

# WDM and Galaxy Formation

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## Outline

### “Ab Initio” Galaxy Formation in DM dominated Universe

- Power Spectrum
- Free Streaming Scale
- Connecting baryon physics to DM haloes: semi-analytic models

### Galaxy Formation in Cold Dark Matter:

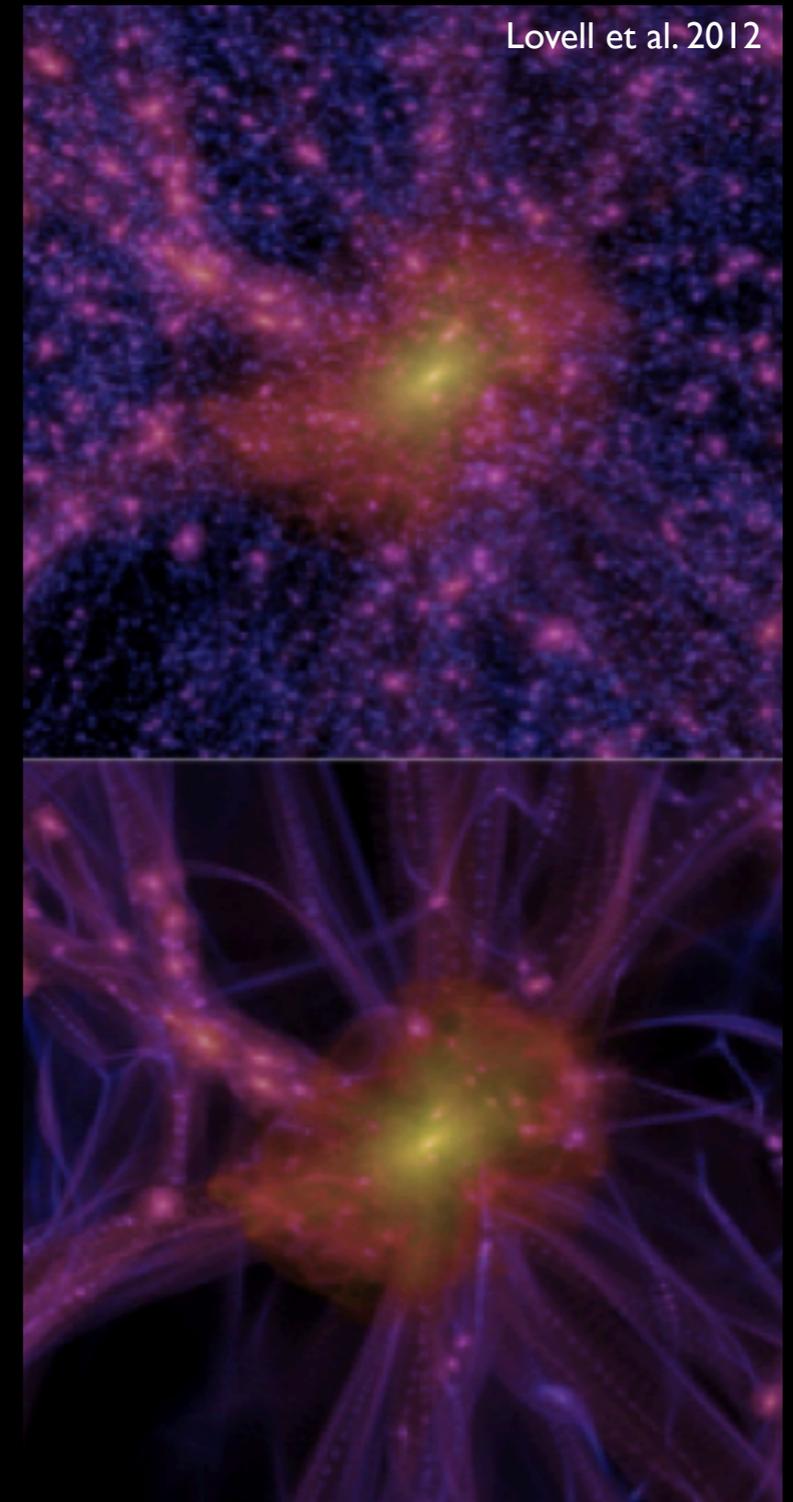
- Basic properties
- The small-scale crisis: Galaxies and AGN
- Feedback scale
- Is baryon physics a solution ?

### Galaxy Formation in Warm Dark Matter scenarios

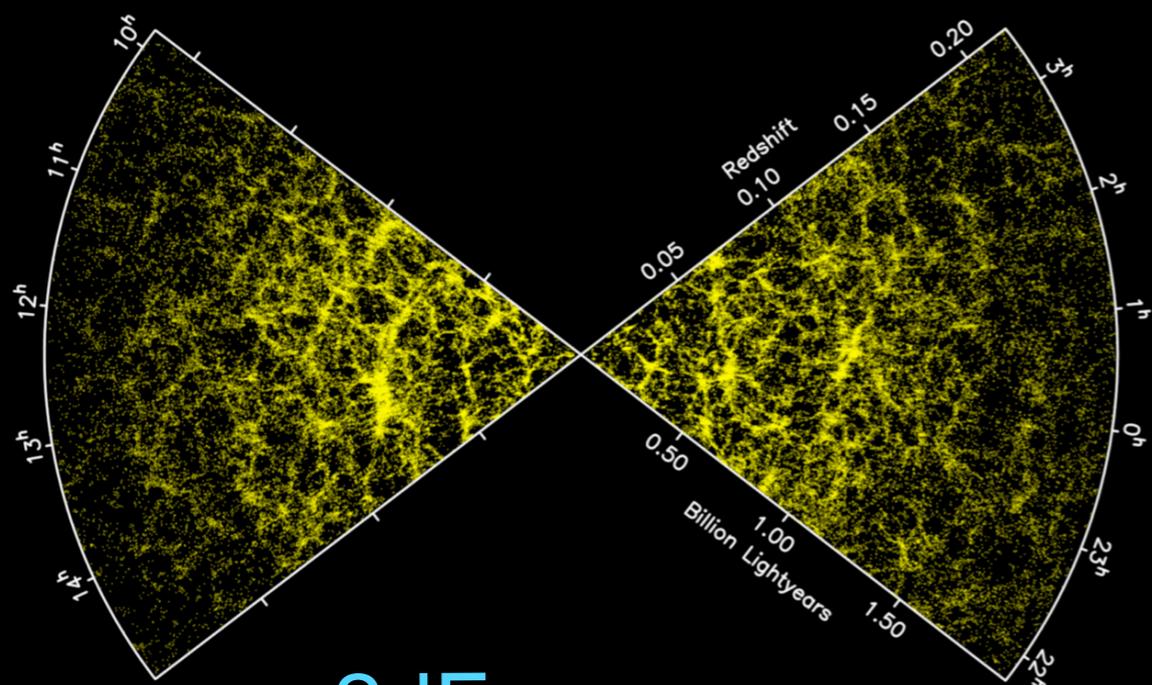
- Galaxy and AGN luminosity functions
- The luminosity function of satellites
- Hints from abundance matching: the  $V_{\max}$ - $M_*$  relation
- The star formation properties of satellites

### Limits to Warm Dark Matter candidate mass

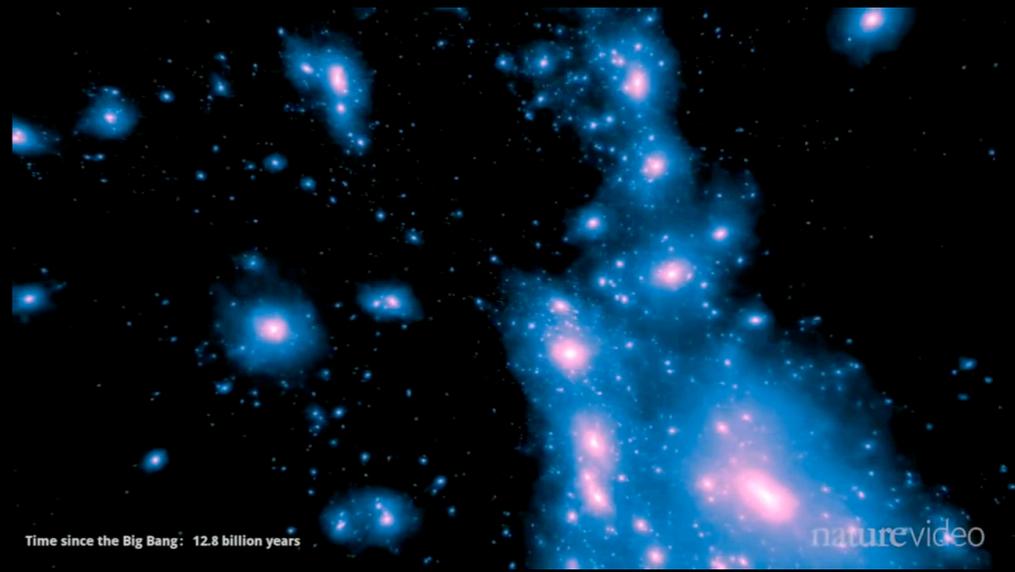
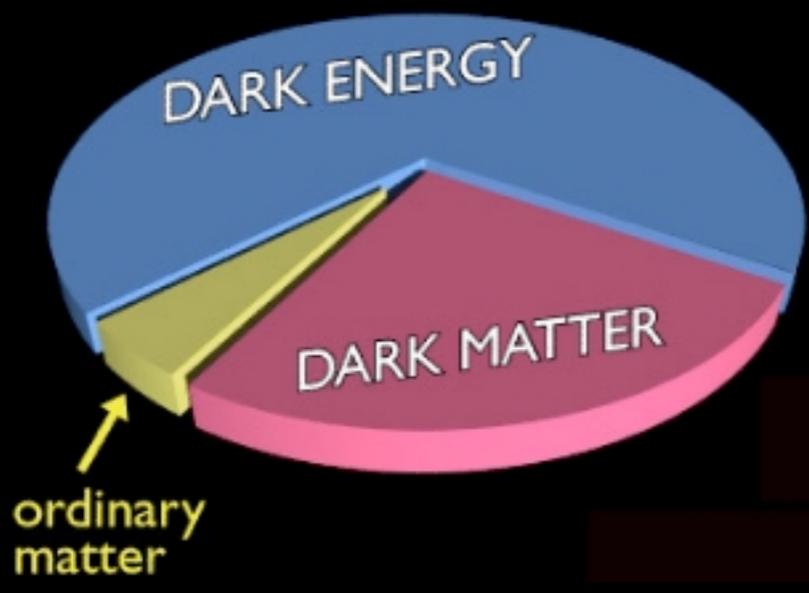
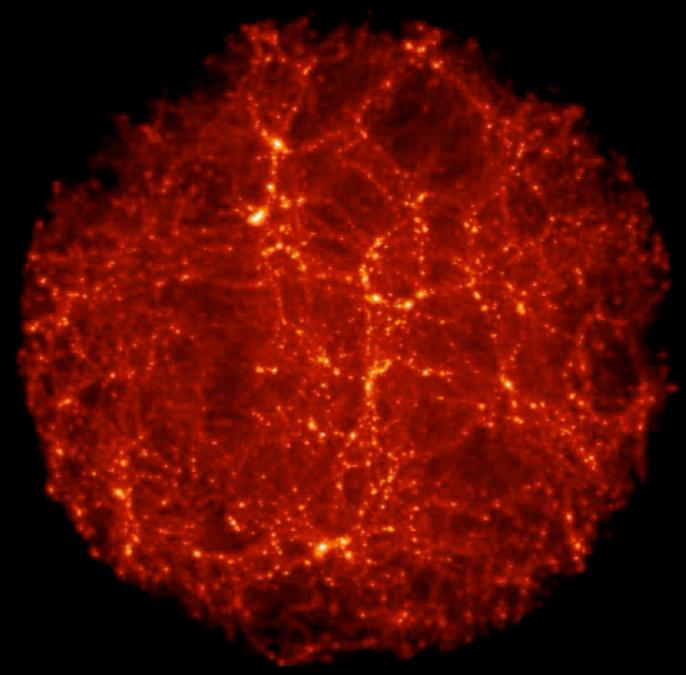
- High-redshift galaxy counts
- Luminosity function of ultra-faint galaxies at  $z=2$
- Dwarf galaxies in clusters down to  $M_{UV}=-10$



# Galaxies are the tip of the iceberg (underlying DM distribution)



2dF survey



Time since the Big Bang: 12.8 billion years

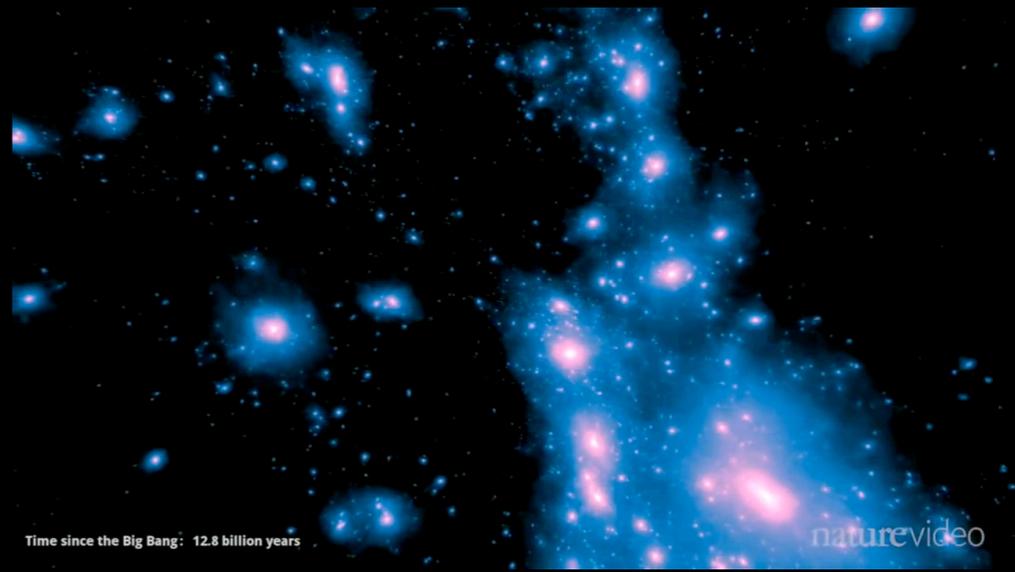
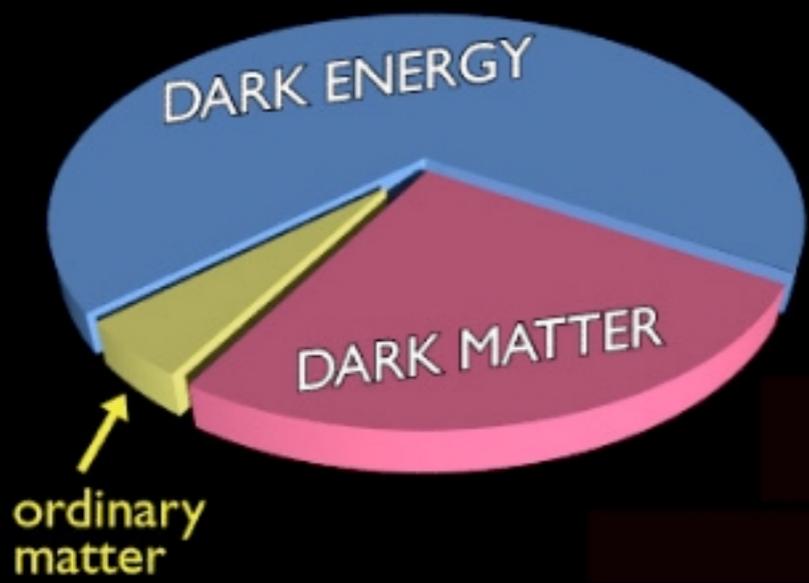
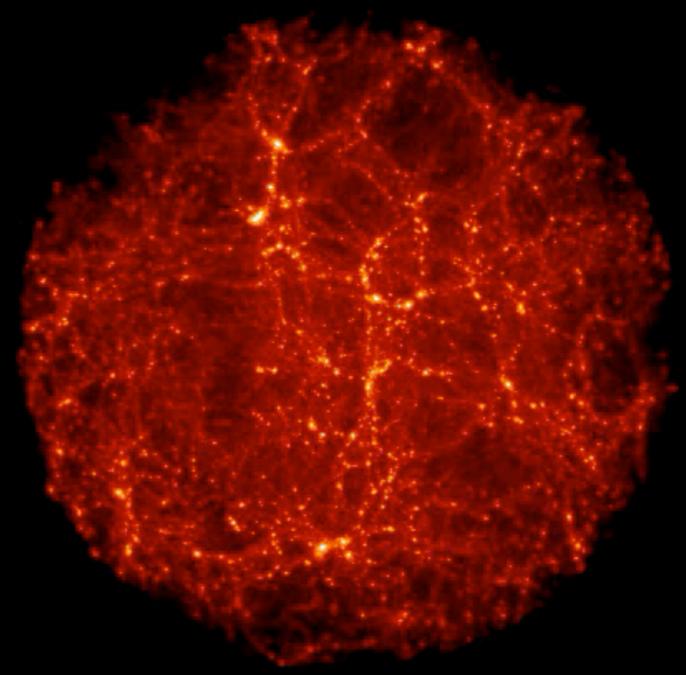
naturevideo

# Galaxies are the tip of the iceberg (underlying DM distribution)

## Galaxy Formation Theory

Describe the collapse and evolution of the DM clumps dominating the gravitational dynamics

Connect properties of ordinary matter (gas physics, star formation, astrophysical processes) to the potential wells of DM condensations



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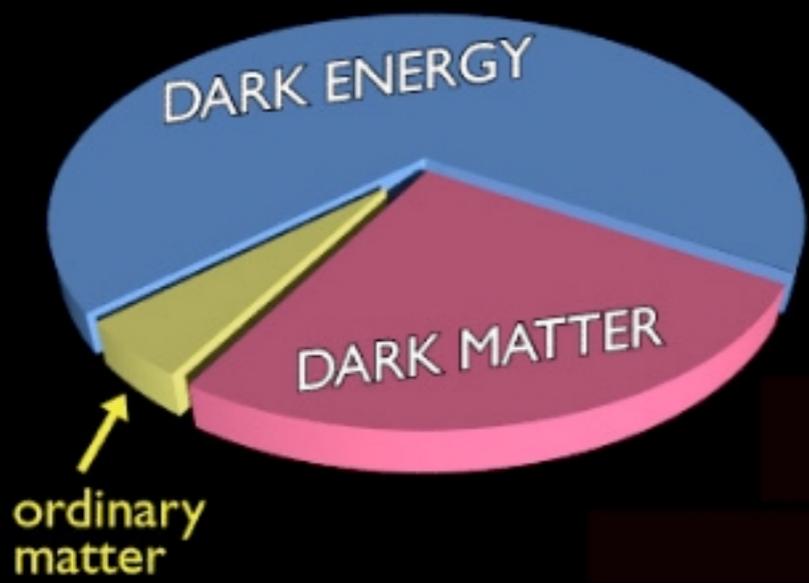
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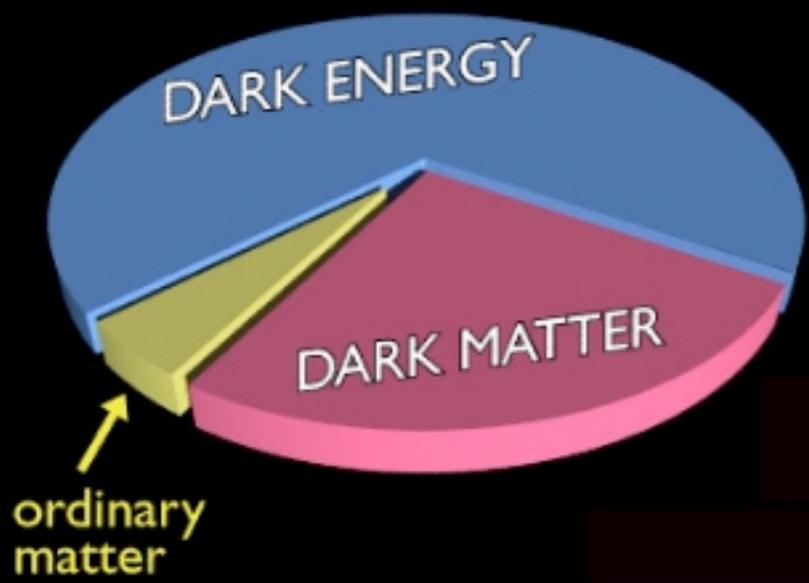
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Diemand et al. 2008

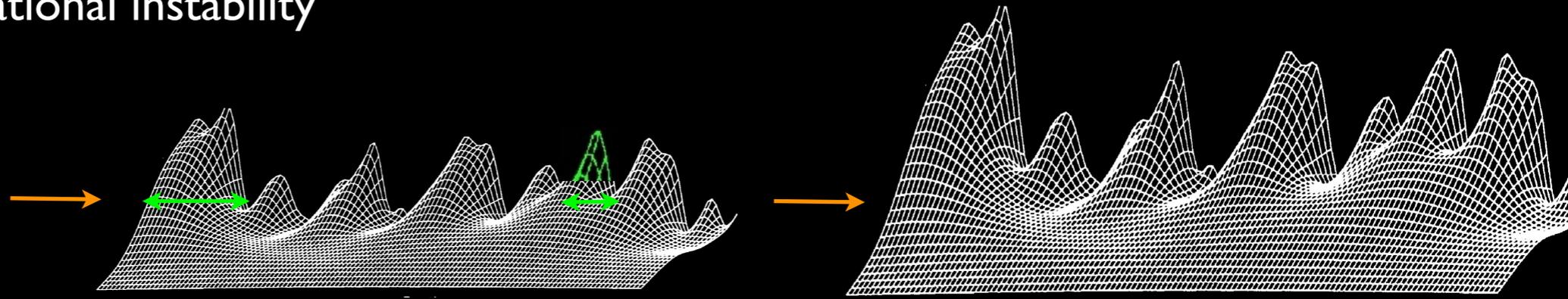
## Galaxy Formation Theory

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Connect properties of ordinary matter (gas physics, star formation, astrophysical processes) to the potential wells of DM condensations



Cosmic Structures form from the collapse of overdense regions in the DM primordial density field, and grow by gravitational instability



Gaussian Random field

$$\delta = \frac{\delta\rho}{\rho}$$

$$p(\delta_k) = \frac{1}{\sqrt{2\pi} \sigma_k} e^{-\frac{\delta_k^2}{2\sigma_k^2}}$$

$$R = 2\pi/k$$

$$M = \frac{4\pi}{3} \rho R^3$$

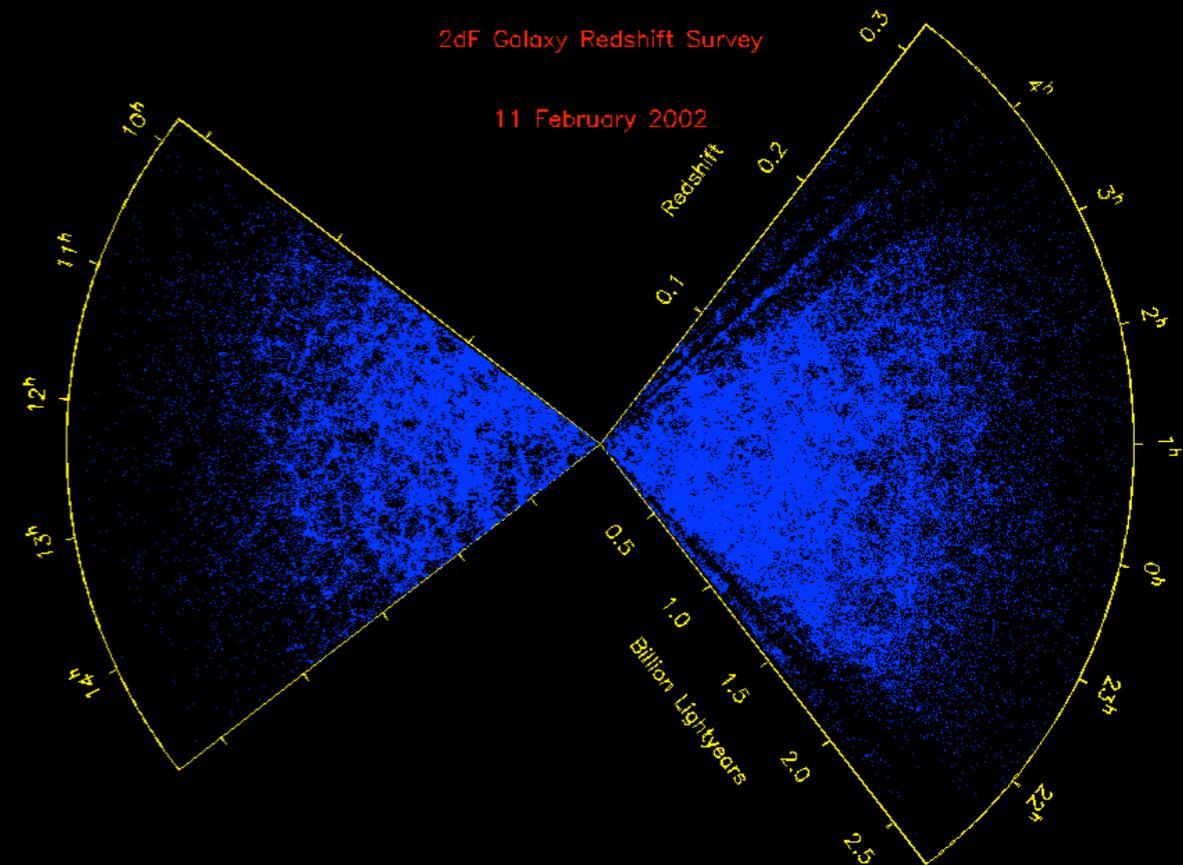
$$\langle \delta_M^2 \rangle = \sigma^2(M) g(t)$$

Mean (square) value of perturbations of size  $R(\sim 1/k)$  enclosing a mass  $M$

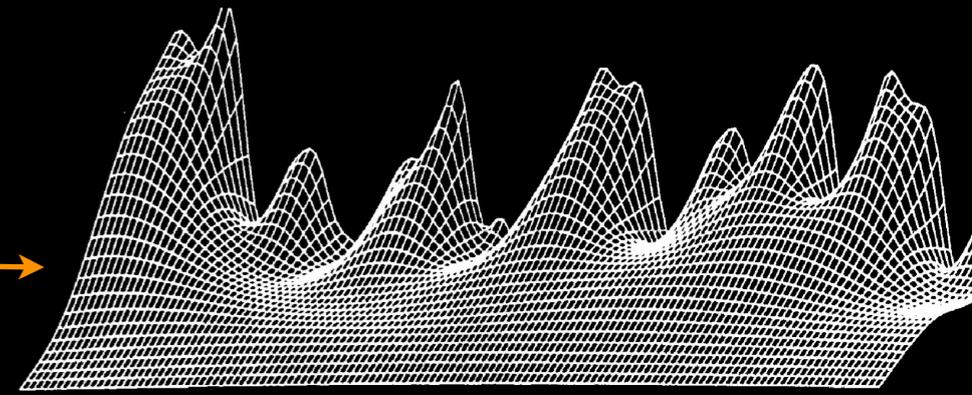
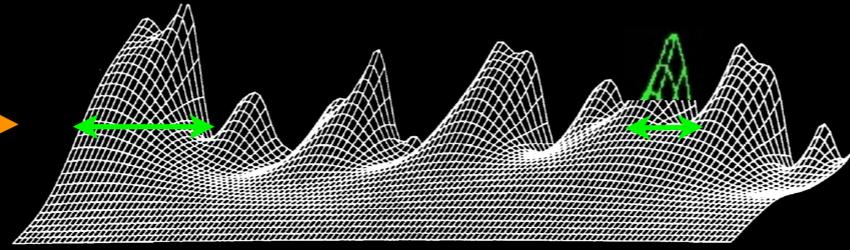
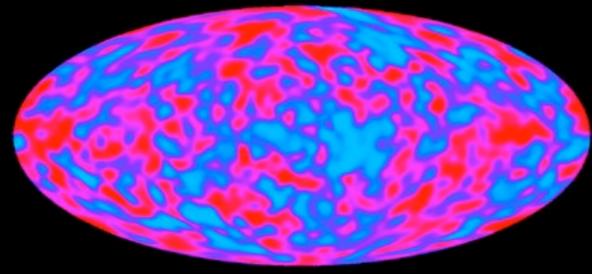
$$P(k) = \frac{1}{V} \langle |\delta_k|^2 \rangle$$

$$\sigma_M^2 = \frac{1}{(2\pi)^3 V} \int^{M \leftrightarrow k} dk k^2 P(k)$$

$$\sigma_M^2 \leftrightarrow P(k)$$



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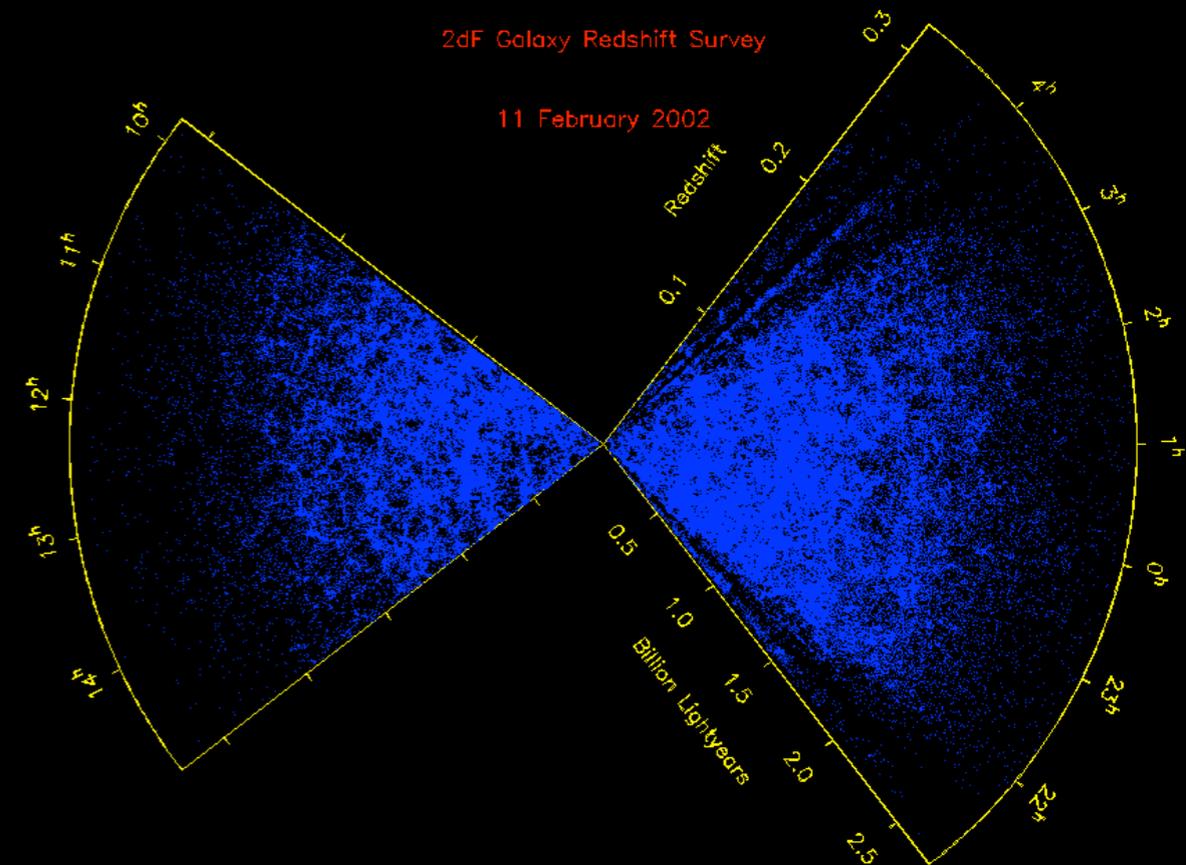


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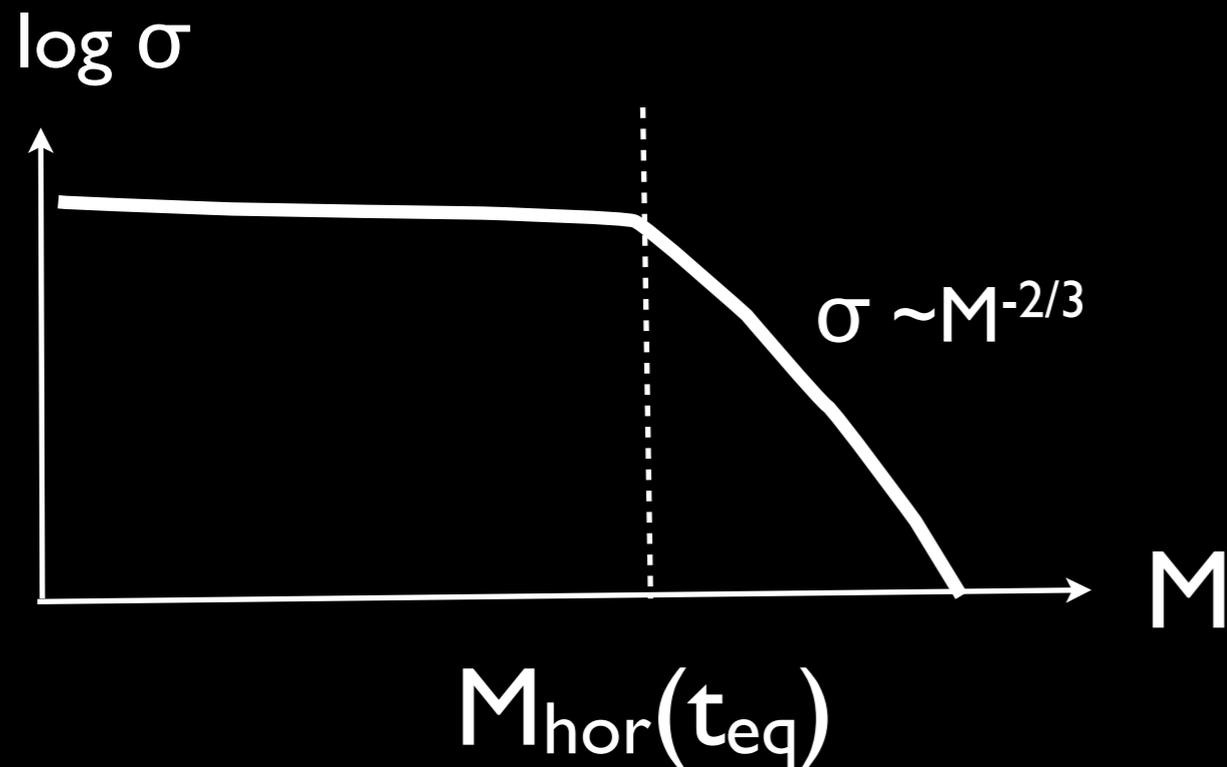
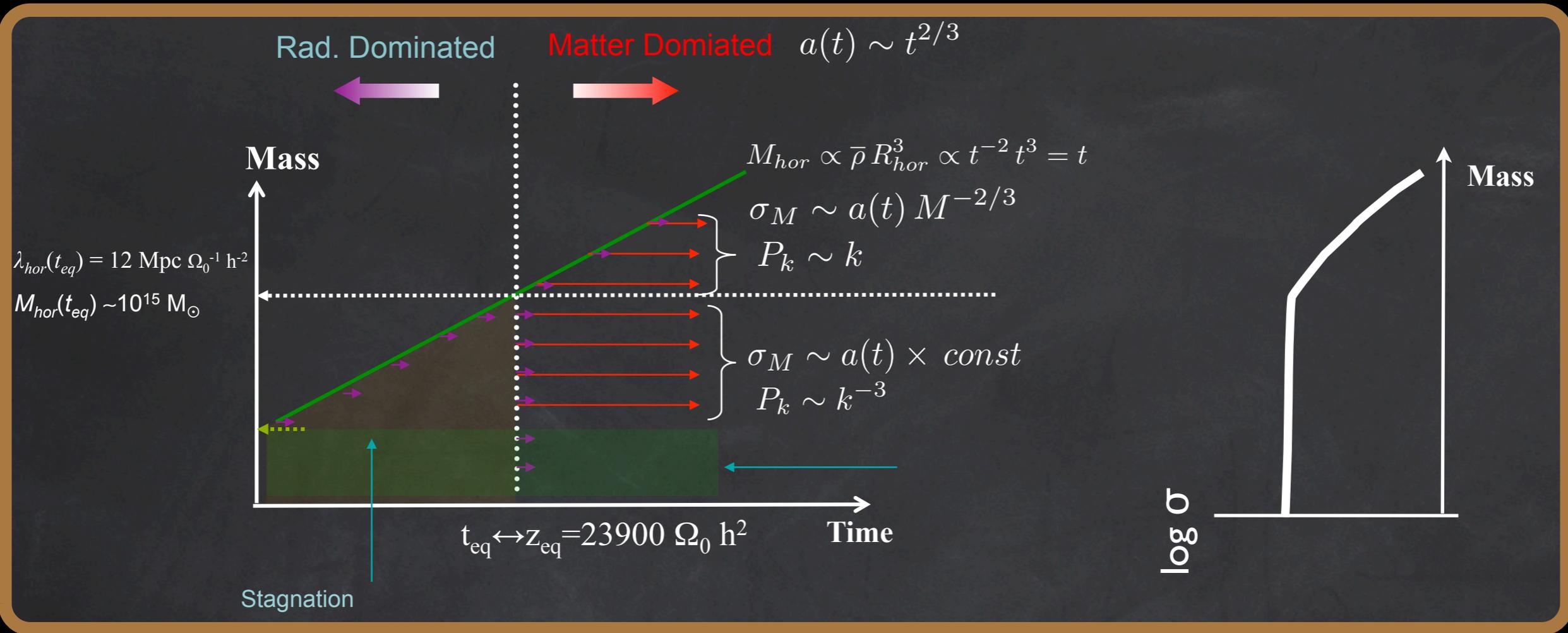
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# The Variance of the perturbation field



Perturbations involving scales larger than that of the horizon at the equivalence start to grow later

$$R_{hor} = 2c t_{hor} = 13 h^{-2} \text{ Mpc} = 110 \text{ Mpc for } \sigma_0 = 0.3 \text{ } h = 0.7$$

# In terms of wavenumber $k \rightarrow$ Power Spectrum

$$\sigma_M^2 = \frac{1}{(2\pi)^3 V} \int^{M \leftrightarrow k} dk k^2 P(k)$$

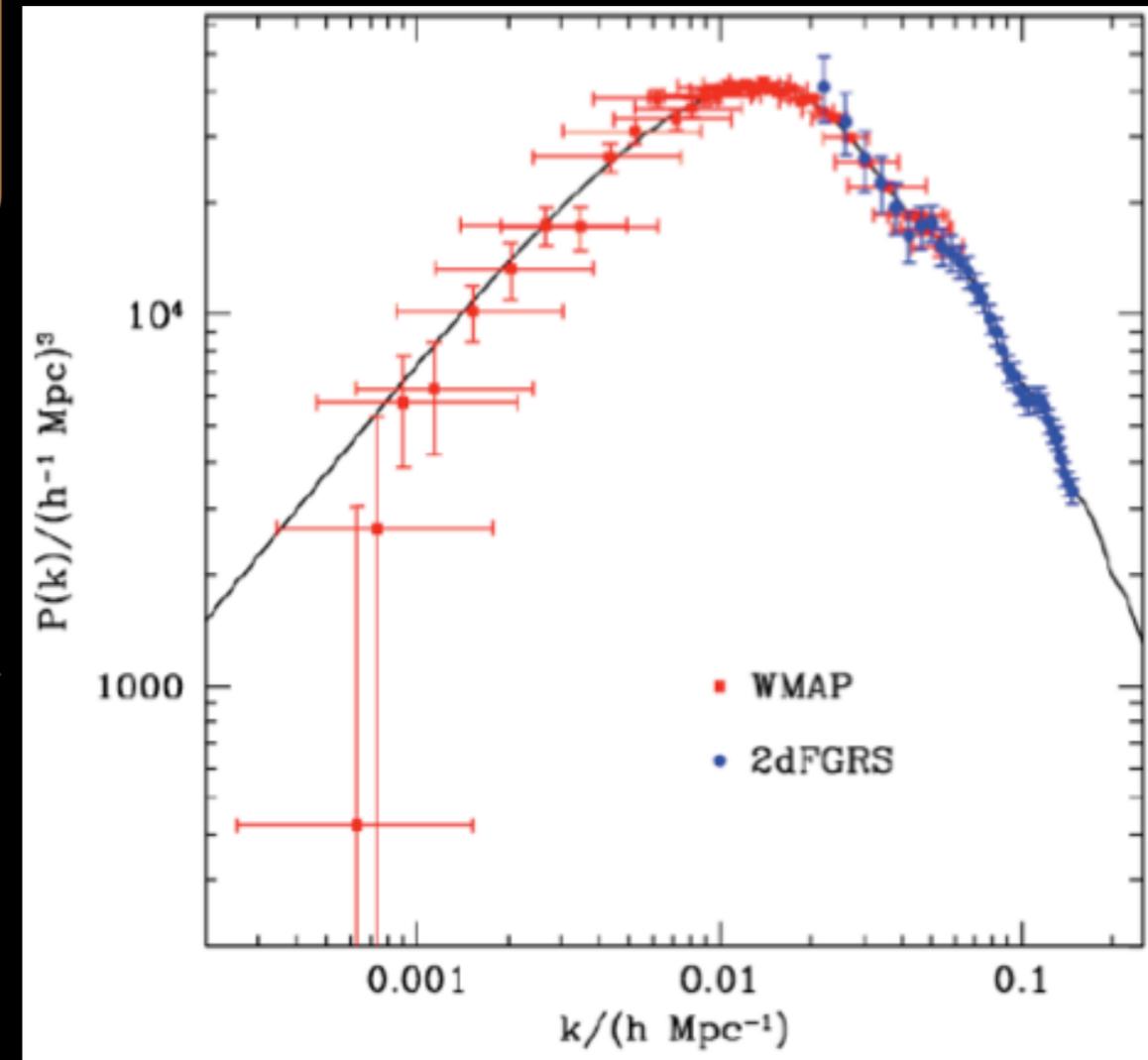
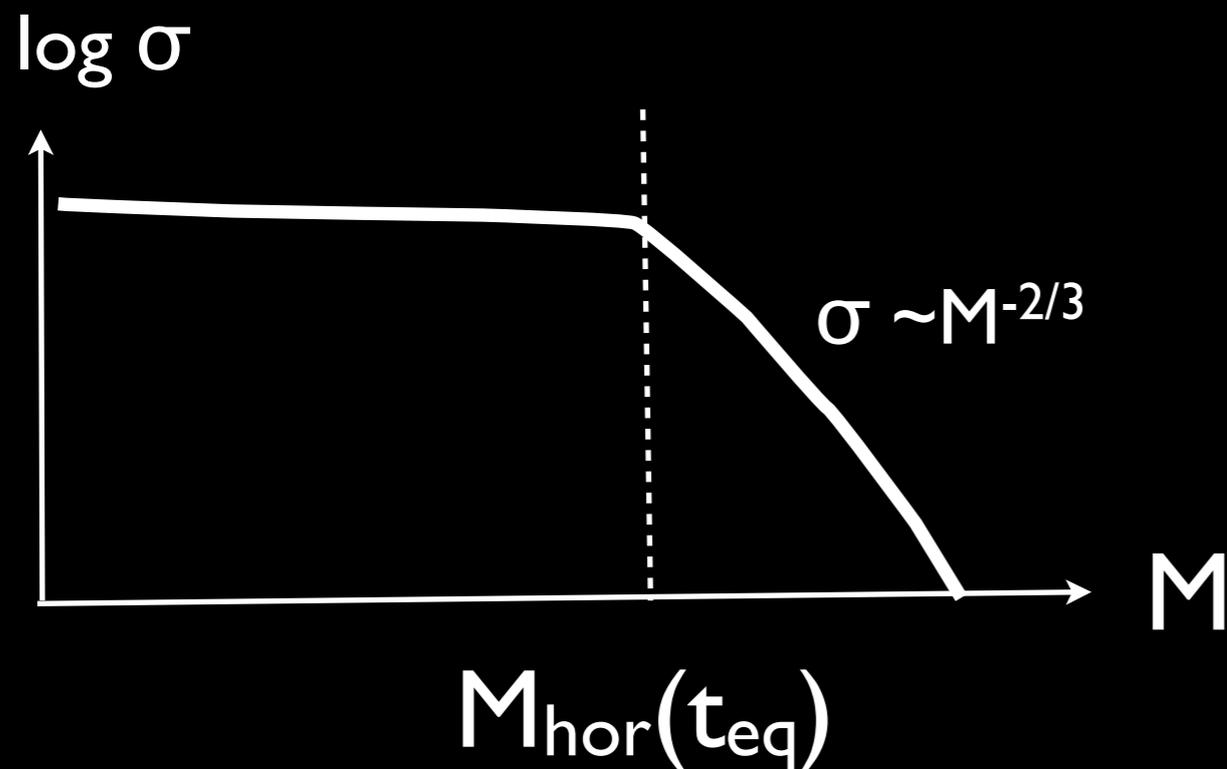
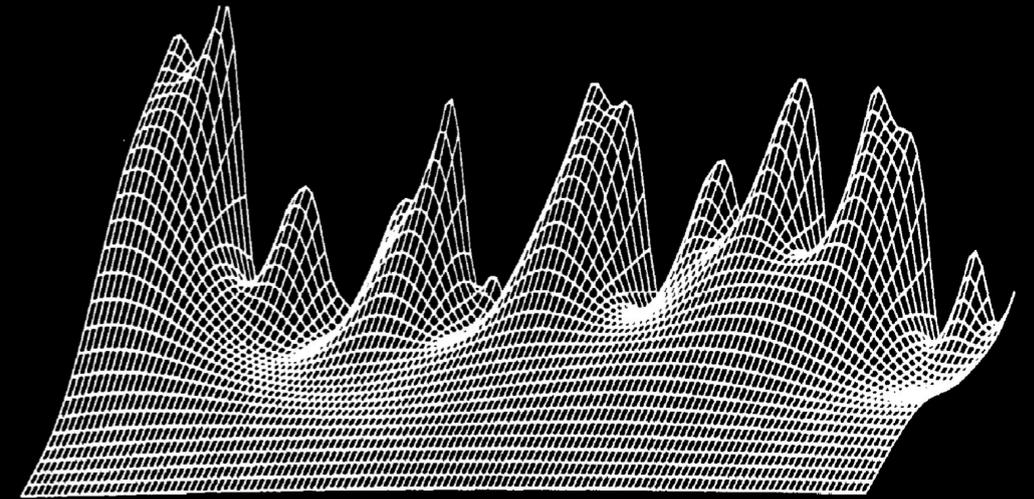
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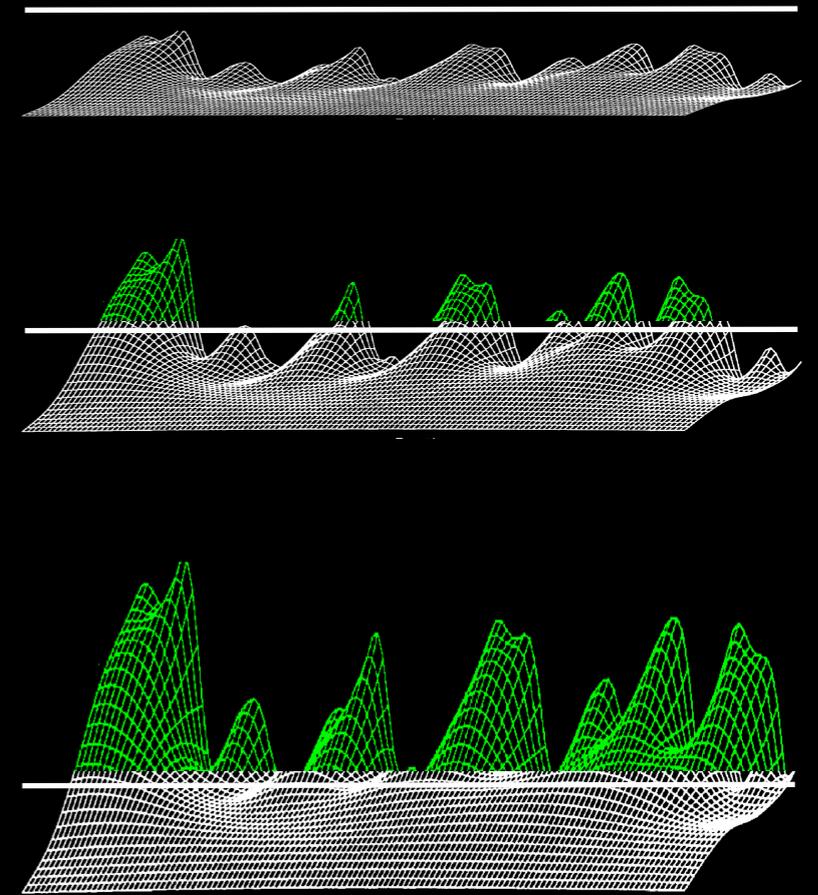
$$\sigma_M \propto M^{-2/3}$$

$$P(k) \propto k$$

$$\sigma_M = \text{const}$$

$$P(k) \propto k^{-3}$$



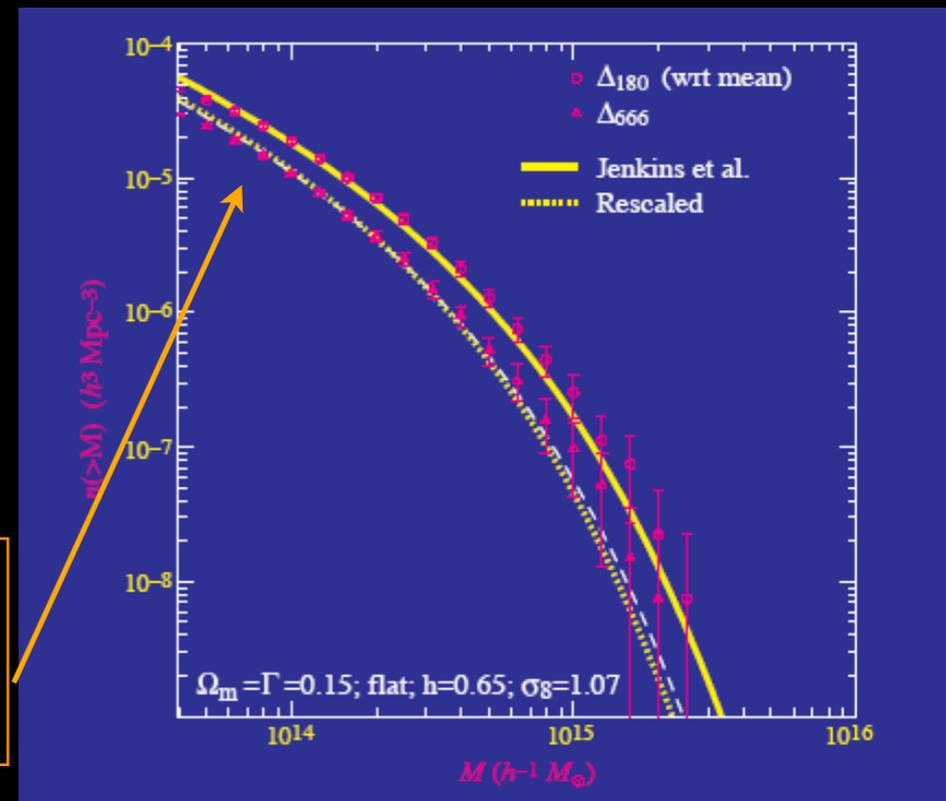


Mass Function: counting the peaks over collapse threshold  $\delta_c$

$$N(M)M dM = \bar{\rho} \frac{d}{dM} \left[ \int_{\delta_c}^{\infty} d\delta \frac{1}{\sqrt{2\pi} \sigma(M,t)} e^{-\frac{\delta^2}{2\sigma^2(M,t)}} \right]$$

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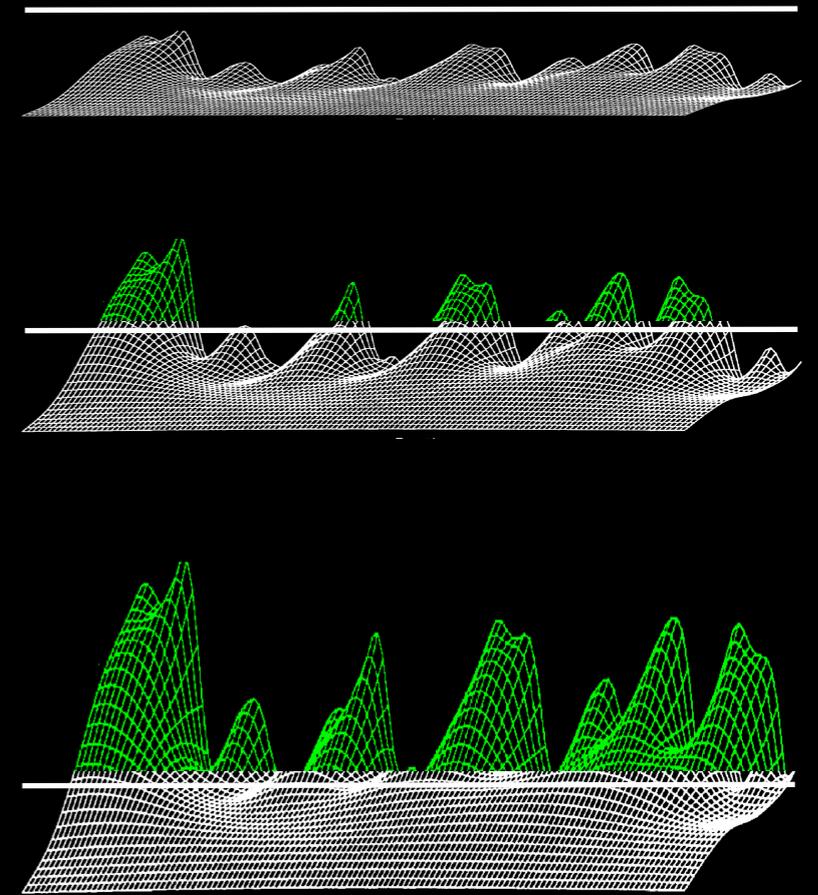
Press & Schechter 1974  
Steep Log Slope at  
low masses



$z = 48.4$

$T = 0.05 \text{ Gyr}$

500 kpc

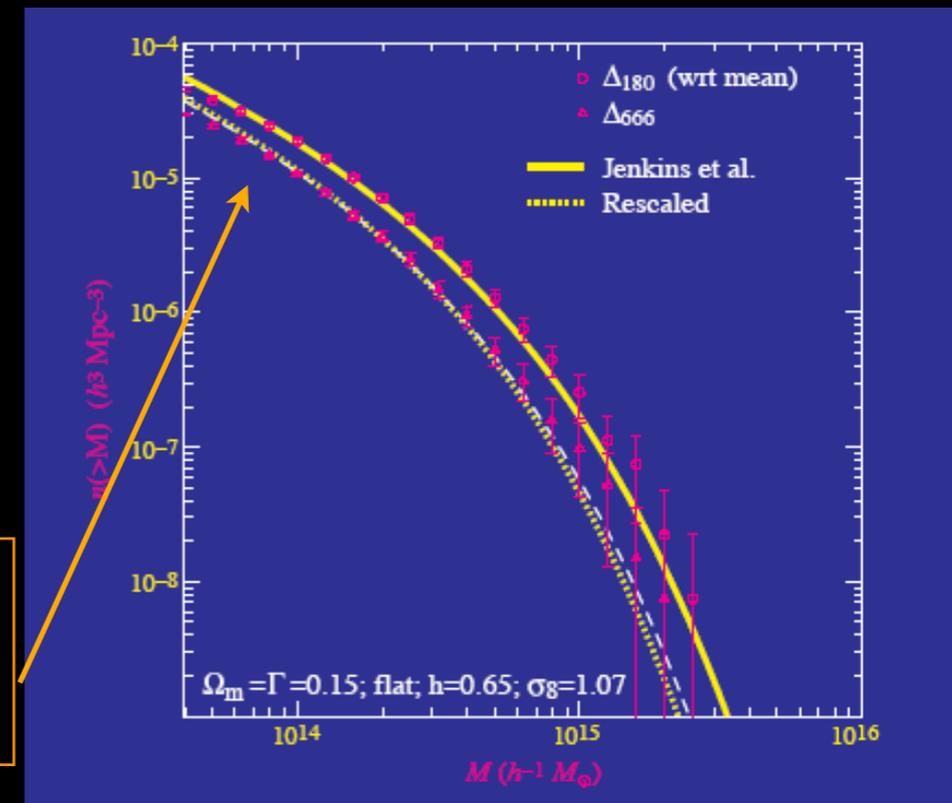


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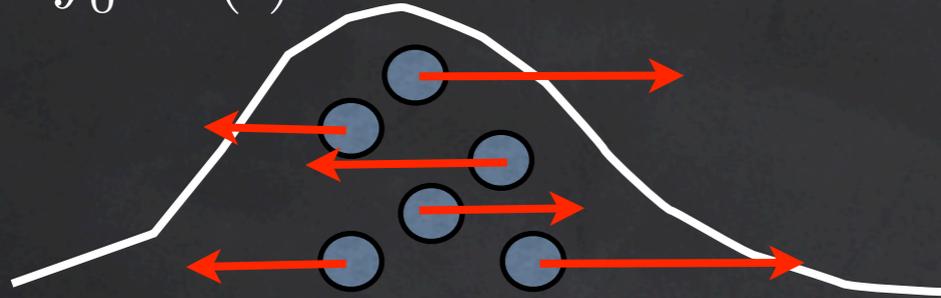
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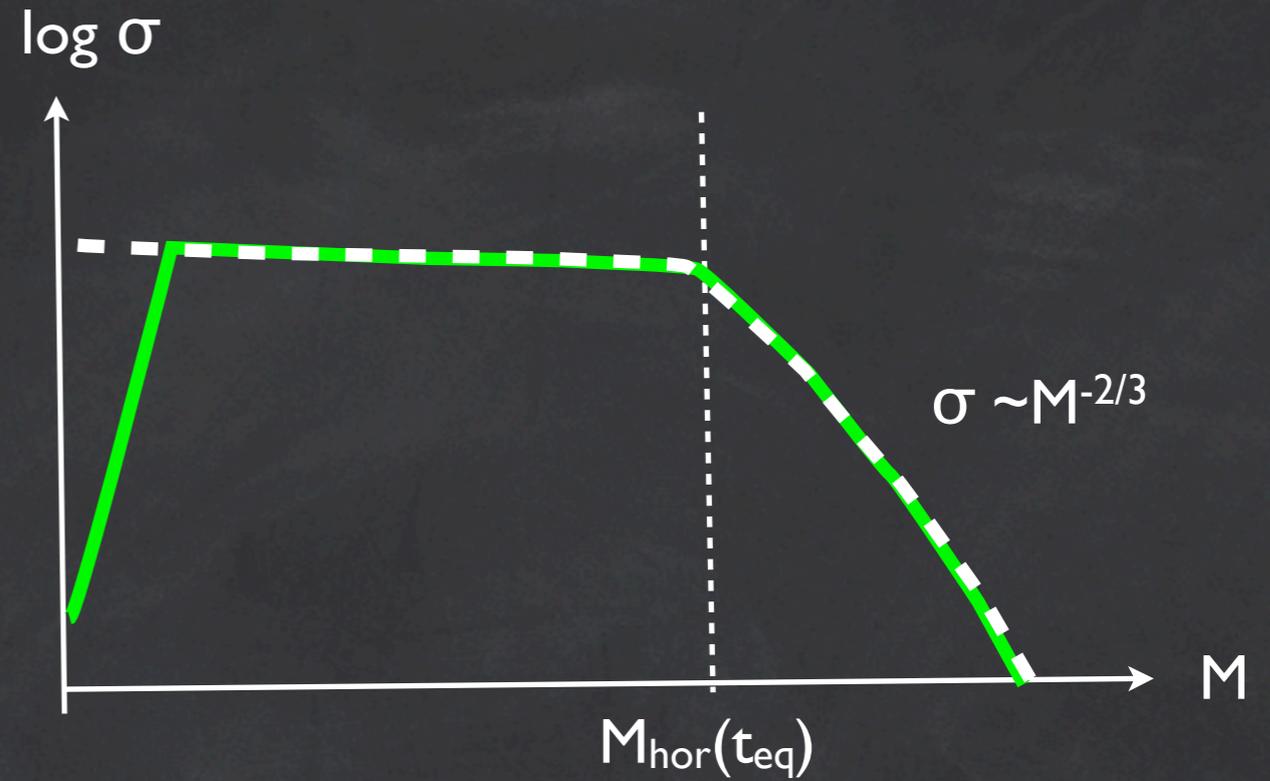
# Dissipation, free-streaming scale

$$r_{fs} = \int_0^t \frac{v(t)}{R(t)}$$

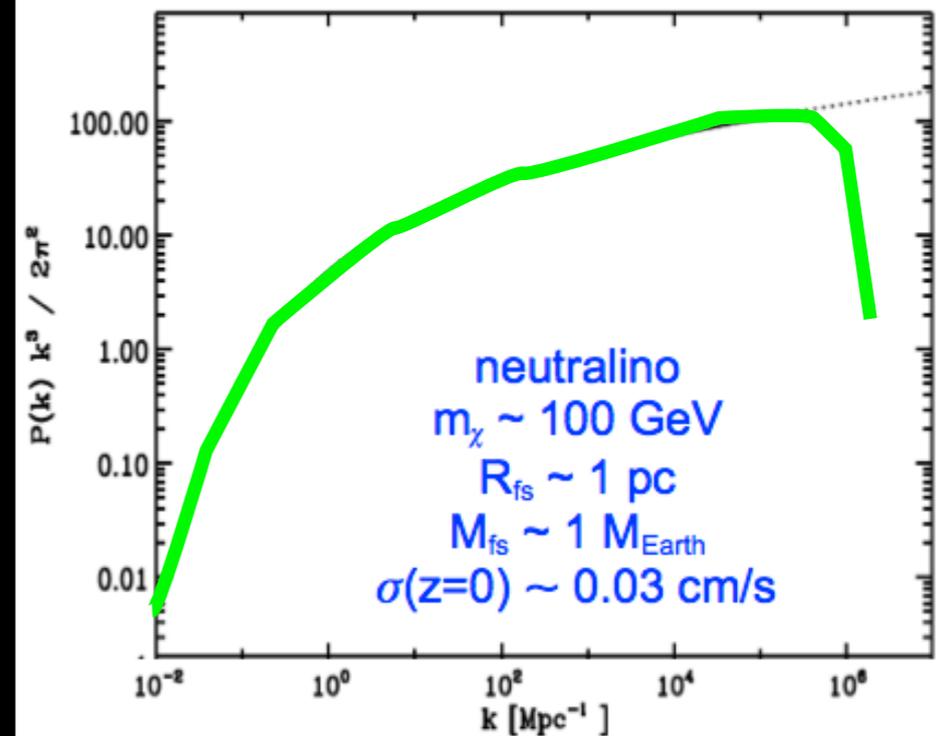


$$\sigma_\chi \propto a^{-1} m_\chi^{-1/2}$$

$$M_{fs} = 4 \times 10^{15} \left( \frac{m_\nu}{30 \text{ eV}} \right)^{-2} M_\odot$$

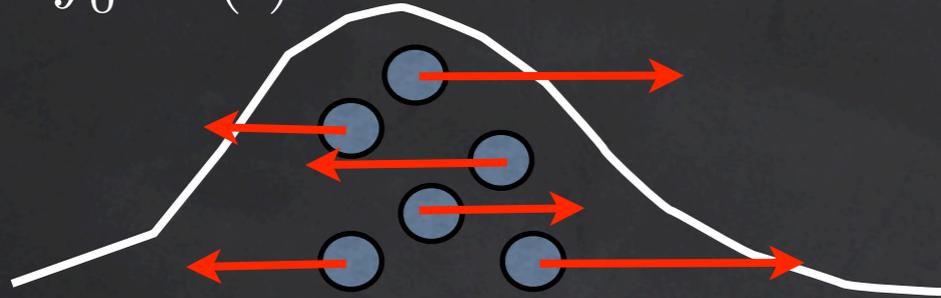


Angulo & White, 2010



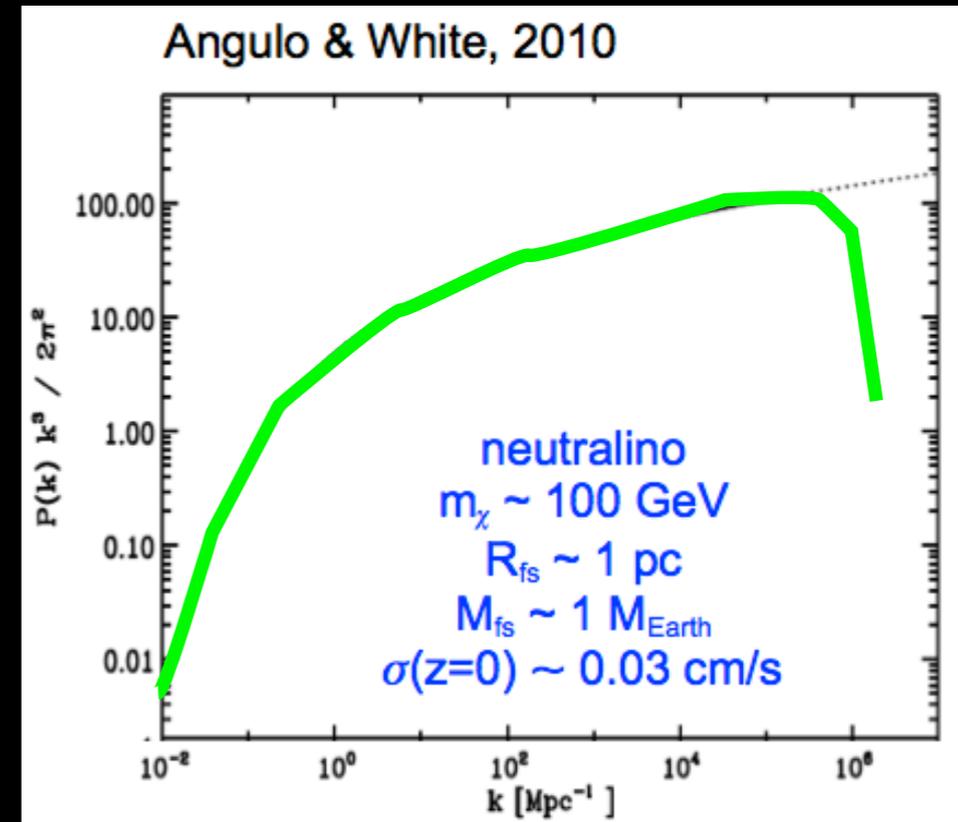
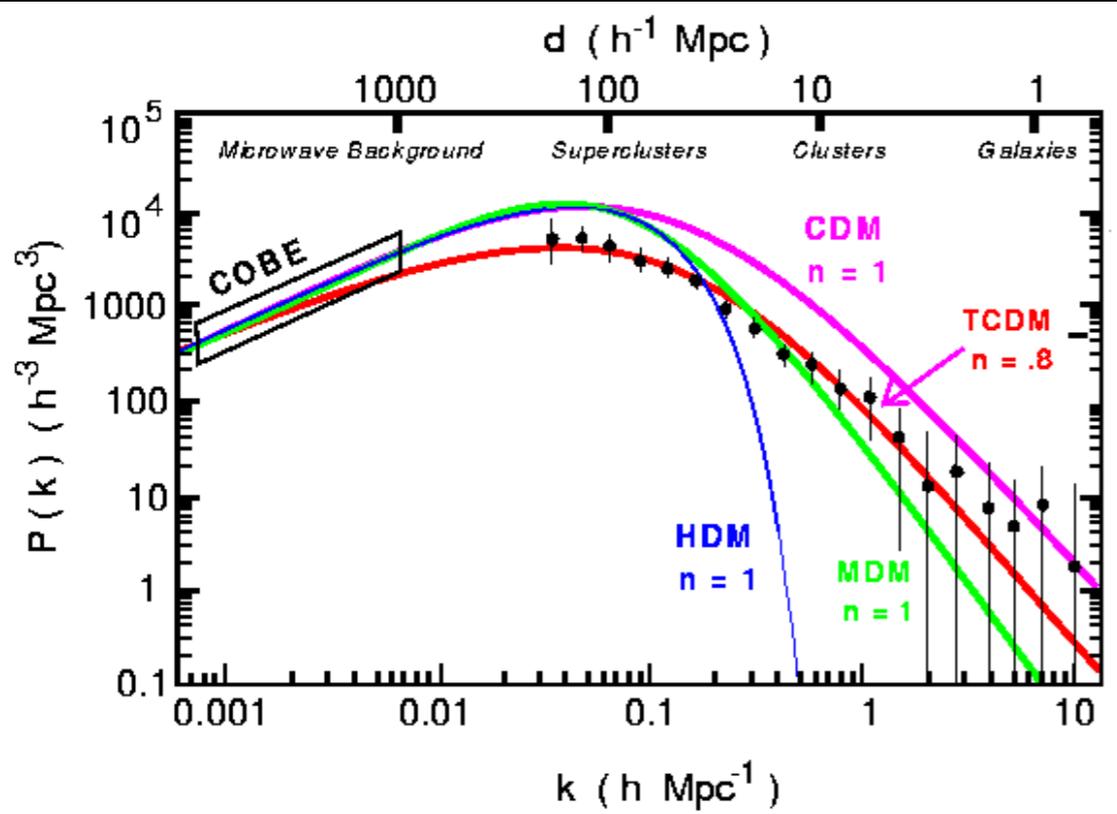
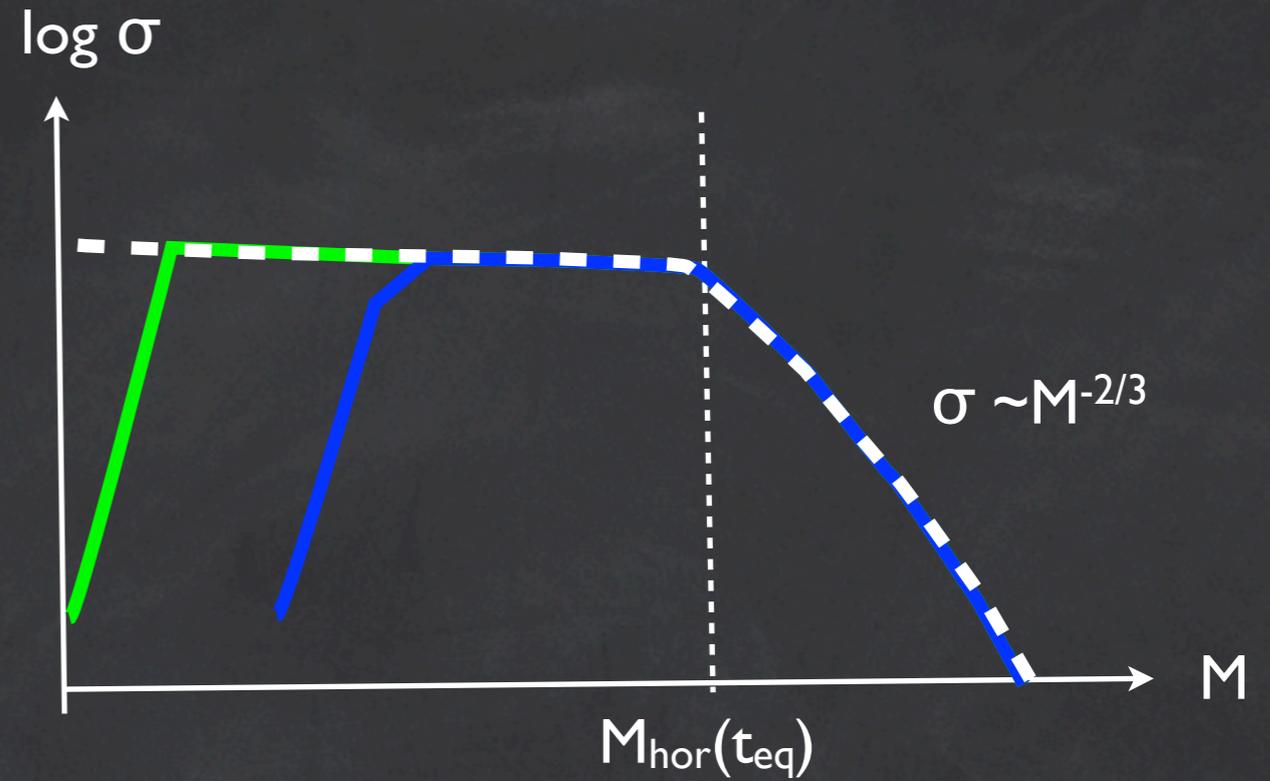
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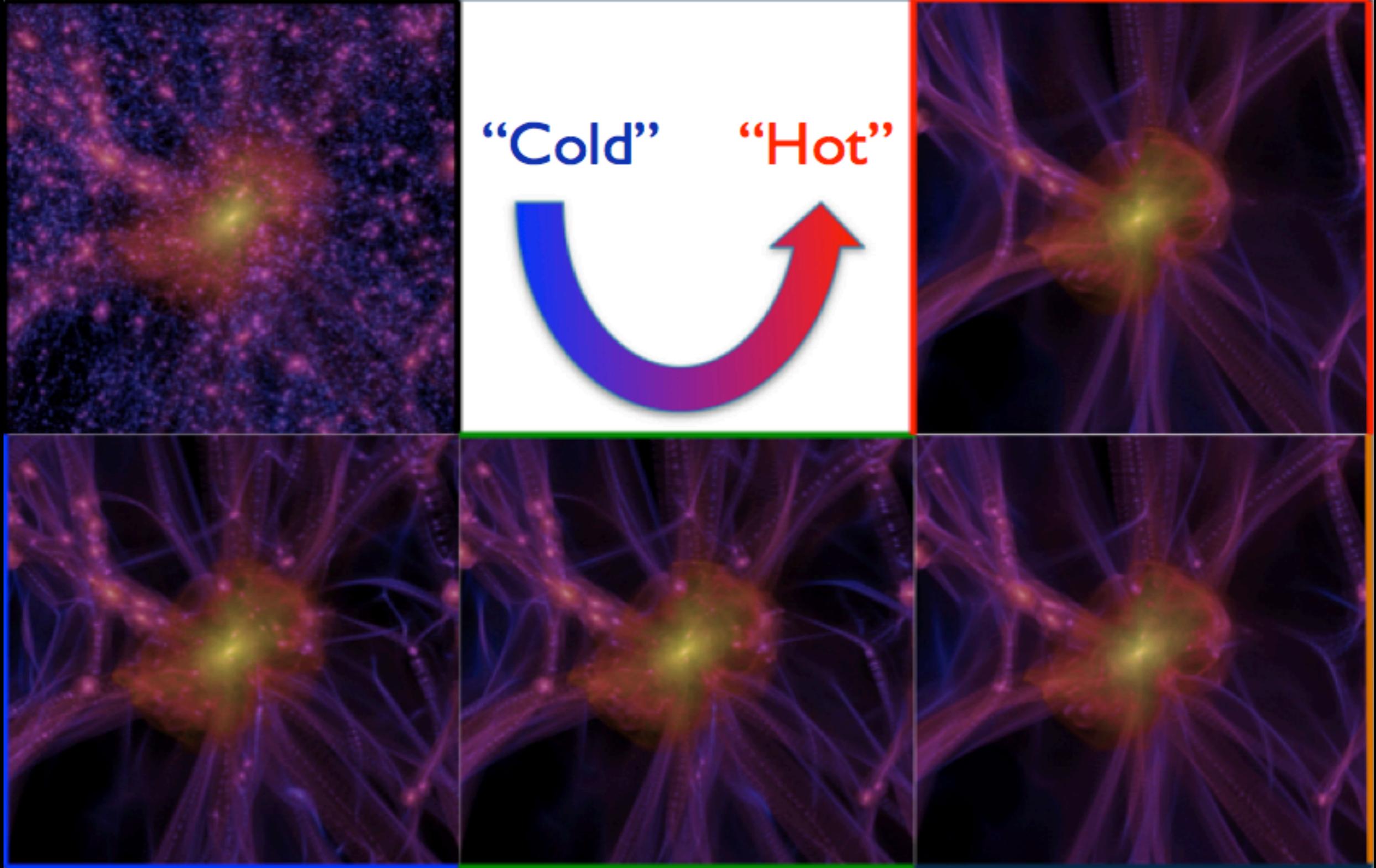


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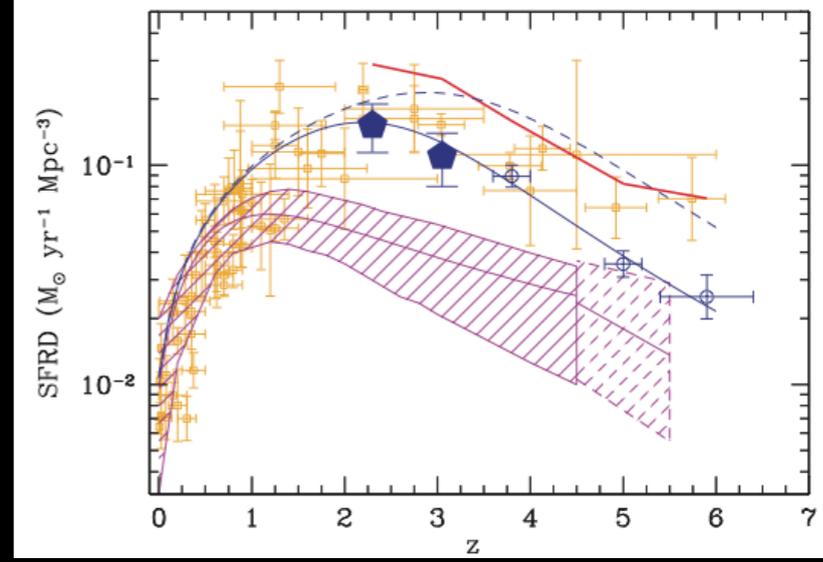
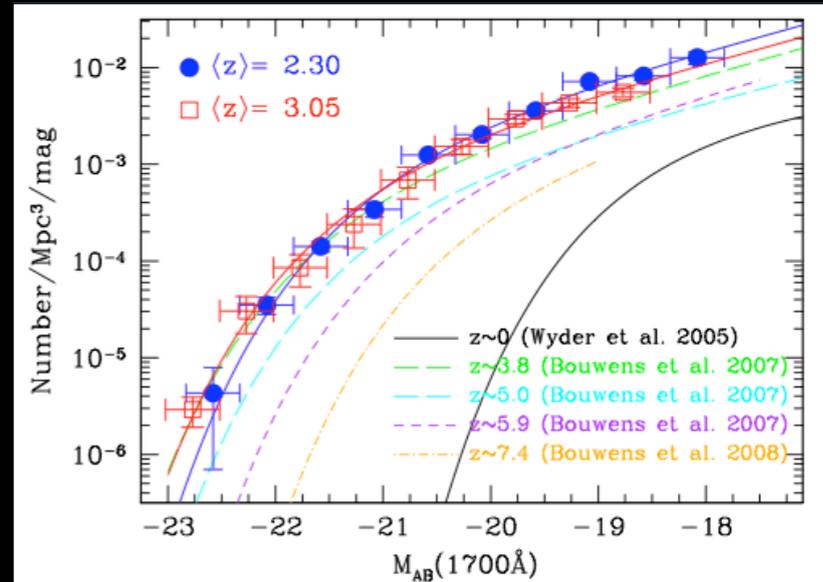
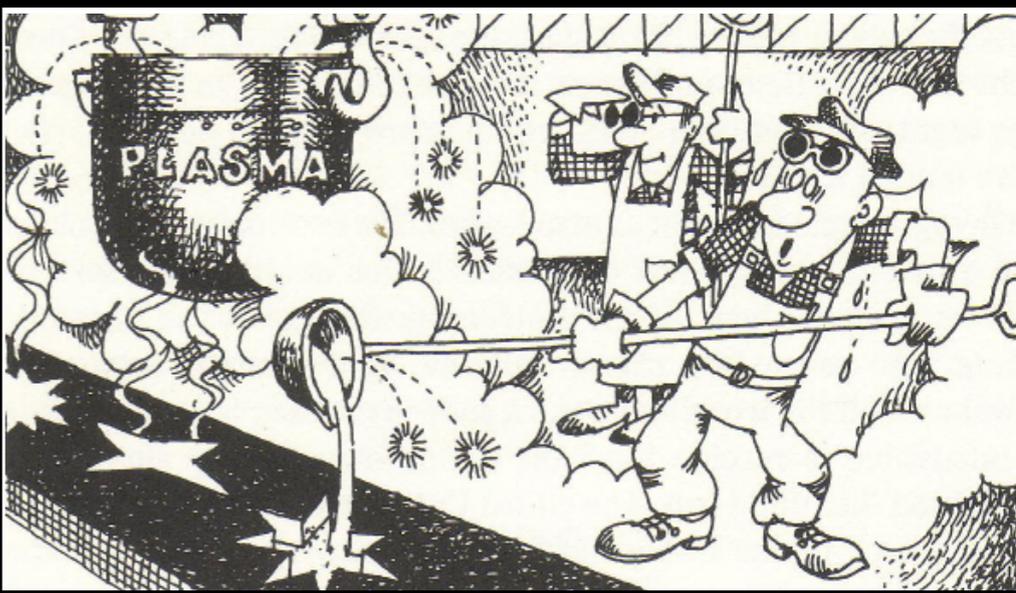
# Varying the particle mass



# Testing the DARK MATTER scenarios against observations: the evolution of galaxies

Requires modelling of baryon physics inside evolving DM potential wells

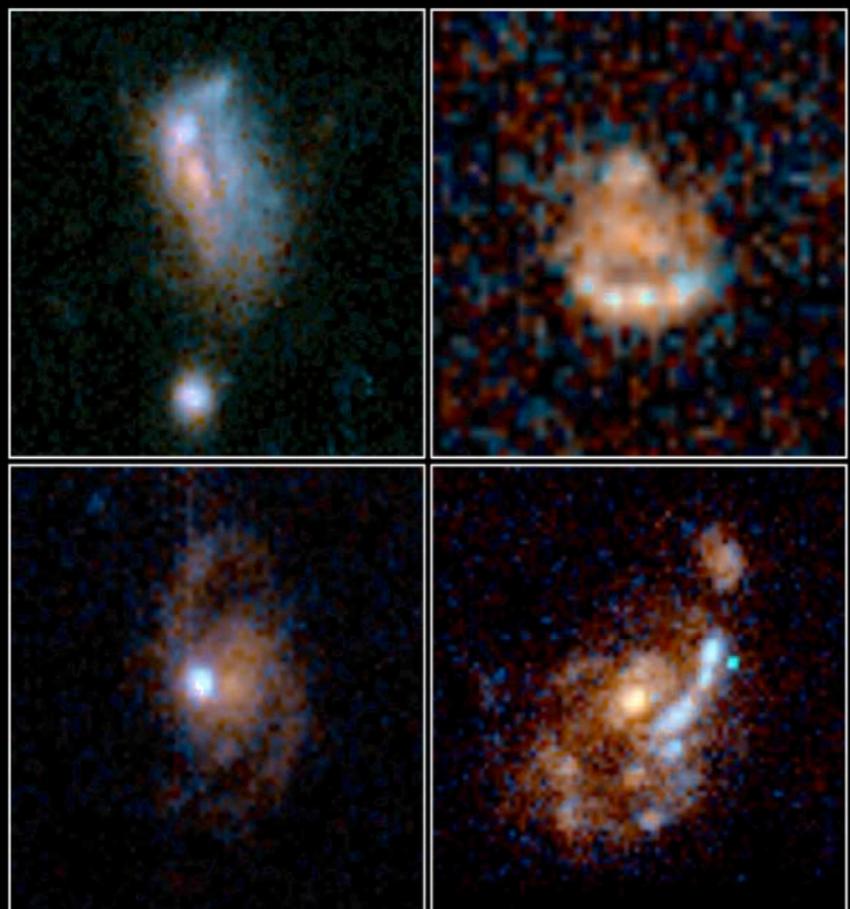
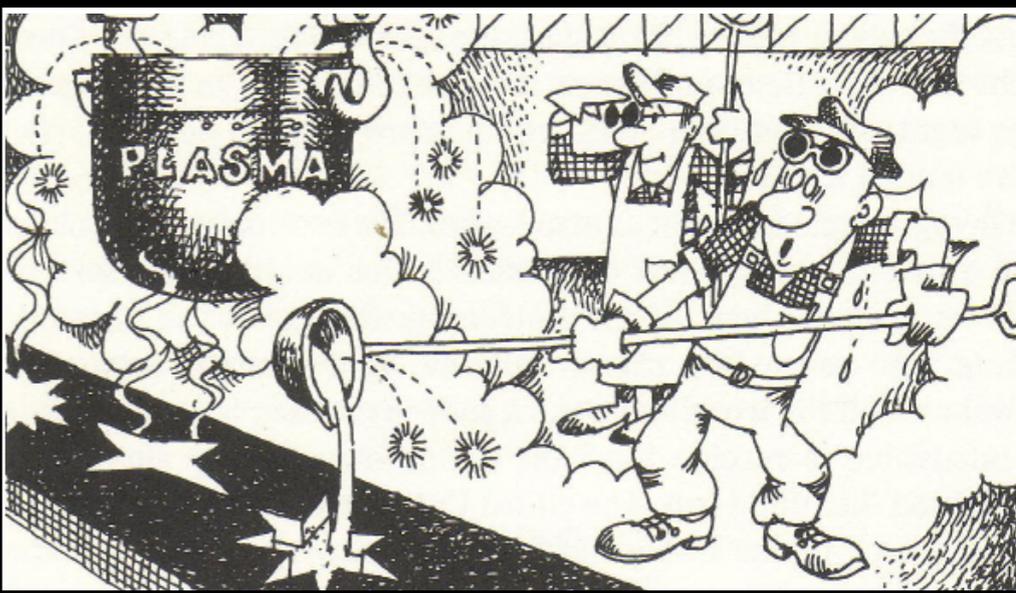
- gas physics (cooling, heating)
- disk formation
- star formation
- evolution of the stellar population
- injection of energy into the gas from SNe



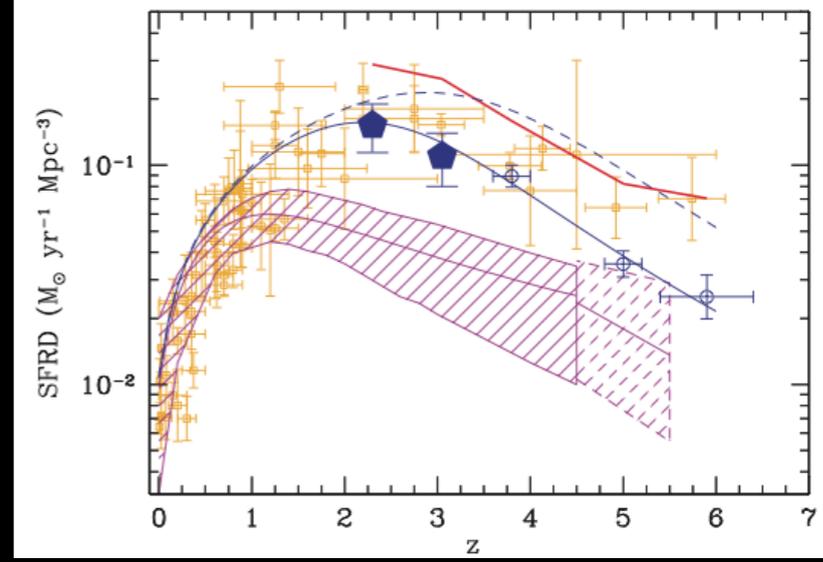
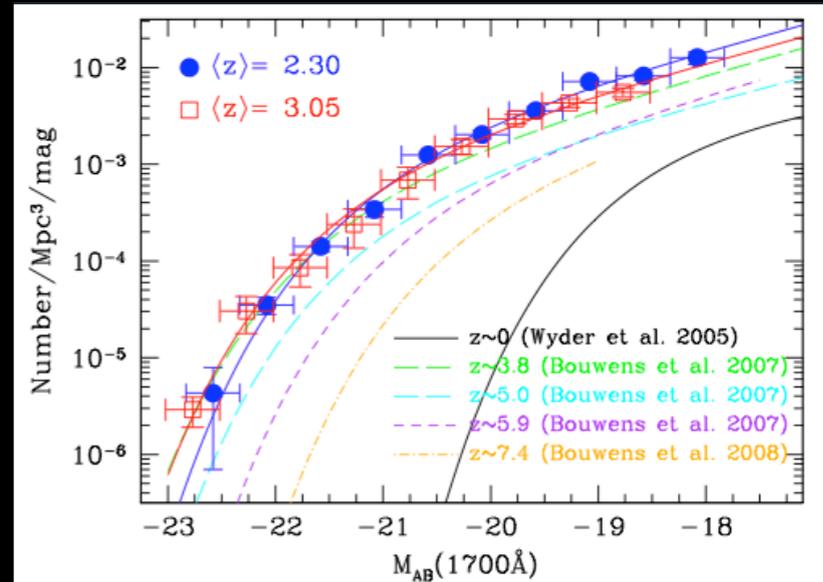
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Medium Deep Survey HST · WFPC2



# Galaxy Formation in a Cosmological Context

## Hydrodynamical N-body simulations

### Pros

include hydrodynamics of gas  
contain spatial information

### Cons

numerically expensive  
(limited exploration of parameter space)  
requires sub-grid physics

## Semi-Analytic Models Monte-Carlo realization of collapse and merging histories

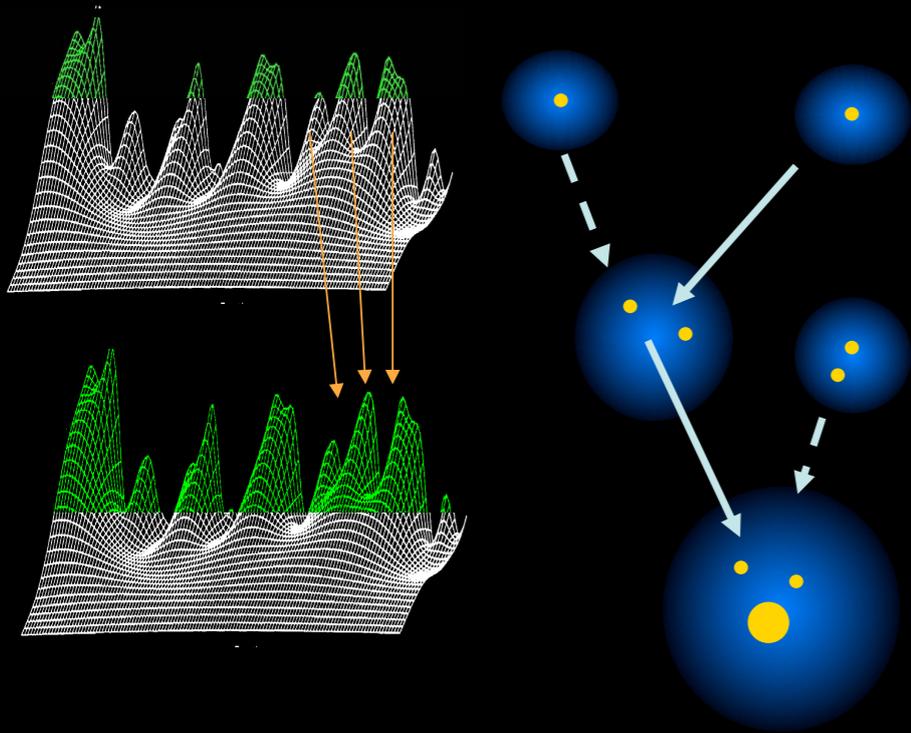
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Physics of baryons linked to DM halos  
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Simplified description of gas physics  
Do not contain spatial informations

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Sub-Halo dynamics:  
dynamical friction, binary aggregation

Halo Properties  
Density Profiles  
Virial Temperature

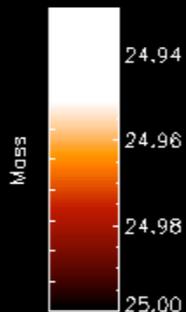
Gas Properties  
Profiles  
Cooling - Heating Processes  
Collapse, disk formation

Star Formation Rate

Gas Heating (feedback)  
SNaE  
UV background

Evolution of stellar populations

Growth of Supermassive BHs  
Evolution of AGNs



## Properties of merging trees

Initial ( $z \approx 4-6$ ) merging events involve small clumps with comparable size

Rapid merging, frequent encounters

Last major merging at  $z \approx 3$  for  $M \approx 3 \cdot 10^{12} M_{\odot}$

At later times, merging rate declines

Accretion of smaller lumps onto the main progenitor

## Baryonic Processes

Frequent galaxy encounters

Rapid cooling (high gas density)

Starbursts with large fraction of Gas converted into stars

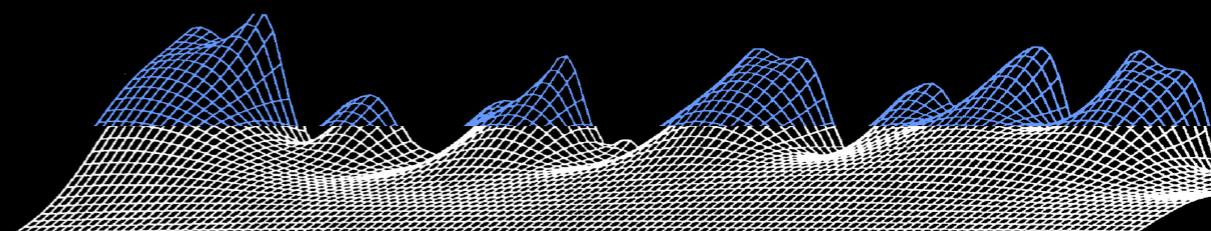
Decline of cooling rate

Drop of encounter rate

Quiescent and declining star formation

$z \gtrsim 2$

$z \lesssim 2$



NM et al. 06

$z$



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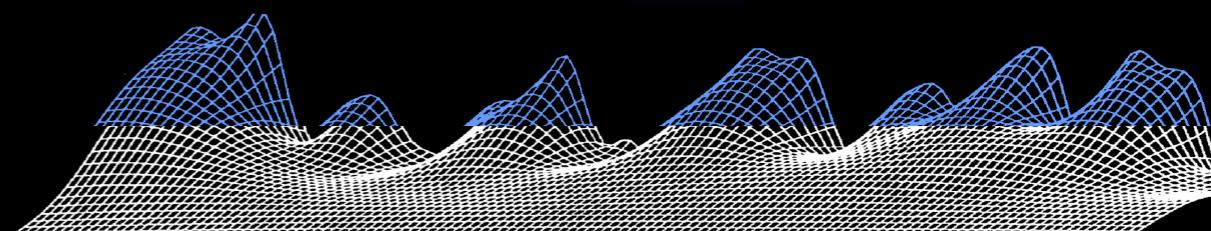
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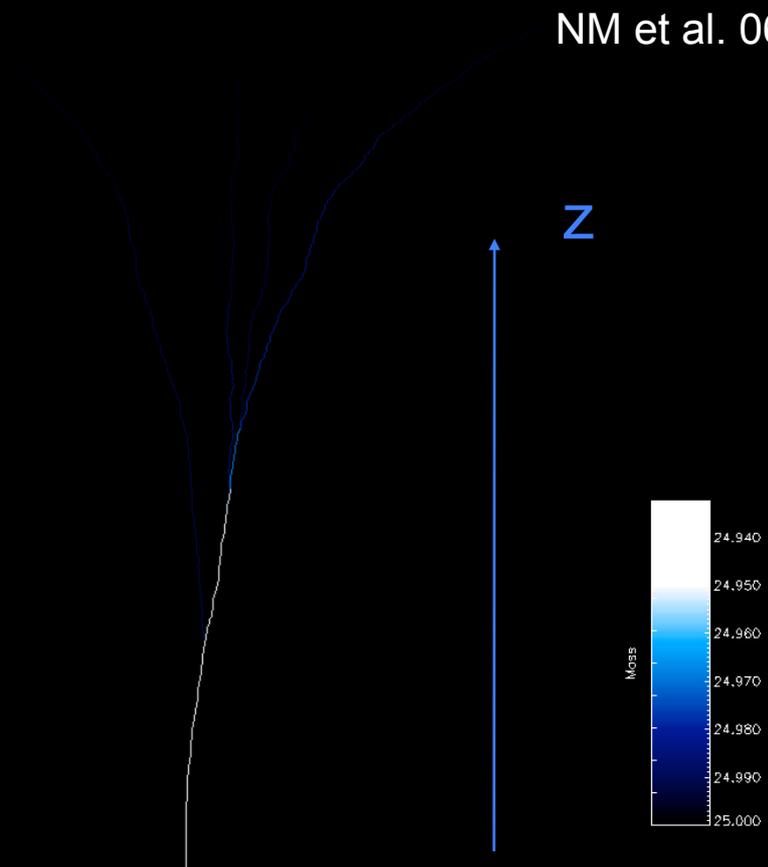
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## Phase 1

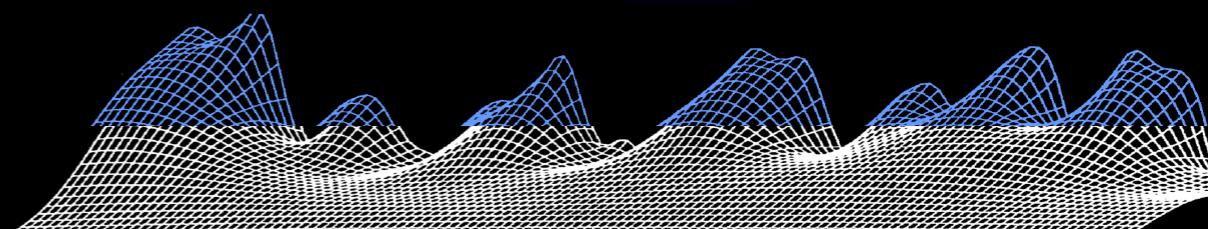
Zhao et al. 2003

Diemand et al. 2007

Hoffman et al. 2007

Ascasibar & Gottloeber 2008

## Phase 2



# Baryonic Processes

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$z \gtrsim 2$

Decline of cooling rate

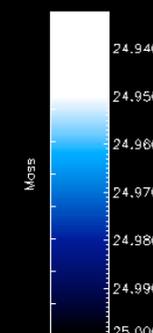
Drop of encounter rate

Quiescent and declining star formation

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NM et al. 06

$z$



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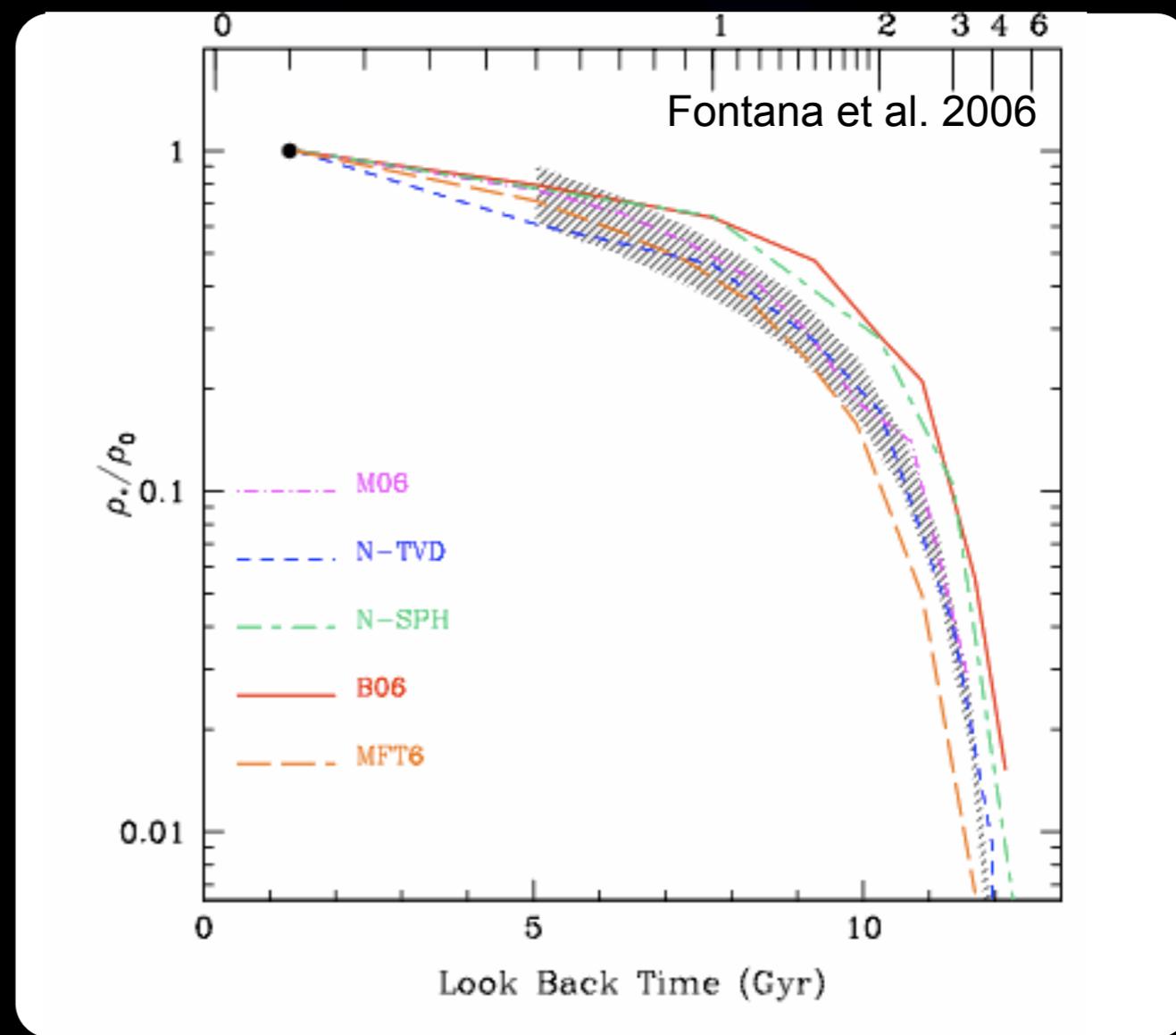
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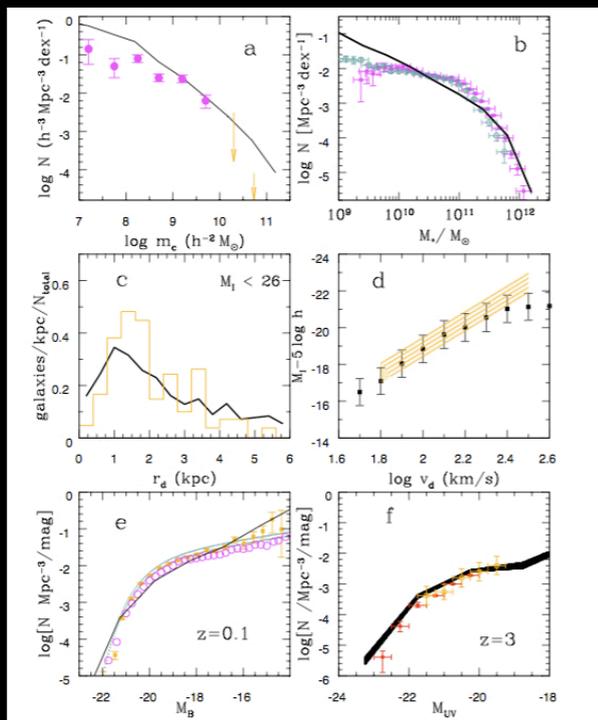
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# Phase 2



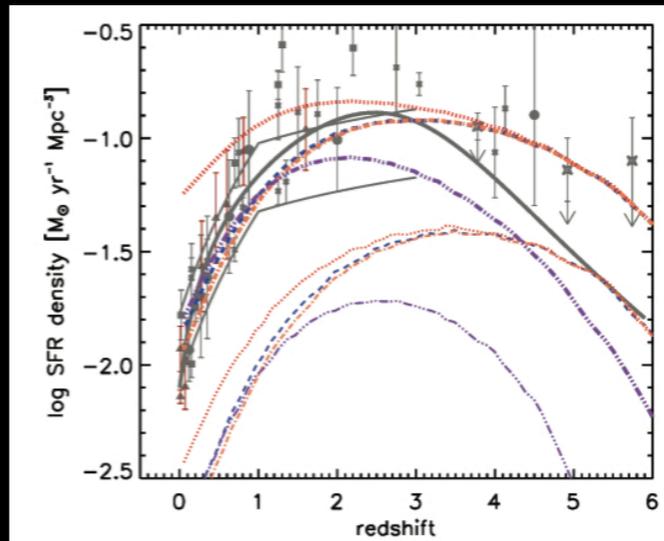
# Galaxy Formation models in CDM scenario

**Local properties:**  
 gas content  
 luminosity distribution  
 disk sizes  
 distribution of the stellar mass content

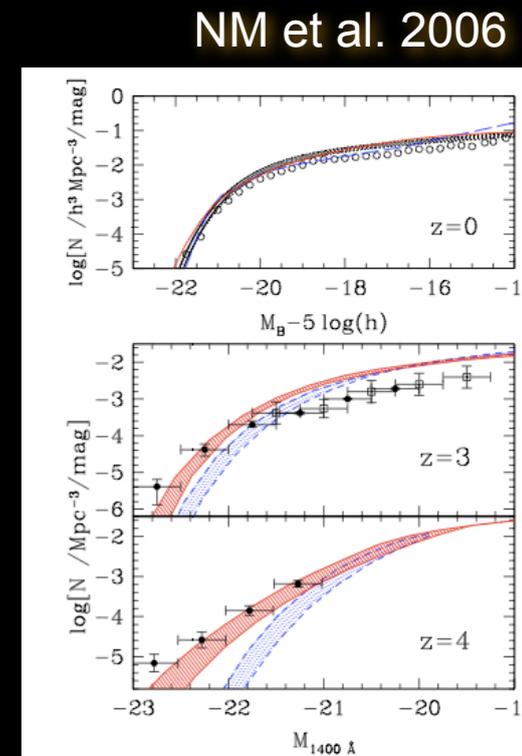


NM et al. 2006

**properties of distant galaxies:**  
 luminosity distribution  
 evolution of the star formation rate

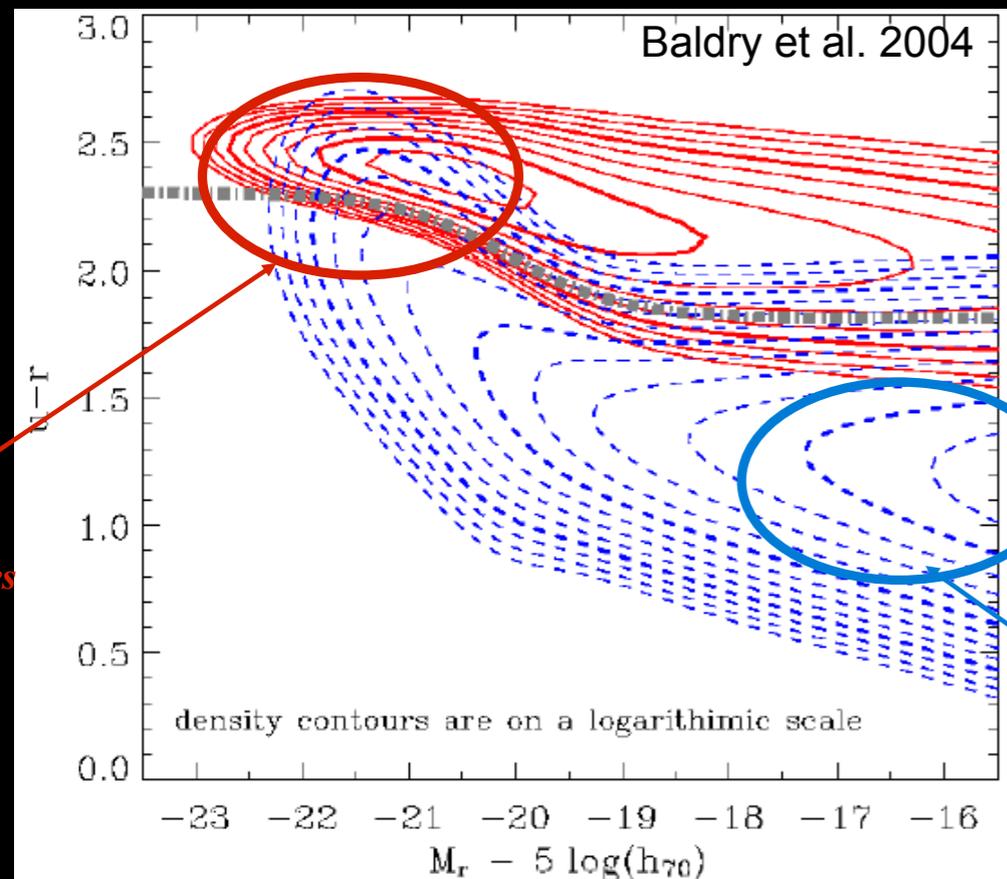


Somerville et al. 2010

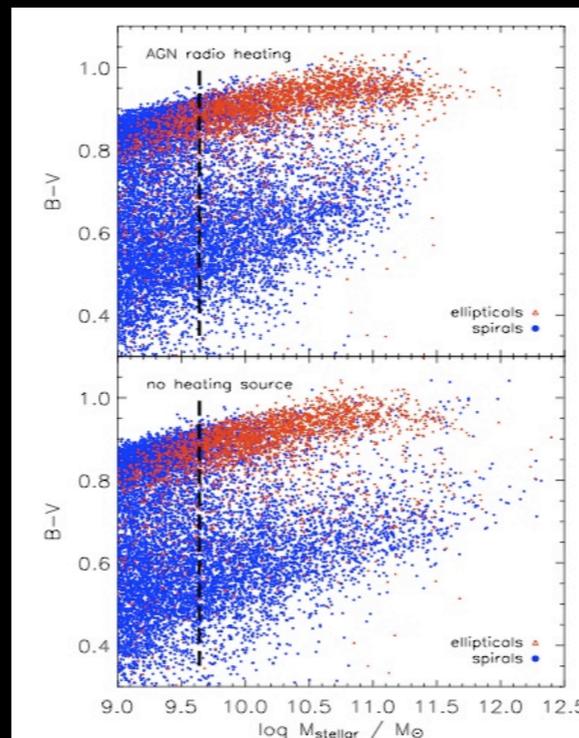


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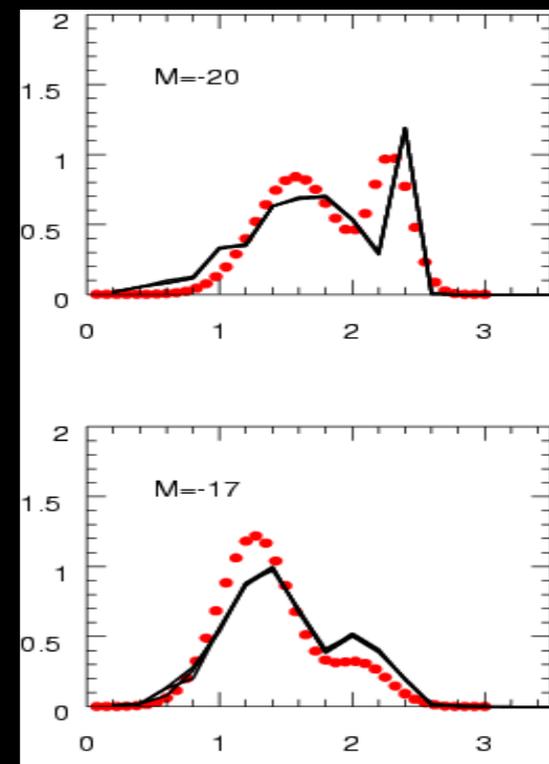
**Color Distributions:** bimodal distribution (early type vs late type)



Baldry et al. 2004



Croton et al. 2006



NM et al. 2008

# Critical Issues

## Overabundance of low-mass objects

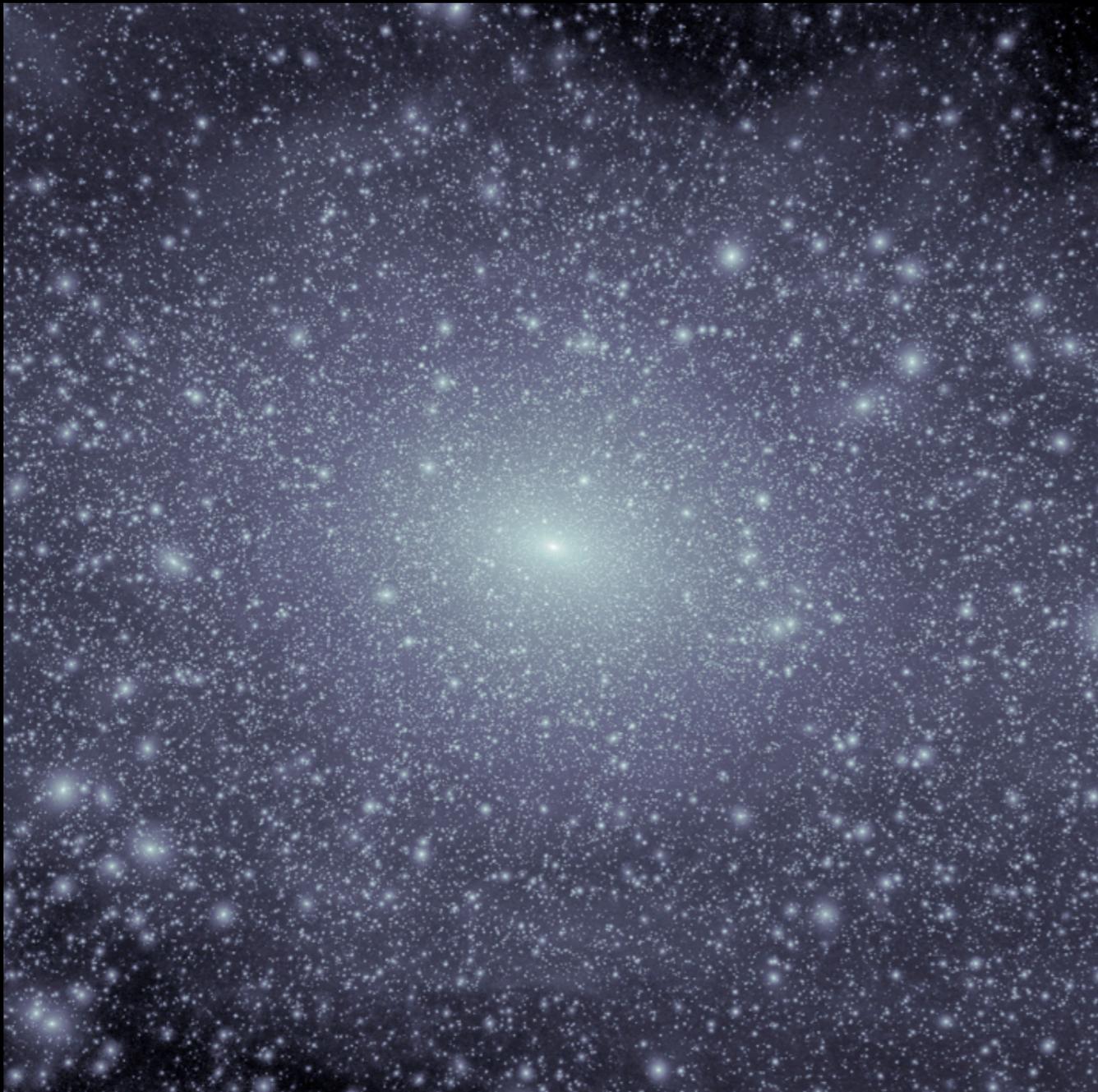
- i) abundance of satellite DM haloes
- ii) density profiles
- iii) abundance of faint galaxies
- iv) abundance of faint AGN
- v) star formation histories of satellites
- vi) the  $v_{\max}$ - $M_*$  relation

- 1) Dependence on specific theoretical model
- 2) Dependence on star formation and feedback effects
- 3) Solution in WDM scenario

# Critical Issues

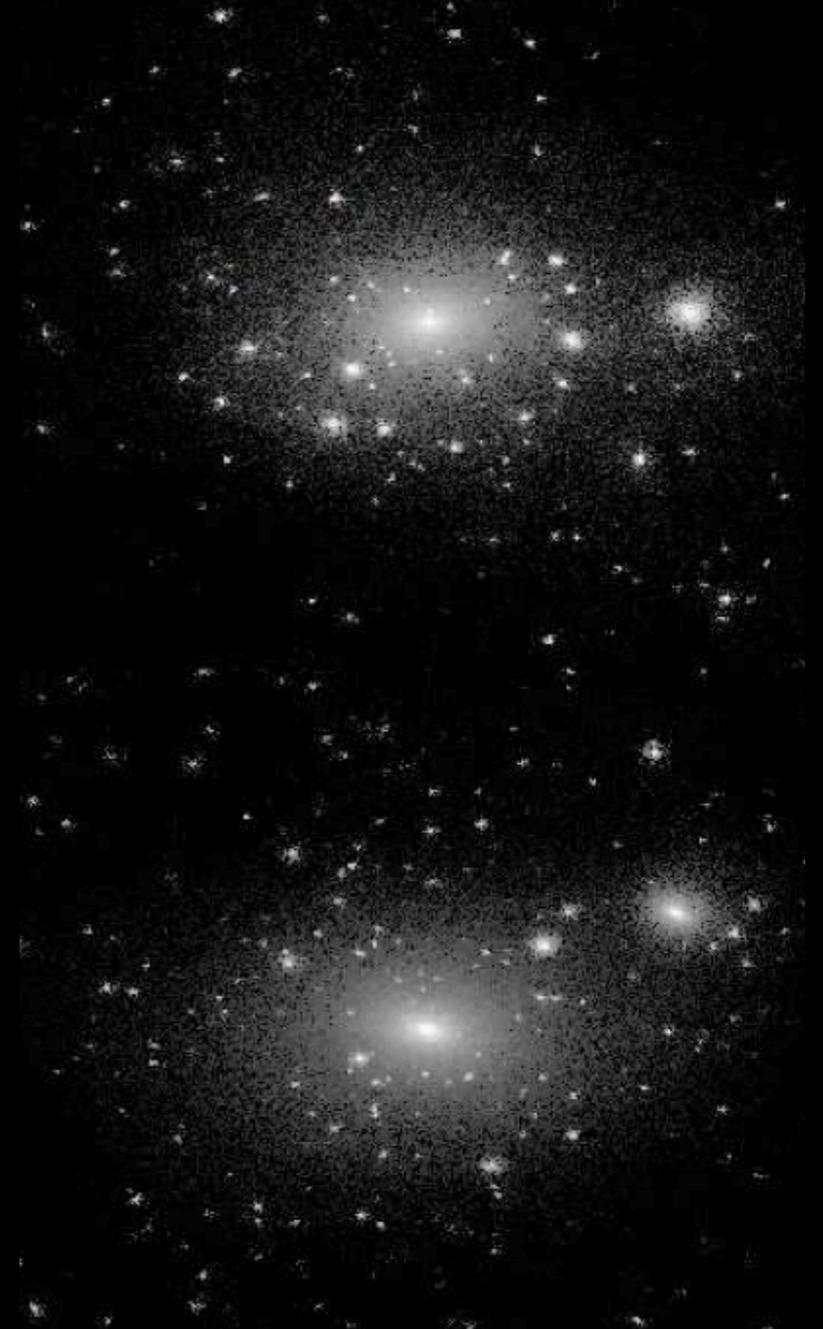
## i) satellite DM haloes

Via Lactea simulation of a Milky Way - like galaxy  
Diemand et al. 2008



CDM Substructure in simulated cluster and galaxy haloes look similar.

Expected number of satellites in Milky Way- like galaxies in CDM largely exceeds the observed abundance.



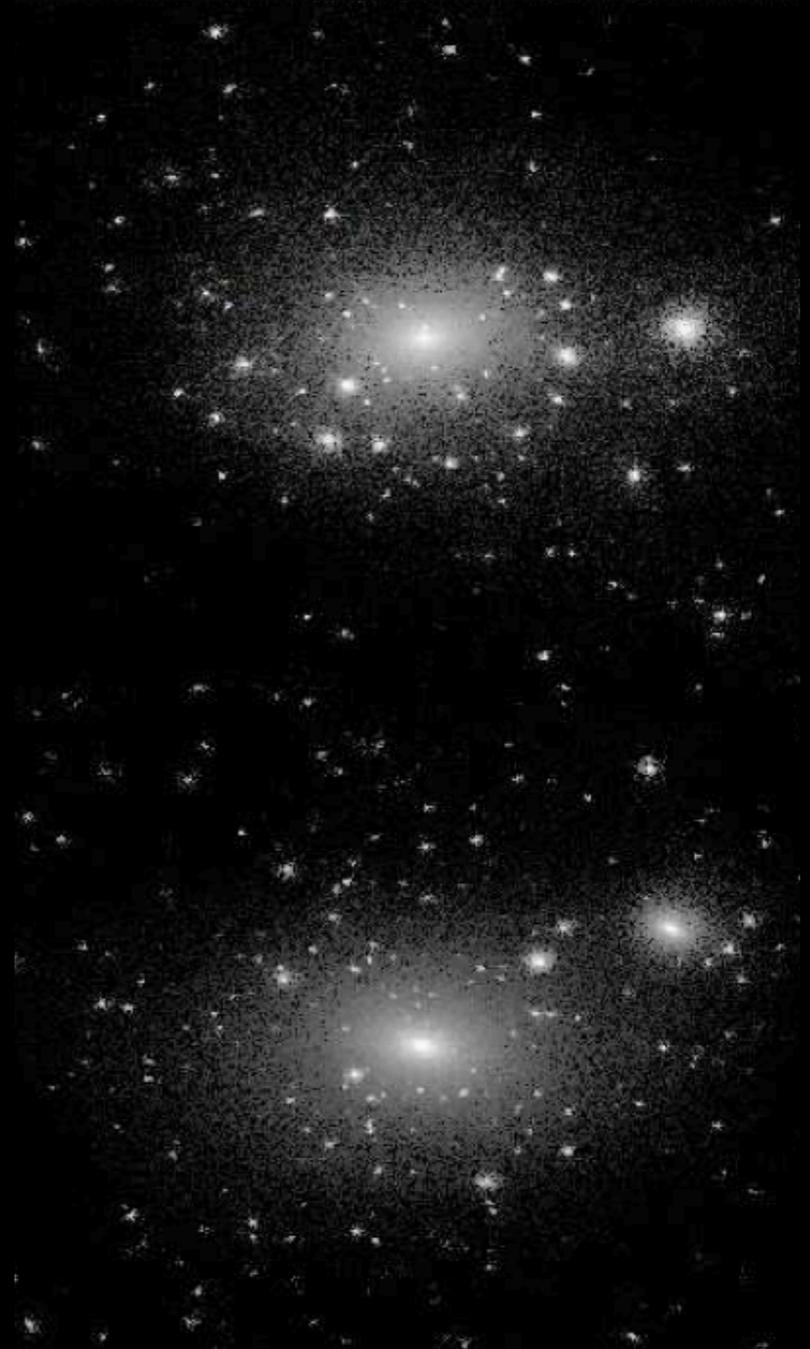
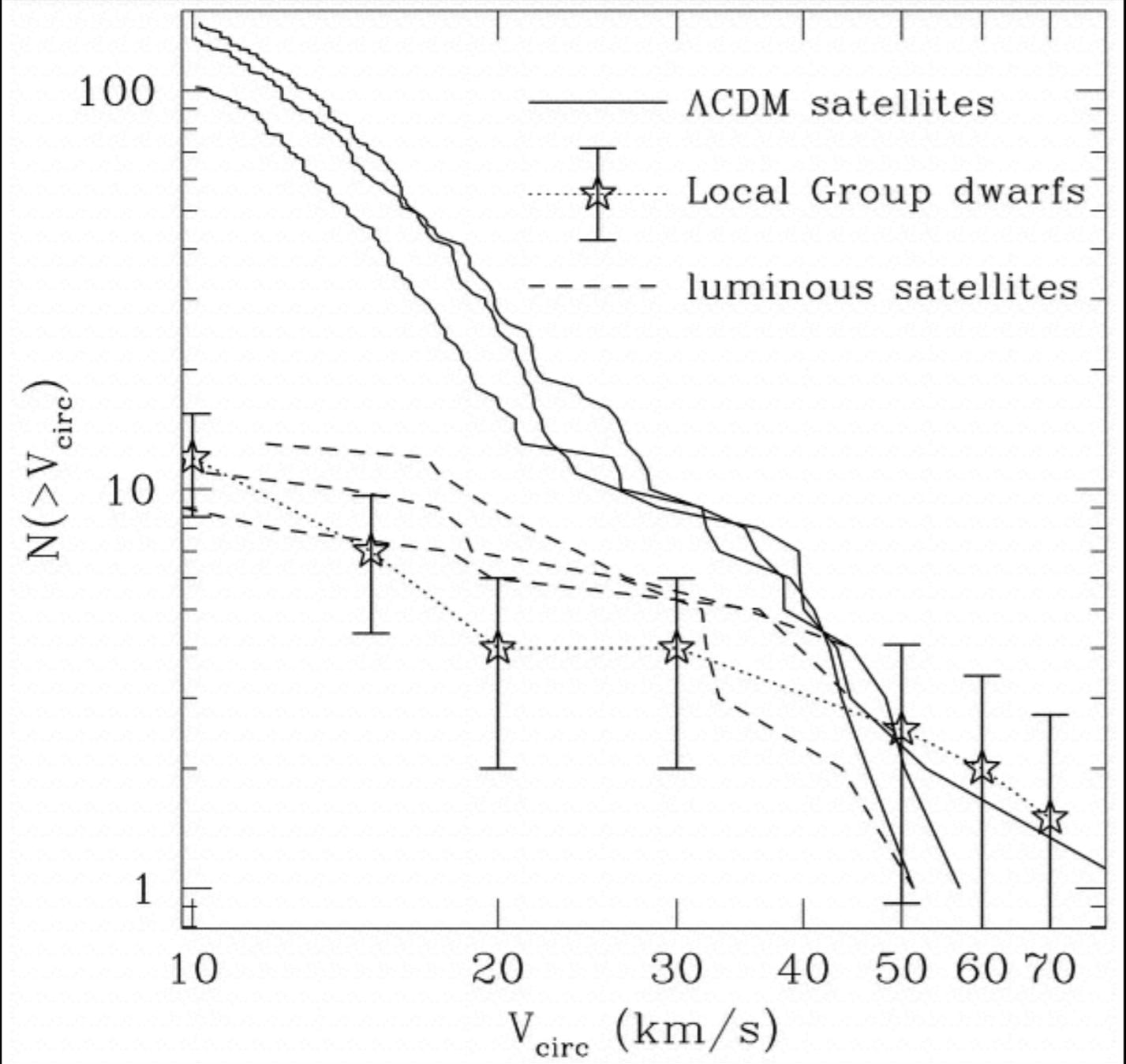
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## i) satellite DM haloes

CDM Substructure in simulated cluster and galaxy haloes look similar.

Expected number of satellites in Milky Way- like galaxies in CDM largely exceeds the observed abundance.

Kravtsov, Klypin, Gnedin 2004



# Critical Issues

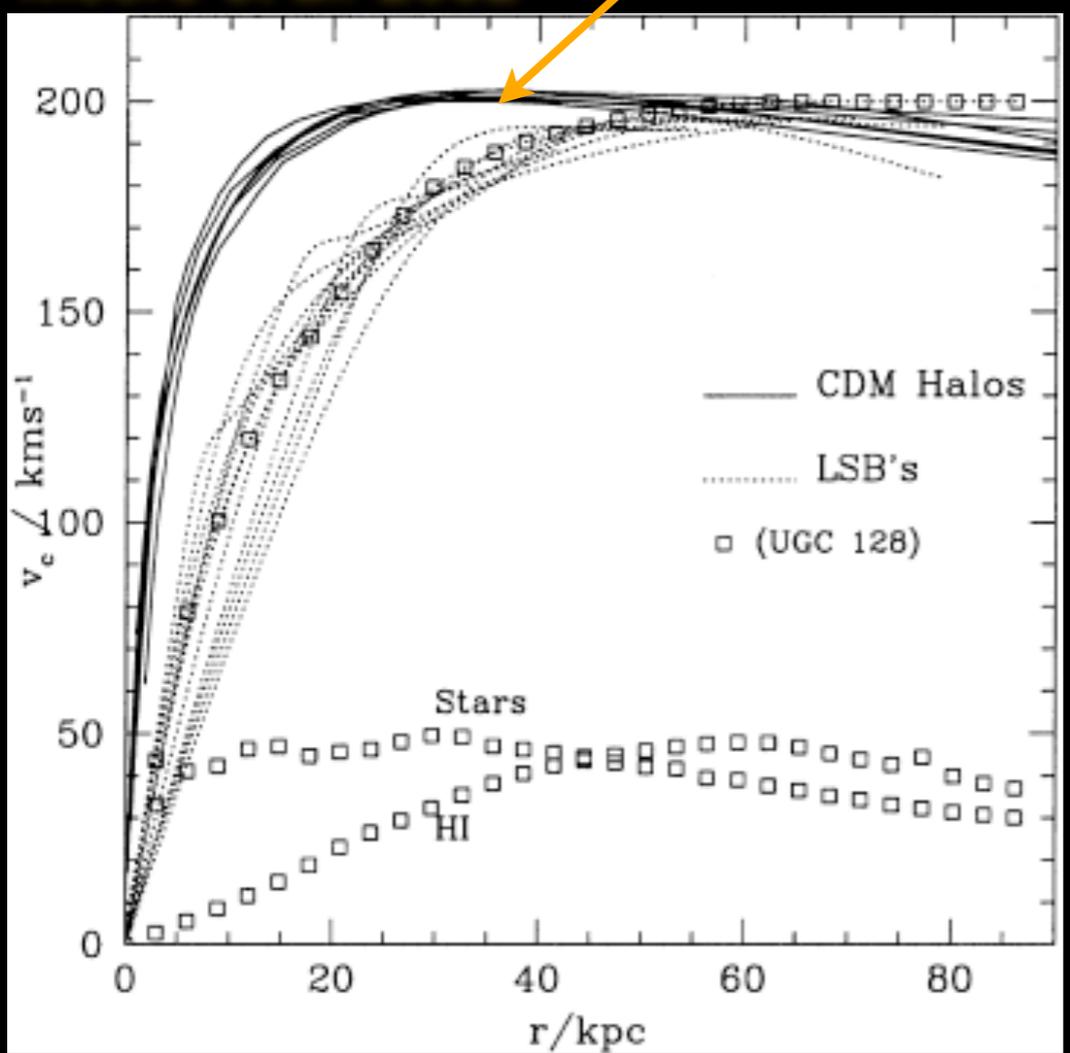
## ii) density profiles

Most observed dwarf galaxies consist of a rotating stellar disk embedded in a massive dark-matter halo with a near-constant-density core. Models based on the dominance of CDM, however, invariably form galaxies with dense spheroidal stellar bulges and steep central dark-matter profiles, because low-angular-momentum baryons and dark matter sink to the centres of galaxies through accretion and repeated mergers.

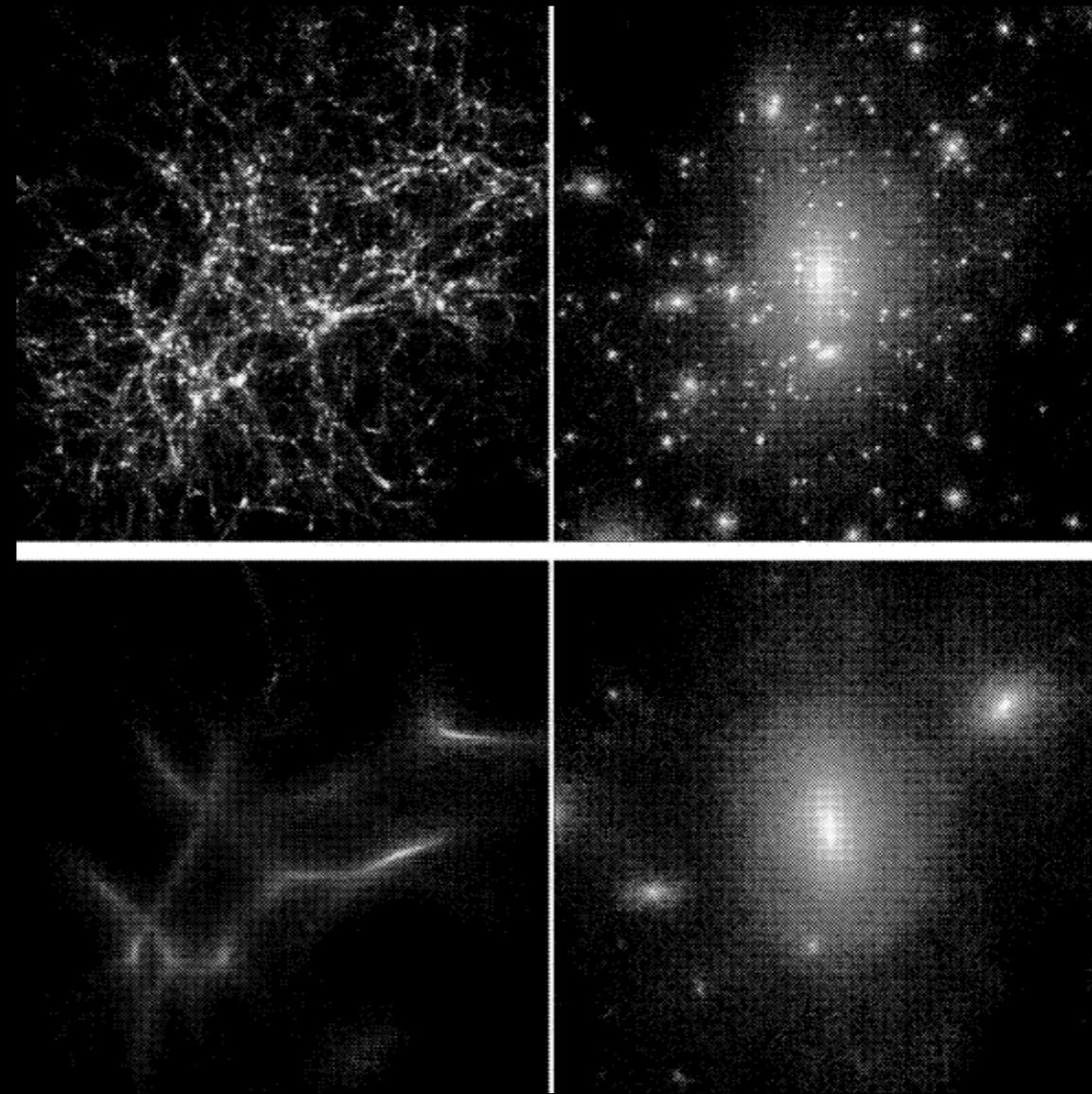
NFW

circular velocity profile

Moore et al. 2002



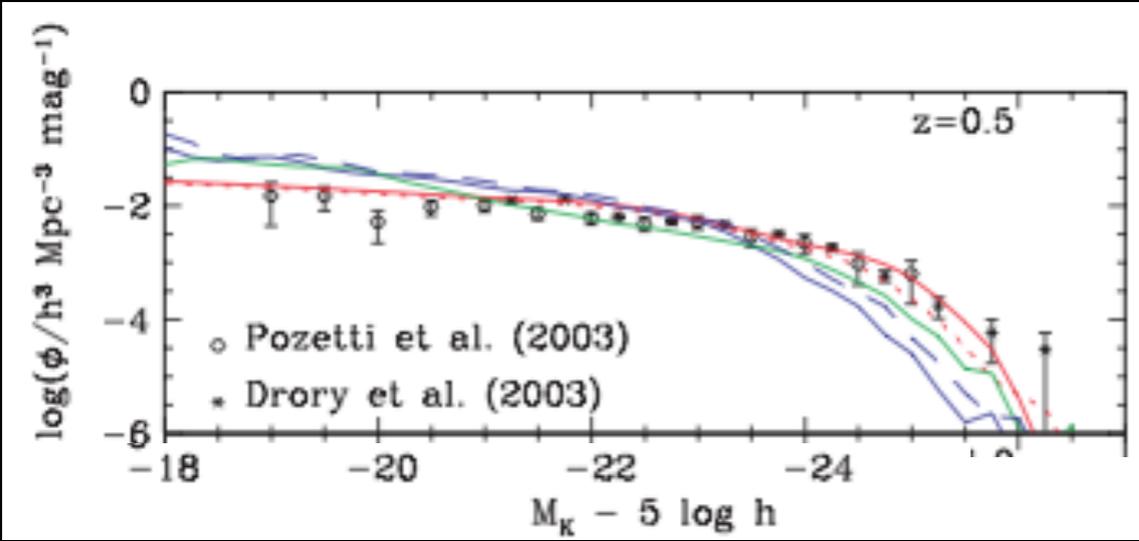
The effect of adopting a cutoff in the power spectrum for  $r < 8 \text{ Mpc}$



# Critical Issues

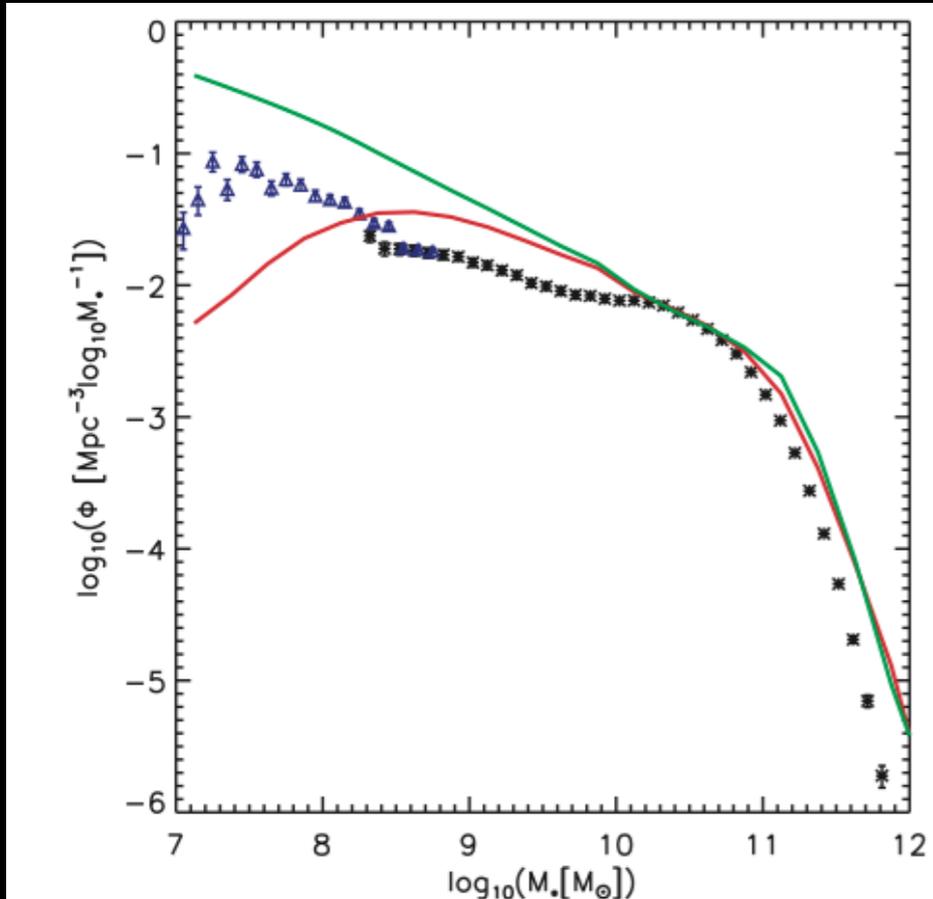
## iii) over-prediction of faint galaxies

In all first-generation SAM the number density of faint (low-mass) galaxies was over-predicted

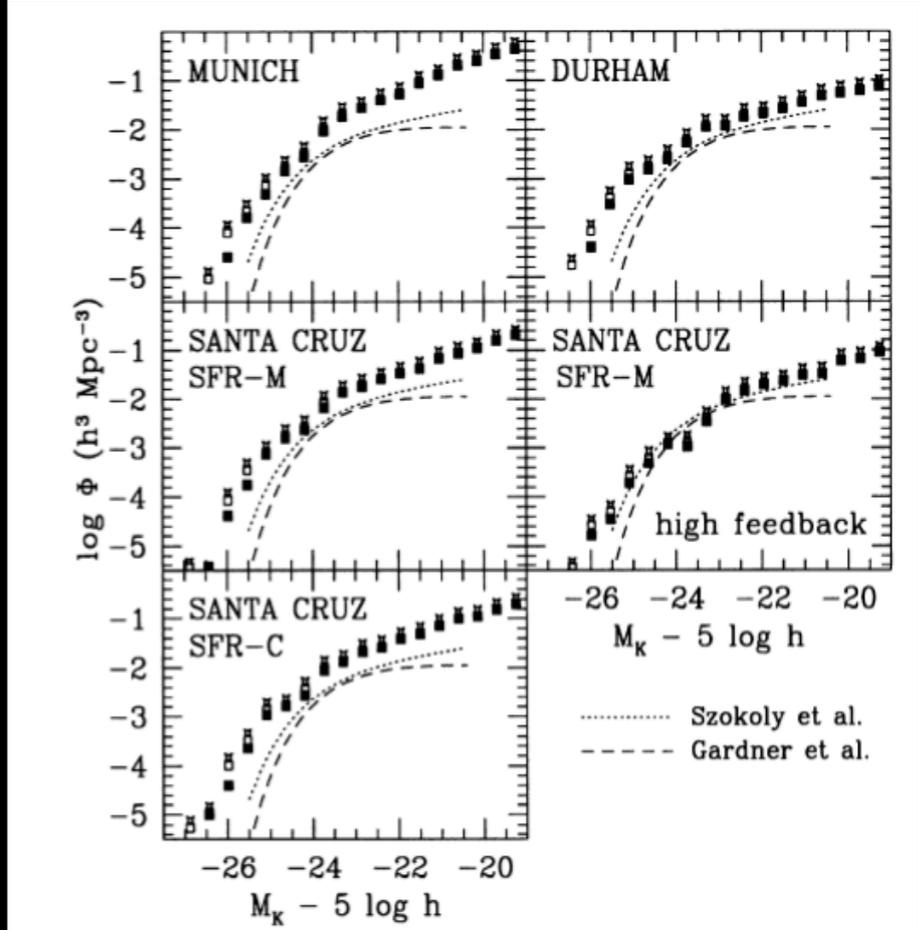


Bower et al. 2006

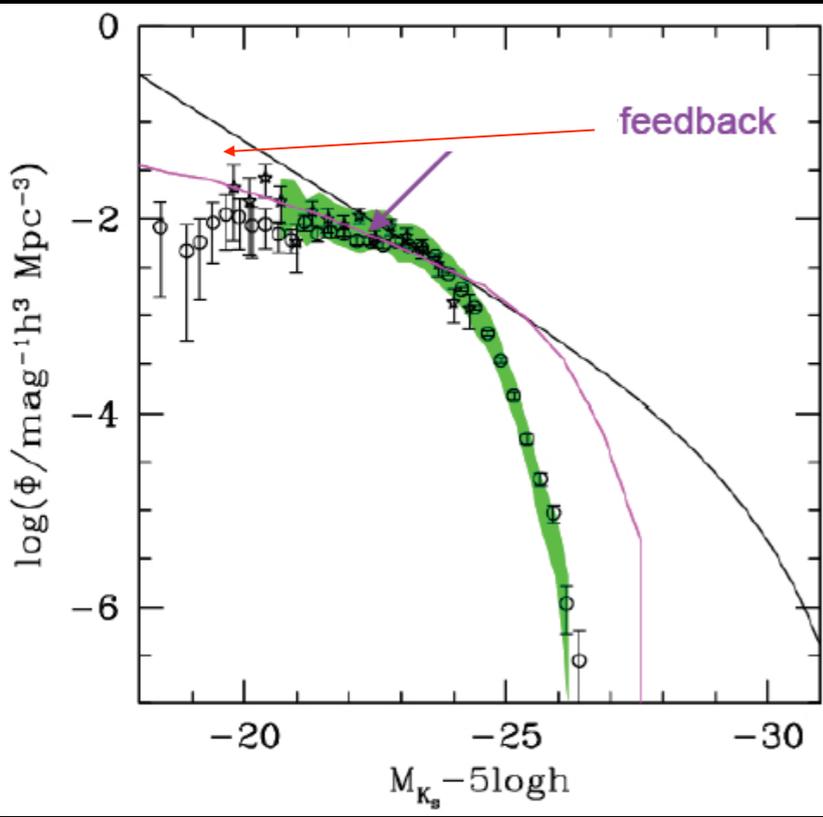
The K-Band Luminosity Function in the Somerville et al. SAM



The Stellar Mass Function in the De Lucia et al. SAM based on Millenium merger trees



# A first-order solution: feedback and UV background



**The origin of the problem:**  
 The DM halo Mass function has a steep log slope  $N \sim M^{-1.8}$   
 While the Observed Galaxy Luminosity Function has a much flatter slope  $N \sim L^{-1.2}$

**A Possible Solution:**  
 Suppress luminosity (star formation) in low-mass haloes  $L/M \sim M^\beta$   $\beta = 1 - 3$   
 Heat - Expell Gas from shallow potential wells

- Enhanced SN feedback
- UV background

$$E_{SN} \approx 10^{51} \eta_0 \eta_{IMF} \Delta M_* \text{ erg/s}$$

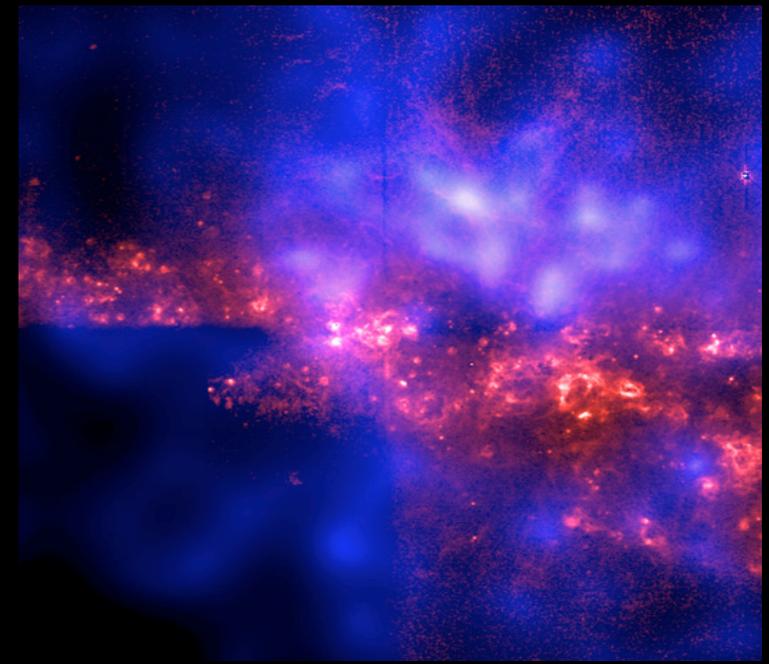
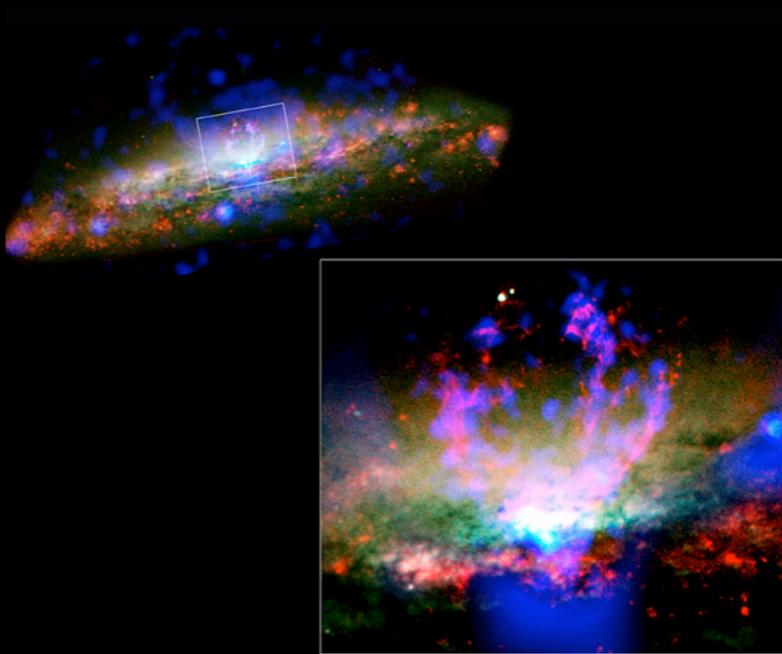
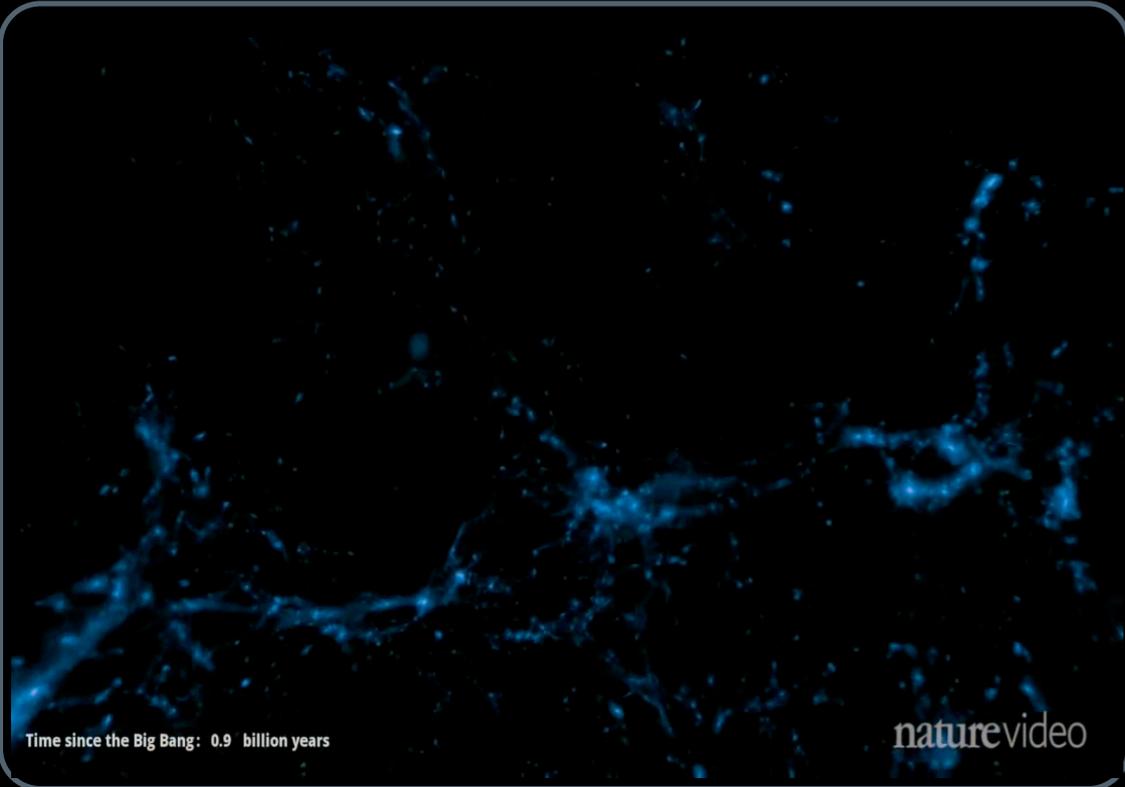
At  $Z=0$  the mass scale at which SN can effectively expell gas from DM potential wells

$$v_{SN} = \sqrt{E_{SN} / M_{gas}} \approx 100 \text{ km/s}$$

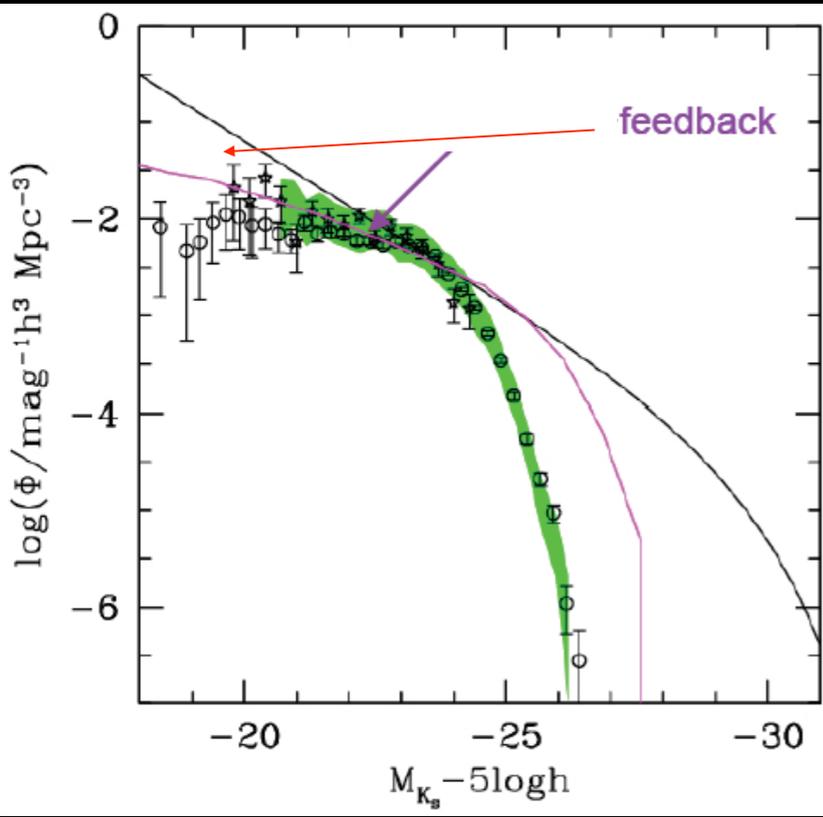
$$M_{SN} \sim 10^{10} M_\odot$$

at low  $z$ , at higher redshift the density is higher an  $M_{SN}$  increases

Vogelsberger et al. 2014



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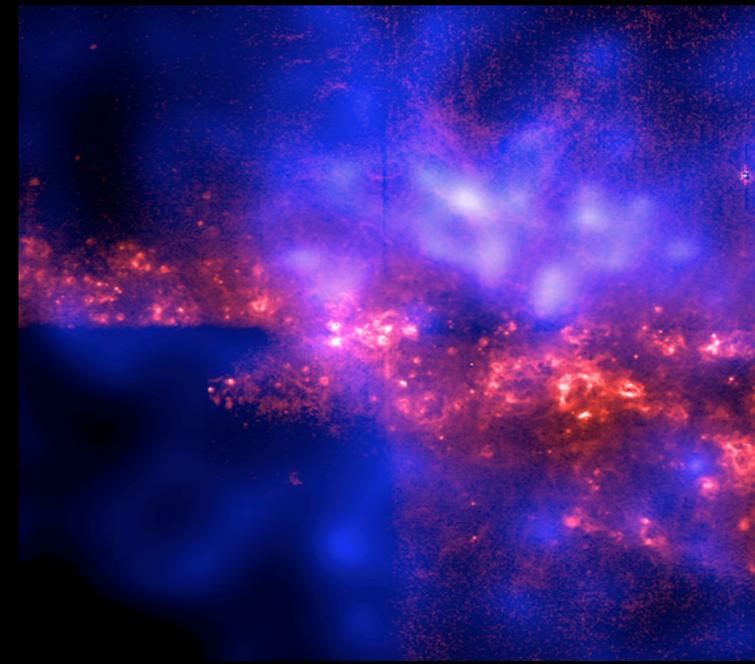
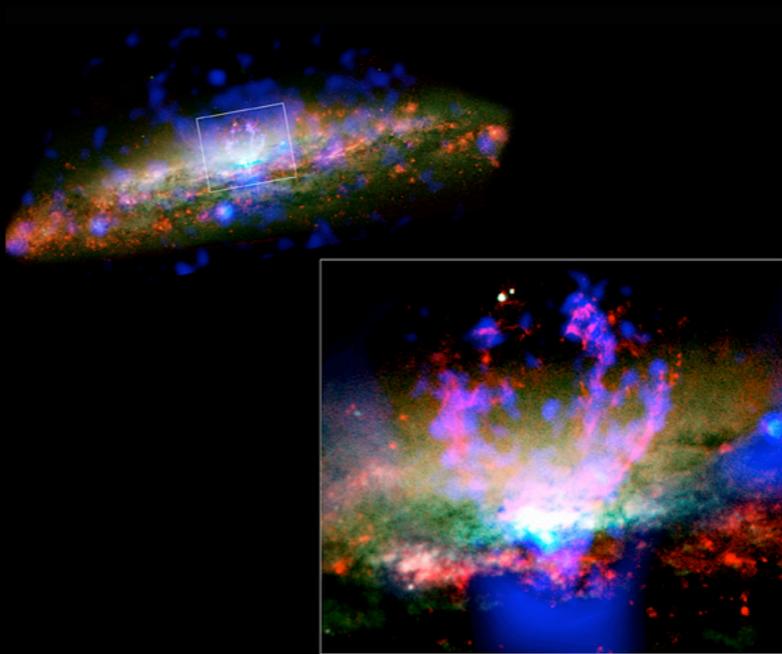
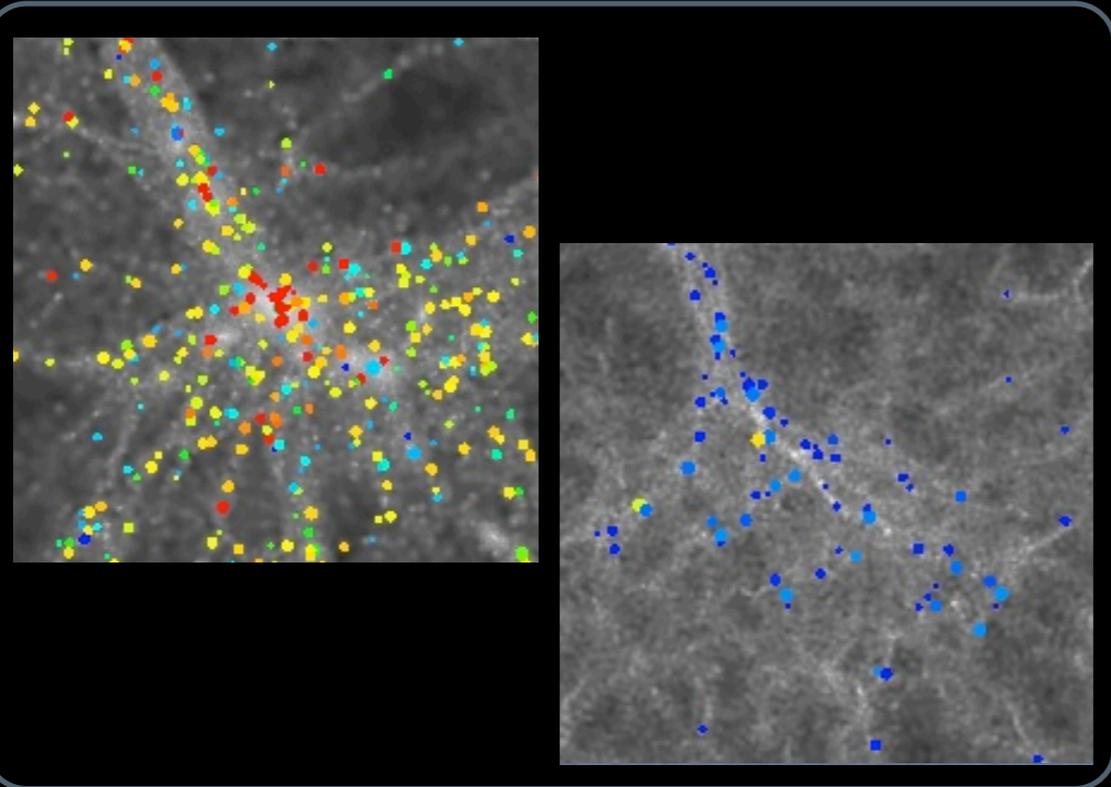
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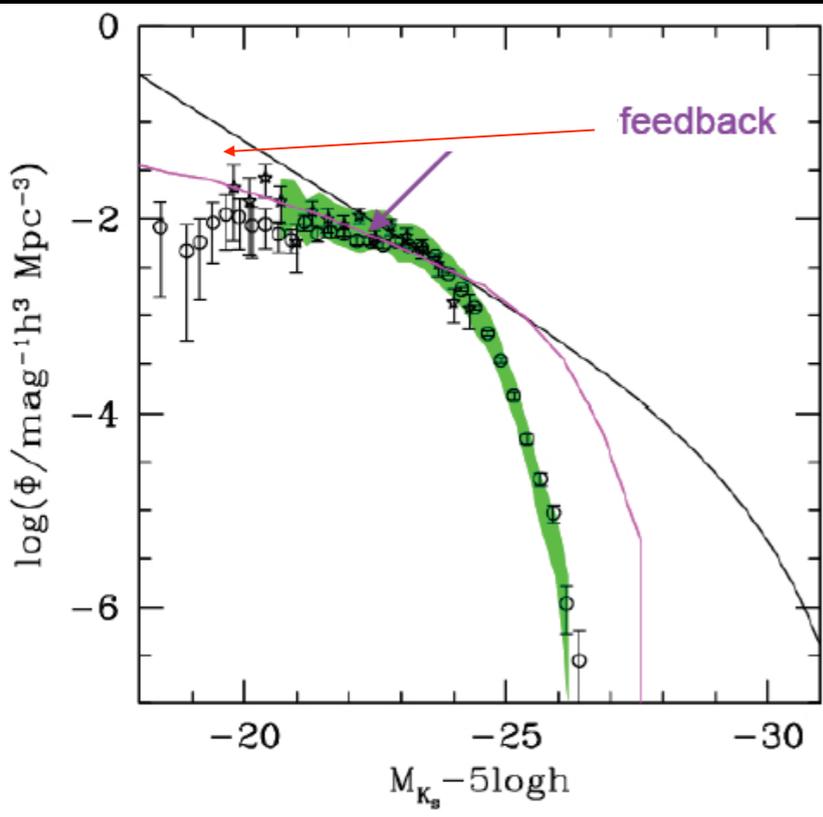
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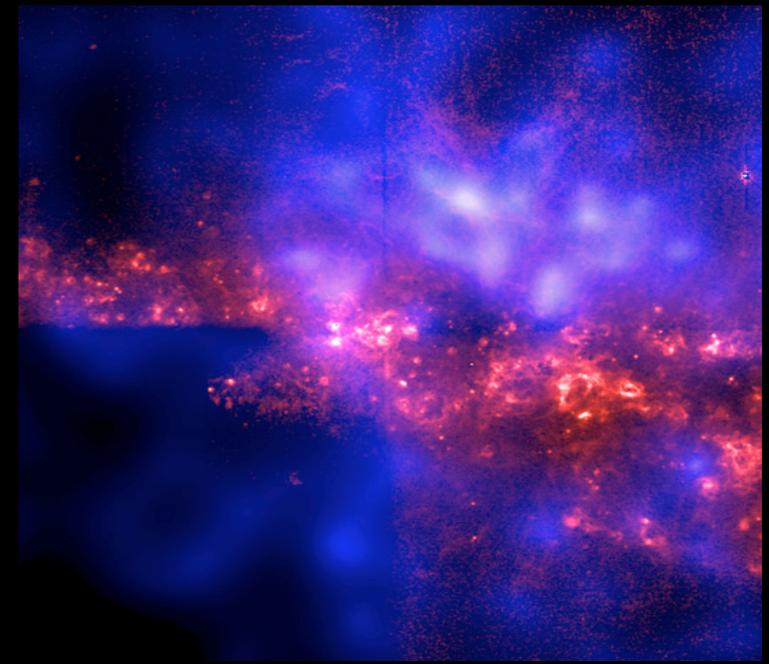
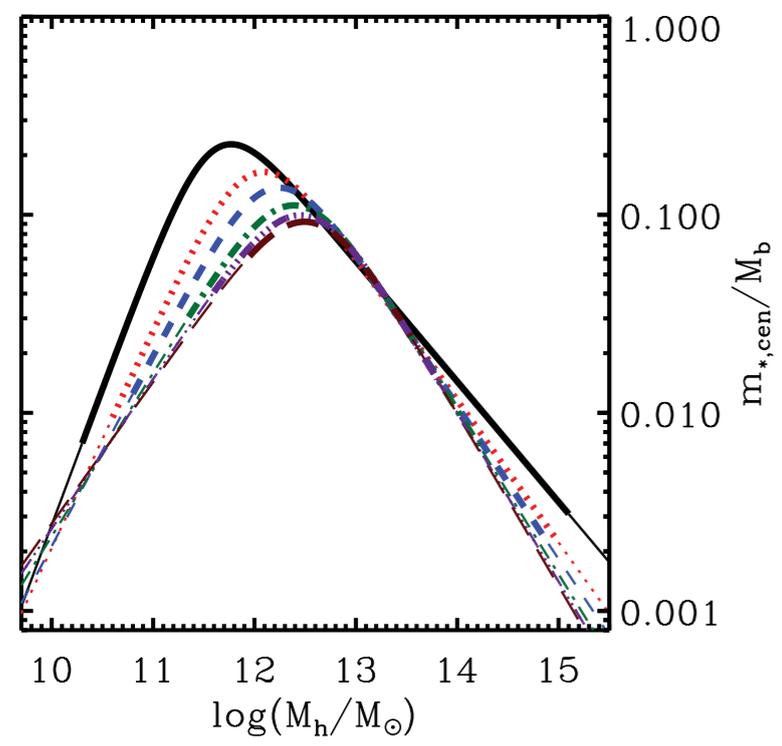
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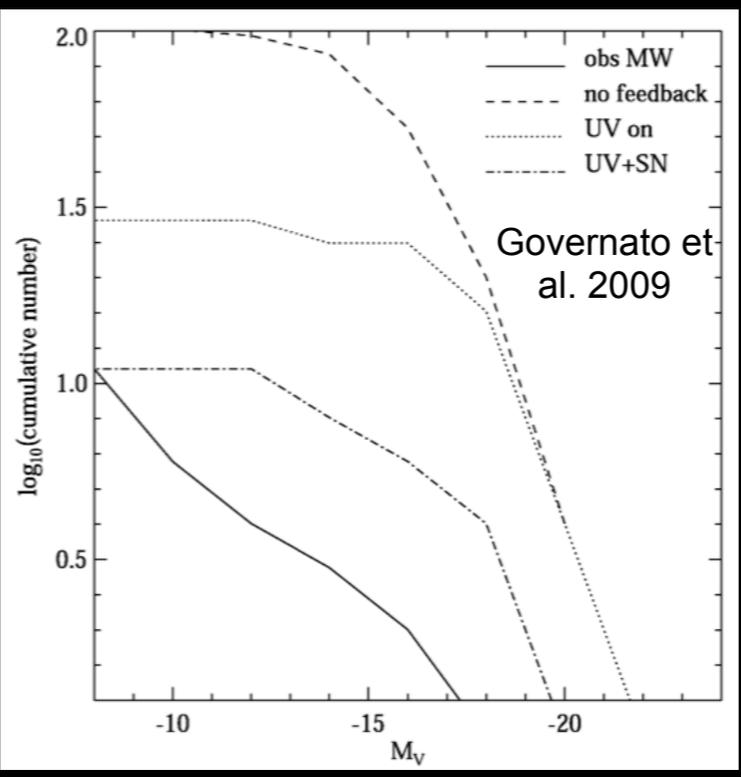
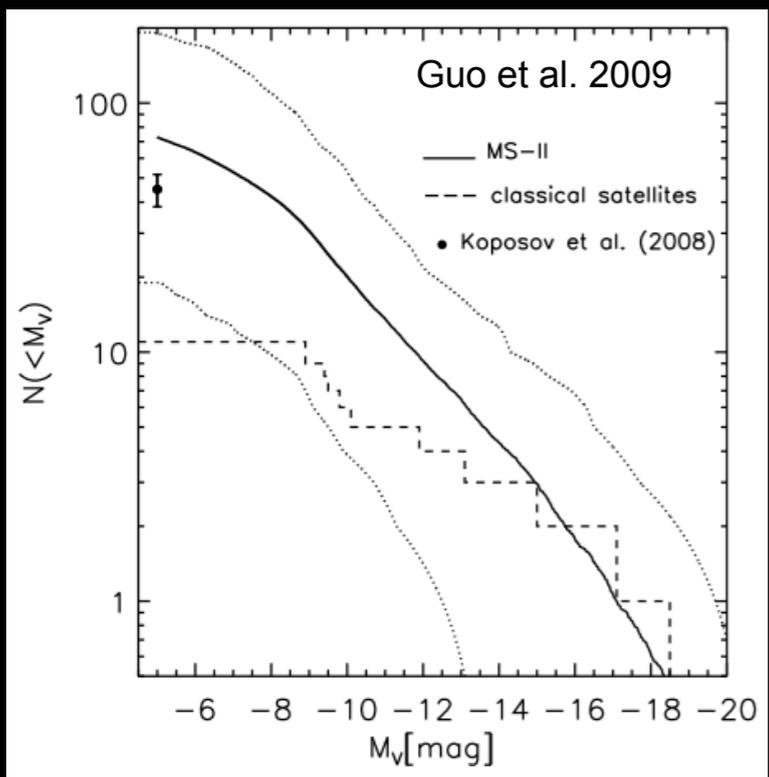
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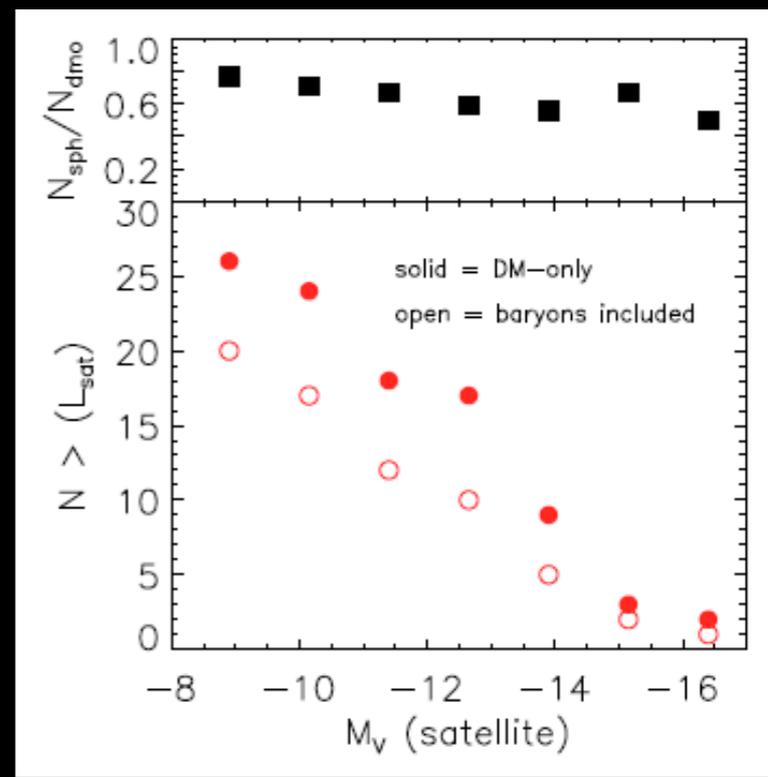


# Feedback and UV background

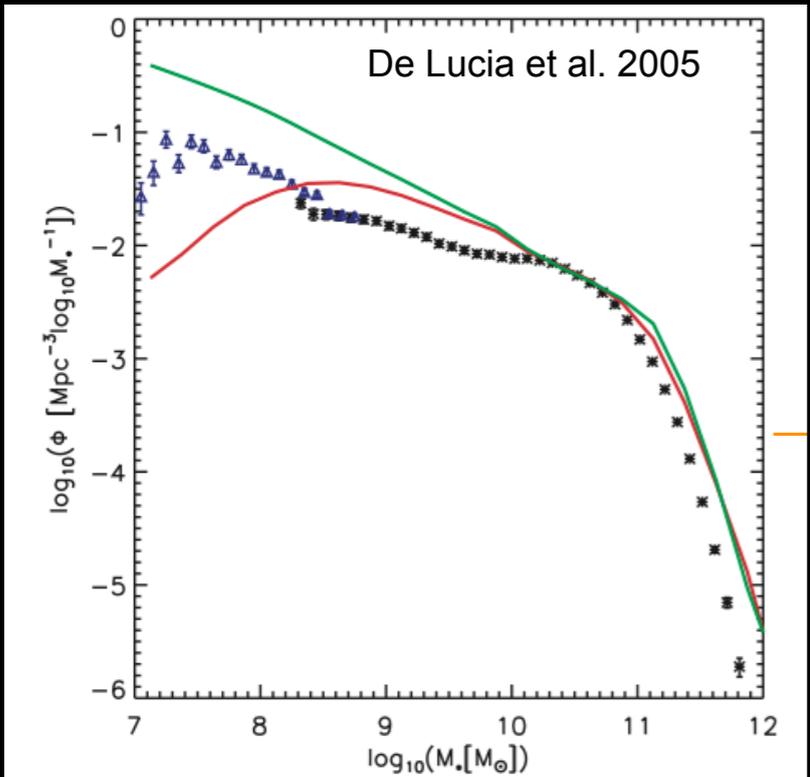
## i) the abundance of satellites



Brooks & Zolotov 2014

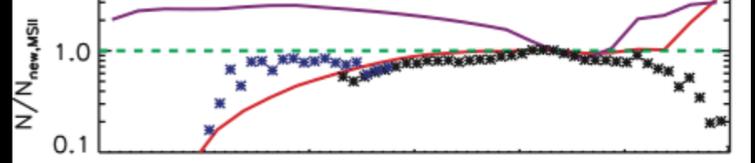
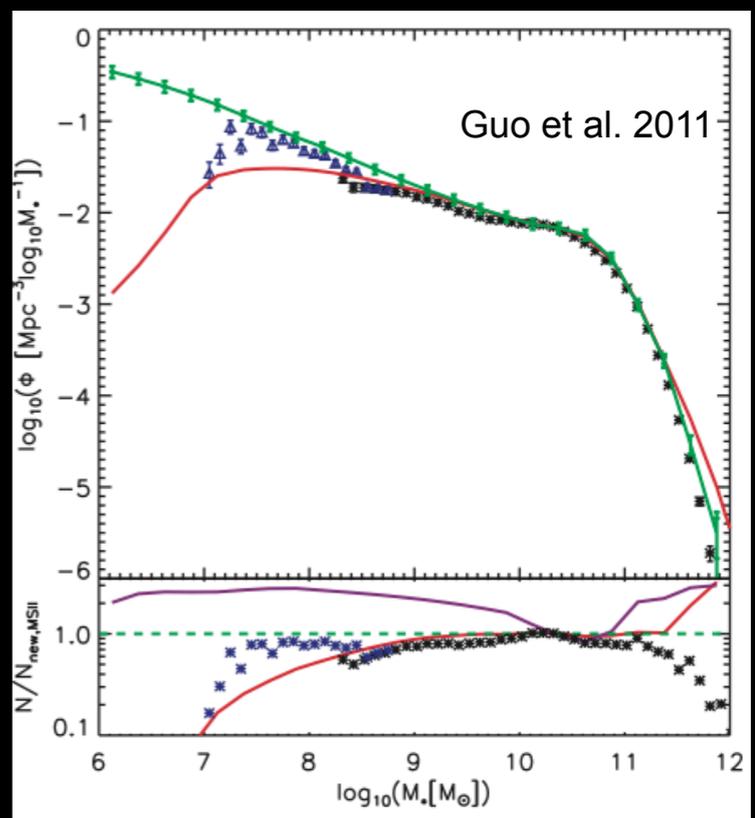


## ii) the abundance of faint galaxies



Refined treatment of Gas and Stellar Stripping

Enhanced (tuned) feedback dependence on the circular velocity of the DM halo

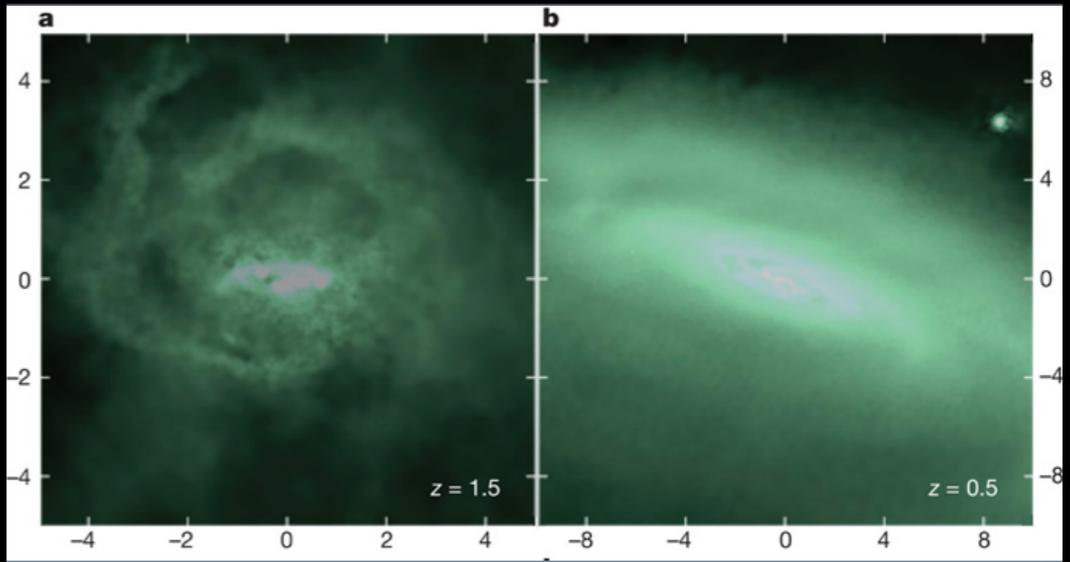


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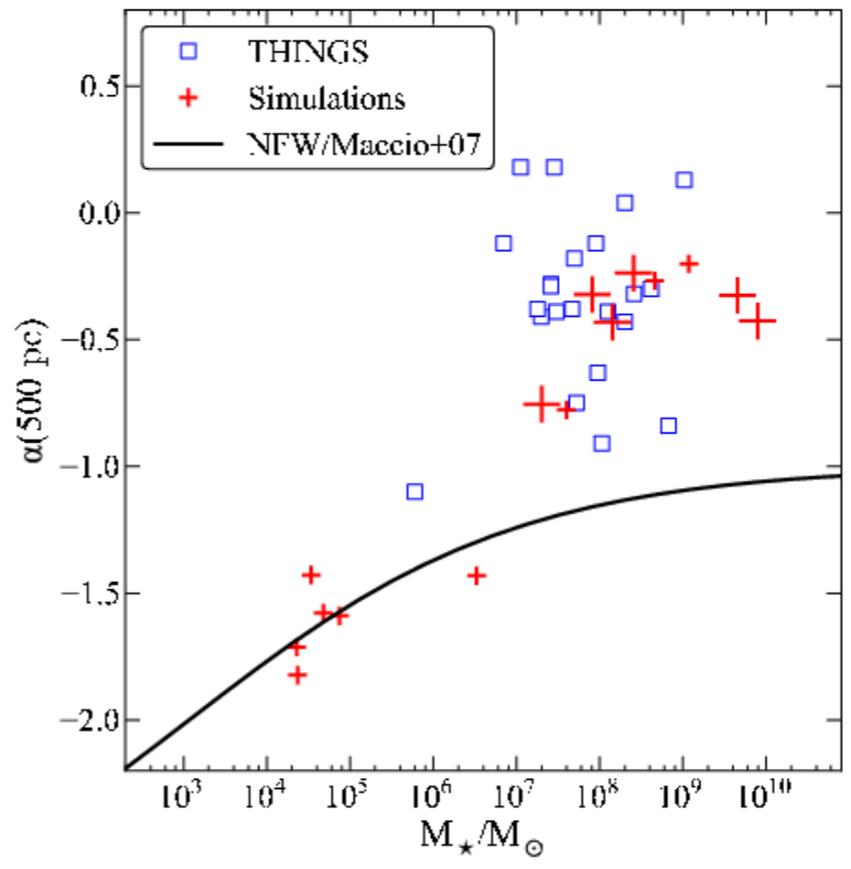
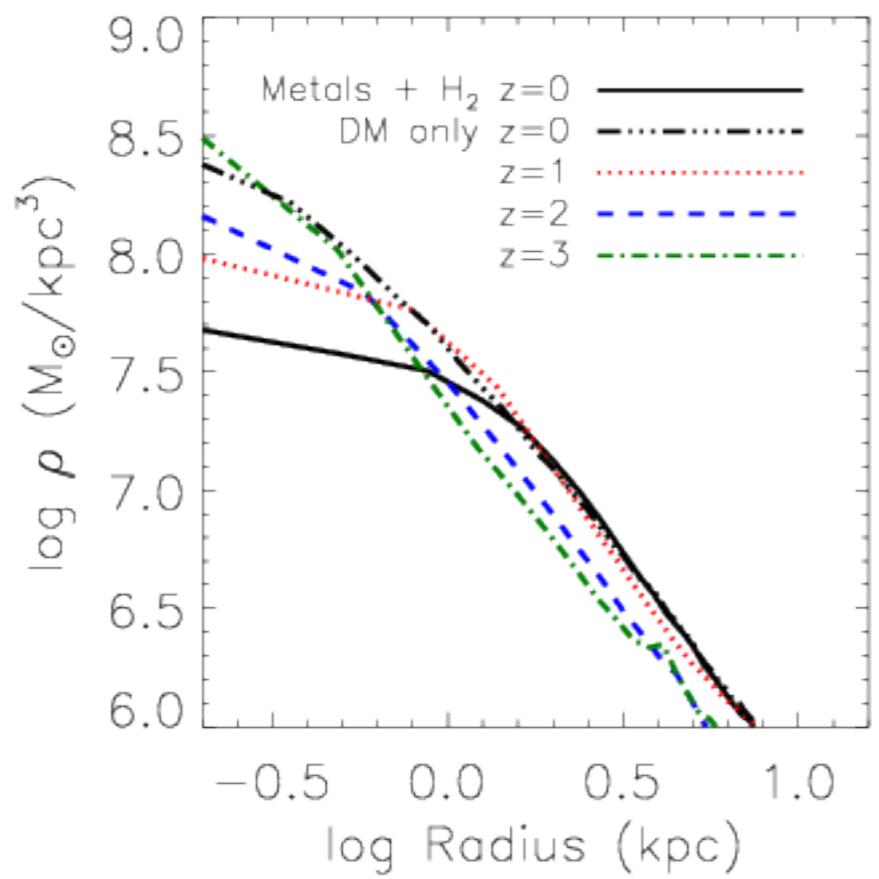
## iii) the density profiles

### A proposed solution at low redshift

"... The rapid fluctuations caused by episodic feedback progressively pump energy into the DM particle orbits, so that they no longer penetrate to the centre of the halo" (Weinberg et al. 2013, Governato et al. 2012)



Governato et al. 2012

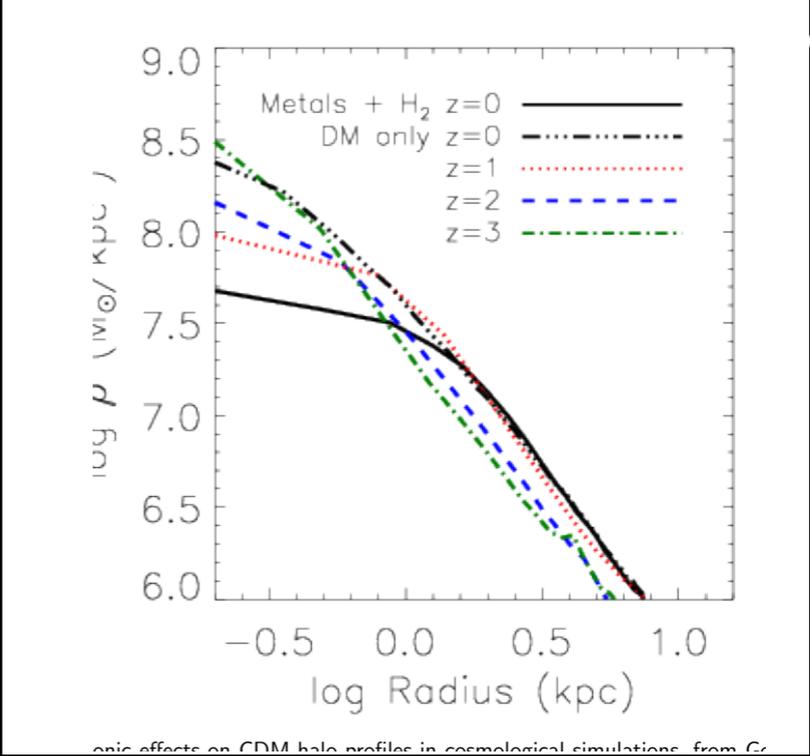
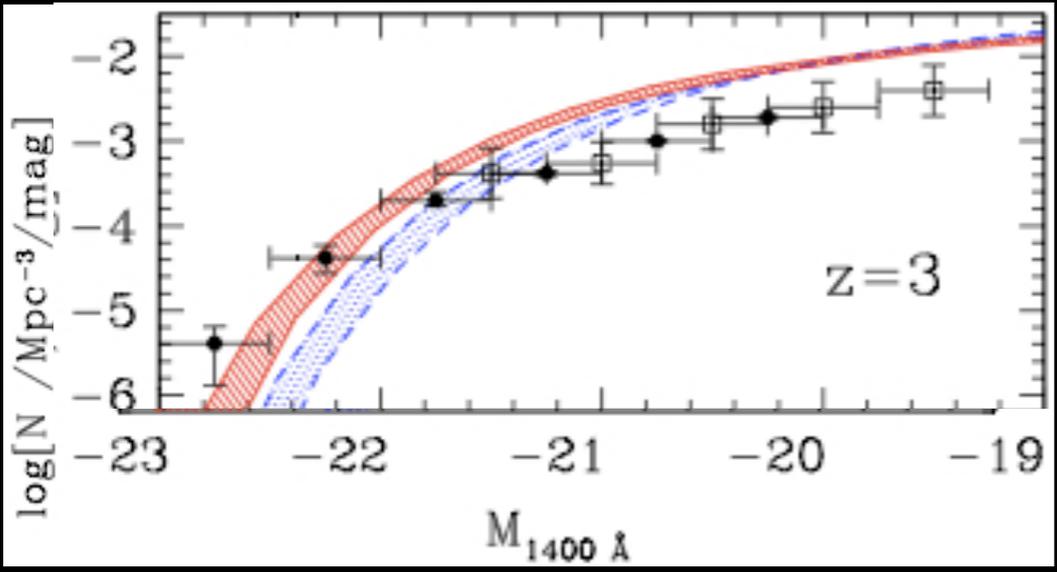


**Fig. 3.** Baryonic effects on CDM halo profiles in cosmological simulations, from Governato et al. (2012). (Left) The upper, dot-dash curve shows the cuspy dark matter density profile resulting from a collisionless N-body simulation. Other curves show the evolution of the dark matter profile in a simulation from the same initial conditions that includes gas dynamics, star formation, and efficient feedback. By  $z = 0$  (solid curve) the perturbations from the fluctuating baryonic potential have flattened the inner profile to a nearly constant density core. (Right) Logarithmic slope of the dark matter profile  $\alpha$  measured at 0.5 kpc, as a function of galaxy stellar mass. Crosses show results from multiple hydrodynamic simulations. Squares show measurements from rotation curves of observed galaxies. The black curve shows the expectation for pure dark matter simulations, computed from NFW profiles with the appropriate concentration. For  $M_* > 10^7 M_\odot$ , baryonic effects reduce the halo profile slopes to agree with observations.

# The problem persists at high redshifts

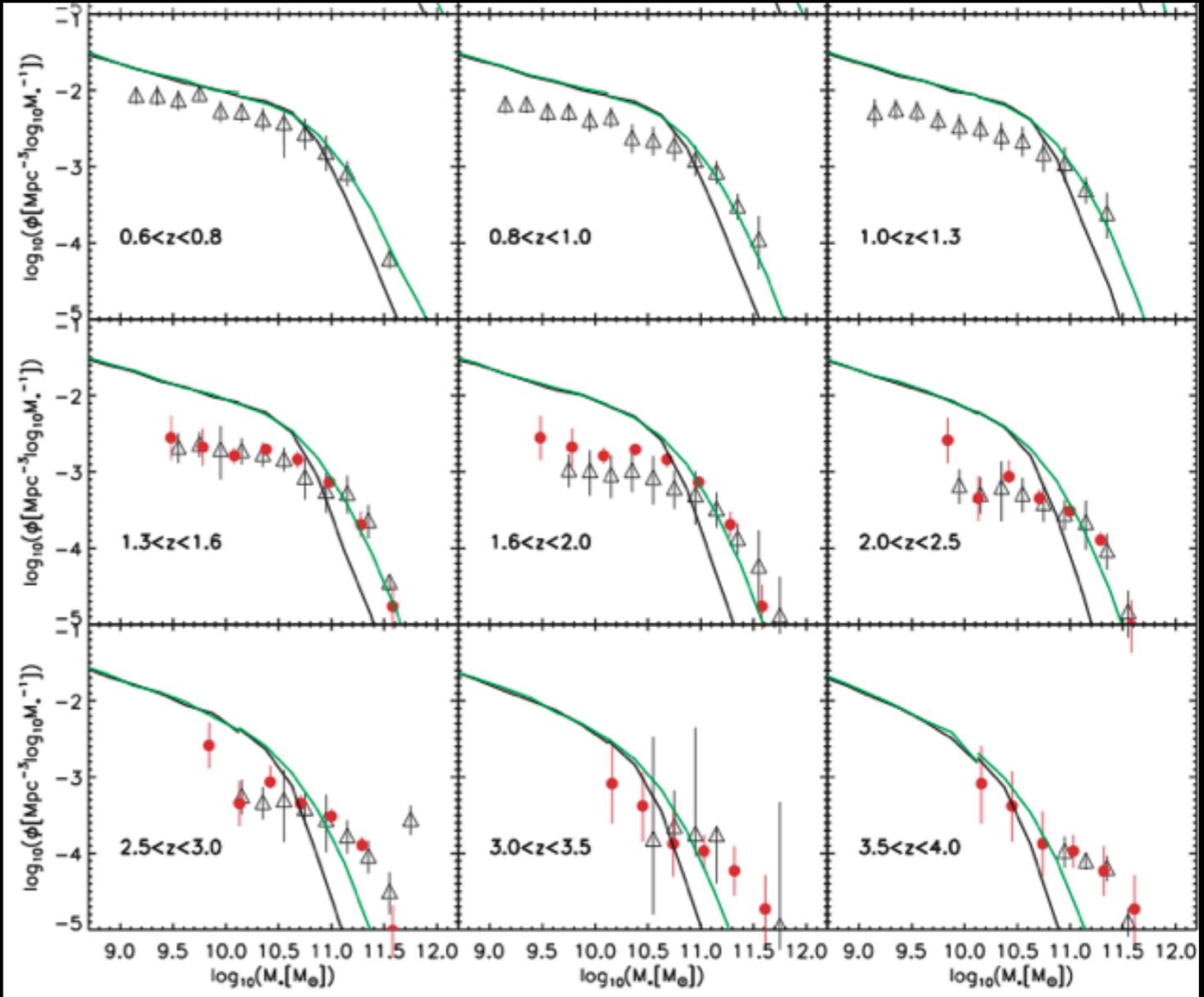
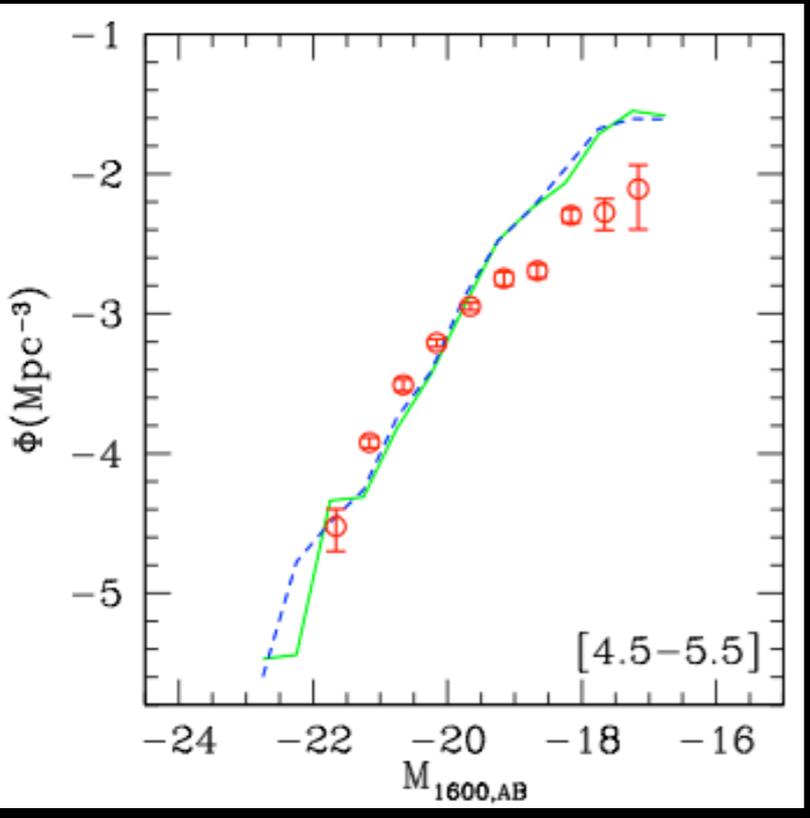
Governato et al. 2012

NM et al. 2006



Guo et al. 2011

Lo Faro et al. 2009



# The problem persists at high redshifts

Corresponds to a mass scale affected by non-gravitational SN energy injection

$$M \approx (v_{esc}^2 / G) r$$

$$r \propto (M/\rho)^{1/3}$$

$$\rho = 180 \rho_u = 180 \rho_u (1+z)^3$$

$$M \approx A v_{esc}^3 (1+z)^{-3/2}$$

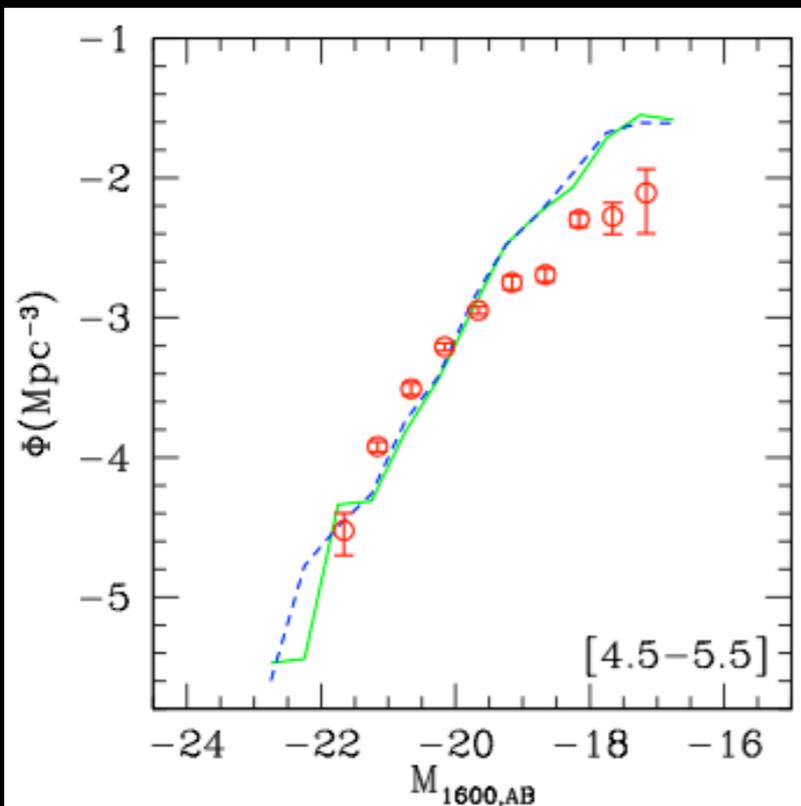
$$A \equiv \sqrt{3/G^3 4\pi \rho_u}$$

$$v_{esc} = v_{SN} \rightarrow M_{SN} \approx A v_{SN}^3 (1+z)^{-3/2}$$

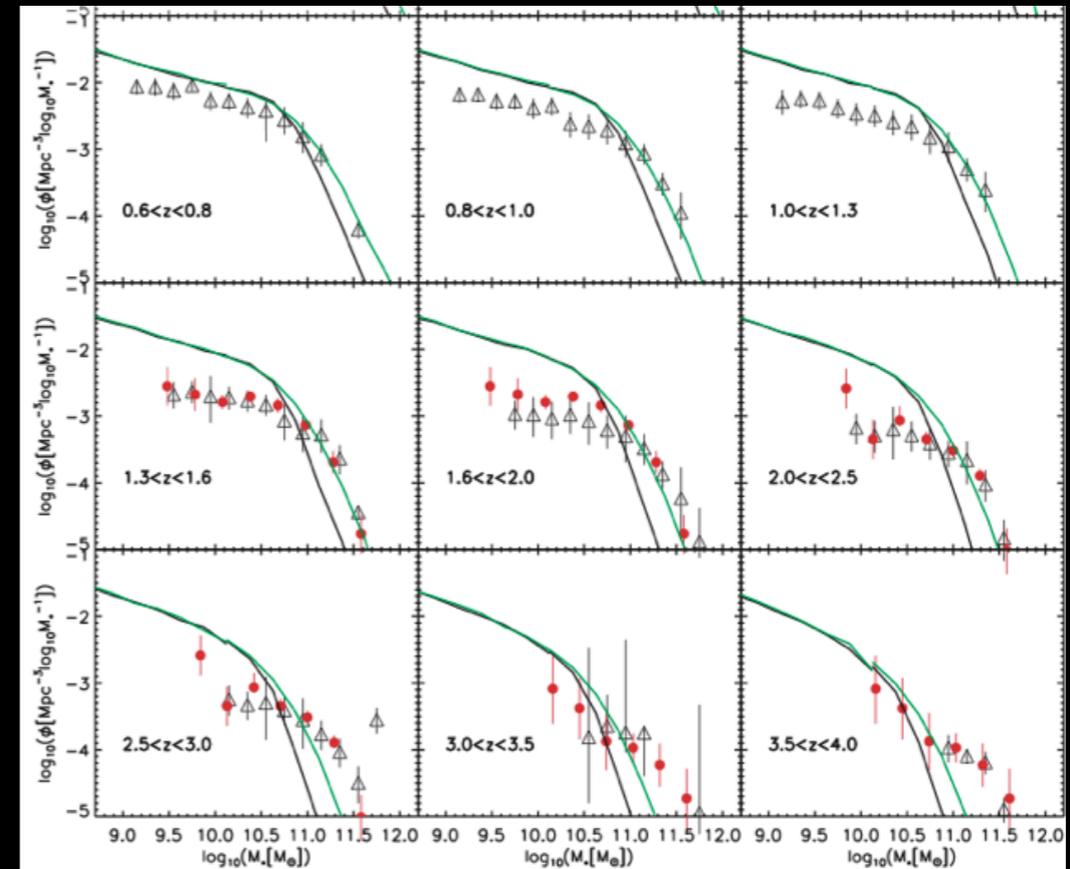
$$\text{at } z \approx 0 \quad M_{SN} \sim 10^{10} M_{\odot}$$

At high- $z$   
larger densities imply  
larger escape velocity  
even for low-mass galaxies  
feedback increasingly  
ineffective

Lo Faro et al. 2009



Guo et al. 2011



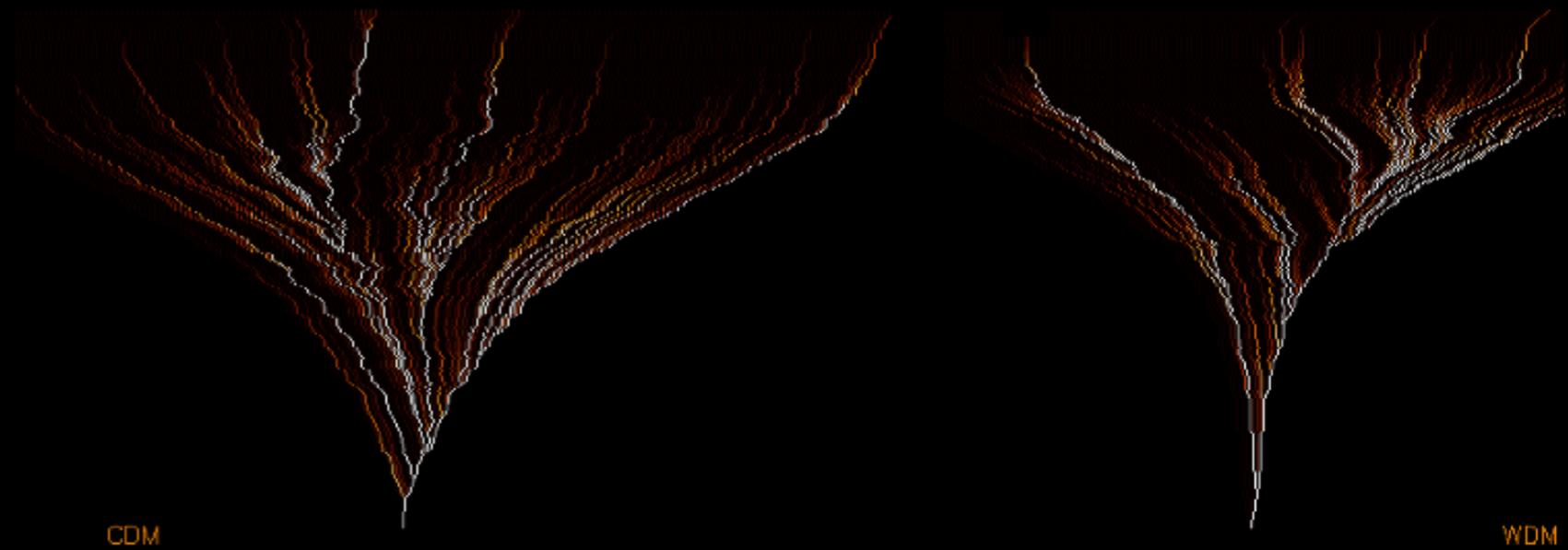
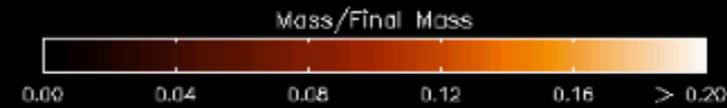
# Galaxy formation in WDM Cosmology

Problem Persists at  
high redshifts

Too many low-mass  
structures

Need to suppress  
Power Spectrum  
at small scales ?

can WDM solve all  
problems  
simultaneously ?



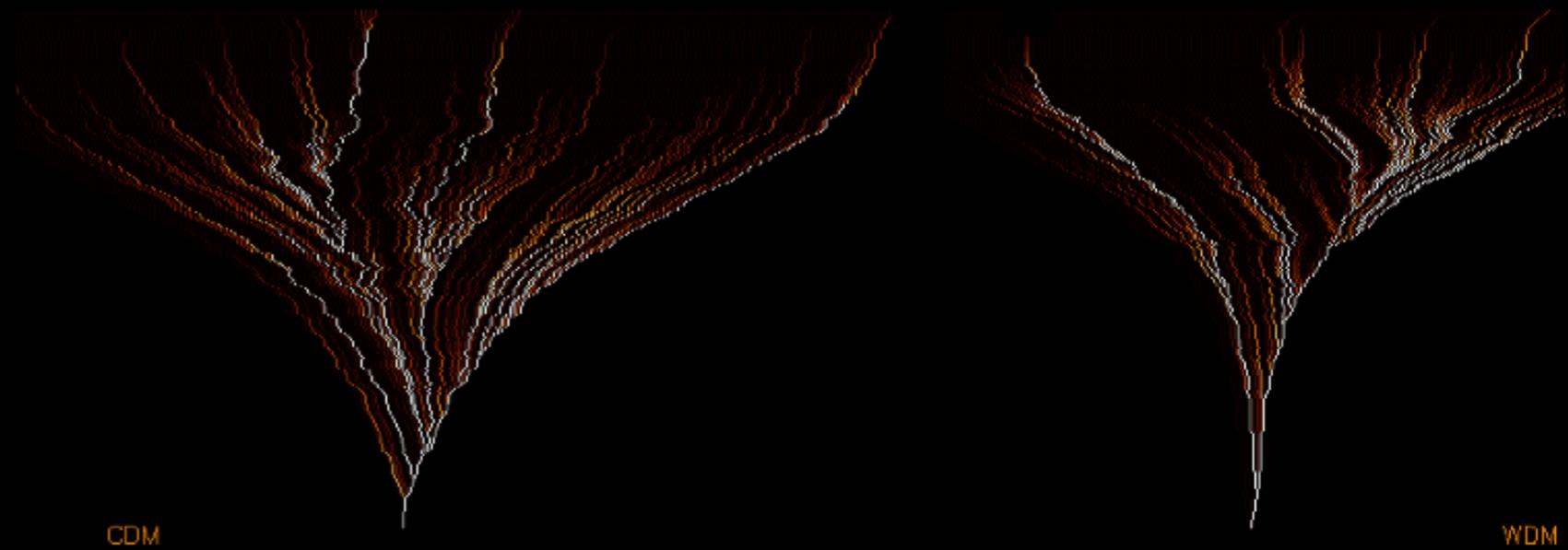
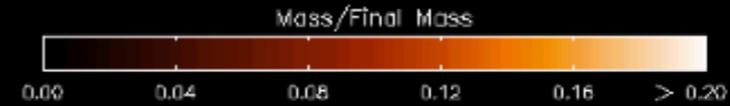
# Galaxy formation in WDM Cosmology

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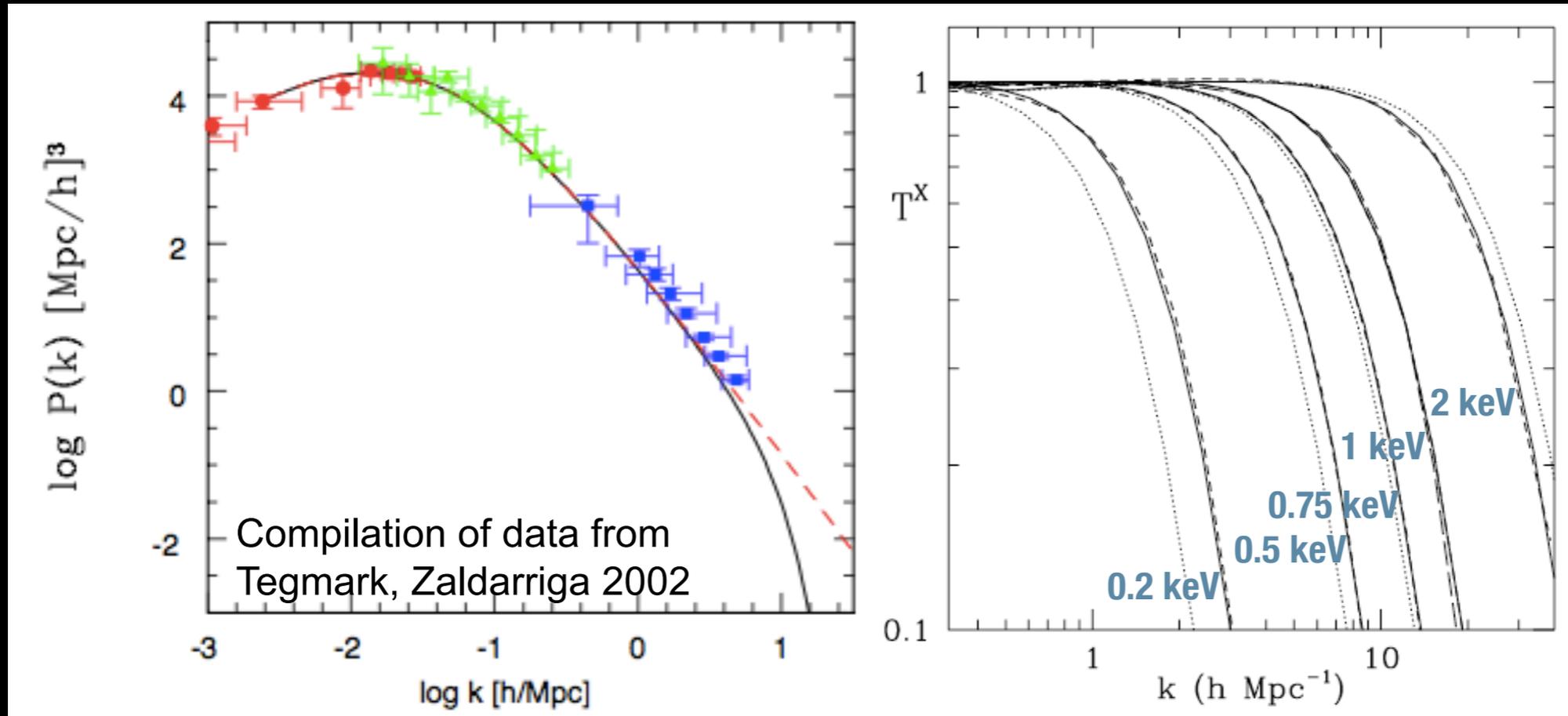
can WDM solve all problems simultaneously ?



Rome PANDA model

NM, A. Lamstra

# Implementing WDM power spectrum in the galaxy formation model



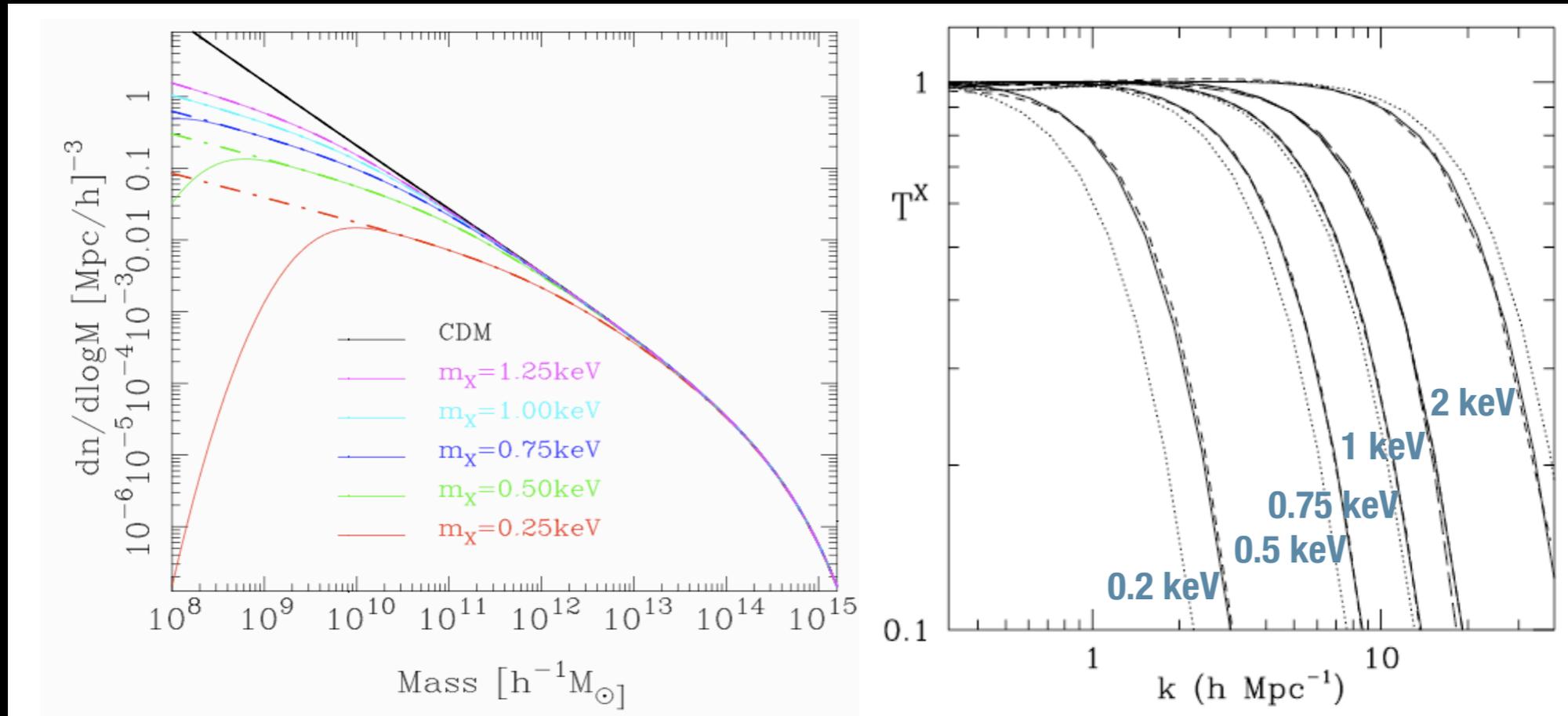
To explore the maximal effect of a power-spectrum cutoff on galaxy formation, we consider a cutoff at scales just below 0.2 Mpc, where data from Lyman- $\alpha$  systems (compared to N-body simulations) yields stringer upper limits on power suppression. This corresponds to mass scales  $M_{fs} \sim 5 \cdot 10^8 M_{\odot}$

$$r_{fs} \approx 0.2 \left[ \frac{\Omega_X h^2}{0.15} \right]^{1/3} \left[ \frac{m_X}{rmkeV} \right]^{-4/3} \text{ Mpc} \quad \frac{P_{WDM}(k)}{P_{CDM}(k)} = \left[ 1 + (\alpha k)^{2\mu} \right]^{-5\mu}$$

$$\alpha = 0.049 \left[ \frac{\Omega_X}{0.25} \right]^{0.11} \left[ \frac{m_X}{keV} \right]^{-1.11} \left[ \frac{h}{0.7} \right]^{1.22} h^{-1} \text{ Mpc}$$

WDM  
particle mass  
1 keV

# Implementing WDM power spectrum in the galaxy formation model



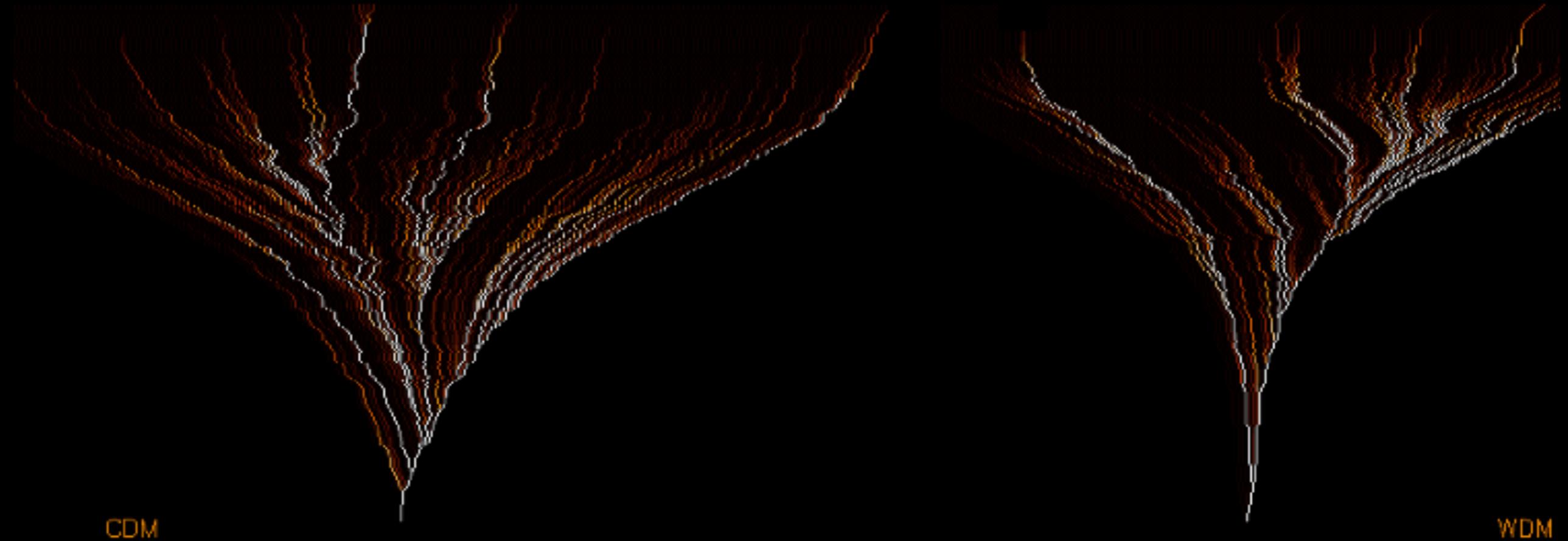
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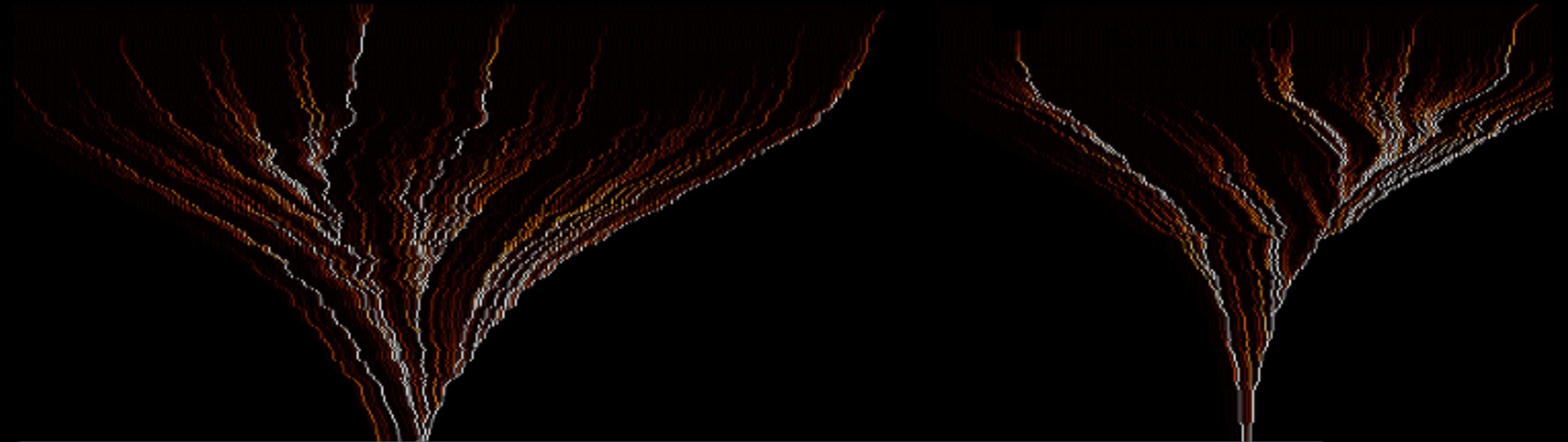
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WDM  
particle mass  
1 keV

# Implementing WDM power spectrum in the galaxy formation model



Halo Properties

Density Profiles

Virial Temperature

Gas Properties

Profiles

Cooling - Heating

Collapse

Disk formation

Star Formation

Gas Heating (feedback)

SNae

UV background

Evolution of stellar

populations

WDM

Galaxy formation in WDM implies computing how modifications of the power spectrum propagate to the above processes

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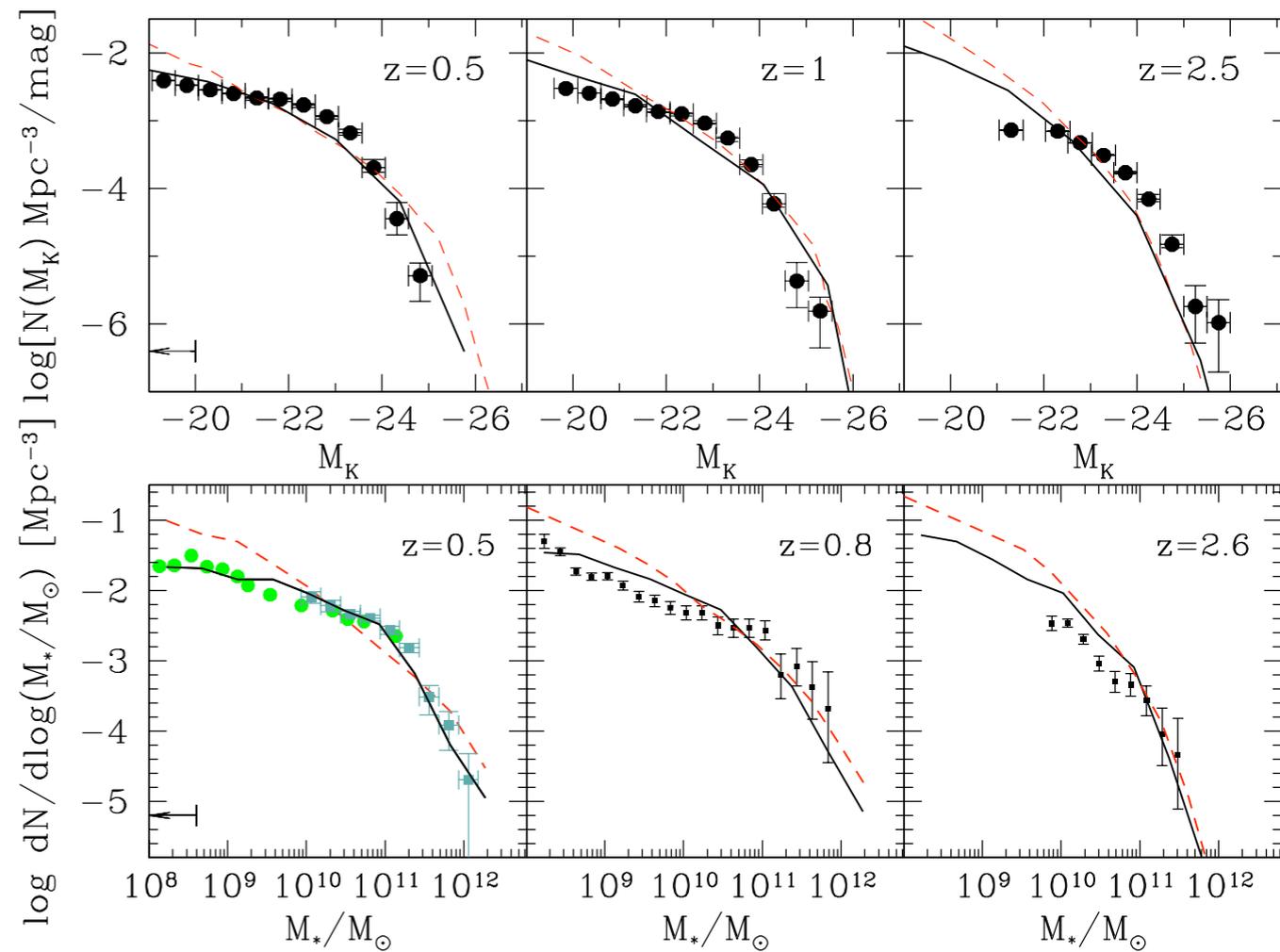
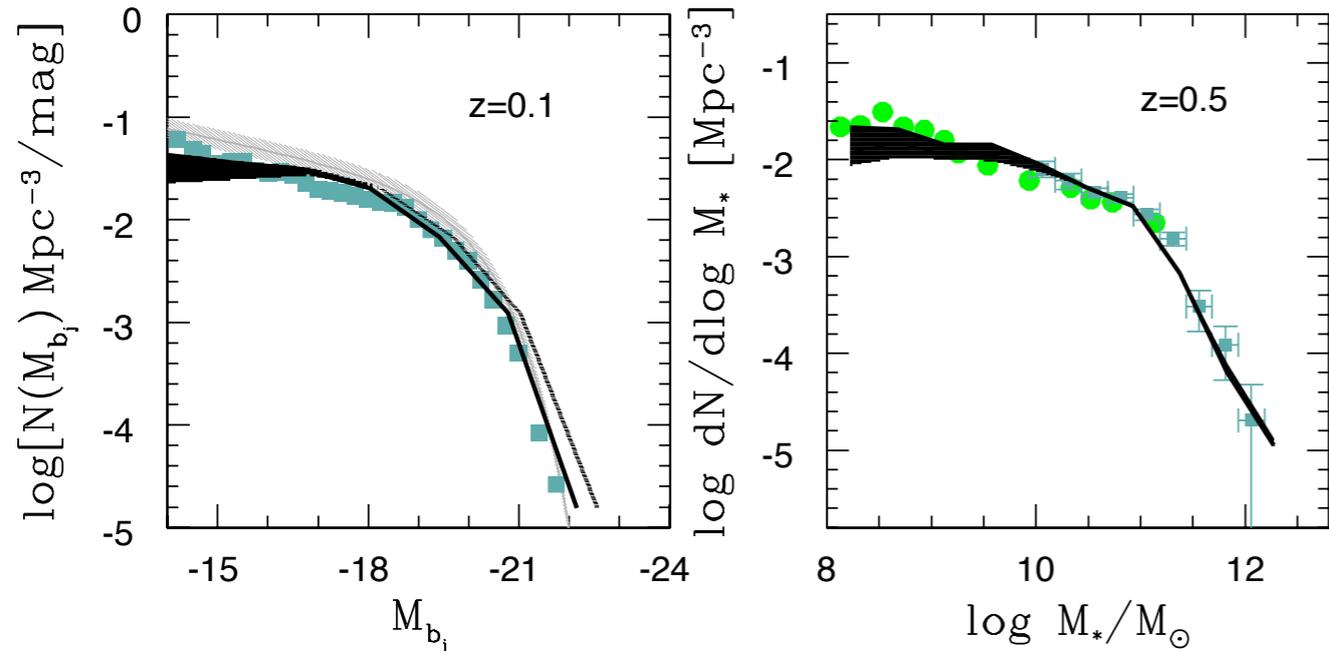
WDM  
particle mass  
1 keV

# Galaxy Formation in WDM cosmology ( $m_{\text{WDM}} \sim 1$ keV)

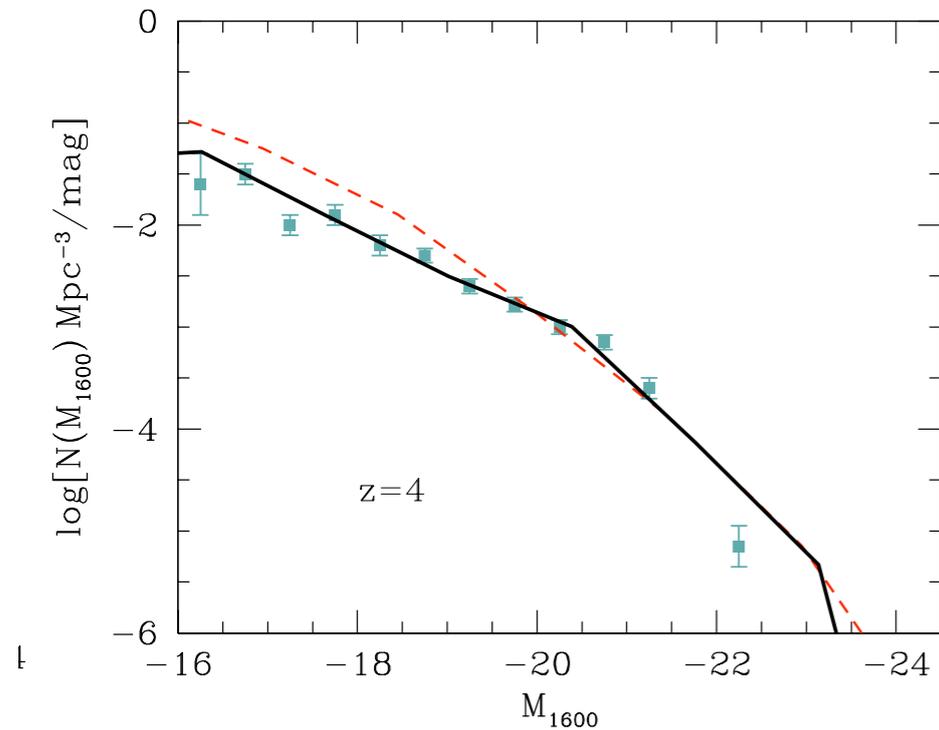
NM et al. 2012-2013

## Evolution

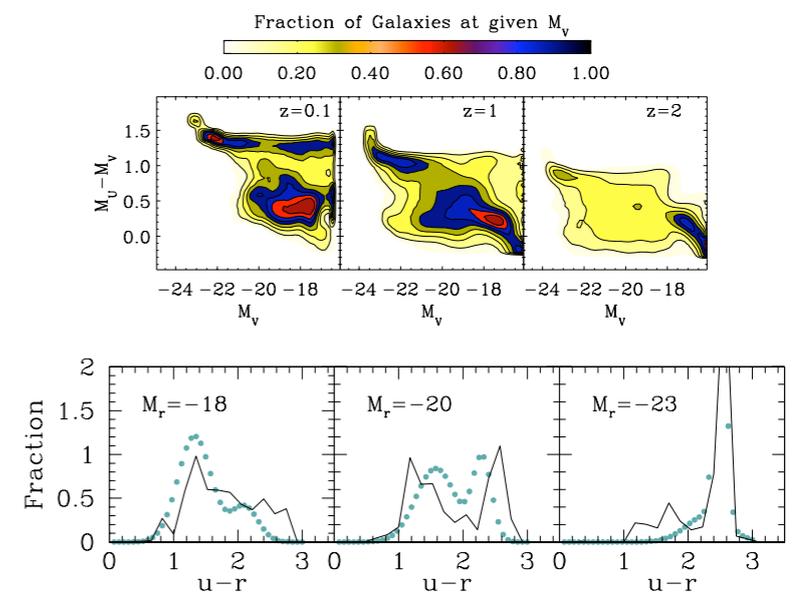
### local lum. and stell. mass distributions



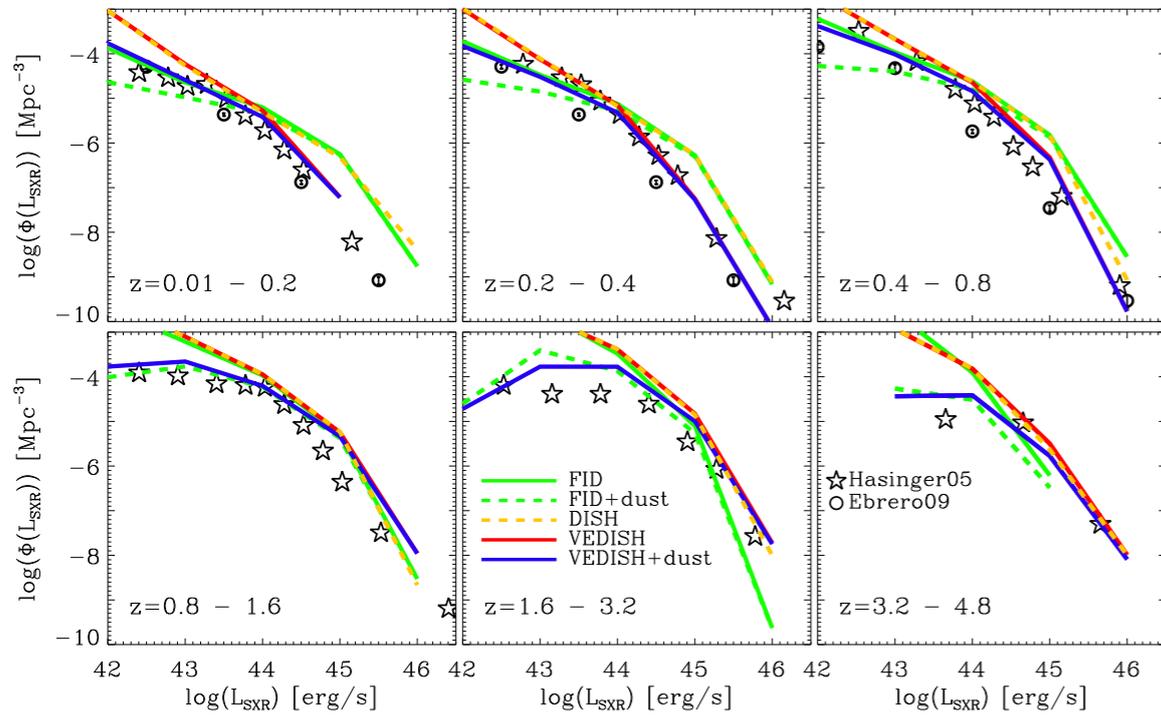
### High-z ( $z=4$ ) lum. distributions



### color distributions

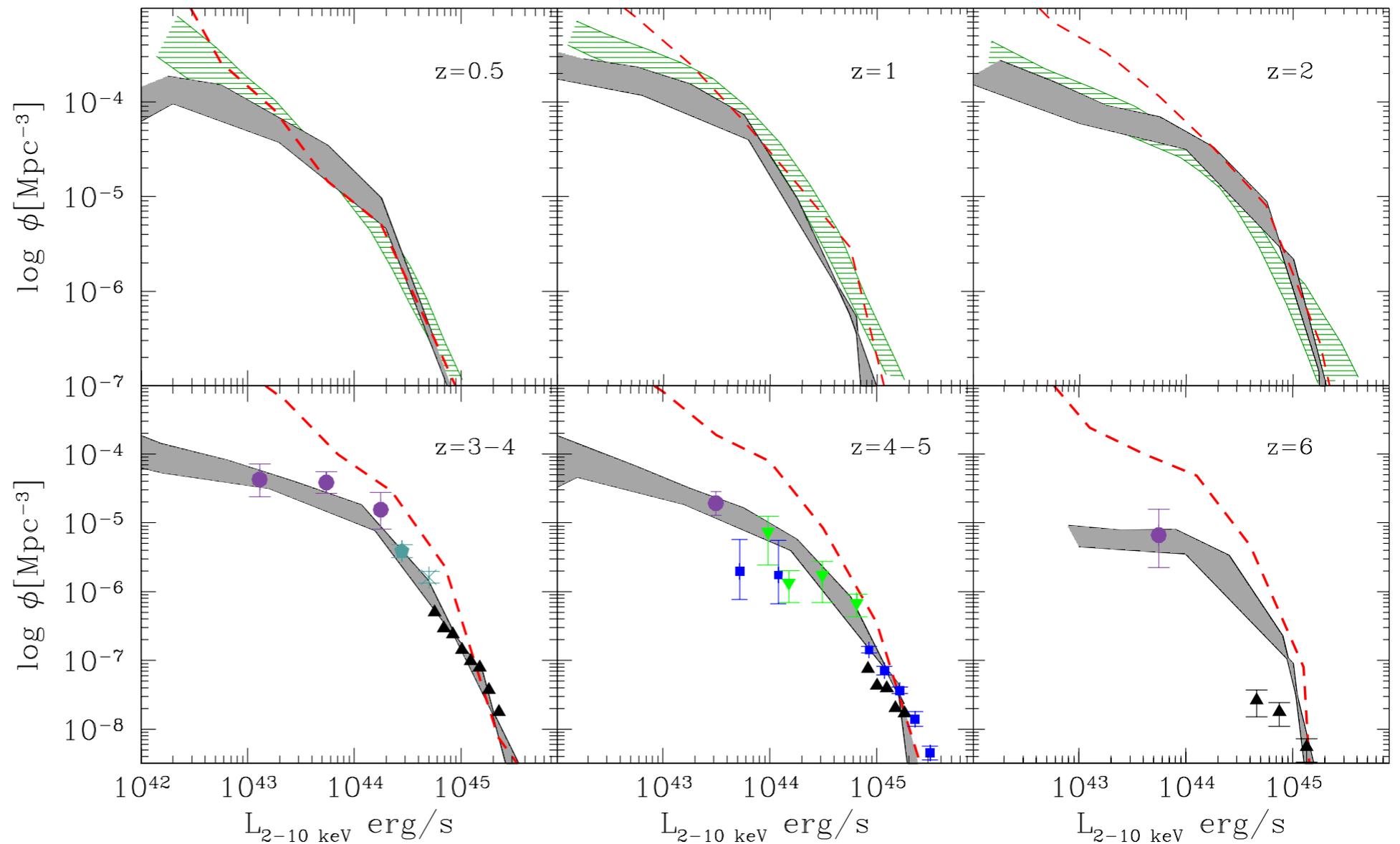


# CDM models overestimate faint AGN abundance at high z

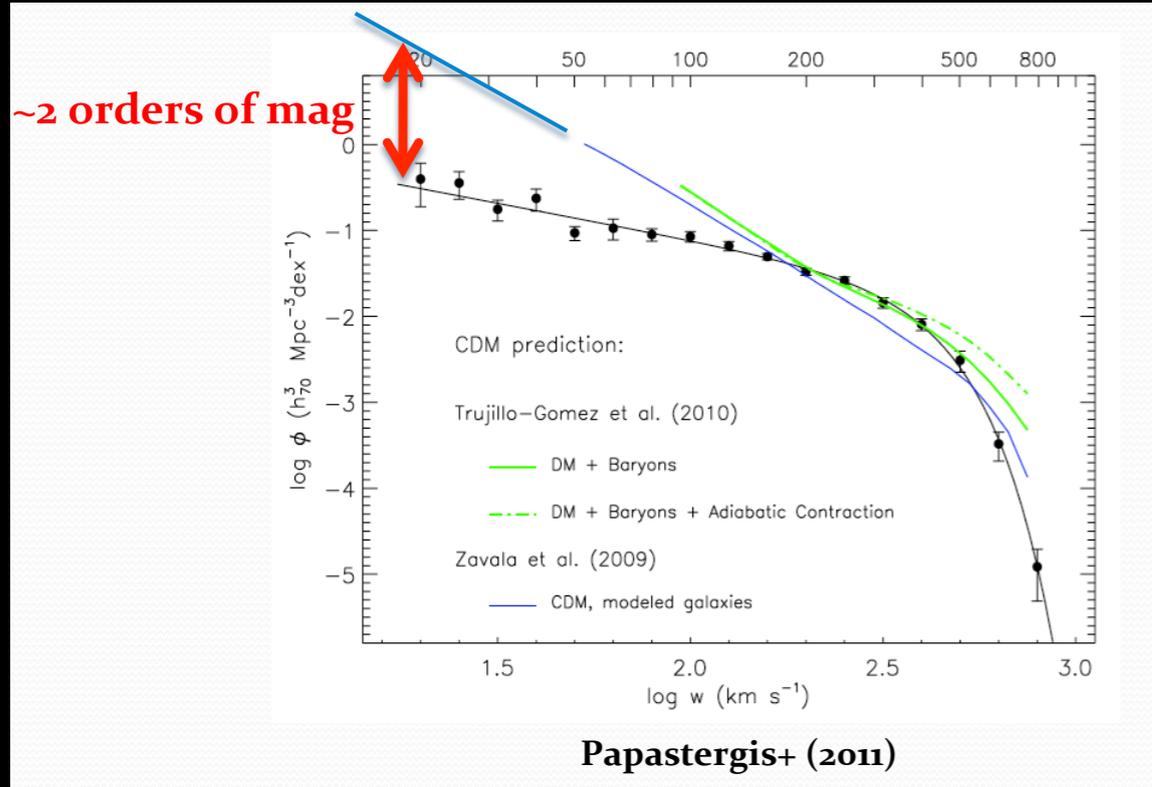


NM, Fiore, Lamastra 2013

Hirschmann et al. 2012



# Abundance of galaxies as a function of their velocity width (gas rotation velocity)

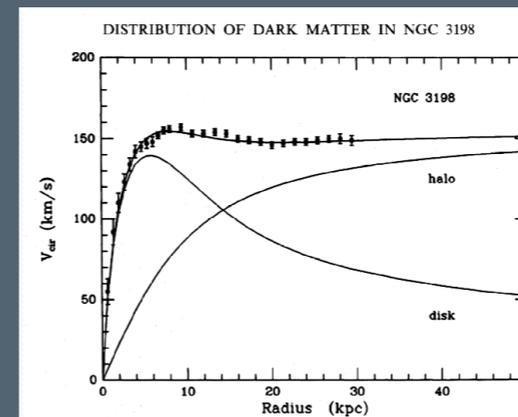


21-cm survey done with Arecibo Telescope: 3000 deg<sup>2</sup>; 11000 detections  
 measures: redshift, velocity width, integrated flux  
 No spatial resolution (size, inclination, shape)

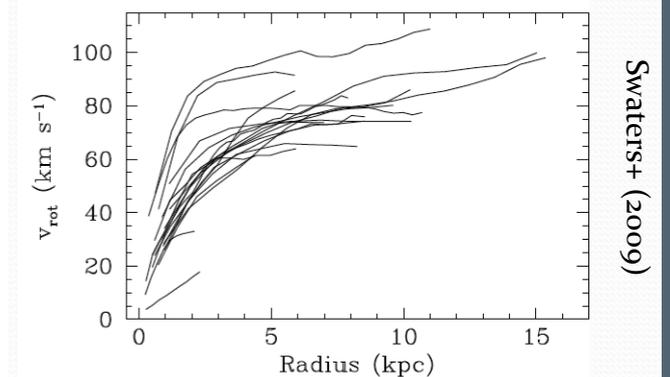
Directly measures the depth of the potential well:  
 less prone to physics of gas (feedback)

## Solutions within CDM scenario ?

- large fraction of galaxies with low gas content (below the sensitivity)
- large fraction of galaxies with rising rotation curve

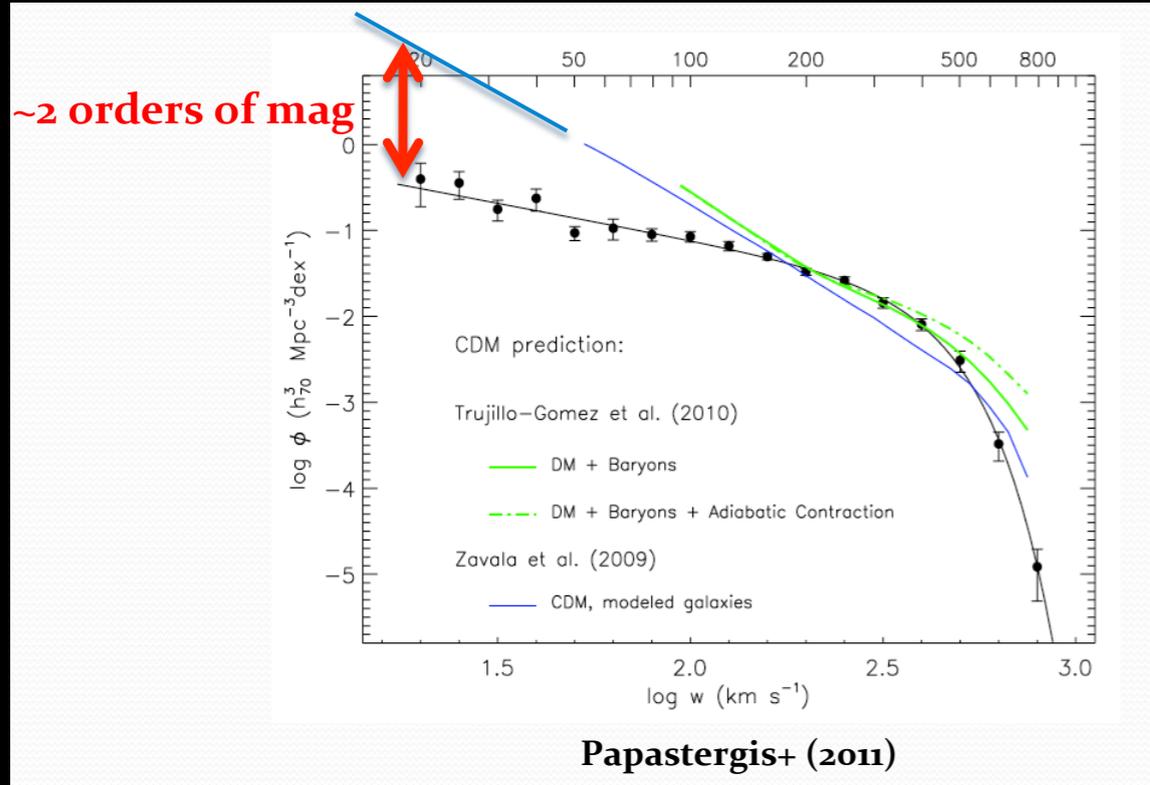


'flat' rotation curve



'rising' rotation curves

# Abundance of galaxies as a function of their velocity width (gas rotation velocity)



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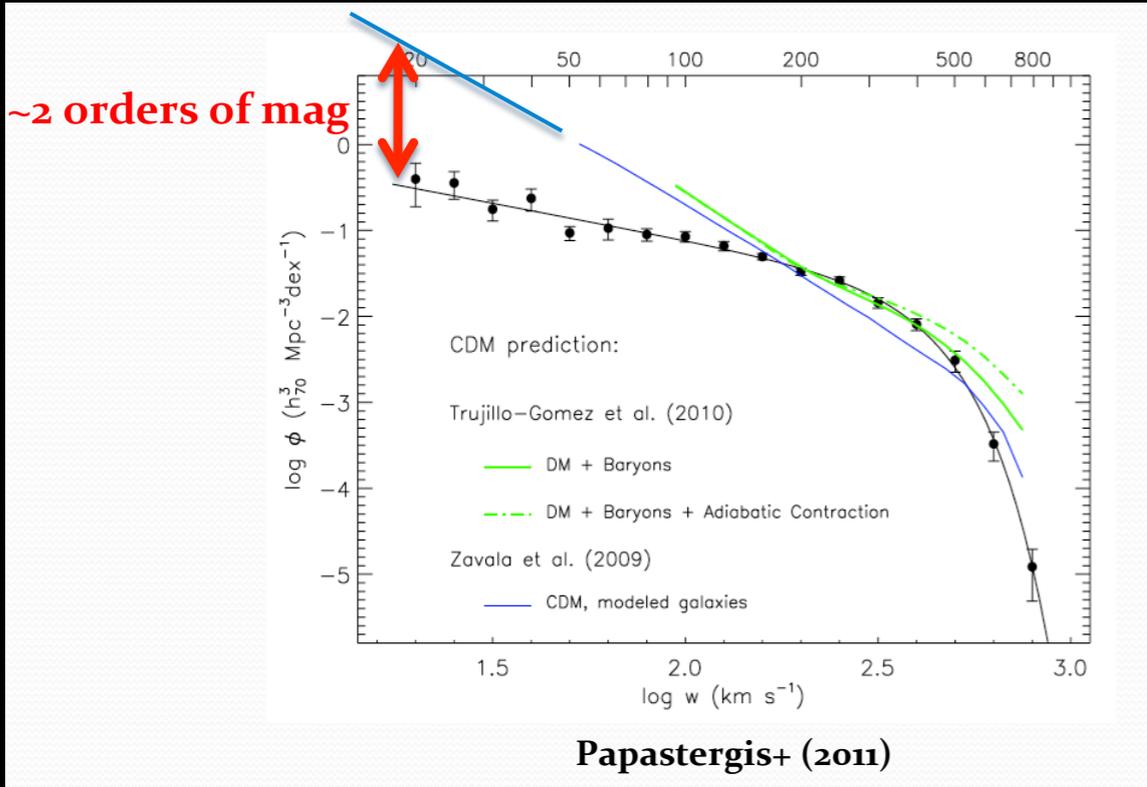
Directly measures  
the depth of the potential well:  
less prone to physics of gas (feedback)

At high redshift, galaxies are denser

Difficult to expel gas from such compact objects

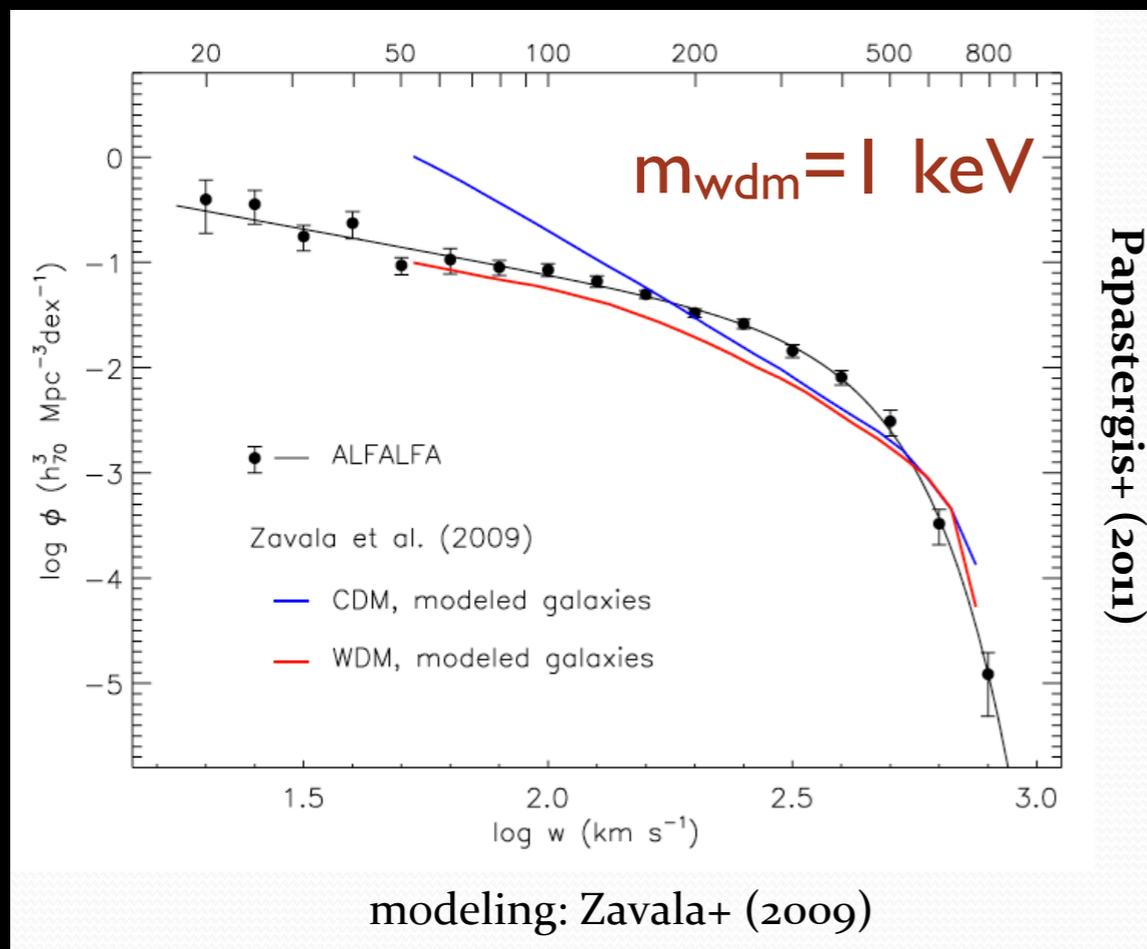
Even with maximized feedback, current models still over estimate the number of small mass galaxies

# Abundance of galaxies as a function of their velocity width (gas rotation velocity)



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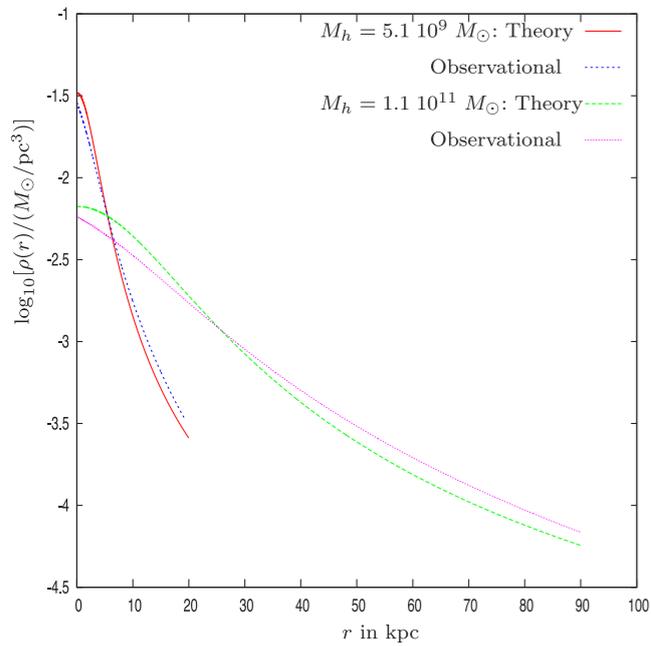
Directly measures the depth of the potential well: less prone to physics of gas (feedback)



WDM naturally yields a flat distribution  
 Zavala et al. 2009

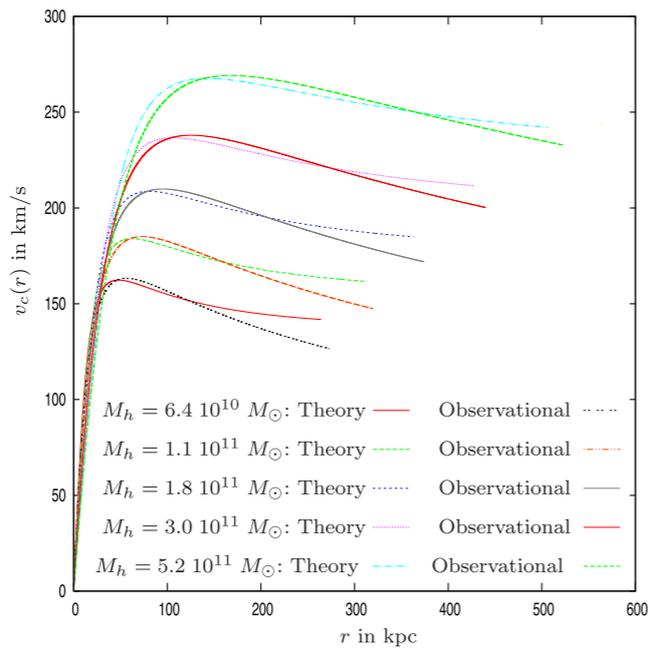
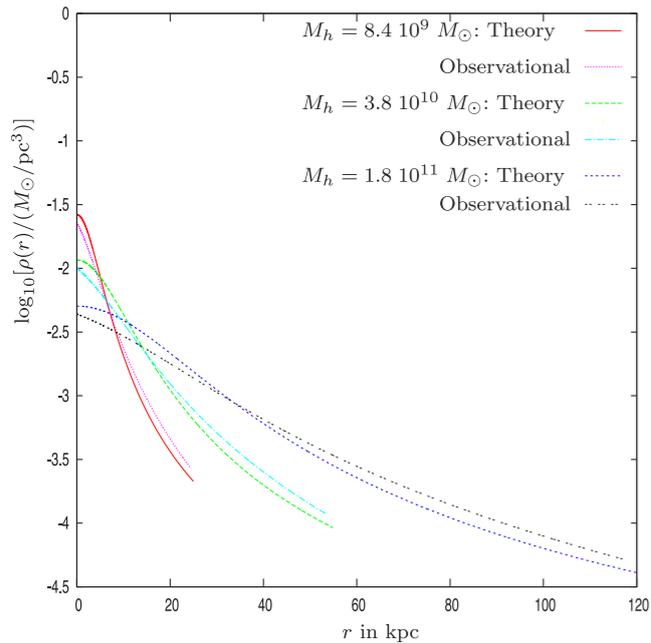
# Substructures, Density profiles, Rotation curves in WDM

## Density Profiles



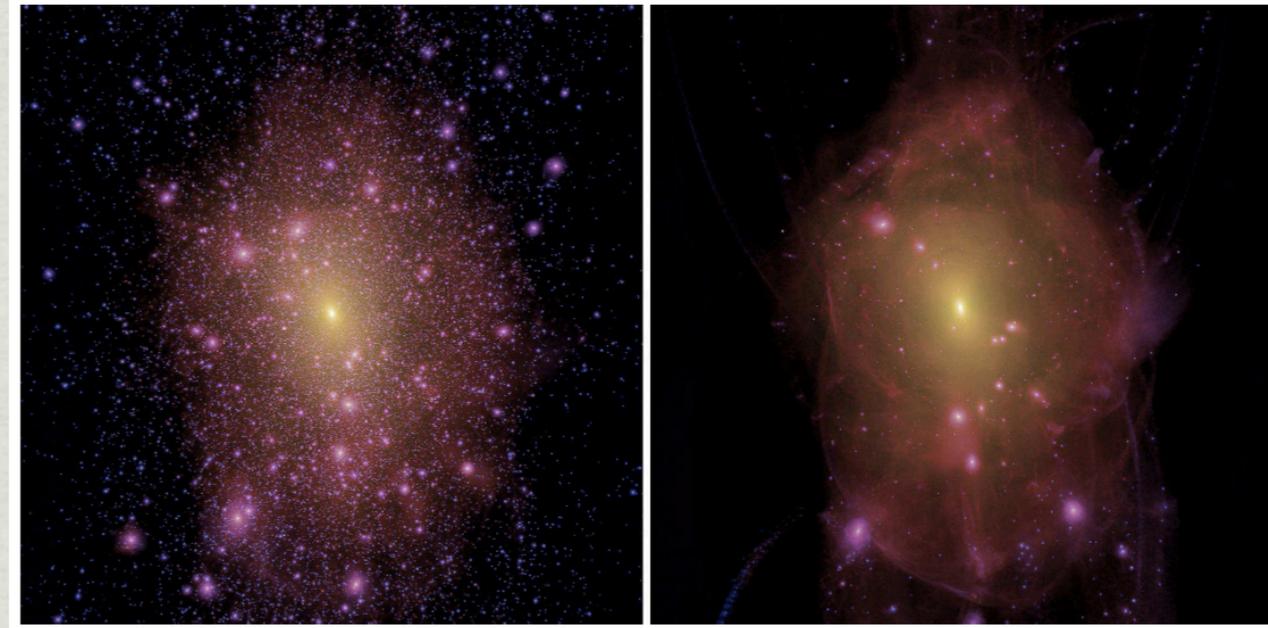
De Vega, Salucci, Sanchez 2014  
Fermionic WDM

## Rotation Curves

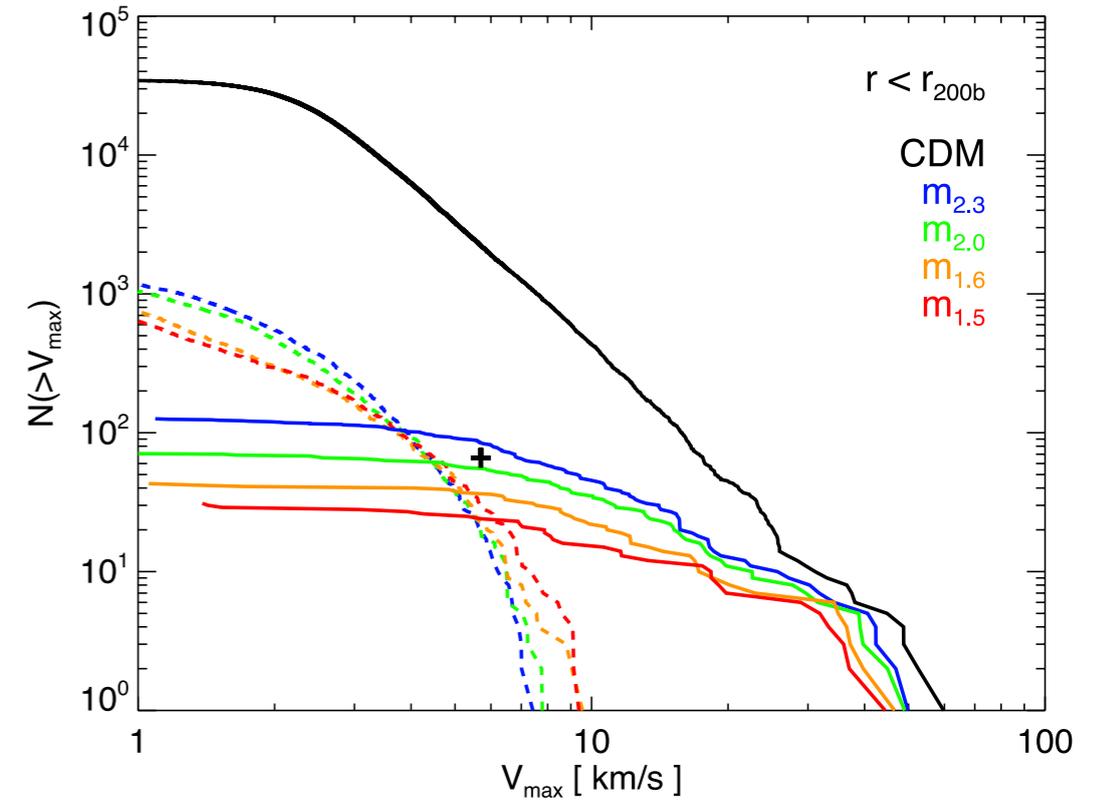


CDM

WDM

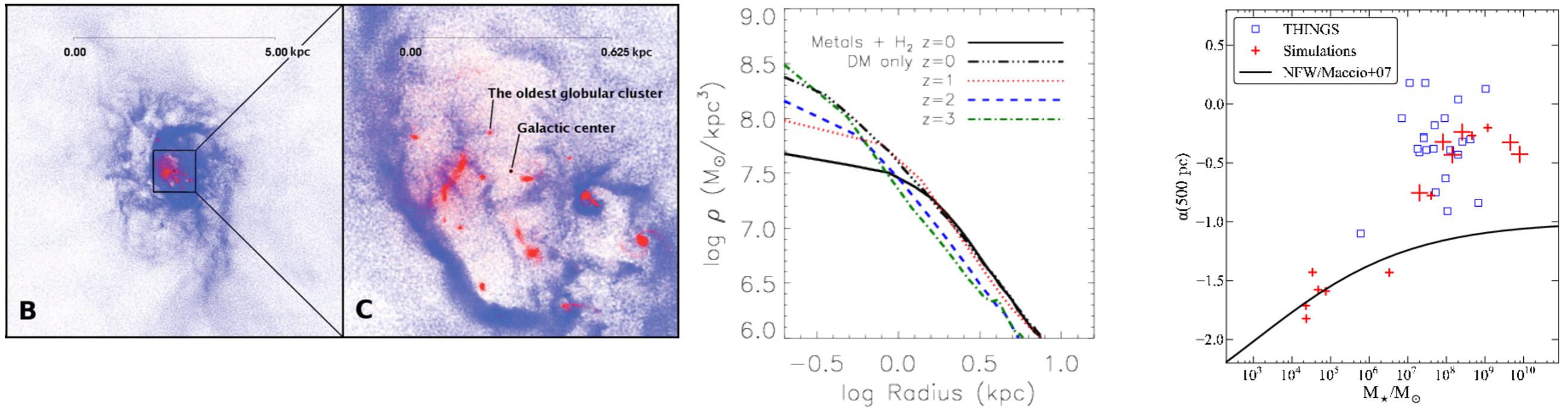


LOVELL ET AL. 2013



**Figure 11.** Cumulative subhalo mass,  $M_{\text{sub}}$ , (top panel) and  $V_{\text{max}}$  (bottom panel) functions of subhaloes within  $r < r_{200b}$  of the main halo centre in the HRS at  $z = 0$ . Solid lines correspond to genuine subhaloes and dashed lines to spurious subhaloes. The black line shows results for CDM-W7 and the coloured lines for the WDM models, as in Fig. 1. The black cross in the lower panel indicates the expected number of satellites of  $V_{\text{max}} > 5.7 \text{ km s}^{-1}$  as derived in the text.

# Disentangling feedback effects from WDM

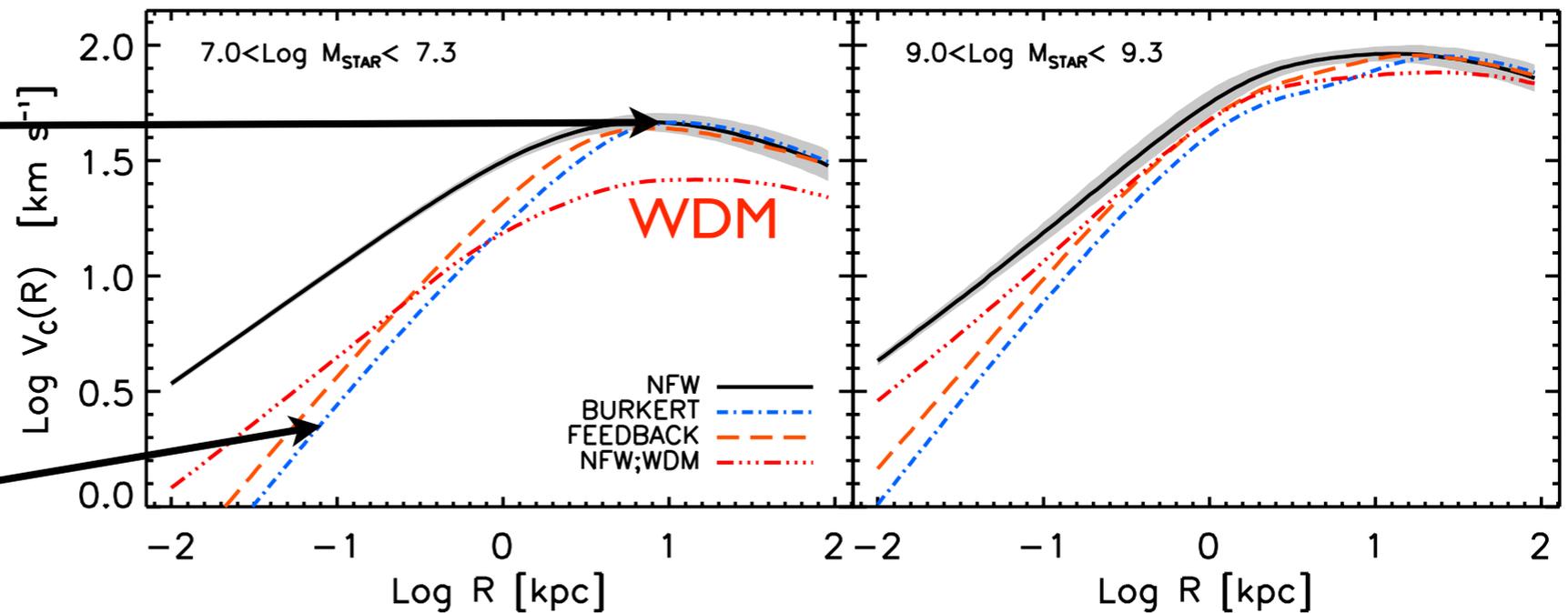


**Fig. 3.** Baryonic effects on CDM halo profiles in cosmological simulations, from Governato et al. (2012). (*Left*) The upper, dot-dash curve shows the cuspy dark matter density profile resulting from a collisionless N-body simulation. Other curves show the evolution of the dark matter profile in a simulation from the same initial conditions that includes gas dynamics, star formation, and efficient feedback. By  $z = 0$  (solid curve) the perturbations from the fluctuating baryonic potential have flattened the inner profile to a nearly constant density core. (*Right*) Logarithmic slope of the dark matter profile  $\alpha$  measured at 0.5 kpc, as a function of galaxy stellar mass. Crosses show results from multiple hydrodynamic simulations. Squares show measurements from rotation curves of observed galaxies. The black curve shows the expectation for pure dark matter simulations, computed from NFW profiles with the appropriate concentration. For  $M_* > 10^7 M_\odot$ , baryonic effects reduce the halo profile slopes to agree with observations.

In the outer region  
profiles with  
feedback are close  
to CDM NFW

Feedback acts in the  
inner regions

Shankar+ 2014



# Matching the $V_{\max}$ - $M^*$ relation

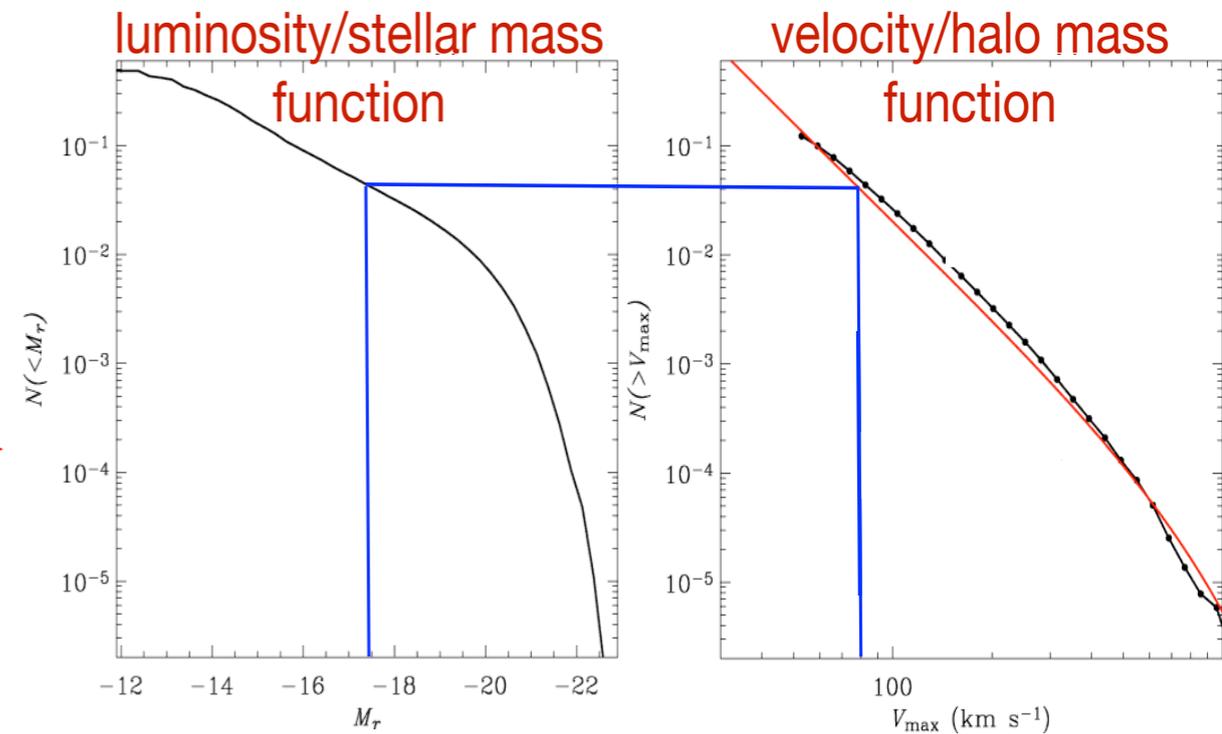
A semi-empirical approach (Shankar et al. 2014)

1. select a sample of DM haloes
2. associate to each halo a galaxy of a given stellar mass according to an abundance matching relation
3. compute rotation velocity curves for each DM halo (for WDM adopt the  $c(M_h)$  relation by Schneider et al 2012 for 1 keV thermal relic DM)
4. infer predicted  $V_{\max}$ - $M^*$  relation (computed at maximum of the rotation curve)

# Matching the $V_{\max}$ - $M^*$ relation

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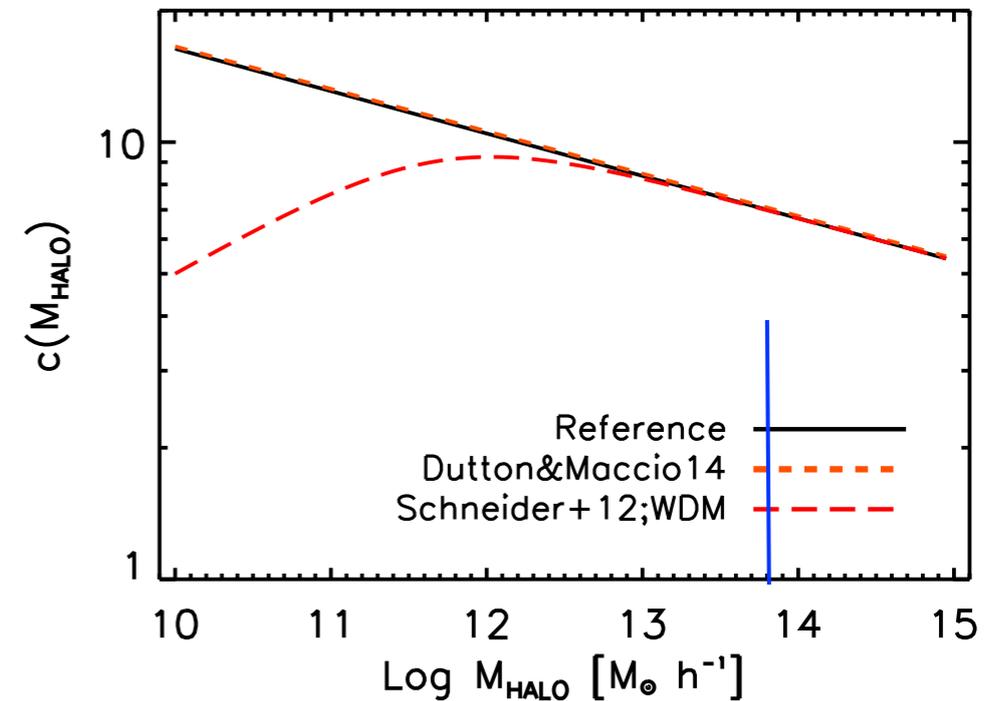
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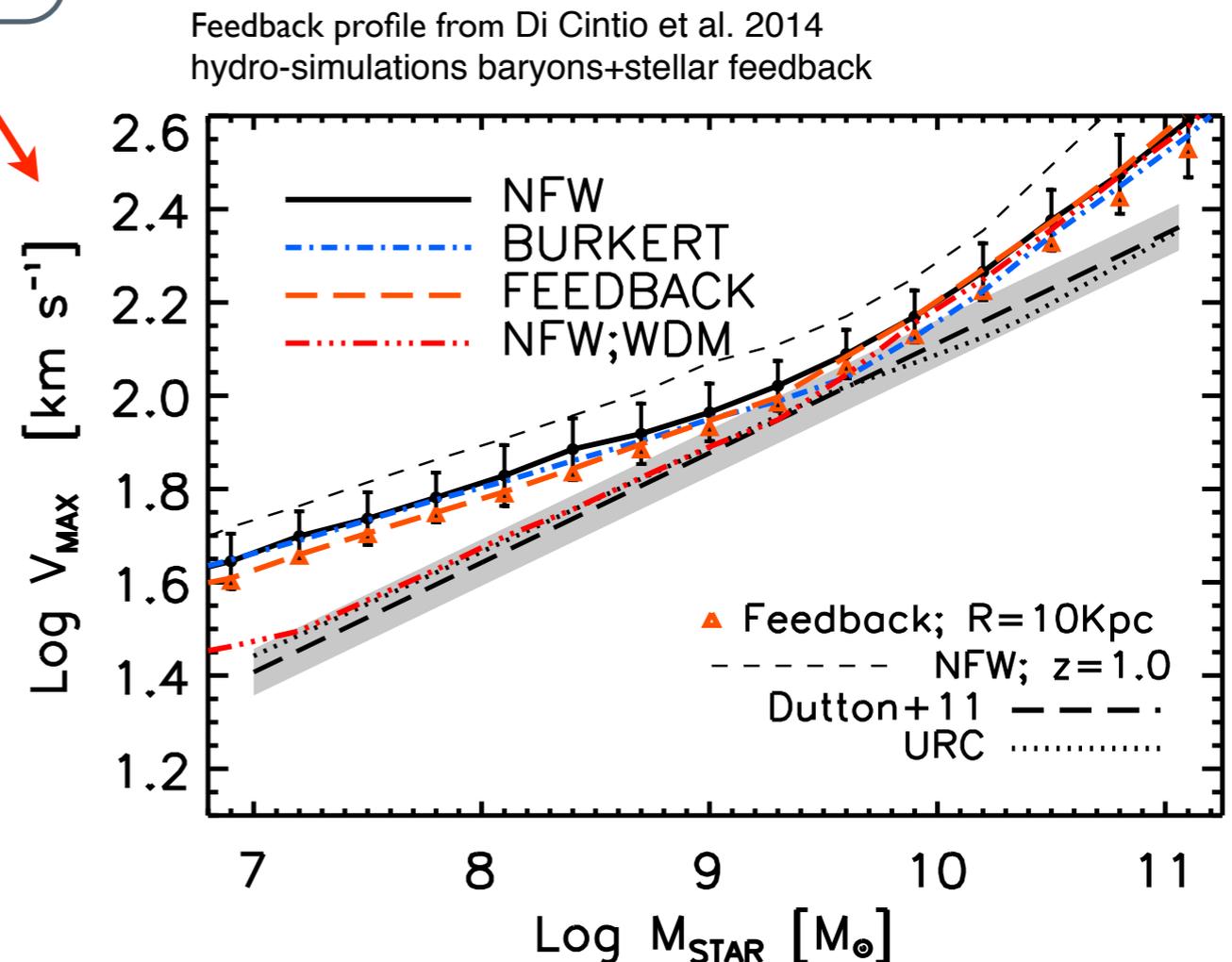
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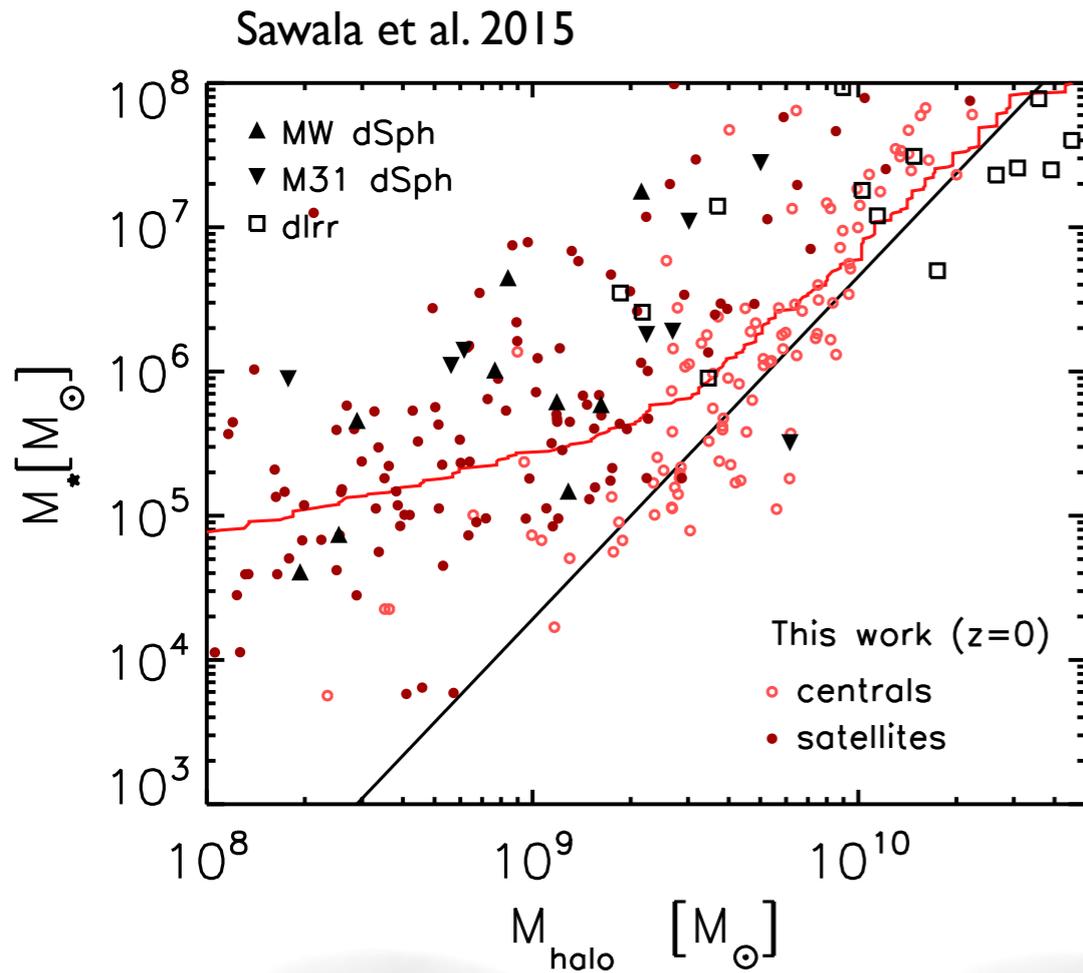
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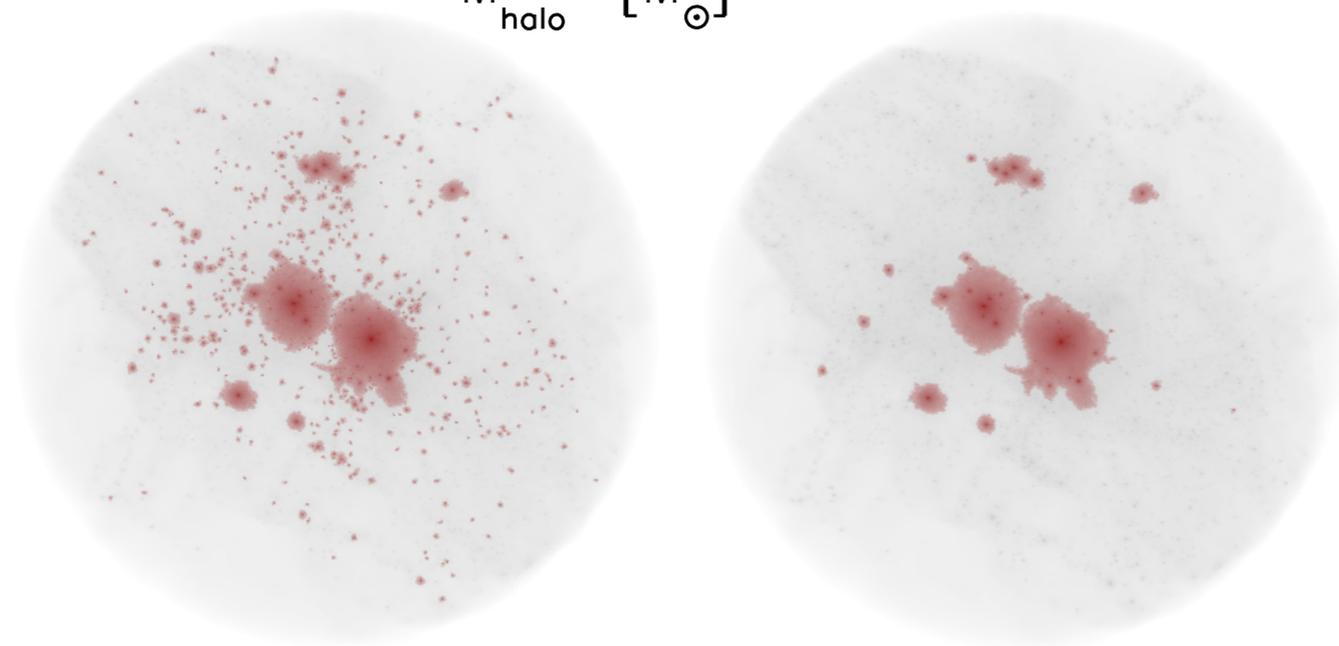
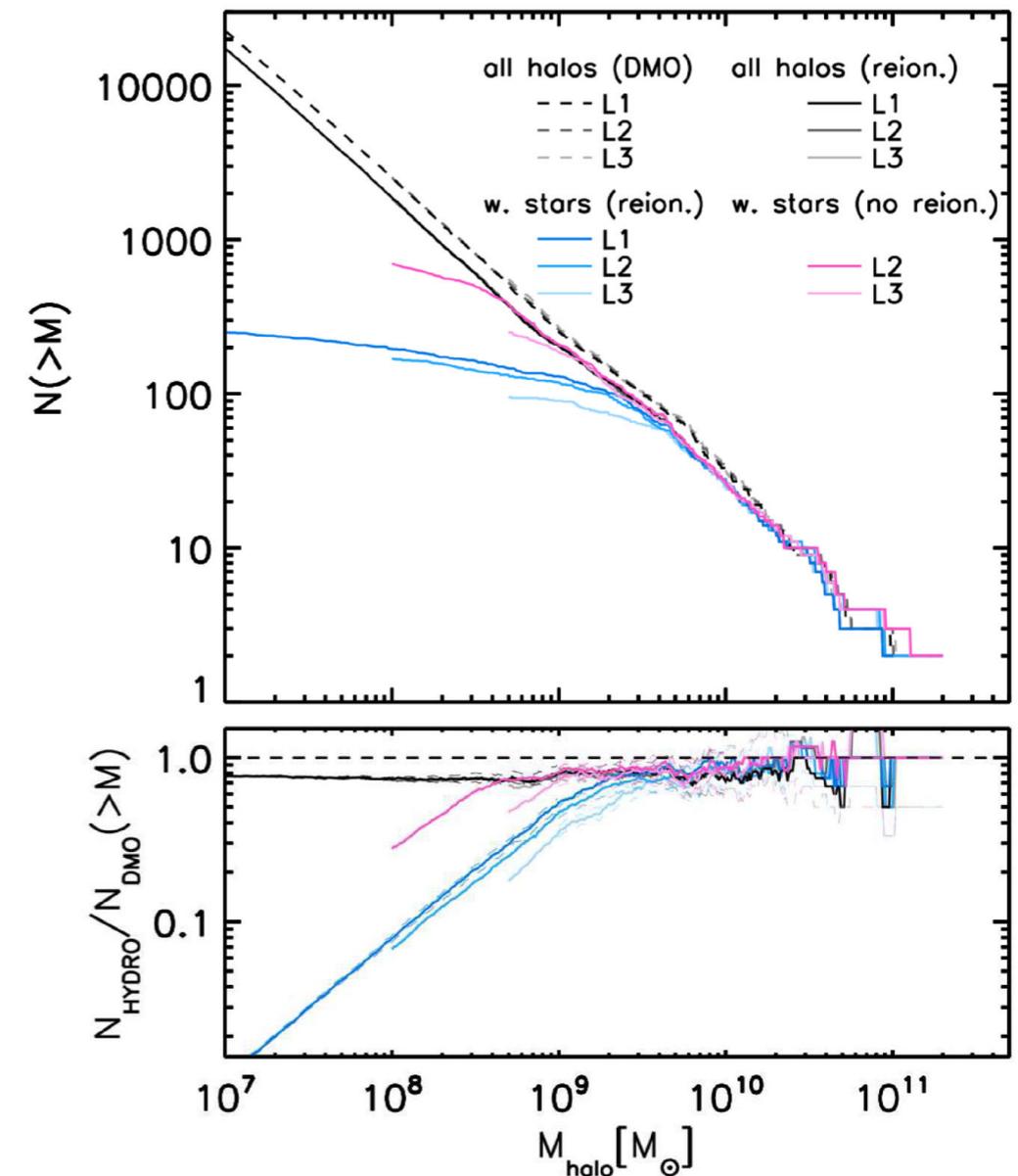


# Solution in CDM scenario

most low-mass haloes do not contain galaxies due to the effect of UV background, feedback and reionization (assuming no self-shielding and H<sub>2</sub> cooling)



Milky-Way like haloes should contain thousands of dark haloes (with no stars or gas)



**Figure 1.** Projected density distribution of dark matter within 2 Mpc around the simulated Milky Way – M31 barycentre at  $z = 0$  from one of our simulation volumes. Highlighted in red on top of the total mass distribution are particles in haloes above  $5 \times 10^7 M_\odot$  (left-hand panel), and particles in just those haloes that contain stars (right-hand panel).

# Luminosity Function of Satellite Galaxies

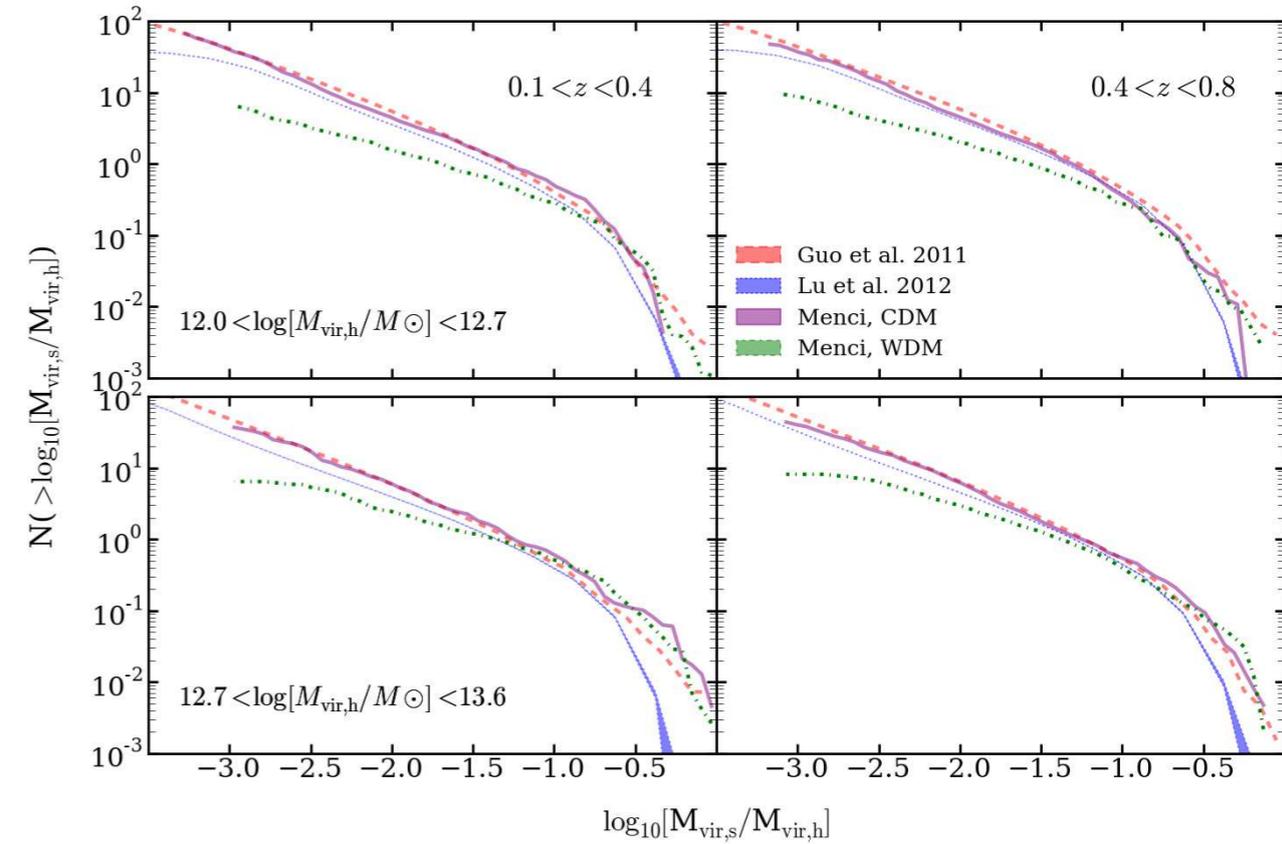
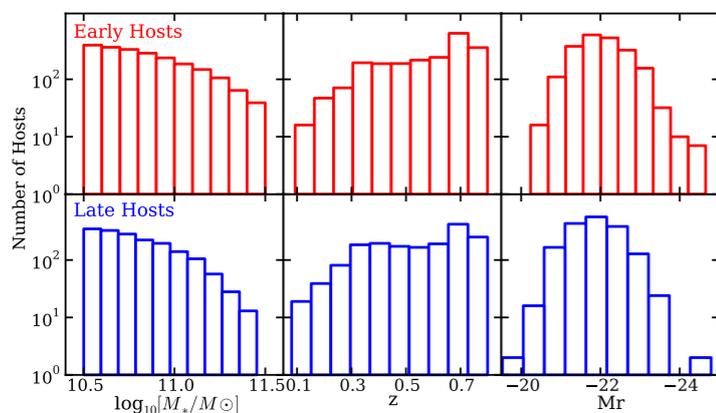
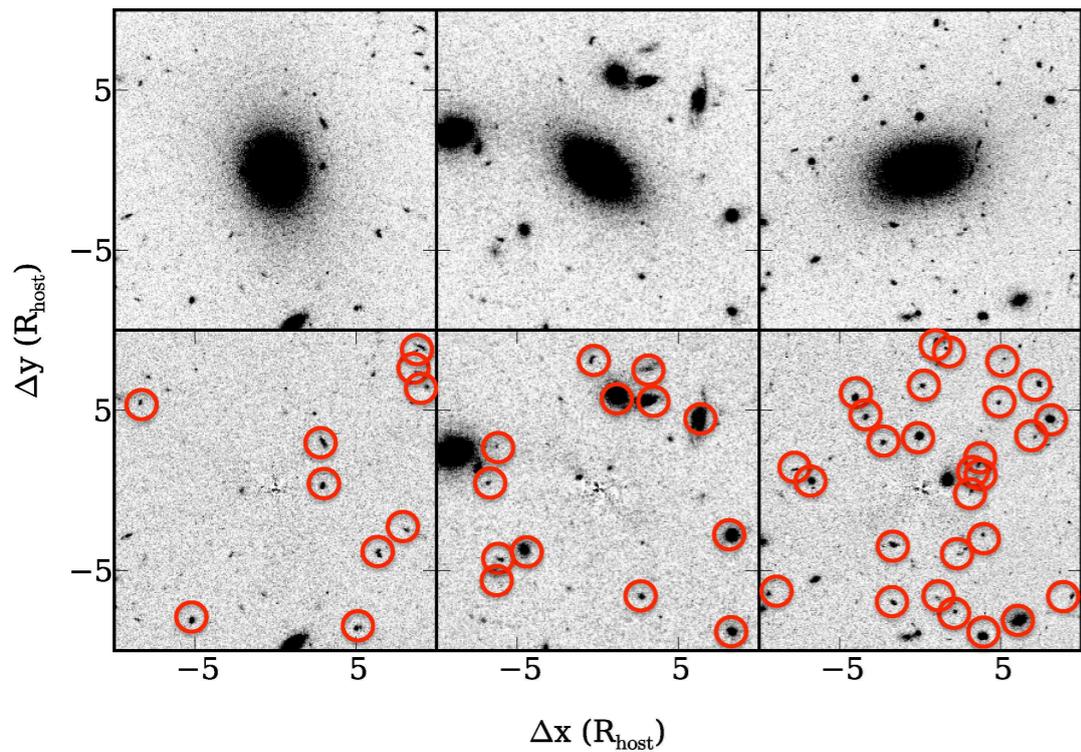
Is Milky Way representative of  $M_{\text{halo}} \approx 10^{12} M_{\odot}$  ?

Compare with a wide set of satellites/host halos through the satellite luminosity function

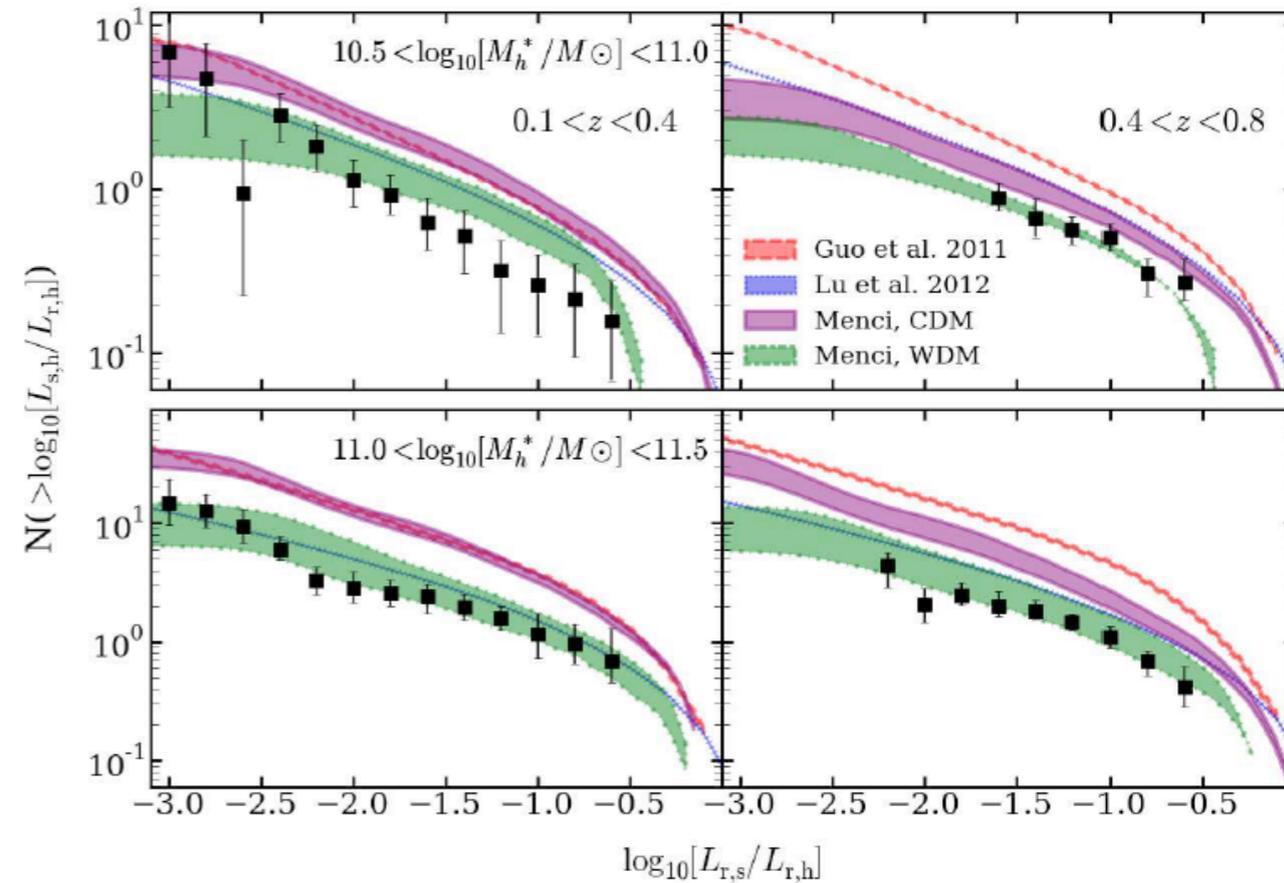
ACS F814W imaging of the COSMOS field,

identify satellites as much as a thousand times fainter than their host galaxies and as close as 0.3 (1.4) arcsec (kpc) and as close as 0.3 (1.4) arcsec (kpc)

Hundreds of hosts



The luminosity distribution of Satellite Galaxies  
Nierenberg, Treu, NM 2013

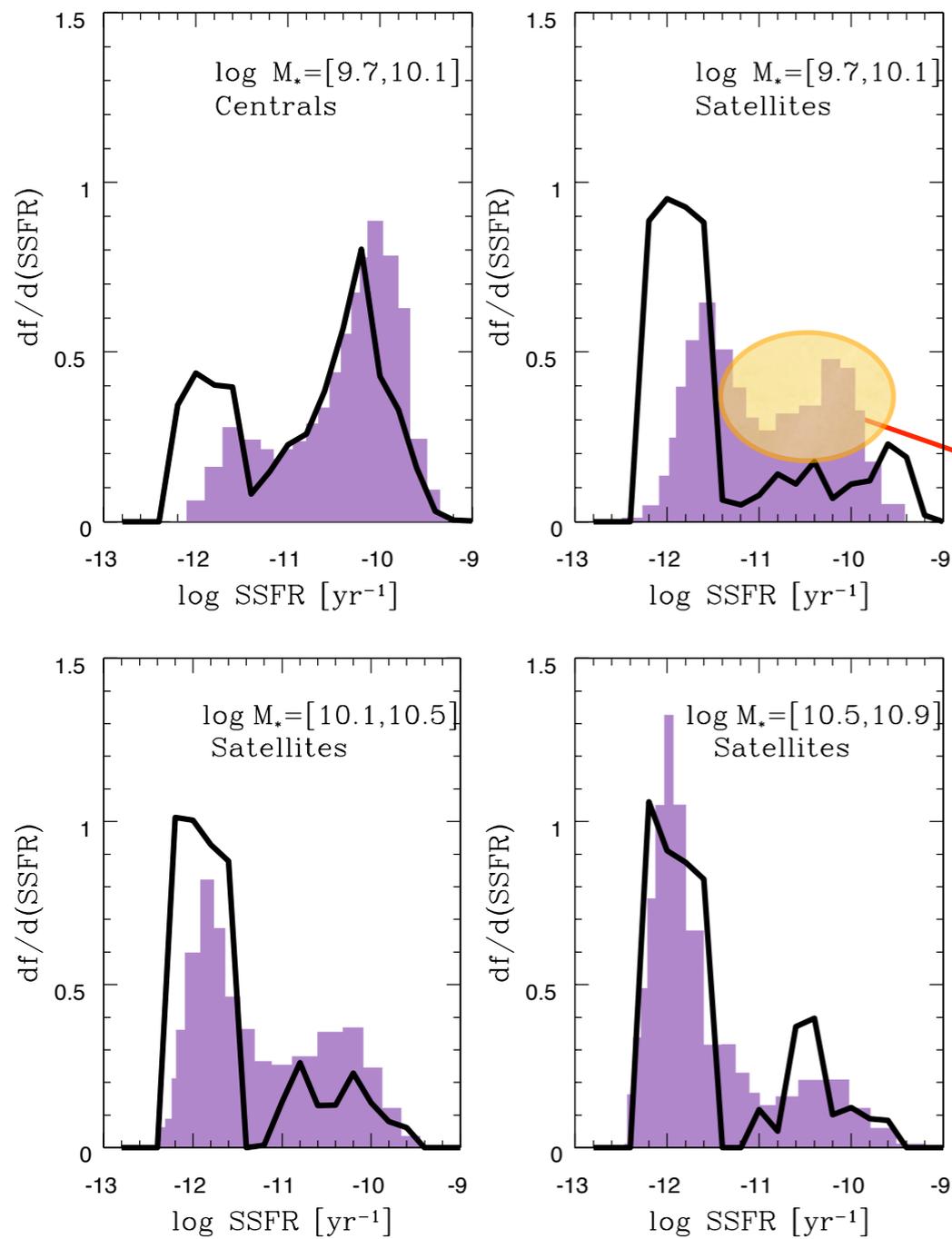


# SATELLITE GALAXIES

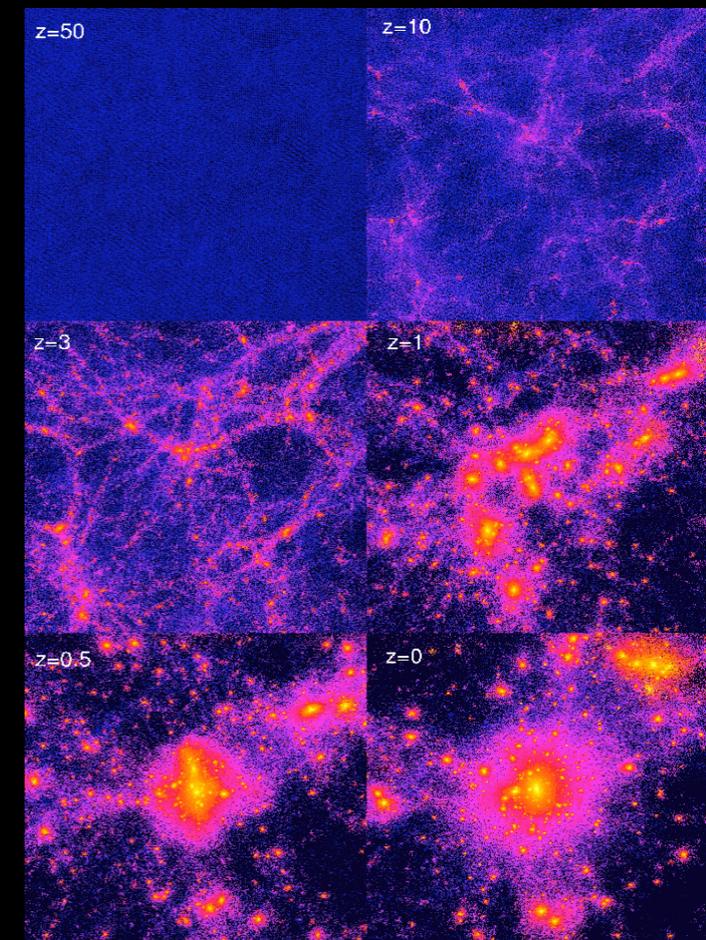
**Specific Star Formation Rate SSFR** measures the current star formation activity with respect to the past

$$SSFR = \dot{M}_* / M_*$$

Population of active satellites missing in CDM models  
Model satellites undergo passive evolution



NM 2014;  
Data from Wetzel et al. 2013



# THE FRACTION OF QUIESCENT SATELLITE GALAXIES

## Quiescent Fraction

Measures the fraction of quiescent satellites

Threshold  $SSFR < 10^{-11}$  yrs  
 corresponds to minimum in the SSFR distribution  
 correspond to  $\Delta t = 3 t_H$   
 (to form  $M_*$  it would need  $3 t_H$  at current SF rate)

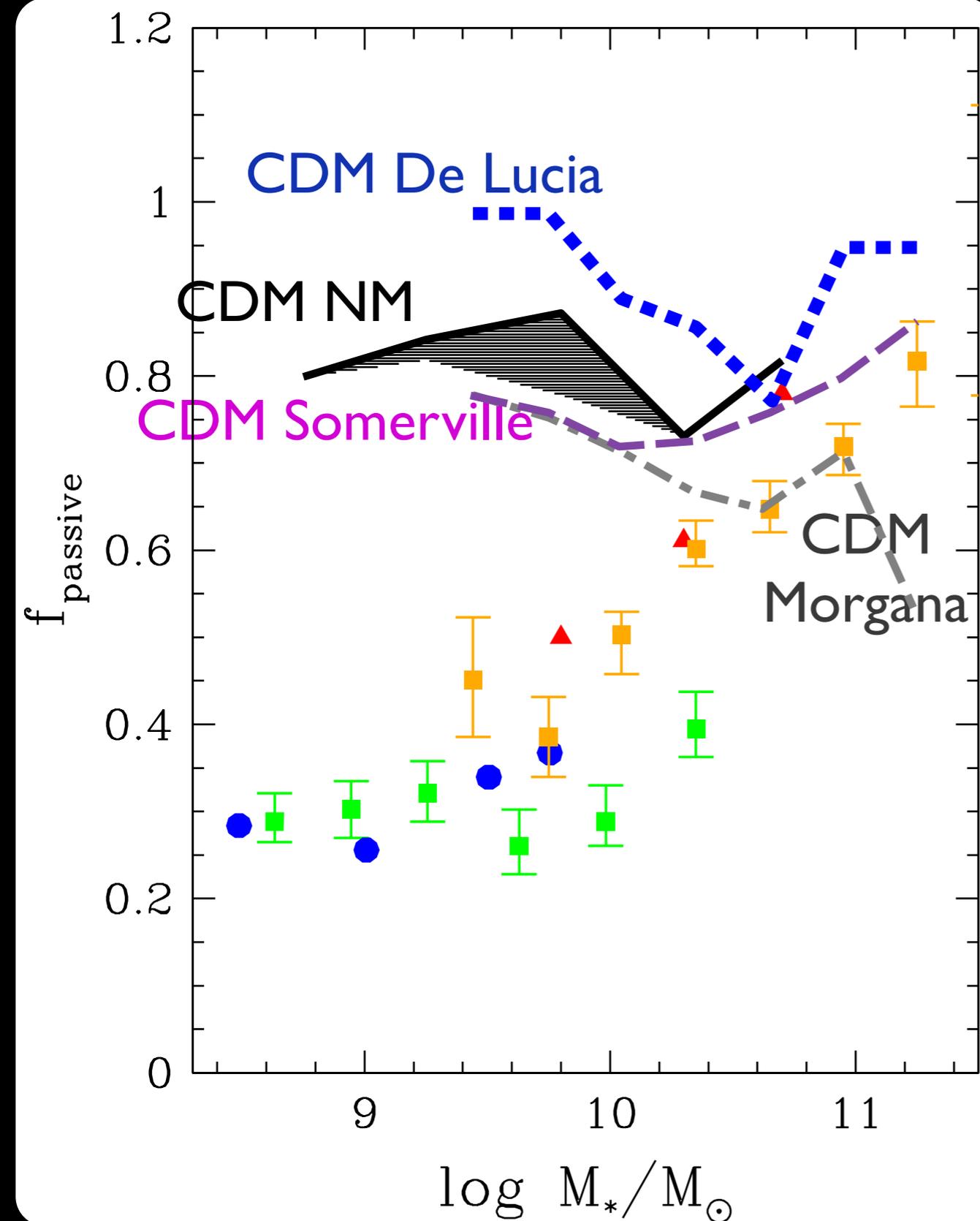
$$SSFR = \dot{M}_*/M_* = 10^{-11} \text{ yrs} \rightarrow M_* = 3 t_H \dot{M}_*$$

Result robust with respect to different CDM models with different feedback modelling

Due to the large number of dense DM clumps collapsed at high redshifts  
 gas rapidly converted into stars at high-redshifts

- Cold gas converted into stars at high  $z$
- Hot gas stripped when they were incorporated into larger DM haloes

No further star formation at low redshift



NM 2014;  
 Data from Wetzel et al. 2013  
 Kimm et al. 2014  
 Phillips 2014  
 Geha 2012

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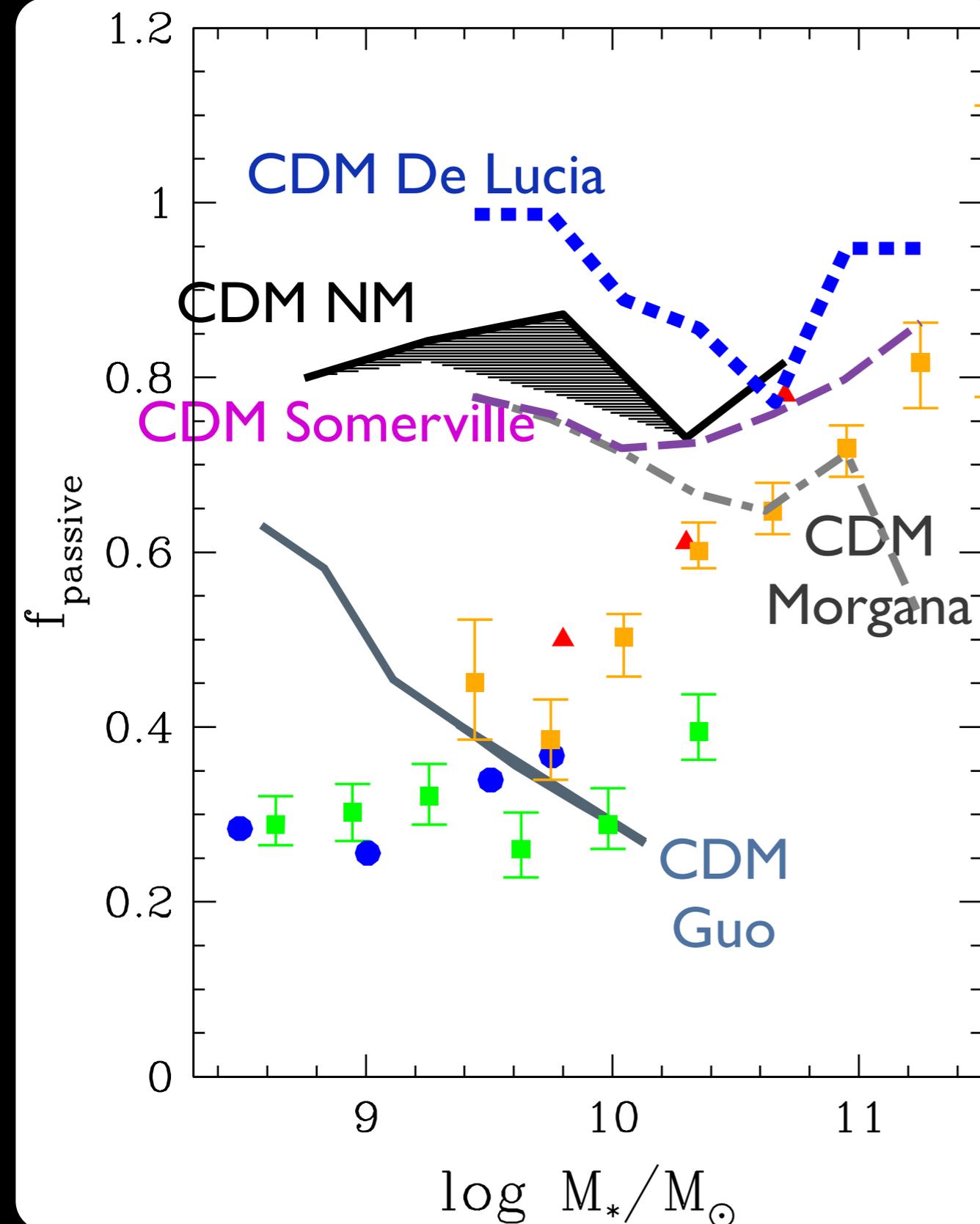
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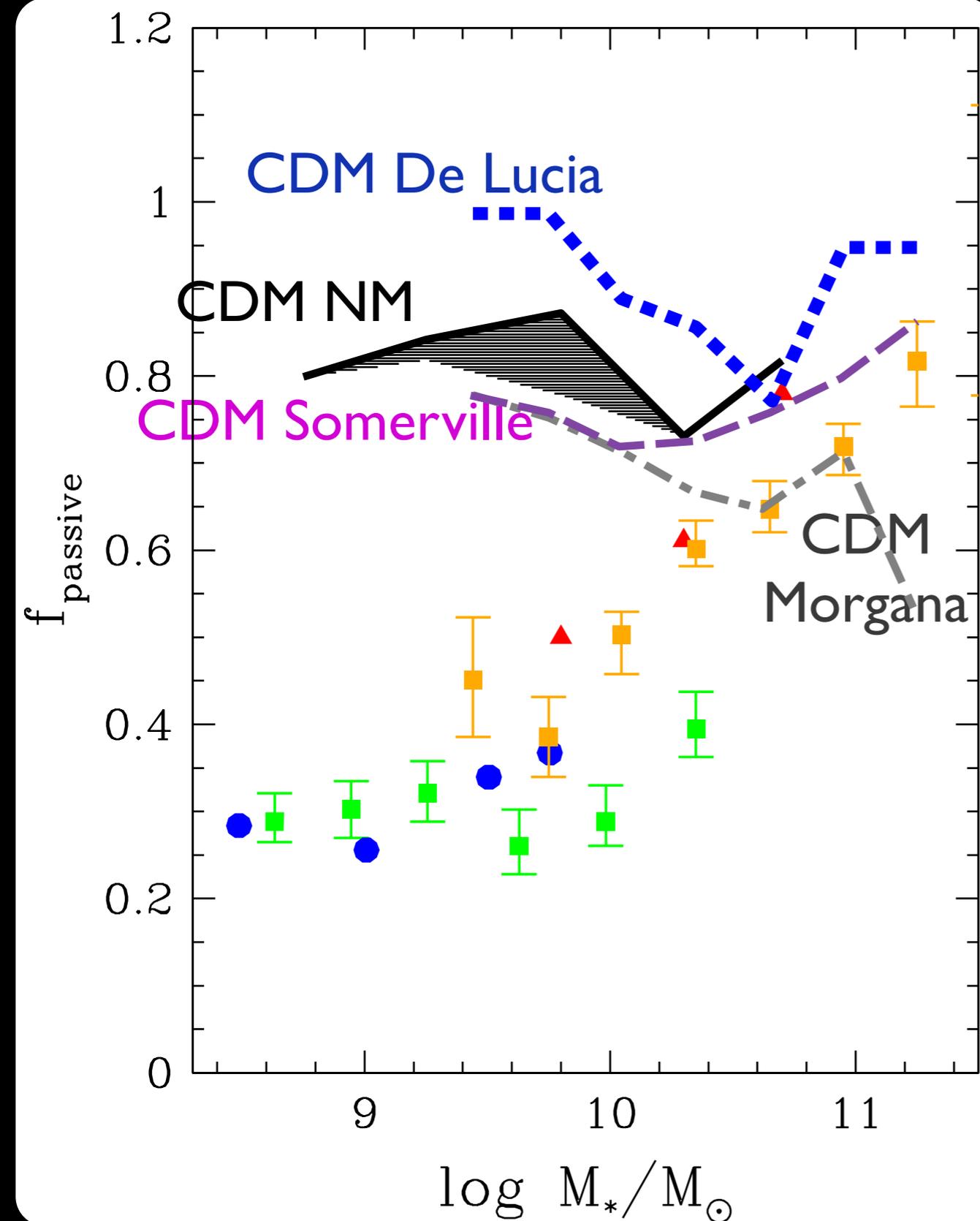
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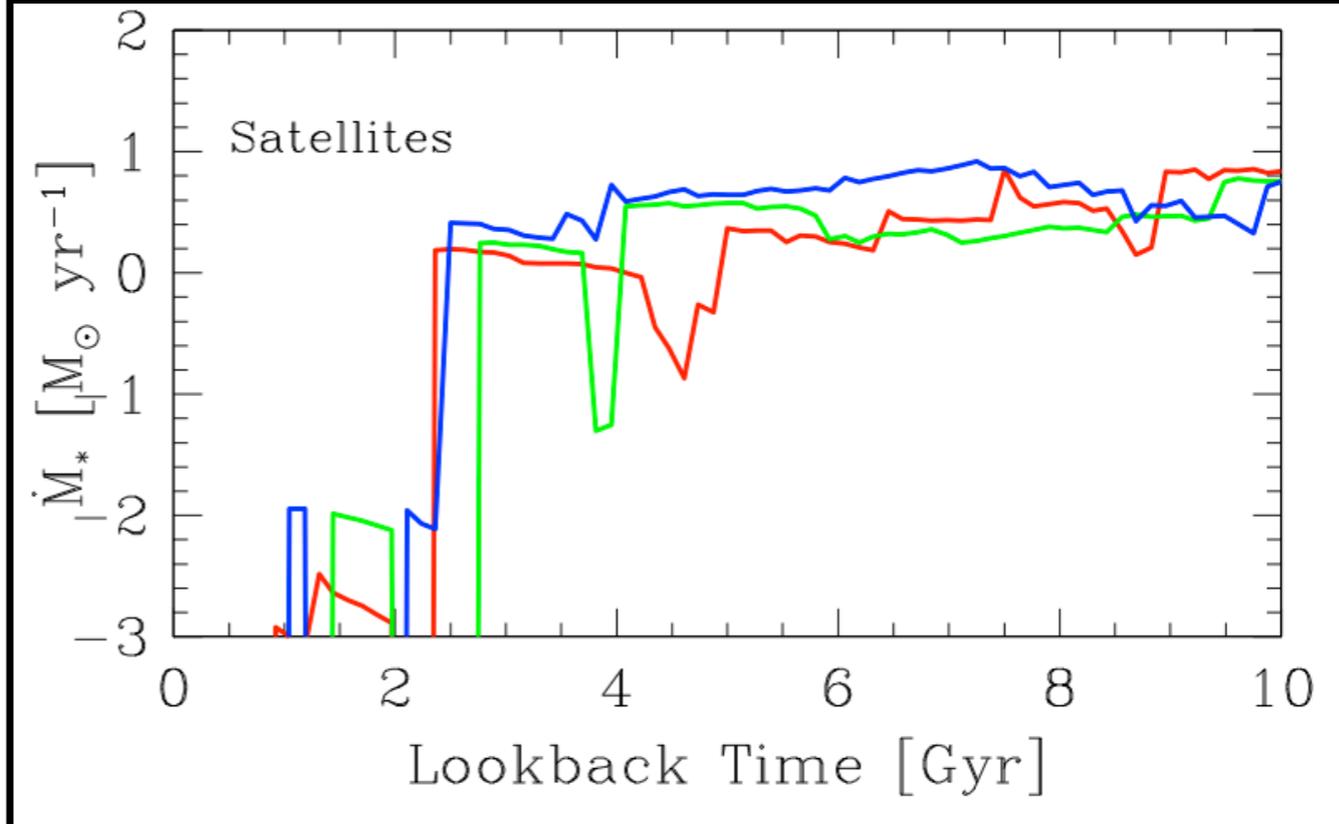
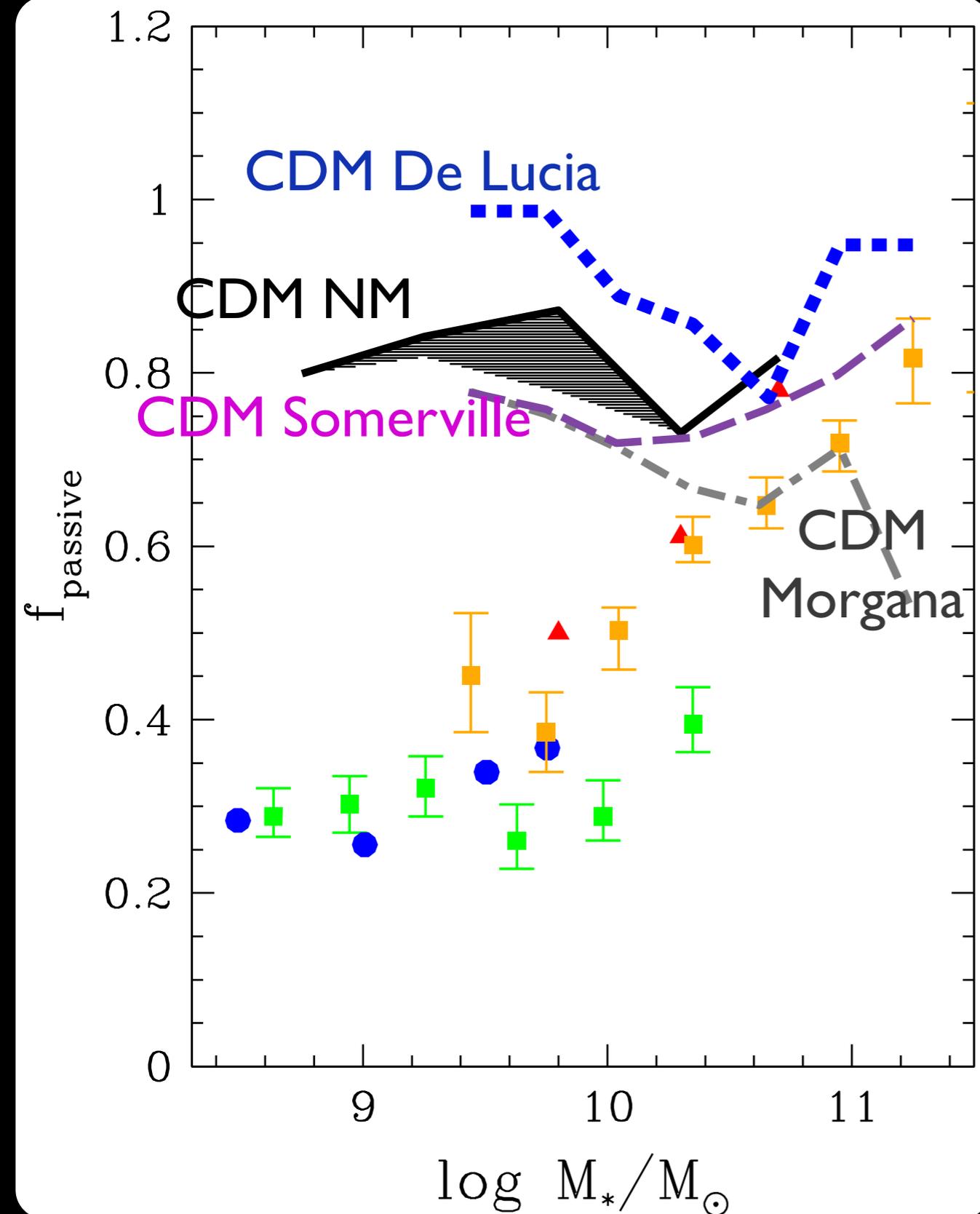
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Phillips 2014

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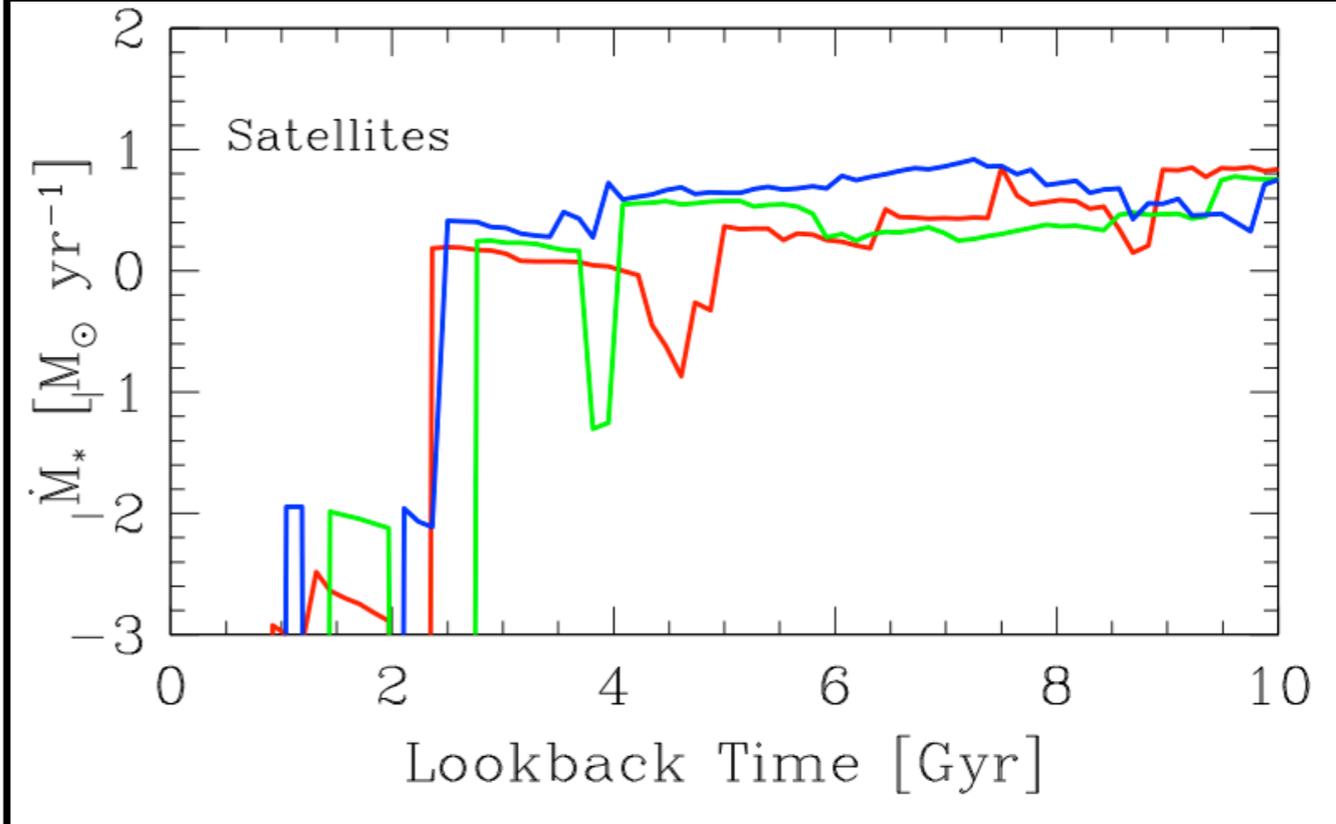
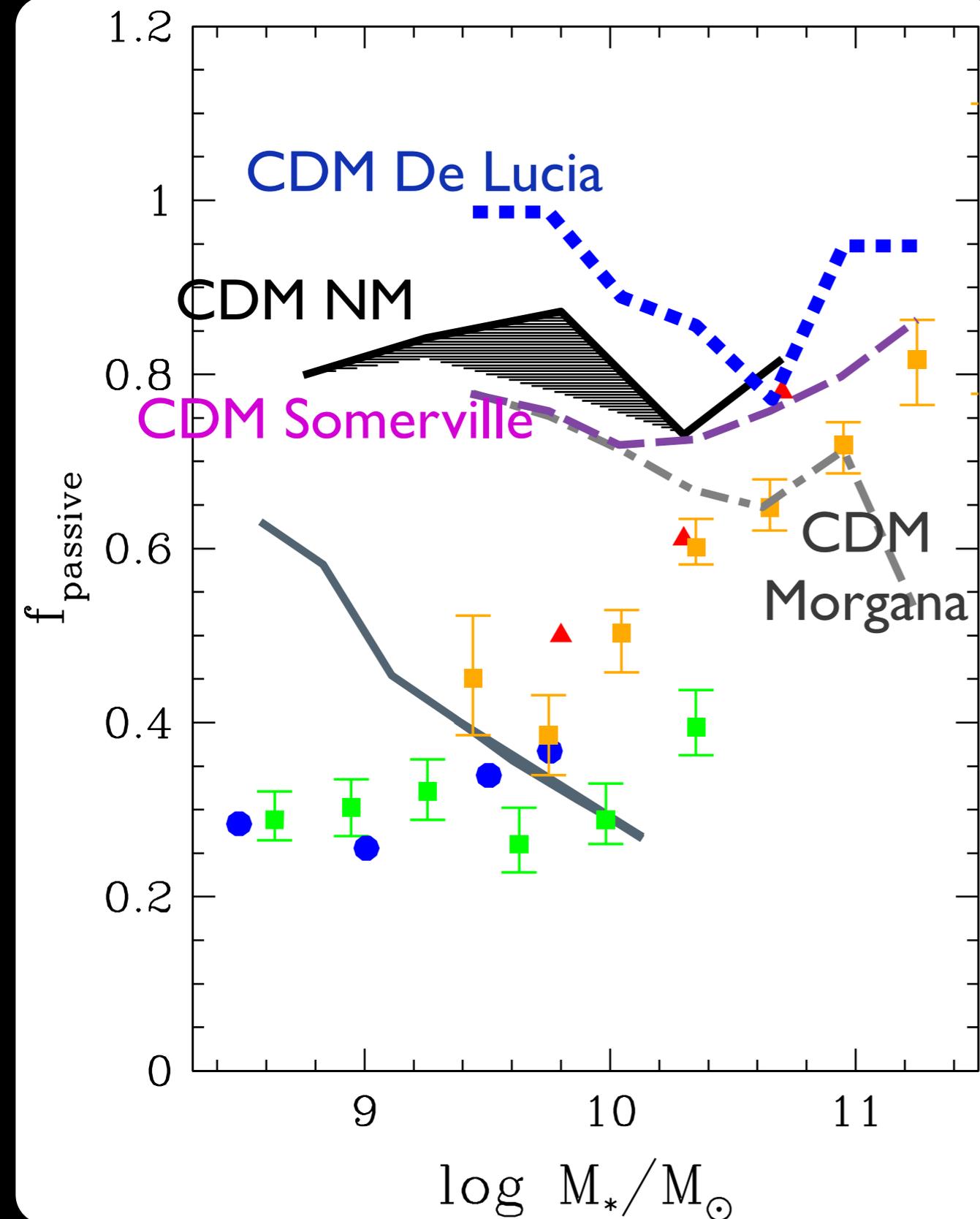
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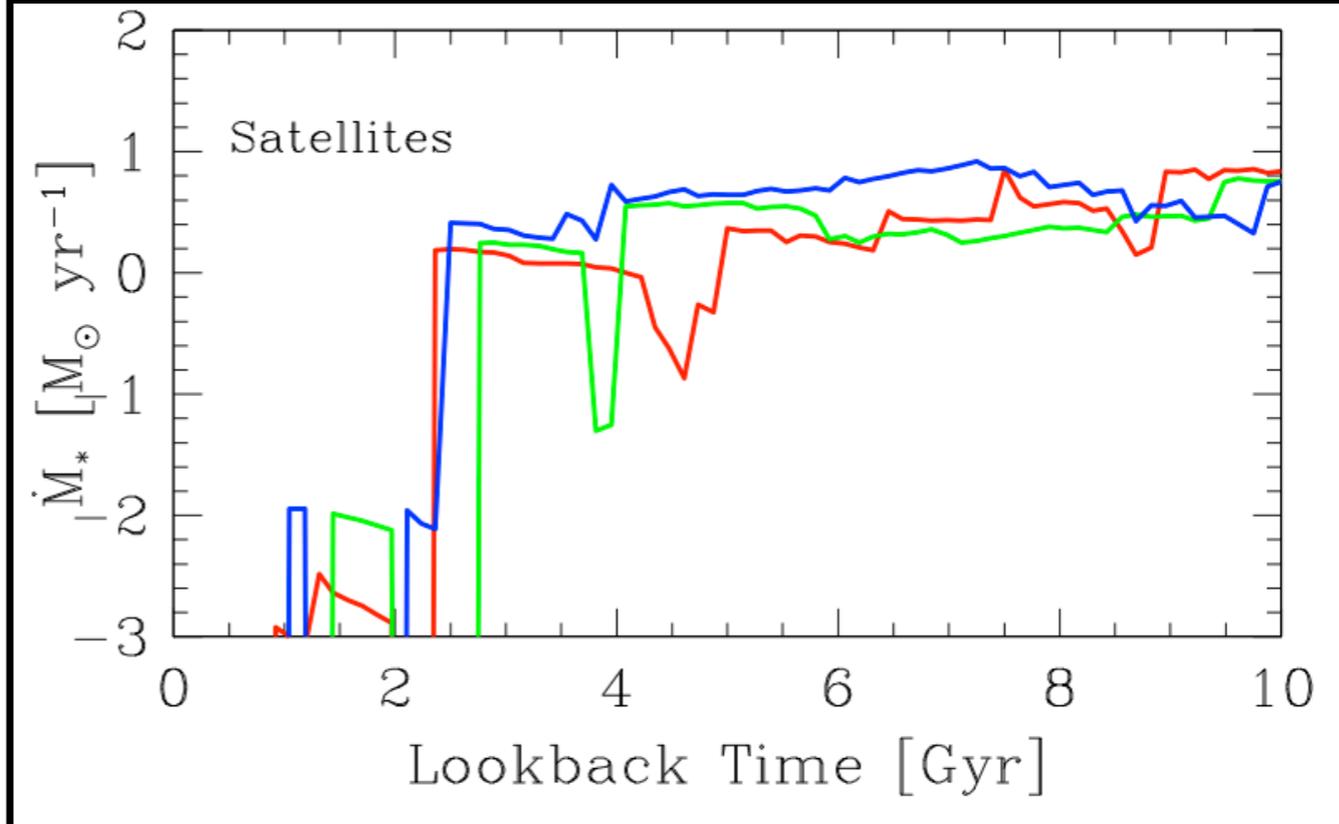
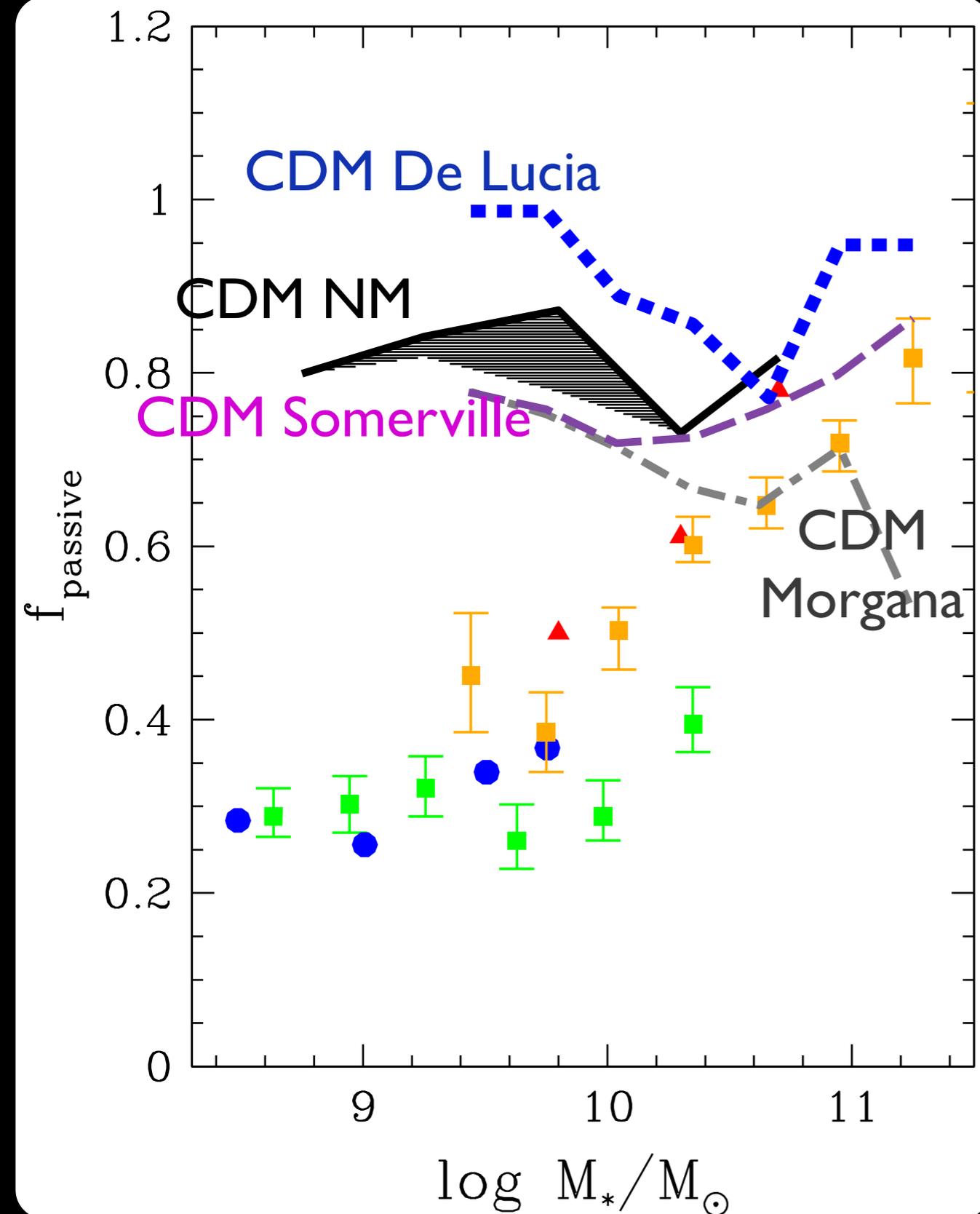
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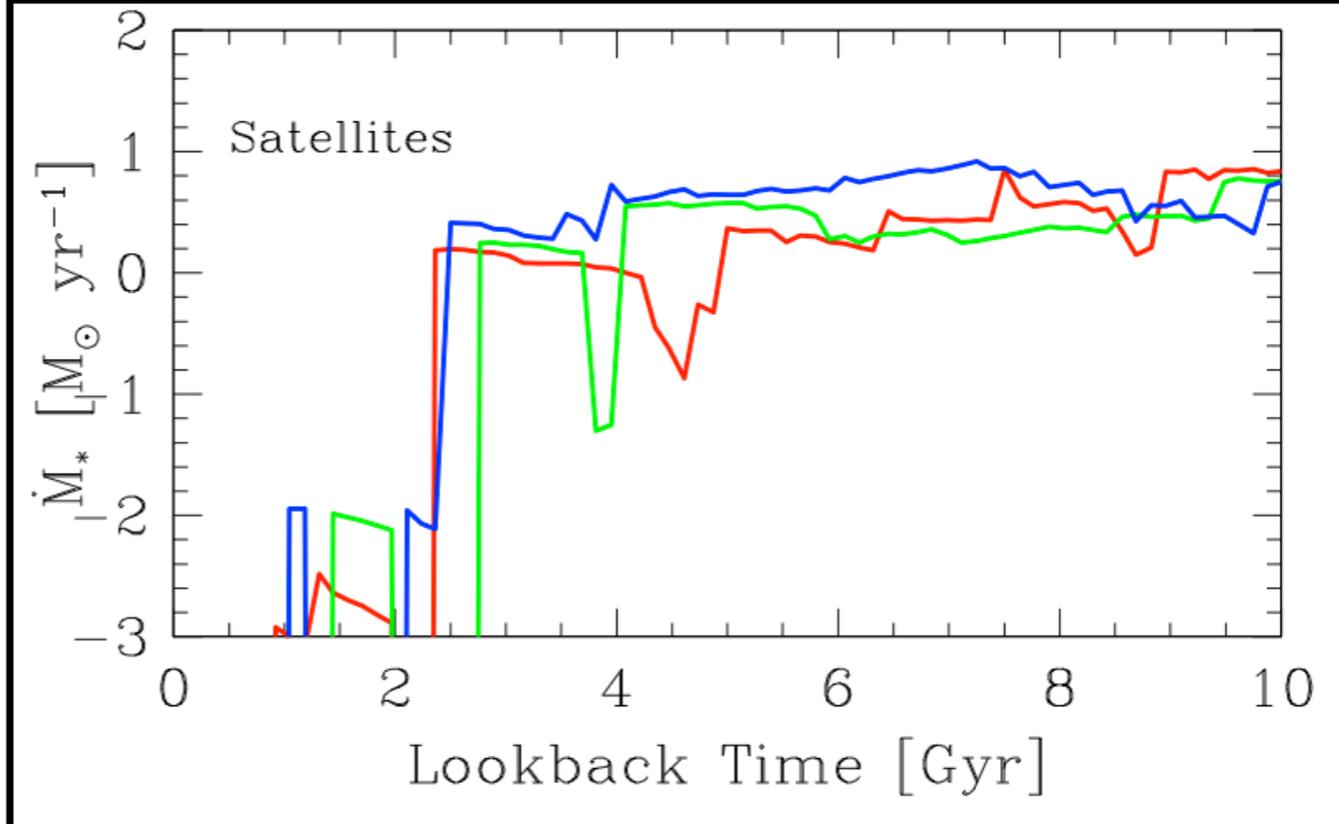
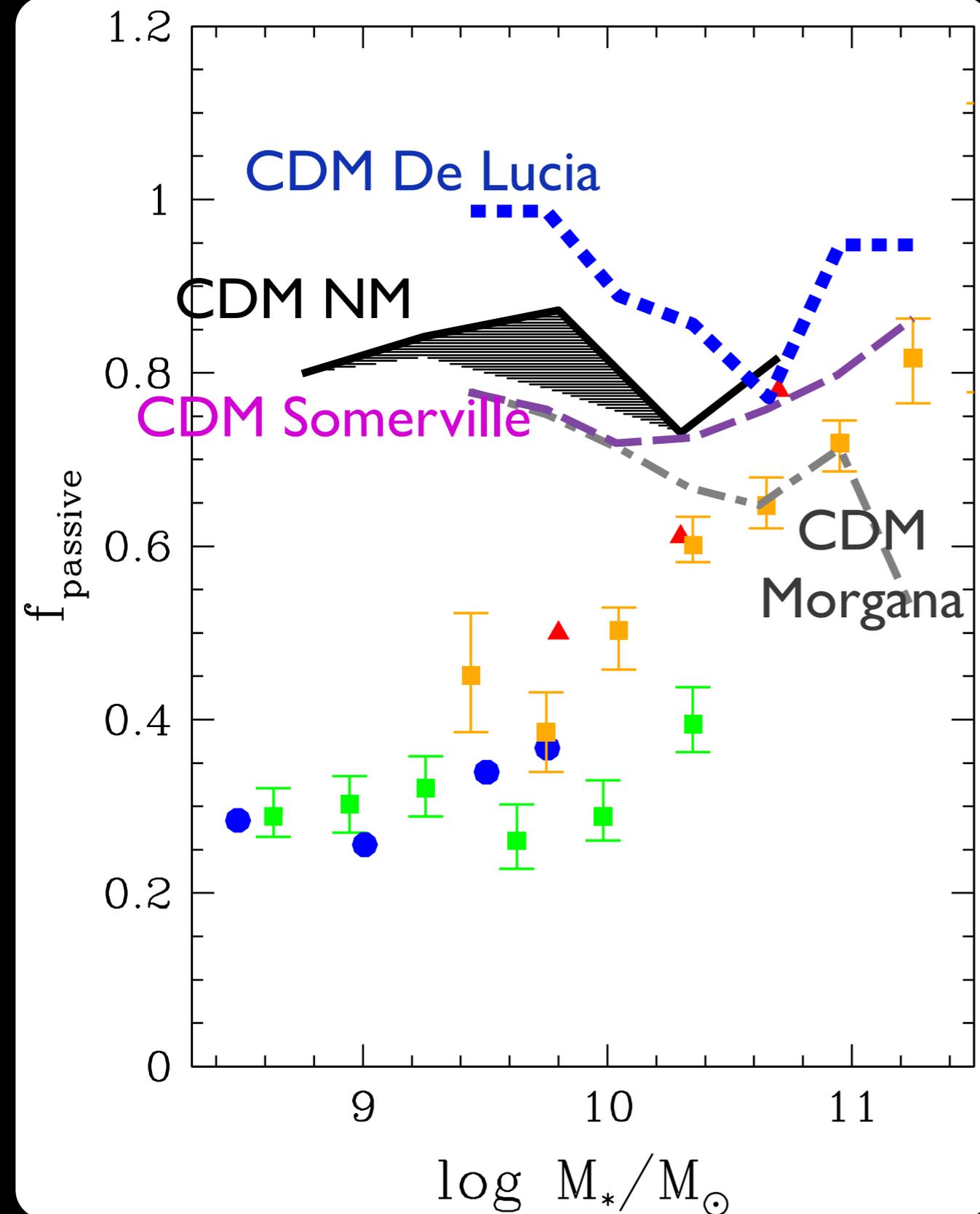
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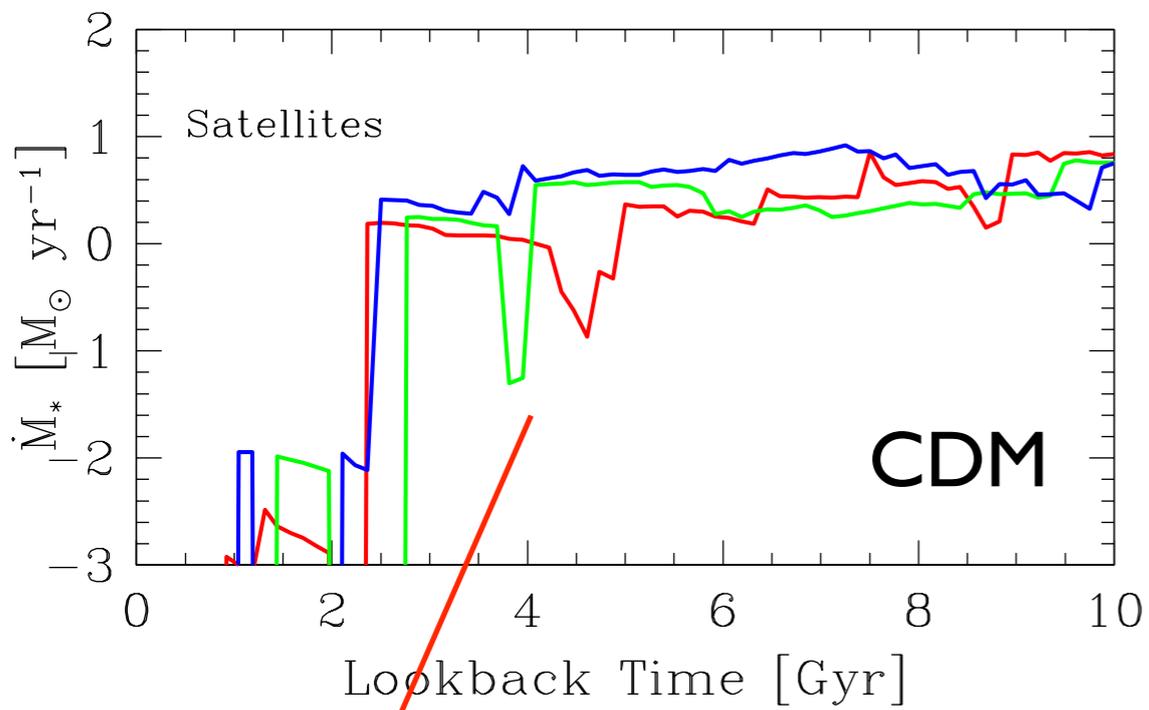
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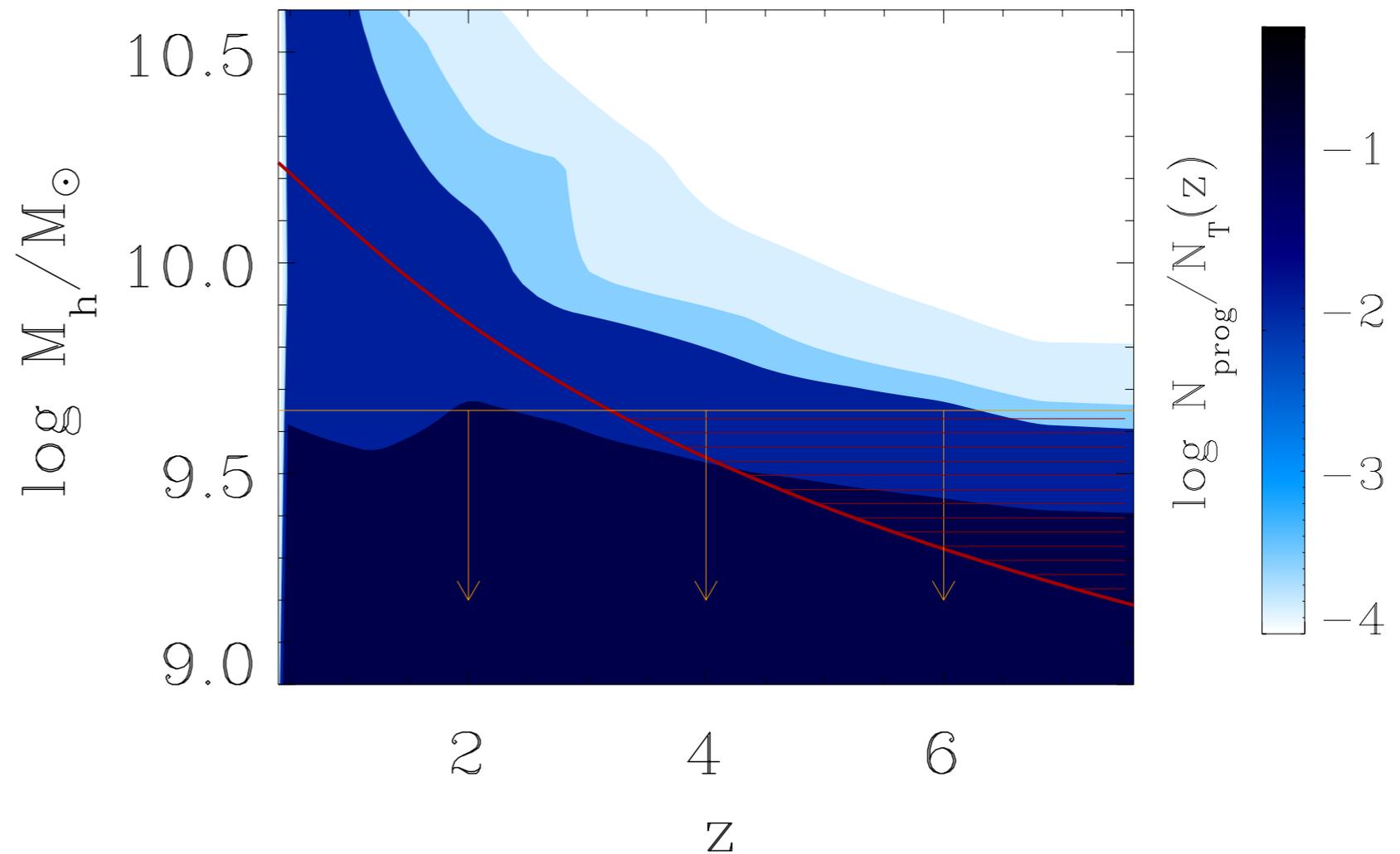
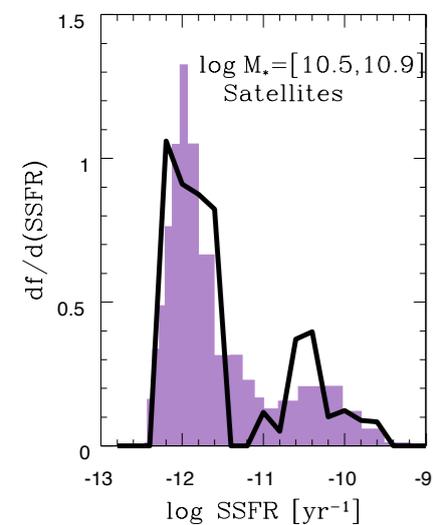
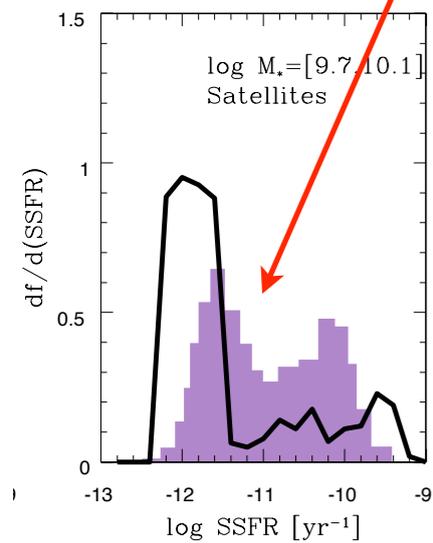
# Star Formation histories of satellites in WDM

Passive Satellites in CDM at low redshift

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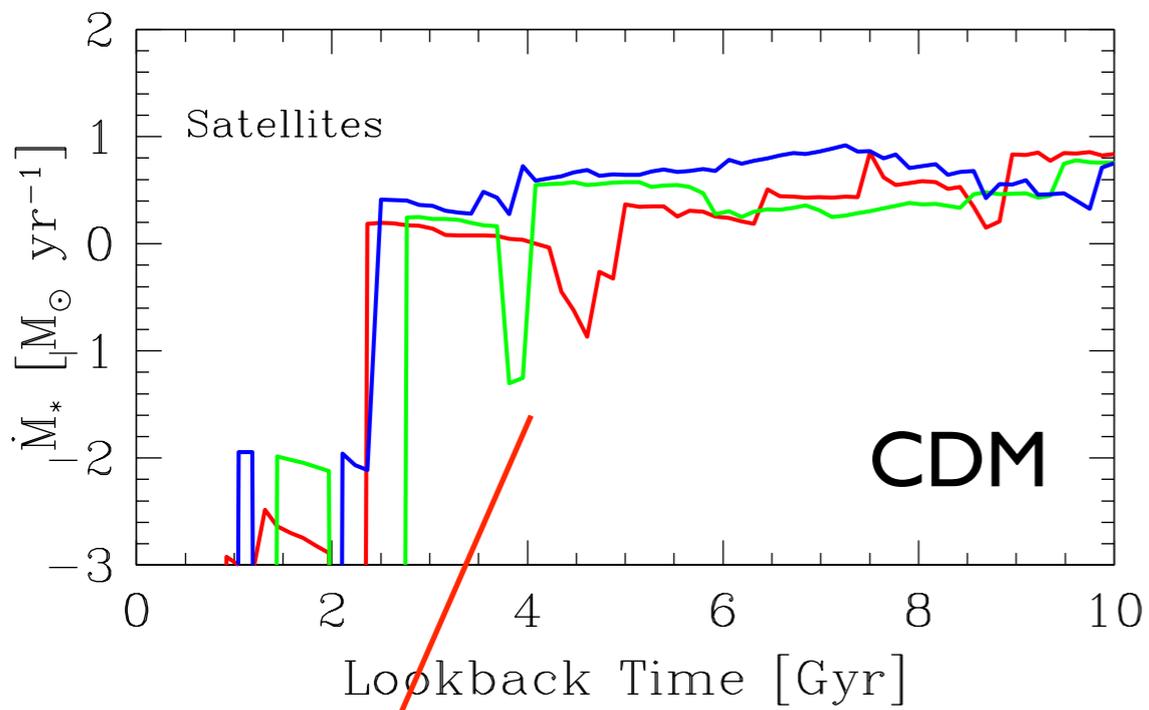
CDM



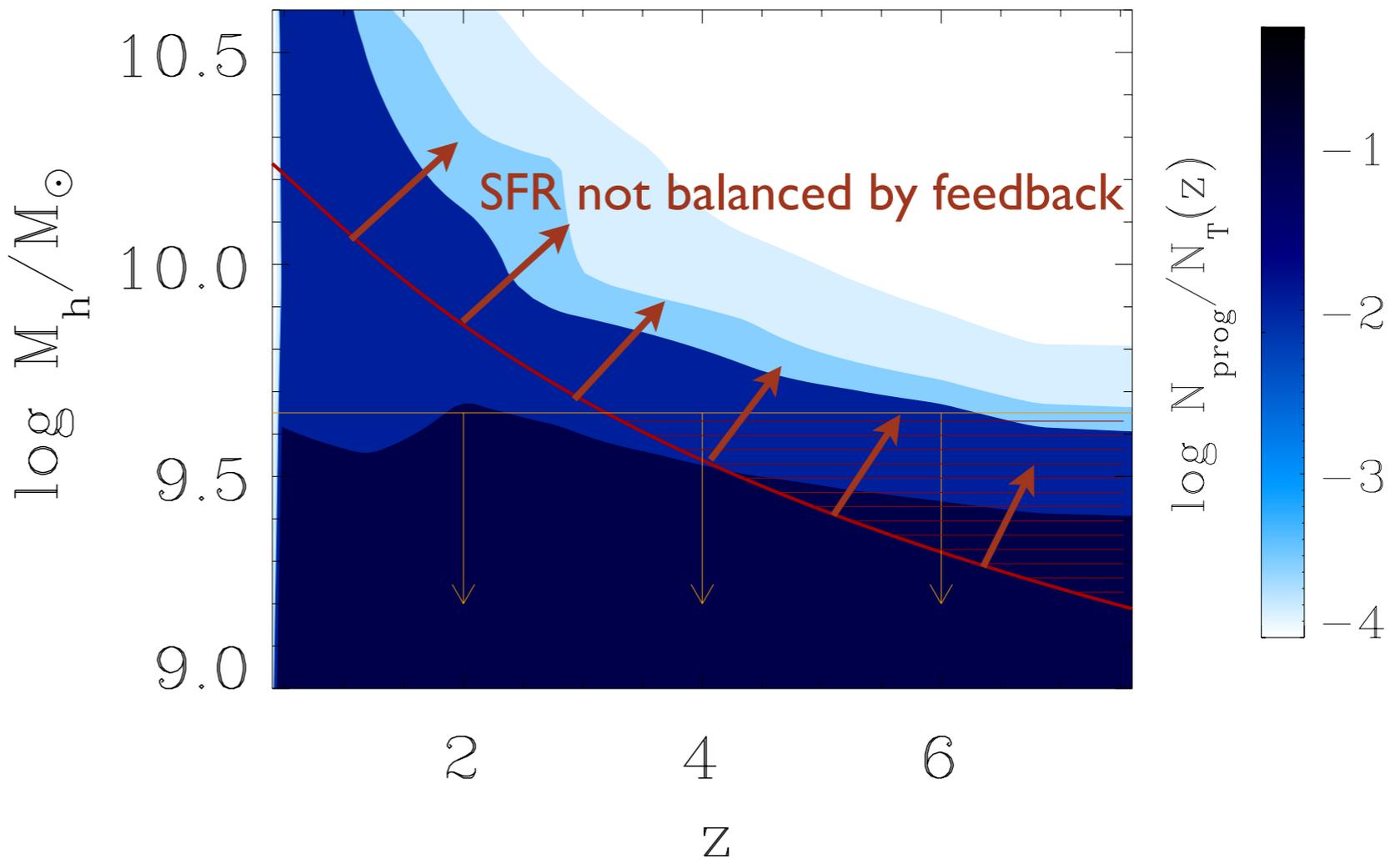
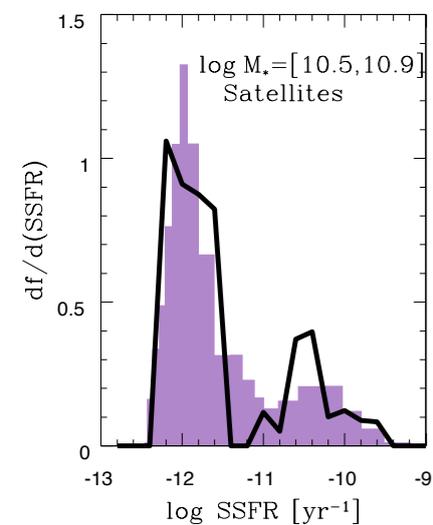
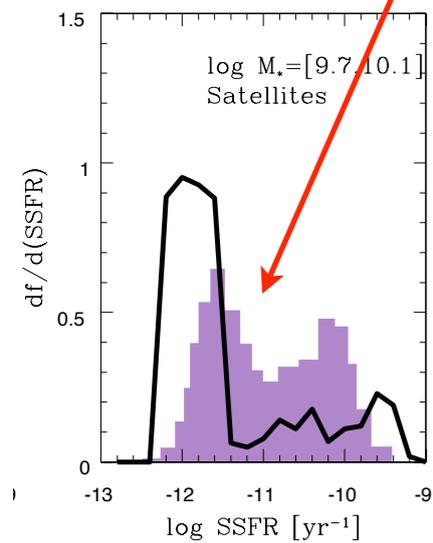
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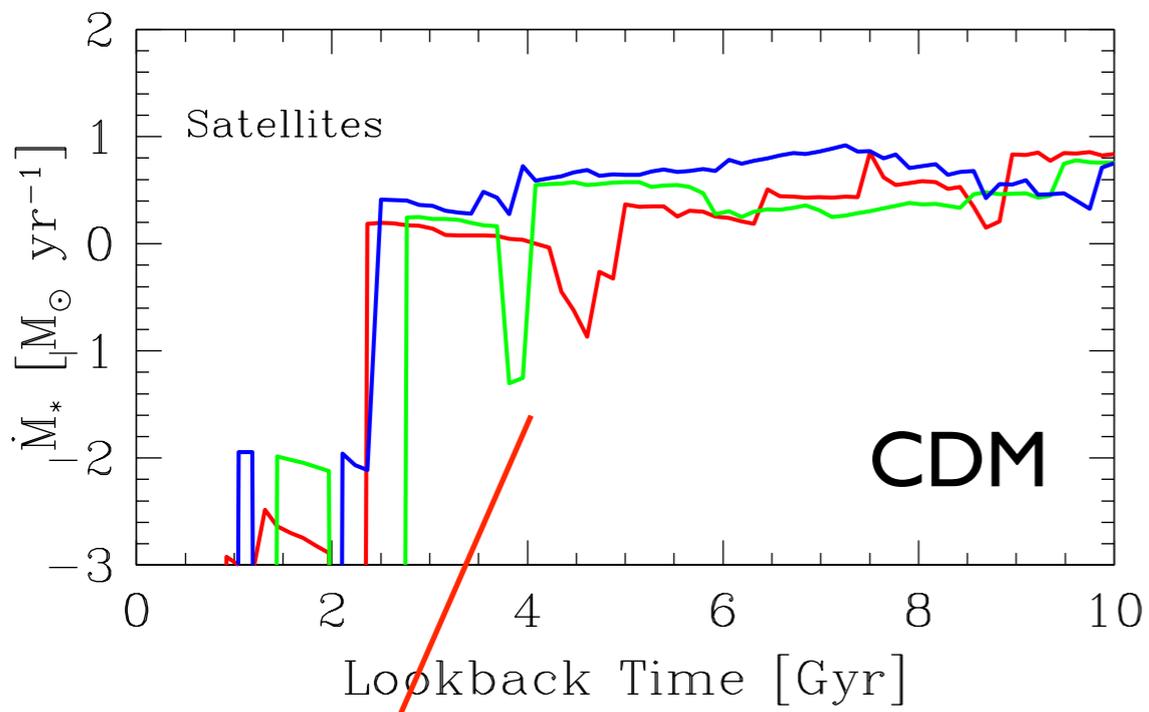
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CDM



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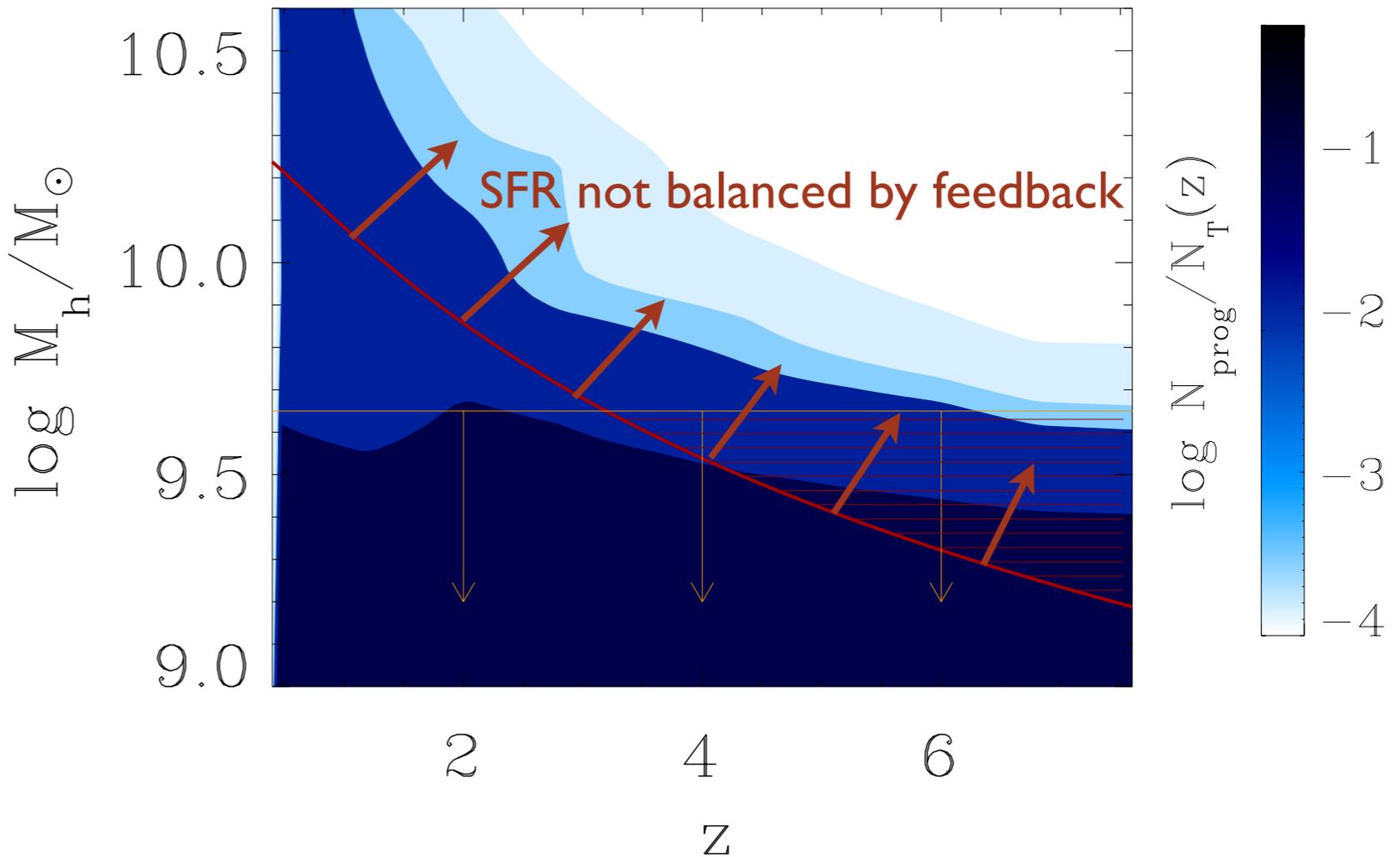
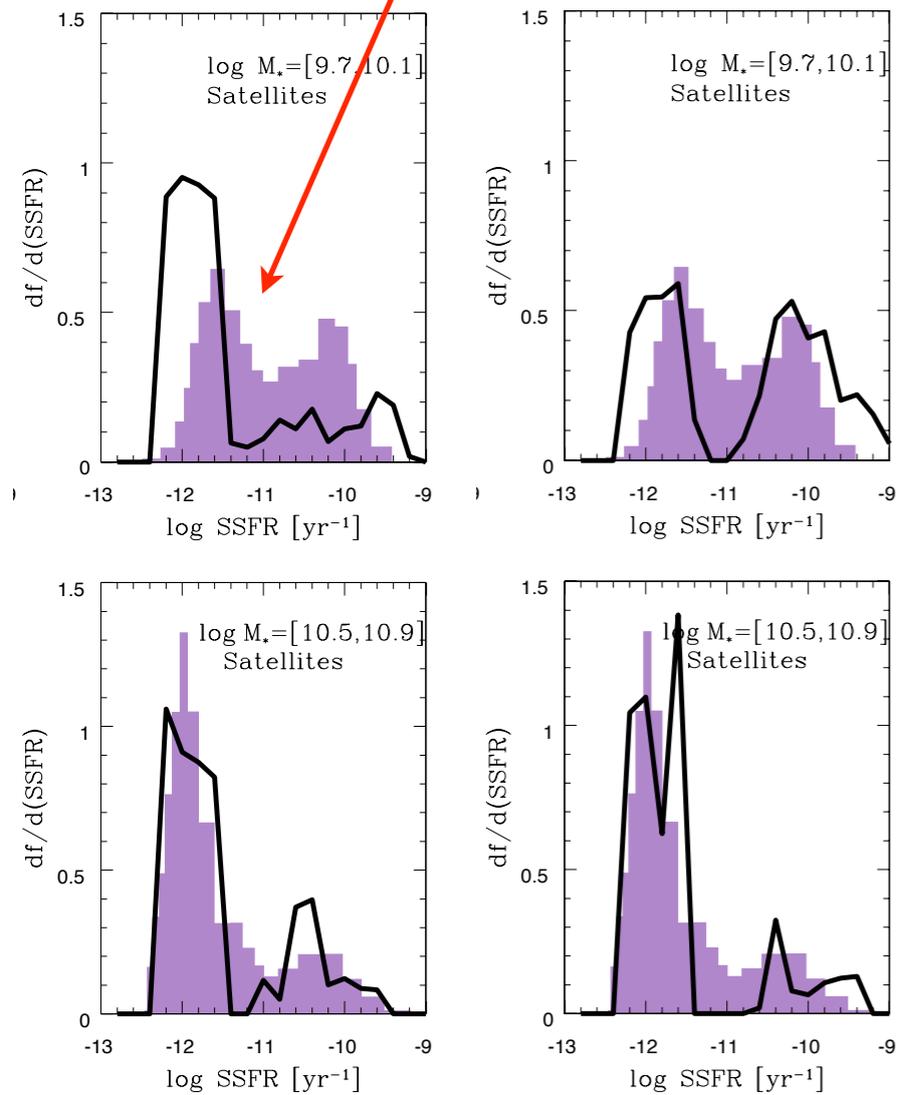


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CDM

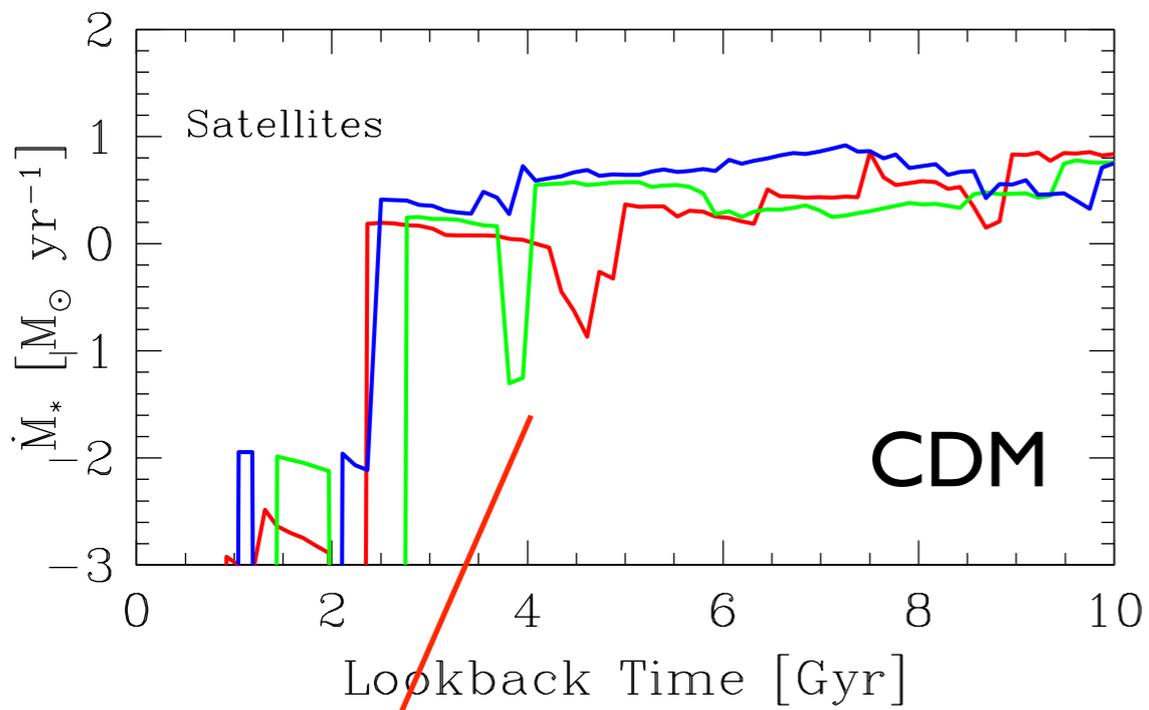
WDM



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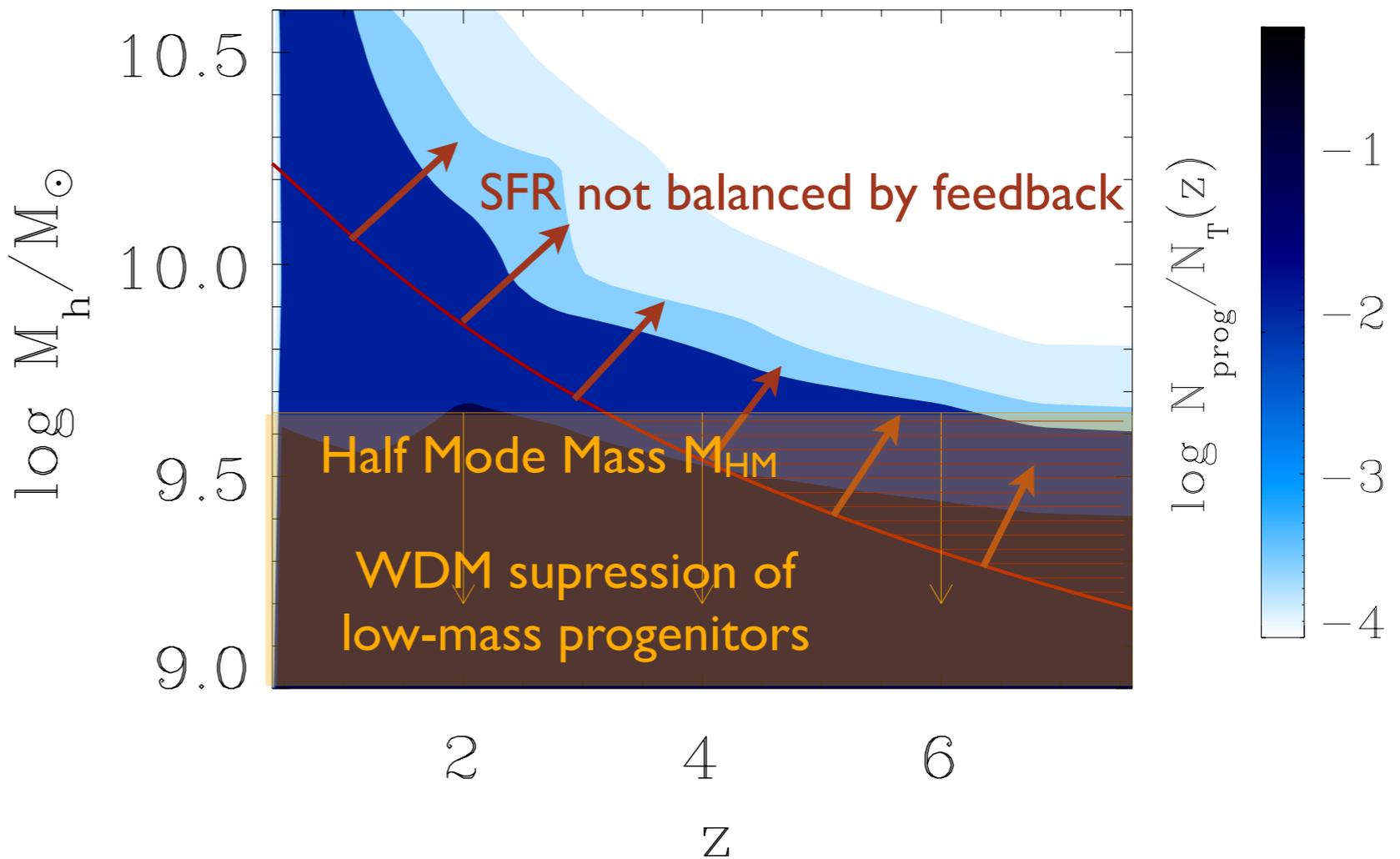
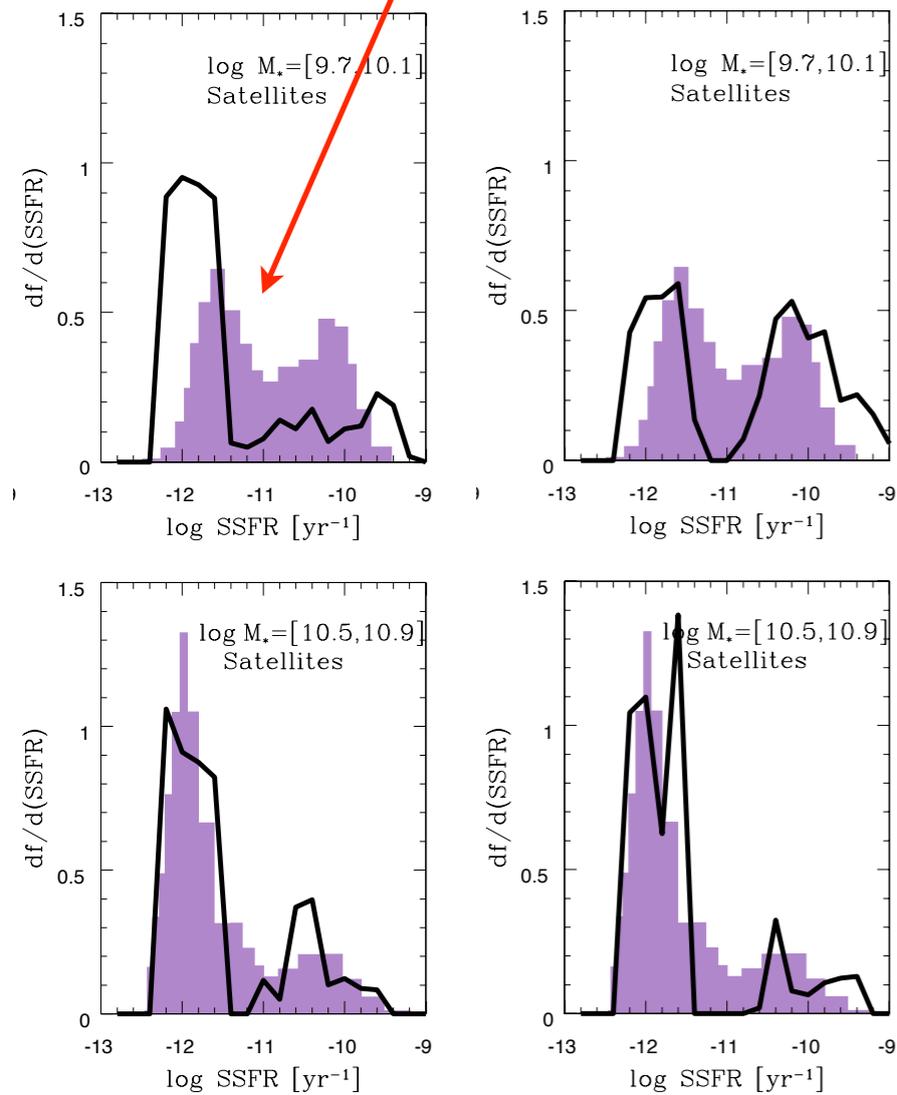
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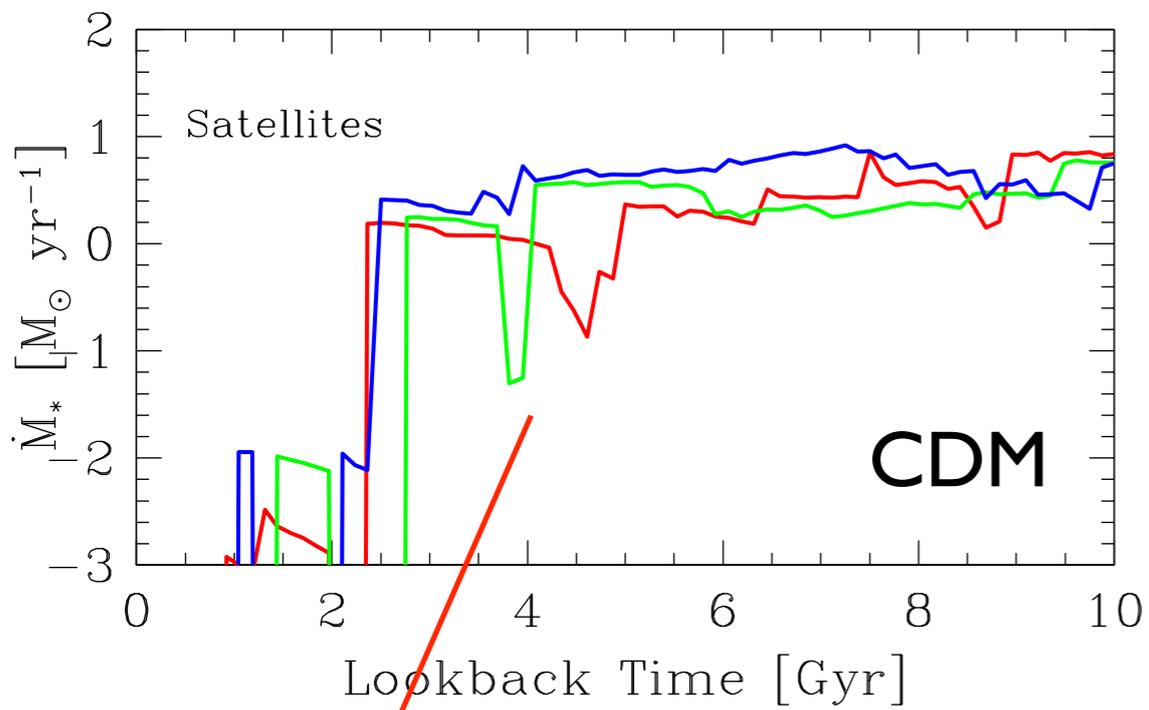
CDM

WDM

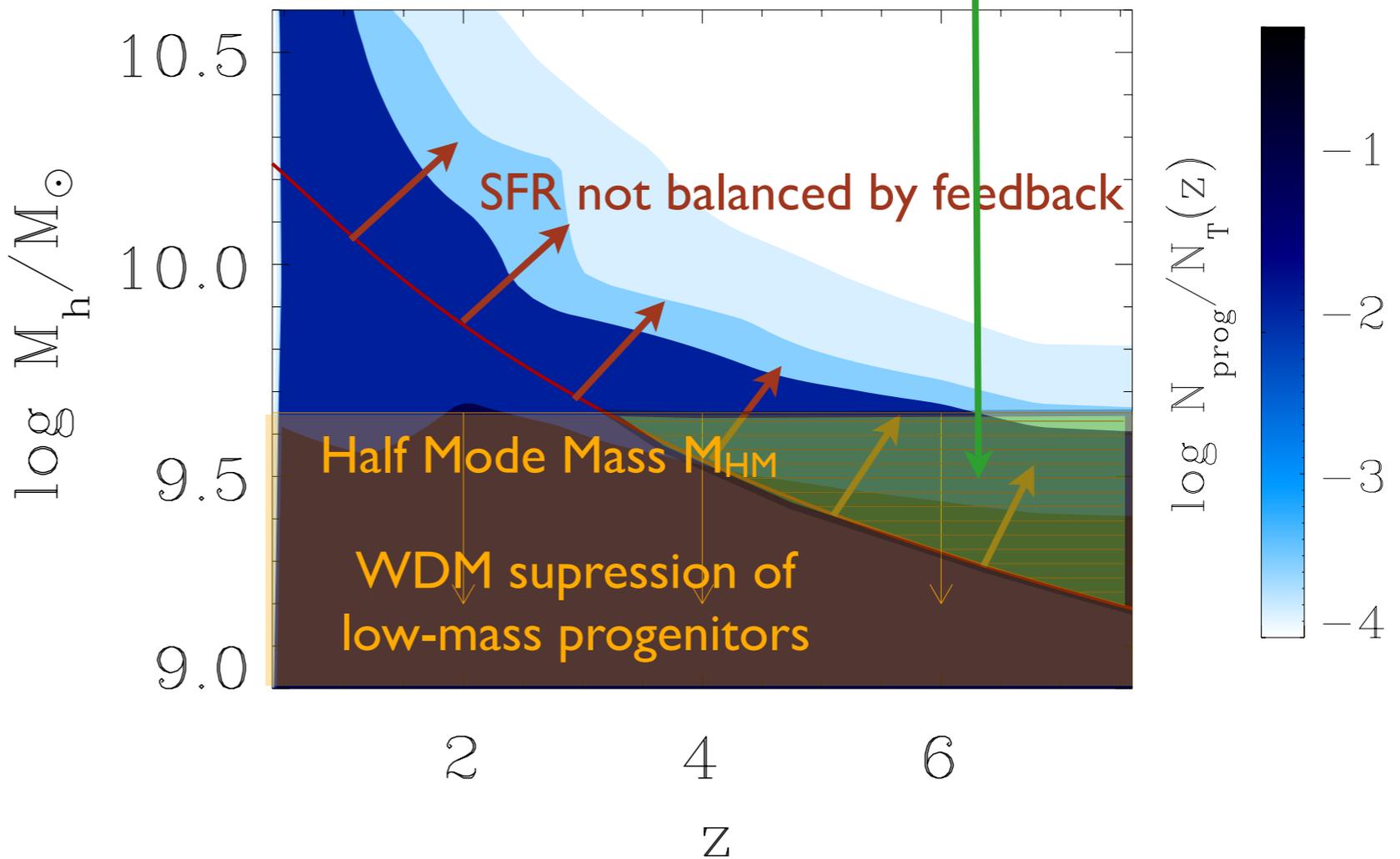
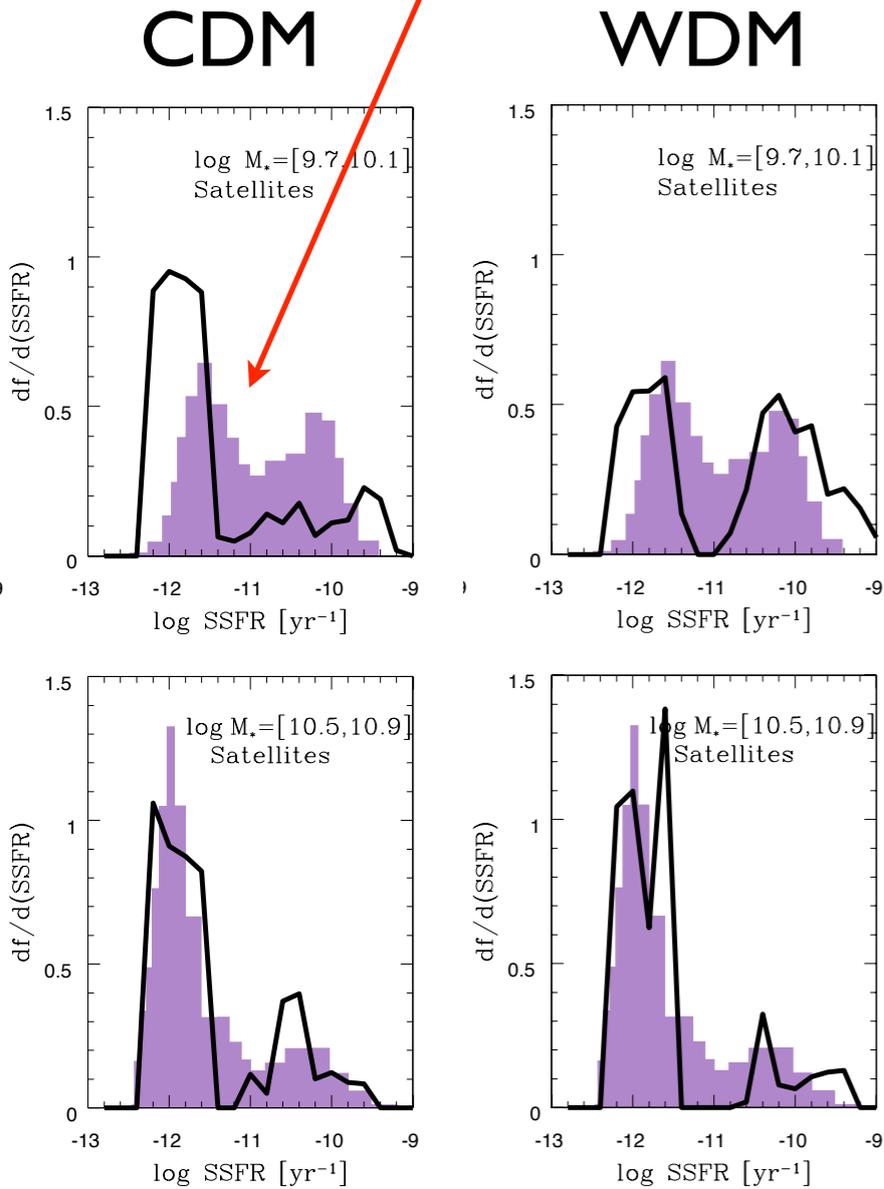


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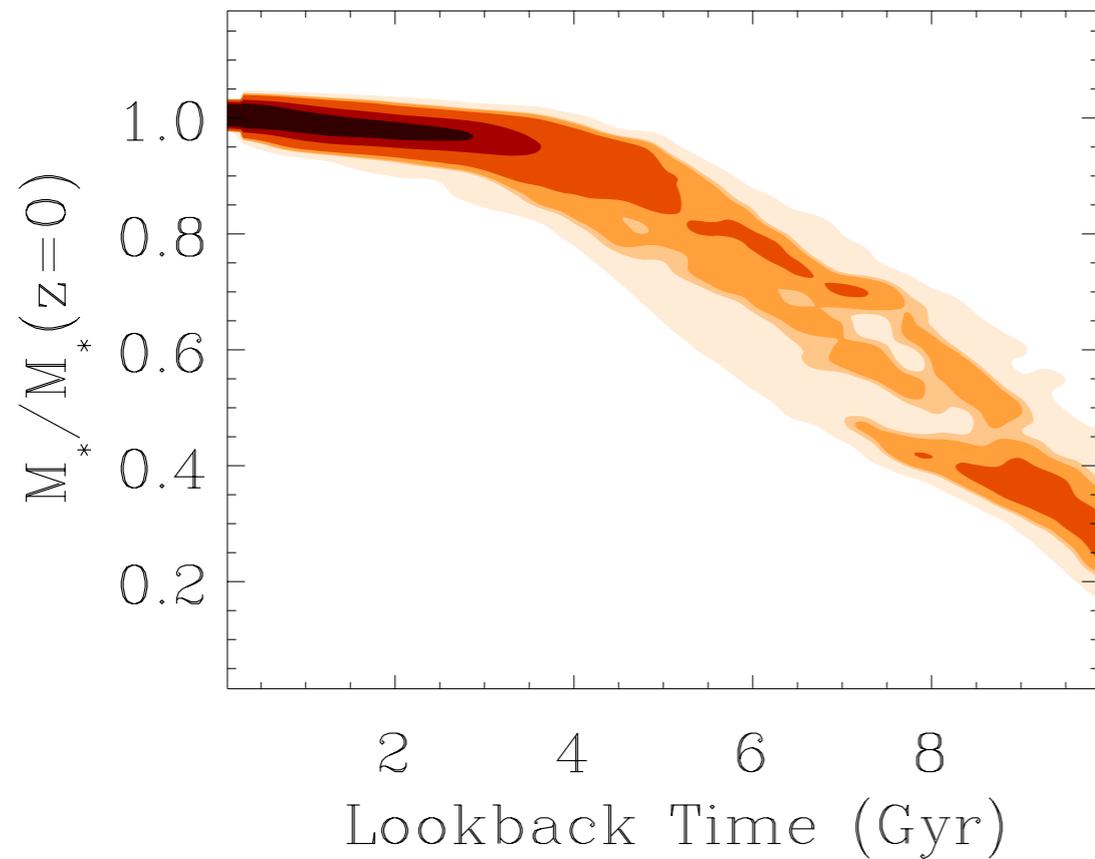
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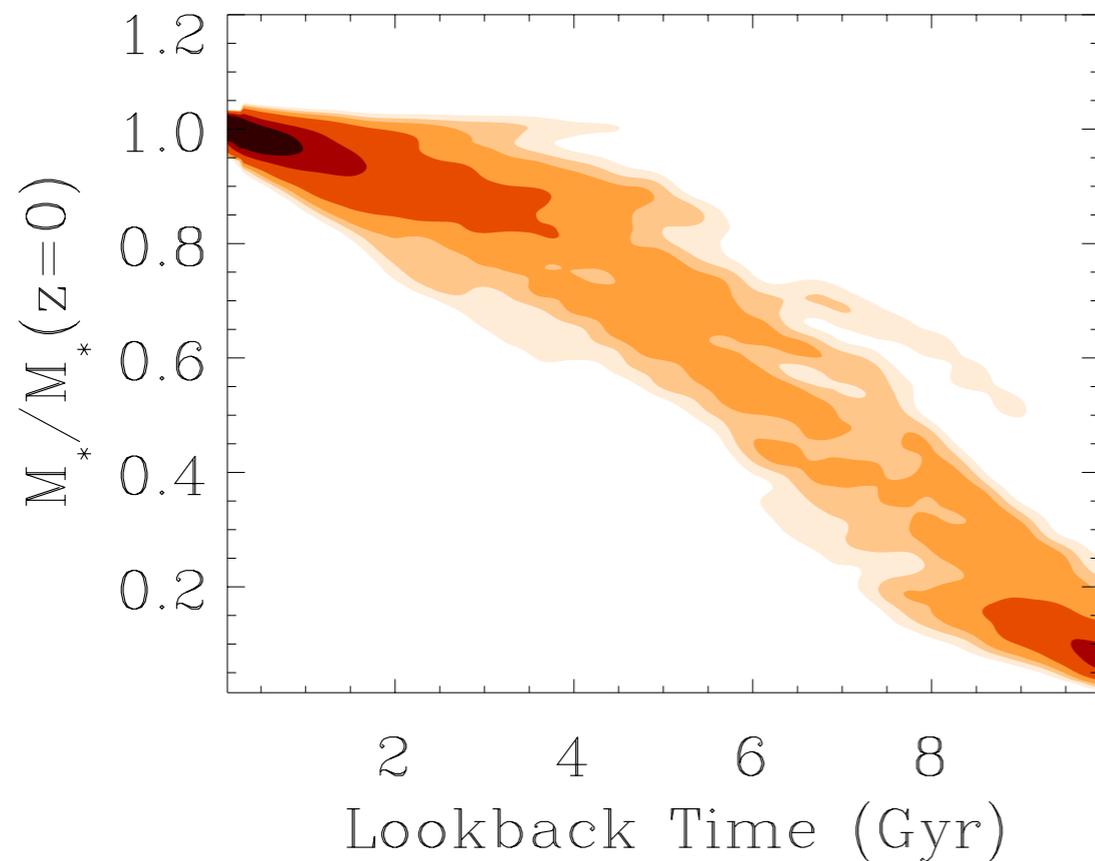
Reduction in the number of progenitors with high SFR at high redshifts



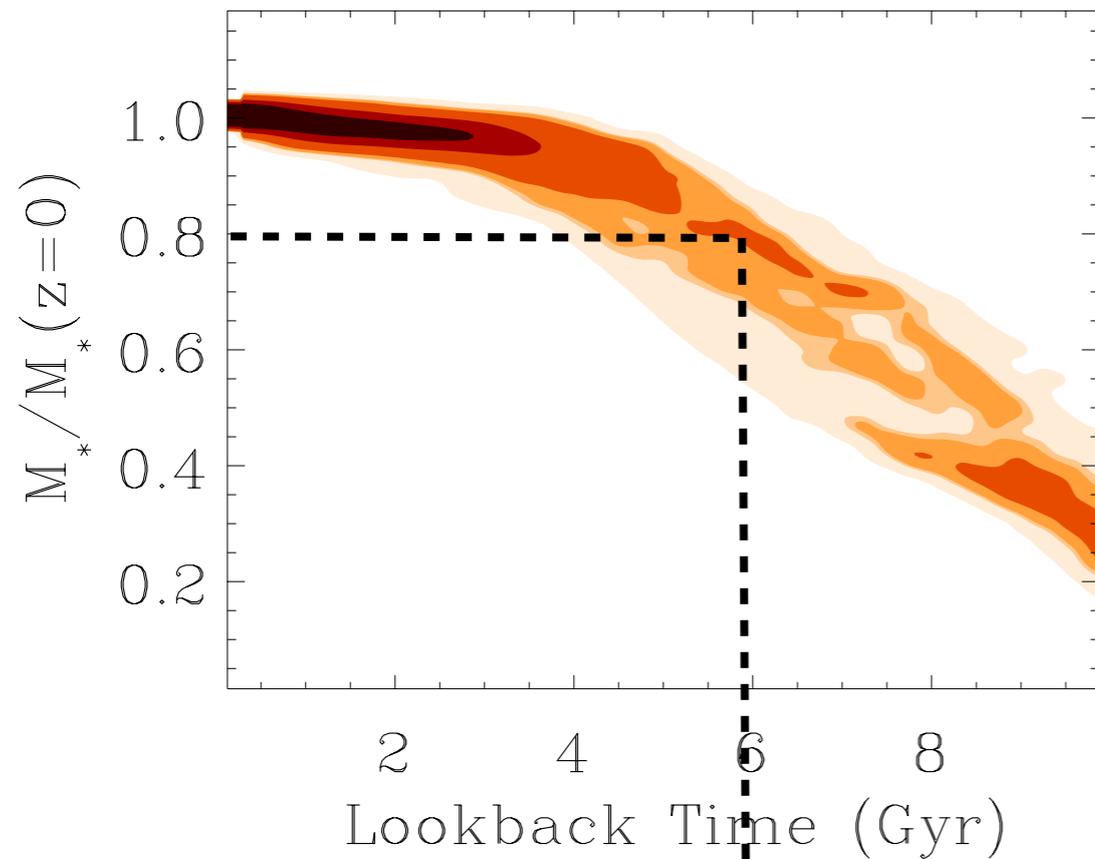
# Growth of Stellar Mass for Satellite Galaxies



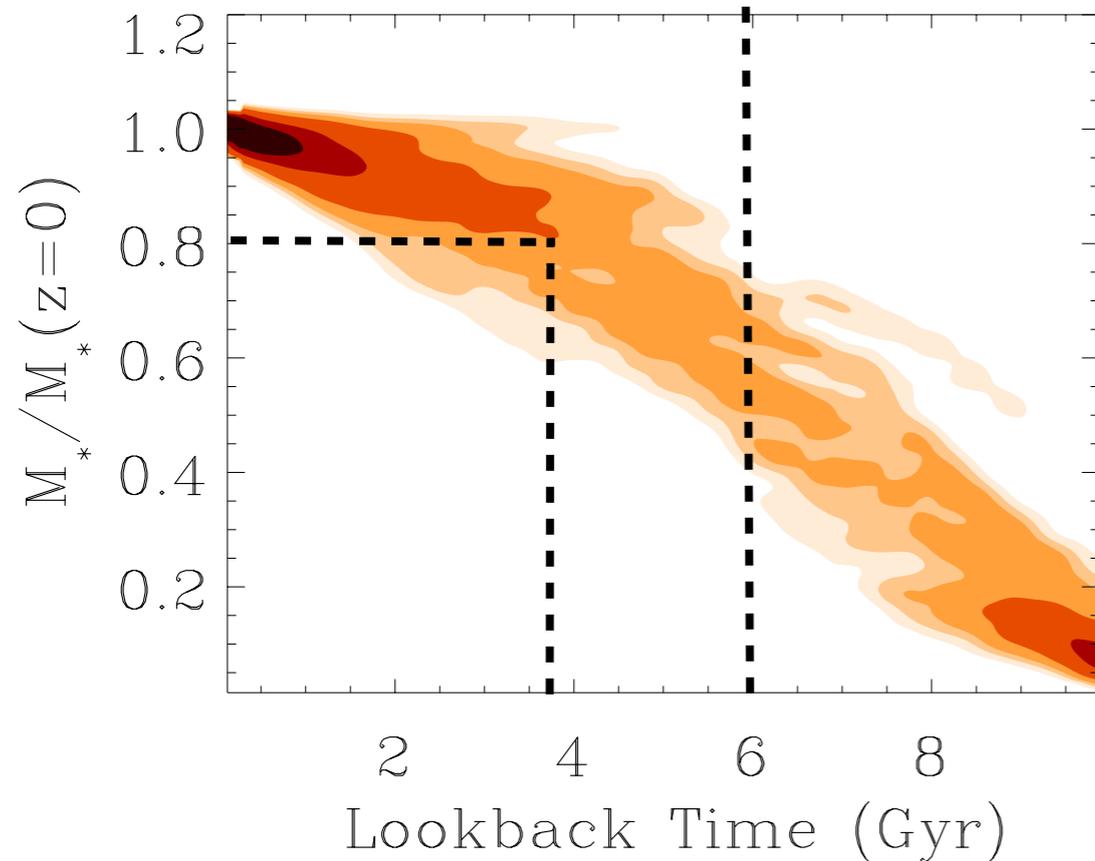
The suppression of progenitors of satellite galaxies with high SFR (those characterized by ineffective feedback) yields Slower growth of stellar mass in WDM



# Growth of Stellar Mass for Satellite Galaxies



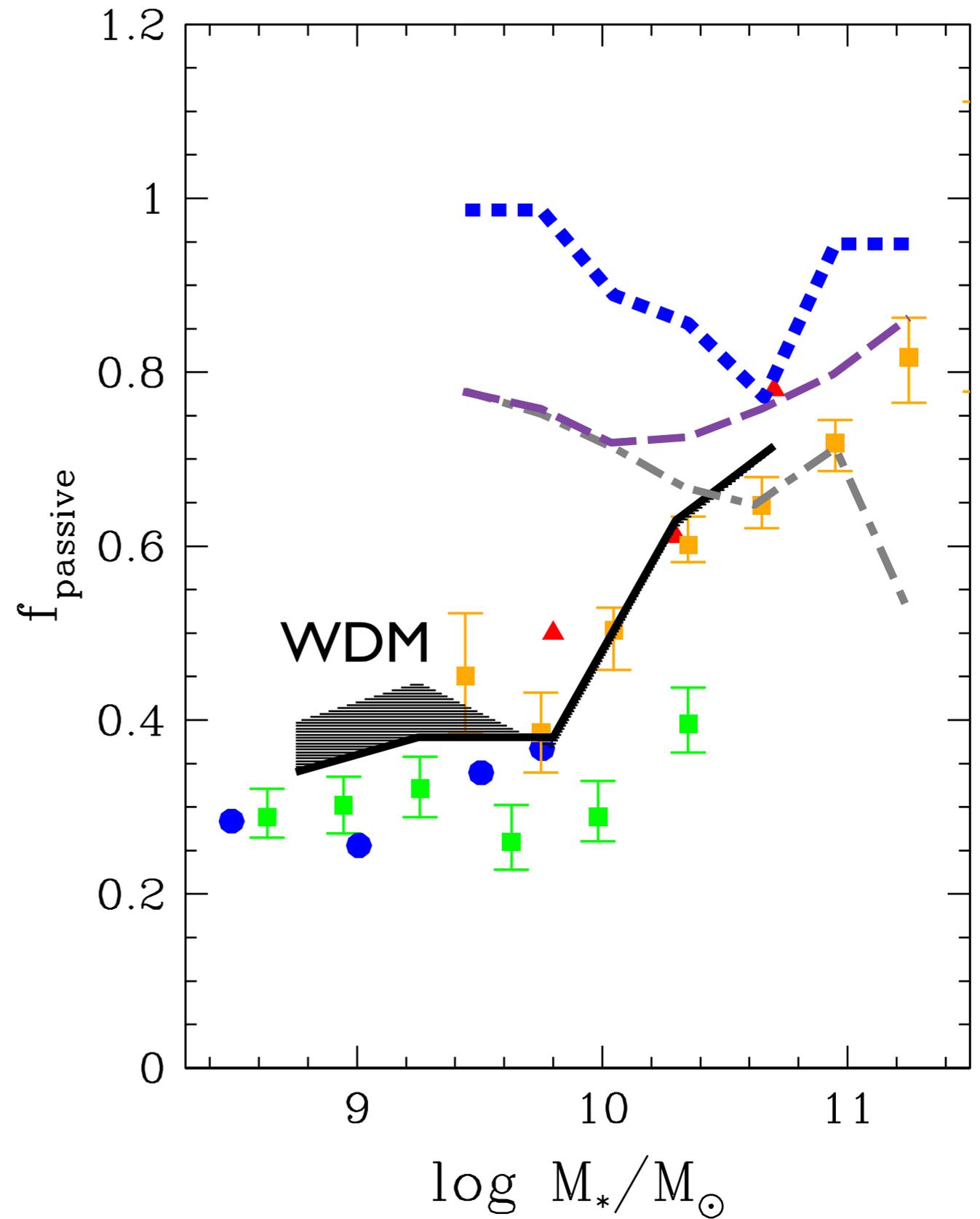
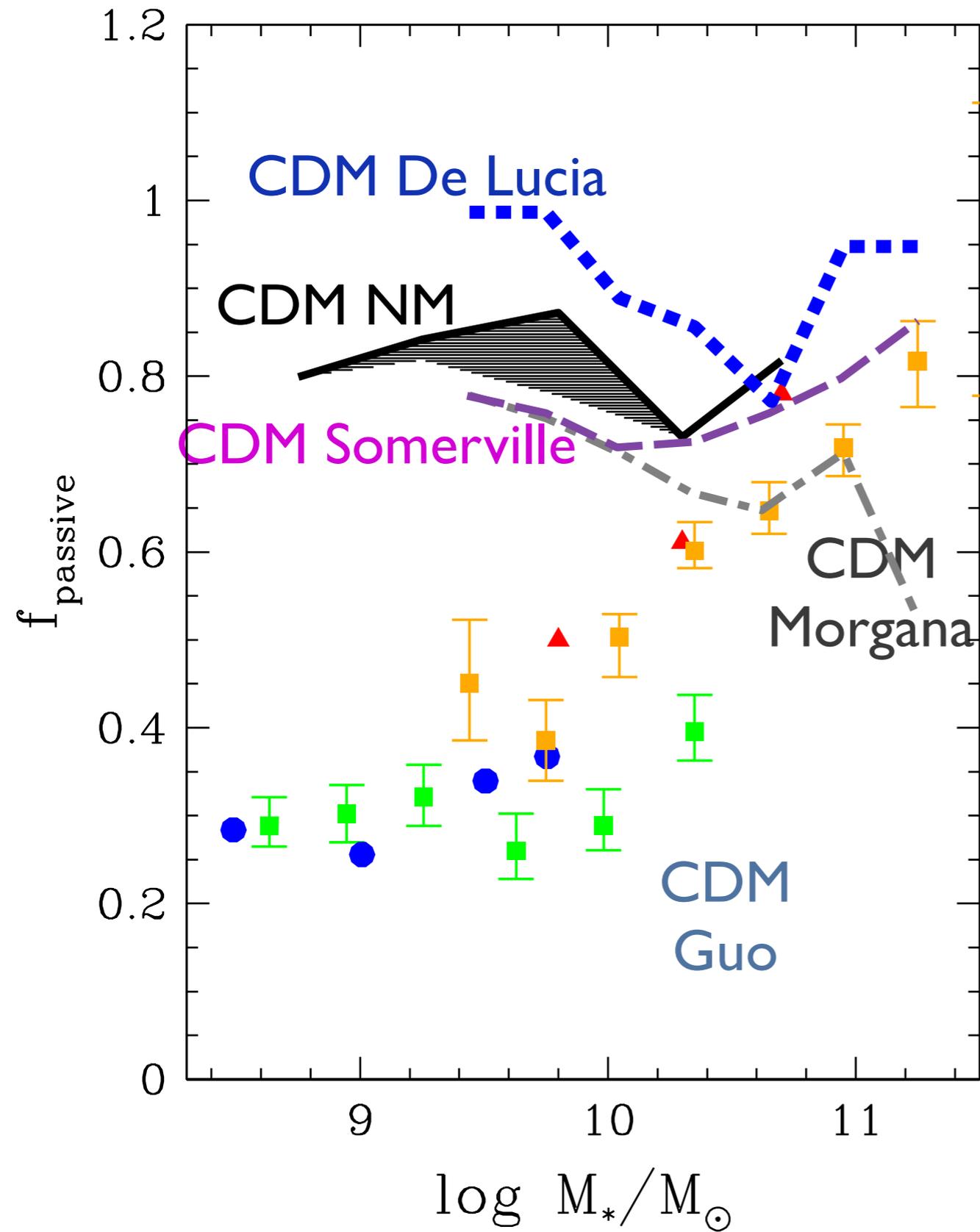
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CDM: 80 % of mass formed 6 Gyr ago  
WDM: 80 % of mass formed 4 Gyr ago

Approx. delay  $\sim$  2 Gyr

# Fraction of Quiescent Satellite Galaxies

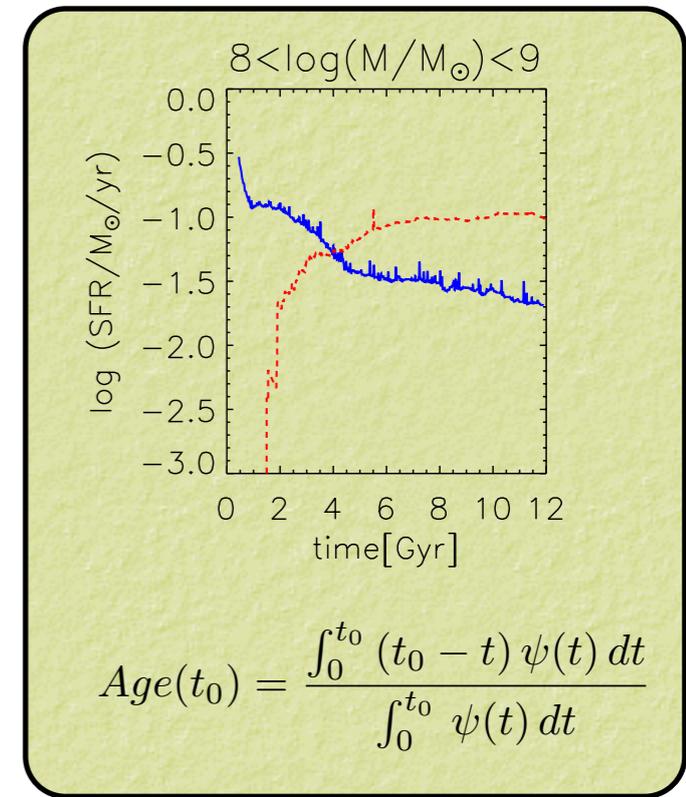


# The Age of stellar populations in low-mass galaxies

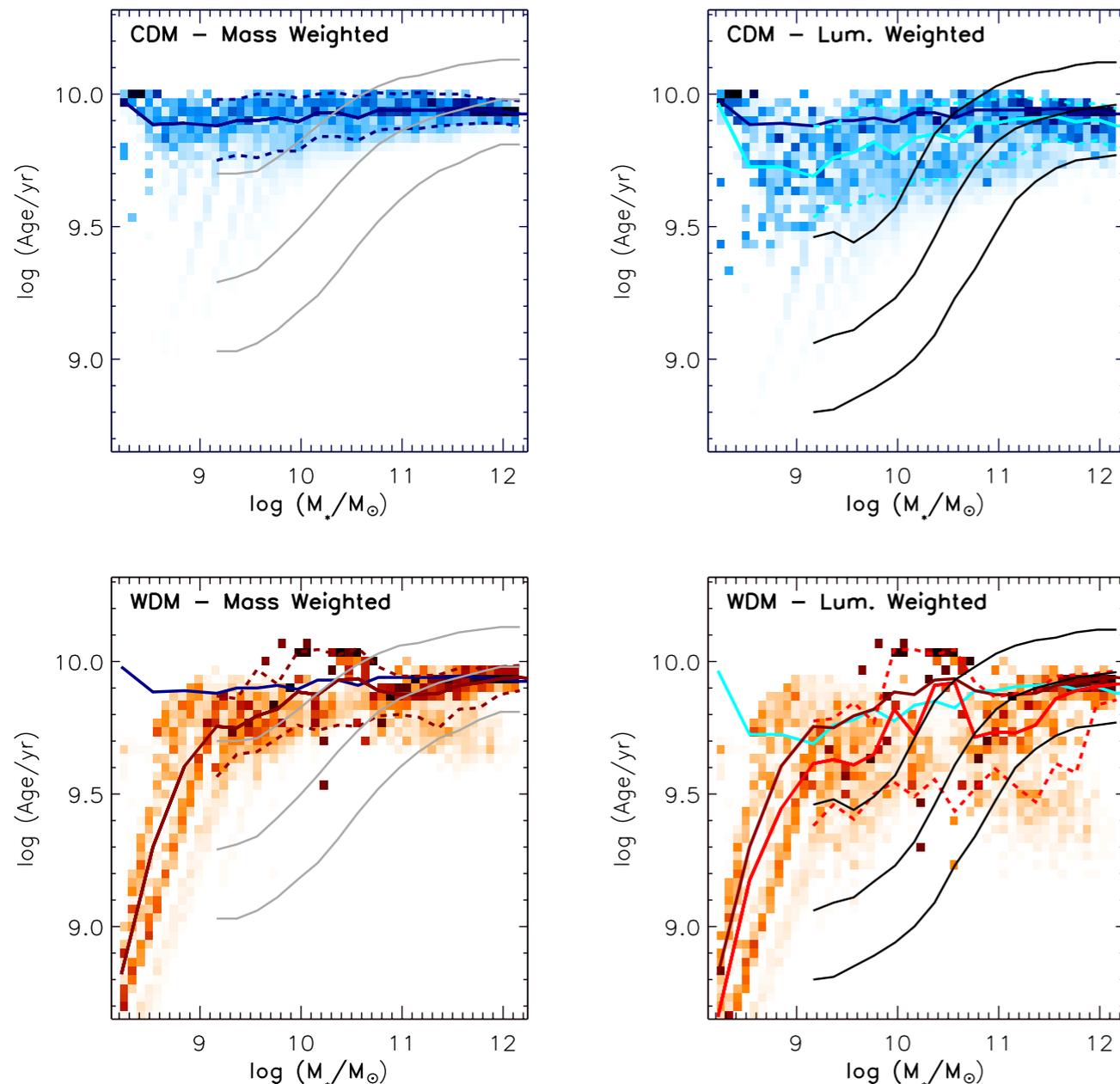
CDM predicts early collapse of a huge number of low-mass halos, which remain isolated at later times retaining the early-formed stellar populations; as a result, CDM-based SAMs generally provide flat age-mass relations (Fontanot et al. 2009; Pasquali et al. 2010; De Lucia & Borgani 2012).

Increasing the stellar feedback worsen the problem

Early SF: WDM induces delay in star formation, affects small-mass objects( see, e.g., Angulo et al. 2013)



Calura, NM, Gallazzi 2014



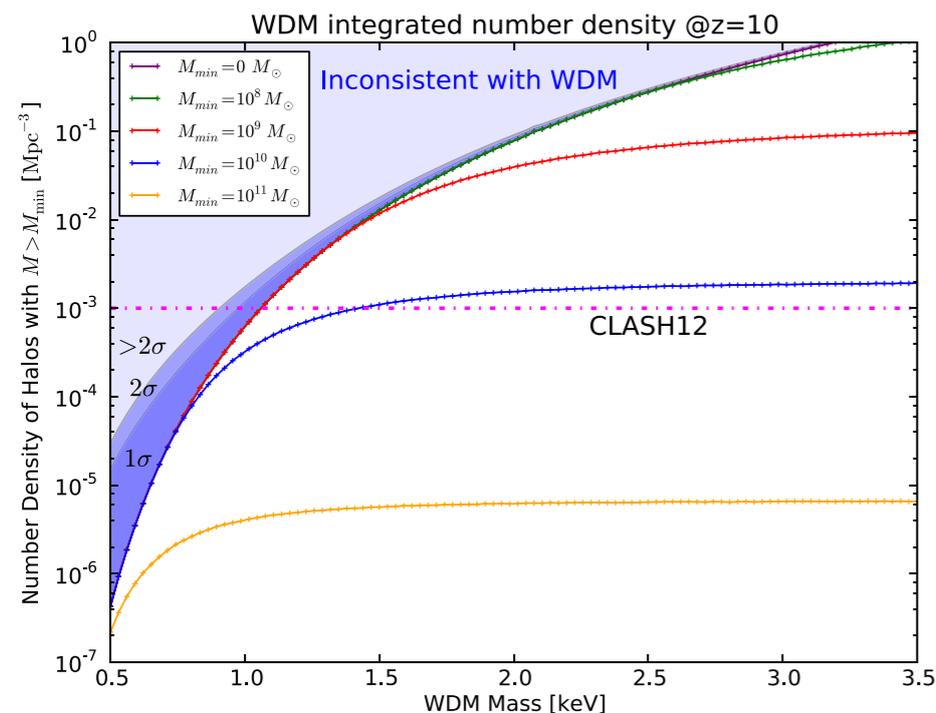
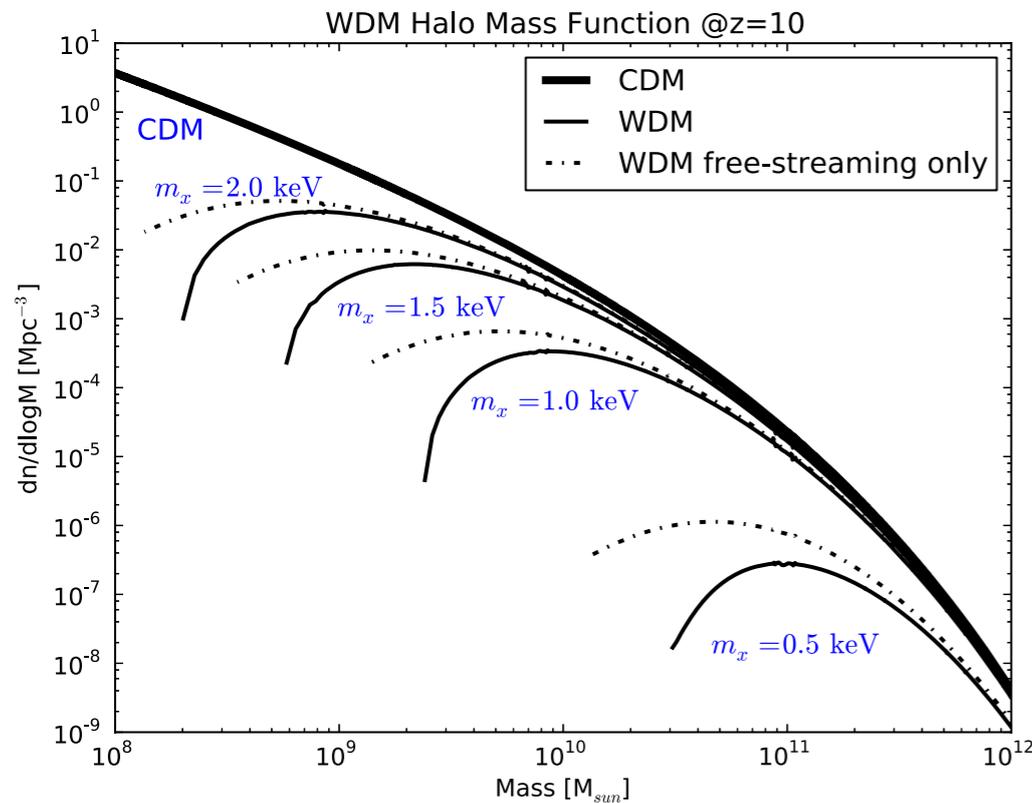
The upper, the middle and the lower grey (black) curves represent the 16th, the 50th (median) and the 84th percentiles of the observed distribution in mass-(light-)weighted stellar age (Gallazzi et al. 2008)

# Constraining the WDM candidate mass through the abundance of low-mass galaxies

Several works compare with MW satellite abundance. But results are subject to strong halo-to-halo variance

Pacucci, Mesinger, Haiman 2013

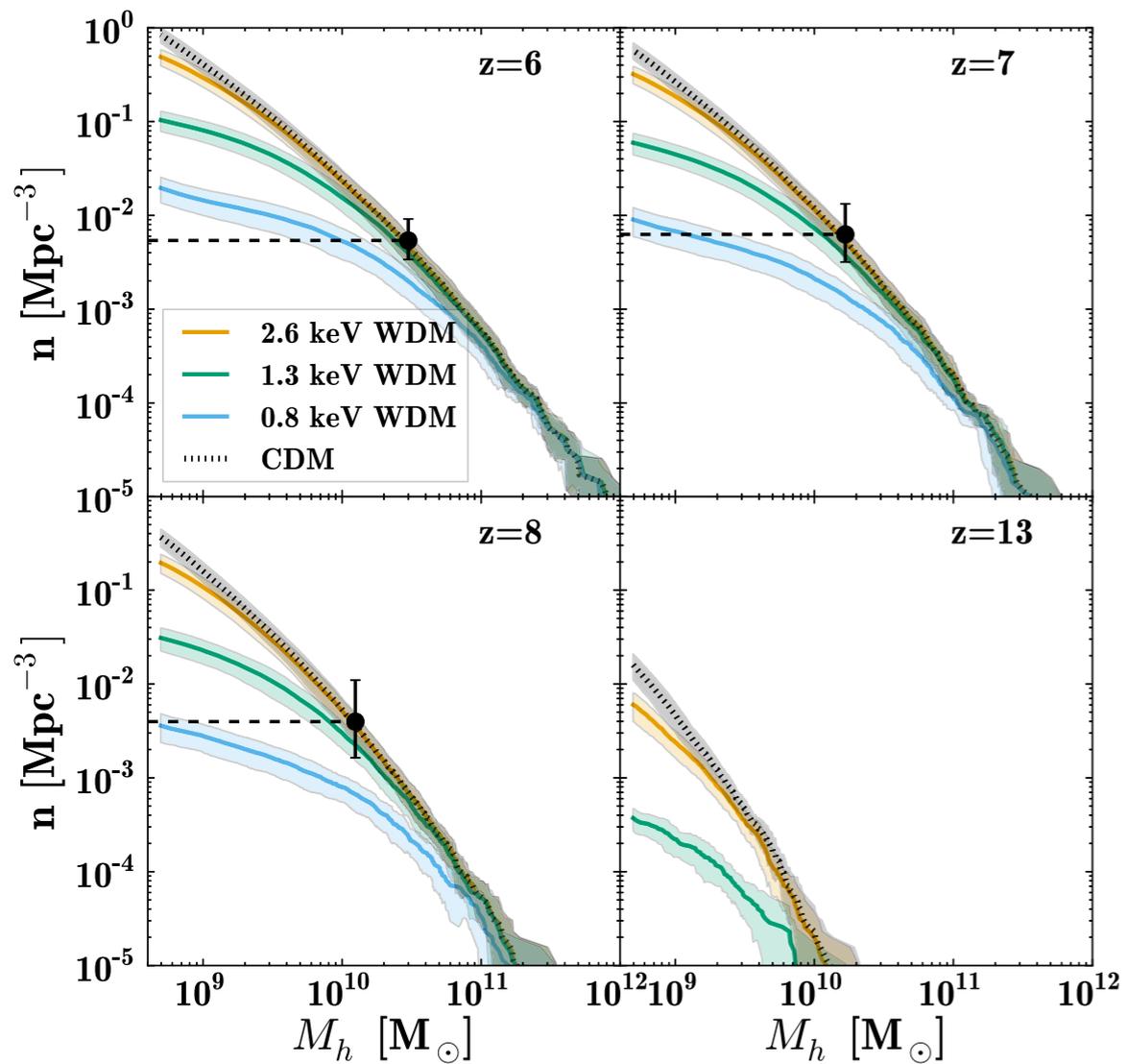
show that the two  $z \approx 10$  galaxies already detected by the Cluster Lensing And Supernova survey with Hubble (CLASH) survey are sufficient to constrain the WDM particle mass to  $m_x > 1$



Schultz et al. 2014

Use abundance matching at the bright end of the the high-z luminosity functions to compute L- $M_h$  relation.

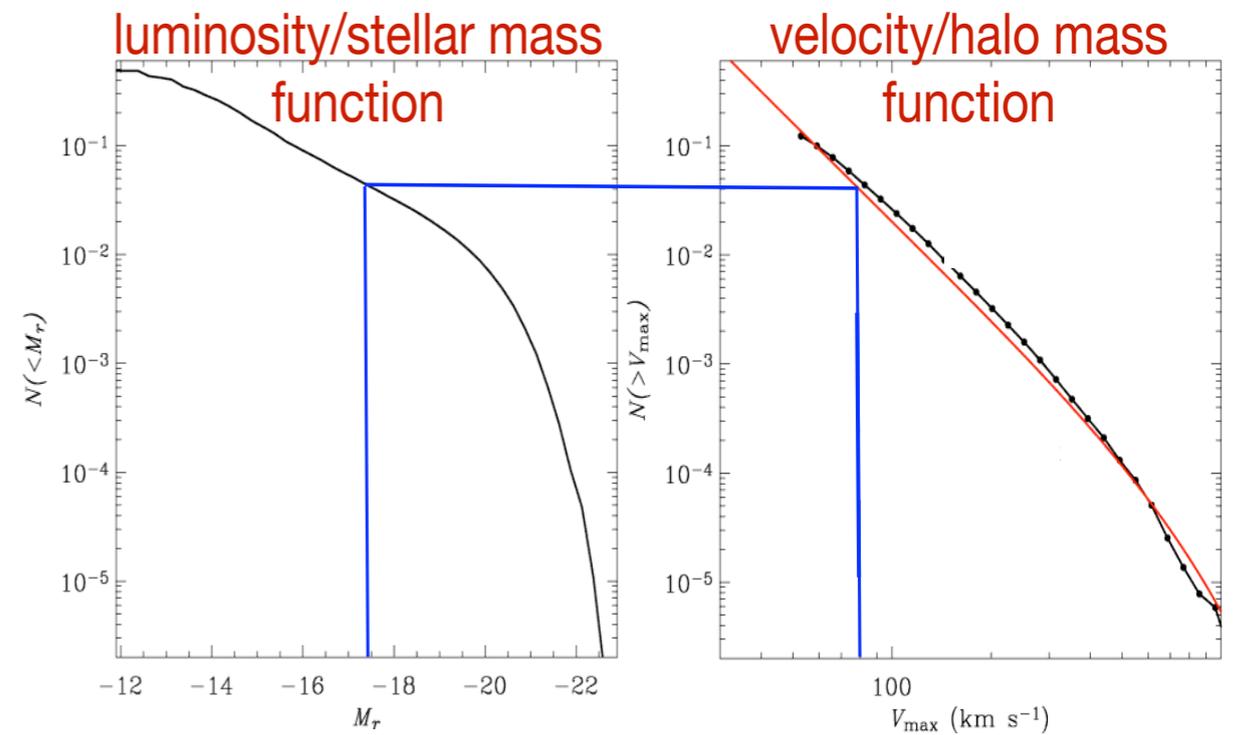
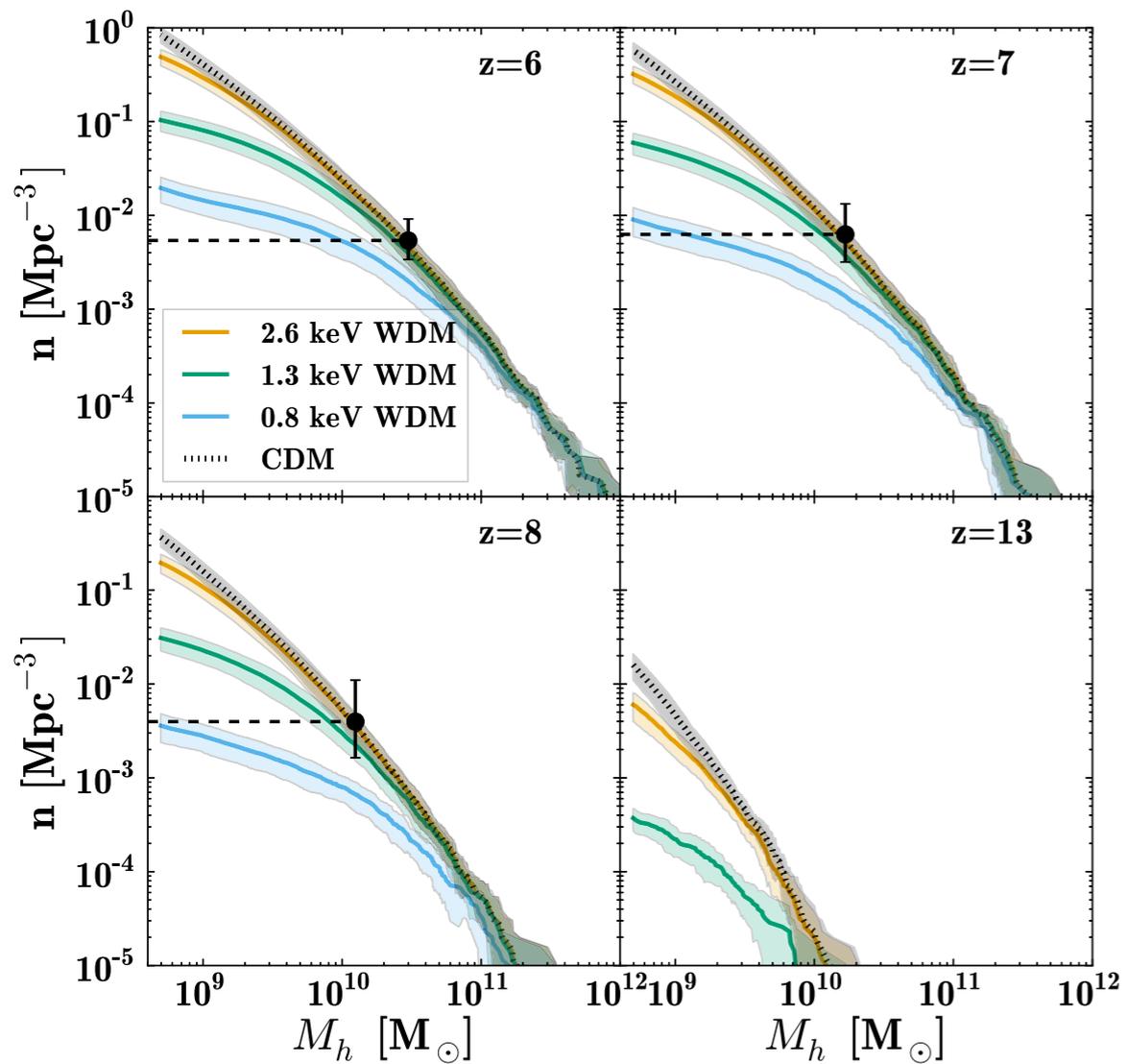
Comparing the observed and the predicted densities of faint galaxies they derive a lower mass limit  $m_\chi > 1$  keV



Schultz et al. 2014

Use abundance matching at the bright end of the the high-z luminosity functions to compute  $L$ - $M_h$  relation.

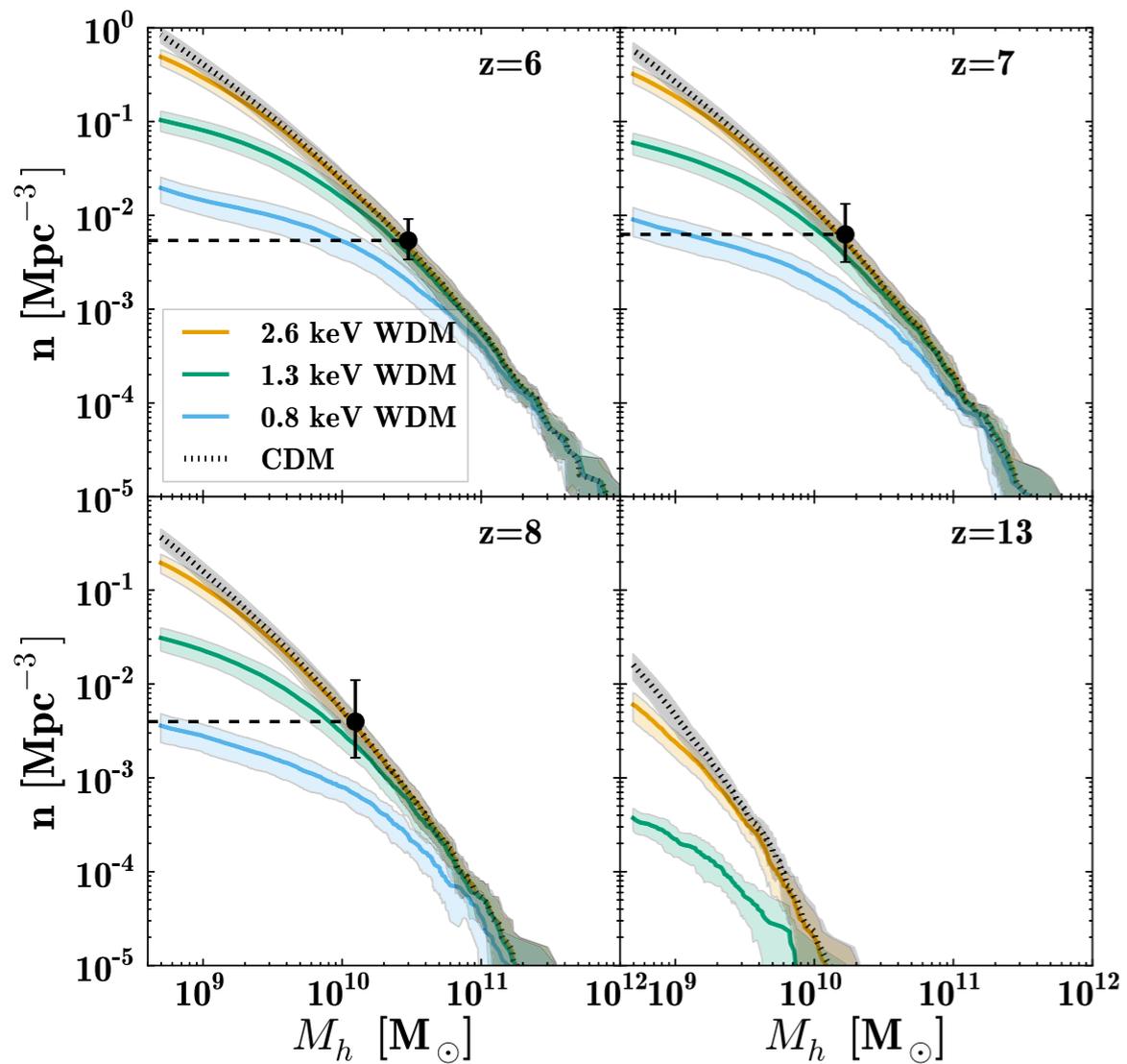
Comparing the observed and the predicted densities of faint galaxies they derive a lower mass limit  $m_\chi > 1$  keV



Schultz et al. 2014

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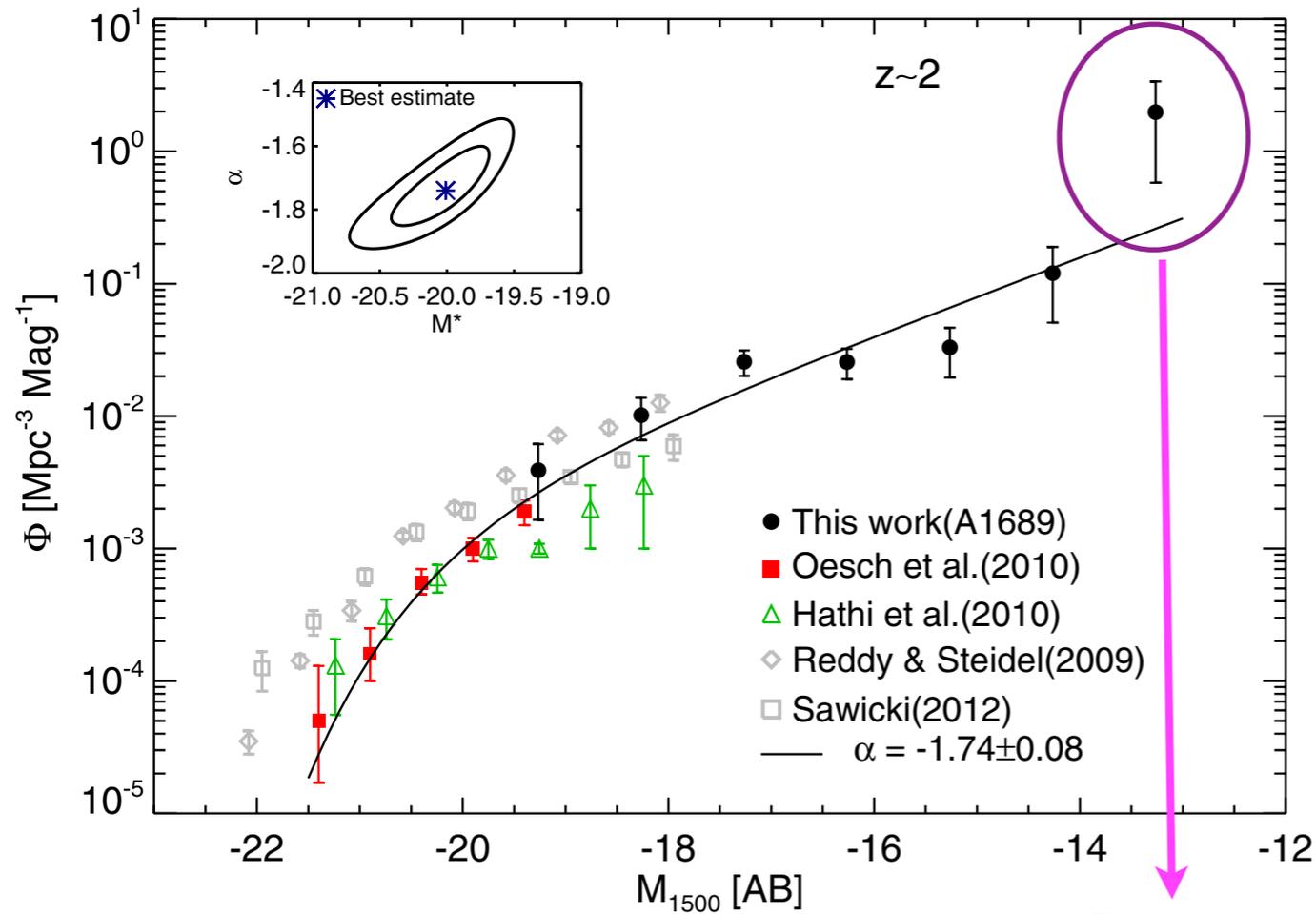
Vertical blue line

# A different approach

## focus on lower redshift but deeper observations

THE ASTROPHYSICAL JOURNAL, 780:143 (14pp), 2014 January 10

ALAVI ET AL.



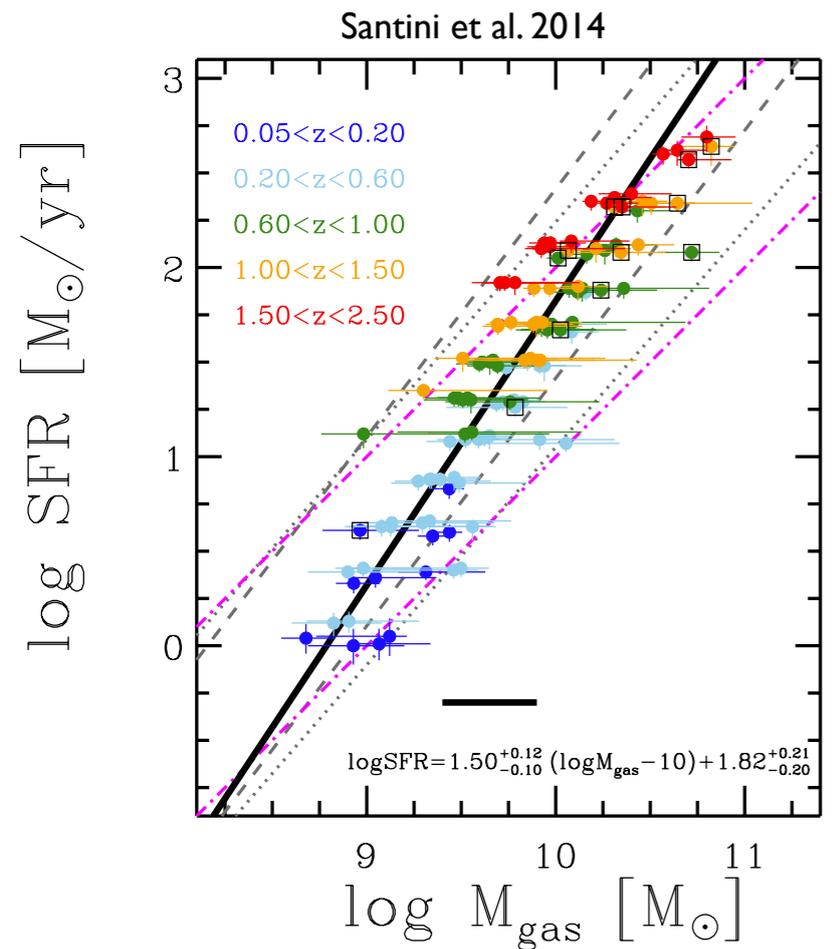
To connect  $M_{1500}$  to DM mass  $M$

1) UV luminosity is directly linked to SFR  
 $\log \text{SFR} = 1 - 2.5(M_{1500} + 20.5)$

Deepest  
Luminosity  
Function measured  
so far

# A different approach

## focus on lower redshift but deeper observations

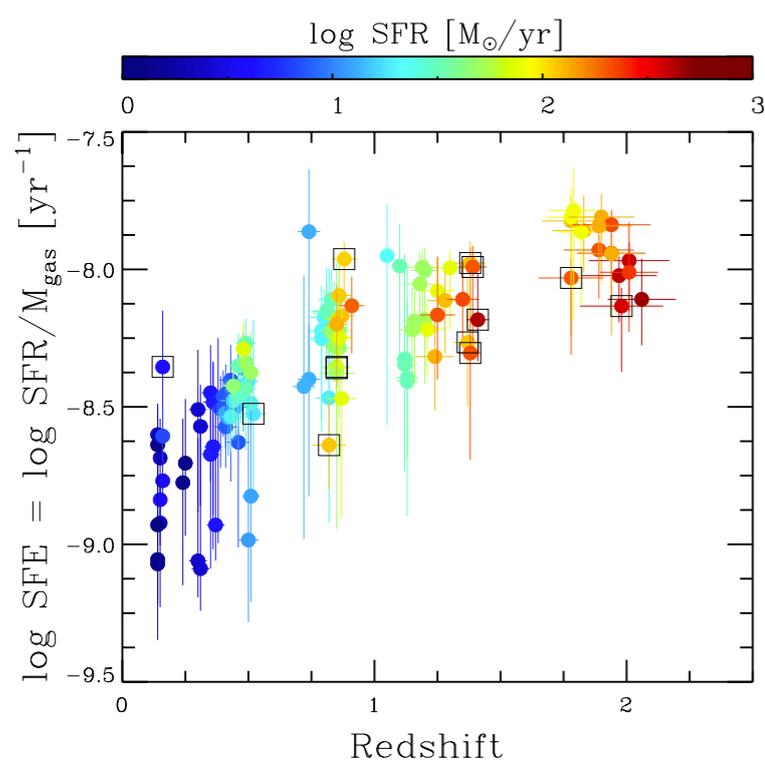


The slope of the SFR -  $M_{\text{gas}}$  relation yields the gas-to-star conversion timescale at  $z=2$   
 $T^* = 3 \cdot 10^7 - 2 \cdot 10^8 \text{ yrs}$

To connect  $M_{1500}$  to DM mass  $M$

1) UV luminosity is directly linked to SFR  
 $\log \text{SFR} = 1 - 2.5(M_{1500} + 20.5)$

2)  $\text{SFR} = M_{\text{gas}}/T^*$



# A different approach

## focus on lower redshift but deeper observations

To connect  $M_{1500}$  to DM mass  $M$

1) UV luminosity is directly linked to SFR  
 $\log \text{SFR} = 1 - 2.5(M_{1500} + 20.5)$

2)  $\text{SFR} = M_{\text{gas}} / \tau^*$

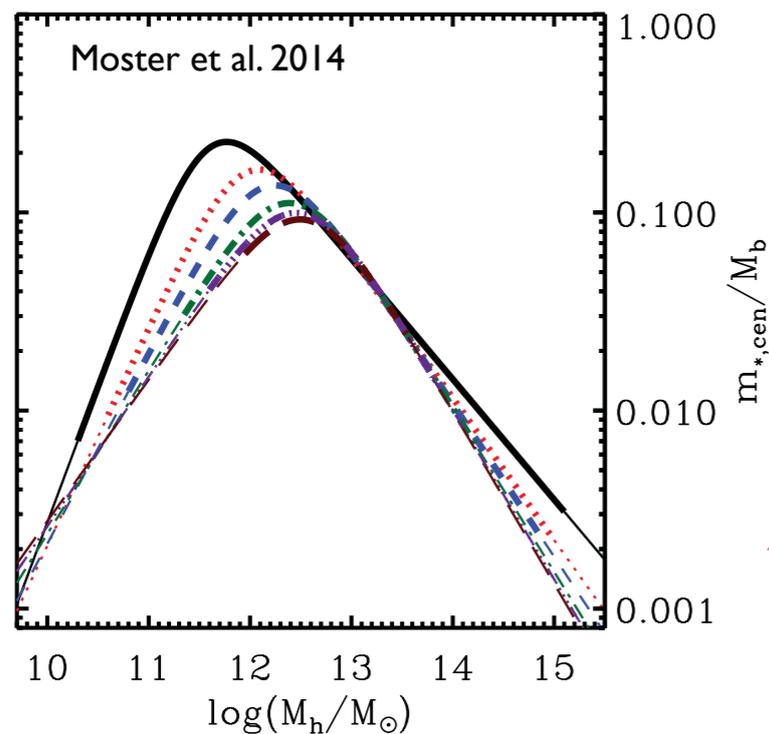
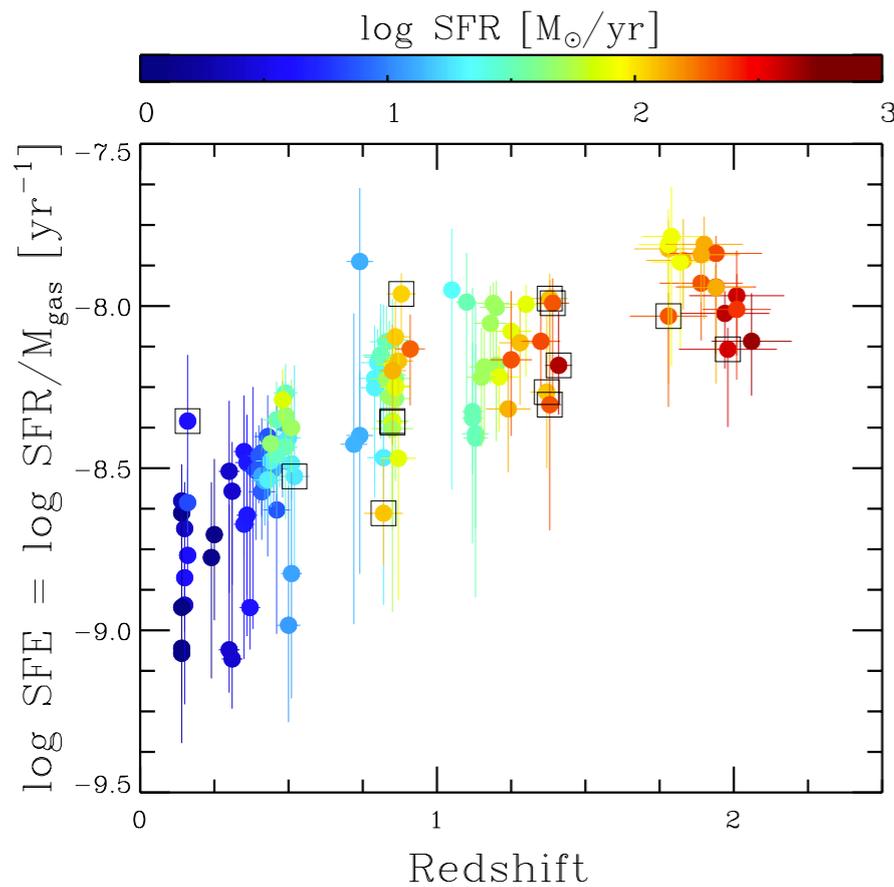
3)  $M_{\text{gas}} = f_g (\Omega_b / \Omega_{\text{DM}}) M_{\text{DM}}$

4)  $\text{SFR} = (f_g / \tau^*) (\Omega_b / \Omega_{\text{DM}}) M_{\text{DM}}$

write  $M_{\text{gas}}$  as a fraction of the baryonic content of DM halo

# A different approach

## focus on lower redshift but deeper observations



To connect  $M_{1500}$  to DM mass  $M$

1) UV luminosity is directly linked to SFR  
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5) Observations yield

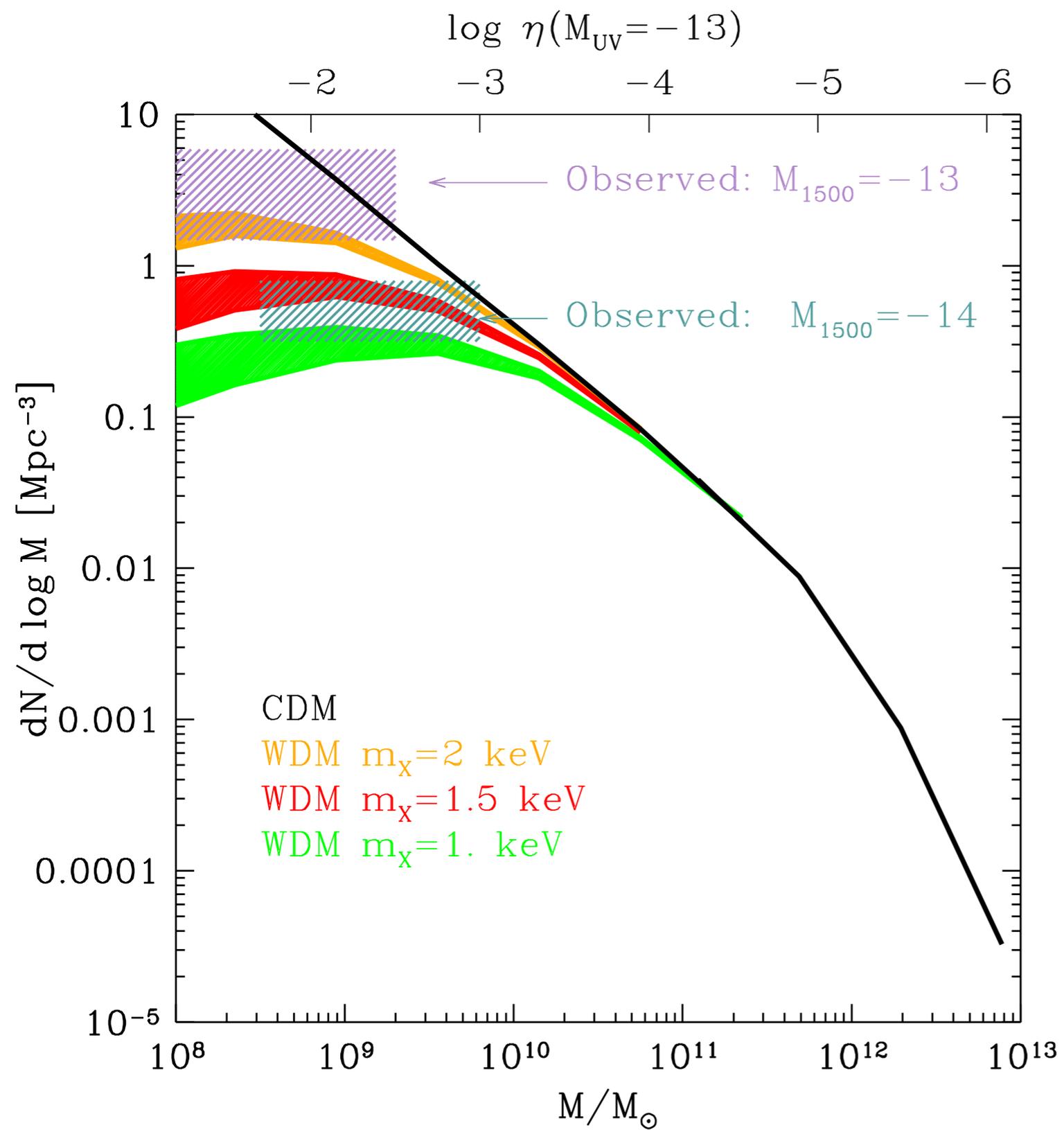
$\tau^* = 0.1 - 1 \text{ Gyr}$  at  $z=2$

$f_g = 0.001 - 0.01$  for dwarf galaxies

6)  $\text{SFR} = \eta (\Omega_b / \Omega_{\text{DM}}) M_{\text{DM}}$

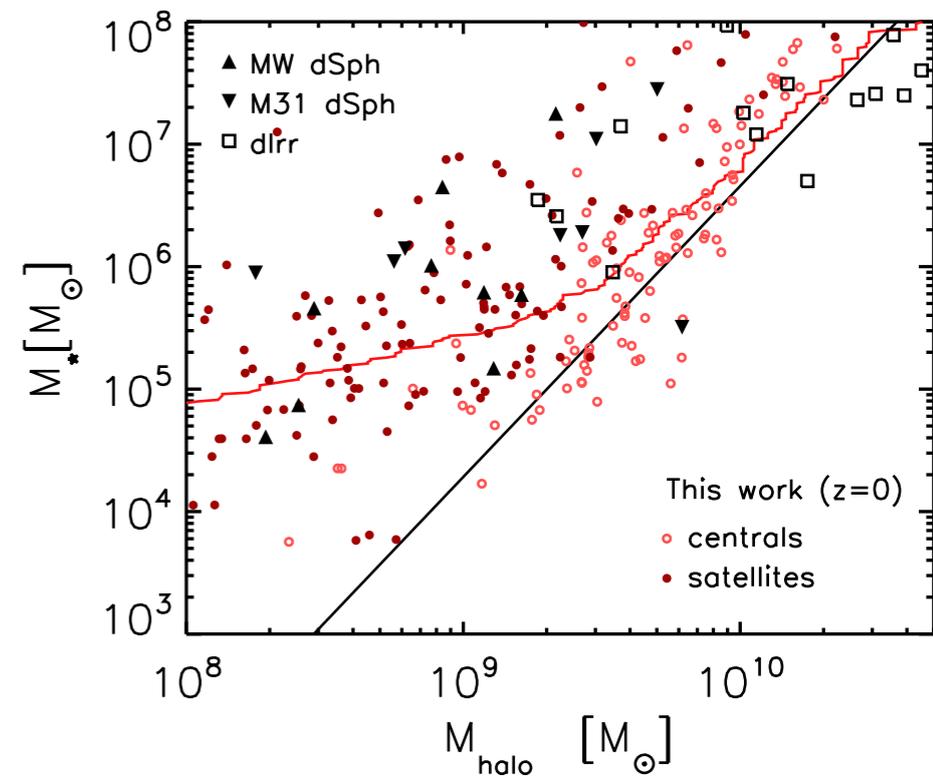
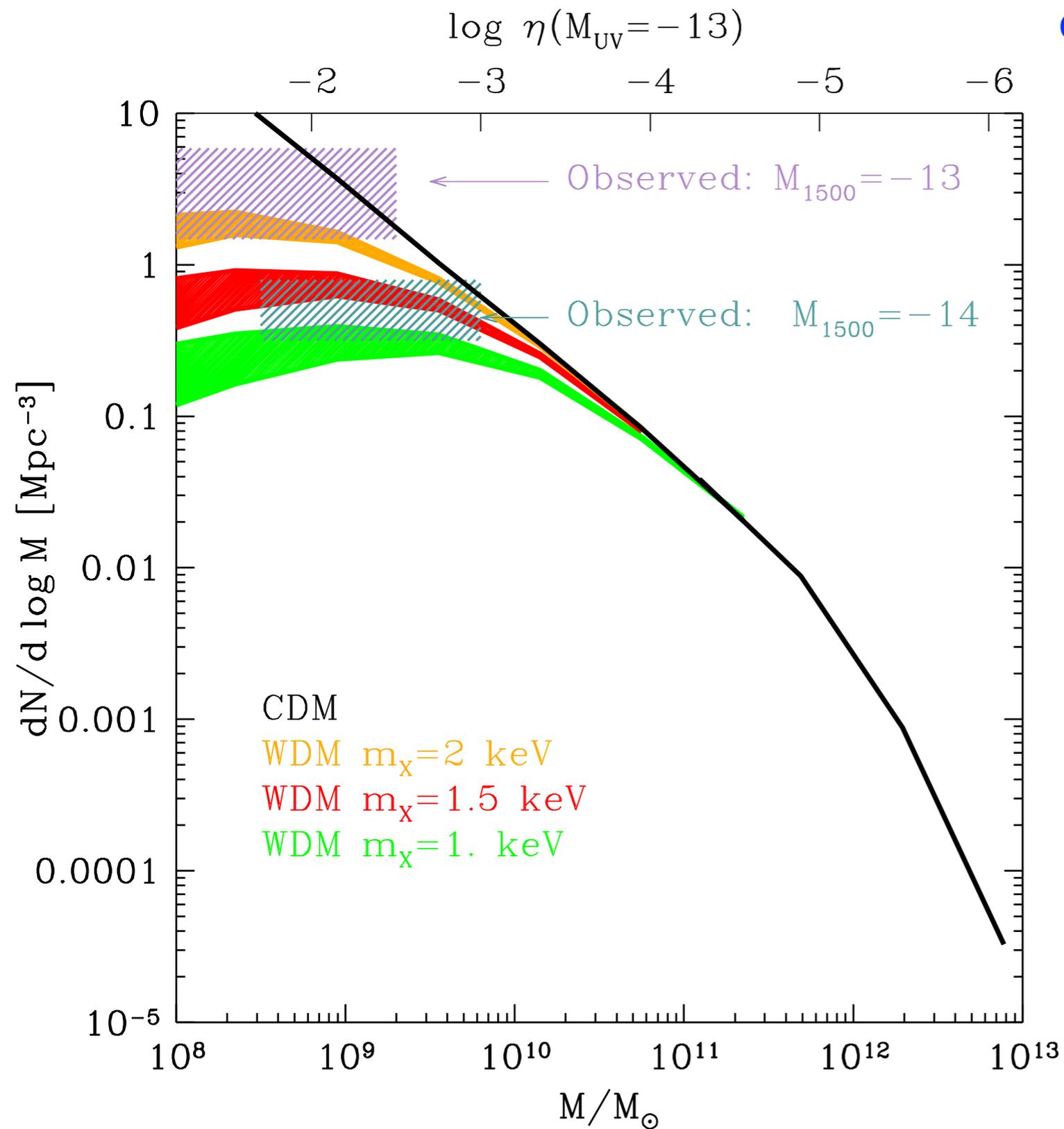
with  $\eta = 0.001 - 0.1$

$\eta \rightarrow$  efficiency of SF for  
 give DM mass (L/M ratios)

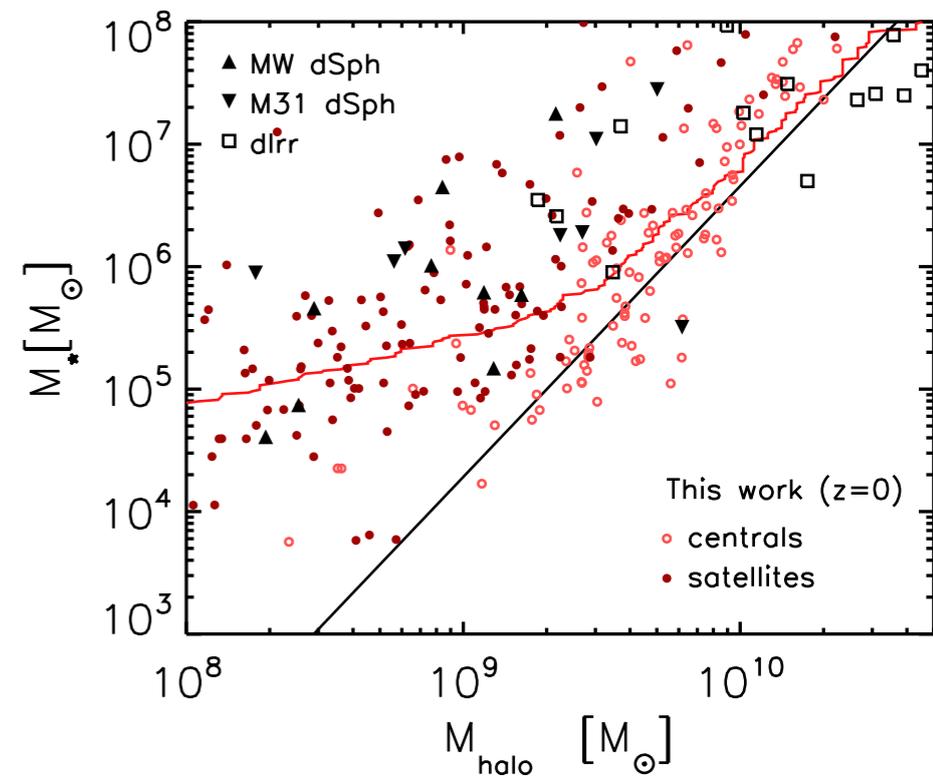
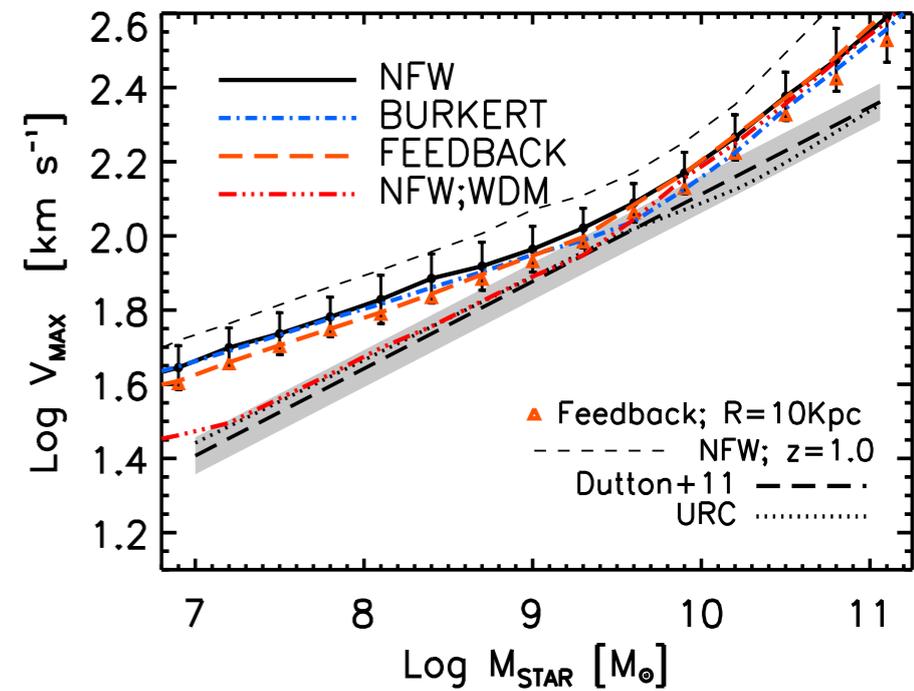
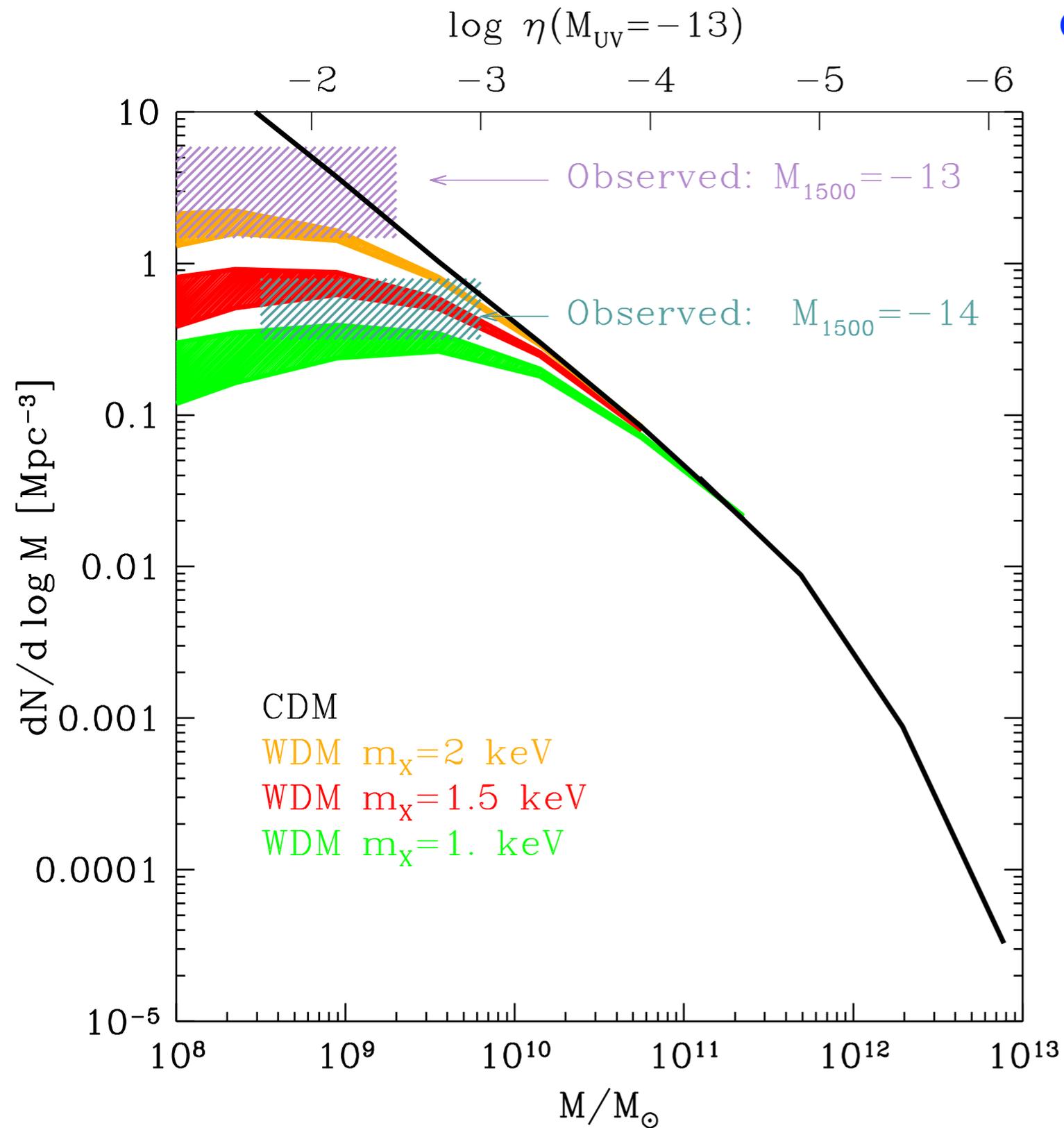


**Note:**  
 baryonic processes  
 can make the LF flatter  
 but not steeper !

CDM requires  
 low  $\eta$ , i.e., low star formation  
 efficiency. Compares critically with  
 observed  $M^*-M_{\text{halo}}$  relations



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# LSB galaxies in Virgo (Giallongo et al. 2015)

TABLE 1  
LSB CATALOG IN THE VIRGO-XMMUJ1230 FIELD

ID	LSB Label	RA	DEC	$R$	$\mu_0$	$n^a$	$M_R^b$	$r^c$ (arcsec)	$r$ (pc) <sup>c</sup>	$b/a$	$R-Z$
6490	A	187.3919684	+13.7704609	21.86	24.91	0.92	-9.24	3.07	246	0.7	0.00
6043	B	187.6635951	+13.7391869	20.38	24.54	0.70	-10.79	4.48	359	0.7	0.31
5833	C	187.5879561	+13.7058350	21.59	26.23	0.55	-9.56	4.37	350	0.9	-0.23
5143	D	187.5483601	+13.6914967	18.30	24.01	0.67	-12.87	7.99	639	0.9	0.44
4739	E	187.3814266	+13.6619273	18.75	23.49	0.72	-12.42	5.71	457	0.7	0.35
4367	F	187.3863203	+13.6222745	21.93	24.54	0.88	-9.25	2.73	218	0.6	0.20
3516	G	187.6600347	+13.6196001	18.05	24.25	0.62	-13.12	10.43	835	0.7	0.11
3214	H	187.6224577	+13.5565951	21.14	25.11	0.57	-10.03	3.14	251	0.9	0.39
2245	J	187.4138959	+13.5075398	21.24	25.53	0.69	-9.93	4.19	335	0.8	0.11
2001	K	187.7070994	+13.5053537	19.07	25.79	0.44	-12.11	10.68	855	0.9	-0.30
2003	L	187.7244716	+13.4939191	21.89	26.12	0.30	-9.28	3.05	244	0.9	0.02

<sup>a</sup> Sérsic index

<sup>b</sup> Absolute magnitudes computed adopting an average distance modulus for Virgo  $\Delta M = 31.1$  (Mei et al. (2007)), an average galactic absorption of  $-0.07$ .

<sup>c</sup> Scale radius from the Sersic profile fitting. An angular scale of  $80 \text{ pc arcsec}^{-1}$  has been adopted.

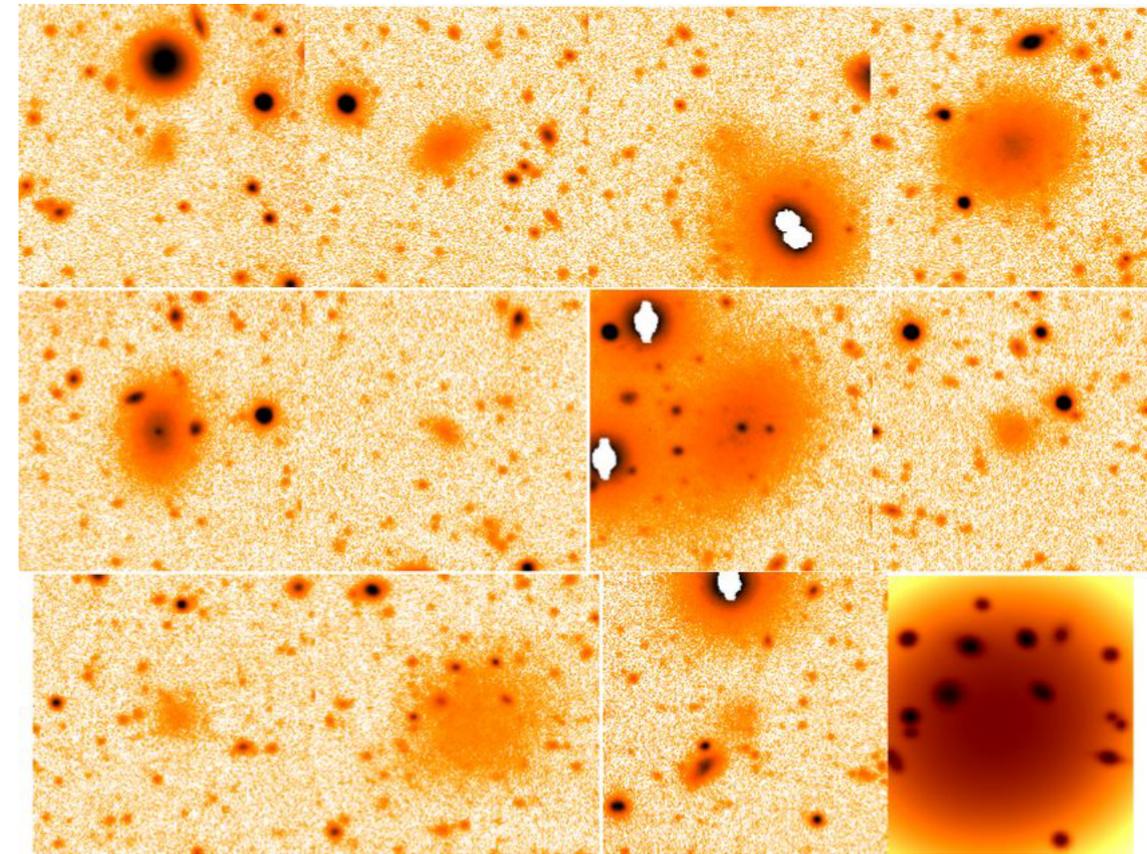


FIG. 2.— Selected LSB dwarfs in the Virgo-xmmuj1230 field; the box size of each image is  $\simeq 57 \text{ arcsec}$ . The sequence from the top to the bottom follows the list in Table 1. The last box on the bottom right show a zoomed image of the Galfit best fit model of the LSB "K". All the small background sources expected within the LSB halo have been fitted separately.

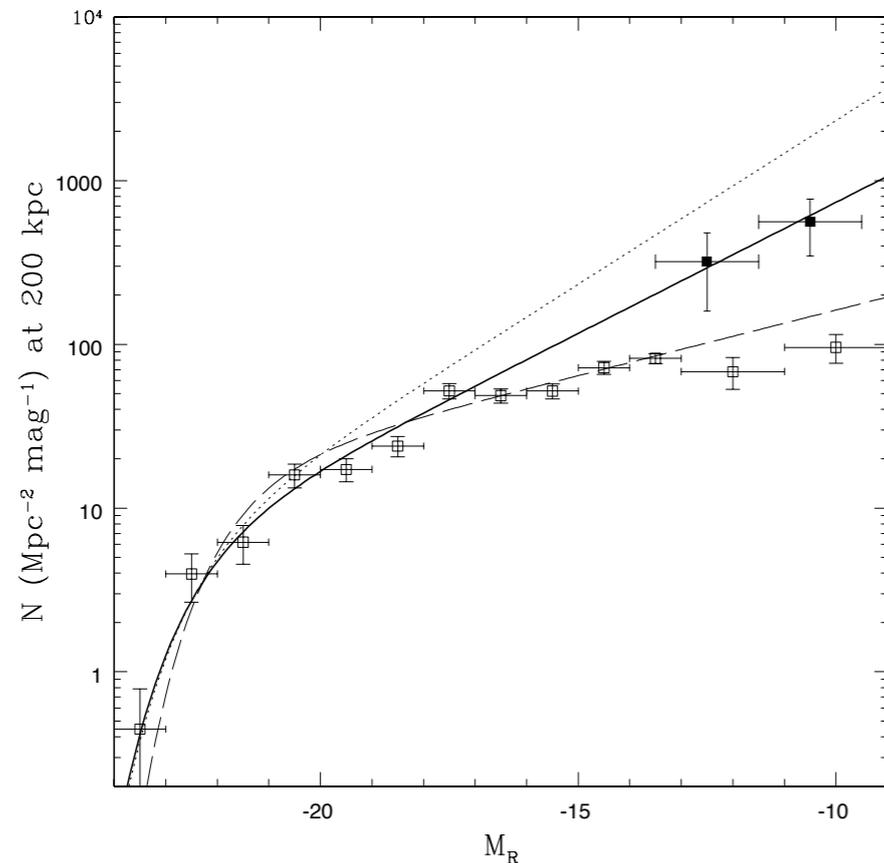


FIG. 3.— Virgo projected luminosity function normalized at 200 kpc. Filled squares are from the present sample after conversion from AB to the Vega magnitude system by  $R(\text{Vega}) - R(\text{AB}) = -0.26$ . Empty squares are from Trentham & Tully (2002) in the Vega system. The continuous curve represents a Schechter shape with slope  $\alpha \sim -1.4$  and  $M^* \sim -22.3$ . Two fainter slopes  $\alpha \sim -1.2, -1.5$  are also shown for comparison (dashed and dotted, respectively).

Steep LF  $N(L) \sim L^{-1.4}$

Compute sub-haloes mass function  $N(M) \sim M^{-\alpha_{DM}}$   
 measure  $\alpha_{DM}$  for different WDM mass

$\propto$

Compute  $N(L)$  for different  $L/M$  ratios  
 i.e., reasonable values of  $\beta$  (assuming  $L \sim M^\beta$ )

Compare with observed slope

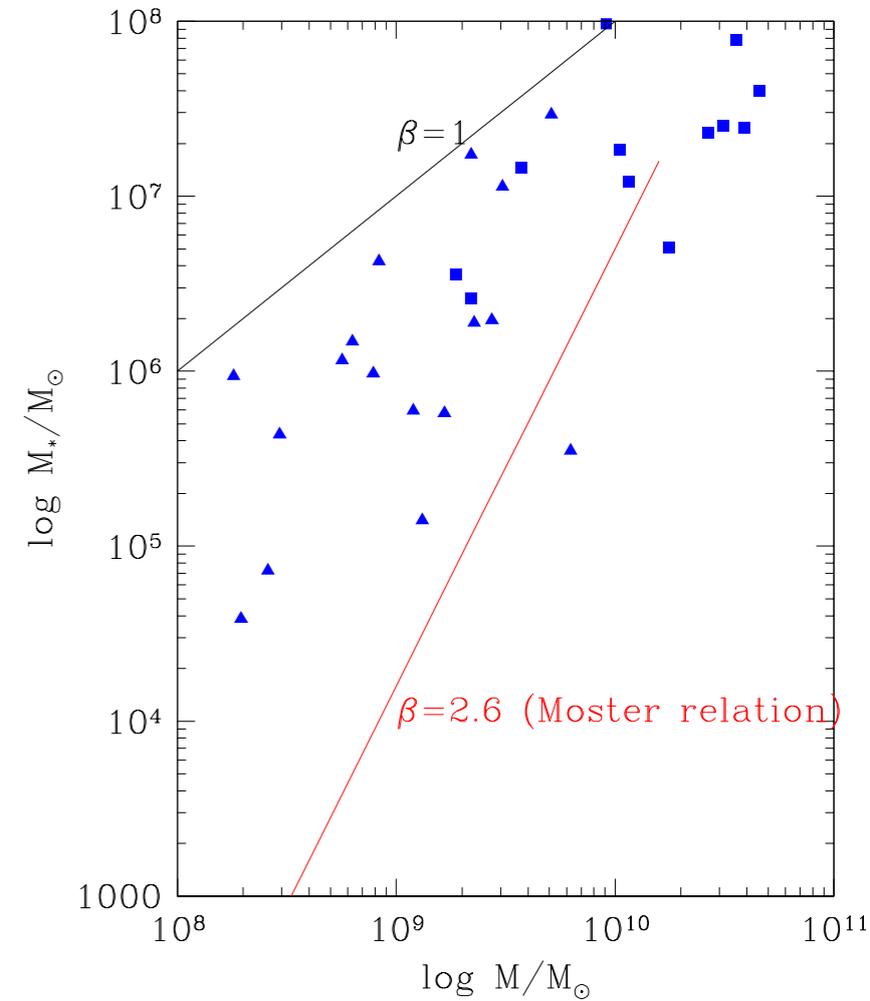
$$L \propto M^\beta$$

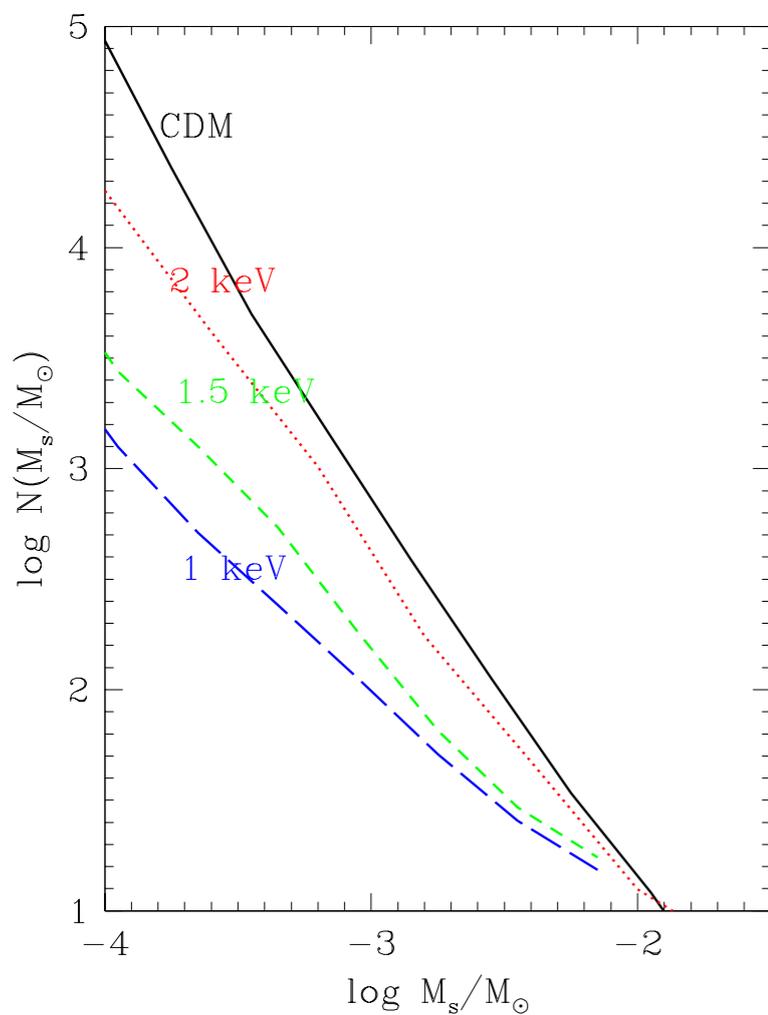
$$L/M \propto M^{\beta-1}$$

$$N(M) \propto M^{-\alpha_{DM}} \rightarrow N(L) \propto L^{-\alpha}$$

$$\alpha = \frac{1 - \alpha_{DM} - \beta}{\beta}$$

E.g.  $\alpha=2$   
 $\beta=1 \longrightarrow N(L) \propto L^{-3/2}$



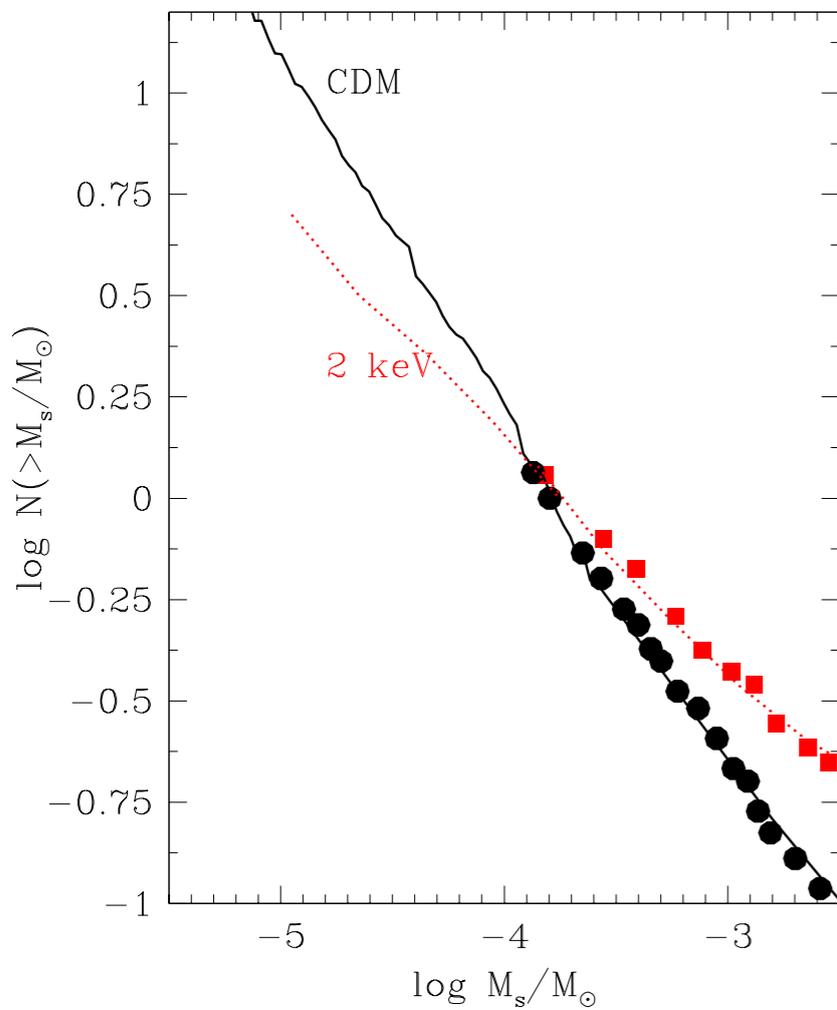


$$\alpha(m_\chi = 1 \text{ keV}) = 1.2$$

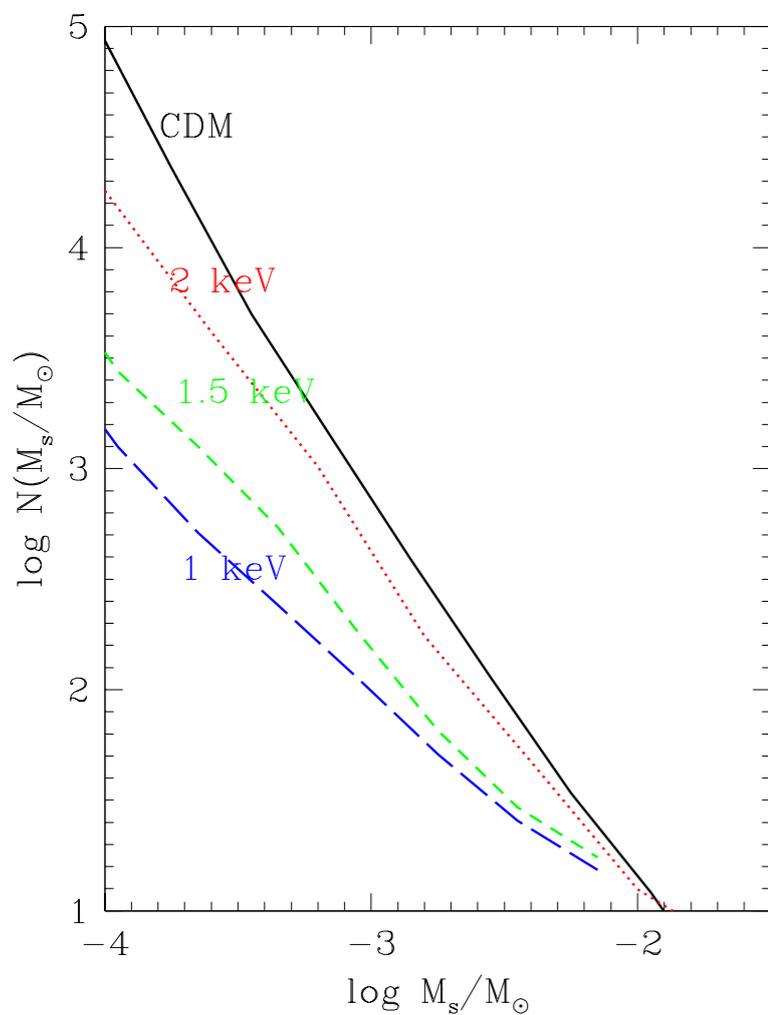
$$\alpha(m_\chi = 1.5 \text{ keV}) = 1.4$$

$$\alpha(m_\chi = 2 \text{ keV}) = 1.6$$

$$\alpha_{\text{CDM}} = 1.8$$

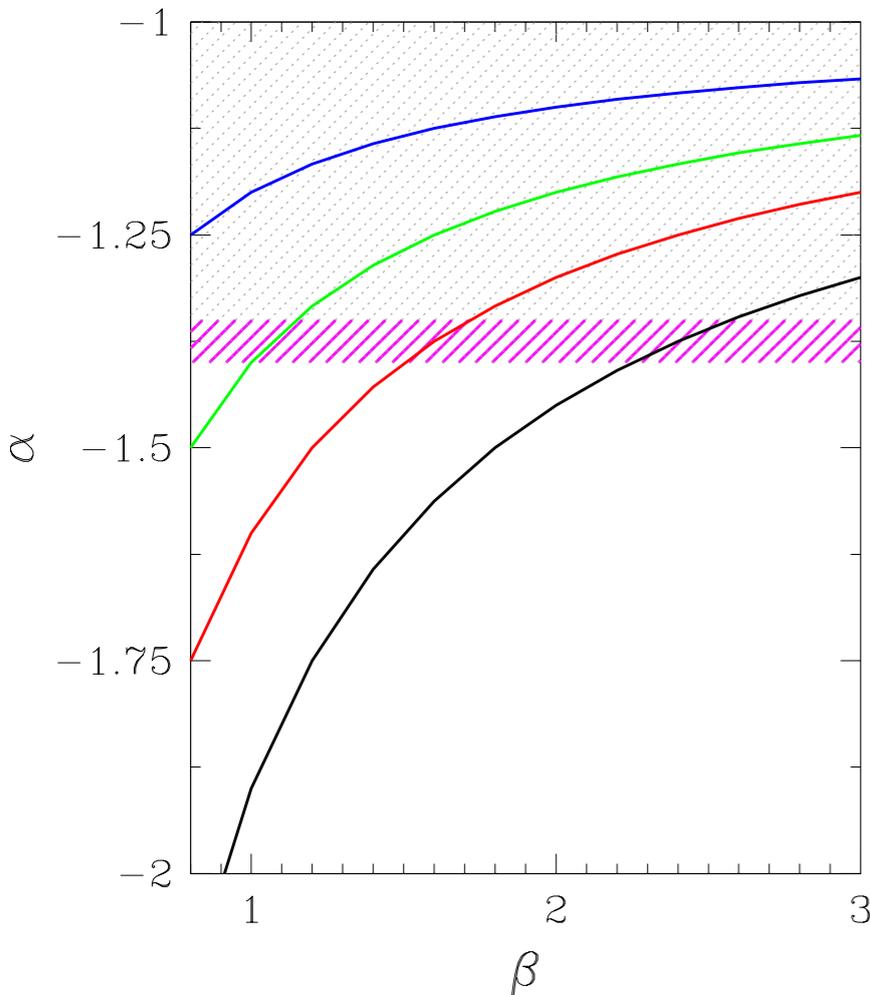


In the CDM and  $m_\chi = 2 \text{ keV}$  case we can test the results against N-body results (but extend to much smaller satellite masses)

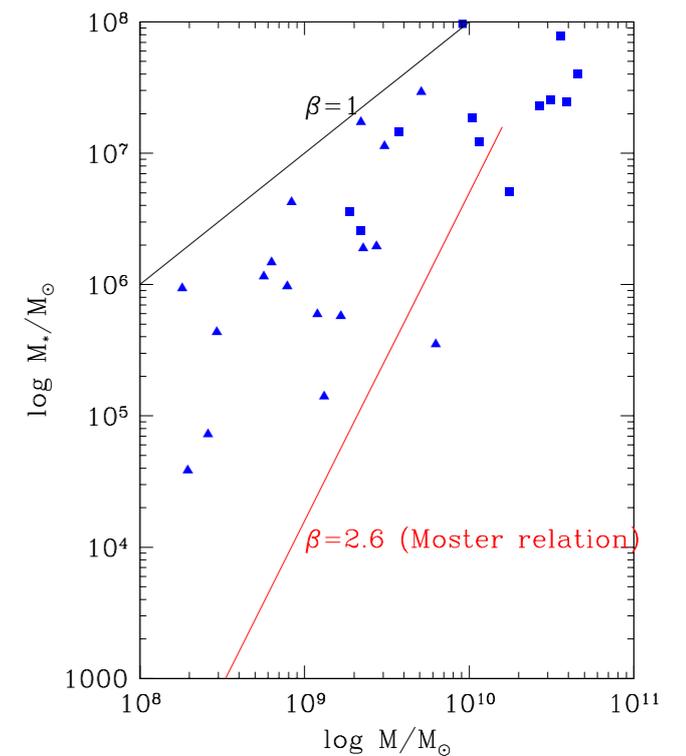


$\alpha(m_\chi=1 \text{ keV})=1.2$   
 $\alpha(m_\chi=1.5 \text{ keV})=1.4$   
 $\alpha(m_\chi=2 \text{ keV})=1.6$   
 $\alpha_{\text{CDM}}=1.8$

slope of  $N(L)$  is too flat in the  
 $m_\chi=1 \text{ keV}$  and  $m_\chi=1.5 \text{ keV}$   
 cases for any  $1 < \beta < 3$



CDM would require  $\beta \sim 2.5$   
 unfavoured by data



## Conclusions

WDM galaxy formation models provides a solution to several critical issues:

- density profiles (also at high- $z$ )
- abundance of low-mass/low-luminosity galaxies at  $z \gtrsim 2$
- luminosity function of AGNs (low-luminosity  $L < 10^{43}$  erg) at  $z \gtrsim 2$
- luminosity function of satellites (large surveys)
- $M^*-M_h$  relation
- Satellite colors (i.e., star formation histories of low-mass galaxies)

Constraints on WDM particle mass

- From MW satellites (but subject to halo-to-halo variance)
- From galaxy luminosity functions/counts
  - a) high-redshift (but present observations still not deep enough: constrain  $m_\chi > 1$  keV)
  - b) lower redshift, ultra-deep (down to  $M_{UV} \approx -10$ )  
UV luminosity function  $m_\chi > 1.5$  keV

## Summary

The mass of DM particles has a major impact on galaxy formation (suppression of small-scale perturbations due to free-streaming)  
CDM is the limit of  $M_{fs} \ll$  masses of cosmological interest

CDM problems on small scales:

- cusps + number of satellite galaxies
- abundance of low-mass (faint) galaxies at low and high redshifts
- fraction of quiescent satellites
- $V_{max}$ - $M_*$  relation

Baryonic physics can hardly solve all the problems

Galaxy formation in WDM cosmology is a viable solution if the spectrum is like that corresponding to a thermal relic DM with  $m \approx 2$  keV (analogous to that corresponding to sterile neutrino produced according to Dodelson & Widrow with  $m_\nu < 8$  keV)

There is a tension with current limits from high- $z$  structure (Lyman- $\alpha$  forest)

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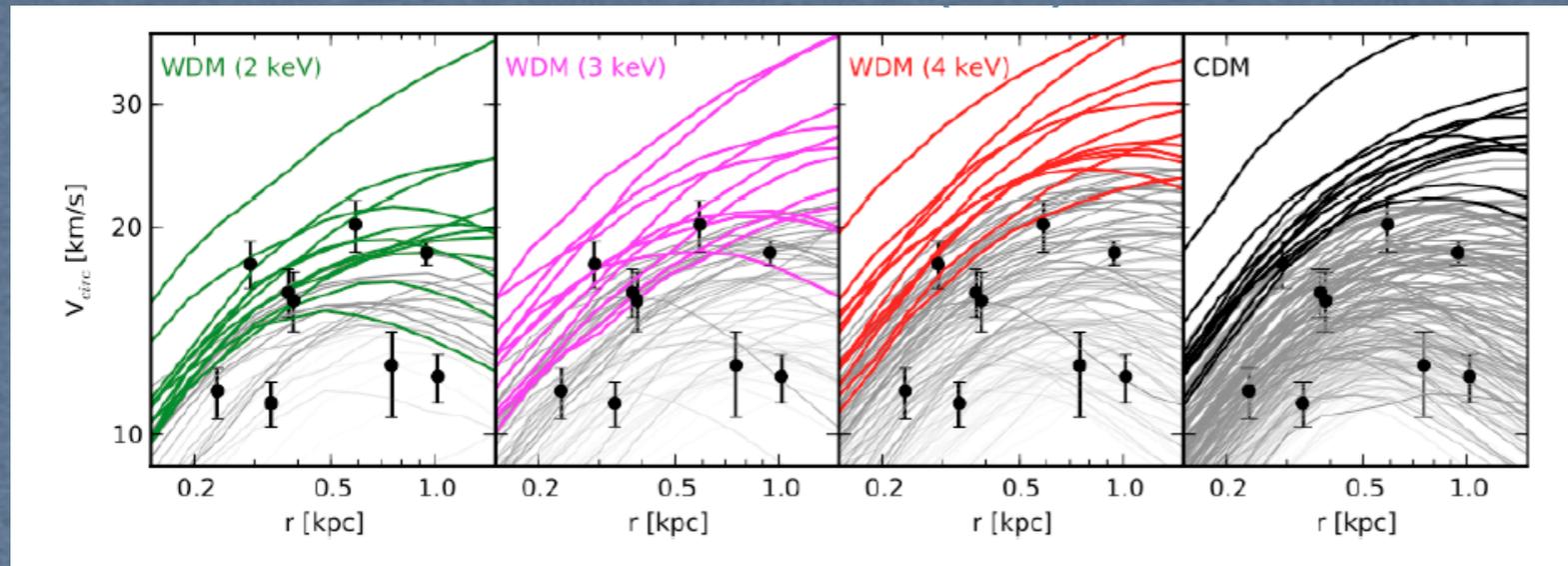
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Advance Access publication 2013 October 24

doi:10.1093/mnras/stt188

### MaGICC-WDM: the effects of warm dark matter in hydrodynamical simulations of disc galaxy formation

Jakob Herpich,<sup>1\*</sup> Gregory S. Stinson,<sup>1</sup> Andrea V. Macciò,<sup>1</sup> Chris Brook,<sup>2</sup>  
James Wadsley,<sup>3</sup> Hugh M. P. Couchman<sup>3</sup> and Tom Quinn<sup>4</sup>

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<sup>2</sup>Departamento de Física Teórica, Universidad Autónoma de Madrid, E-28049 Cantoblanco, Madrid, Spain  
<sup>3</sup>Department of Physics and Astronomy, McMaster University, Hamilton, Ontario L8S 4M1, Canada  
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Accepted 2013 October 2. Received 2013 September 20; in original form 2013 August 5

**ABSTRACT**  
We study the effect of warm dark matter (WDM) on hydrodynamic simulations of galaxy formation as part of the Making Galaxies in a Cosmological Context (MaGICC) project. We simulate three different galaxies using three WDM candidates of 1, 2 and 5 keV and compare results with pure cold dark matter simulations. WDM slightly reduces star formation and produces less centrally concentrated stellar profiles. These effects are most evident for the 1 keV candidate but almost disappear for  $m_{\text{WDM}} > 2$  keV. All simulations form similar stellar

with  $m \approx 2$  keV  
according to

(n-a forest)

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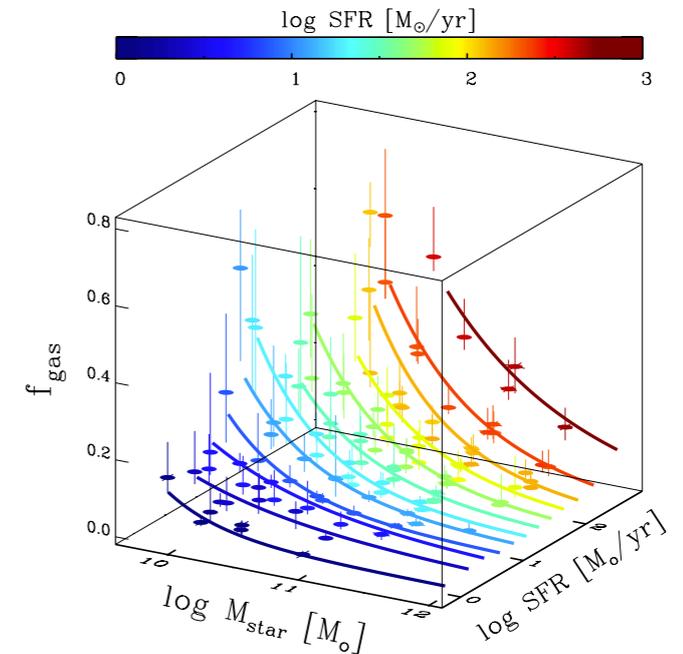
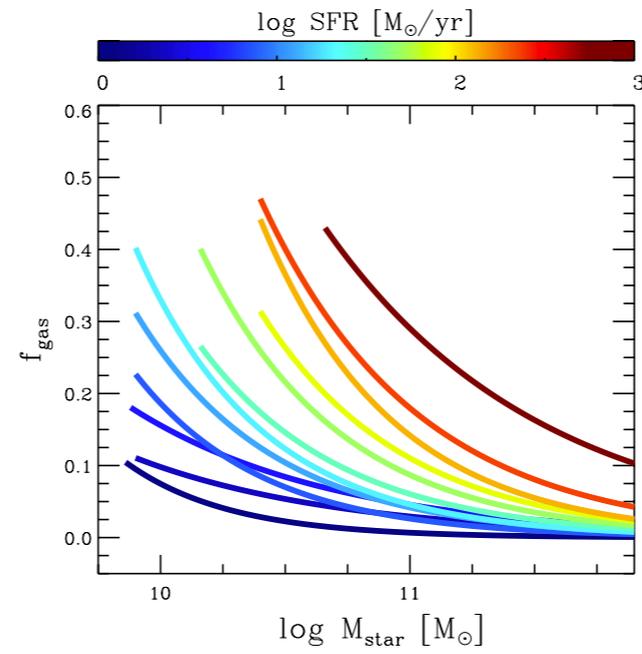
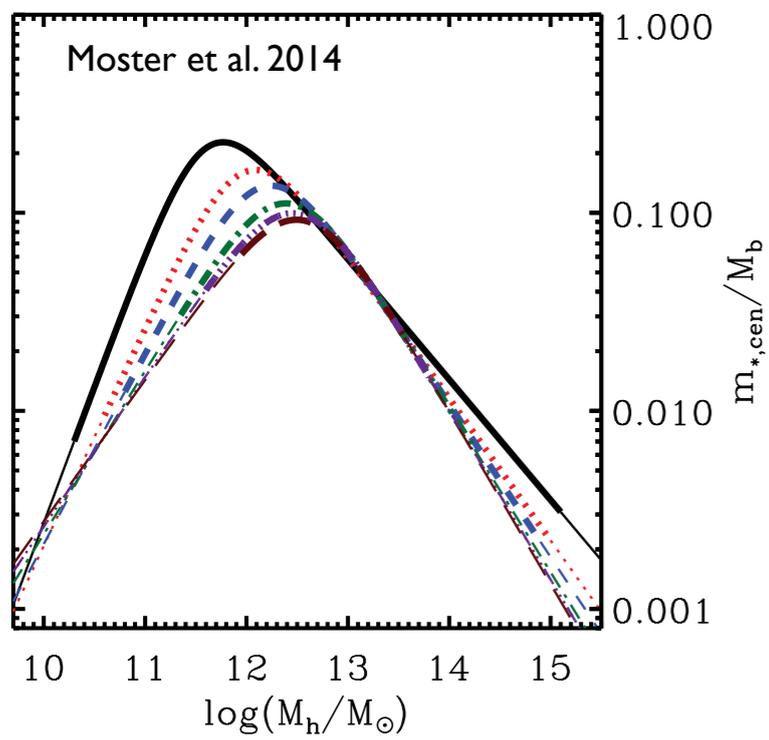
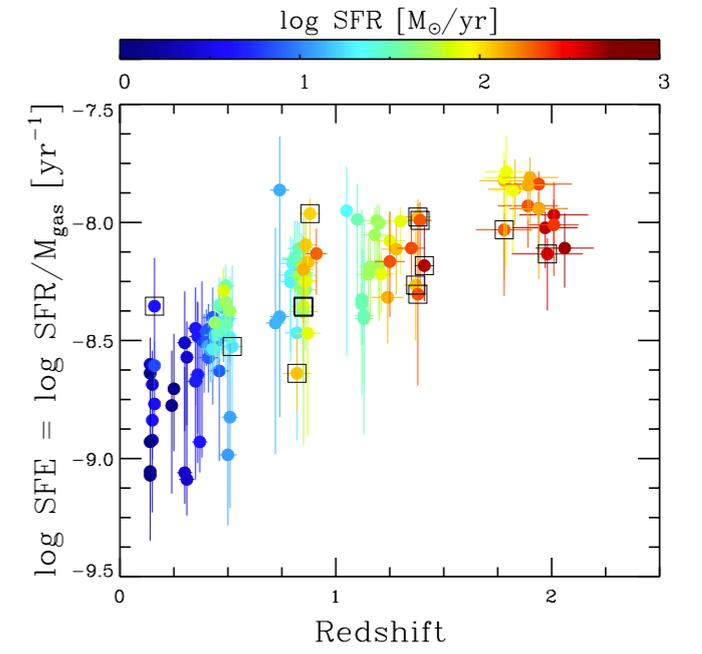
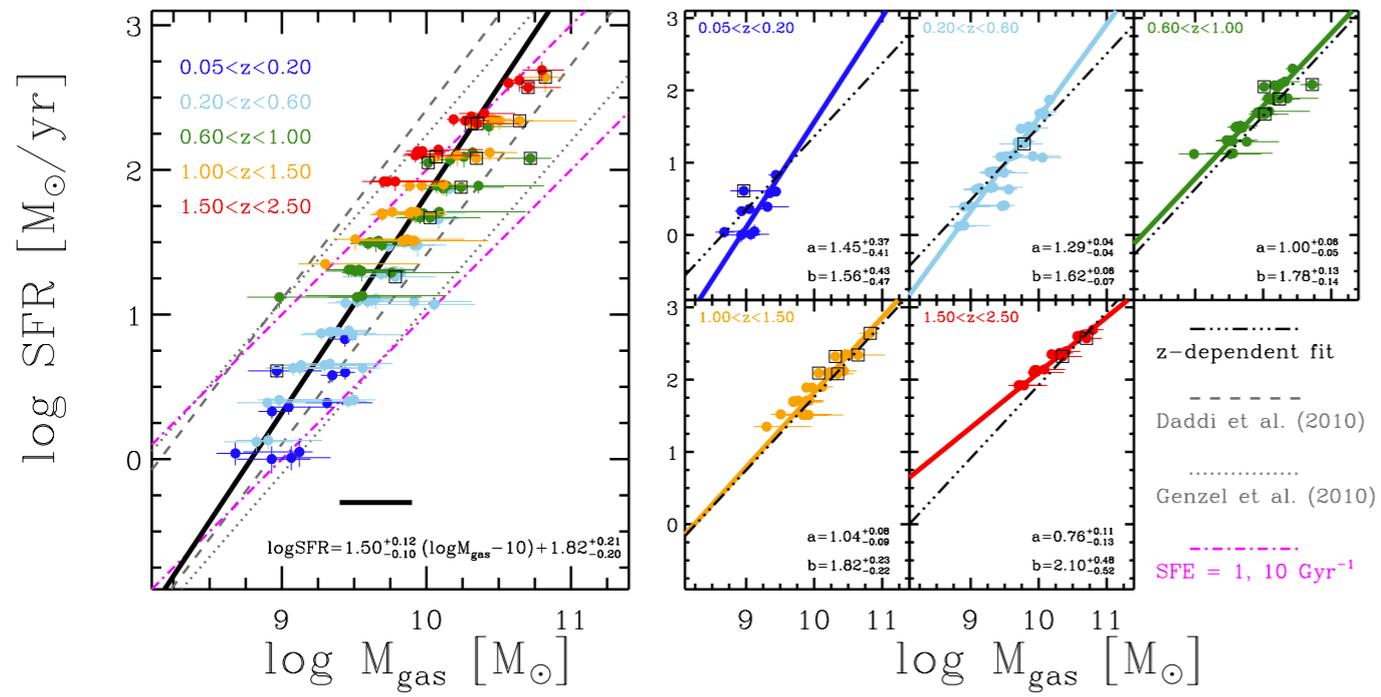
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# WDM particle mass: limits from the Ly- $\alpha$ forest

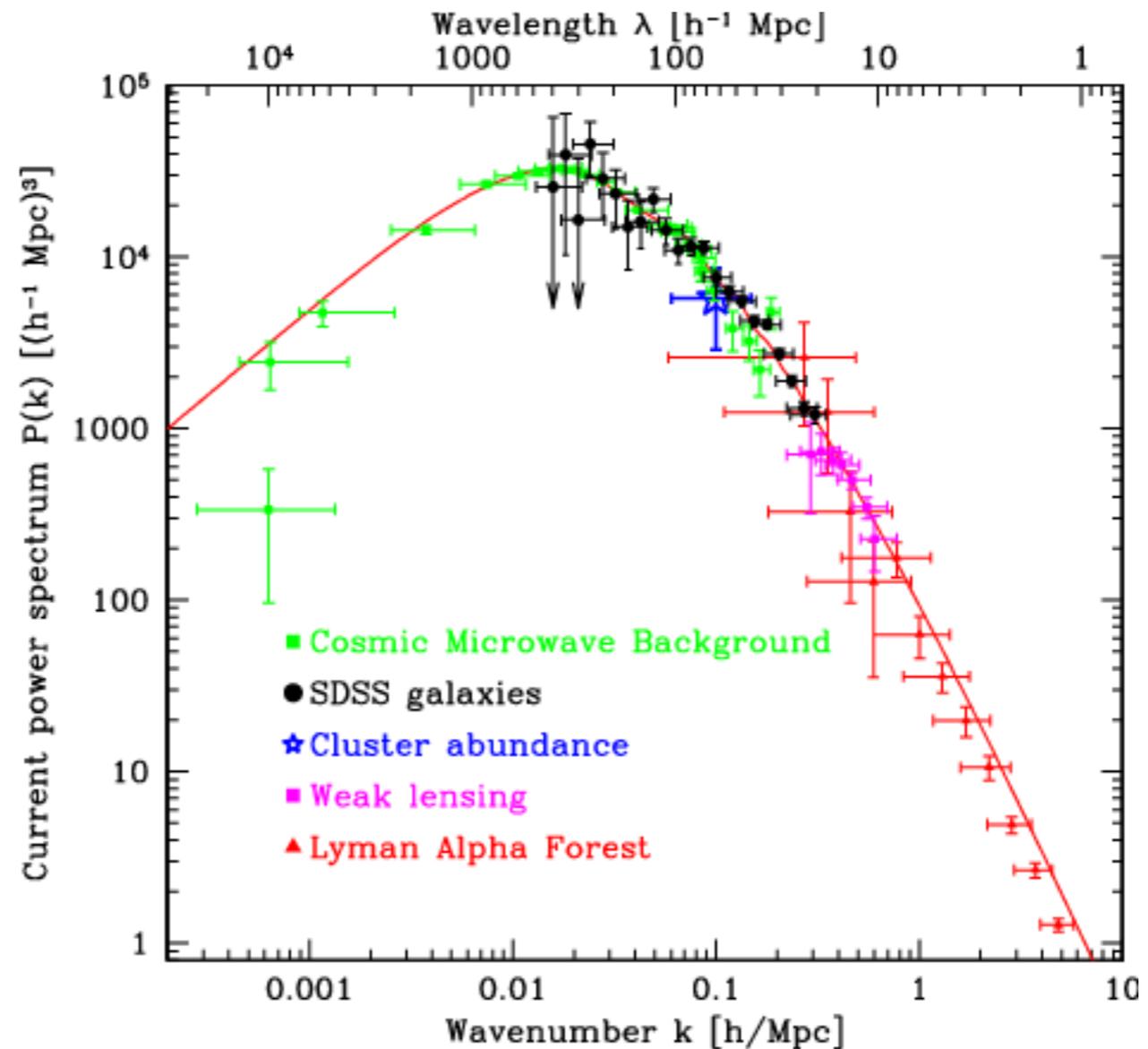
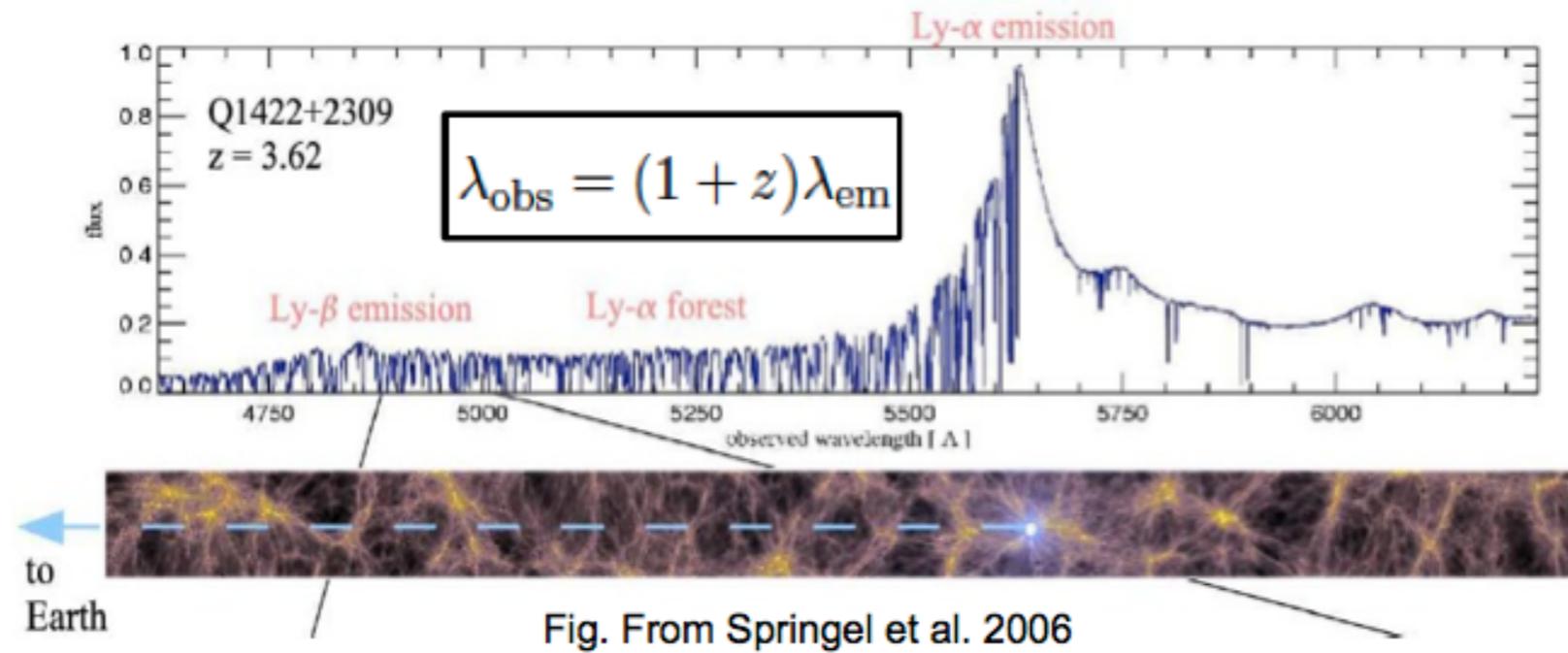
Viel et al. 2005-2013

$m_{\text{WDM}} > 3.5 \text{ keV}$  Thermal relics WDM  
 $m_{\nu} > 12 \text{ keV}$  Sterile  $\nu$  WDM (DW) Dodelson-Widrow

Results subject to further investigations

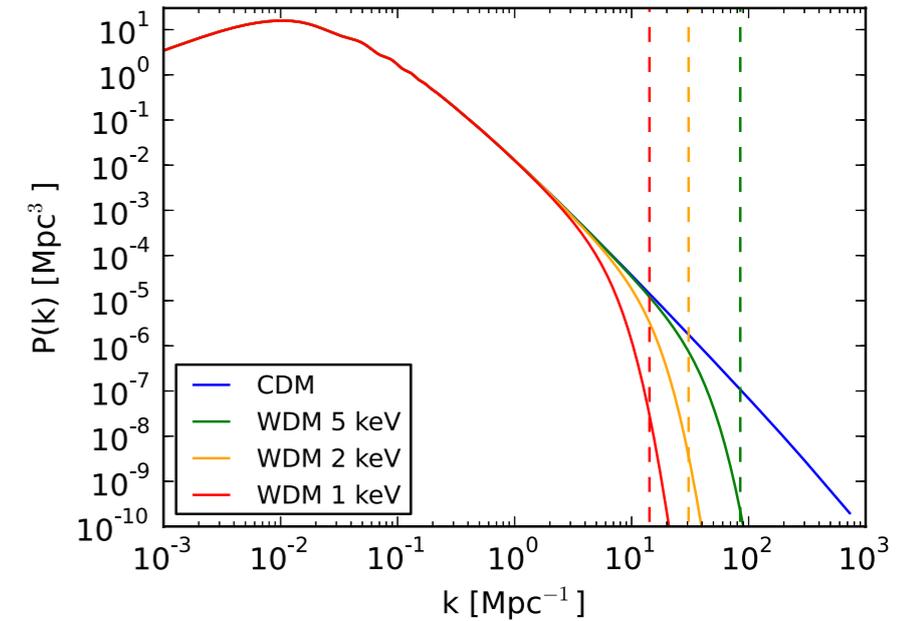
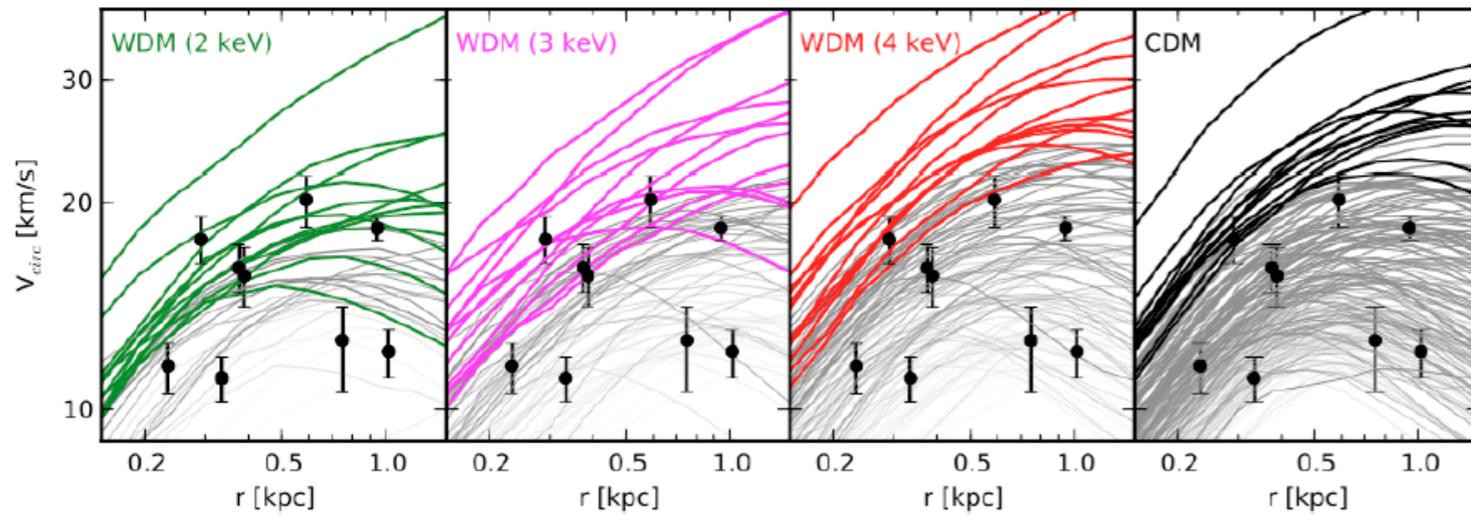
Still affected by the difficult-to-characterize non-linear growth of baryonic and DM structures (Watson et al. 2012) and uncertainties in the WDM simulations themselves.

WDM particles are  $10^{68}$  times heavier ( $10^5 M_{\odot}$ ) than the real WDM particles. This makes difficult to infer the initial velocity distribution of the effective particles from the known initial velocity distribution of the real WDM particles (Lovell et al. 2012, 2014; Maccio' et al. 2012; Viel et al. 2013).



# Mass should be $m \sim 2$ keV (thermal relics)

Schneider et al. 2013



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# Constraints from X-ray emission from clusters and galaxies

if  $m_s > m_\alpha$  the radiative decay  $\nu_s \rightarrow \nu_\alpha + \gamma$  becomes allowed

$$E_\gamma = \frac{1}{2} m_s \left( 1 - \frac{m_\alpha^2}{m_s^2} \right).$$

Emission lines in X-rays from DM concentrations:

- clusters (large signal but also large background)
- galaxies

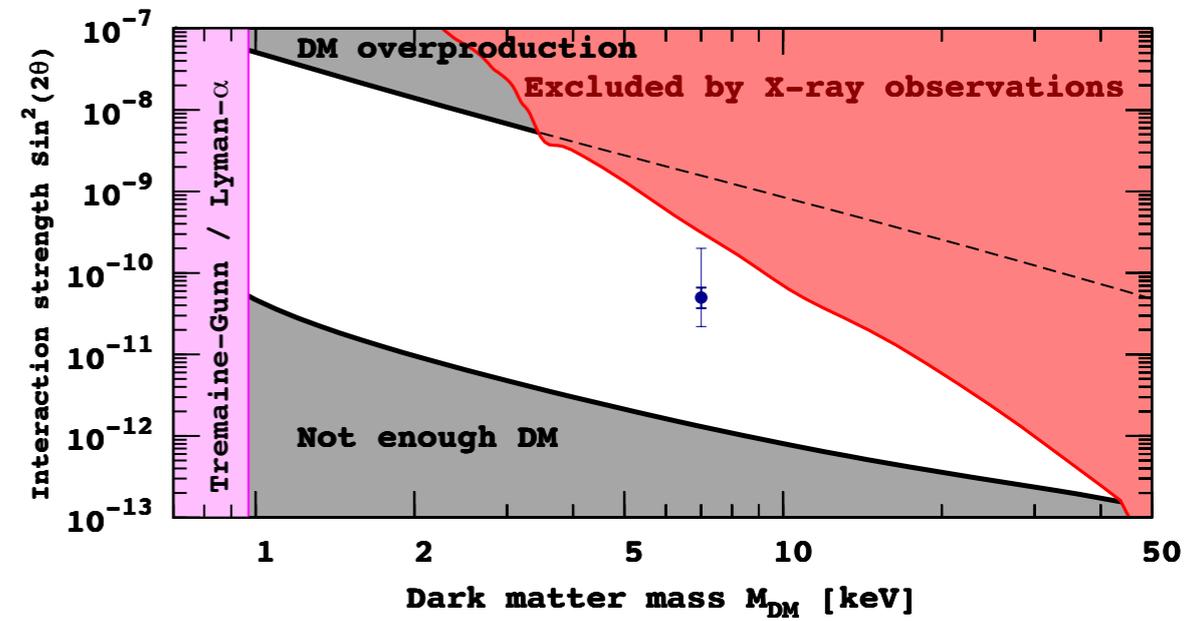
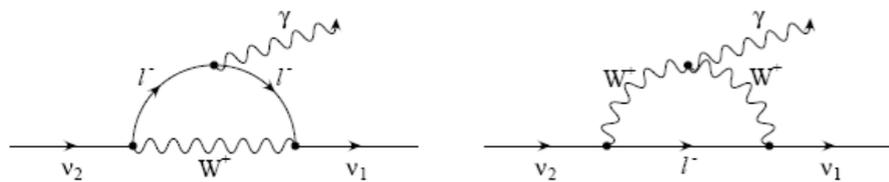
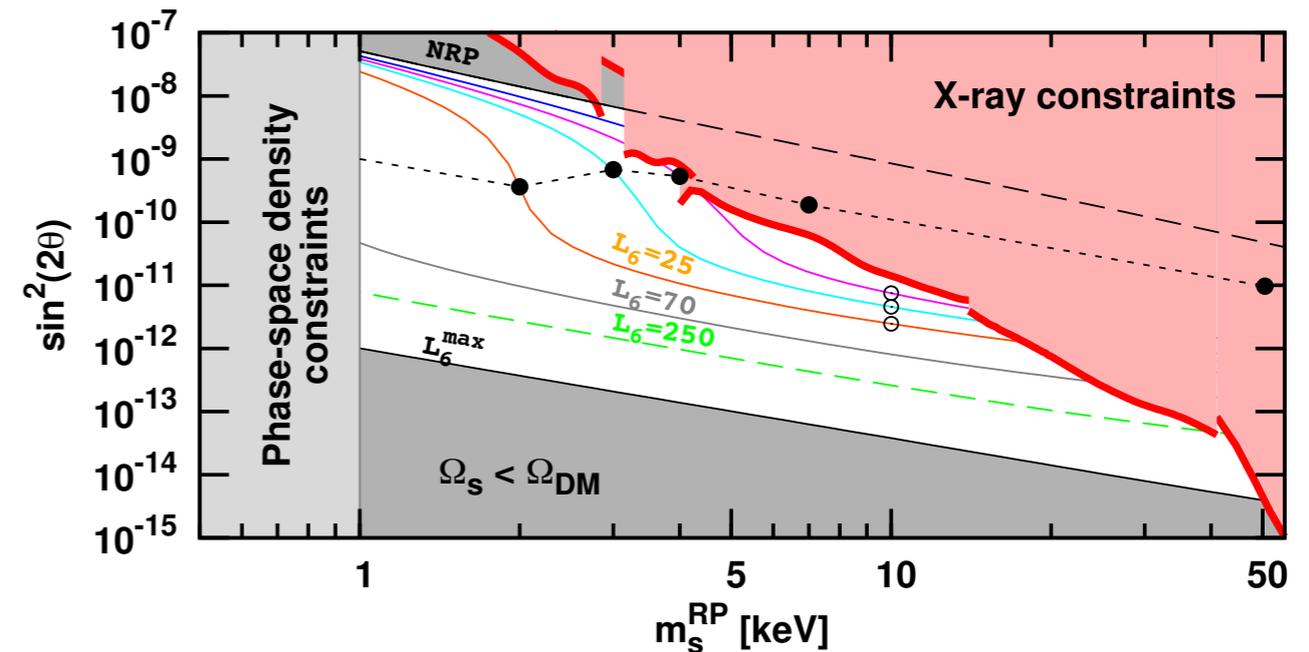


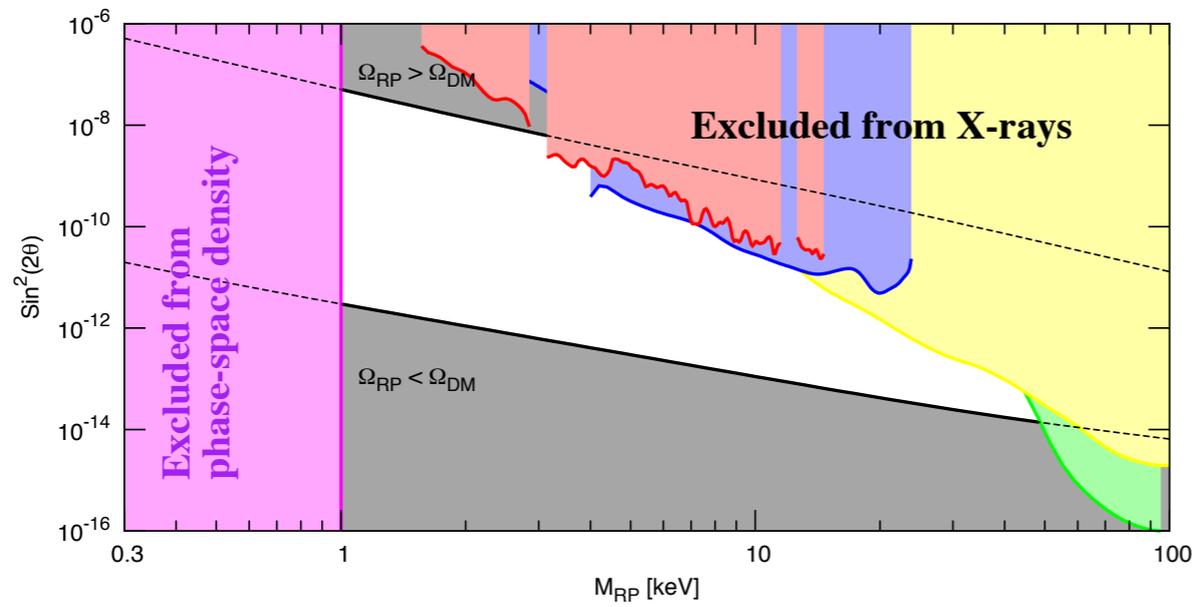
FIG. 4: Constraints on sterile neutrino DM within  $\nu$ MSM [4]. The blue point would correspond to the best-fit value from M31 if the line comes from DM decay. Thick errorbars are  $\pm 1\sigma$  limits on the flux. Thin errorbars correspond to the uncertainty in the DM distribution in the center of M31.

Boyarsky et al. 2014



Abazajian et al. 2001-2005





Window corresponds to resonant production  
 Upper boundary - zero lepton asymmetry  
 Lower boundary - maximal lepton asymmetry

Boyarsky et al 2009



## 6 – Sterile neutrino resonant production

In presence of a large lepton asymmetry,  $\mathcal{L} \equiv (n_\nu - n_{\bar{\nu}})/n_\gamma$ , matter effects become important and the mixing angle can be resonantly enhanced. [Shi,

Fuller, 1998; Abazajian et al., 2001

$$\sin^2 2\theta_m = \frac{\Delta^2(p) \sin^2 2\theta}{\Delta^2(p) \sin^2 2\theta + D^2 + (\Delta(p) \cos 2\theta - \frac{2\sqrt{2}\zeta(3)}{\pi^2} G_F T^3 \mathcal{L} + |V_T|)^2}$$

The mixing angle is maximal  $\sin^2 2\theta_m = 1$  when the **resonant condition** is satisfied (with  $\Delta(p) \equiv m_4^2/(2p)$ )

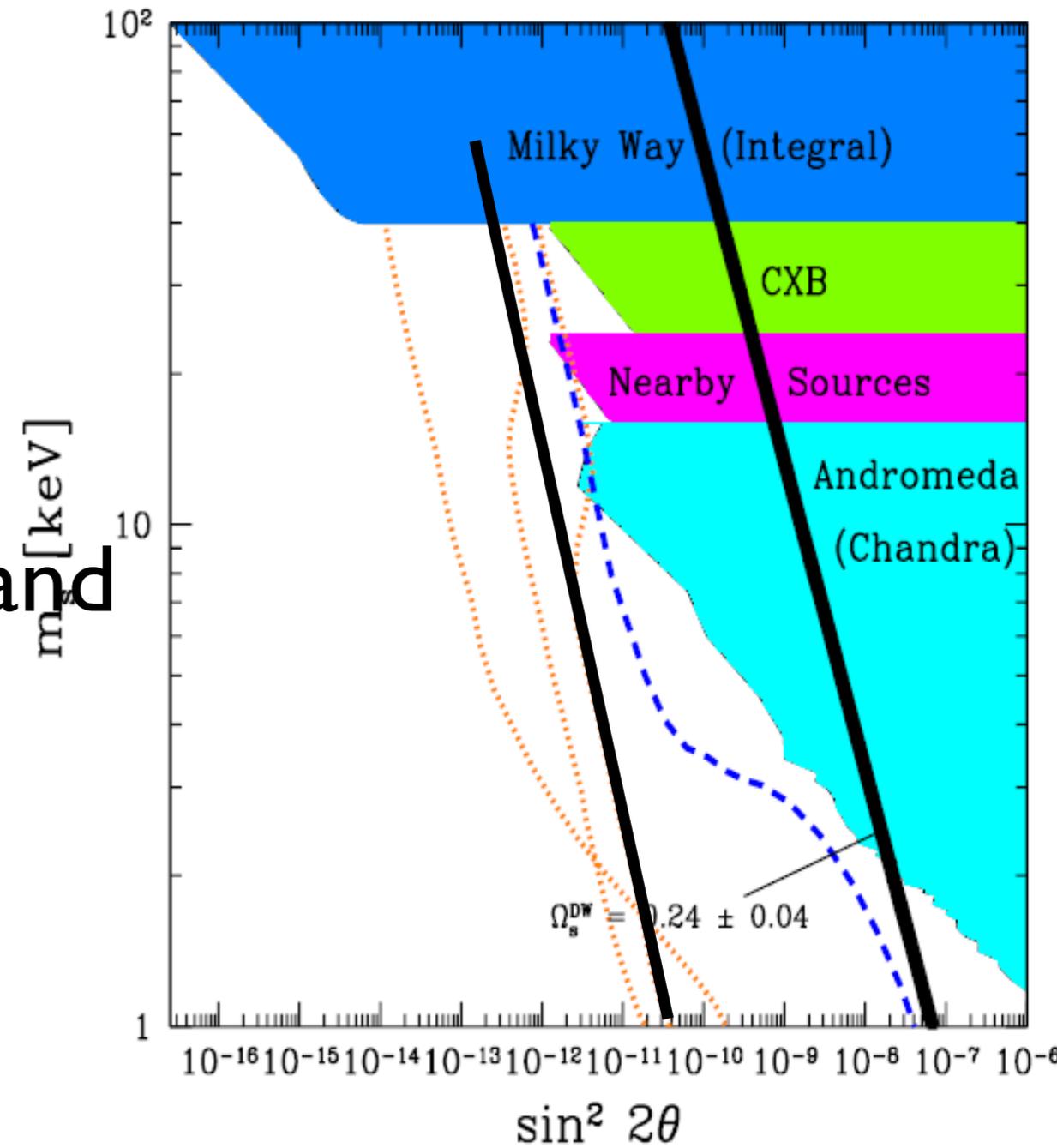
$$\Delta(p) \cos 2\theta - \frac{2\sqrt{2}\zeta(3)}{\pi^2} G_F T^3 \mathcal{L} + |V_T| = 0$$

$$\left(\frac{m_4}{1\text{keV}}\right)^2 \simeq 0.08 \frac{p}{T} \frac{\mathcal{L}}{10^{-4}} \left(\frac{T}{100\text{MeV}}\right)^4 + 2 \left(\frac{p}{T}\right)^2 \frac{B}{\text{keV}} \left(\frac{T}{100\text{MeV}}\right)^6$$

Sterile neutrinos are produced in primordial plasma through

- off-resonance oscillations. [Dodelson, Widrow; Abazajian, Fuller; Dolgov, Hansen; Asaka, Laine, Shaposhnikov et al.]
- oscillations on resonance, if the lepton asymmetry is non-negligible [Fuller, Shi]
- production mechanisms which do not involve oscillations
  - inflaton decays directly into sterile neutrinos [Shaposhnikov, Tkachev] – Higgs physics: both mass and production [AK, Petraki]

# Limits from the X-ray emission from clusters and galaxies



**Very small mixing** ( $\sin^2 2\theta \lesssim 10^{-7}$ ) **between**

**mass**  $|\nu_{1,2}\rangle$  **&**

**flavor**  $|\nu_{\alpha,s}\rangle$  **states:**

$$|\nu_\alpha\rangle = \cos\theta|\nu_1\rangle + \sin\theta|\nu_2\rangle$$

$$|\nu_s\rangle = -\sin\theta|\nu_1\rangle + \cos\theta|\nu_2\rangle$$

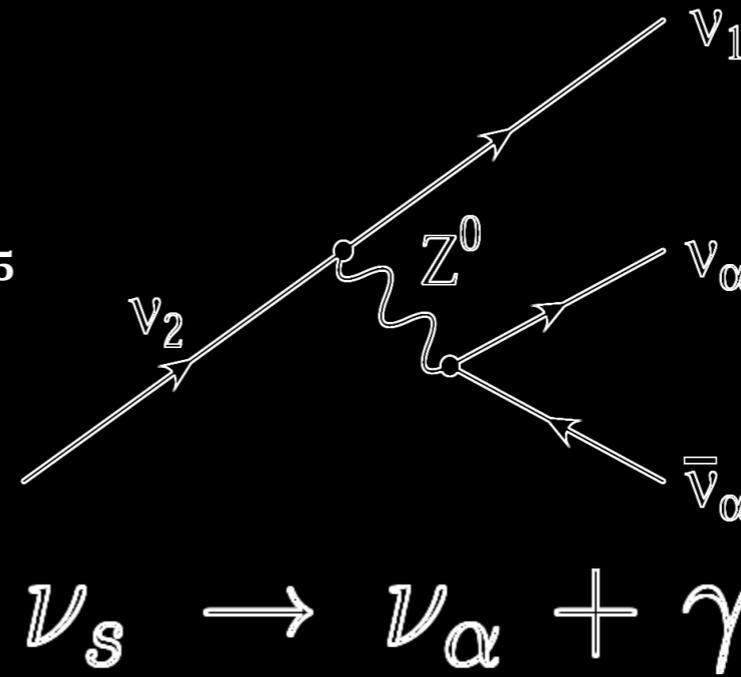
**For**  $m_s < m_e$ ,

**3ν Decay Mode Dominates:**

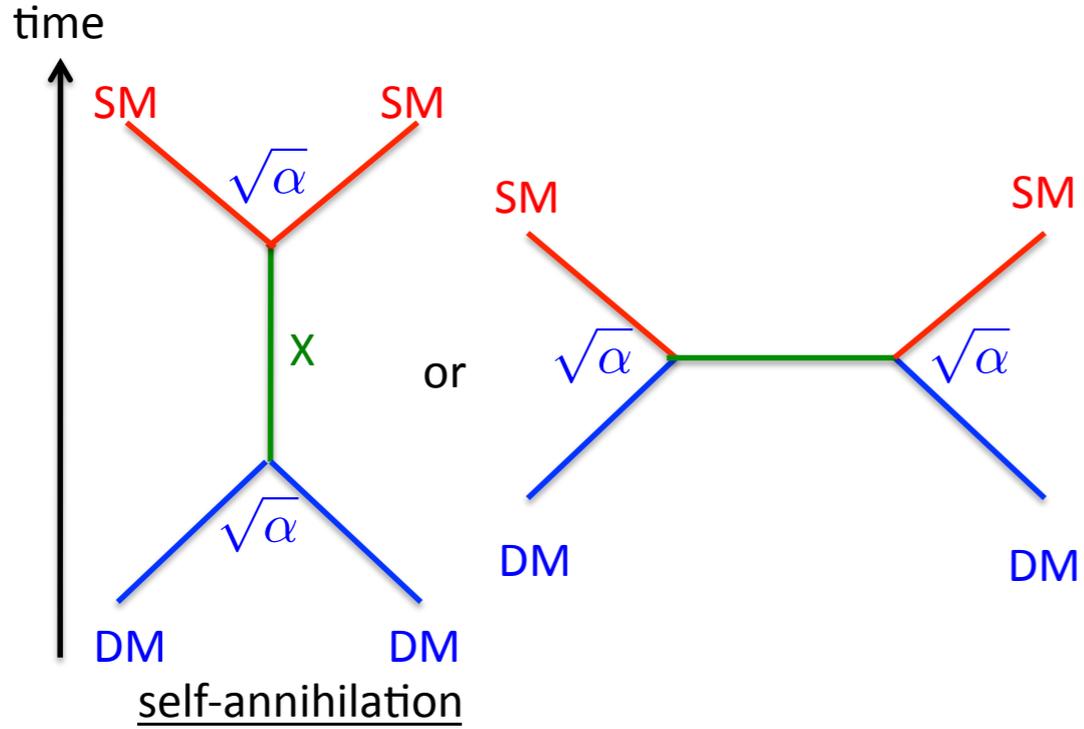
$$\Gamma_{3\nu} \simeq 1.74 \times 10^{-30} s^{-1} \left( \frac{\sin^2 2\theta}{10^{-10}} \right) \left( \frac{m_s}{\text{keV}} \right)^5$$

**Radiative Decay Rate is:**

$$\Gamma_s \simeq 1.36 \times 10^{-32} s^{-1} \left( \frac{\sin^2 2\theta}{10^{-10}} \right) \left( \frac{m_s}{\text{keV}} \right)^5$$



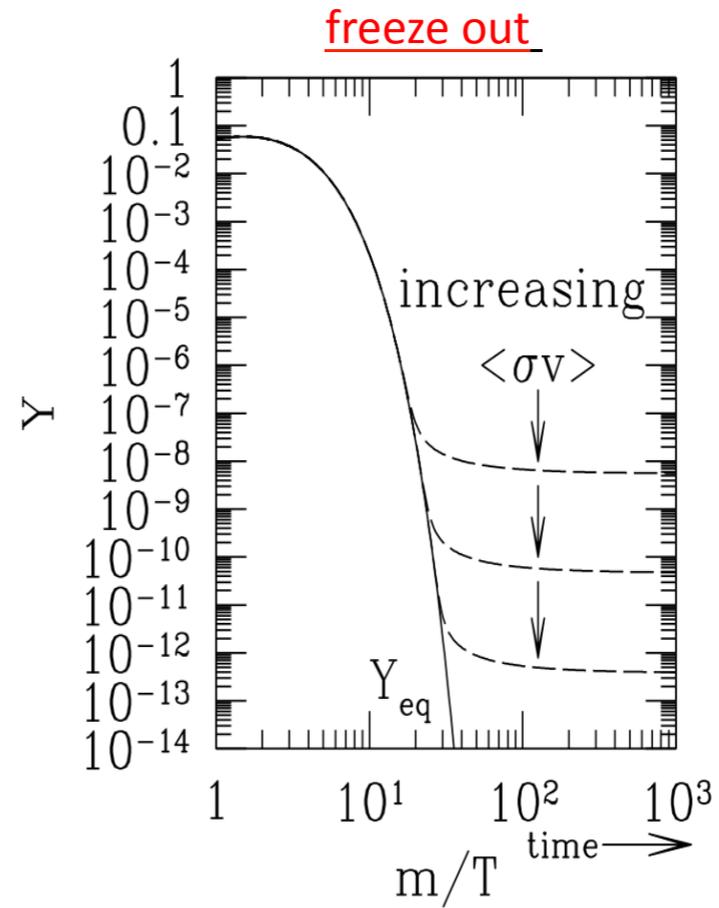
# WIMP



self-annihilation

$$\Omega h^2 \approx \frac{3 \times 10^{-27} \text{ cm}^3/\text{s}}{\langle \sigma_{\text{ann}} v \rangle}$$

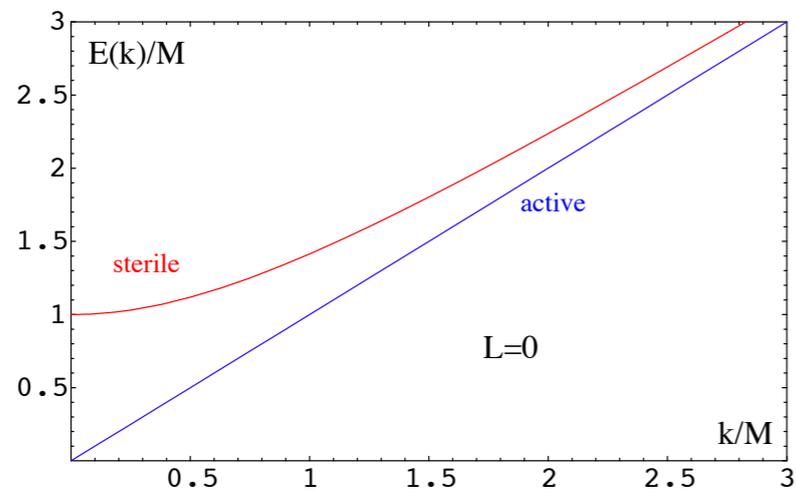
$$\langle \sigma_{\text{ann}} v \rangle \sim 10^{-25} \text{ cm}^3 \text{ s}^{-1} \left( \frac{\alpha}{10^{-2}} \right)^2 \left( \frac{100 \text{ GeV}}{m_{\text{X}}} \right)^2$$



Electro Weak Scale ( $\sim 100 \text{ GeV}$ ) WIMP naturally explains the relic abundance.

TeV scale SUSY & neutralino dark matter

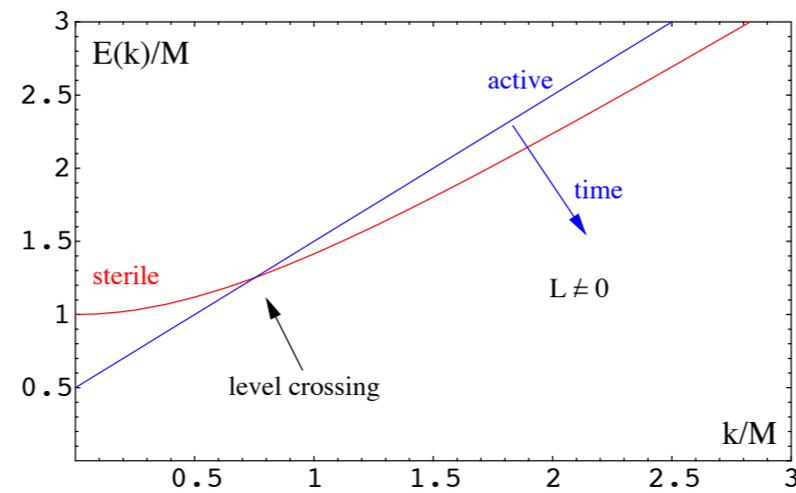
## Dispersional relations for active and sterile neutrinos (from real part)



Transitions  $\nu \rightarrow N_1$

Dodelson-Widrow

Zero lepton asymmetry



Resonant transitions

Shi-Fuller

Lepton asymmetry  
created in  $N_{2,3}$  decays

## Dark matter and the Lyman- $\alpha$ forest.

The bounds depend on the production mechanism.

$$\lambda_{FS} \approx 1 \text{ Mpc} \left( \frac{\text{keV}}{m_s} \right) \left( \frac{\langle p_s \rangle}{3.15 T} \right)_{T \approx 1 \text{ keV}}$$

The ratio

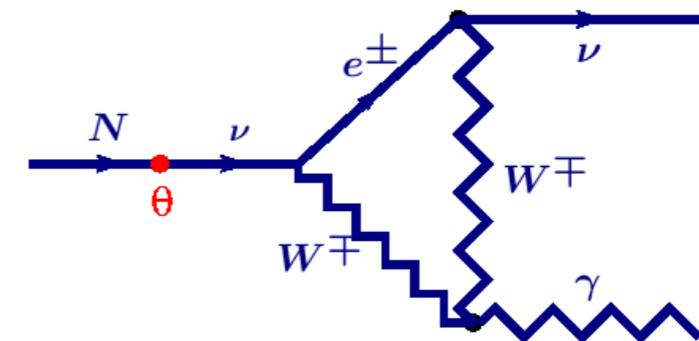
$$\left( \frac{\langle p_s \rangle}{3.15 T} \right)_{T \approx 1 \text{ keV}} = \begin{cases} 0.9 & \text{for production off - resonance} \\ 0.6 & \text{for MSW resonance (depends on } L) \\ 0.2 & \text{for production at } T > 100 \text{ GeV} \end{cases}$$

- Photon energy:

$$E_\gamma = \frac{M_1}{2}$$

- Radiative decay width

$$\Gamma = \frac{9\alpha_{EM} G_F^2}{256\pi^4} \theta^2 M_1^5$$



Dark matter made of sterile neutrino is not completely dark

## Where to look for DM decay line?

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- Extragalactic diffuse X-ray background (XRB) Dolgov & Hansen, 2000; Abazajian et al., 2001  
Mapelli & Ferrara, 2005; **Boyarsky et al. 2005**

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- Clusters of galaxies Abazajian et al., 2001  
**Boyarsky et al. astro-ph/0603368**

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- DM halo of the Milky Way.  
Signal increases as we increase FoV! **Boyarsky et al. astro-ph/0603660**  
Riemer-Sørense et al. astro-ph/0603661  
**Boyarsky, Nevalainen, O.R.** (in preparation)

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- Local Group galaxies **Boyarsky et al. astro-ph/0603660**  
Watson et al. astro-ph/0605424

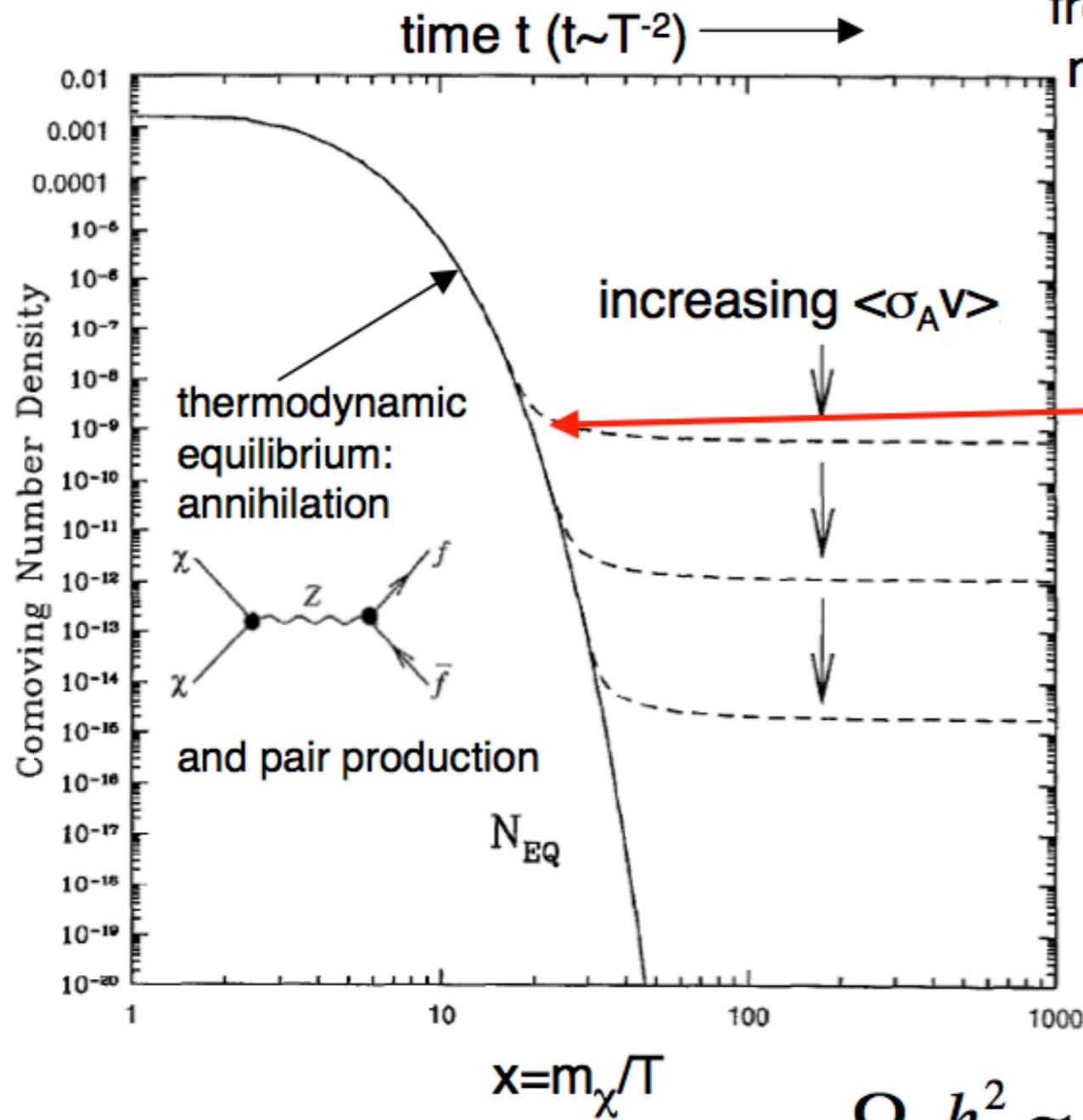
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- “Bullet” cluster 1E 0657-56 **Boyarsky, Markevitch, O.R.** (in preparation)

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- Cold nearby clusters **Boyarsky, Vikhlinin, O.R.** (in preparation)

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- Soft XRB **Boyarsky, Neronov, O.R.** (in preparation)

Need to find the best ratio between the DM decay *signal* and object's X-ray emission

# CDM as particle Dark Matter



freeze-out of a weakly interacting massive particle (WIMP  $\chi$ ) when reaction rate drops below expansion rate

$$T_{\text{freeze-out}} \sim 1/20 \times m(\text{WIMP})$$

**Cold Dark Matter:**  
 $\triangleright$  non-relativistic

“survival of the weakest”  
 At or below the weak scale

$$\Omega_\chi h^2 \approx \frac{m_\chi n_\chi}{\rho_c} \approx \frac{3 \times 10^{-27} \text{ cm}^3 / \text{sec}}{\langle\sigma_A v\rangle}$$