Neutrinos in the Early Universe

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Picture from Hubble ST



Outline

Introduction: the Cosmic Neutrino Background

Primordial Nucleosynthesis, neutrinos and radiation

Effect of neutrino masses on cosmological observables

Current cosmological bounds on neutrino masses

Future sensitivities











Neutrino cosmology is interesting because Relic neutrinos are very abundant:

- The CNB contributes to radiation at early times and to matter at late times (info on the number of neutrinos and their masses)
- Cosmological observables can be used to test non-standard neutrino properties

The Cosmic Neutrino Background

Neutrinos decoupled at T~MeV, keeping a $f_v(p,T) =$ spectrum as that of a relativistic species

• Number density

At present $112(v + \overline{v}) \text{ cm}^{-3}$ per flavour

• Energy density

Contribution to the energy density of the Universe

$$\Omega_{\nu} h^{2} = 1.7 \times 10^{-5}$$
Massless
$$\Omega_{\nu} h^{2} = \frac{\sum_{i} m_{i}}{93.2 \text{ eV}}$$
Massive
$$m_{\nu} > T$$



Relativistic particles in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\rho_{\rm r} = \rho_{\gamma} + \rho_{\nu} = \frac{\pi^2}{15} T_{\gamma}^4 + 3 \times \frac{7}{8} \times \frac{\pi^2}{15} T_{\nu}^4 = \left[1 + \frac{7}{8} \left(\frac{4}{11} \right)^{4/3} 3 \right] \rho_{\gamma}$$

$$\rho_{\rm r} = \rho_{\gamma} + \rho_{\nu} = \left[1 + \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} N_{\rm eff}\right] \rho_{\gamma}$$

Relativistic particles in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\rho_{\rm r} = \rho_{\gamma} + \rho_{\nu} + \rho_x = \left[1 + \frac{7}{8} \left(\frac{4}{11}\right)^{4/3} N_{\rm eff}\right] \rho_{\gamma}$$

Effective number of relativistic neutrino species Traditional parametrization of the energy density stored in relativistic particles # of flavour neutrinos: $N_{\nu} = 2.984 \pm 0.008$ (LEP data)

Constraints on N_{eff} from BBN and from CMB+LSS



Effect of neutrinos on BBN

1. N_{eff} fixes the expansion rate during BBN



2. Direct effect of electron neutrinos and antineutrinos on the n-p reactions

$$\nu_e + n \longleftrightarrow p + e^- \quad e^+ + n \longleftrightarrow p + \bar{\nu}_e$$

BBN: Predictions vs Observations



BBN: allowed ranges for N_{eff}



Future bounds on N_{eff}

Forecast analysis: Bowen et al, MNRAS 334 (2002) 760



 $\Delta N_{eff} \sim 3 (WMAP)$ $\Delta N_{eff} \sim 0.2 (Planck)$

Error Forecasts									
Experiment	$f_{\rm sky}$	θ_b	$w_T^{-1/2}$	$w_{P}^{-1/2}$	ΔN_{ν}	ΔN_{ν}	ΔN_{ν} (free Y)		
			[μ Κ']	[μ Κ']	TT	TT+TE+EE	TT+TE+EE		
Planck	0.8	7'	40	56	0.6	0.20	0.24		
ACT	0.01	1.7'	3	4	1	0.47	0.9		
ACT + Planck					0.4	0.18	0.24		
CMBPOL	0.8	4'	1	1.4	0.12	0.05	0.09		

Bashinsky & Seljak, PRD 69 (2004) 083002

Evolution of the background densities: 1 MeV \rightarrow now



Neutrinos as Dark Matter

Neutrinos are natural DM candidates

$$\Omega_{v}h^{2} = \frac{\sum_{i} m_{i}}{93.2 \text{ eV}} \quad \Omega_{v} < 1 \rightarrow \sum_{i} m_{i} < 46 \text{ eV}$$

$$\Omega_{v} < \Omega_{m} \approx 0.3 \rightarrow \sum_{i} m_{i} < 15 \text{ eV}$$

 First structures to be formed when Universe became matter -dominated are very large

Ruled out by structure formation CDM

Neutrinos as Hot Dark Matter

Massive Neutrinos can still be subdominant DM: limits on m_v from Structure Formation (combined with other cosmological data)



baryons and CDM (matter) experience gravitational clustering



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baryons and CDM (matter) experience gravitational clustering



growth of $\delta \rho / \rho$ (k,t) fixed by gravity vs expansion balance

 $\Rightarrow \delta
ho /
ho$ a a





neutrinos experience free-streaming with v = c or /m

baryons and CDM (matter) experience gravitational clustering



neutrinos cannot cluster below a diffusion length

 $\lambda = \int v dt < \int c dt$



for $(2\pi/k) < \lambda$, free-streaming supresses growth of structures during MD $\Rightarrow \delta \rho / \rho \propto a^{1-3/5 fv}$ with $f_v = \rho_v / \rho_m \approx (\Sigma m_v) / (15 eV)$

Power Spectrum of density fluctuations



Neutrinos as Hot Dark Matter: effect on P(k)

Massive Neutrinos can still be subdominant DM: limits on m_v from Structure Formation (combined with other cosmological data)

• Effect of Massive Neutrinos: suppression of Power at small scales



Effect of massive neutrinos on P(k)

Observable signature of the total mass on P(k):



Lesgourgues & SP, Phys. Rep. 429 (2006) 307

Cosmological observables: LSS



Cosmological observables : LSS



Cosmological observables: CMB



CMB temperature/polarization anisotropies \Rightarrow photon power spectra

Effect of massive neutrinos on the CMB spectra

- Direct effect of sub-eV massive neutrinos on the evolution of the baryon-photon coupling is very small
- 2) Impact on CMB spectra is indirect: non-zero Ω_v today implies a change in the spatial curvature or other Ω_i . The background evolution is modified





How to get a bound (measurement) of neutrino masses from Cosmology

Fiducial cosmological model: $(\Omega_b h^2, \Omega_m h^2, h, n_s, \tau, \Sigma m_v)$









Cosmological Data

• CMB Temperature: WMAP plus data from other experiments at large multipoles (CBI, ACBAR, VSA...)

- CMB Polarization: WMAP,...
- Large Scale Structure:

* Galaxy Clustering (2dF,SDSS)

* Bias (Galaxy, ...): Amplitude of the Matter P(k) $(SDSS,\sigma_8)$

* Lyman-a forest: independent measurement of power on small scales

* Baryon acoustic oscillations (SDSS)

Bounds on parameters from other data: SNIa ($\Omega_{\rm m}$), HST (h), ...

Cosmological Parameters: example

Parameter	Meaning	Status
τ	Reionization optical depth	Not optional
ω_b	Baryon density	Not optional
ω_d	Dark matter density	Not optional
f_{ν}	Dark matter neutrino fraction	Well motivated
Ω_{Λ}	Dark energy density	Not optional
w	Dark energy equation of state	Worth testing
Ω_k	Spatial curvature	Worth testing
A_{5}	Scalar fluctuation amplitude	Not optional
n_s	Scalar spectral index	Well motivated
α	Running of spectral index	Worth testing
r	Tensor-to-scalar ratio	Well motivated
n_t	Tensor spectral index	Well motivated
b	Galaxy bias factor	Not optional

SDSS Coll, PRD 69 (2004) 103501

Cosmological bounds on neutrino mass(es)

A unique cosmological bound on m_v DOES NOT exist!

Different analyses have found upper bounds on neutrino masses, since they depend on

- The combination of cosmological data used
- The assumed cosmological model: number of parameters (problem of parameter degeneracies)
- The properties of relic neutrinos

Cosmological bounds on neutrino masses using WMAP

Dependence on the data set used:

Cosmological data set	With WMAP3	Σ bound (2σ)
WMAP		< 2.3 eV
WMAP + SDSS		< 1.2 eV
$WMAP + SDSS + SN_{Riess} + HST$	$\Gamma + BBN$	$< 0.78 \ {\rm eV}$
$CMB + LSS + SN_{Astier}$		$< 0.75 \ {\rm eV}$
$CMB + LSS + SN_{Astier} + BAO$		$< 0.58 \ {\rm eV}$
$CMB + LSS + SN_{Astier} + Ly-\alpha$		$< 0.21 \ \mathrm{eV}$
$CMB + LSS + SN_{Astier} + BAO +$	- Ly- α	$< 0.17 \ {\rm eV}$

Fogli et al., PRD 75 (2007) 053001

Cosmological data set	With WMAP5	Σ (at 2σ)
CMB		< 1.19 eV
CMB + HST + SN-Ia		$< 0.75 \ \mathrm{eV}$
CMB + HST + SN-Ia + BAO		$< 0.60 \ \mathrm{eV}$
CMB + HST + SN-Ia + BAO + Ly α		$< 0.19 \ \mathrm{eV}$

Fogli et al., PRD 78 (2008) 033010

Neutrino masses in 3-neutrino schemes



Current cosmological bounds on neutrino masses

Dependence on the data set AND the cosmological model used.

Data	$m_{\nu} \ (95\% \text{ C.L.})$	Goobar et al	JCAP 06 (2006) 019
1: CMB, LSS, SNIa	$0.70 \mathrm{eV}$		
2: CMB, LSS, SNIa, BAO	$0.48 \ \mathrm{eV}$		
3: CMB, LSS, SNIa, Ly- α	$0.35 \ \mathrm{eV}$		
4: CMB, LSS, SNIa, BAO, Ly-	$\alpha = 0.27 \text{ eV}$		
Standard cosmological model+neu	ıtrino masses (8 par)		
	Data		$m_{\nu} \ (95\% \text{ C.L.})$
	1: CMB, LSS, SNIa	,	1.72 eV
	2: CMB, LSS, SNIa	, BAO	$0.62 \mathrm{eV}$
	3: CMB, LSS, SNIa	, Ly- α	$0.83 \ \mathrm{eV}$
	4: CMB, LSS, SNIa	, BAO, Ly- α	$0.49 \mathrm{eV}$
	SCM+neutrino mass	ses+N _{eff} +n _s +w _c	_{be} (11 par)









Future sensitivities to Σm_v

Future cosmological data will be available from

 CMB (Temperature & Polarization anis.)
 High-z Galaxy redshift surveys Hannestad & Wong, JCAP 07 (2007) 004
 Takada et al, PRD 73 (2006) 083520

- o Galaxy cluster surveys Wang et al, PRL 95 (2005) 011302
- Weak lensing surveys (tomography)
 Hannestad et al, JCAP 06 (2006) 025
 Song & Knox, PRD 70 (2004) 063510

o CMB lensing Perotto et al, JCAP 10 (2006) 013 Lesgourgues et al, PRD 73 (2006) 045021

Fluctuations in the 21 cm H line
 Loeb & Wyithe, PRL 100 (2008) 161301
 Pritchard & Pierpaoli, arXiv:0805.1920

Forecasts indicate 0.01-0.15 eV sensitivities to ∑m, are possible

PLANCK+SDSS

• Fisher matrix analysis: expected sensitivities assuming a fiducial cosmological model, for future experiments with known specifications

Fiducial cosmological model: $(\Omega_{b}h^{2}, \Omega_{m}h^{2}, h, n_{s}, \tau, \Sigma m_{v}) =$ $(0.0245, 0.148, 0.70, 0.98, 0.12, \Sigma m_{v})$ Σ m detectable at 2 σ if larger than

0.21 eV (PLANCK+SDSS) 0.13 eV (CMBpol+SDSS)

> Lesgourgues, SP & Perotto, PRD 70 (2004) 045016







No bias uncertainty Small scales much closer to linear regime Tomography: 3D reconstruction



Measure a large number of elliptically shaped galaxies



No bias uncertainty Small scales much closer to linear regime Tomography: 3D reconstruction sensitivity of future weak lensing survey (4000°)² to m_v

 $\sigma(m_v) \sim 0.1 \text{ eV}$

Abazajian & Dodelson PRL 91 (2003) 041301

lensing of the CMB signal



Makes CMB sensitive to smaller neutrino masses

sensitivity of CMB (primary + lensing) to m_v

 $\sigma(m_v) = 0.15 \text{ eV} (Planck)$ $\sigma(m_v) = 0.044 \text{ eV} (CMBpol)$

Kaplinghat, Knox & Song PRL 91 (2003) 241301

CMB lensing: recent forecast analysis

$\sigma(M_{v})$ in eV for future CMB experiments alone :

Lesgourgues et al, PRD 73 (2006) 045021

Free parameters:	meters: 8 parameters of minimal Λ MDM								
Lensing extraction:	no	no	yes	yes					
Foreground cleaning:	perfect	none	perfect	none					
QUaD+BICEP	1.3	1.6	0.31	0.36					
BRAIN+ClOVER	1.5	1.8	0.34	0.43					
Planck	0.45	0.49	0.13	0.14					
SAMPAN	0.34	0.40	0.10	0.17					
Planck+SAMPAN	0.32	0.36	0.08	0.10					
Inflation Probe	0.14	0.16	0.032	0.036					
Free parameters:		same –	- $\{\alpha, w, N_{\text{eff}}\}$						
Lensing extraction:	no	no	yes	yes					
Foreground cleaning:	perfect	none	perfect	none					
QUaD+BICEP	1.5	1.9	0.36	0.40					
BRAIN+ClOVER	1.7	2.0	0.42	0.51					
Planck	0.51	0.56	0.15	0.15					
SAMPAN	0.37	0.44	0.12	0.18					
Planck+SAMPAN	0.34	0.40	0.10	0.12					
Inflation Probe	0.25	0.26	0.035	0.039					

"Measuring" even m_v=0.05 eV ?

New cosmological observable as a potential probe of fluctuations at intermediate redshifts (6<z<20) \Rightarrow study of fluctuations in the 21cm line emitted by neutral H



Fig. 5.8. The origin of the hydrogen 21 cm line. The spins of the electron and the proton may be either parallel or opposite. The energy of the former state is slightly larger. The wavelength of a photon corresponding to a transition between these states is 21 cm

Karttunen et al. 2007

"Measuring" even m_v=0.05 eV ?

New cosmological observable as a potential probe of fluctuations at intermediate redshifts (6<z<20) \Rightarrow study of fluctuations in the 21cm line emitted by neutral H



Future sensitivities on Σm_v from 21cm observ.

		$\Omega_m h^2$	$\Omega_b h^2$	Ω_{Λ}	w	n_s	A_s^2	τ	Y_{He}	M_{ν}
	Fiducial	0.147	0.023	0.7	-1	0.95	26.6	0.1	0.24	0.3
	SDSS	0.456	0.083	0.117	1.21	0.503	∞	-	-	6.16
	G1	0.119	0.0207	0.0358	0.574	0.174	∞	-	-	1.28
	G_2	0.0354	0.00593	0.295	1.22	0.0482	∞	-	-	1.01
	G3	0.0252	0.00438	0.0076	0.122	0.037	∞	-	-	0.272
	MWA	0.0317	0.00761	0.972	3.13	0.0487	∞	-	-	0.749
	SKA	0.00191	0.00056	0.234	0.747	0.0054	∞	-	-	0.175
	\mathbf{FFTT}	4.94e-05	$4.77 \mathrm{e}{\text{-}} 05$	0.0045	0.014	0.0002	∞	-	-	0.009
	Planck	0.0045	0.00024	0.068	0.18	0.0074	0.26	0.0048	0.011	0.38
	+SDSS	0.0033	0.00024	0.023	0.11	0.0074	0.254	0.0046	0.0103	0.272
	+G1	0.0016	0.00021	0.013	0.081	0.0068	0.245	0.0044	0.01	0.136
Future	+G2	0.00089	0.00022	0.037	0.149	0.0067	0.243	0.0044	0.0099	0.104
Low-v radio telescopes	1-G3	0.00051	0.00016	0.003	0.021	0.0051	0.24	0.0043	0.0081	0.052
	+MWA	0.00146	0.00021	0.053	0.17	0.0066	0.242	0.0044	0.0101	0.144
	+SKA	0.00029	0.00014	0.020	0.065	0.003	0.236	0.0043	0.0044	0.080
	+FFTT	4.23e-05	3.97e-05	0.004	0.011	0.0002	0.23	0.0043	0.0030	0.0075
	$\operatorname{CosmicVar}$	0.00244	4.16e-05	0.030	0.033	0.0024	0.124	0.0023	0.0028	0.222
	+FFTT	3.3e-05	2.58e-05	0.0024	0.0076	0.0002	0.111	0.0021	0.0011	0.0068
										-

Pritchard & Pierpaoli, PRD 78 (2008) 065009

(also Loeb & Wyithe, PRL 100 (2008) 161301; Mao et al, PRD 78 (2008) 023529)

Summary of future sensitivities



Conclusions

Cosmological observables can be used to bound (or measure) neutrino properties, in particular the sum of neutrino masses (info complementary to laboratory results)

The radiation content of the Universe (N_{eff}) will be very constrained in the near future

Current bounds on the sum of neutrino masses from cosmological data (best Σm_v<0.2-0.4 eV, conservative Σm_v<1 eV)

Different cosmological observations in the next future Sub-eV sensitivity (0.1-0.2 eV and better) Test degenerate mass region and eventually the mimimum total mass for IH case