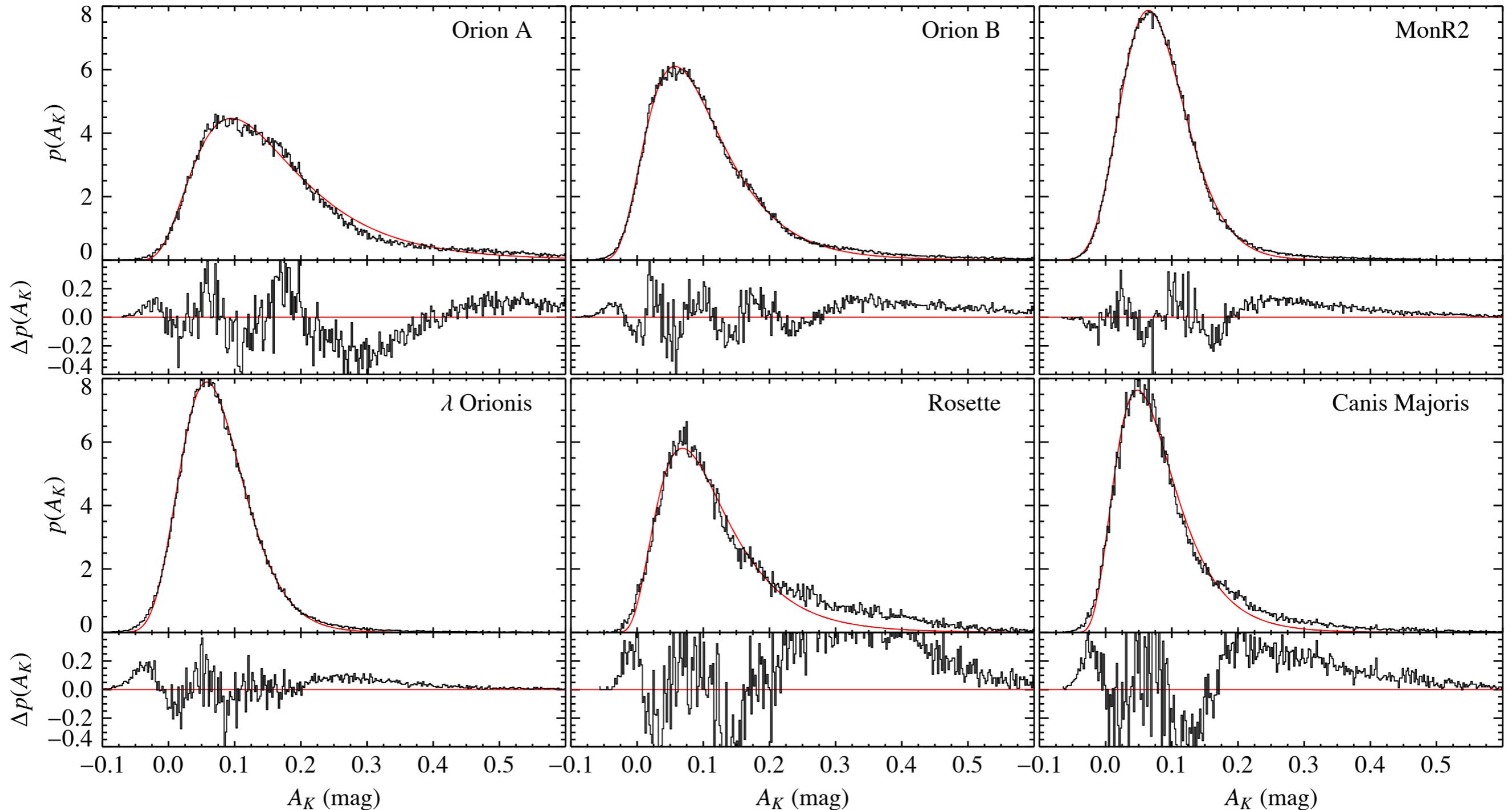
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- Makes sense to study the PDF of molecular clouds



# Log-normal fits to cloud projected density distributions



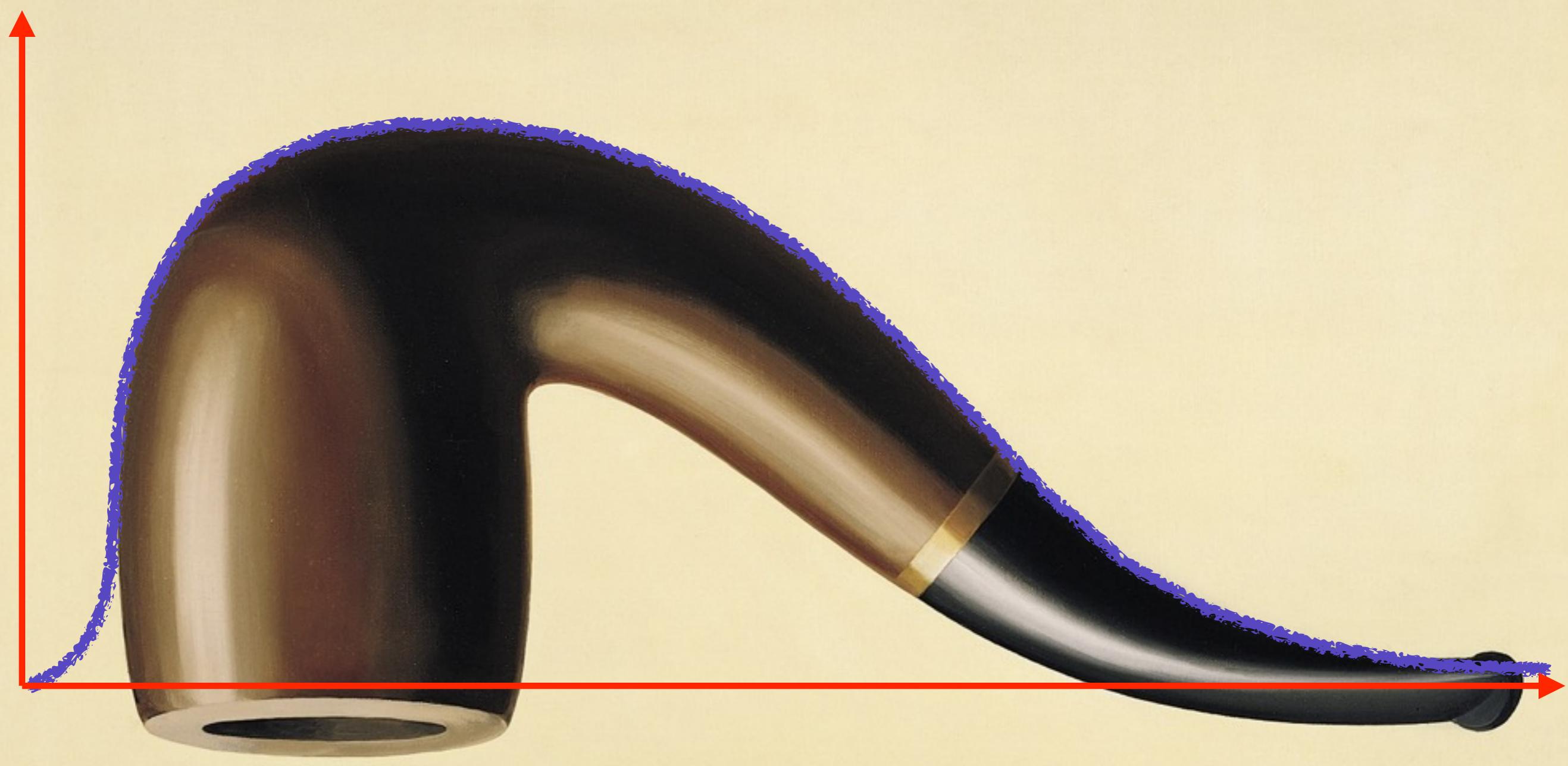


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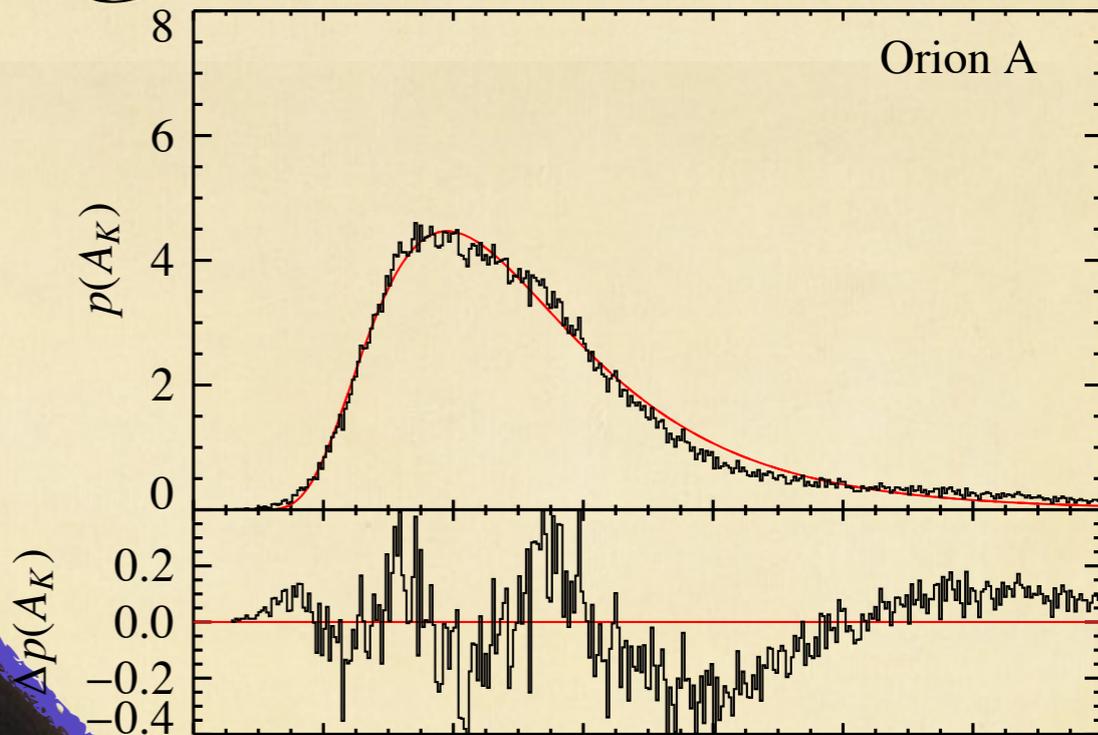
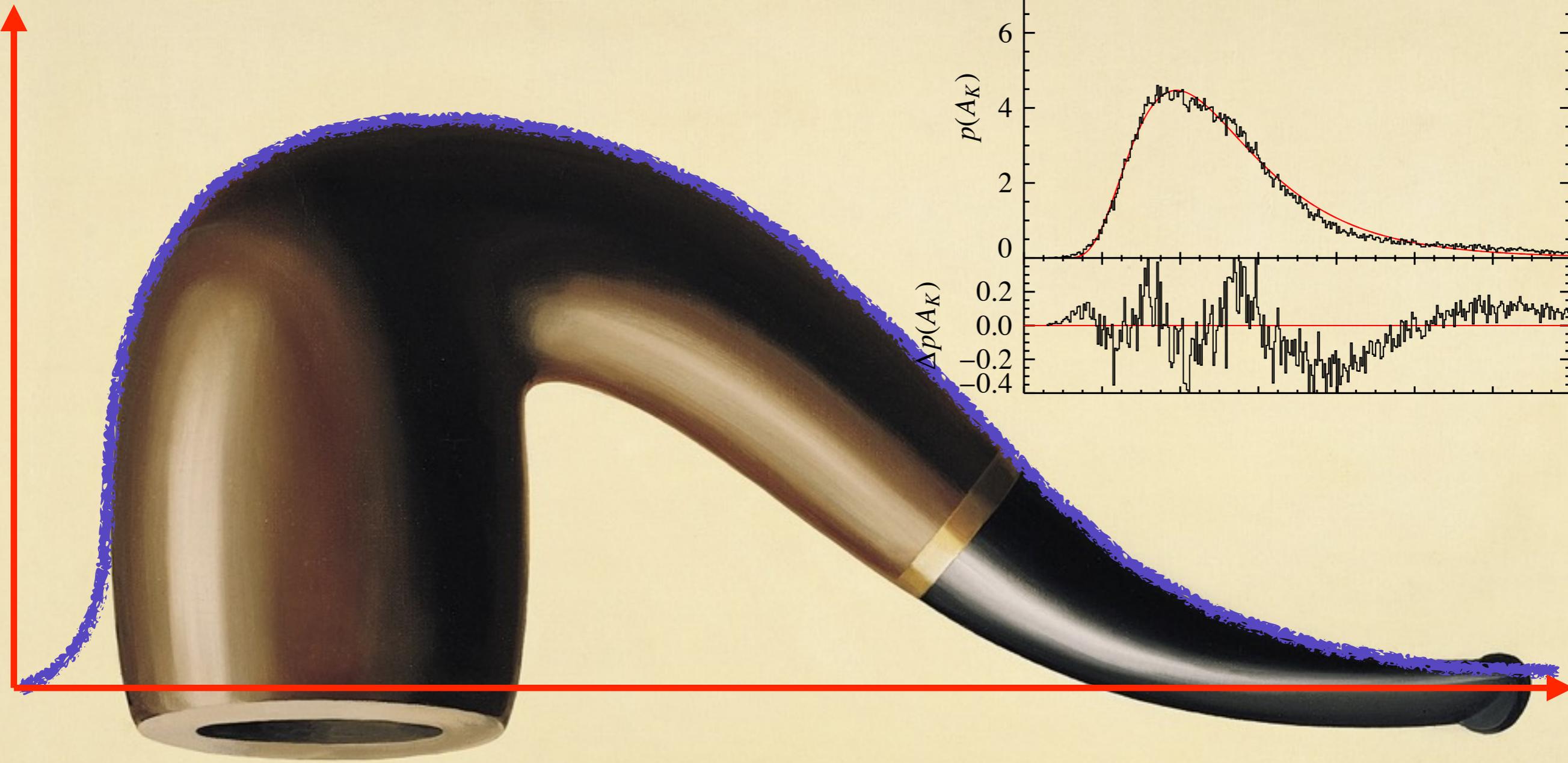
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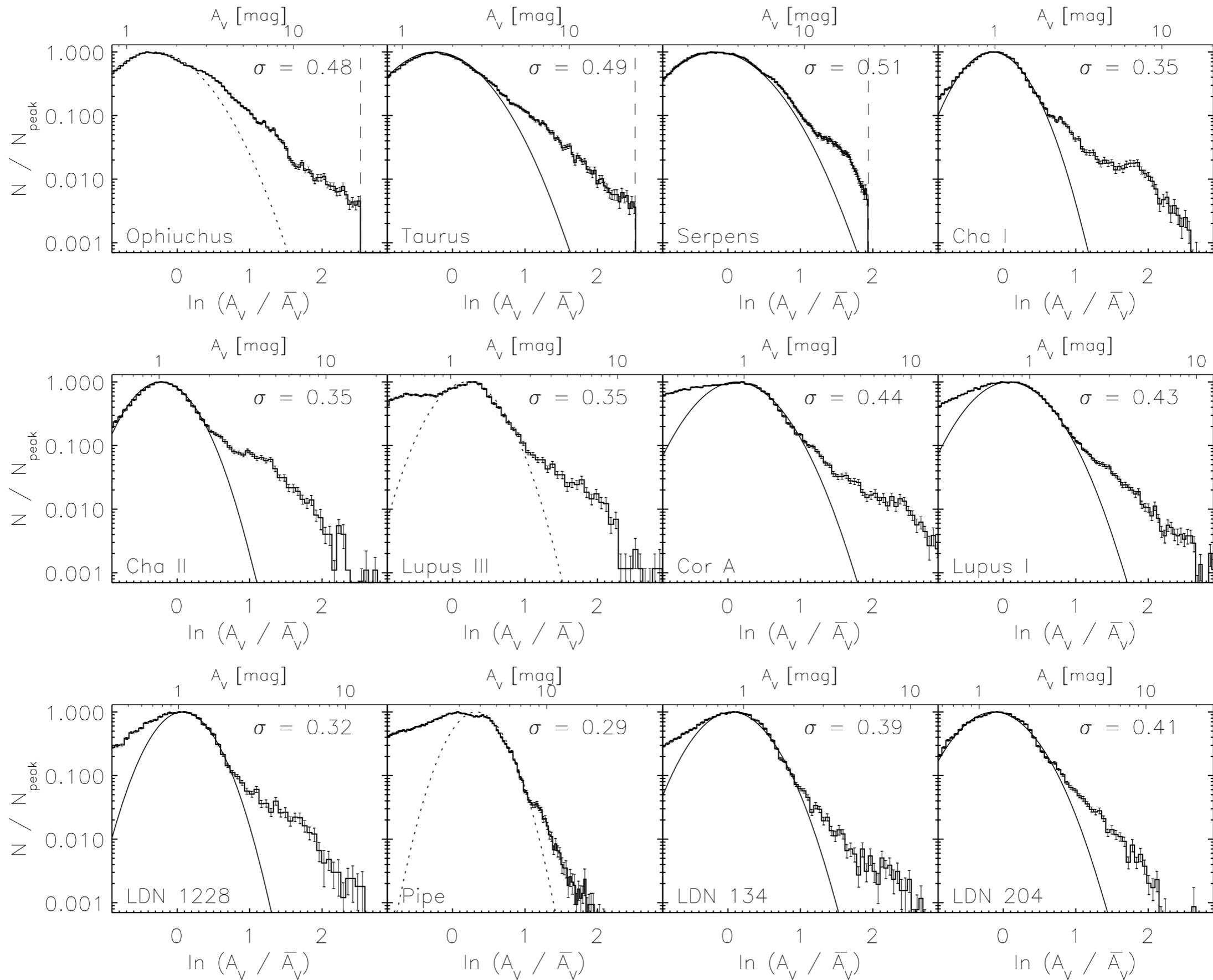
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# Log-normals everywhere!



Kainulainen et al. (2009; see also 2014)

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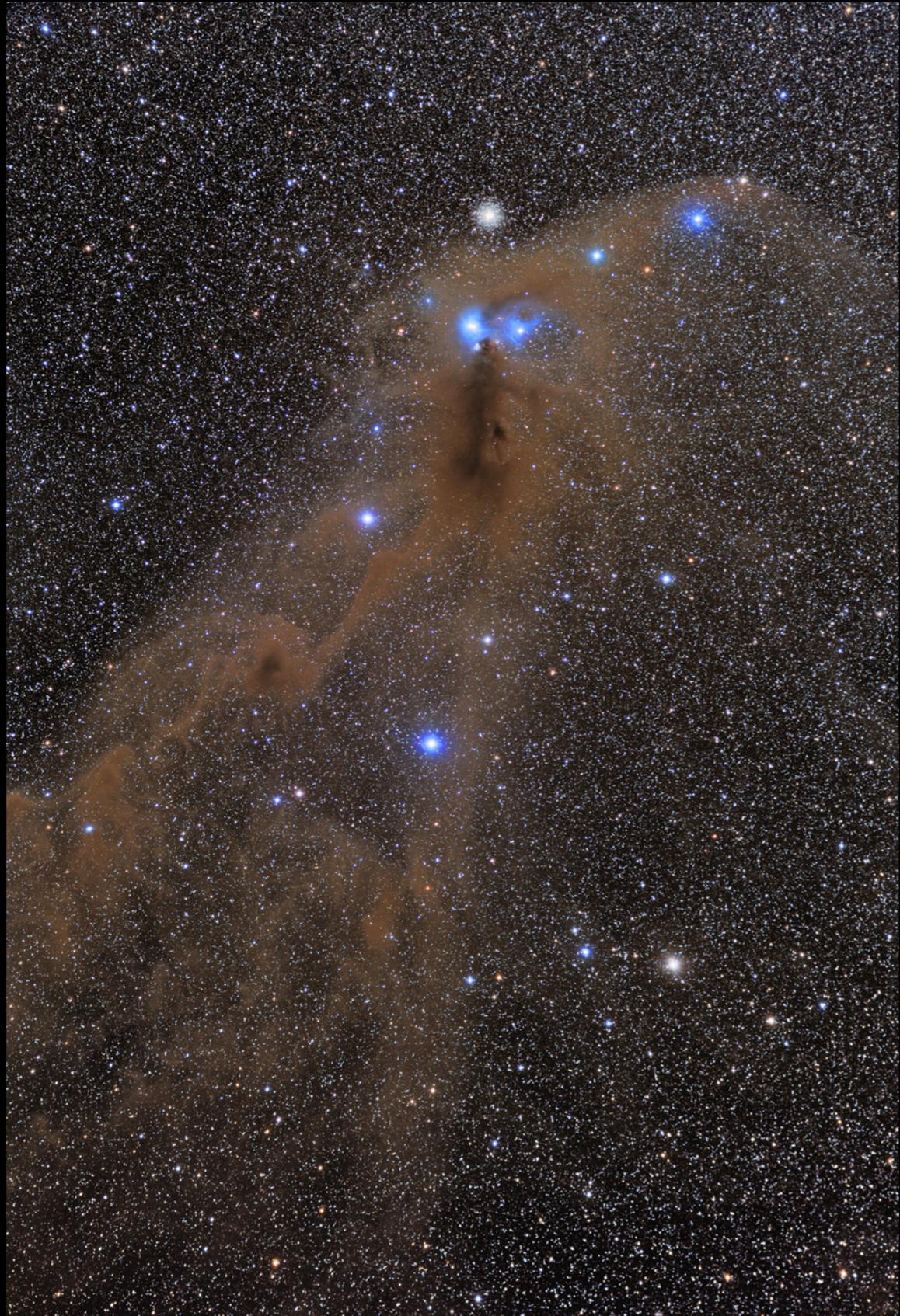
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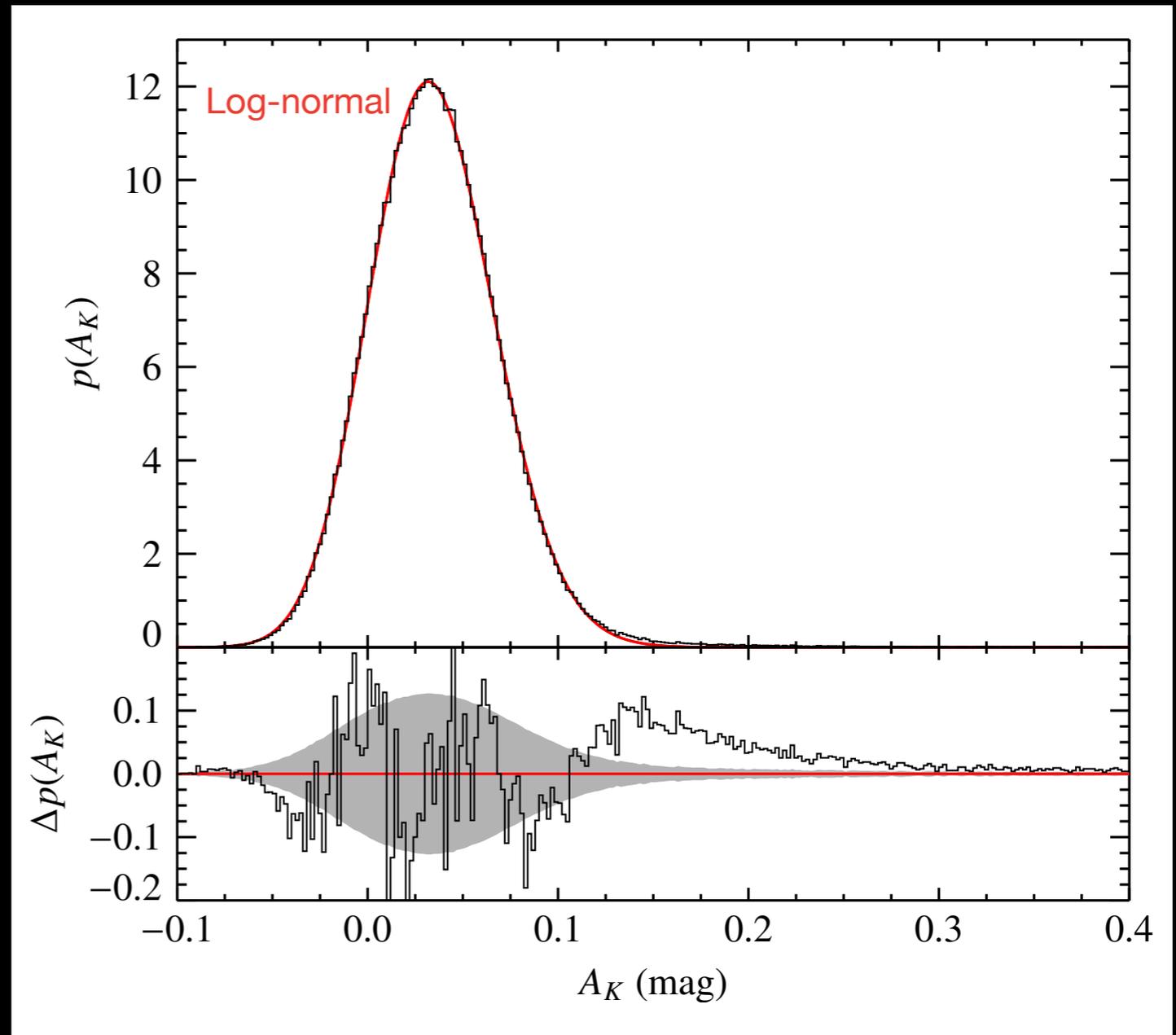
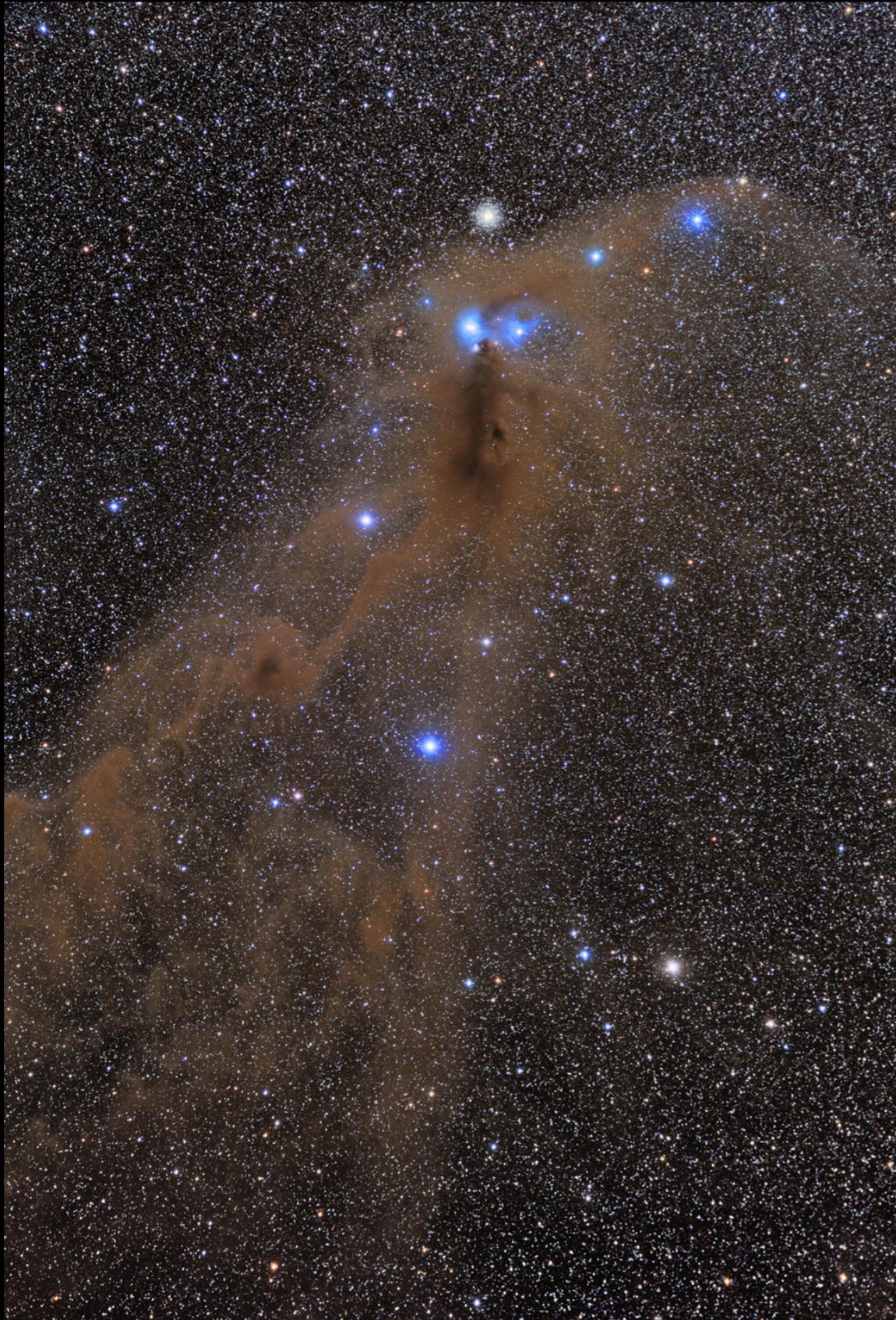
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- Projection effects (in most cases...) do not significantly alter this expectation (Vázquez-Semadeni & García 2001)



# The end of a dream

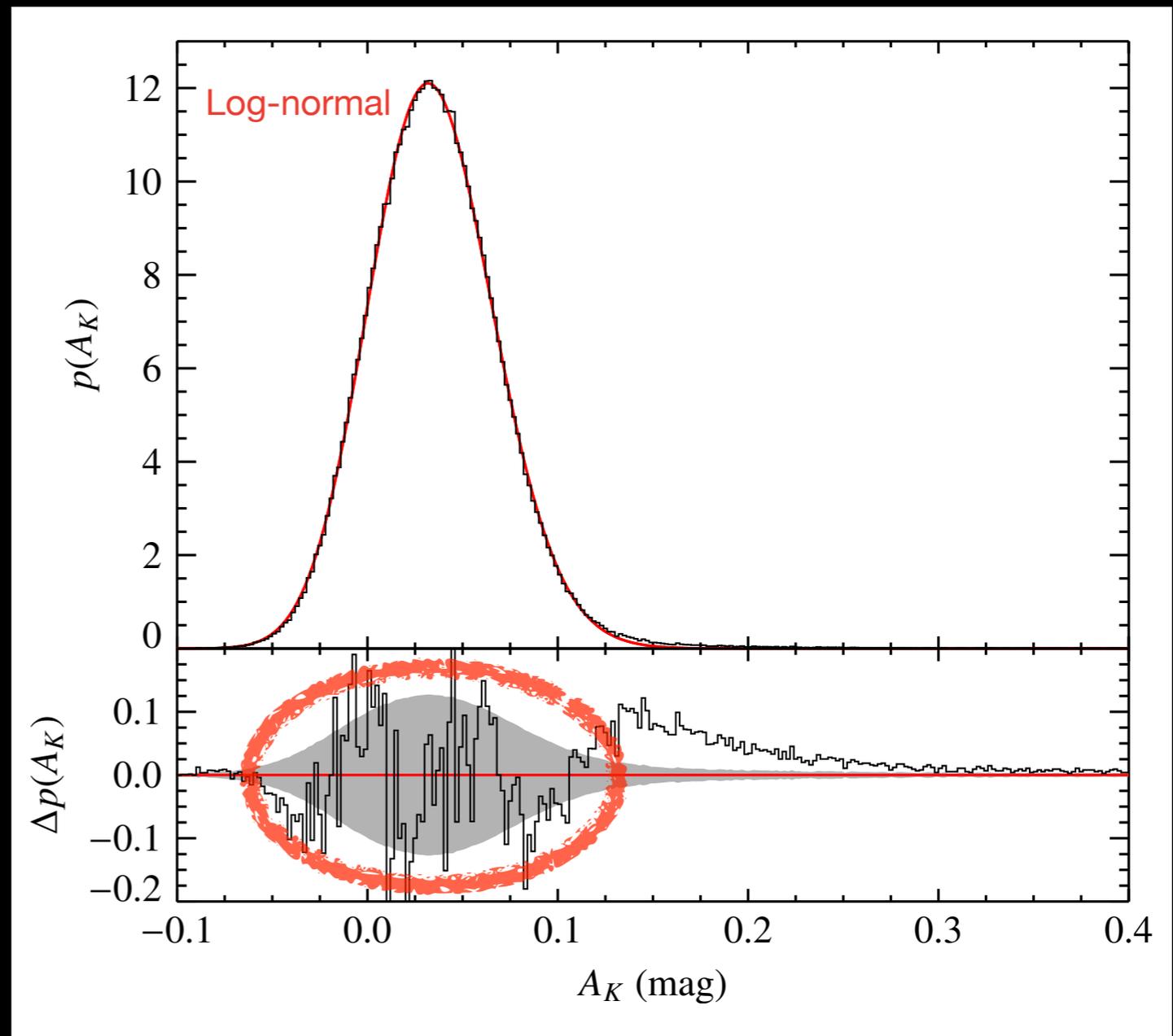
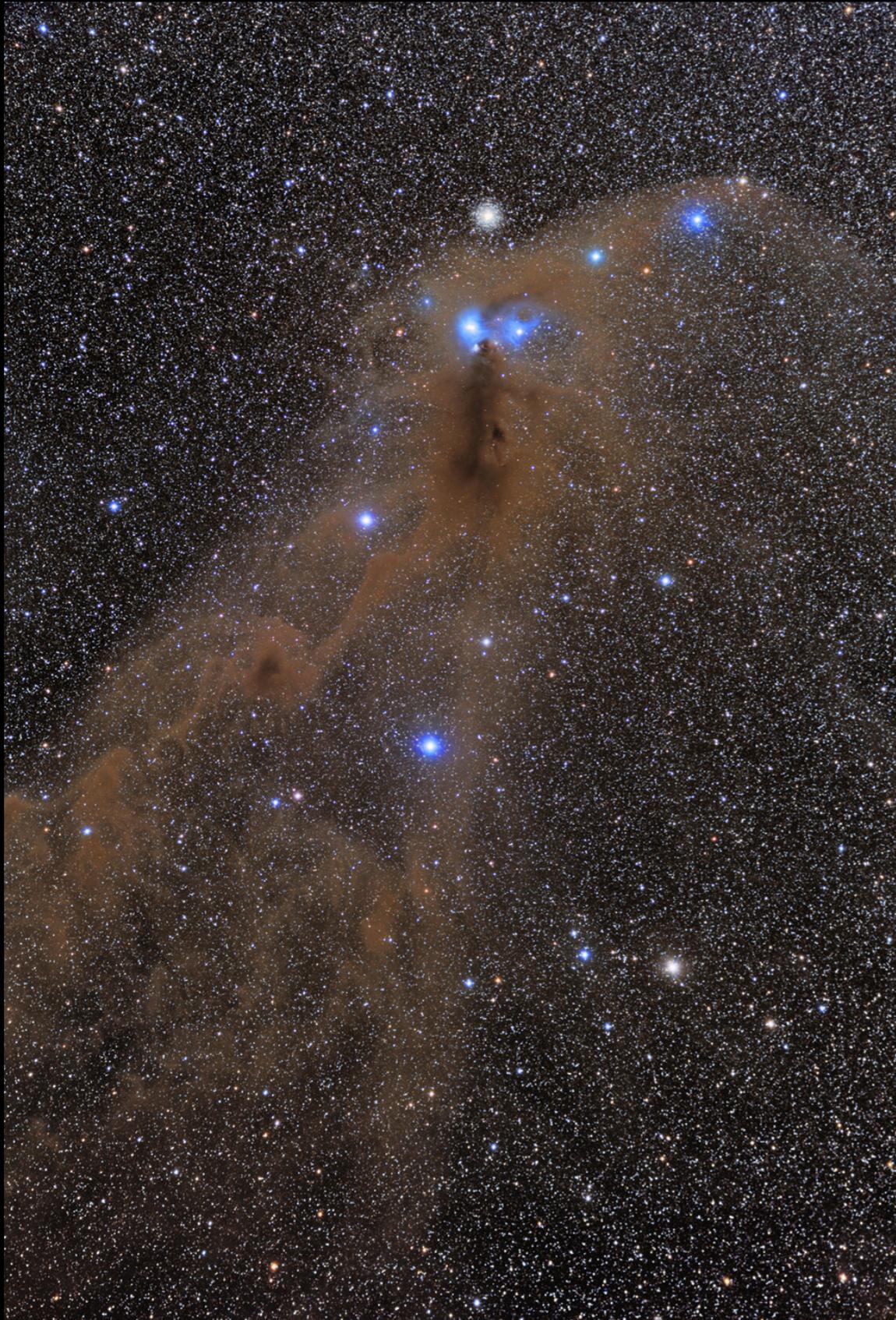


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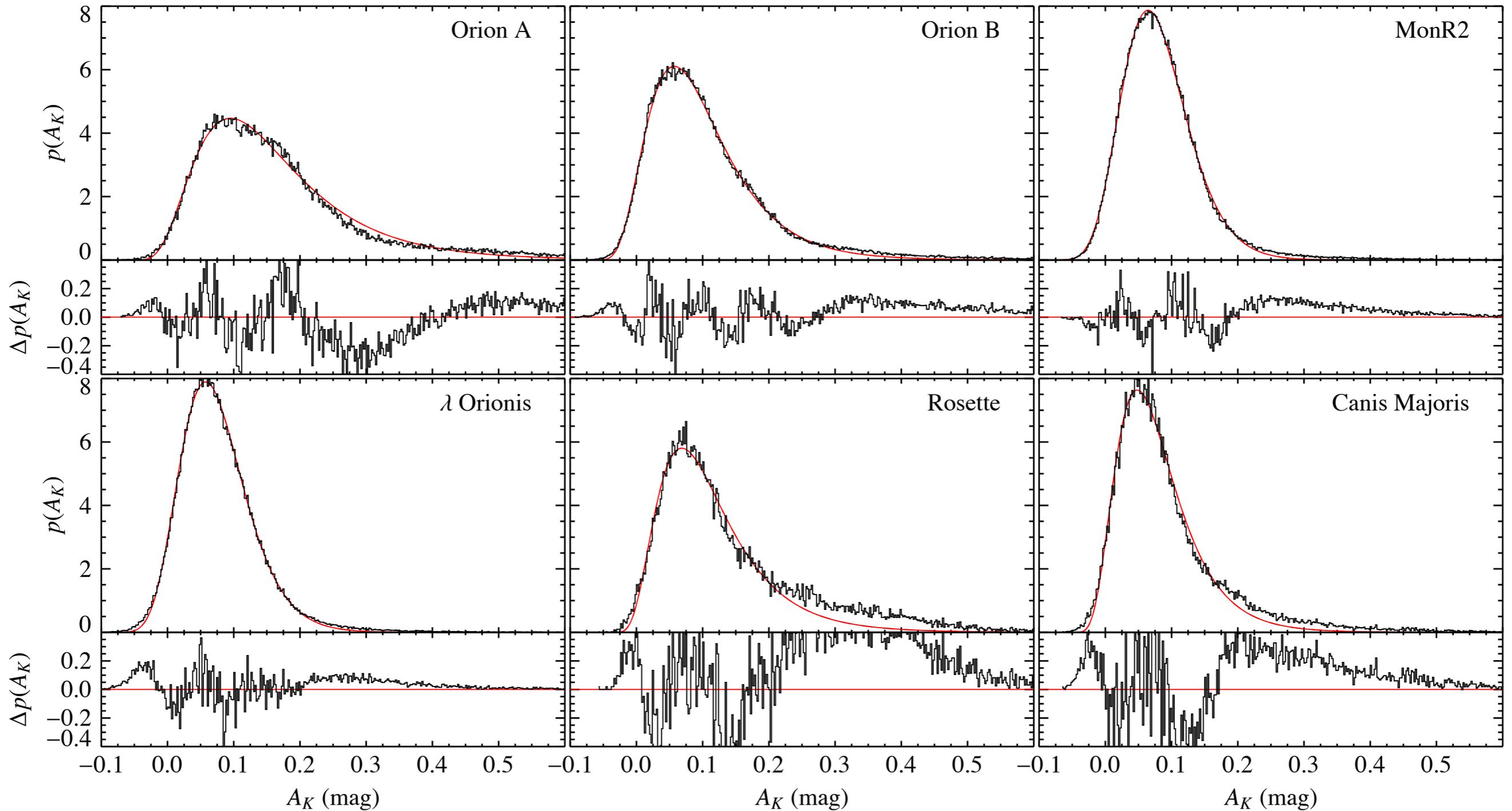
Systematic residuals in the entire fitting region!

# The end of a dream

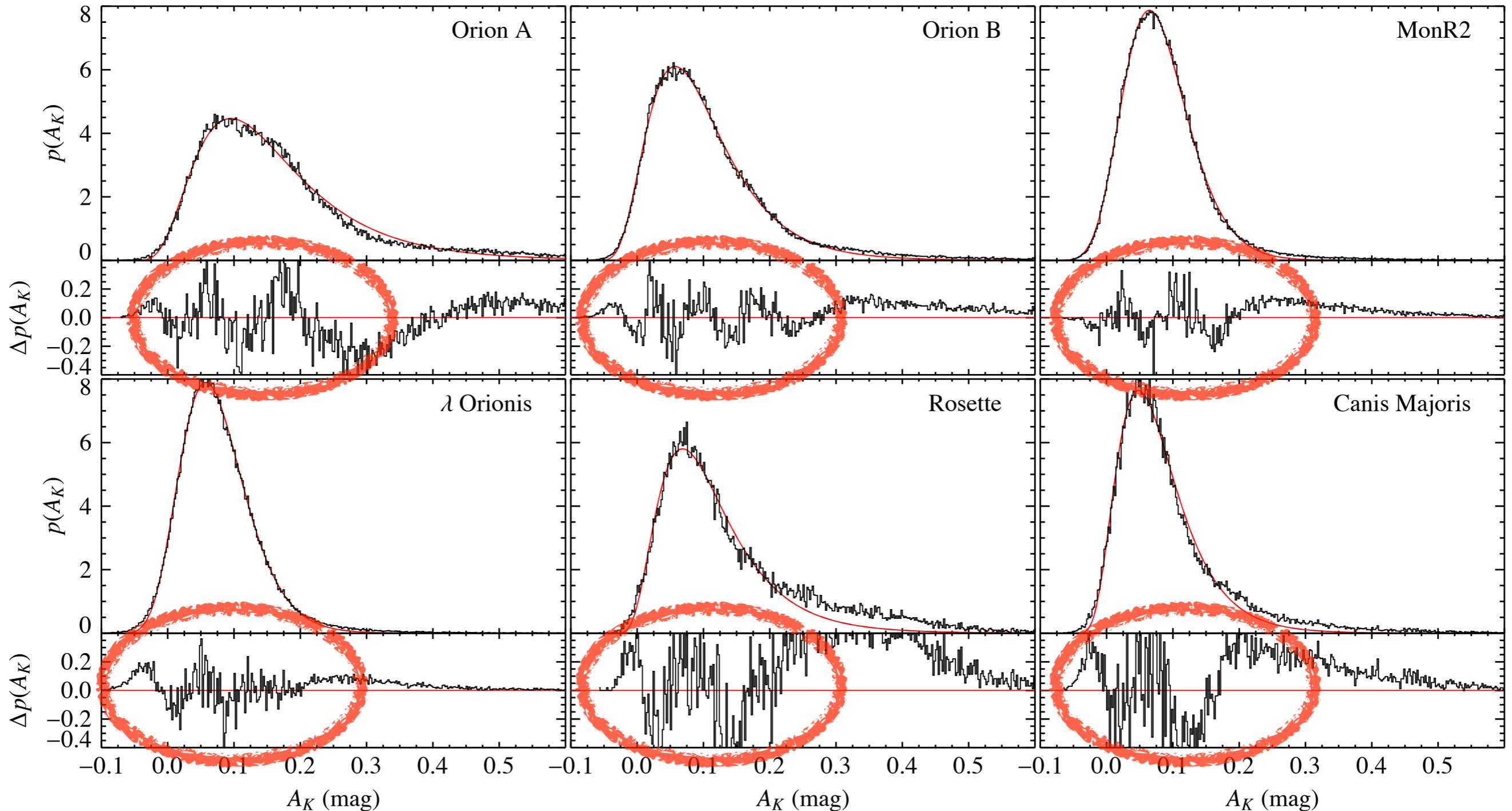


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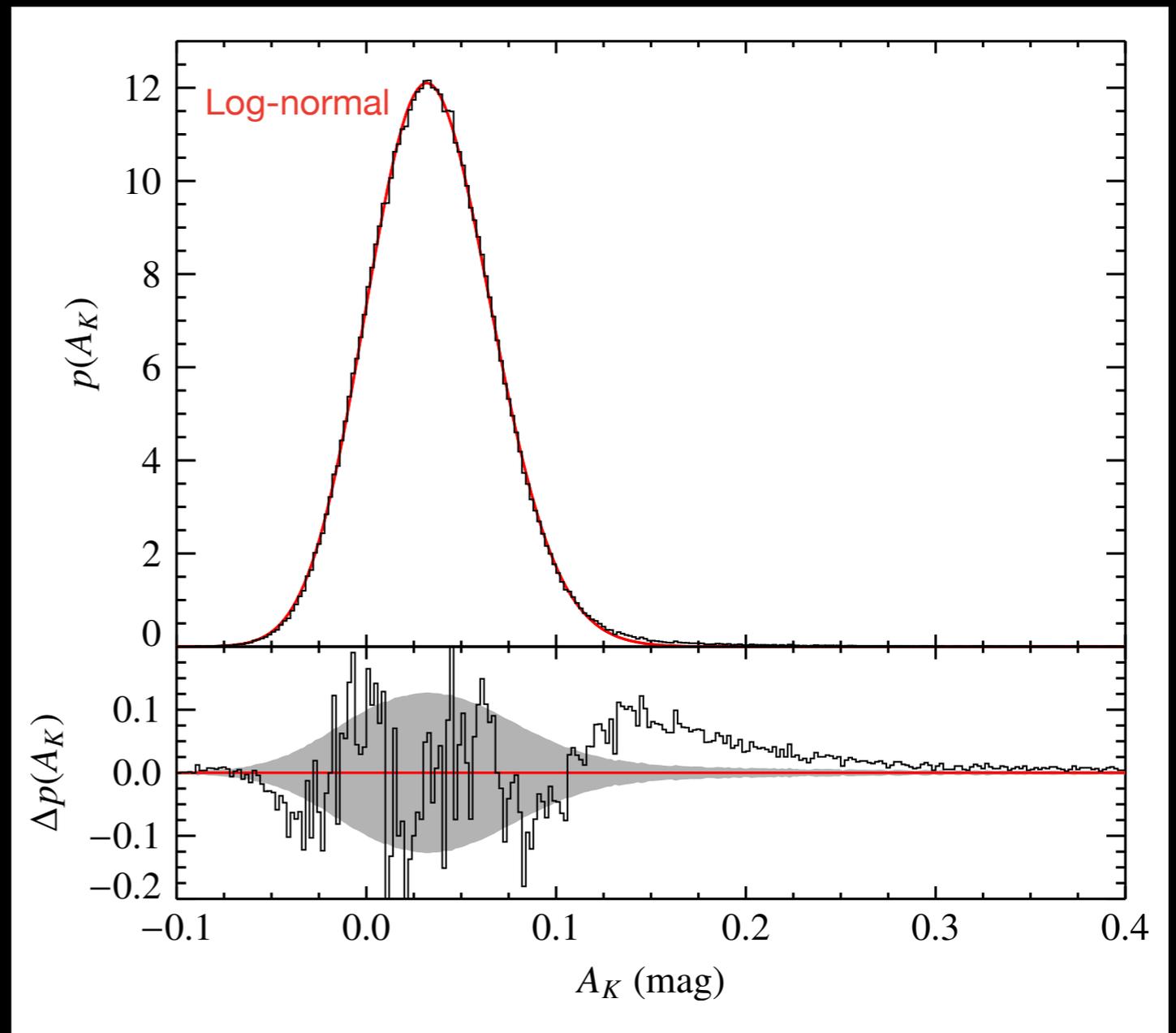
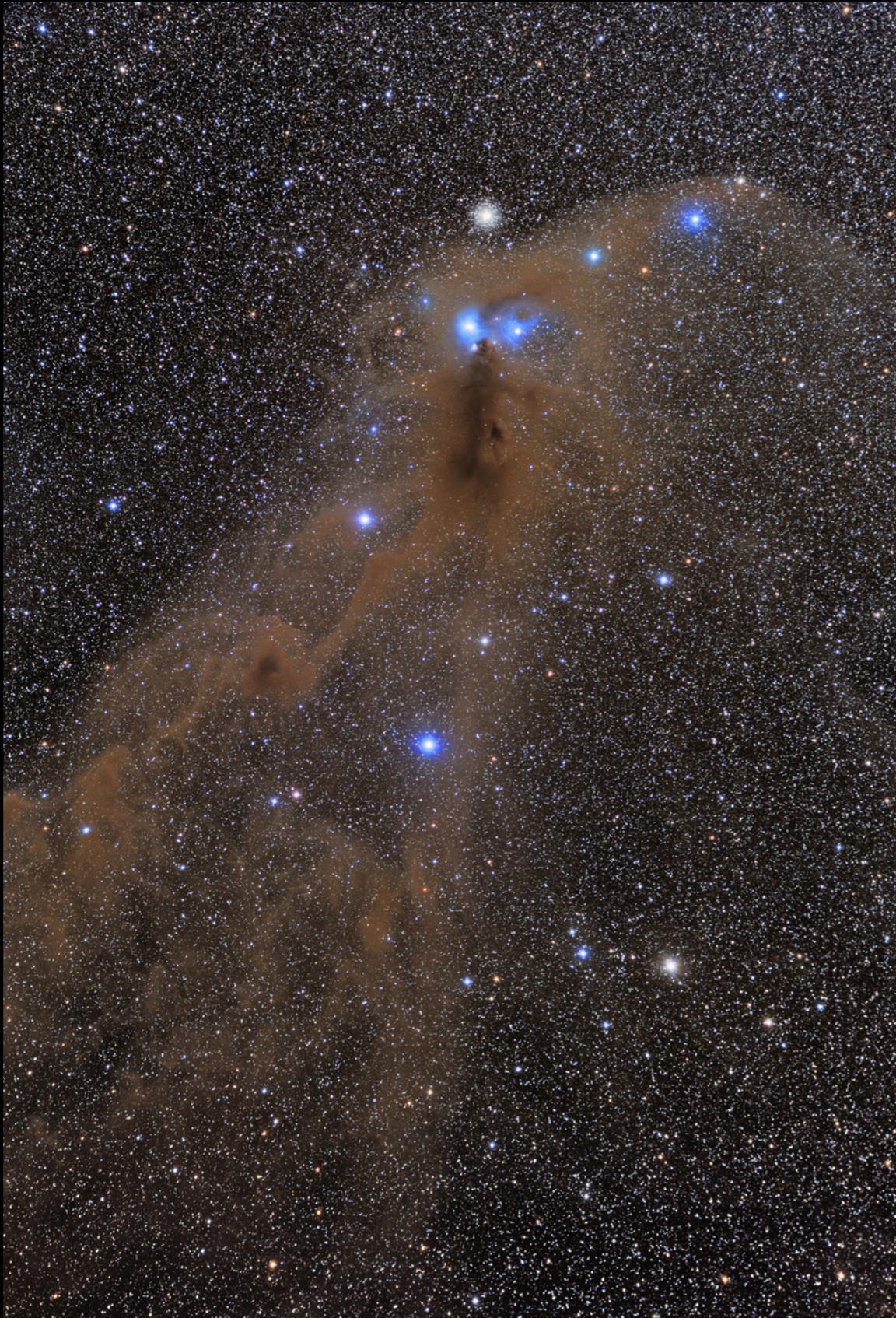
# All log-normal fits show systematic residuals



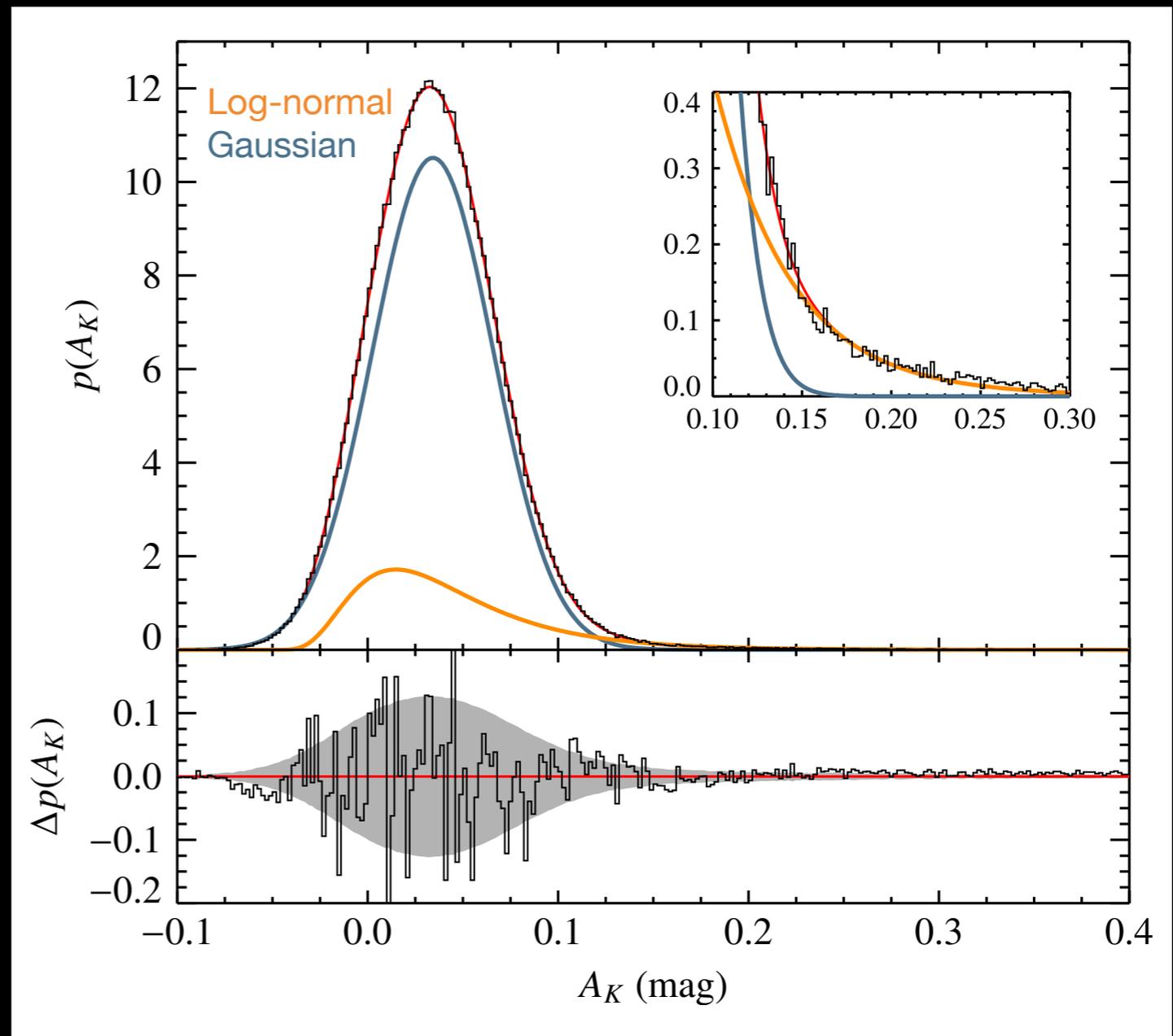
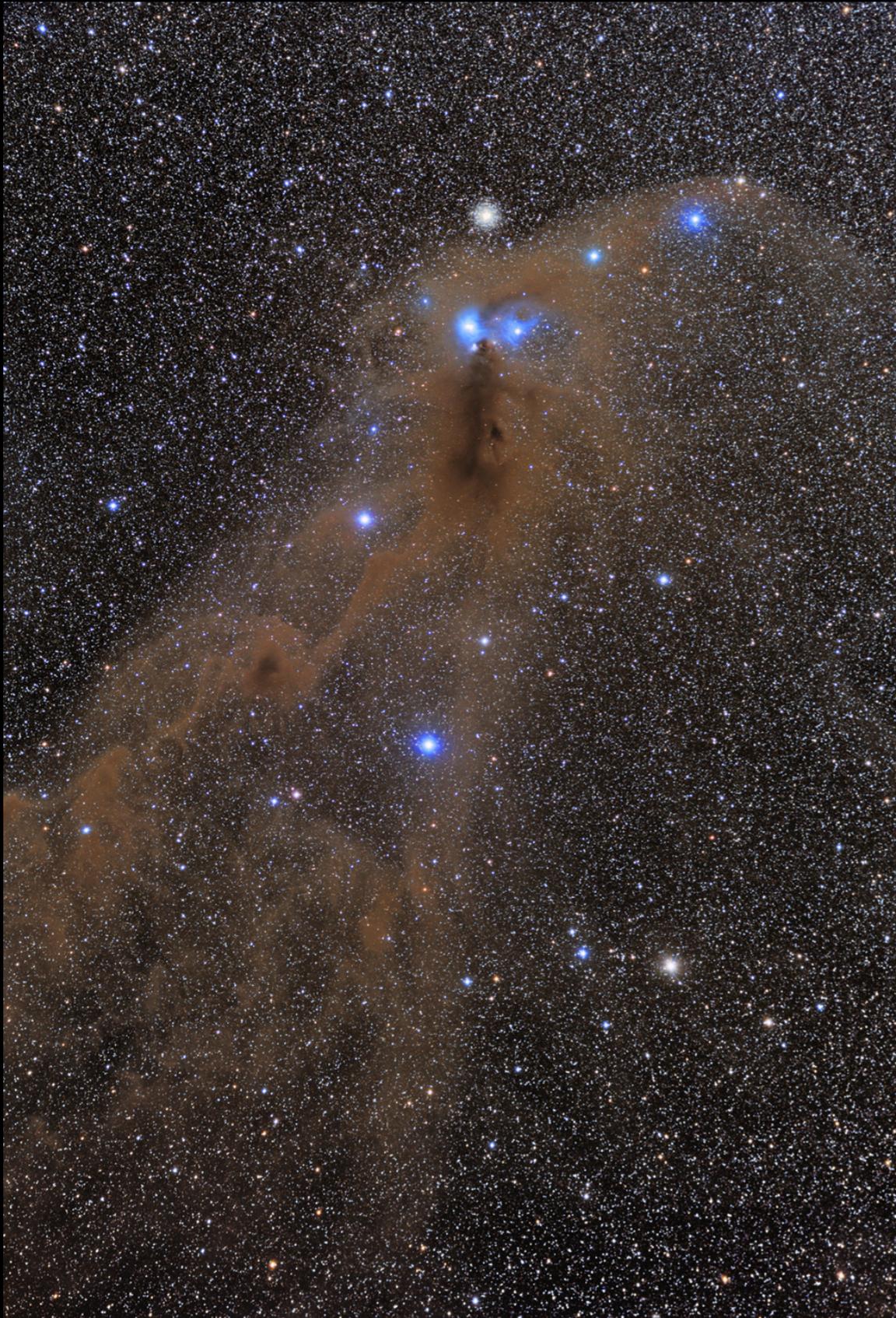
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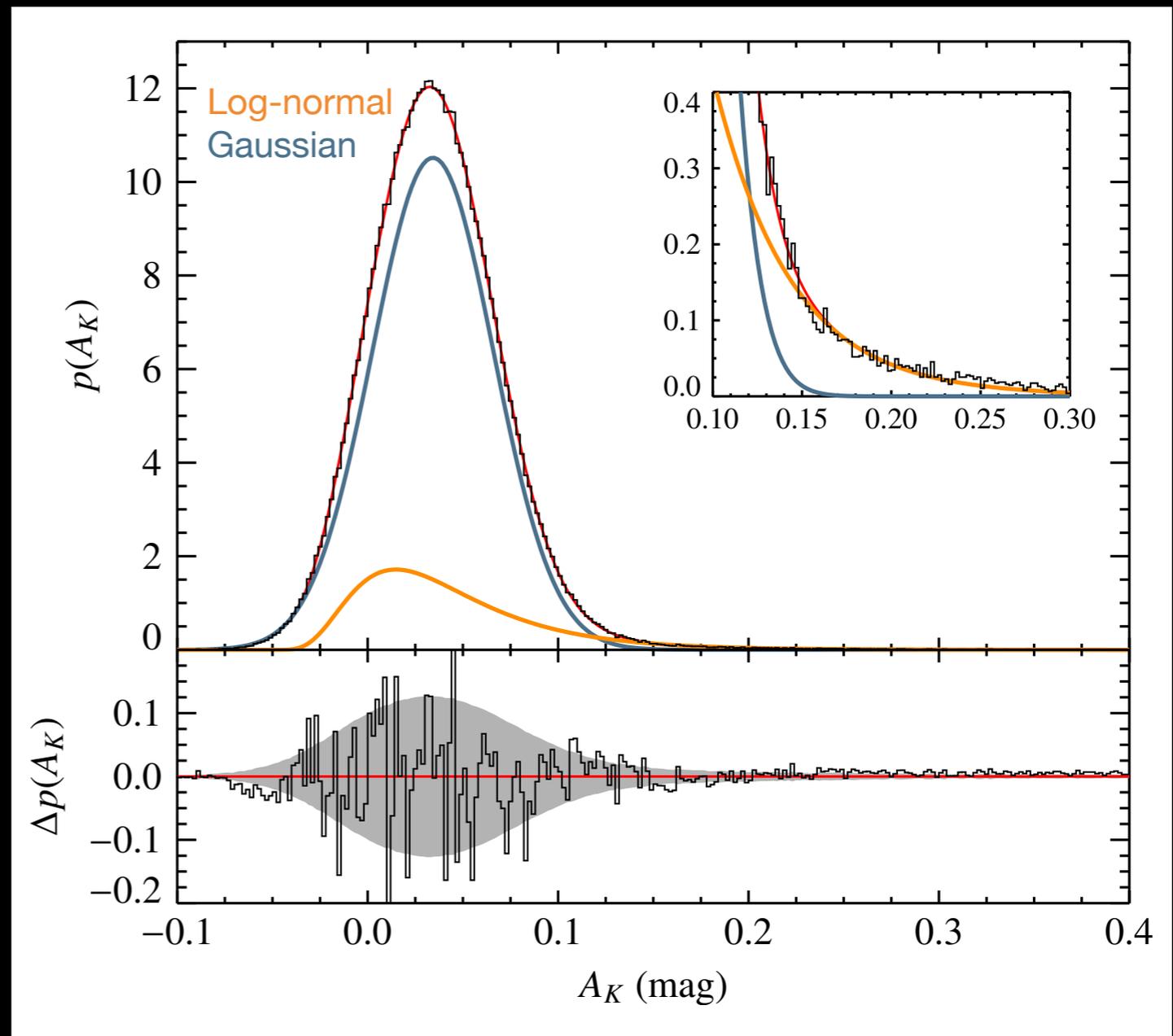


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Residuals disappear when fitting a  
Gaussian + Log-normal.

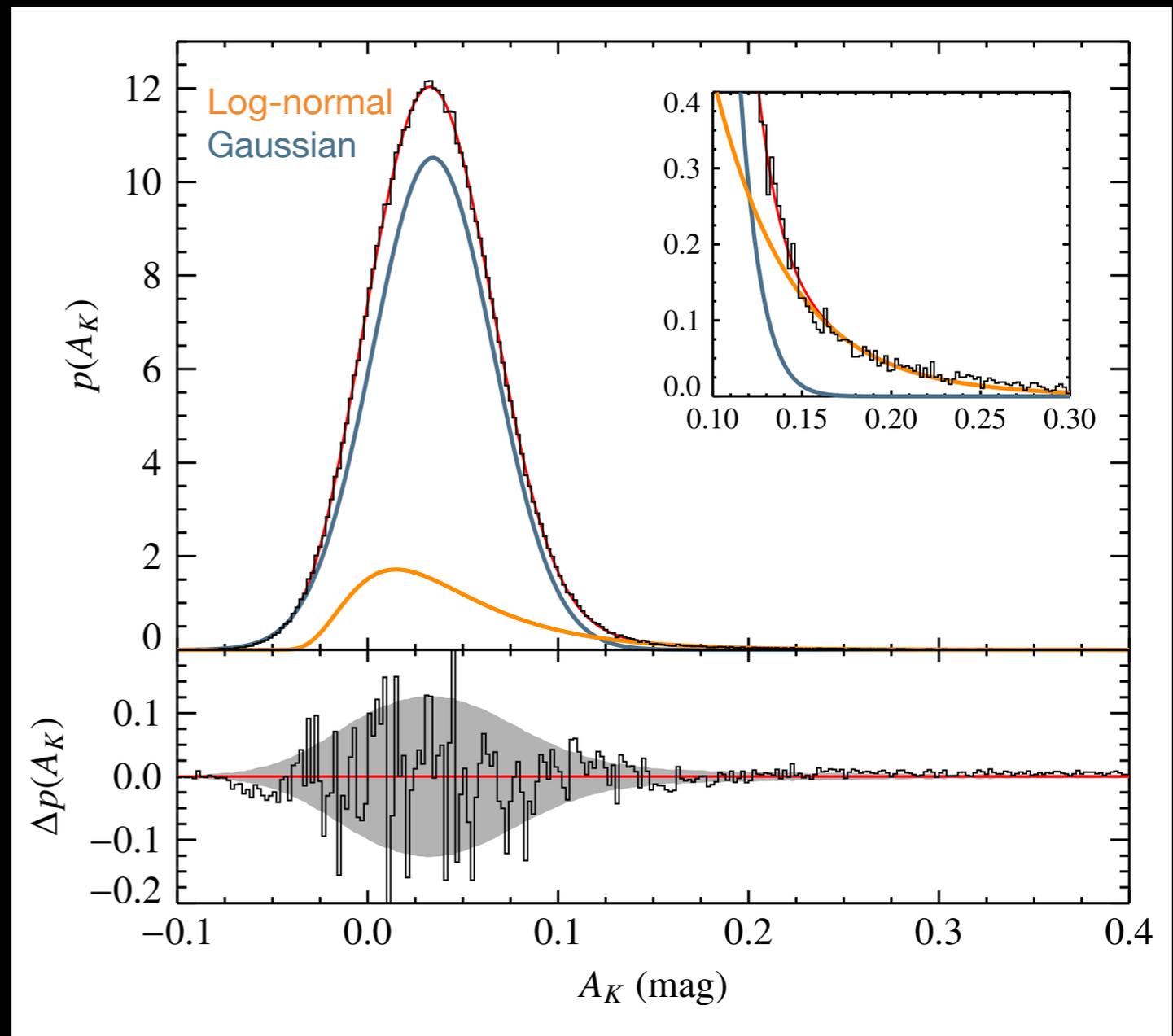
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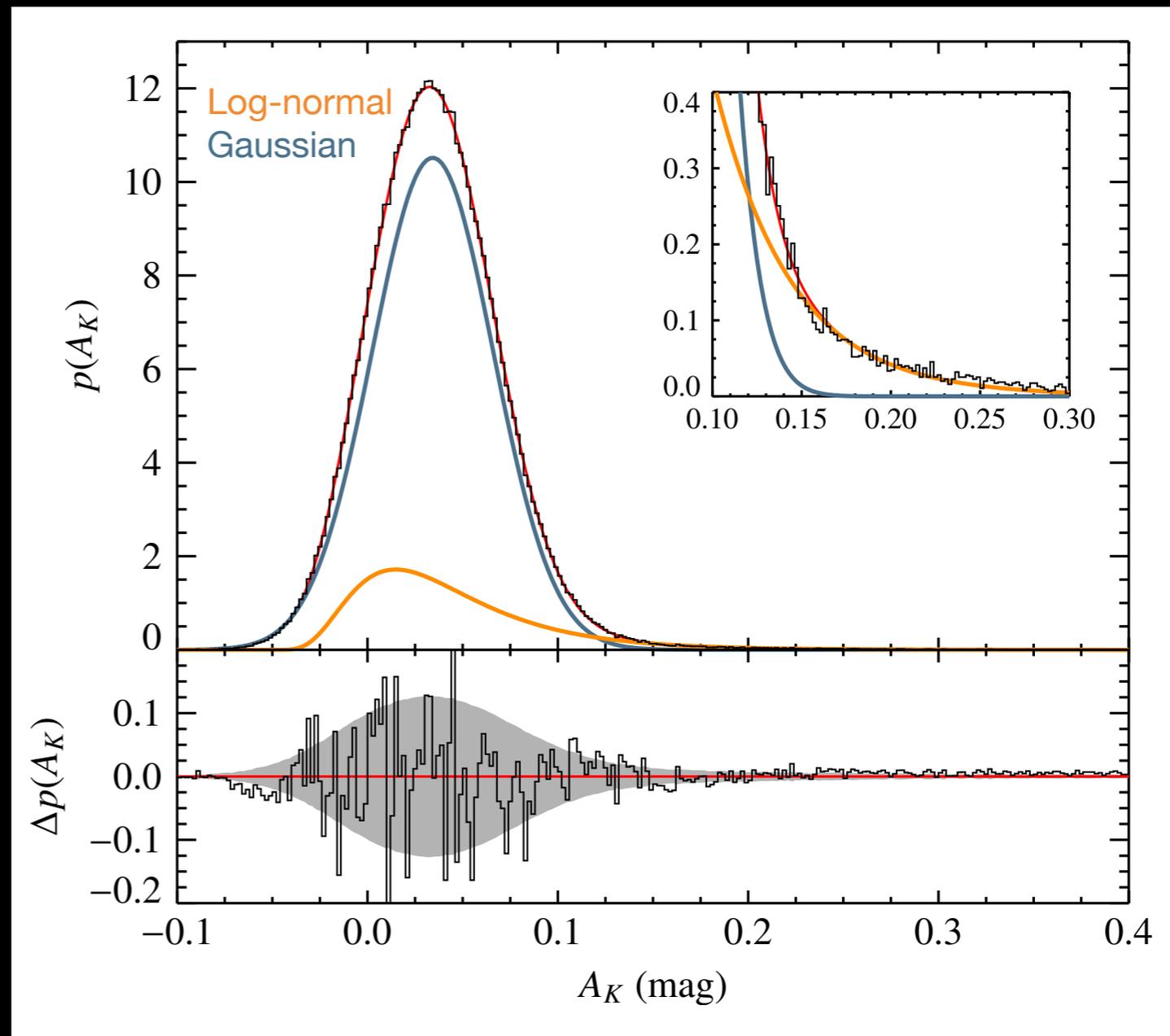
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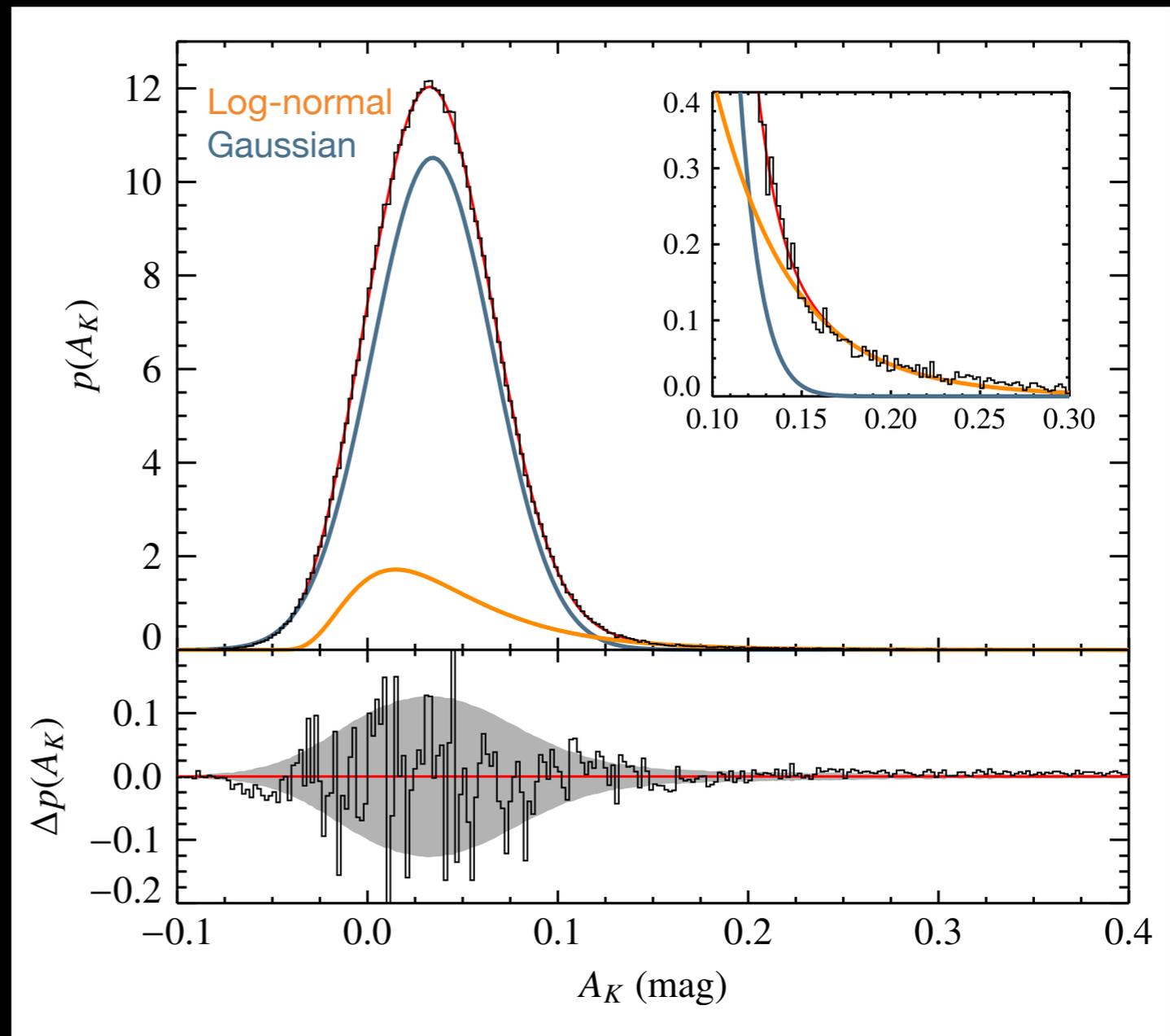
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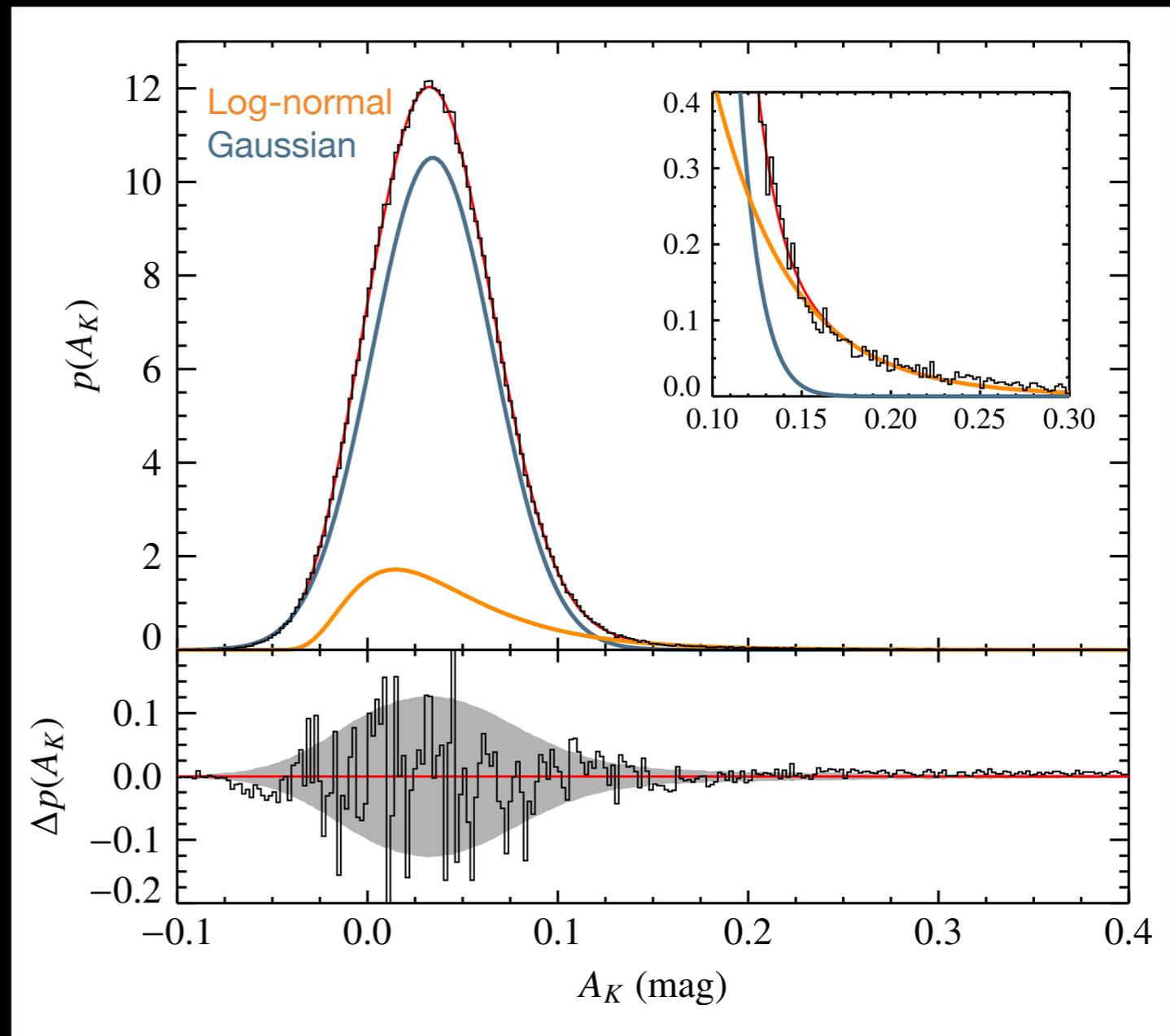
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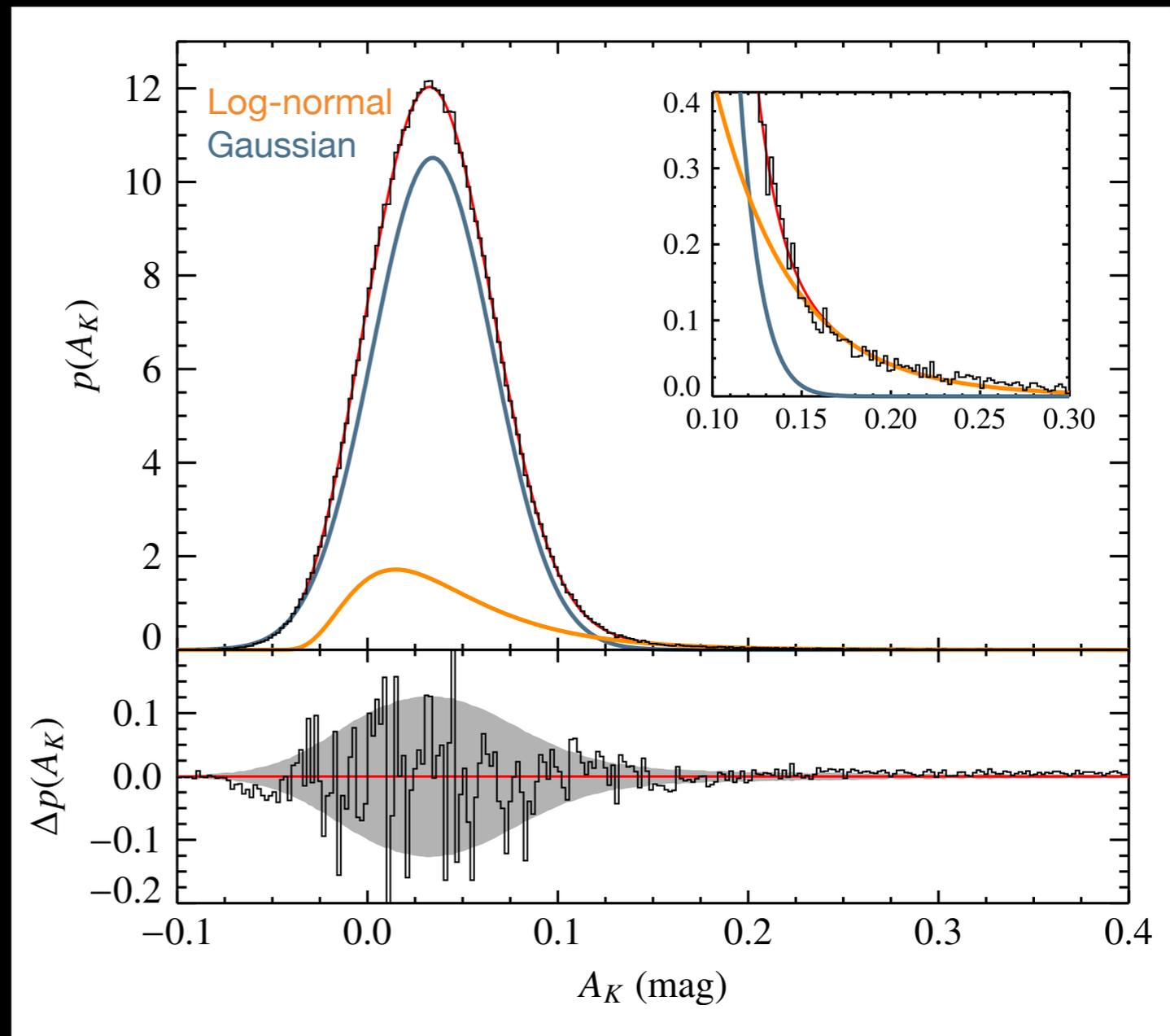
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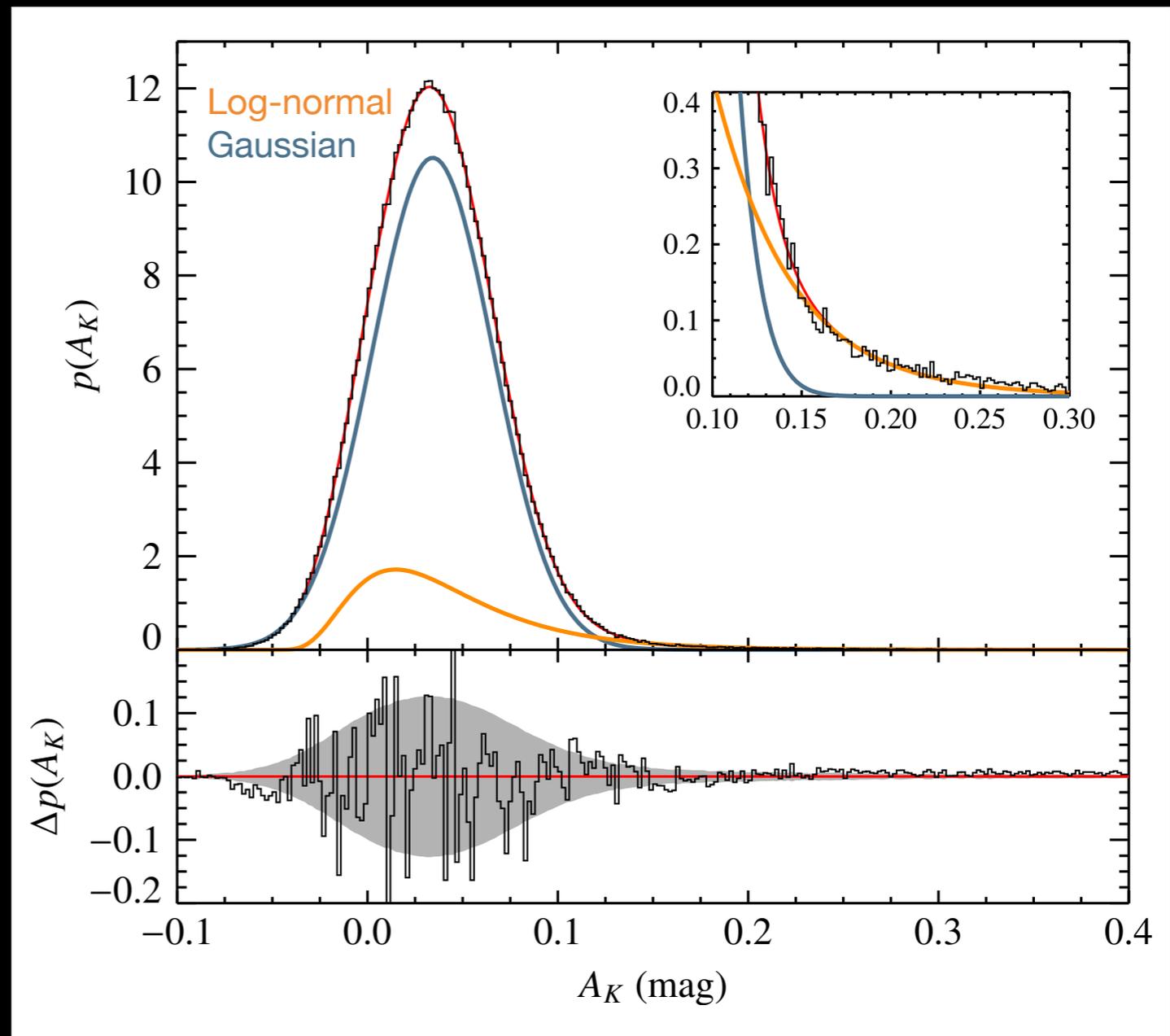
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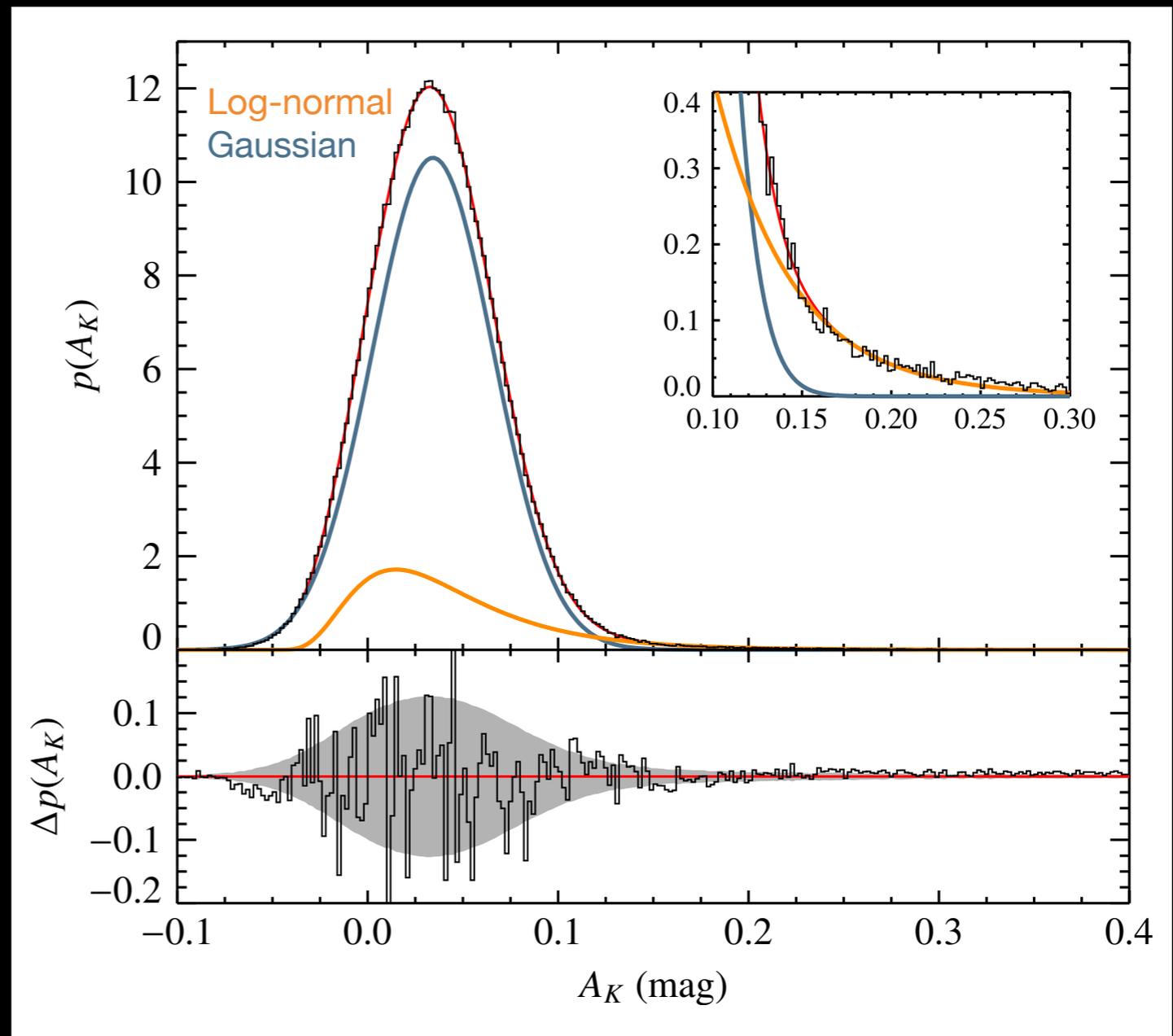
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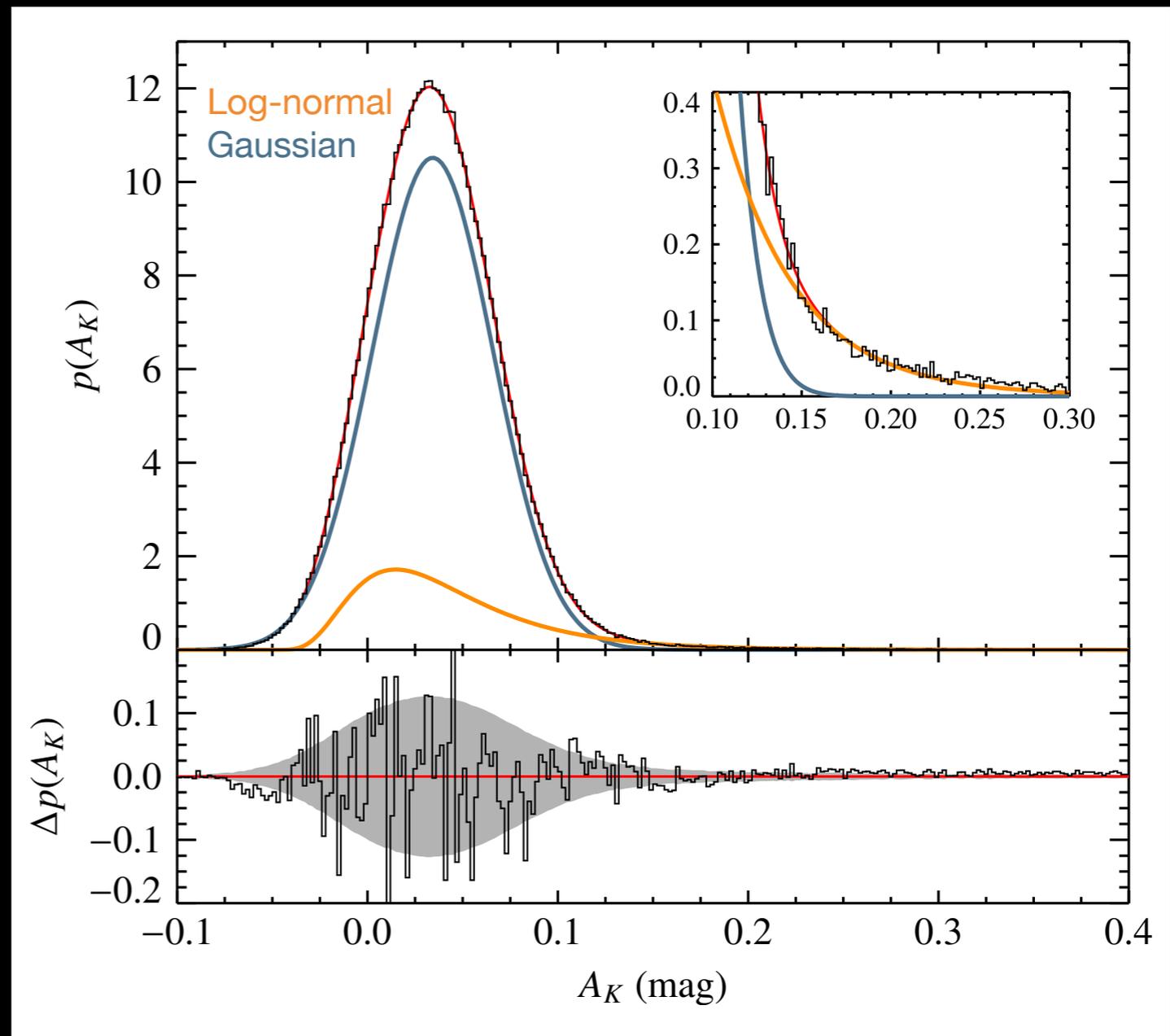
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  - Dominates at low  $A_K$ !
  - Is still present at large  $A_K$
- PDFs more difficult to measure than we expected...
- Log-normals: are they real?



Residuals disappear when fitting a Gaussian + Log-normal.

Do yourself your log-normal!

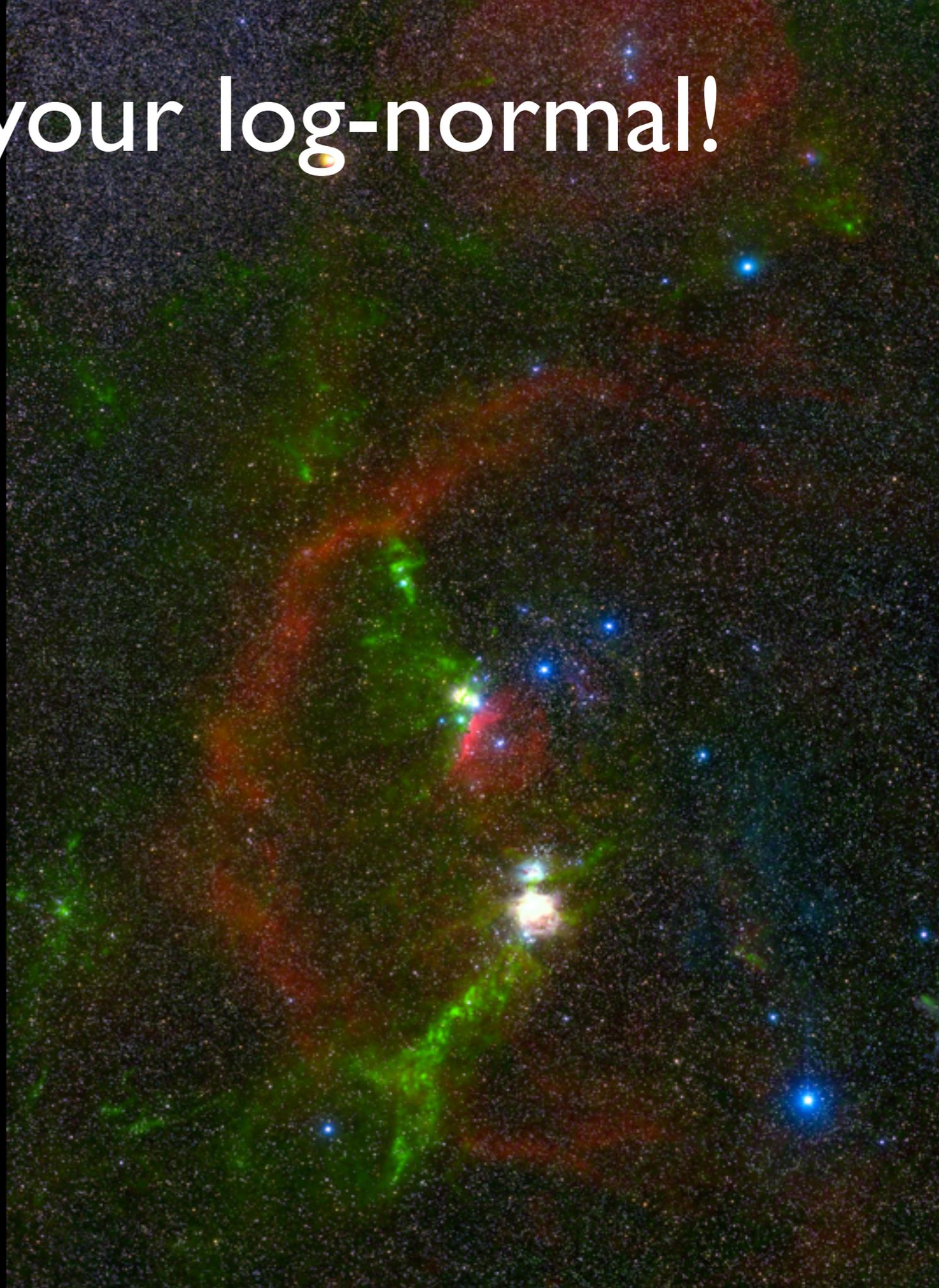
# Do yourself your log-normal!

Recipe

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## Recipe

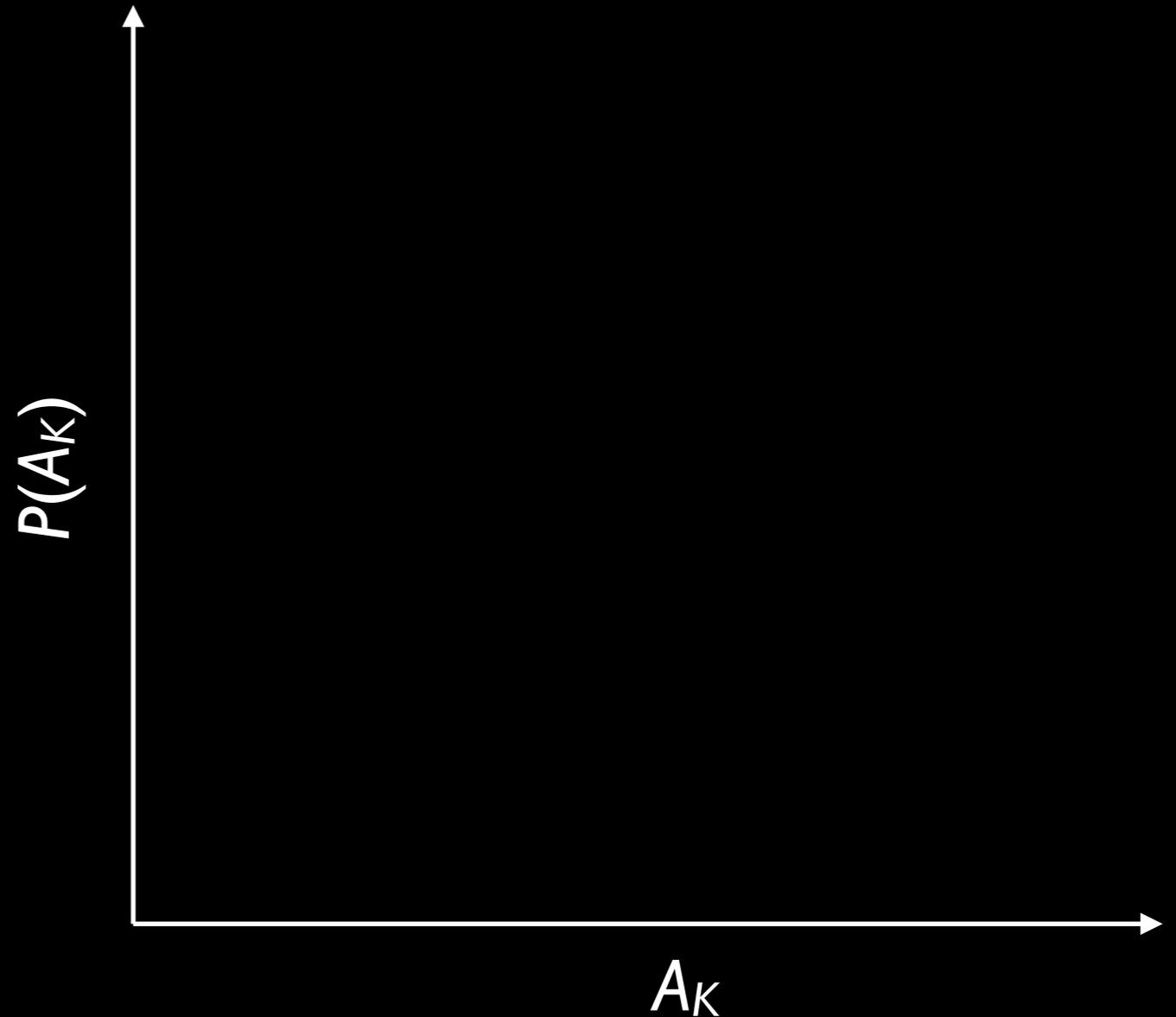
- Take any nice cloud



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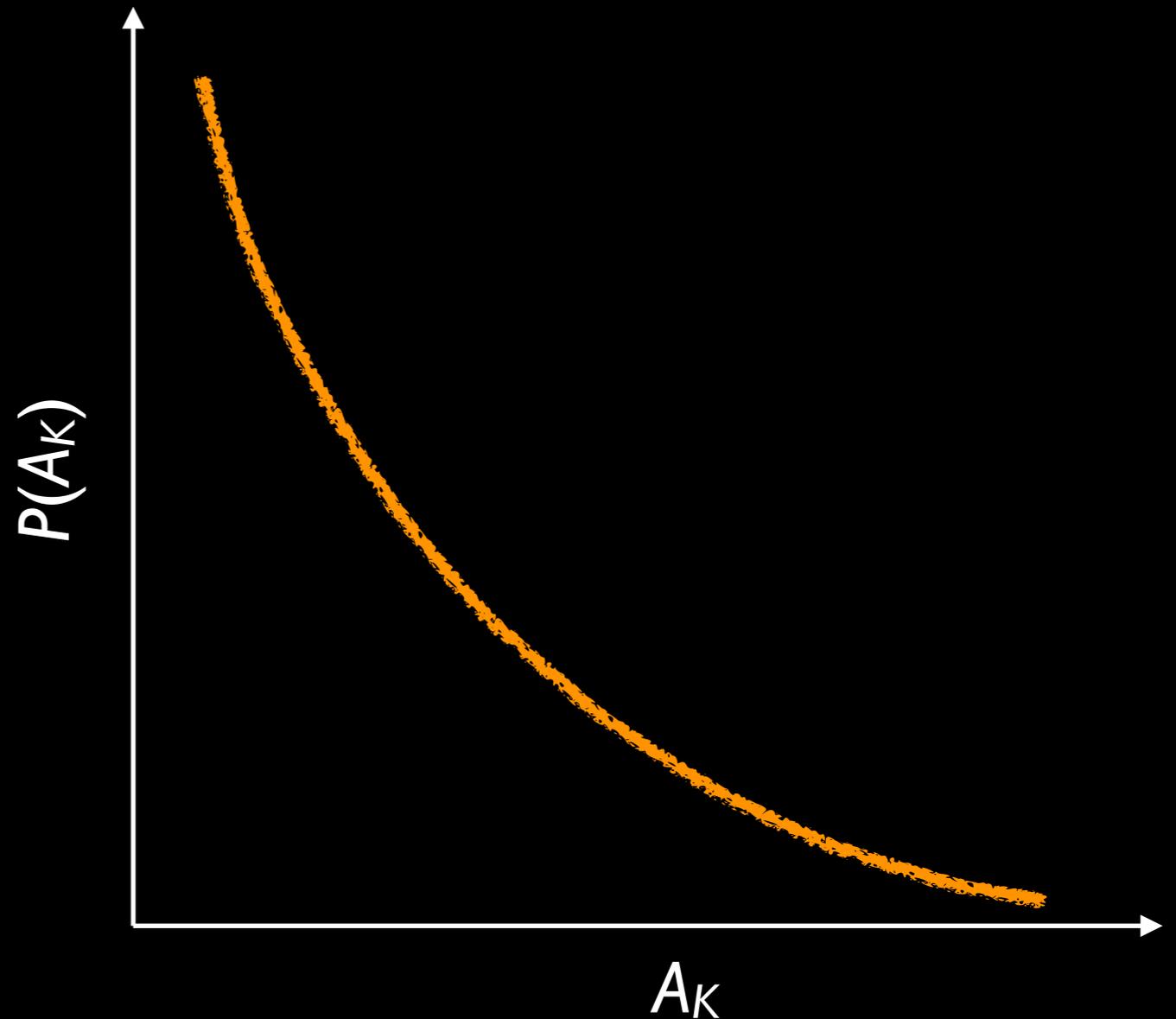
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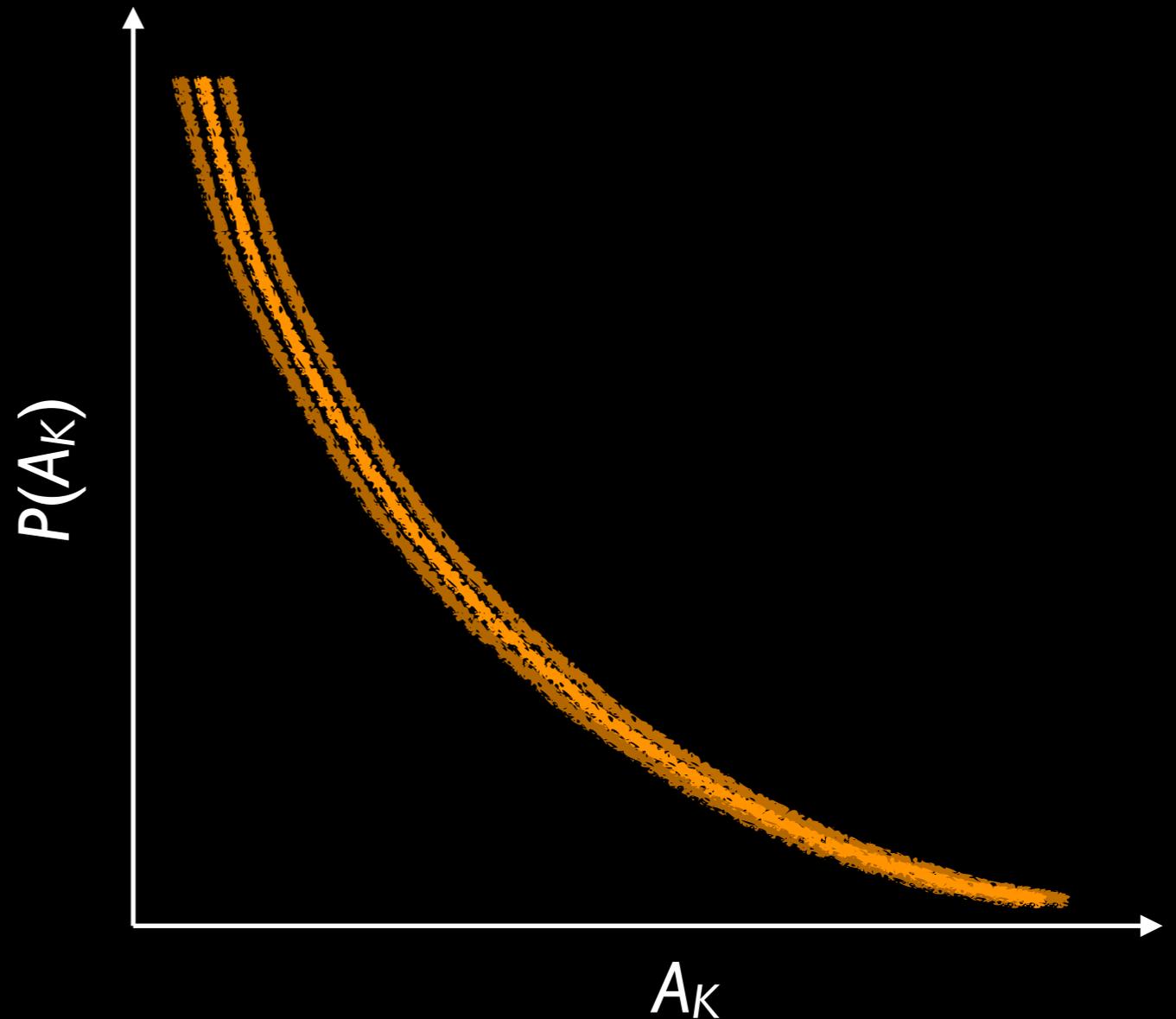
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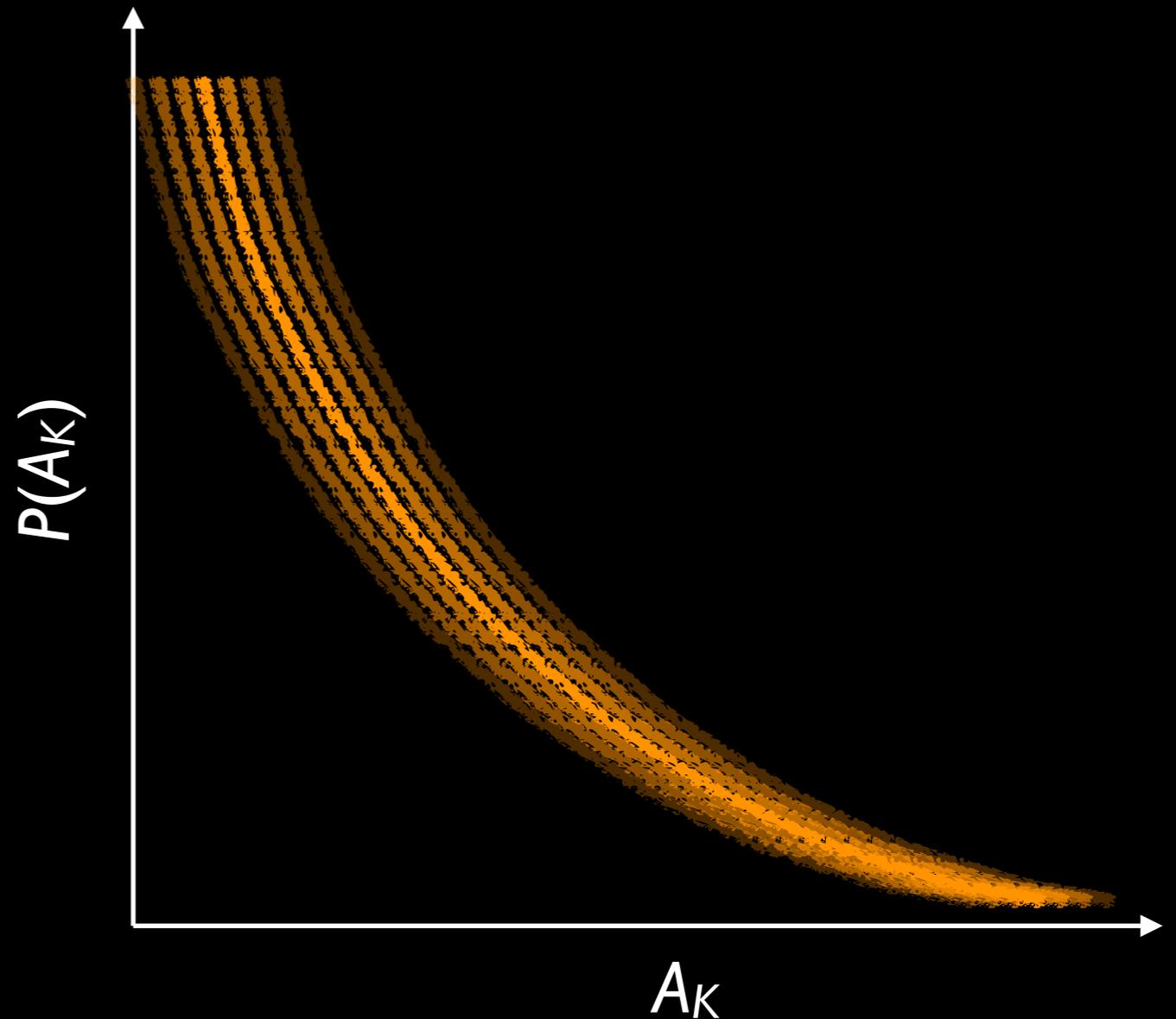
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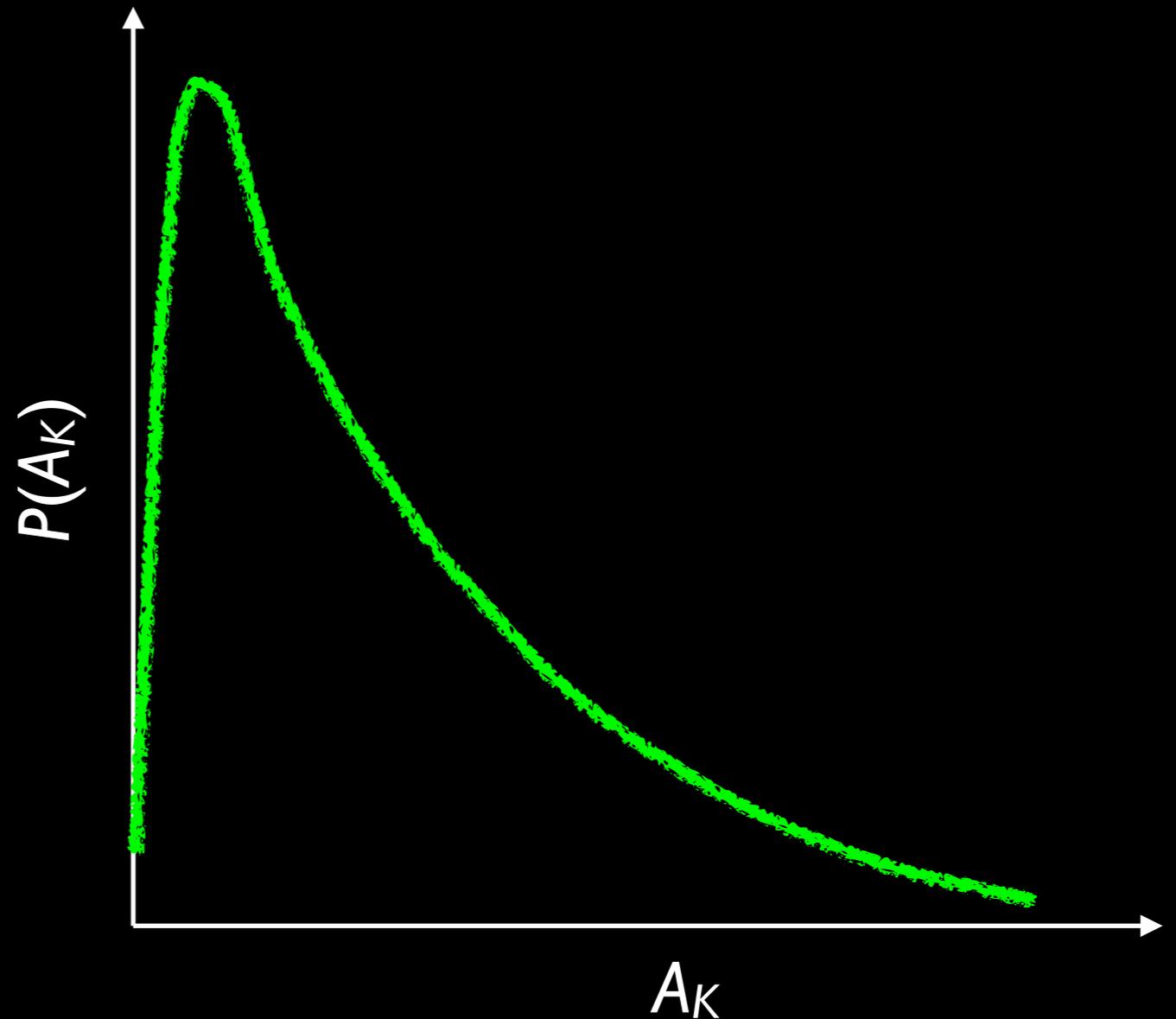
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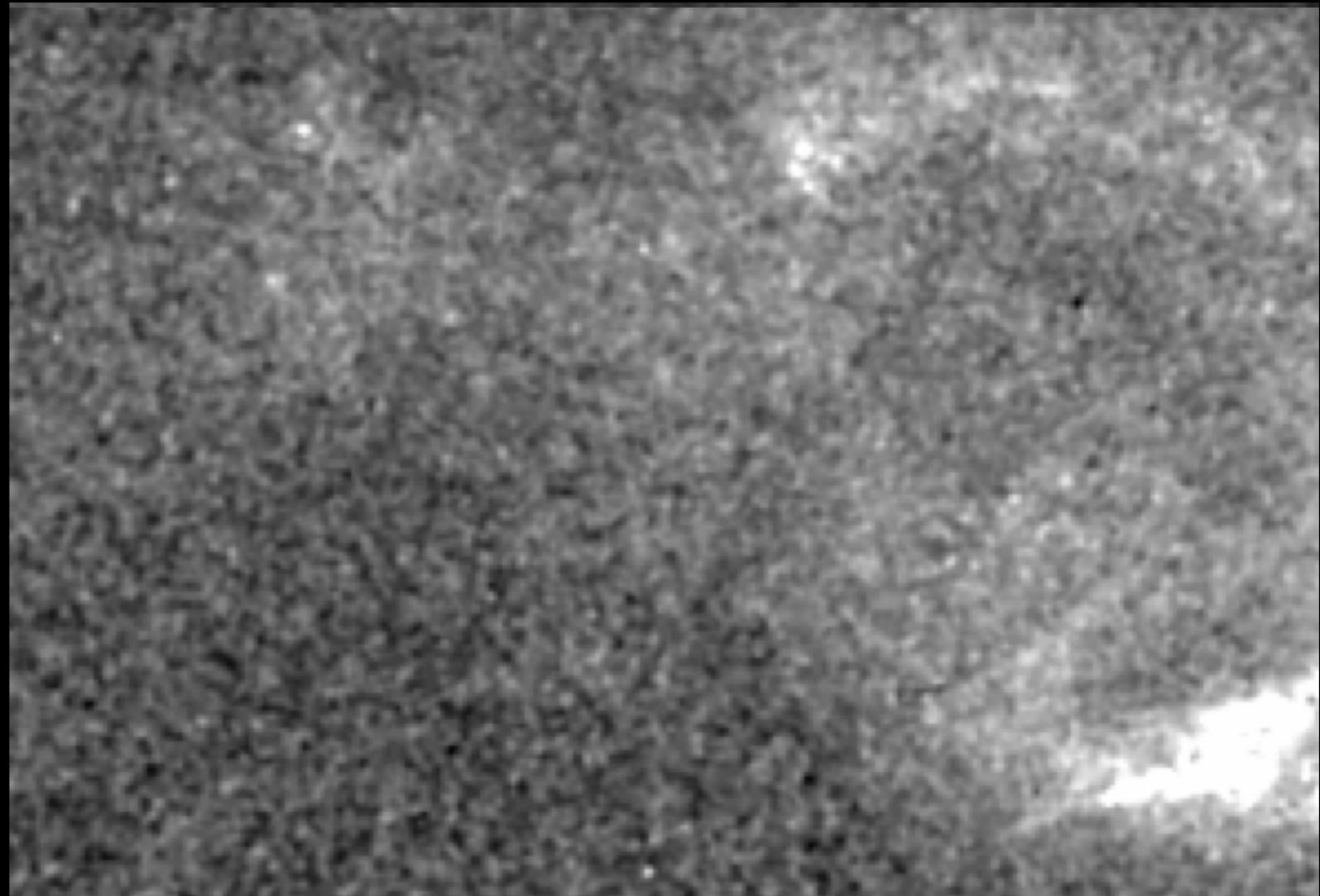
# Do yourself your log-normal!

## Recipe

- Take any nice cloud
- For optimal results, make sure the *true* PDF is decreasing
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- Observe the cloud
  - Make sure you make significant statistical errors
- You are done! The *observed* PDF looks like a log-normal!

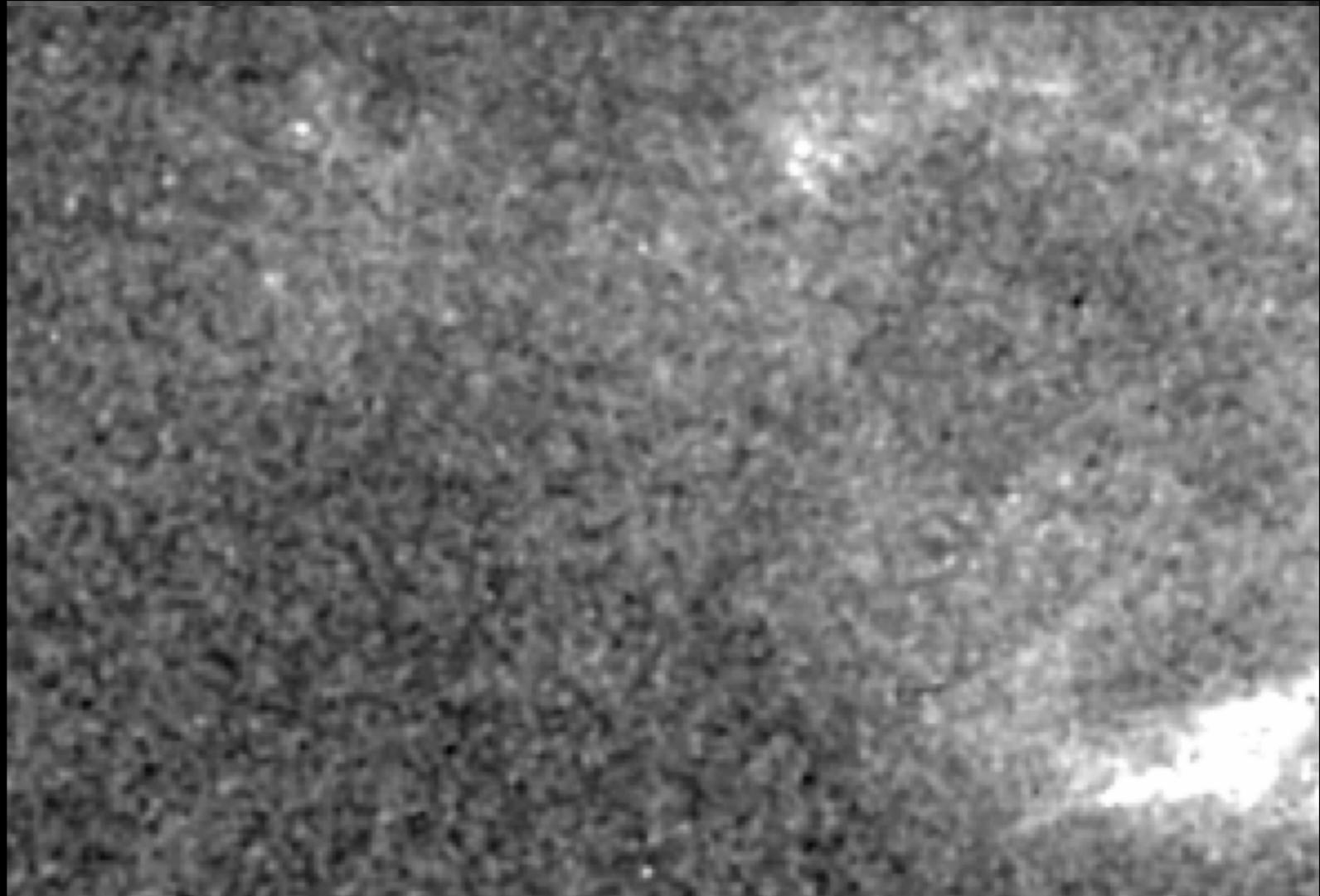


# PDFs, noise, and resolution



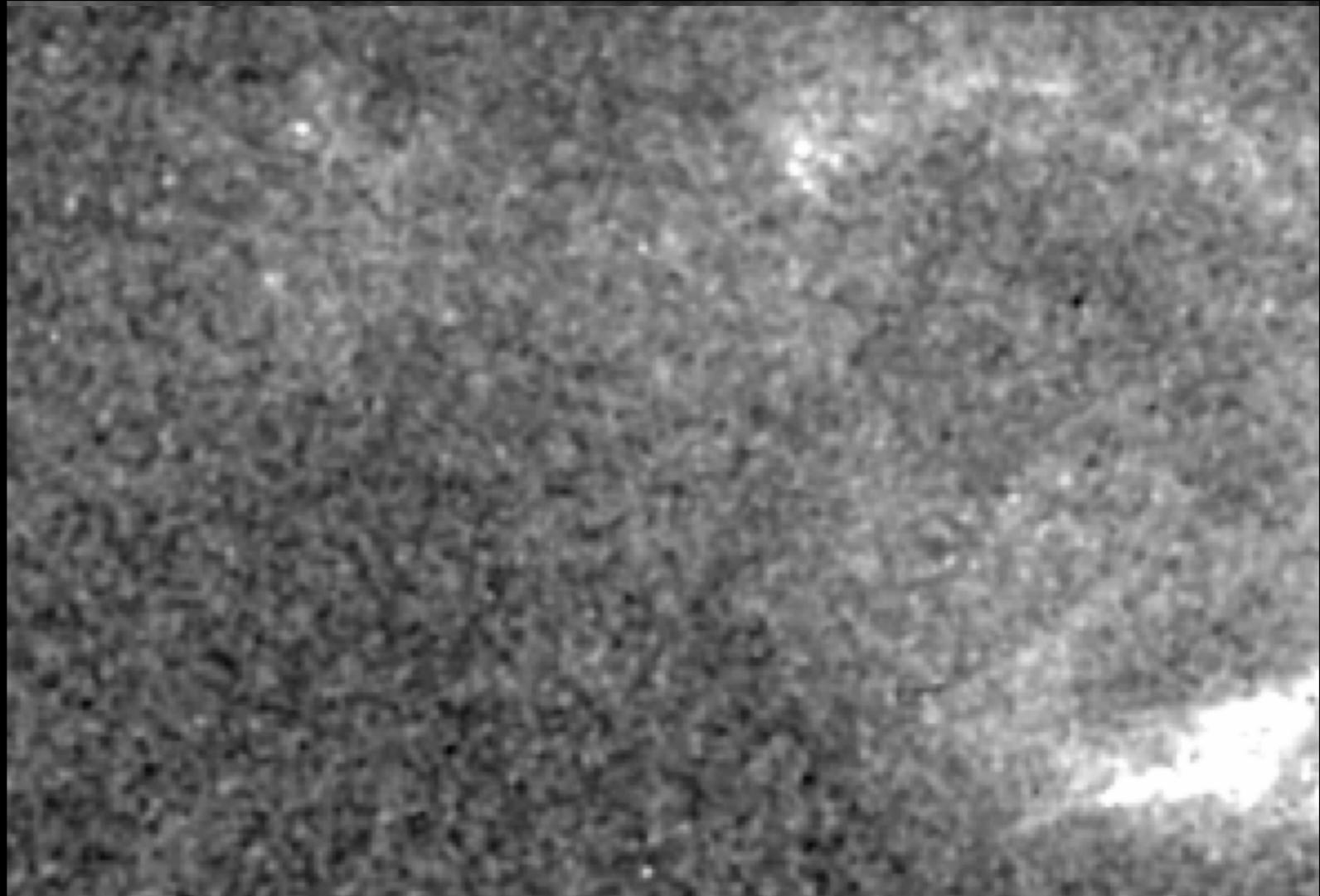
# PDFs, noise, and resolution

- Noise can be significant at low column densities



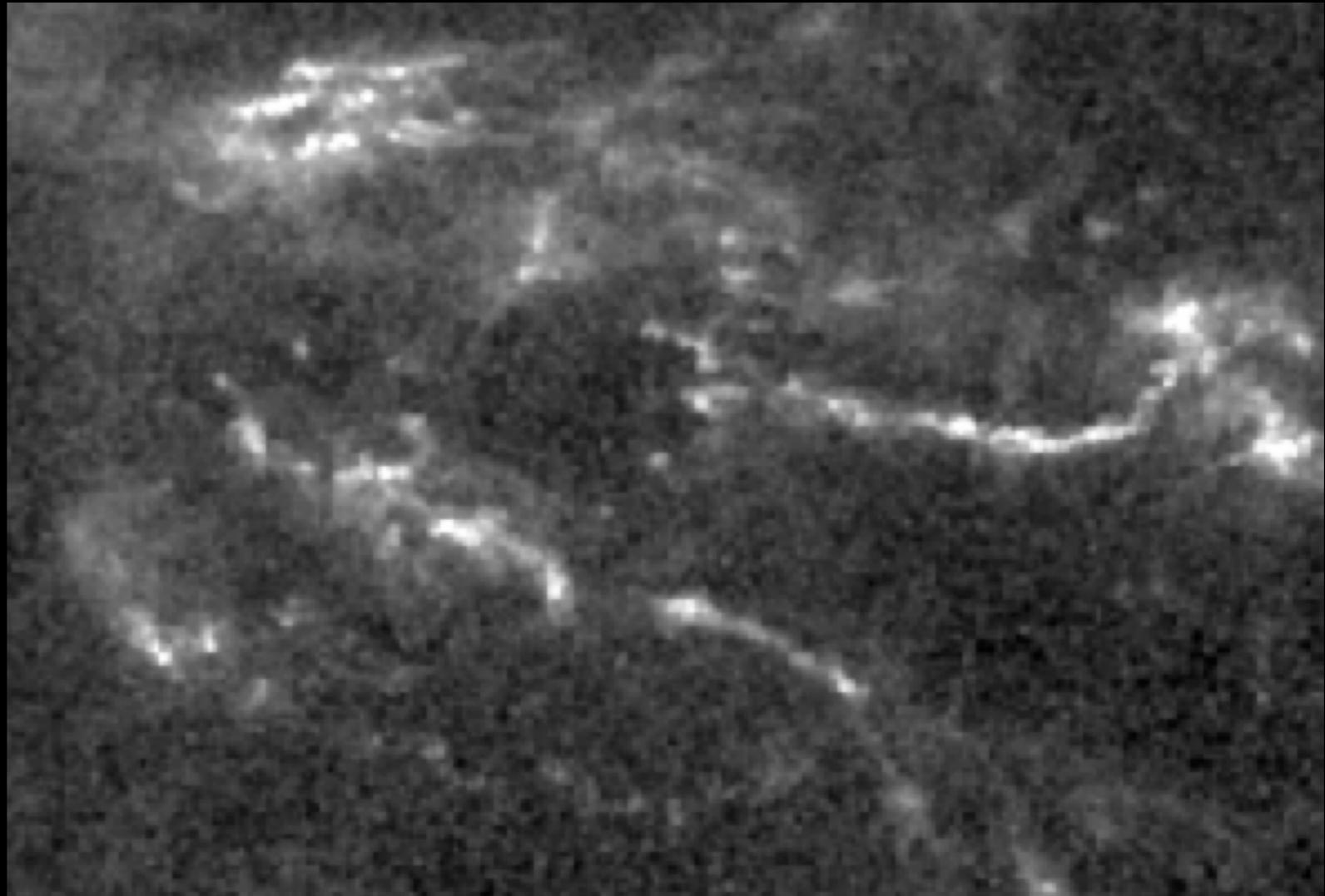
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- Noise can be significant at low column densities
- It affects mostly extinction maps of clouds at high  $b$



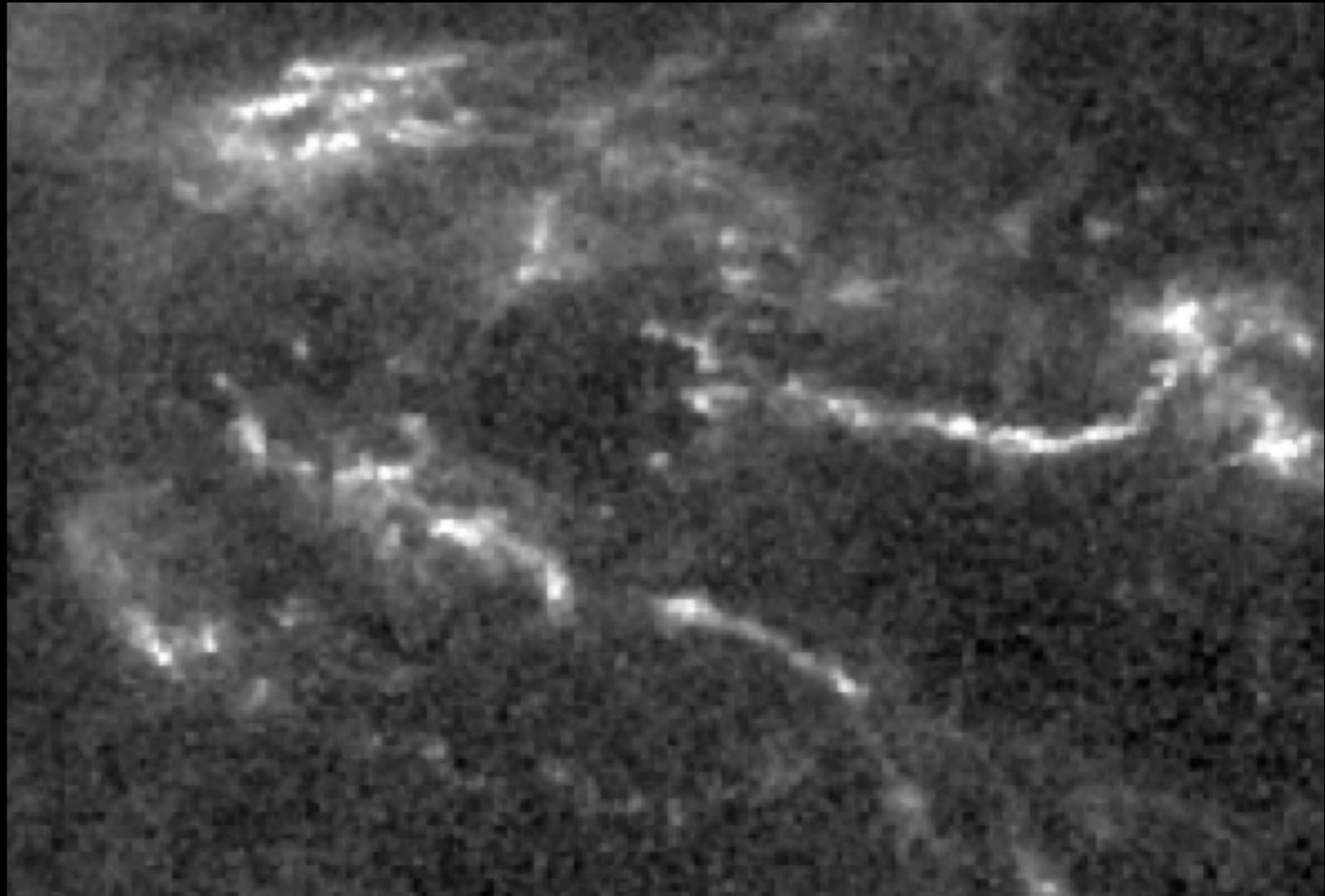
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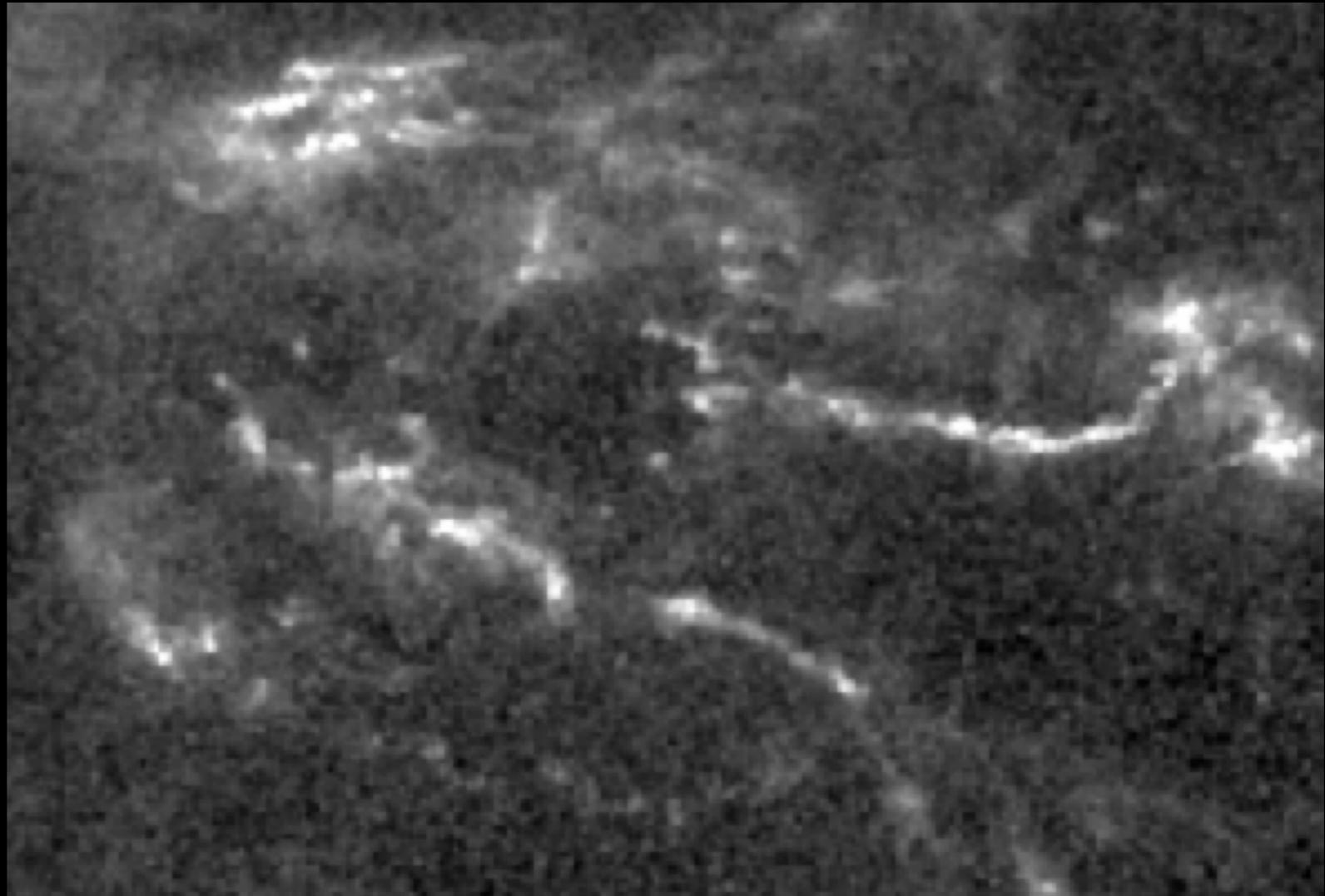
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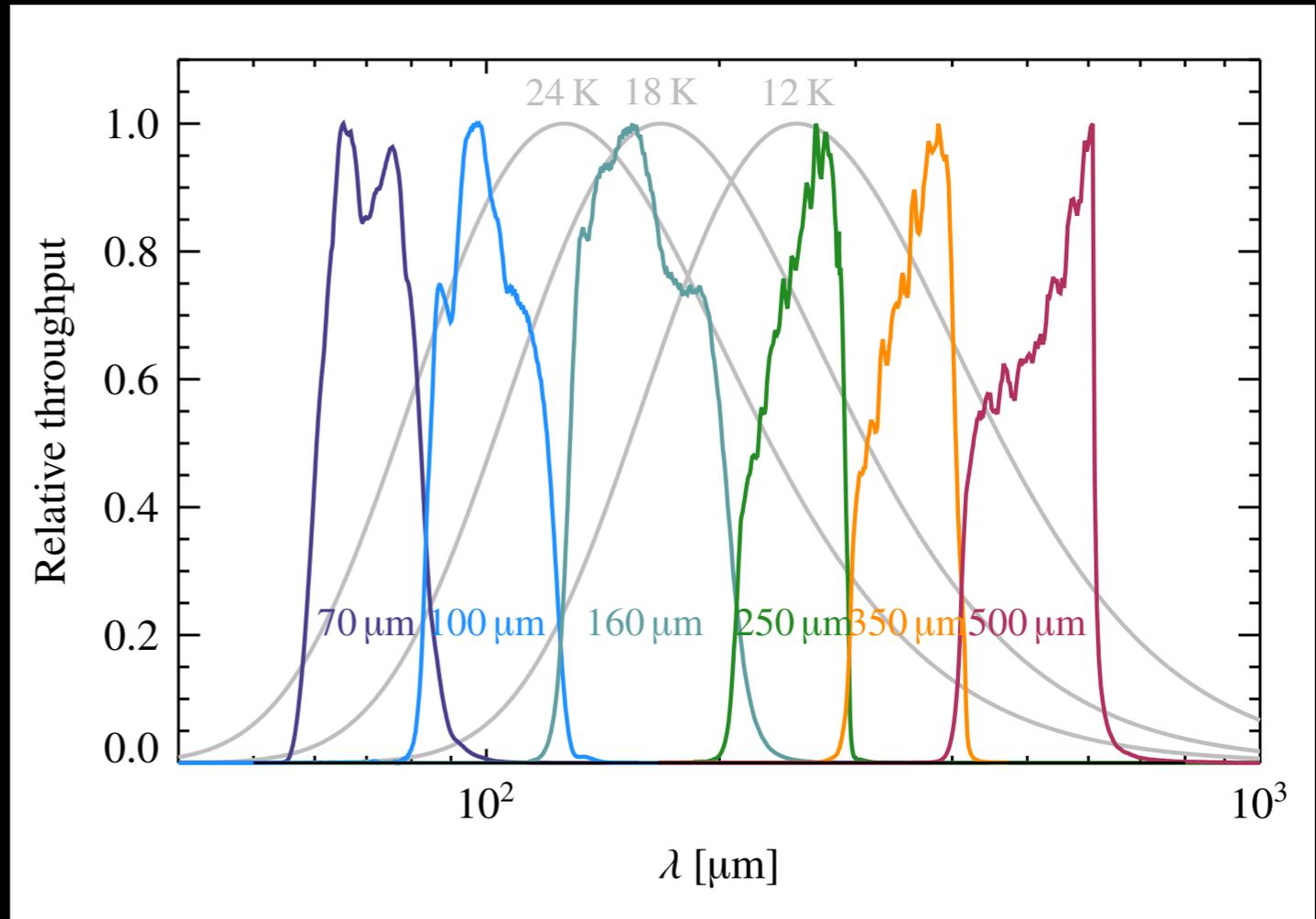
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Ideally we would like to have high-res, low-noise density maps of clouds

**Beat the noise: Herschel maps!**

# Dust emission data

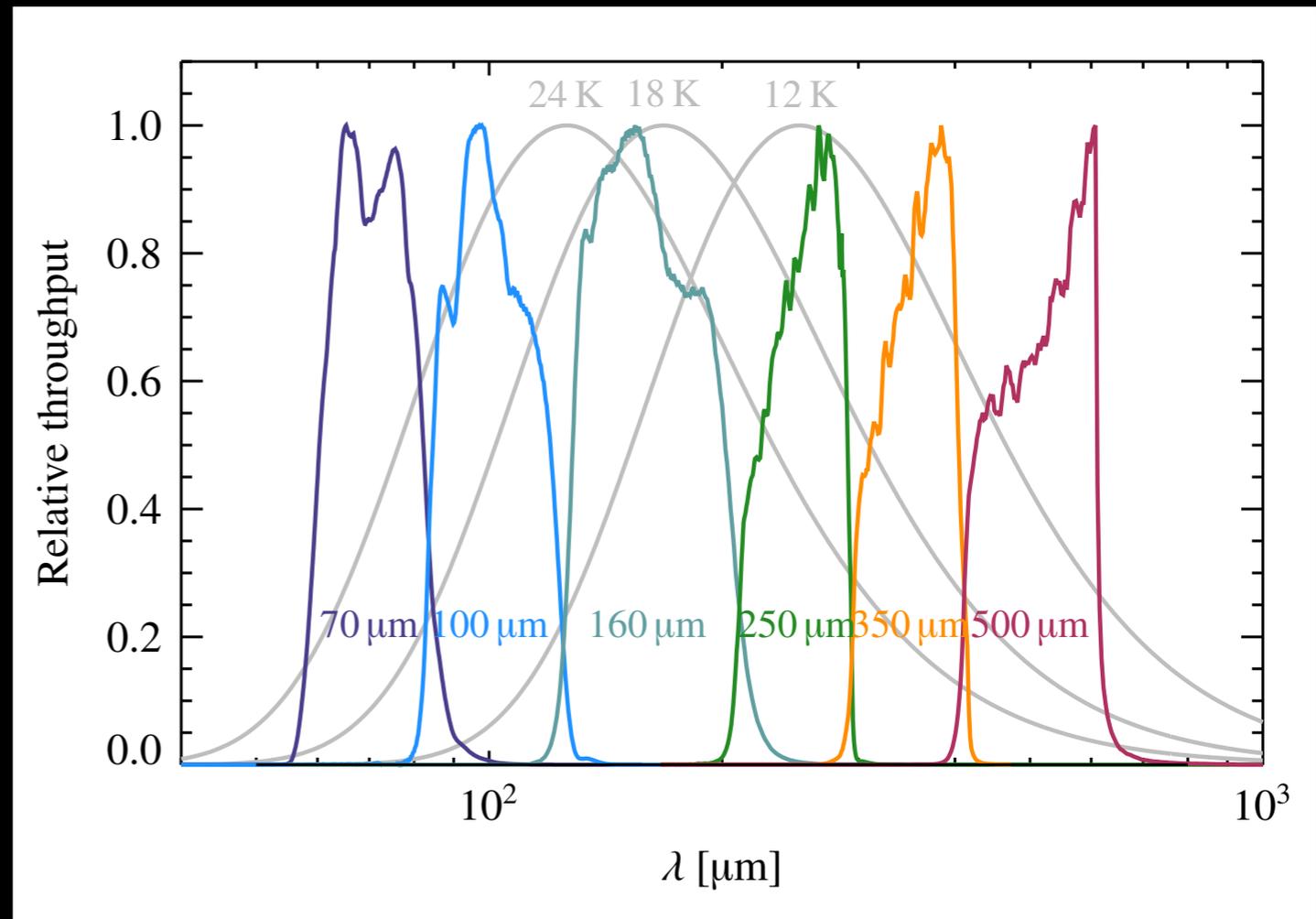


# Dust emission data

- A cloud emits a (modified) black body spectrum

$$I_\nu = B_\nu(T) [1 - e^{-\tau_\nu}] \simeq B_\nu(T) \tau_\nu$$

$$\tau_\nu = \kappa_\nu \Sigma_{\text{dust}} \propto \nu^\beta$$



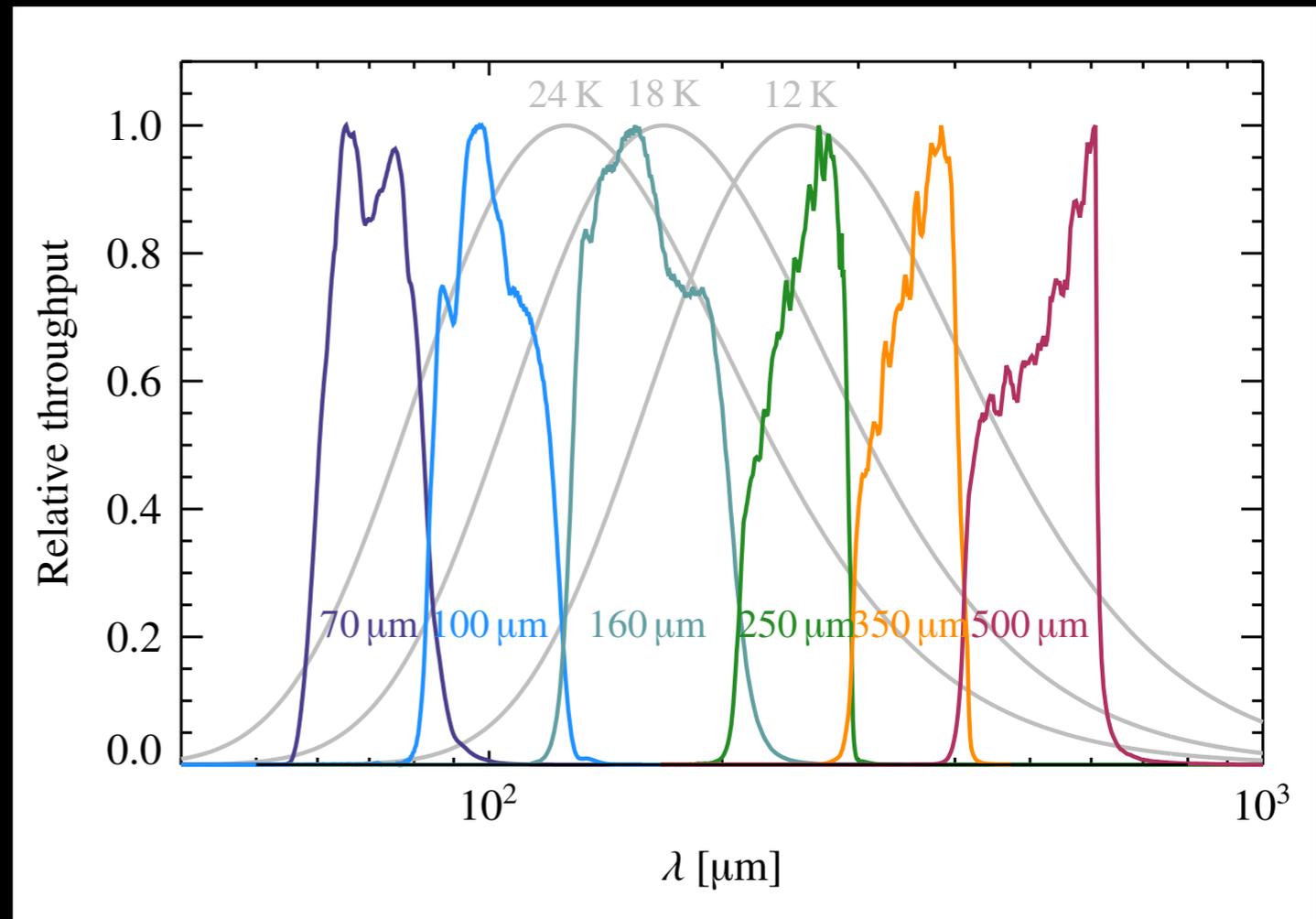
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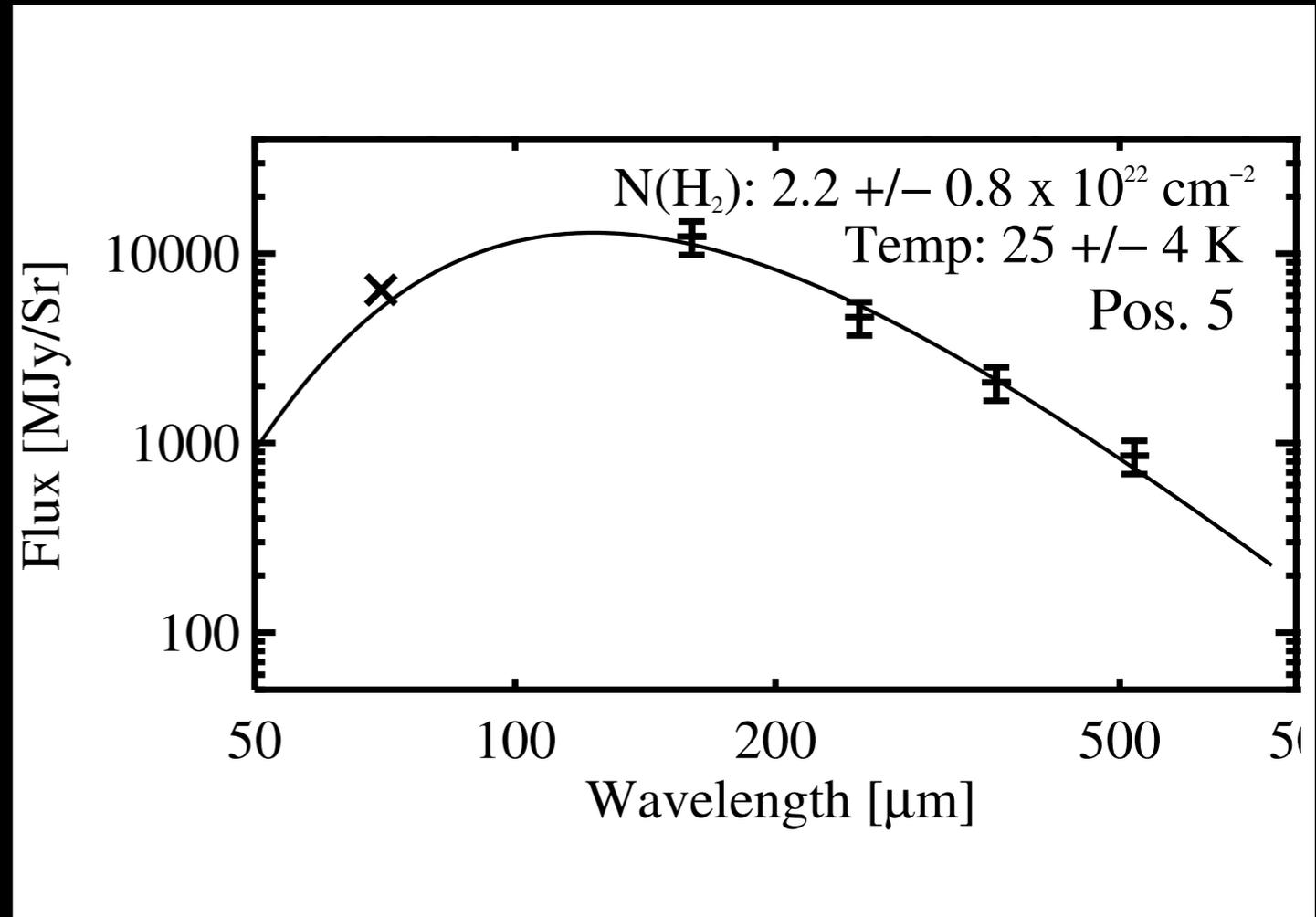
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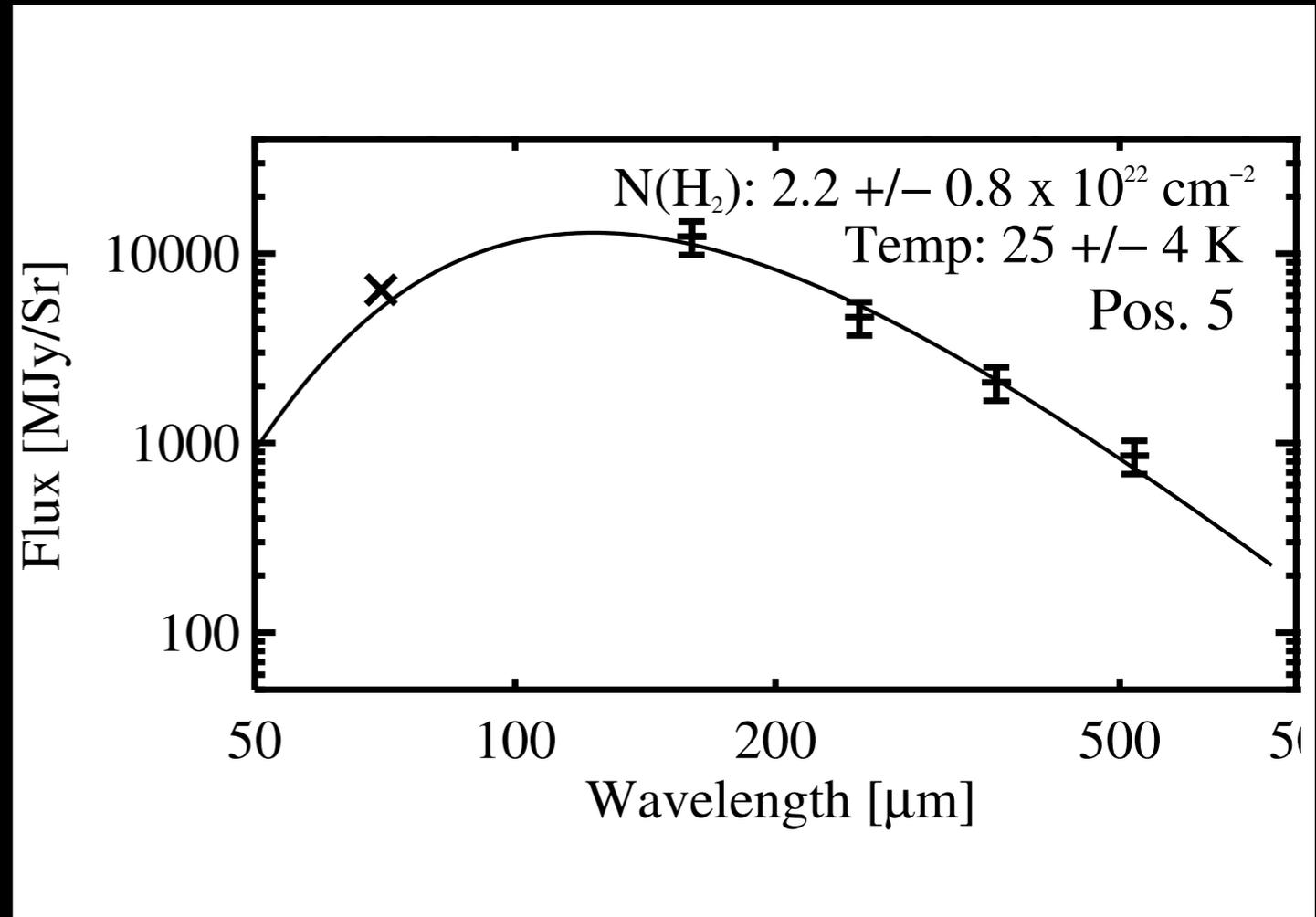
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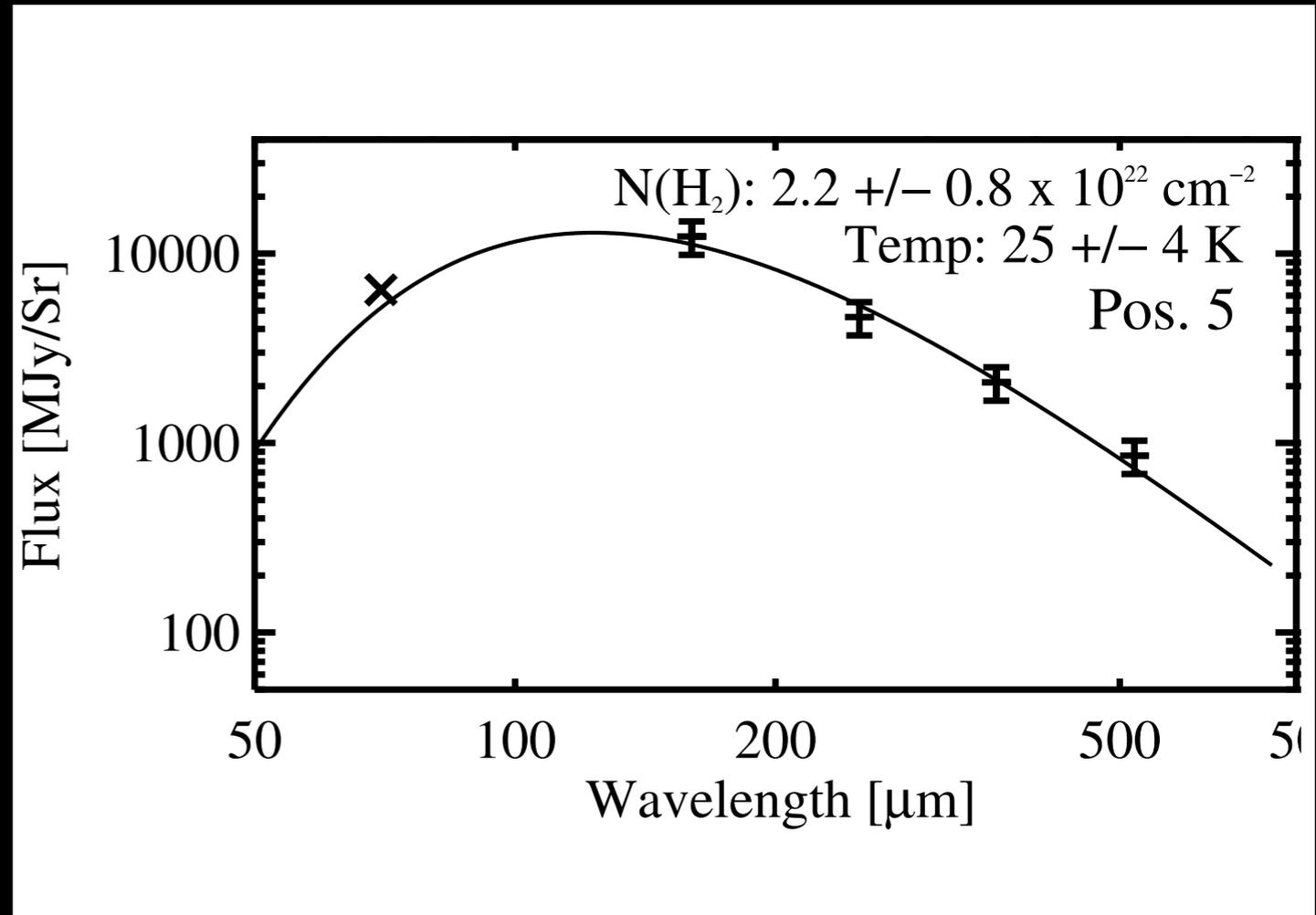
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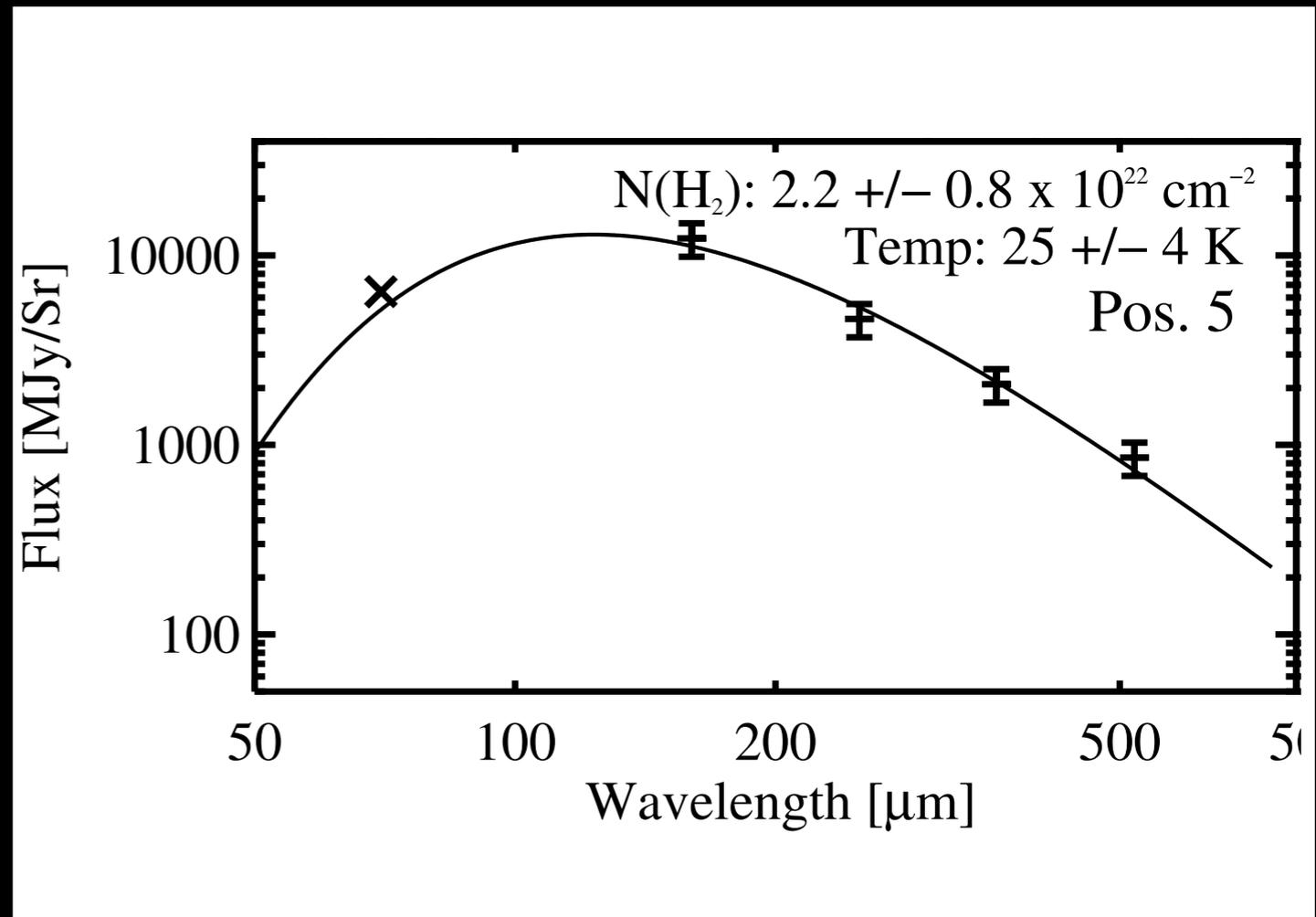
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- Temperature gradients along the l.o.s. bias  $\tau$  low
- Things almost certainly go wrong near OB associations  $\gamma$

# Orion A & B

(Lombardi et al. 2014)

Mon R2

NGC 2071 —  
NGC 2068 —

Orion B

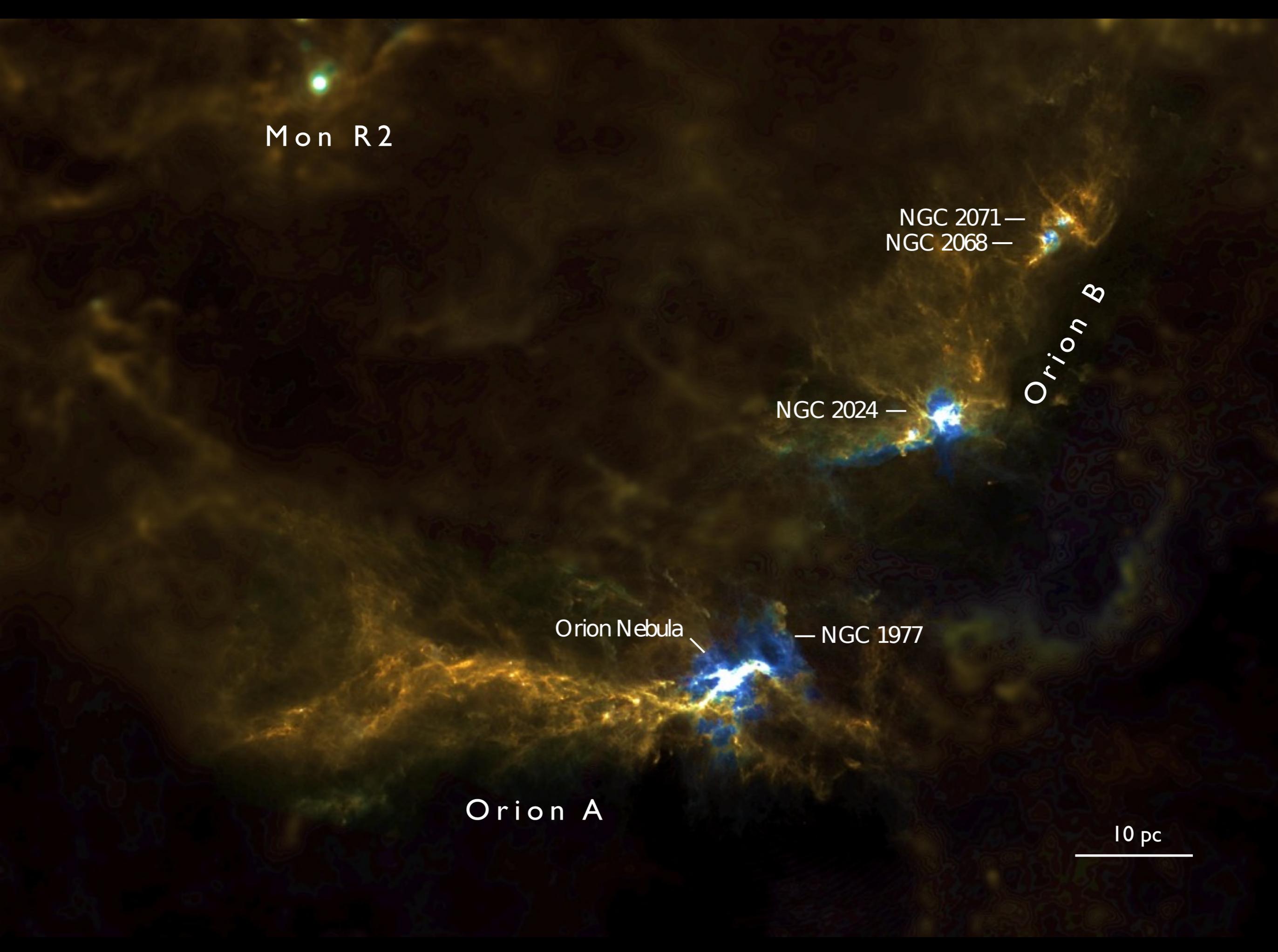
NGC 2024 —

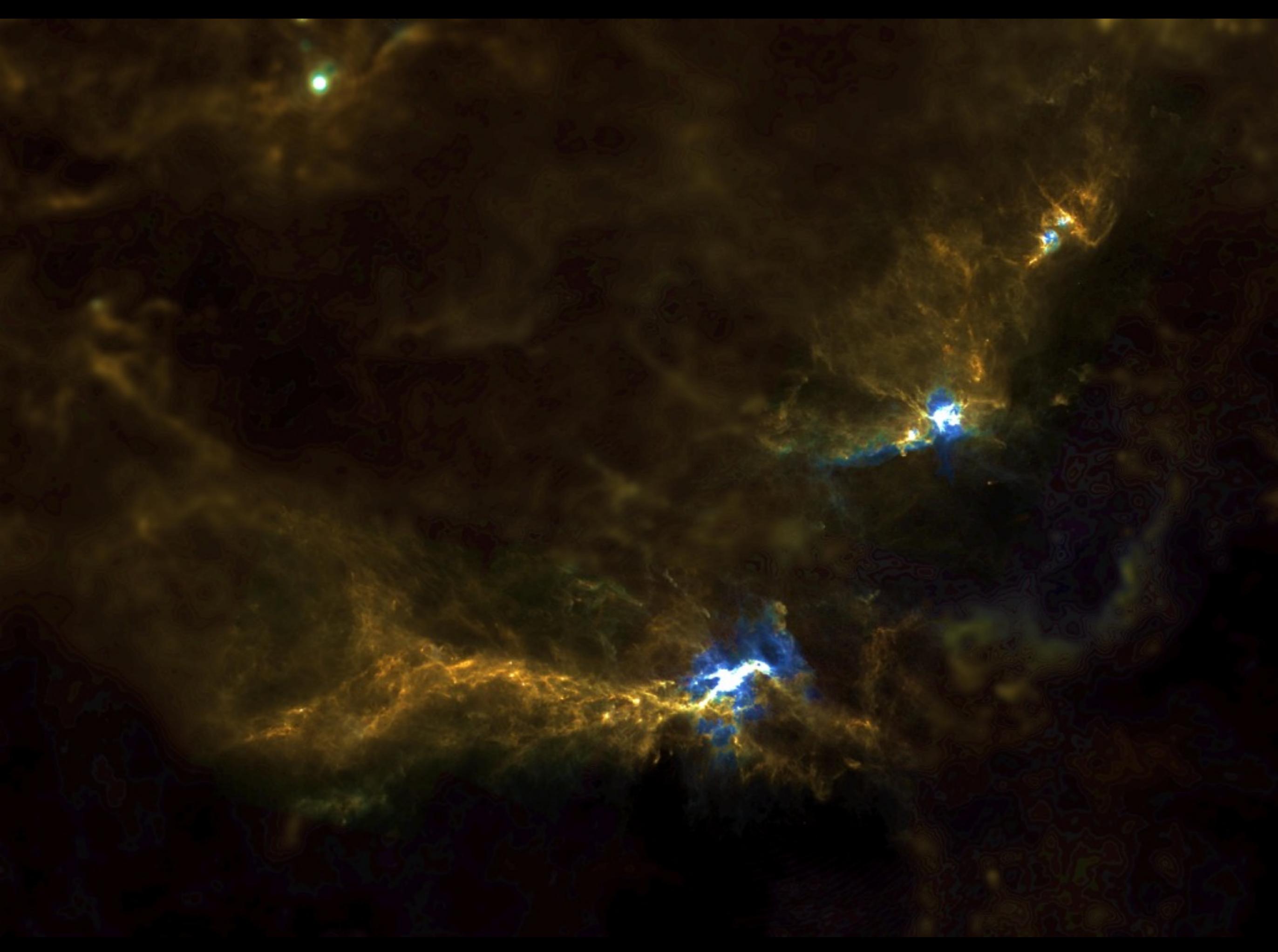
Orion Nebula

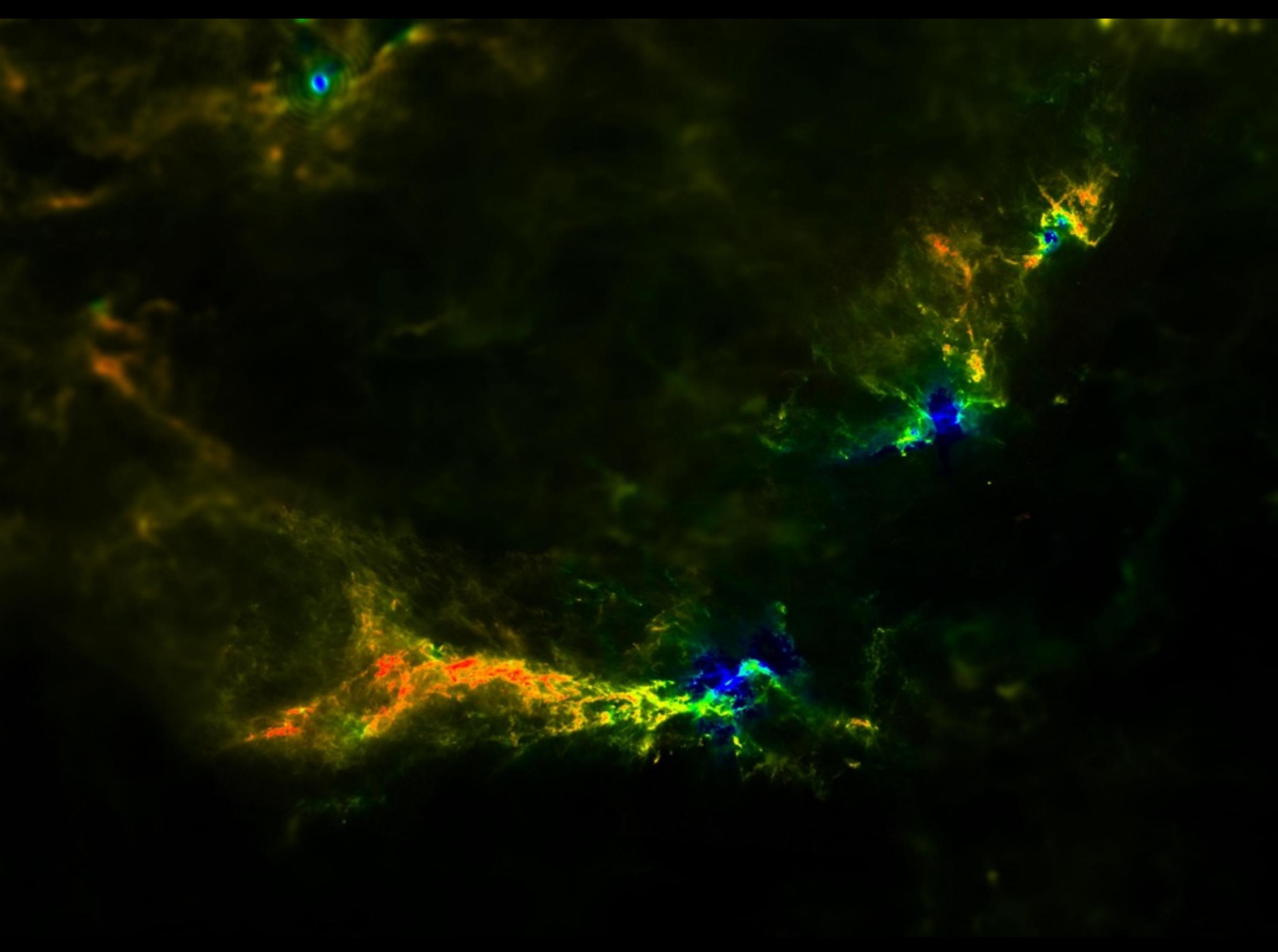
— NGC 1977

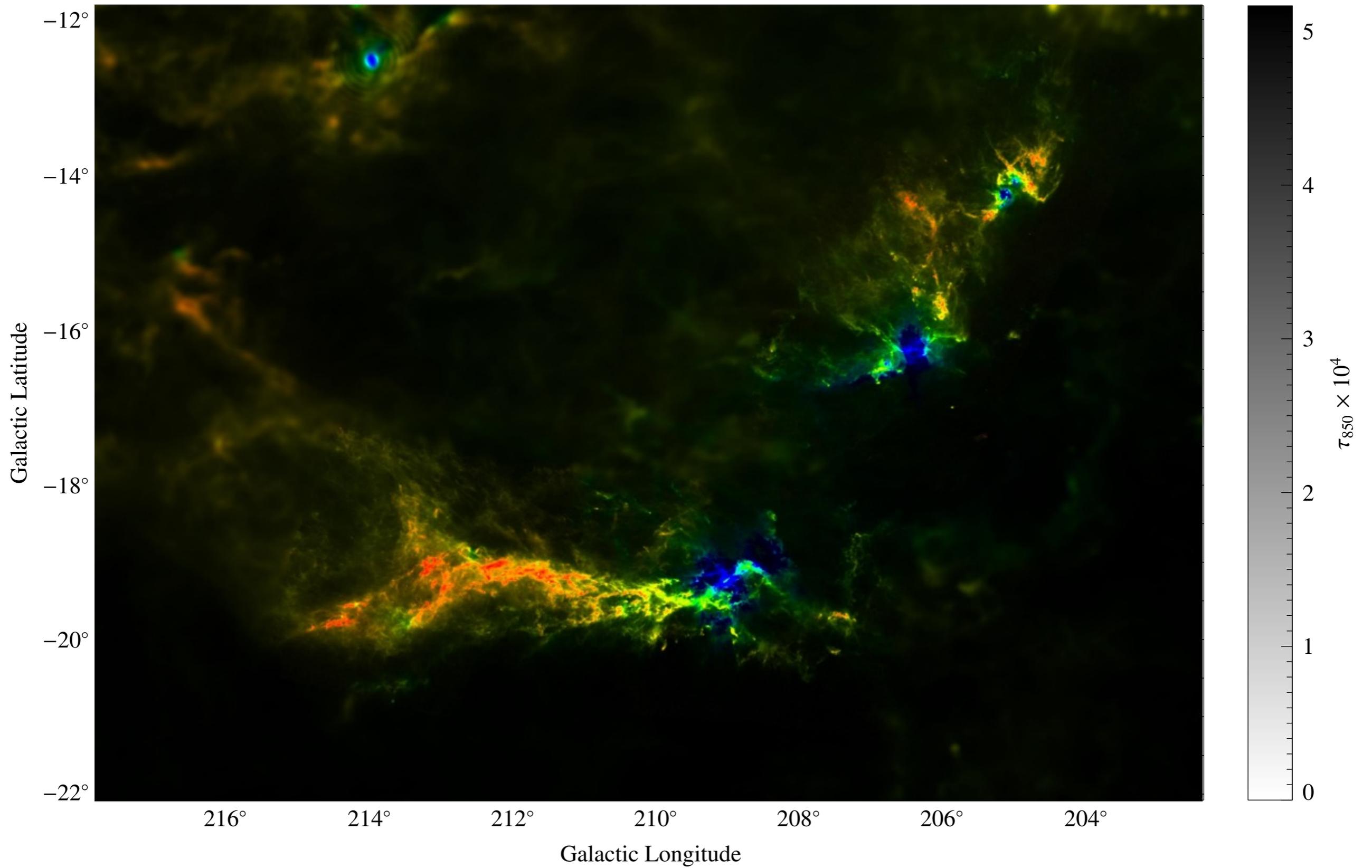
Orion A

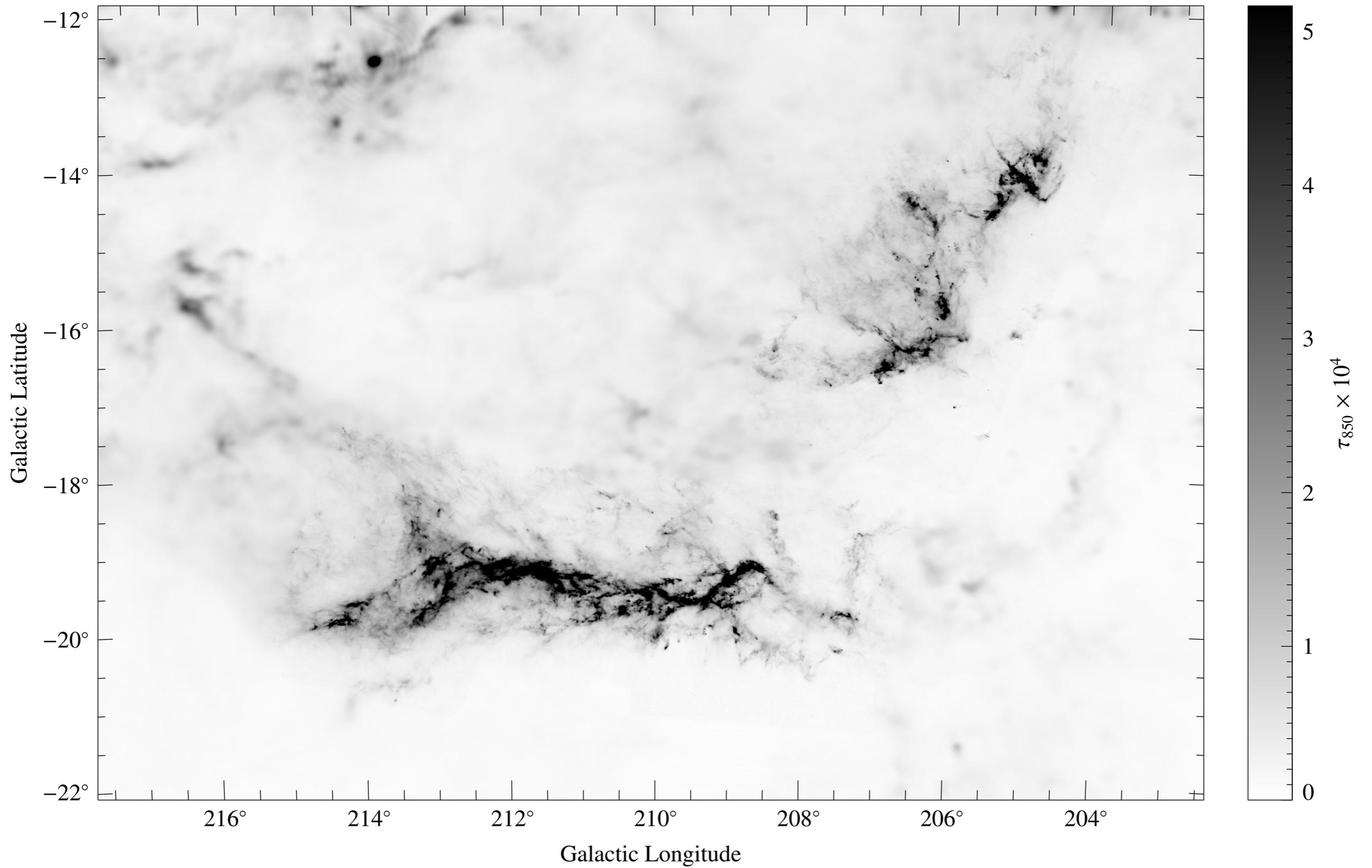
10 pc

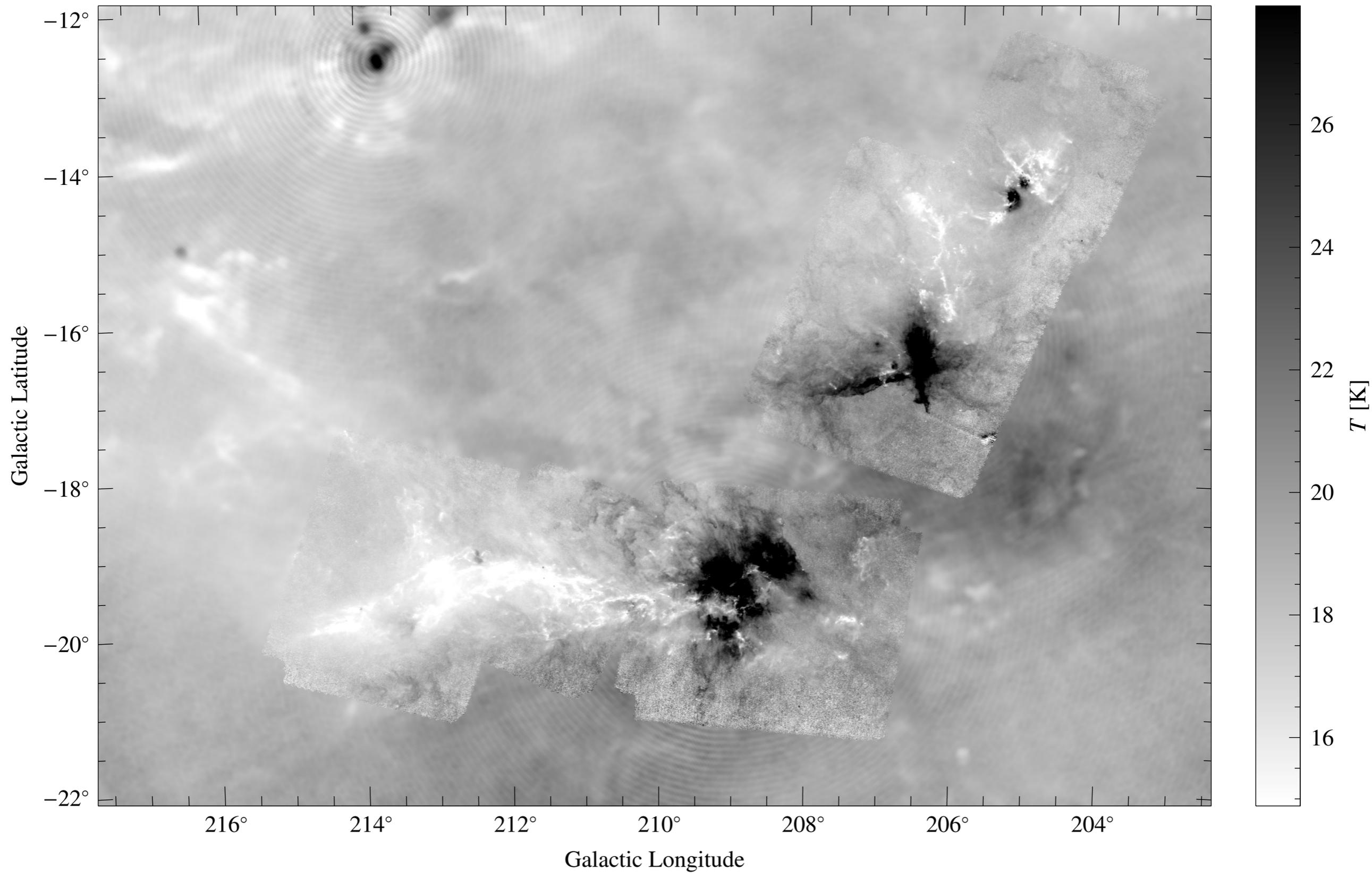




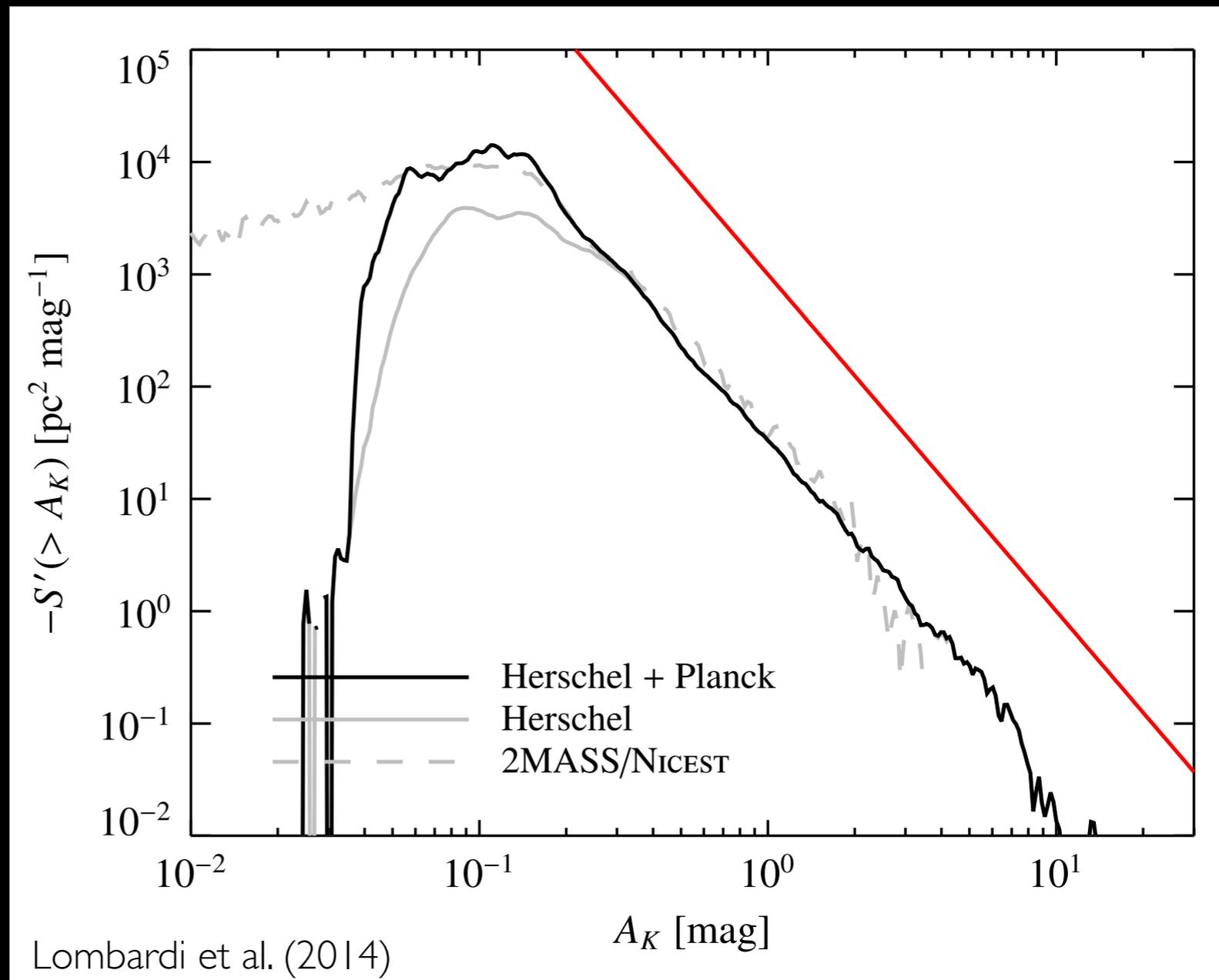






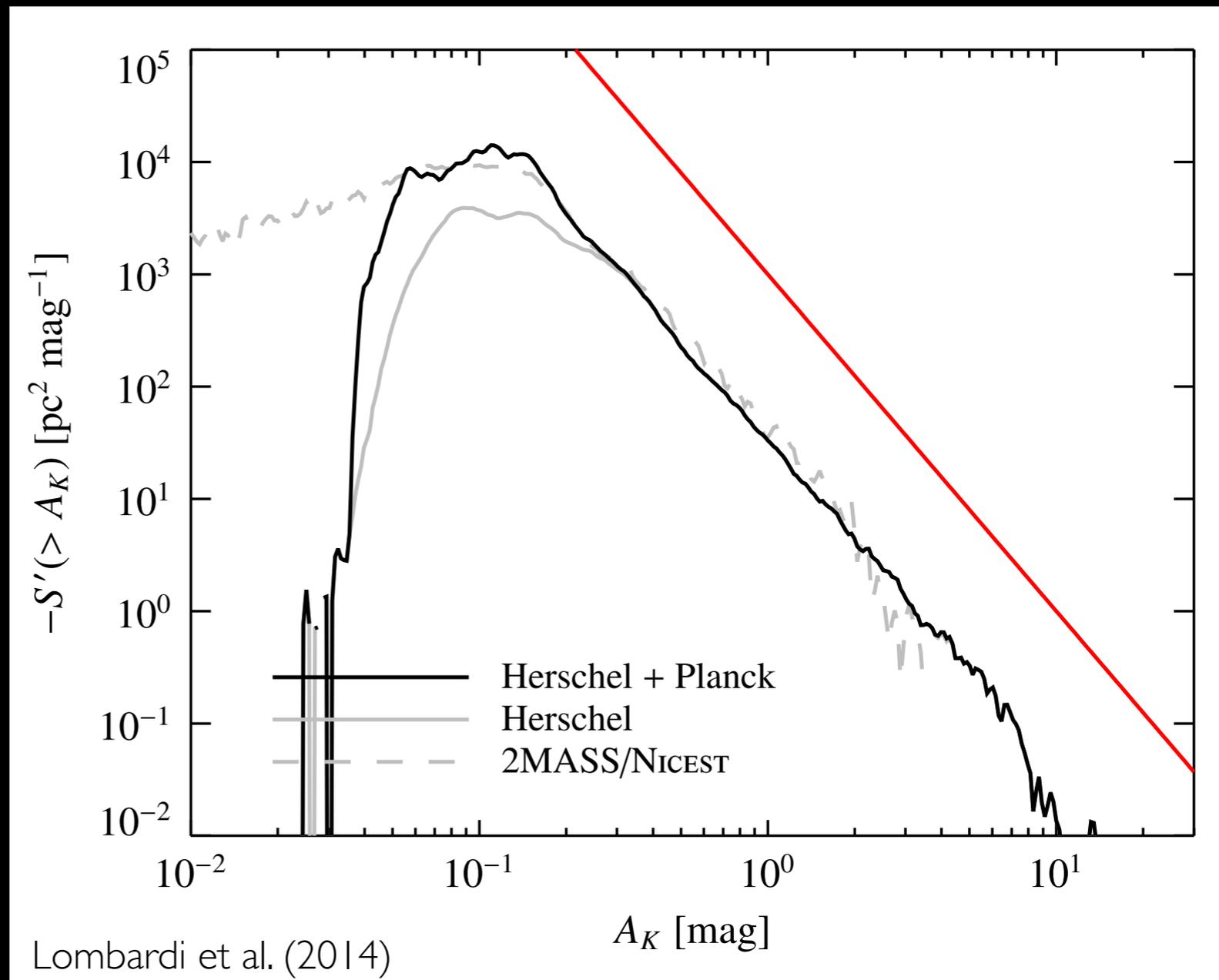


# Herschel PDF for Orion B



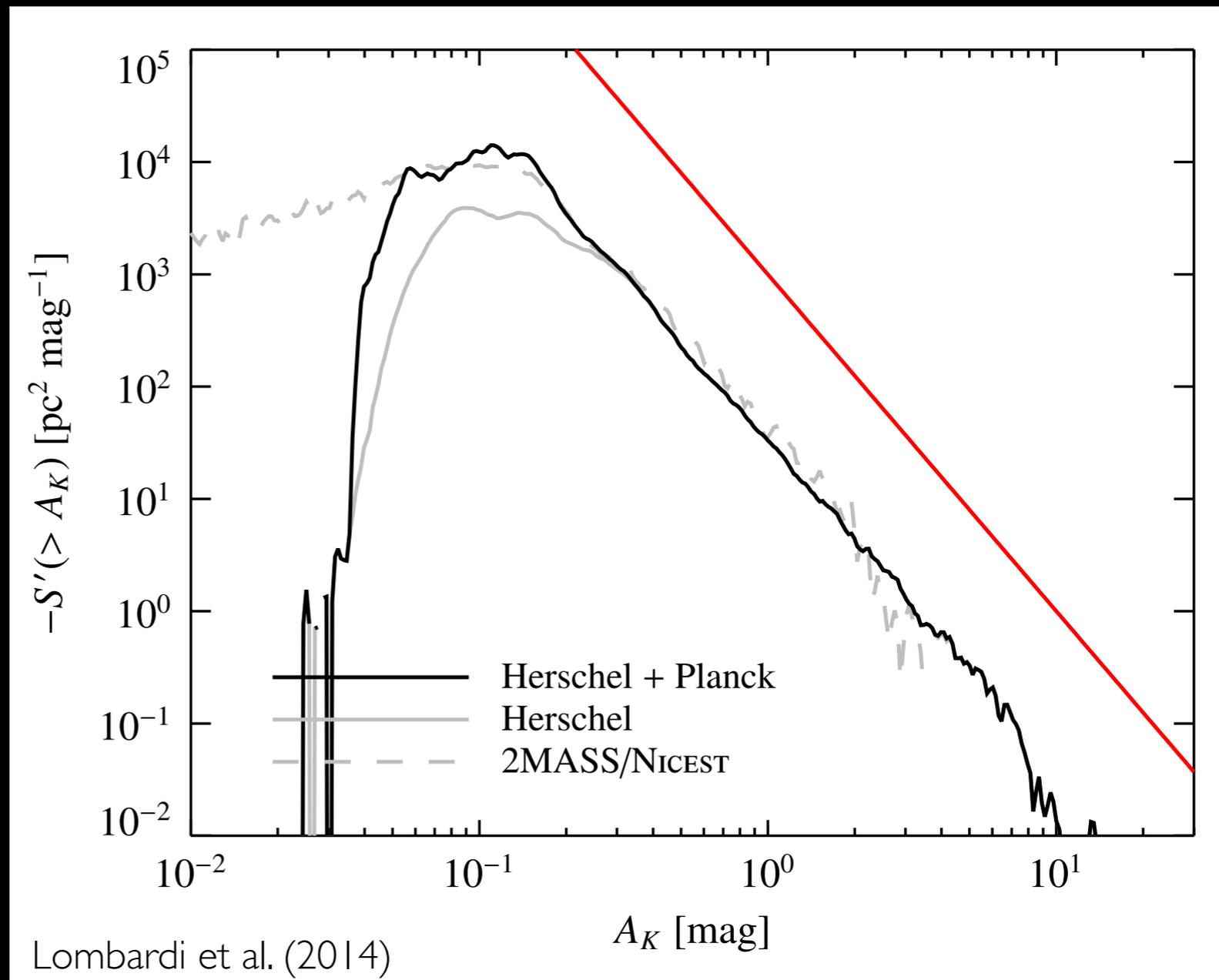
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- PDF is hardly symmetric in log-log



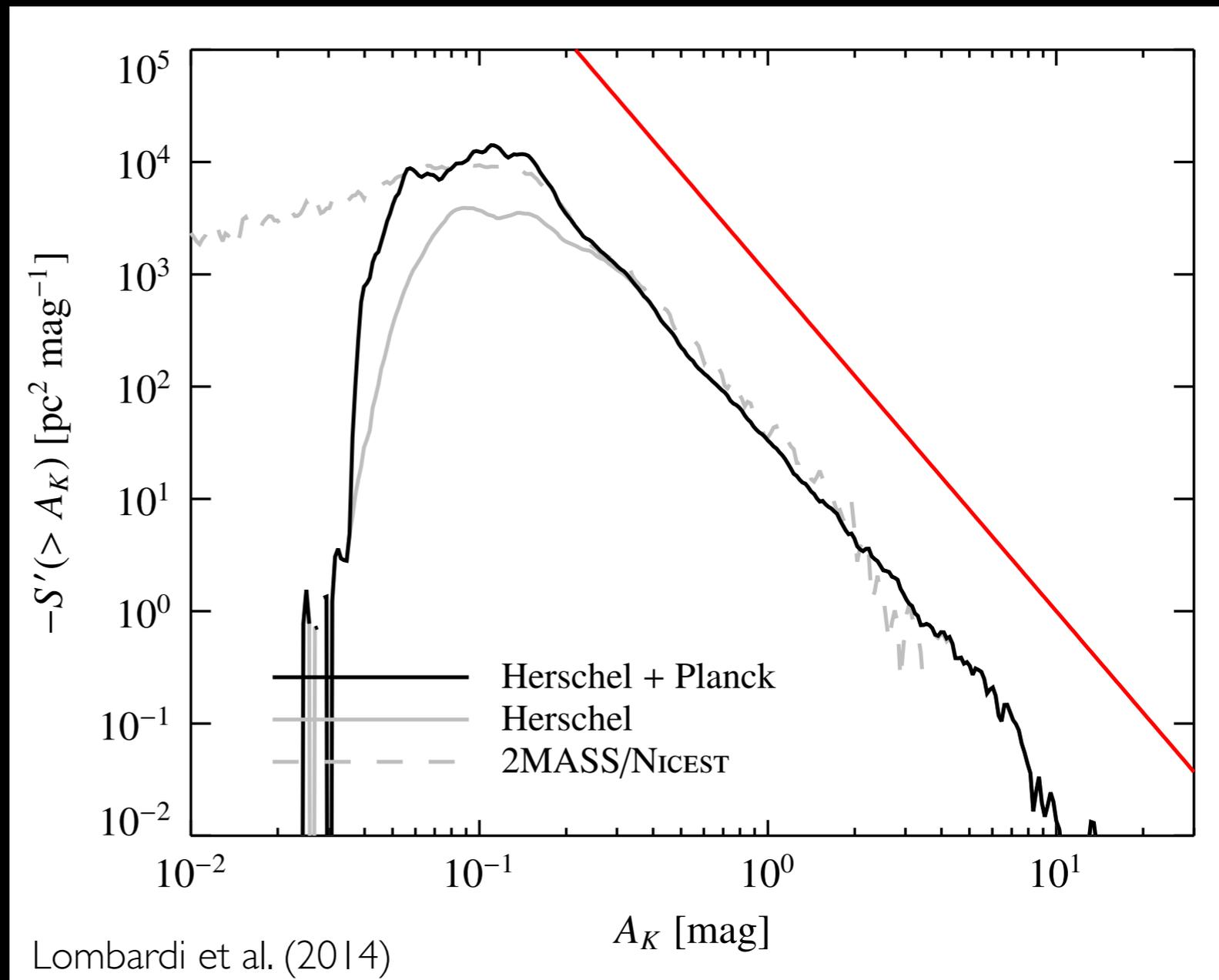
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- Turn @  $A_K \sim 0.15$  mag



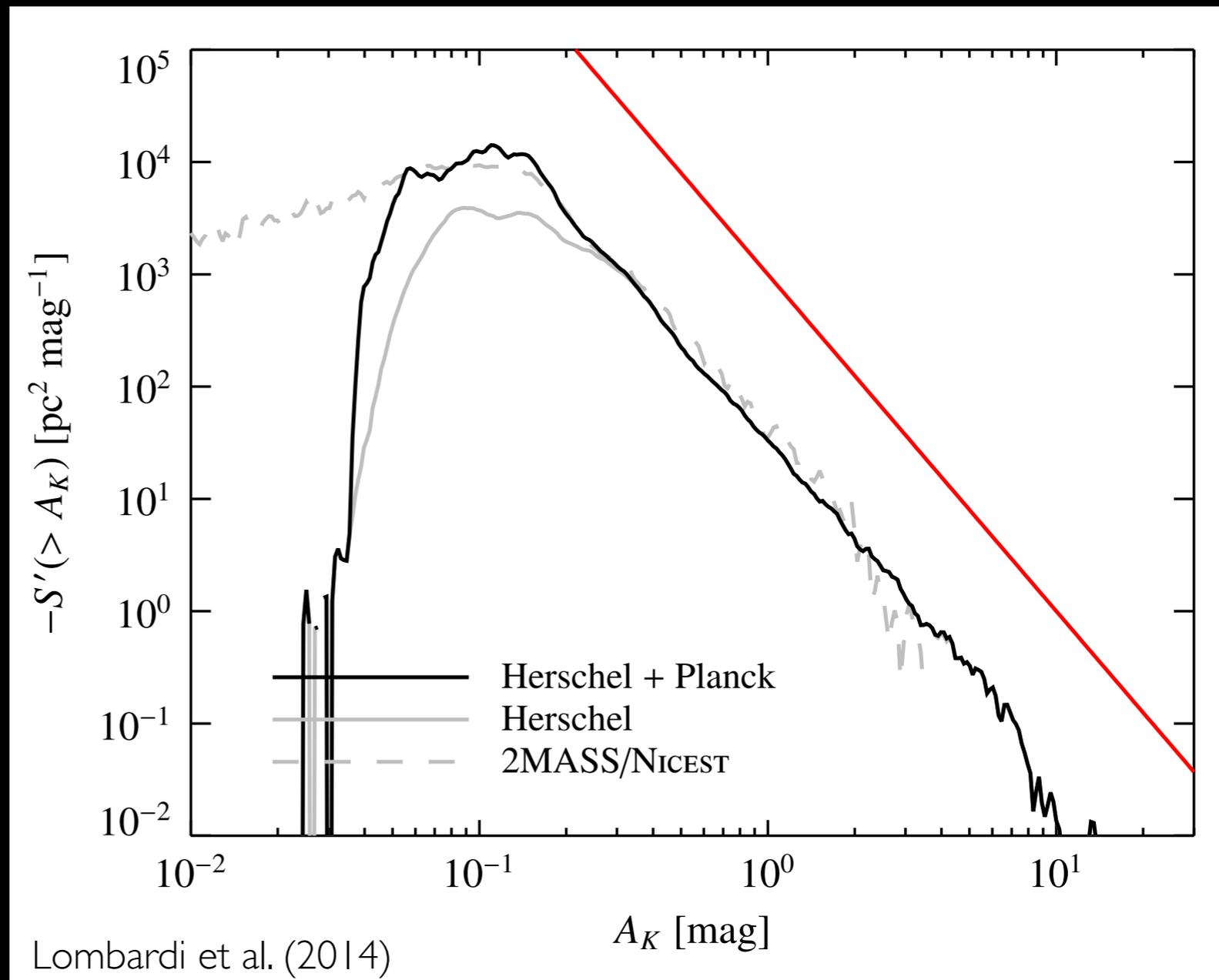
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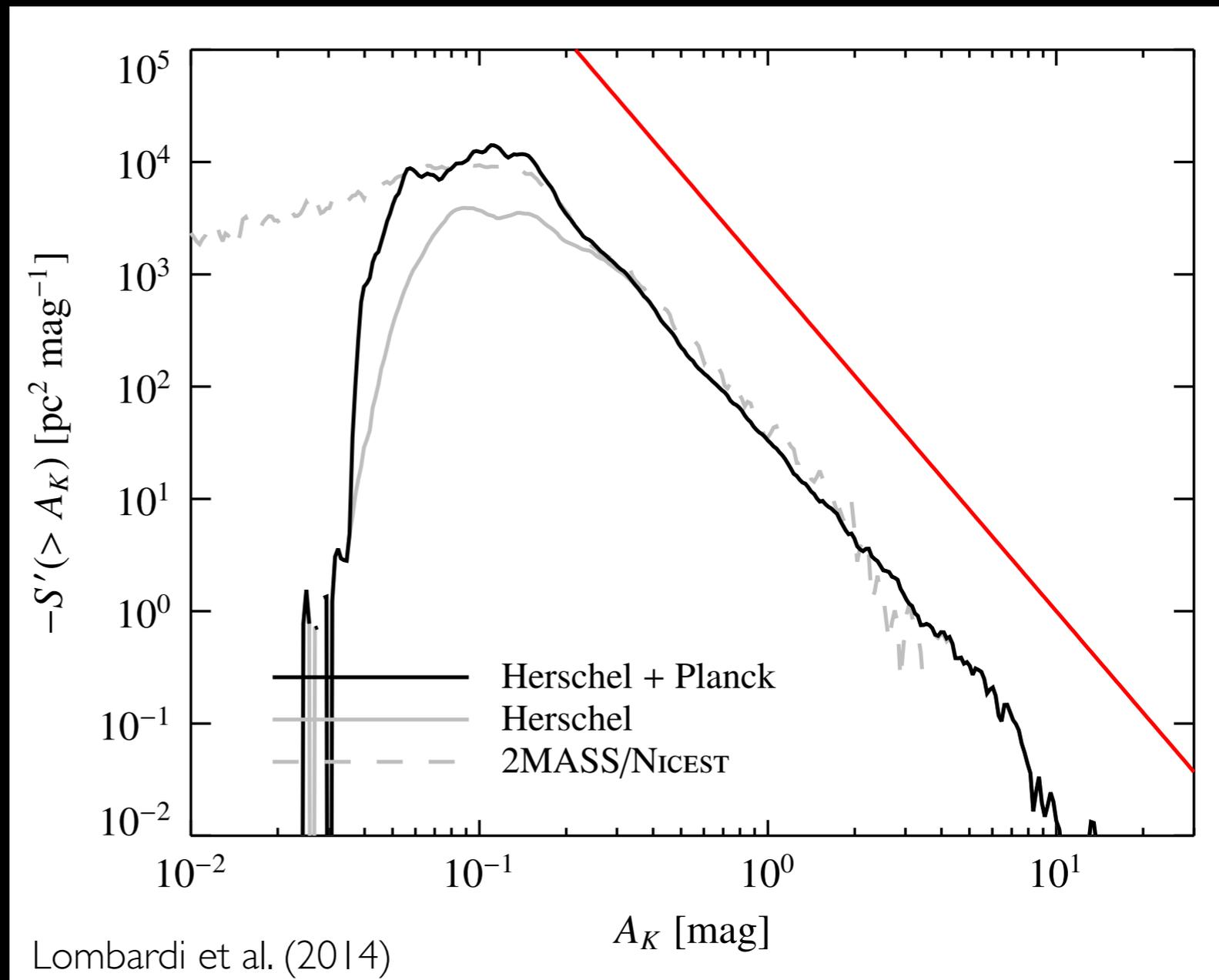
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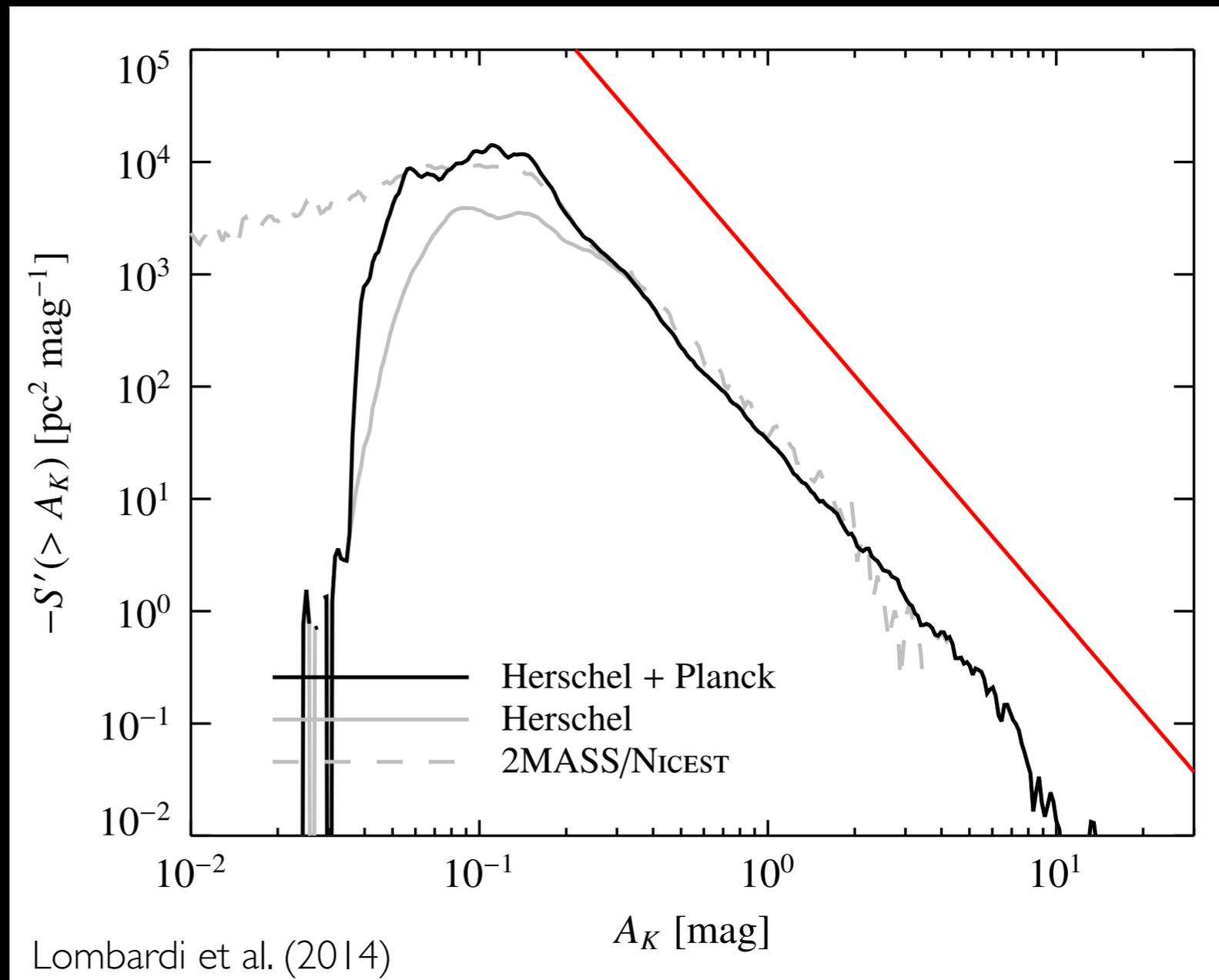
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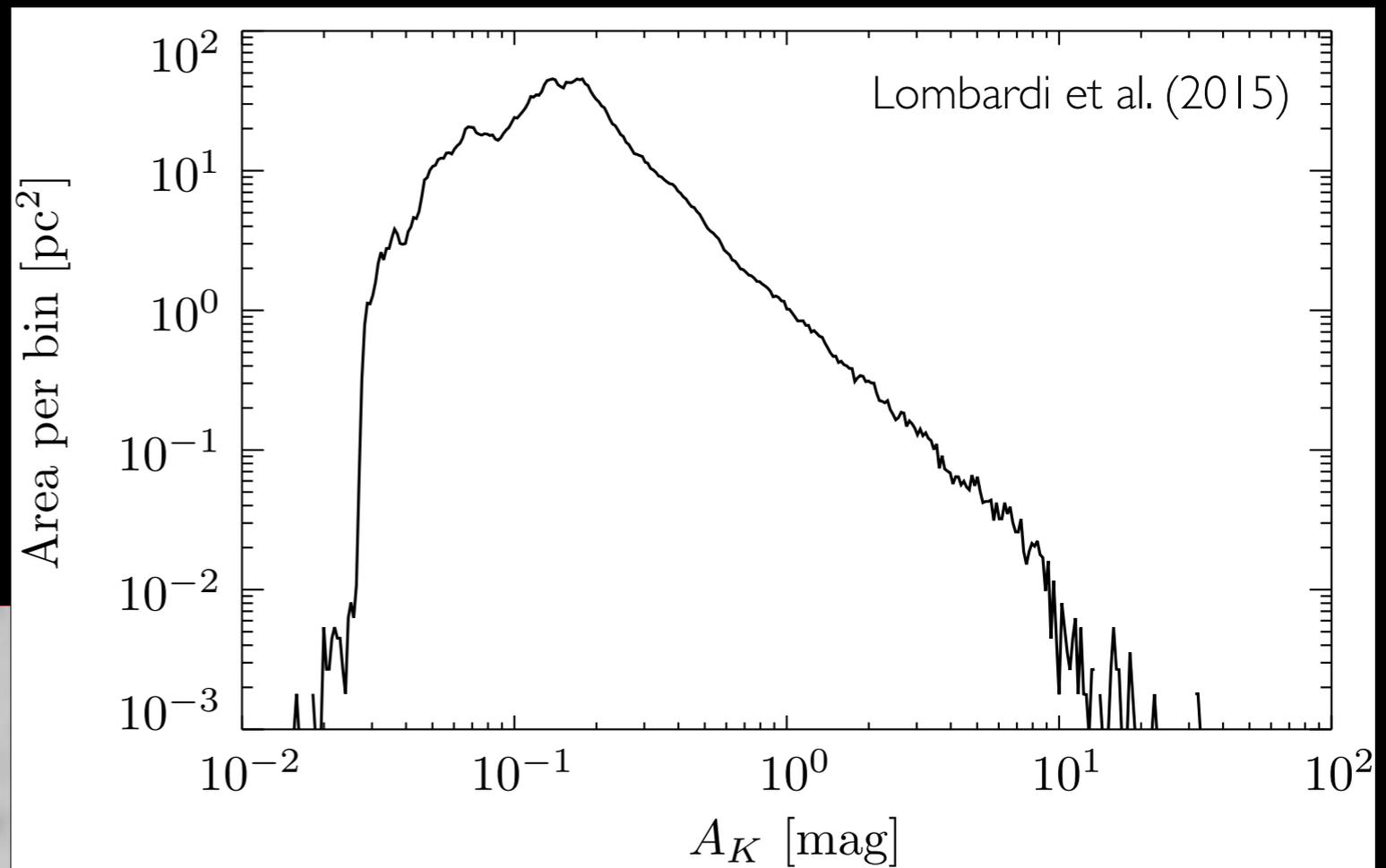
Log-normals, if present, confined to low  $A_K$

# Can we actually probe the low $A_K$ ?

Lombardi et al. (2015)

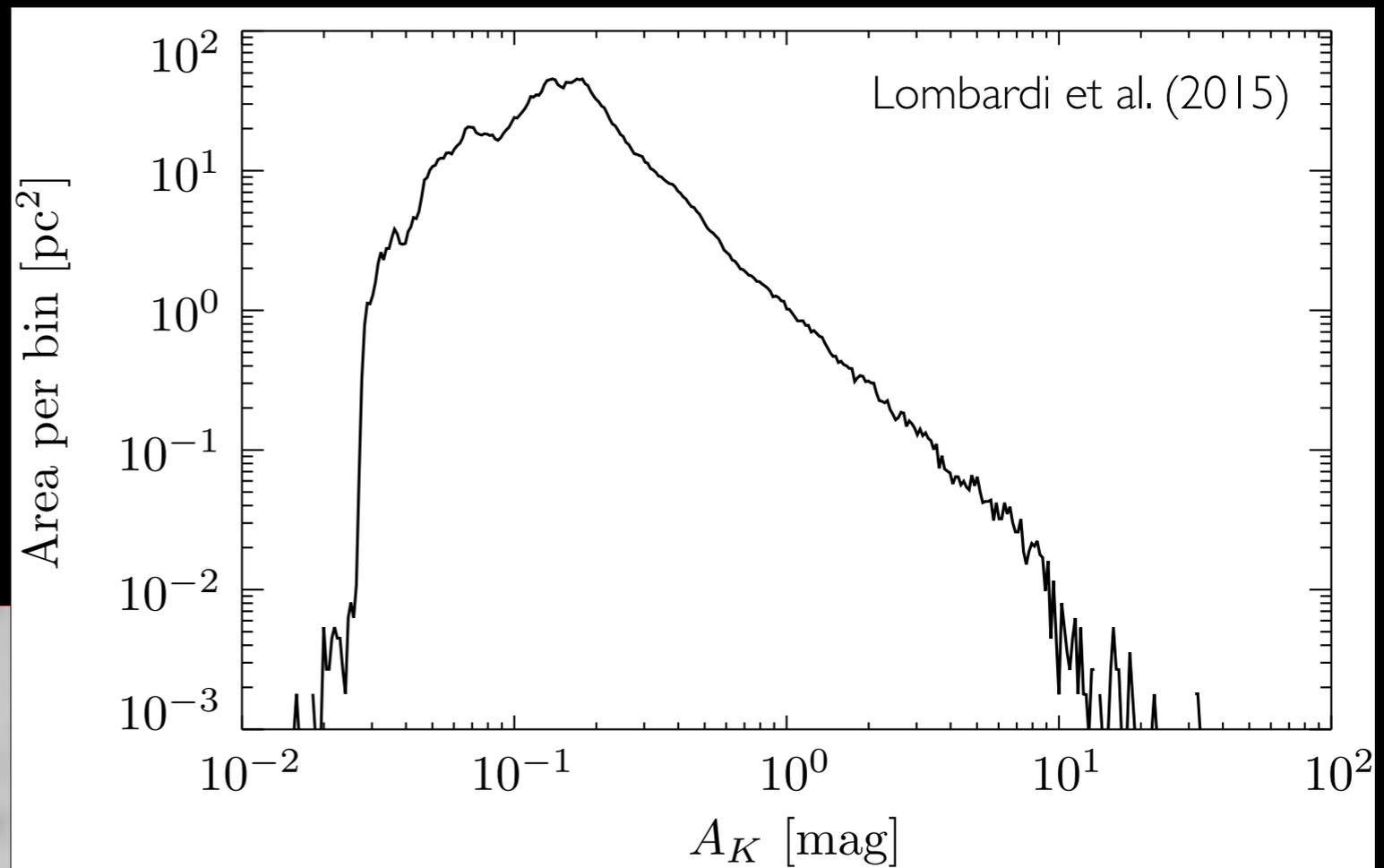
# Can we actually probe the low $A_K$ ?

- Cloud boundaries are not well defined!



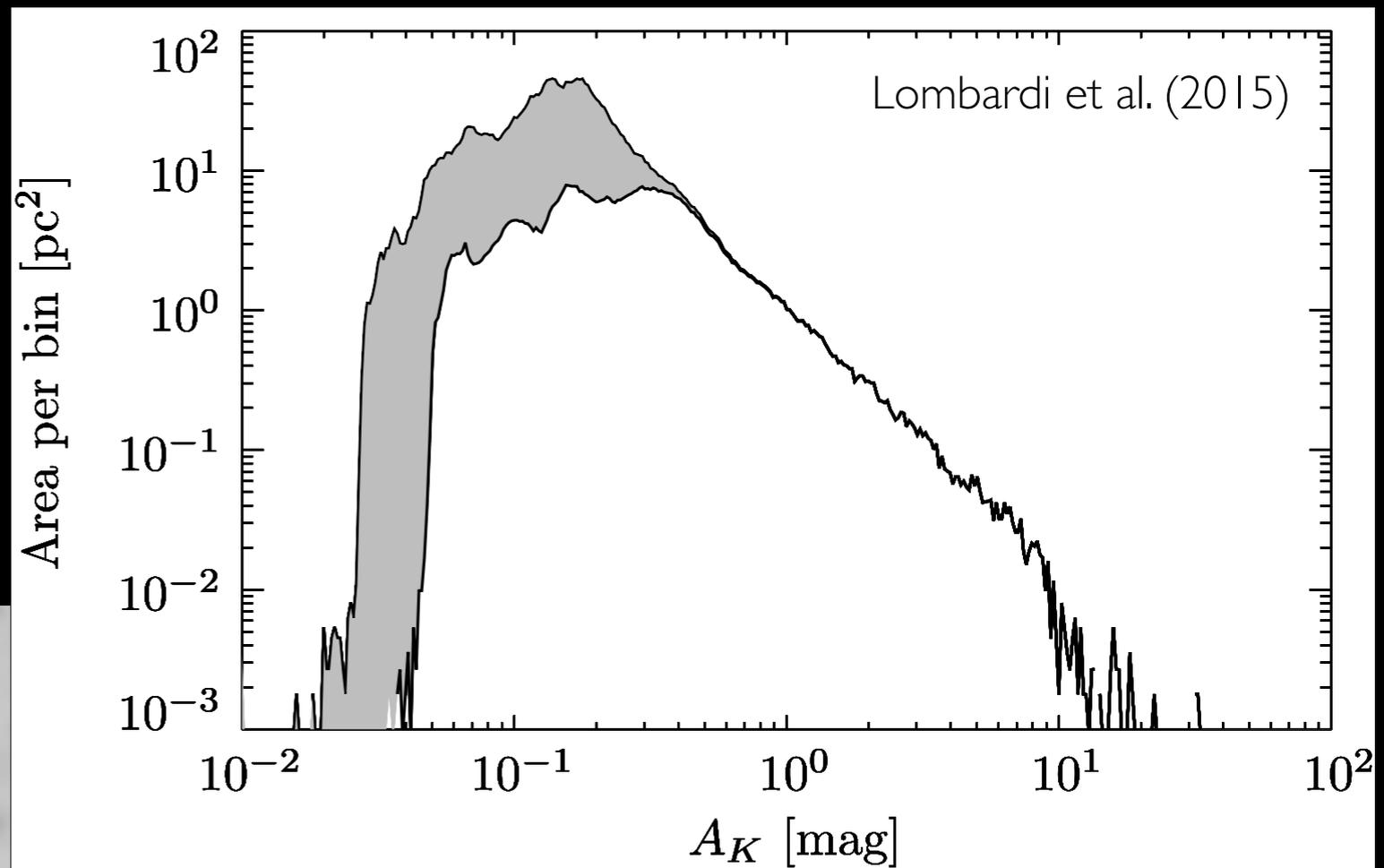
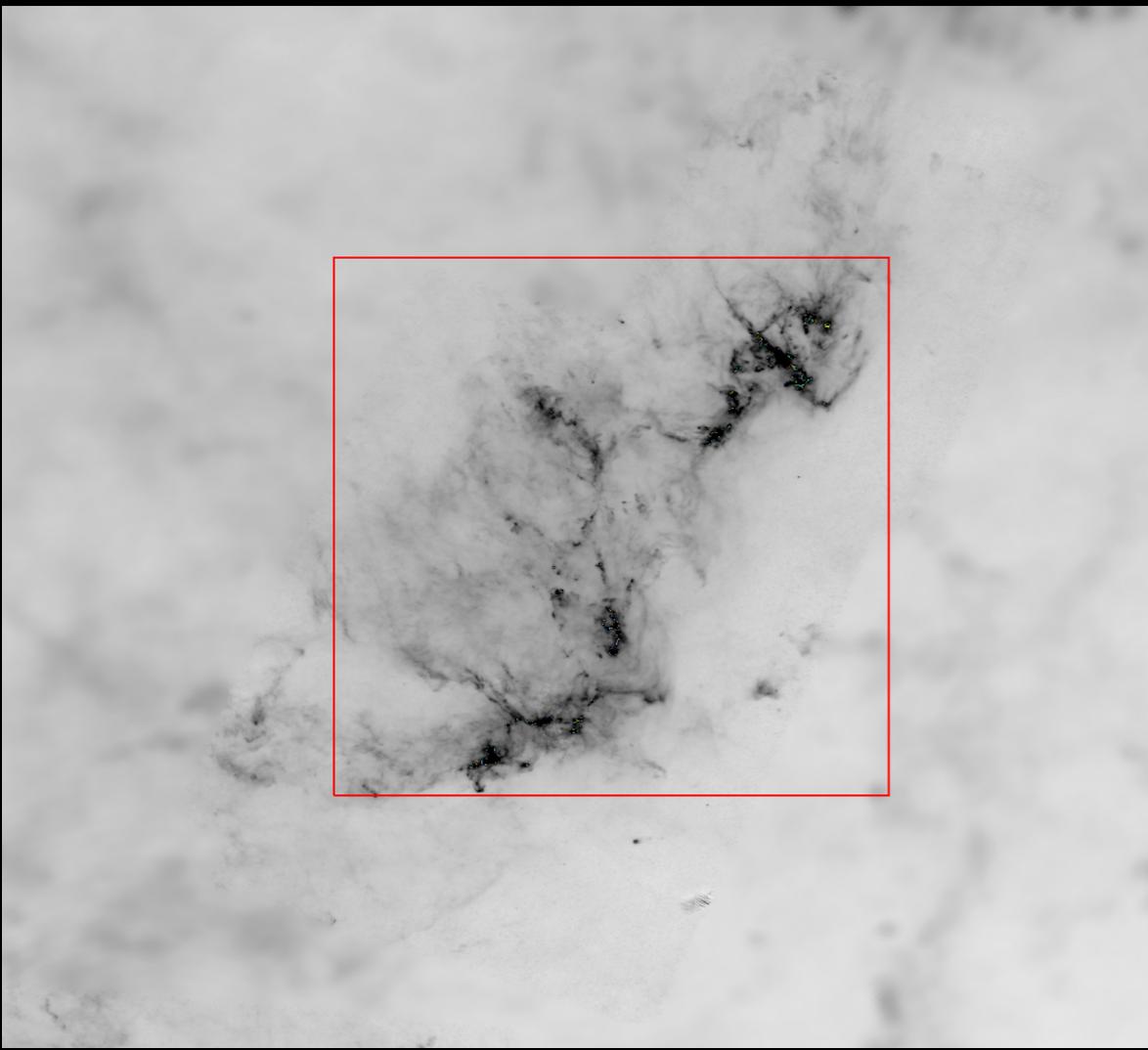
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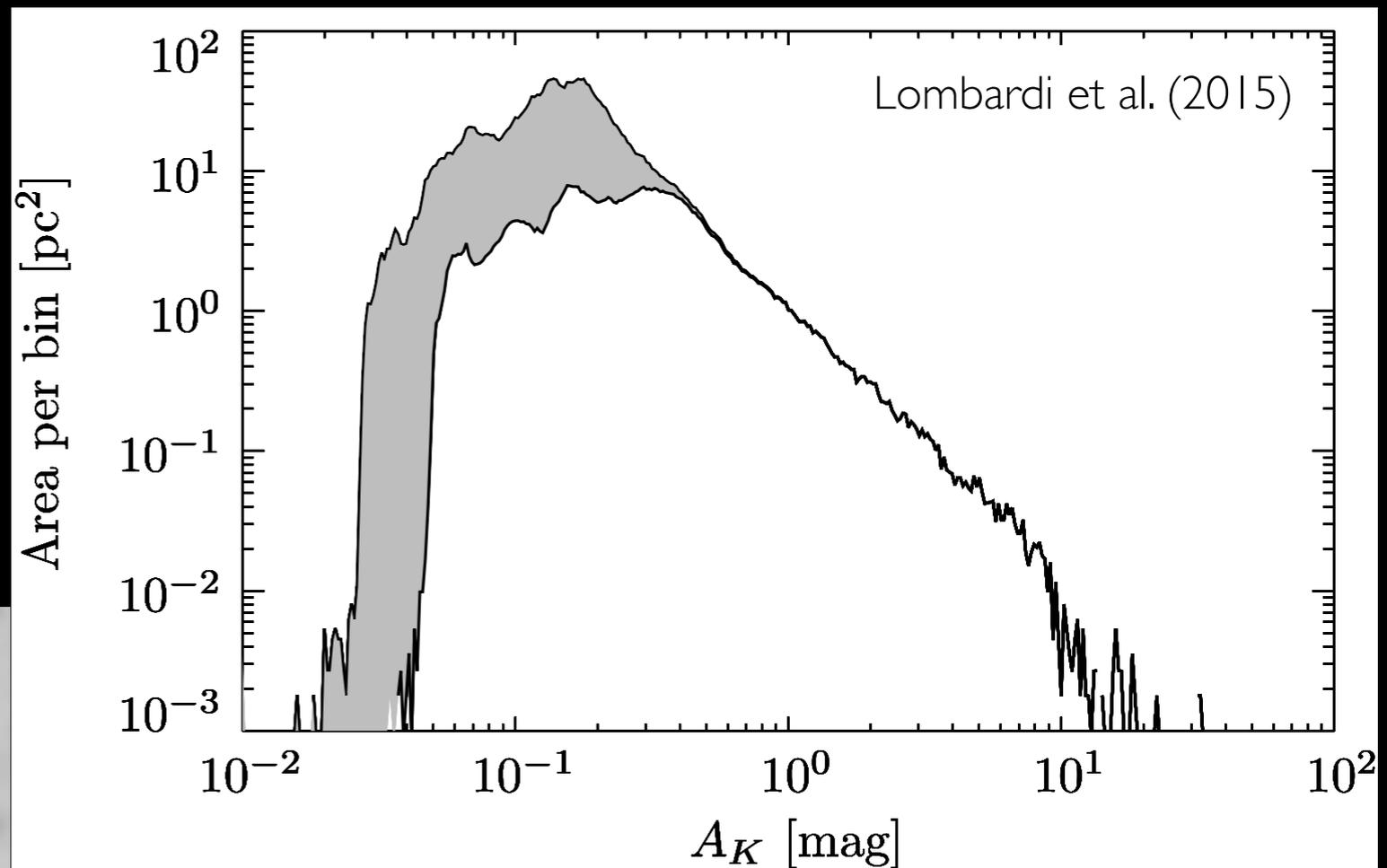
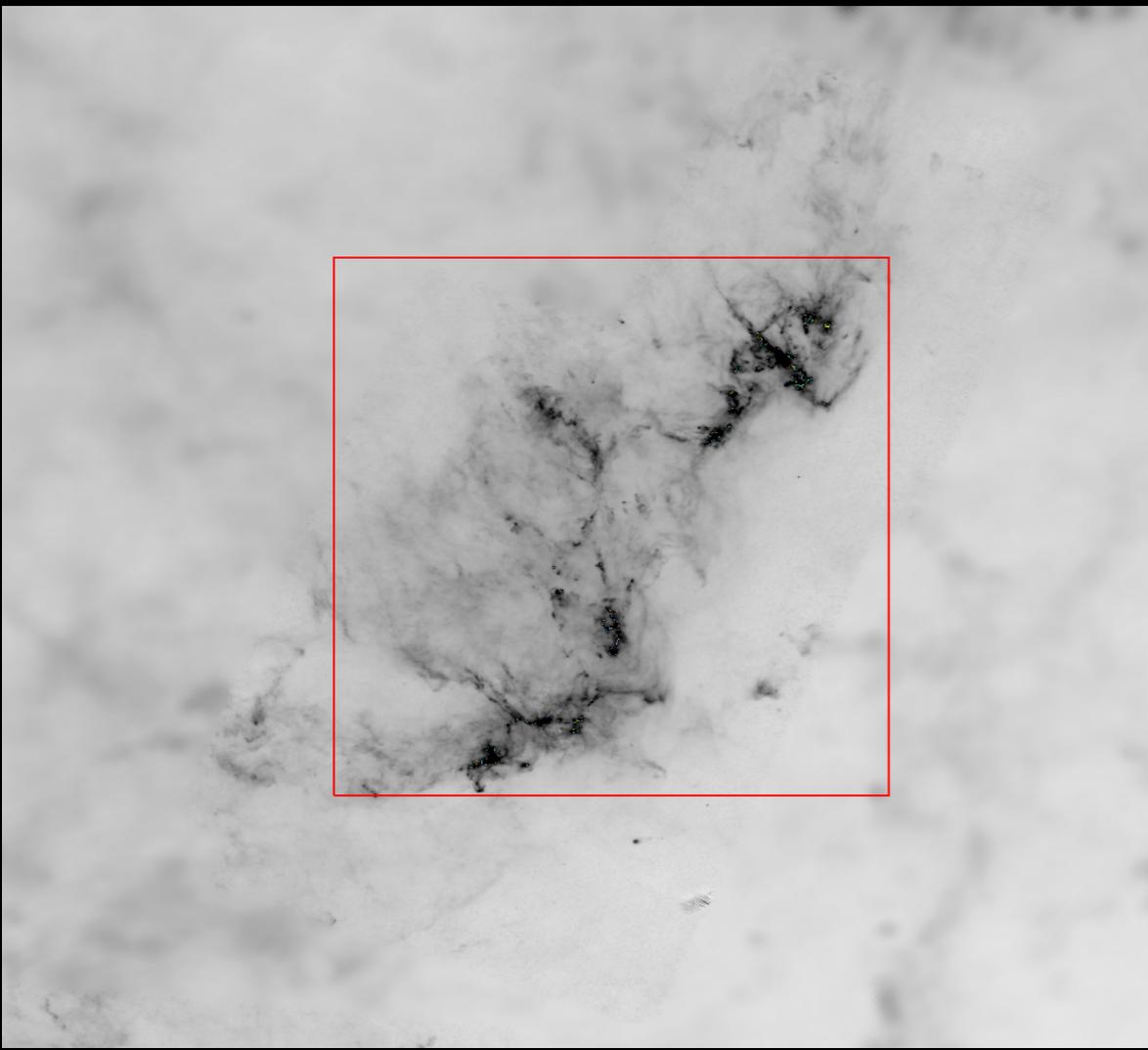
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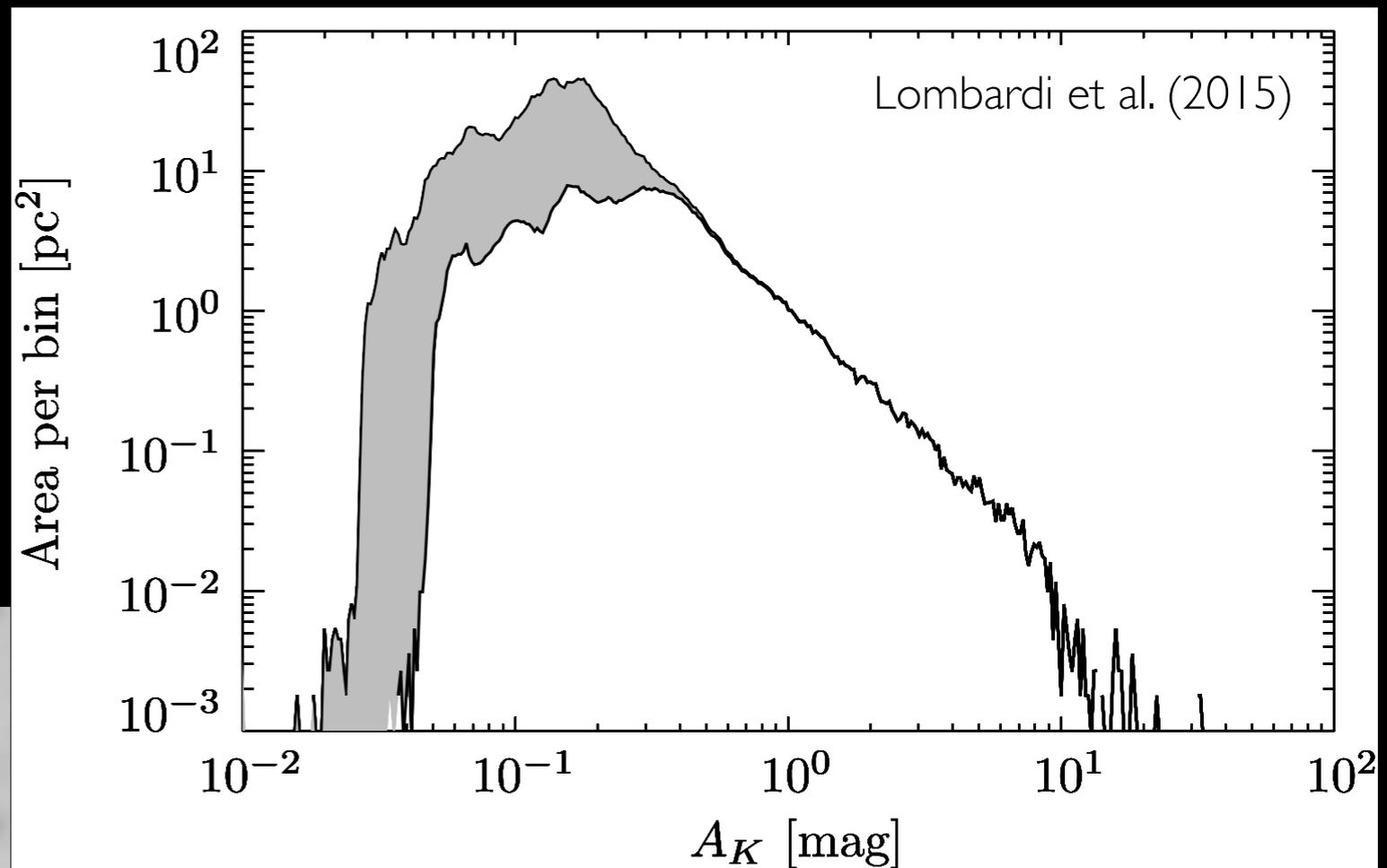
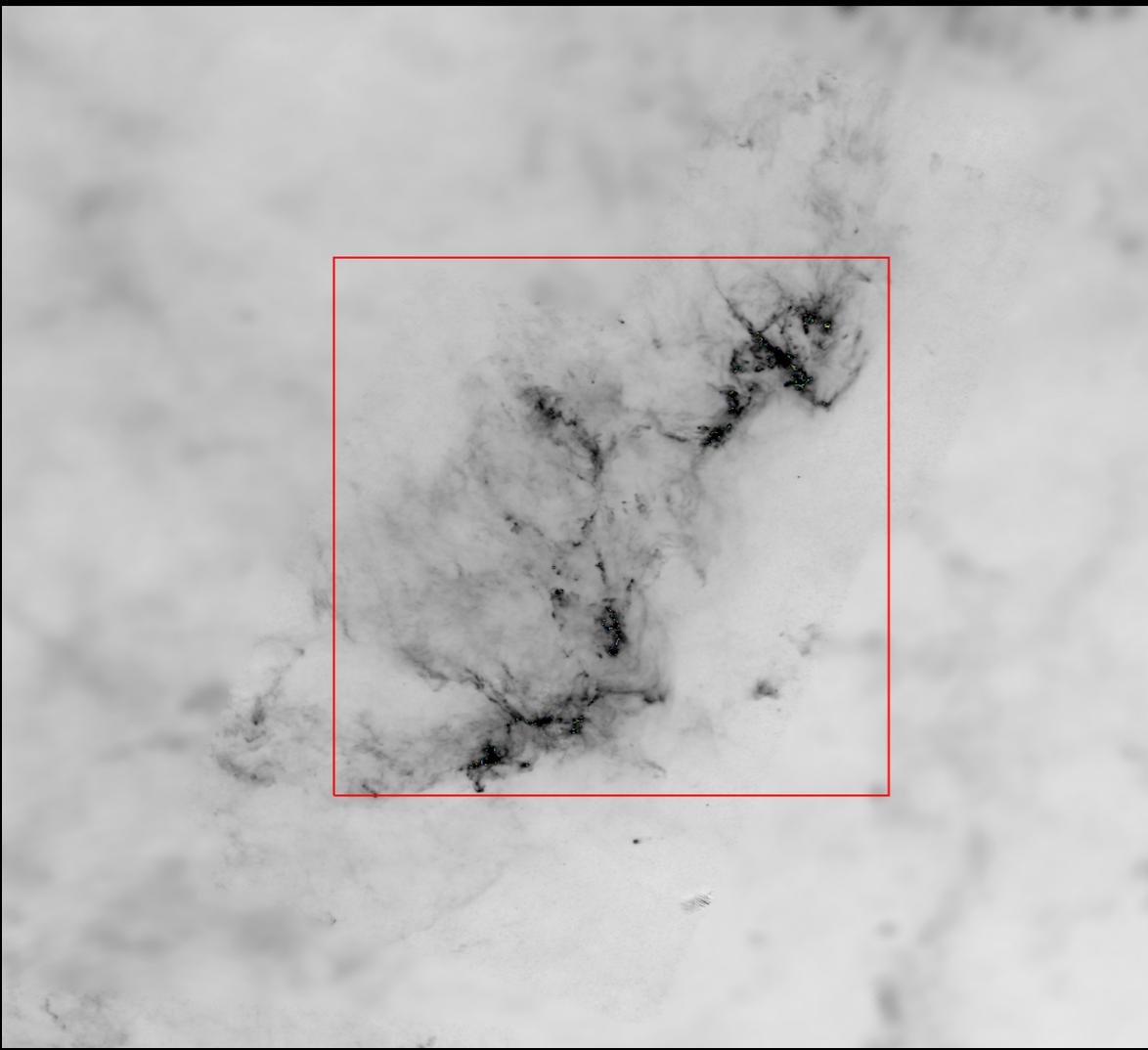
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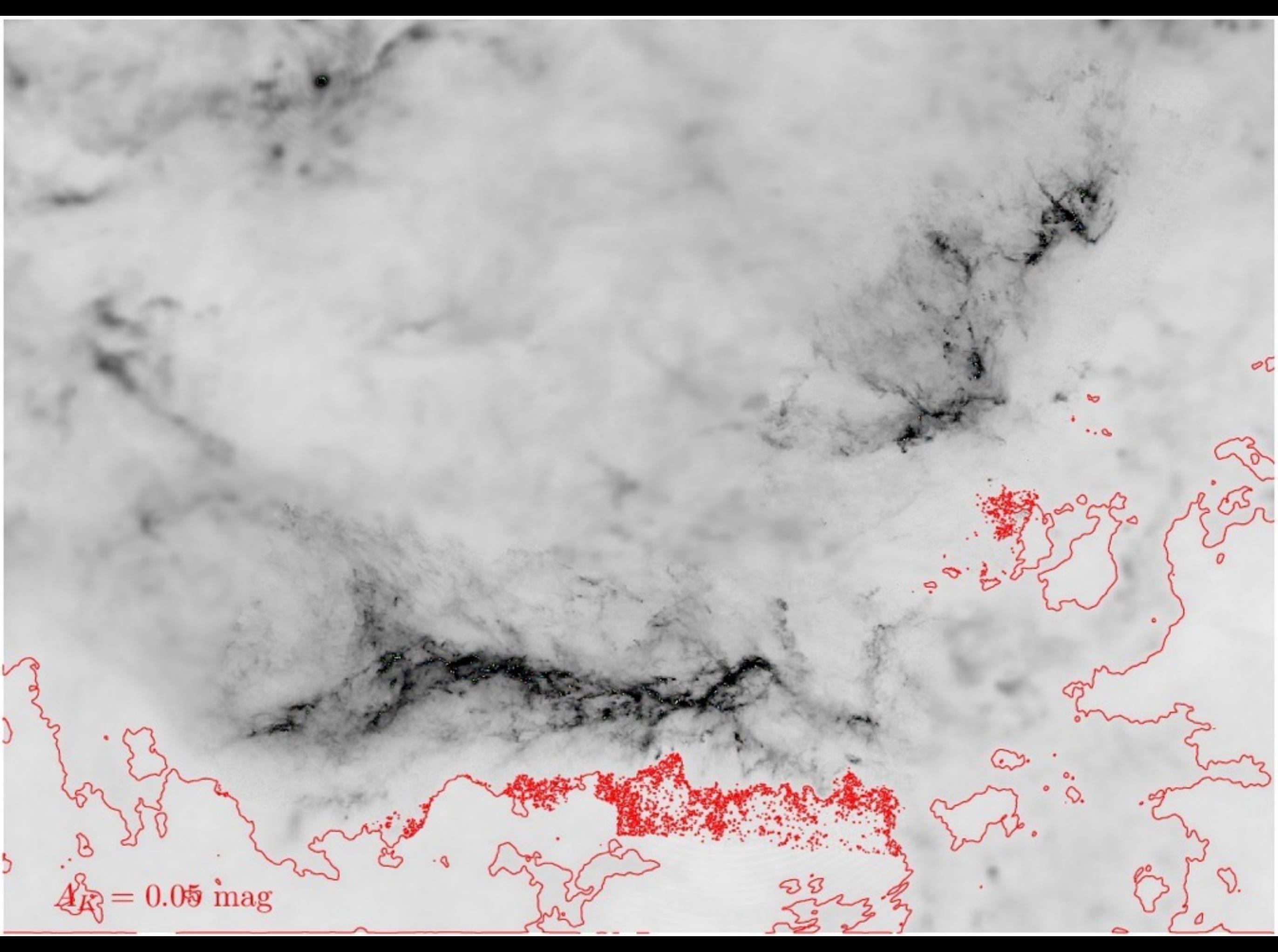
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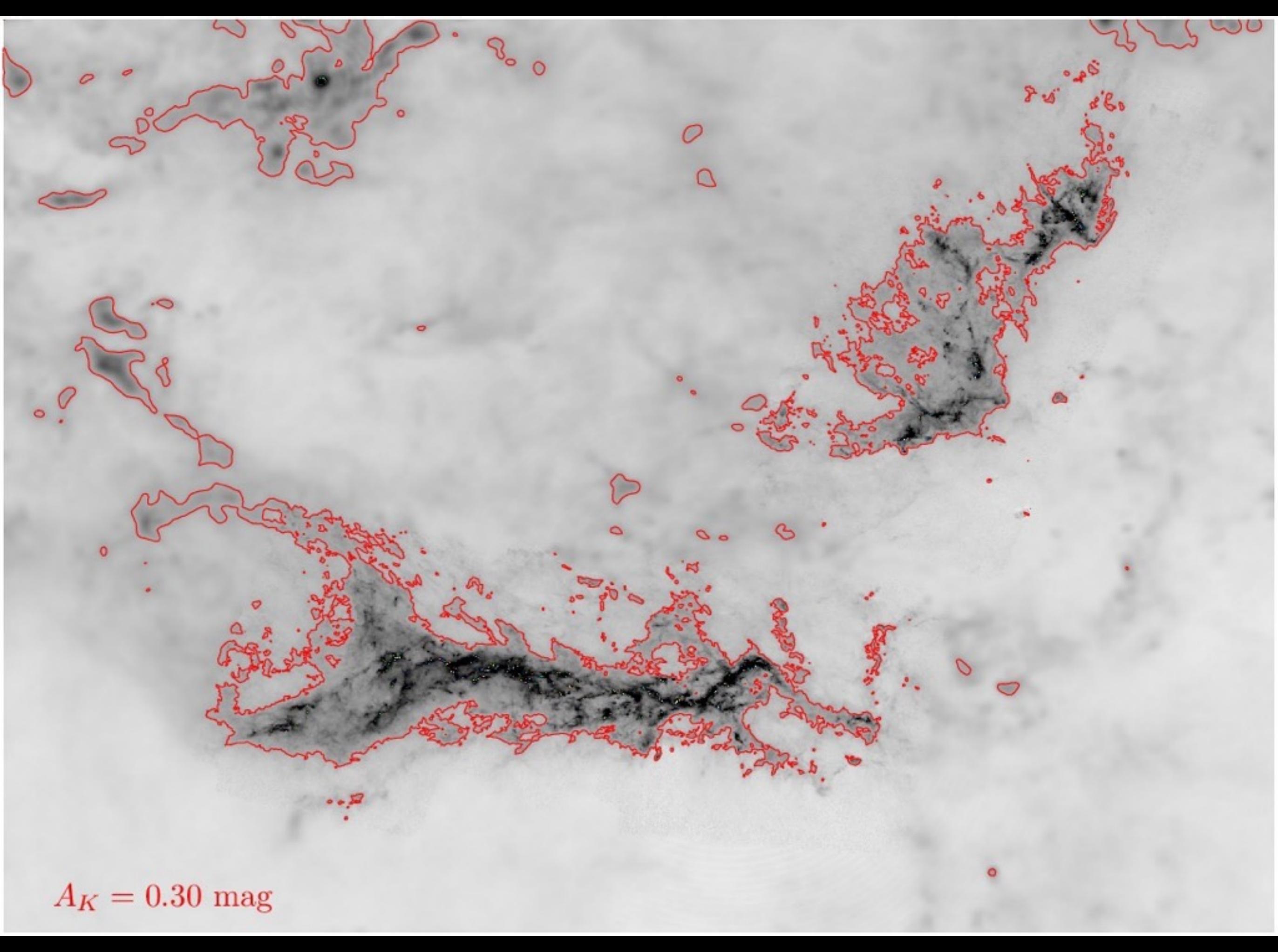


- The only sensible definition of a cloud boundary is using iso-density contours.
- Which contour levels are we able to use securely?





$AK = 0.05 \text{ mag}$



$A_K = 0.30$  mag



Things are actually worse than  
they appear



An aerial photograph of a volcanic eruption. A large, dark, billowing plume of ash and steam rises from a central vent, surrounded by a sea of smaller, white, puffy clouds. The sky is a deep blue with wispy white clouds. The text "Things are actually worse than they appear" is overlaid in white, sans-serif font in the upper half of the image.

Things are actually worse than  
they appear

If something can go wrong, it will.

An aerial photograph showing a vast, flat landscape, possibly a salt flat or a desert, under a clear blue sky. The ground is a mix of light and dark patches, suggesting different mineral compositions or perhaps a thin layer of water reflecting the sky. In the foreground, a large, dark, irregularly shaped cloud formation, possibly a volcanic plume or a large fire, rises from the ground. The cloud is dense and dark, contrasting sharply with the lighter ground and sky. The overall scene is one of a stark, desolate environment.

Things are actually worse than  
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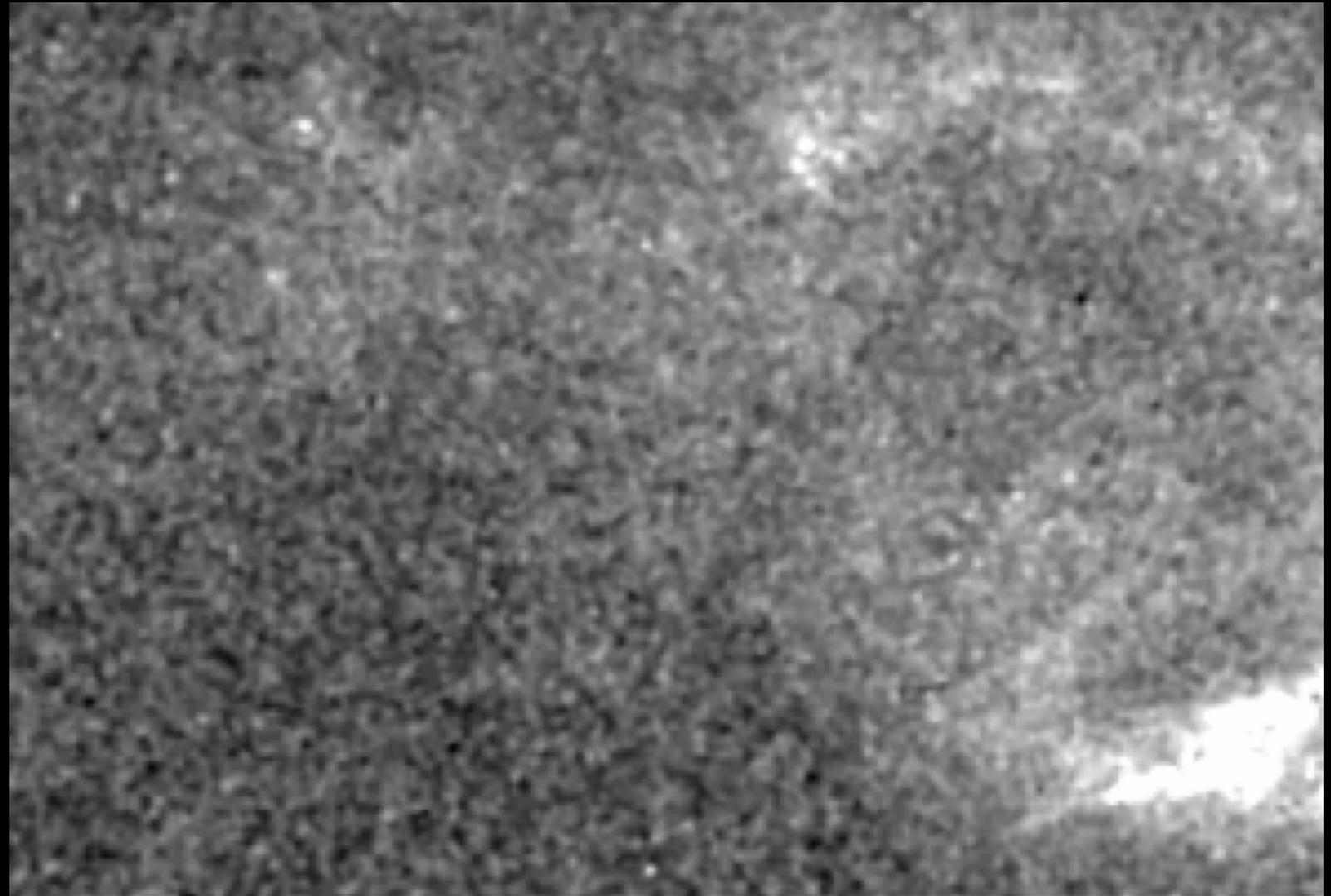
If something cannot go wrong, it will anyway.





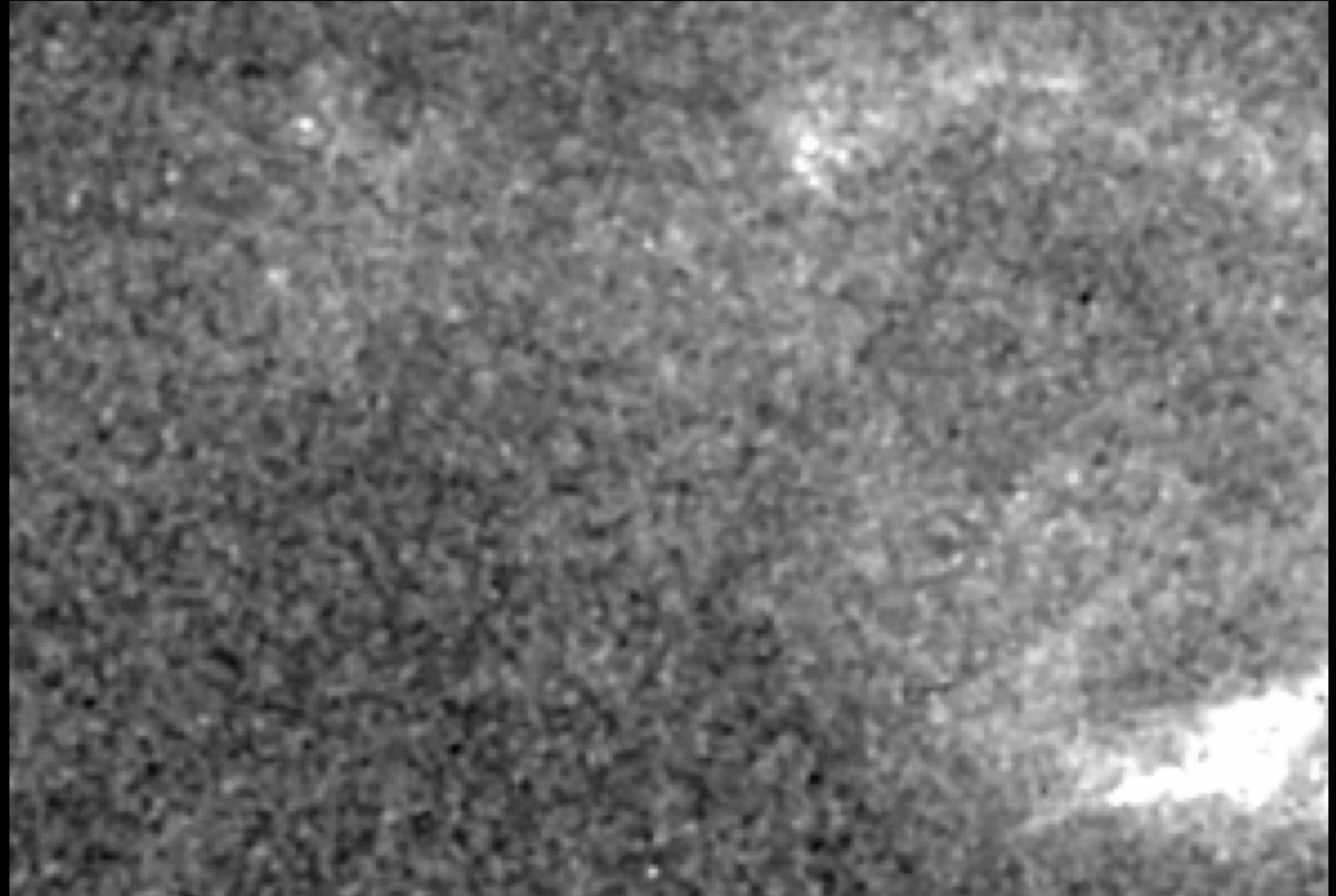


# Low-column density part of PDFs



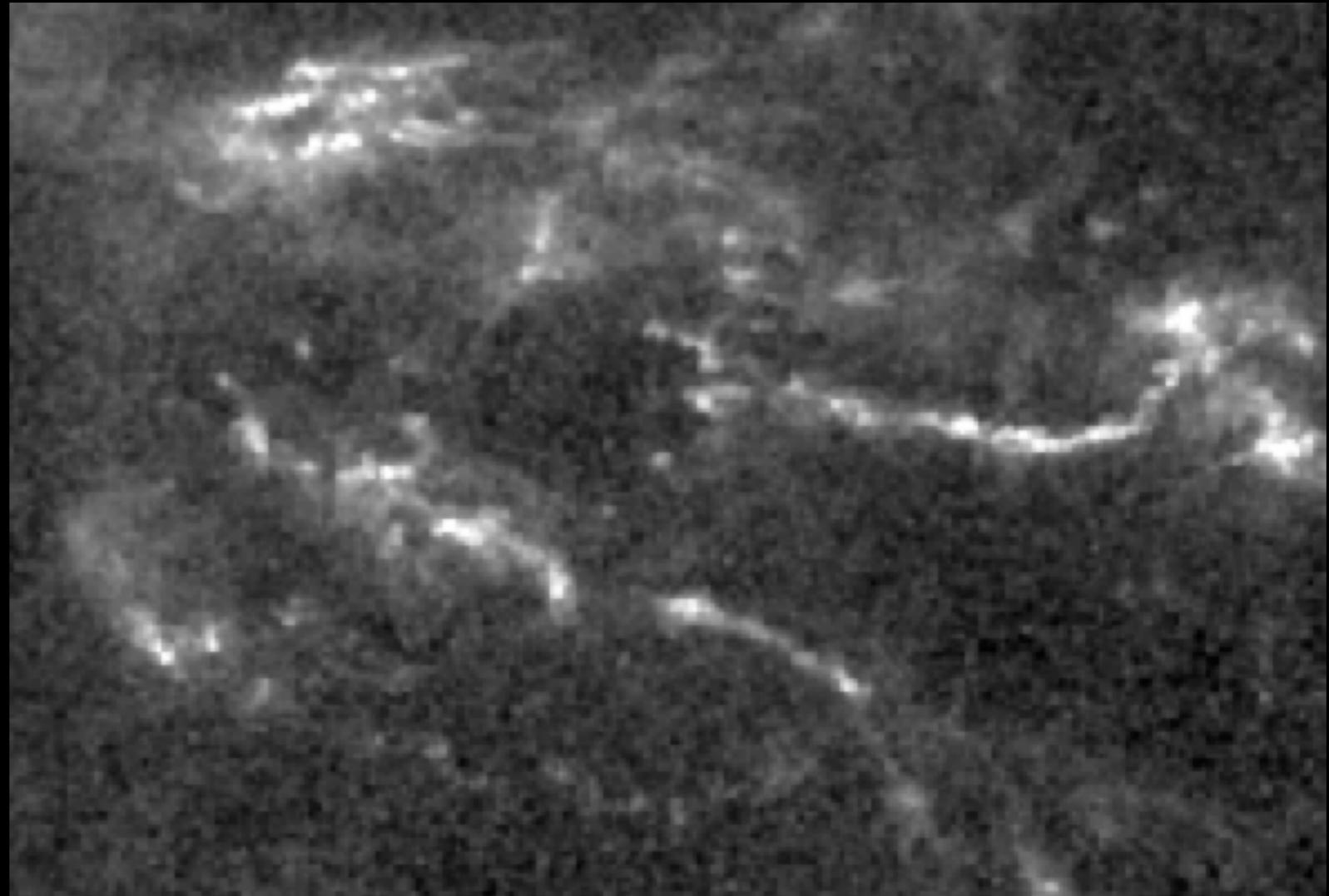
# Low-column density part of PDFs

- Noise can be significant at low column densities



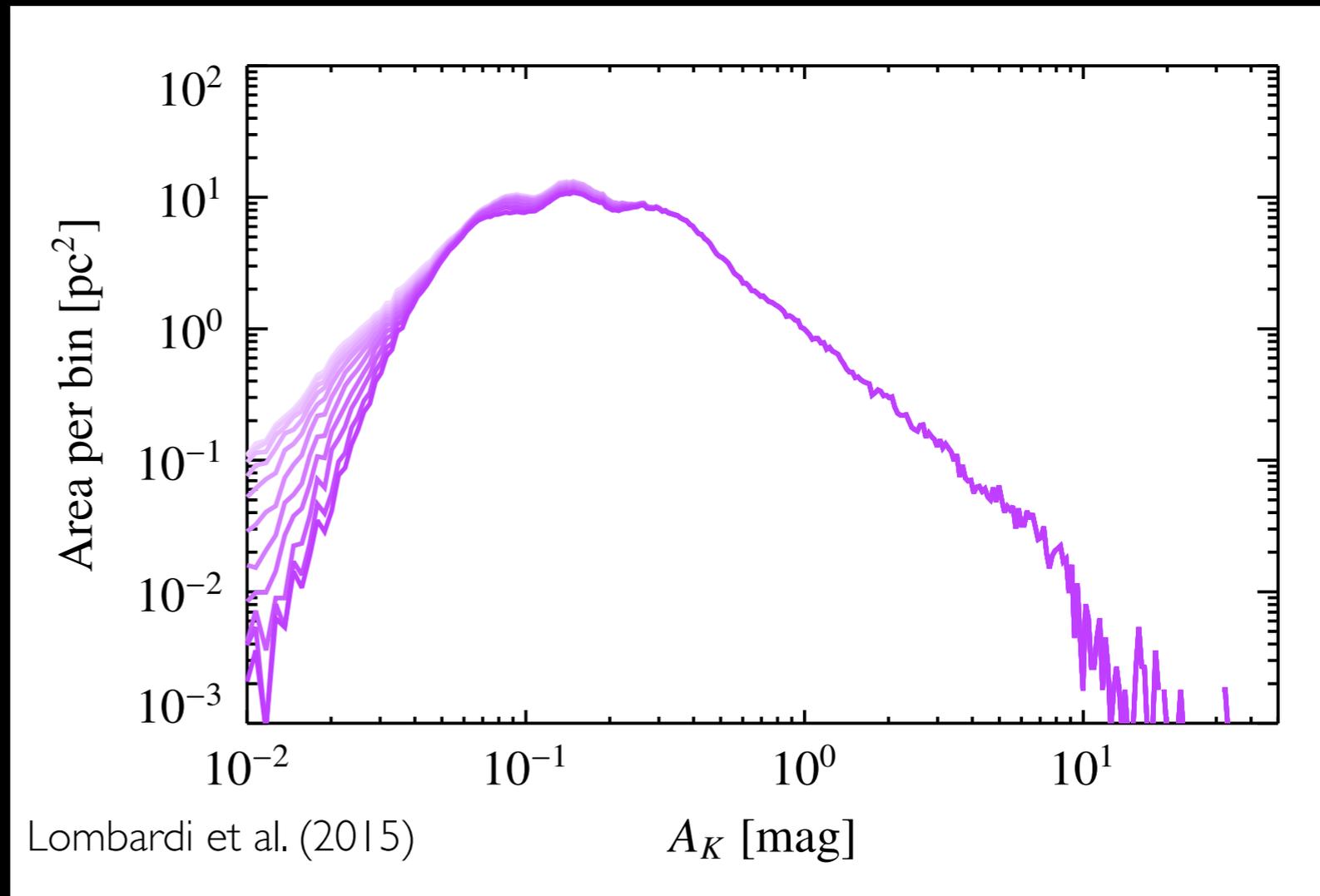
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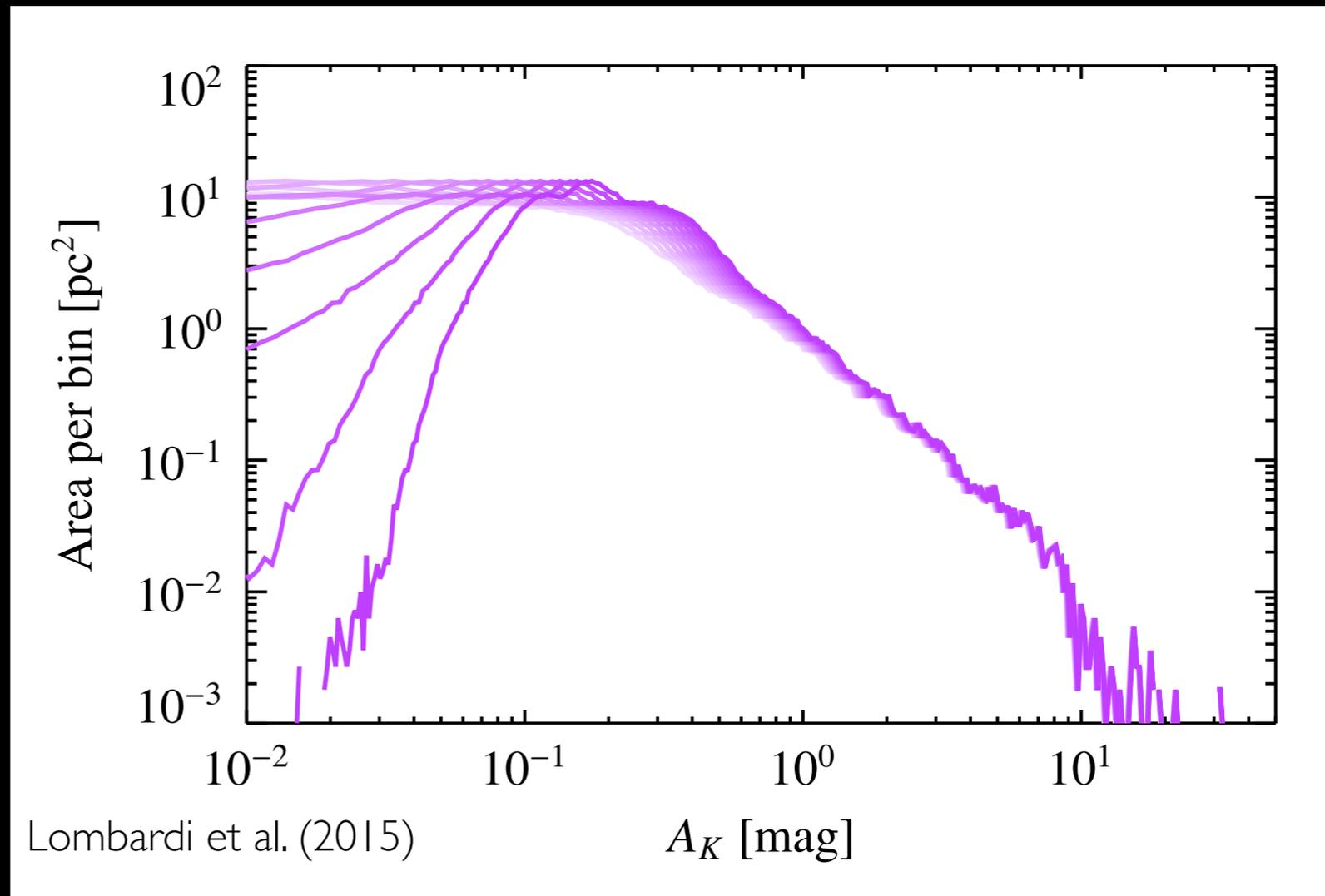
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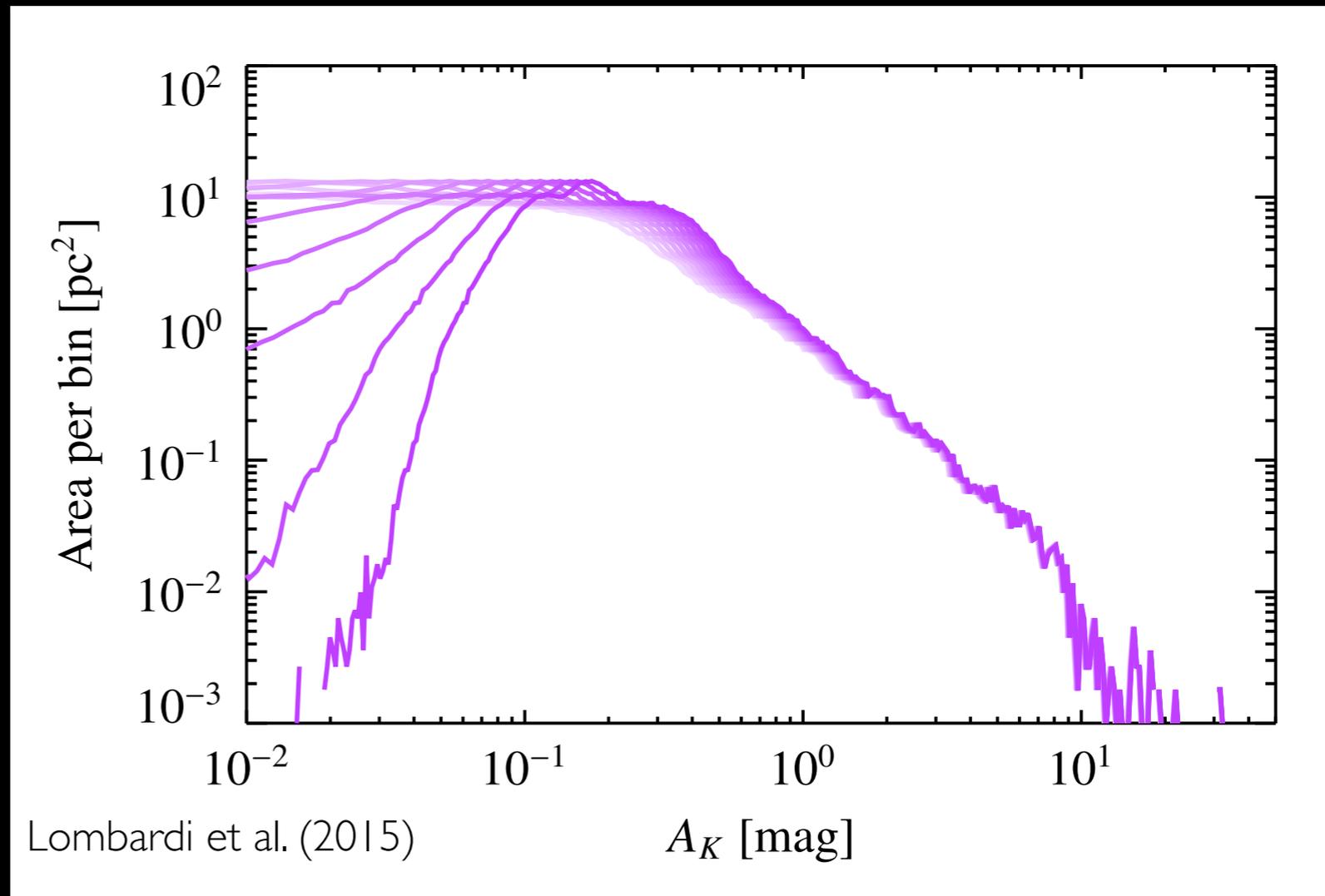
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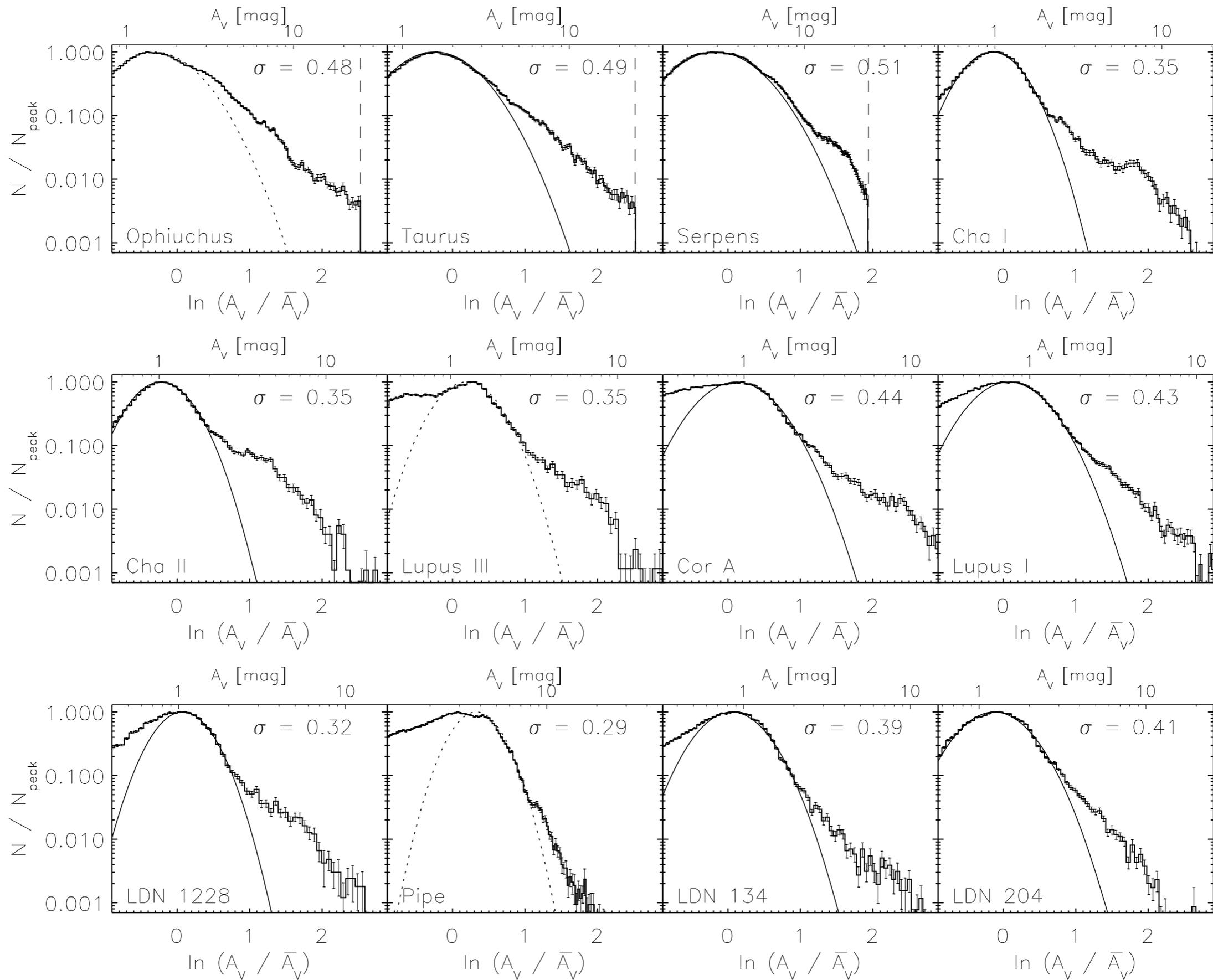
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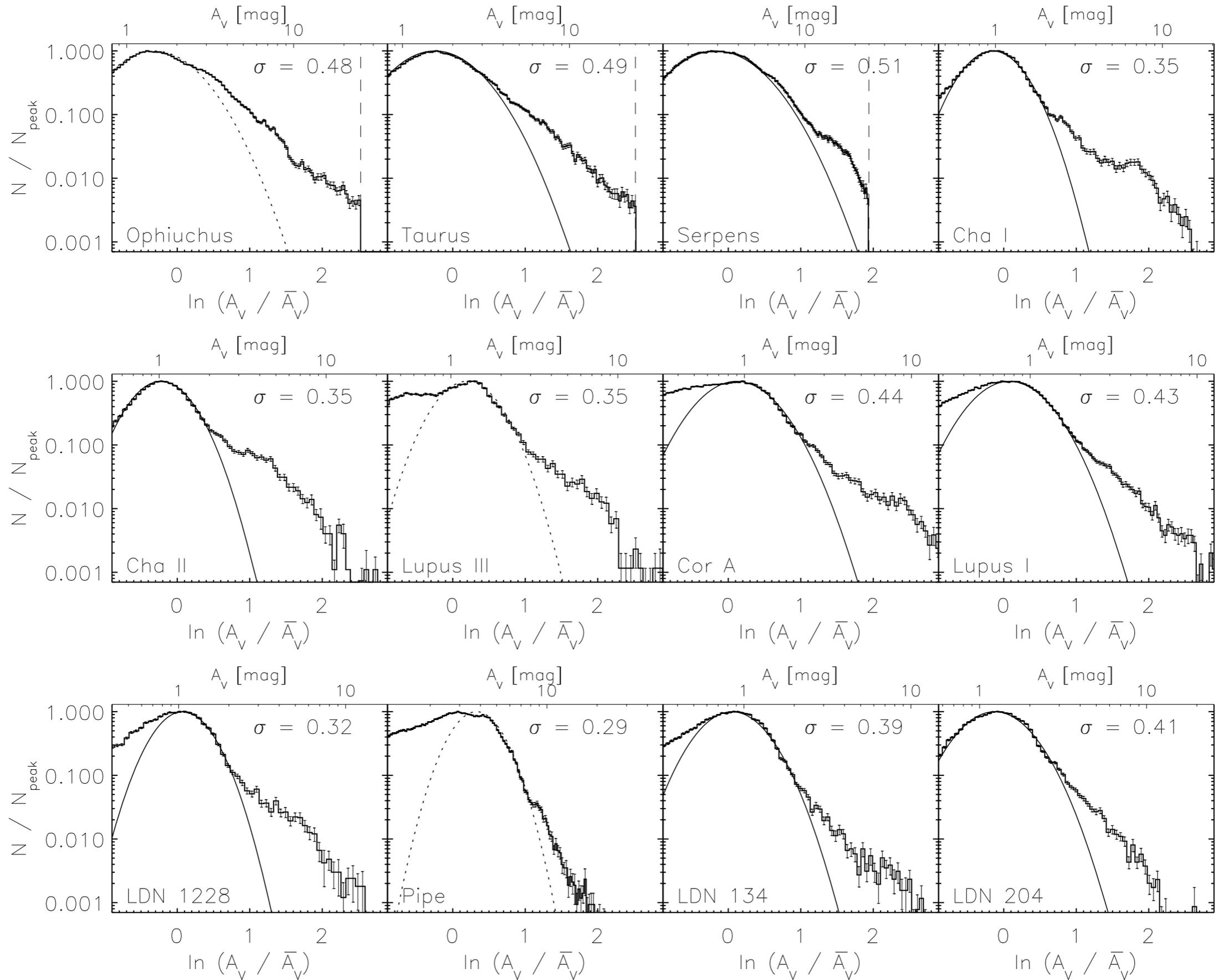
**We are virtually unable to study the PDF below  
(at least)  $A_K \sim 0.15$  mag**

# Log-normals everywhere!



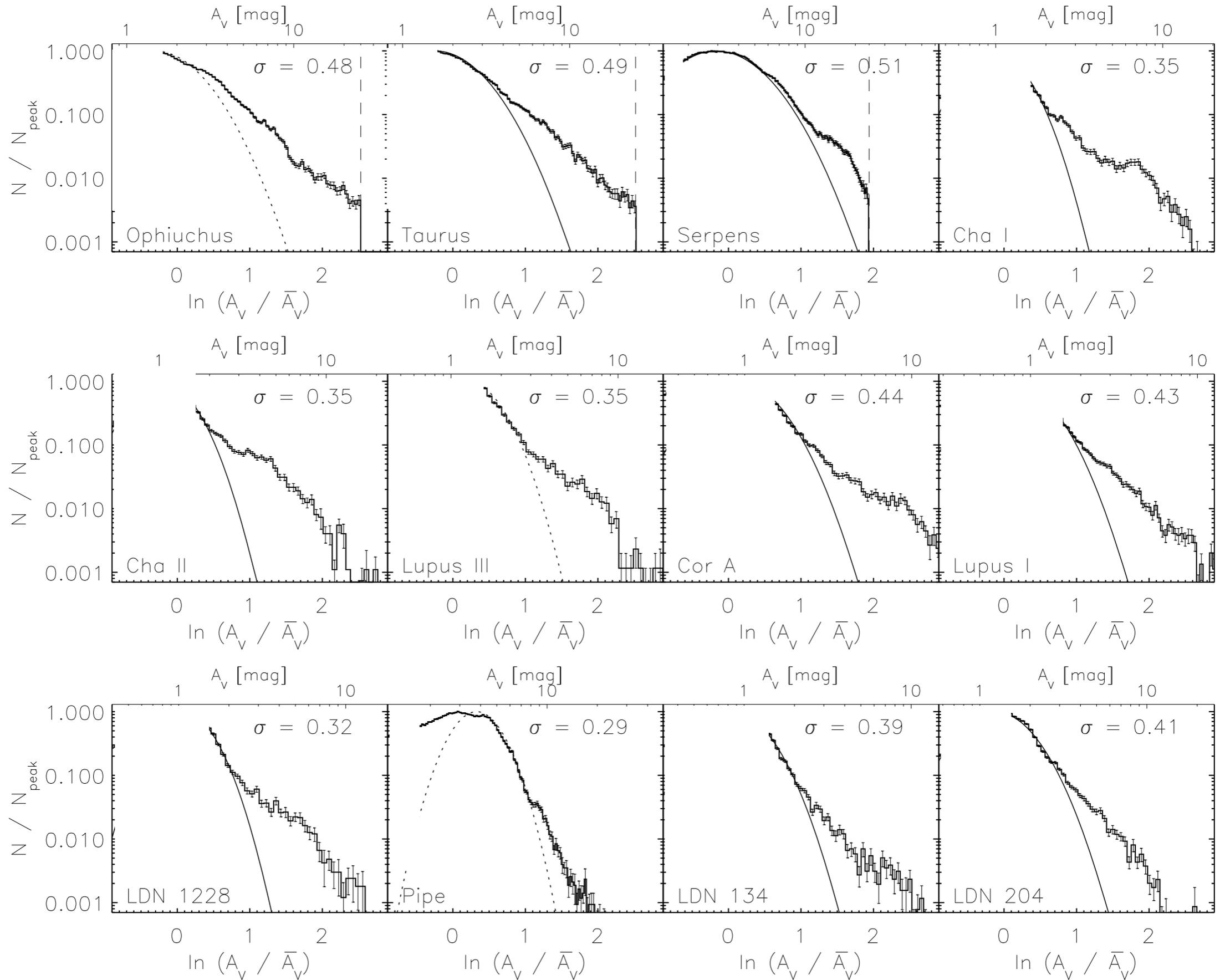
Kainulainen et al. (2009)

# Log-normals everywhere?



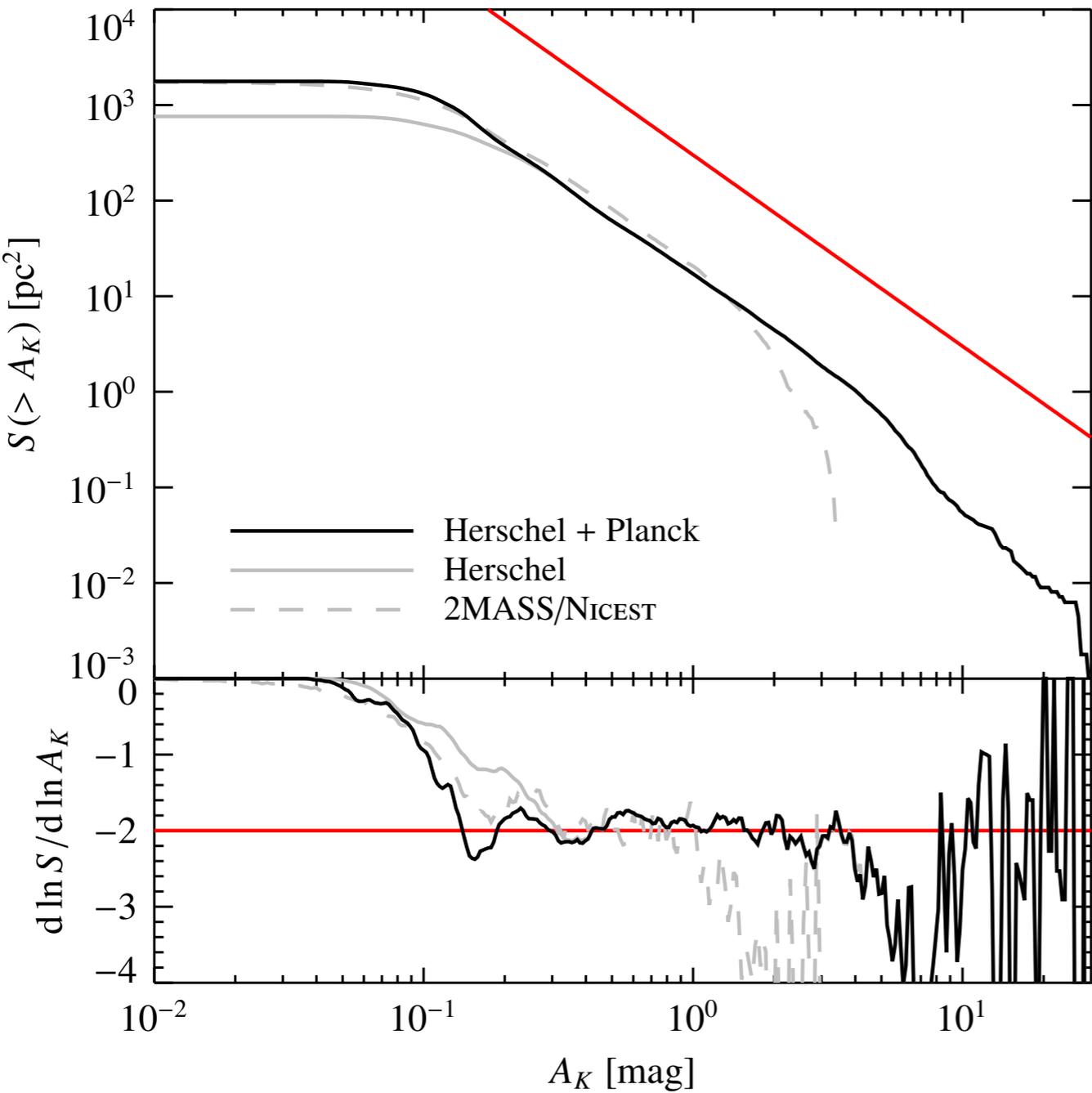
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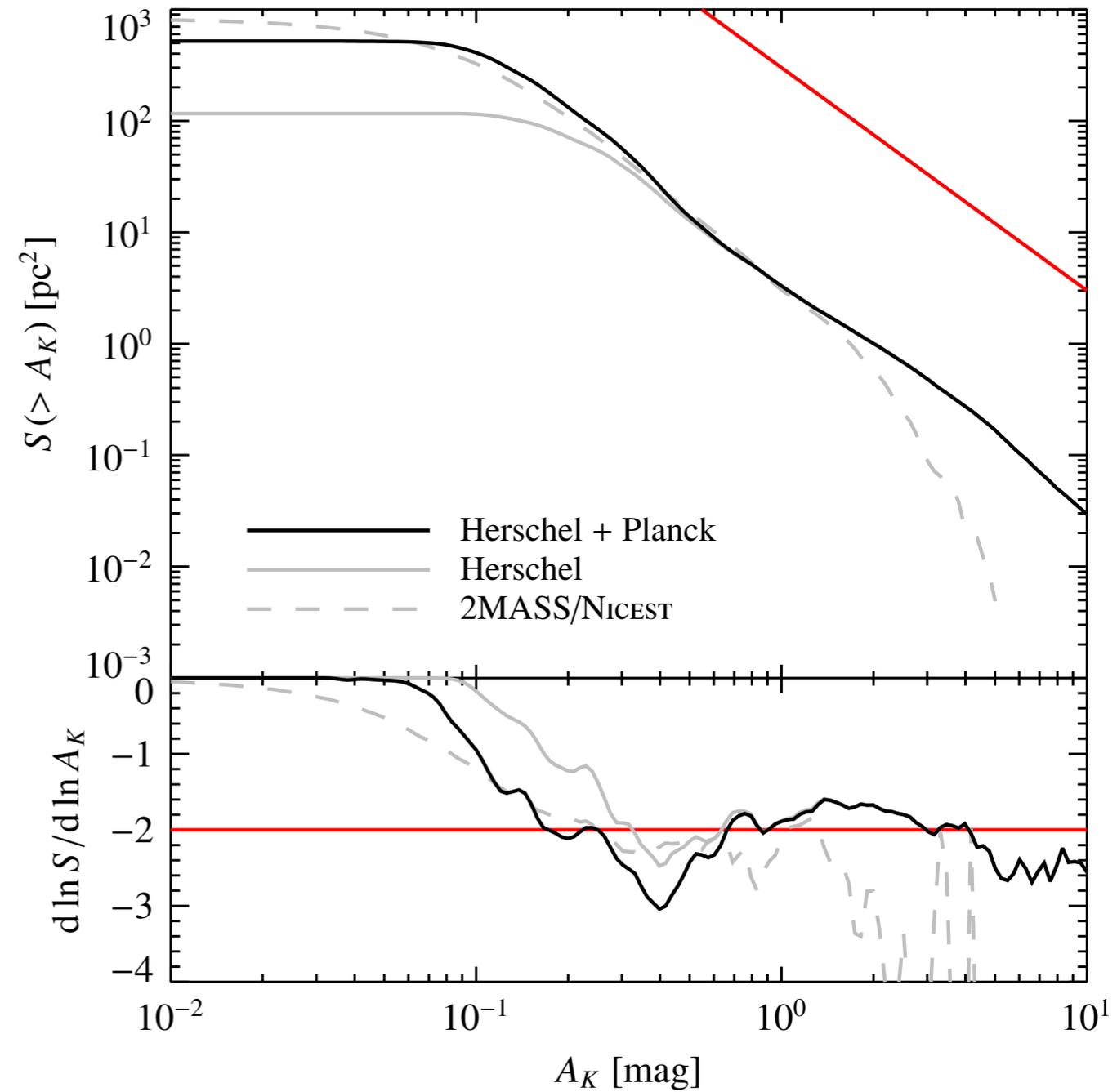


Kainulainen et al. (2009), censored

# Area functions (integrals of PDFs)

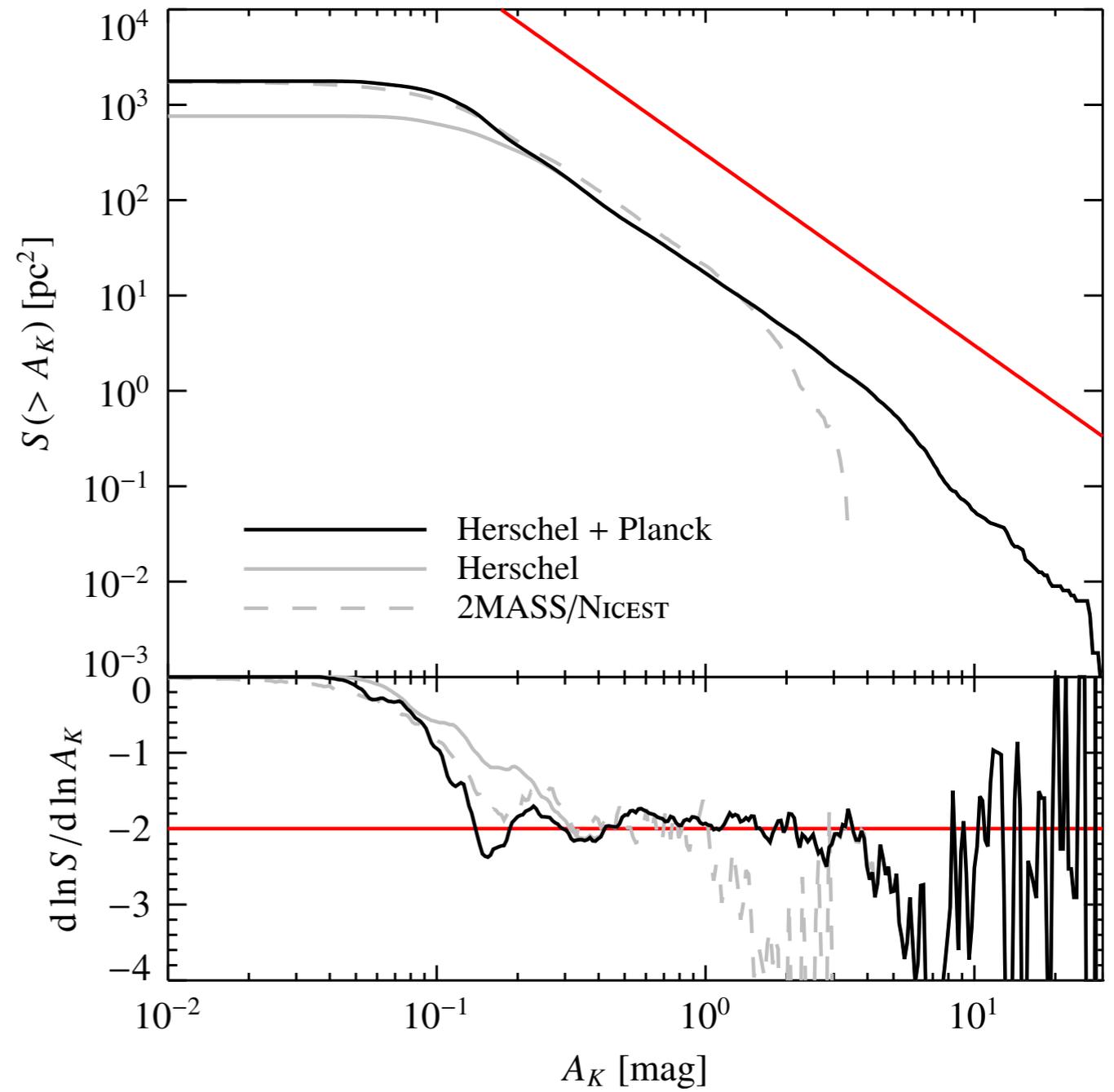


Lombardi et al. (2014)



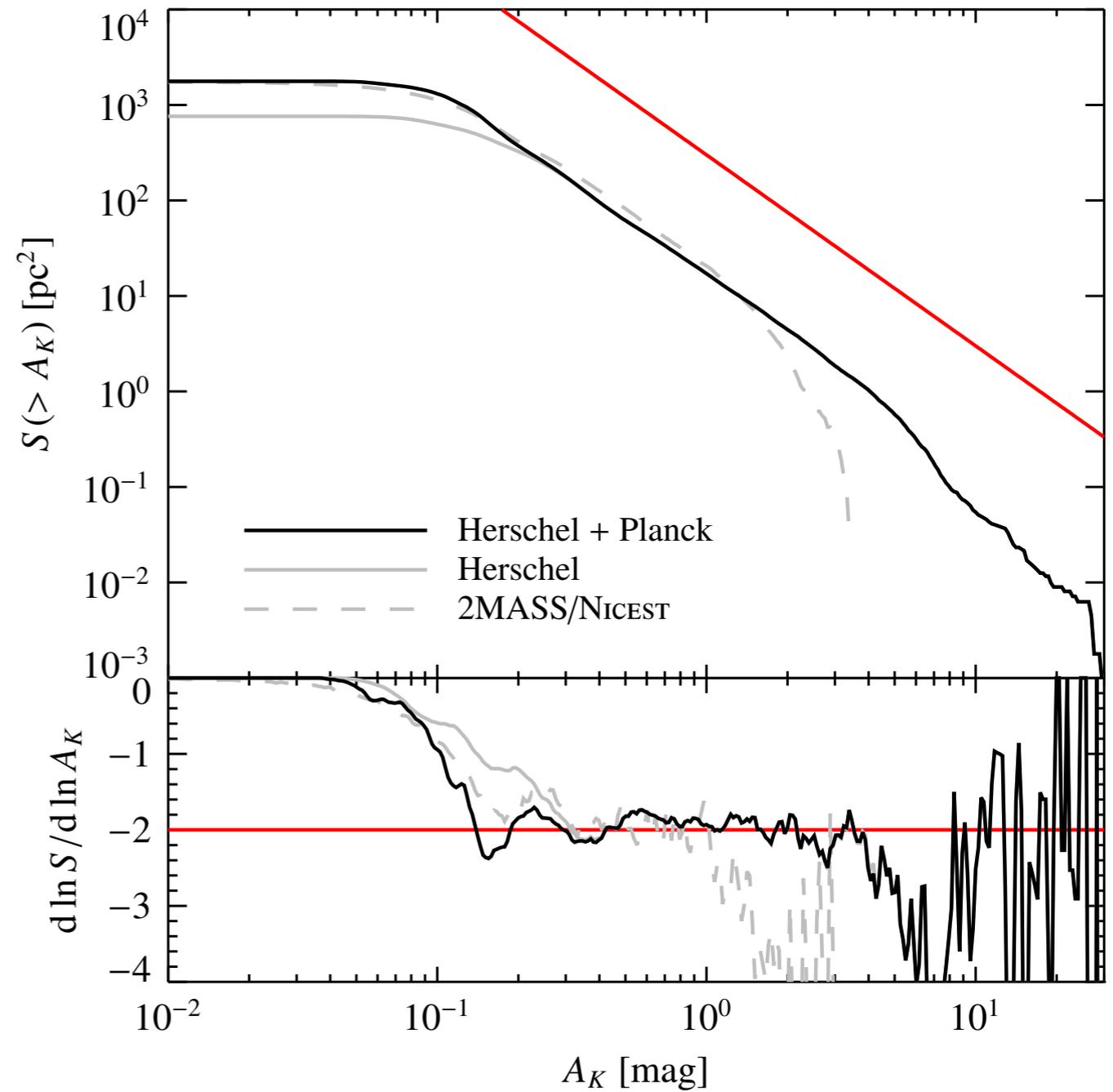
Alves et al. (2015)

# Toy model



# Toy model

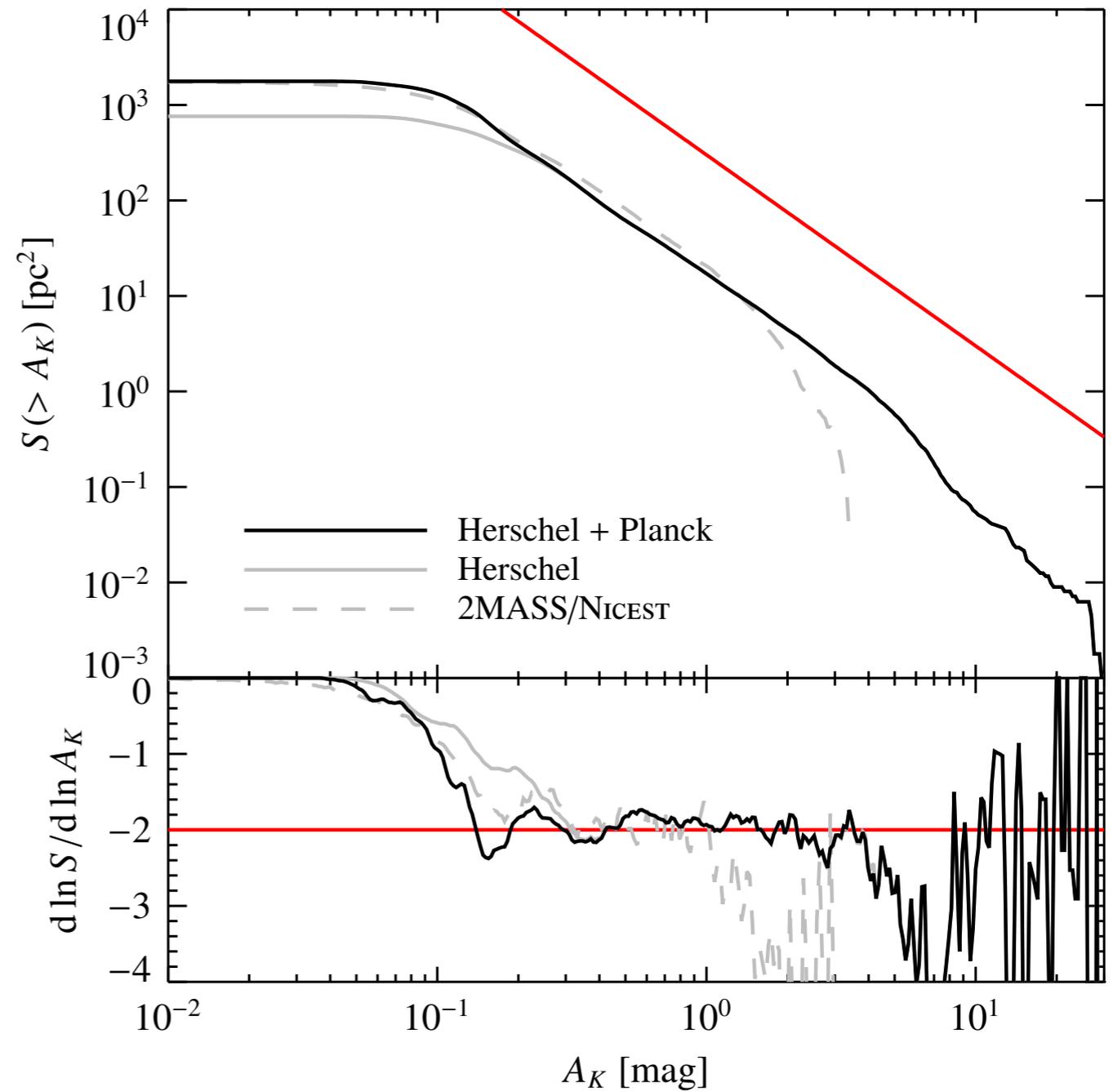
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$$\rho \sim R^{-2}$$

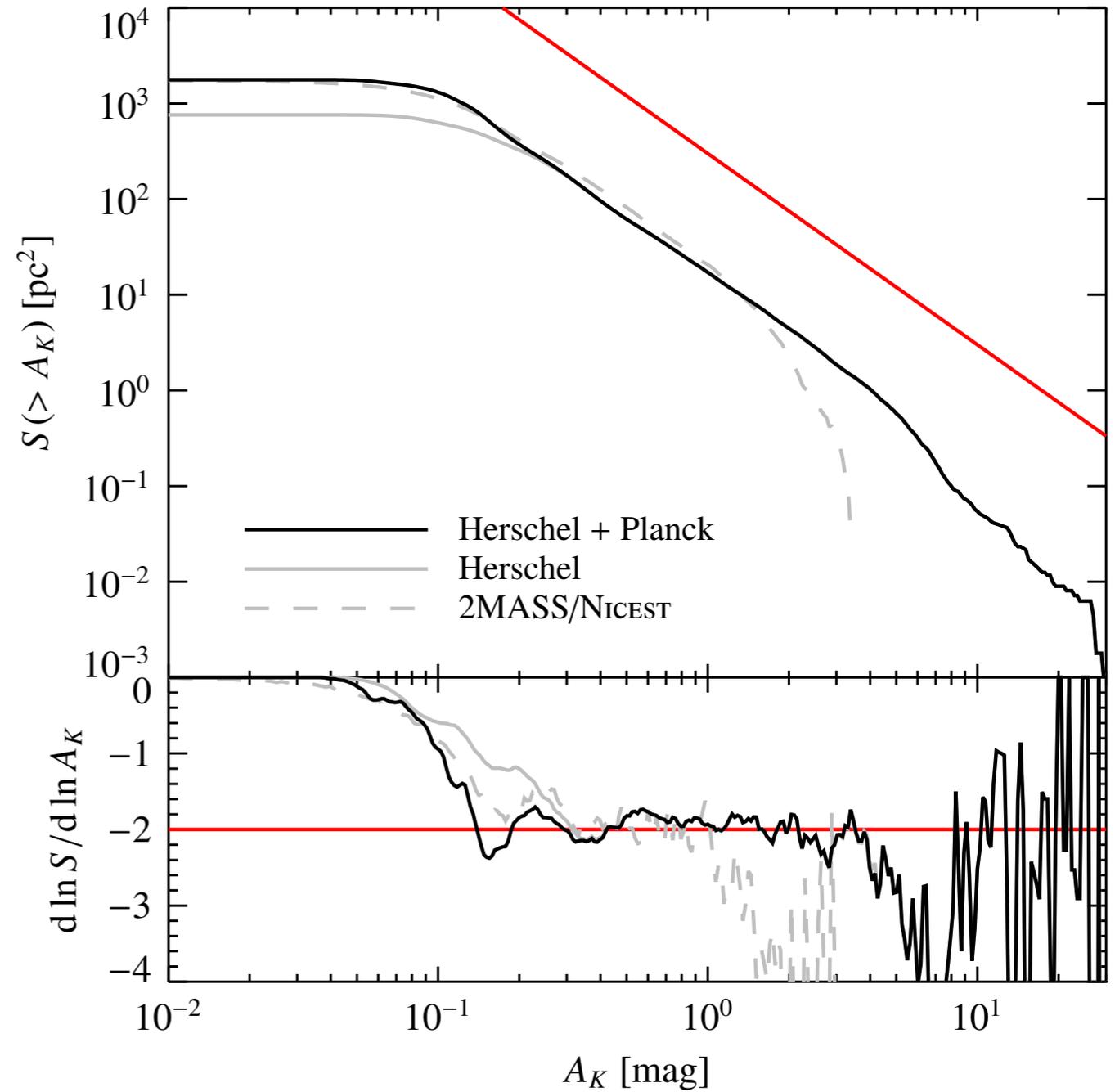


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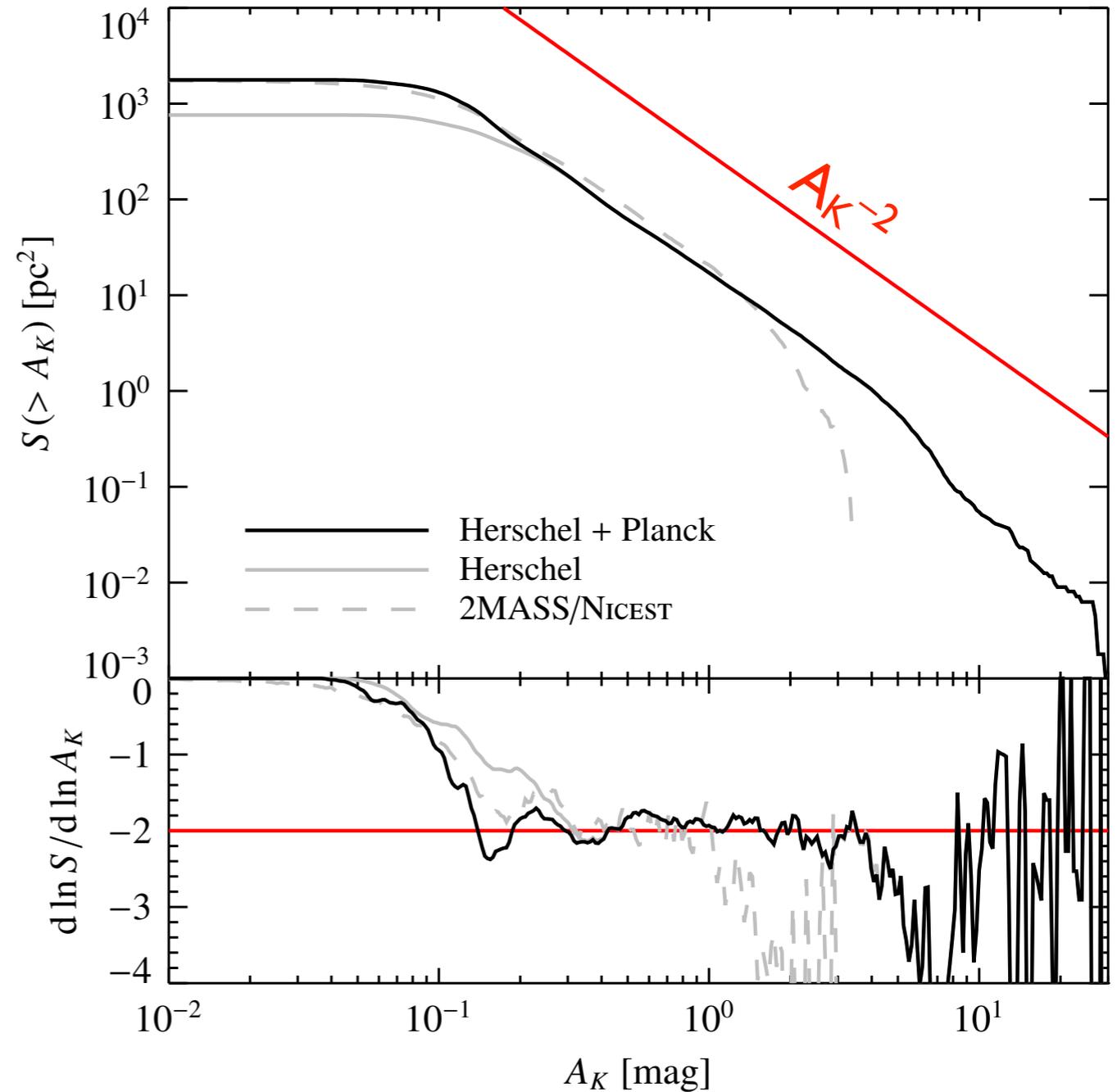
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$$S(> A_K) \sim R^2 \sim A_K^{-2}$$



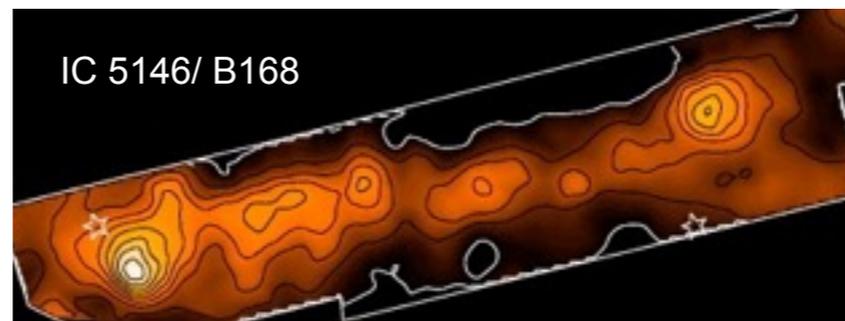
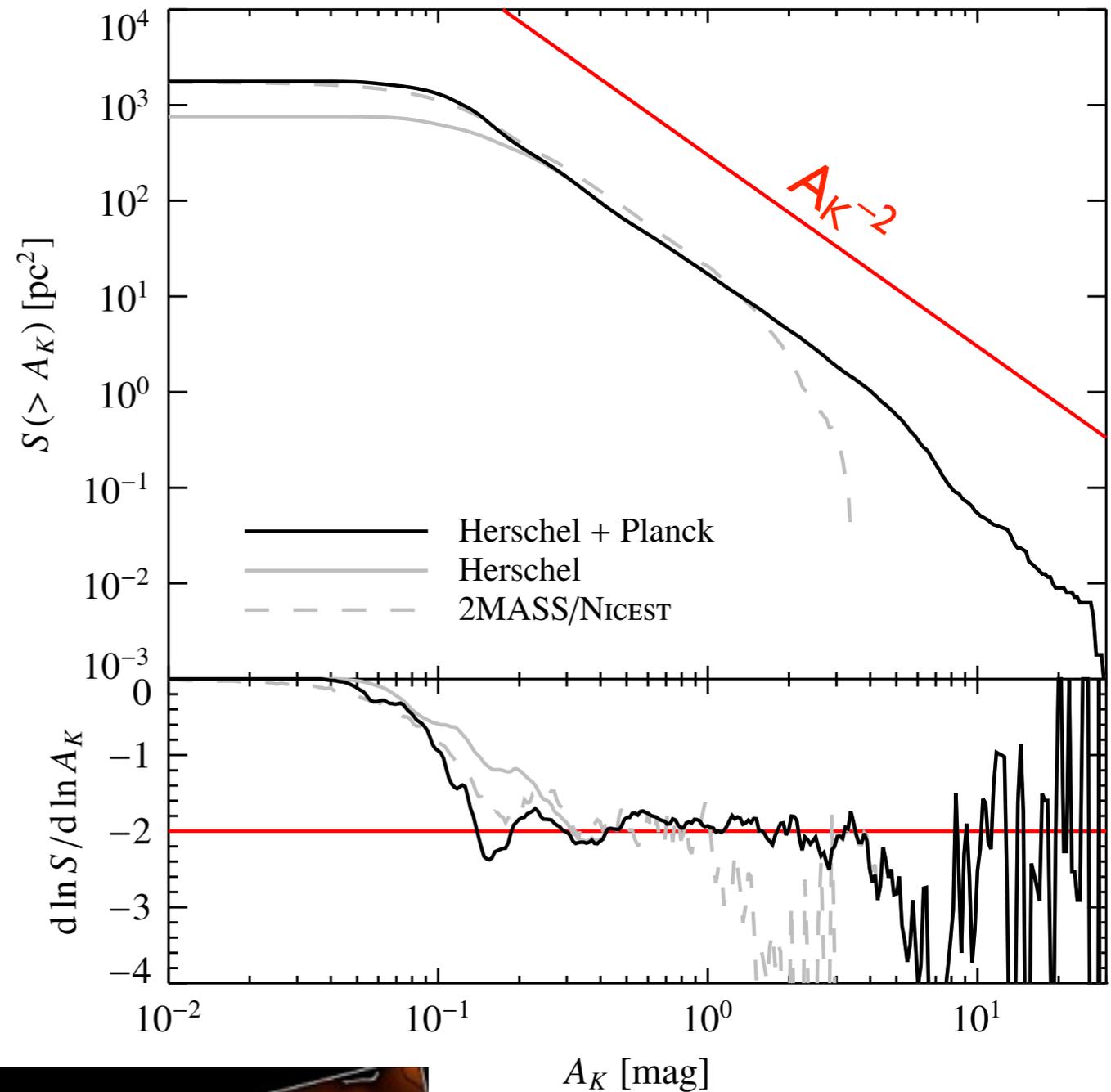
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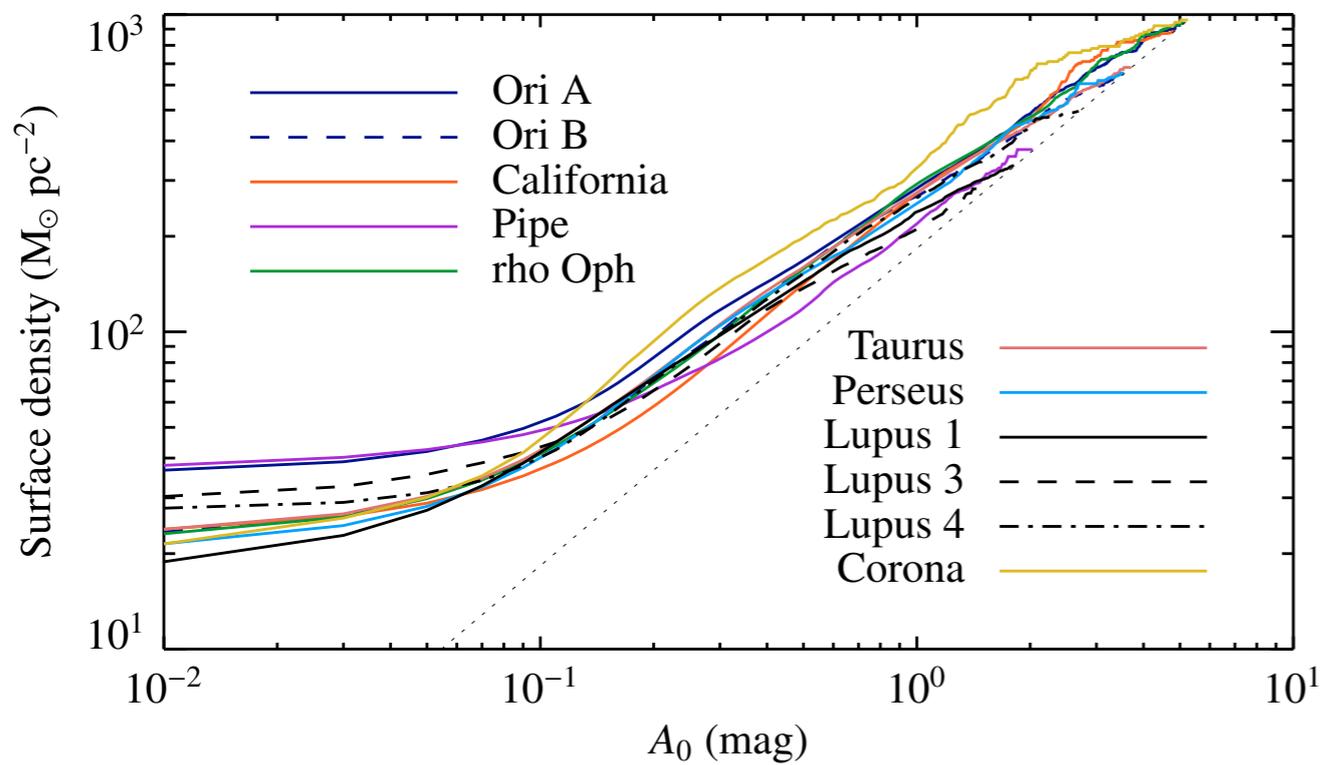
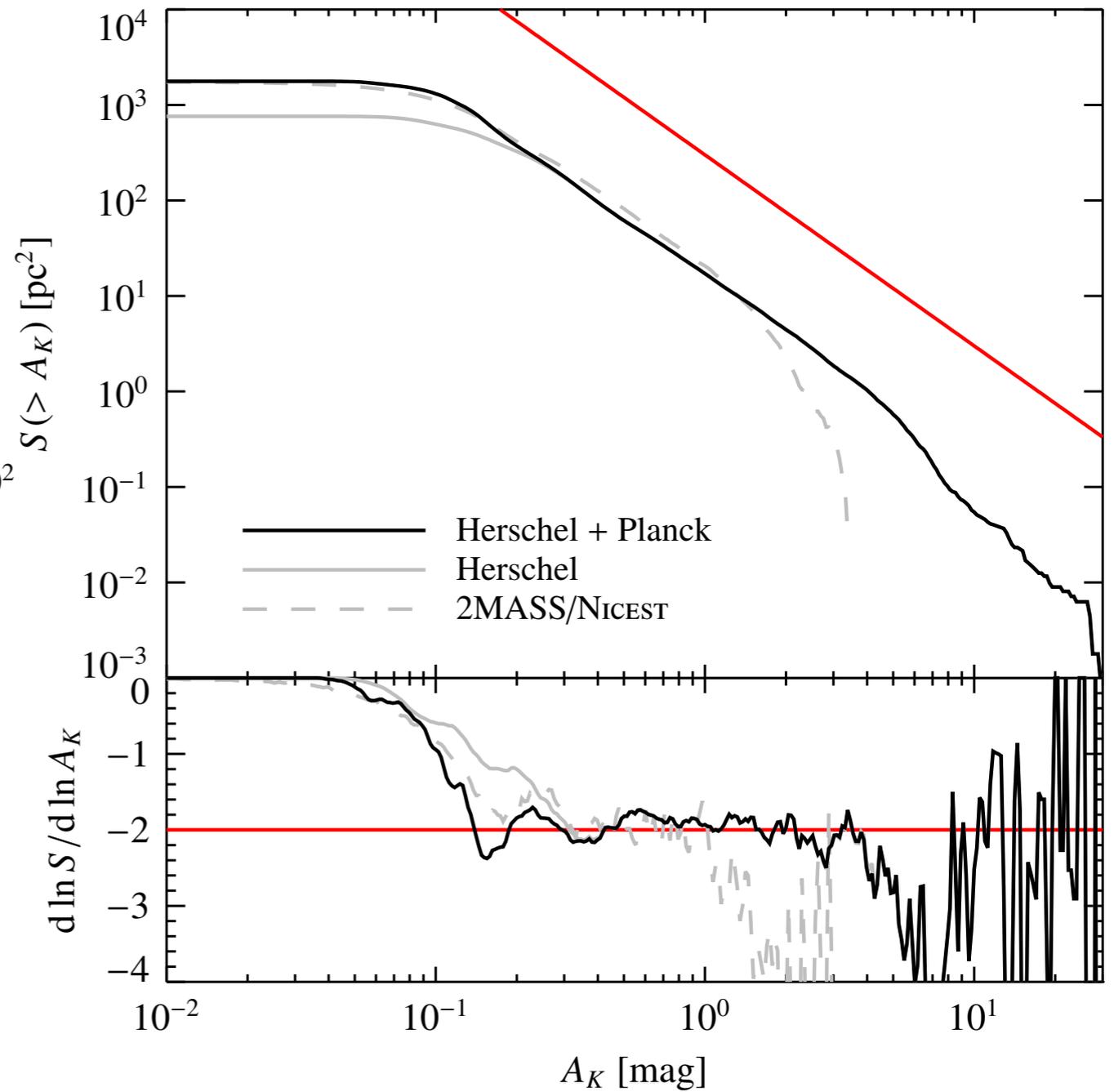
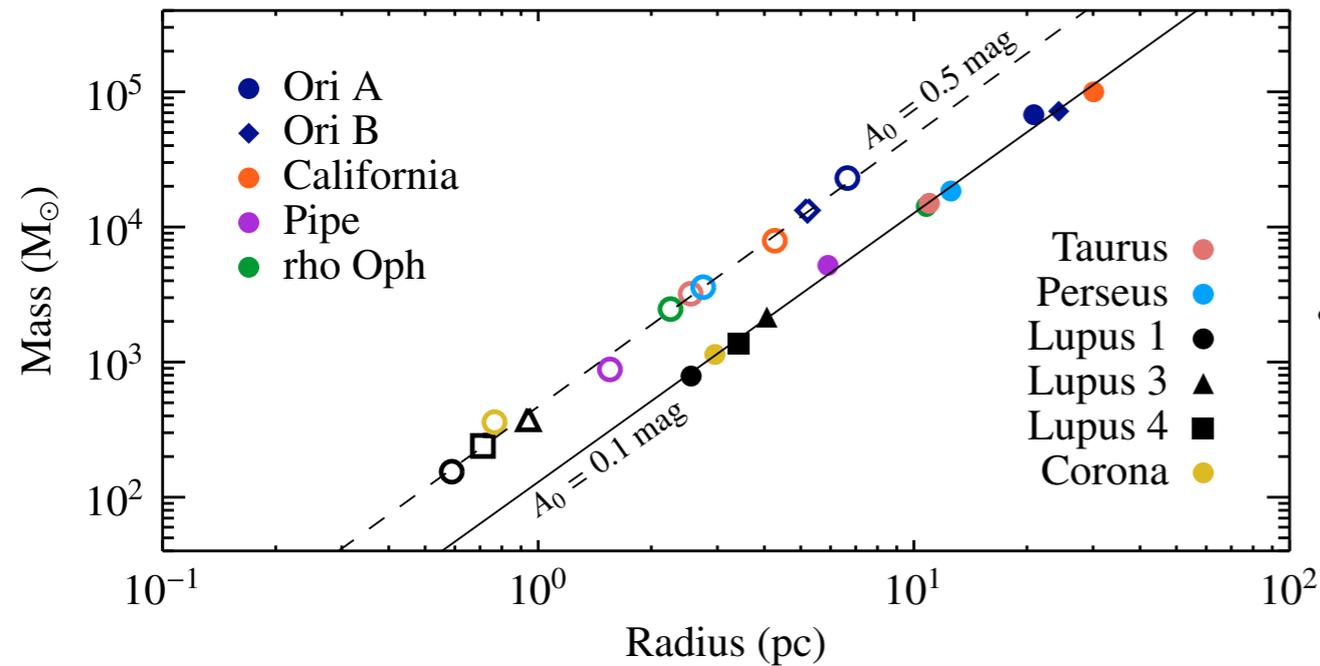
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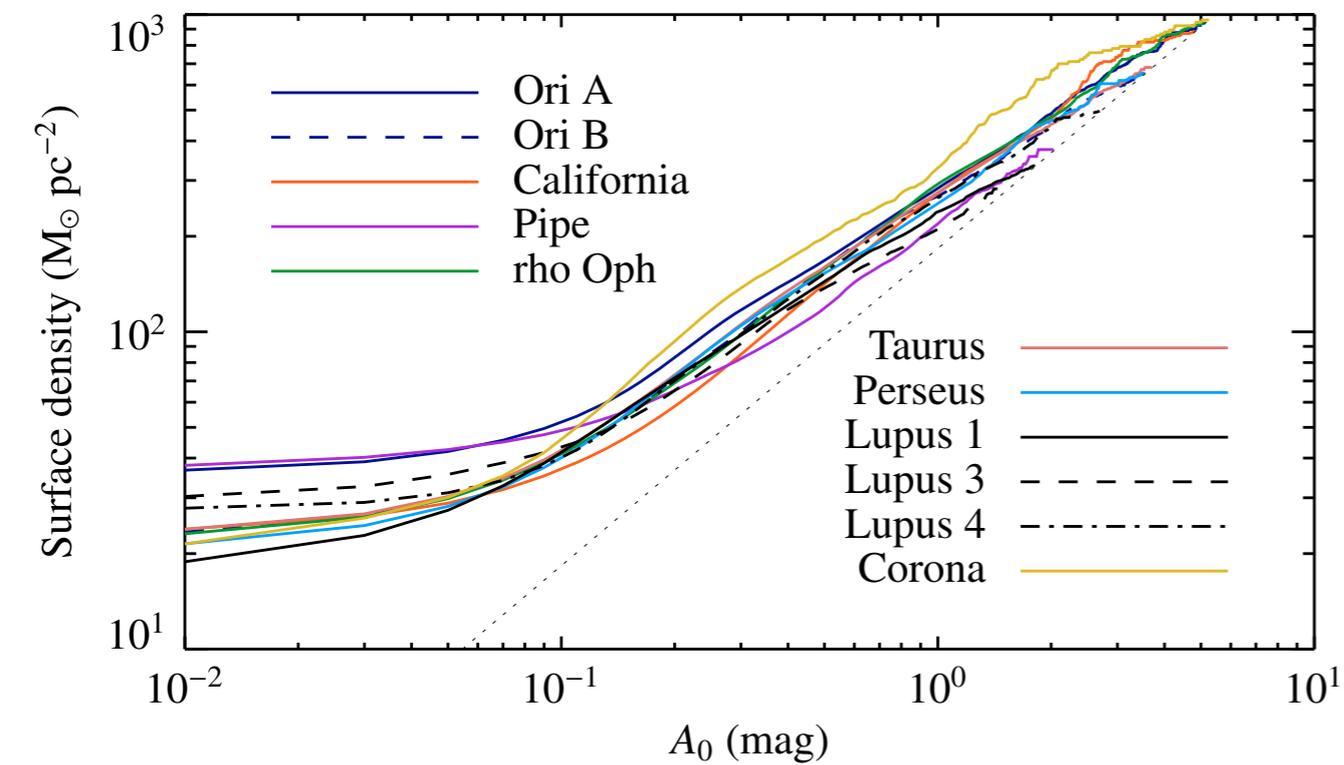
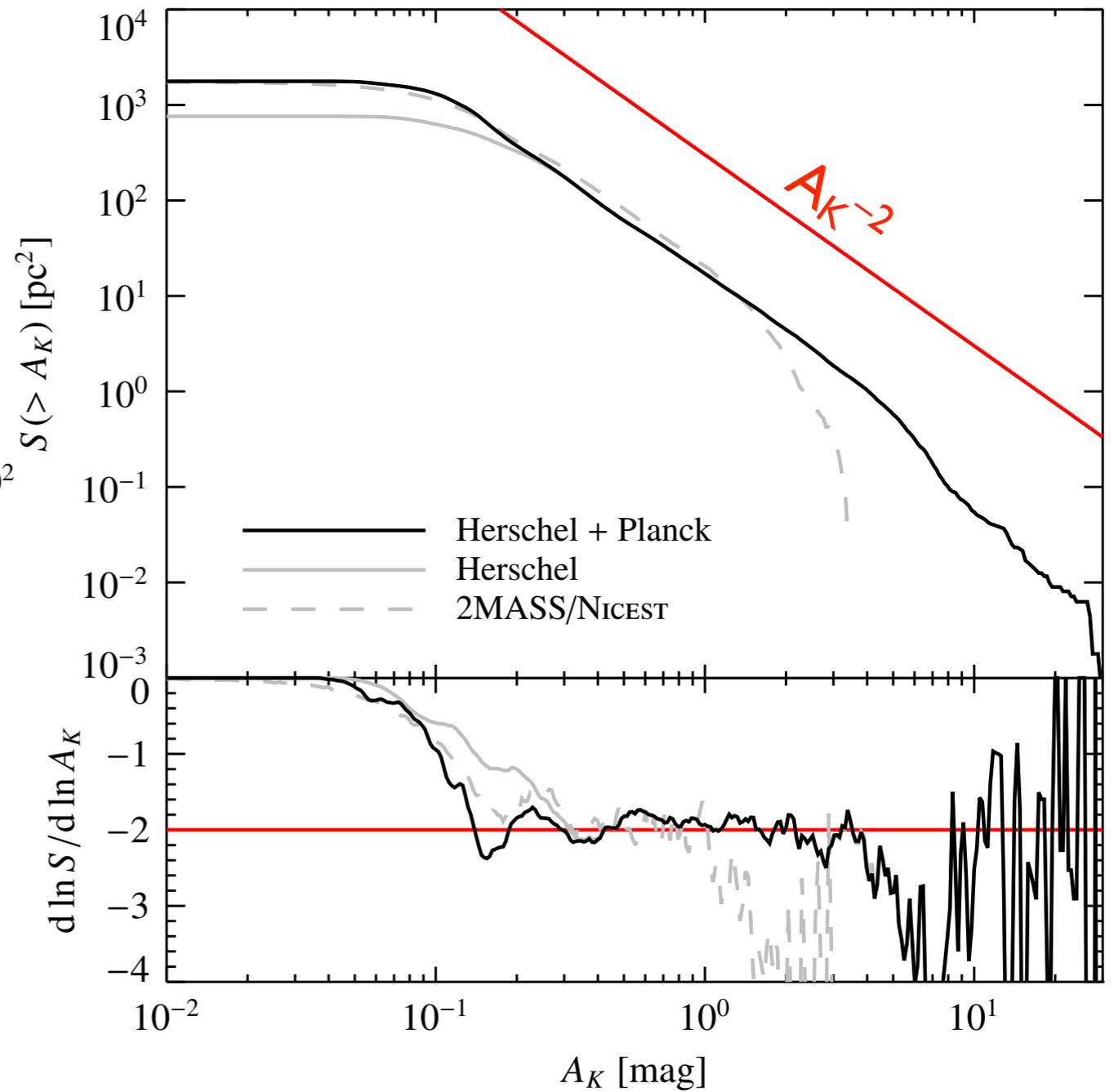
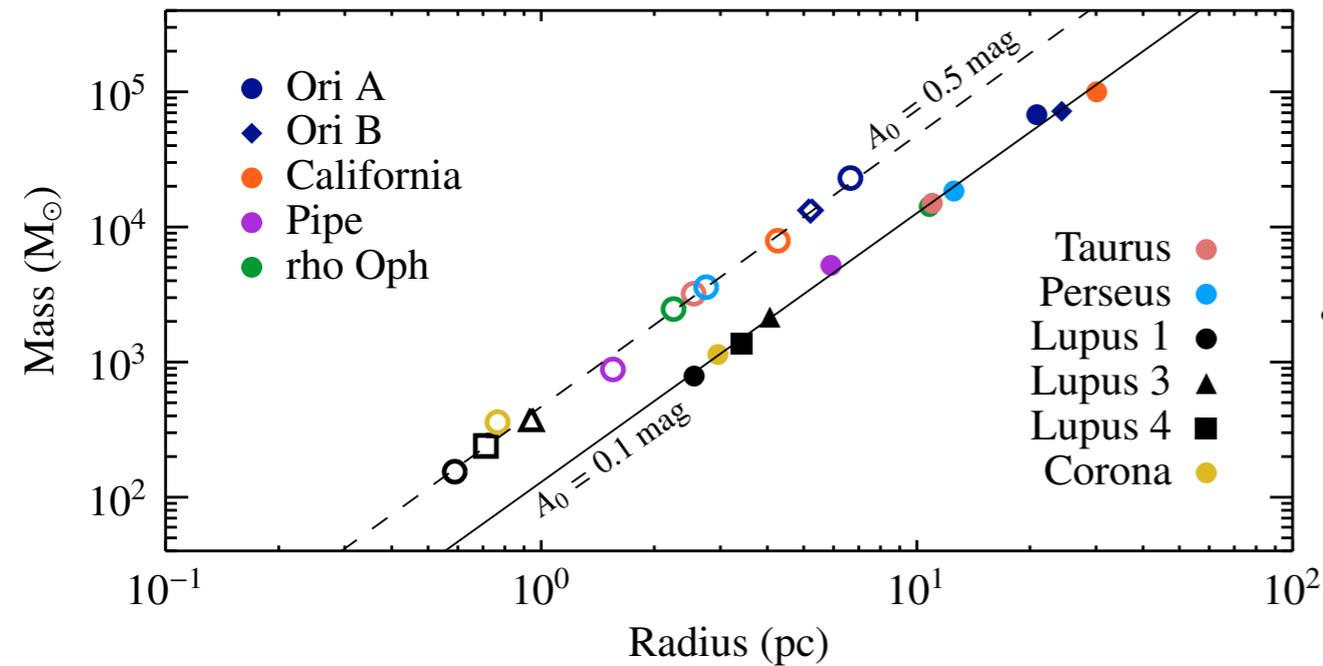


Lombardi et al. (2014)

# 3rd Larson's law

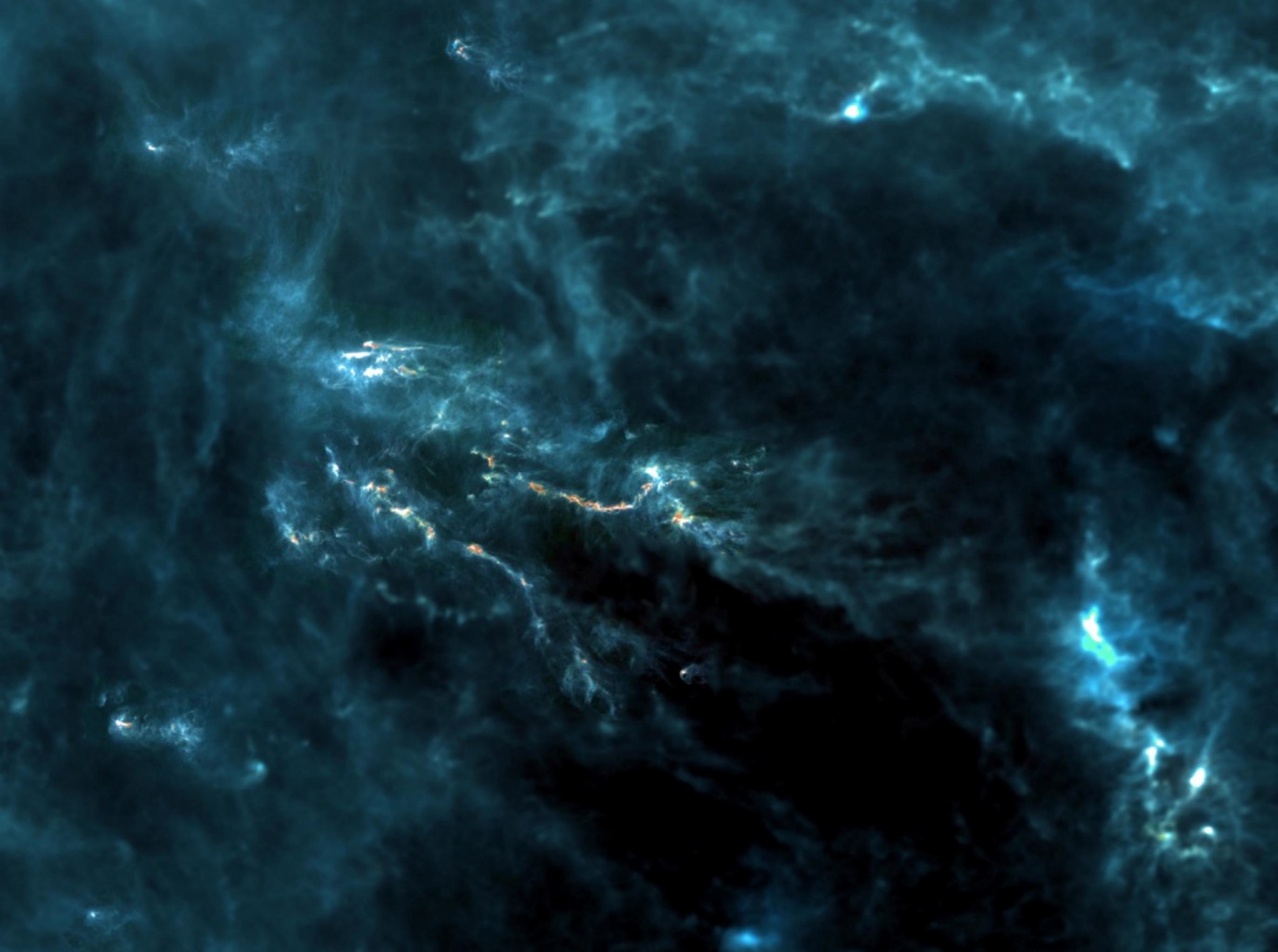


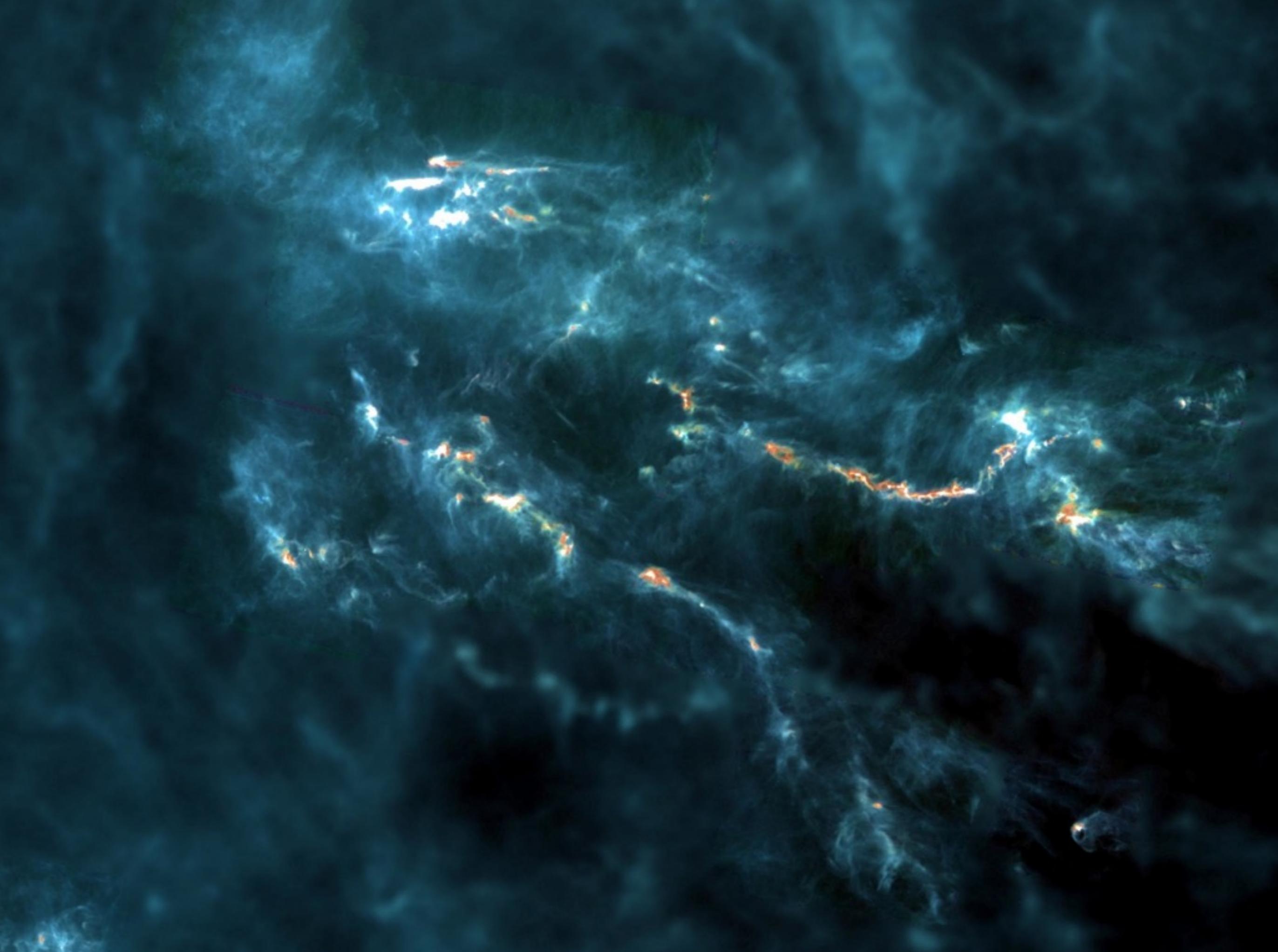
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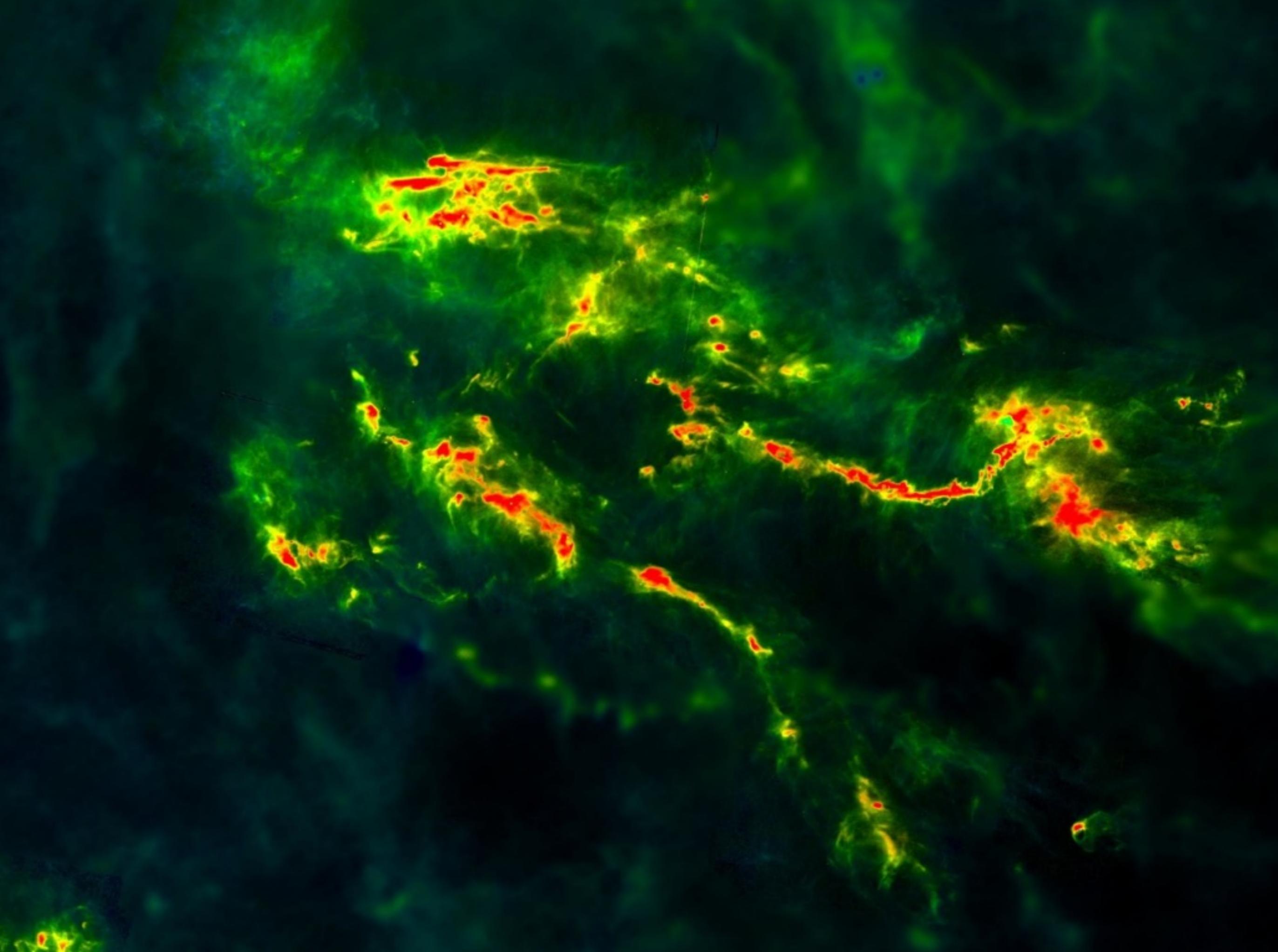


# Taurus

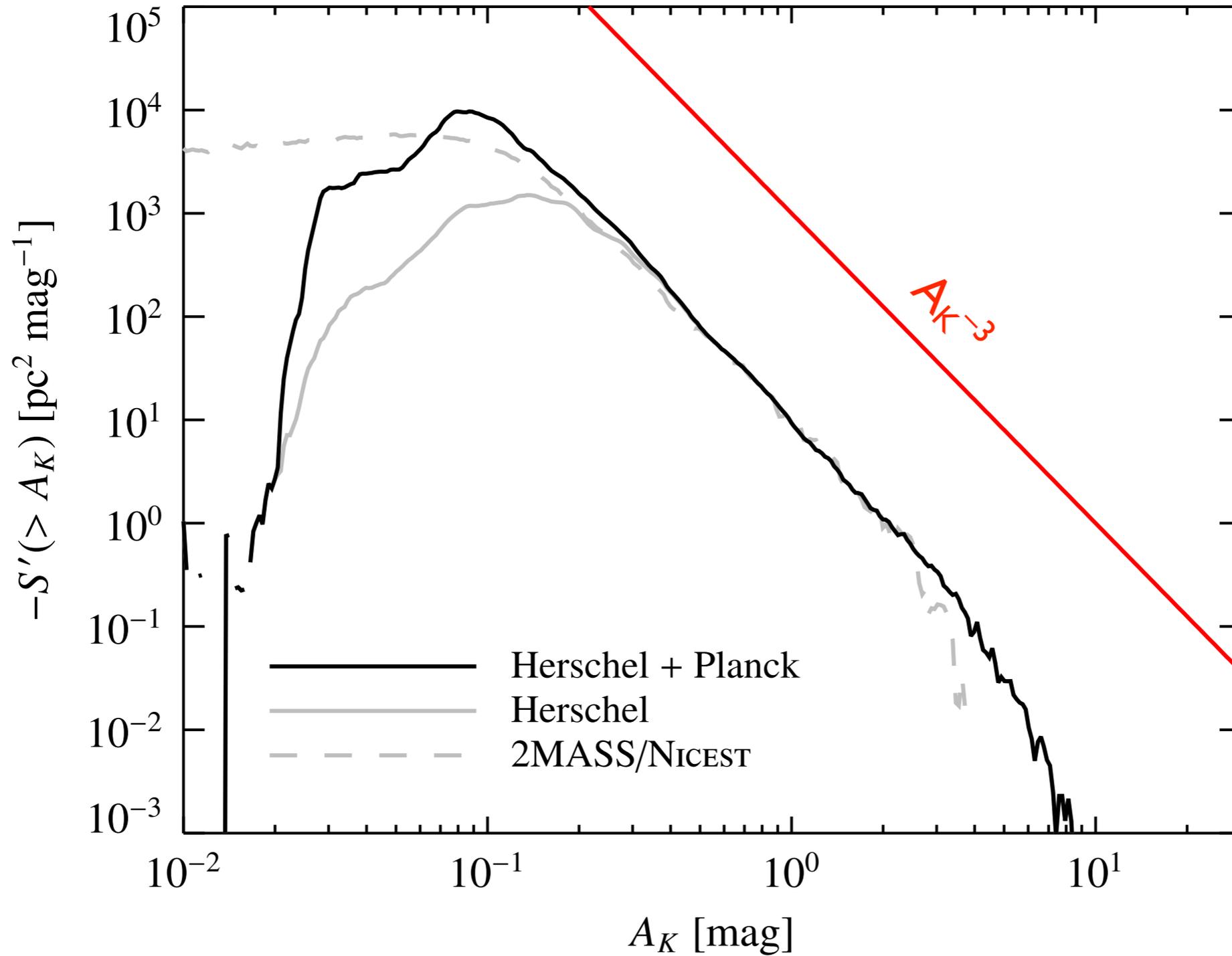
(Lombardi et al. 2015)





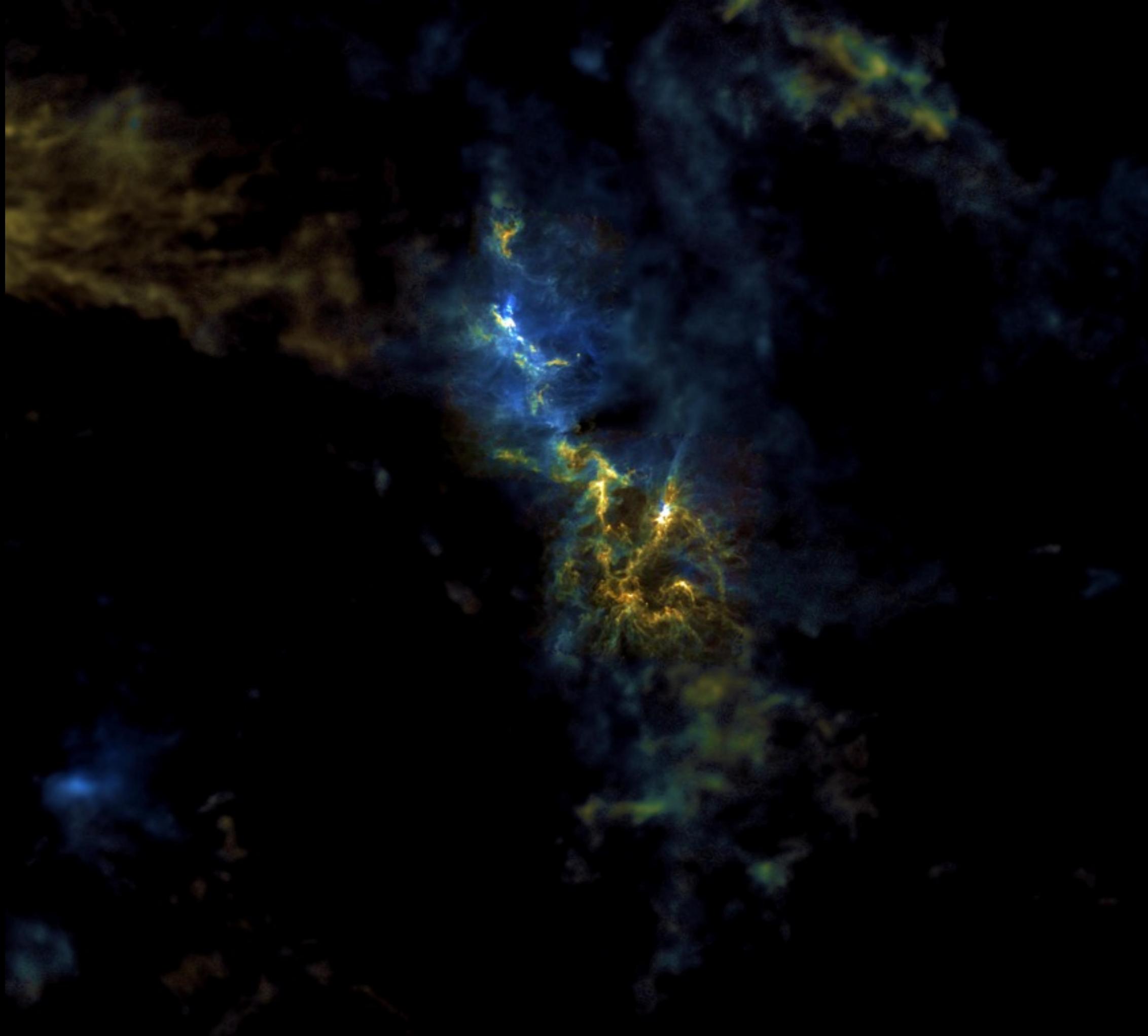


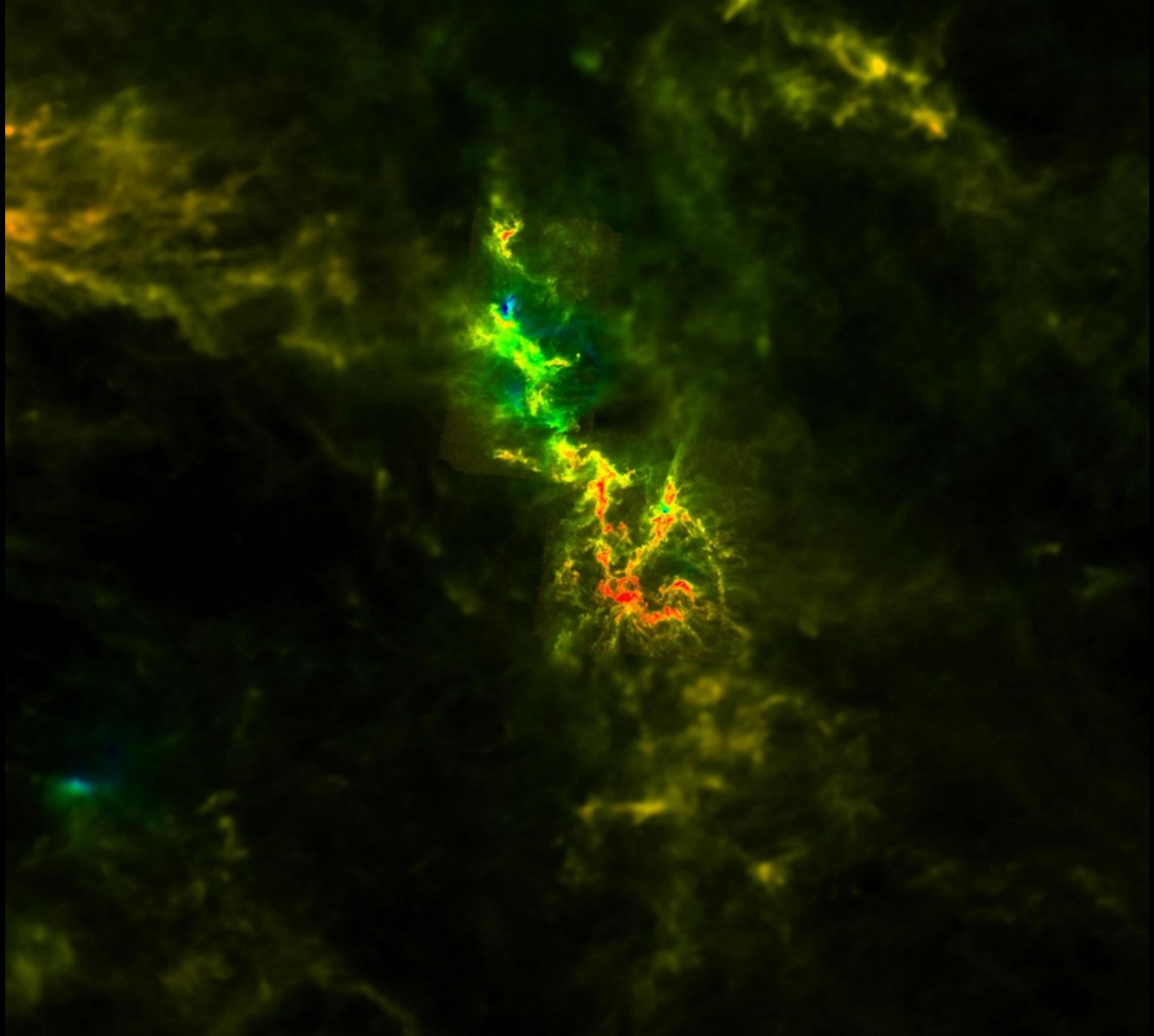
# Herschel PDF for Taurus

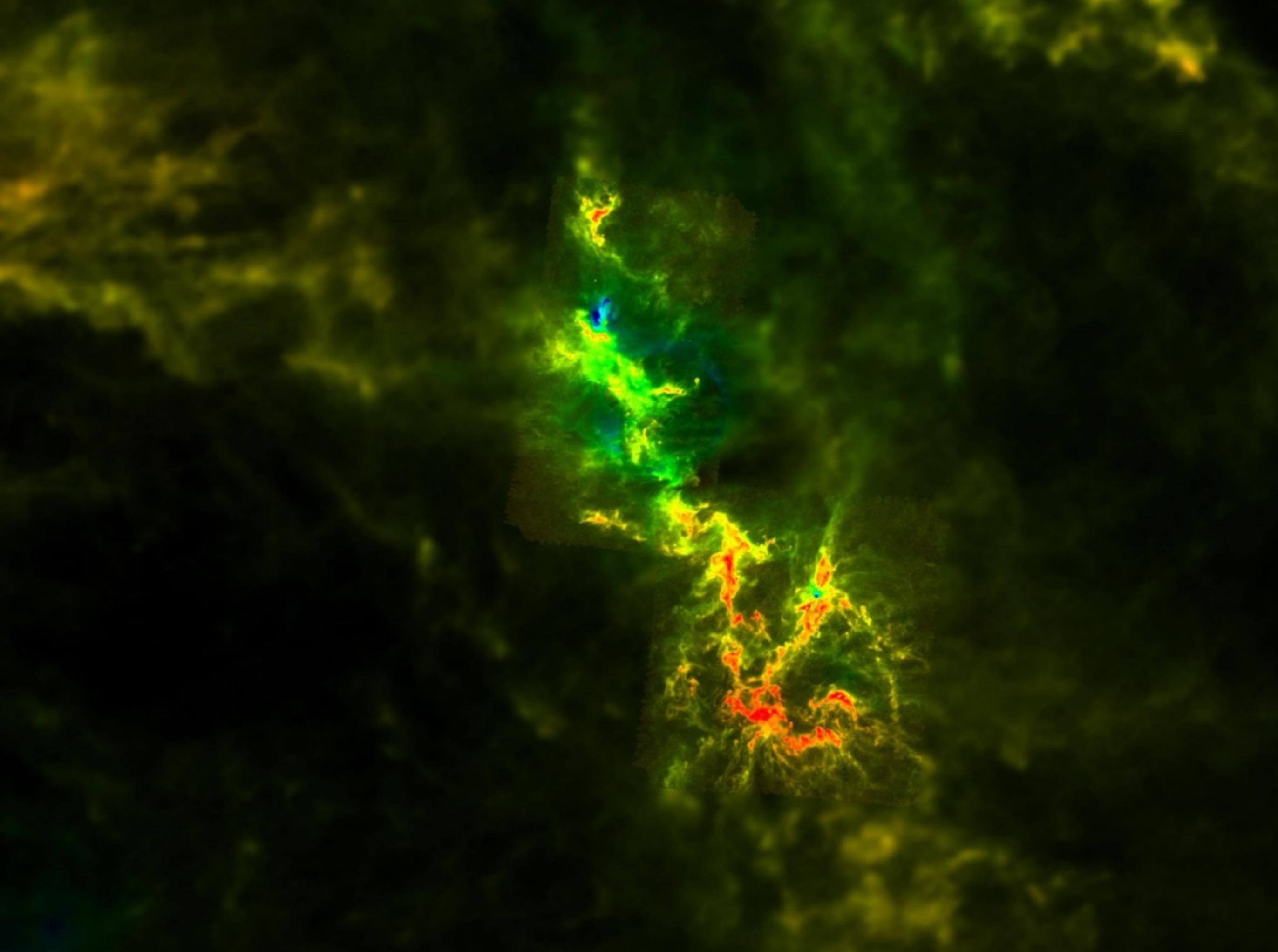


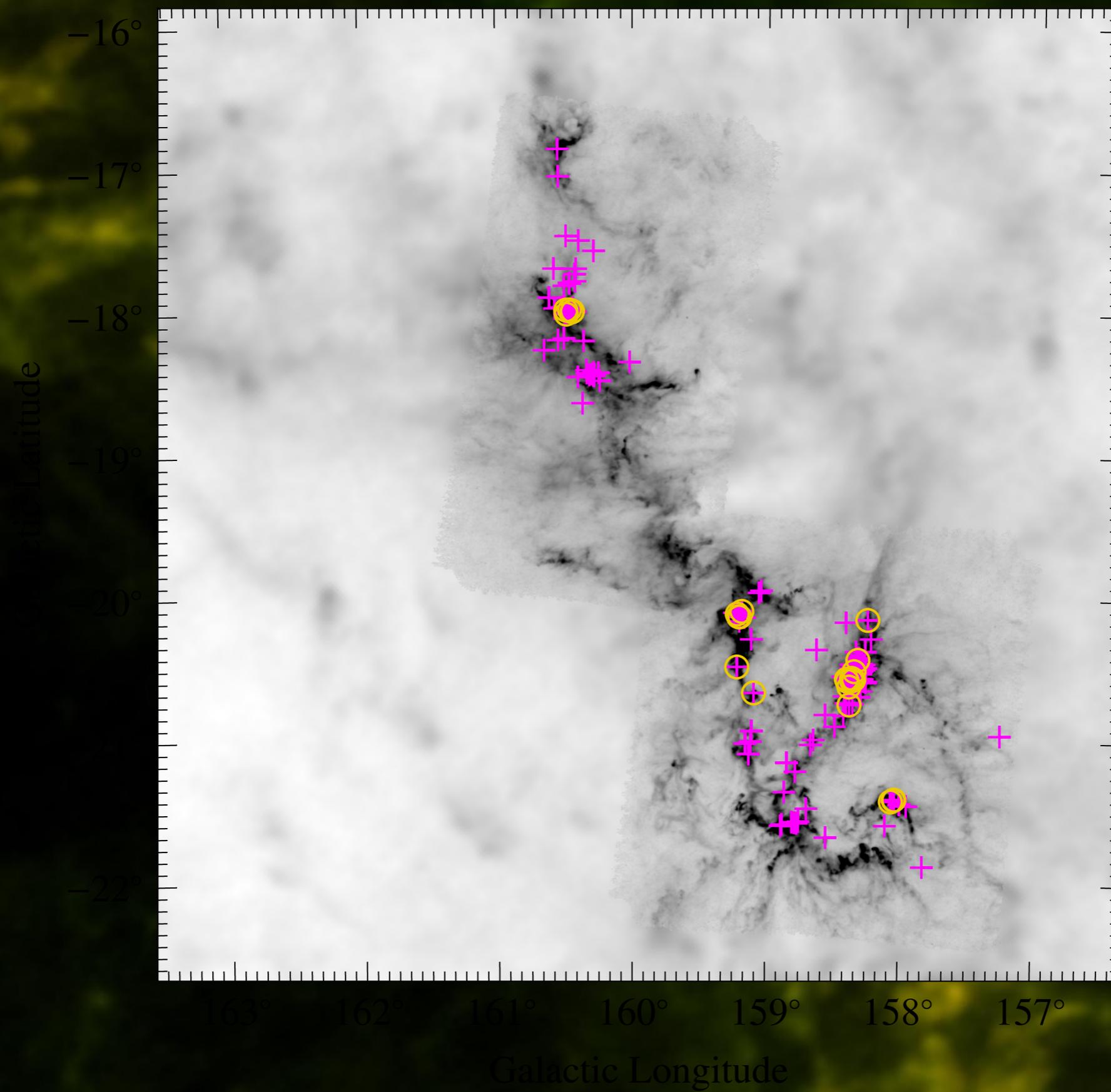
# Perseus

(Zari et al. 2015)

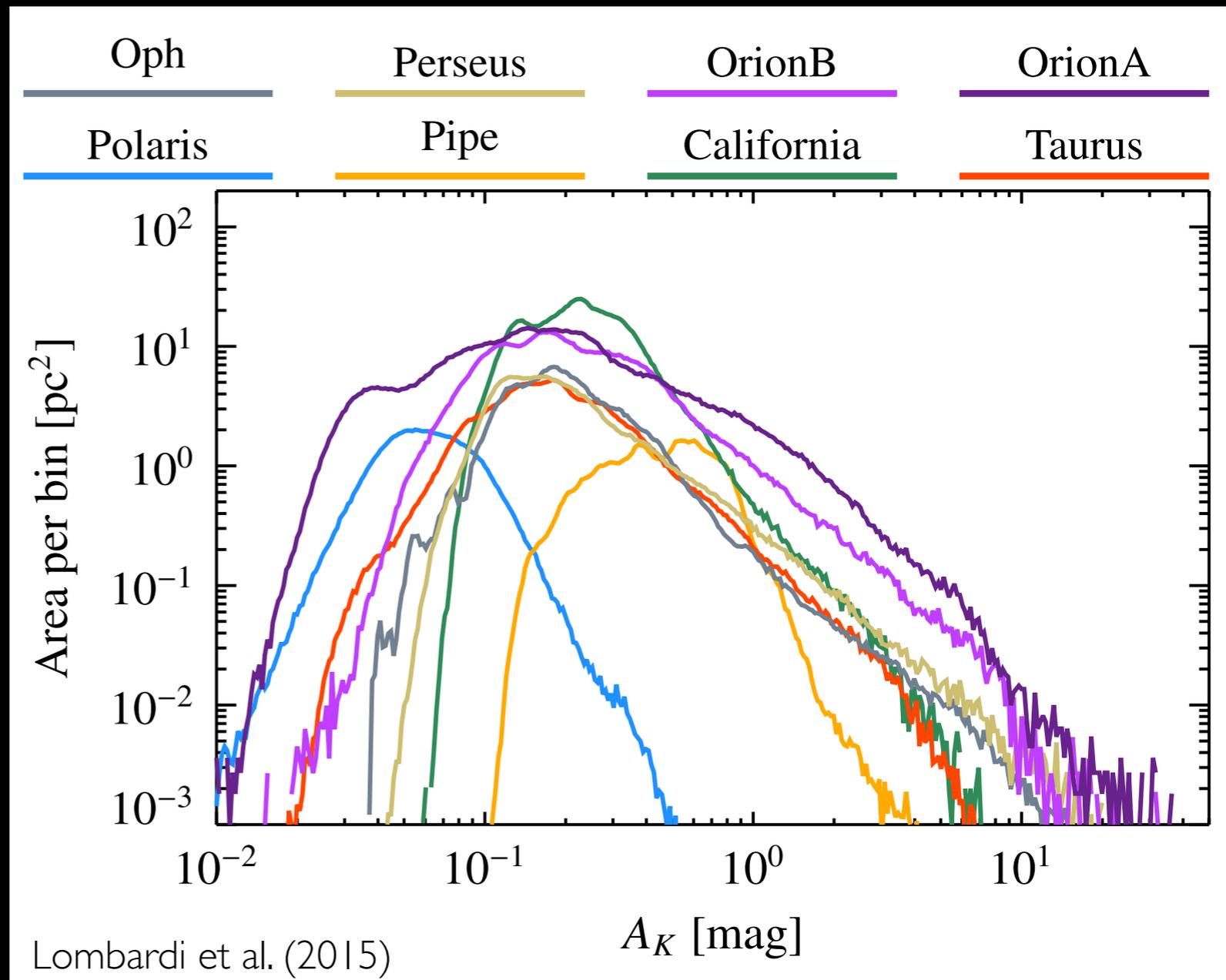






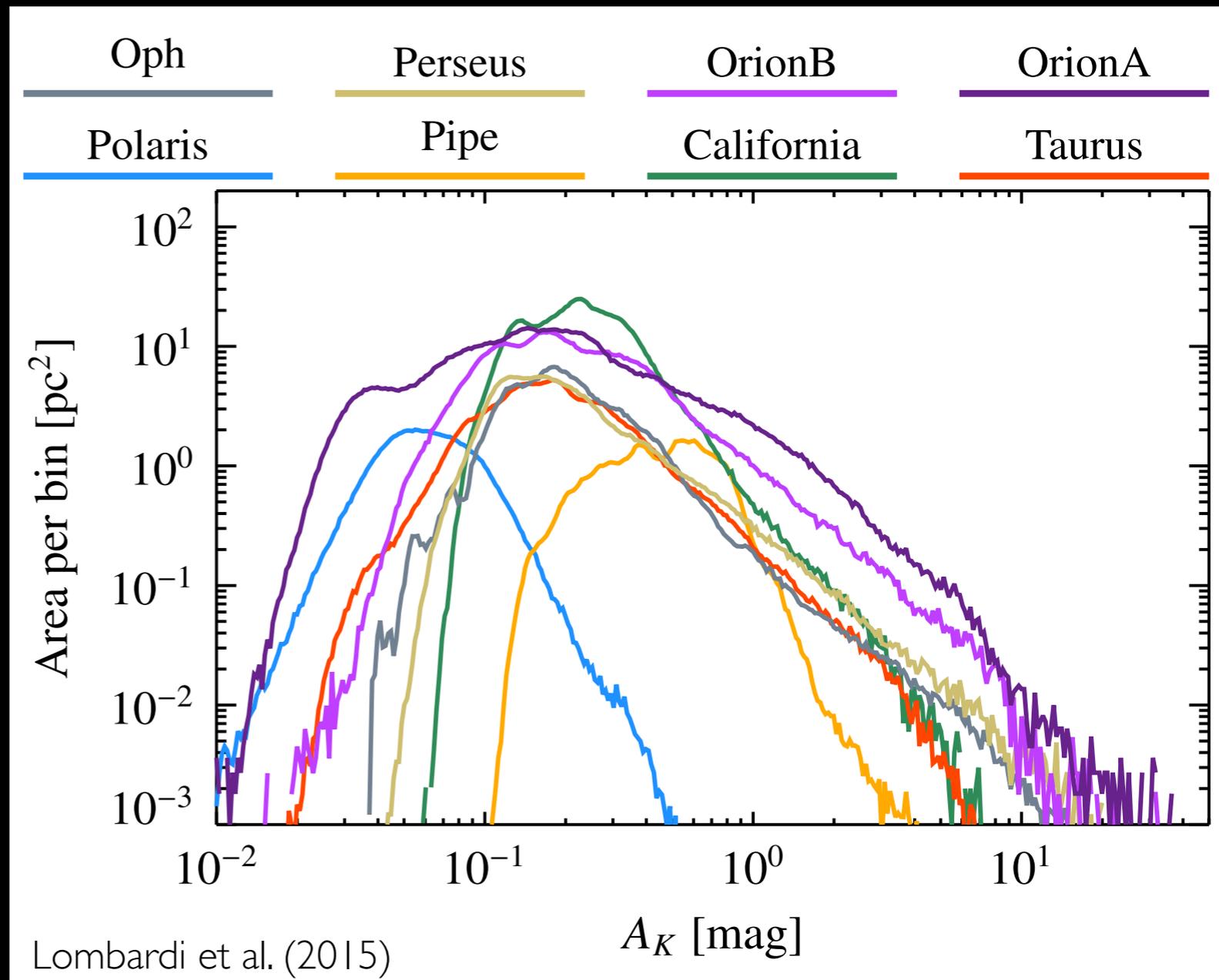


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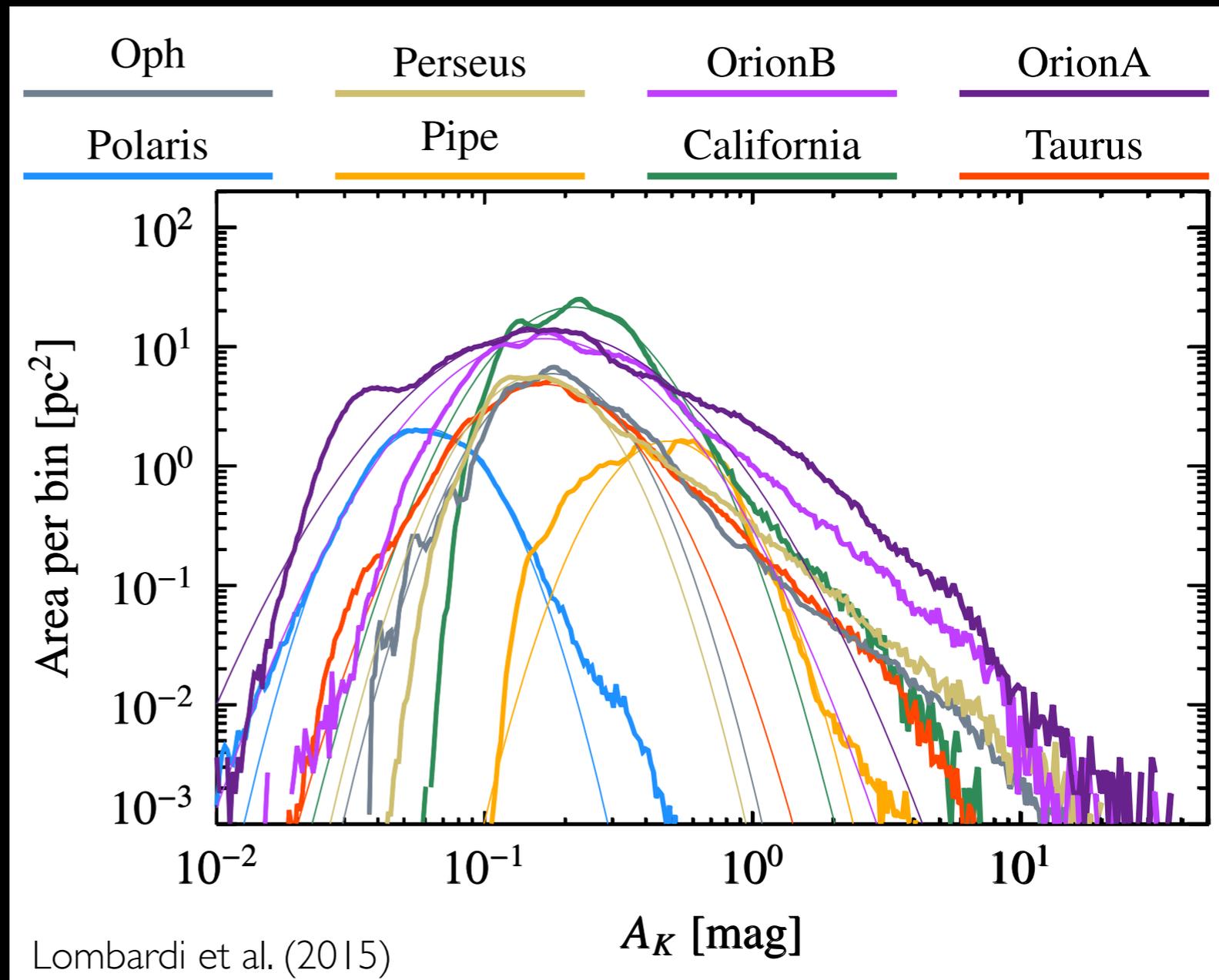
# PDFs from Herschel

- PDFs are hardly symmetric in log-log



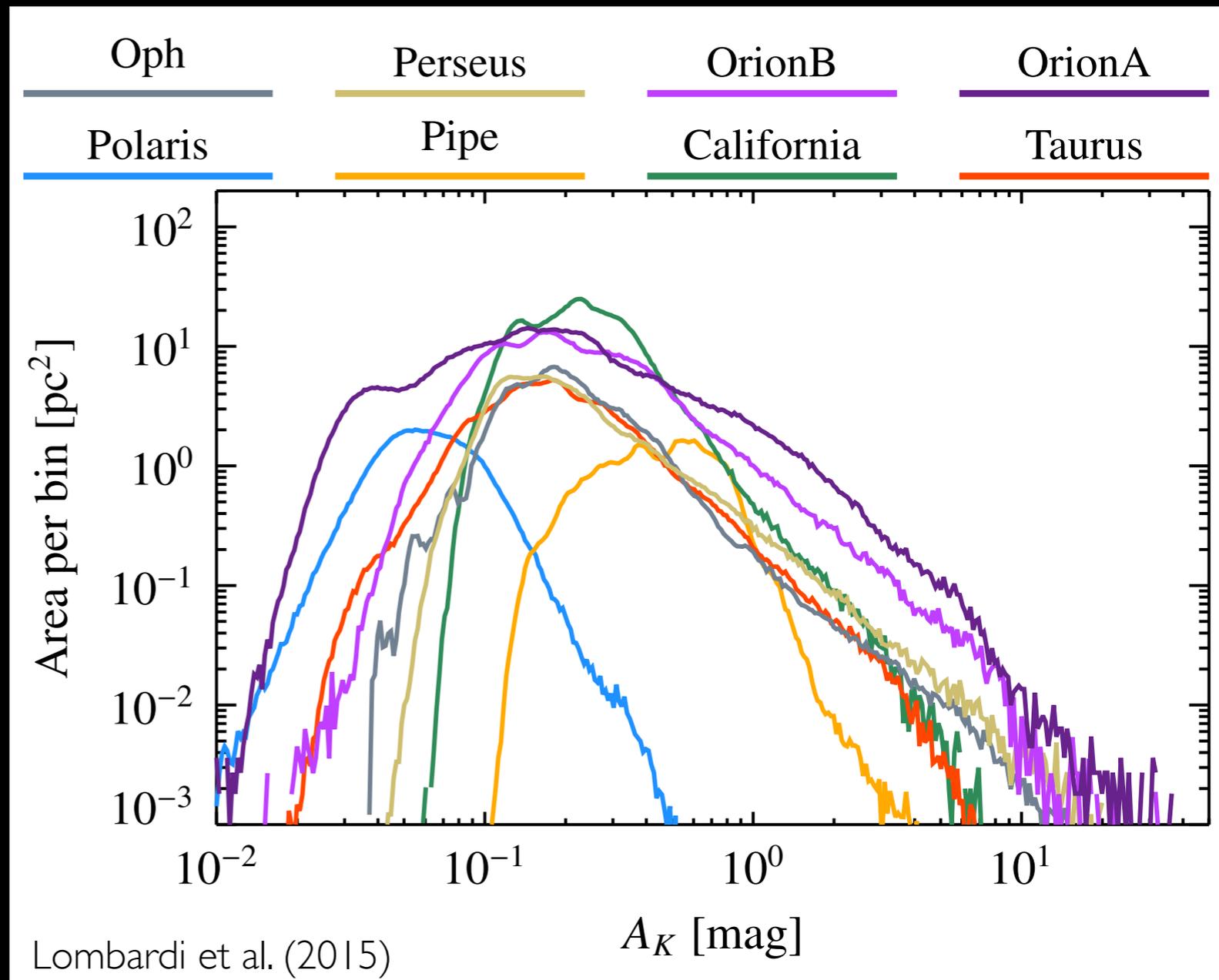
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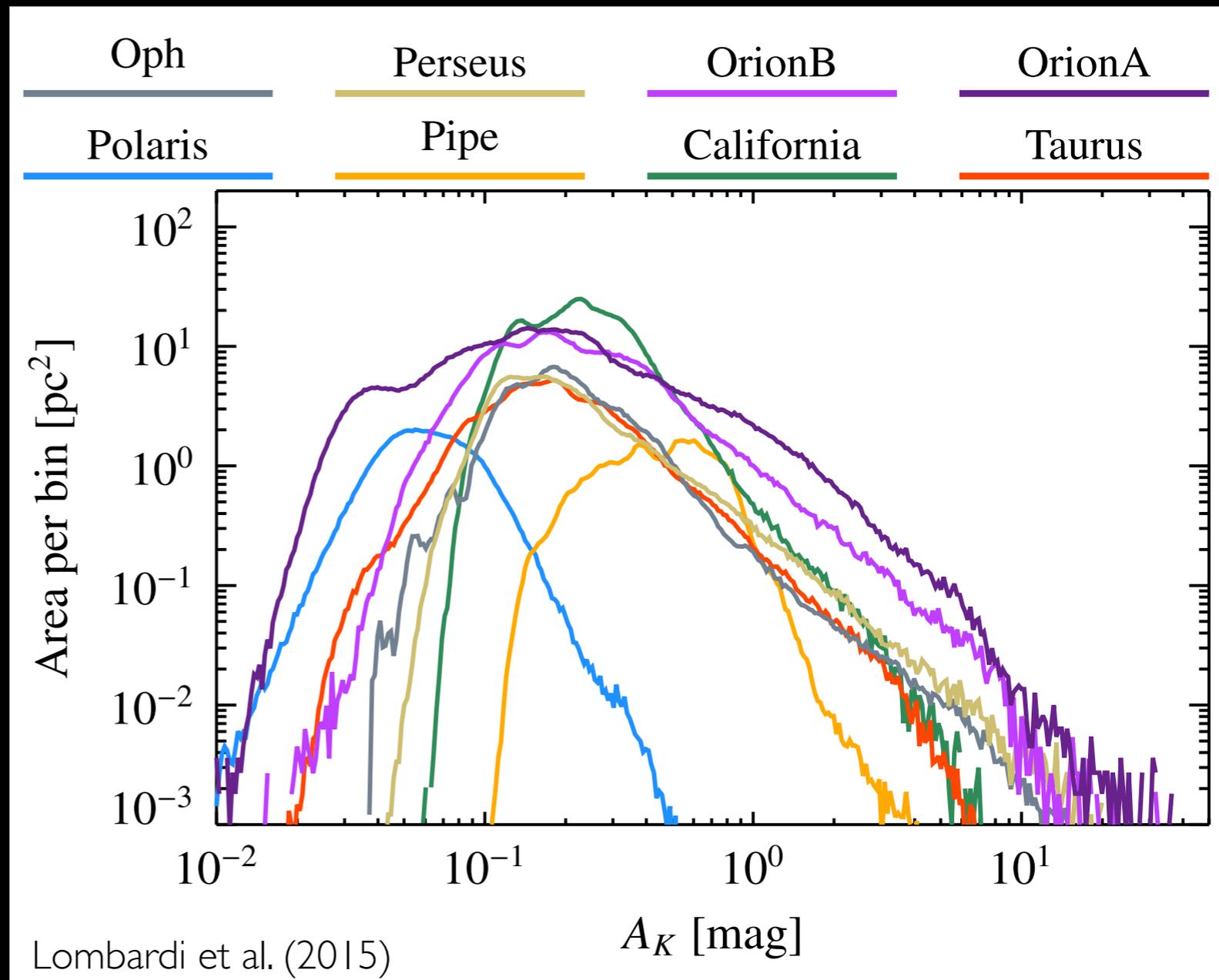
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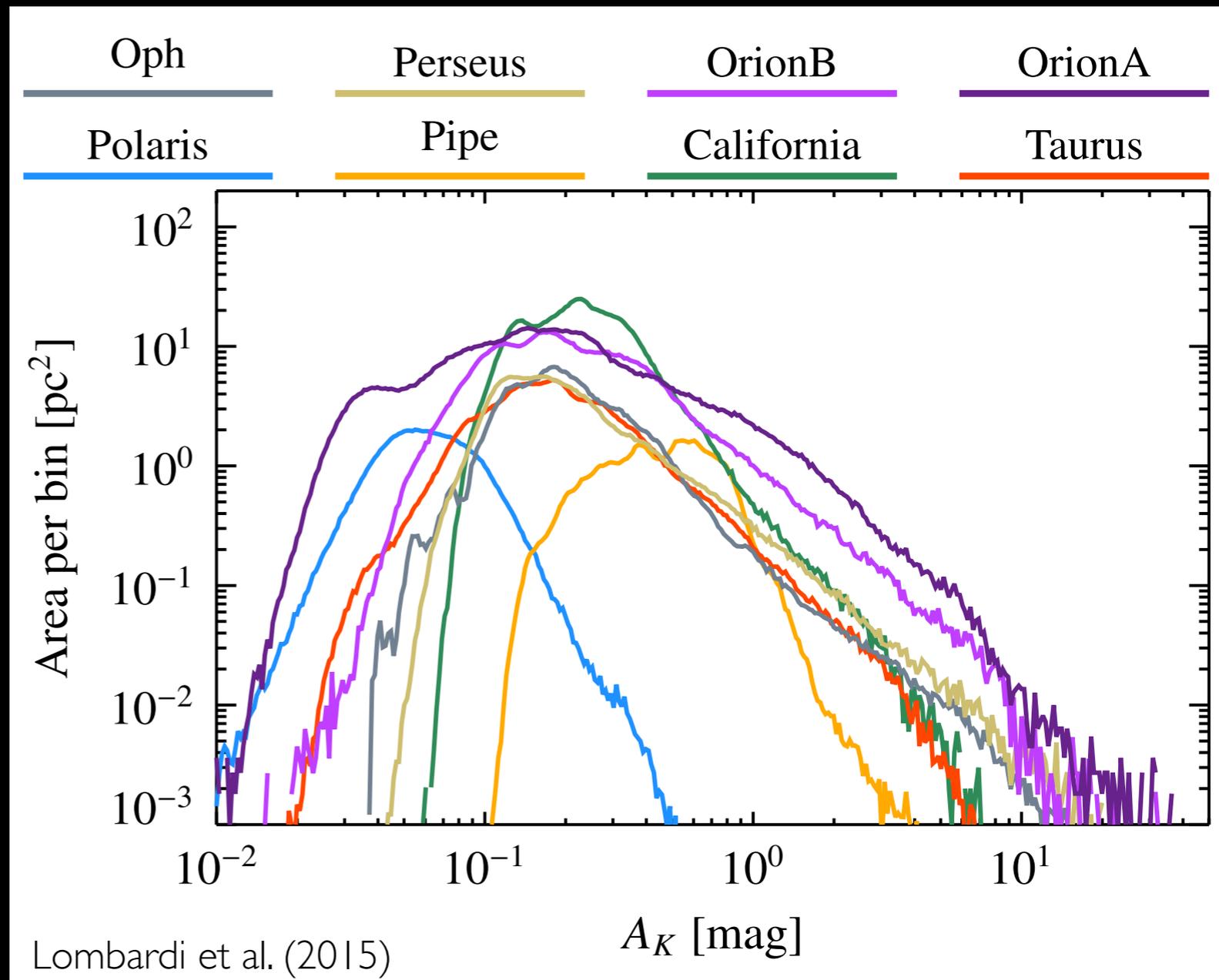
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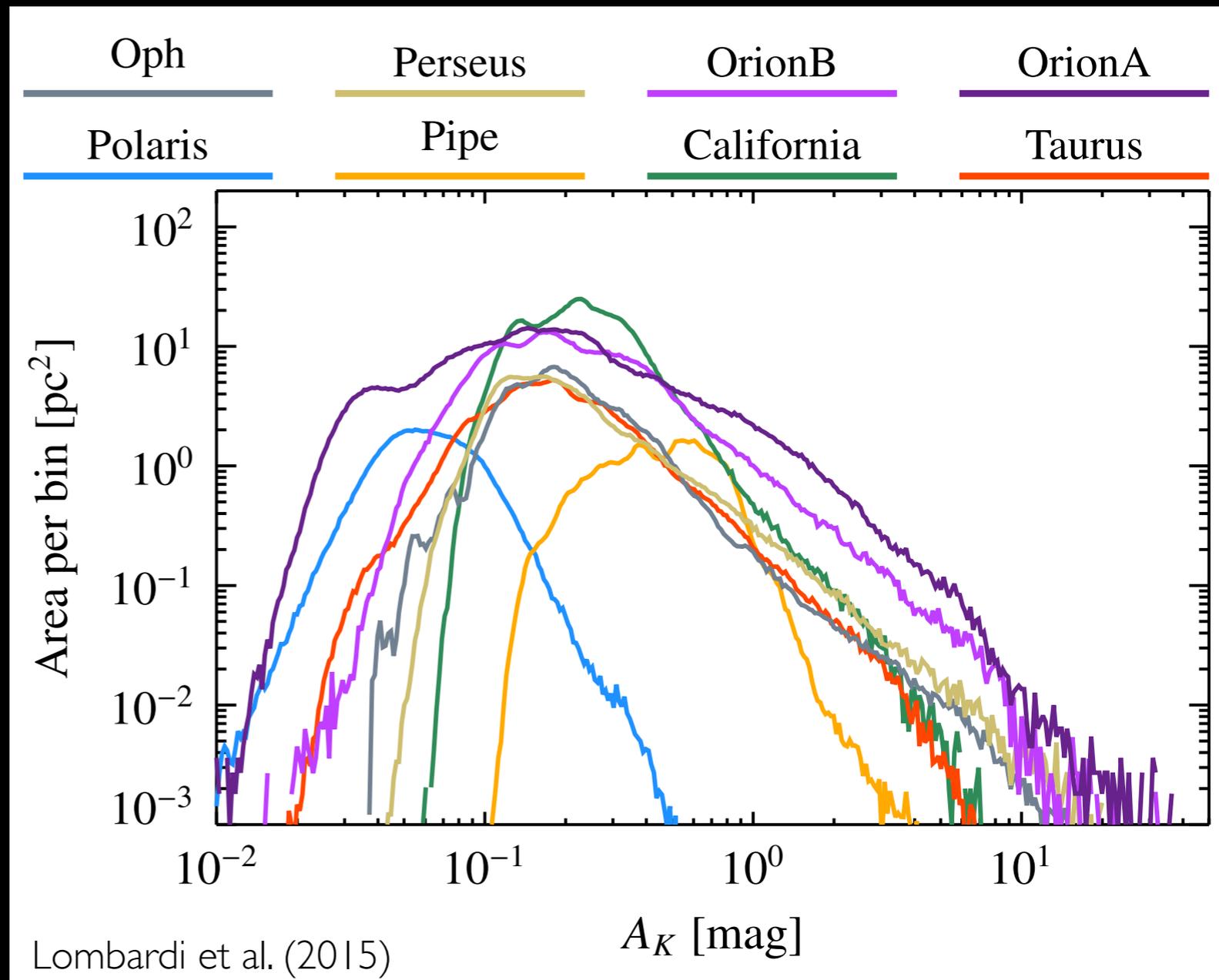
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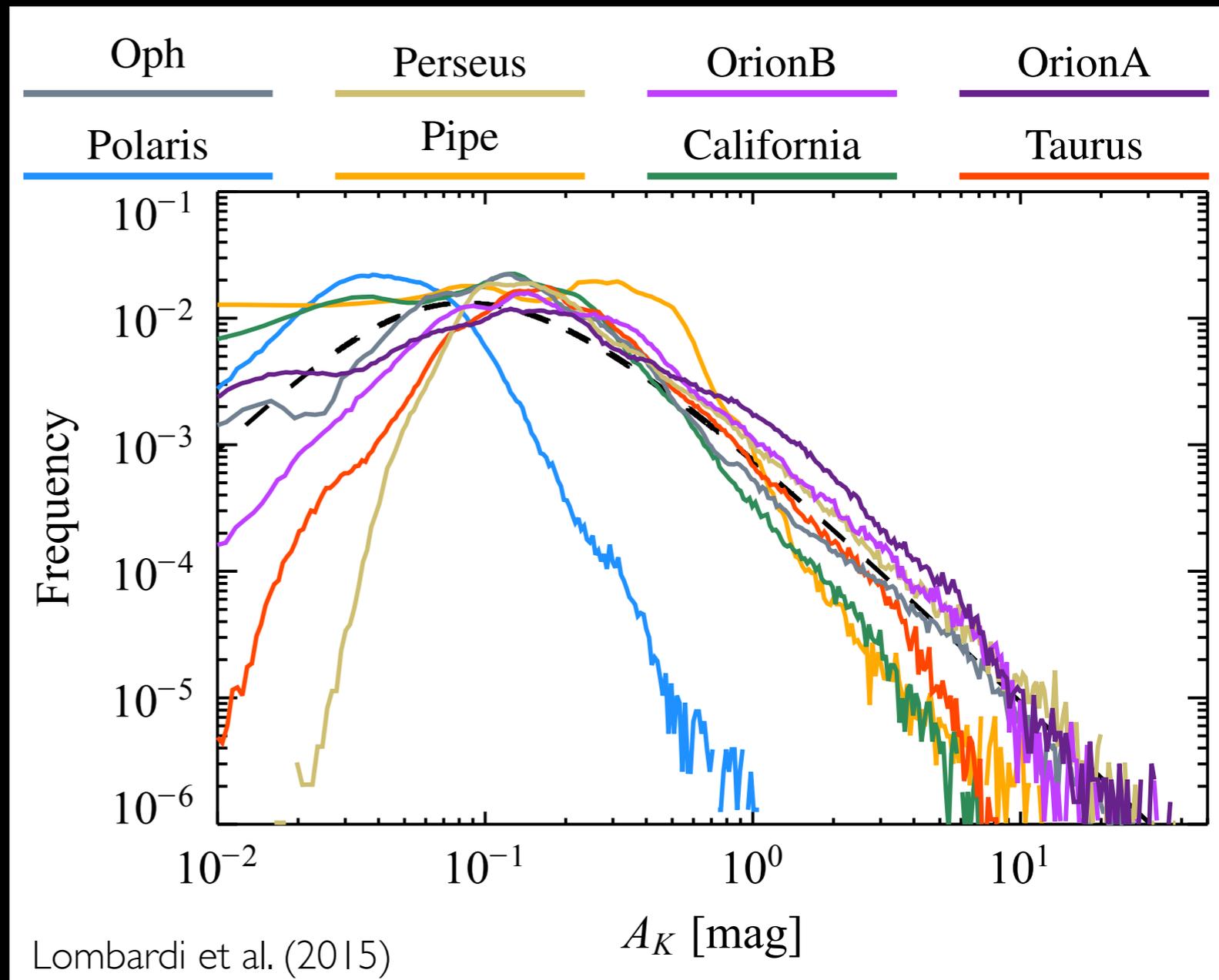
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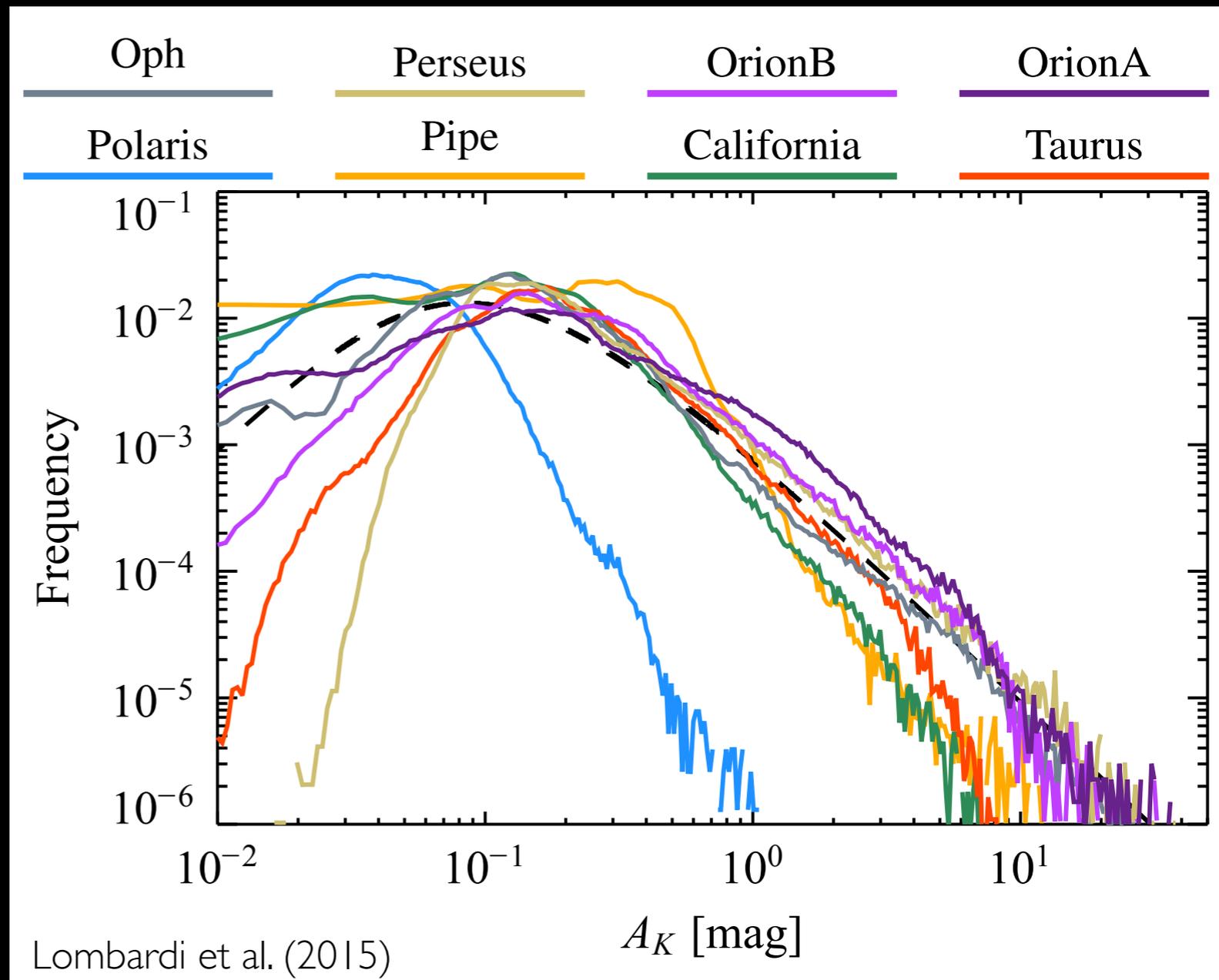
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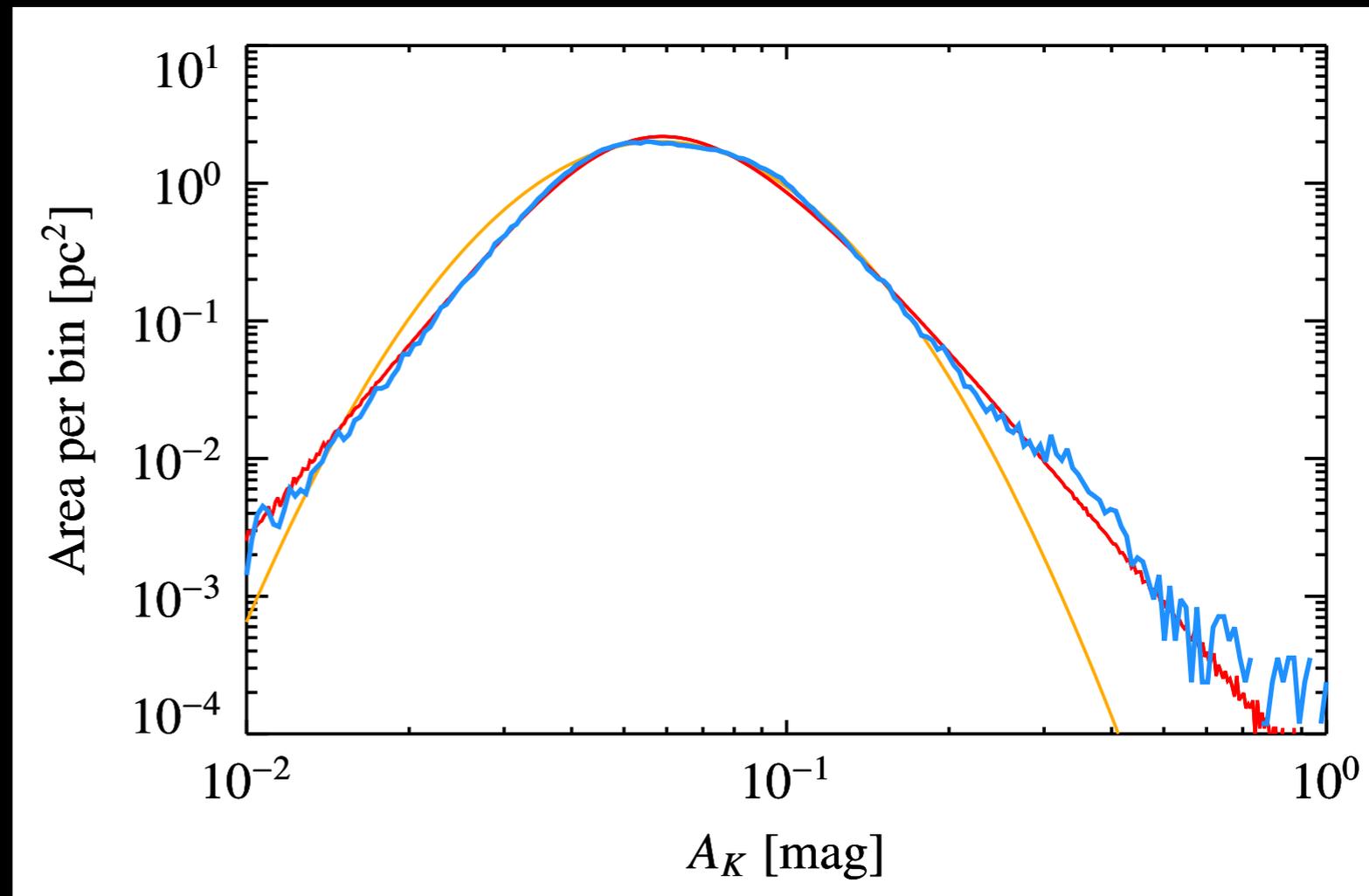
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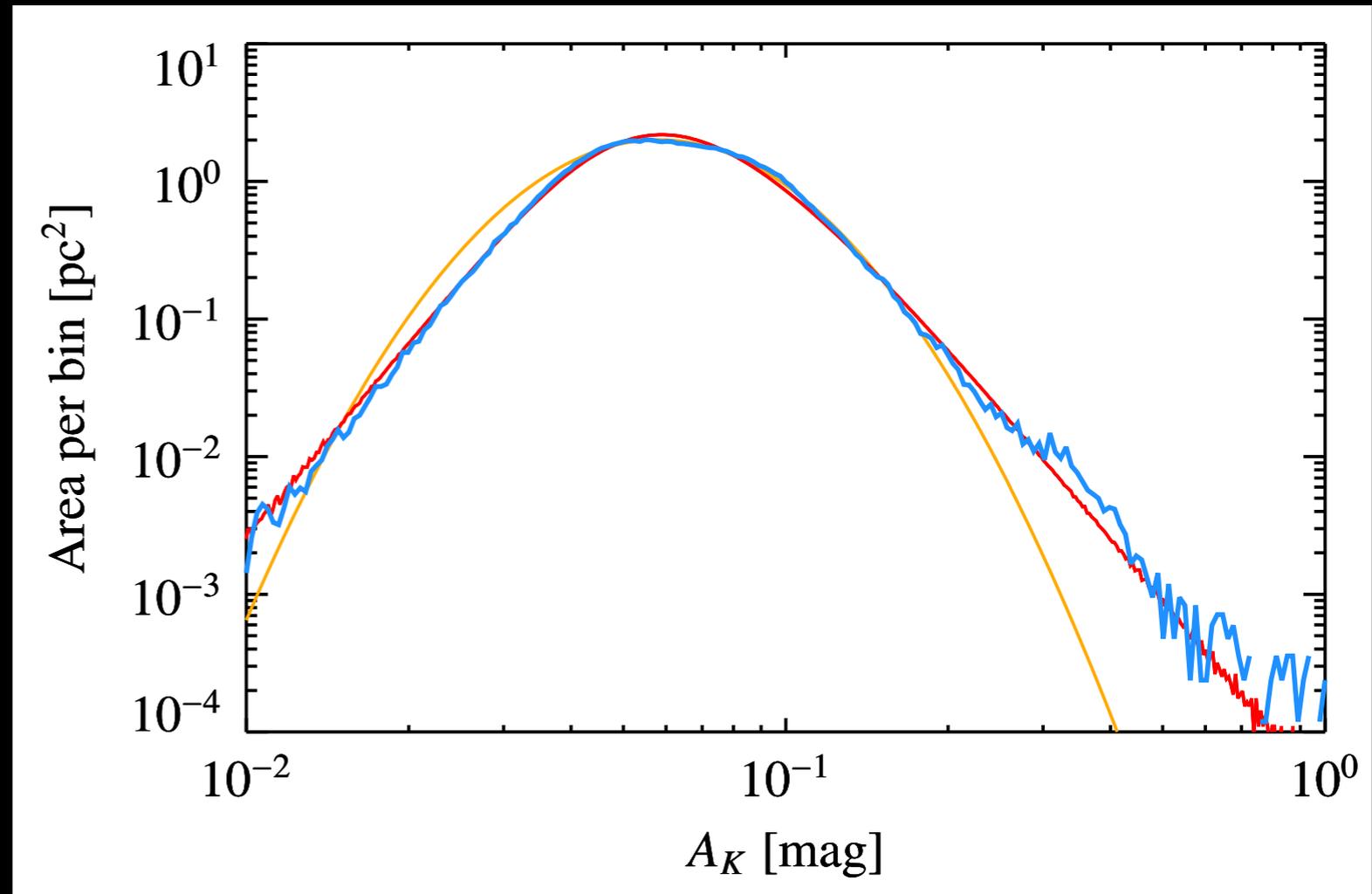
Can Polaris be described as log-normal?

# Polaris log-normal fit



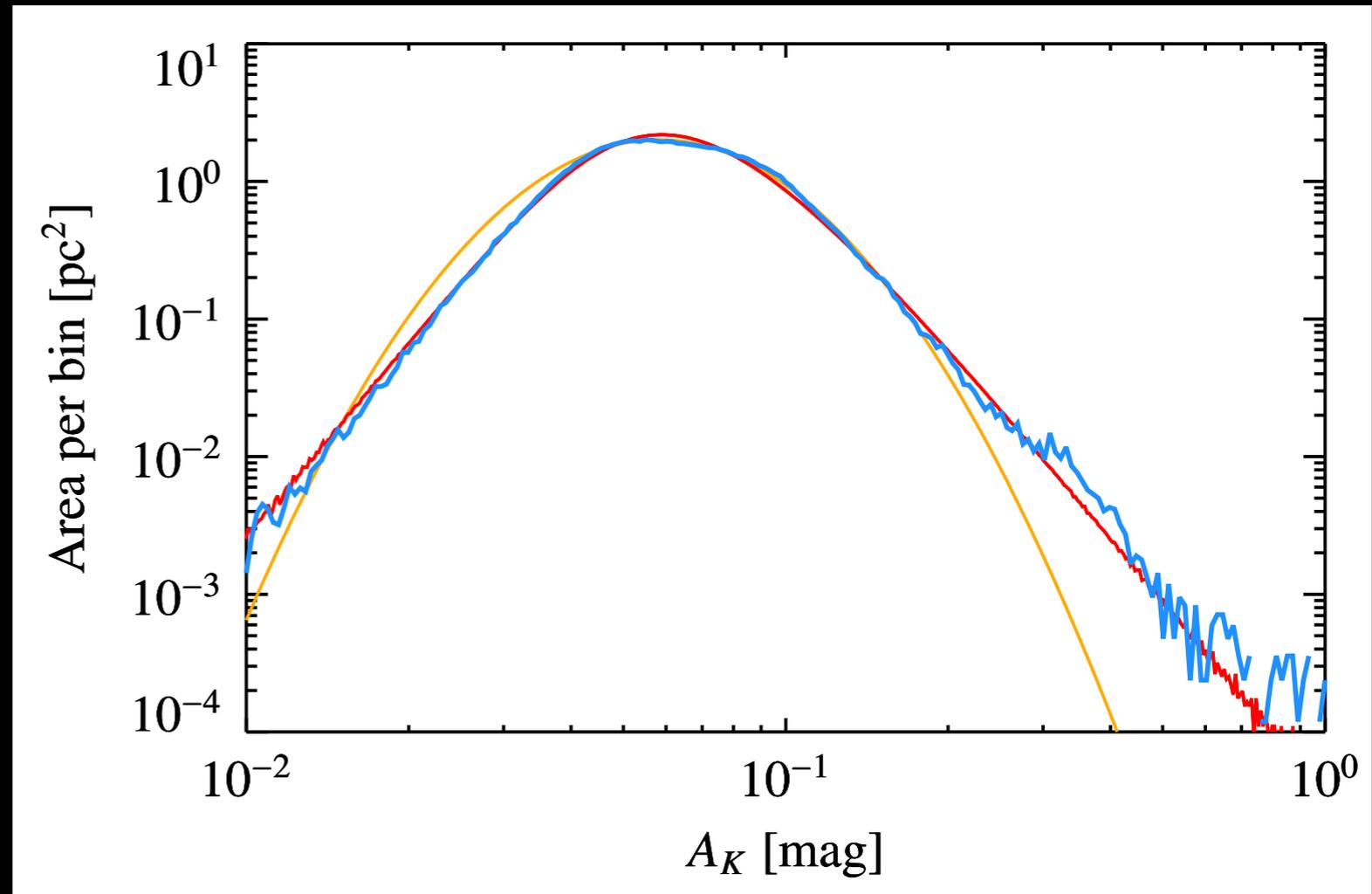
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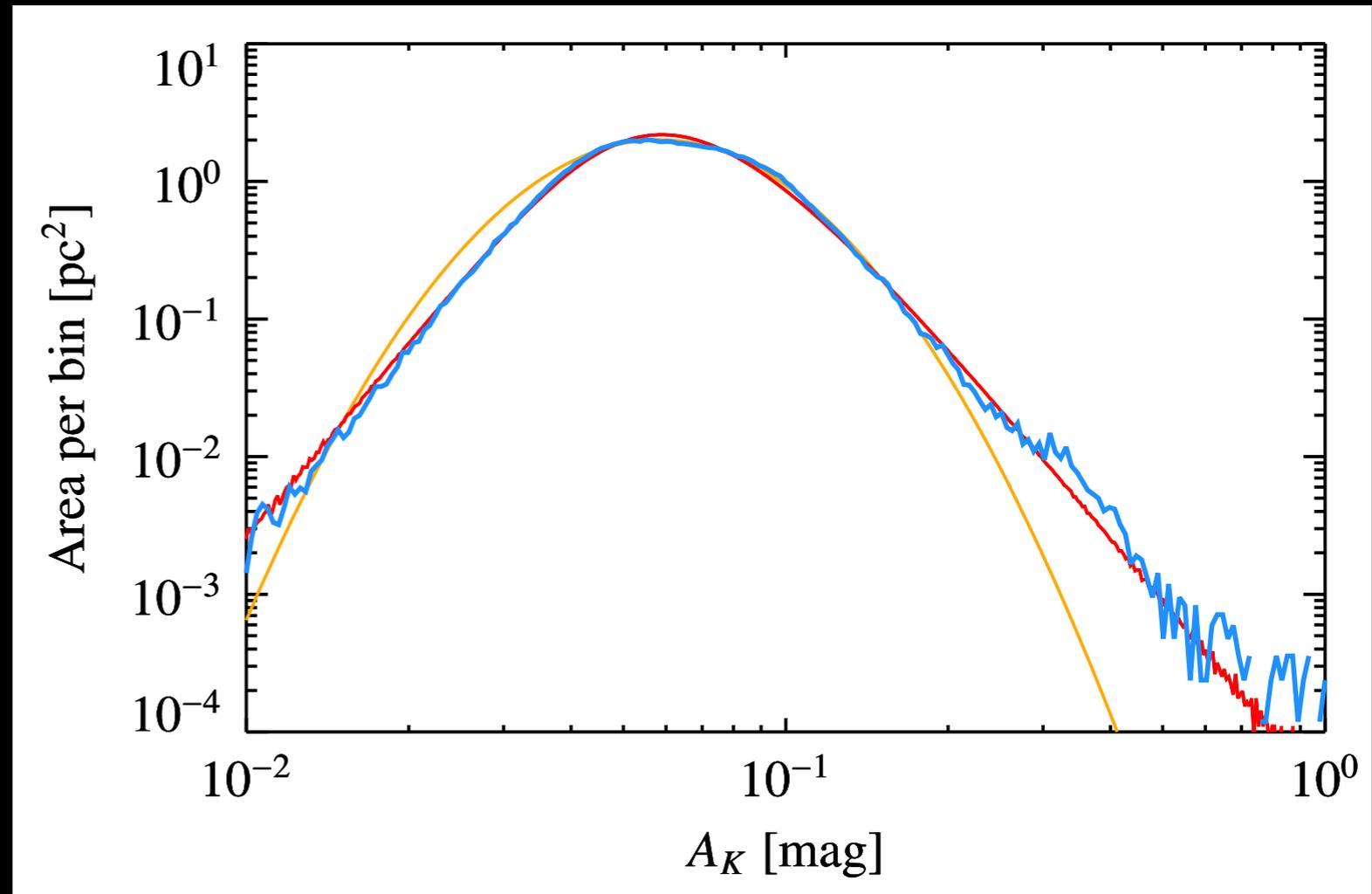
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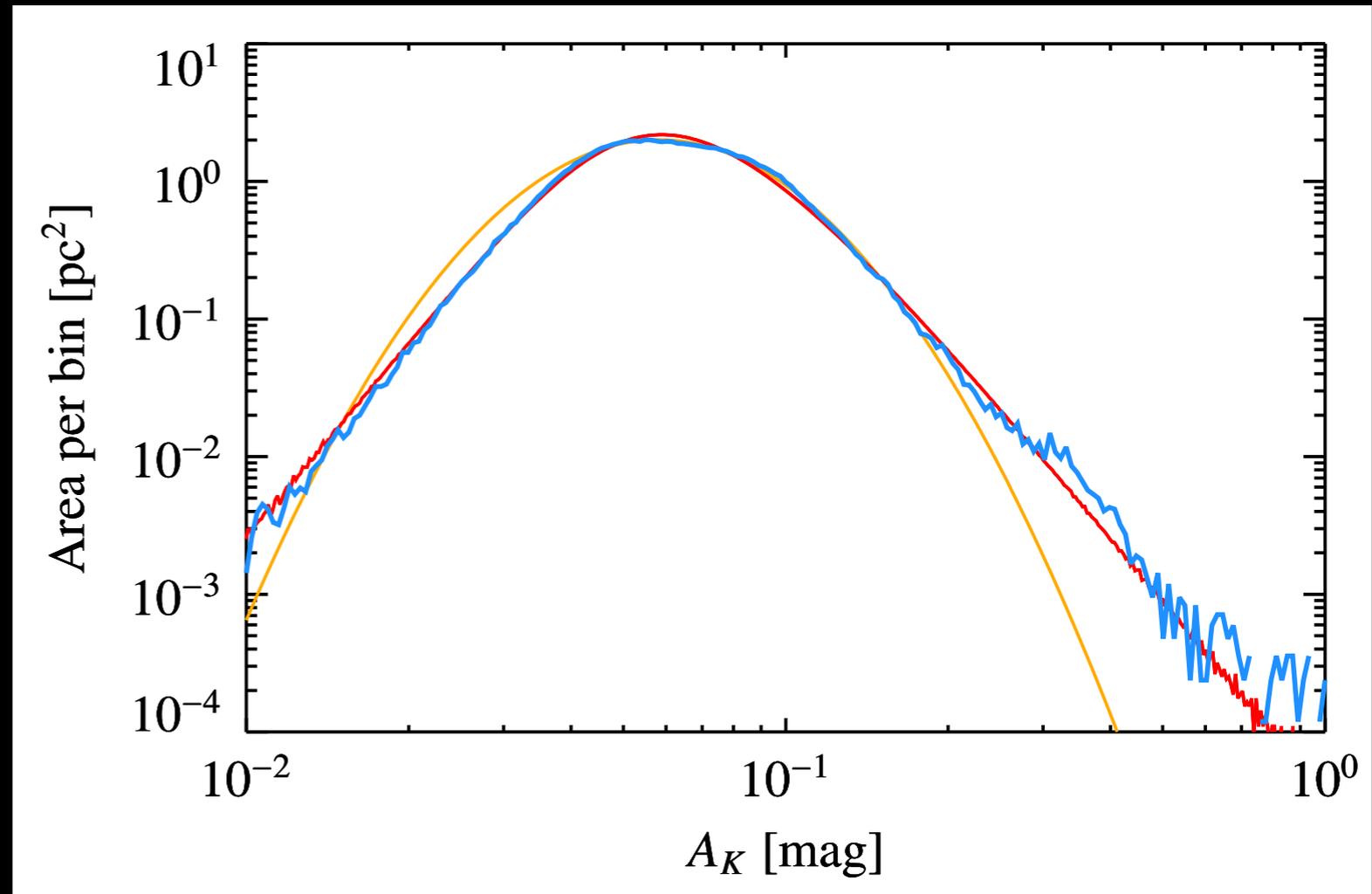
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- The associated PDF fits the measured one over 2 order of magnitudes!
- Caveat: ad-hoc model, but shows that log-normal is not that good



# The local Schmidt law

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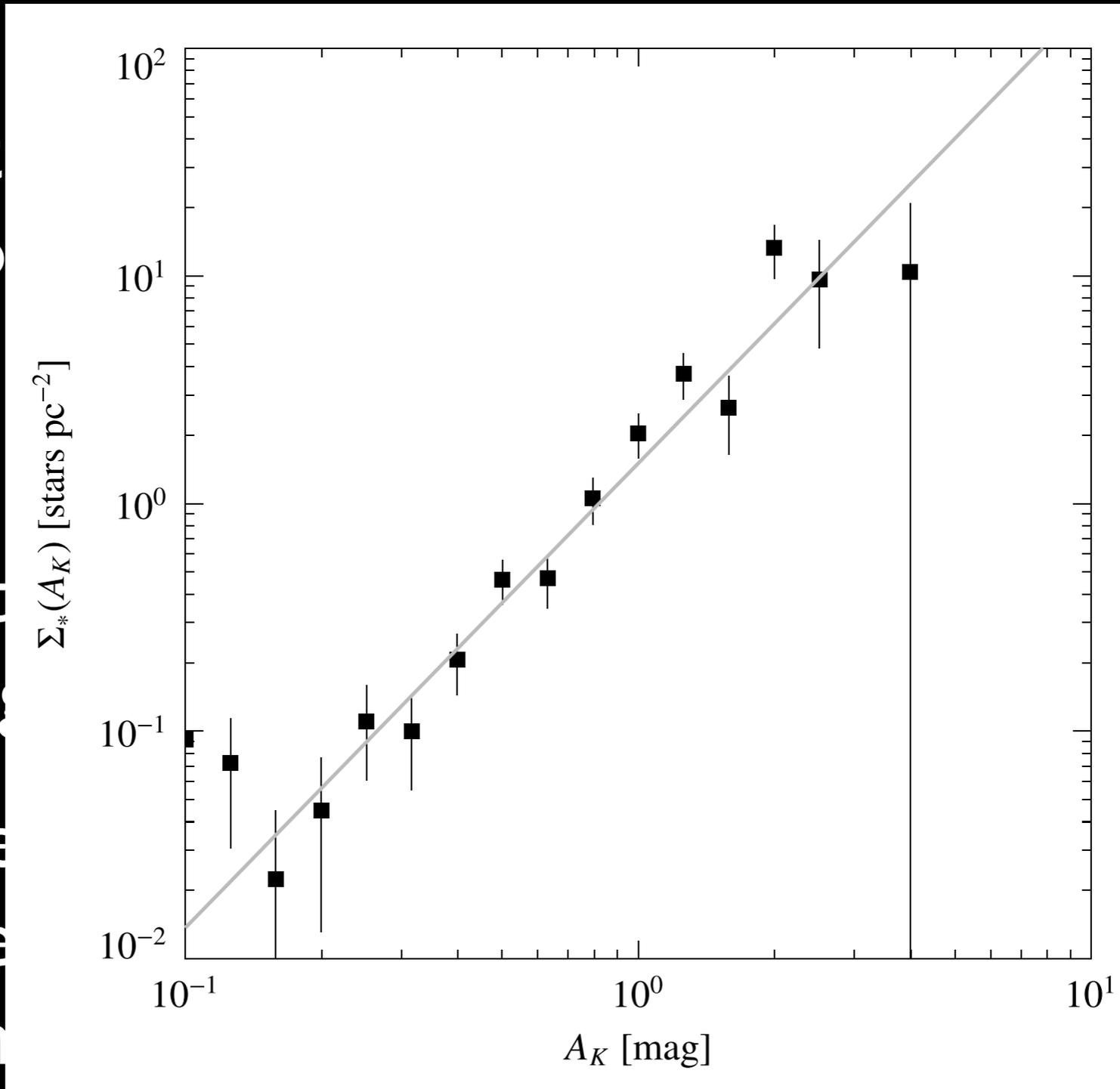
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- Both coefficients seem to have a limited range of variation
- The SFE of a cloud is ultimately linked to its internal structure and PDF (amount of dense gas)

# The local Schmidt law

- In the...
- Both...
- The...



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# SUMMARY

1. For 20 years we have screwed up the simplest characterization of cloud structure, the PDF... but we now know PDFs are power laws
2. Various other scaling laws hold (Larson's 3rd law, the local Schmidt law)
3. Large differences in the SFRs of molecular clouds are to be linked to their internal structure (slope of the PDF)

