

# Cosmic Reionization and the End of the Dark Ages

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Observatoire de Paris

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Eiichiro Komatsu, Jun Koda, Elizabeth Fernandez (U. Texas)

# The Epoch of Reionization

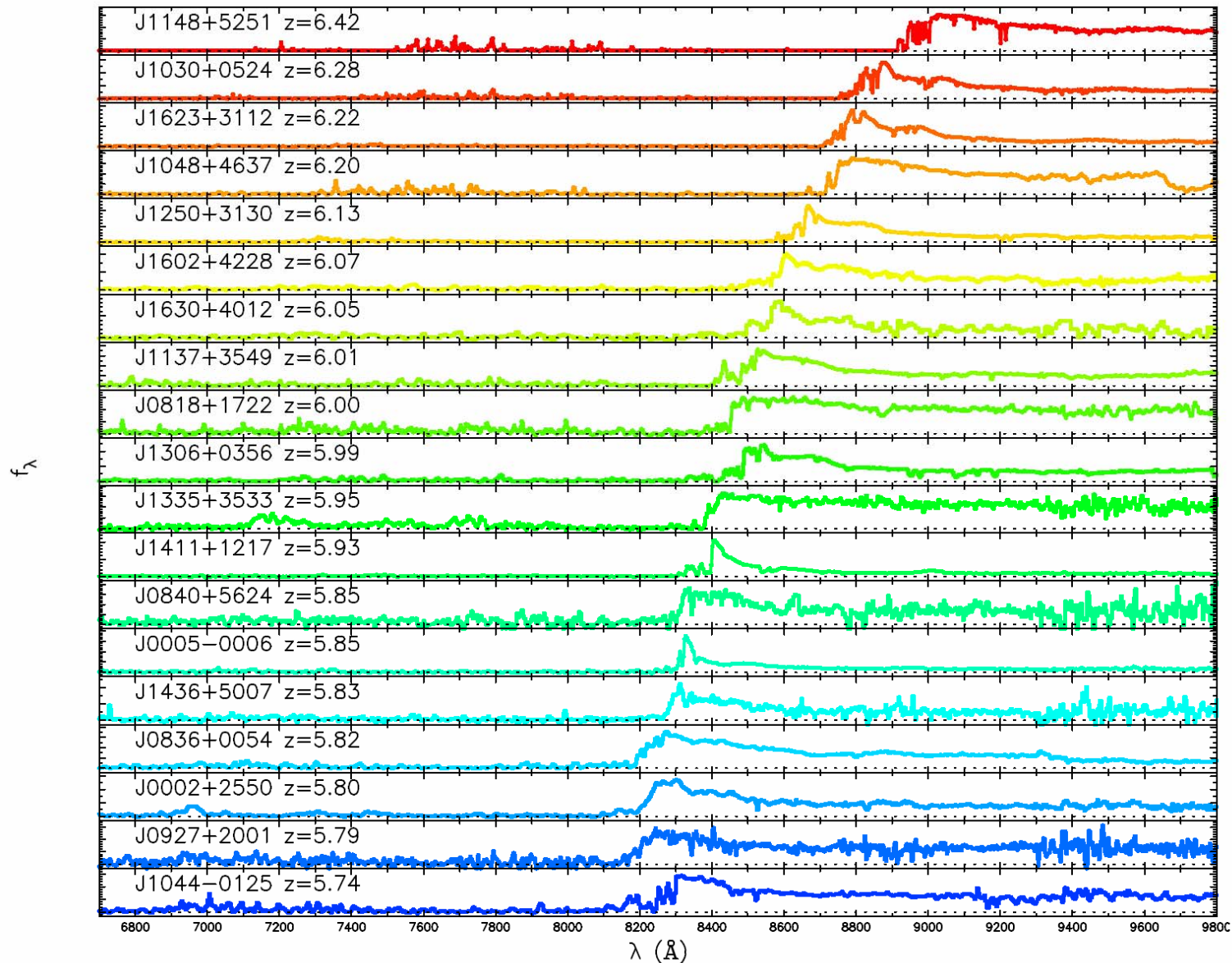
- Absorption spectra of quasars have long shown that the intergalactic medium at redshifts  $z < 6$  is highly ionized, with a residual neutral H atom concentration of less than 1 atom in  $10^4$ .  
====> universe experienced an “epoch of reionization” before this.

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- Sloan Digital Sky Survey quasars have been observed at  $z > 6$  whose absorption spectra show dramatic increase in the H I fraction at this epoch as we look back in time.  
====> epoch of reionization only just ended at  $z \gtrsim 6$ .



SDSS quasars show Lyman  $\alpha$  opacity of intergalactic medium rises with increasing redshift at  $z = 6 \rightarrow$  IGM more neutral  $\rightarrow$  reionization just ending?

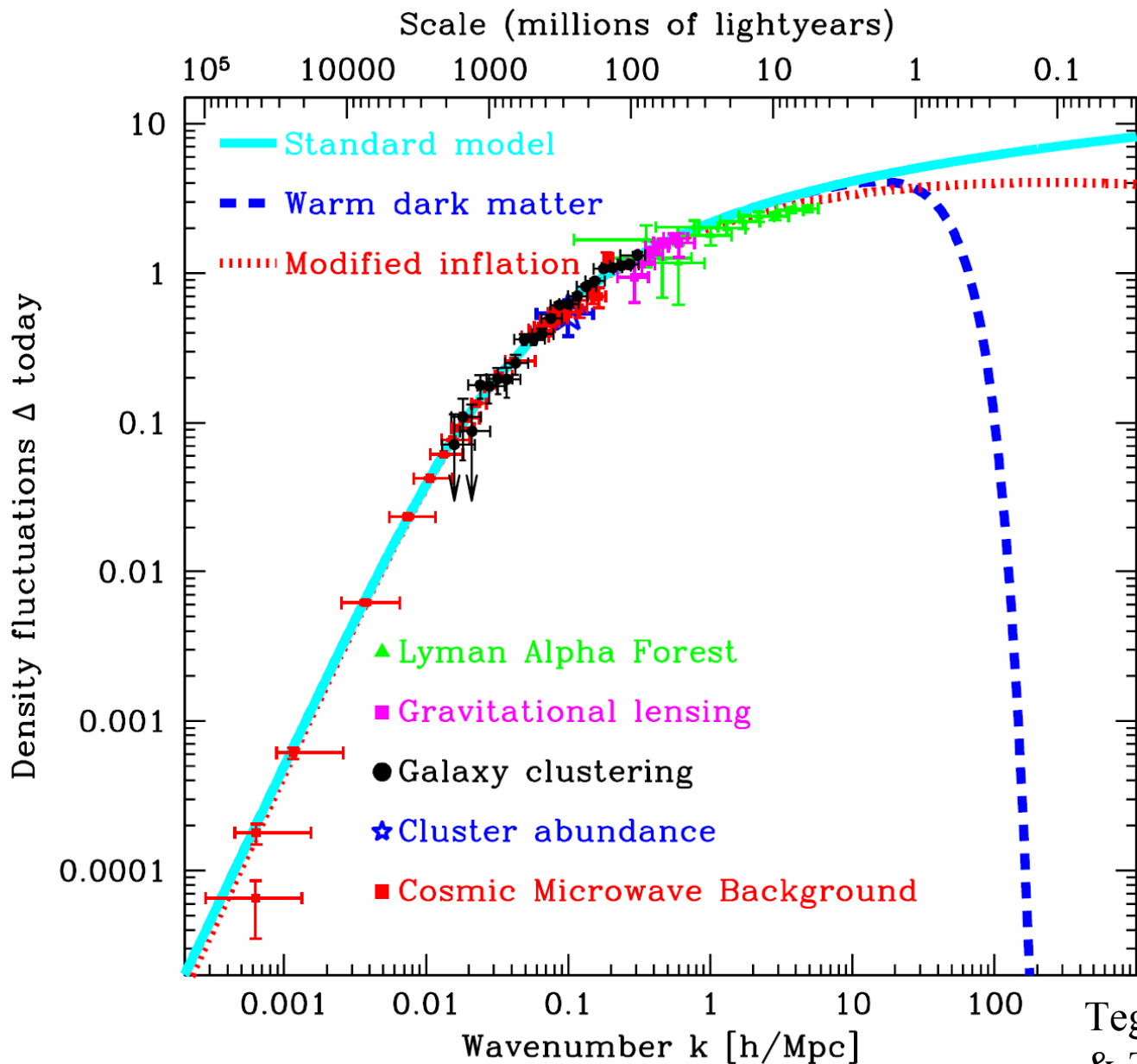


Fan et al  
(2005)

# The Epoch of Reionization

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====> epoch of reionization only just ended at  $z \gtrsim 6$ .
- **The cosmic microwave background (CMB ) exhibits polarization which fluctuates on large angular scales; WMAP finds that almost 10% of the CMB photons were scattered by free electrons in the IGM**  
====> **IGM must have been ionized much earlier than  $z = 6$  to supply enough electron scattering optical depth**  
====> **reionization already substantial by  $z \gtrsim 11$**

# EoR Probes the Primordial Power Spectrum on the Smallest Scales



Tegmark  
& Zaldarriaga (2008)

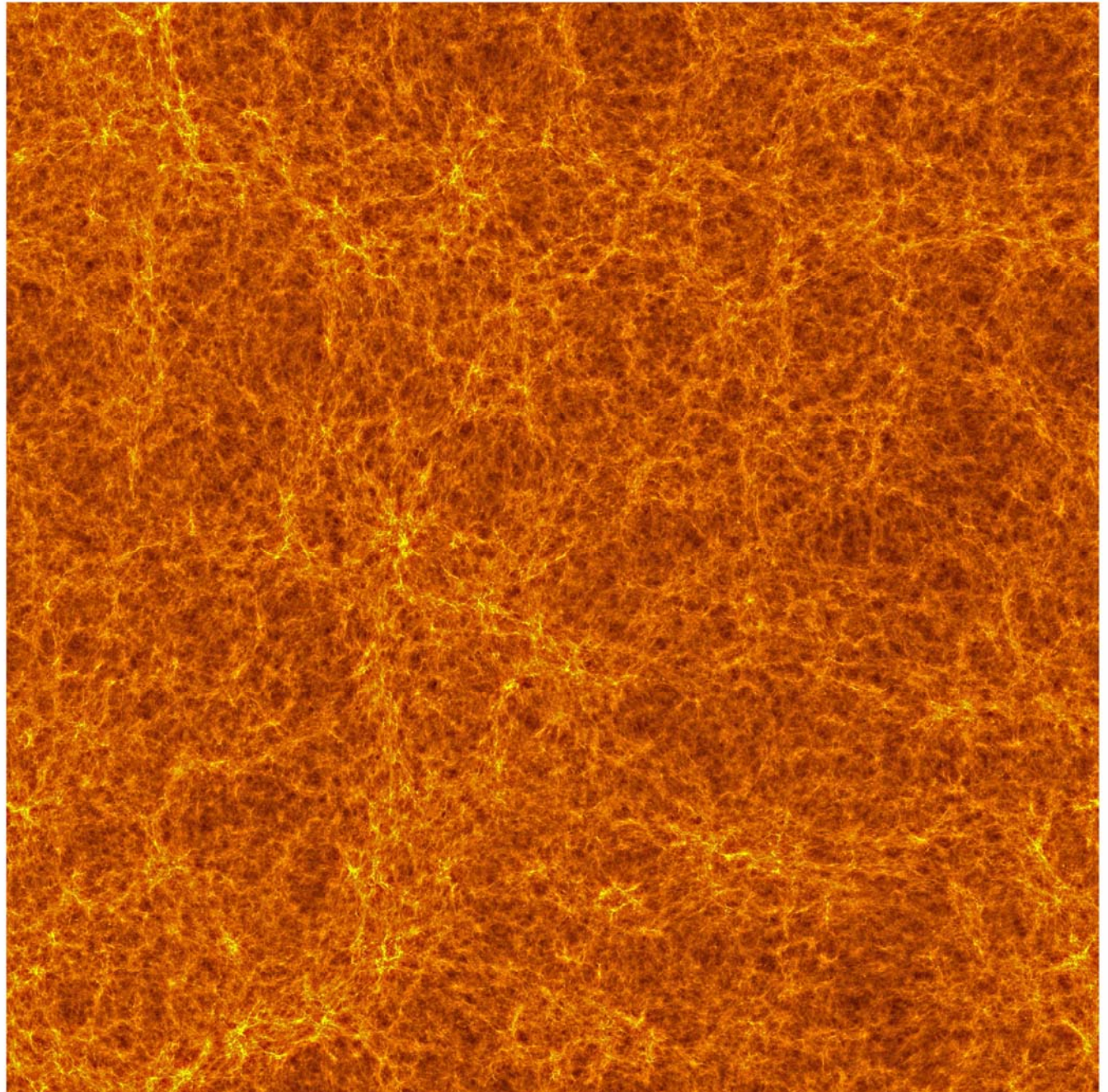


# Structure formation in $\Lambda$ CDM at $z = 10$

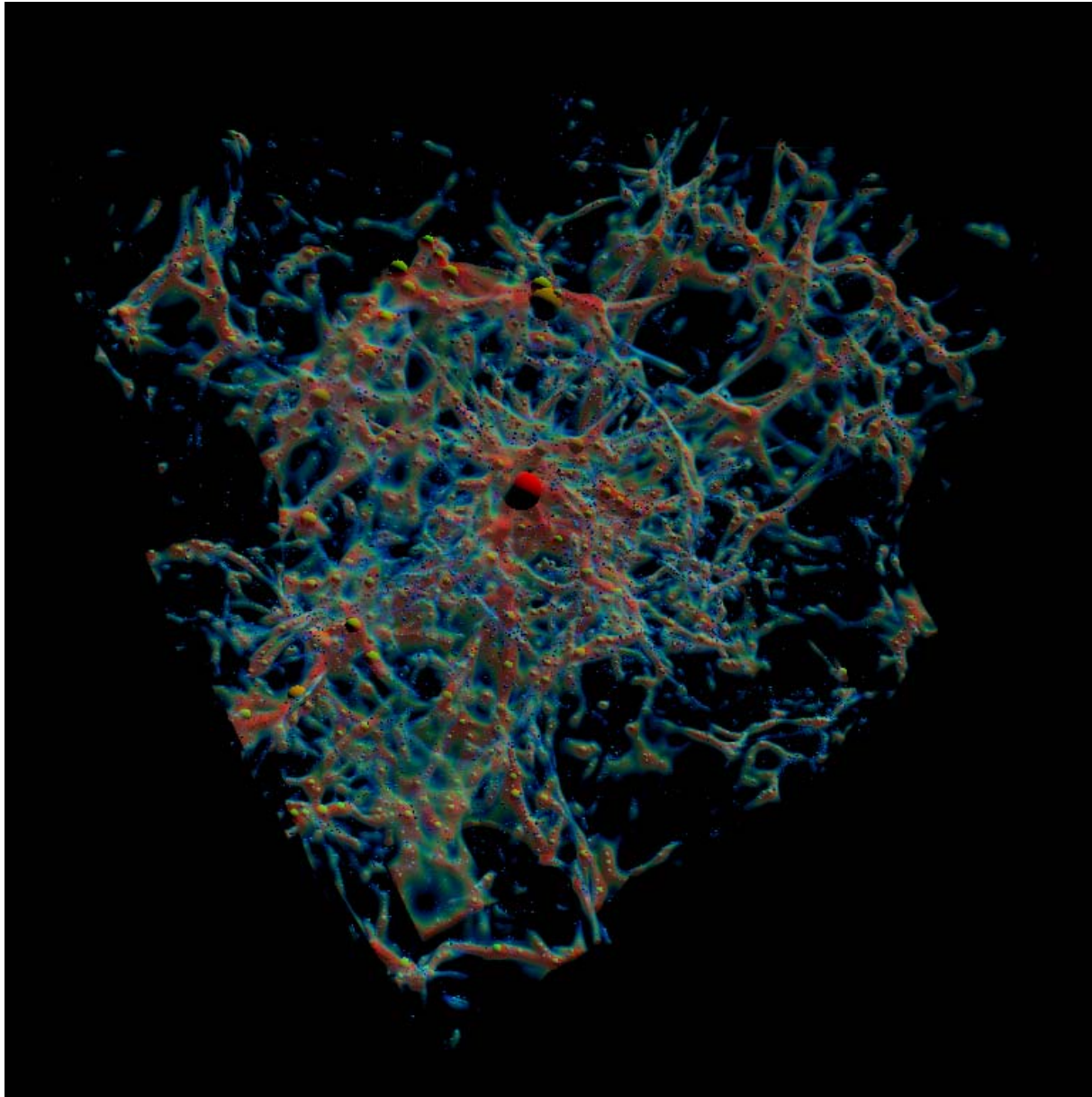
simulation volume  
=  
(100  $h^{-1}$ Mpc)<sup>3</sup>,  
comoving

1624<sup>3</sup> particles on  
3248<sup>3</sup> cells

Projection of  
cloud-in-cell  
densities of 20  
Mpc slice



# A Dwarf Galaxy Turns on at $z=9$

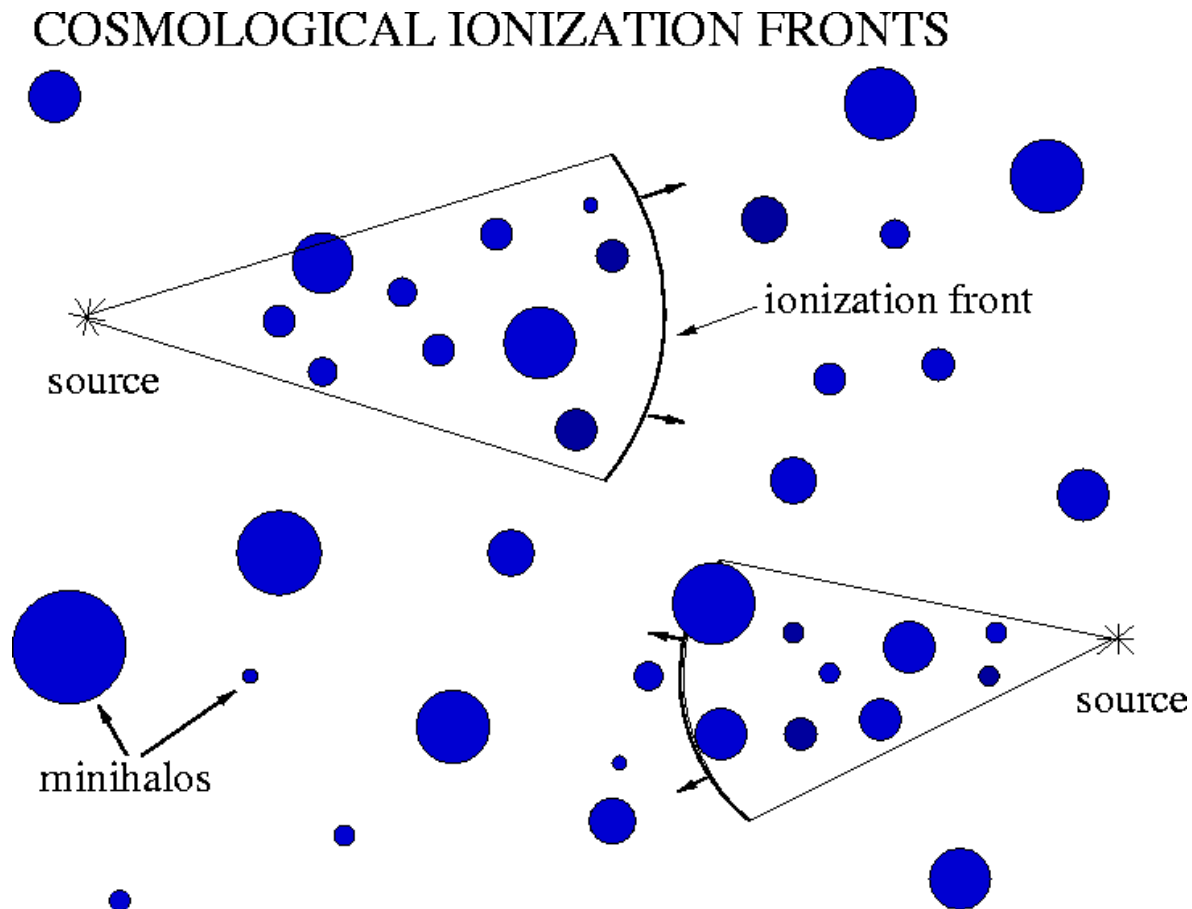




# THE PHOTOEVAPORATION OF MINIHALOS OVERTAKEN BY COSMOLOGICAL I-FRONTS

(Shapiro, Iliev & Raga 2004, MNRAS, 348, 753;  
Iliev, Shapiro, & Raga 2005, MNRAS, 361, 405)

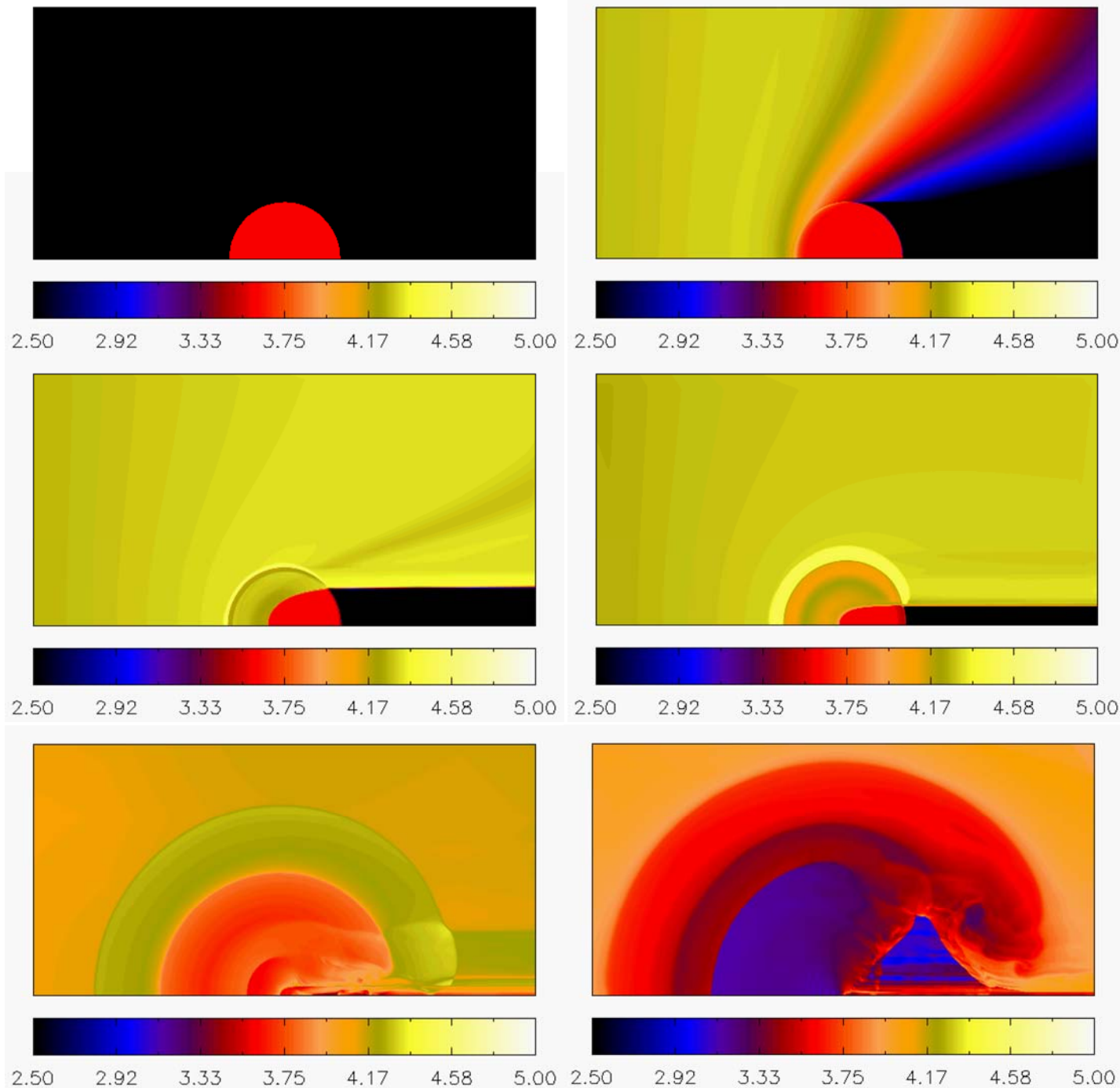
- We performed radiation-hydrodynamical simulations of the photoevaporation of a cosmological minihalo overrun by a weak, R-type I-front in surrounding IGM, created by external source of radiation.
- 2D, axisymmetric, Eulerian hydro code with Adaptive Mesh Refinement and the van Leer flux-splitting algorithm, including radiative transfer (H, He bound-free opacity).
- Nonequilibrium ionization rate equations: H, He + (C, N, O, Ne, S) @  $10^{-3}$  solar abundance



Temperature at  
times  $t = 0.0, 0.2,$   
 $2.5, 10, 60, 150$   
Myrs.

$(M_{\text{halo}}, z_{\text{initial}}, F_0) =$   
 $(10^7 M_{\text{sun}}, 9, 1).$

Pop II source.



# ANIMATIONS

## Pop II

- TEMPERATURE
- DENSITY
- H I
- He II
- C IV

## Pop III

- TEMPERATURE
- DENSITY
- H I
- He II
- C IV



# Simulating Cosmic Reionization at Large Scales I. : The Geometry of Reionization

Iliev, Mellema, Pen, Merz, Shapiro & Alvarez (2006)

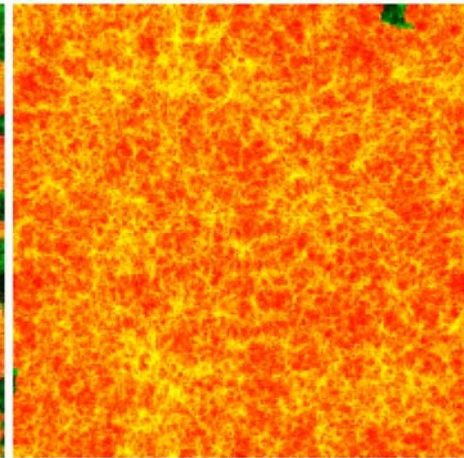
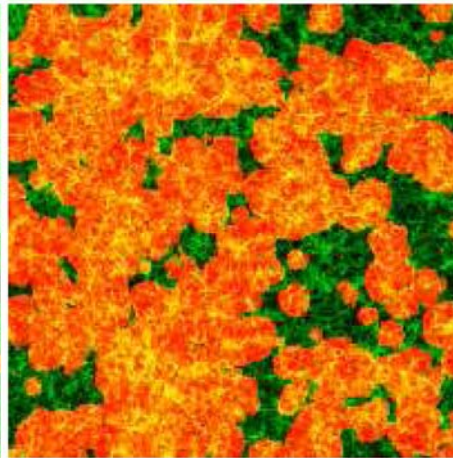
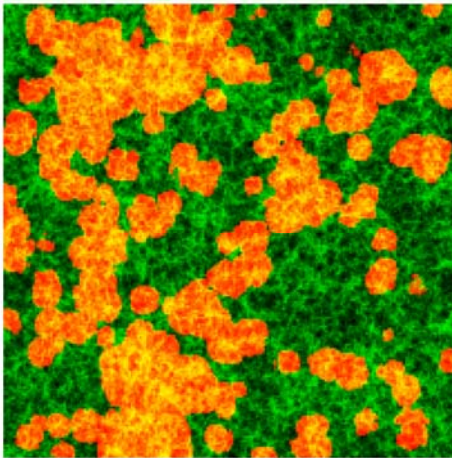
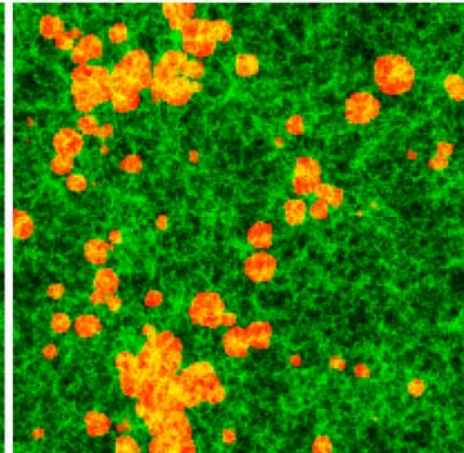
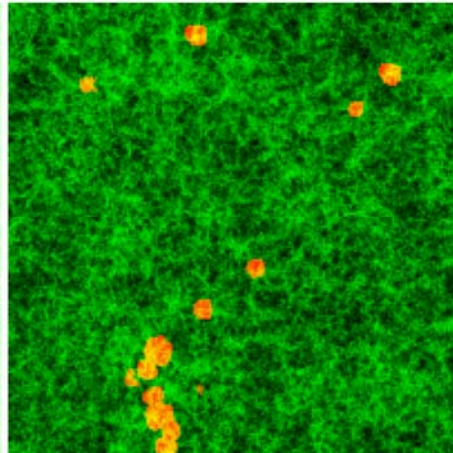
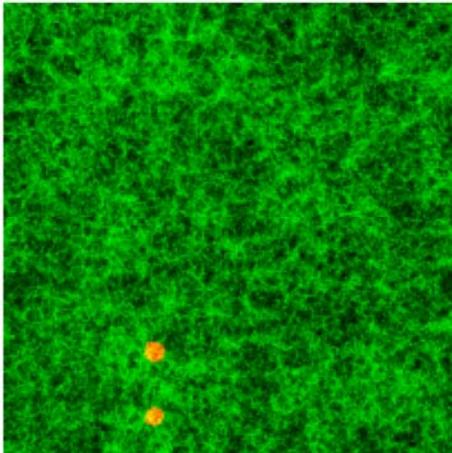
MNRAS, 369, 1625 (astro-ph/0512187)

$z =$

18.5

16.1

14.5



13.6

12.6

11.3

# N-body + Radiative Transfer → Reionization simulation

- N-body simulation yields the density field and sources of ionizing radiation
    - PMFAST code (Merz, et al. 2005) with  
 $1624^3 = 4.28$  billion particles,  $3248^3$  cells,  
particle mass =  $2.5 \times 10^7 M_{\text{sun}}$  ( $100 h^{-1}\text{Mpc}$  box),
    - Halo finder “on-the-fly” yields location, mass, other properties of all galaxies,  
 $M \geq 2.5 \times 10^9 M_{\text{sun}}$  ( $100 h^{-1}\text{Mpc}$  box),
- e.g.  $N_{\text{halo}} \sim 4 \times 10^5$  by  $z \sim 8$  (WMAP1)  
 $\sim 3 \times 10^5$  by  $z \sim 6$  (WMAP3)

# N-body + Radiative Transfer → Reionization simulation

- Radiative transfer simulations evolve the radiation field and nonequilibrium ionization state of the gas
  - New, fast, efficient C<sup>2</sup>-Ray code (Conservative, Causal Ray-Tracing) (Mellema, Ilev, Alvarez, & Shapiro 2006, *New Astronomy*, 11, 374) uses short-characteristics to propagate radiation throughout the evolving gas density field provided by the N-body results, re-gridded to  $(203)^3$  and  $(406)^3$  cells, for different resolution runs, from each and every galaxy halo source in the box.

e.g.  $N_{\text{halo}} \sim 4 \times 10^5$  by  $z \sim 8$  (WMAP1)

$\sim 3 \times 10^5$  by  $z \sim 6$  (WMAP3)

# Every galaxy in the simulation volume emits ionizing radiation

- We assume a constant mass-to-light ratio for simplicity:

$$\begin{aligned} f_{\gamma} &= \# \text{ ionizing photons released} \\ &\quad \text{by each galaxy per halo baryon} \\ &= f_{*} f_{\text{esc}} N_i, \end{aligned}$$

where  $f_{*}$  = star-forming fraction of halo  
baryons,

$f_{\text{esc}}$  = ionizing photon escape fraction,

$N_i$  = # ionizing photons emitted per stellar  
baryon over stellar lifetime

e.g.  $N_i = 50,000$  (top-heavy IMF),  $f_{*} = 0.2$ ,  $f_{\text{esc}} = 0.2 \rightarrow$   
 $f_{\gamma} = 2000$

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 $f_{\gamma} = 2000$

- This yields source luminosity:  $dN_{\gamma}/dt = f_{\gamma} M_{\text{bary}} / (\mu m_{\text{H}} t_{*})$ ,  
 $t_{*}$  = source lifetime (e.g.  $2 \times 10^7$  yrs),  
 $M_{\text{bary}}$  = halo baryonic mass

# $C^2$ - Ray : A New Method for Photon-Conserving Transport of Ionizing Radiation

Mellema, Iliev, Alvarez & Shapiro (2006) *New Astronomy*, 11, 374

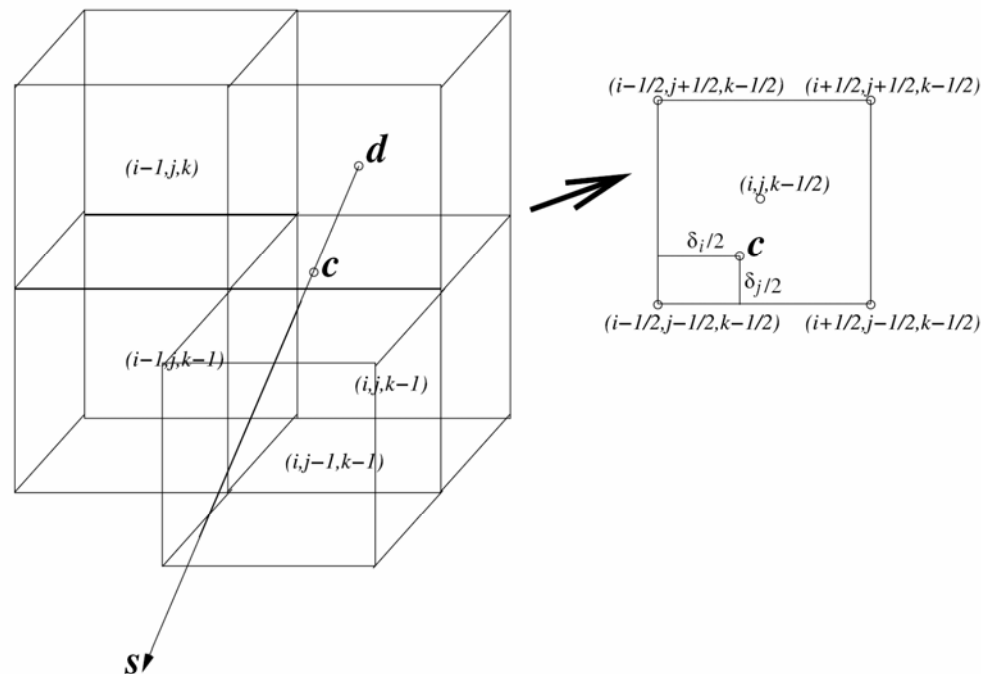
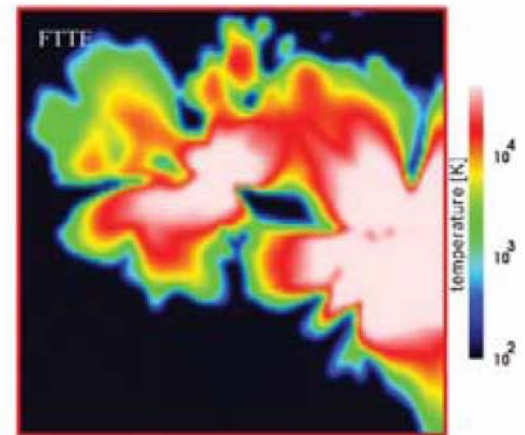
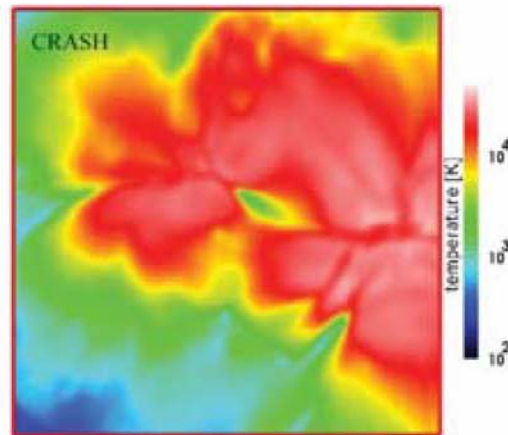
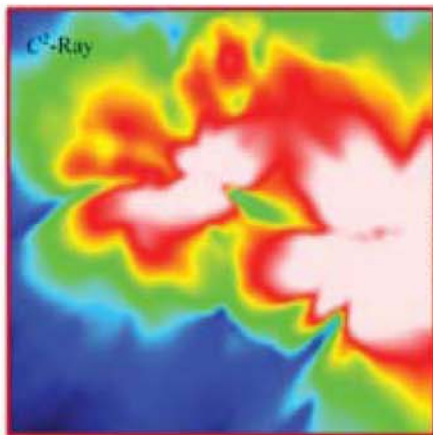


Fig. A.1. Short-characteristics ray tracing.



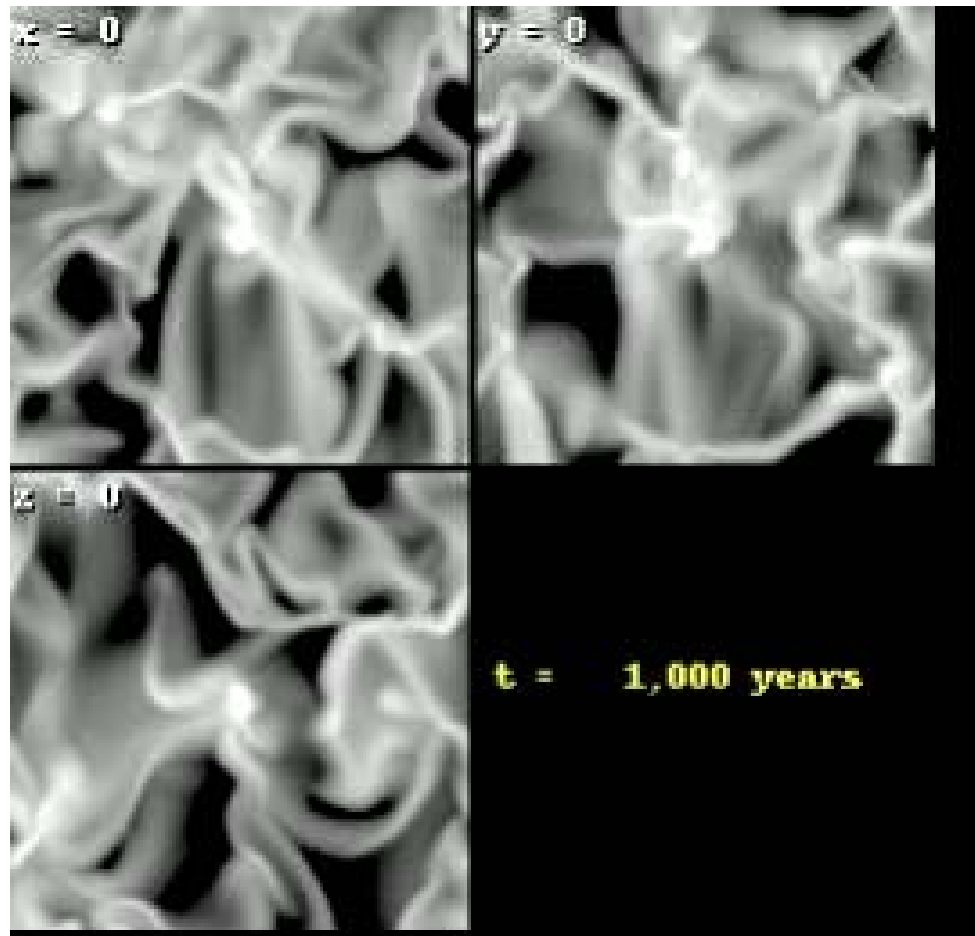
# Cosmological Radiative Transfer Codes Comparison Project I. : The Static Density Field Tests

Iliev, Ciardi, ..., Shapiro, ... (2006) MNRAS, 371, 1057



# Dynamical H II Region Evolution in Turbulent Molecular Clouds

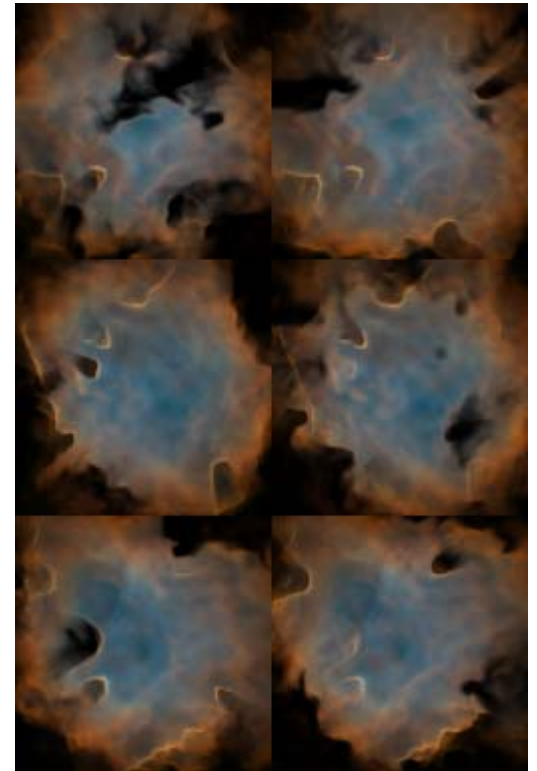
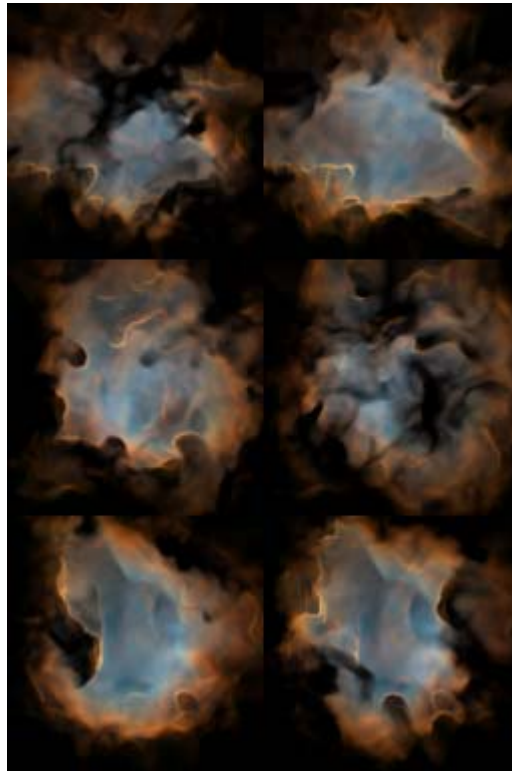
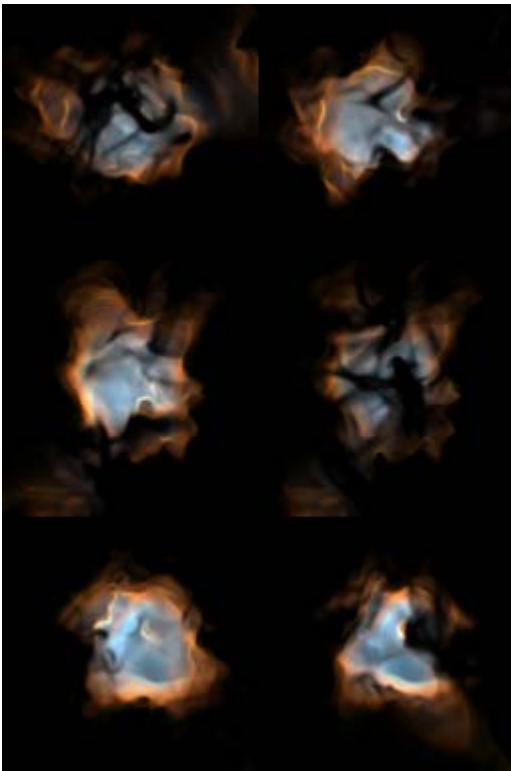
Mellema, Arthur, Henney, Iliev & Shapiro (2006) ApJ,  
647, 397 (astro-ph/0512187)





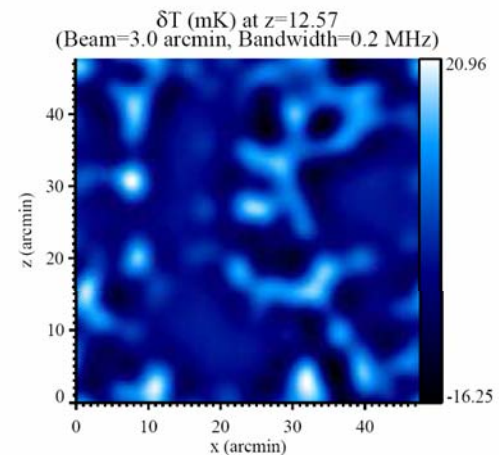
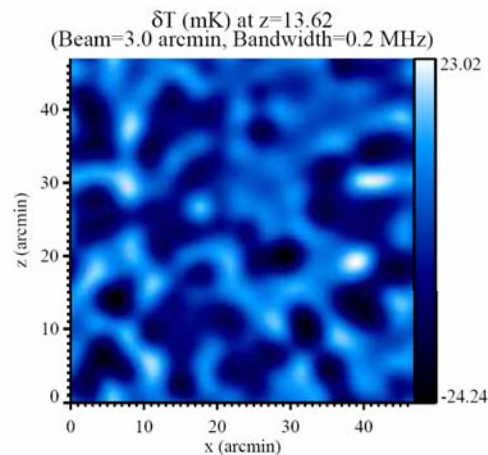
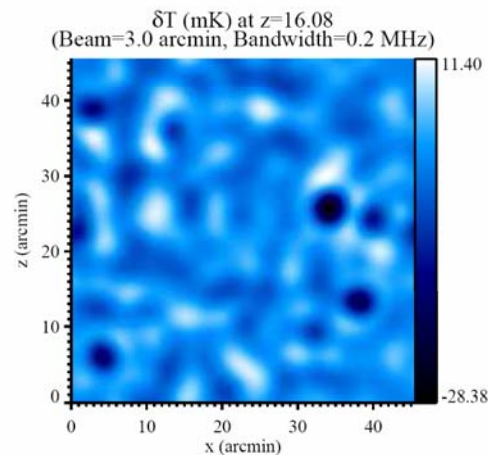
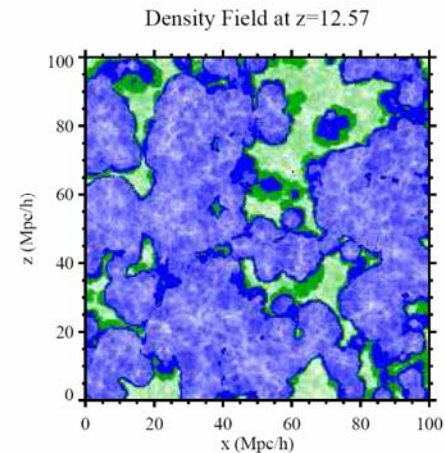
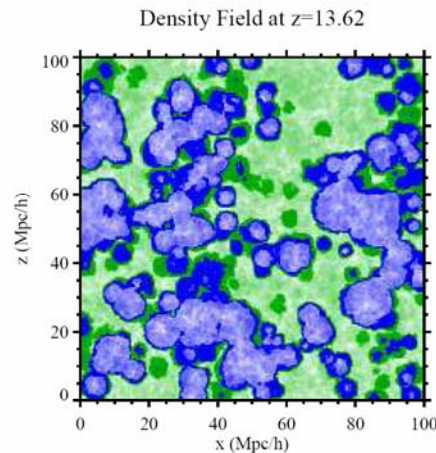
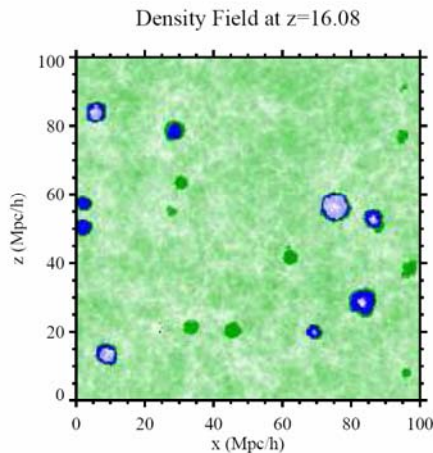
# Dynamical H II Region Evolution in Turbulent Molecular Clouds

Mellema, Arthur, Henney, Iliev & Shapiro (2006) ApJ,  
647, 397 (astro-ph/0512187)



# Simulating Reionization at Large Scales II : The 21-cm Emission Features and Statistical Signals

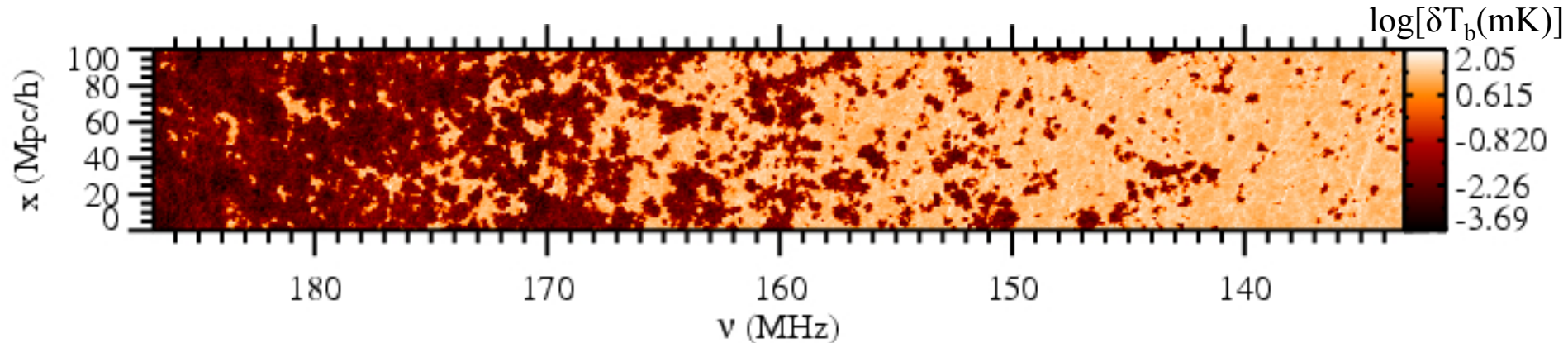
Mellema, Iliev, Pen, & Shapiro (2006), MNRAS, 372,679  
(astro-ph/0603518)



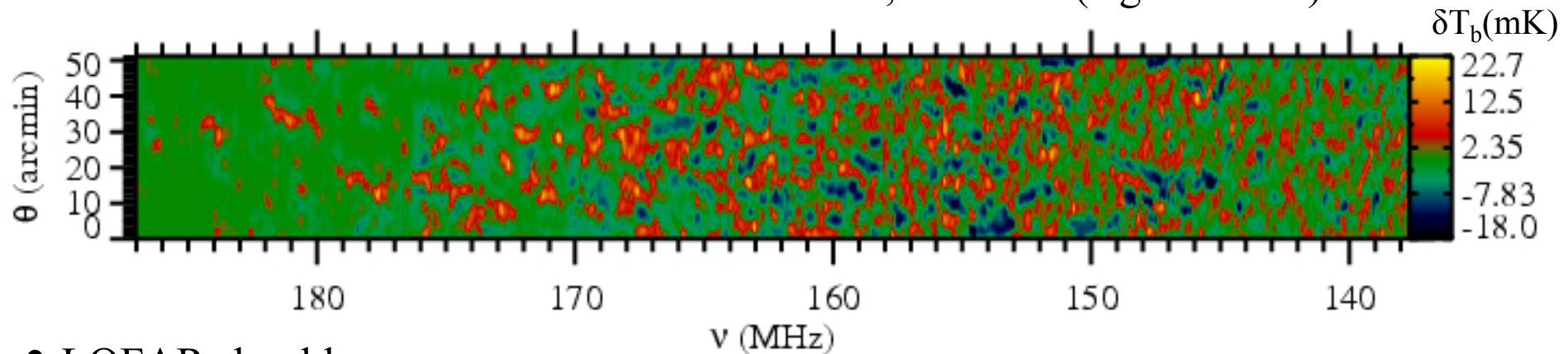
# Reionization topology revealed by fluctuations in 21-cm brightness temperature, $\delta T_b$ , along the line of sight

Iliev, Mellema, Pen, Bond, & Shapiro (2008), MNRAS, 384, 863 (astro-ph/0702099)

- mapping the sky along the LOS: high-resolution cuts in position-redshift space



- beam- and bandwidth-smoothed : 3 arcmin, 0.2 MHz (e.g. LOFAR)



- LOFAR should see  
large ionized bubbles!

Case:  $f_\gamma = 250$ , subgrid clumping factor  $C(z)$ , WMAP3



# Q: How large must a reionization simulation volume be to predict 21-cm background fluctuations?

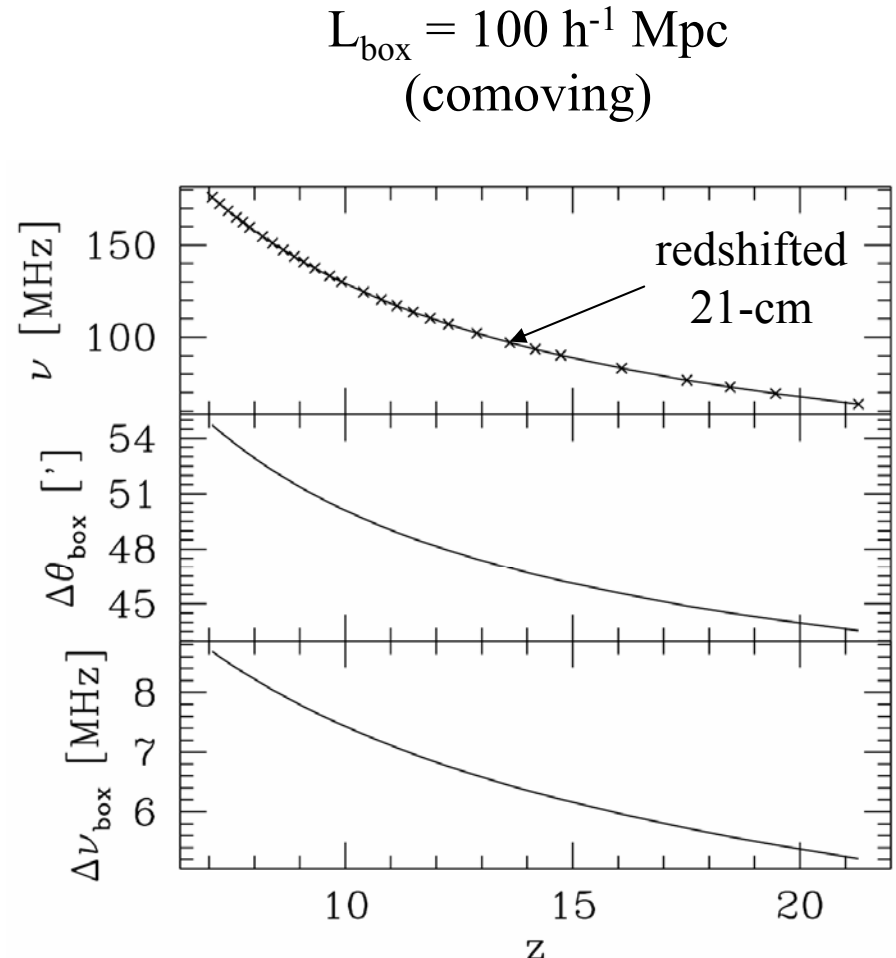
- Simulation volumes must exceed the beamsize and bandwidth of future radio arrays by a large enough factor to make 21-cm predictions meaningful.

e.g. for GMRT, MWA, LOFAR,

$$\Delta\theta_{\text{beam}} \geq 3'$$

$$\Delta\nu_{\text{bandwidth}} > 0.1 \text{ MHz}$$

- Our  $(143 \text{ Mpc})^3$  comoving volume simulation is the first to be large enough to predict 21-cm fluctuations.



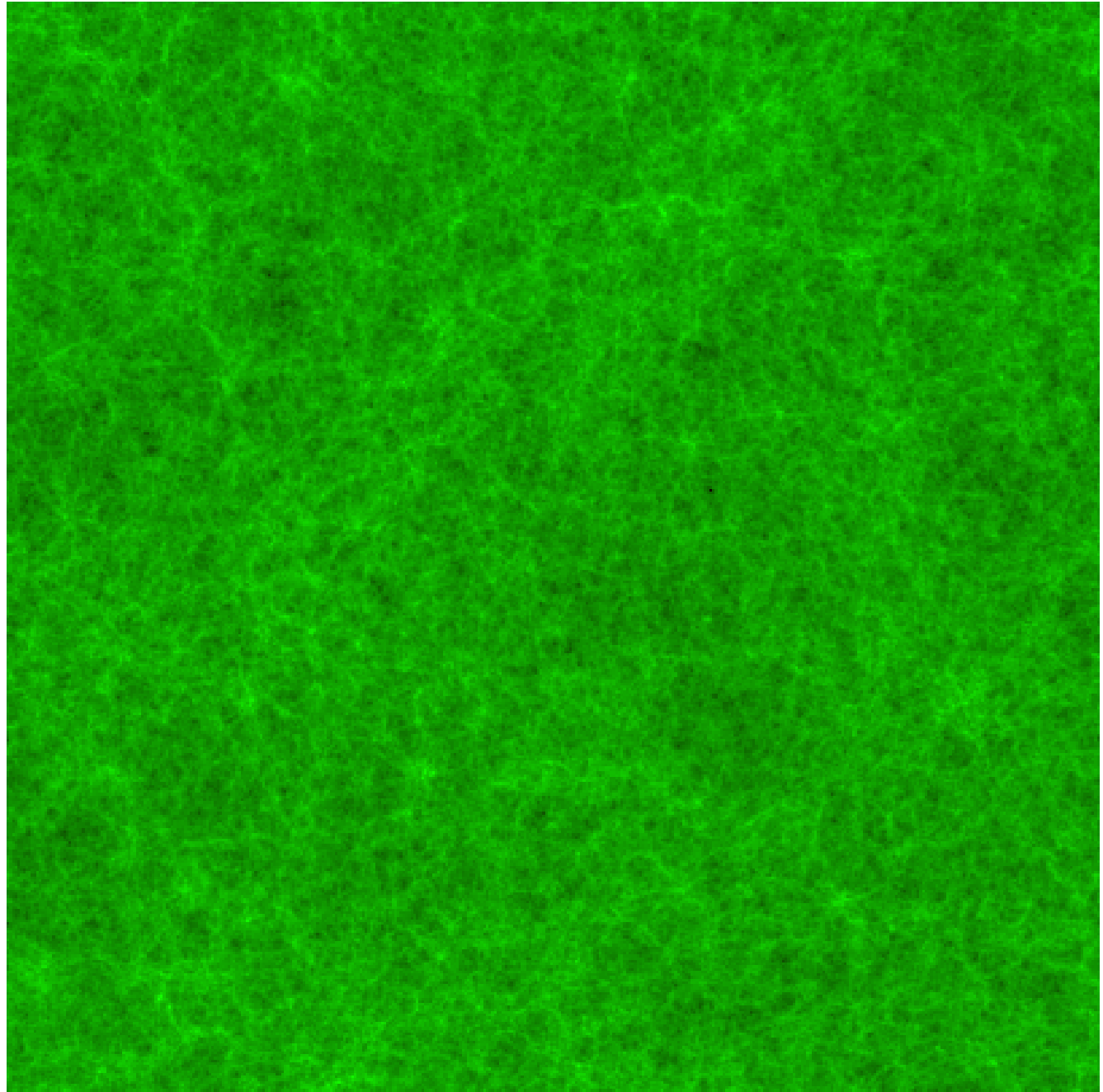
# The Geometry of Reionization

for source efficiency  
 $f_{\gamma} = 2000$

from  $z = 20$  to  $z = 12$

a cut through the  
simulation volume,  
one cell deep

gas density (green in  
neutral regions, yellow  
in ionized regions),  
H II regions (red)  
and  
sources (dots)



# Kinetic Sunyaev-Zel'dovich Effect from Patchy Reionization

- kSZ effect is the CMB temperature anisotropy induced by electron scattering by free electrons moving along the line-of-sight:

$$\frac{\Delta T}{T_{\text{CMB}}} = \int d\eta e^{-\tau_{\text{es}}(\eta)} a n_e \sigma_T \mathbf{n} \cdot \mathbf{v},$$

where  $\eta$  is conformal time,

$$\eta = \int_0^t dt' / a(t')$$

# $(\delta T/T_{\text{CMB}})$ Maps of the Kinetic Sunyaev-Zel'dovich Effect from Radiative Transfer Simulations of Patchy Reionization

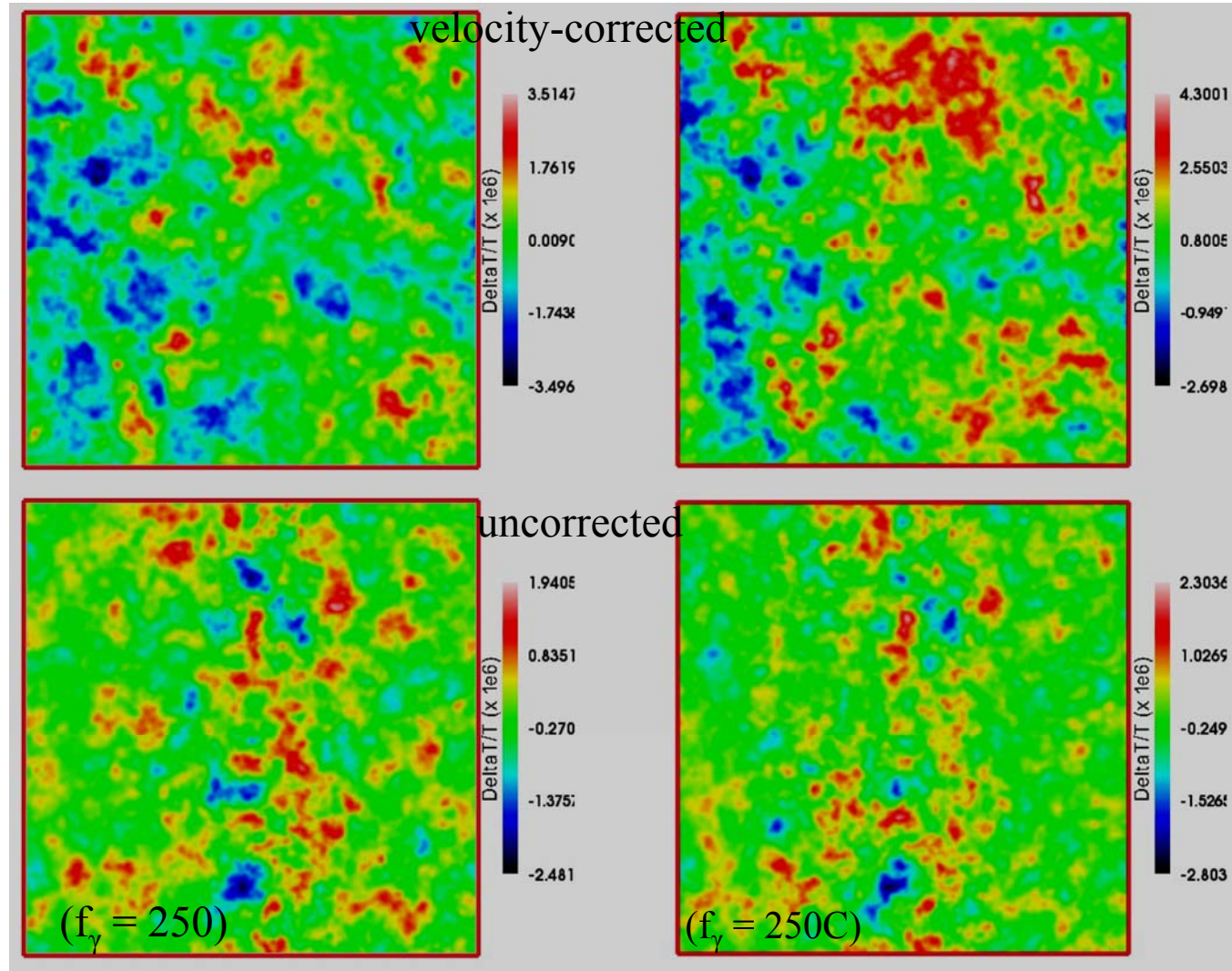
Iliev, Pen, Bond, Mellema & Shapiro (2007), ApJ, 660, 933; (astro-ph/0609592)

Iliev, Mellema, Pen, Bond, & Shapiro (2008), MNRAS, 384, 863; (astro-ph/0702099)

- Box size 100/h  
Mpc comoving  
→ 50' x 50'

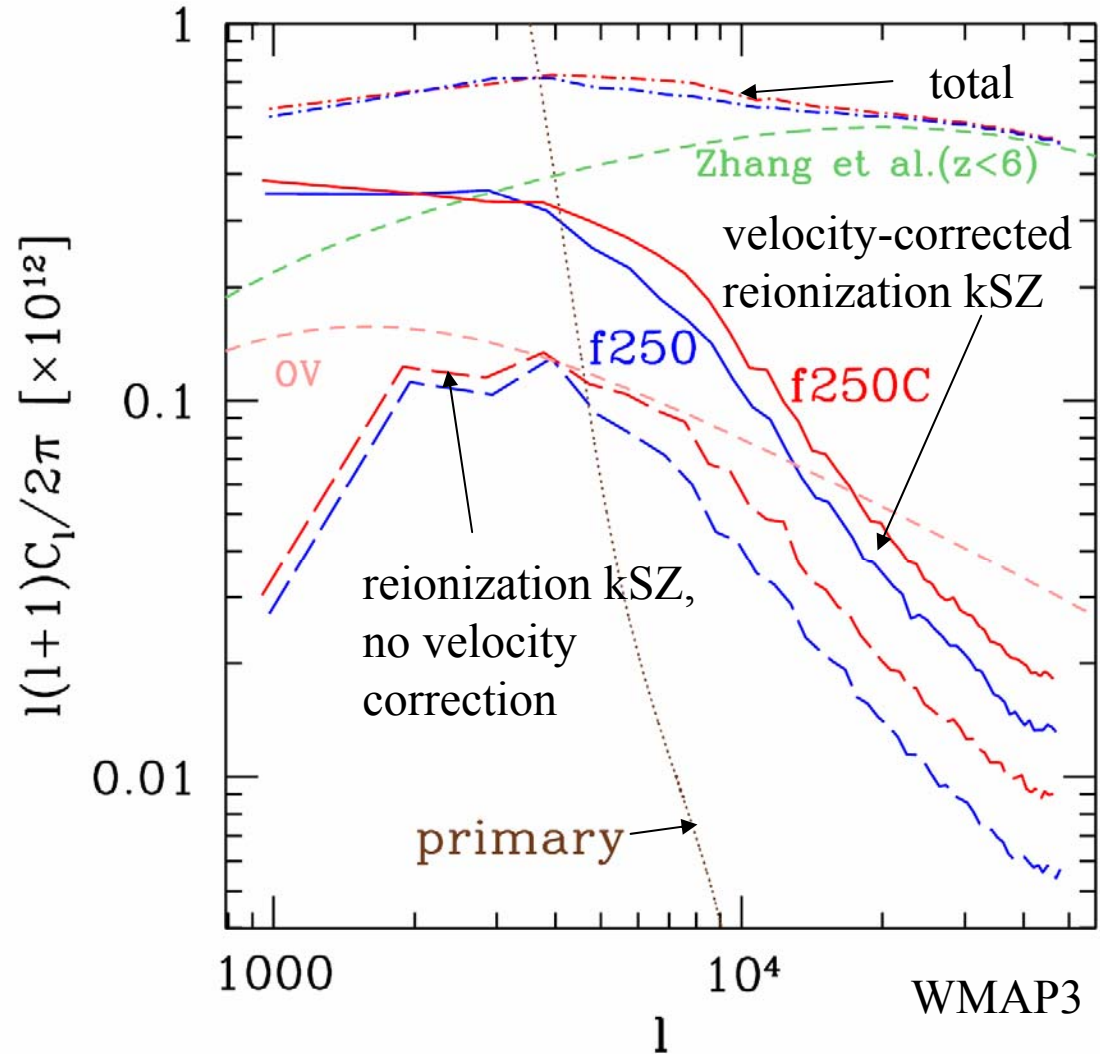
- Even so large a  
box is missing  
large-scale  
power in  
velocity field  
perturbations

- must correct  
for missing  
large-scale  
velocity  
perturbations



# kSZ CMB Anisotropy Signal: Sky Power Spectra of $\delta T_{\text{kSZ}} / T_{\text{CMB}}$

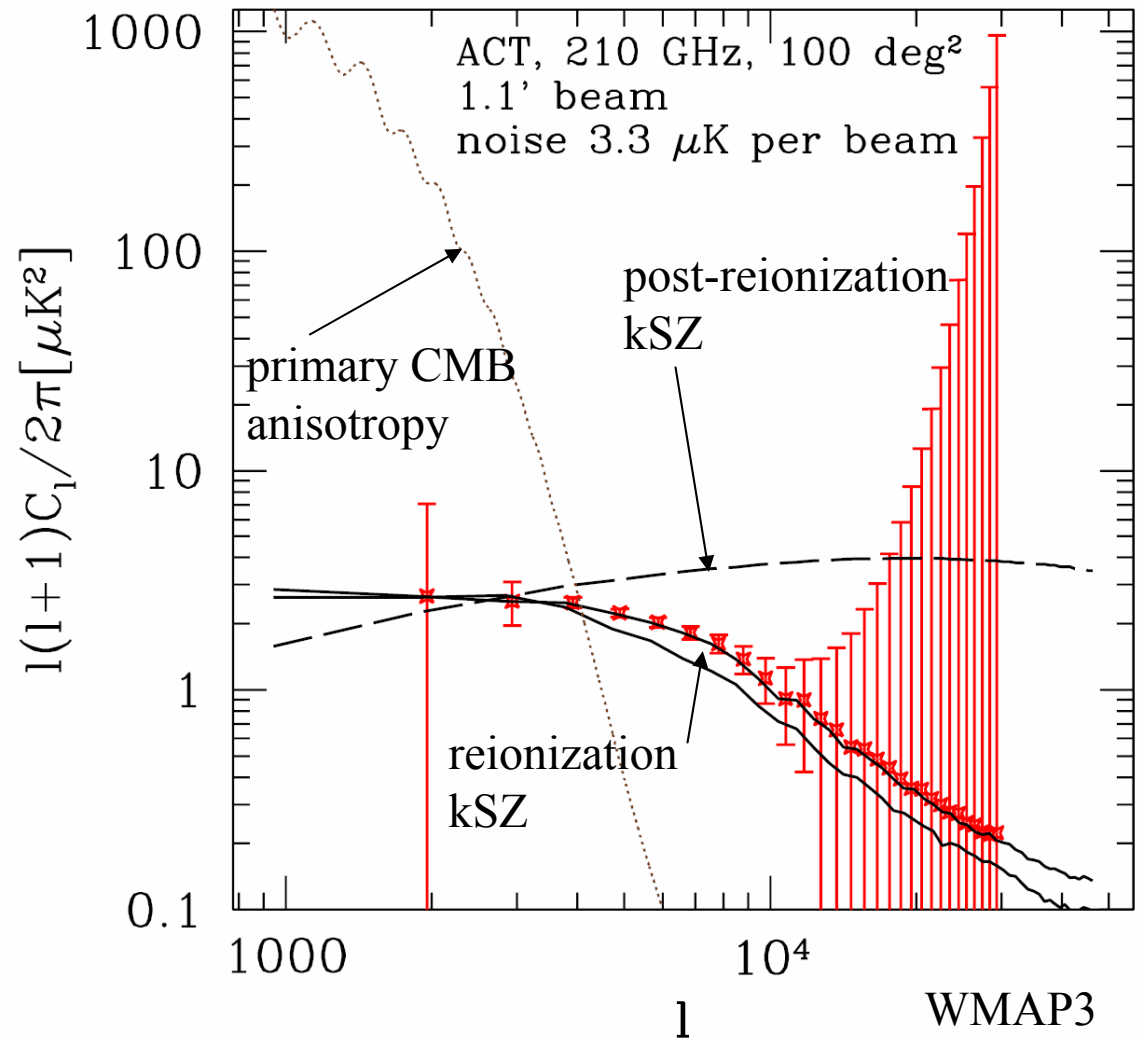
- kSZ anisotropy from inhomogeneous reionization dominates primary CMB anisotropy for  $\ell > 4000$ , peaking at  $\ell = 3000 - 4000$ , determined by typical sizes of H II regions,  $5 - 20$  Mpc.
- Patchy reionization doubles *total* kSZ for  $\ell = 3000 - 10,000$  compared to homogeneous reionization with the same total  $\tau_{\text{es}}$ .
- This predicted kSZ signal at arcminute scale experiments. e.g. Atacama Cosmology Experiment ( $\sim 1'$  resolution,  $\sim \mu\text{K}$  sensitivity).





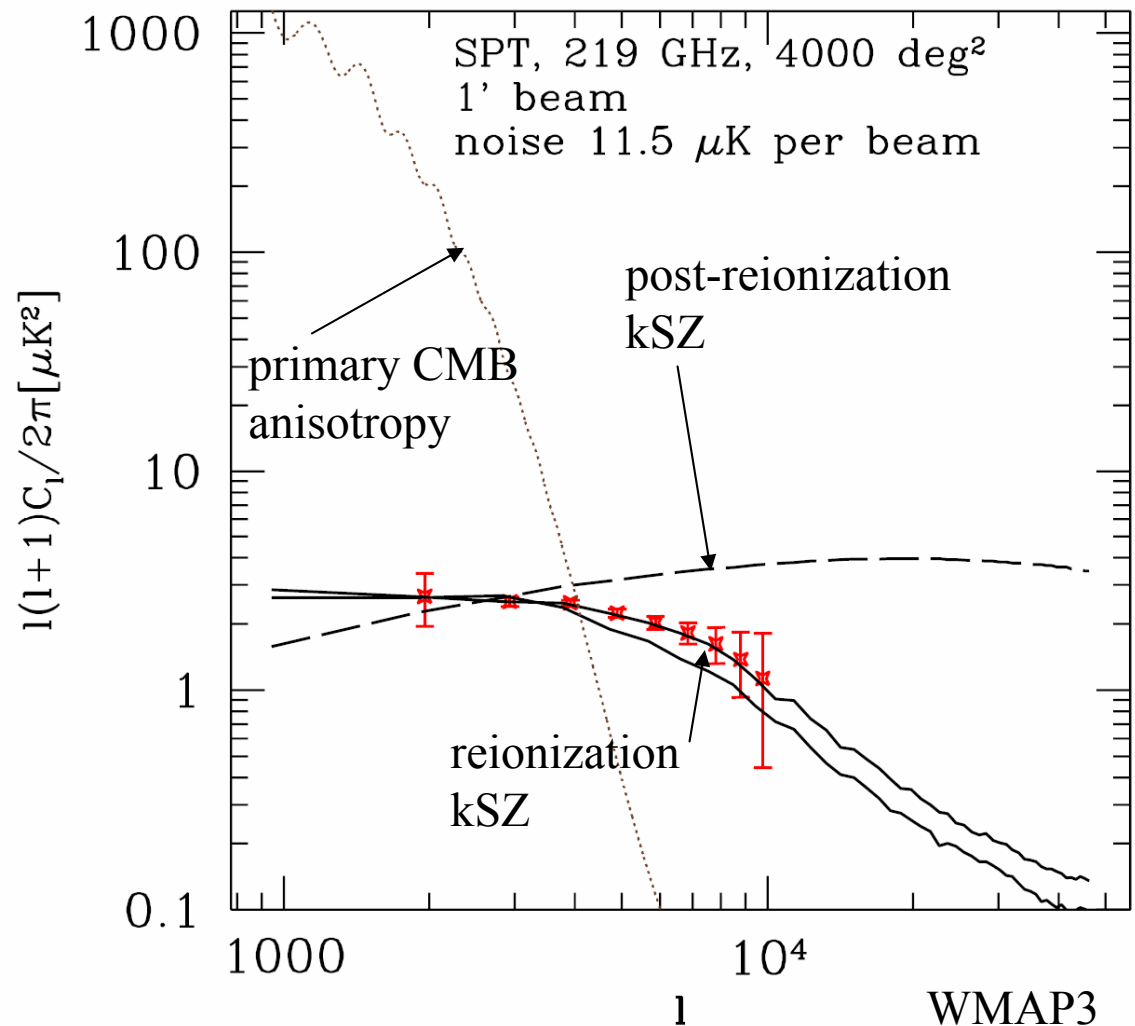
# Observability of the kSZ from reionization: sky power spectrum

- Predicted kSZ from reionization simulations and *Atacama Cosmology Telescope* (ACT) expected sensitivity;
- primary CMB and post-reionization kSZ added to noise error bars for reionization signal;
- reionization kSZ signal is comparable to that from post-reionization, so necessary to separate them to extract info on reionization, alone.
- In principle, results show that reionization signal should be observable.



# Observability of the kSZ from reionization: sky power spectrum

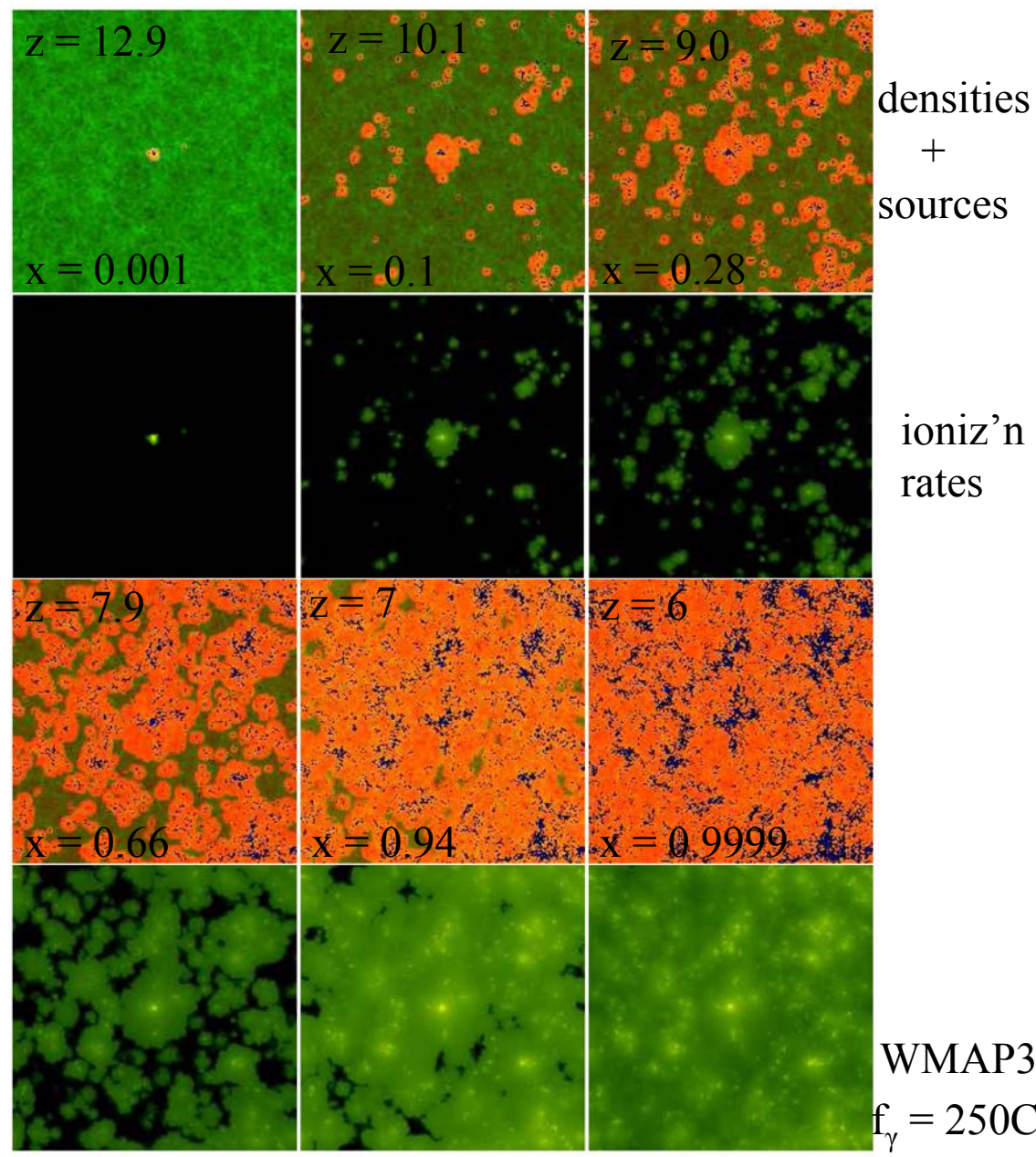
- Predicted kSZ from reionization simulations and *South Pole Telescope* (SPT) expected sensitivity;
- primary CMB and post-reionization kSZ added to noise error bars for reionization signal;
- reionization kSZ signal is comparable to that from post-reionization, so necessary to separate them to extract info on reionization, alone.
- In principle, results show that reionization signal should be observable.



# Effect of IGM on Observability of Ly- $\alpha$ Sources During Reionization

Iliev, Shapiro, McDonald, Mellema, Pen 2007, MNRAS, submitted, astro-ph/0711.2944

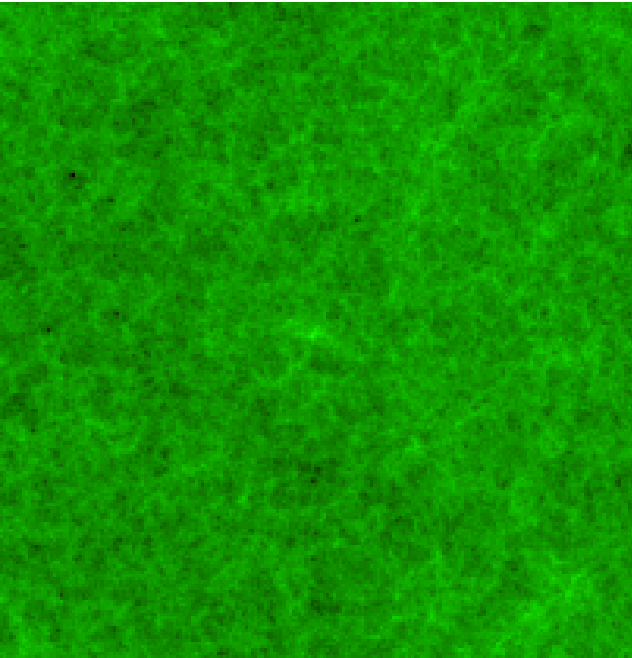
- reionization, centered on most massive halo in  $(100h^{-1} \text{ Mpc})^3$ :  
 $M(z = 6) = 1.5 \times 10^{12} M_{\text{solar}} \rightarrow$   
rare ( $\sim 5\text{-}\sigma$ ) density peak  $\rightarrow$   
bright Ly- $\alpha$  emitter ;
- H II regions form first around such density peaks and grow continuously, as halos form inside, clustered around peak  $\rightarrow$   
Ly- $\alpha$  emitters will be centered on large HII regions ;  
(blue dots = source cells)
- Fluctuating GP optical depth inside H II regions can still affect Ly- $\alpha$  source detection, though;



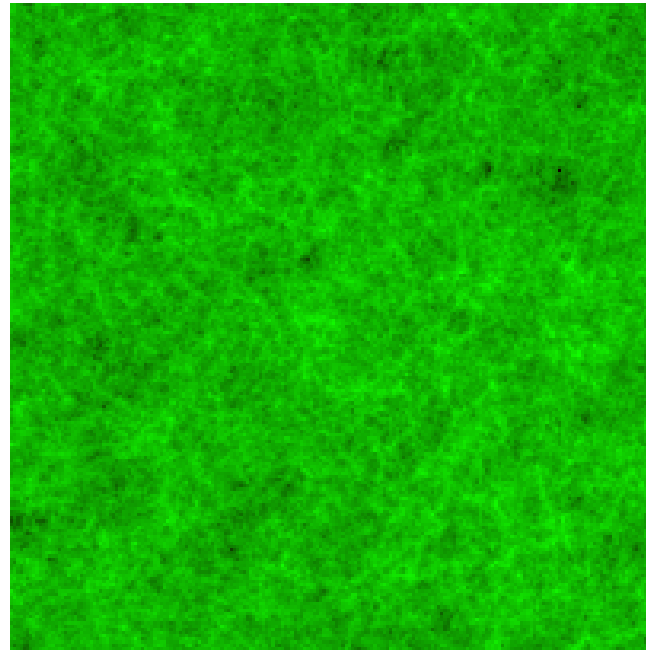
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Iliev, Shapiro, McDonald, Mellema, Pen 2007, MNRAS, submitted, astro-ph/0711.2944

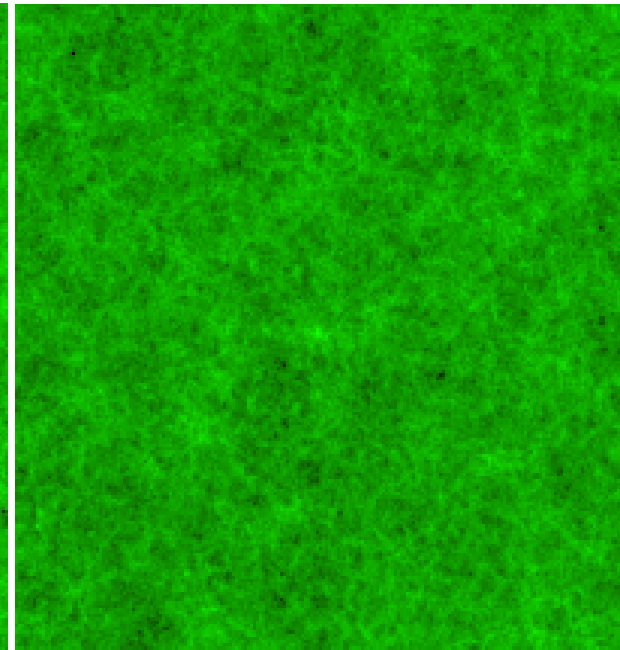
← 143 Mpc →



xZ



xy



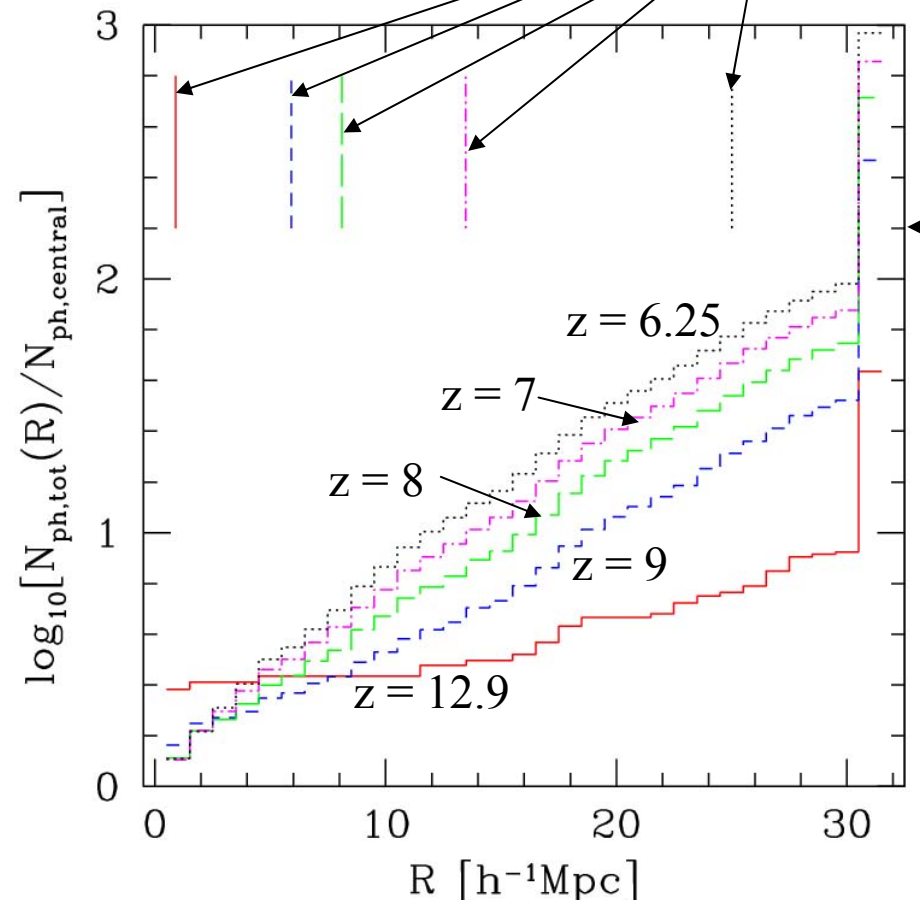
yz

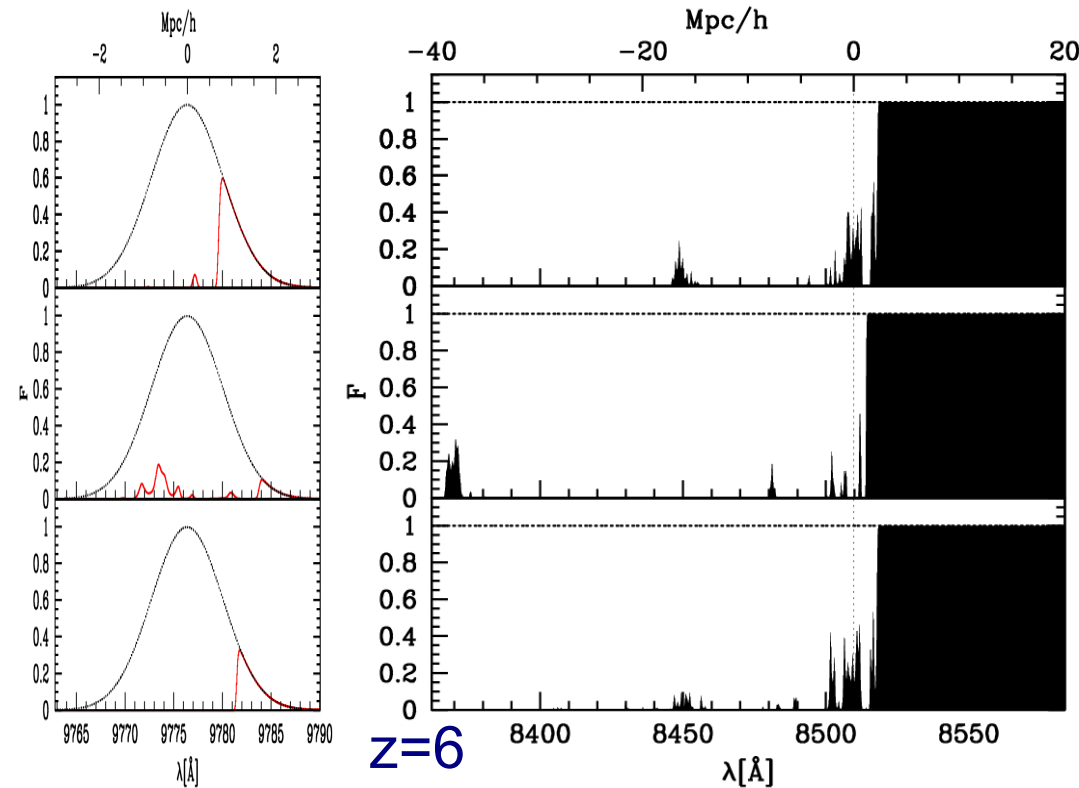
# Q: Do luminous Lyman alpha emitters observed during the EOR dominate the ionization of their own H II regions?

- **A:** not really (“they get by with a little help from their friends...”)
  - LAE forms at high- $\sigma$  density peak, surrounded by a cluster of smaller mass halos  $\rightarrow$  smaller halos dominate ionization
  - e.g. most massive source contributed only  
~50% by  $z = 12.9$   
~10% by  $z = 7$   
~1% by  $z = 6.25$ !

# ionizing photons released over time by halos within a sphere of distance  $R$  from most massive object

H II region sizes @  $z = 12.9, 9, 8, 7, 6.25$



$x_{\text{HI}}, n, \tau$ 



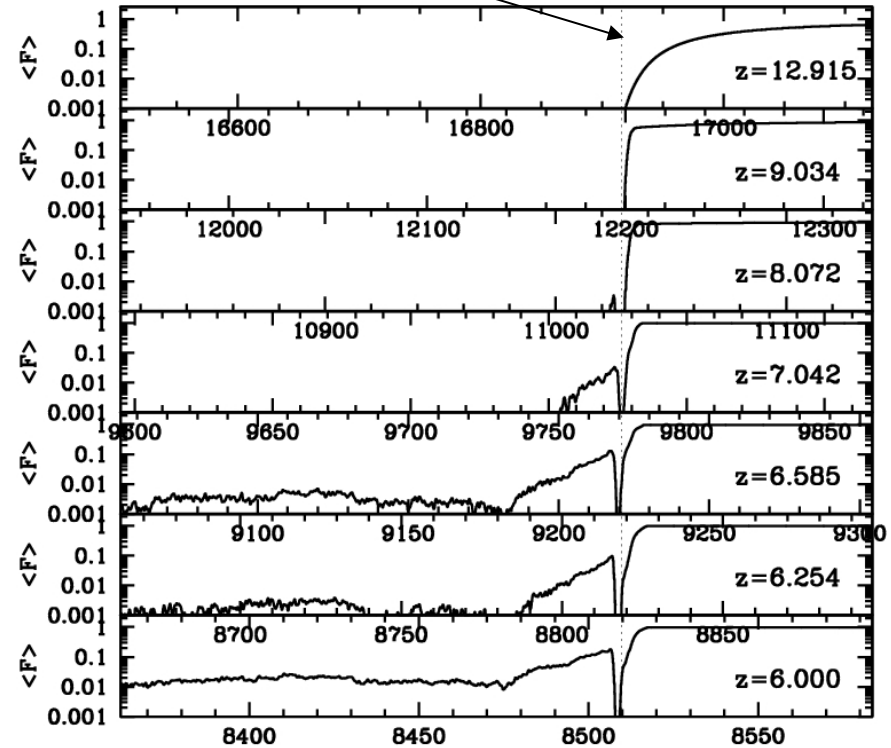
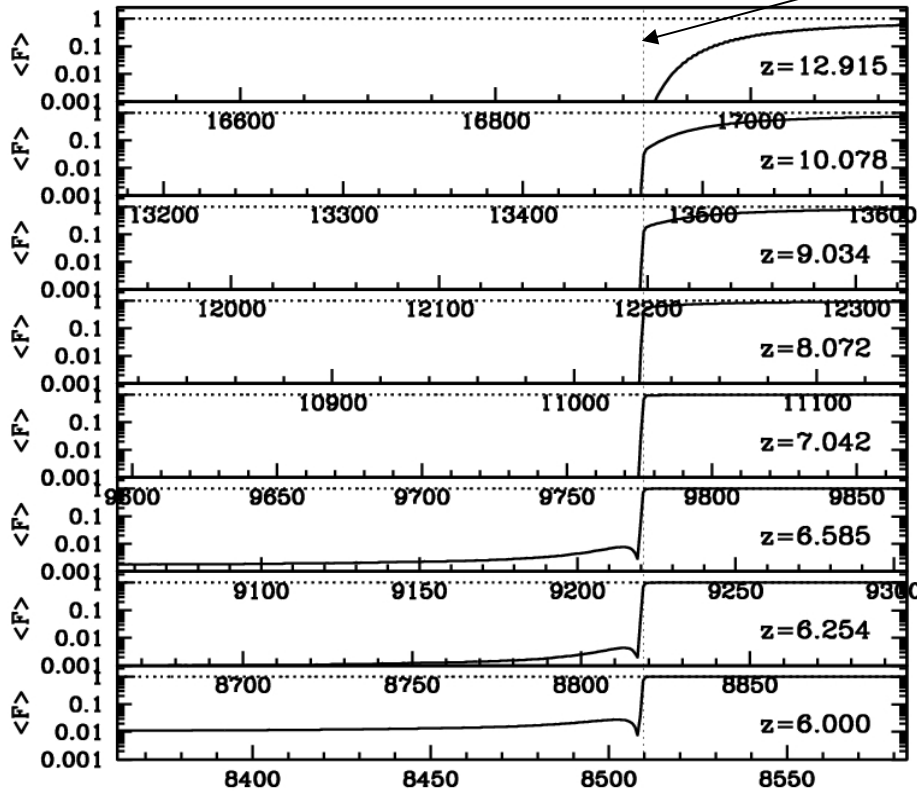
# Mean Ly- $\alpha$ transmission vs. redshift

- Strong damping wings at  $z > 10$ , only minor differences between average and luminous source.
- Some transmission on blue side of line, as IGM slowly becomes transparent; large proximity transmission region for luminous sources.

Average (typical source)

redshifted Ly  $\alpha$

Luminous source

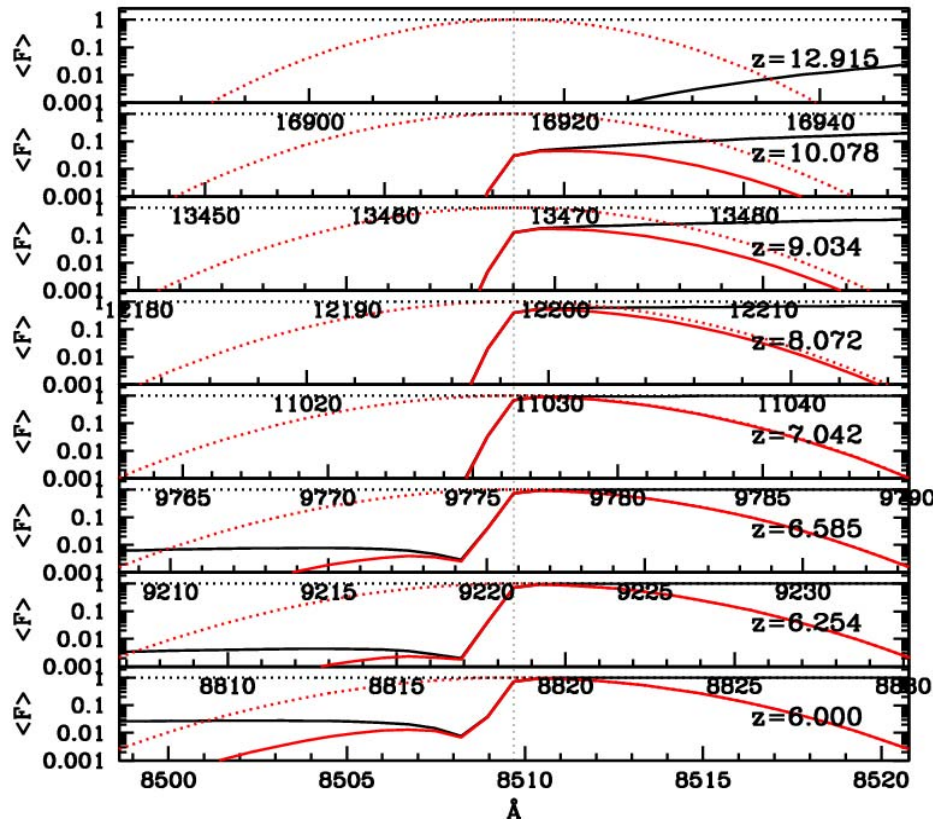


spherically-averaged transmission around sources

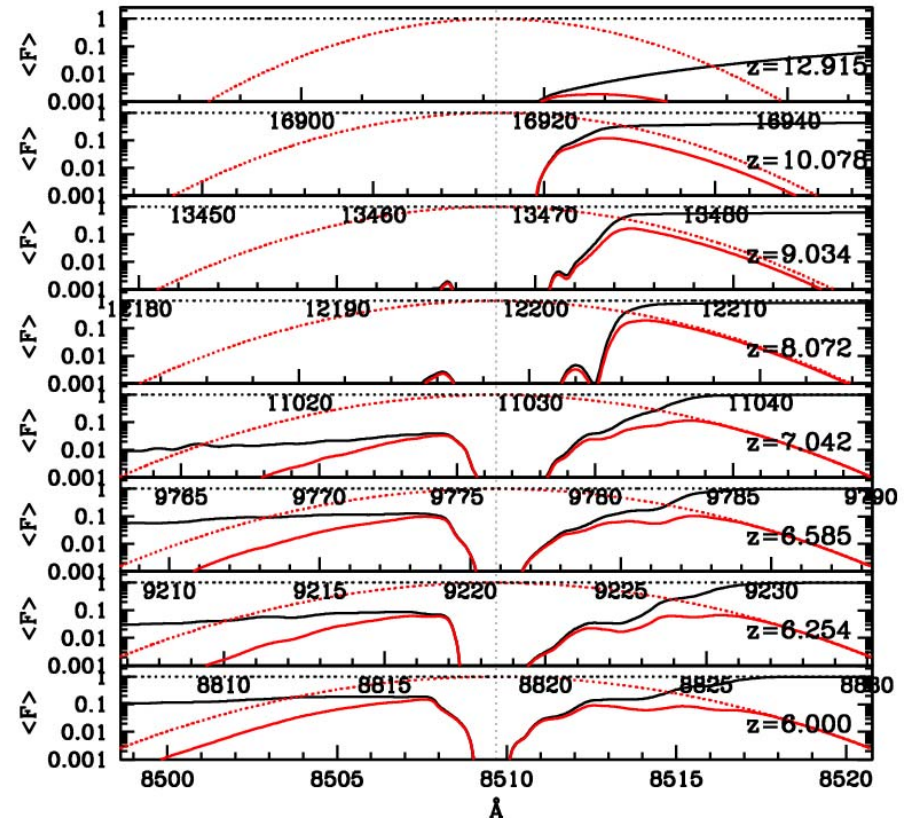
# Mean transmitted Ly- $\alpha$ line profile vs. redshift

- Mostly, the red wing comes through (but damped at  $z > 10$ ).
- Infall more important for luminous sources, changes the line shape.

Average (typical source)



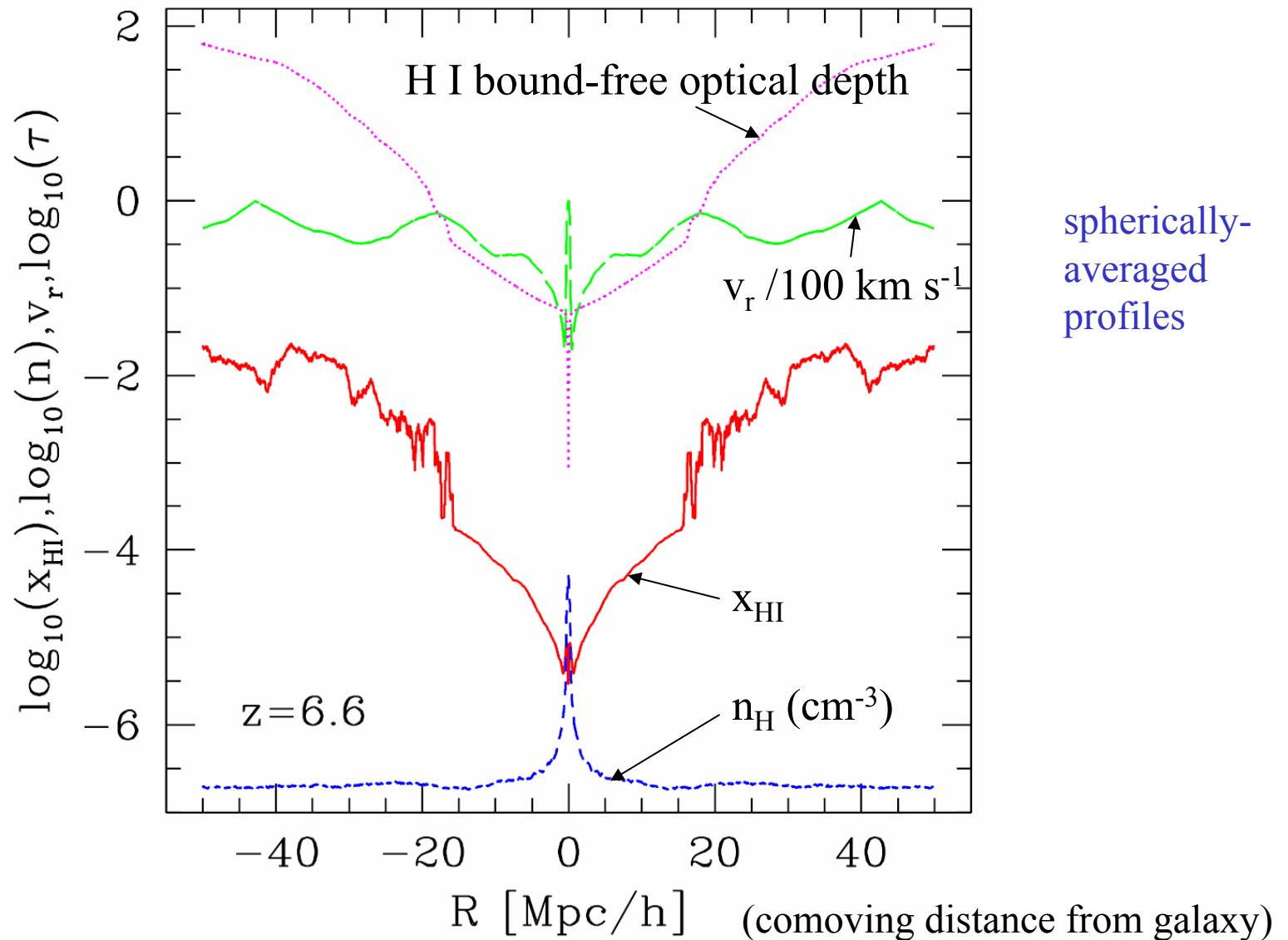
Luminous source



spherically-averaged transmitted line profiles

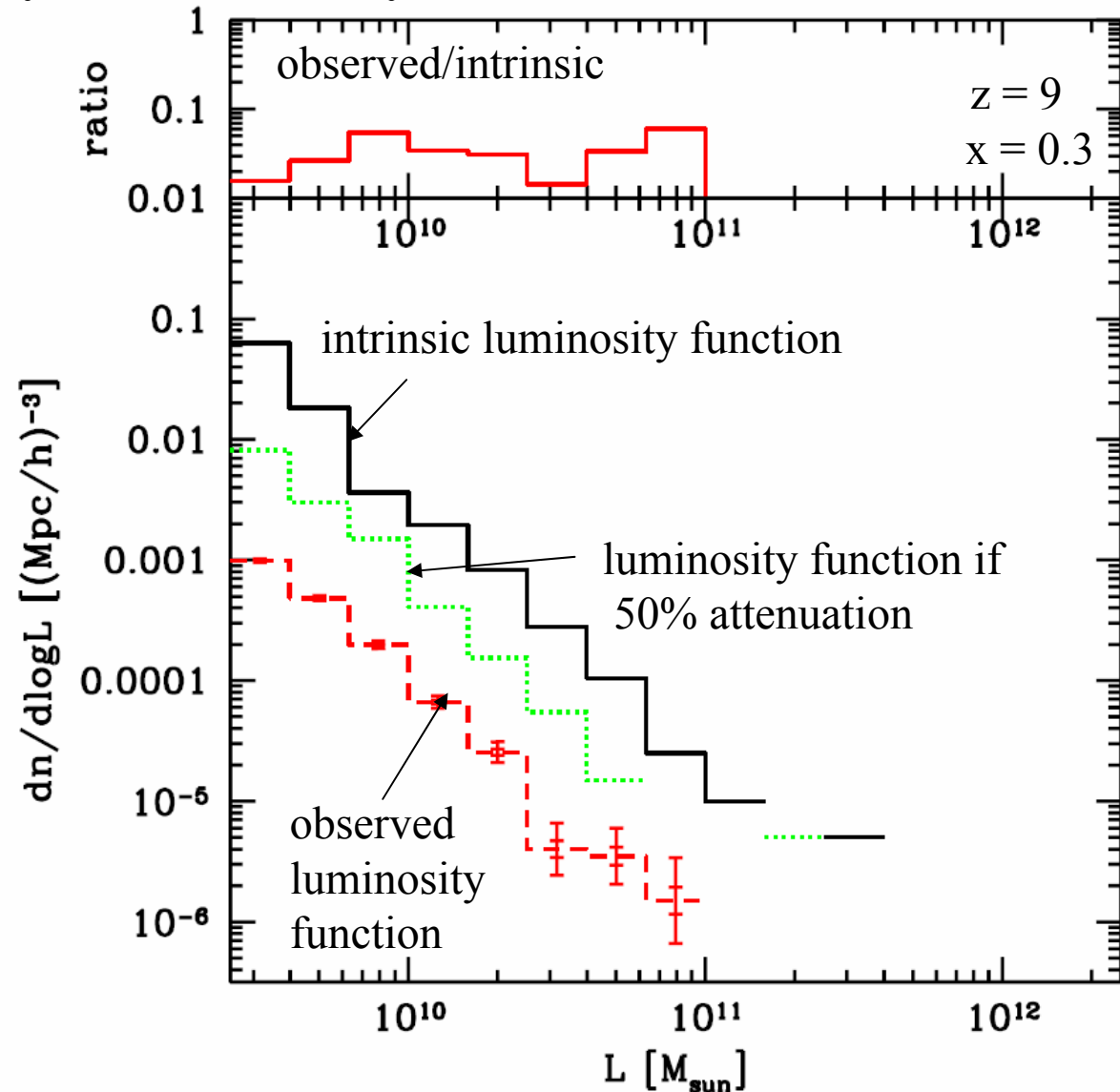


# The Intergalactic Medium Surrounding the Most Massive Galaxy at the End of Reionization : $\langle x_{\text{H II}} \rangle = 99\%$



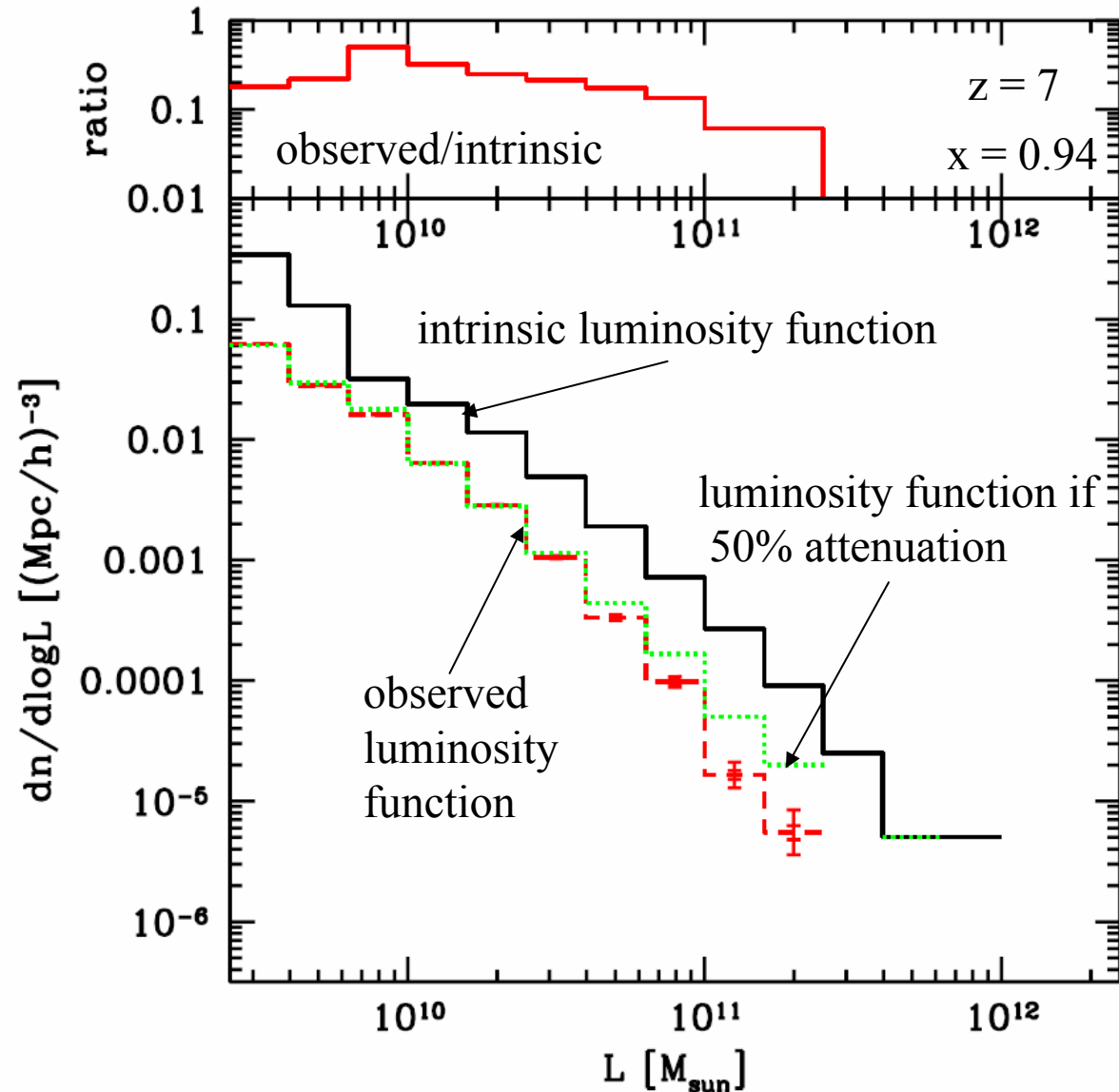
# Luminosity Function of High-Redshift Ly- $\alpha$ Sources is Filtered By the Partially Ionized IGM

- Assuming all halos are Ly- $\alpha$  emitters with  $M/L = \text{constant}$  and 160 km/s Gaussian line profile;
- At  $z = 9$ , observed luminosity function is reduced by 0.01 -0.1 from intrinsic luminosity function;
- Attenuation exceeds 50% (i.e. blue-half absorbed, red-half not), since damping wings reduce the red-half, as well..



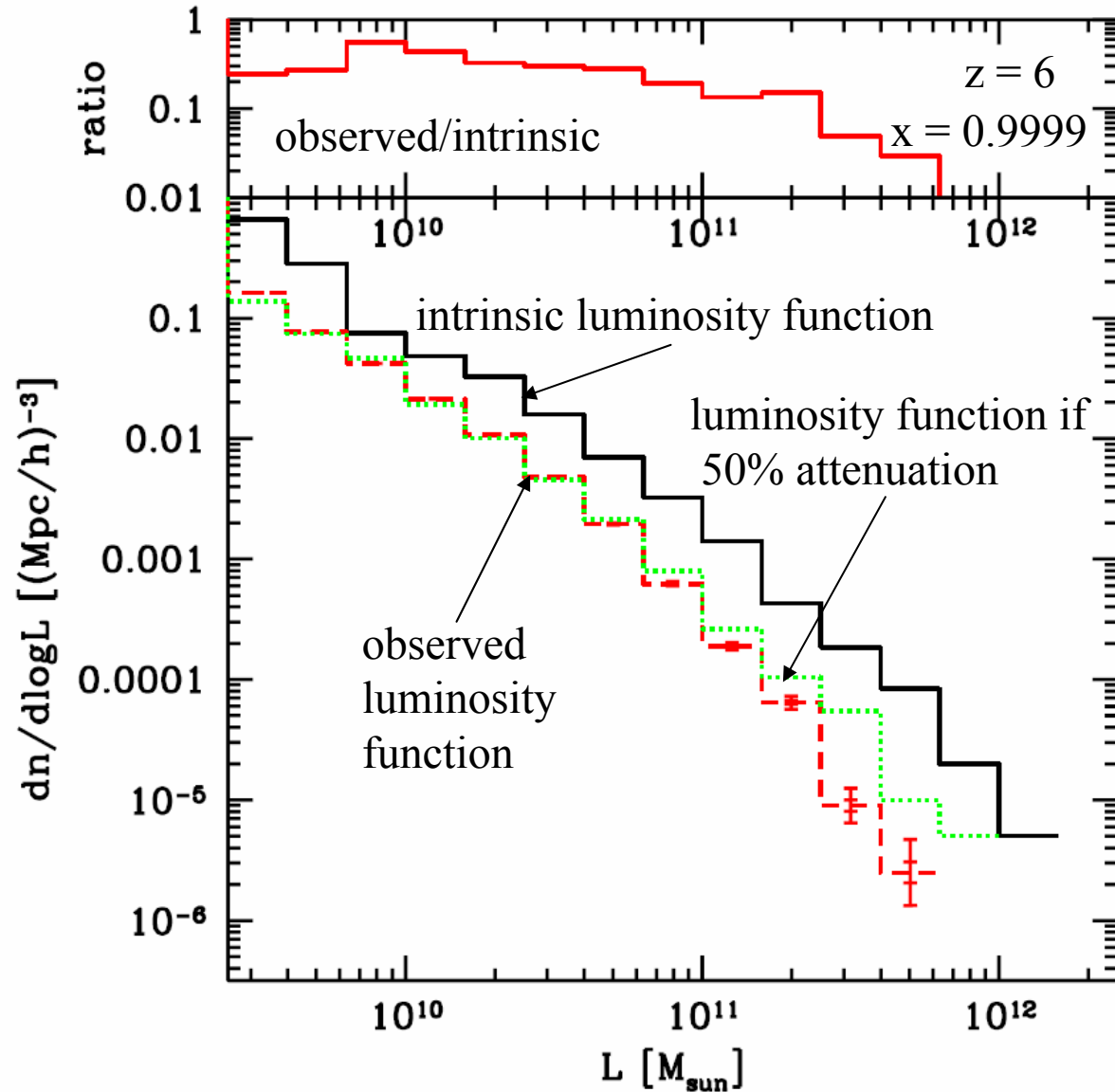
# Luminosity Function of High-Redshift Ly- $\alpha$ Sources is Filtered By the Partially Ionized IGM

- Assuming all halos are Ly- $\alpha$  emitters with  $M/L = \text{constant}$  and 160 km/s Gaussian line profile;
- At  $z = 7$ , observed luminosity function is reduced by 0.5 from intrinsic luminosity function, except at bright end where factor is 0.1 or below;
- Attenuation exceeds 50% (i.e. blue-half absorbed, red-half not), now, only at bright end.



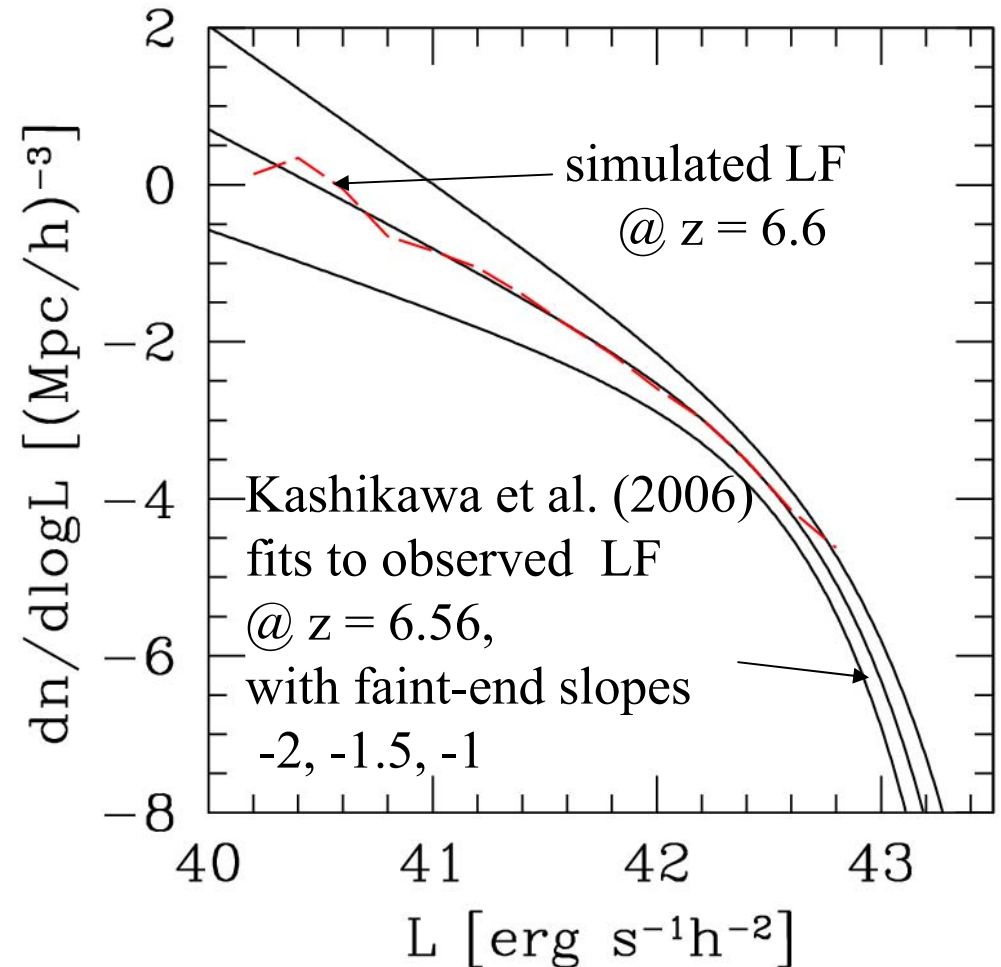
# Luminosity Function of High-Redshift Ly- $\alpha$ Sources is Filtered By the Partially Ionized IGM

- Assuming all halos are Ly- $\alpha$  emitters with  $M/L = \text{constant}$  and 160 km/s Gaussian line profile;
- Even at  $z = 6$ , observed luminosity function is reduced by 0.5 from intrinsic luminosity function, except at bright end where factor is 0.1 or below;
- Attenuation exceeds 50% (i.e. blue-half absorbed, red-half not), now, but only at bright end.



# Predicting the observed luminosity function of Ly- $\alpha$ sources at the end of the EOR : simulations vs. observations

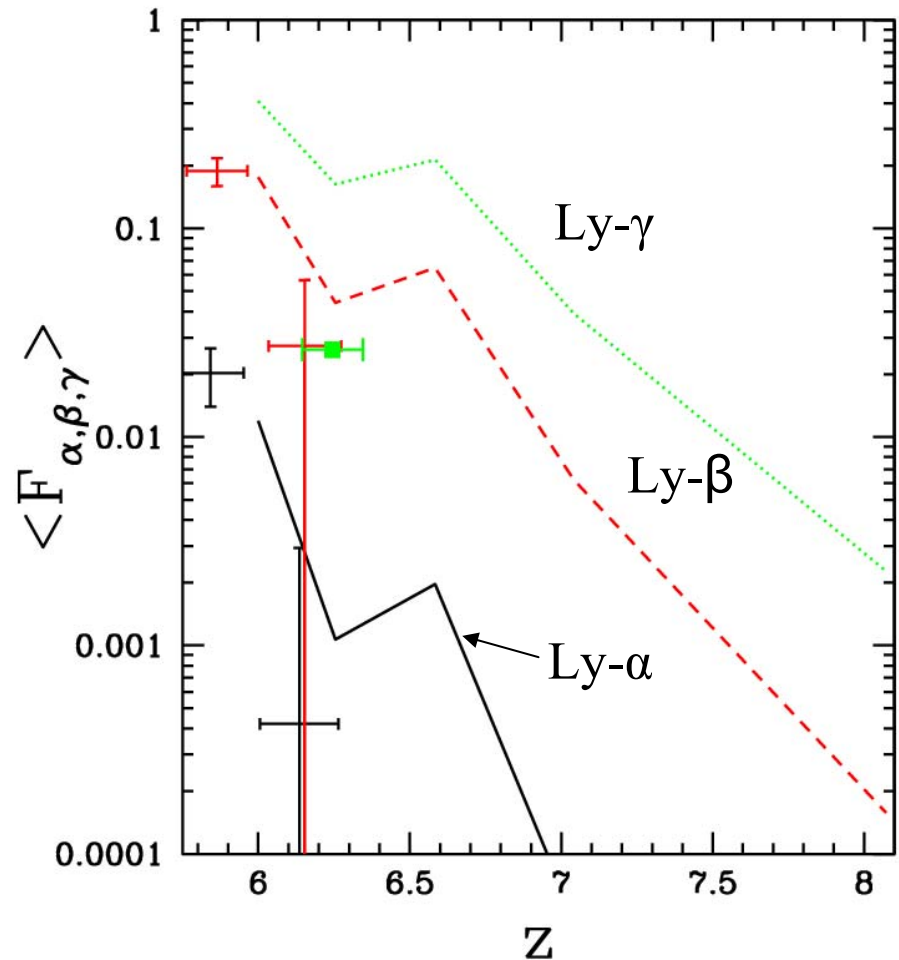
- To use our simulations to predict the observed LF, we “tune” the assumed M/L per halo to match the number density of sources in our simulations to the observed one reported by Kashikawa et al. (2006)
- → simulated LF is an excellent match of the shape, for an assumed faint-end slope of -1.5 for the fit to the observations.
- → the **majority** of sources responsible for reionization are **too faint** to be observed at present.



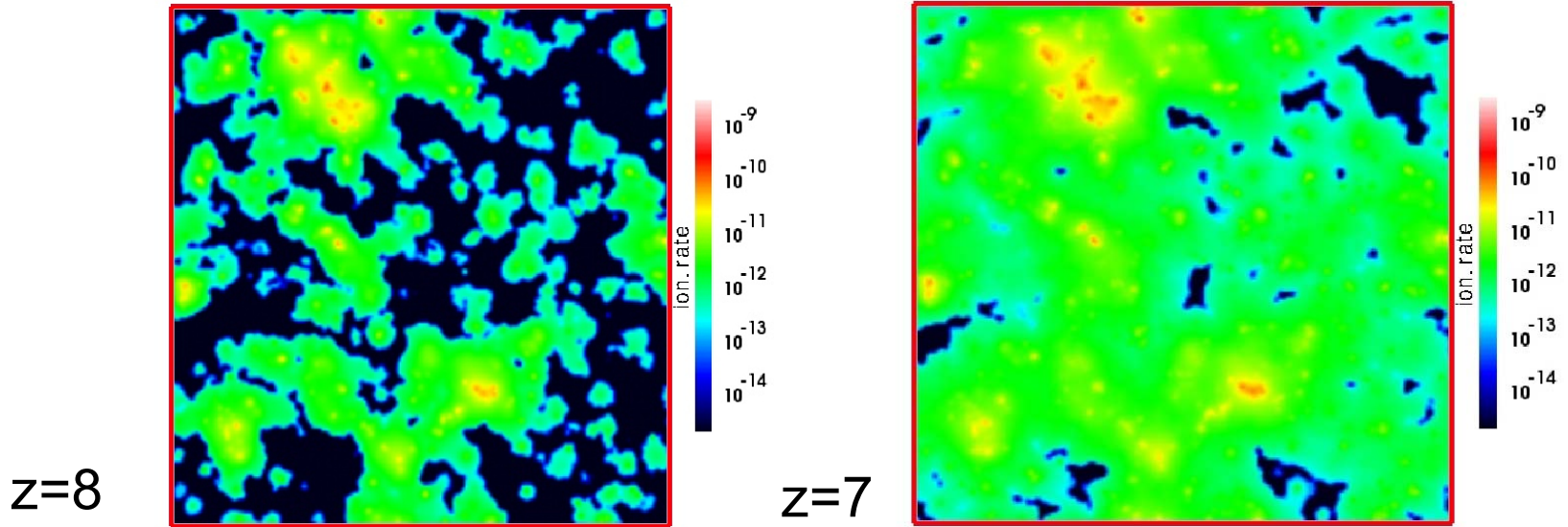


# Mean IGM transmission due to Lyman-line resonance scattering at the end of the EOR : the Gunn-Peterson Effect at $z > 6$

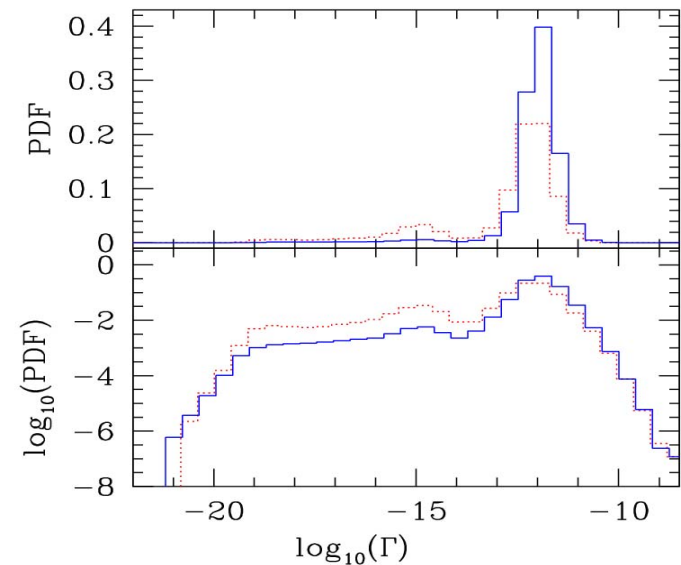
- Simulations predict the Ly- $\alpha$ , Ly- $\beta$ , and Ly- $\gamma$  opacity of the IGM and its evolution during the EOR  $\rightarrow$  compare with the absorption spectra of observed high-redshift quasars to test the theory and the efficiencies assumed for the release of ionizing photons by early galaxies.
- e.g. for this illustrative simulation, EOR ended a bit too early to match the data from Fan et al. (2006)  $\rightarrow$  predicts somewhat higher transmission than observed, but captures the observed trend with redshift well  $\rightarrow$  lower source efficiencies are required for a better fit.
- Higher- $z$  data can constrain reionization parameters better.



# The inhomogeneous intergalactic photoionization rate during the EOR



- Photoionization rates highly inhomogeneous
- Ionization is non-equilibrium behind I-fronts
- Average rate peaks at  $\Gamma_{-12} \sim 1$  (@  $z = 6$ )  
(post-overlap)



# Self-Regulated Reionization

Iliev, Mellema, Shapiro, & Pen (2007), MNRAS, 376, 534; (astro-ph/0607517)

- Jeans-mass filtering →

low-mass source halos

( $M < 10^9 M_{\text{solar}}$ ) cannot form

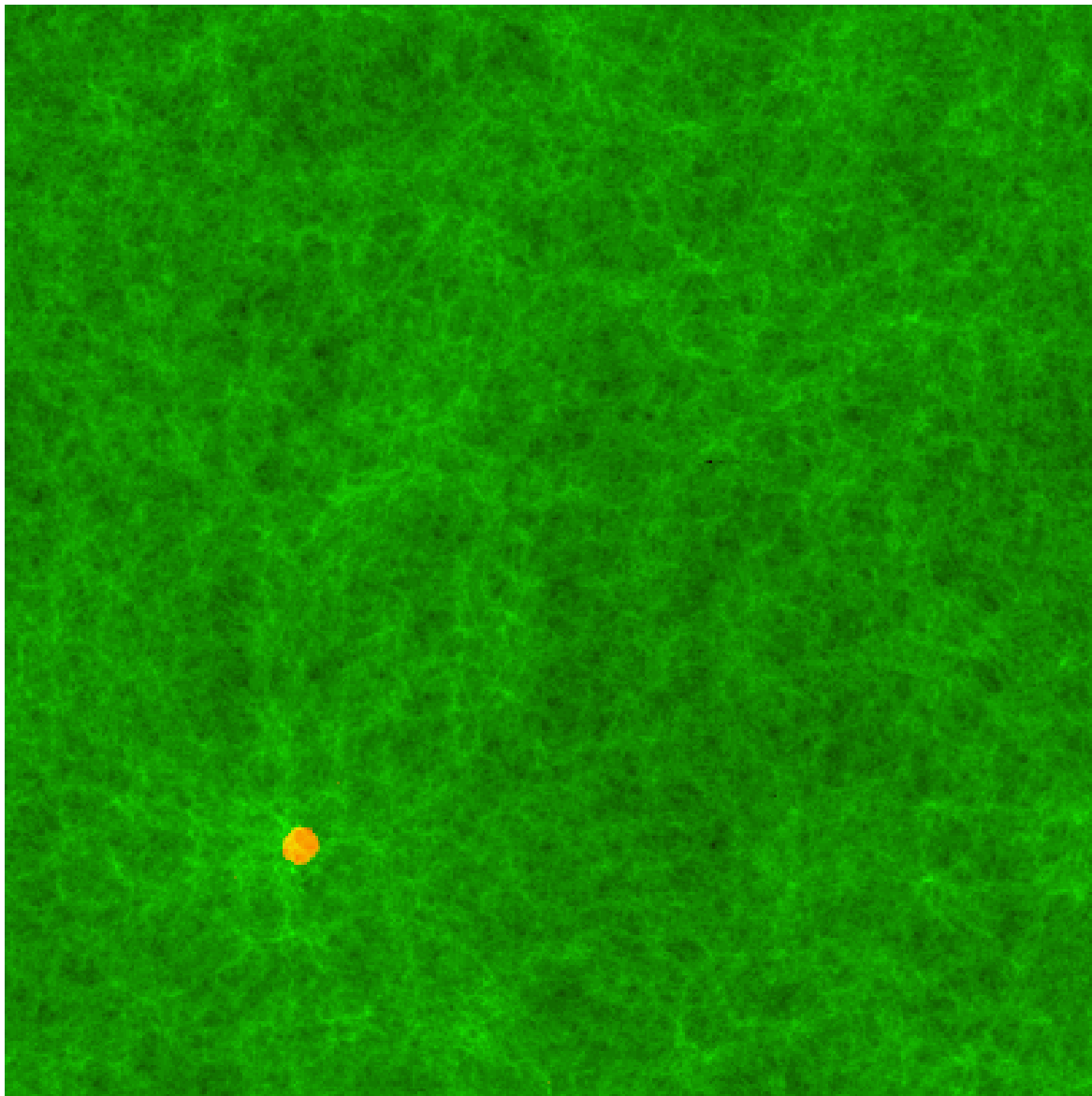
inside H II regions ;

- 35/h Mpc box,  $406^3$  radiative transfer simulation, WMAP3,  $f_{\gamma} = 250$ ;

- resolved all halos with

$M > 10^8 M_{\text{solar}}$  (i.e. all atomically-cooling halos),  
(blue dots = source cells);

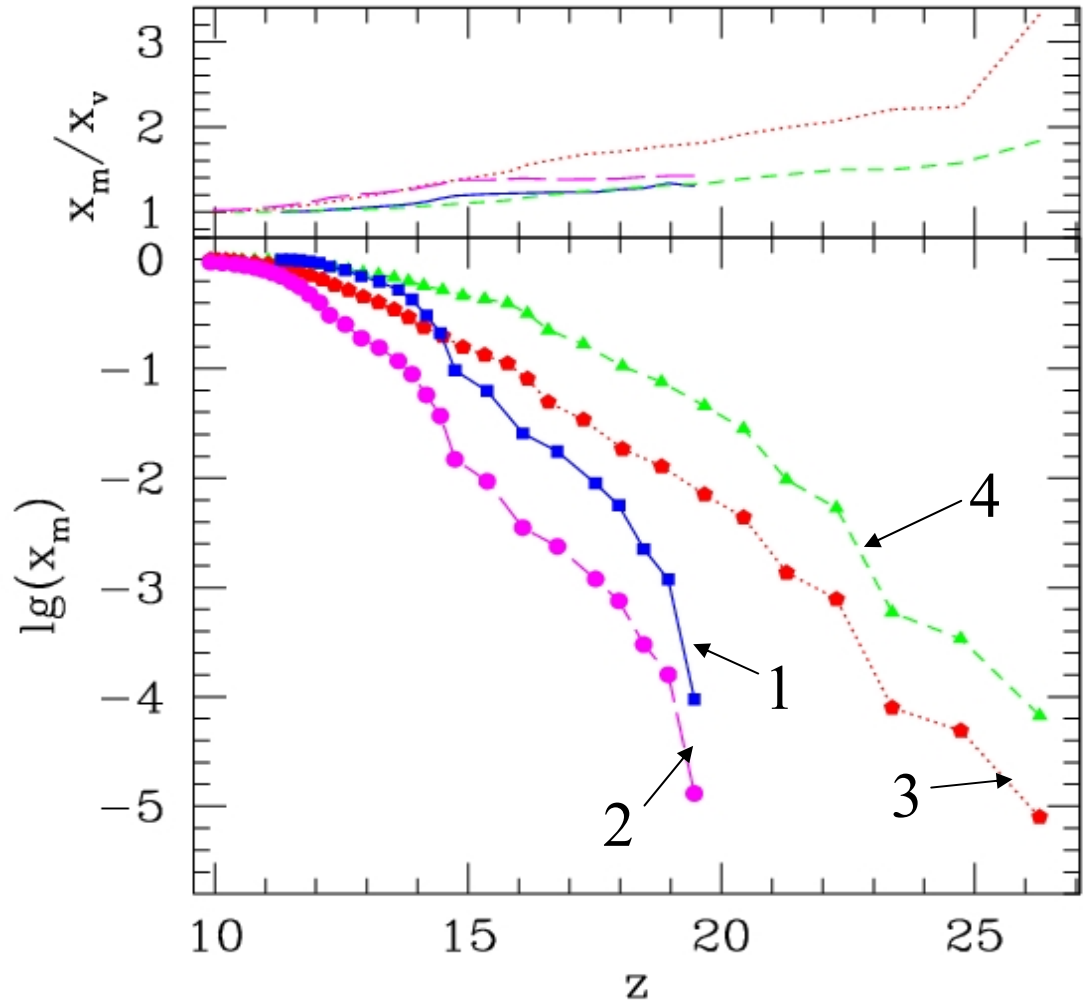
- Evolution:  $z=21$  to  $z_{\text{ov}} = 7.5$ .



# Extended reionization: Jeans-mass filtering, halo-mass-dependent emissivity

## Cases

1. Halo masses  $M_{\text{solar}} > 10^9$   
 $f_{\gamma} = 2000$  (e.g. Pop III);
2. Halo masses  $M_{\text{solar}} > 10^9$   
 $f_{\gamma} = 250$  (e.g. Pop II);
3. Halo masses  $M_{\text{solar}} > 10^8$   
 $f_{\gamma} = 250$  (e.g. Pop II),  
lower-mass halos  
suppressed inside H II regions  
(Jeans-mass filtering) ;
4. Same as 3., but  
 $f_{\gamma} = 2000$  ( $M_{\text{solar}} < 10^9$ )  
 $f_{\gamma} = 250$  ( $M_{\text{solar}} > 10^9$ )



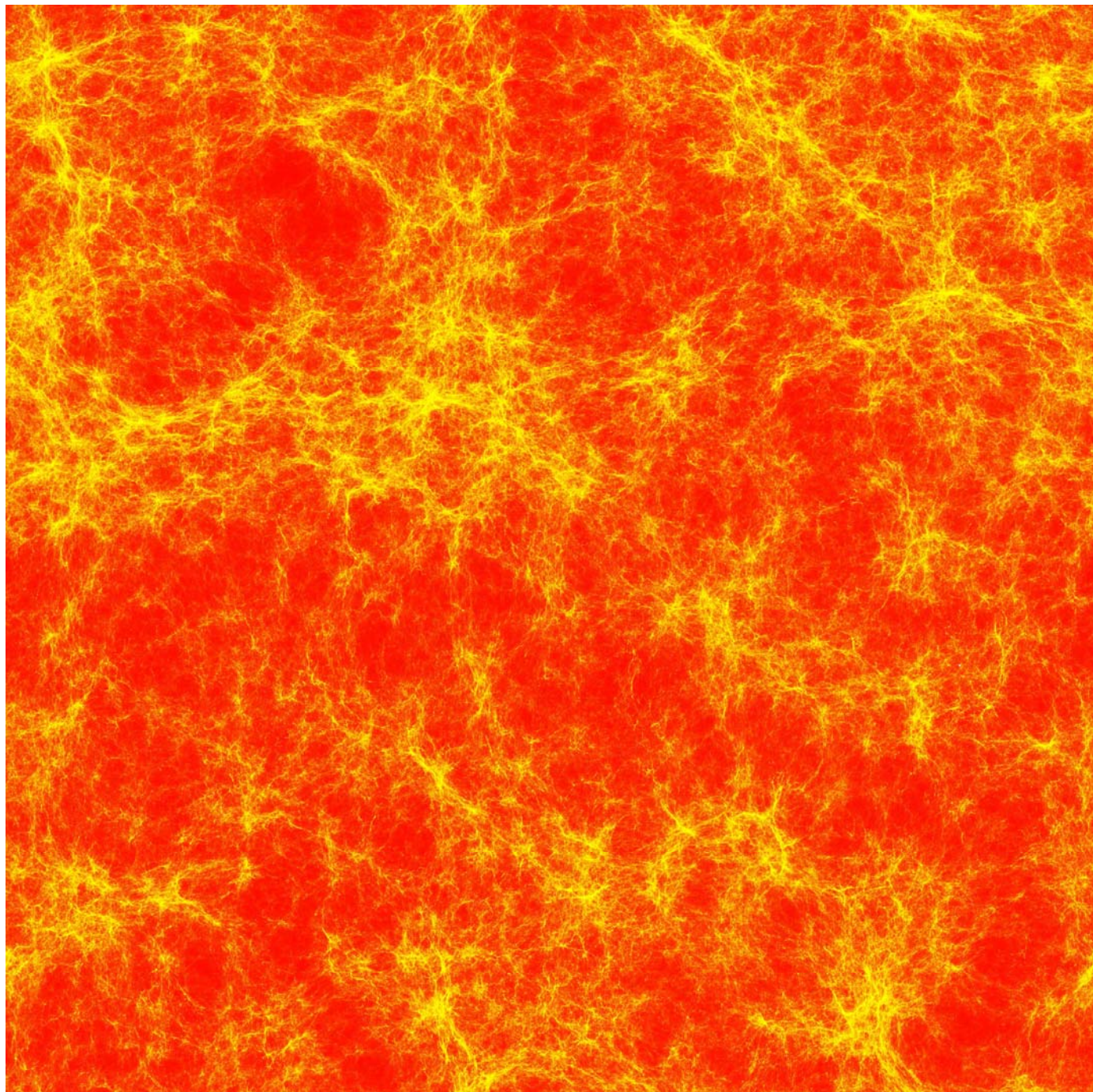


# New, Large-Scale Simulations of Self-Regulated Reionization

Iliev, Mellema, Pen,  
Shapiro, and Merz  
(2008), in press  
(astro-ph/0806.2887);

Shapiro, Iliev,  
Mellema, Pen, &  
Merz (2008), in press  
(astro-ph/0806.3091)

**CubeP<sup>3</sup>M** N-body  
 $\Lambda$ CDM sim with  
 $3072^3$  (29 billion)  
particles,  
 $6144^3$  cells,  
box size = 160 Mpc;  
particle mass =  
5 million solar  
masses



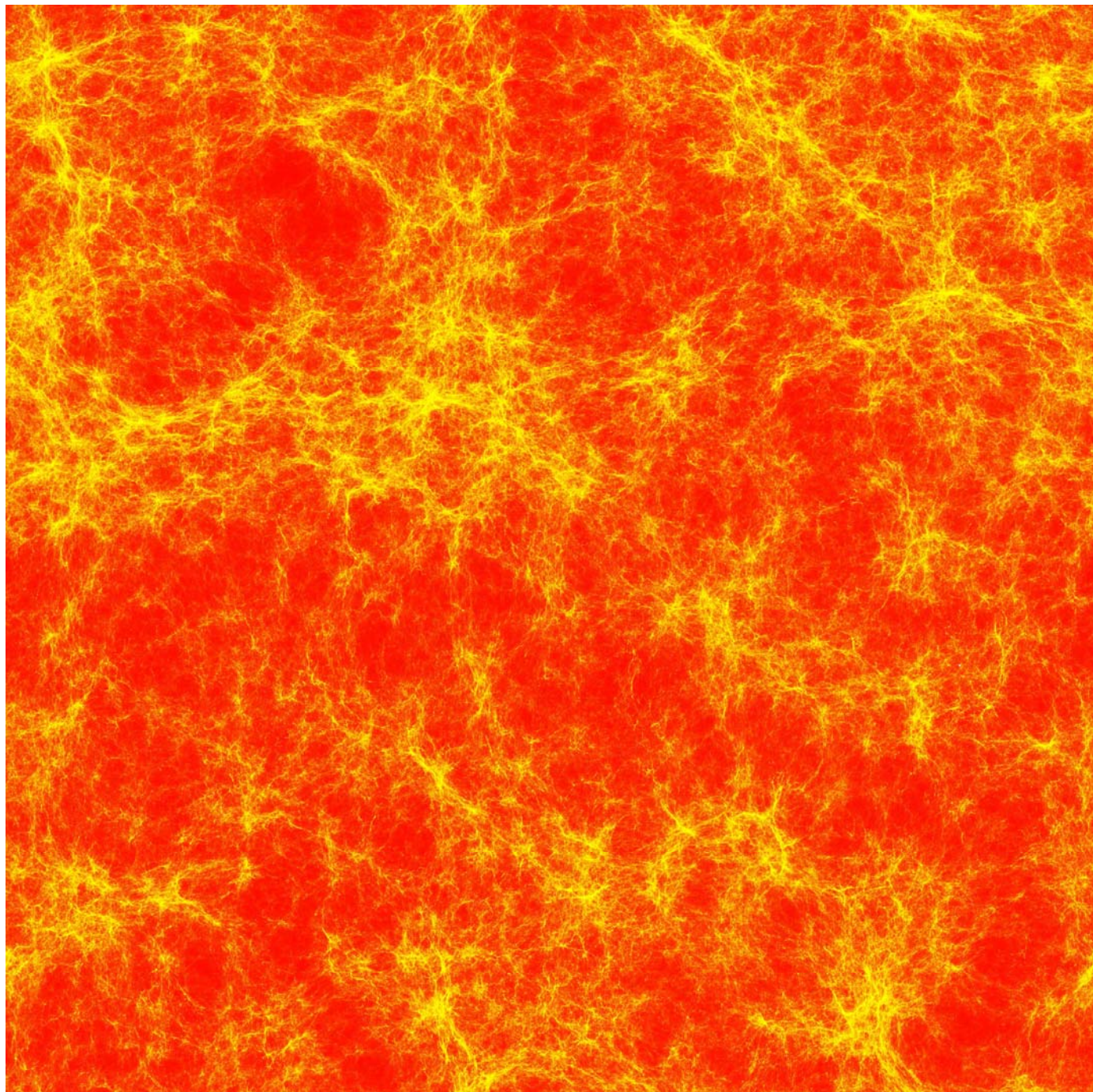


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Merz (2008), in press  
(astro-ph/0806.3091)

**CubeP<sup>3</sup>M** N-body  
 $\Lambda$ CDM sim with  
 $3072^3$  (29 billion)  
particles,  
resolves halos above  
 $10^8$  solar masses





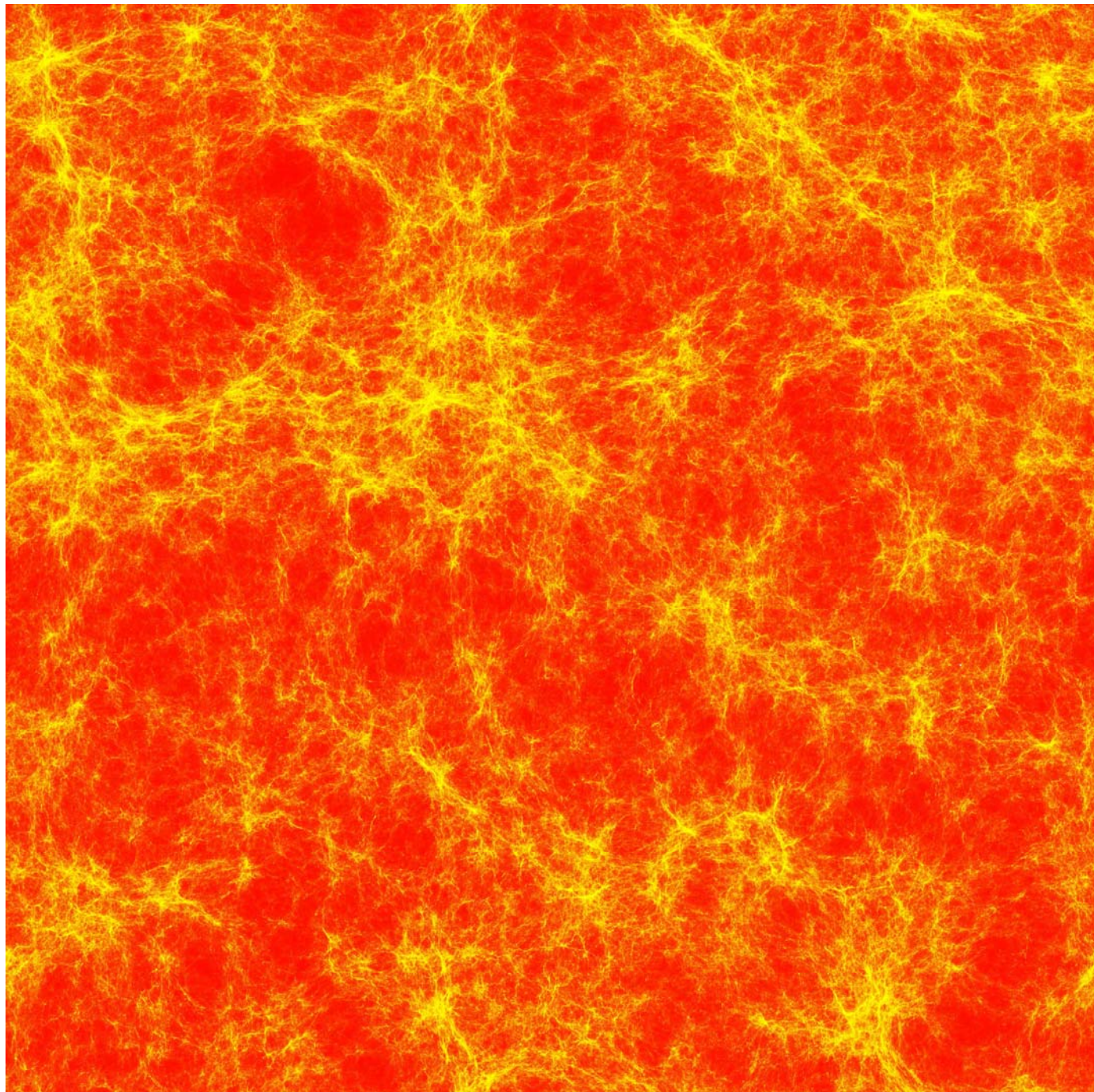
# New, Large-Scale Simulations of Self-Regulated Reionization

Iliev, Mellema, Pen,  
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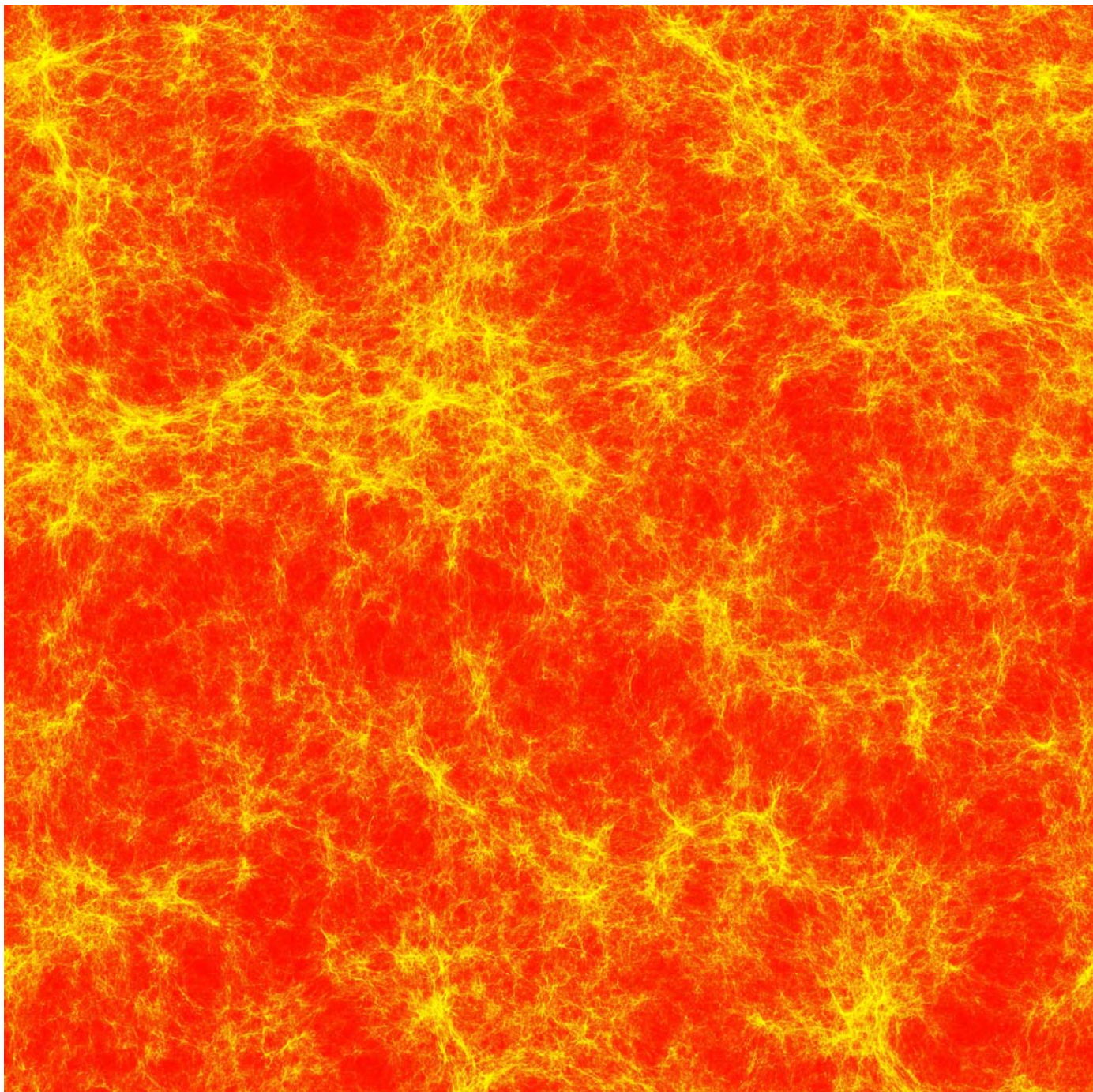
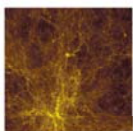
Shapiro, Iliev,  
Mellema, Pen, &  
Merz (2008), in press  
(astro-ph/0806.3091)

## **CubeP<sup>3</sup>M** N-body

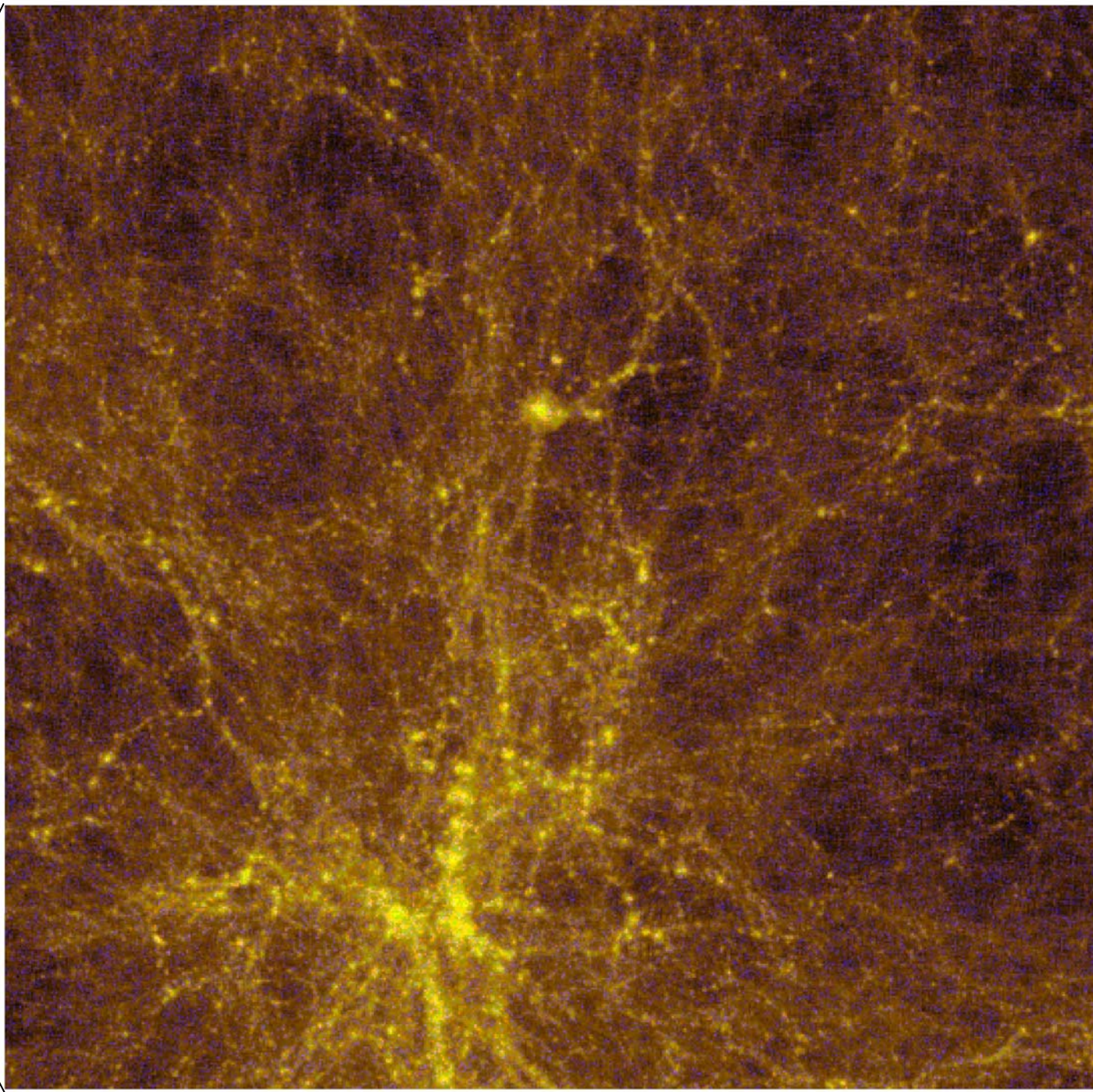
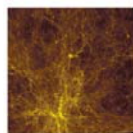
- new Texas Sun  
Constellation Linux  
Cluster, *Ranger*,  
2048 cores, 159,000  
SUs (cores x hours)





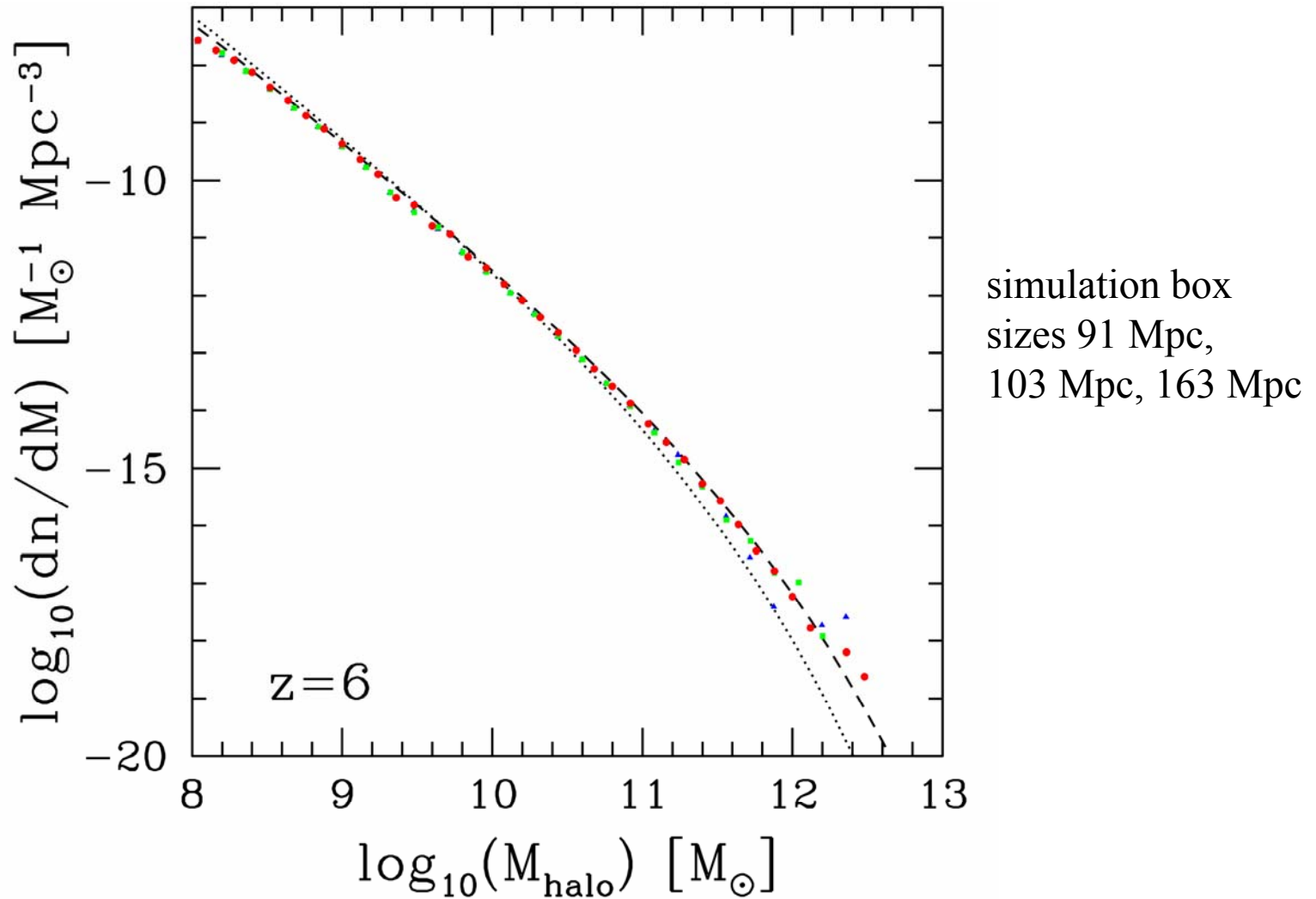






# $\Lambda$ CDM Halo Mass Function ( $M > 10^8$ Solar Masses)

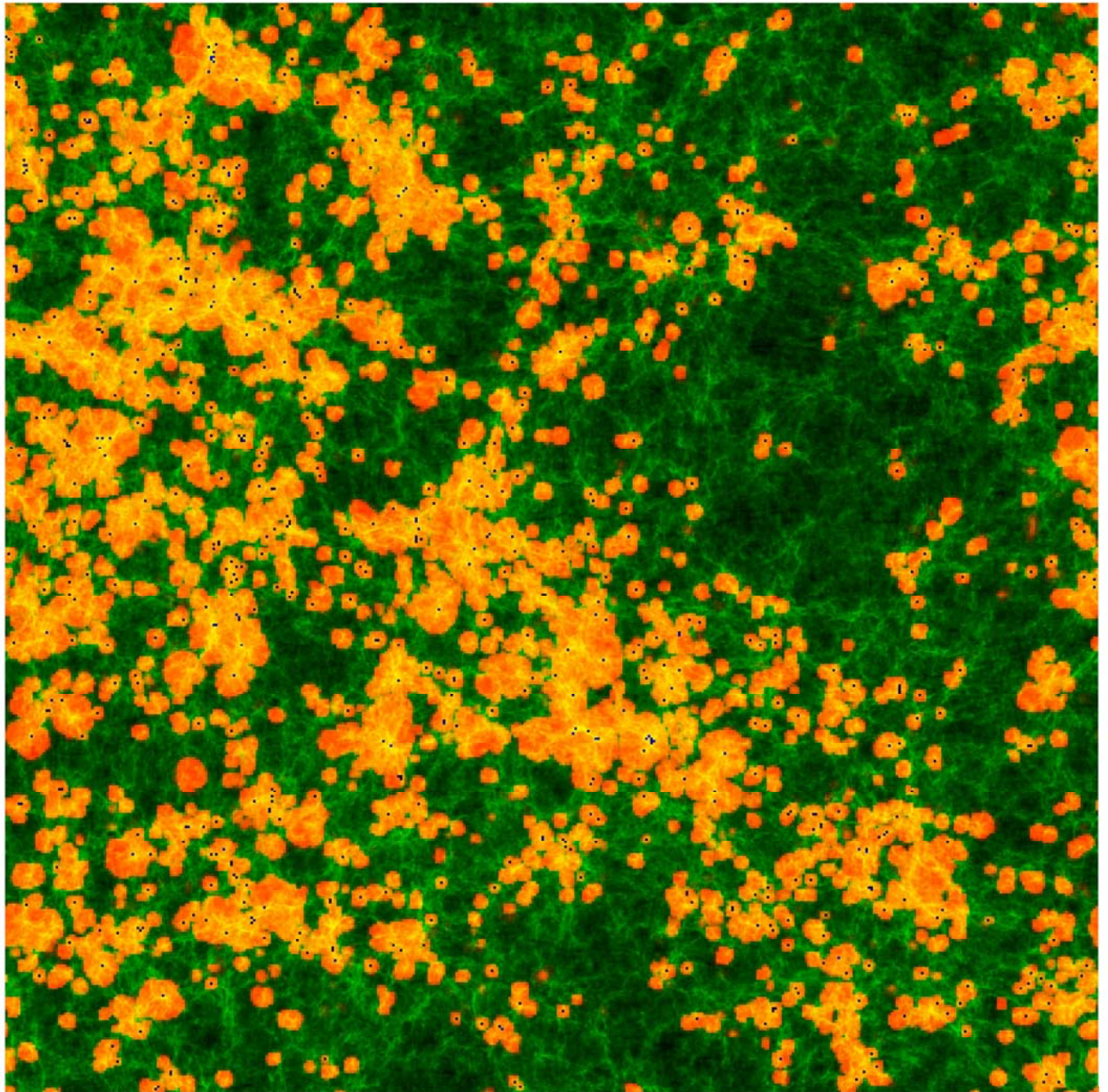
from CubeP<sup>3</sup>M N-body Simulations





# C<sup>2</sup>Ray radiative transfer

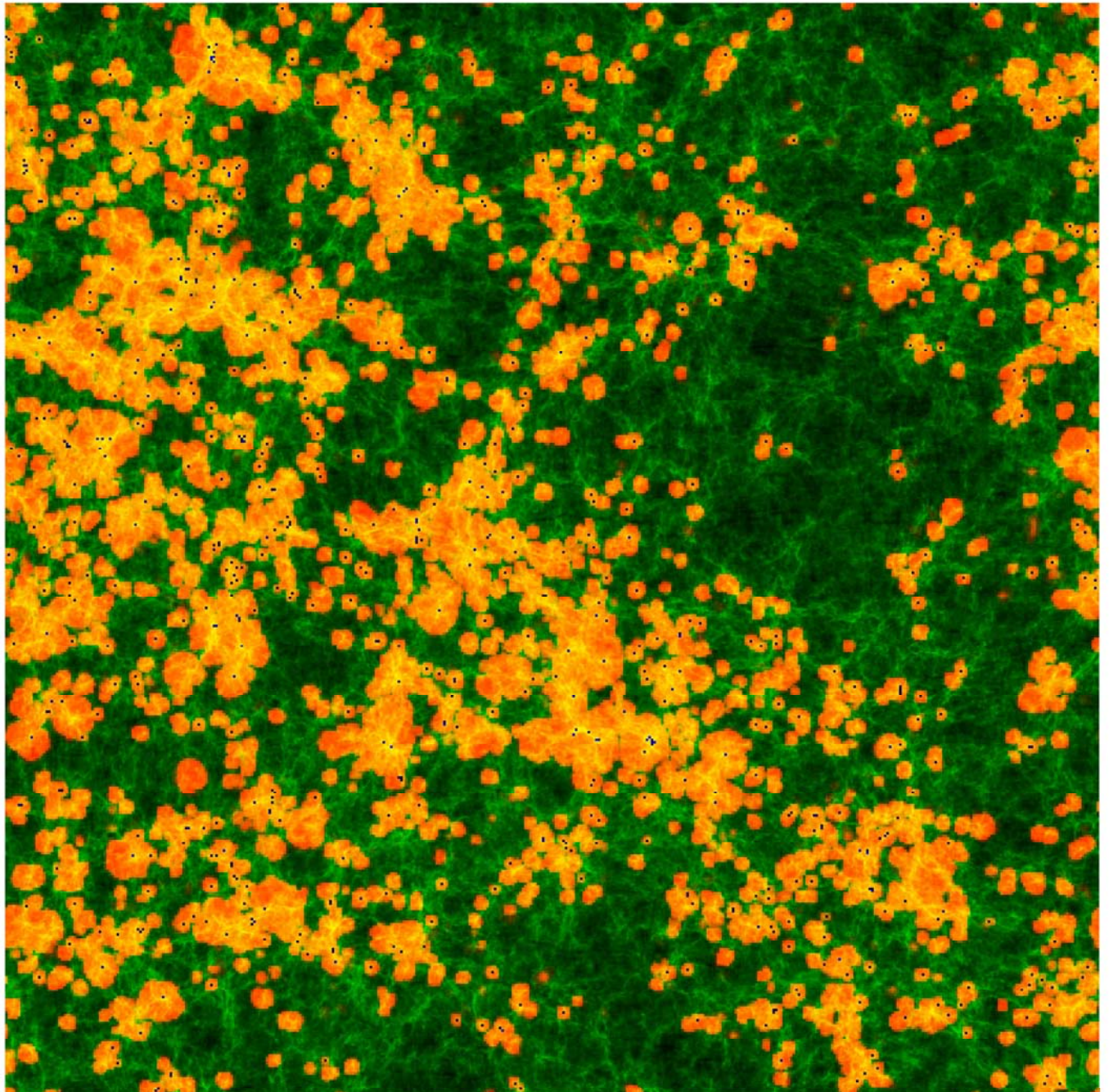
- RT grid  $432^3$   
cells
- box size = 90  
Mpc





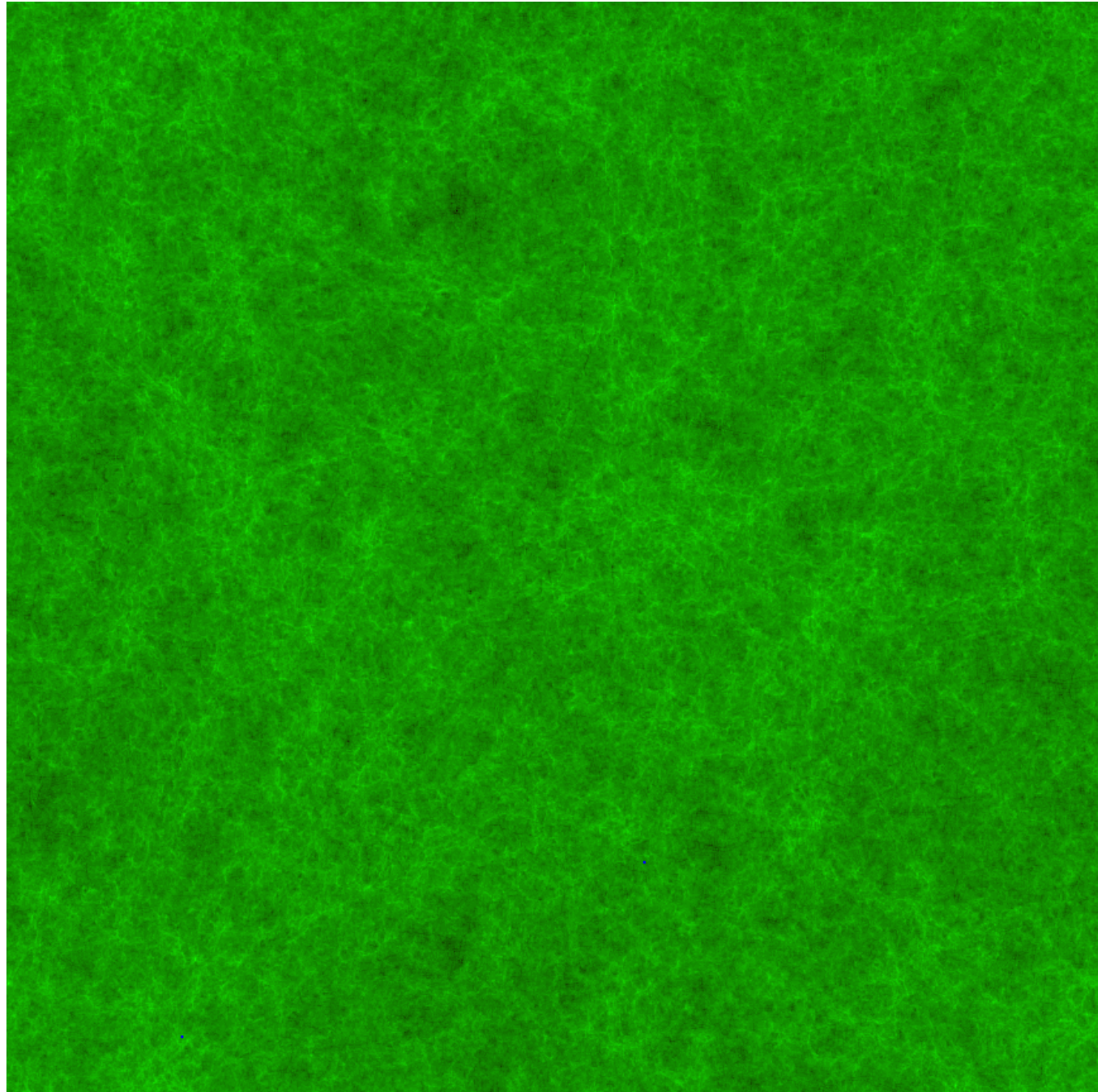
# C<sup>2</sup>Ray radiative transfer

- RT grid  $432^3$  cells
- box size = 90 Mpc
- *Ranger*,  
Texas Sun  
Constellation  
Linux Cluster,  
700,000 SUs  
(cores x hours),  
up to 10,000  
cores



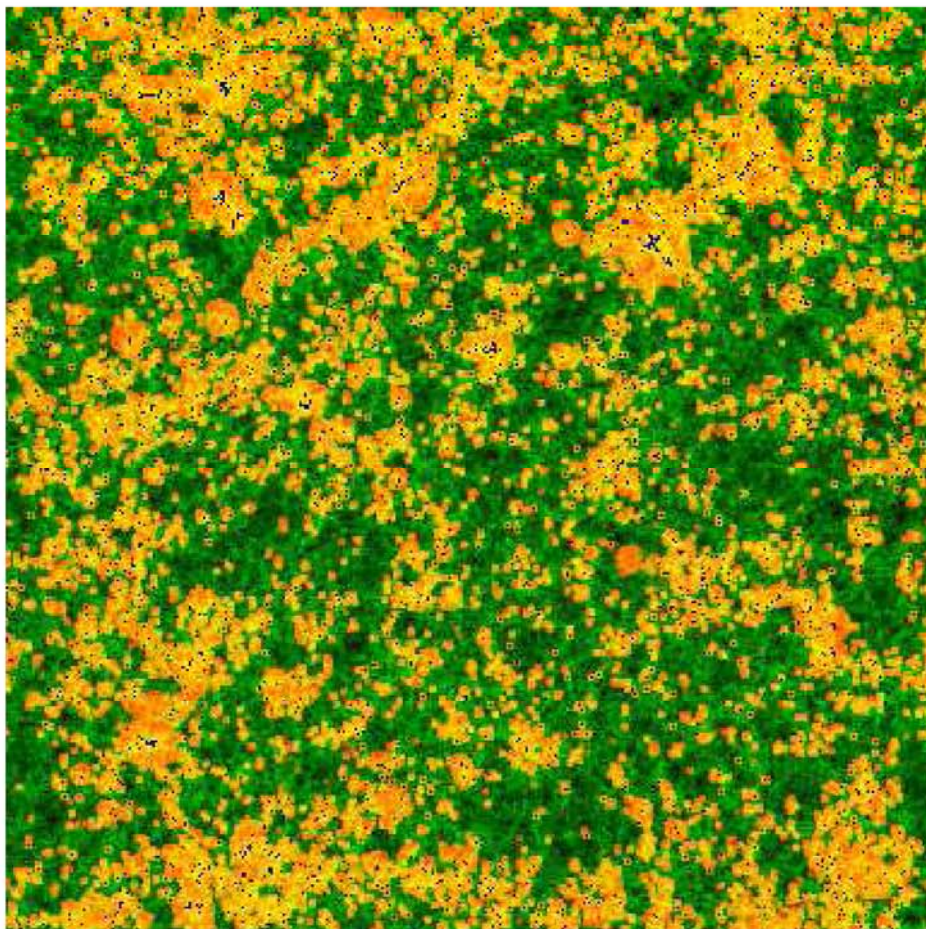


# Self-Regulated Reionization in $\Lambda$ CDM



- 90 Mpc box

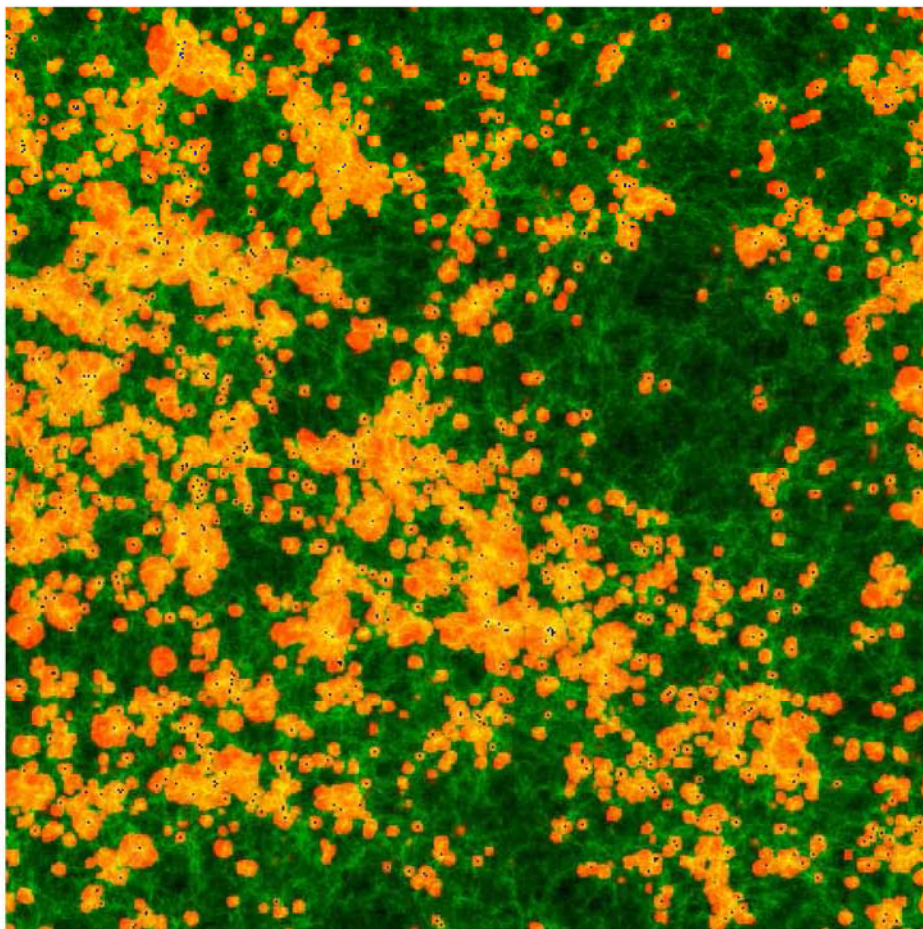




160 Mpc box

$$z = 11.6$$

when mass-weighted mean ionized fraction of universe  $x_m = 0.3$

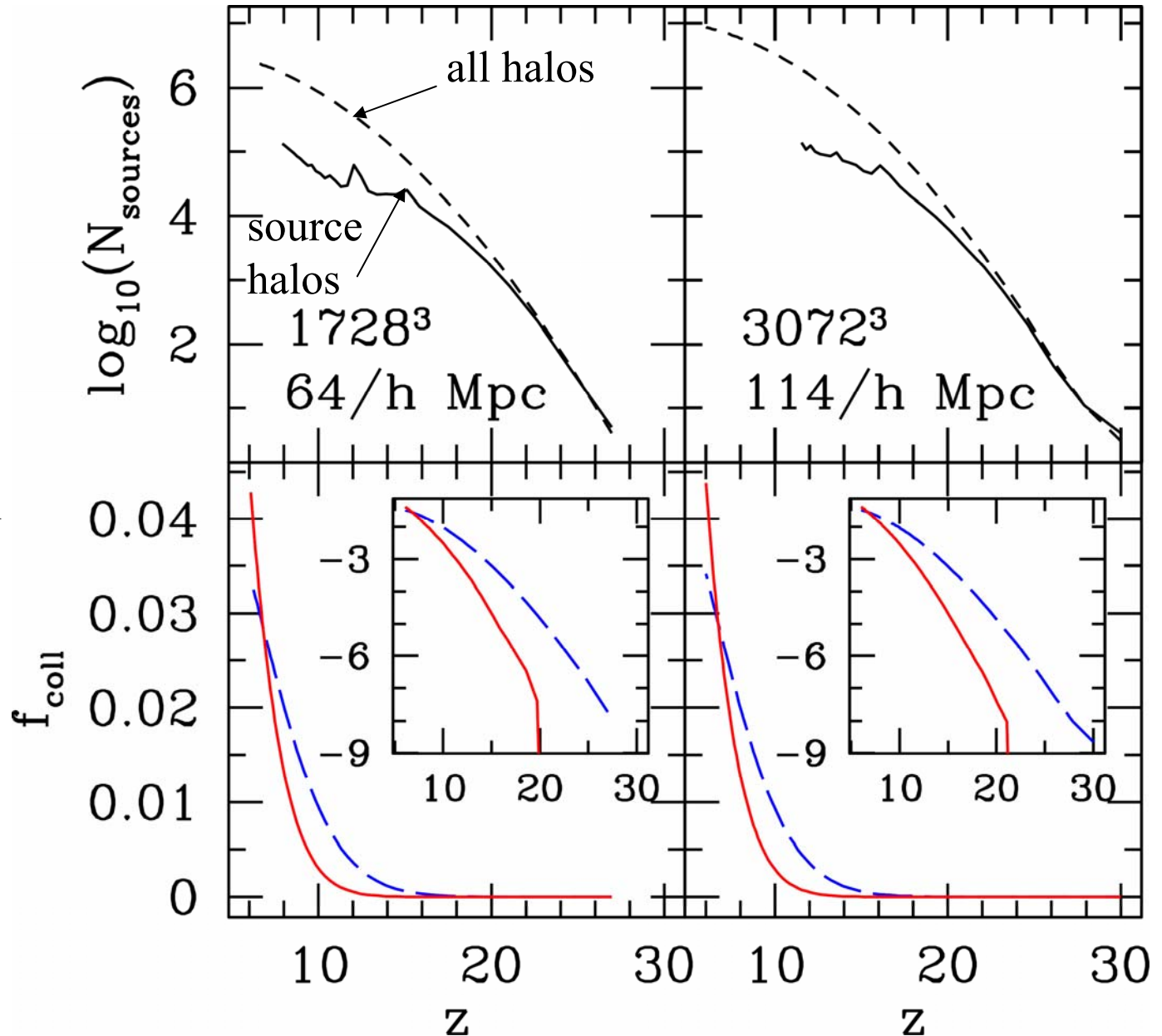


90 Mpc box

$$z = 11.9$$

# Self-regulated halo mass function

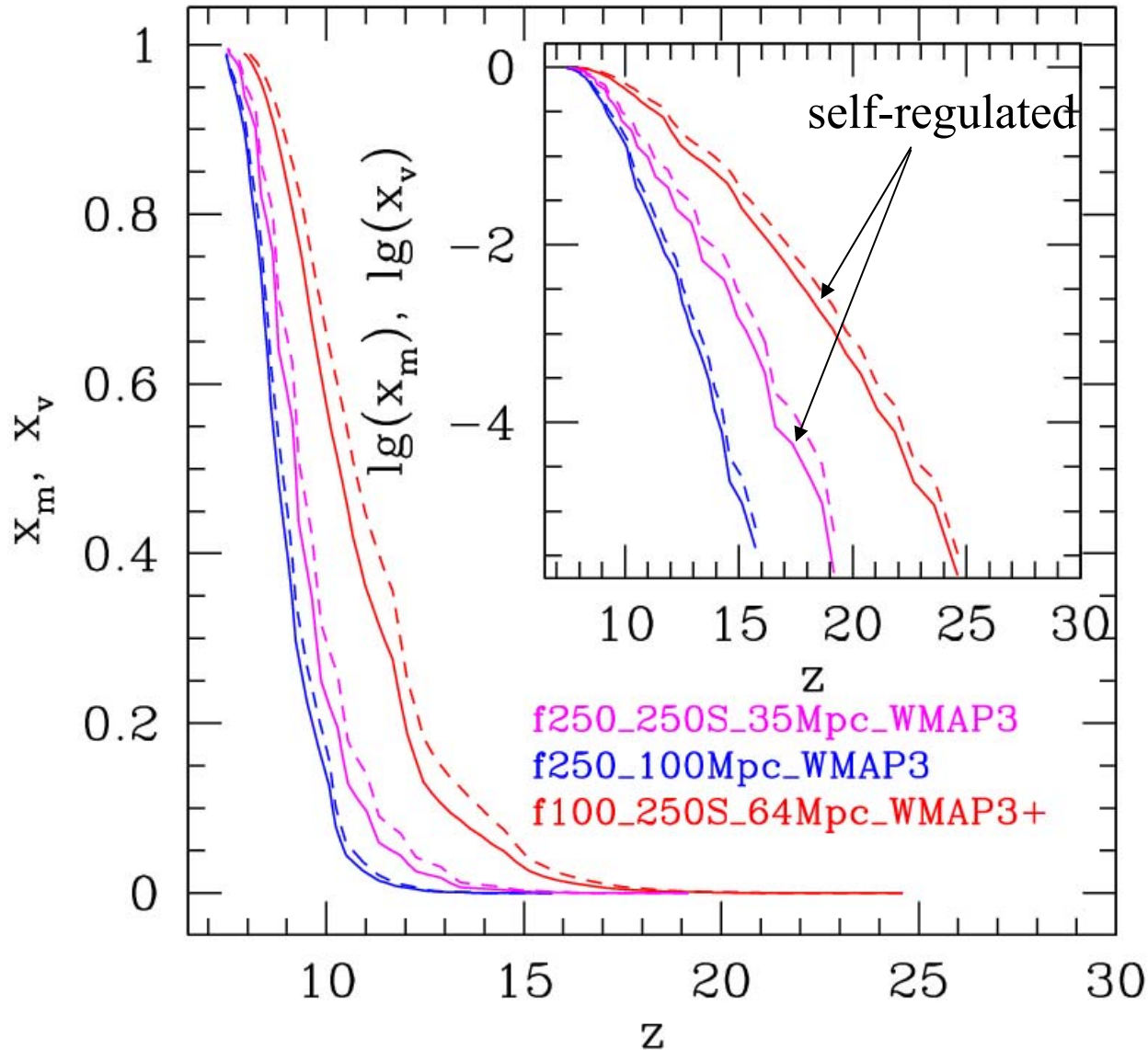
- Jeans-mass filtering suppresses formation of sources in small-mass halos which form inside H II regions
- clustering of small-mass halos around density peaks enhances this effect → suppression is strongly **biased**





# Evolution of the Mean Ionized Fraction of the Universe

- self-regulated reion.  
(i.e. small-mass halos resolved)  
starts earlier, but ends about the same time →
- high-mass halos dominate the end of EOR





# Seeing Invisible Light From the Dark Ages and the Epoch of Reionization that Ended Them

- Hydrogen atoms in the early universe can be detected in absorption or emission against the Cosmic Microwave Background (CMB) at redshifted radio wavelength 21 cm.
- Halos formed during the dark ages are dense and hot enough to appear in emission.
- The intergalactic medium, too, can appear in either emission or absorption.
- Future radio astronomy antenna arrays are being designed and built to detect this 21 cm emission.

## Low Frequency Array (LOFAR)

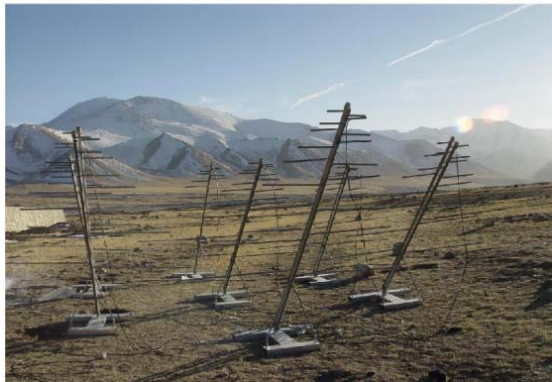


## Murchison Widefield Array (MWA)



## Primeval Structure Telescope (PAST/21CMA)

Prototype Tests, Ulaanbaatar,  
Mongolia



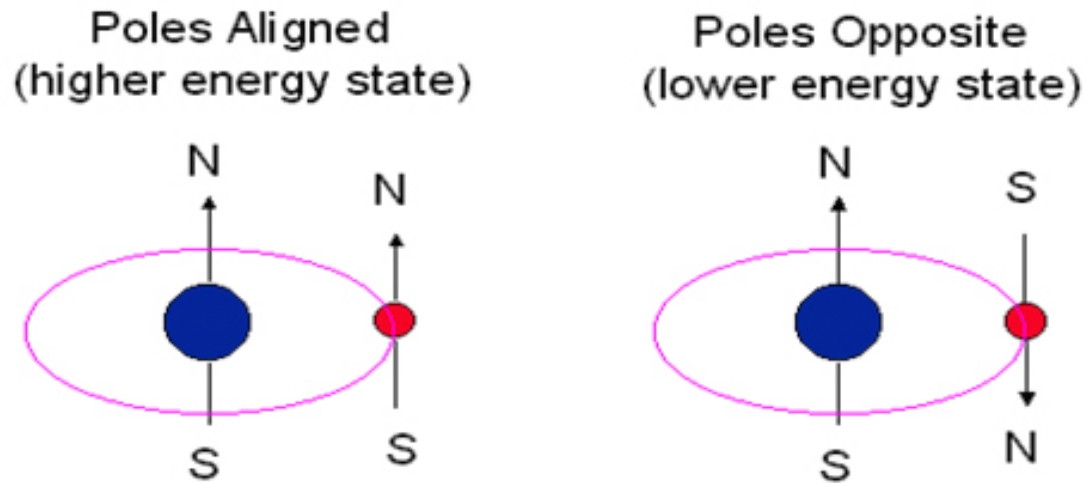
## Giant Meterwave Radio Telescope (GMRT)



## Square Kilometer Array (SKA)



# 21-cm Level Population of Atomic Hydrogen



$$\frac{n_2}{n_1} = 3 \exp\left(-\frac{h\nu_0}{kT_{spin}}\right)$$

# 21-cm Radiation Background

- Foreground emission or absorption by H atoms at redshift  $z$  seen against CMB at redshifted wavelength  $21(1+z)$  cm.

Emission  $\leftrightarrow T_{\text{spin}} > T_{\text{CMB}}$

Absorption  $\leftrightarrow T_{\text{spin}} < T_{\text{CMB}}$

Transparent  $\leftrightarrow T_{\text{spin}} = T_{\text{CMB}}$

# 3 Ways to Change the 21-cm Level Population

- An H atom can:
  - Absorb a 21-cm photon from the CMB  
(CMB Pumping)
  - Collide with another atom (or an electron or ion)  
(Collisional Pumping)
  - Absorb a UV photon at 1215 Angstrom to make Lyman alpha transition of H atom, then decay to one of 21-cm levels  
(Lyman Alpha Pumping)

# 3 Ways to Change the 21-cm Level Population

- An H atom can:
  - Absorb a 21-cm photon from the CMB  
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(Collisional Pumping)
  - **Absorb a UV photon at 1215 Angstrom to make Lyman alpha transition of H atom, then decay to one of 21-cm levels**  
**(Lyman Alpha Pumping)**



# Stages of 21-cm Background

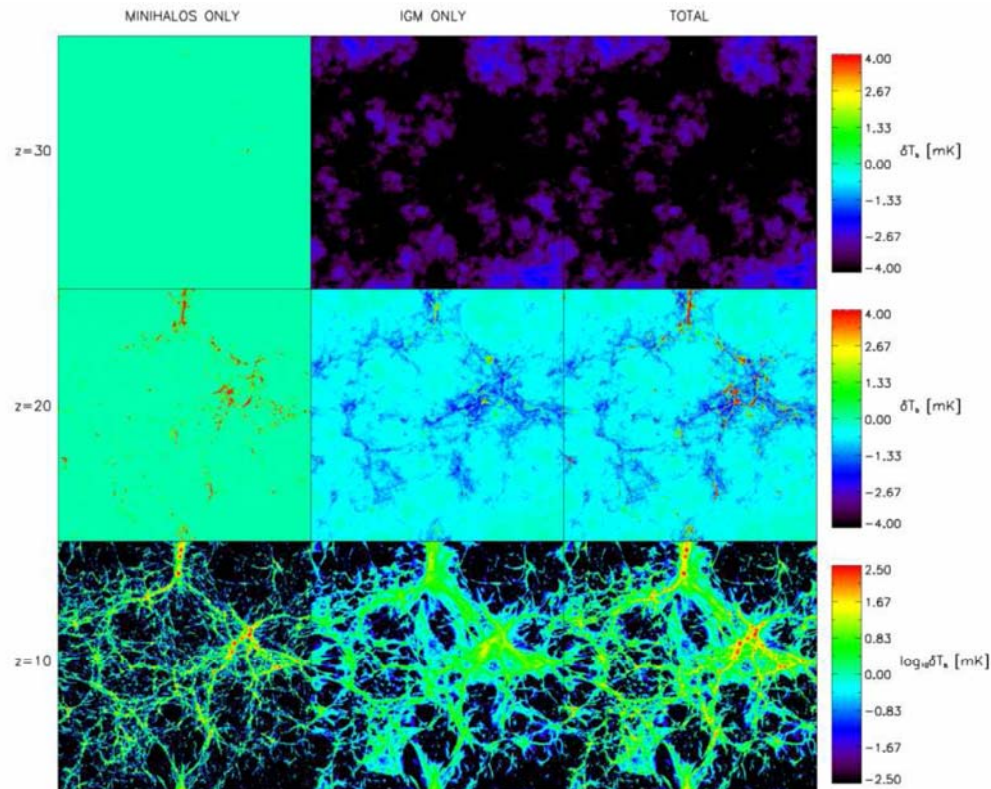
- Dark Ages
  - $z \geq 150$ ,  $T_{\text{spin}} = T_{\text{CMB}} \rightarrow$  nothing
  - $20 \leq z \leq 150$ ,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  absorption
  - $z \leq 20$ ,  $T_{\text{spin}} > T_{\text{CMB}}$  in minihalos  $\rightarrow$  emission
- Epoch of Reionization ( $6 \leq z \leq 20$ )
  - $T_{\text{spin}} > T_{\text{CMB}}$  in minihalos  $\rightarrow$  emission
  - After sources turn on, Lyman alpha pumping  $\rightarrow$ 
    - Without heating,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  IGM in absorption
    - With heating,  $T_{\text{spin}} > T_{\text{CMB}} \rightarrow$  IGM in emission

# Stages of 21-cm Background

- Dark Ages
  - $z \geq 150$ ,  $T_{\text{spin}} = T_{\text{CMB}} \rightarrow$  nothing
  - **$20 \leq z \leq 150$ ,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  absorption**
  - **$z \leq 20$ ,  $T_{\text{spin}} > T_{\text{CMB}}$  in minihalos  $\rightarrow$  emission**
- Epoch of Reionization ( $6 \leq z \leq 20$ )
  - $T_{\text{spin}} > T_{\text{CMB}}$  in minihalos  $\rightarrow$  emission
  - After sources turn on, Lyman alpha pumping  $\rightarrow$ 
    - Without heating,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  IGM in absorption
    - With heating,  $T_{\text{spin}} > T_{\text{CMB}} \rightarrow$  IGM in emission

# The 21-cm Background from the Cosmic Dark Ages: Minihalos and the Intergalactic Medium Before Reionization : Collisionally Pumped Spin Temperature

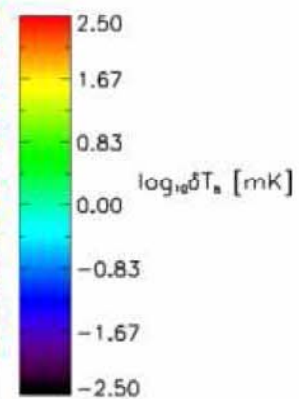
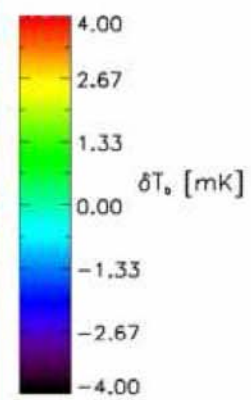
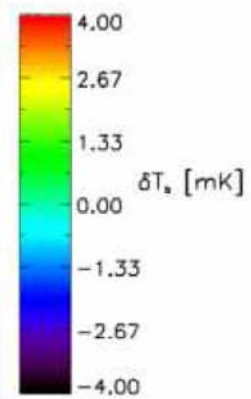
- Iliev, Shapiro, Ferrara & Martel 2002, ApJL, 572, L123
- Iliev, Scannapieco, Shapiro, & Martel 2003, MNRAS, 341, 81
- Shapiro, Ahn, Alvarez, Iliev, Martel & Ryu (2006), ApJ, 646, 681; (astro-ph/0512516)



MINIHALOS ONLY

IGM ONLY

TOTAL

 $z=30$  $z=20$  $z=10$ 

# Stages of 21-cm Background

- Dark Ages
  - $z \geq 150$ ,  $T_{\text{spin}} = T_{\text{CMB}} \rightarrow$  nothing
  - $20 \leq z \leq 150$ ,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  absorption
  - $z \leq 20$ ,  $T_{\text{spin}} > T_{\text{CMB}}$  in minihalos  $\rightarrow$  emission
- **Epoch of Reionization ( $6 \leq z \leq 20$ )**
  - $T_{\text{spin}} > T_{\text{CMB}}$  in minihalos  $\rightarrow$  emission
  - **After sources turn on, Lyman alpha pumping  $\rightarrow$** 
    - Without heating,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  IGM in absorption
    - With heating,  $T_{\text{spin}} > T_{\text{CMB}} \rightarrow$  IGM in emission



# Stages of 21-cm Background

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  - $z \geq 150$ ,  $T_{\text{spin}} = T_{\text{CMB}} \rightarrow$  nothing
  - $20 \leq z \leq 150$ ,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  absorption
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  - **After sources turn on, Lyman alpha pumping  $\rightarrow$** 
    - **Without heating,  $T_{\text{spin}} < T_{\text{CMB}} \rightarrow$  IGM in absorption**
    - **With heating,  $T_{\text{spin}} > T_{\text{CMB}} \rightarrow$  IGM in emission**

# Decoupling the spin temperature of the 21-cm transition of H I from the CMB

(Chuzhoy and Shapiro 2006, ApJ, 651, 1; astro-ph/0512206)

- Spin temperature

$$T_s = \frac{T_{\text{CMB}} + y_\alpha T_\alpha + y_c T_k}{1 + y_\alpha + y_c},$$

where  $y_\alpha = (P_{10} T_*) / (A_{10} T_\alpha)$

$P_{10} \propto J_\alpha =$  mean intensity at Ly  $\alpha$

(Field 1958, 1959)

- Standard assumption:

scattering  $\rightarrow$  atomic recoil  $\rightarrow T_\alpha = T_k$

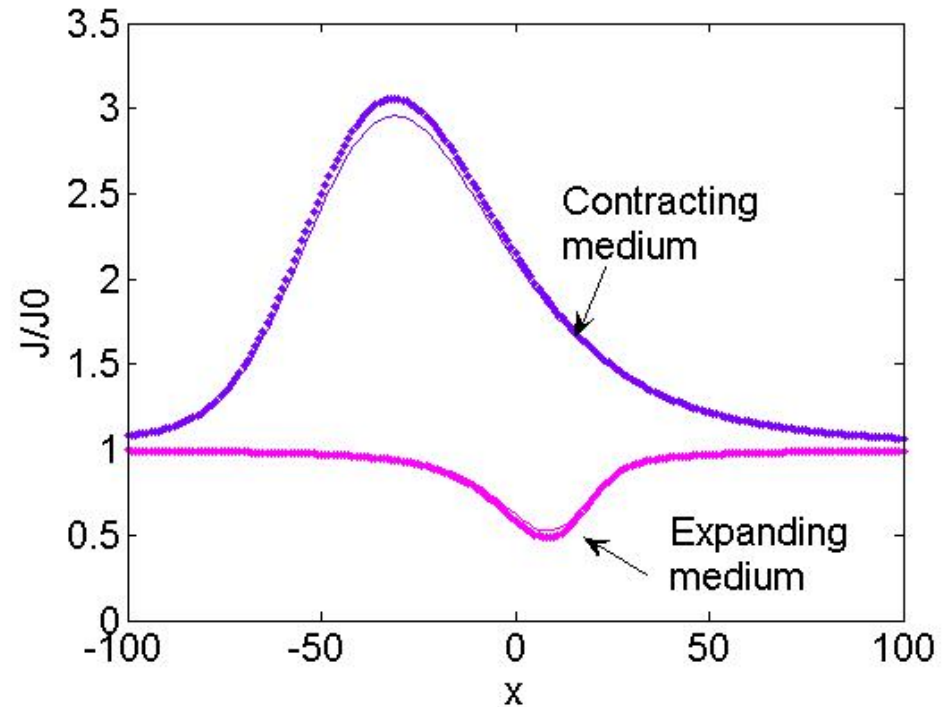
and

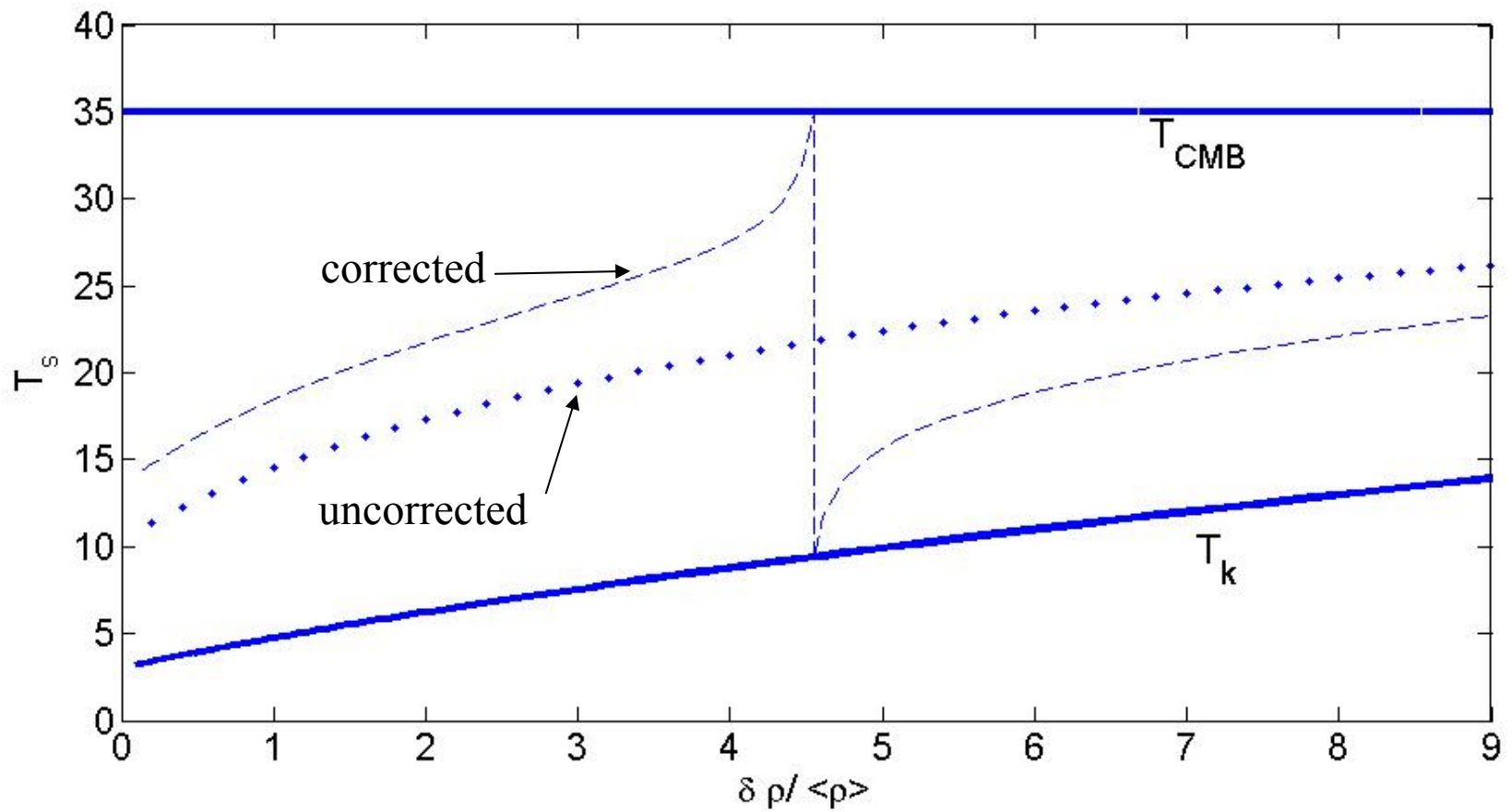
$J_\alpha = J_{\alpha,0} =$  background level

- But there is a backreaction of the Ly  $\alpha$  scattering :

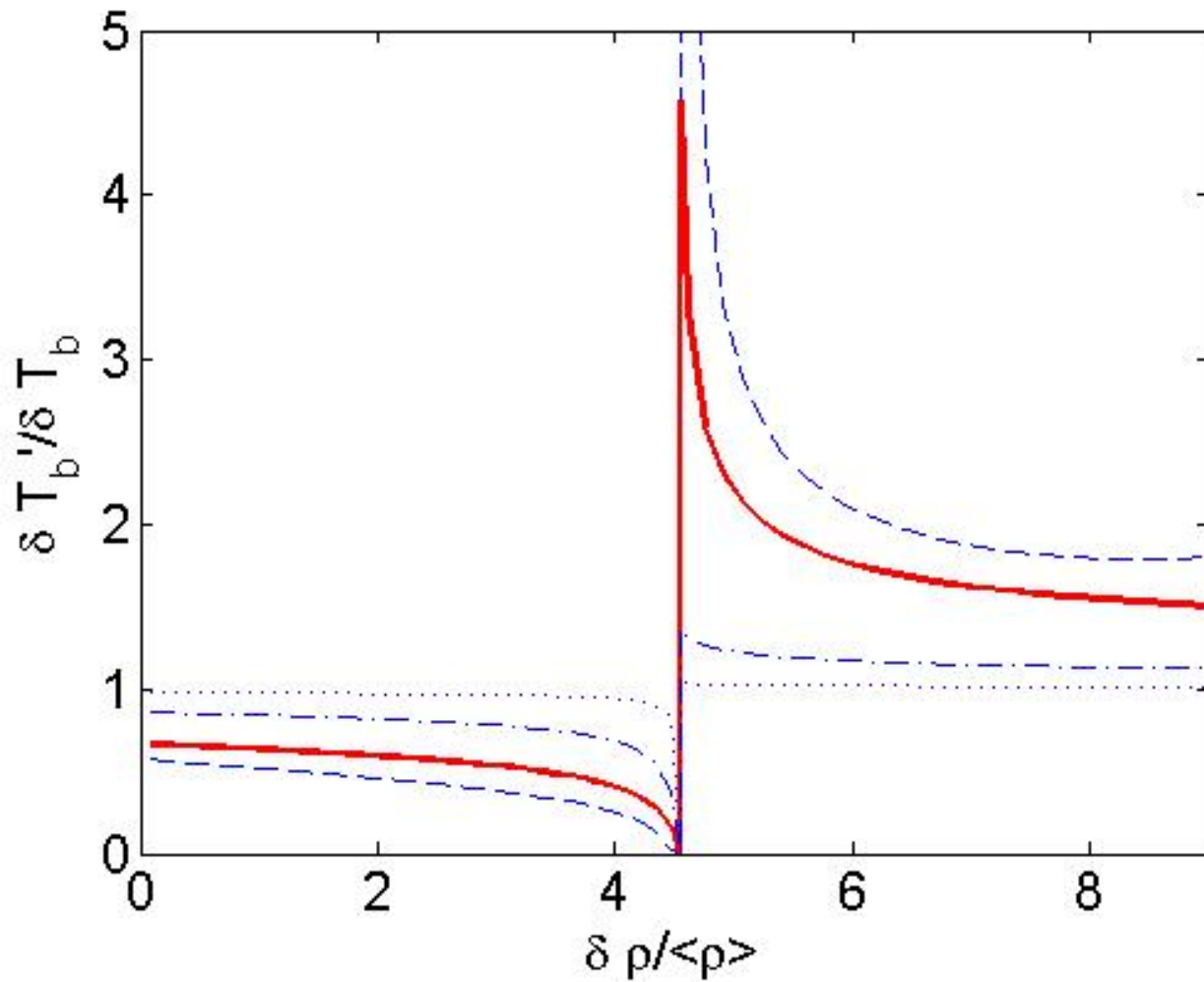
hyperfine splitting + atomic recoil  
 $\implies$

- (1)  $T_\alpha \neq T_k$   
 ( $T_\alpha$  between  $T_k$  and  $T_{\text{CMB}}$ )
- (2)  $J_\alpha \neq J_{\alpha,0}$   
 (Chen and Miralda-Escude 2004;  
 without hyperfine splitting)
- (3)  $T_\alpha, J_\alpha$  both depend on local  
 departure from Hubble flow  
 $\implies$  small-scale structure  
 affects mean 21-cm signal





Hydrogen spin temperature at  $z \sim 12$  for an illustrative radiation intensity, for different overdensities



The correction factor to the differential brightness temperature  
(the 21-cm absorption signal) for different radiation intensities,  
for different overdensities



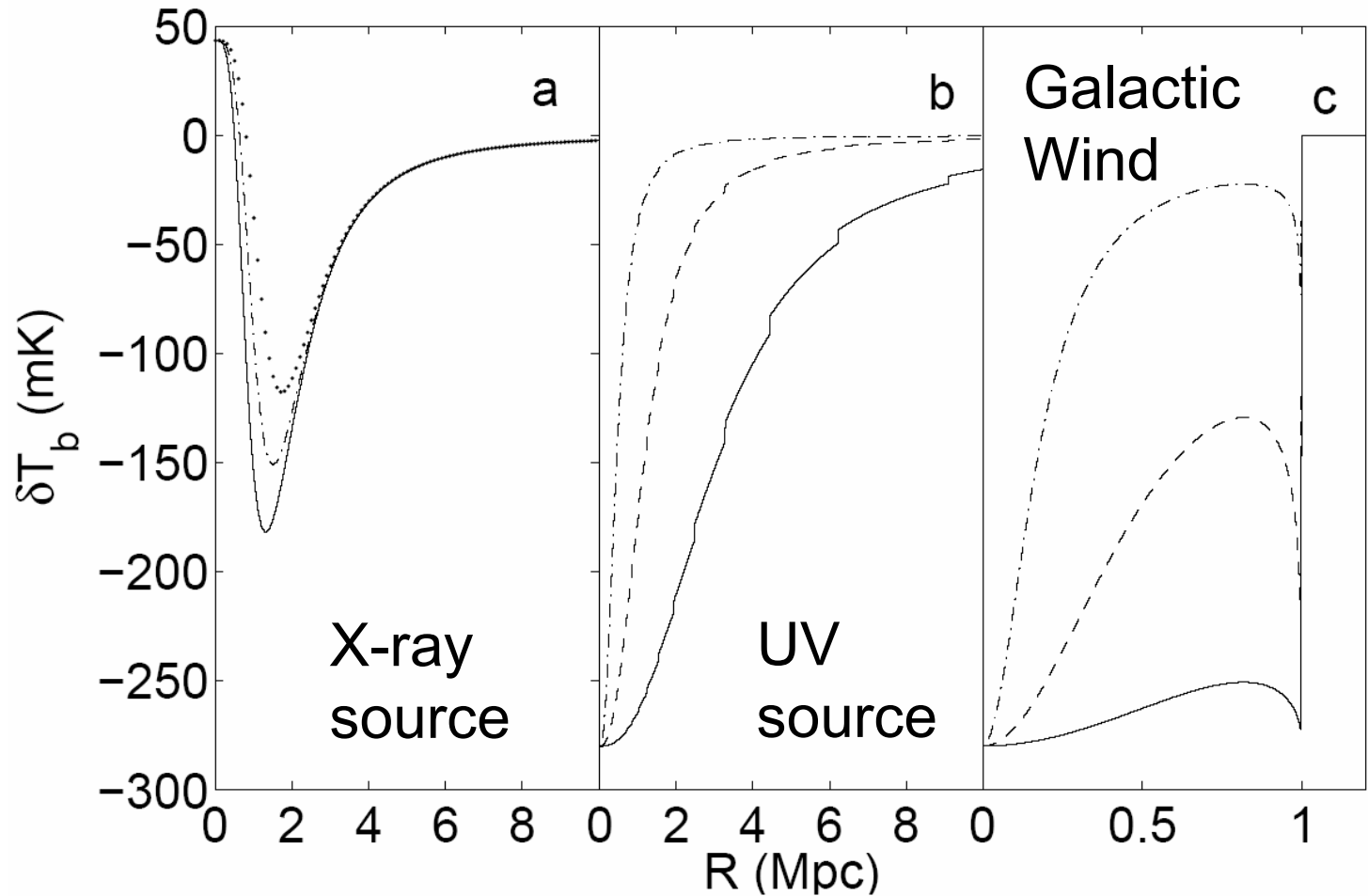
# Recognizing the First Radiation Sources Through Their 21-cm Signature :

Brightness temperature vs. comoving radius around a radiation source at  $z = 20$

a. X-ray source,  
 $L = 5e40$  erg/s,  
@  $t$  (Myrs) ,  
10 (solid),  
20 (dash-dot),  
40 (dotted);

b. UV source,  
 $L$  (Ly  $\alpha$  to LL)  
in erg/s =  
 $5e41$  (dashed),  
 $5e42$  (dash-dot),  
 $5e43$  (solid);

c. Galactic wind,  
 $L\alpha$  (erg/s) =  
 $1e41$  (solid),  
 $1e40$  (dashed),  
 $1e39$  (dash-dot).

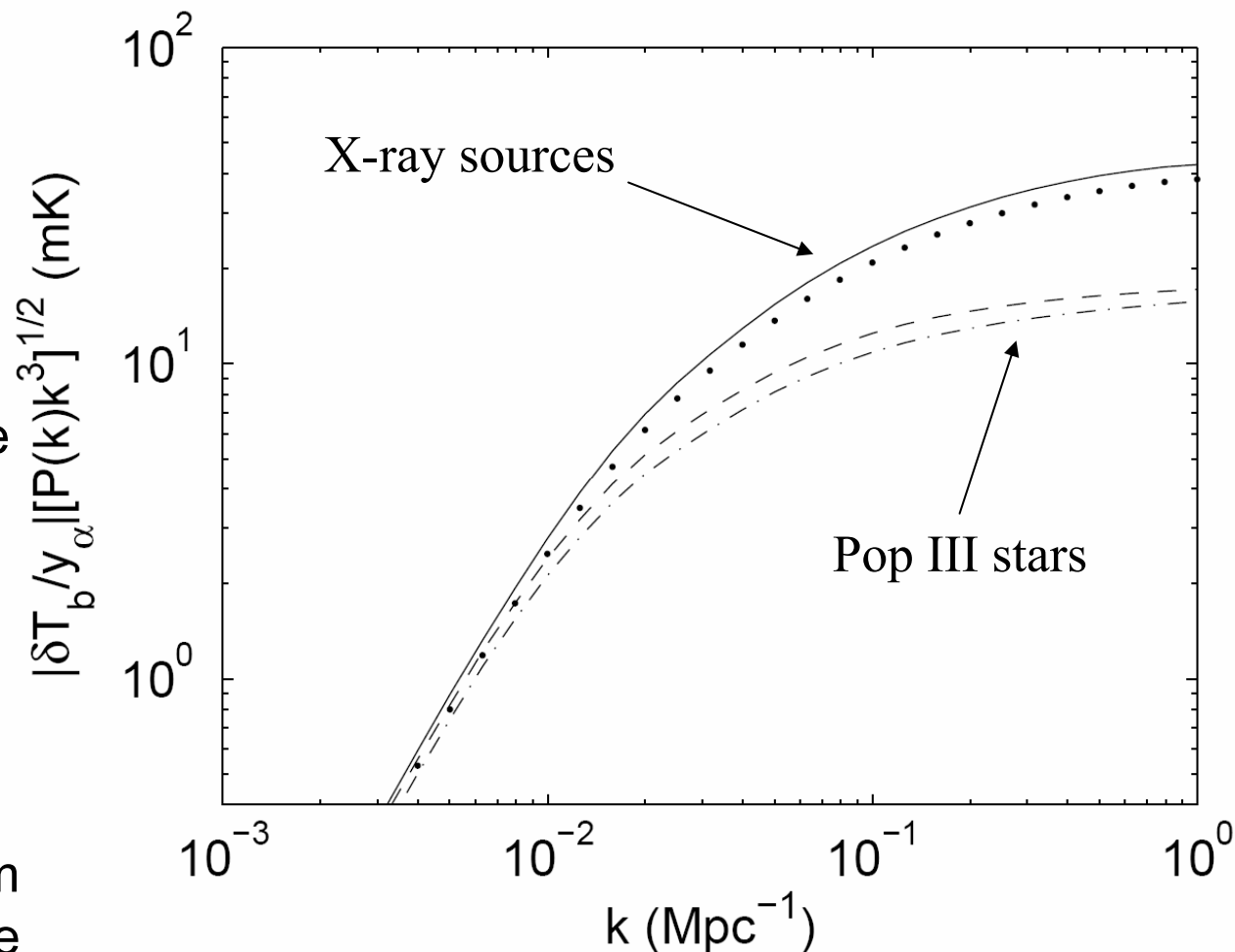


# Recognizing the First Radiation Sources Through Their 21-cm Signature

(Chuzhoy, Alvarez & Shapiro 2006, ApJL, 648, L1; astro-ph/0605511)

## Power spectrum of fluctuating 21-cm signal at $z = 20$

- Ly  $\alpha$  pumping is by halo sources clustered in space
- Assume each halo is either an X-ray source or a UV source from Pop III stars
- X-ray sources influence smaller regions than Pop III stellar sources, typically, so they yield greater fluctuations on small scales
- Future radio arrays plan to detect the 21-cm background and may be able to distinguish this.

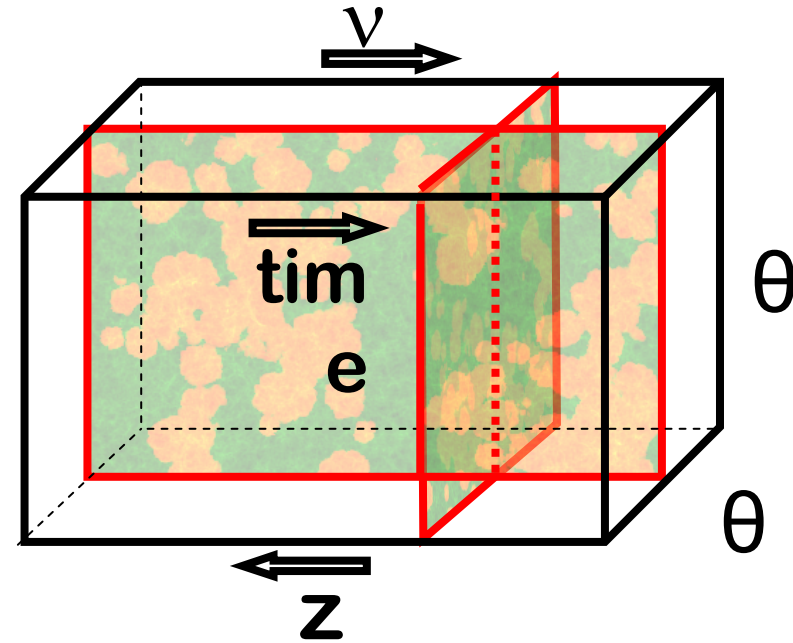


# Stages of 21-cm Background

- Dark Ages
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    - **With heating,  $T_{\text{spin}} > T_{\text{CMB}} \rightarrow$  IGM in emission**

# The Redshifted 21cm Signal From the EoR

- The measured radio signal is the **differential brightness temperature**
- $\delta T_b = T_b - T_{\text{CMB}}$ :  
 $\delta T_b(z) \approx 27 x_{\text{HI}} (1 + \delta) (1 - T_{\text{CMB}}/T_s) [(1+z)/10]^{1/2}$  mK  
(for WMAP3 cosmological parameters).
- Depends on:
  - $x_{\text{HI}}$ : neutral fraction
  - $\delta$ : overdensity
  - $T_s$ : spin temperature
- For  $T_s \gg T_{\text{CMB}}$ , the dependence on  $T_s$  drops out
- The signal is a spectral *line*: carries **spatial, temporal, and velocity information**.



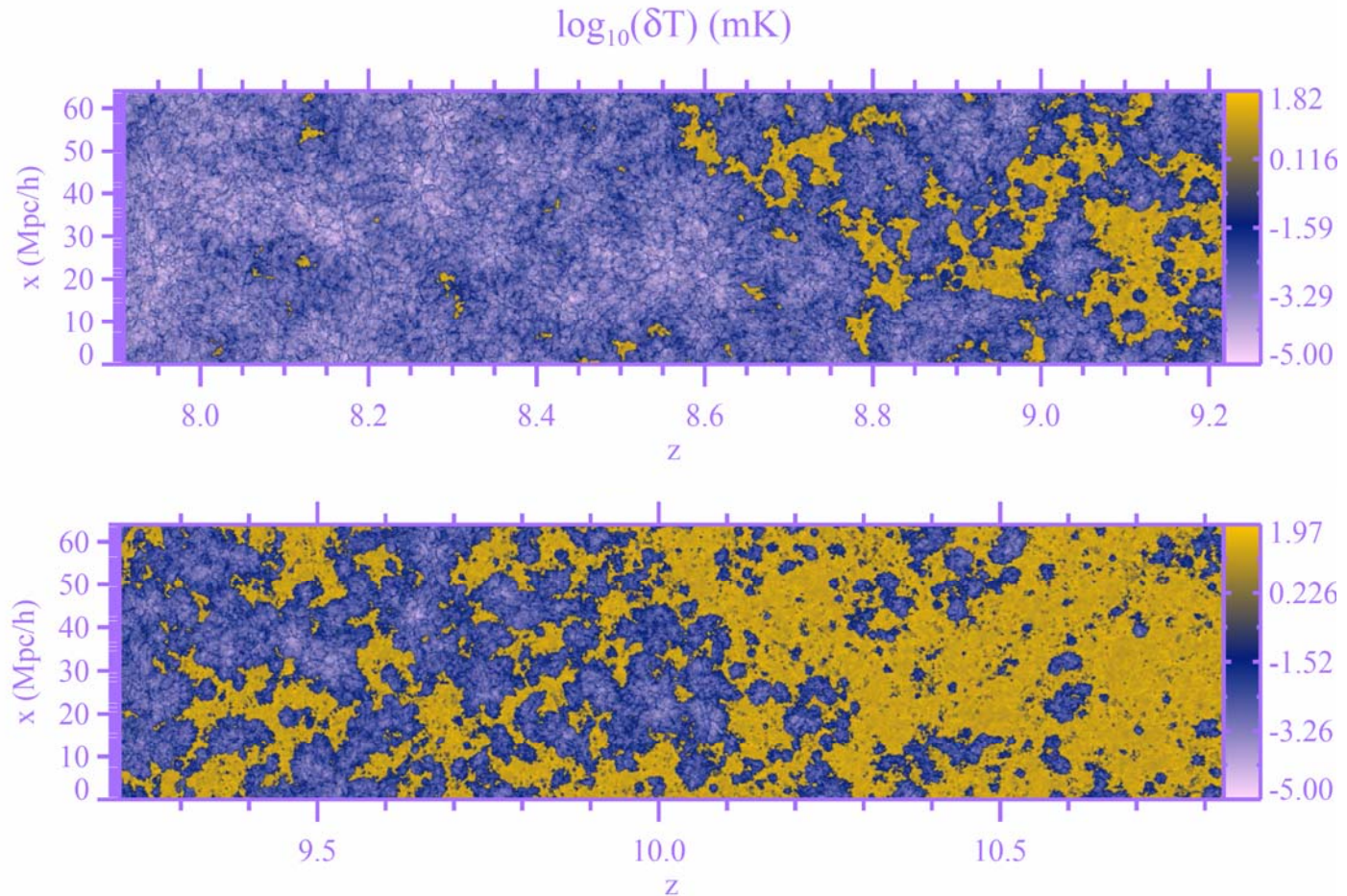
The image cube: images stacked in frequency space



# Reionization topology revealed by fluctuations in 21-cm brightness temperature, $\delta T_b$ , along the line of sight

(Shapiro, Iliev, Mellema, Pen, and Merz 2008, in press; astro-ph/0806.3091)

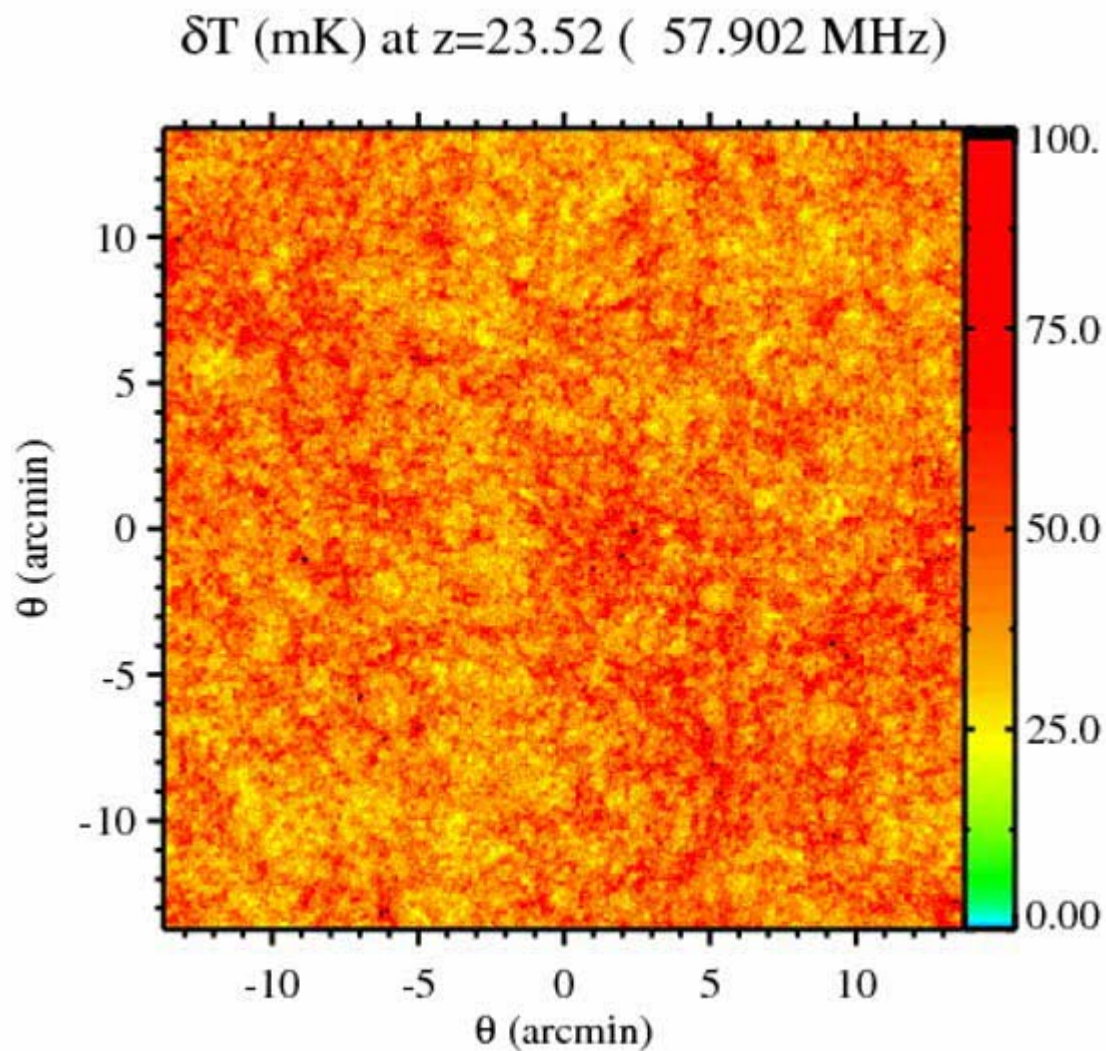
- mapping the sky along the LOS: high-resolution cuts in position-redshift space



- LOFAR should see  
large ionized bubbles!

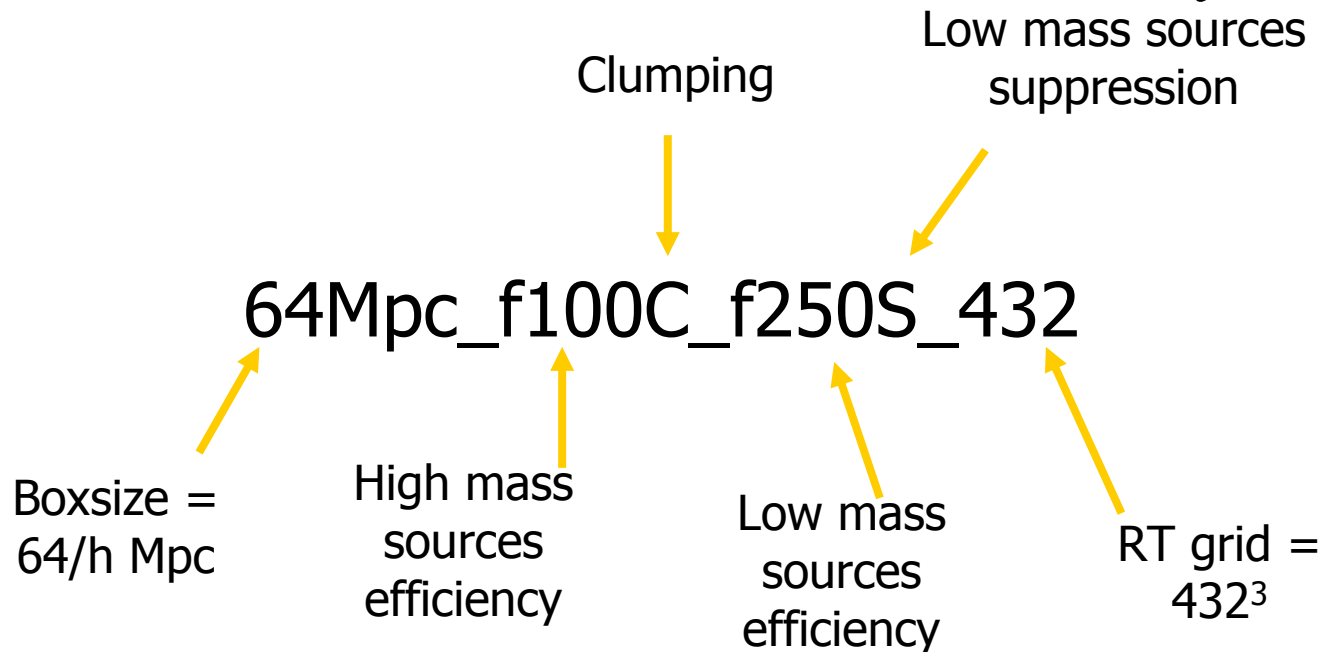
90 Mpc box, WMAP3+

# Sky Maps of 21cm Background Brightness Temperature Fluctuations During Epoch of Reionization : Travel through Time



# Notation

- Our simulations are characterized by



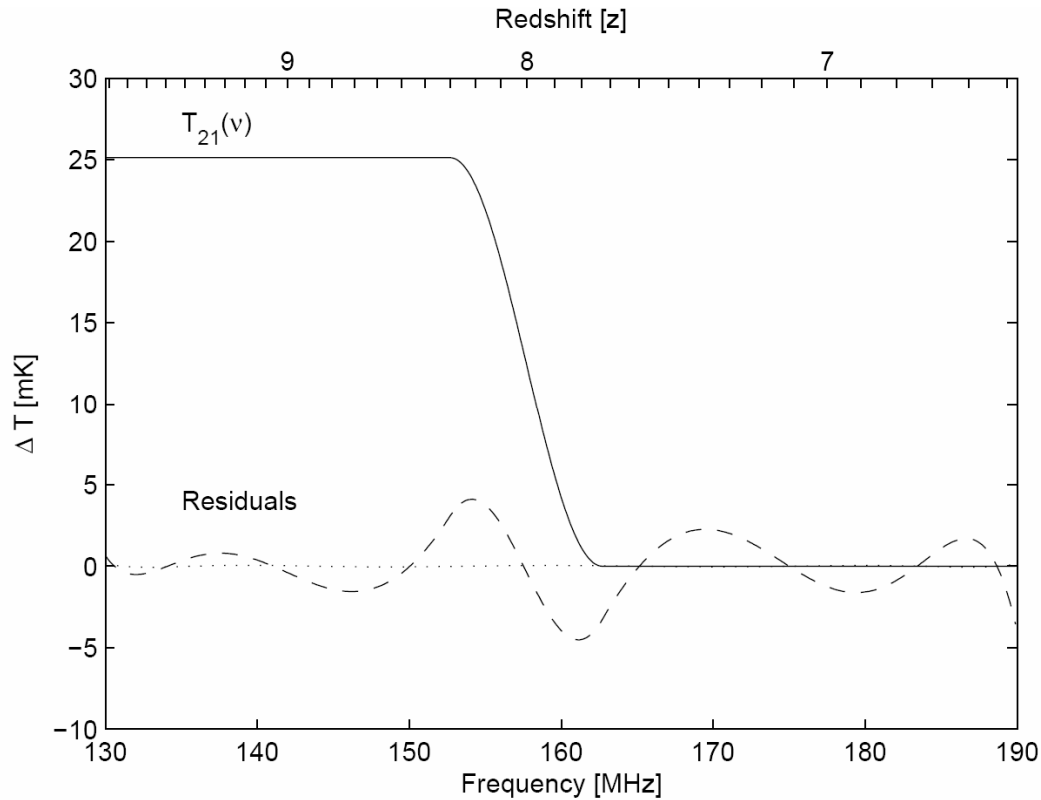
# Statistical Measurements of the 21cm Background During the EoR

- The sensitivity of the upcoming EoR experiments will be too low to image 21cm from reionization pixel by pixel: Statistical measurements needed.
  - **First goal:** to reliably detect signatures from reionization (and separate them from foreground and instrumental effects).
  - **Second goal:** to interpret them in terms of astrophysics (source population and properties).
- Luckily, the 21cm line signal is rich in properties:
  1. Global signals: mean signal, fluctuations.
  2. Angular properties: power spectra
  3. Frequency properties: correlation length, Kaiser effect
  4. Non-Gaussianity.



# EDGES (Mileura Station, Western Australia)

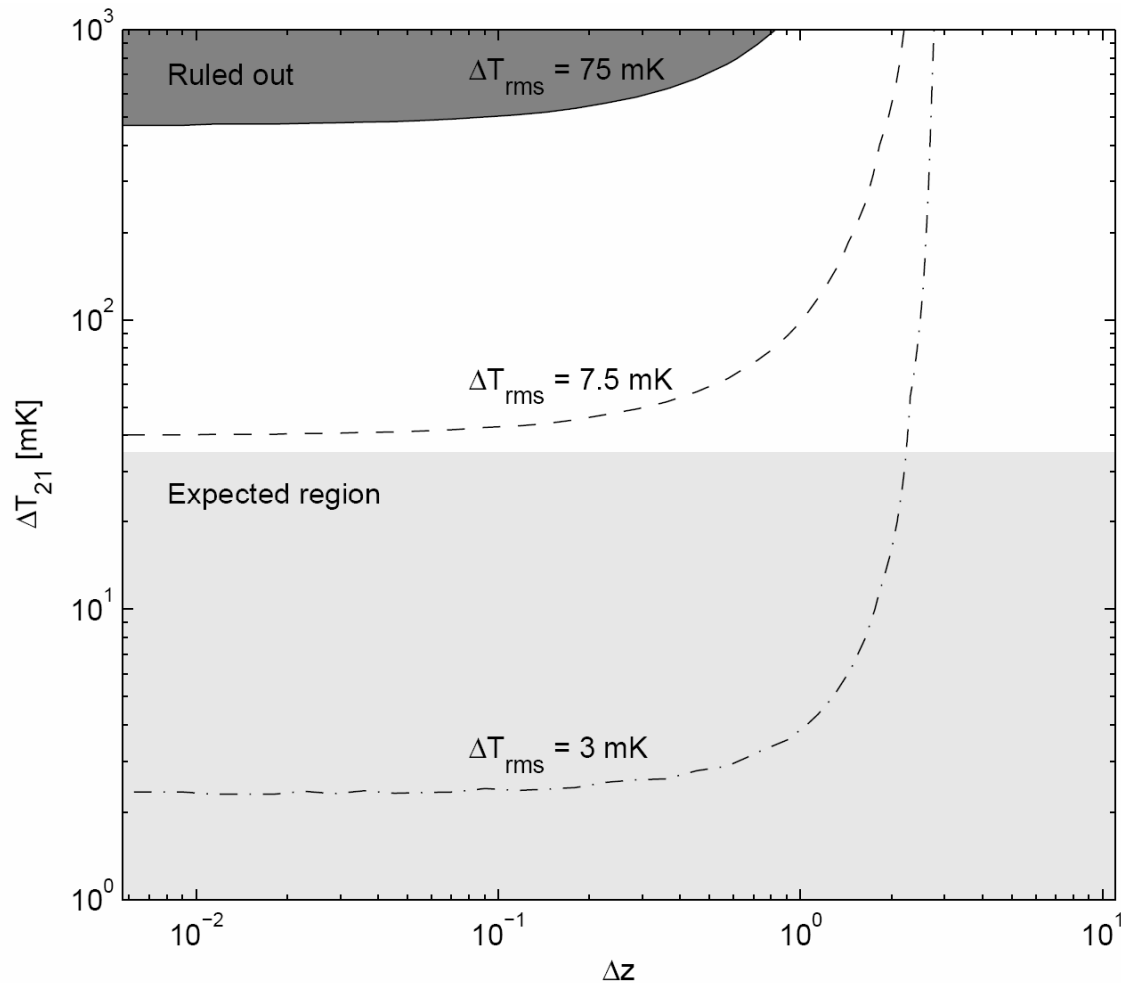
## Bowman, Rogers, and Hewitt (2008)



- Search for a “jump” in the global mean brightness temperature when reionization ends

# EDGES (Mileura Station, Western Australia)

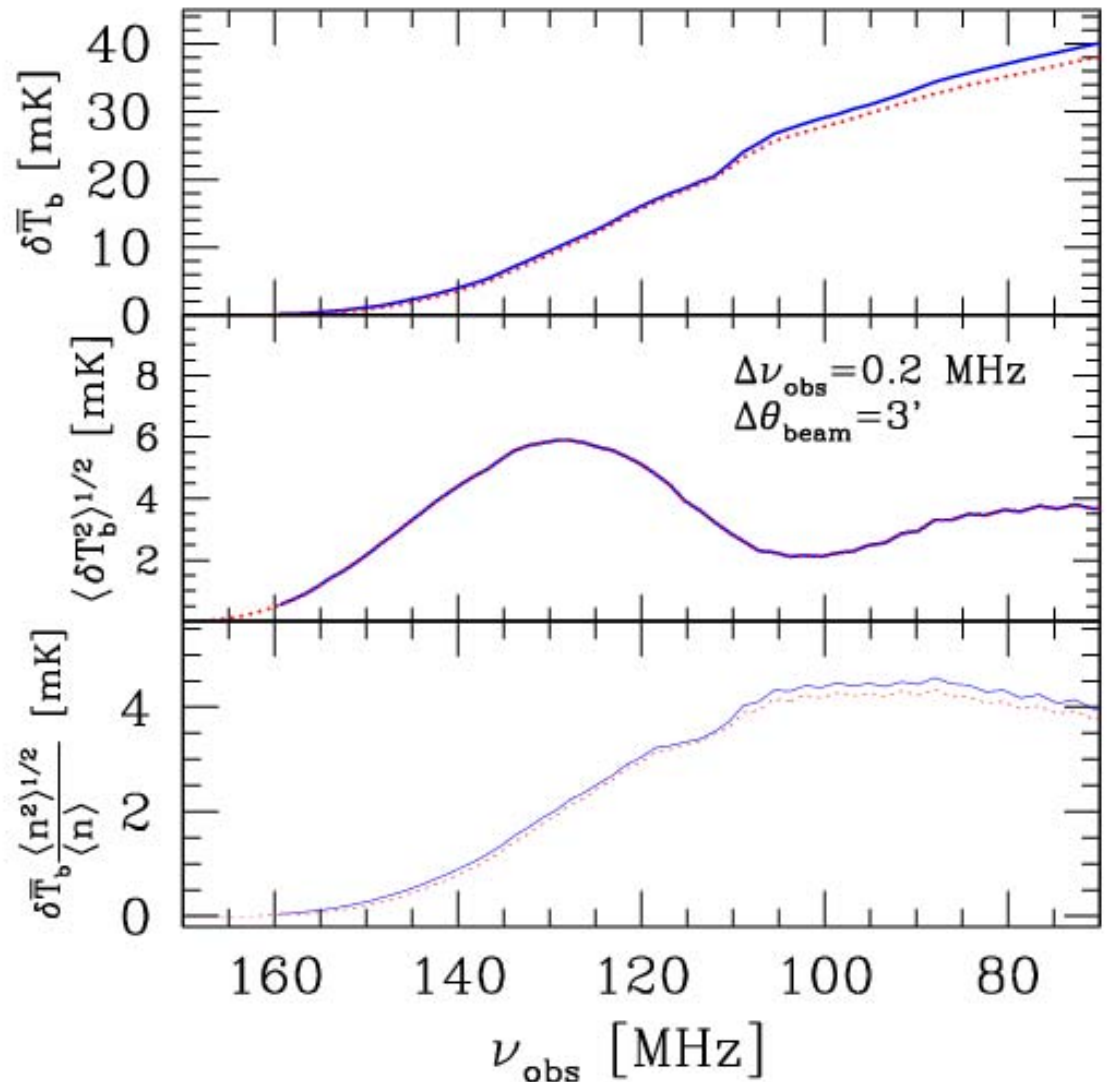
## Bowman, Rogers, and Hewitt (2008)



- First results only rule out extreme cases.

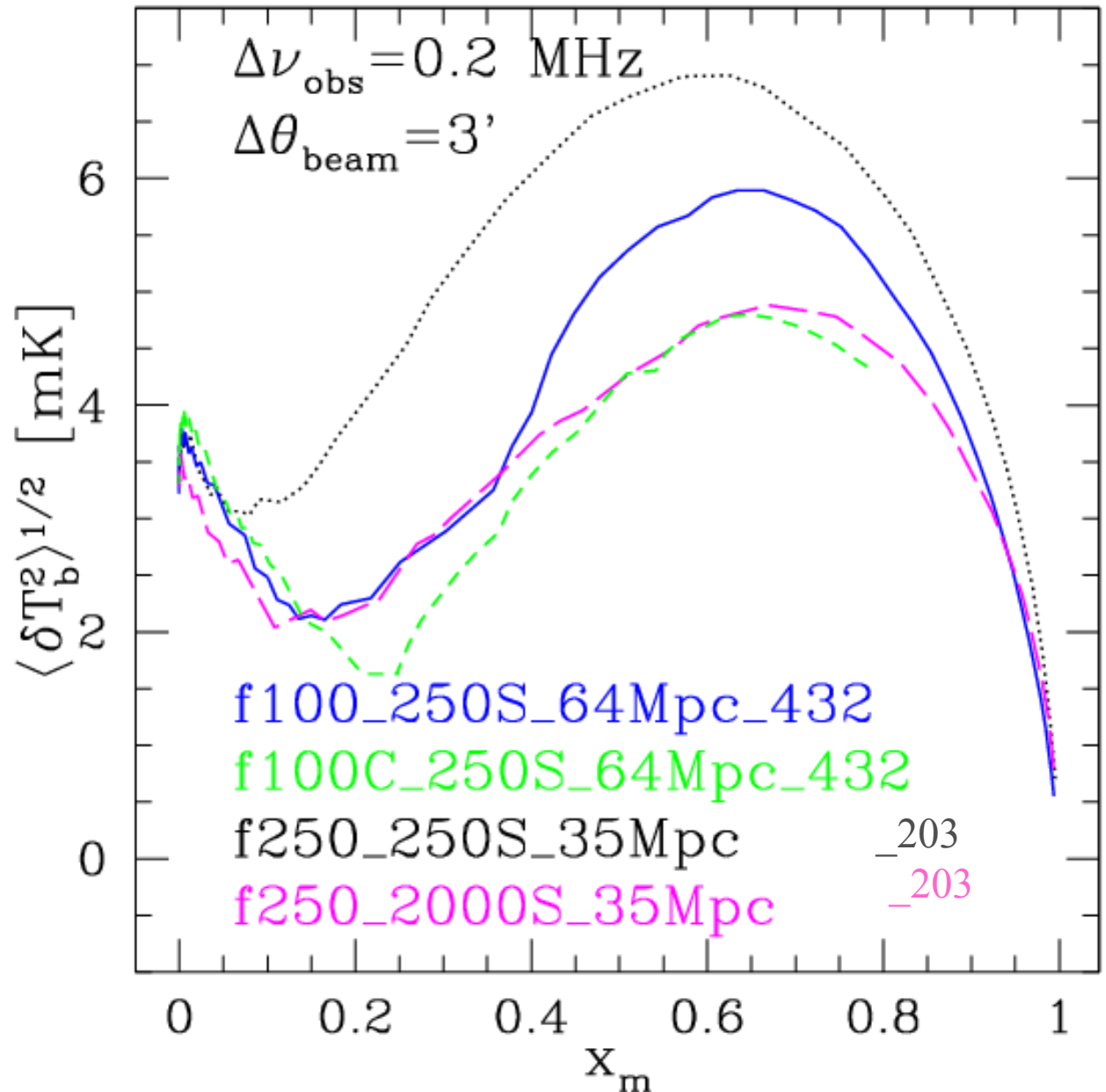
# Global Signals

- In principle, a single dish telescope could measure the change of the global signal with frequency: contrary to early expectations, however, simulations do not show a sharp transition.
- The corresponding measurement by an interferometer would be the change of the 21cm (rms) fluctuations.
- Simulations:  
64Mpc\_f100\_f250S\_432  
and  
64Mpc\_f100\_f250S\_216



# Evolution of 21cm Brightness Temperature Fluctuations

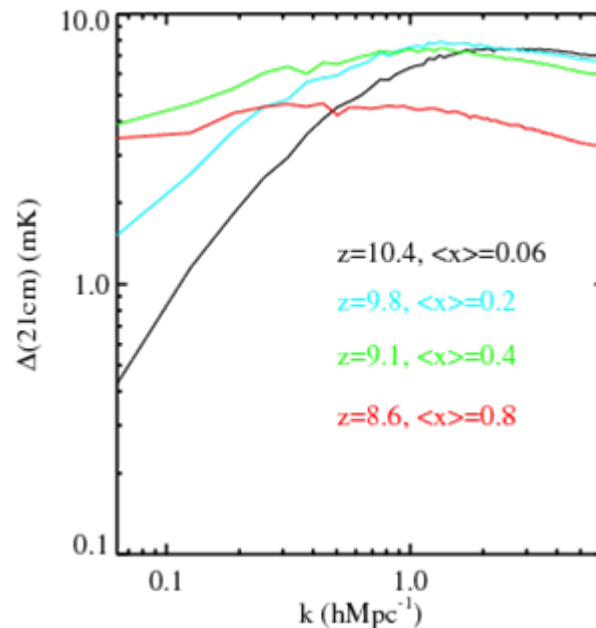
- When plotted against the **mean mass-weighted ionization fraction  $x_m(\text{H II})$** , the evolution of fluctuations shows roughly similar behaviour for different (simulation) resolution and source parameters, but the amplitude differs.
- Peak** around  $x_m(\text{H II}) \sim 0.6-0.7$  (shifts to lower values for higher angular resolution).



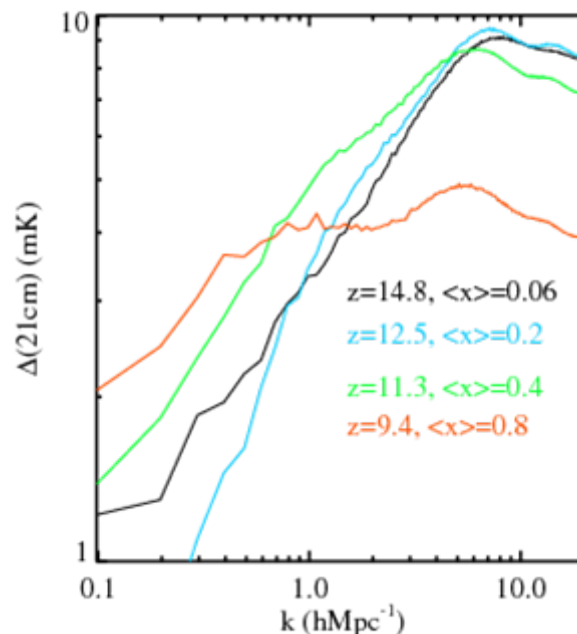


# 21cm Brightness Temperature Fluctuation Power Spectra

- Information about the **length scales** can be obtained from the power spectra.
- Power shifts to larger scales as reionization progresses, and the power spectrum **flattens**.
- Note that the angular power spectrum is measured directly by an interferometer, the multipole  $l$  is equivalent to  $\sqrt{(u^2+v^2)}$  in a visibility map.



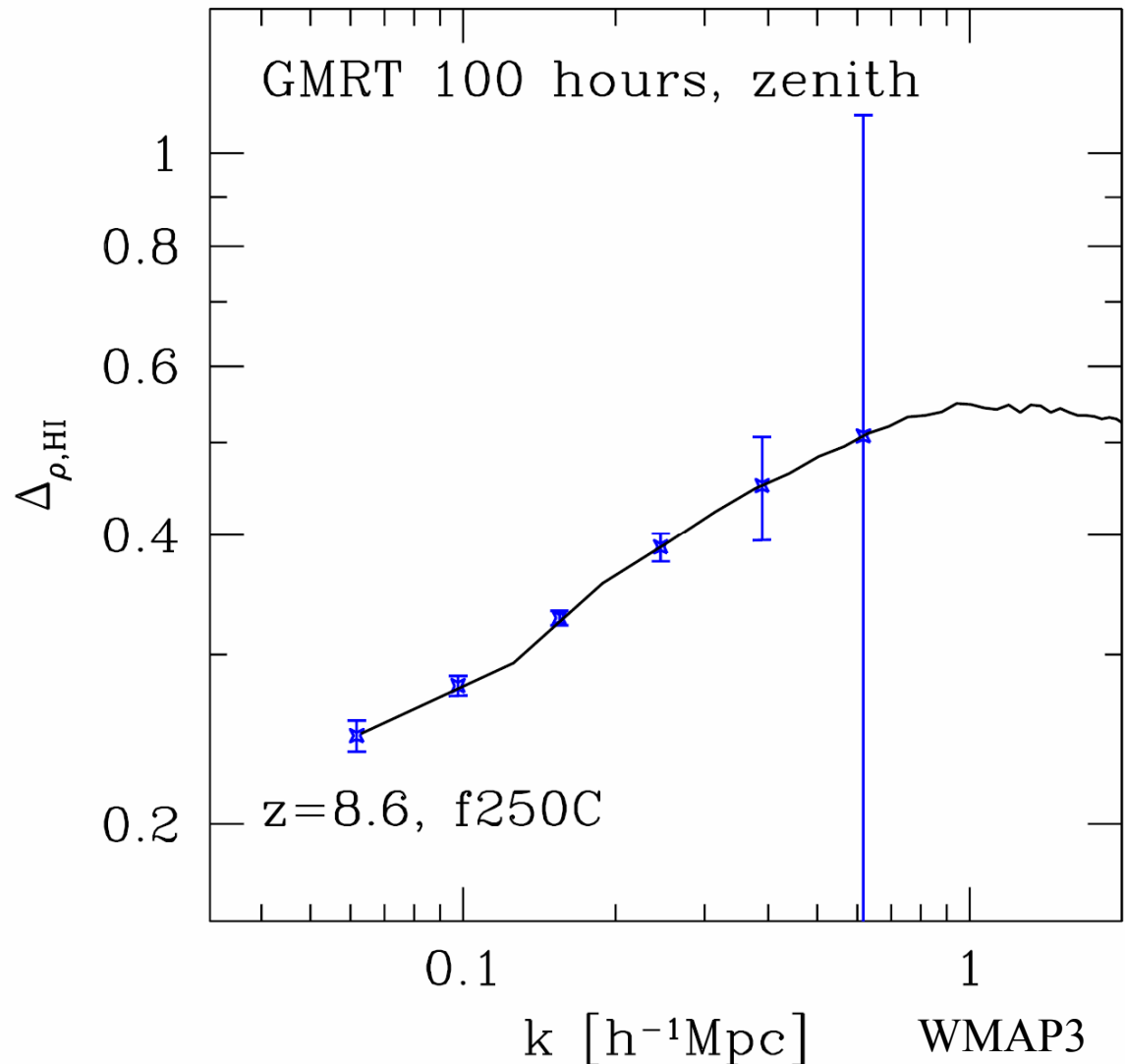
100Mpc\_f250C\_f0\_203



64Mpc\_f100\_f250S\_432

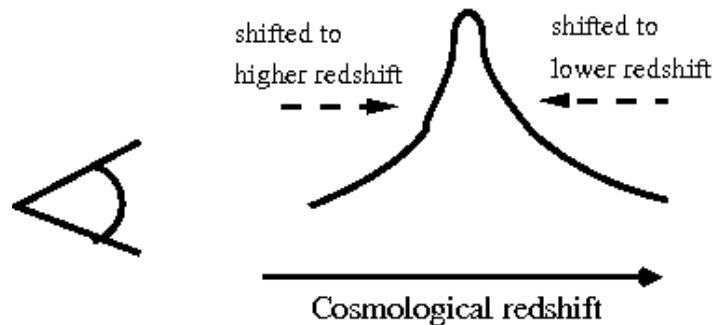
# Observability of the 21-cm signal : 3D power spectrum of the neutral hydrogen density

- We show our predicted 21-cm signal at  $z = 8.6$  ( $x \sim 0.5$ ) for case with  $z_{\text{ov}} = 6.6$ , with GMRT sensitivity, for 100 hrs integration, 15 MHz bandwidth and  $T_{\text{sys}} = 480$  K, pointing at zenith.



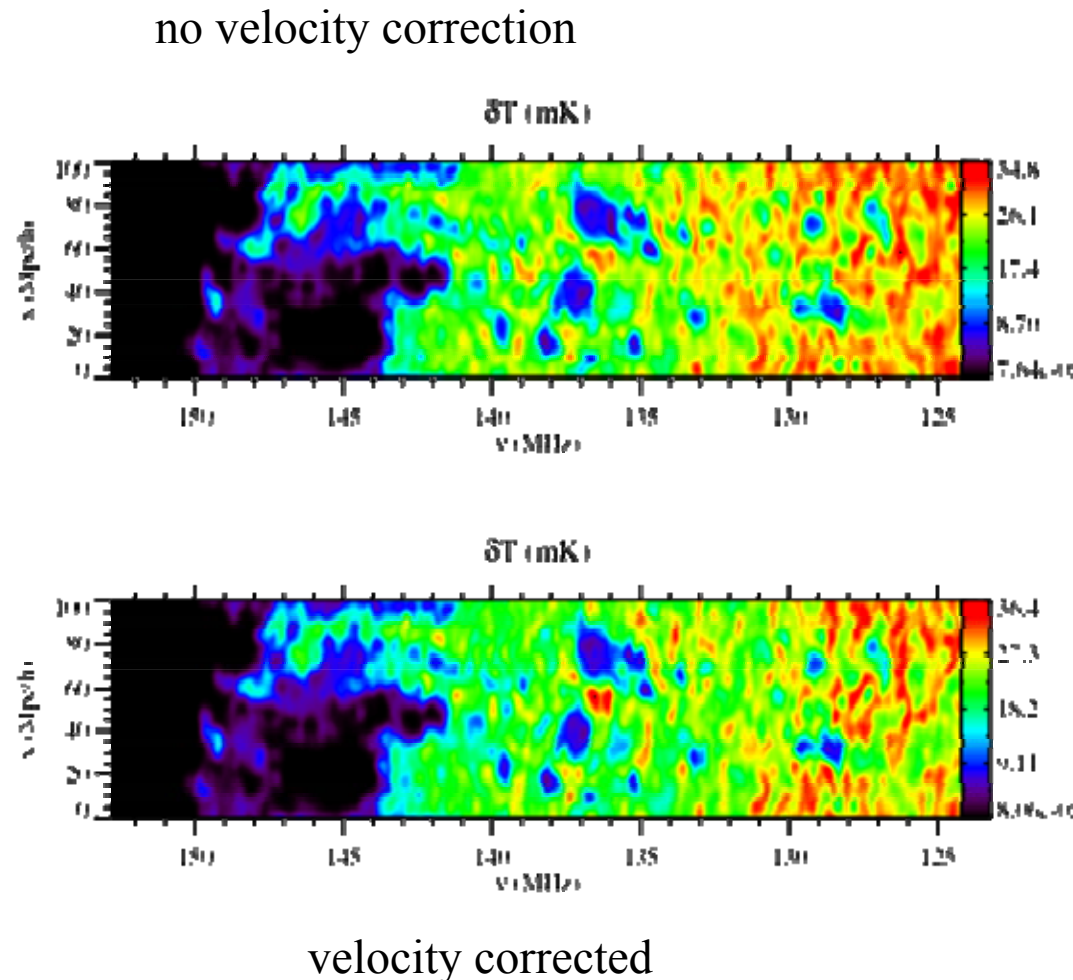
# Peculiar Velocities Cause Redshift Distortions

- Due to the peculiar velocity field, the signal can be displaced from its cosmological redshift.
- '**Kaiser effect**' or '**velocity compression**': due to **infall**, signal concentrates at the high density peaks.
- This is clearly seen in the simulations and gives **~30% increase in fluctuations** (and up to a factor of 2).



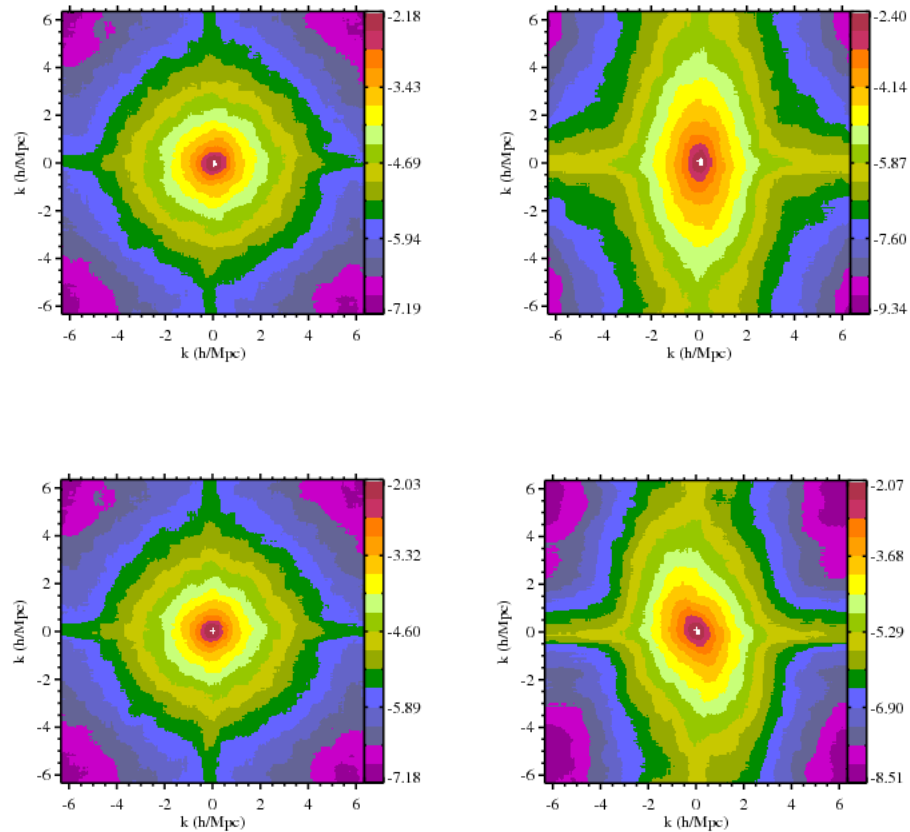
# Effect of the Peculiar Velocity Field : Redshift Distortion

- Adding the velocity distortions visibly **increases the fluctuations** in the neutral medium.
- Maximum value also larger.
- The effect remains noticeable even at LOFAR-like resolution ( $3'$ , 200 kHz).
- Simulation: 100Mpc\_f250C\_f0\_203.



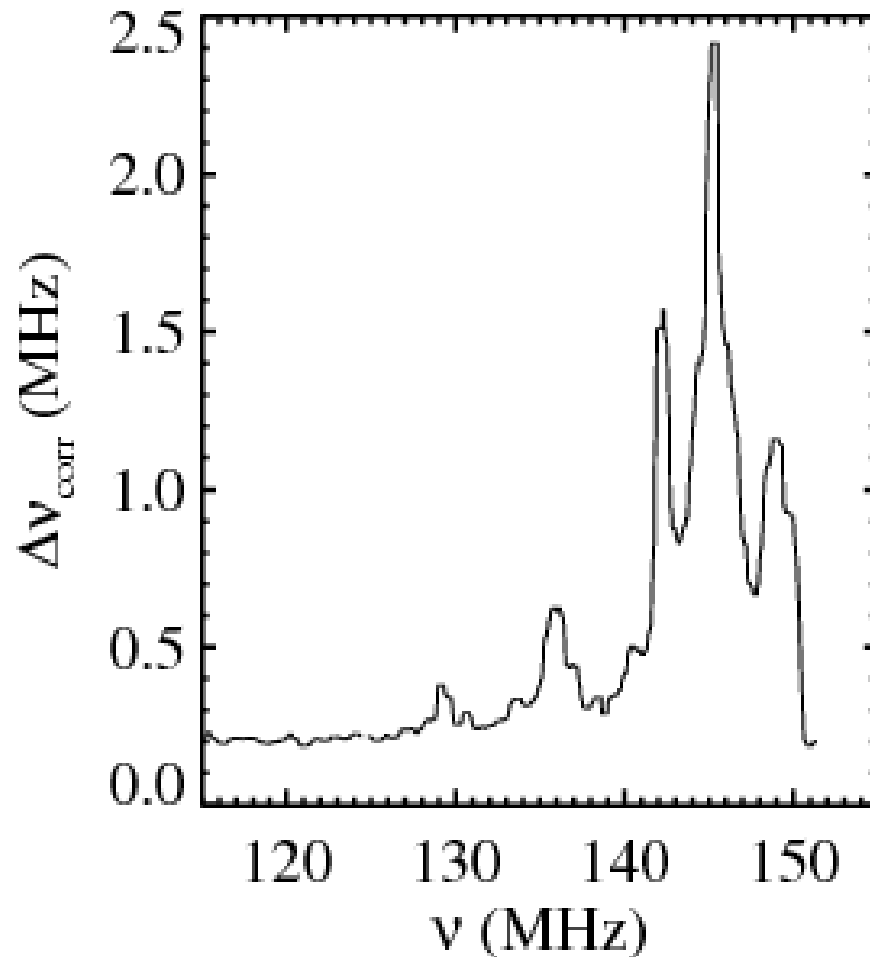


And Peculiar Velocity  $\rightarrow$  Anisotropy in Fourier Space...



# Correlation Length

- Reionization changes the correlation length along the frequency axis in a characteristic way: formation of large H II regions increases correlation length from  $\sim 200$  kHz to  $\sim 1$  MHz.
- Still substantially shorter than for the continuum foregrounds, so it could be used as a test for proper foreground subtraction.

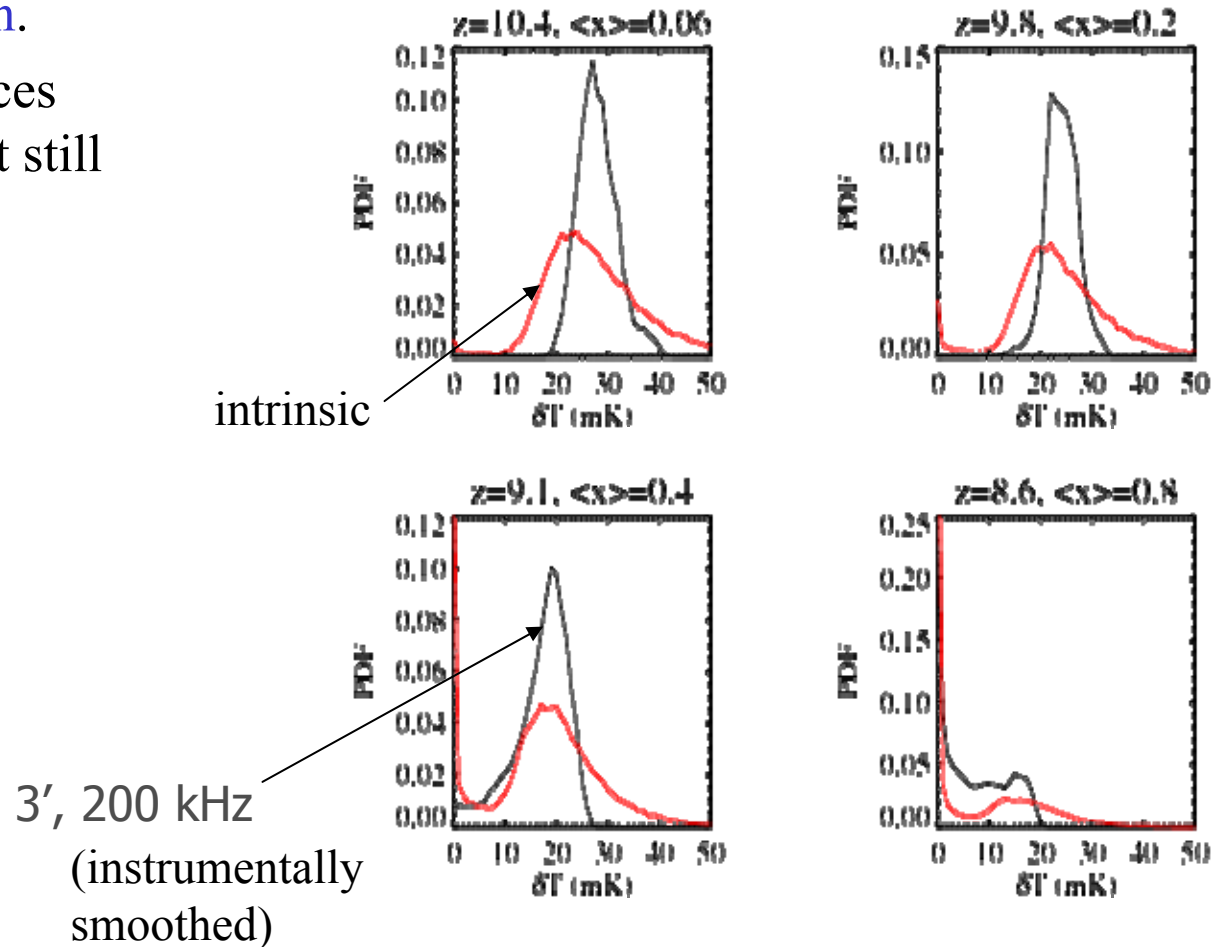


Simulation 100Mpc\_f250C\_f0\_203

# Non-Gaussianity

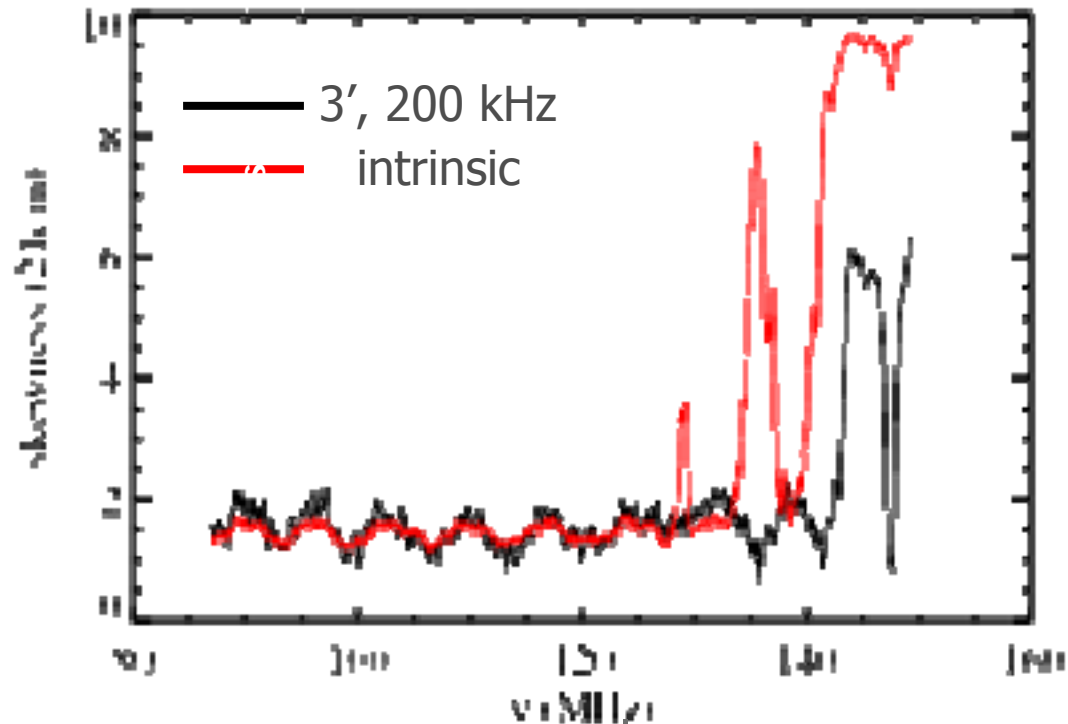
- Probability distribution functions of the 21cm signal are clearly **non-Gaussian**.
- Limited resolution reduces the effect somewhat, but still noticeable.
- Towards the end of reionization the effect is largest.

Simulation 100Mpc\_f250C\_f0\_203



# Skewness

- Non-Gaussianity suggests that measuring the **skewness** could be an interesting diagnostic.
- The simulations show a clear evolution of skewness with increasing ionization.
- Finite resolution modifies skewness, but does not remove it.
- Skewness may offer a good way to detect the signal, if remnants of foreground subtractions and other effects are dominantly Gaussian (cf. Harker et al. 2008).





# The Fluctuating H<sub>2</sub> Dissociating Background During Reionization

Ahn, Shapiro, Iliev, Mellema, & Pen 2008, ApJ, submitted (astro-ph/0807.2254; 0807.0920)

- Simulations suggest first stars formed inside minihalos of mass  $\sim 10^{5-6}$  solar masses at redshift  $z > \sim 20$ , when H<sub>2</sub> molecules cooled the primordial, metal-free gas and gravitational collapse ensued.
- **But** H<sub>2</sub> Lyman-Werner (“LW”) band photons (11.2 – 13.6 eV) dissociate H<sub>2</sub>, so too much LW background intensity (i.e.  $J_{\text{LW}} > (J_{\text{LW}})_{\text{threshold}}$ )
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• **How high does it get?**

# The Fluctuating H<sub>2</sub> Dissociating Background During Reionization

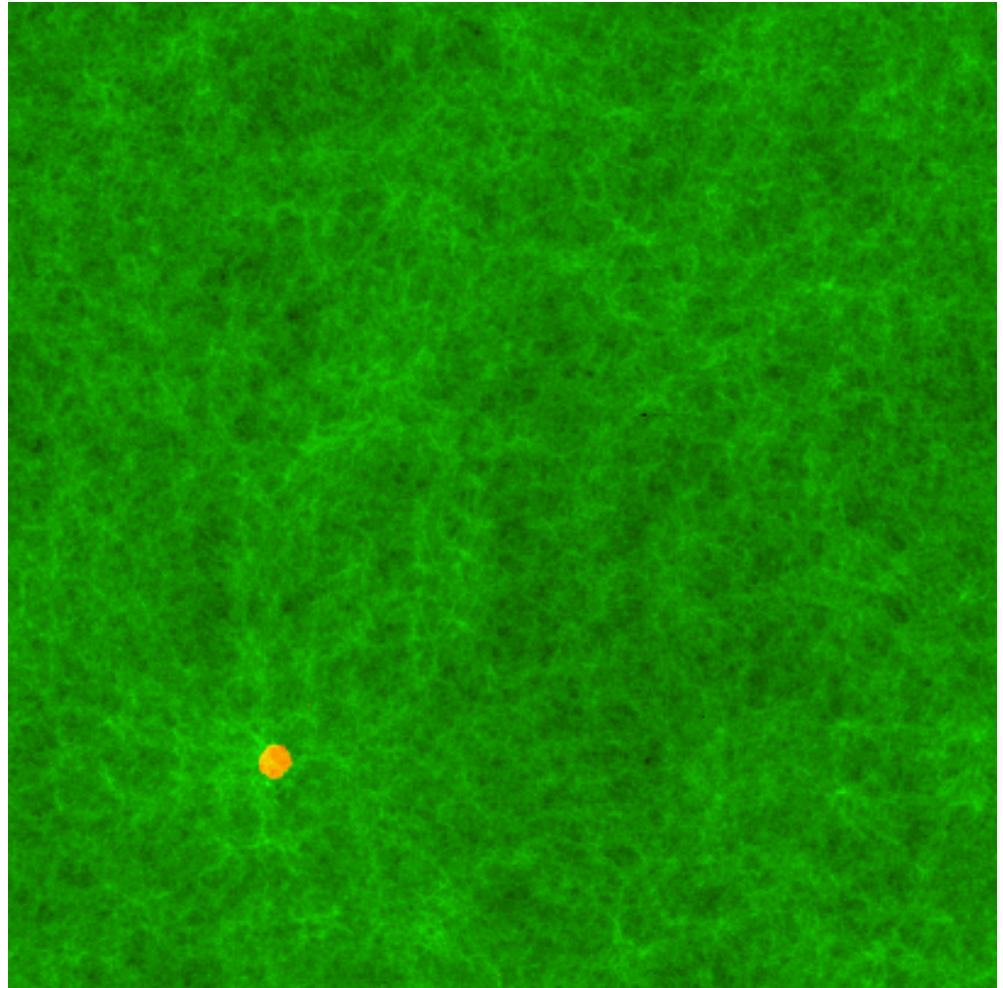
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- Ionization sources also emit continuum below Lyman limit, in the H<sub>2</sub> Lyman-Werner bands (11.2 – 13.6 eV).
- In IGM, this radiation is attenuated by scattering in H Lyman series lines and downgrading to lower energy photons.
- By transferring this radiation from each source halo thru the IGM, we compute the inhomogeneous LW band intensity field during reionization.
- e.g. Pop II sources,  
 $f_{\text{esc}} = 0.2$ ,  $f_* = 0.2$ ,  
 $f_\gamma = 250$ .

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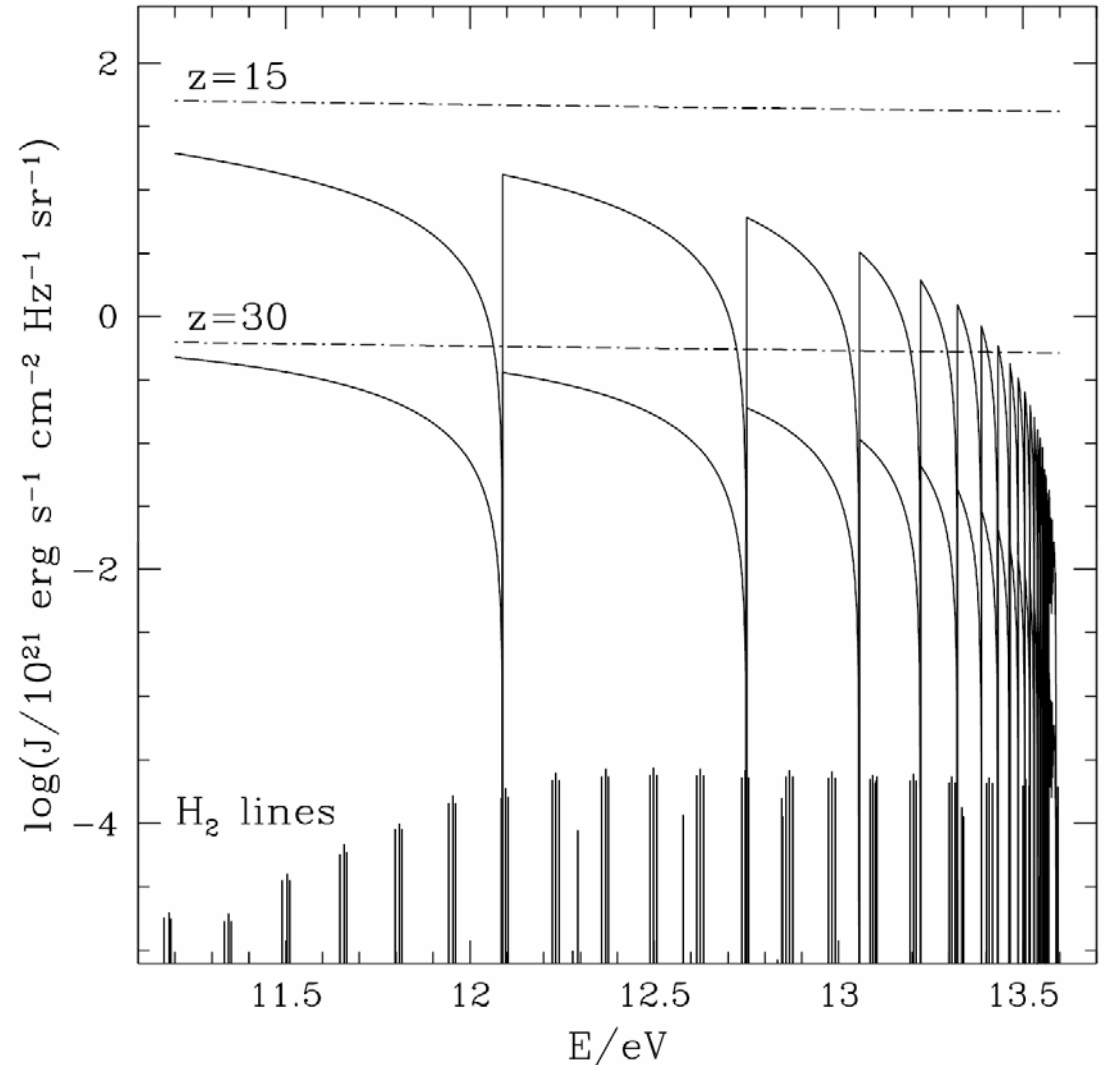
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 $f_\gamma = 250$ .



35/h Mpc box

# Previous approximation for cosmic mean LW Background during EOR: homogeneous universe → “saw-tooth” modulation

- assume sources of UV emissivity *uniformly* distributed in space (e.g. Haiman et al. 2000; Ricotti et al. 2002; Yoshida et al. 2003)
- assume  $H_2$  dissociating photons, emitted below H Lyman limit, are removed whenever they redshift into an H Lyman series line and are resonantly scattered by the IGM, down-converting them out of LW bands
- uniform IGM opacity filters uniformly distributed LW emitters by “saw-tooth” modulation.

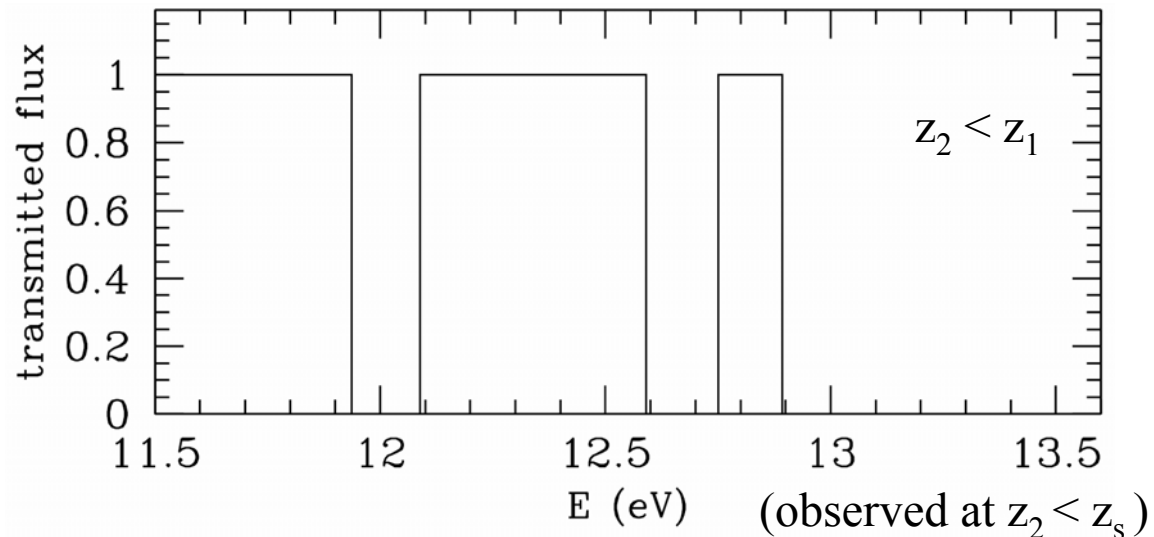
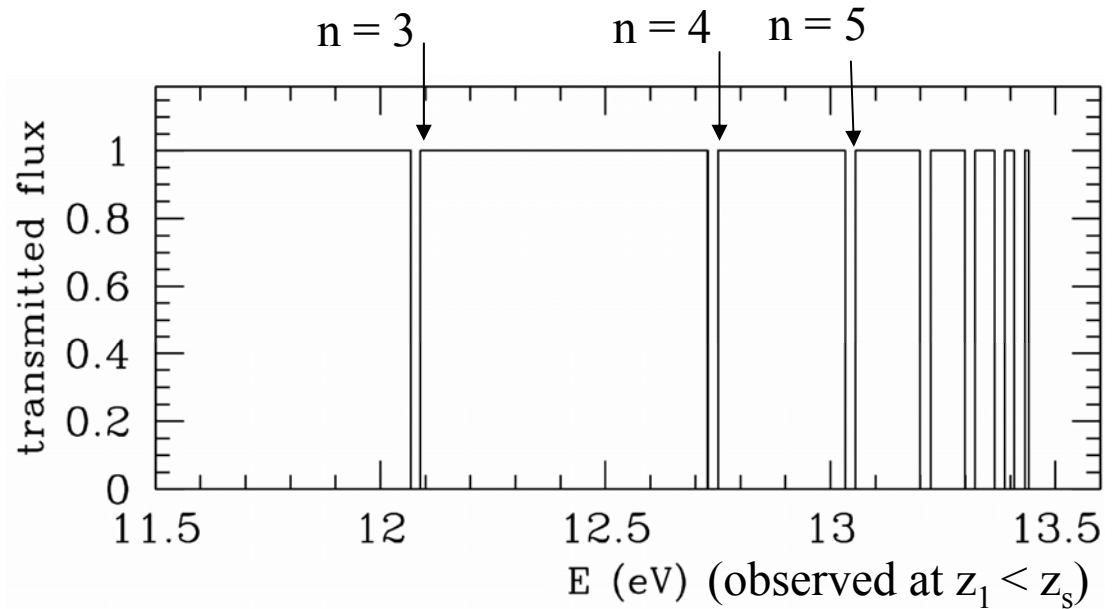


(Haiman, Abel, and Rees 2000)

# Attenuation of LW photons from a single source: “picket-fence” modulation

- A source at redshift  $z_s$  observed at different distances suffers different amounts of attenuation, dilution, and redshift
- When LW photon redshifts into the nearest lower H Lyman series line, it is scattered and destroyed (converted to lower energy photon).
- Source is completely attenuated at comoving distance

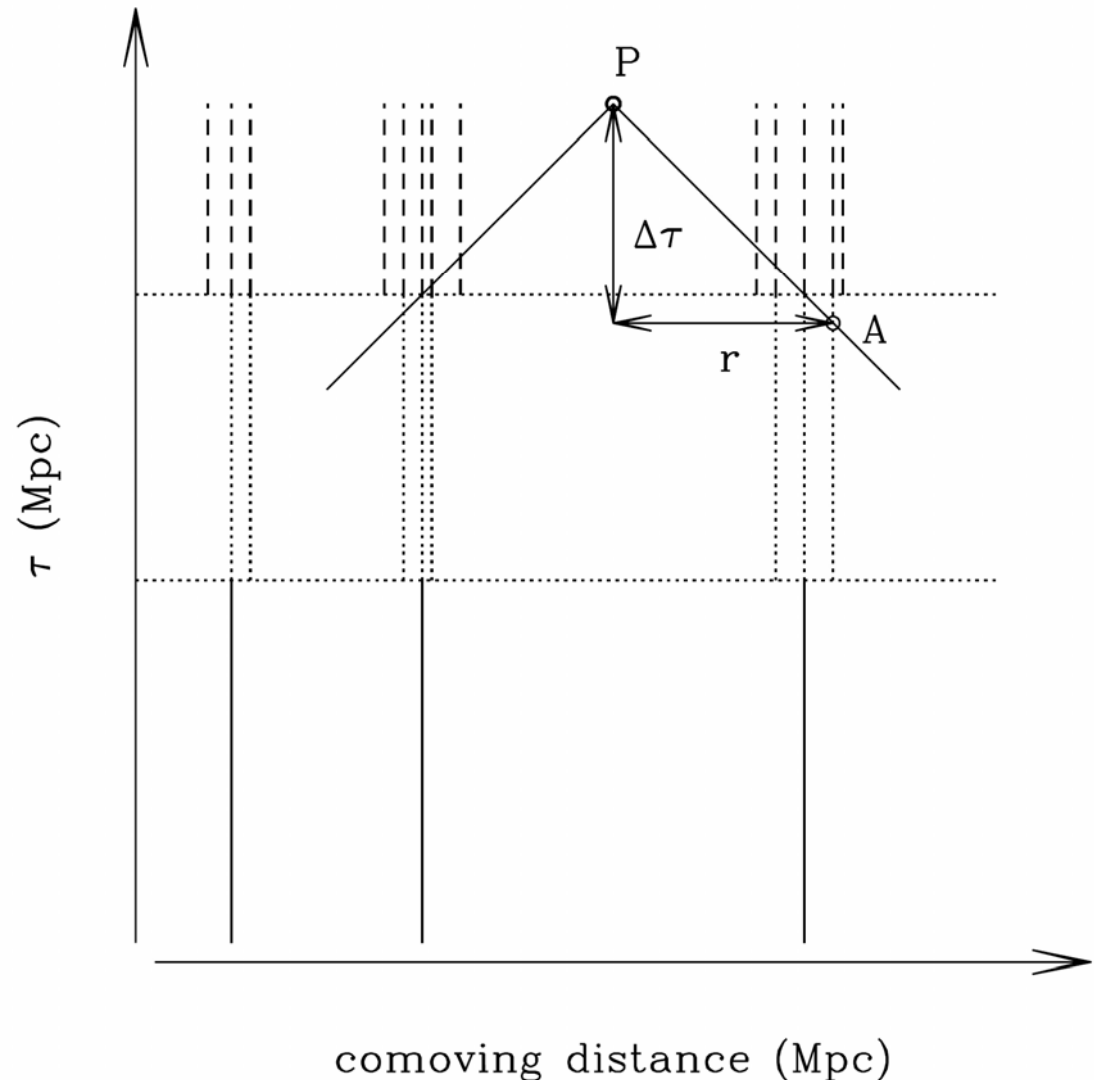
$$r_{\text{cMpc}} = 97 [(1 + z)/21]^{-0.5}$$





LW background radiative transfer is intrinsically cosmological : sources along the “past light-cone” of every point in space

- Space-time diagram of radiation sources and observer at point P at conformal time  $\tau$
- luminosity of each halo source is constant during finite time-step
- observer at point P will see sources whose world lines intersect the past light-cone
- must determine the attenuation, dilution, and redshift of the LW photons emitted at A and received at P



# Computational Challenge

$J_\nu(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}})$  at observed frequency  $\nu_{\text{obs}}$  at some comoving position  $\mathbf{x}_{\text{obs}}$  at redshift  $z_{\text{obs}}$  is given by

$$J_\nu(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}}) = \frac{1}{4\pi} \sum_s F_{\nu,s}(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}}), \quad (5)$$

where  $F_{\nu,s}$  is the flux received at  $(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}})$  that was emitted at  $(\mathbf{x}_s, z_s, \nu_s)$  by a source (denoted by subscript  $s$ ), where

$$\frac{\nu_s}{\nu_{\text{obs}}} = \frac{1 + z_s}{1 + z_{\text{obs}}}. \quad (6)$$

# Computational Challenge

The position and redshift,  $(\mathbf{x}_s, z_s)$ , of a source are related to those of the observer at  $(\mathbf{x}_{\text{obs}}, z_{\text{obs}})$  by the fact that the signal emitted at the epoch  $z_s$  must reach the position  $\mathbf{x}_{\text{obs}}$  at the epoch  $z_{\text{obs}}$ , travelling at the speed of light while the universe expands. We express this implicitly by writing the comoving separation,  $r_{\text{os}}$ , of the source and observer as follows:

$$r_{\text{os}} = |\mathbf{x}_{\text{obs}} - \mathbf{x}_s| = \int_{t(z_s)}^{t(z_{\text{obs}})} \frac{cdt}{a(t)} = - \int_{z_{\text{obs}}}^{z_s} c \frac{dz}{H(z)}. \quad (7)$$

# Computational Challenge

The differential flux,  $F_{\nu,s}$ , received at  $(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}})$  from a source of differential luminosity  $L_\nu$  emitted at  $(\mathbf{x}_s, z_s, \nu_s)$  is given by

$$F_{\nu,s}(\mathbf{x}_{\text{obs}}, z_{\text{obs}}, \nu_{\text{obs}}) = \frac{L_\nu(\nu = \nu_s)}{4\pi D_L^2(z_{\text{obs}}, z_s)} \cdot \left( \frac{1 + z_s}{1 + z_{\text{obs}}} \right) \cdot \exp[-\tau_{\nu_{\text{obs}}}], \quad (9)$$

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- Expected number of computational operations :  $\sim N_{\text{sources}} * N_{\text{cells}} * N_{\text{frequencies}}$   
where  $N_{\text{sources}} > \sim 10^7$  within the LW horizon of  $r_{\text{LW}} \sim 100$  cMpc  
 $N_{\text{cells}} > \sim 10^6$  grid cells for sufficient resolution and statistical accuracy  
 $N_{\text{frequencies}} \gg 1$  for multi-frequency transfer of optically thick Lyman series lines  
➔ *full 3D, multi-frequency radiative transfer would be prohibitive!!*



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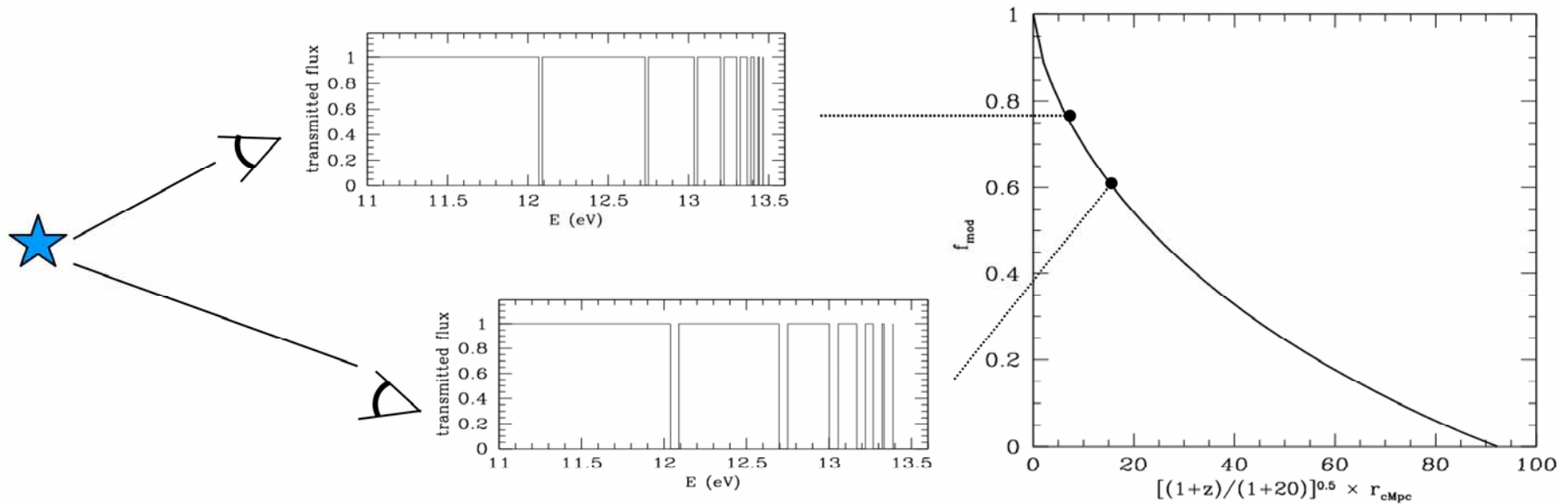
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- ➔ *full 3D, multi-frequency radiative transfer would be prohibitive!!*
- ➔ **We solve this by making a grey opacity approximation equivalent to multi-frequency...**

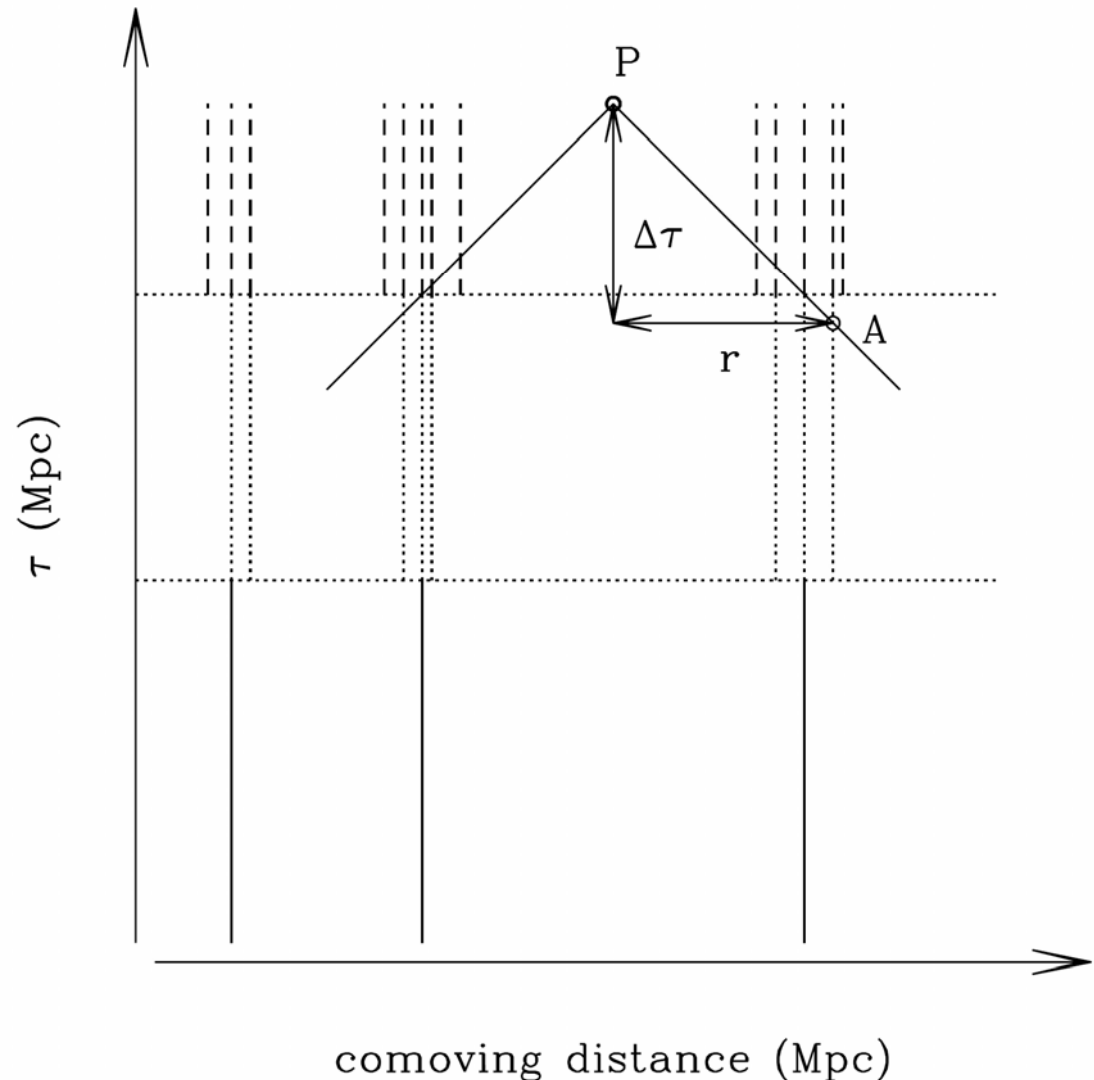
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Modulation Factor

LW background radiative transfer is intrinsically cosmological : sources along the “past light-cone” of every point in space

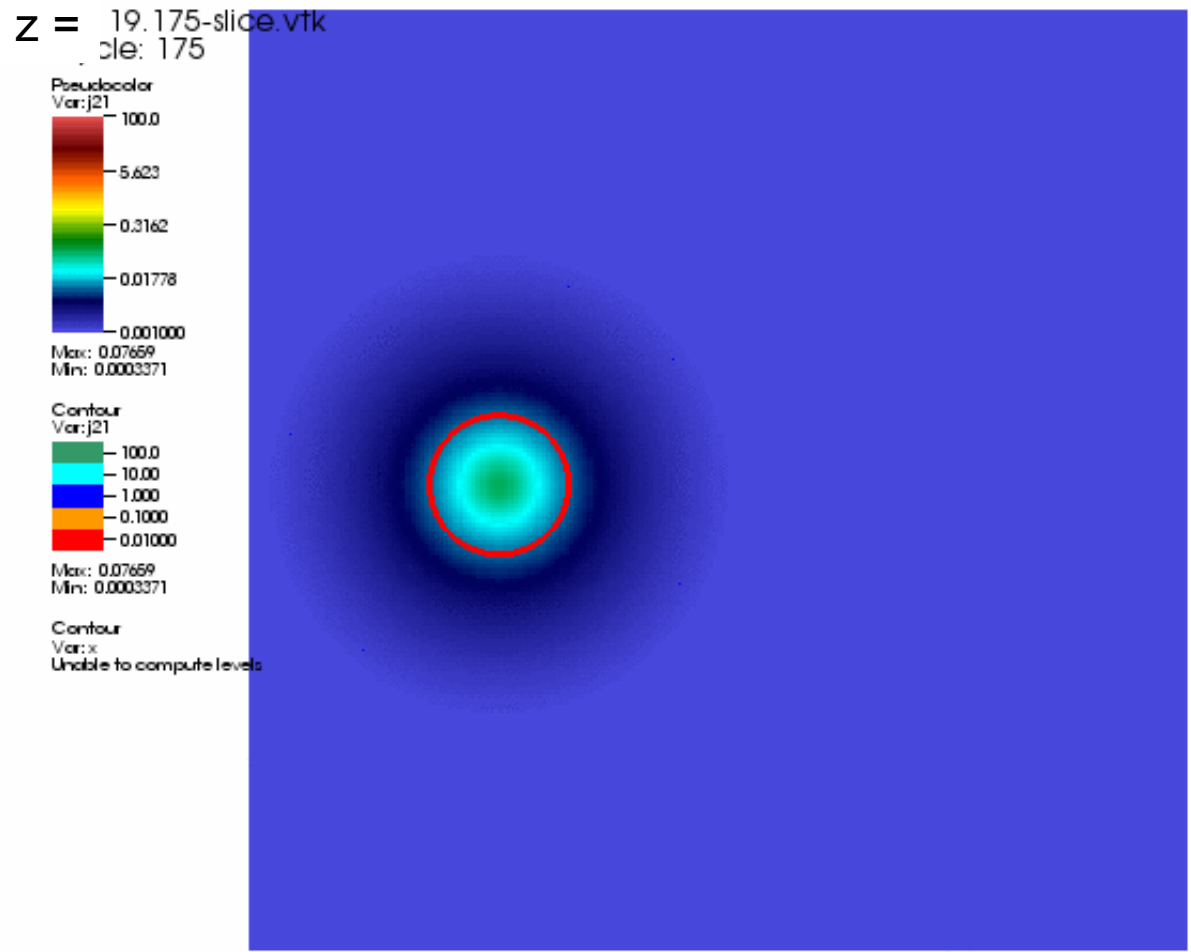
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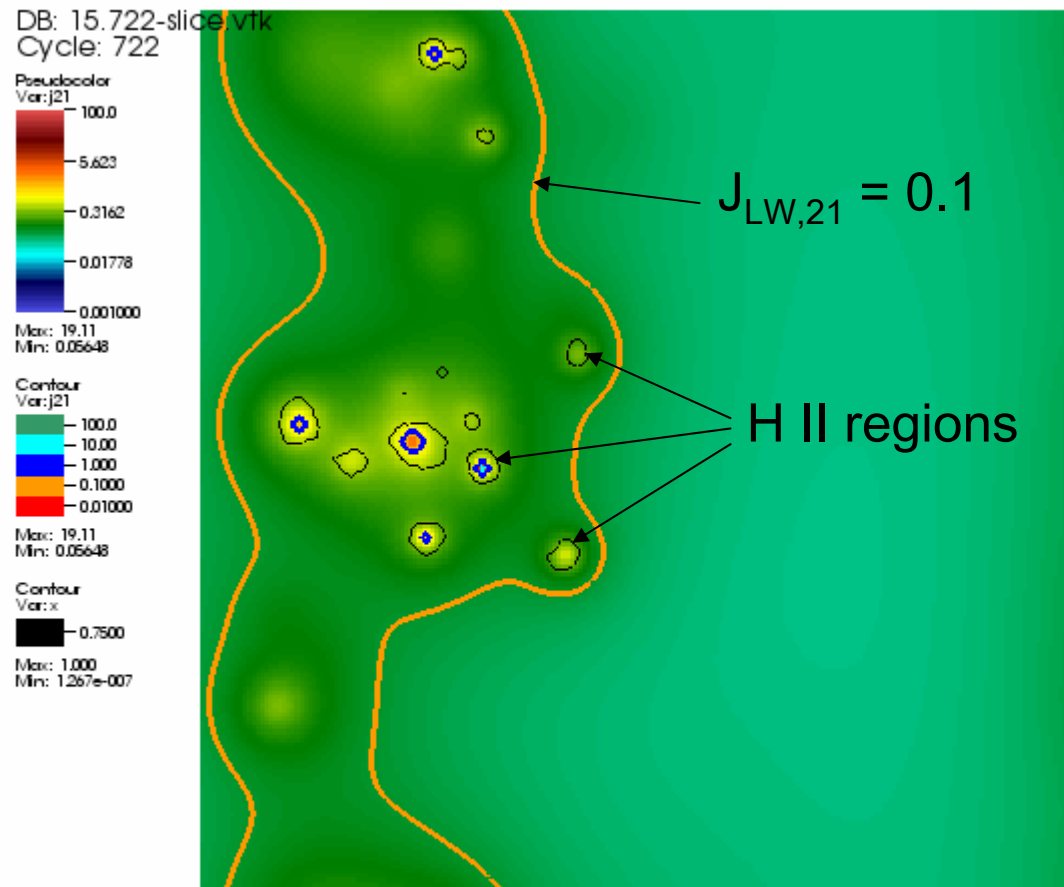
Ahn, Shapiro, Iliev, Mellema, & Pen 2008, MNRAS, submitted (astro-ph/0807.0920)

- LW background radiative transfer code parallelized using MPI for distributed-memory parallel computers;
- e.g. 35/h Mpc reionization simulation has  $(203)^3$  cells,  $N_{\text{sources}} = 200,000$  by  $z = 8$ , but must do LW transfer in  $5^3$  boxes stacked around the central box to fill 100 Mpc LW horizon →  $N_{\text{sources}}$ , total > 20 million!
- Ran for 22 hours, on 320 computing cores, 1.5 GB memory per core, Texas supercomputer *Lonestar* (5200 cores of dual-core Intel Xeon processors, with 11.6 TB aggregate memory).



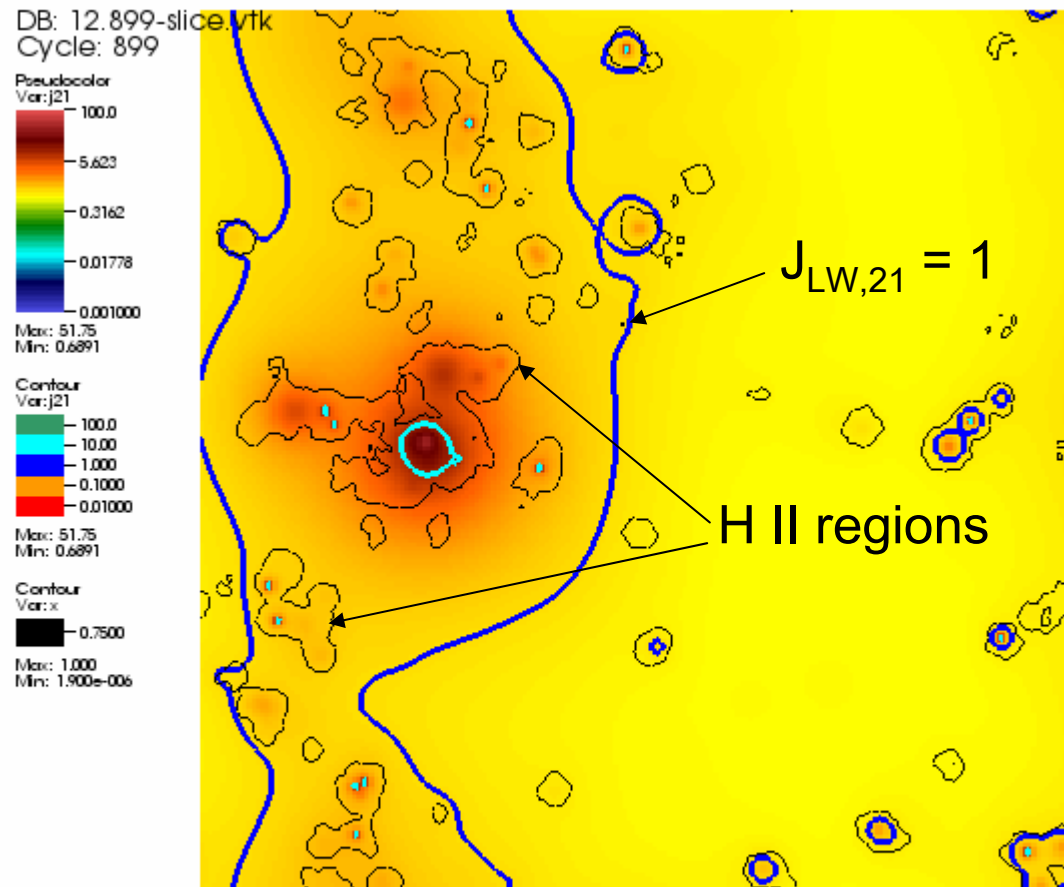
35/h Mpc box

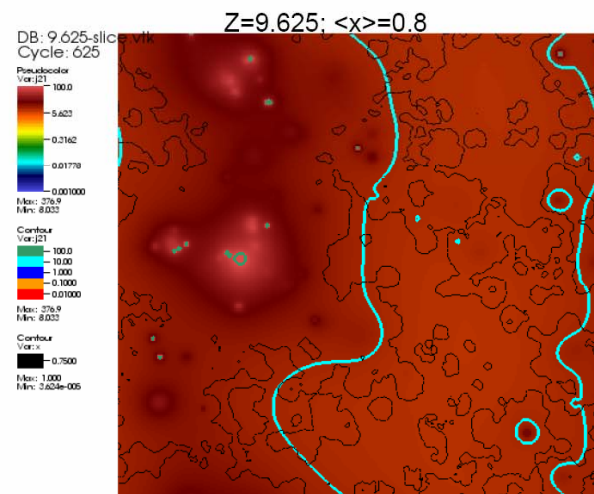
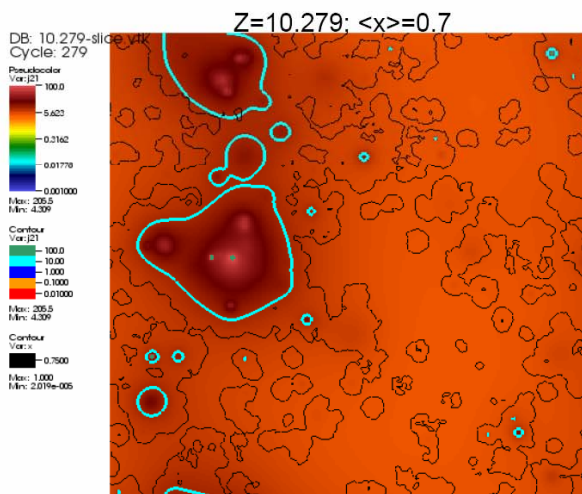
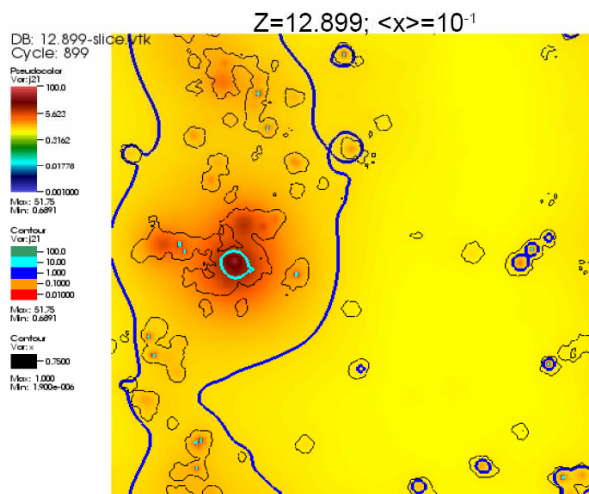
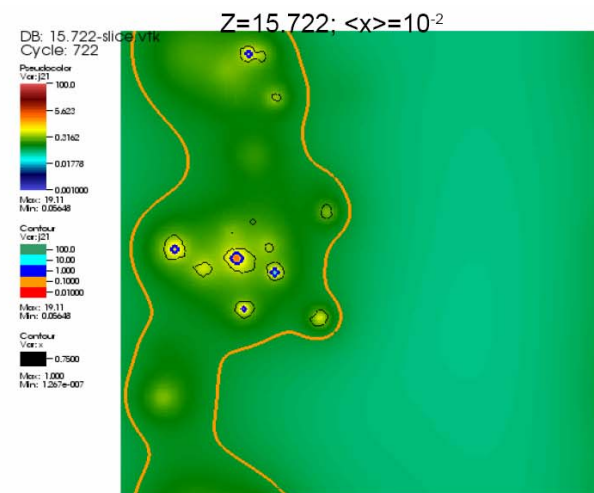
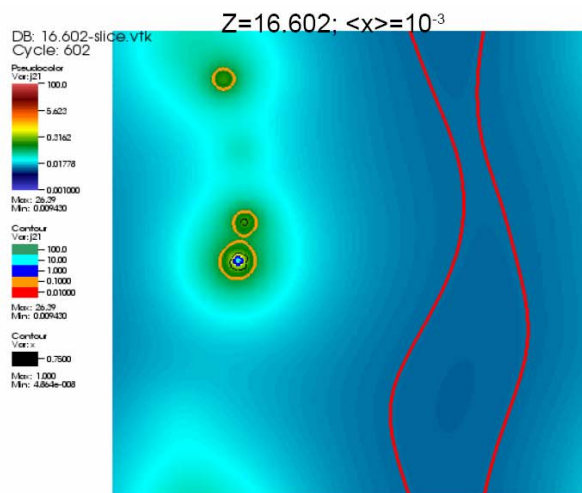
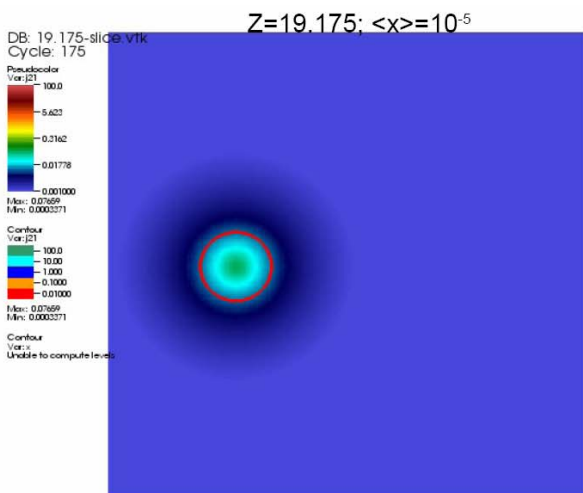
# H<sub>2</sub> Dissociating Background during EOR



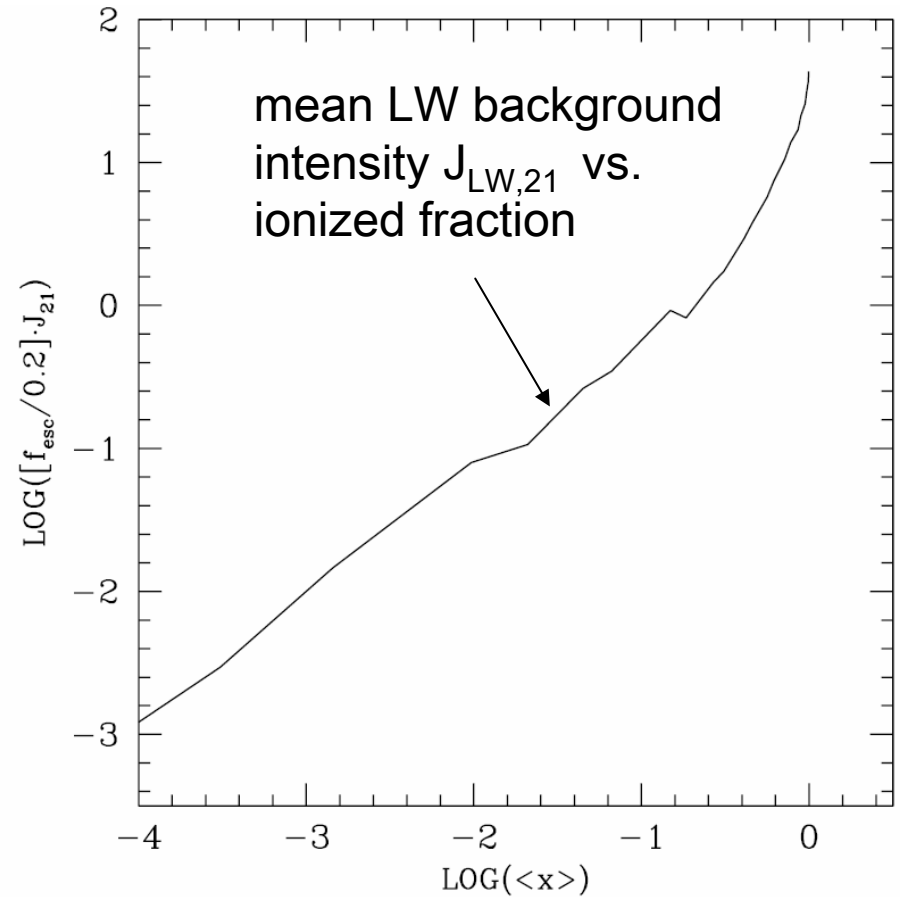
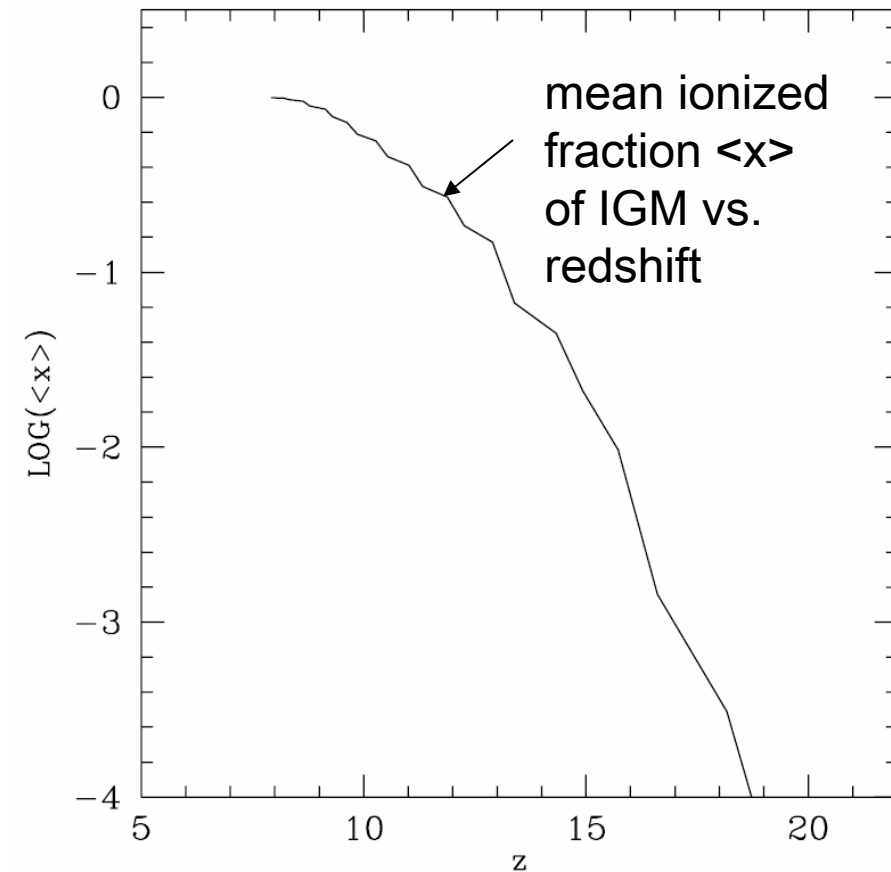


# H<sub>2</sub> Dissociating Background during EOR



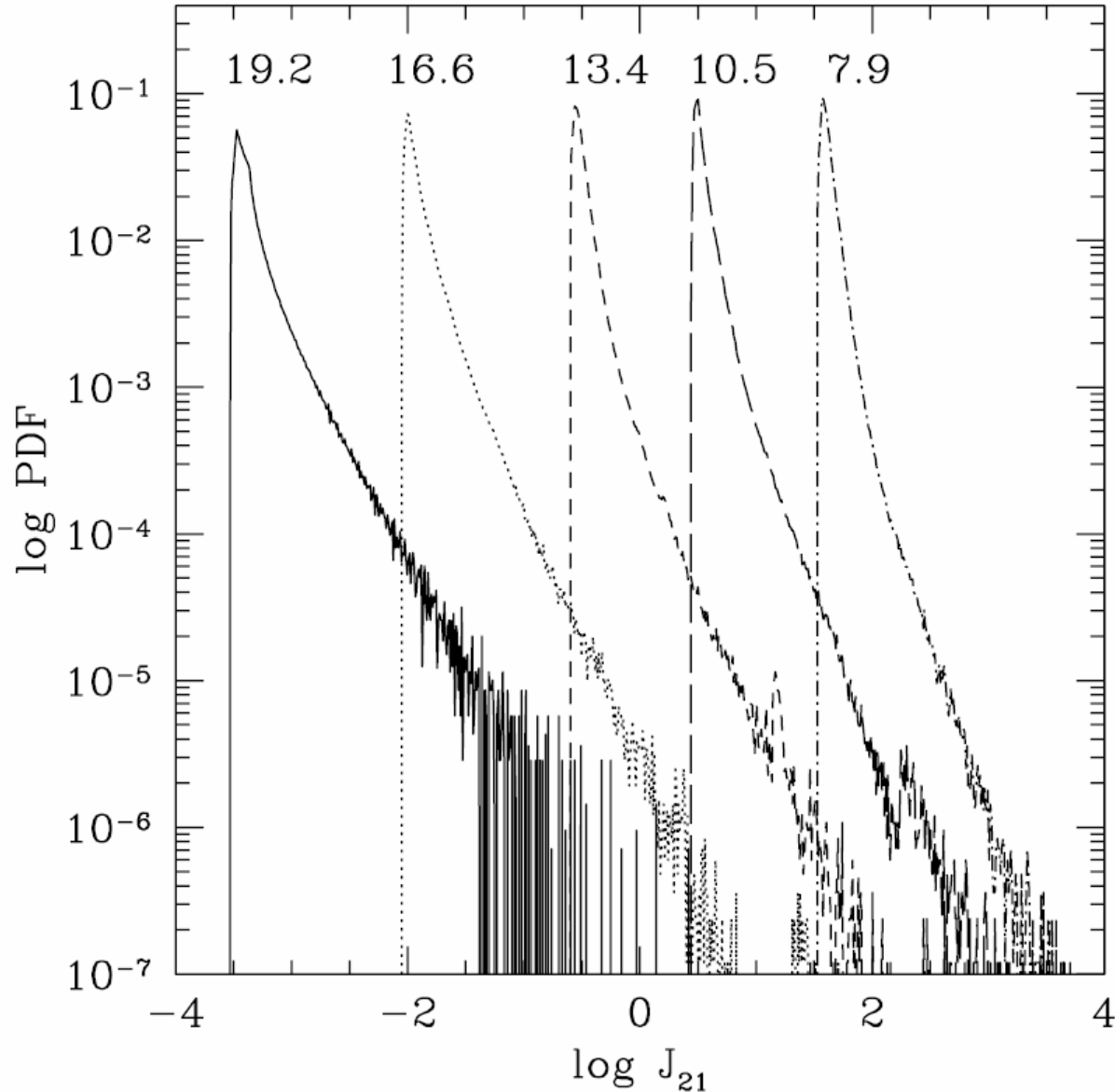


# The Mean $H_2$ Dissociating UV Background During EOR



$$J_{\text{LW},21} = J / (10^{-21} \text{ erg s}^{-1} \text{ cm}^{-2} \text{ Hz}^{-1} \text{ ster}^{-1})$$

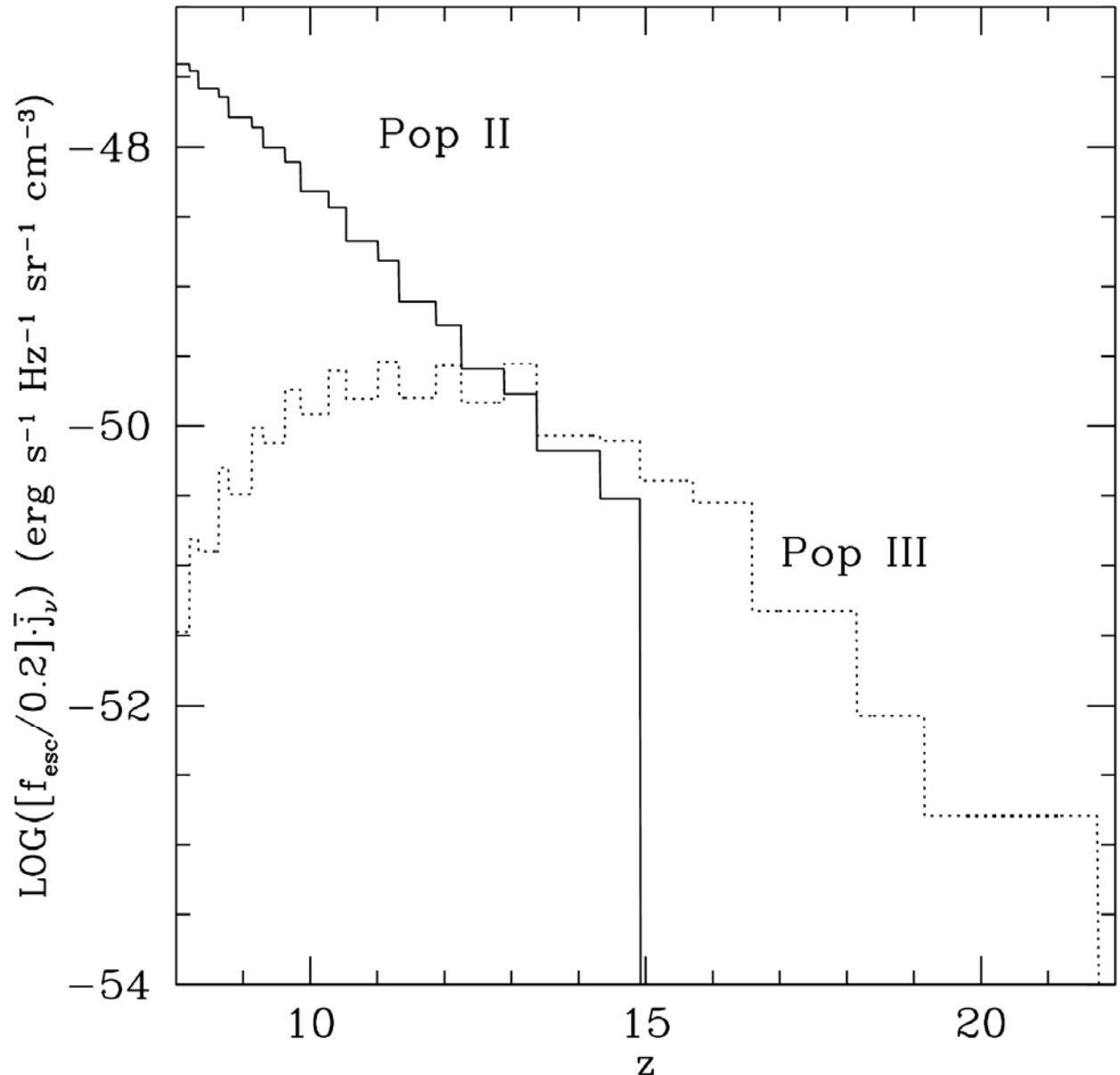
# Distribution of Intensity Fluctuations for the LW Background During Reionization



(35/h Mpc box)

# What are the dominant sources of the LW background during the EOR?

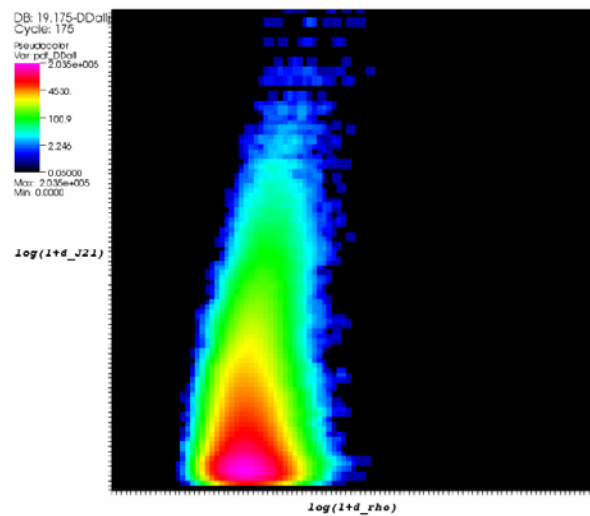
- Self-regulation of reionization
  - ➔ early LW background is dominated by low-mass sources that are suppressed if they form inside H II regions,
  - BUT the rise of the small-mass sources saturates long before end of EOR
  - ➔ the high-mass sources eventually dominate the LW background



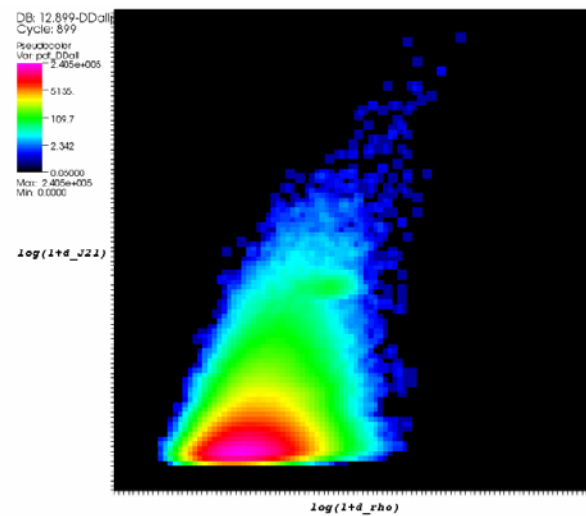


LW background intensity fluctuations in space are correlated  
with matter density fluctuations

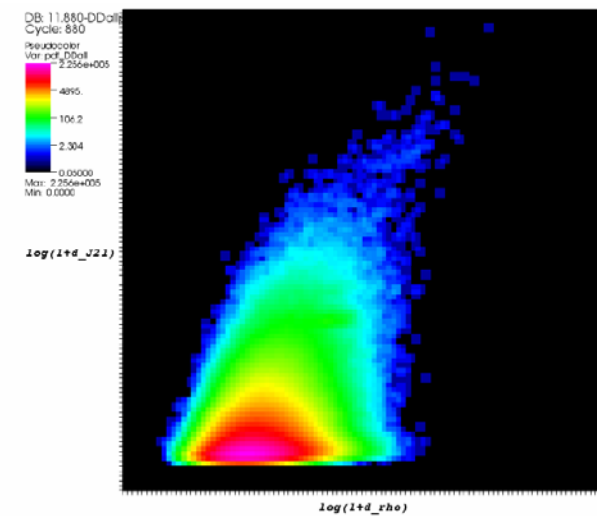
$z = 19$



$z = 13$



$z = 12$



# LW Background Conclusions

- Picket-fence modulation of LW background photons
  - makes computation of inhomogeneous LW background tractable
- LW rises above the threshold for suppressing star formation in minihalos long before end of the EOR → supports the idea that MHs, on average, not significant reionization source, but
- LW intensity fluctuates significantly in space → may be “safe spots” early on, to form Pop III stars in minihalos where LW background minima occur, far from the large-scale H II regions made by clustered dwarf galaxies.
- Fluctuation in LW background comes from source clustering, at a scale of  $\sim 10$  comoving Mpc
- May contribute to NIR background fluctuations
- Understanding radiative feedback on Pop III star formation in minihalos may be important to complete the theory of reionization

# Feedback From First Radiation Sources: H<sup>-</sup> Photodissociation

Chuzhoy, Kuhlen, & Shapiro (2007), *ApJL*, 665, L85 (astro-ph/0704.0426)

- Rate for H<sub>2</sub> formation in primordial gas,  
$$\text{H}^- + \text{H} \rightarrow \text{H}_2 + \text{e}^-$$
is proportional to abundance of H<sup>-</sup> ==> destroying H<sup>-</sup> will reduce H<sub>2</sub> formation rate;
- Photodissociation can destroy H<sup>-</sup>,



- During reionization, as sources release ionizing radiation, they also cause a background of H<sup>-</sup> dissociating radiation to build up, which reduces the H<sub>2</sub> formation rate by factor F<sub>s</sub>,

$$F_s \sim 1 + 1000 k_s x / (f_{\text{esc}} \delta),$$

where x = cosmic mean ionized fraction, δ = local baryon gas overdensity, and k<sub>s</sub> = a constant of order unity which depends on type of radiation source (e.g. recombination radiation, direct stellar or quasar emission, or secondary emission by nonthermal electrons following X-ray background ionization) ;

- Hence, by the time x ≥ 0.1, H<sup>-</sup> photodissociation may significantly reduce H<sub>2</sub> abundance and cooling, and the rate of primordial star formation.

# More Feedback From First Radiation Sources: $\text{H}^-$ Photodissociation

Chuzhoy, Kuhlen, & Shapiro (2007), *ApJL*, 665, L85 (astro-ph/0704.0426)

- Rate for  $\text{H}_2$  formation in primordial gas,  
$$\text{H}^- + \text{H} \rightarrow \text{H}_2 + \text{e}^-$$
is proportional to abundance of  $\text{H}^-$   $\implies$  destroying  $\text{H}^-$  will reduce  $\text{H}_2$  formation rate;
- Photodissociation can destroy  $\text{H}^-$ ,



- **During reionization, as sources release ionizing radiation, they also cause a background of  $\text{H}^-$  dissociating radiation to build up, which reduces the  $\text{H}_2$  formation rate by factor  $F_s$ ,**

$$F_s \sim 1 + 1000 k_s x / (f_{\text{esc}} \delta),$$

**where  $x$  = cosmic mean ionized fraction,  $\delta$  = local baryon gas overdensity, and  $k_s$  = a constant of order unity which depends on type of radiation source (e.g. recombination radiation, direct stellar or quasar emission, or secondary emission by nonthermal electrons following X-ray background ionization) ;**

- **Hence, by the time  $x \gtrsim 0.1$ ,  $\text{H}^-$  photodissociation may significantly reduce  $\text{H}_2$  abundance and cooling, and the rate of primordial star formation.**

# Cosmological Radiative Transfer Codes Comparison Project I. : The Static Density Field Tests

Iliev, Ciardi, ..., Shapiro, ... (2006) MNRAS, 371, 1057

