



# Testing LCDM on large and small scales

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## The emergence of a cosmological paradigm

⇒  $\Lambda$ CDM model

cosmological constant  
or dark energy

cold dark matter

The CDM model:

- What is it?
- How do we test it?

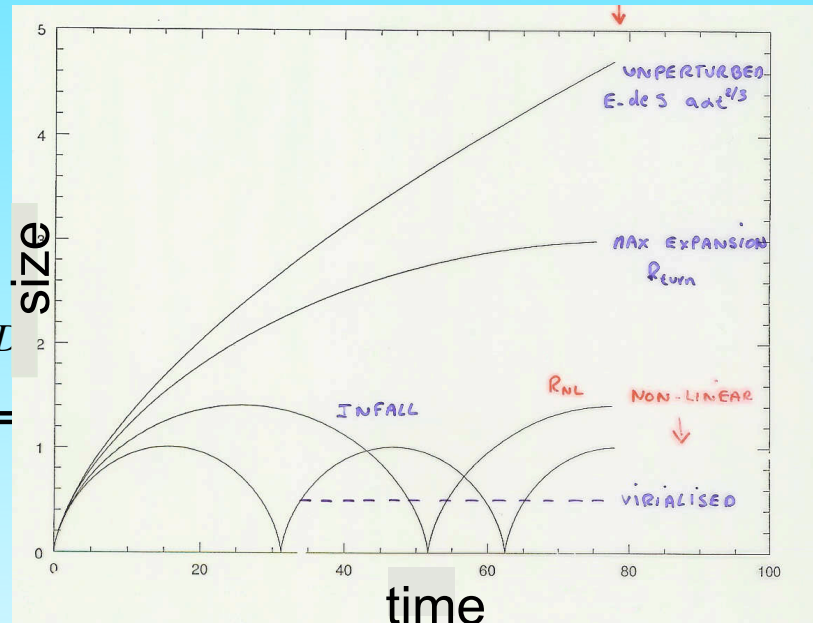
# The $\Lambda$ CDM model

- Material content: { Cold dark matter (eg neutralino; 21%), baryons (4%), dark energy ( $\Lambda$ ; 75%)
- Initial conditions for formation of structure: { Quantum fluctuations during inflation:  $|\delta_k|^2 \propto k^n$ ,  $n \approx 1$ ; Gaussian amplitudes

- Growth processes:

- Parameters:

$$\left\{ \begin{array}{l} \Omega_{CD} \\ h = \end{array} \right.$$



# The density & geometry of the Universe

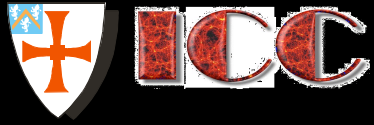
$$\Omega = \frac{\text{density}}{\text{critical density}}$$

$$\rho = \rho_{\text{rel}} + \rho_{\text{mass}} + \rho_{\text{vac}}$$

critical density = density that makes univ. flat:

$$\text{In } \Lambda\text{CDM: } \Omega_{\text{tot}} = \Omega_{\text{matter}} + \Omega_{\Lambda} + \Omega_{\text{radn}} = 1$$

consistent with the **flat universe** expected in **inflation**



# The cold dark matter cosmogony

The CDM model is an intrinsically implausible model, all the more so when the cosmological constant  $\Lambda$  is required.

Couldn't we have something simpler?



In particular, couldn't we just have

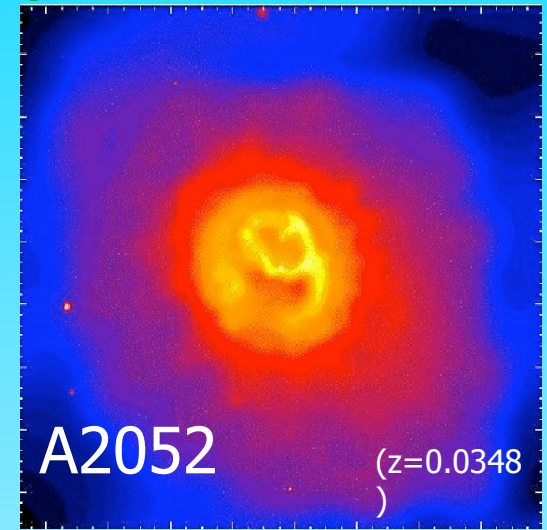
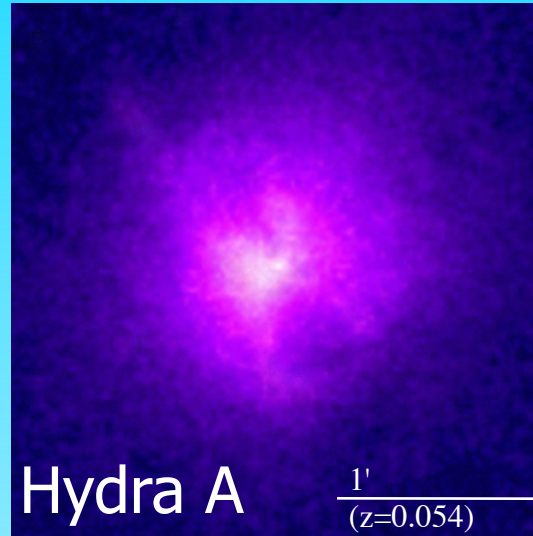
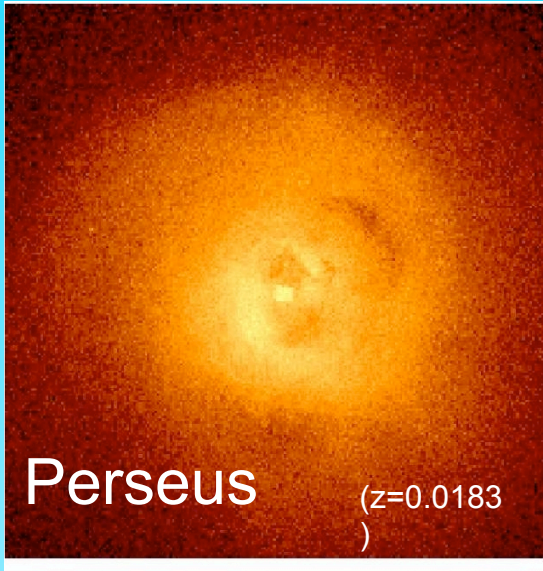
$$\Omega_{\text{matter}} = 1$$

Clusters give direct  
evidence for  $\Omega_{\text{matter}} < 1$

# Galaxy clusters

X-ray emission from hot plasma in clusters

Images from David Buote



About 90% of baryons in clusters are in hot gas

X-rays  $\Rightarrow$  gas mass

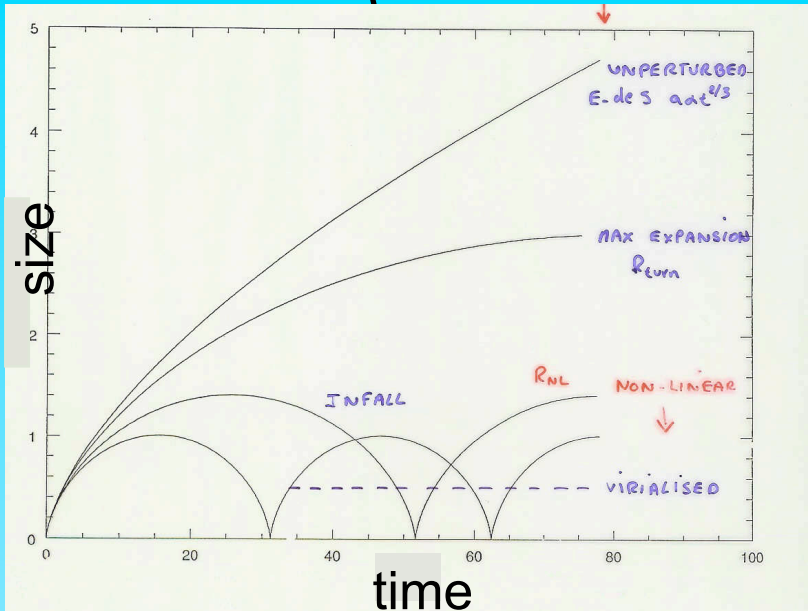
Photometry  $\Rightarrow$  stellar mass

Gas in hydrostatic equilibrium so X-rays

(or lensing)  $\Rightarrow$  total gravitating mass



# $\Omega$ from the baryon fraction in clusters



In clusters matter that has fallen in is still in the cluster ( $r_{\text{vir}} \sim r_{\text{non-linear}}$ )

⇒ baryon fraction in clusters  $\approx$  baryon fraction of universe

$$f_{\text{baryon}} = \frac{\text{mass in baryons}}{\text{total mass}}$$

$$M_b = M_{\text{gas}} + M_{\text{stars}}$$

$$f_b = \gamma \frac{\Omega_b}{\Omega}$$

White, Navarro,  
Evrard & Frenk '93

where  $\gamma=1$  if  $f_b$  has the universal value

Simulations ⇒  $\gamma=0.9$



The baryon fraction in clusters,  $f_b$ , is related to the universal baryon fraction by:

$$f_b = \frac{M_b}{M_{tot}} = \gamma \frac{\Omega_b}{\Omega_m}$$

White, Navarro,  
Evrard & Frenk '93

where  $\gamma=1$  if  $f_b$  has the universal value

simulations  $\rightarrow \gamma = 0.9 \pm 10\%$

X-rays+lensing  $\rightarrow f_b = (0.060h^{-3/2} + 0.009) \pm 10\%$

BBNS, CMB  $\rightarrow \Omega_b h^2 = 0.019 \pm 20\%$

HST  $\rightarrow h = 0.7 \pm 10\%$

$$\rightarrow \Omega_m = \frac{\Omega_b \gamma}{f_b} = 0.31 \pm 0.12$$

Allen etal '04

# $\Omega < 1$ : open or flat universe?

$\Omega_{\text{matter}} < 1 \Rightarrow \left\{ \begin{array}{l} \text{Open universe} \\ \text{Cosmological constant to give } \Omega_{\text{tot}}=1 \end{array} \right.$

White et al 1993



# **(Some) evidence for dark energy**

# Evidence for $\Lambda$ from high- $z$ supernovae

SN type Ia (standard candles) at  $z \sim 0.5$  are fainter than expected even if the Universe were empty

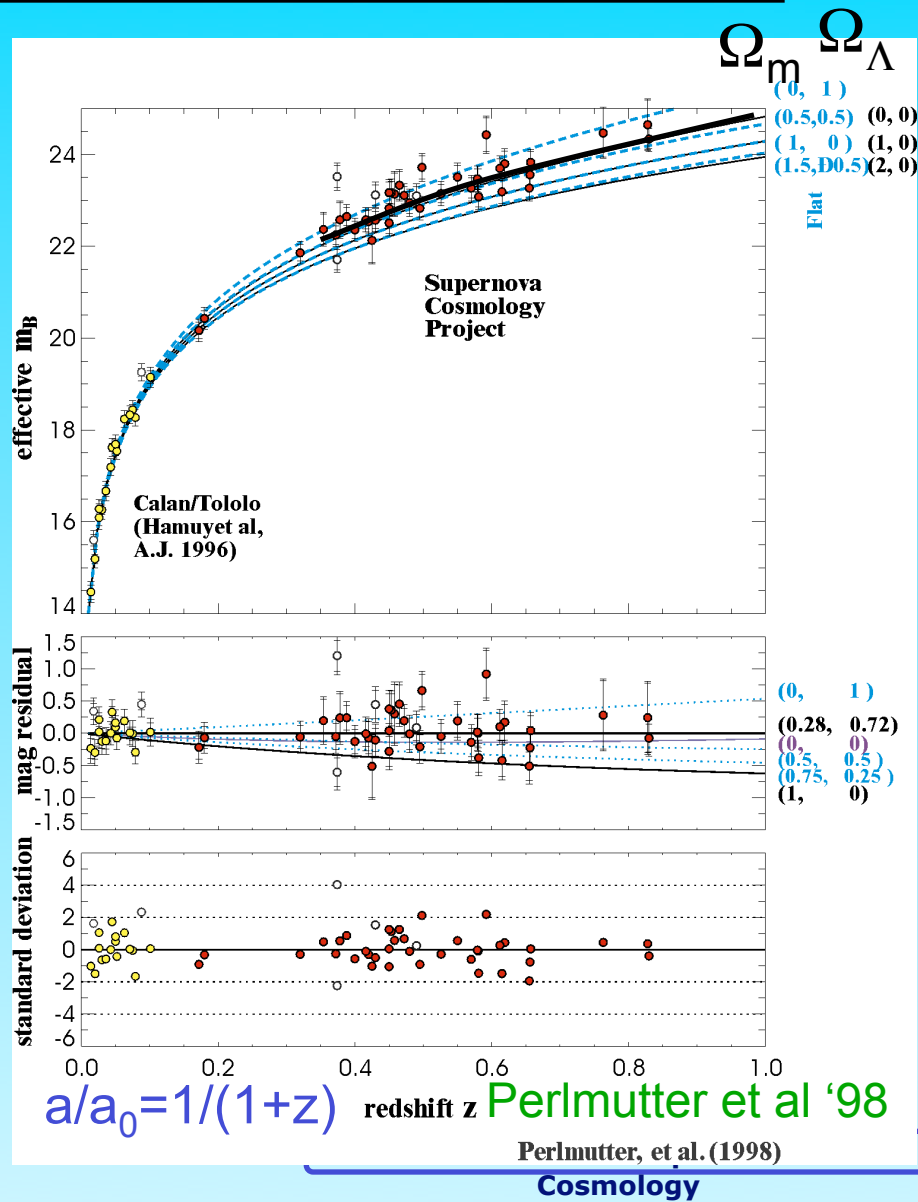
The cosmic expansion must have been accelerating since the light was emitted

$$\ddot{a} = -\frac{4\pi}{3} G \rho a (3w + 1)$$

where  $p = w\rho c^2$

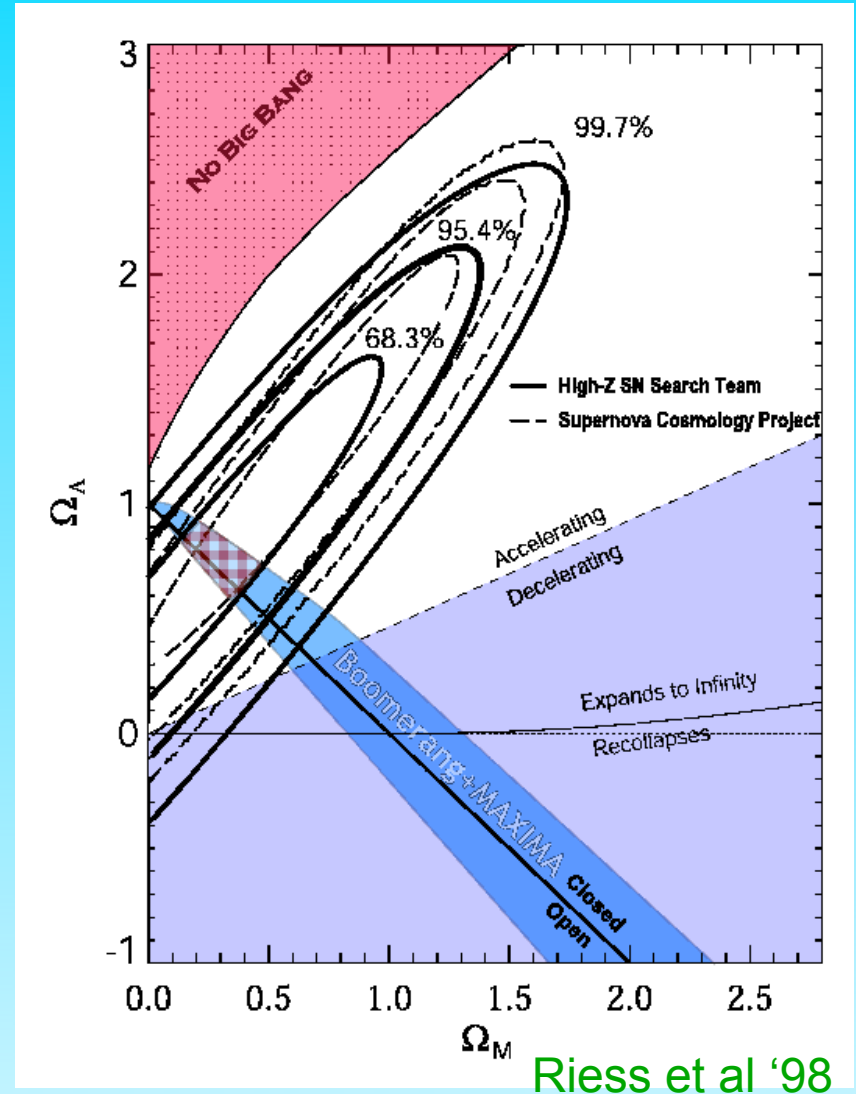
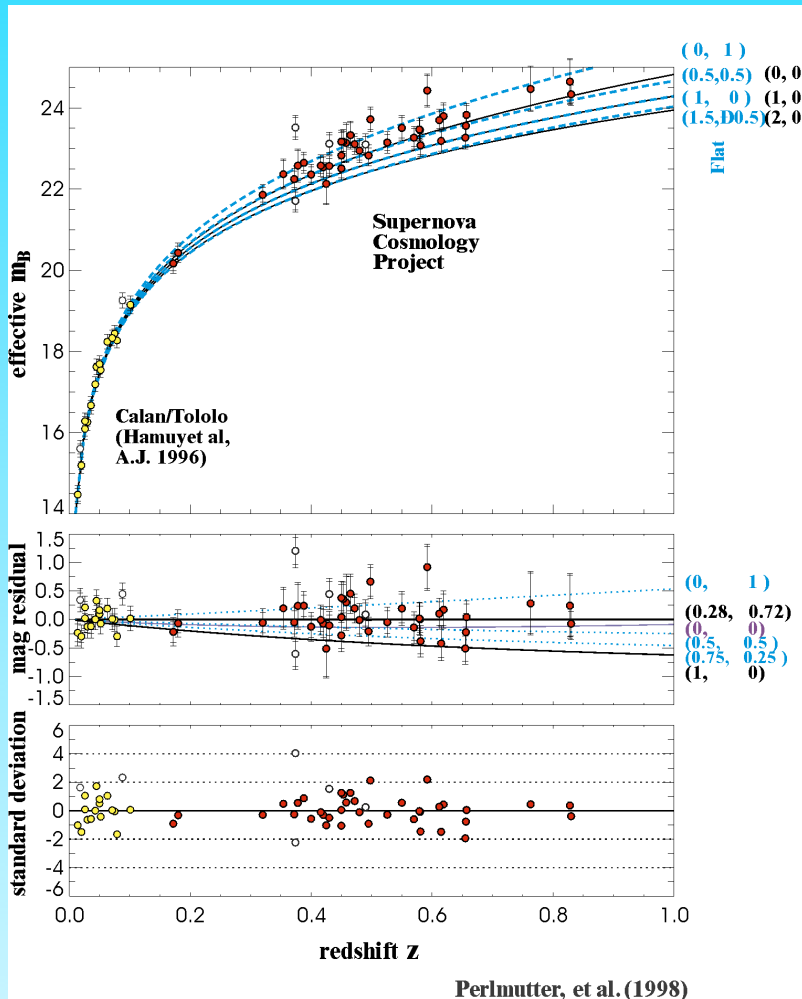
$$\rho_{\text{tot}} = \underbrace{\rho_{\text{mass}}}_{a^{-3}} + \underbrace{\rho_{\text{rel}}}_{a^{-4}} + \underbrace{\rho_{\text{vac}}}_{\text{const ?}}$$

flux ↓



# Evidence for $\Lambda$ from high-z supernovae

Distant SN are fainter than expected if expansion were decelerating



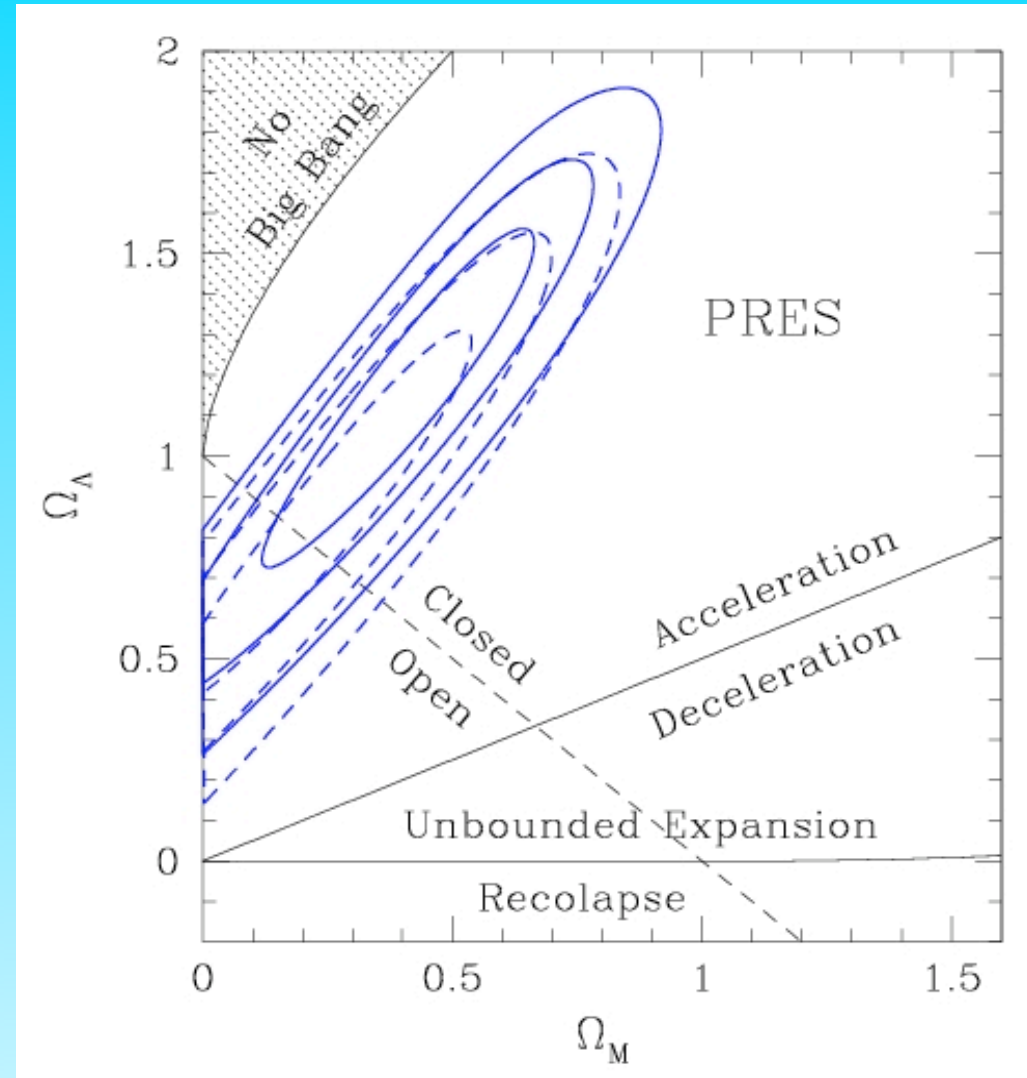
# Evidence for $\Lambda$ from high- $z$ supernovae

Latest data **rules out**  $\Omega_{\Lambda} = 0$ .

Main concerns:

- Physics of SNIa not understood
- Systematic errors?

Clocchiatti et al '06





# The cold dark matter cosmogony

So (implausibly), we seem to need  
dark energy

But why cold dark matter?

# Non-baryonic dark matter candidates

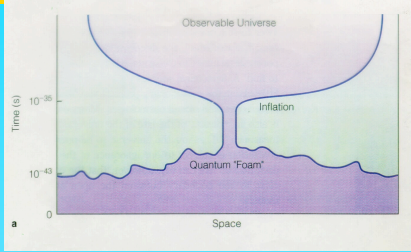
Type candidate mass

hot	neutrino	a few eV
warm	Sterile neutrino	keV-MeV
cold	axion neutralino	$10^{-5}$ eV->100 GeV



# The origin of cosmic structure

Inflation ( $t \sim 10^{-35}$  s)



→ QUANTUM FLUCTUATIONS:

$$\left\{ \begin{array}{l} |\delta_k|^2 \propto k^n \quad n \approx 1 \\ \text{Gaussian amplitudes} \end{array} \right.$$

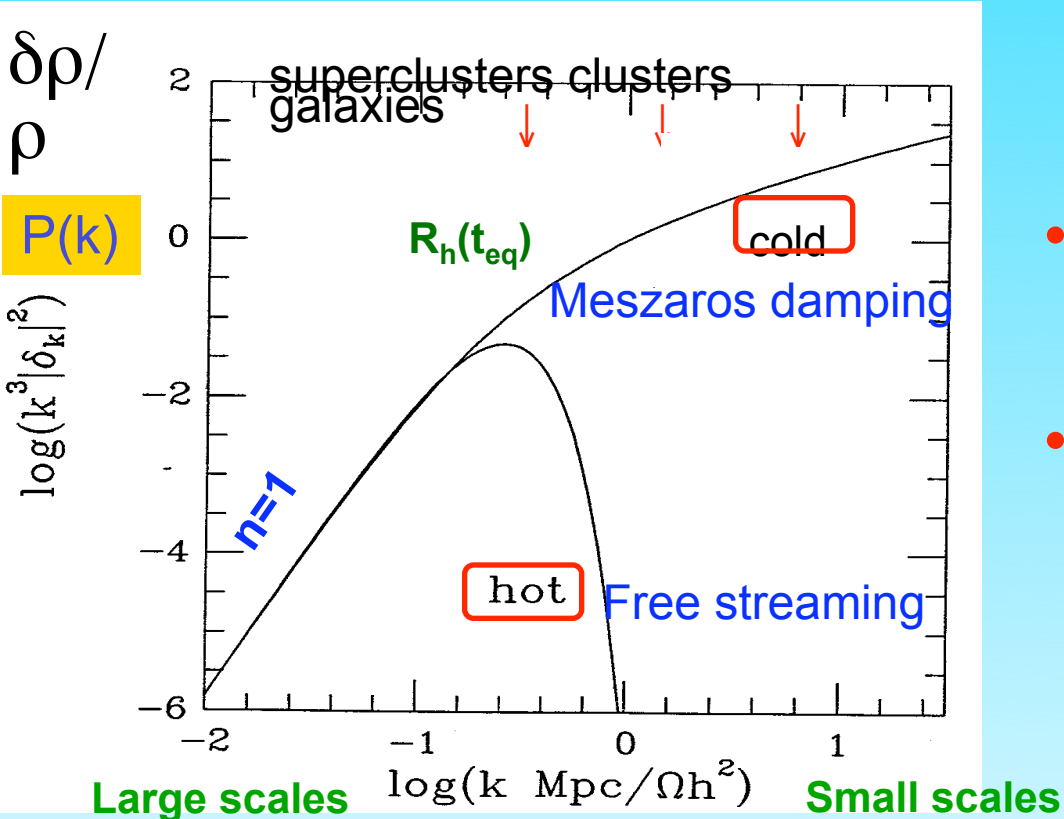
+

Damping (nature of dark matter)

→ FLAT UNIVERSE

$$P(k) = A k^n T^2(k, t)$$

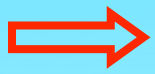
↳ Transfer function



- Hot DM (eg  $\sim 30$  eV neutrino)
  - Top-down formation
- Cold DM (eg  $\sim$  neutralino)
  - Bottom-up (hierarchical)

# Neutrino (hot) dark matter

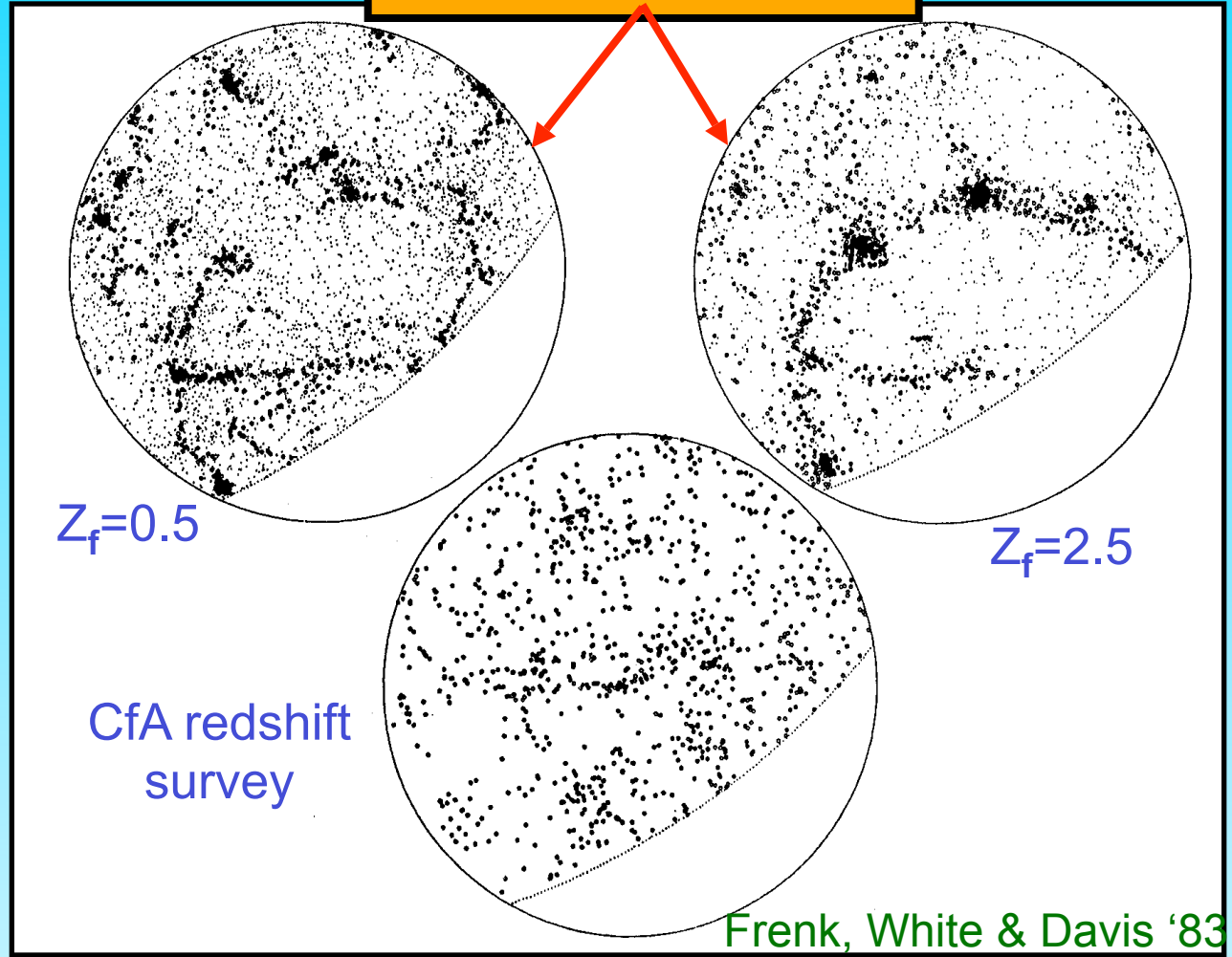
Free-streaming length so large that superclusters form first and galaxies are too young



Neutrinos cannot make an appreciable contribution to  $\Omega$  and

$$m_\nu \ll 10 \text{ eV}$$

$$\Omega_\nu = 1 \quad (m_\nu = 30 \text{ eV})$$



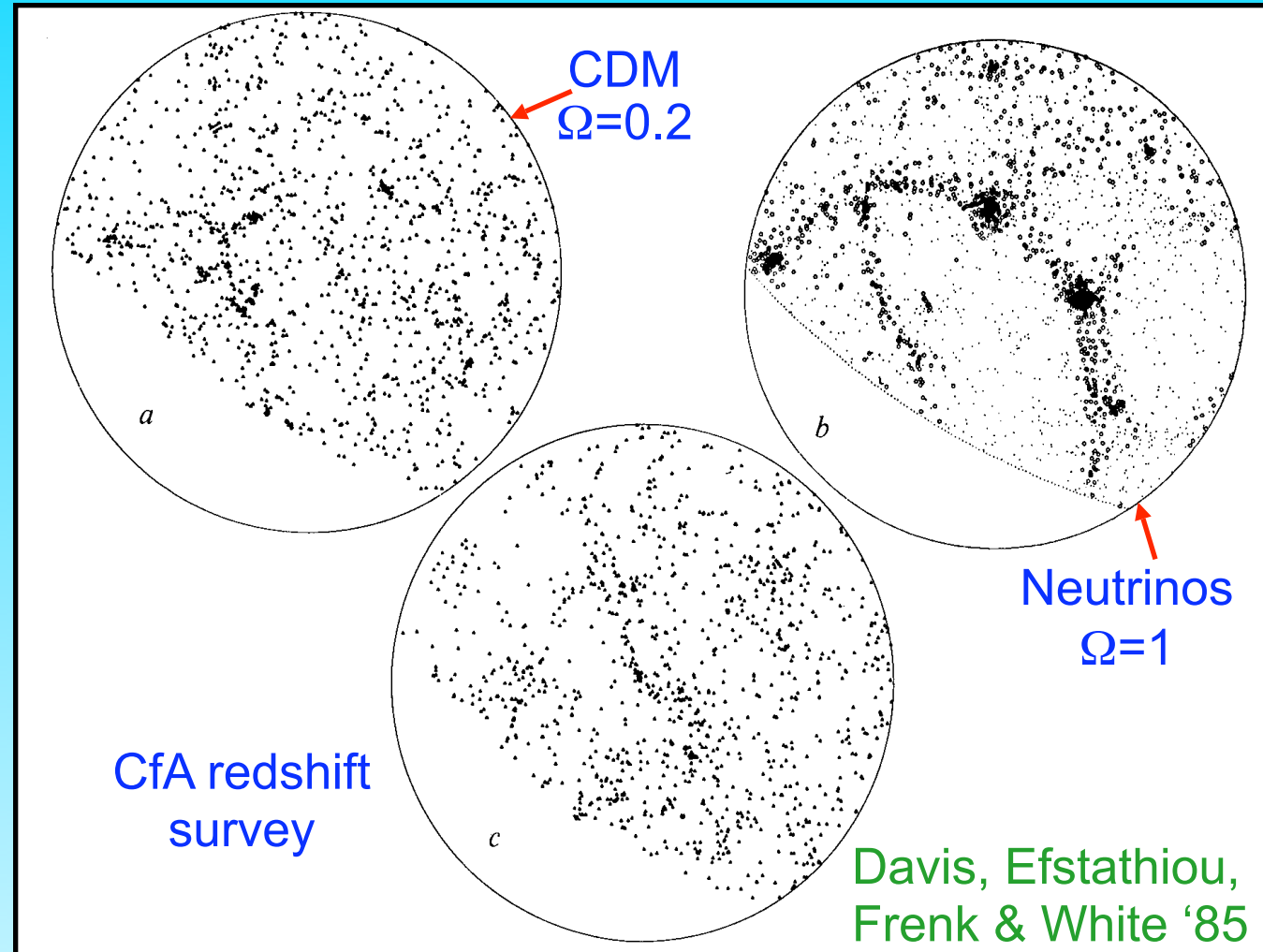
Frenk, White & Davis '83

# Non-baryonic dark matter cosmologies

Neutrino dark matter produces unrealistic clustering

Early CDM N-body simulations gave promising results

In CDM structure forms hierarchically



# The cold dark matter cosmogony

THE ASTROPHYSICAL JOURNAL, 263:L1-L5, 1982 December 1  
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Peebles '82

## LARGE-SCALE BACKGROUND TEMPERATURE AND MASS FLUCTUATIONS DUE TO SCALE-INVARIANT PRIMEVAL PERTURBATIONS

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Joseph Henry Laboratories, Physics Department, Princeton University

THE ASTROPHYSICAL JOURNAL, 292:371-394, 1985 May 15  
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Davis, Efstathiou, Frenk & White 1985

## THE EVOLUTION OF LARGE-SCALE STRUCTURE IN A UNIVERSE DOMINATED BY COLD DARK MATTER

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THE ASTROPHYSICAL JOURNAL, 304:15-61, 1986 May 1  
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Bardeen, Bond, Kaiser & Szalay 1986

## THE STATISTICS OF PEAKS OF GAUSSIAN RANDOM FIELDS

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REVIEW ARTICLE

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## Formation of galaxies and large-scale structure with cold dark matter

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Blumenthal, Faber, Primack & Rees 1984

## Cold dark matter candidates:

- Axion  $m_a \sim 10^{-5} \text{ eV}$
- Sterile neutrino  $m_\nu \sim 100 \text{ MeV}$
- Neutralino (lightest stable susy particle)  $m_\chi > 100 \text{ GeV}$



# Modelling large-scale structure

**Cosmological model**  
( $\Omega, \Lambda, h \dots$ ); dark matter

Primordial fluctuations  
 $\delta\rho/\rho(M, t)$

**Standard model:**  
 $\Lambda$ CDM

- Material content: { Cold dark matter (eg neutralino; **21%**), baryons (**4%**), dark energy ( $\Lambda$ ; **75%**)
- Initial conditions: { Quantum fluctuations during inflation:  $|\delta_k|^2 \propto k^n, n \approx 1$ ; Gaussian amplitudes
- Growth processes: { Gravitational instability
- Parameters: {  $\Omega_{CDM} = 0.21, \Omega_b = 0.04, \Omega_\Lambda = 0.75,$   
 $h = 0.70, \sigma_8 = 0.9, \dots$



# Testing $\Lambda$ CDM on very large scales (and very early times)

# The microwave background radiation

380 000 years after the big Bang

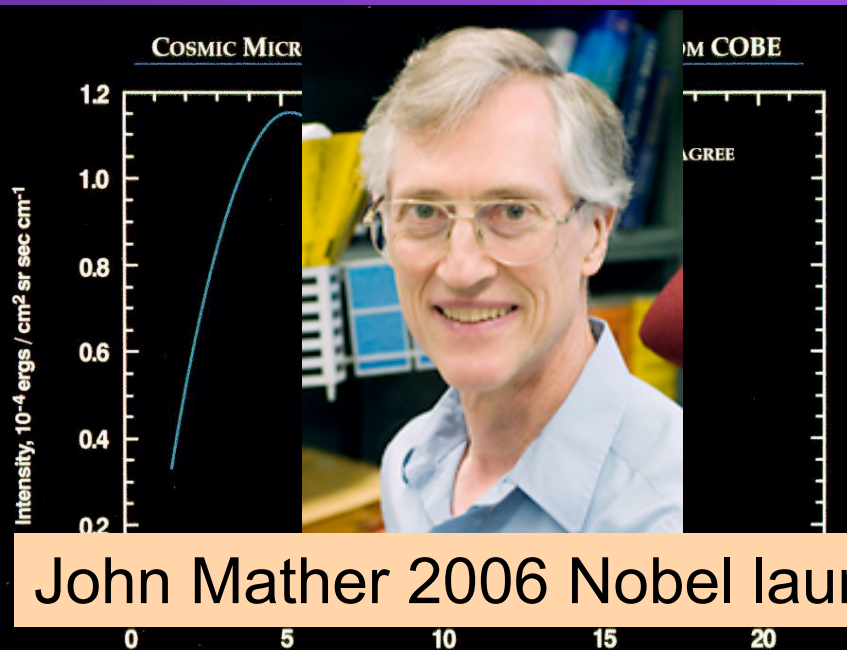


Plasma

t=0



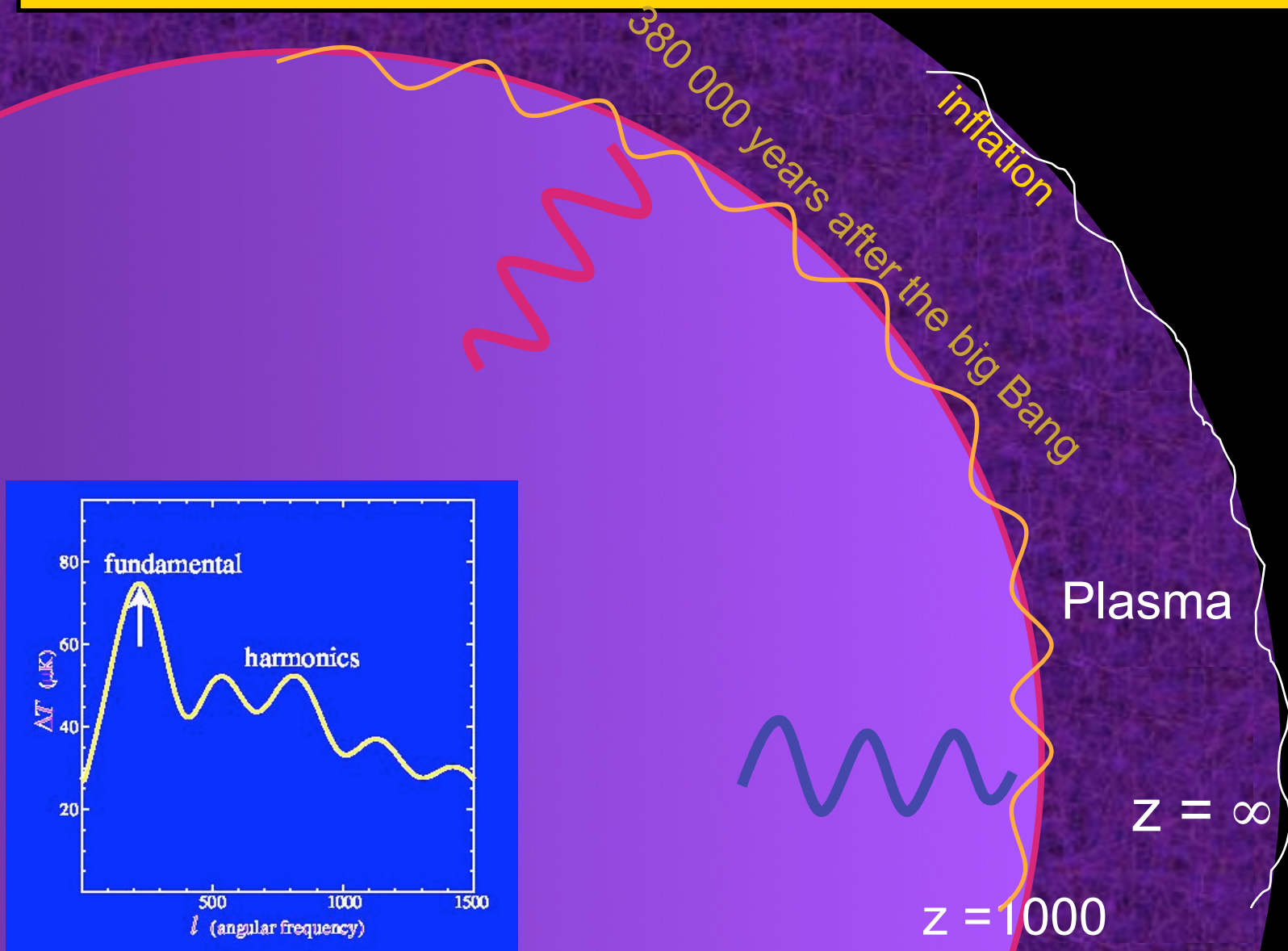
t=380 000 yrs



John Mather 2006 Nobel laureate



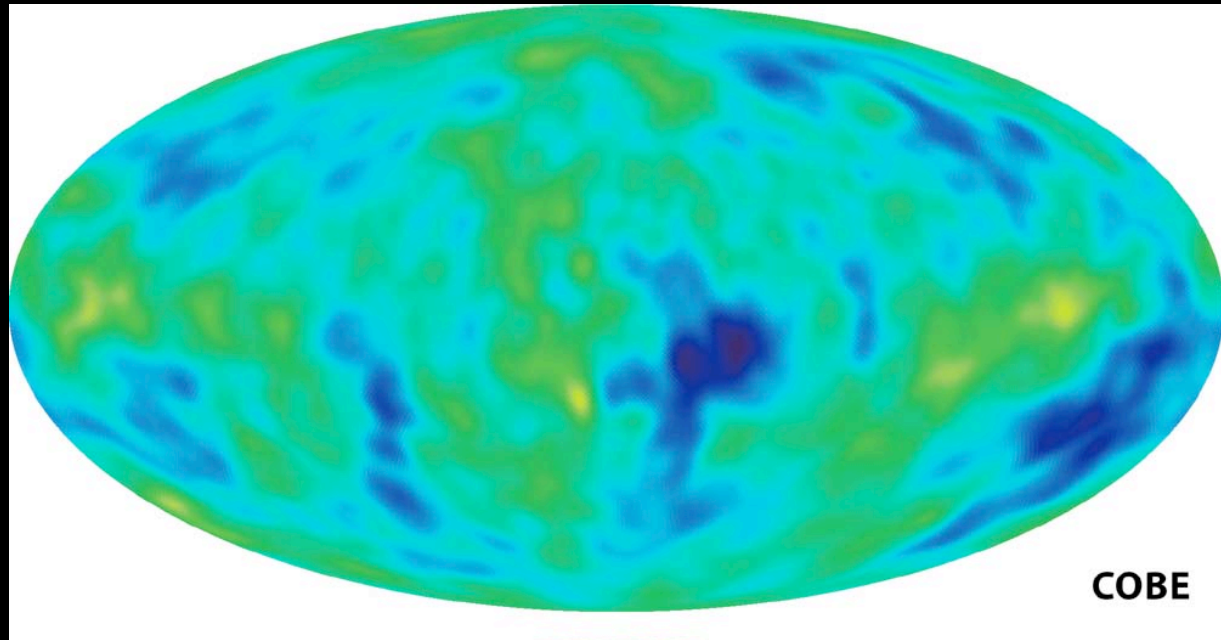
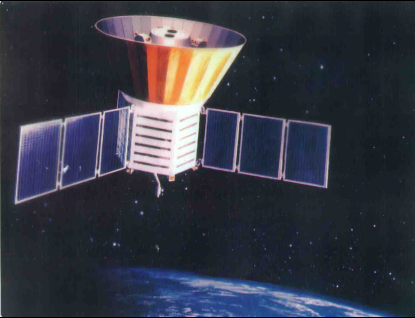
# The microwave background radiation





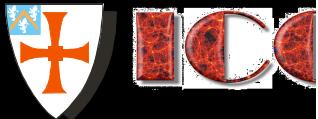
# The CMB

1992



The cosmic microwave background radiation (CMB) provides a window to the universe at  $t \sim 3 \times 10^5$  yrs

In 1992 COBE discovered temperature fluctuations ( $\Delta T / T \sim 10^{-5}$ ) consistent with inflation predictions



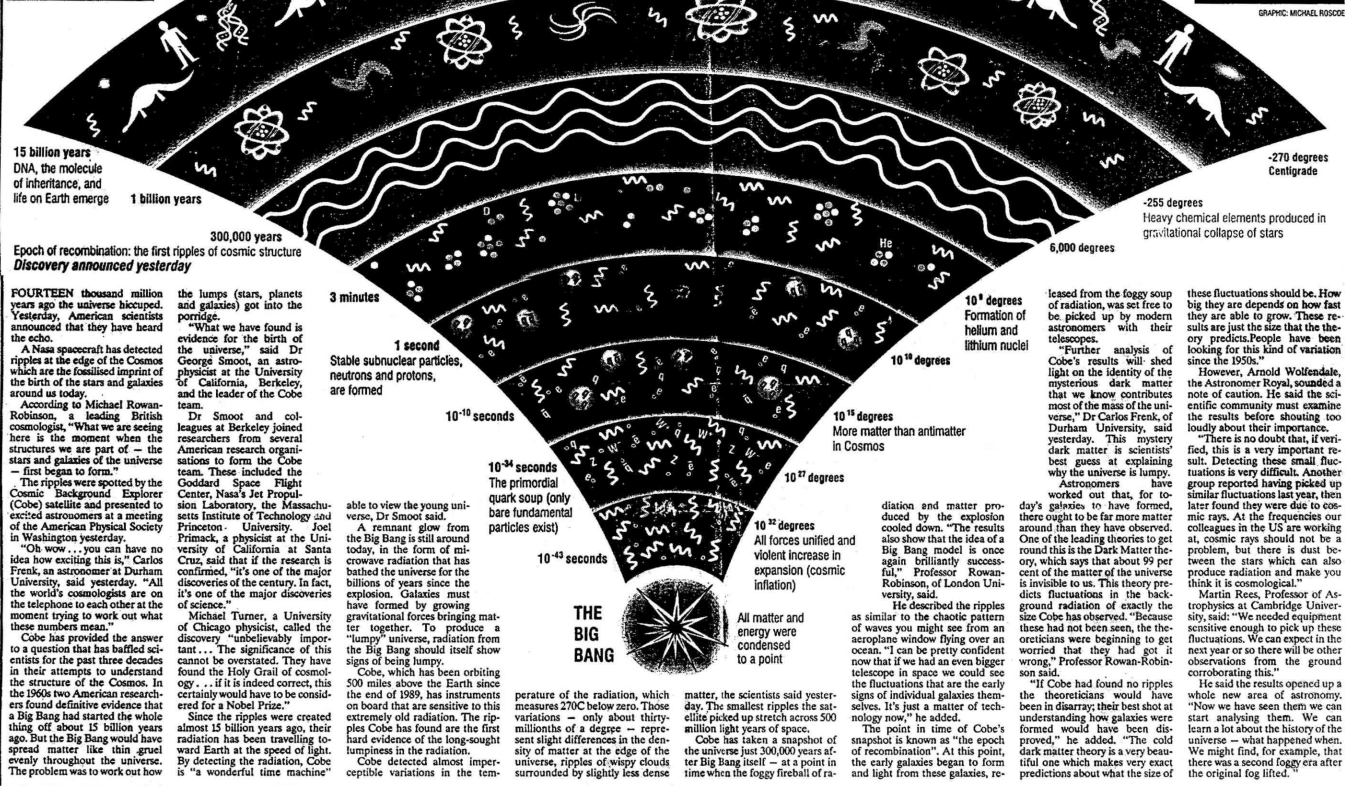
# THE INDEPENDENT

A Nasa spacecraft has detected echoes of the galaxies' birth fourteen thousand million years ago. The discovery about the formation of the stars after the Big Bang has been hailed by excited scientists as the Holy Grail of cosmology. Susan Watts and Tom Wilkie report

## How the universe began

### BACK TO CREATION

How the universe evolved from the Big Bang, through the first three minutes, to the first clusters of matter 300,000 years on. By 15 billion years humanity had emerged from the dust of the stars.



15 billion years  
DNA, the molecule of inheritance, and life on Earth emerge

300,000 years  
Epoch of recombination: the first ripples of cosmic structure  
*Discovery announced yesterday*

14 thousand million years ago the universe hiccuped. Yesterday, American scientists announced that they have heard the echo.

A Nasa spacecraft has detected ripples at the edge of the Cosmos which are the fossilised imprint of the birth of the stars and galaxies around us today.

According to Michael Rowan-Robinson, a leading British cosmologist, "What we are seeing here is the moment when the structures we are part of - the stars and galaxies of the universe - first began to form."

The ripples were spotted by the Cosmic Background Explorer (Cobe) satellite and presented to excited astronomers at a meeting of the American Physical Society in Washington yesterday. "Oh wow... you can have no idea how exciting this is," Carlos Frenk, an astronomer at Durham University, said yesterday. "All the world's cosmologists are on the telephone to each other at the moment trying to work out what these numbers mean."

Cobe has provided the answer to a question that has baffled scientists for the past three decades in their attempts to understand the structure of the Cosmos. In the 1960s two American researchers found definitive evidence that a Big Bang had started the whole thing off about 15 billion years ago. But the Big Bang would have spread matter like thin gruel evenly throughout the universe. The problem was to work out how

the lumps (stars, planets and galaxies) got into the porridge.

"What we have found is evidence for the birth of the universe," said Dr George Smoot, an astrophysicist at the University of California, Berkeley, and the leader of the Cobe team.

Dr Smoot and colleagues at Berkeley joined researchers from several American research organisations to form the Cobe team. These included the Goddard Space Flight Center, Nasa's Jet Propulsion Laboratory, the Massachusetts Institute of Technology and Princeton University. Joel Primack, a physicist at the University of California at Santa Cruz, said that if the research is confirmed, "it's one of the major discoveries of the century. In fact, it's one of the major discoveries of science."

Michael Turner, a University of Chicago physicist, called the discovery "unbelievably important". The significance of this cannot be overstated. They have found the Holy Grail of cosmology... if it is indeed correct, this certainly would have to be considered for a Nobel Prize.

Since the ripples were created about 15 billion years ago, their radiation has been travelling toward Earth at the speed of light. By detecting the radiation, Cobe is "a wonderful time machine"

able to view the young universe, Dr Smoot said. A remnant glow from the Big Bang is still around today, in the form of microwave radiation that has bathed the universe for the billions of years since the explosion. Galaxies must have formed by growing gravitational forces bringing matter together. To produce a "lumpy" universe, radiation from the Big Bang should itself show signs of being lumpy. Cobe, which has been orbiting 500 miles above the Earth since the end of 1989, has instruments on board that are sensitive to this extremely old radiation. The ripples Cobe has found are the first hard evidence of the long-sought lumps in the radiation. Cobe detected almost imperceptible variations in the tem-

perature of the radiation, which measures 2700 below zero. Those variations - only about thirty-millionths of a degree - represent slight differences in the density of matter at the edge of the universe, ripples of wispy clouds surrounded by slightly less dense

matter, the scientist said yesterday. The smallest ripples the satellite picked up stretch across 500 million light years of space. Cobe has taken a snapshot of the universe just 300,000 years after the Big Bang itself - at a point in time when the foggy fireball of ra-

diation and matter produced by the explosion cooled down. "The results also show that the idea of a Big Bang model is once again brilliantly successful," Professor Rowan-Robinson, of London University, said.

He described the ripples as similar to the chaotic pattern of waves you might see from an aeroplane window flying over an ocean. "I can be pretty confident now that if we had an even bigger telescope in space we could see the fluctuations that are the early signs of individual galaxies themselves. It's just a matter of technology now," he added.

The point in time of Cobe's snapshot is known as "the epoch of recombination". At this point, the early galaxies began to form and light from these galaxies, re-

leased from the foggy soup of radiation, was set free to be picked up by modern astronomers with their telescopes.

"Further analysis of Cobe's results will shed light on the identity of the mysterious 'dark' matter that we know contributes most of the mass of the universe," Dr Carlos Frenk, of Durham University, said yesterday. This mystery dark matter is scientists' best guess at explaining why the universe is lumpy.

Astronomers have worked out that, for galaxies to have formed, there ought to be far more matter around than they have observed. One of the leading theories to get round this is the Dark Matter theory, which says that about 99 per cent of the matter of the universe is invisible to us. This theory predicts fluctuations in the background radiation of exactly the size Cobe has observed. "Because these had not been seen, the theoreticians were beginning to get worried that they had got it wrong," Professor Rowan-Robinson said.

"If Cobe had found no ripples the theoreticians would have been in disarray; their best shot at understanding how galaxies were formed would have been disproved," he added. "The cold dark matter theory is a very beautiful one which makes very exact predictions about what the size of

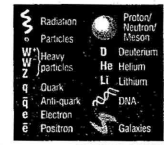
these fluctuations should be. How big they are depends on how fast they are able to grow. These results are just the size that the theory predicts. People have been looking for this kind of variation since the 1950s."

However, Arnold Wolfendale, the Astronomer Royal, sounded a note of caution. He said the scientific community must examine the results before showing too loudly about their importance.

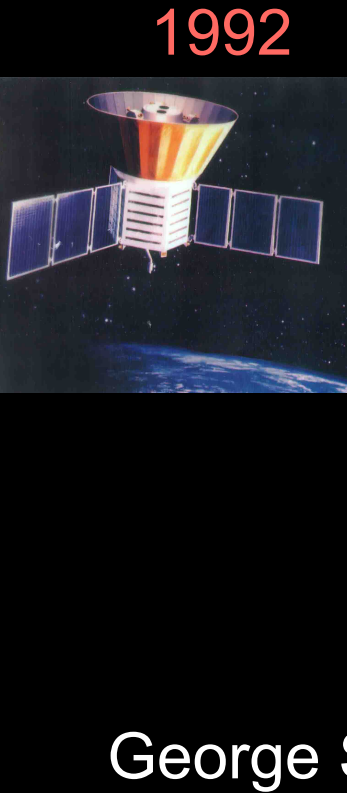
"There is no doubt that, if verified, this is a very important result. Detecting these small fluctuations is very difficult. Another group reported having picked up similar fluctuations last year, then later found they were due to cosmic rays. At the frequencies our colleagues in the US are working at, cosmic rays should not be a problem, but there is dust between the stars which can also produce radiation and make you think it is cosmological."

Martin Rees, Professor of Astrophysics at Cambridge University, said: "We needed equipment sensitive enough to pick up these fluctuations. We can expect in the next year or so there will be other observations from the ground corroborating this."

He said the results opened up a whole new era of astronomy. "Now we have seen them we can start analysing them. We can learn a lot about the history of the universe - what happened when. We might find, for example, that there was a second foggy era after the original fog lifted."



GRAPHIC: MICHAEL ROSSICE

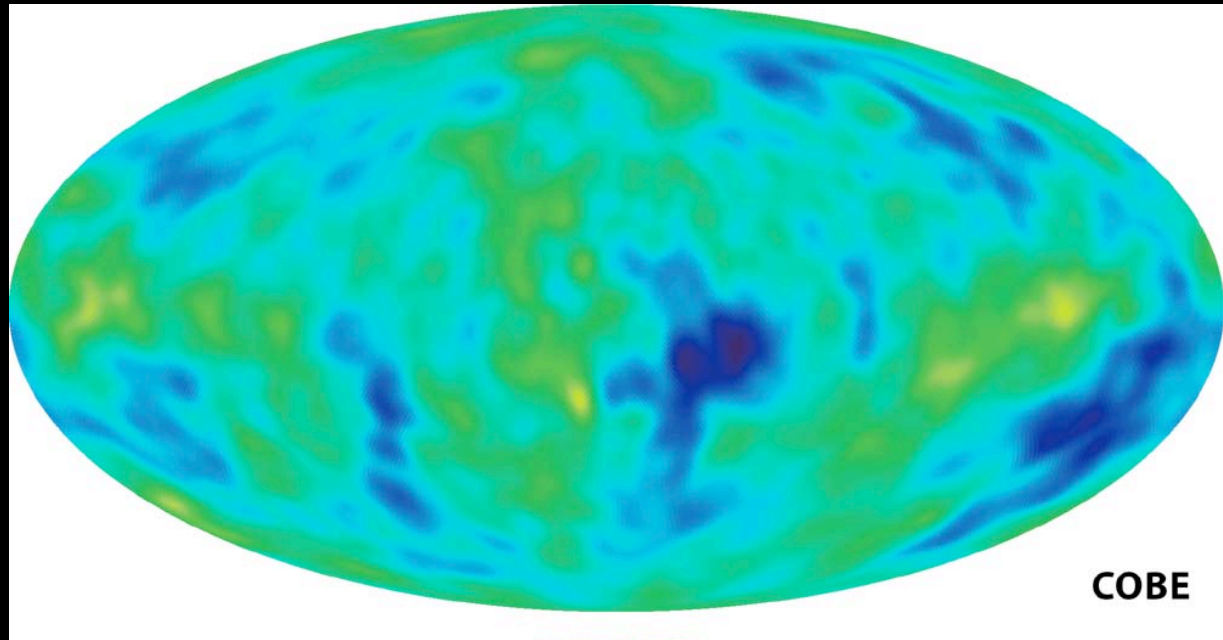


# George

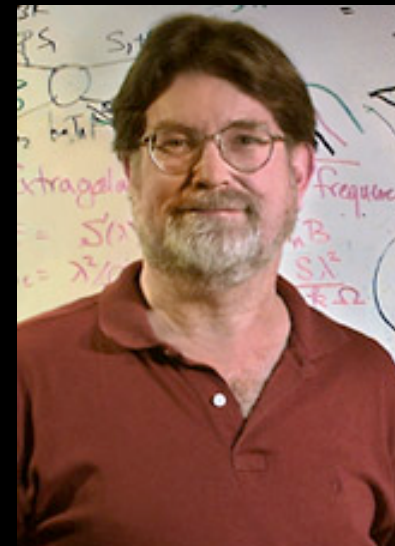


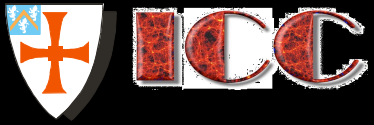
# The CMB

1992



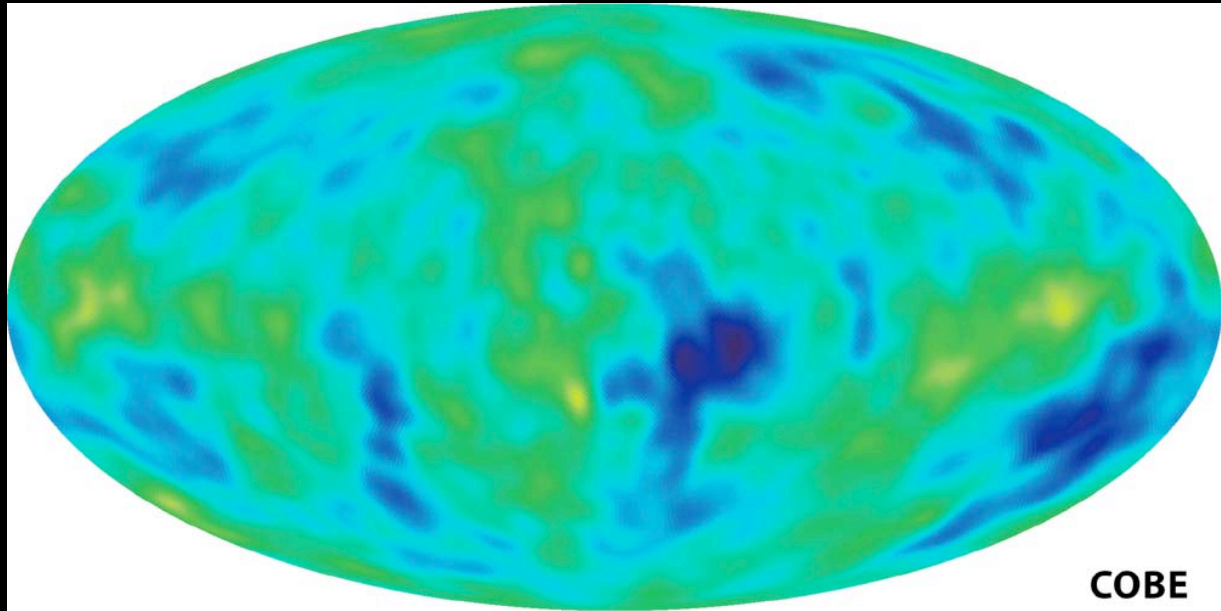
George Smoot - Nobel Prize 2006





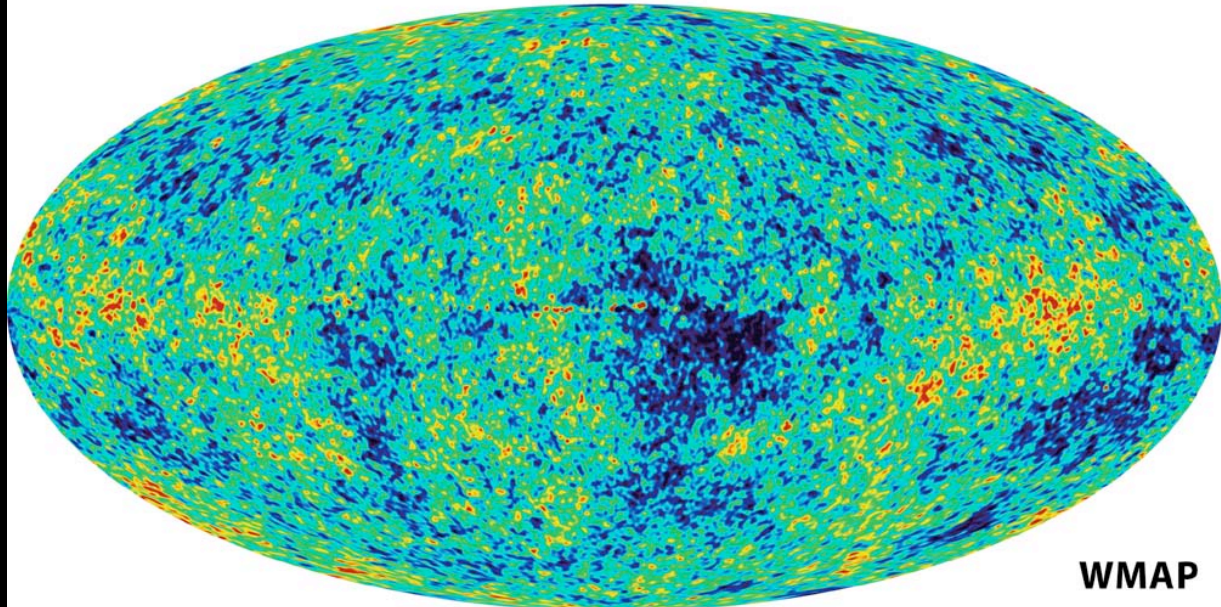
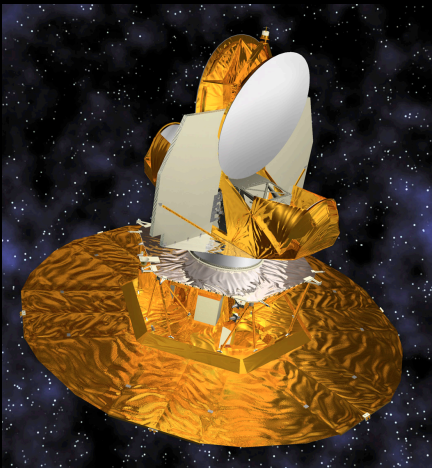
# The CMB

1992

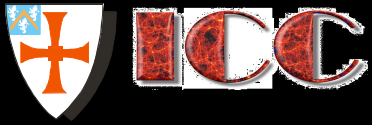


COBE

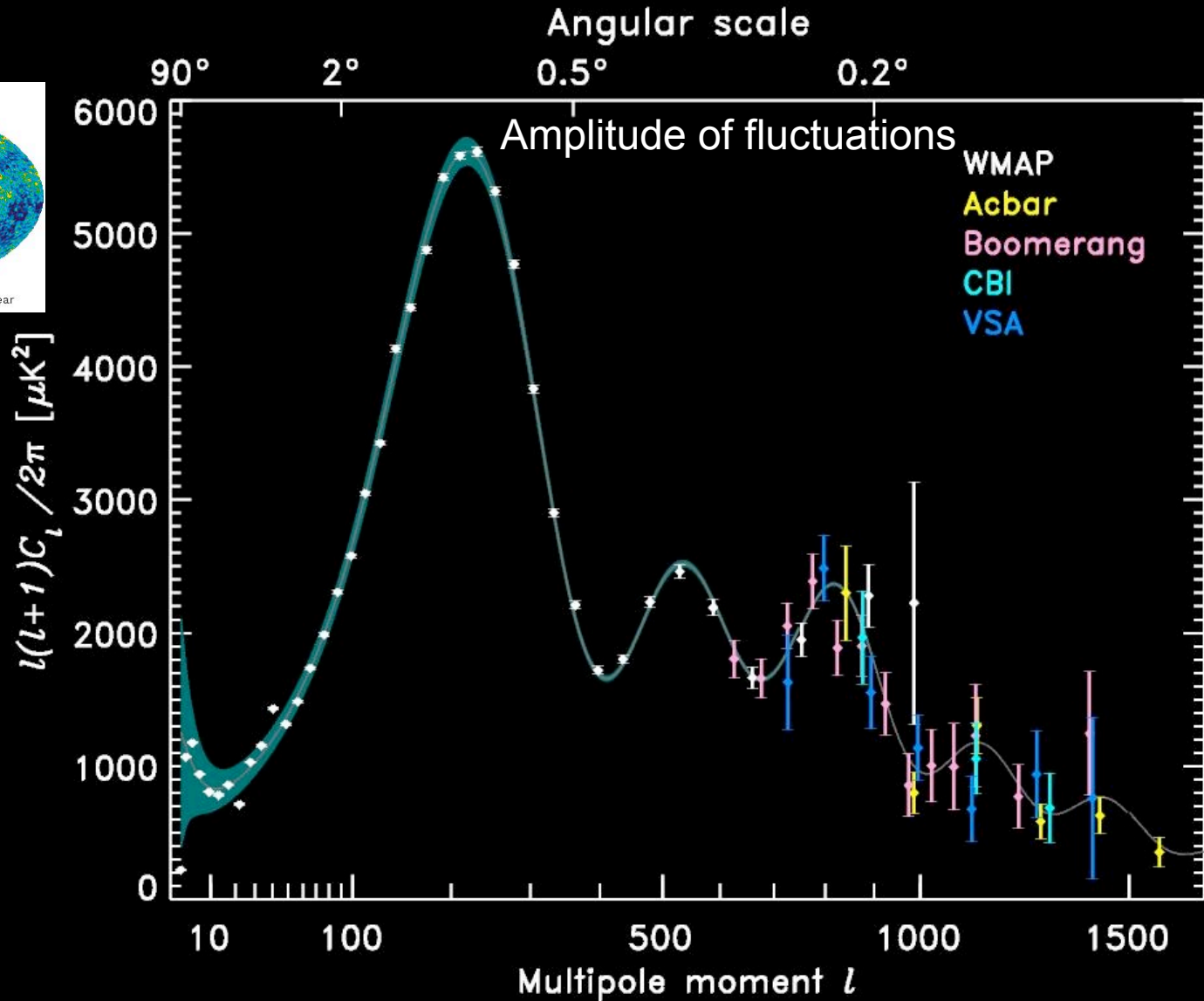
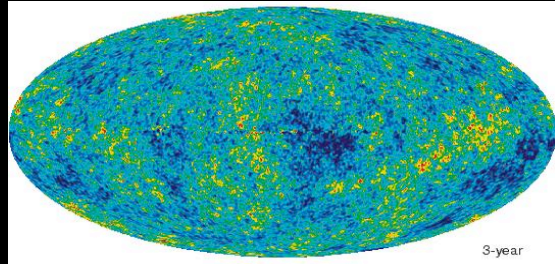
2003



WMAP



# WMAP temp anisotropies in CMB



The amplitude of the CMB ripples is exactly as predicted by inflationary cold dark matter theory

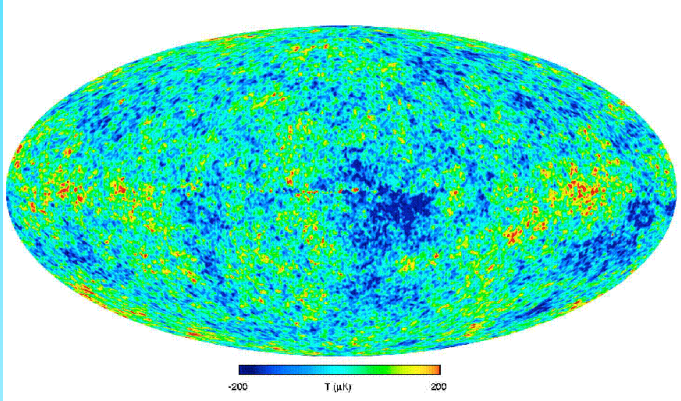
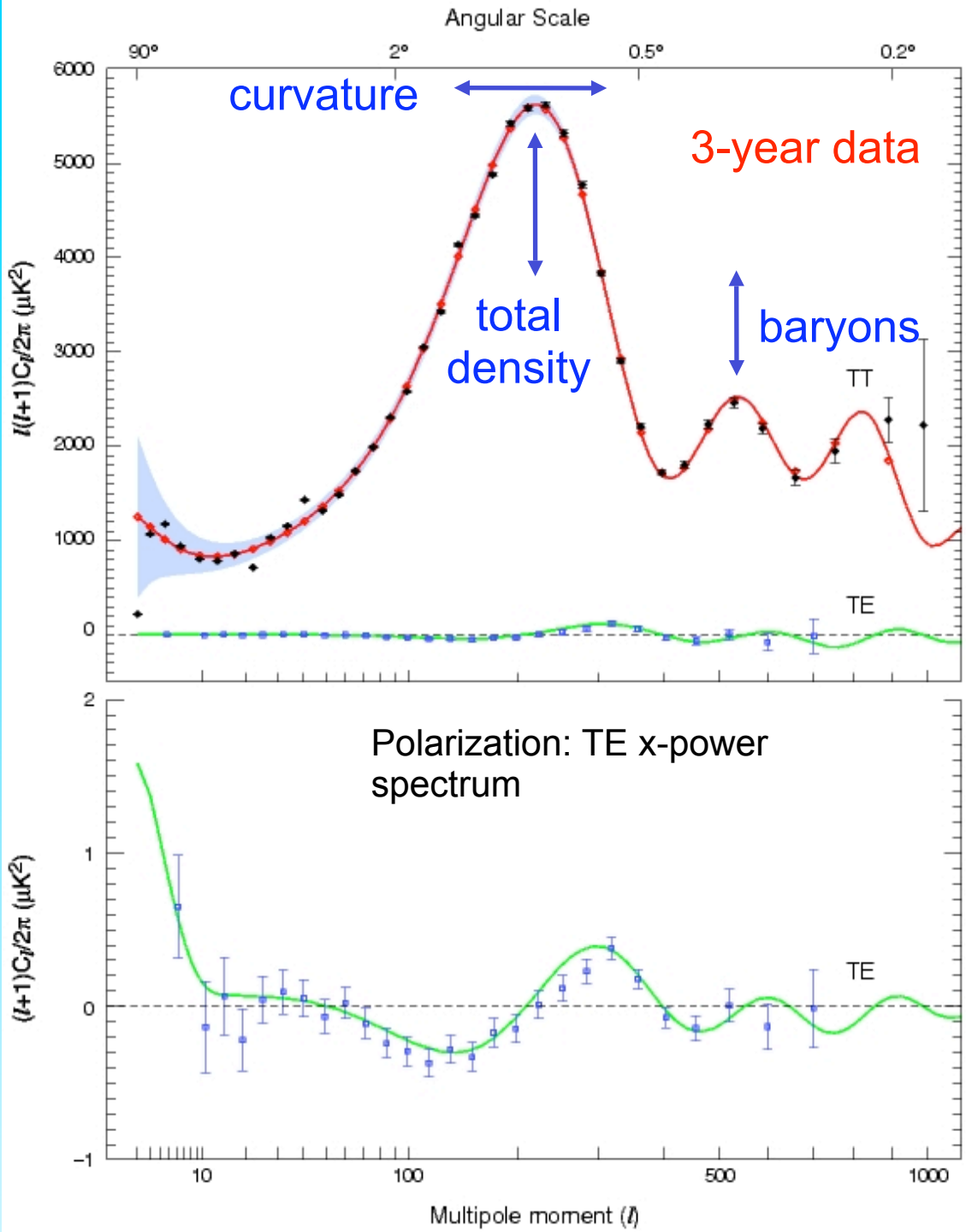
The position of the first peak

→ FLAT UNIVERSE

Hinshaw et al '06

# The Emergence of the Cosmic Initial Conditions

> 105 independent ~ 5s measurements of T are fit by a priori model: LCDM



T-P x-corr  $\rightarrow$  Adiabatic fluctns

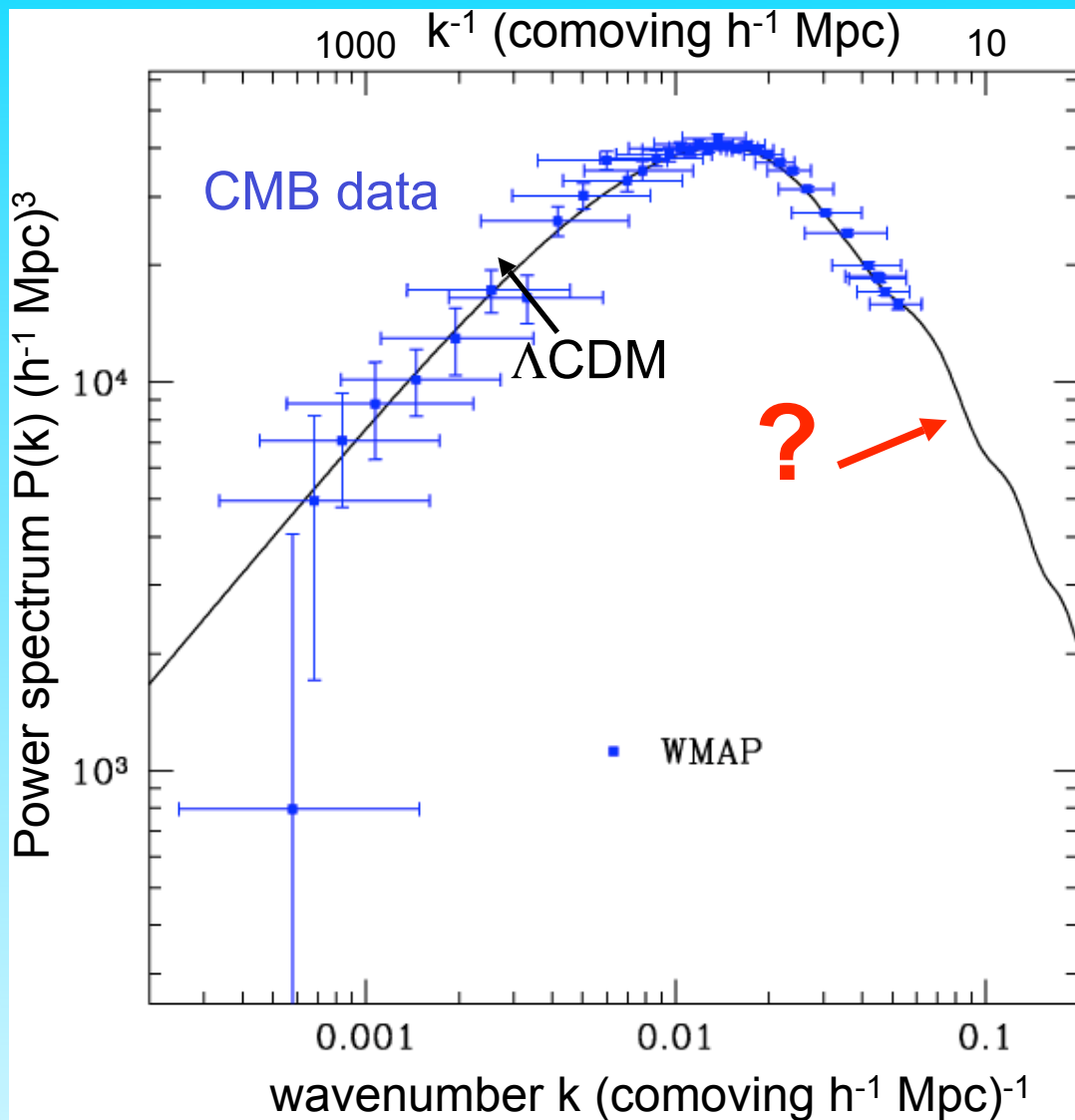
# The cosmic power spectrum: from the CMB to the 2dFGRS

$\Lambda$ CDM provides an excellent description of mass power spectrum from 10 - 1000 Mpc

## CMB:

- Convert angular separation to distance (and  $k$ ) assuming flat geometry
- Extrapolate to  $z=0$  using linear theory

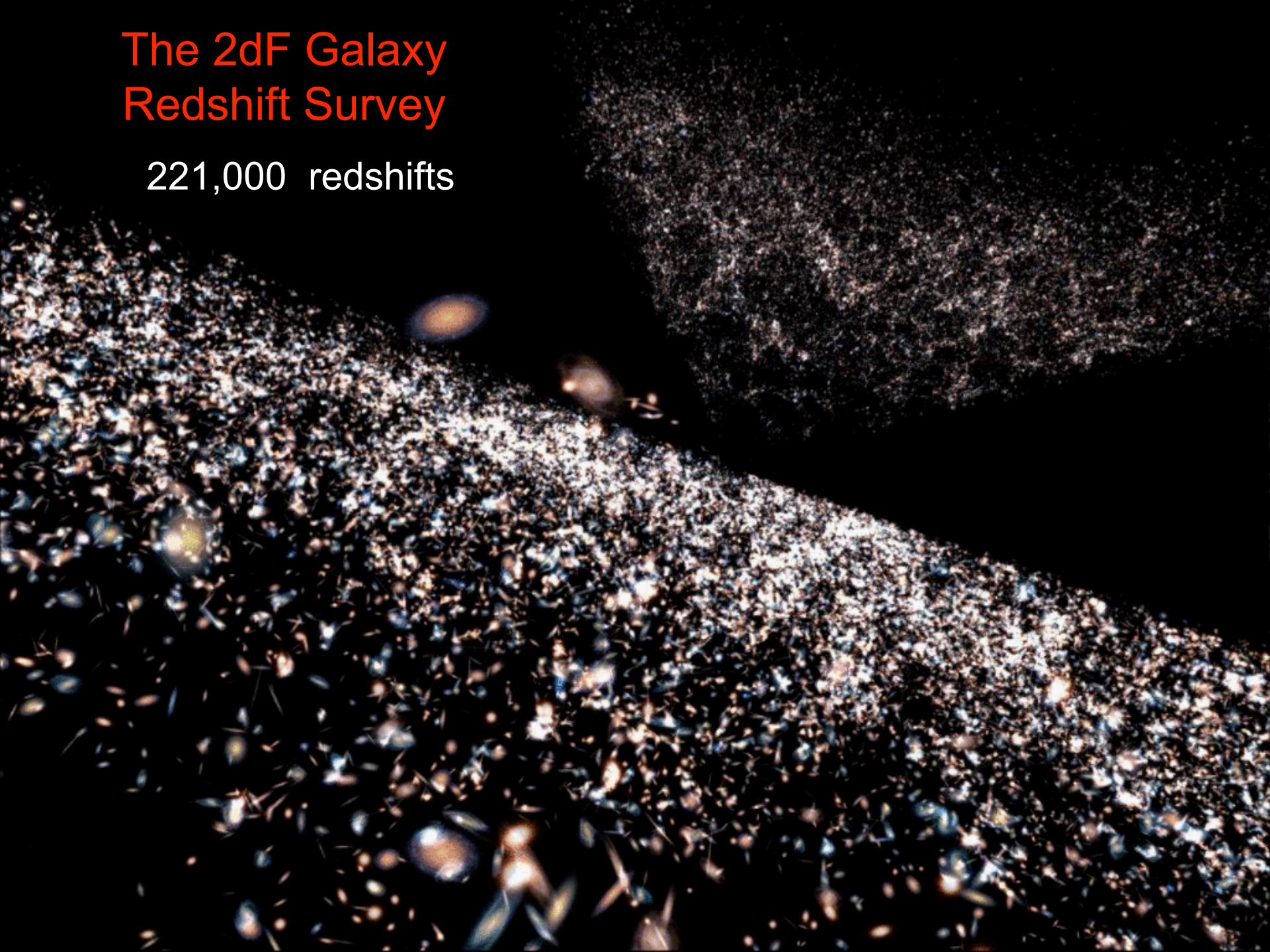
Sanchez et al 06





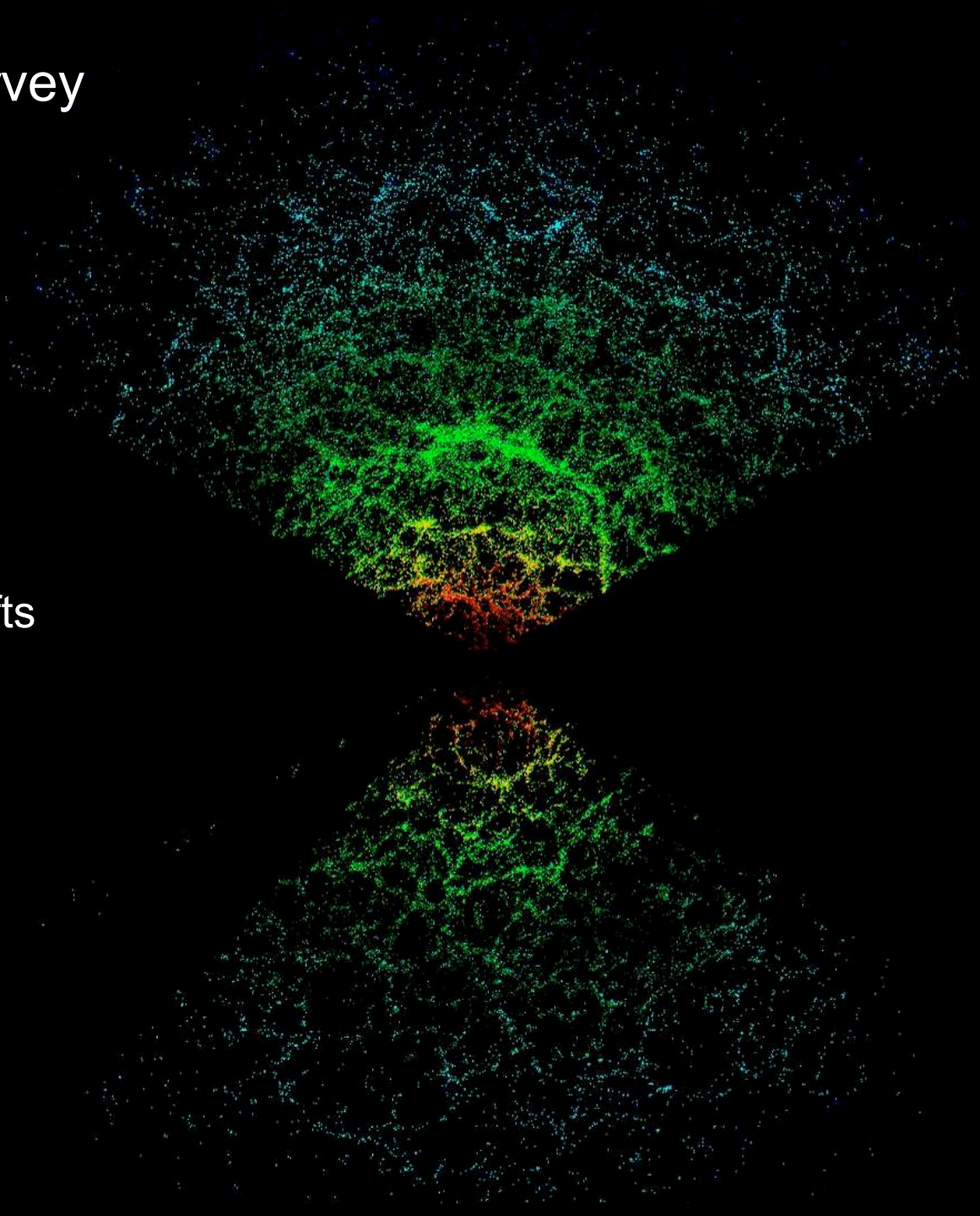
# The 2dF Galaxy Redshift Survey

221,000 redshifts



# Sloan Digital Sky Survey

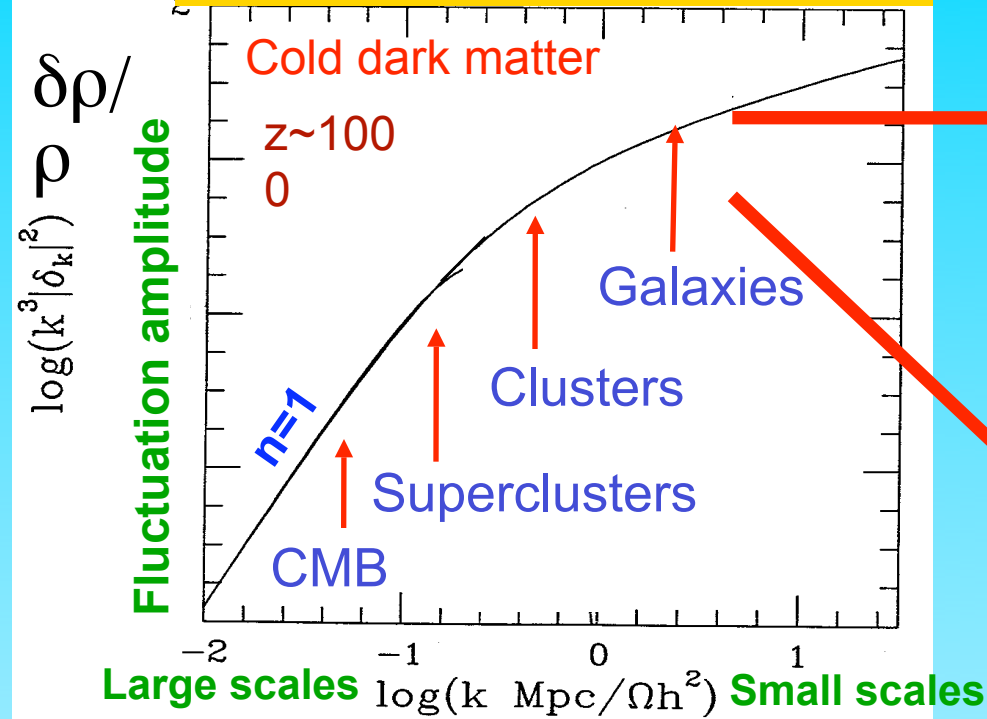
~500,000 galaxy redshifts



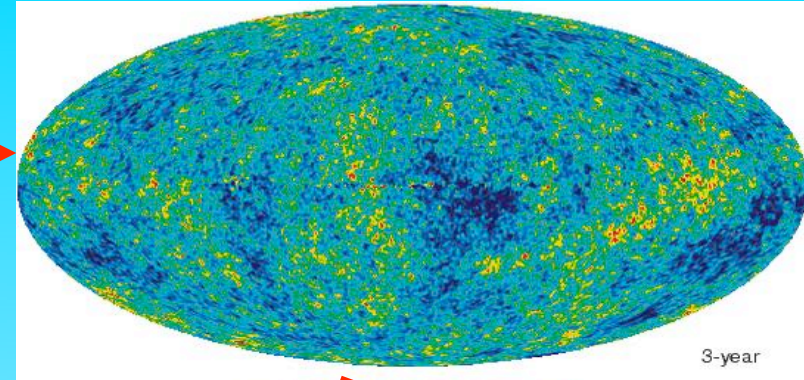


# Testing the CDM paradigm

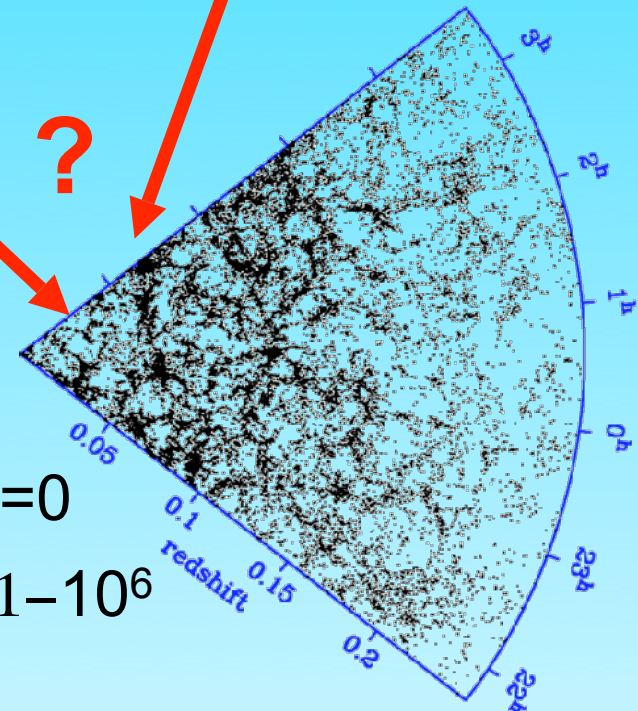
$P(k)$  Initial conditions :  $\Lambda$ CDM



$z=1000$   $\delta\rho/\rho \sim 10^{-5}$



?

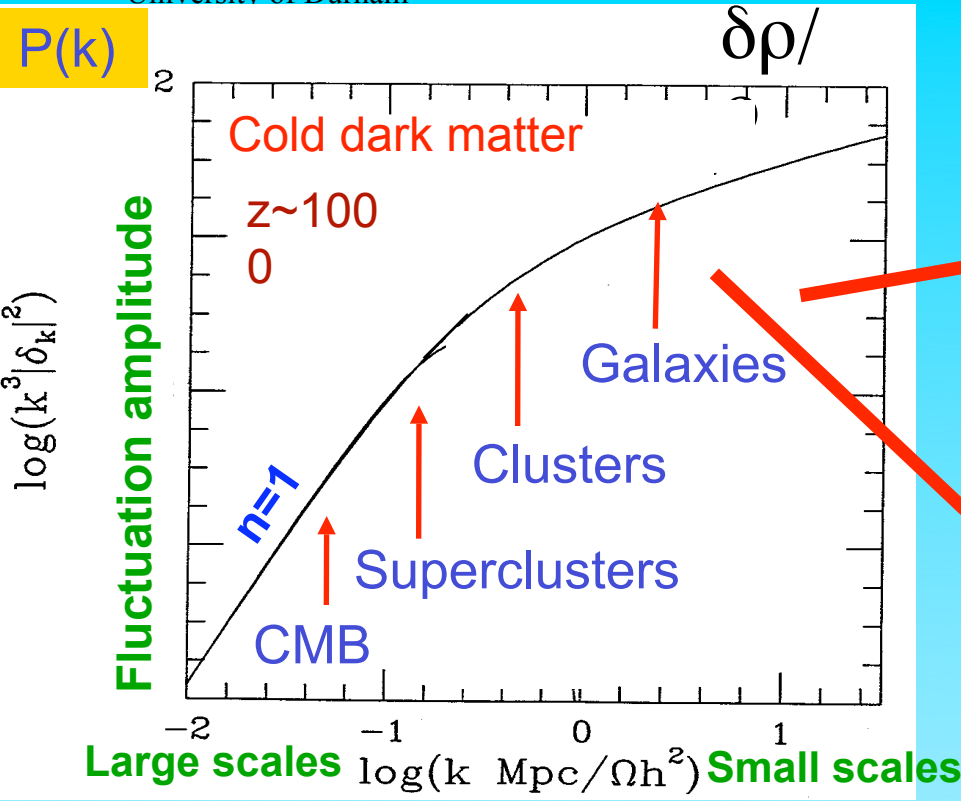


The galaxy distribution evolves from by fluctuations seen in CMB by gravitational amplification.

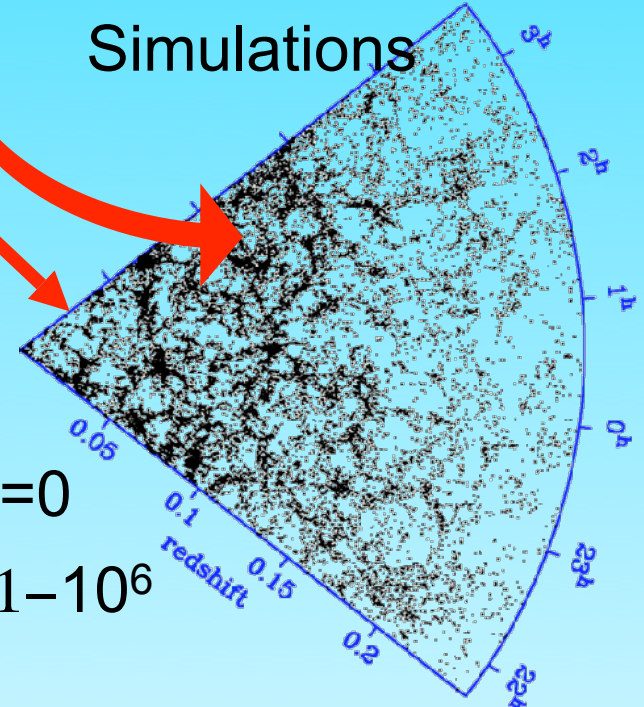
$z=0$   
 $\delta\rho/\rho \sim 1-10^6$

# Testing the CDM paradigm

“Cosmology machine”



Simulations

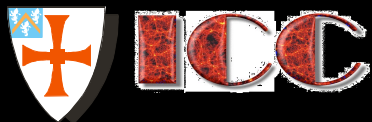


Initial conditions :  $\Lambda$ CDM

Basic DM physics simple: structure grows primarily by gravity

$\delta\rho/\rho \sim 1-10^6$

→ N-body simulations



dalla Vechia,  
Jenkins & Frenk



150 Mpc/h

Comoving  
coordinates

$t = 0.06 \text{ Gyr}$

# The Millennium simulation



UK, Germany, Canada, US  
collaboration

## Cosmological N-body simulation

- 10 billion particles
- 500  $h^{-1}$  Mpc box
- $m_p = 8 \times 10^8 h^{-1} M_\odot$
- $\Omega = 1$ ;  $\Omega_m = 0.25$ ;  $\Omega_b = 0.045$ ;  
 $h = 0.73$ ;  $n = 1$ ;  $\sigma_8 = 0.9$
- Carried out at Garching using  
 $20 \times 10^6$  gals brighter than LMC  
L-Gadget by V. Springel

(27 Tbytes of data)

Simulation data available at:

<http://www.mpa-garching.mpg.de/Virgo>

Pictures and movies available at:

[www.durham.ac.uk/virgo](http://www.durham.ac.uk/virgo)

Nature, June/05

# Virgo consortium for supercomputer simulations

## **Core members and associates**

- Carlos Frenk – ICC, Durham (P.I.)
- Adrian Jenkins – ICC, Durham
- Tom Theuns – ICC, Durham
- Gao Laing – ICC, Durham
- Simon White – Max Plank Institut für Astrophysik (co-P.I.)
- Volker Springel – Max Plank Institut für Astrophysik
- Frazer Pearce – Nottingham
- Naoki Yoshida – Tokyo
- Peter Thomas – Sussex
- Hugh Couchman – McMaster
- John Peacock – Edinburgh
- George Efstathiou – Cambridge
- Joerg Colberg – Pittsburgh
- Scott Kay – Oxford
- Rob Thacker – McGill
- Julio Navarro – Victoria
- Gus Evrard – Michigan
- Joop Schaye – Leiden



**Simulation data available at:**

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***Virgo junior associates***

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Nature, June/05

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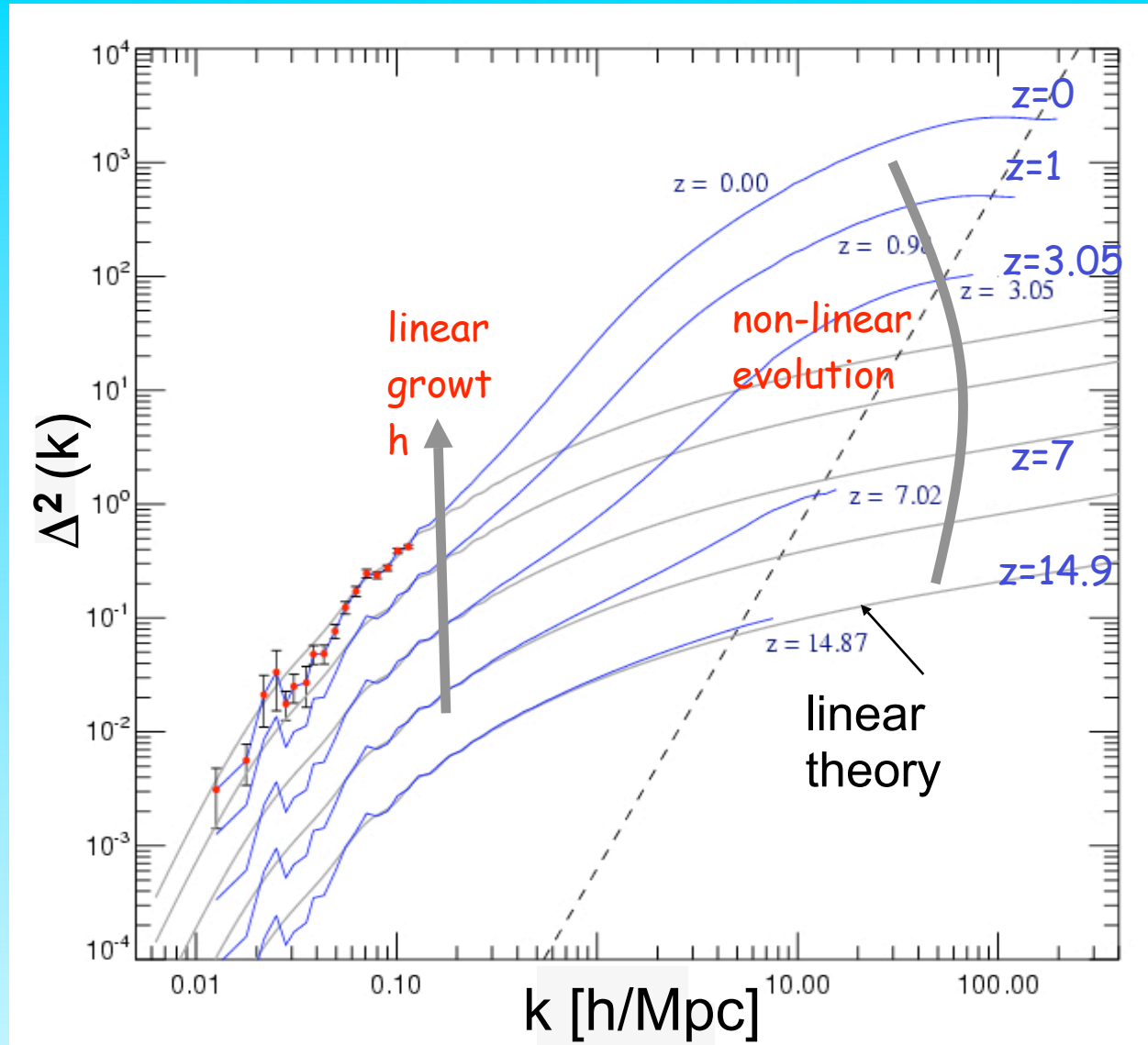
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- Carried out at Garching using  
L-Gadget by V. Springel  
20  $\times 10^6$  gals brighter than LMC

(27 Tbytes of data)



# The mass power spectrum

The non-linear mass power spectrum is accurately determined by the Millennium simulation over large range of scales



$z = 0$  Dark Matter

## Populating the MS with galaxies

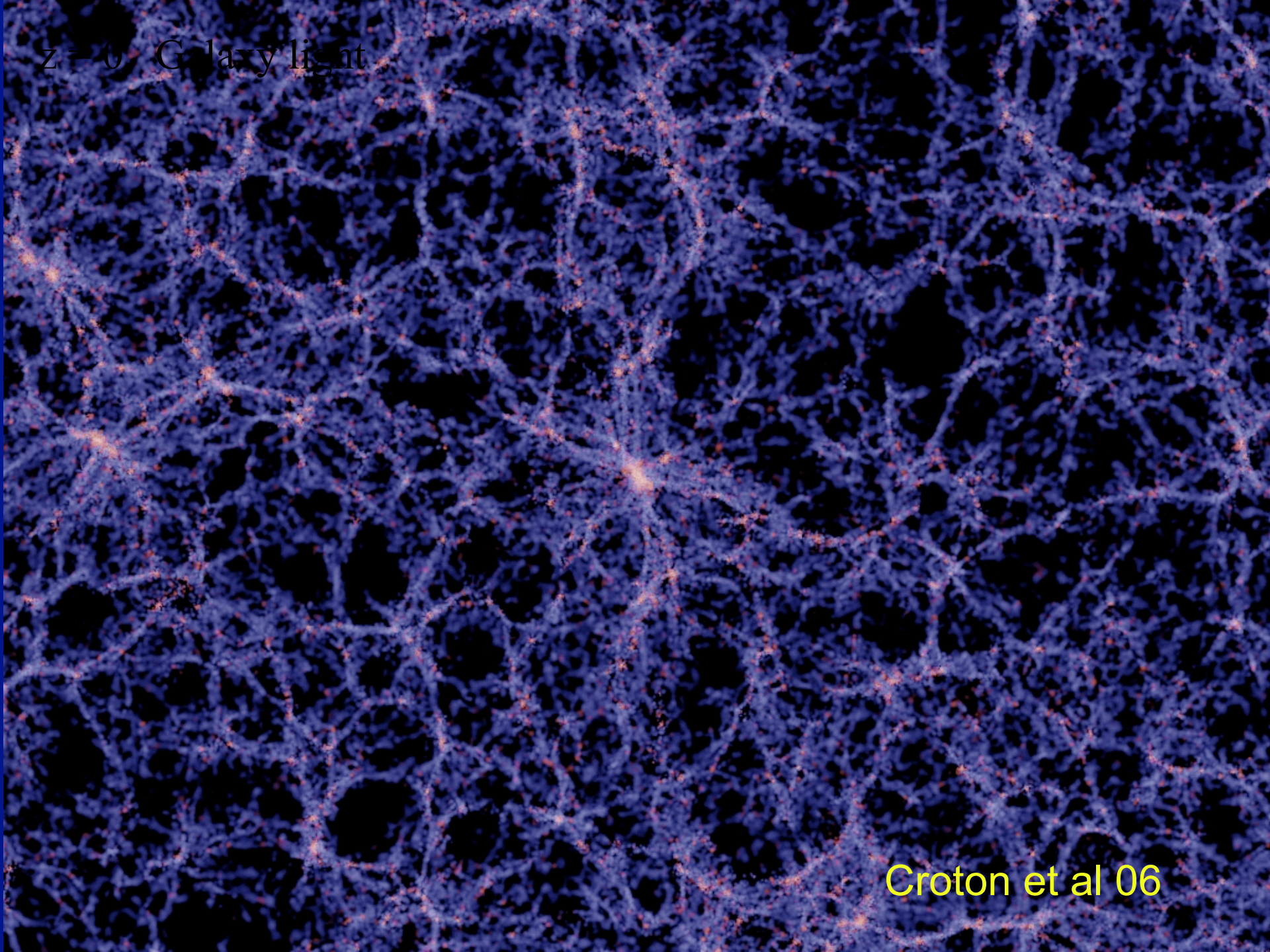
125 Mpc/h

### Semi-analytic modelling

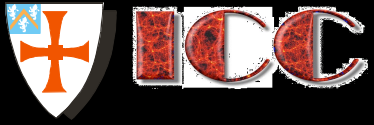
- Find dark matter halos
- Construct halo merger trees
- Apply SA model (gas cooling, star formation, feedback)

Springel et al 05

$z = 0$  Galaxy light



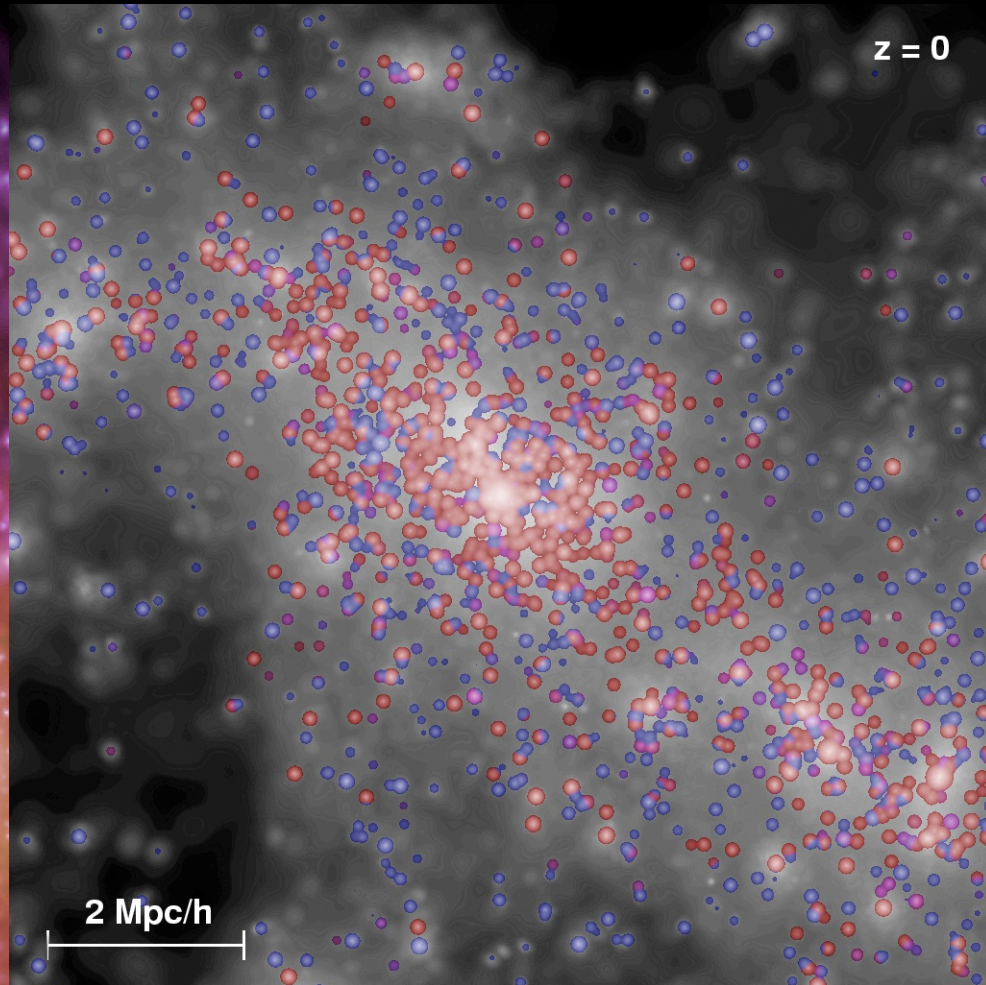
Croton et al 06



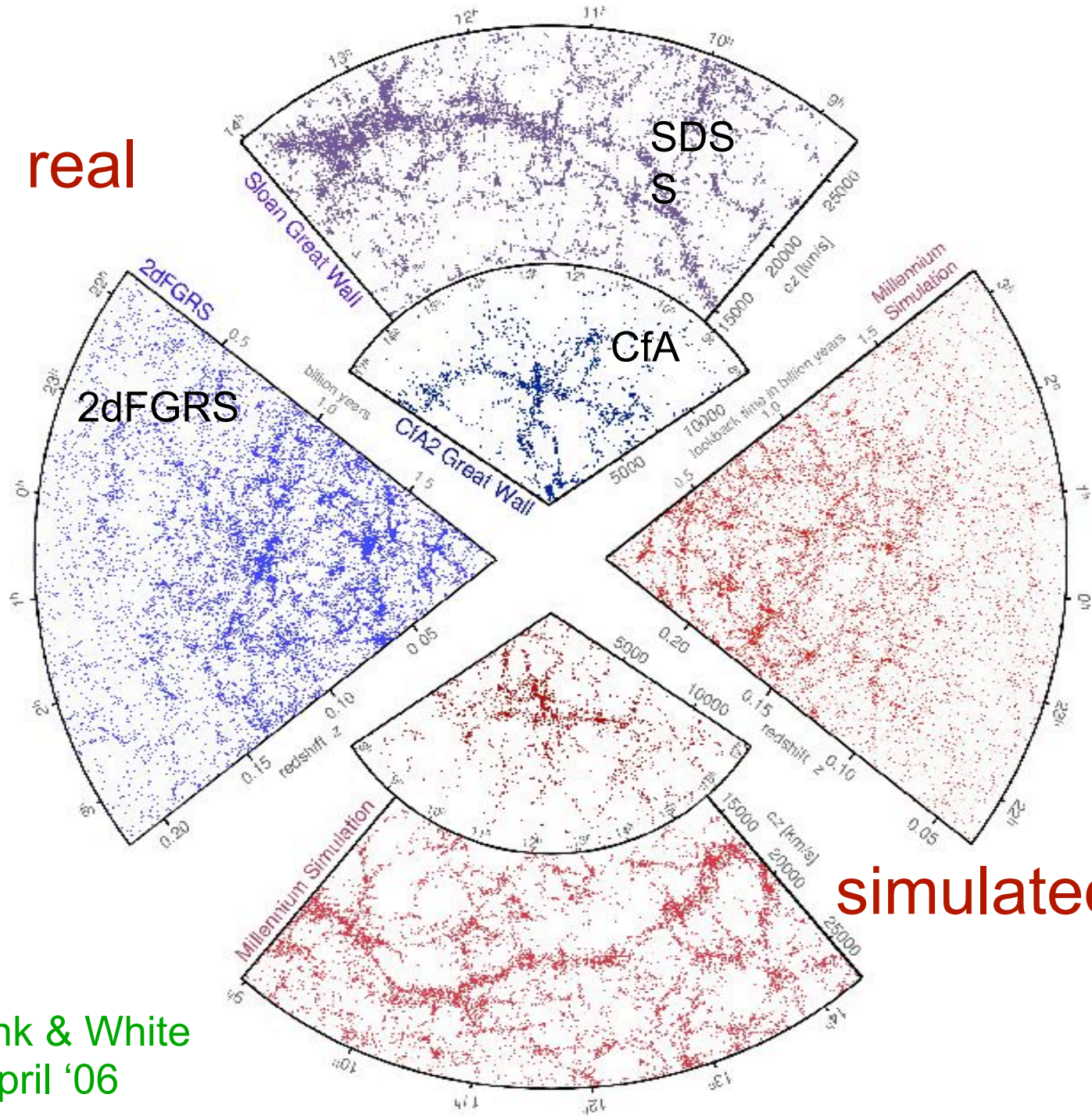
$10^{14} M_{\odot}$

Dark matter

Galaxies

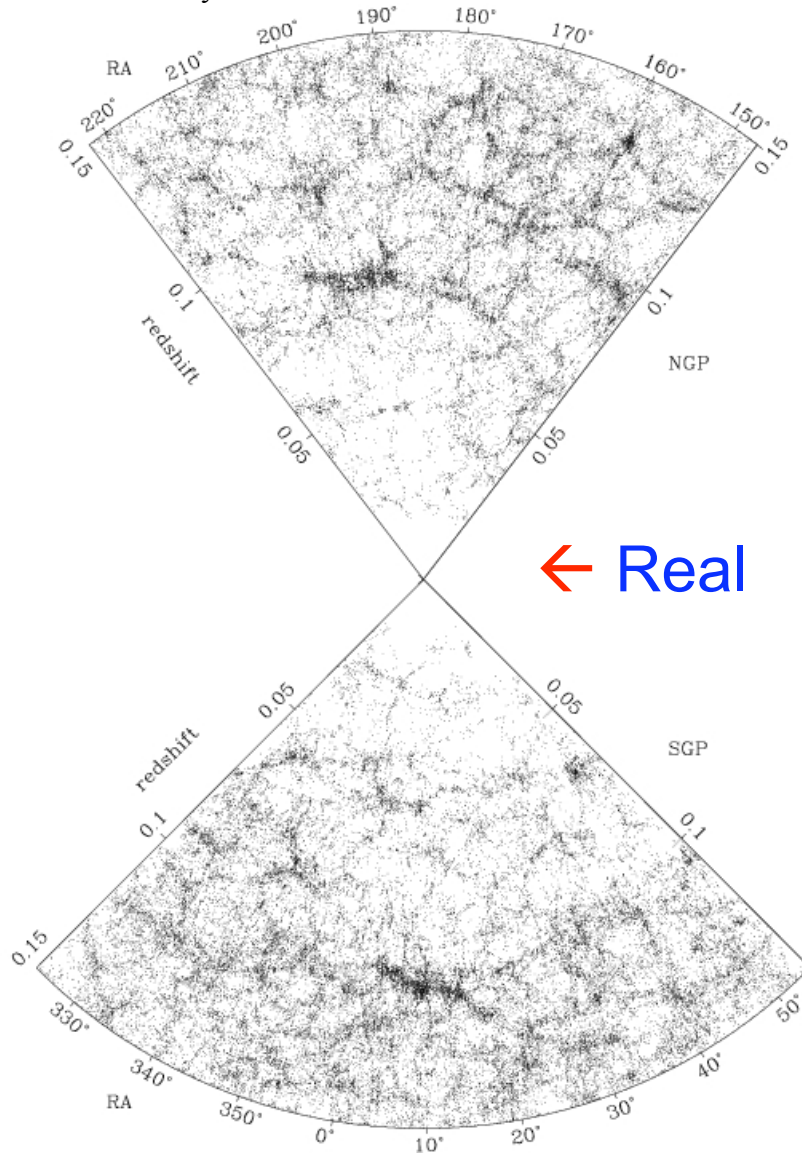


real



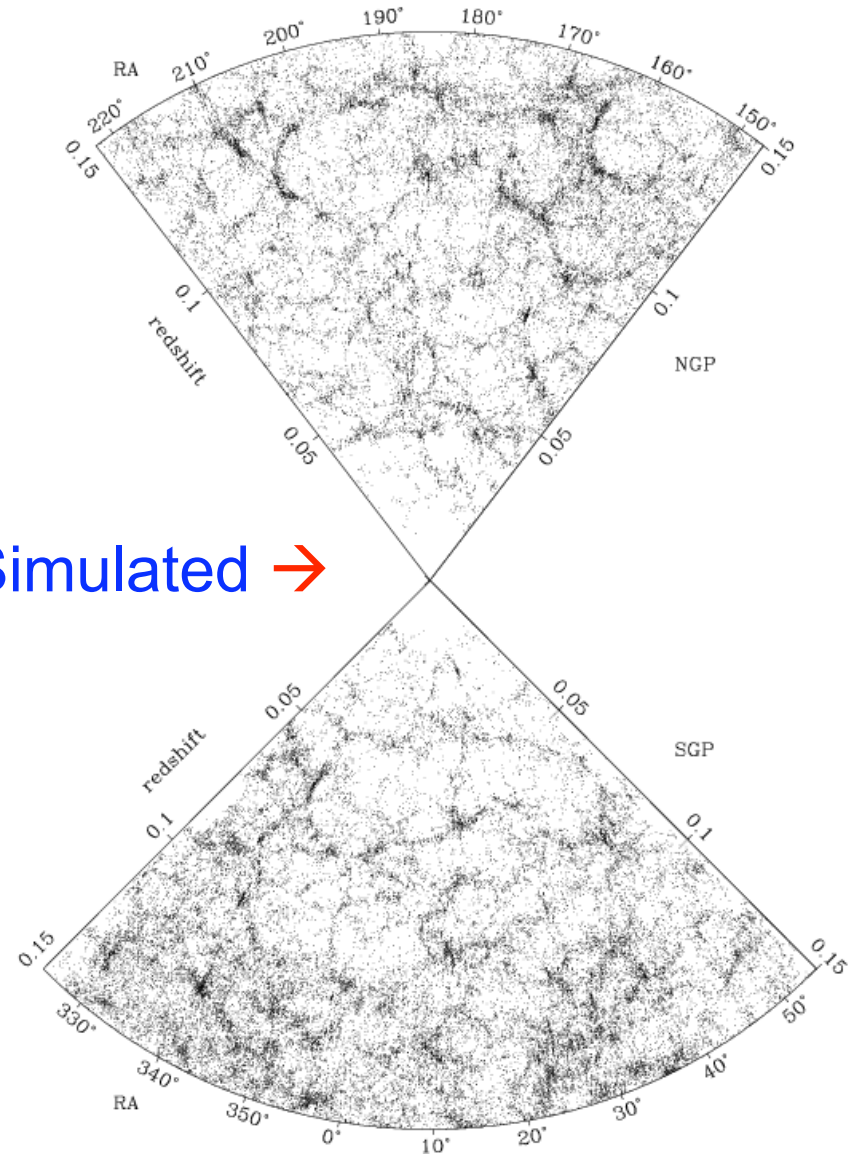
Springel, Frenk & White  
Nature, April '06

# Real and simulated 2dF galaxy survey



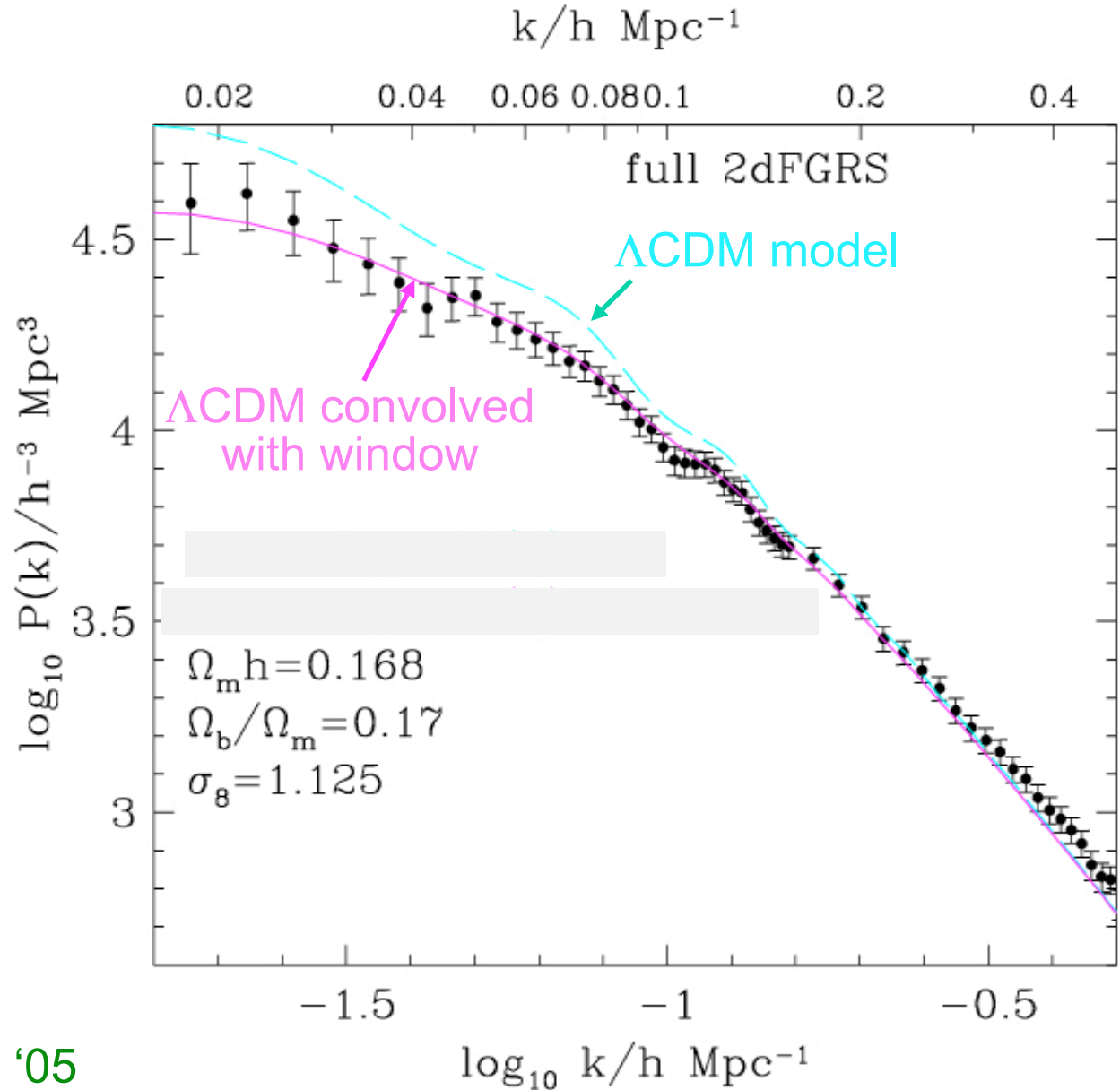
← Real

Simulated →



# The final 2dFGRS power spectrum

2dFGRS  $P(k)$   
well fit by  $\Lambda$ CDM  
model convolved  
with window  
function



Cole, Percival, Peacock,  
Baugh, Frenk + 2dFGRS '05

# The 2dF Galaxy Redshift Survey

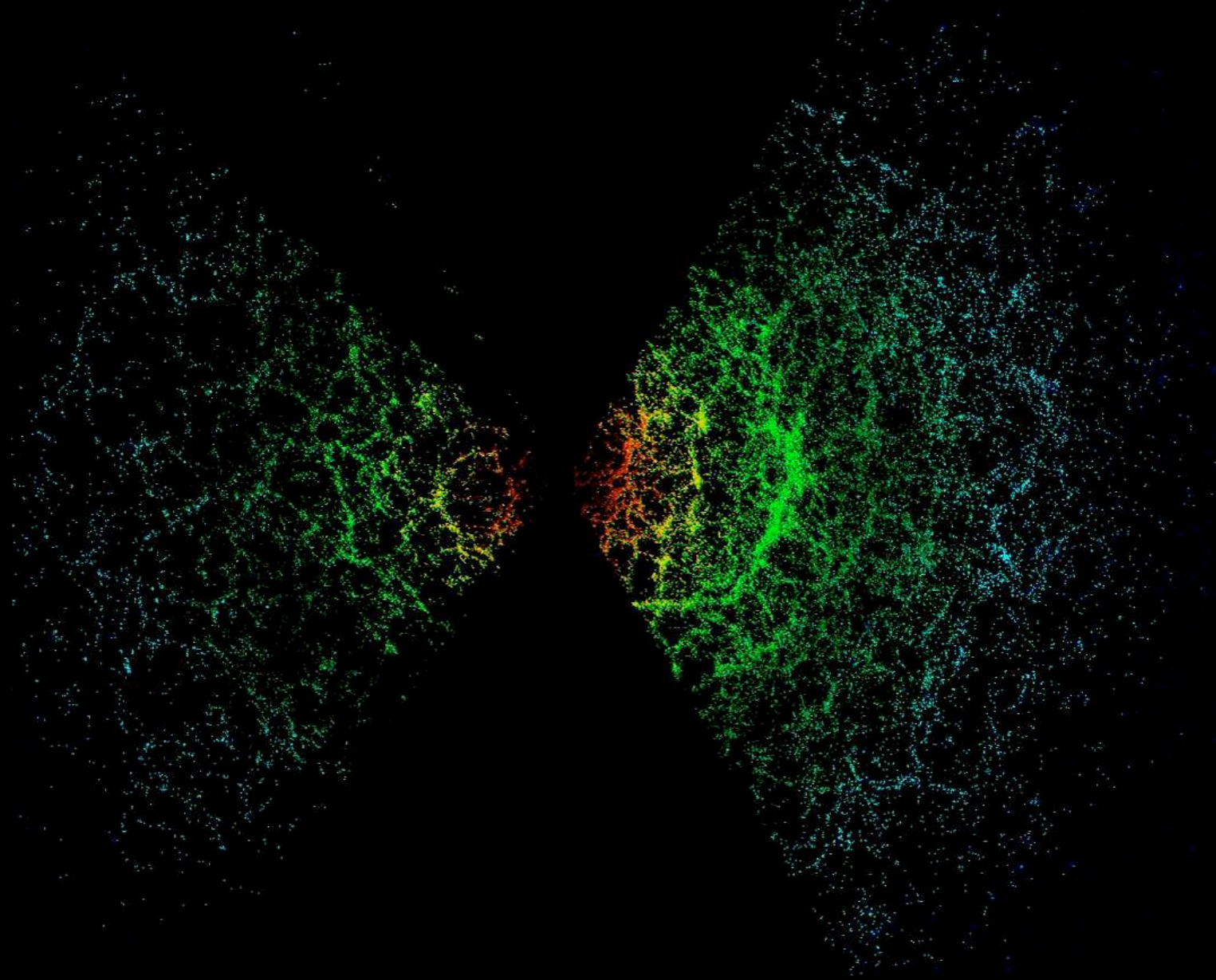
A collaboration between (primarily)  
UK and Australia  
250 nights at the AAT

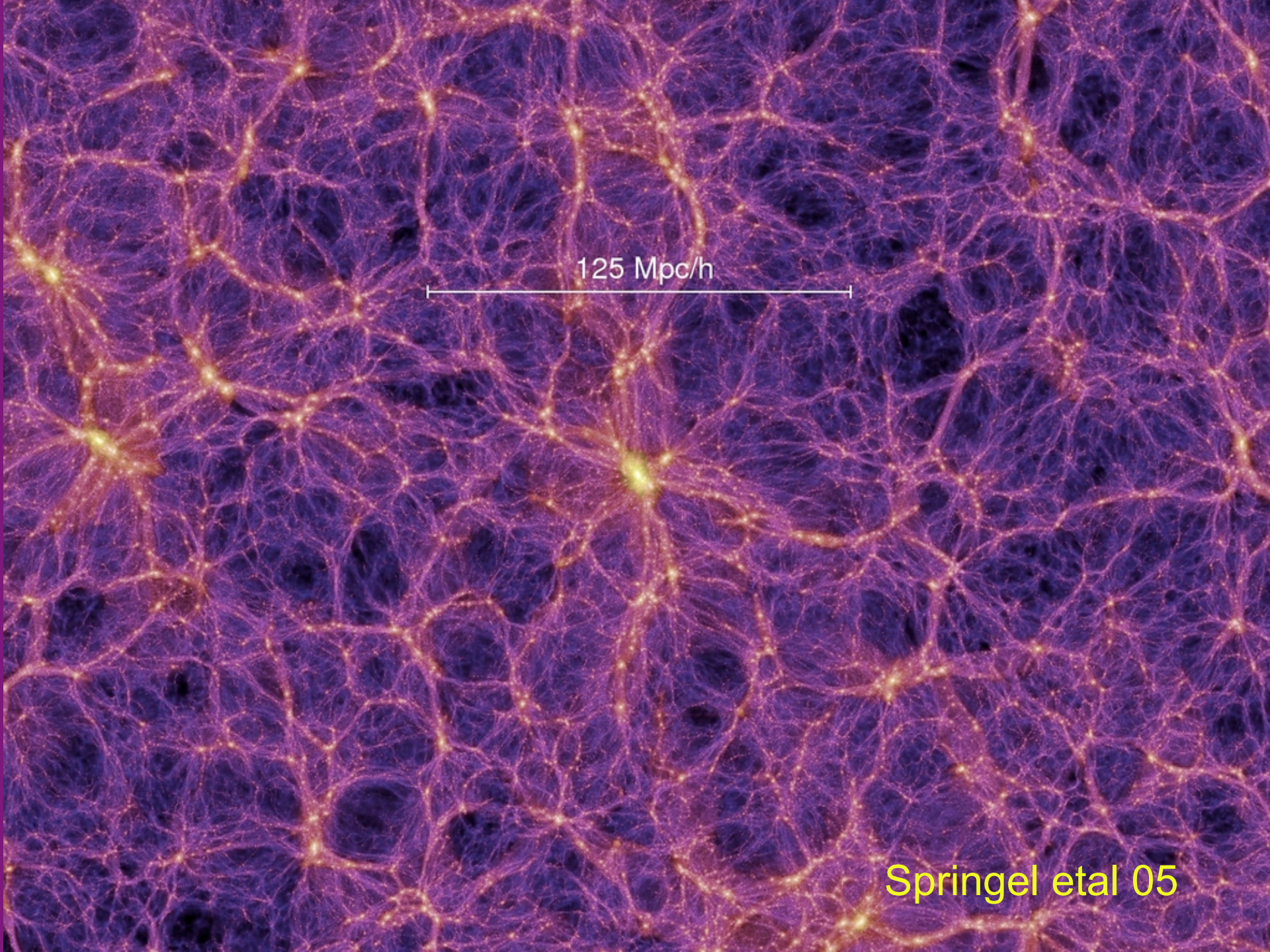
→ 221,000 redshifts  
to  $b_j < 19.45$  median  $z=0.11$

Survey complete and catalogue  
released in July/03



Sloan Digital Sky Survey ~500,000 galaxy redshifts



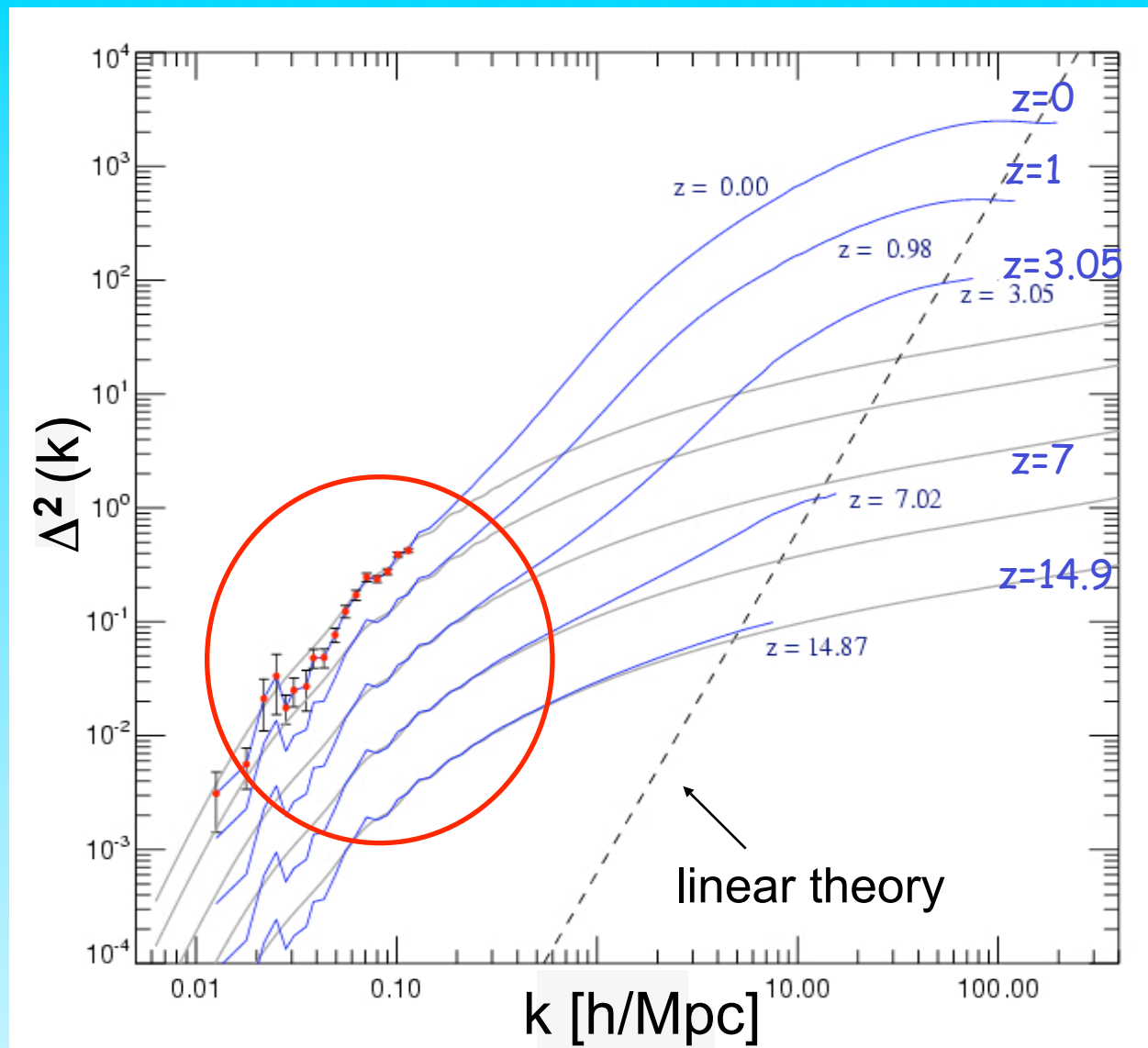


125 Mpc/h

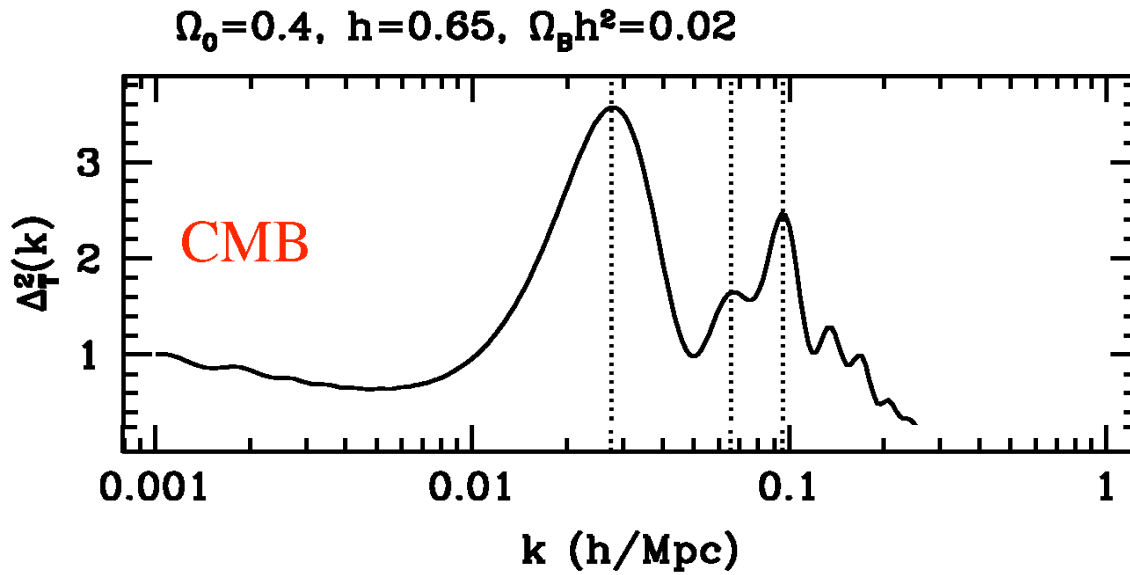
Springel et al 05

# The mass power spectrum

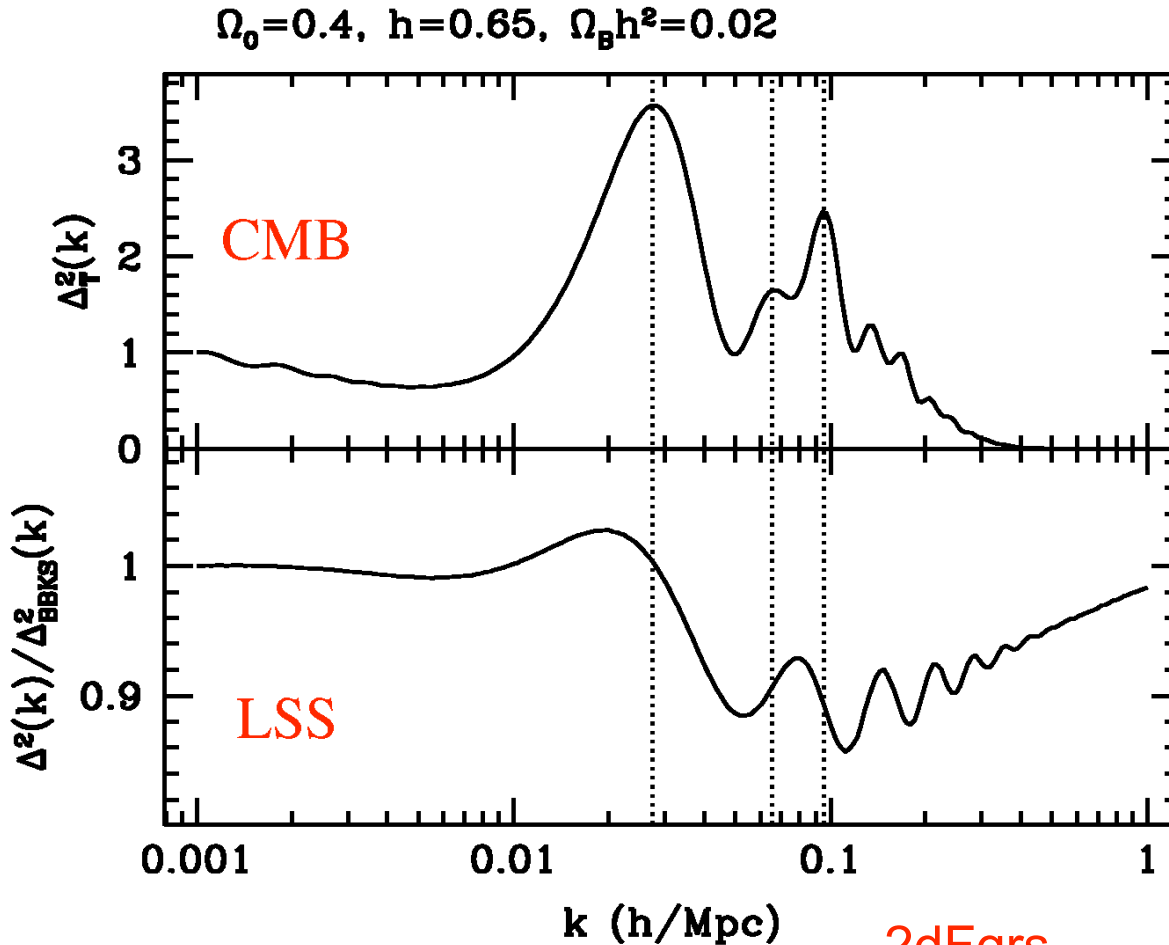
The non-linear mass power spectrum is accurately determined by the Millennium simulation over large range of scales



# CMB anisotropies and large-scale structure



# CMB anistropies and large-scale structure



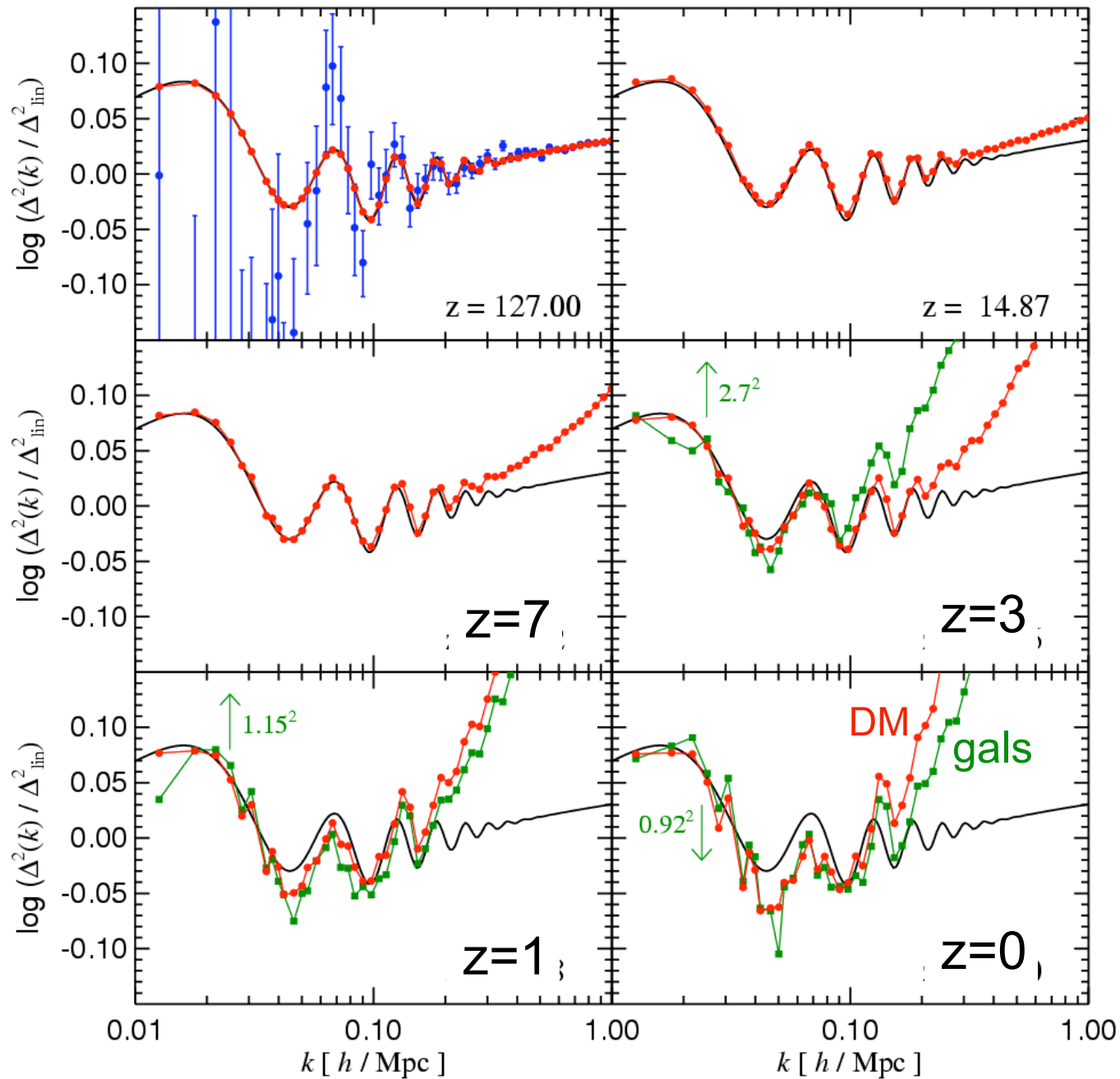
CMB and LSS  
out of phase:

‘velocity overshoot’

LSS amplitude  
smaller than CMB

Meiksin etal 99

# Millennium simulation



Baryon  
wiggles in  
the galaxy  
distribution

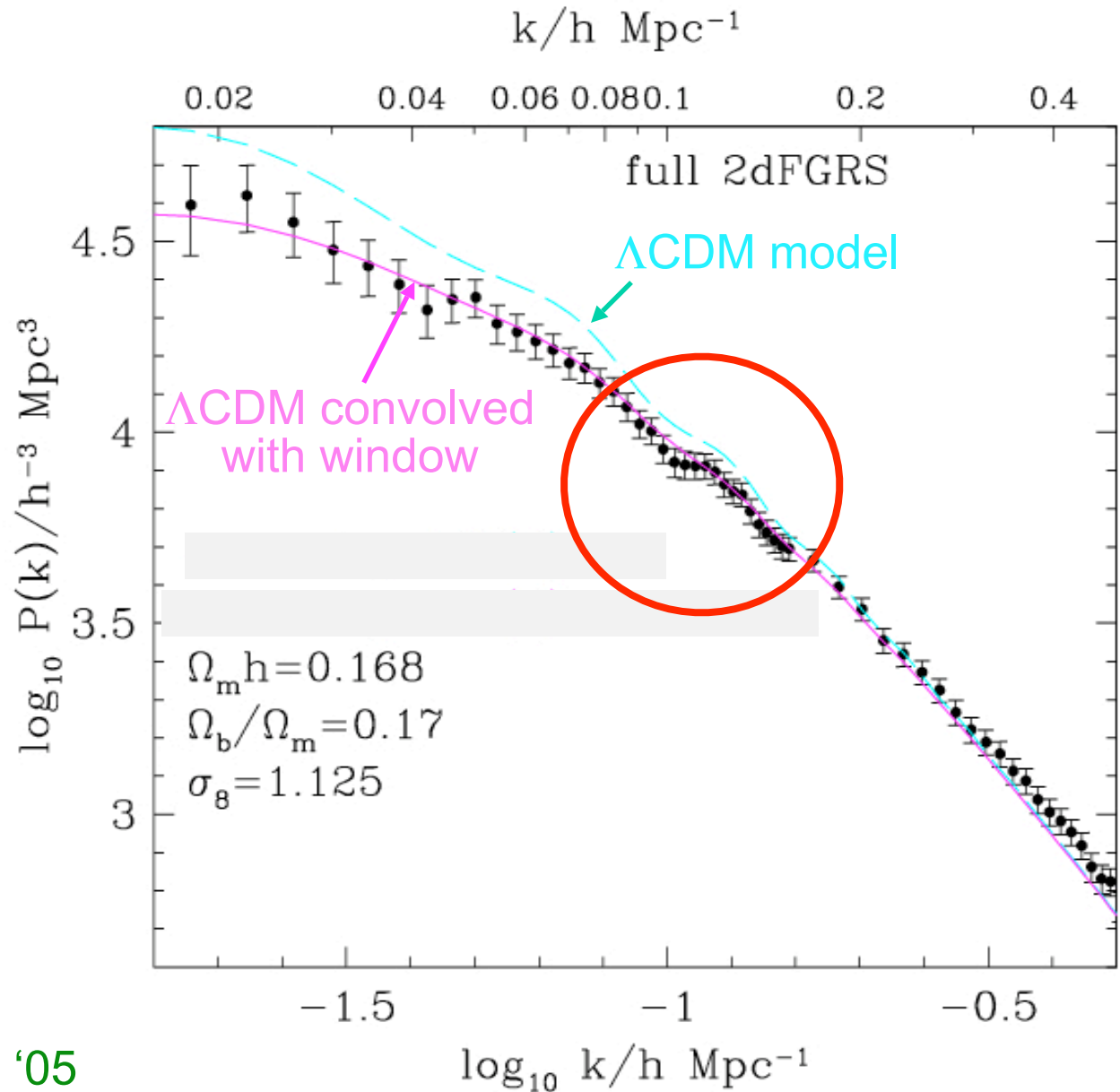
Power spectrum  
from MS divided  
by a baryon-free  
LCDM spectrum

Galaxy samples  
matched to  
plausible large  
observational  
surveys at given  $z$

Springel et al  
2005

# The final 2dFGRS power spectrum

2dFGRS  $P(k)$   
well fit by  $\Lambda$ CDM  
model convolved  
with window  
function



Cole, Percival, Peacock,  
Baugh, Frenk + 2dFGRS '05

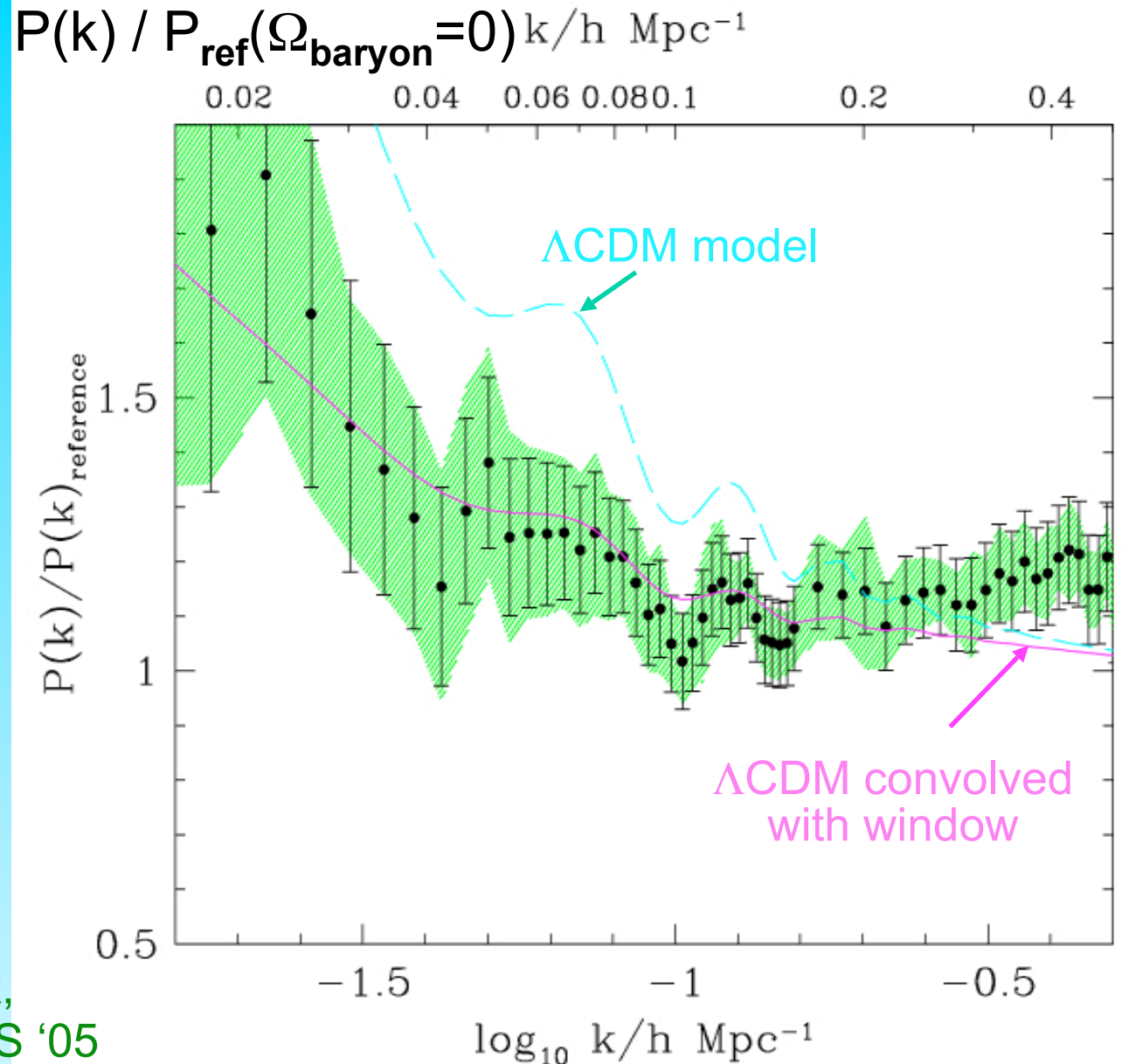
# The final 2dFGRS power spectrum

Baryon oscillations conclusively detected in 2dFGRS!!!

Demonstrates that structure grew by gravitational instability in  $\Lambda$ CDM universe

Also detected in SDSS LRG sample (Eisenstein et al 05)

Cole, Percival, Peacock, Baugh, Frenk + 2dFGRS '05



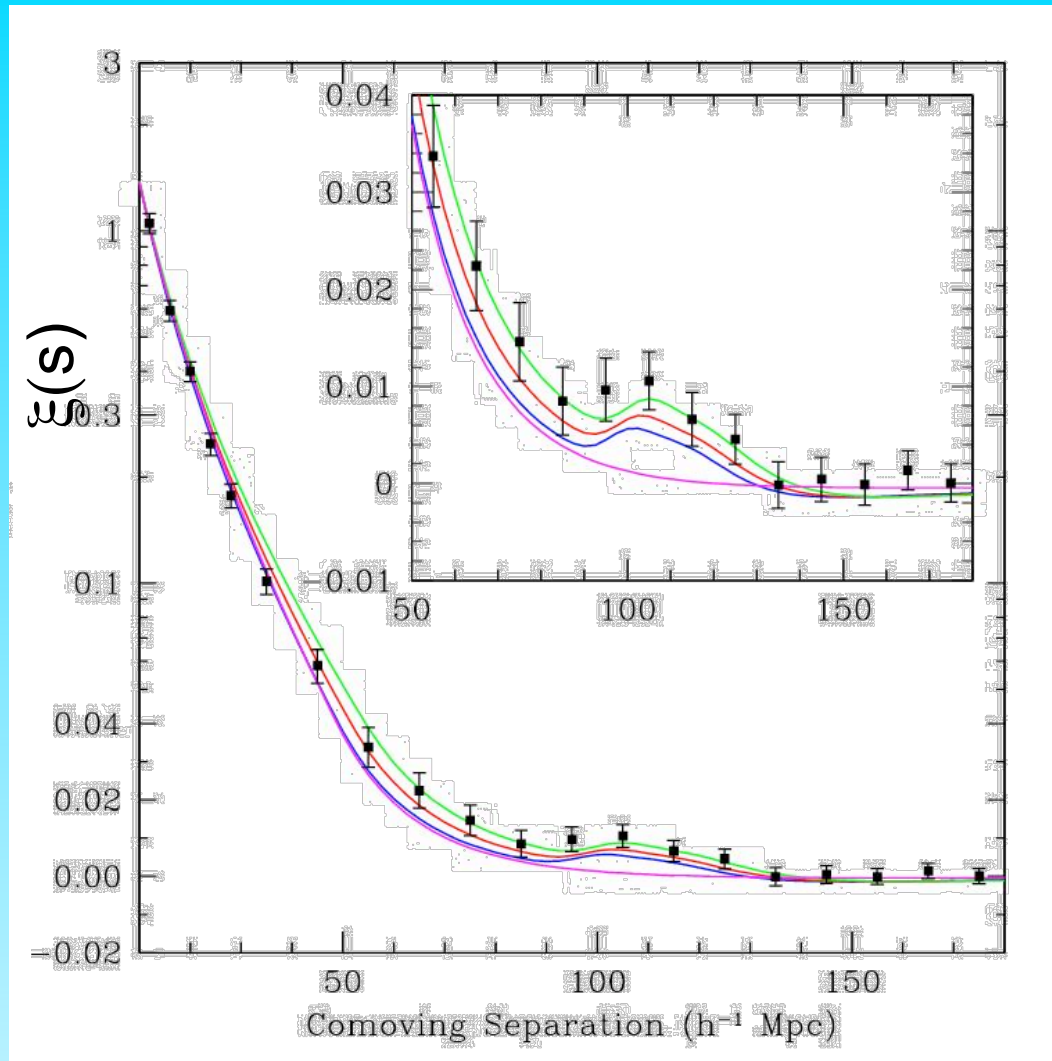


Again, CDM models fit the correlation function adequately well (although peak height is slightly too large; assuming  $n_s=1$ ,  $h=0.72$ )

$$\Omega_b h^2 = 0.024,$$

$$\Omega_m h^2 = 0.133 \pm 0.011,$$

$$\Rightarrow \Omega_b / \Omega_m = 0.18$$



Eisenstein et al. 05

Comoving sound horizon at  $t_{\text{rec}}$   
 (depends mostly on  $\Omega_m h^2$   
 and weakly on  $\Omega_b h^2$ )

$$s = \frac{1}{H_0 \Omega_m^{1/2}} \int_0^{a_r} \frac{c_s}{(a + a_{eq})^{1/2}} da$$

“wavenumber” of acoustic oscillations:

$$k_A = 2\pi/s$$

Comoving distance/redshift:  
 (depends on  $\Omega_m h^2$  and  $w$ )

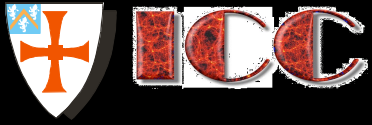
$$\frac{dx}{dz} = \frac{c}{H_0 \Omega_m^{1/2}} \frac{1}{\sqrt{(1+z)^3 + (\Omega_m^{-1} - 1)(1+z)^{3(1+w)}}$$

Apparent size of standard ruler depends on cosmology  
 $\Rightarrow$  dark energy eqn of state  $w$

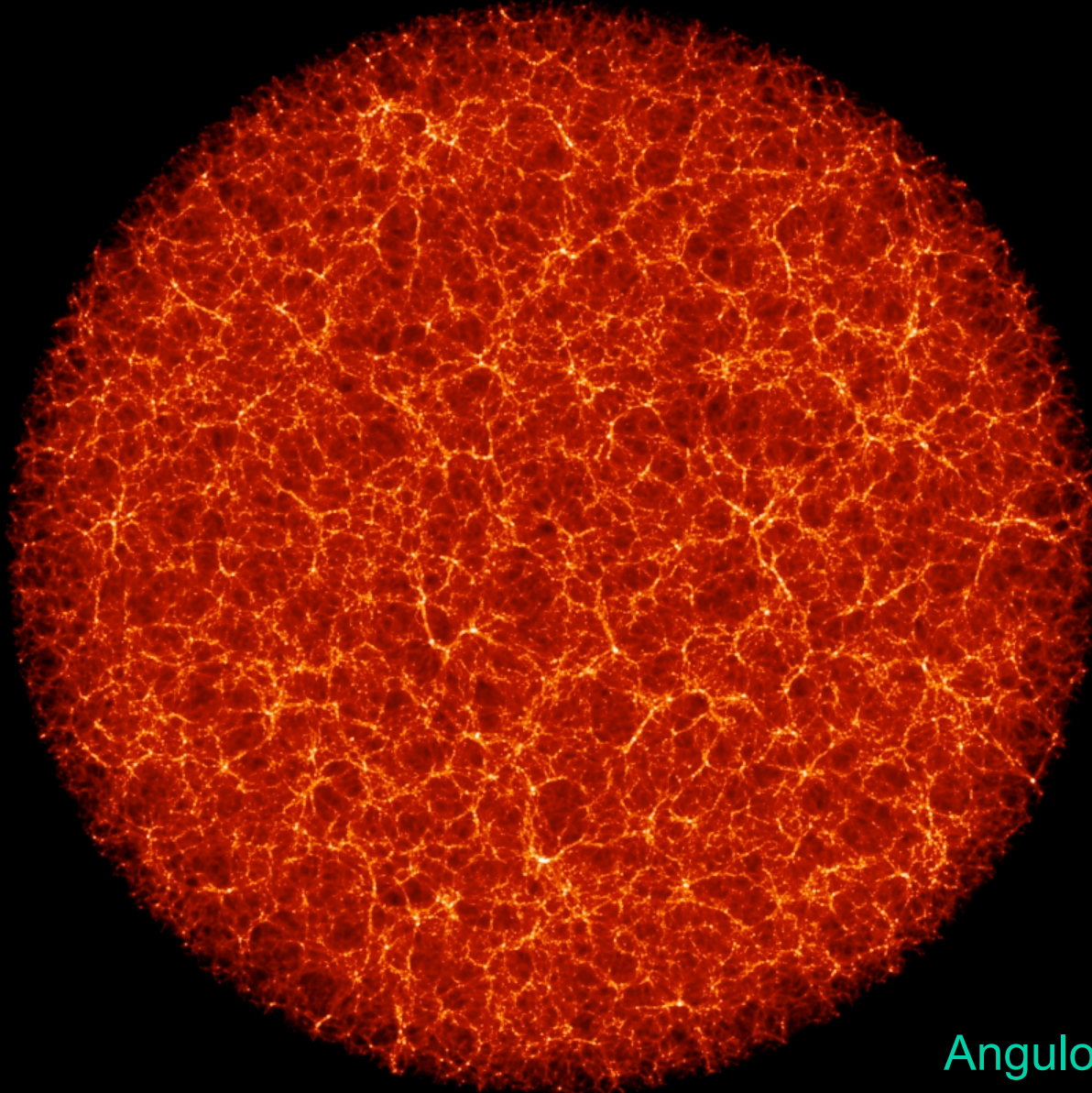
(e.g. Eisenstein & HU 1998; Blake & Glazebrook 2003, 2005;  
 Seo & Eisenstein 2003; 2005.....)

What are the **prospects** for determining  $k_A$  in **realistic surveys**?

What is the **optimal** strategy?



# N-body simulations of large cosmological volumes



**BASICC**

$L=1340/h$  Mpc

$N=3,036,027,392$

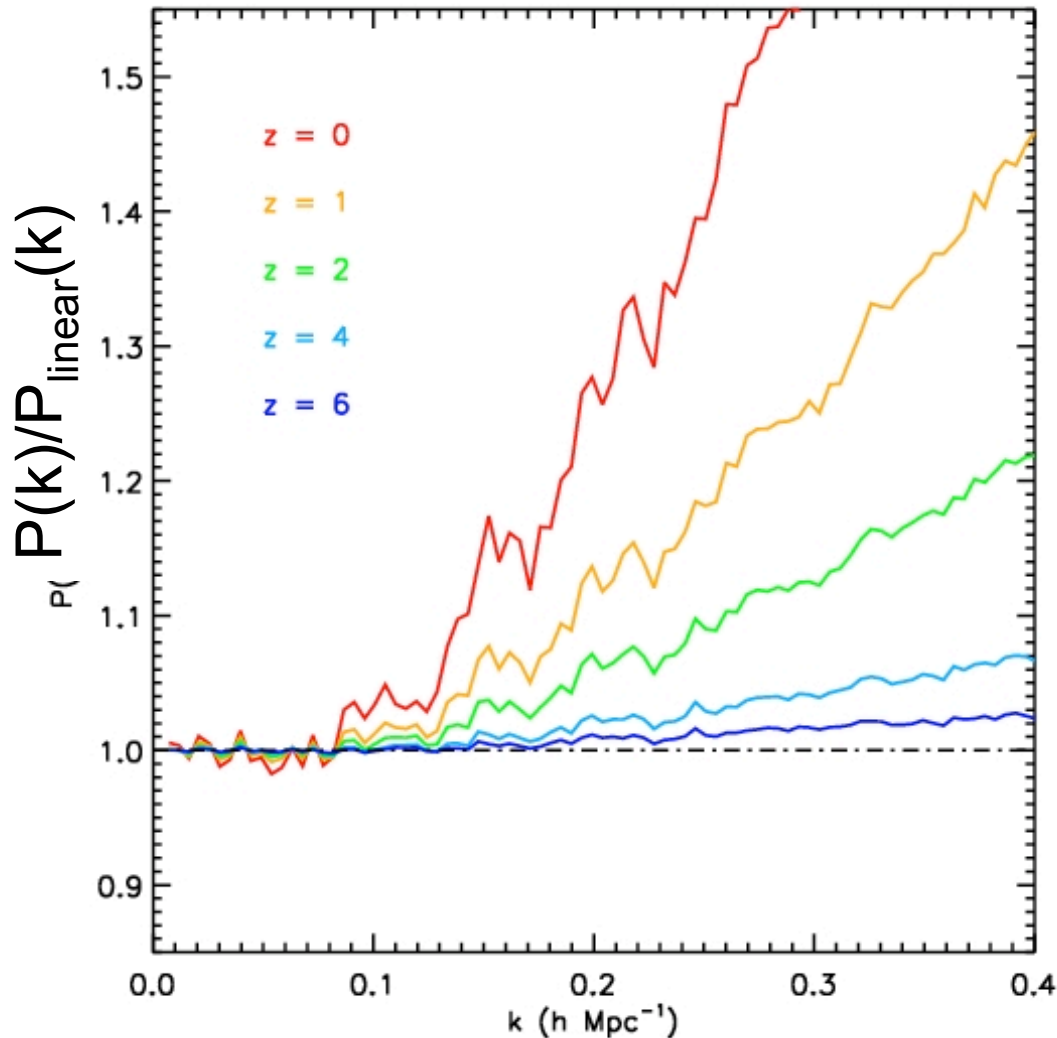
20 times the Millennium volume

Halo resolution:  
(10 particle limit)  
 $5.5 e+11/h$  Mpc

130,000 cpu hours on  
the Cosmology Machine

Angulo, Baugh, Frenk & Lacey '07

# Non-linear evolution of matter fluctuations

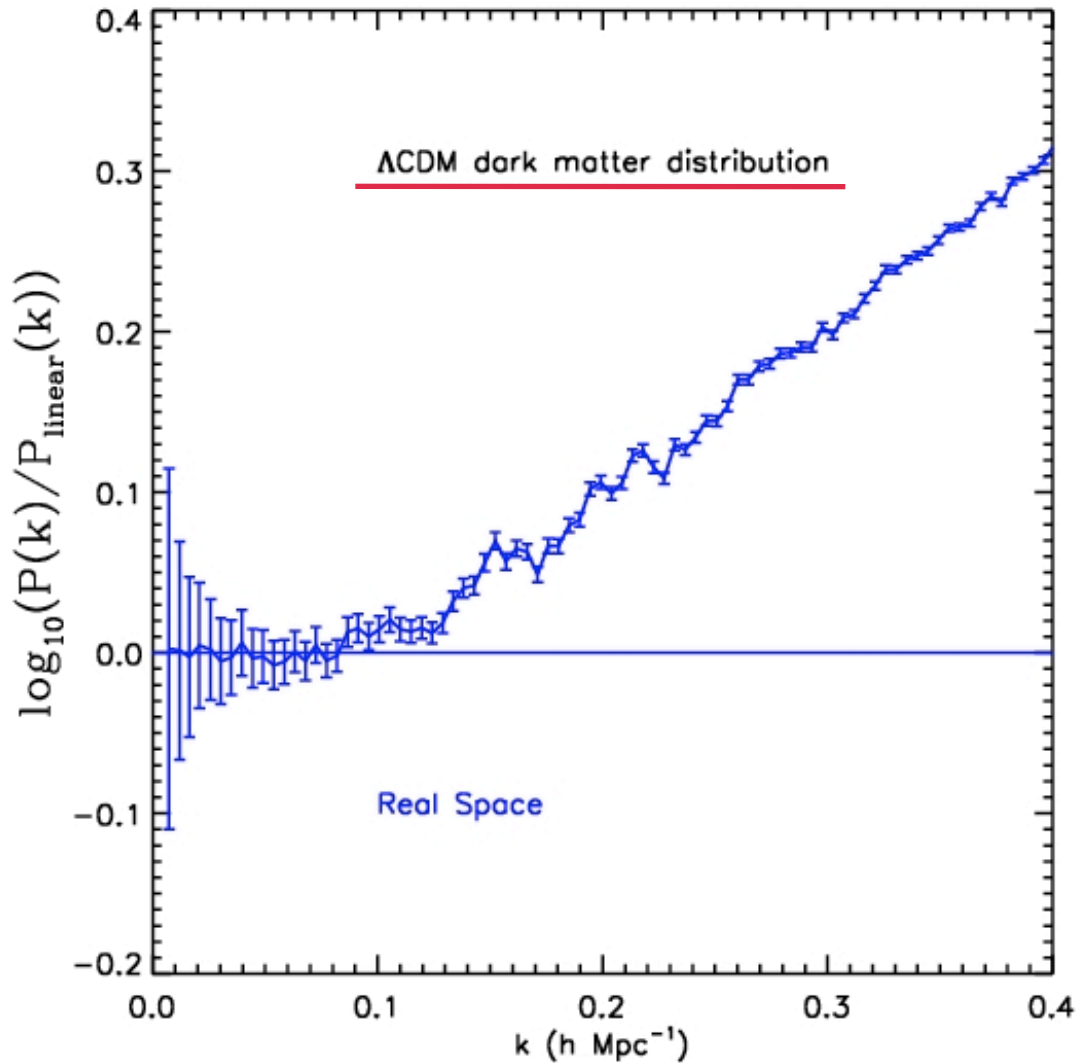


**BASICC simulation**  
**dark matter real space**

$P(k)$  divided  
by linear theory  $P(k)$ ,  
scaling out growth factor

Angulo, Baugh, Frenk &  
Lacey '07

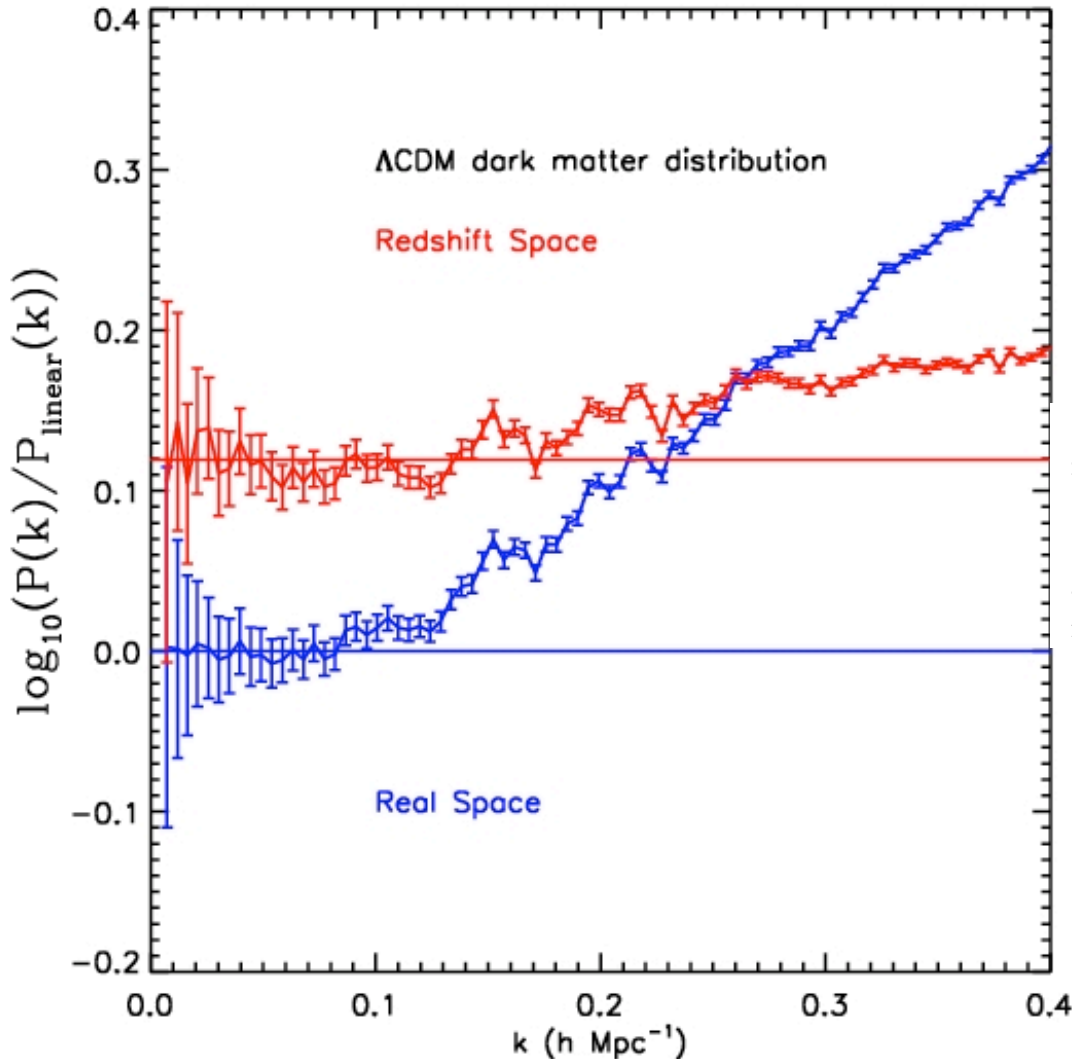
# Non-linear evolution of matter fluctuations



$\text{Log } (P(k)/P_{\text{linear}}(k))$   
at  $z=1$

Angulo, Baugh, Frenk &  
Lacey '07

# Redshift space distortions



Peculiar motions distort clustering pattern

Coherent bulk flows boost large scale power (Kaiser 1987)

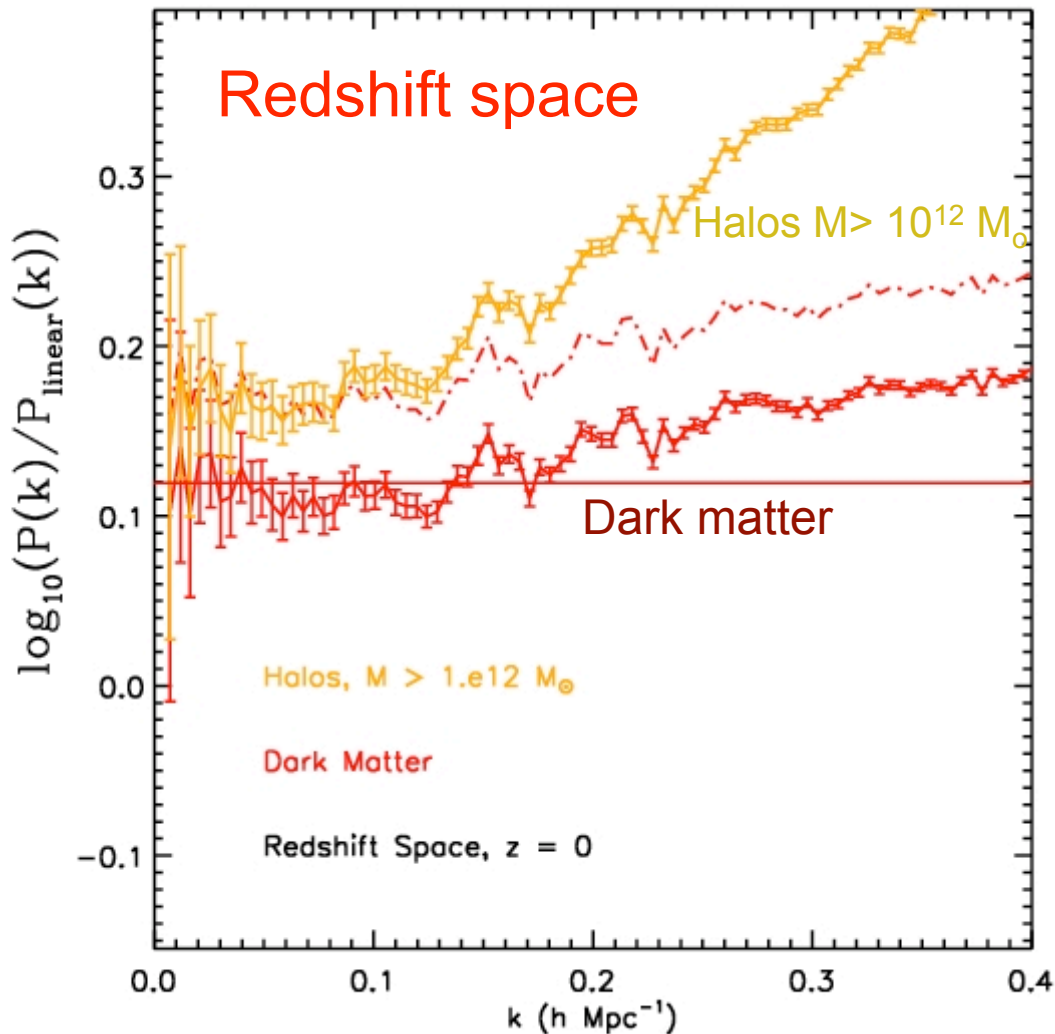
Kaiser (1987) related the spherically averaged power spectrum measured in redshift ( $P_s$ ) and that in real space ( $P$ ):

$$P_s(k) = \left(1 + \frac{2}{3}\beta + \frac{1}{5}\beta^2\right) P(k). \quad (1)$$

where  $\beta(\Omega_m) = d \log \delta / d \log a / b \simeq \Omega_m^{0.6} / b$  and  $b$  is the bias factor.

Motions of particles inside virialised structures damp power at high  $k$

# Redshift space distortions



Peculiar motions distort clustering pattern

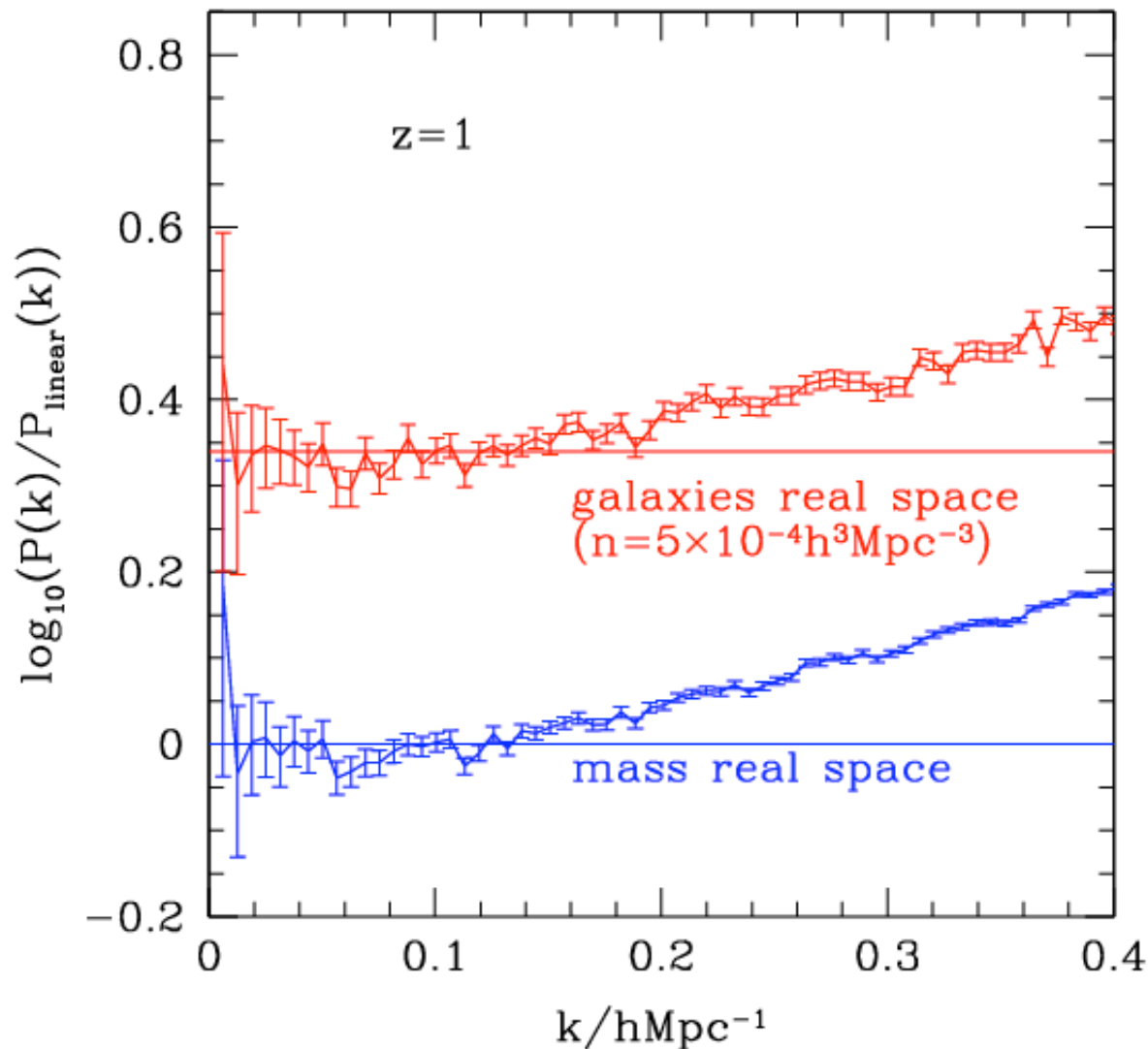
Boost in power on large scales due to coherent flows

Damping at higher  $k$  affects DM but not the halos

In  $z$ -space, halo bias is scale-dependent



# Galaxy bias in real space

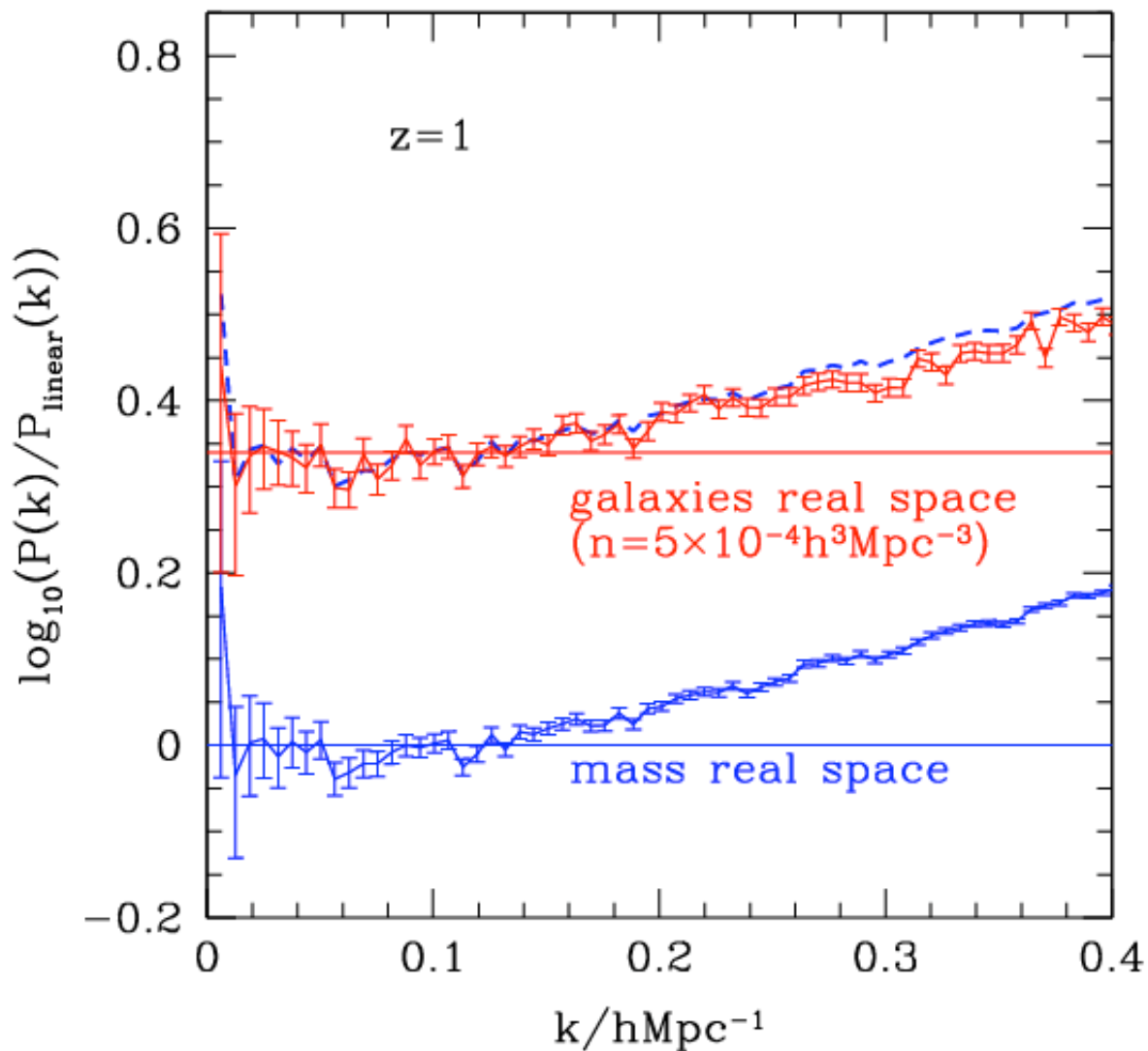


Magnitude limited sample.

Galaxy clustering boosted relative to mass in real space

Angulo, Baugh, Frenk & Lacey '07

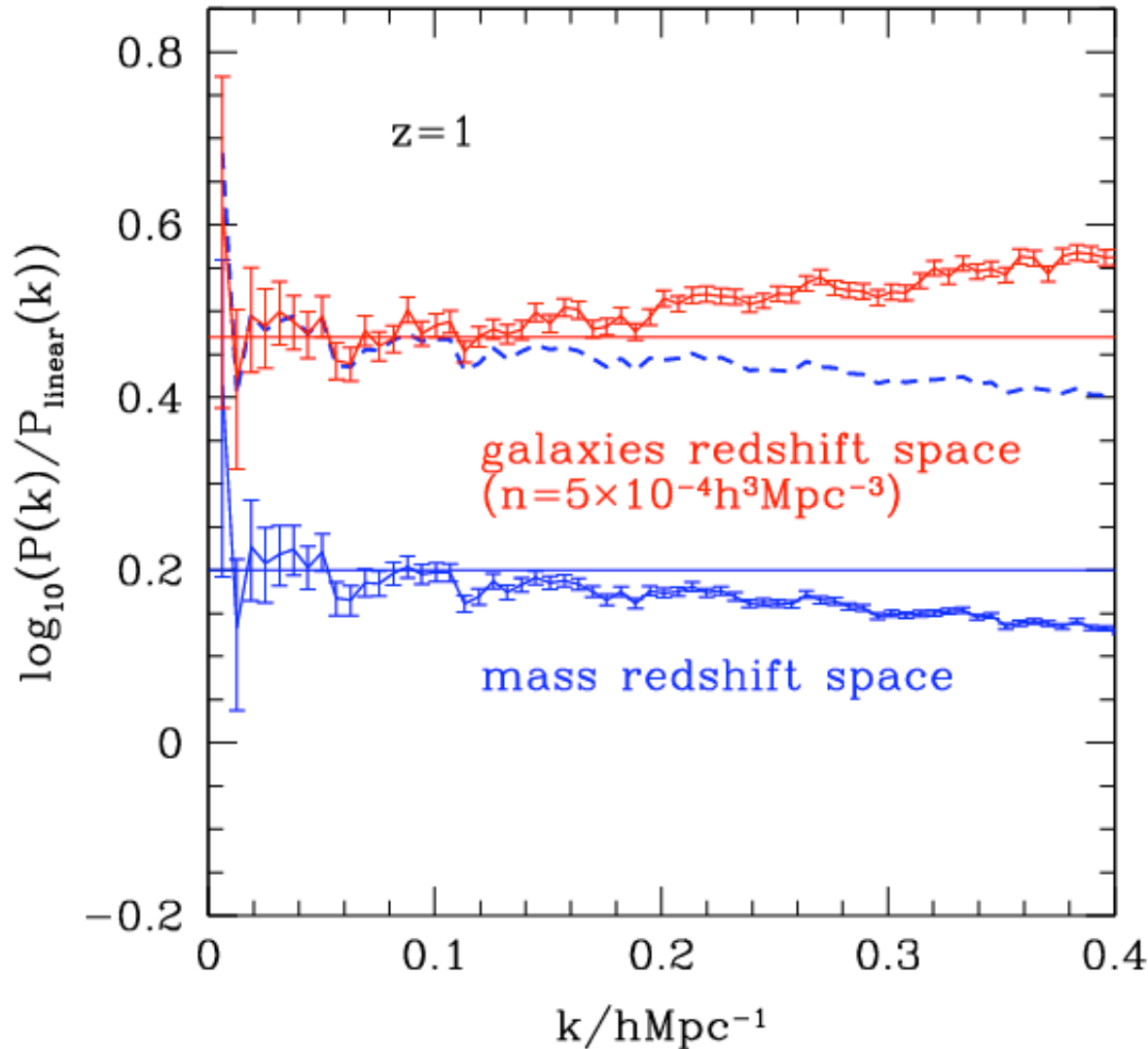
# Galaxy bias in real space



Boost in clustering approximates to a constant bias factor on large scales.

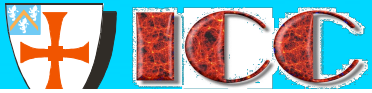
Angulo, Baugh, Frenk & Lacey '07

# Galaxy bias in redshift space

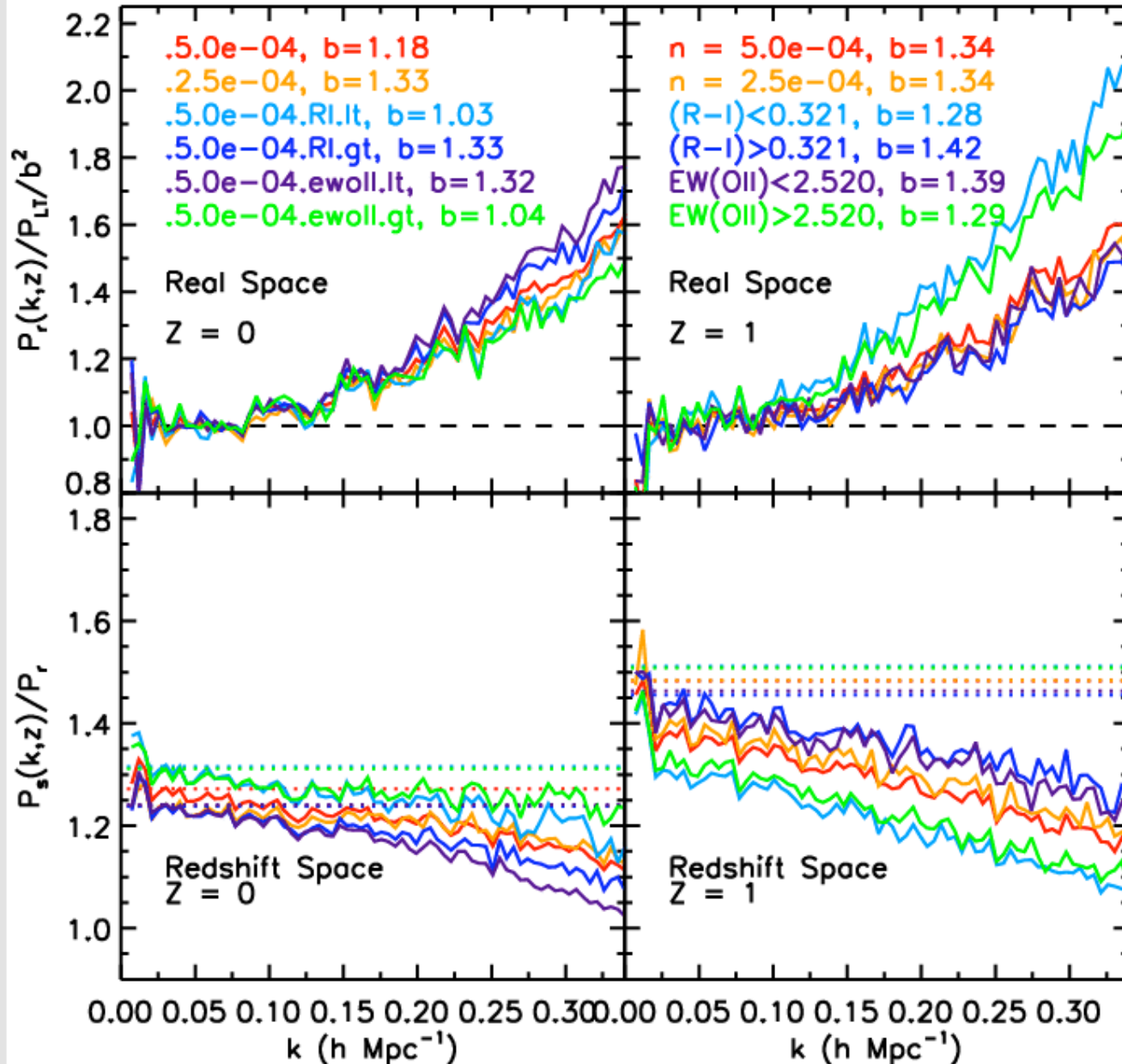


Galaxy  $P(k)$  cannot be reproduced by multiplying mass  $P(k)$  by constant factor in redshift space.

⇒ In  $z$ -space, galaxies have a **scale-dependent bias** out to  $k \sim 0.1$



# Galaxy bias in redshift space

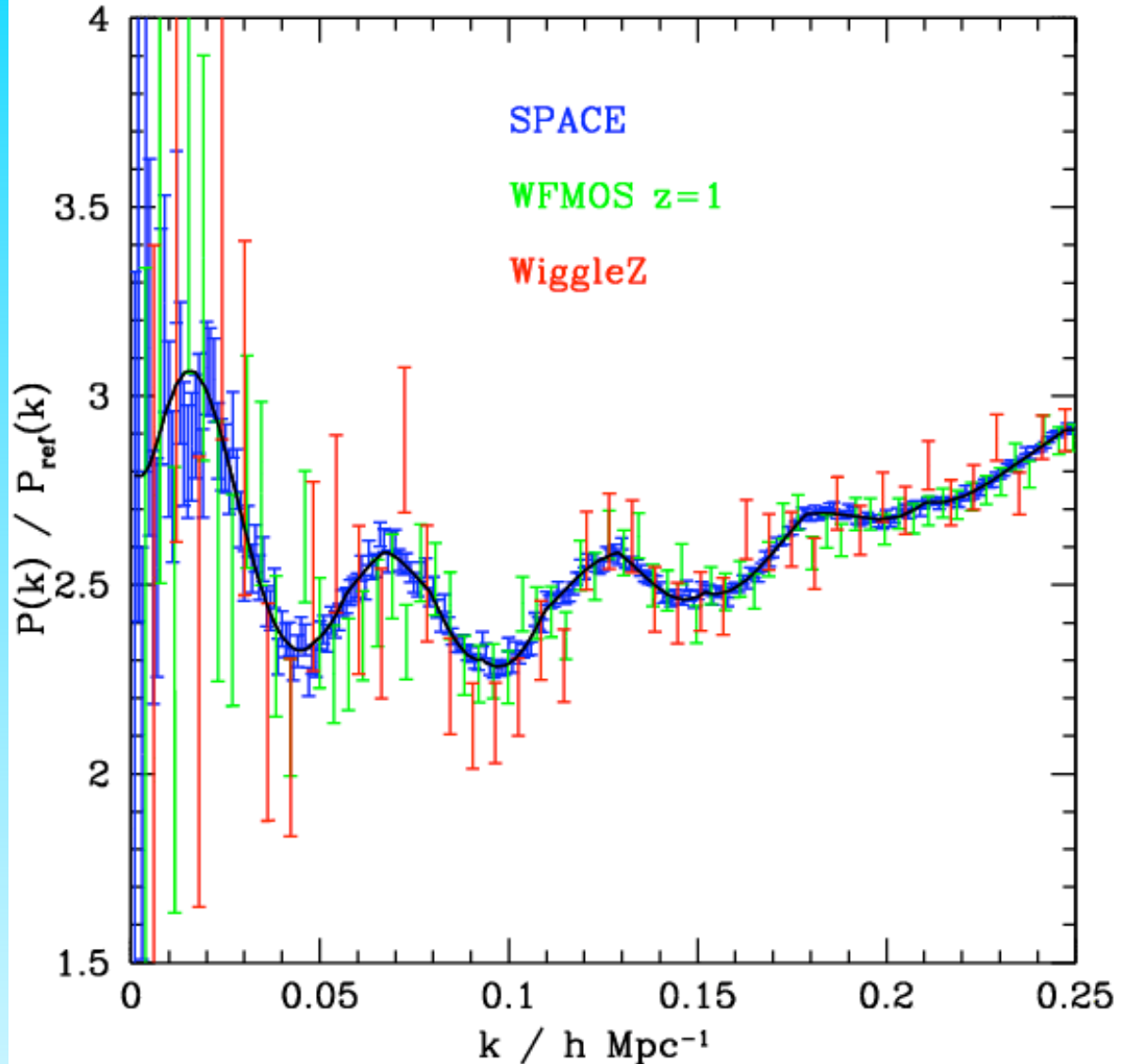


Comparison of different selections e.g. colour, emission line strength

Angulo et al '07

# Projected BAO data for planned surveys at $z=1$

Projections based on mock catalogues made from large N-body simulation plus semi-analytic galaxy formation model

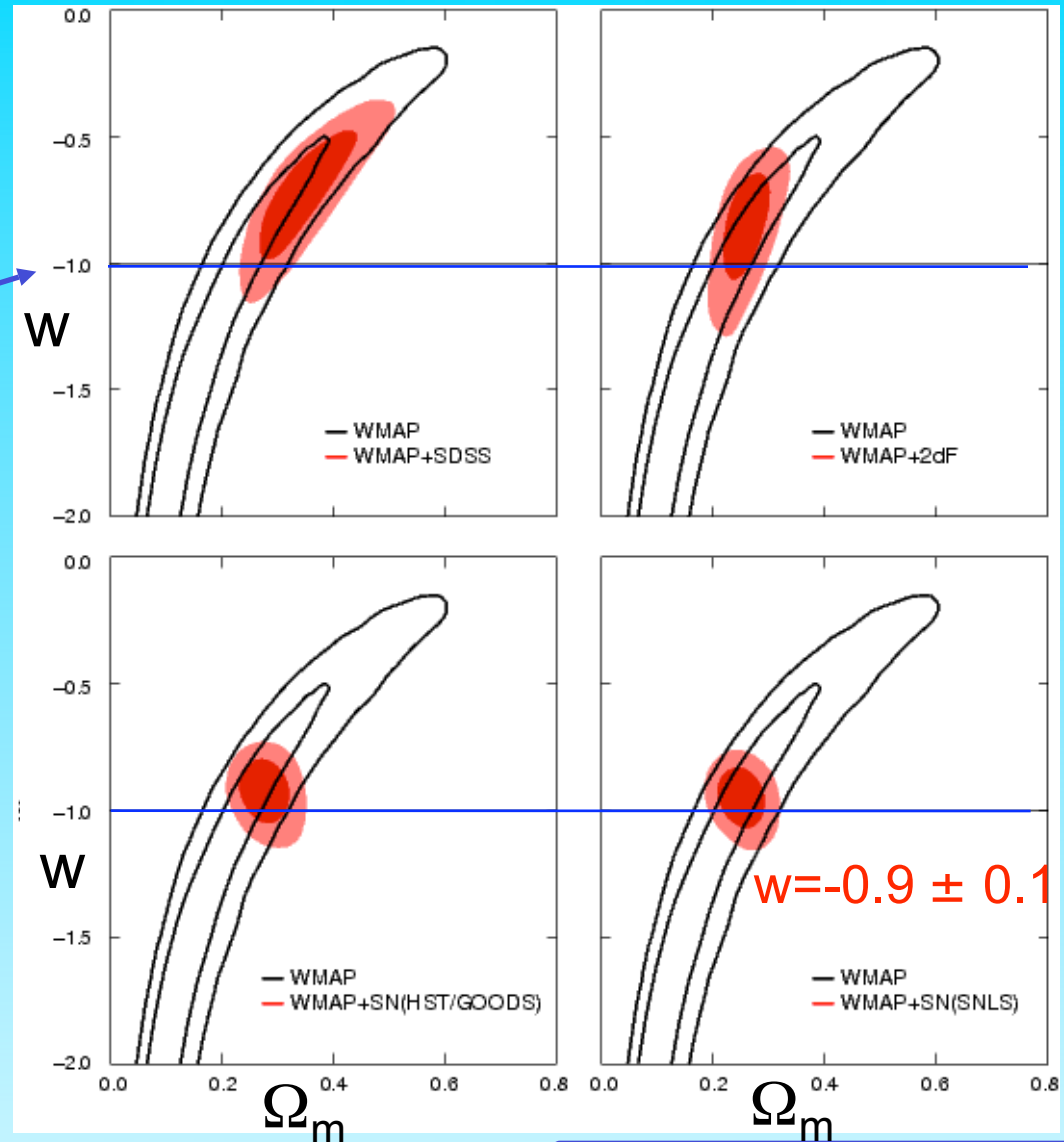


# Constraints on $w$ from S<sub>nl</sub>a, WMAP and 2dFGRS

$$p = w\rho c^2$$

Cosmological constant

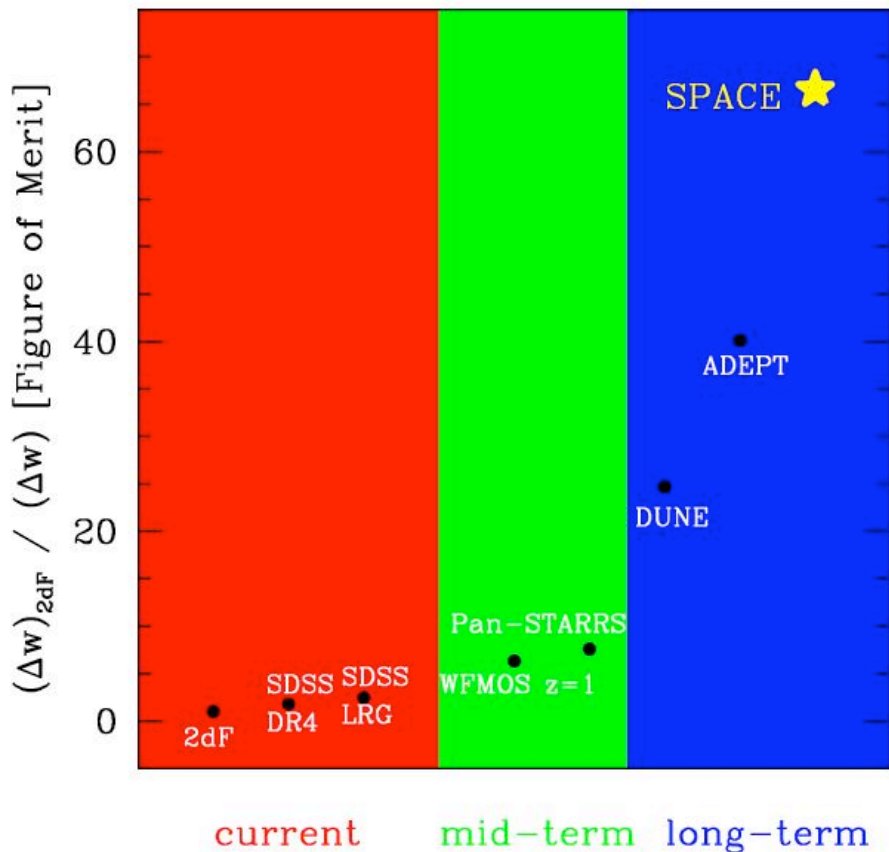
Assume  $w = \text{const}$   
(cosmological constant)



Spergel et al 2006

# Headline forecasts for $w$

BAO performance for constant  $w$



Survey	Error in $w$
WiggleZ	5.0 - 9.5 %
WFMOS	3.6 - 4.0 %
Pan-STARRS 0.03 photo-z 0.06 photo-z	1.6 - 3.5 % 2.2 - 4.9 %
DUNE 3% photo-z 20,000 sq deg	1.2 - 2.5%
SPACE $10^9$ galaxies 27,000 sq deg	0.25 - 0.5%

Angulo et al 07

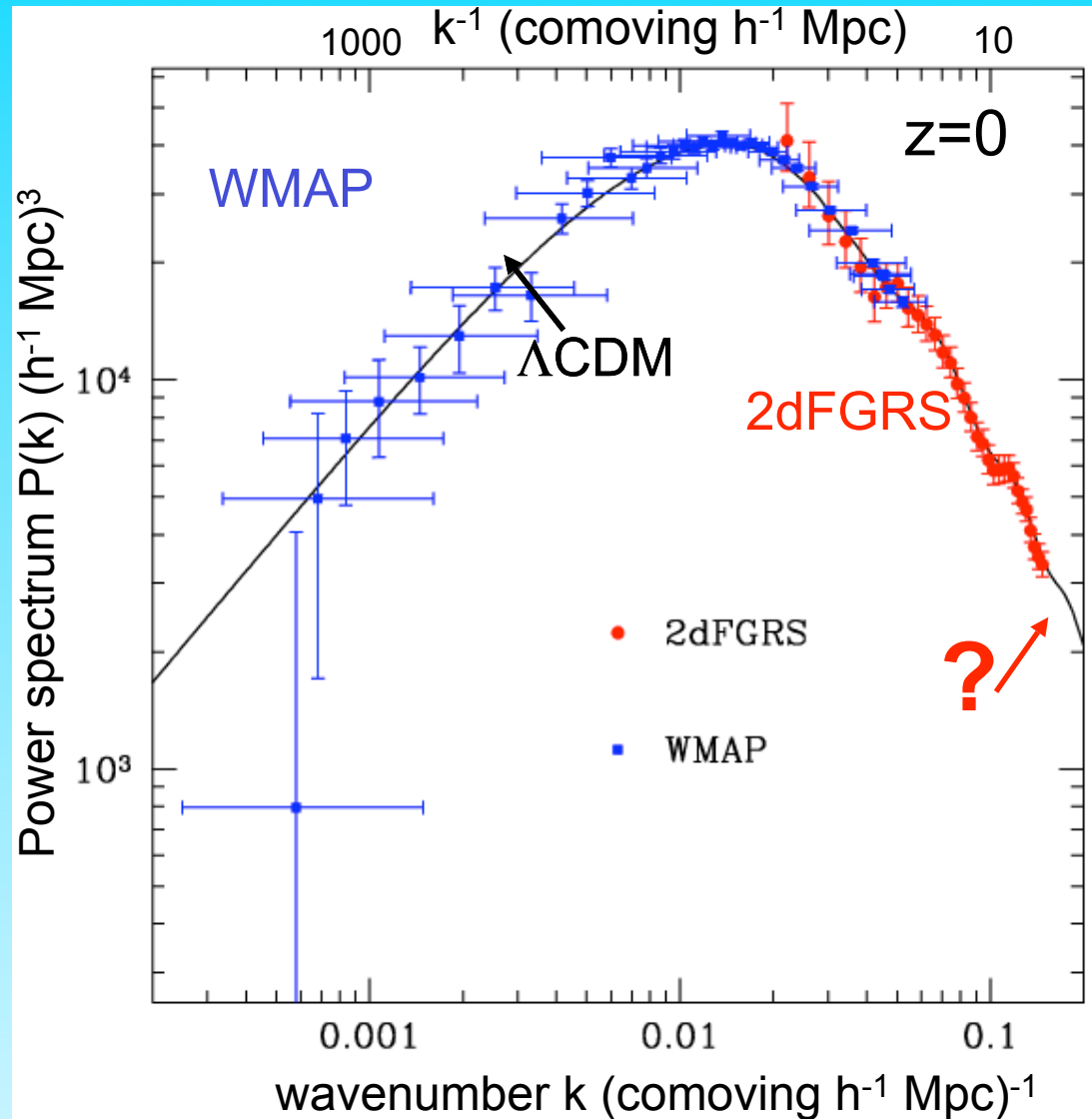
# The cosmic power spectrum: from the CMB to the 2dFGRS

## CMB:

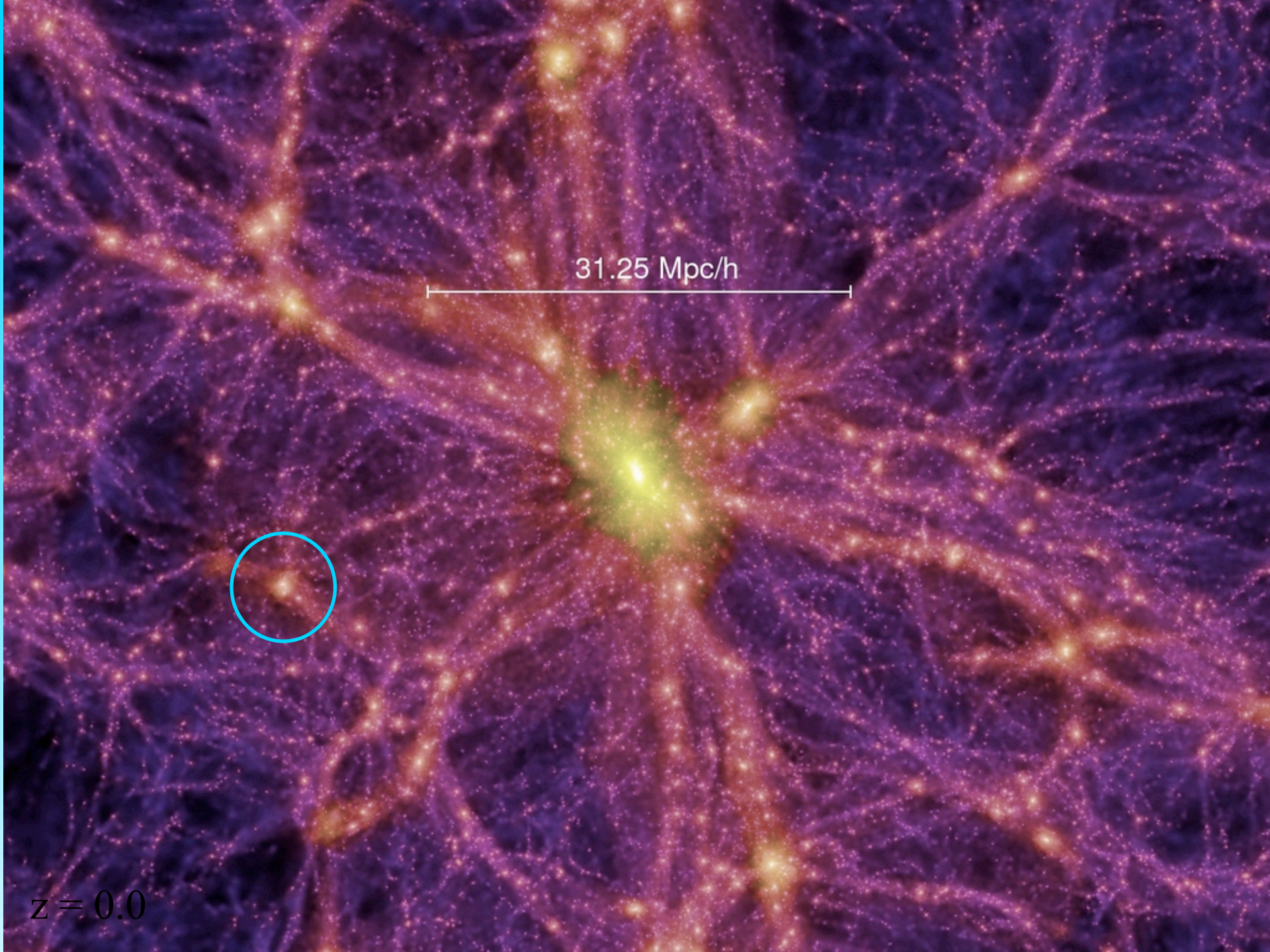
- Convert angular separation to distance (and  $k$ ) assuming flat geometry
- Extrapolate to  $z=0$  using linear theory

⇒  $\Lambda$ CDM provides an excellent description of mass power spectrum from 10-1000 Mpc

Sanchez et al 06





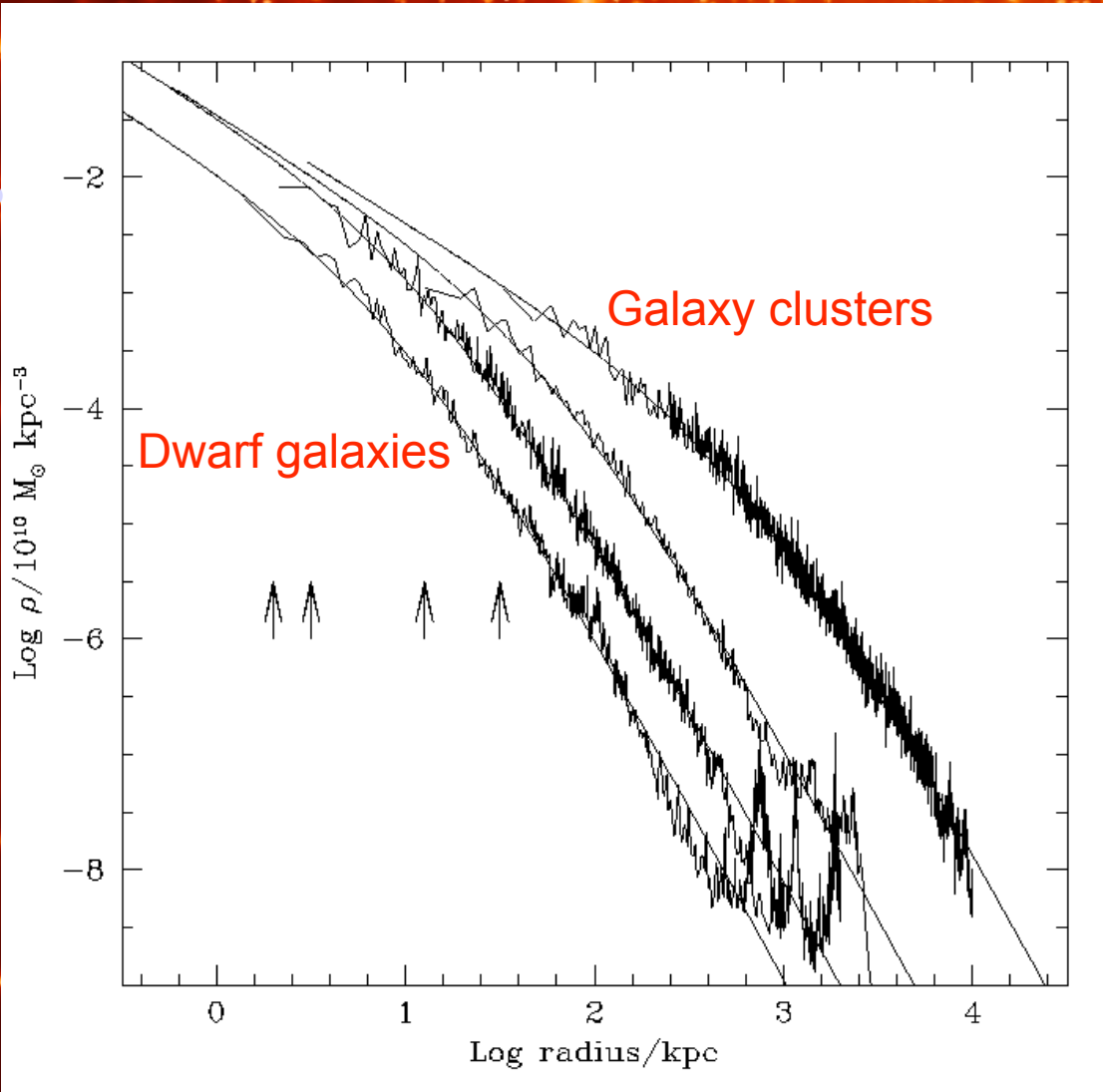


$31.25 \text{ Mpc}/h$

$z = 0.0$

# The Density Profile of Cold Dark Matter Halos

Log density ( $10^{10} M_{\odot} \text{ kpc}^{-3}$ )



Log radius (kpc)

Halo density profiles are independent of halo mass & cosmological parameters

There is no obvious density plateau or 'core' near the centre.

(Navarro, Frenk & White '97)

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

# A cold dark matter universe

N-body simulations show that cold dark matter halos (from galaxies to clusters) have:

- “Cuspy” density profiles
- Large number of self-bound substructures (**10% of mass**)

This has led to two well-publicized “problems”:

- The “halo core” problem
- The “satellite” problem

## Explanations for the core/satellite "crises"

- The dark matter is warm
- The dark matter has a finite self-scattering cross-section
- The primordial density power spectrum has a break (or running spectral index)
- There is no dark matter -- gravity needs modifying
- Astrophysics: baryon effects, black holes, bars
- The comparison of models and data is incorrect



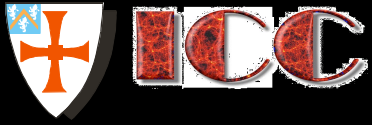
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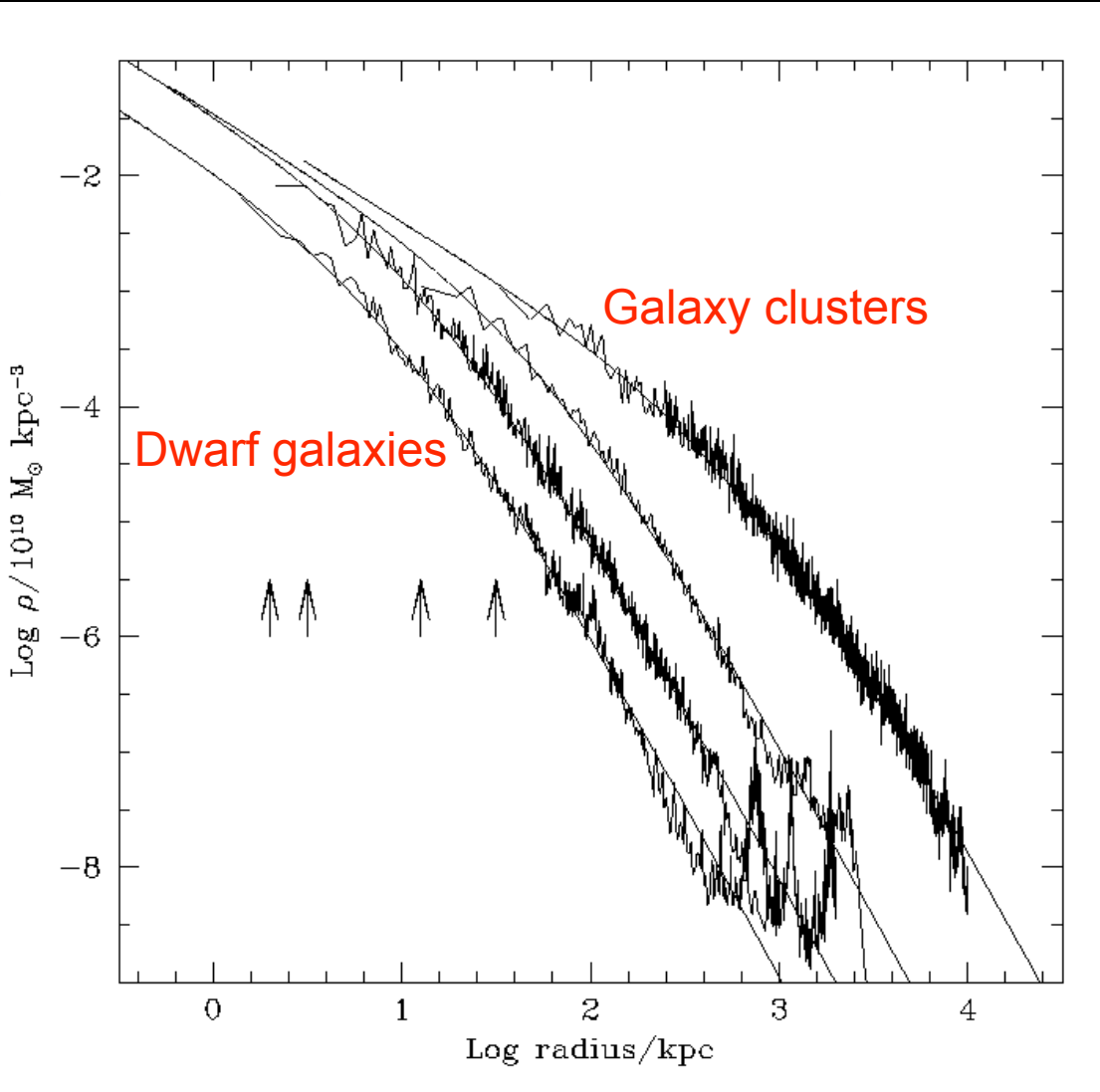
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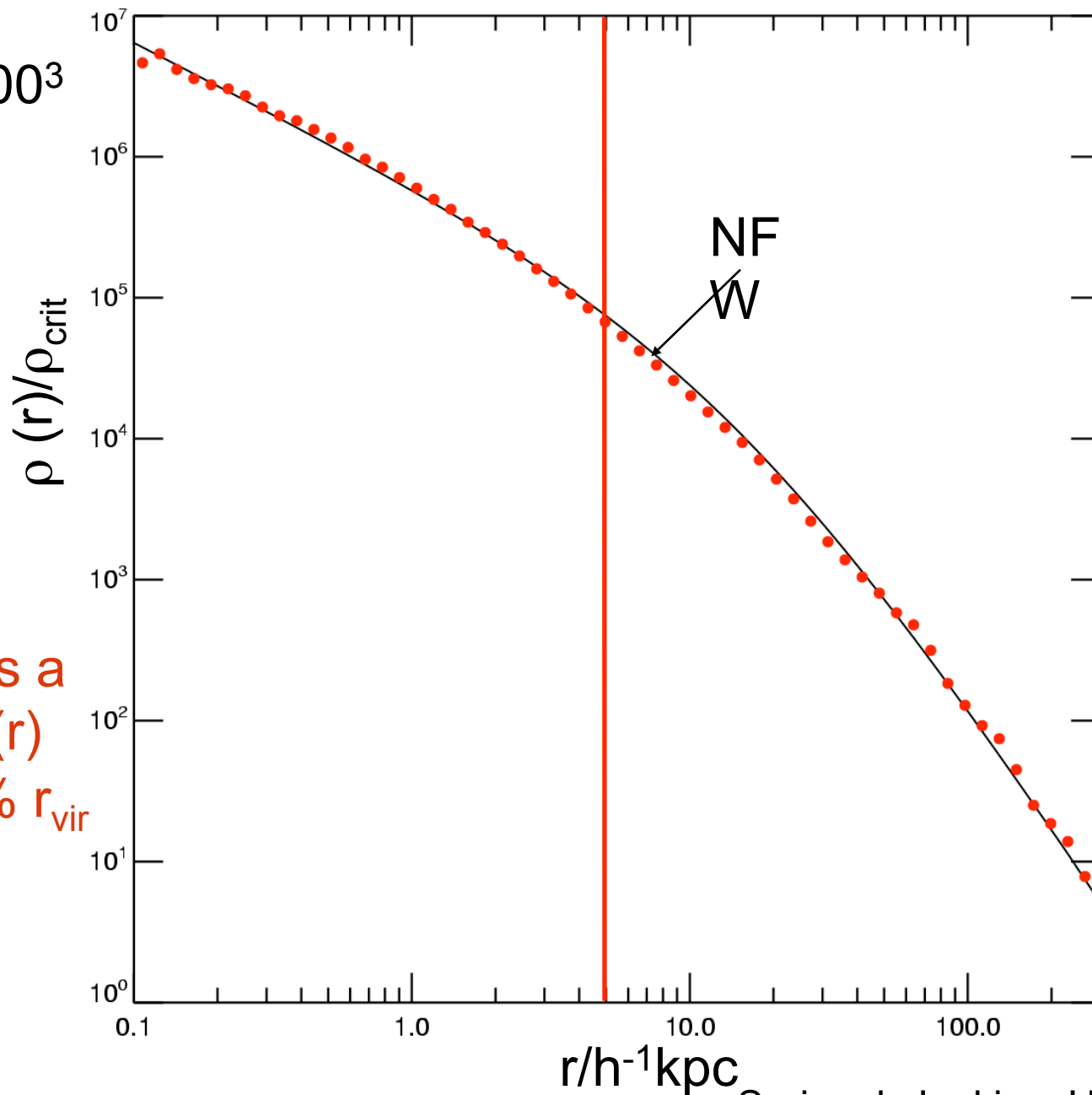
# A galactic dark matter halo



60 million particles inside  $r_{\text{vir}}$

Springel, Jenkins, Helmi,  
Navarro, Frenk & White '07

$N=800^3$



NFW profile is a  
good fit to  $\rho(r)$   
down to  $\sim 0.1\%$   $r_{\text{vir}}$

Springel, Jenkins, Helmi,  
Navarro, Frenk & White '06



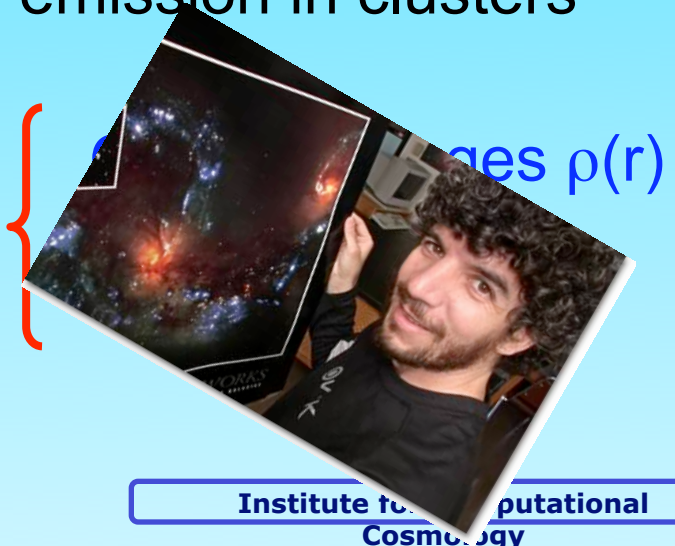
# The density profile of galaxy cluster dark halos

Do real dark halos have the profiles found in the simulations?

Profiles can be probed by:

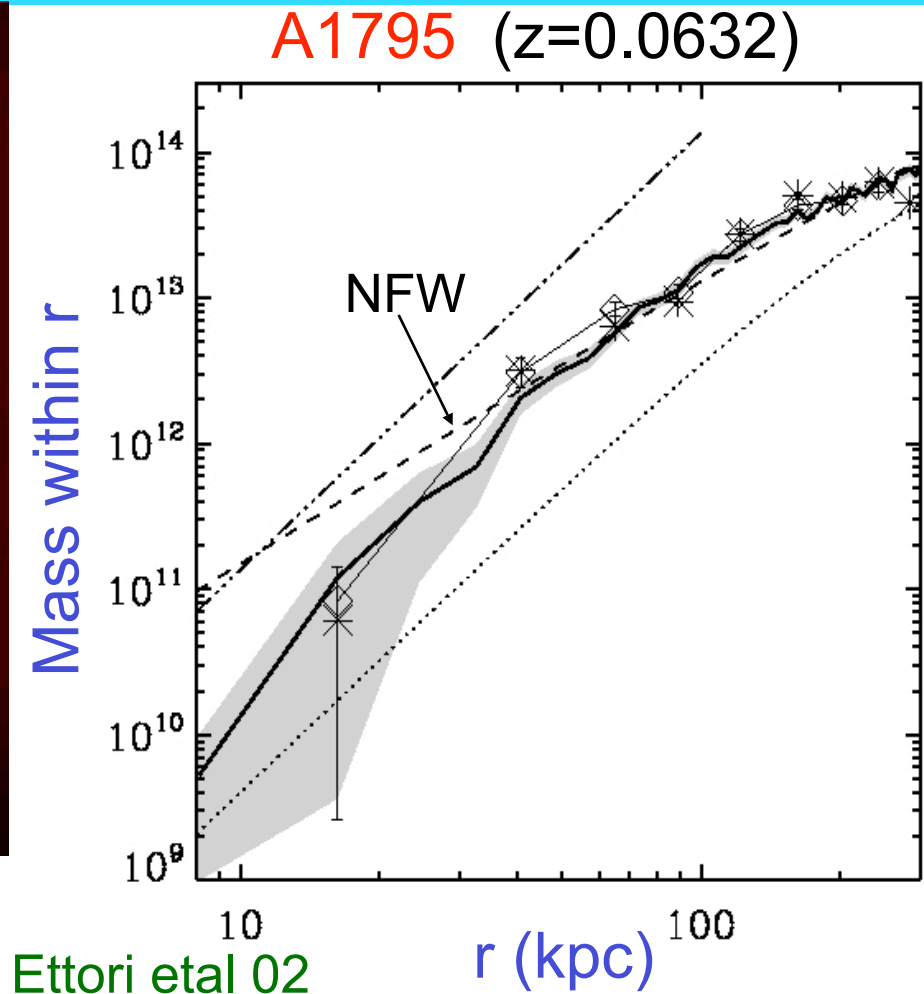
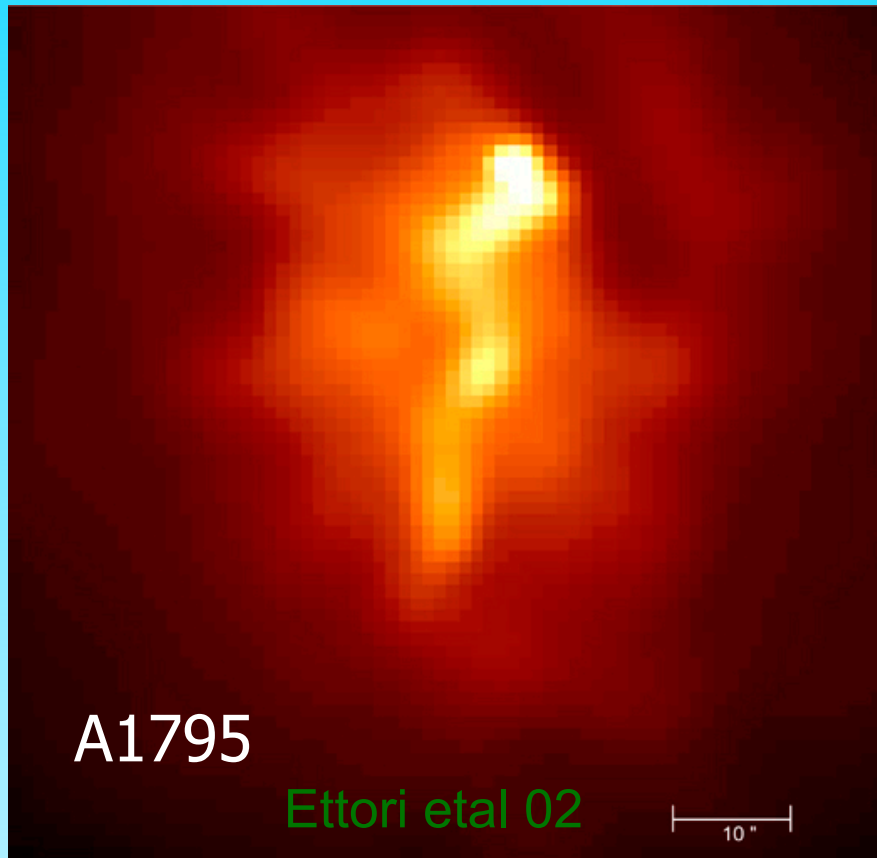
- Gravitational lensing and/or X-ray emission in clusters

- Galaxy rotation curves → messy



# The central density profile of galaxy cluster dark halos

Inner DM density profile inferred from X-ray data (Chandra)



Profile shallower than  
NFW ( $\beta = 0.59 \pm 0.15$ )

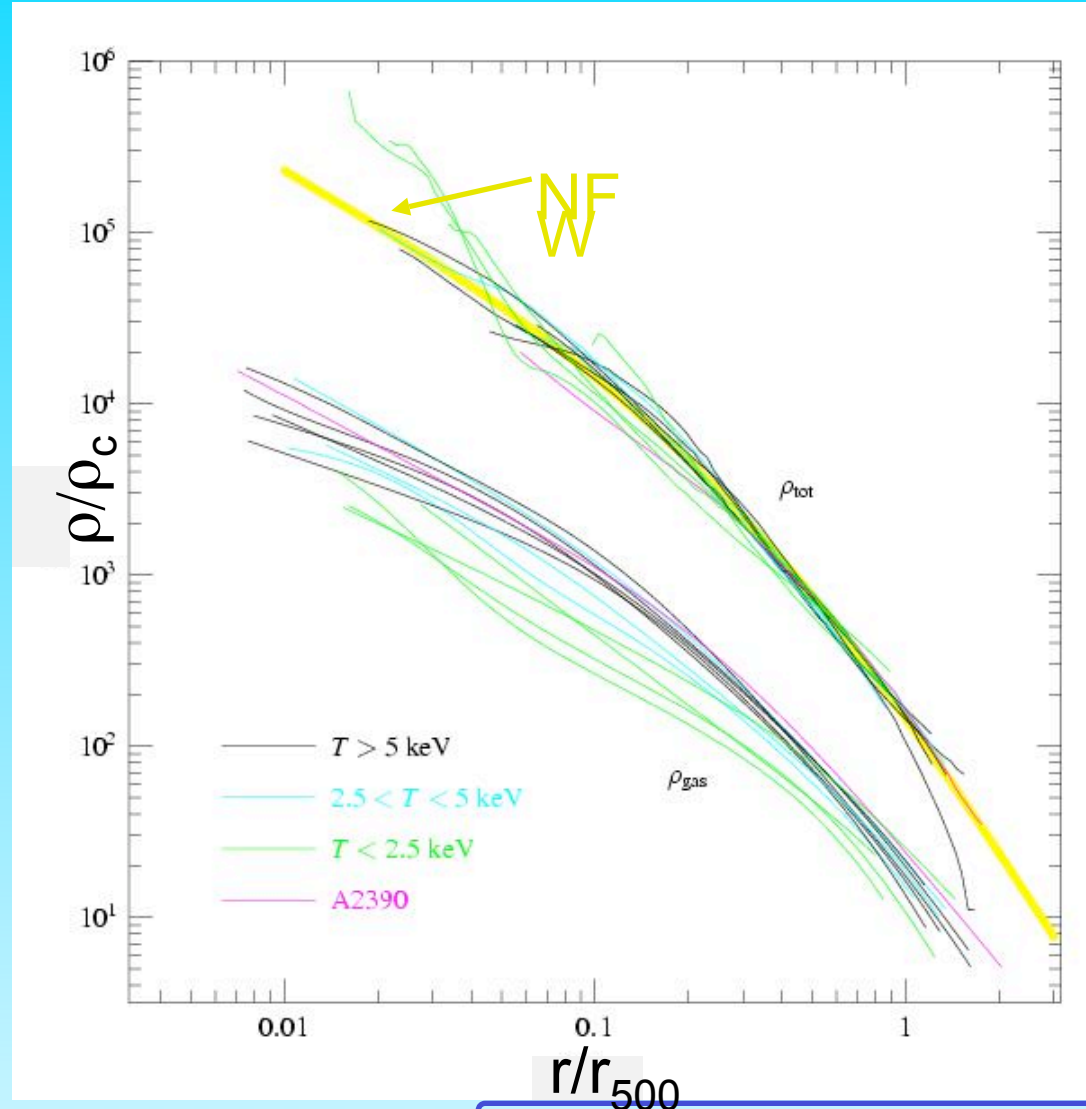
# The central density profile of galaxy cluster dark halos

X-ray data

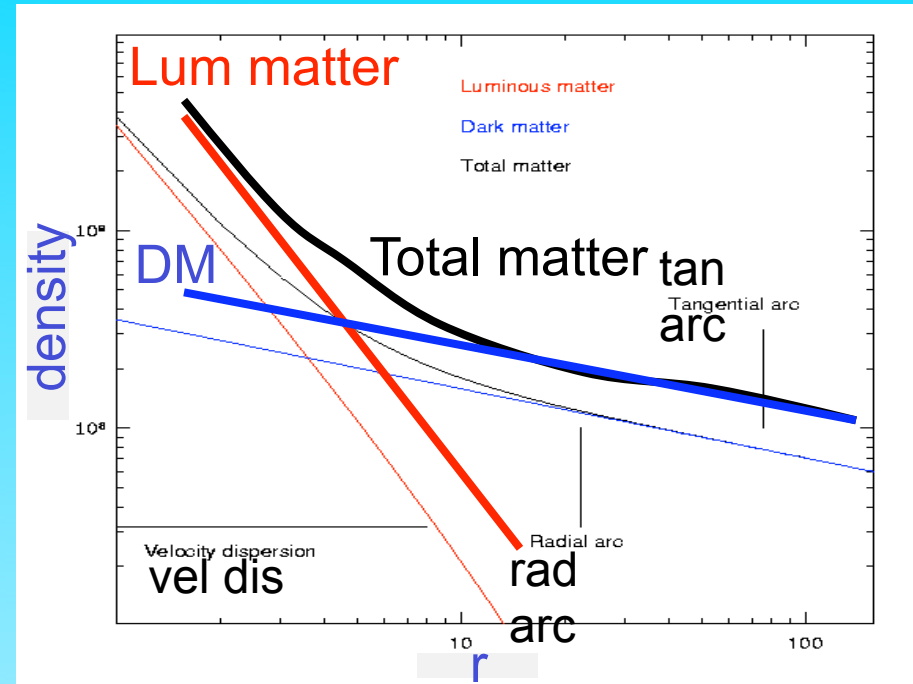
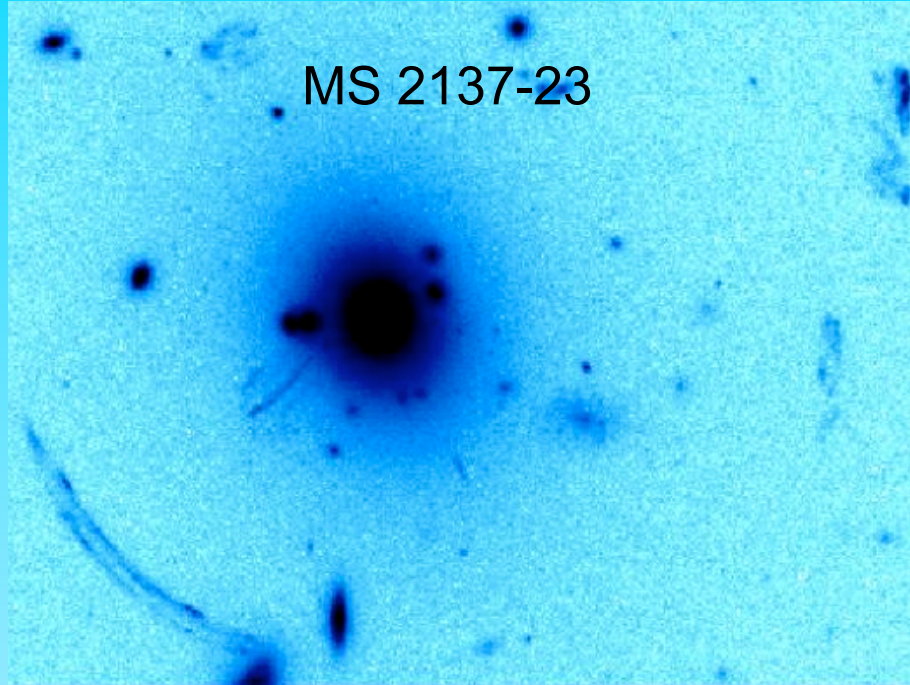
Mass profile of galaxy clusters, from X-ray data & assumption of hydrostatic equilibrium



Excellent agreement with CDM halo predictions



# Mass profile in cluster cores from strong lensing



Sand et al 05

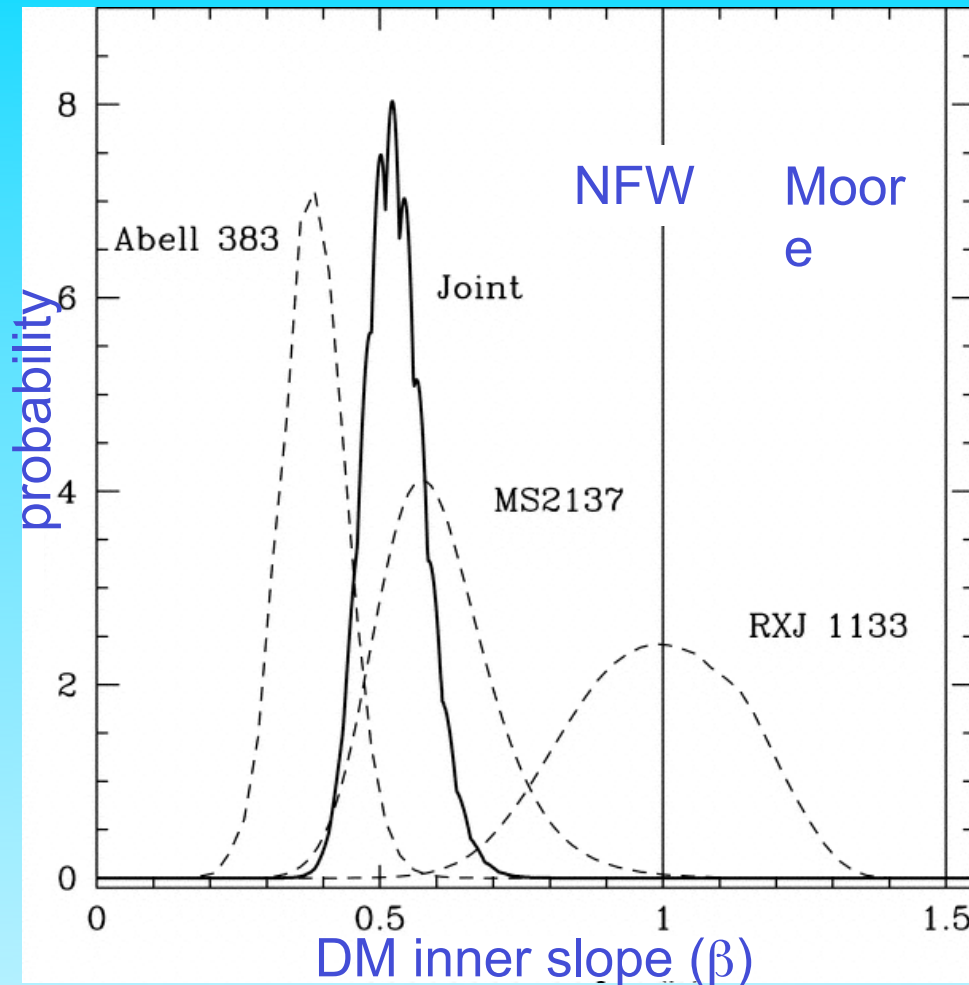
- Assume spherical symmetry
- Model potential as power-law DM + galaxy with constant M/L
- Constrain inner slope of DM profile using tangential arc

# Mass profile in cluster cores from strong lensing

$$\rho(r) \propto r^{-\beta} (r_s + r)^{\beta-3}$$

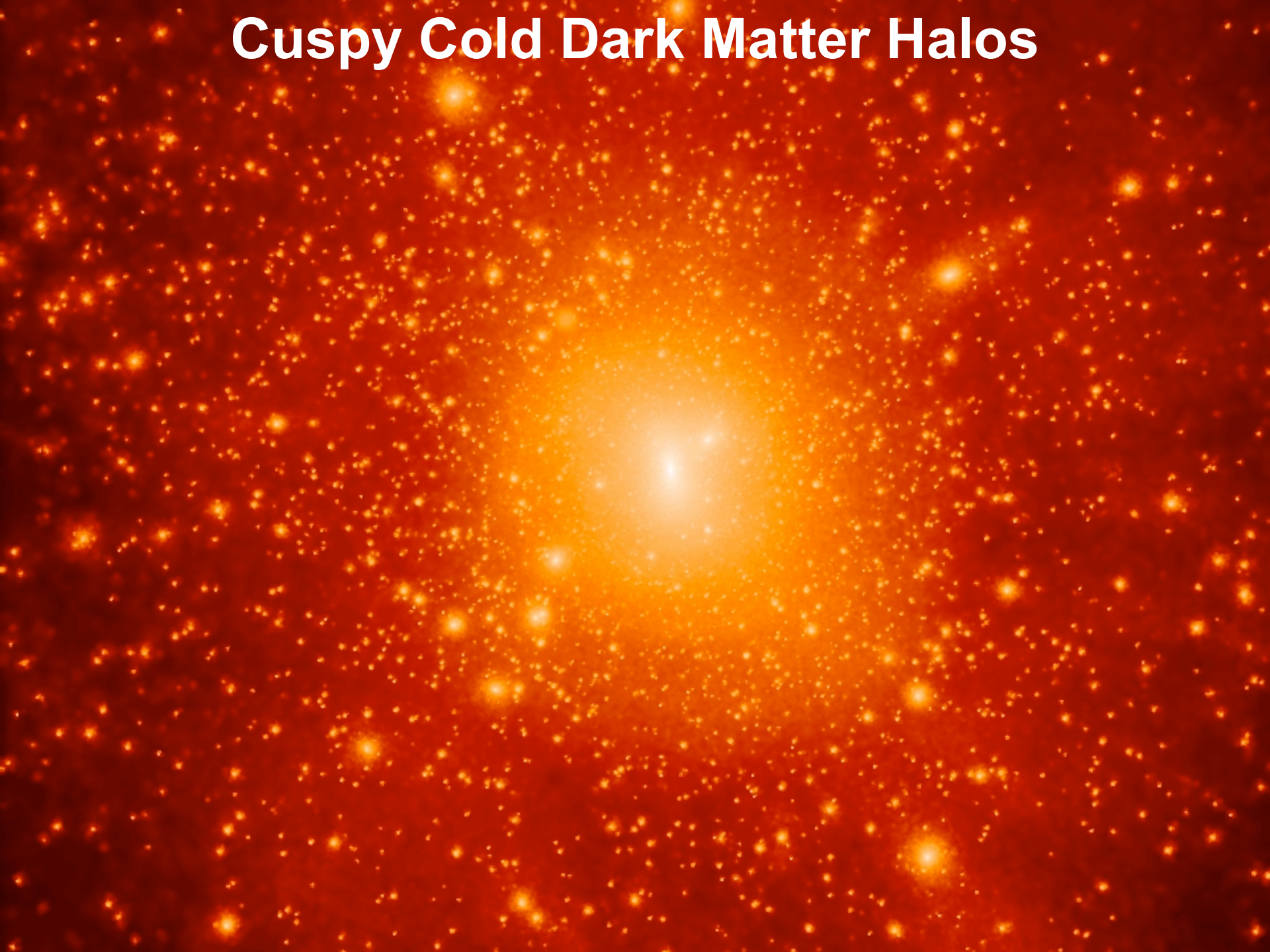
$\beta=1$  for NFW

Sand et al find  $\beta=0.5$ ,  
in disagreement with CDM



Sand et al 04

# Cuspy Cold Dark Matter Halos



# Mass profile in cluster cores from strong lensing

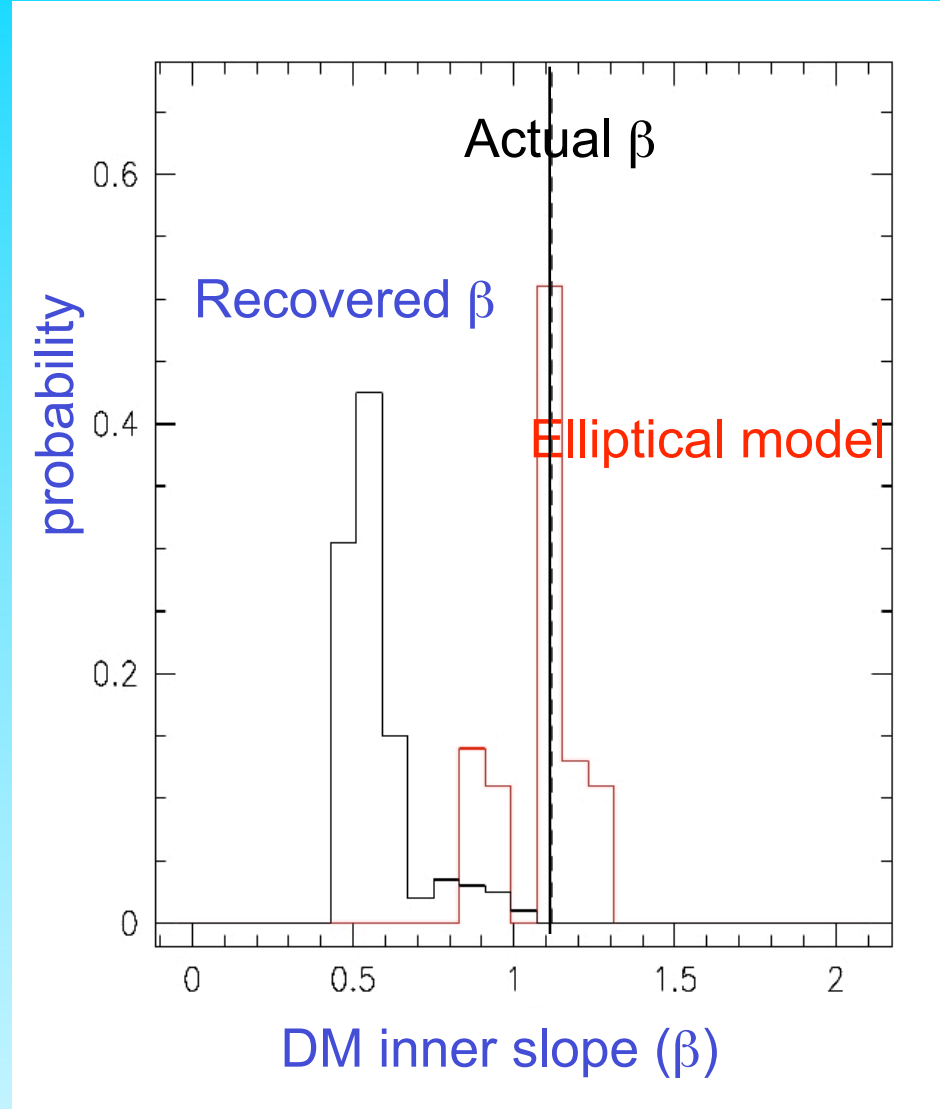
$$\rho(r) \propto r^{-\beta} (r_s + r)^{\beta-3}$$

$\beta=1$  for NFW

For this simulation,  $\beta=1.2$

Sand et al (spherically symm)  
analysis returns  $\beta \sim 0.5!!!$

Reason: Sand et al assume  
spherical symmetry





## The “halo-core problem” ?

The inner profiles of cluster halos  
seen consistent with the cusps  
predicted in  $\Lambda$ CDM



# A Cold dark matter universe

N-body simulations show that cold dark matter halos (from galaxies to clusters) have:

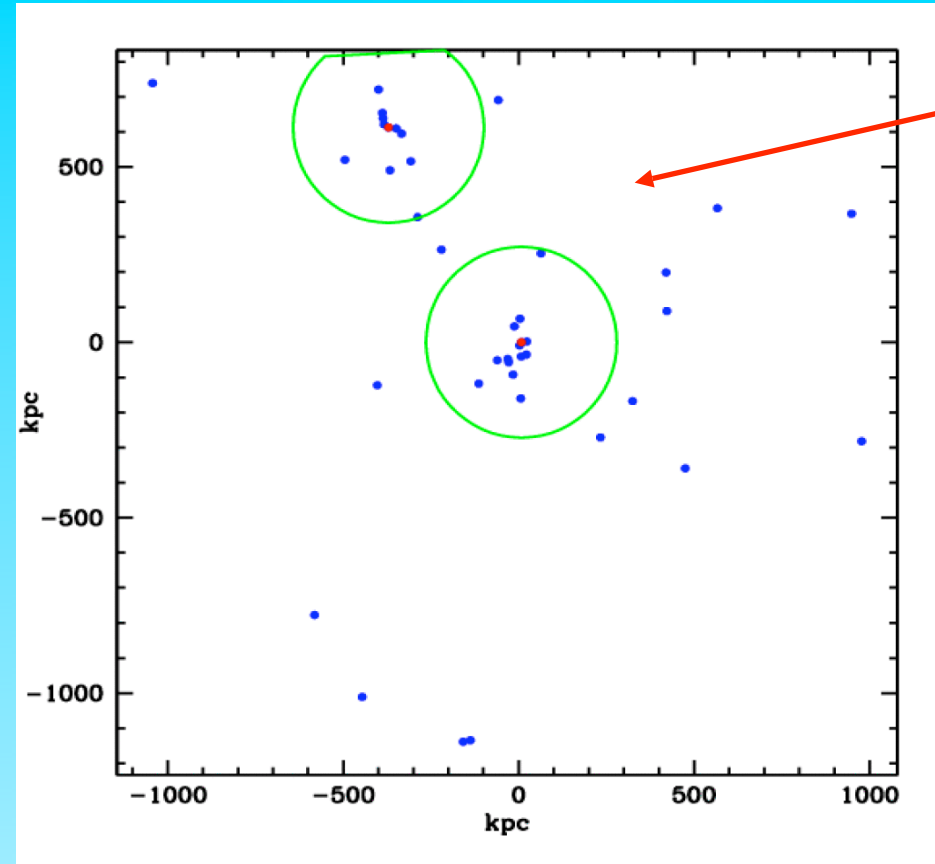
- “Cuspy” density profiles
- Large number of self-bound substructures (10% of mass)

This has led to two well-publicized “problems”:

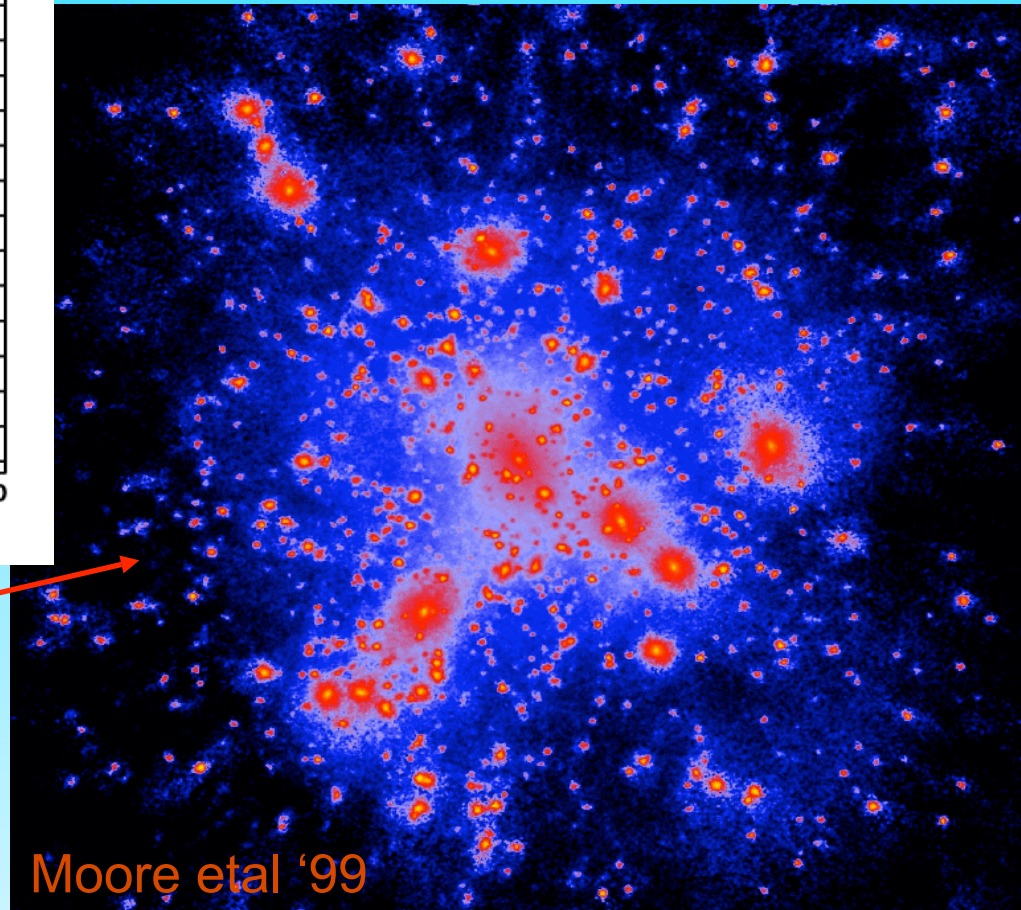
- The “halo core” problem
- The “satellite” problem

# The satellites of the Local Group

The Local Group contains only about 40 bright satellites



N-body simulations produce 1000s of small subhalos



Moore et al '99

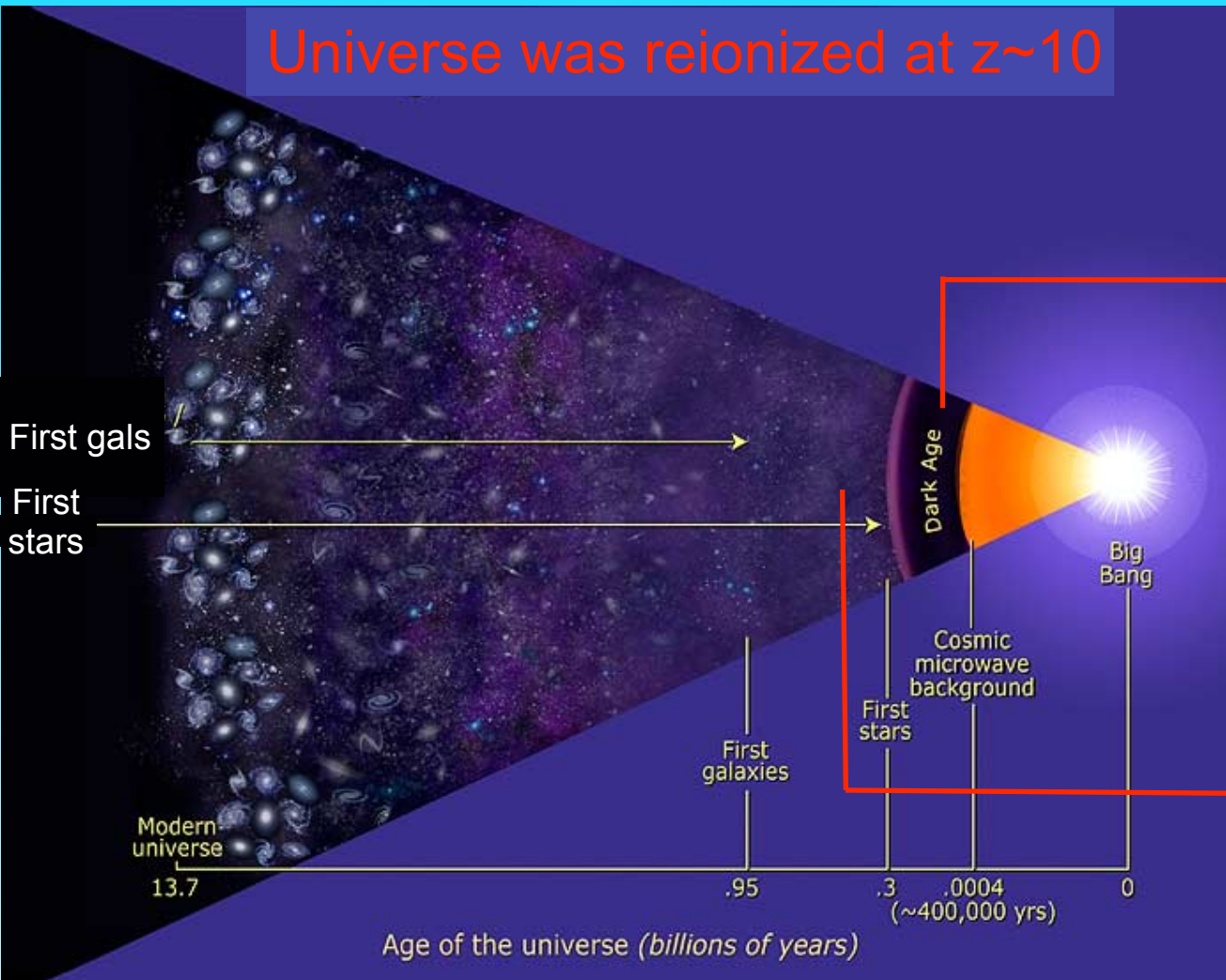
# Substructure in cold dark matter halos



60 million particles inside  $r_{\text{vir}}$

Springel, Jenkins, Helmi,  
Navarro, Frenk & White '07

# Feedback in galaxy formation



Effects of reionization

Gas is neutral  $\rightarrow$  cools in small halos

H is reionized at  $z \sim (10-6)$

Gas heated  $\sim 10^4\text{K}$   $\rightarrow$  cannot cool in halos with  $V < 40 \text{ km/s}$

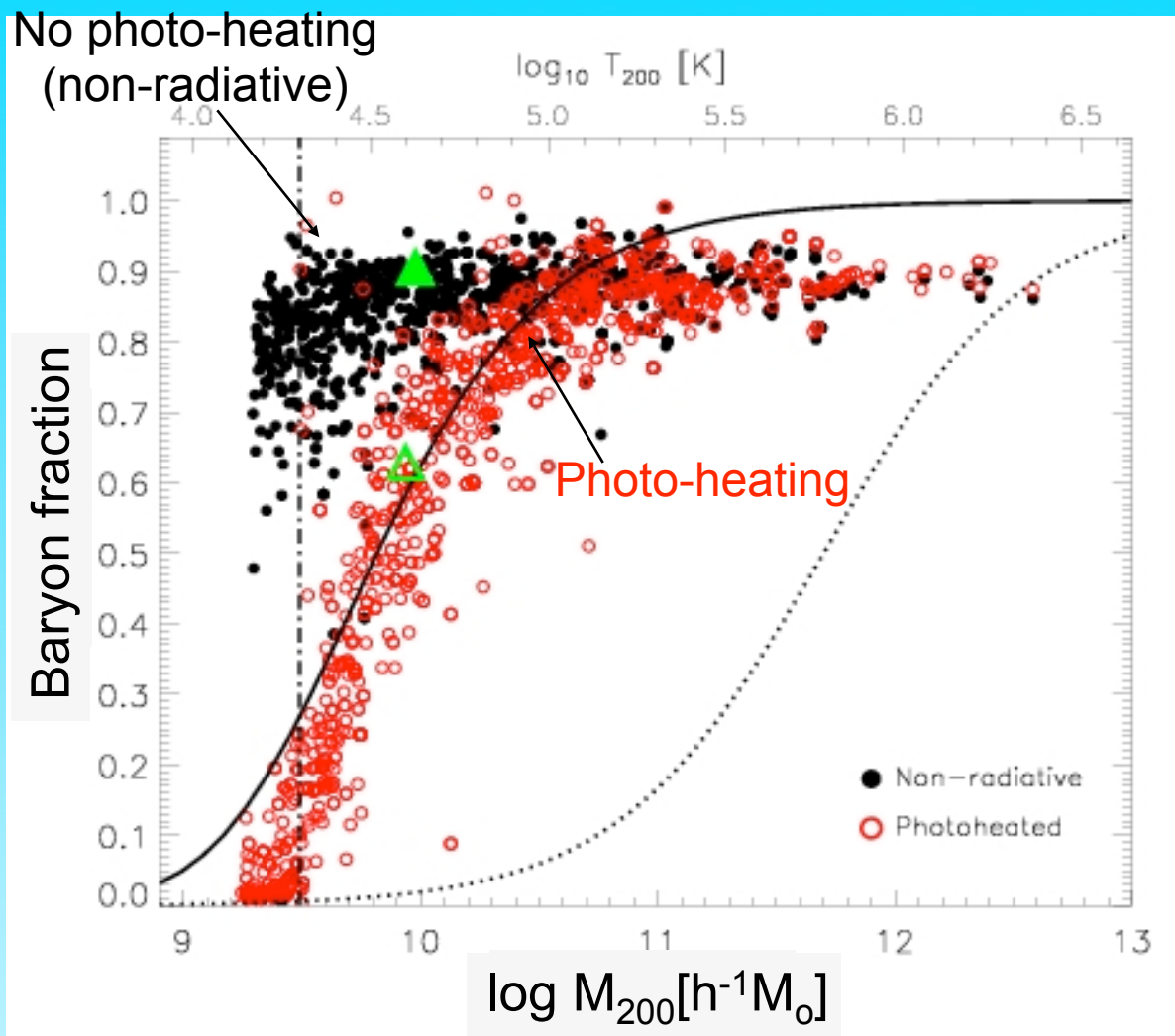
# Baryon habitats

Simple photo-heating model:  $T_{\text{floor}} = 2 \times 10^4 \text{K}$  at  $z=11$

Prevents collapse of baryons in halos with

$$V_{200} < 35 \text{ km/s}$$

$$(M_{200} < 10^{10} M_{\odot})$$



Crain, Eke, Frenk, Jenkins, McCarthy, Navarro & Pearce 07

# Substructure in cold dark matter halos

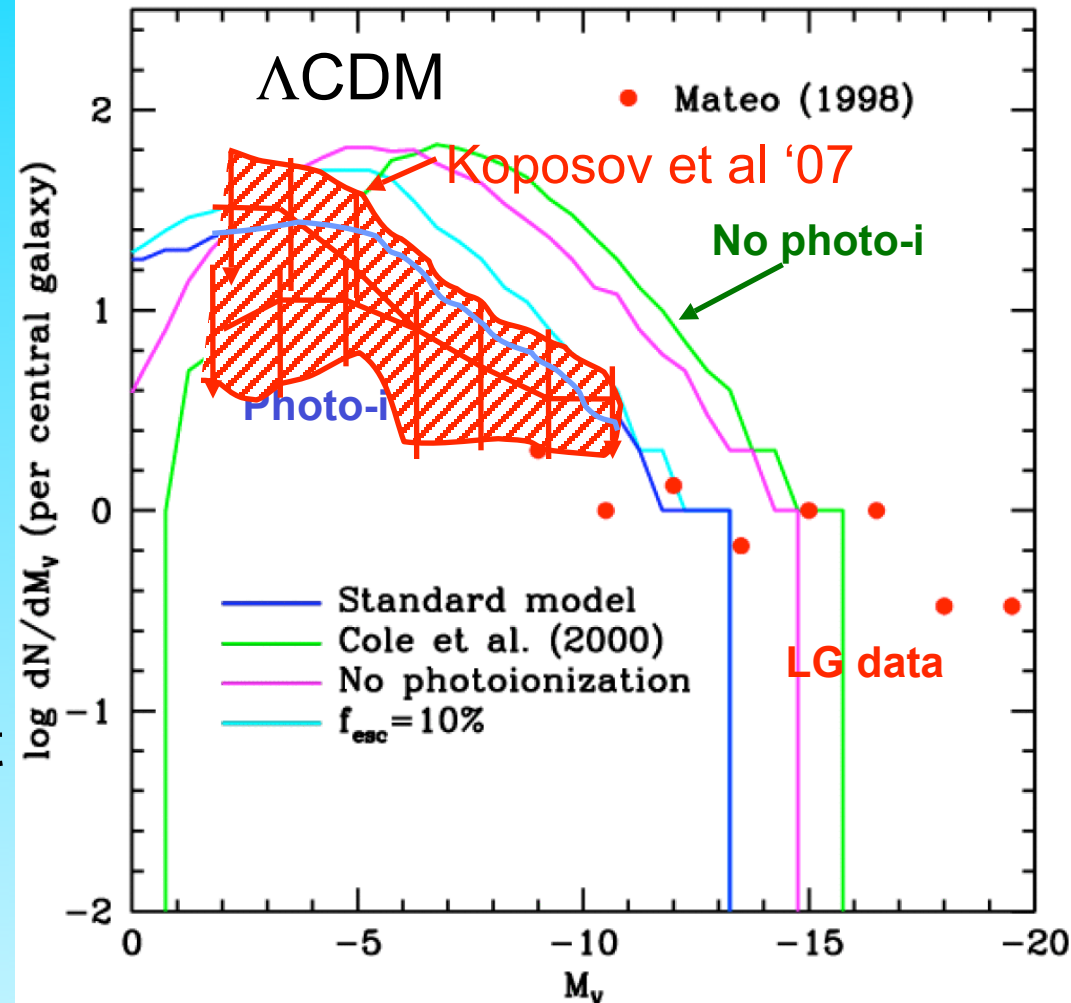
Only the few small subhalos that formed before reionization can cool gas and make a visible galaxy

60 million particles inside  $r_{\text{vir}}$

Springel, Jenkins, Helmi,  
Navarro, Frenk & White '07

# Luminosity Function of Local Group Satellites

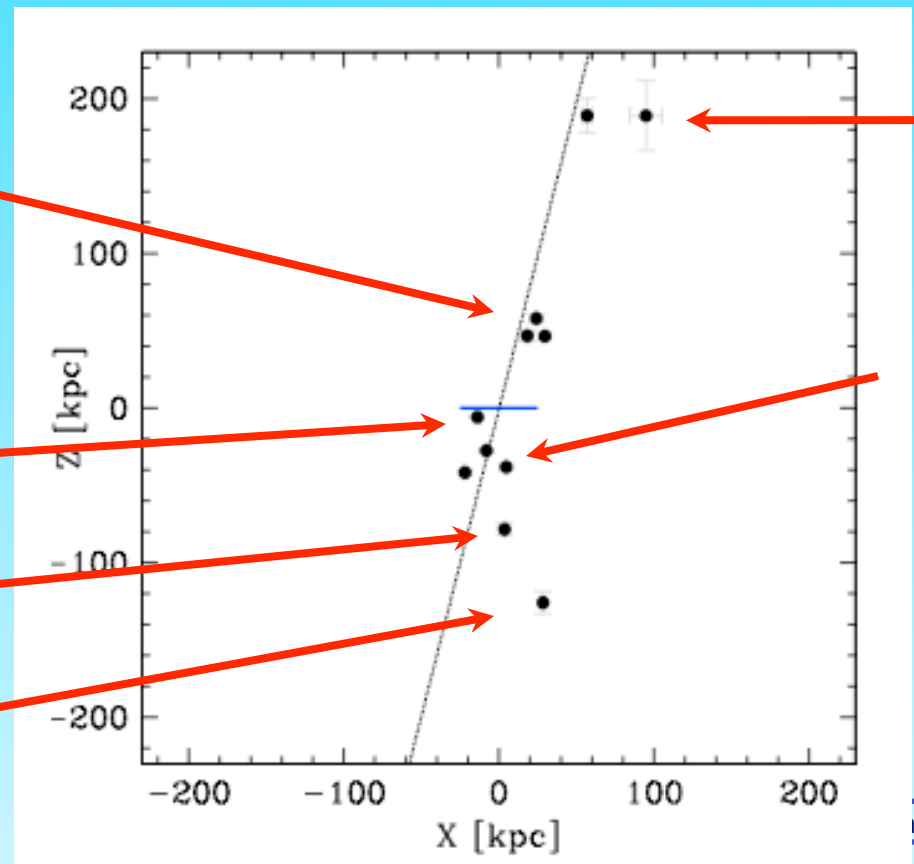
- **Photoionization** inhibits the formation of satellites
- Abundance reduced by factor of 10!
- Median model gives correct abundance of sats brighter than  $M_V = -9$ ,  $V_{\text{cir}} > 12$  km/s
- Model predicts many, as yet undiscovered, faint satellites



Benson, Frenk, Lacey, Baugh & Cole '02  
(see also Kauffman et al '93, Bullock et al '01)

# The satellites of the Milky Way

The 11 bright satellites within 250 kpc of the Milky Way lie roughly on a great circle on the sky (Lynden-Bell '67, Kroupa, etal '05)



Sculptor, Draco,  
Sextans

Leo I & II

Sagittarius Dw

LMC, SMC,  
Ursa Minor

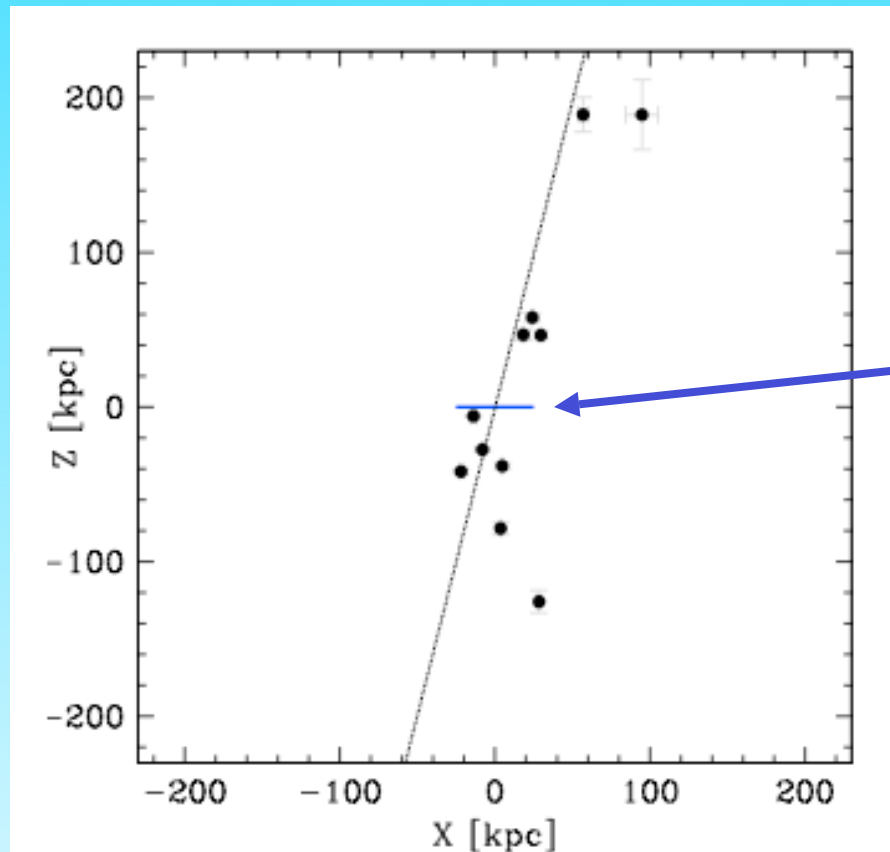
Carina

Fornax



# The satellites of the Milky Way

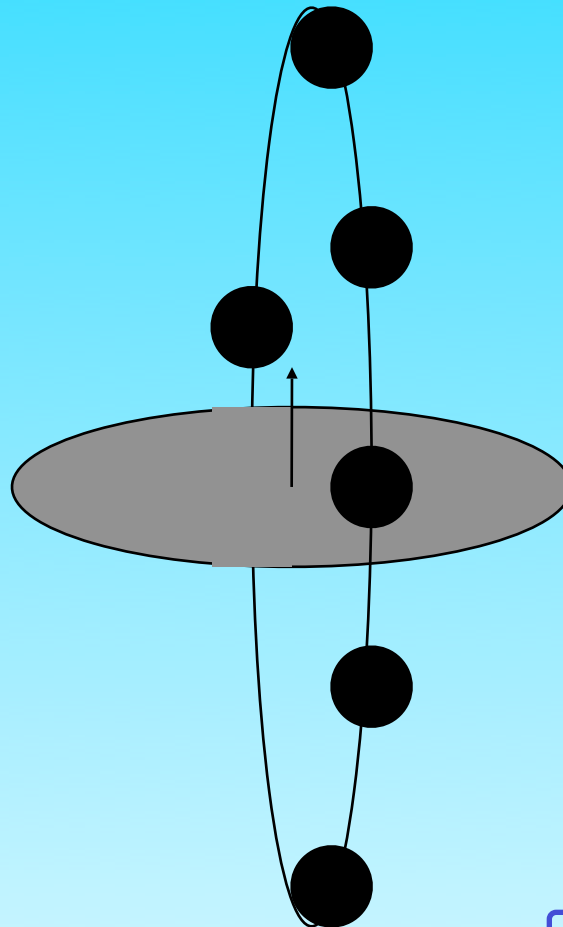
The 11 bright satellites within 250 kpc of the Milky Way lie on a great circle on the sky (Lynden-Bell '67, Kroupa, etal '05)



Milky Way's  
disk is  
perpendicular  
to the great  
circle

# The satellites of the Milky Way

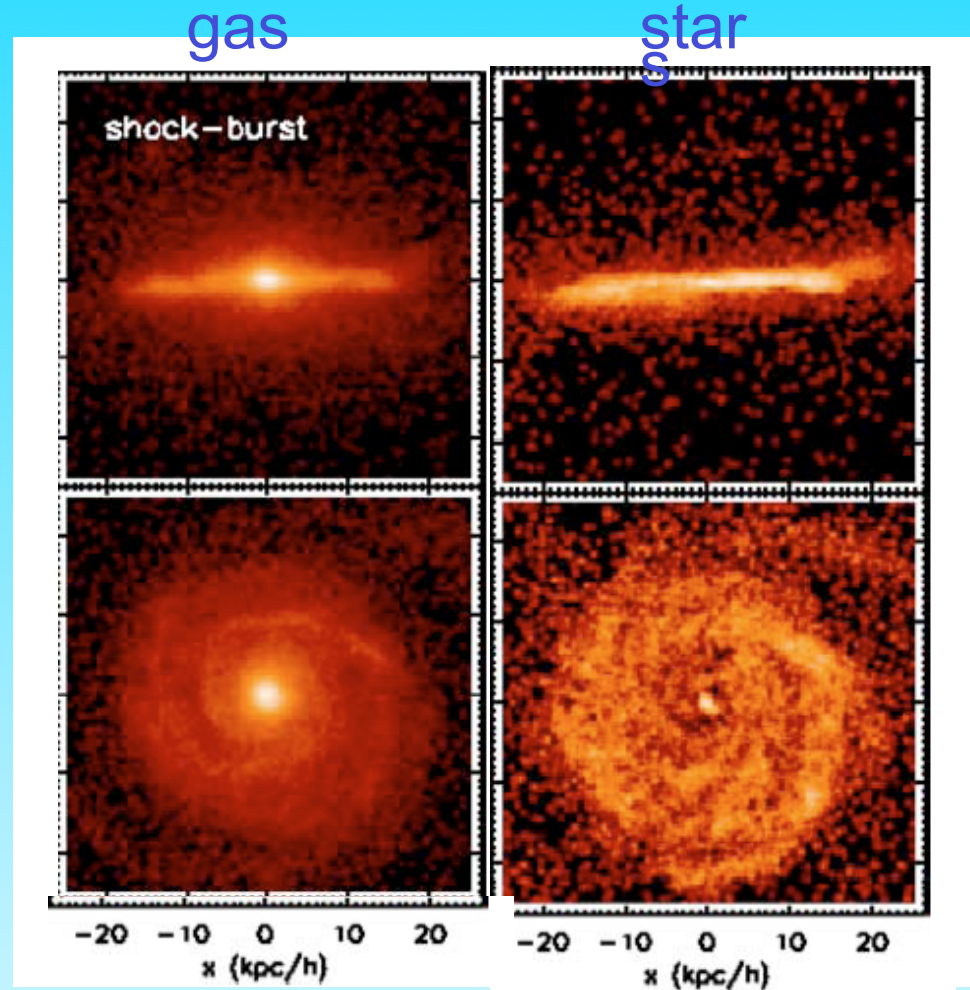
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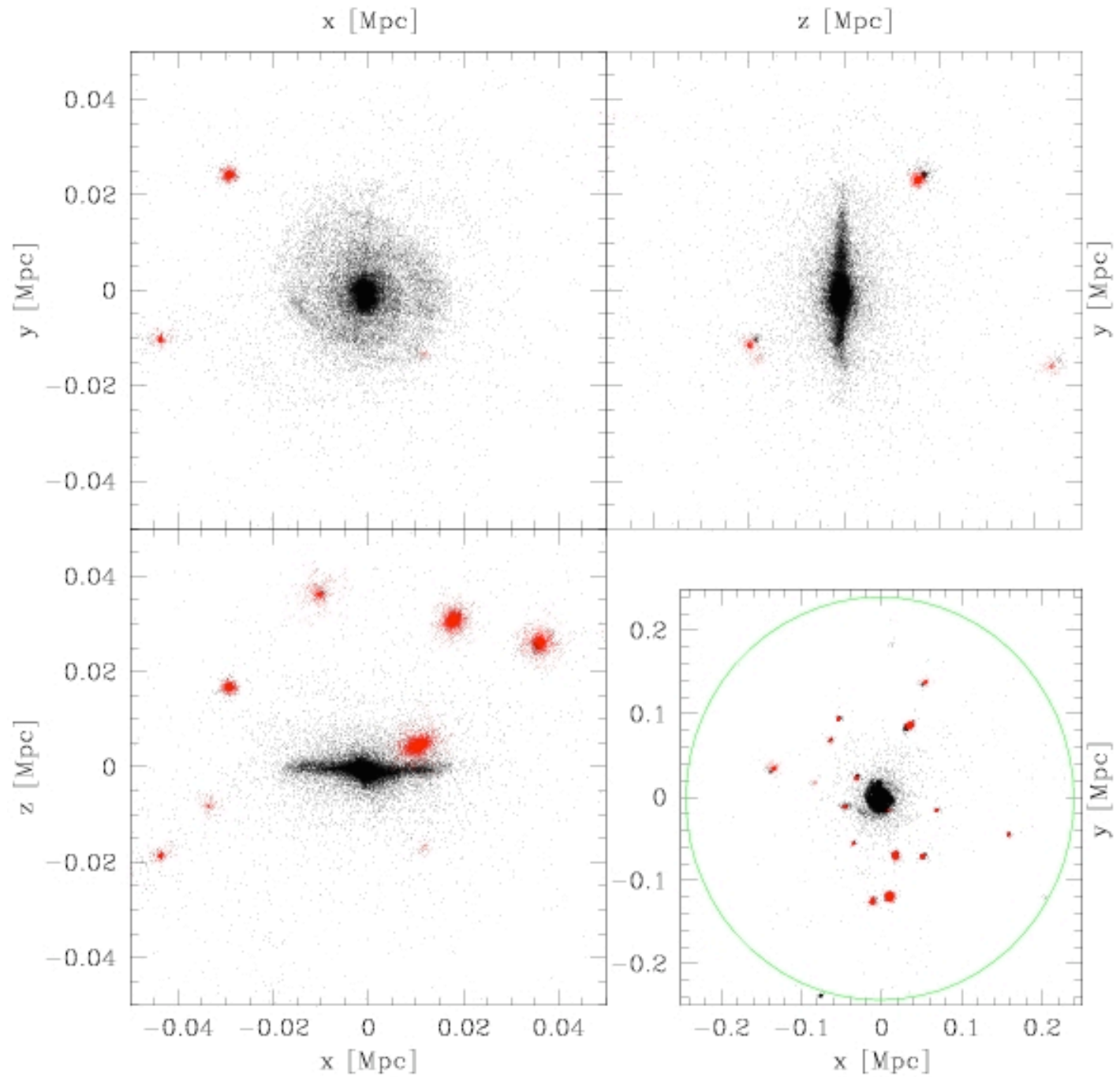
# Simulations of disc galaxy formation

$\Lambda$ CDM initial conditions

Smooth Particle  
Hydrodynamics  
(SPH)

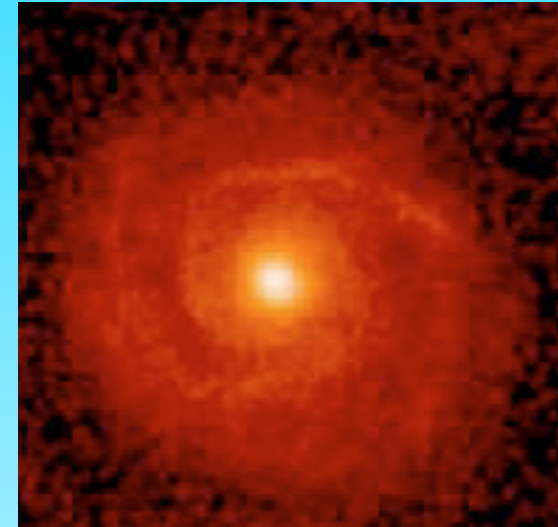
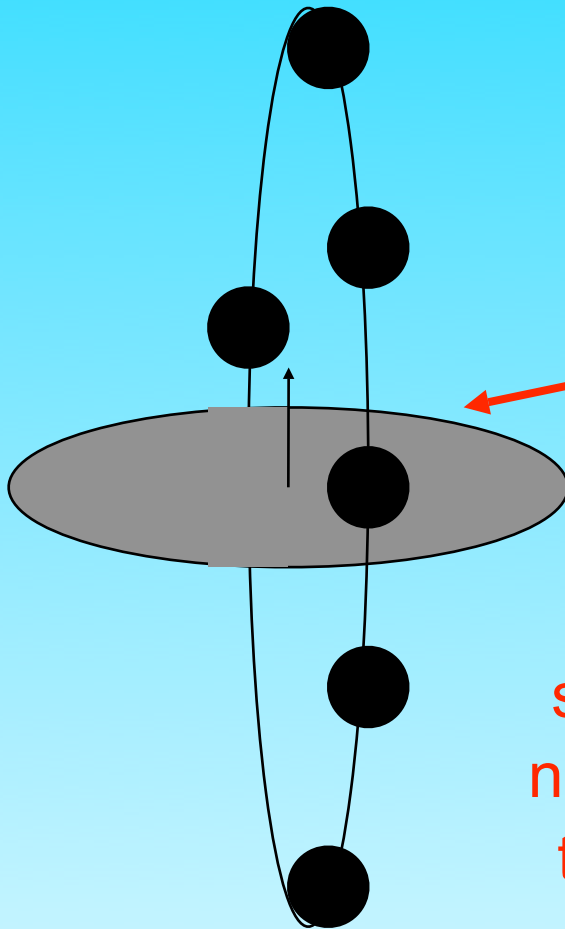


Okamoto, Jenkins, Eke, & Frenk '05

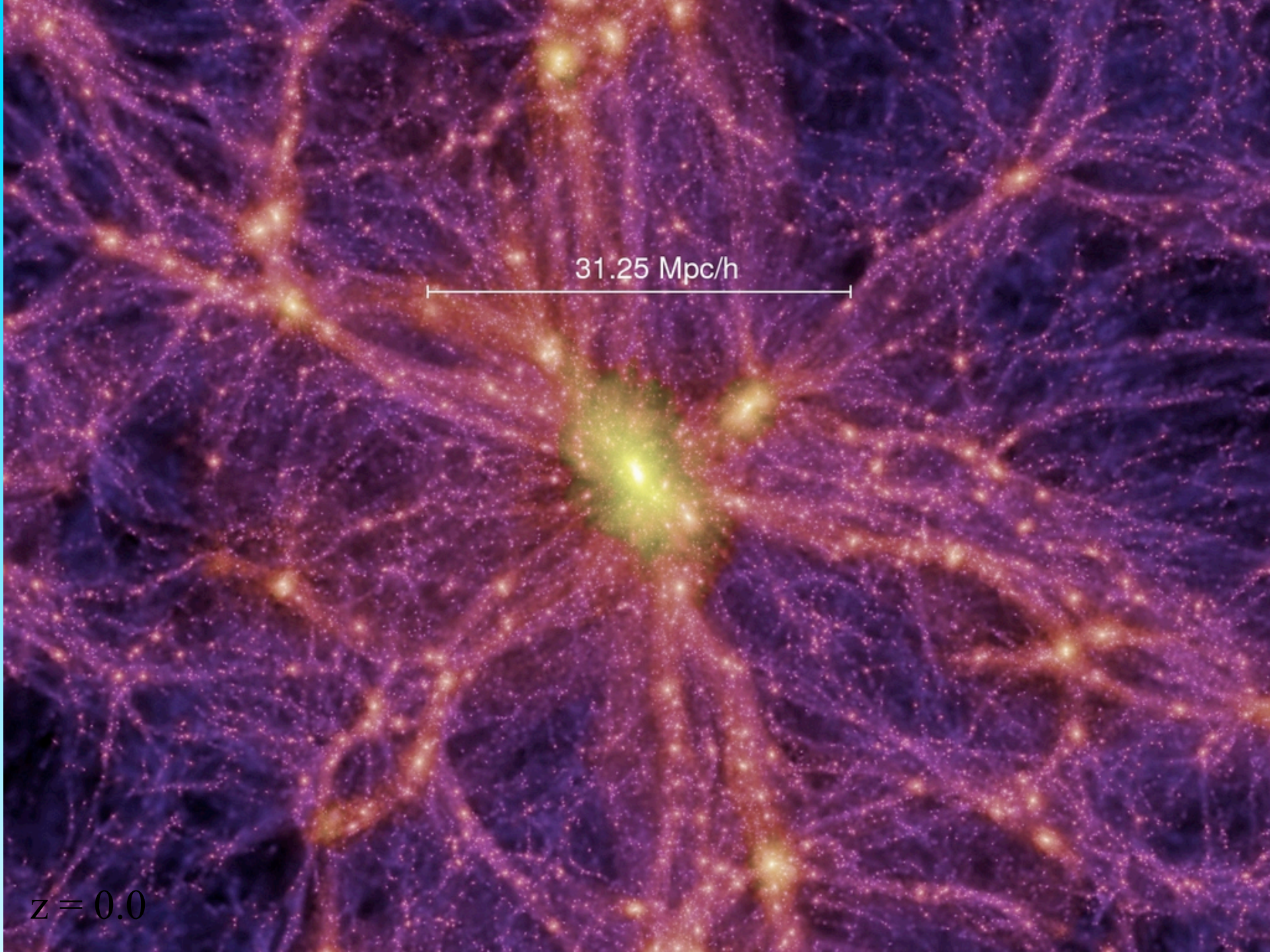


# The satellites of the Milky Way

The 11 bright satellites within 250 kpc of the Milky Way lie on a great circle on the sky (Lynden-Bell '67, Kroupa, etal '05)



In 2/3 simulations, satellites system is nearly perpendicular to disk (within  $20^\circ$ )



31.25 Mpc/h

$z = 0.0$

# Substructure in cold dark matter halos



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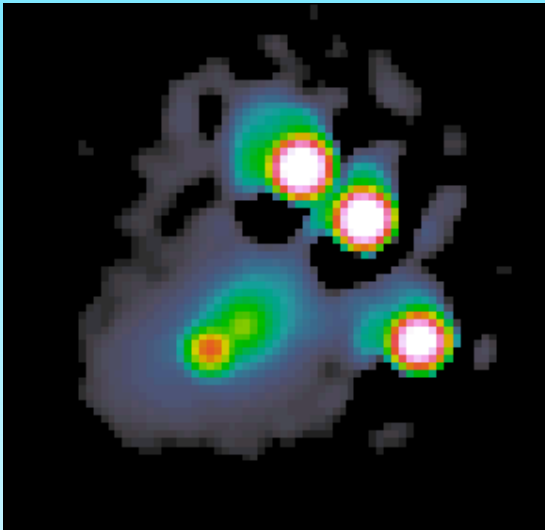
Springel, Jenkins, Helmi,  
Navarro, Frenk & White '07

# Substructure in CDM halos

Halos have large number of self-bound substructures containing  $\sim 10\%$  of the mass and with  $dN/dM \sim M^{-1.8}$

→ Substructures may be observable

- Gravitational lensing effects
- $\gamma$ -ray annihilation emission



Anomalous flux ratios in multiply-imaged quasars  $\Rightarrow$  **Substructure**

Dalal & Kochanek '02, Metcalfe & Zhao '02



# Conclusions: the $\Lambda$ CDM model

→  $\Lambda$ CDM is an intrinsically implausible model that requires:

- An early epoch of inflation
- Quantum fluctuations in the early universe
- Non-baryonic dark matter
- Dark energy

→ Yet, it agrees with staggering amount of data, from CMB to gals

→ Baryon acoustic oscillations detected in 2dFGRS and SDSS

→ Current generation of surveys to detect BAO at  $z \sim 1$  will constrain  $w$  but only to  $\sim 5\%$

→ Data consistent with cusps in cluster halos

→ “Satellite problem” probably solved by photoionization

The “golden” era in cosmology is not over



It has probably just begun!