

Dark Matter on small astrophysical scales

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Have we found the first galaxies?
Do we understand their histories well
enough to probe their DM?
What are their DM properties?

**Dynamics with Mark Wilkinson, Rosie Wyse, Jan Kleyna,
Andreas Koch, Wyn Evans, Walter Dehnen, Eva Grebel,
Chemistry with Andreas Koch and John Norris
Discovery work with Vasily Belokurov, Dan Zucker, Sergey
Koposov, et al**

Simple extrapolation of the power-spectrum in CDM produces many astrophysics challenges

- Anti-hierarchical problem
- Top-down, old red & dead..
- Satellite problem- too many small galaxies
- Void problem – model voids are not empty
- Angular momentum problem – real galaxies are too big
- Phase-space density problem – galaxy centres are lower density than models
- Large disks problem – late mergers should not allow large cold disks, which are common
- etc, etc, etc, etc, etc, etc, etc.....
- → these allow a probe of both astrophysics and particle properties on kpc scales

Particle-astrophysics joint challenges

do very many puzzles imply very many particle types??

- MSSM has 120+ free parameters... and is just one of very many possible theories:
- neutrino masses and mixing
- baryogenesis
 - matter anti-matter asymmetry
- dark matter
- dark energy, gravity, CPT, Higgs/mass,...

Scale invariant power spectrum implies a UV divergence

→ a physical cut-off at some scale:

Astrophysics → `satellite problem`

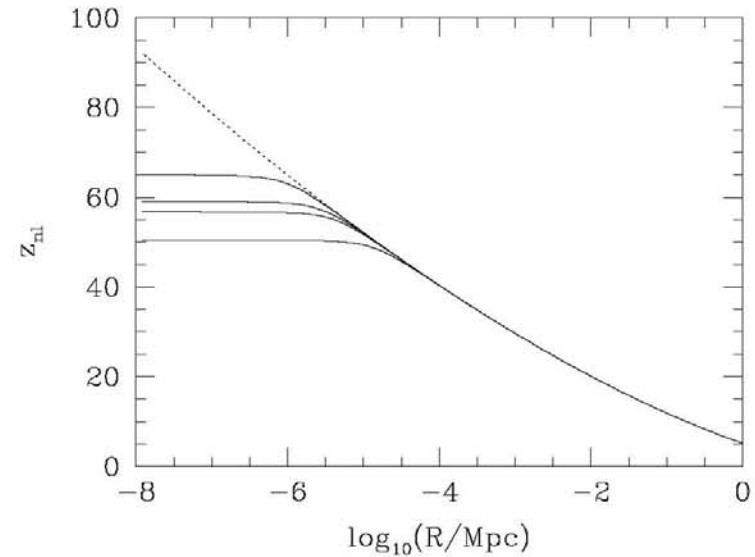
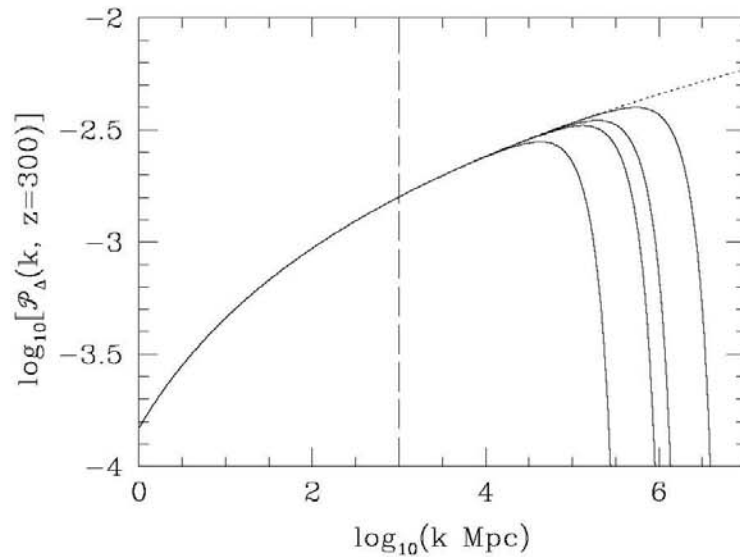
Is that scale astrophysically relevant?

Can it be deconvolved from feedback?

Anticipated DM effects on scales of pc up \rightarrow first systems

Linear power spectrum at $z \sim 300$ and z_{nl}

influence of WIMP microphysics



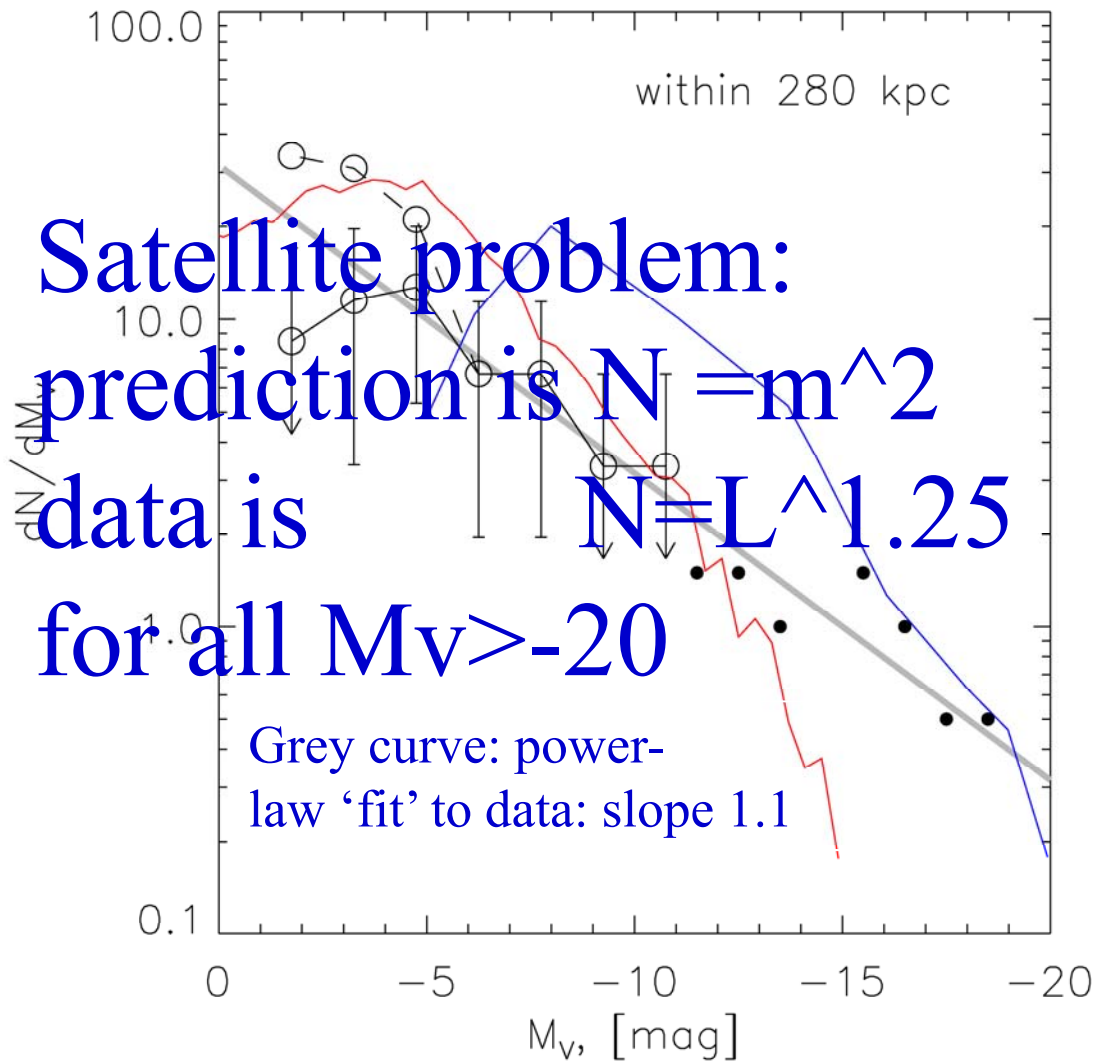
Green, Hofmann & Schwarz 2004; 2005

The smallest, oldest galaxies: dwarf Spheroidals

- Low luminosity, low surface-brightness satellite galaxies, ‘classical’ $L \sim 10^6 L_{\odot}$, $\mu_V \gg 24$ mag/sq”
- Apparently dark-matter dominated
 - $\sigma \sim 10$ km/s, $10 < M/L < 100$
- Very metal-poor, all contain very old stars; but intermediate-age stars dominate
- They survive from a time before general pre-enrichment, and avoided extreme histories
- Their DM halos remain primordial
- Are they the first halos, as CDM requires?

Derived satellite luminosity function

Koposov et al 2008 ApJ 686 279



Open symbols:
Volume-corrected
satellite LF from DR5

Filled symbols:
'all Local Group dSph'

Coloured curves:
Semi-analytic fit
(Benson et al 02, red
Somerville 02, blue)
We ignore BIG surface-
brightness discrepancies
REALLY NEED MASS

All satellites have some old stars, but they are mostly young
they have survived a Hubble time \rightarrow no violent histories

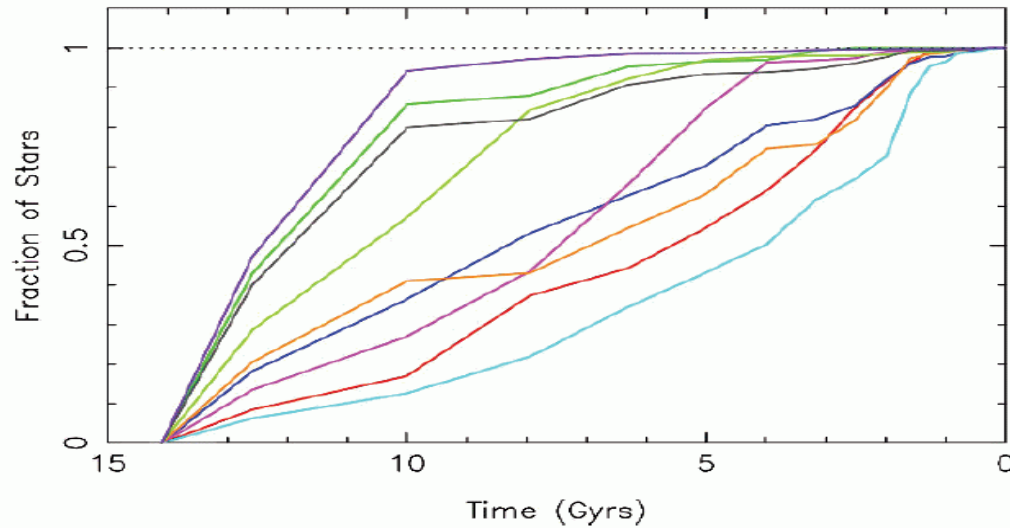


Fig. 1. Comparison of cumulative SFHs for several Local Group dSphs.

24

E.D. Skillman

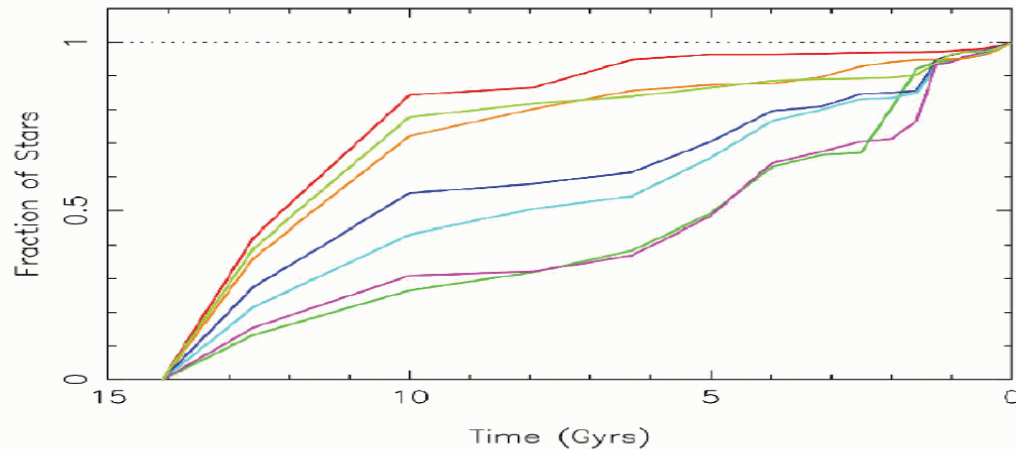
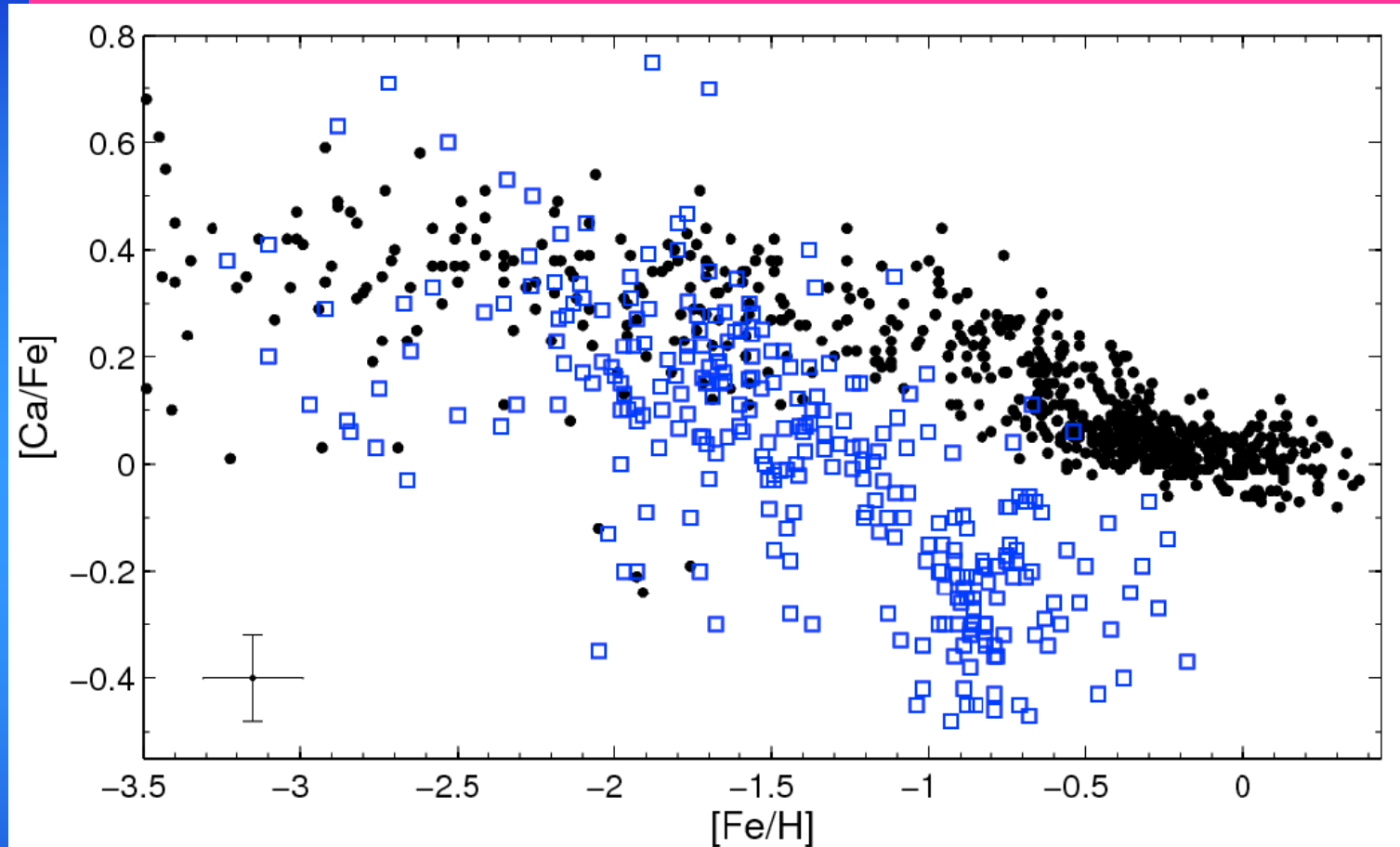


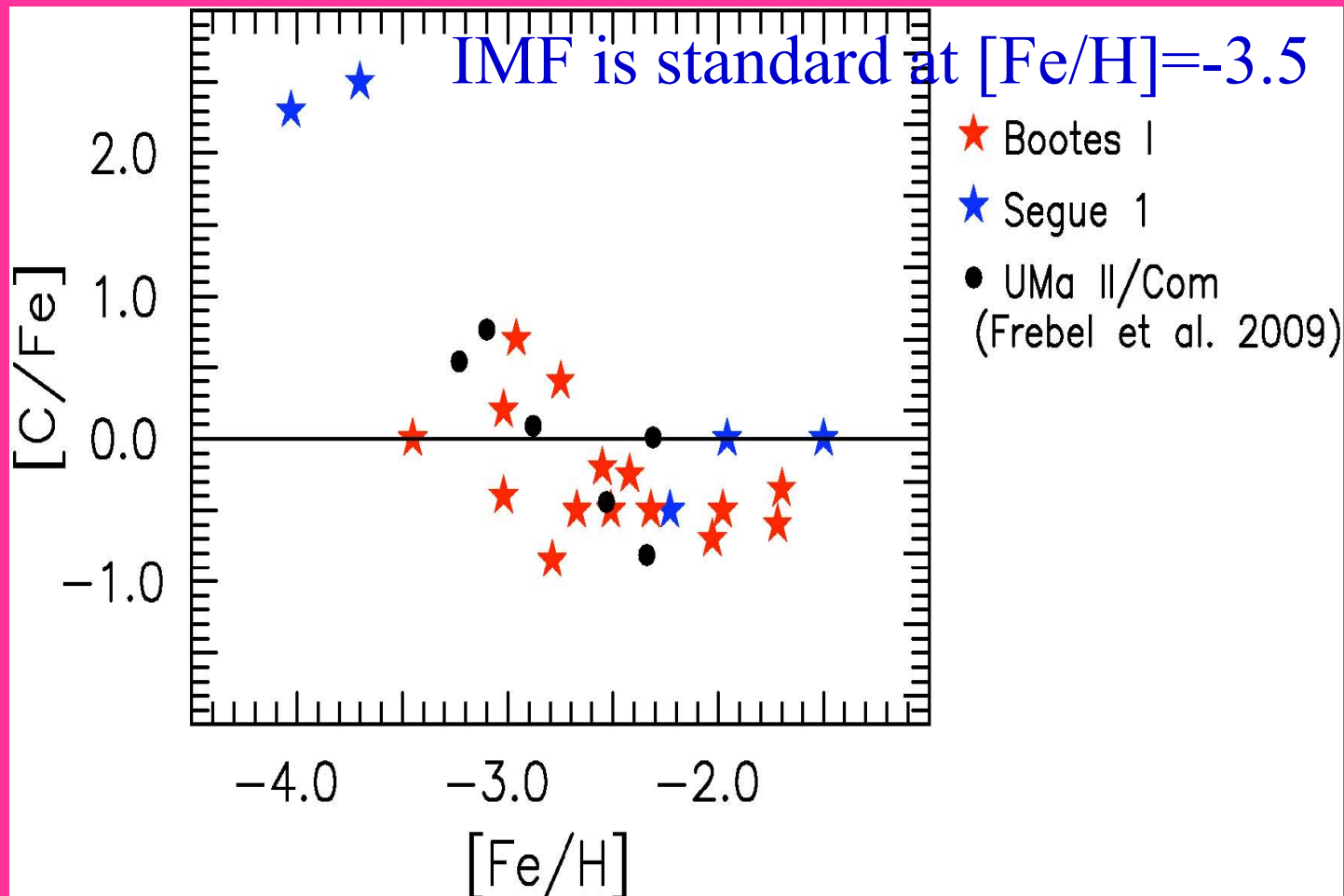
Fig. 2. Comparison of cumulative SFHs for several Local Group dIrrs.

dSphs did not form the Galaxy



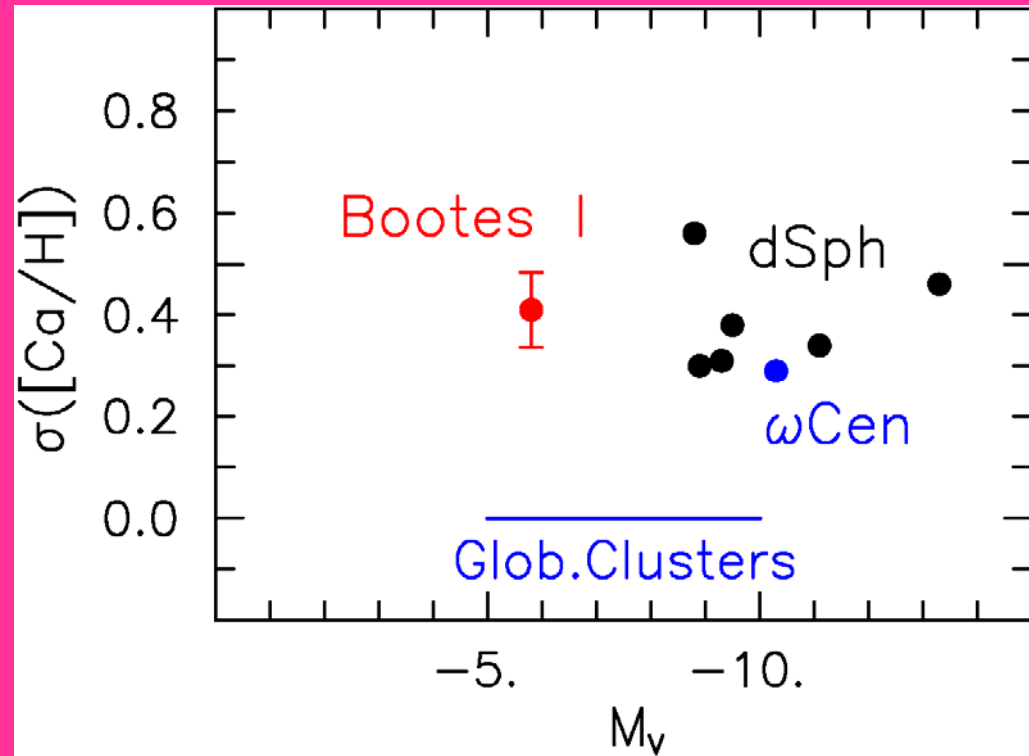
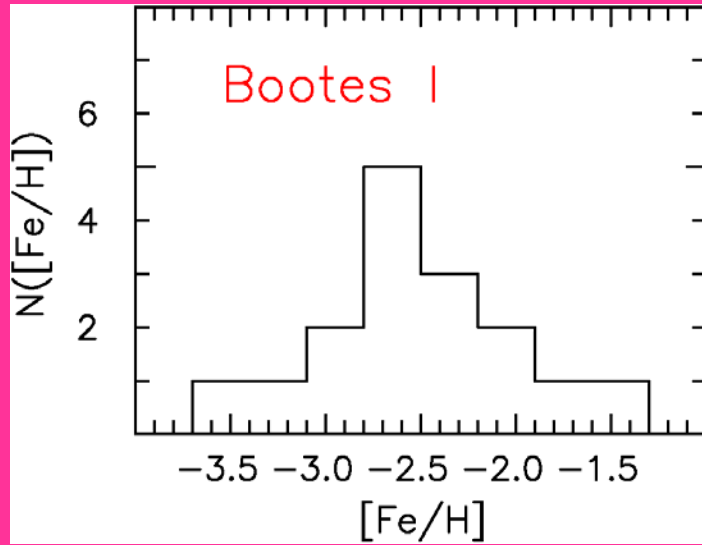
strong $[\alpha/Fe]$ discrepancy between dSph and halo stars, but note the overlap at the metal poor halo \rightarrow generic stellar IMF, not mergers (Koch 2009, Rev. Mod. Ast., 21, 9)

The faintest dSph contain the oldest most metal-poor stars
Are these the first stars? Why are they in the faintest dSph?
The first bound galaxies? Does PopIII underproduce Fe?



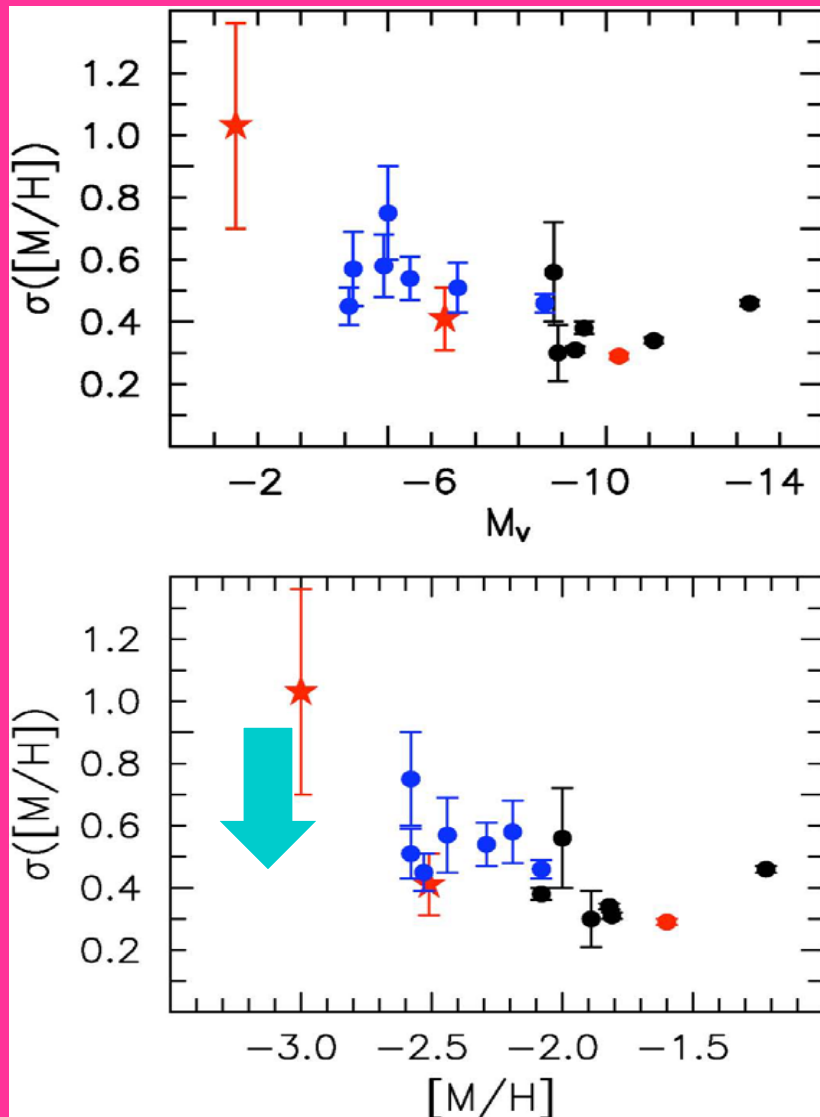
Abundance mean and dispersion is a mass proxy: even at extreme low luminosity, self-enrichment happened.

What is doing the pre-enrichment in more massive dSph?



Norris, GG, Wyse et al
2008 – apj 689 L113
cf Kirby et al ApJ 685 L43
NB: self-enrichment on these
scales requires low SFR, and
weak feedback

Chemical enrichment dispersion is a mass proxy for smallest systems



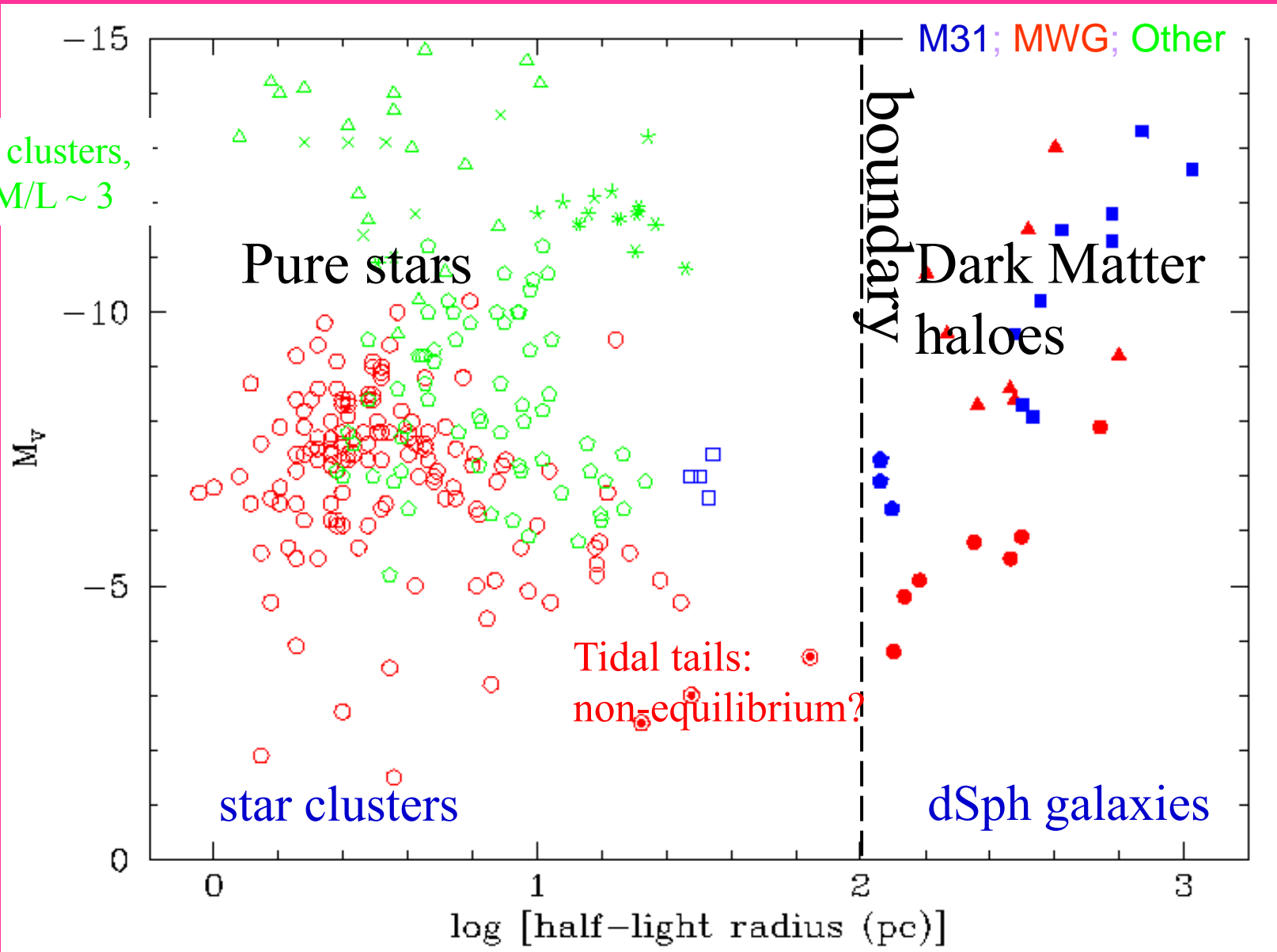
The lowest luminosity dSph are the most primordial, -more so than the most extreme Galactic stars and more massive dSph \rightarrow preenrichment happened: effect on Ly α ??.

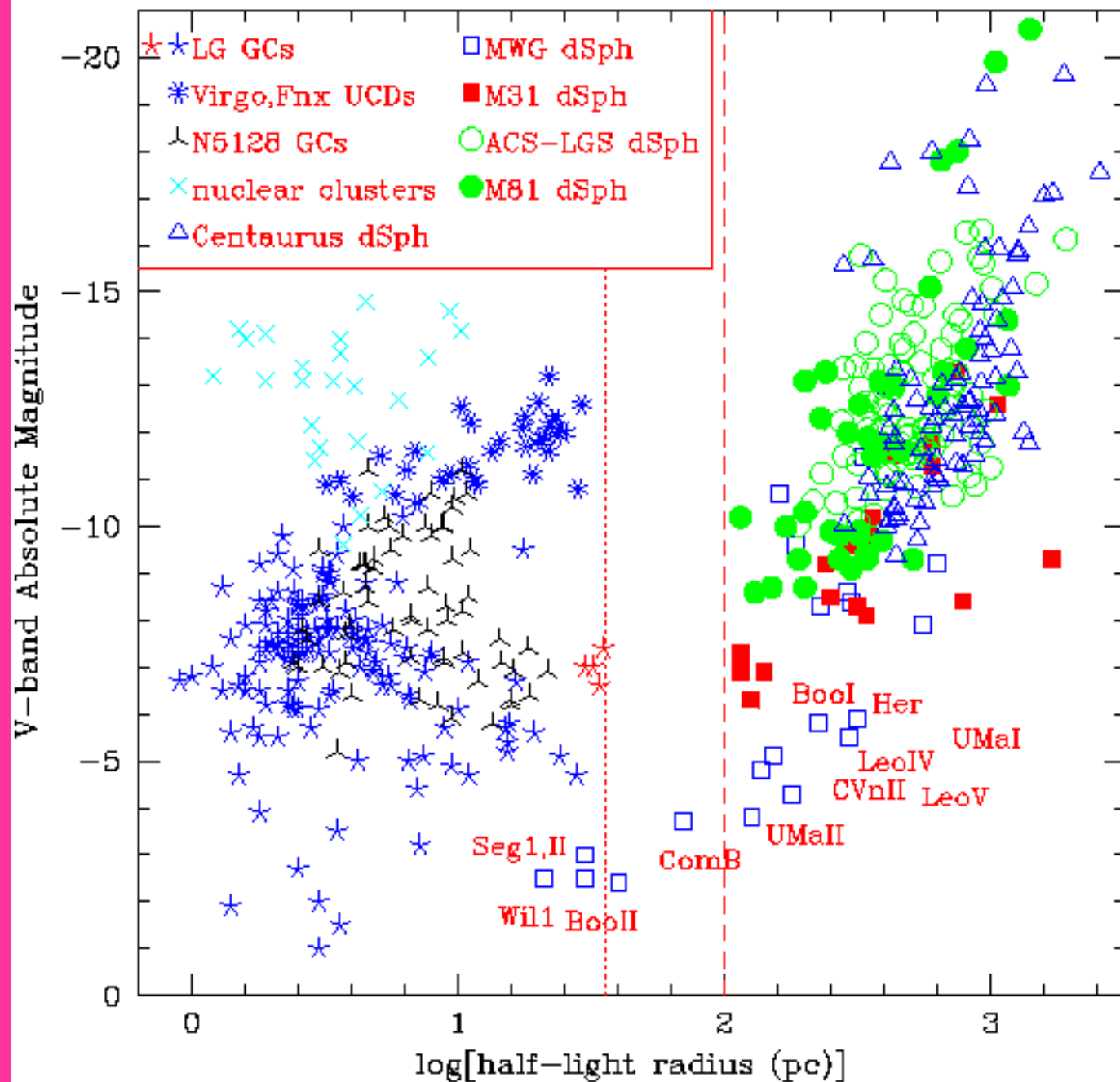
Now look at dark matter content

Norris, Wyse, GG etal ApJL 2008

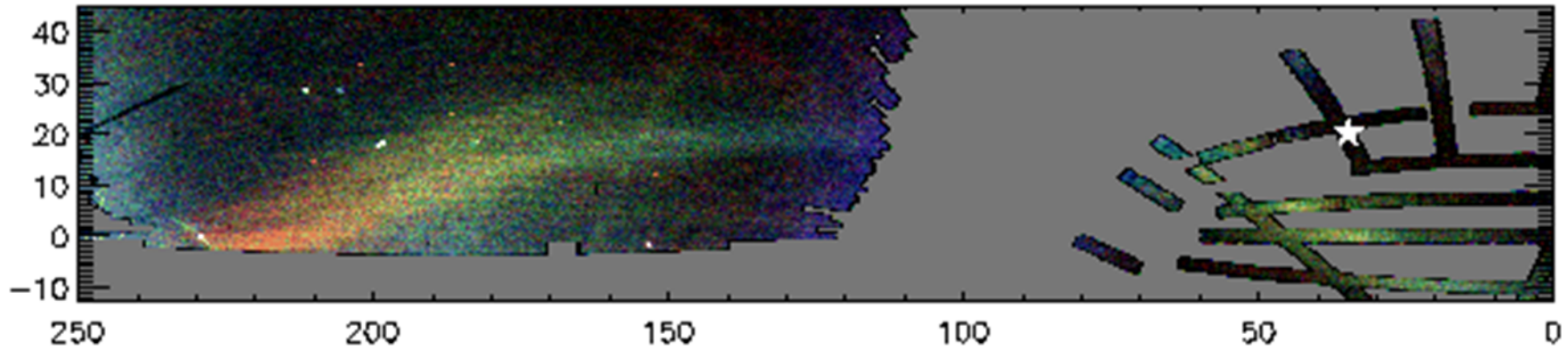
Faint galaxies are not star clusters...

Nuclear clusters,
UCDs, $M/L \sim 3$



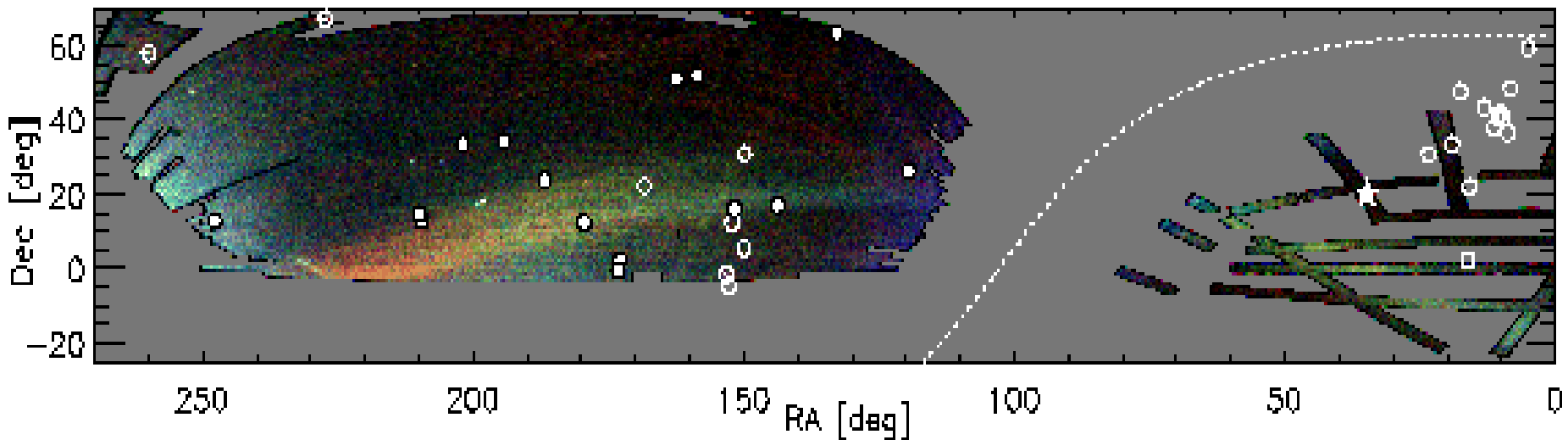


BEWARE: many dSph are in complex places!!



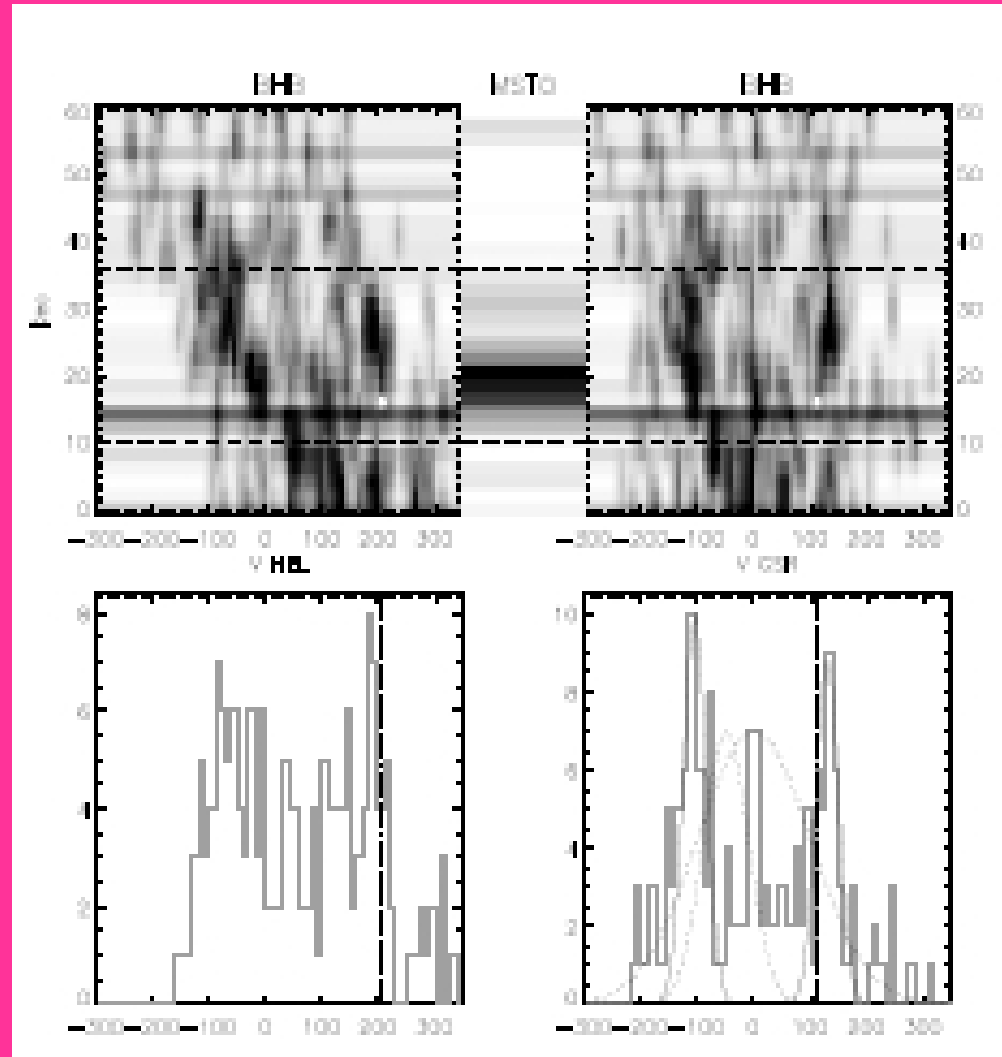
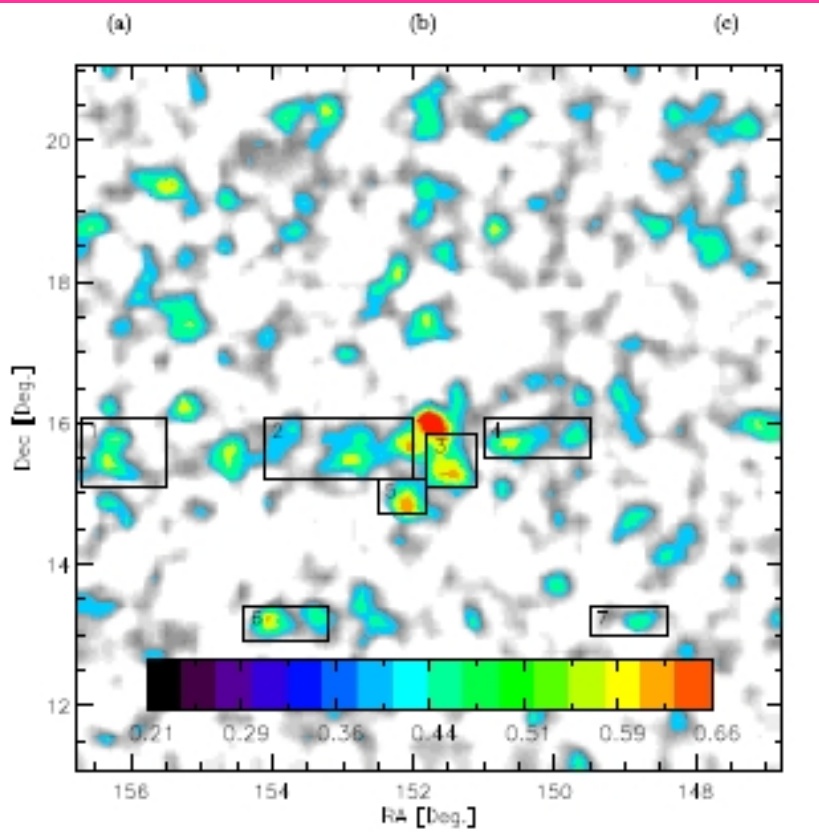
Segue-2 discovery paper : Belokurov etal arXiv: 0903.0818

Classical dSph – open circles; ultra-faint – closed
note the several along the Sgr tail



Segue-1 is embedded in Sgr tails, in a complex velocity field

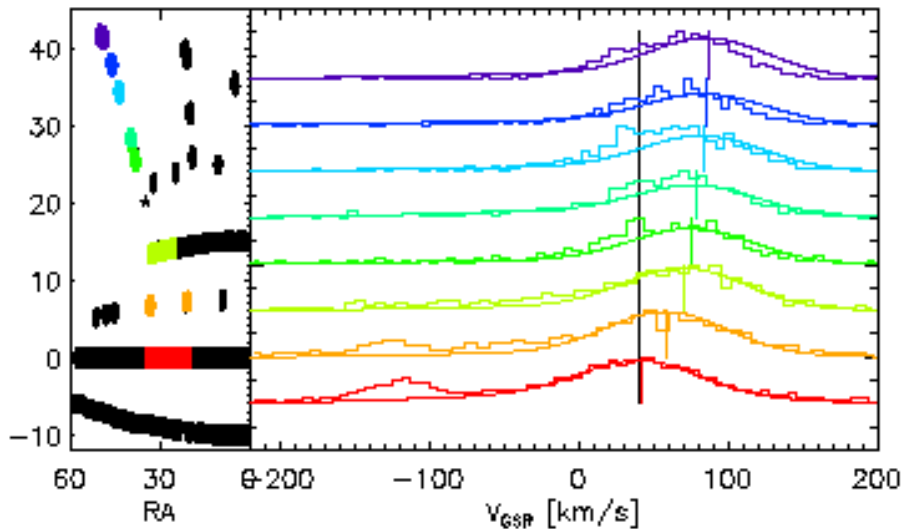
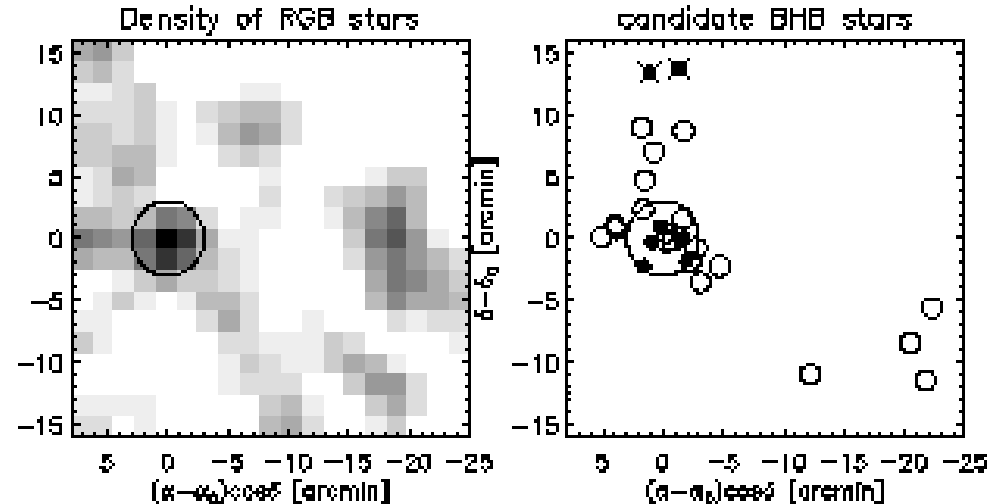
note confusion with Leo I...



Niederste, Evans, Belokurov, Gilmore, Wyse, Norris - 2009

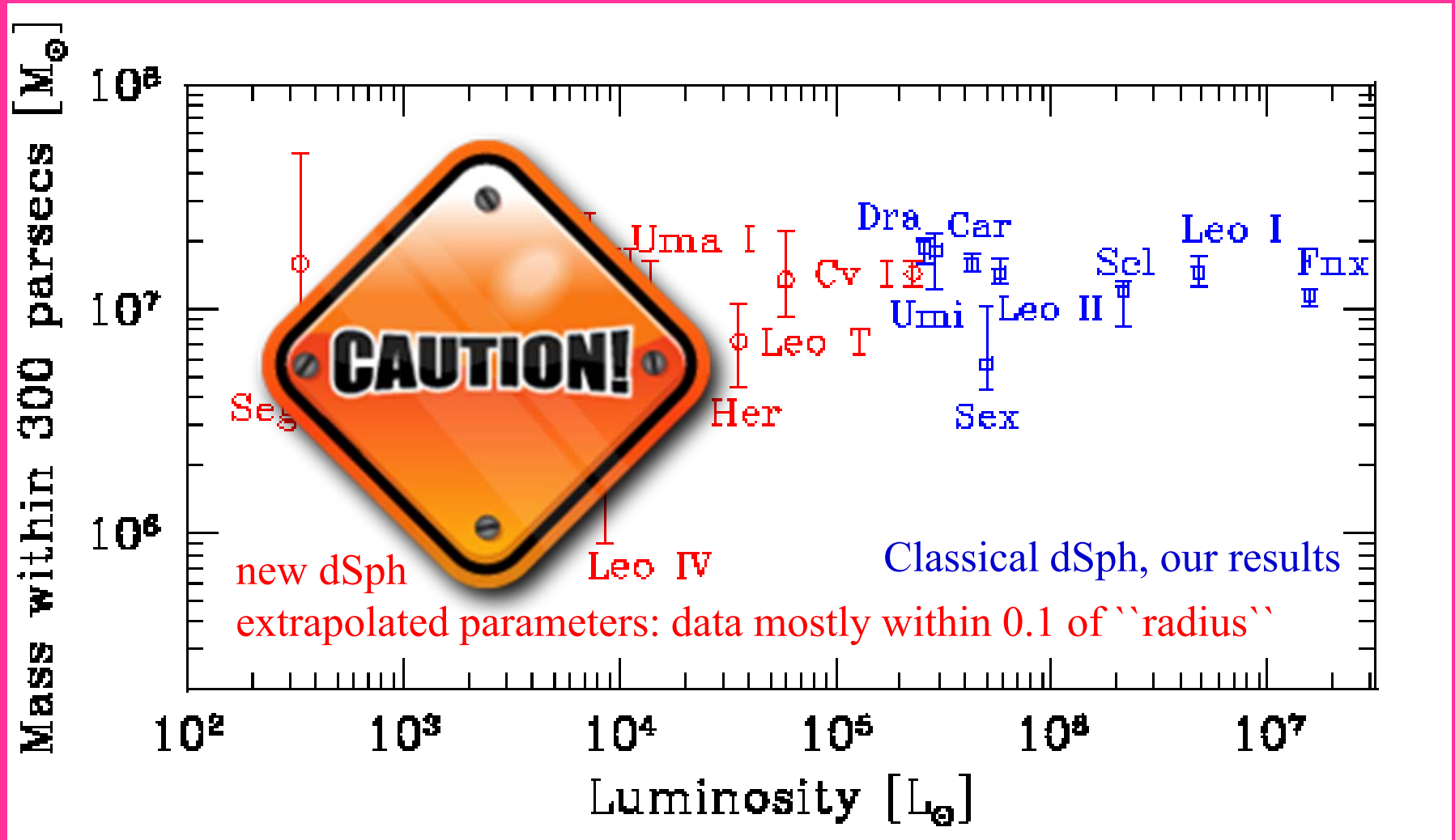
Some more complexity

Leo V – complex
density profile
Outermost BHBs are
velocity members



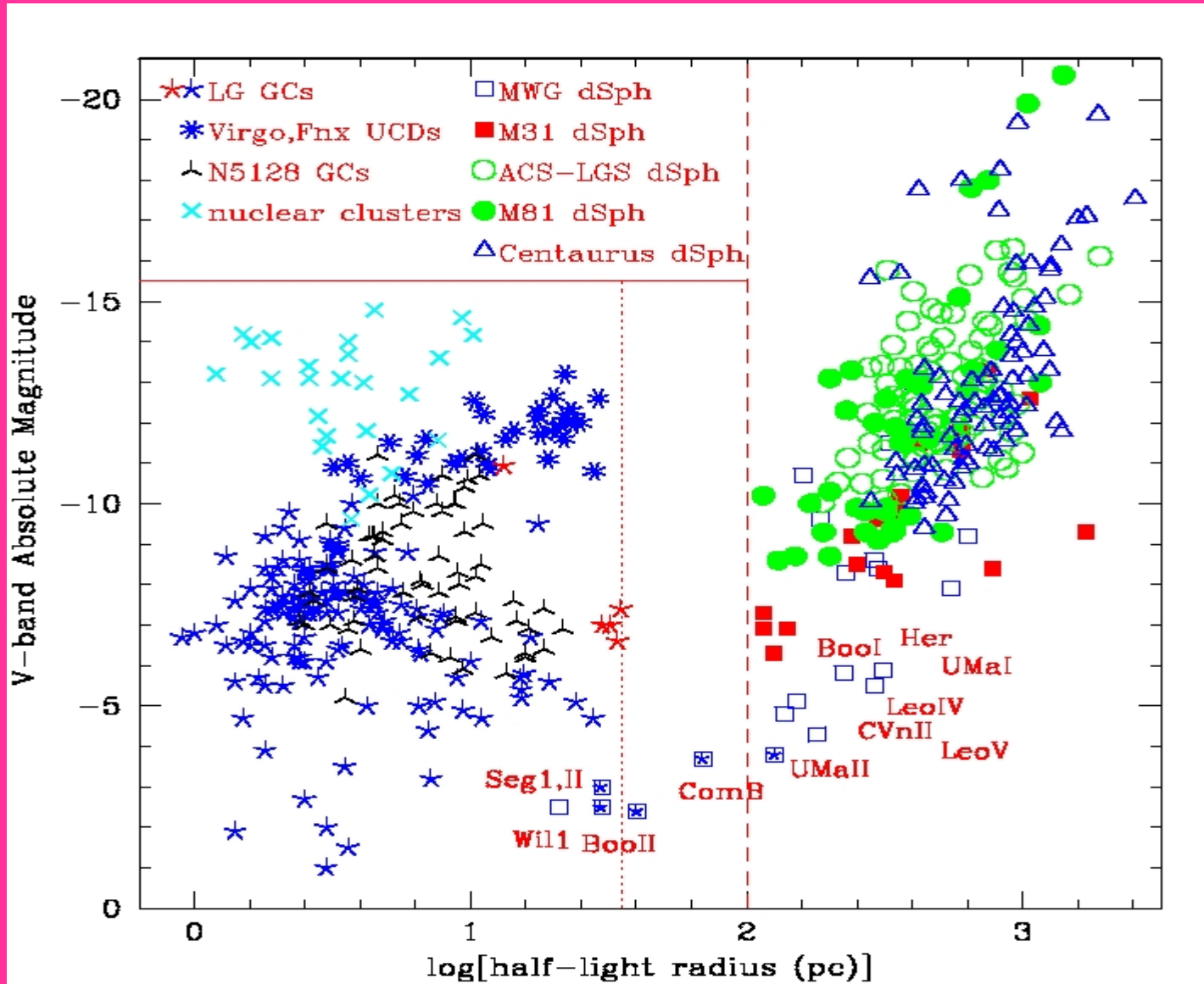
Seg-II – another
halo stream connection

Claims of correlations are overdone:
the ultra-faints have limited data, many are in complex environs



Strigari et al Nature 454 1096 2008

Some systematic results seem robust – dSph are big at least when safe from galactic tides



Conclusion one: structures

There is a well-established size bi-modality:

- all systems with size $< 30\text{pc}$ are purely stellar
- all systems with size greater than $\sim 100\text{pc}$ have a dark-matter halo
- There are no known (virial equilibrium) galaxies with half-light radius $r < 100\text{pc}$
- The smallest systems are nearby, and messy
- Distant dSph are the oldest things, and have led gentle lives: they are the place to measure DM profiles

What can we say about the distribution of dark matter on small scales from dSph internal kinematics?

- 1) classical Jeans' models
 - 2) sophisticated Jeans' models
 - 3) full distribution function MCMC models
-
- Discount central velocity dispersion models

From kinematics to dynamics: Jeans equation, and full distribution function modelling

- Relates spatial distribution of stars and their velocity dispersion tensor to underlying mass profile

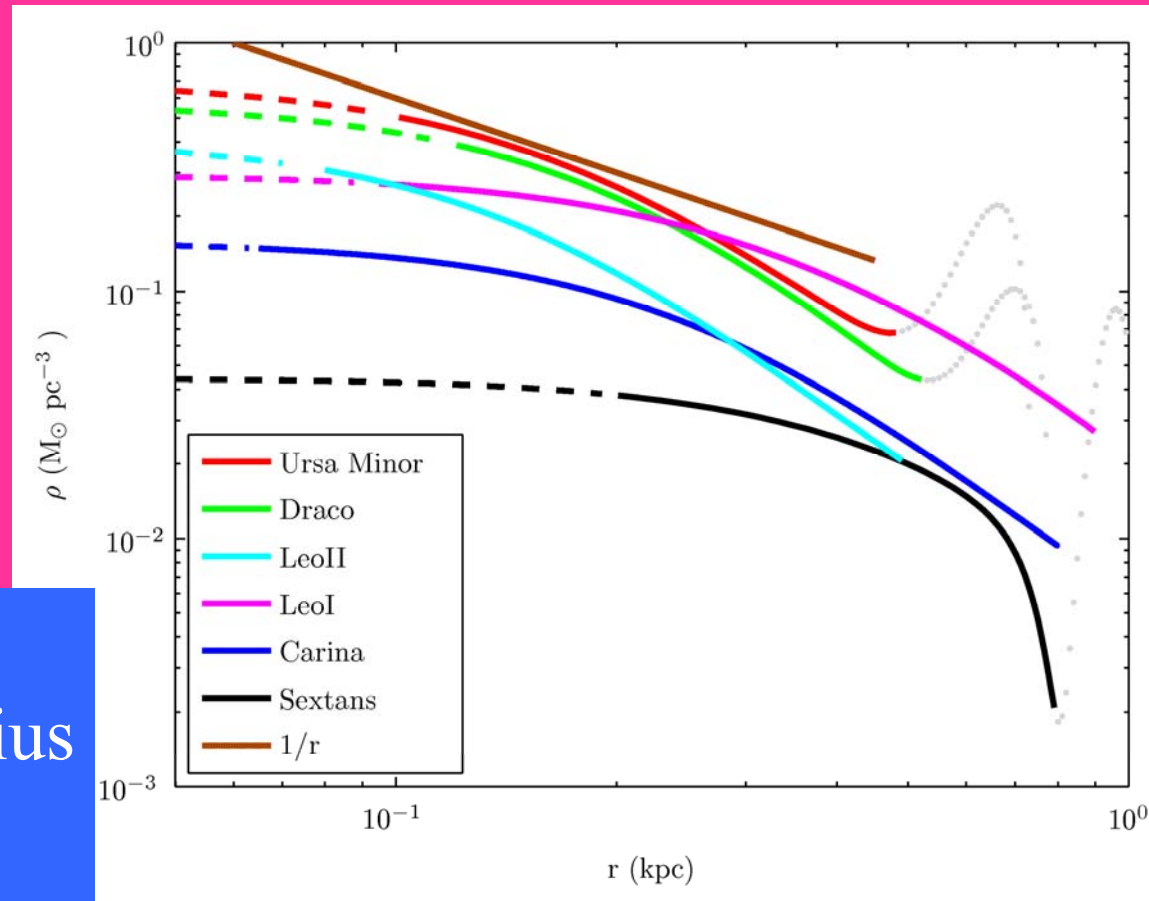
$$M(r) = -\frac{r^2}{G} \left(\frac{1}{\nu} \frac{d\nu\sigma_r^2}{dr} + 2\frac{\beta\sigma_r^2}{r} \right)$$

- ◆ Either (i) determine mass profile from projected dispersion profile, with assumed isotropy, and smooth functional fit to the light profile
- ◆ Or (ii) assume a parameterised mass model $M(r)$ and velocity dispersion anisotropy $\beta(r)$ and fit dispersion profile to find best forms of these (for fixed light profile)
- We use distribution function modelling, as opposed to velocity moments: need large data sets. DF and Jeans' models agree
- Show Jeans' results here first.
- [King models are not appropriate for dSph]

Derived mass density profiles:

Jeans' equation with assumed isotropic velocity dispersion: all consistent with cores.

CDM predicts slope of -1.3 at 1% of virial radius and asymptotes to -1 (Diemand et al. 04)

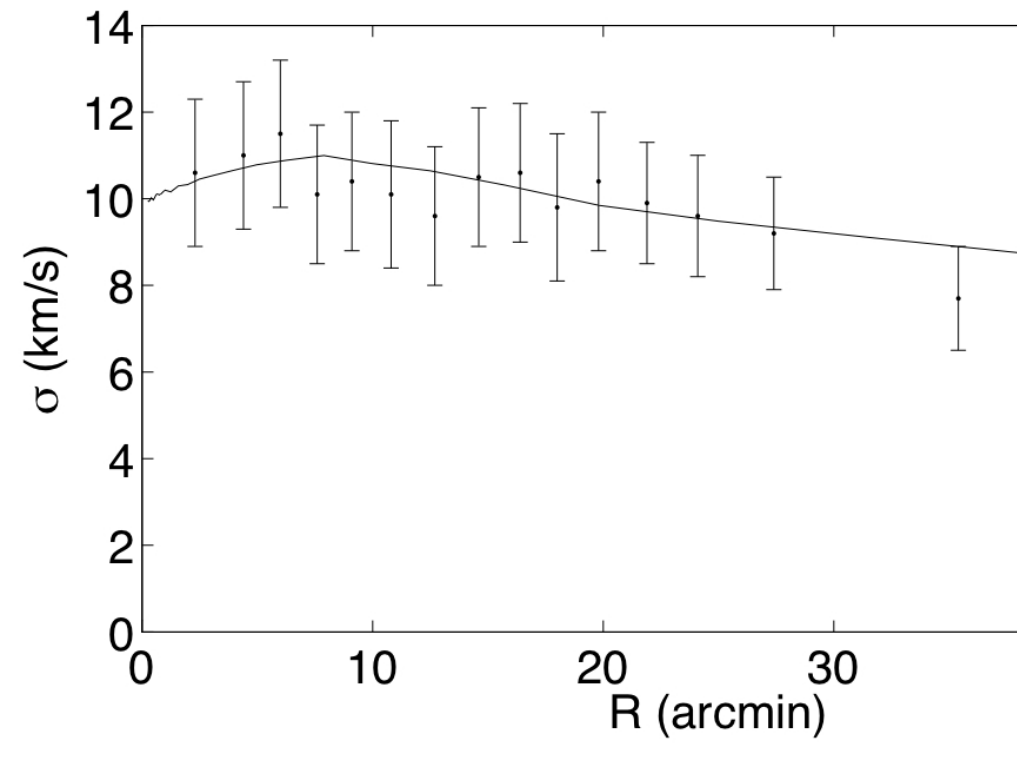


NB these Jeans' models are to provide the most objective sample comparison – DF fitted models next.

What are we really measuring with non-DF, analyses?

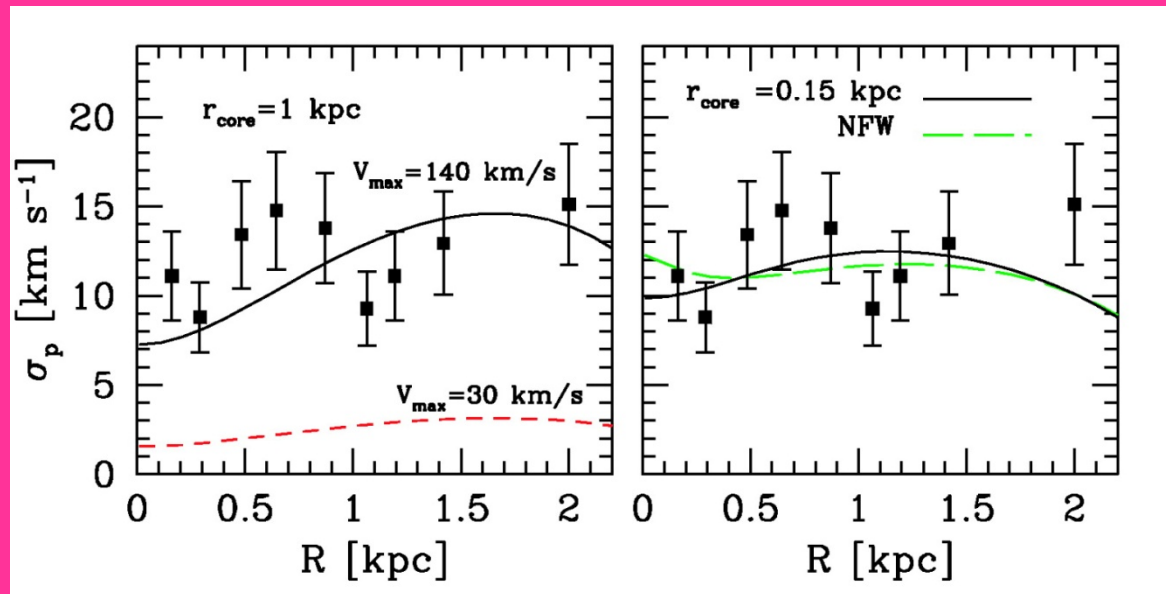
$$M(r) = \frac{r^2}{G} \left(\frac{1}{\nu} \frac{d\nu\sigma_r^2}{dr} + 2 \frac{\beta\sigma_r^2}{r} \right)$$

- Dispersion profile close to flat, so $\sigma \sim \text{cst}$, and range of σ is small (data < 2)
- derivative term is (log) luminosity profile : light, NOT mass, and this is similar in scale for all the dSph (factor of few)
- So the derived `mass` in a standard analysis is a measure of the radial extent of the data, and only a weak function of anything else
- \rightarrow but one can do better

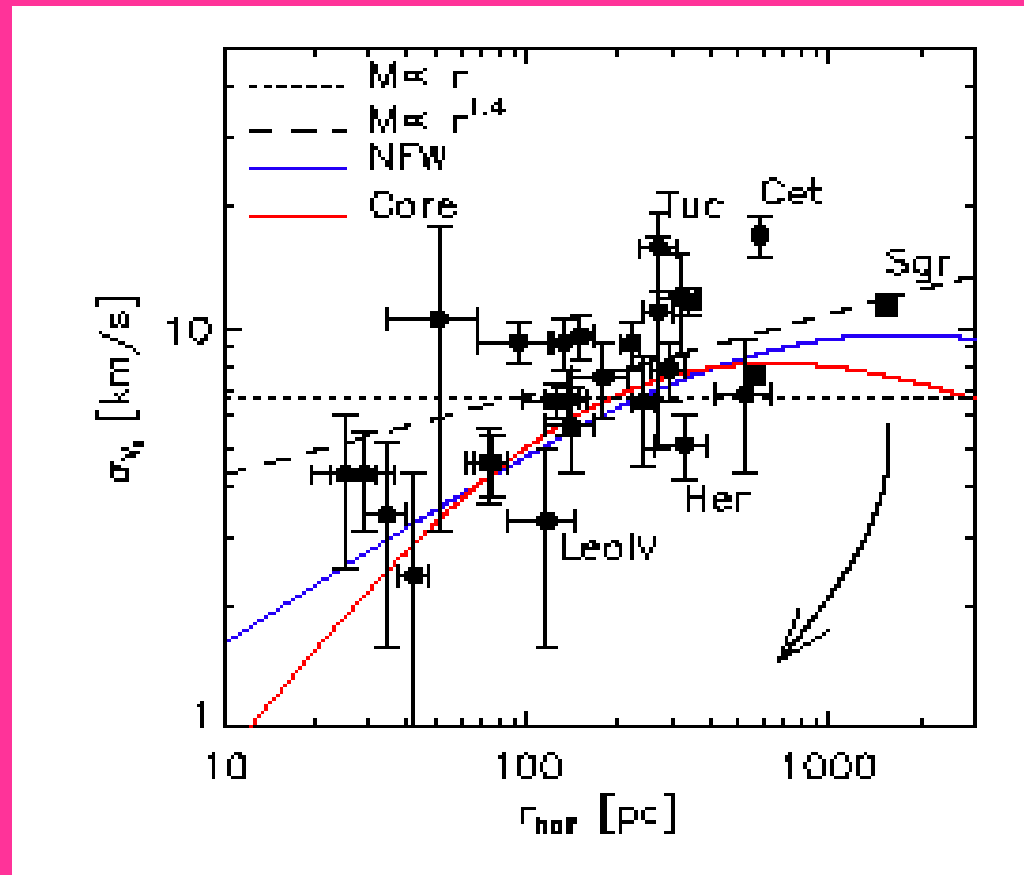


Note the data quality improvement:
 First declining dispersion profile
 → Robust $V_{\text{max}}=20\pm 4$ km/s

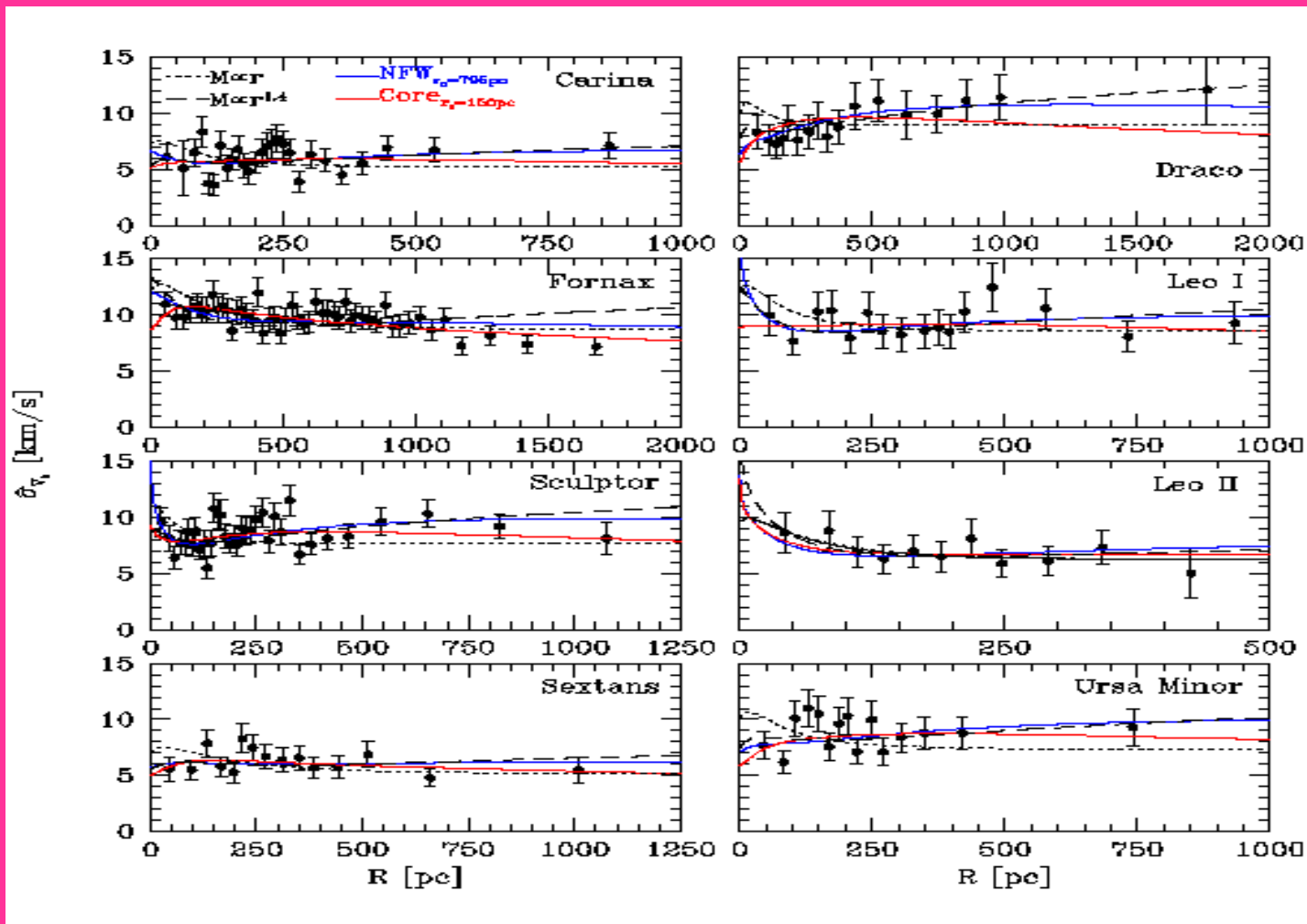
Top Walker et al 2009
 Lower Strigari et al 2006 fit to
 Walker et al 2006



One can use MCMC for optimal Jeans' analyses
[robust mass within the observed radius]
and there is new information: [Walker etal 0906.0341]
there is a velocity dispersion *vs* size relation!
albeit poor data for smallest and nearest systems, and real scatter
→ mass vs radius statistical relation



MCMC Jeans' models – Walker et al 0906.0341 –
 fit for anisotropy/stress: core-cusp degenerate
 But require $V_{\text{max}} < 20 \text{ km/s}$. These are low-mass.
 → the higher mass halos really are missing.



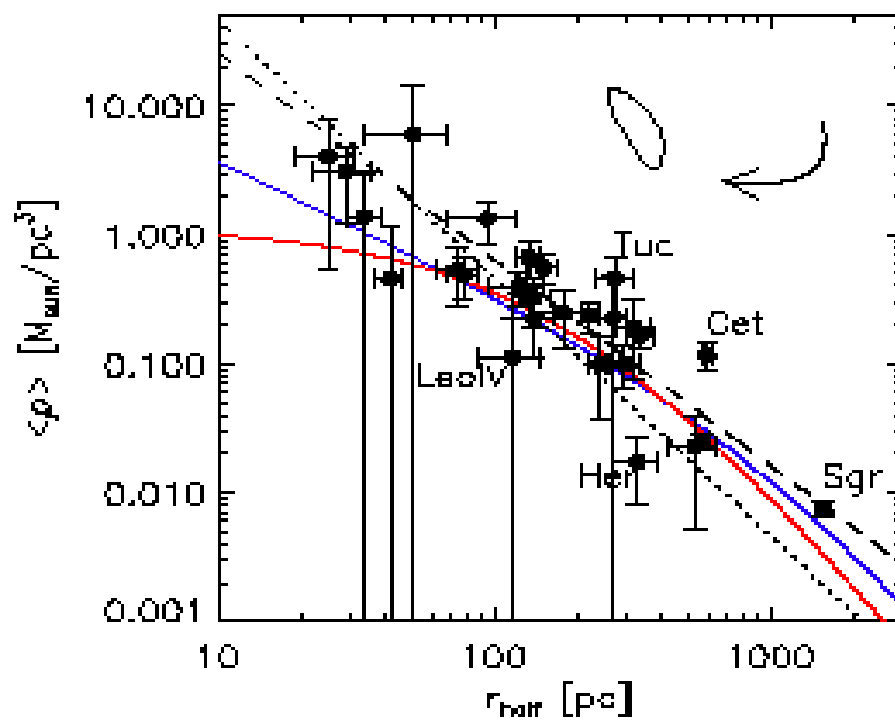
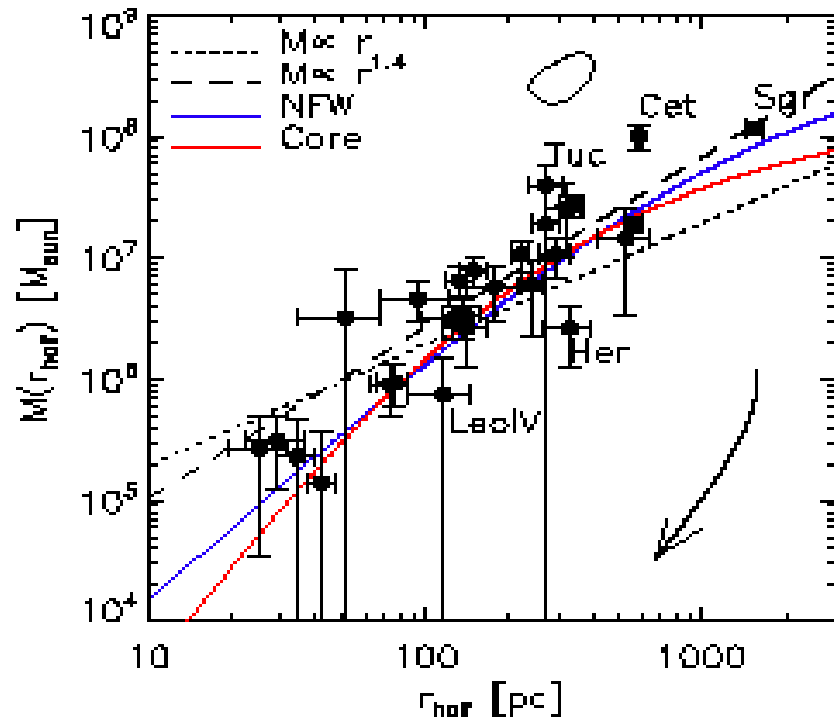
Scaling relations based on kinematic data:

➔ universal mass profile? NFW, $r_0=1\text{kpc}$, core $r=200\text{pc}$

Beware smallest galaxies – complex!

Beware largest – tidal damage!

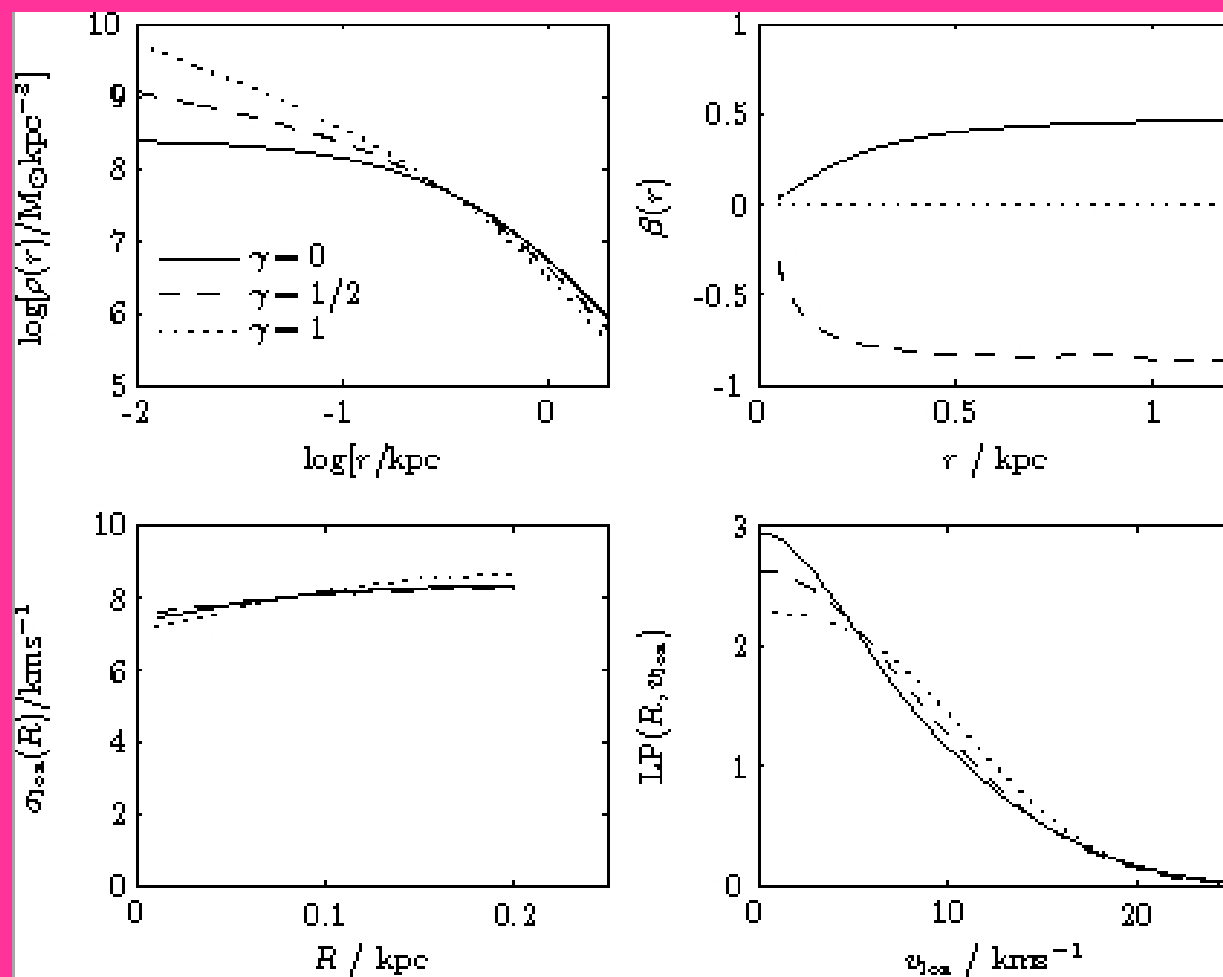
This is the best one can do without real modelling



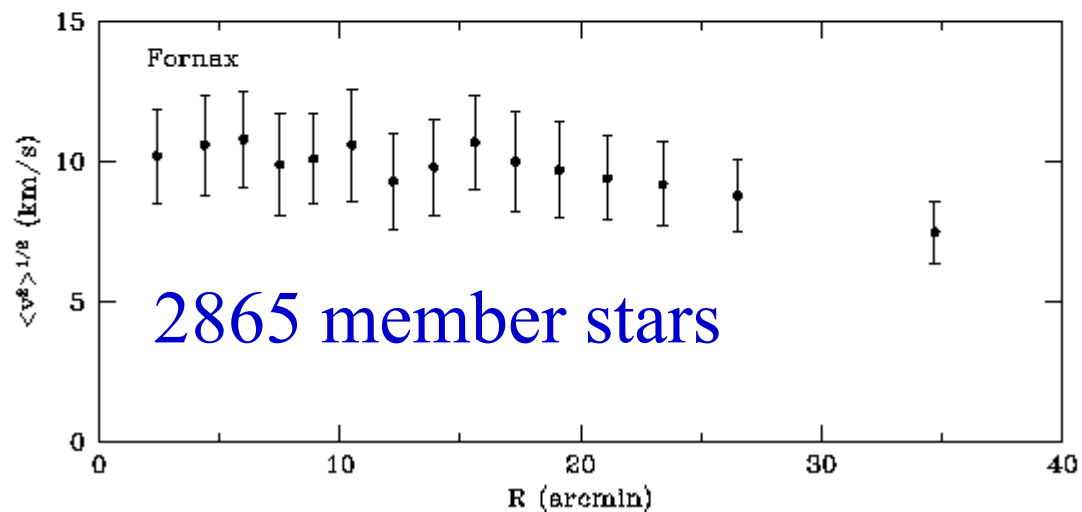
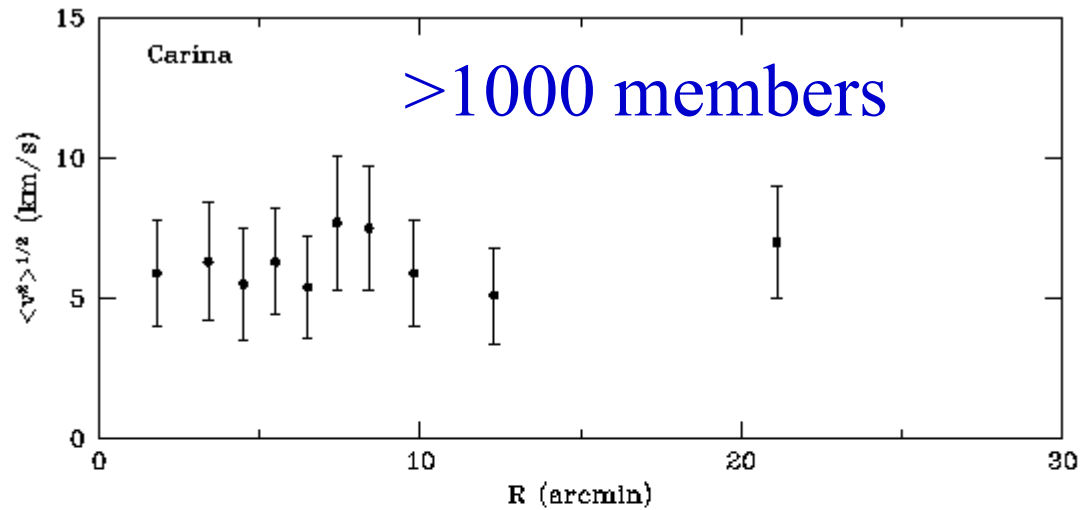
- Mass – anisotropy degeneracy prevents robust cusp/core distinction, but core + small radial bias always provides slightly better fit than cusp + tangential bias (cf Wu 2007 astro-ph/0702233)
- Break degeneracy by complementary information:
 - ◆ Ursa Minor has a cold subsystem, requiring shallow gradients for survival (Kleyna et al 2003 ApJL 588 L21)
 - ◆ Fornax globular clusters should have spiralled in through dynamical friction unless core (e.g. Goerdt et al 2006)
- Simplicity argues that cores favoured for all?
- New data and df-models underway
- (GG etal, VLT/Magellan core/cusp project)

From kinematics to dynamics:
 radial velocities have the information to measure
 gravitational potentials:
 anisotropy vs mass profile

$$M(r) = -\frac{r^2}{G} \left(\frac{1}{\nu} \frac{d\nu\sigma_r^2}{dr} + 2 \frac{\beta\sigma_r^2}{r} \right)$$



- Very large precision kinematics now exist: Magellan+VLT
- vastly superior to the best rotation curves
 - large samples after population selection



New models

Assumptions:

- Spherical symmetry
- Currently extending to tri-axial
- Equilibrium
- Tracer surface density from star counts

Models

$$\rho_{\text{halo}}(r) = \frac{\rho_0}{\left(\frac{r}{r_s}\right)^\gamma \left(1 + \left(\frac{r}{r_s}\right)^{1/\alpha}\right)^{\alpha(\beta-\gamma)}}$$

$$\Sigma_*(R) = 2 \int_R^\infty \frac{\rho_*(r)r dr}{\sqrt{r^2 - R^2}}$$

Same form used for both halo and stars, but stellar parameters held fixed

Zhao model = generalised Hernquist/NFW/...

Distribution function

$$F(E, L) = w(E)g(E, L) \quad \text{Gerhard (1991)}$$

$$g(E, L) = \begin{cases} c + (1 - c)(1 - (1 - x^2))^a & \text{tangential} \\ c + (1 - c)(1 - x^2)^a & \text{radial} \end{cases}$$

$$x(E, L) = \frac{L}{L_0 + L_{\text{circ}}(E)}$$

Constructing the line of sight velocity distributions

- Fit surface brightness profile
- Use method by P. Saha to invert integral equation for DF:

$$\rho(\Phi) = \frac{4\pi}{r^2} \int_0^\Phi w(E) dE \int_0^{L_{\max}} \frac{g(E, L)L dL}{\sqrt{2(\Phi - E) - L^2/r^2}}$$

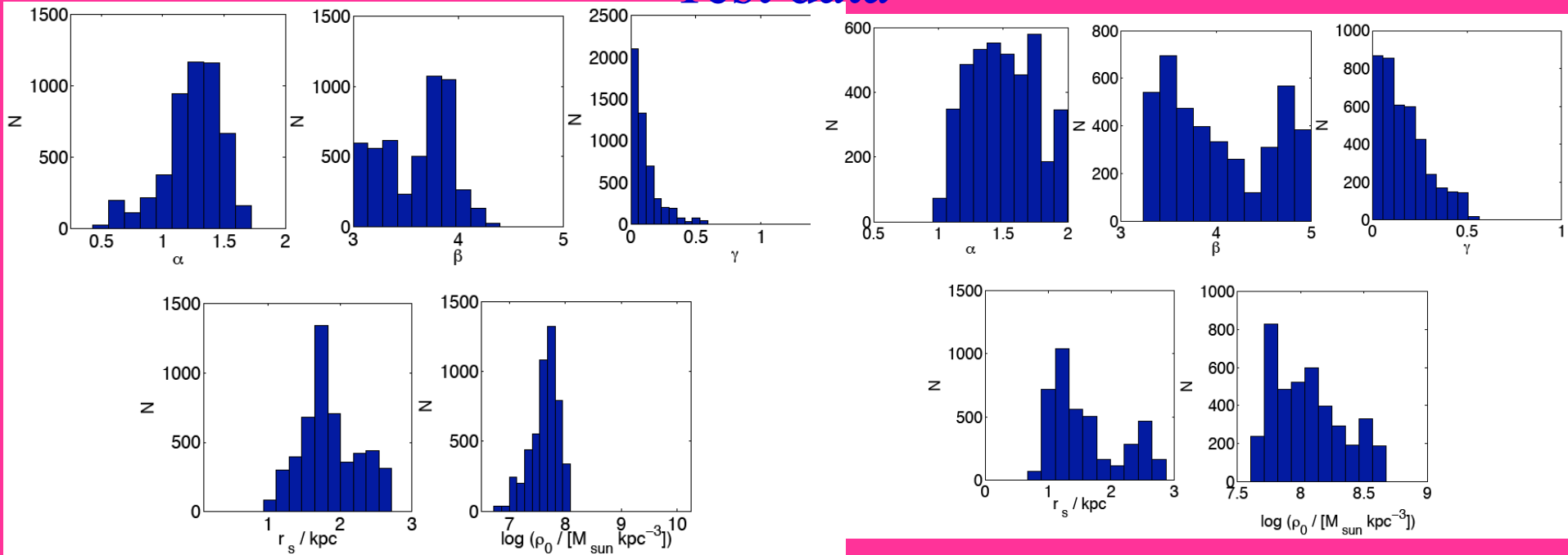
$$L_{\max} = \sqrt{2(\Phi - E)r}$$

- Project to obtain LOS velocity distribution on a grid of R and v_{los}
- Spline to required radii for observed stars, and convolve with individual velocity errors

Fitting the kinematic data

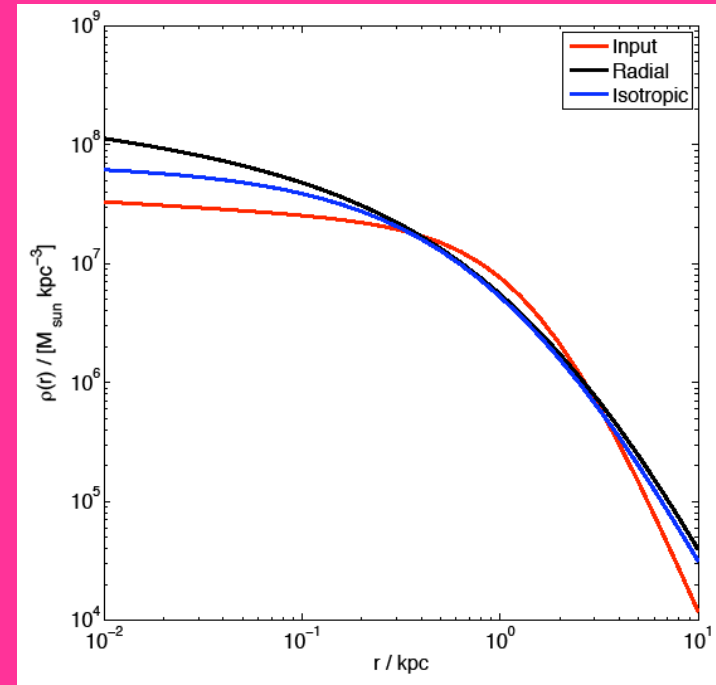
- Surface brightness profile determined from metal-poor data (v. similar to overall profile of Fornax)
- Markov-Chain-Monte-Carlo used to scan parameter space
- Parameters: 3 velocity distribution parameters
(a, c, L_0); 4 halo parameters ($\alpha, \beta, \gamma, \rho_0$)
- Multiple starting points for MCMC used - chains run in parallel and combined once “converged”
- Error convolution included - using only data with
 $\Delta v_{\text{los}} < 2 \text{ km s}^{-1}$

Test data



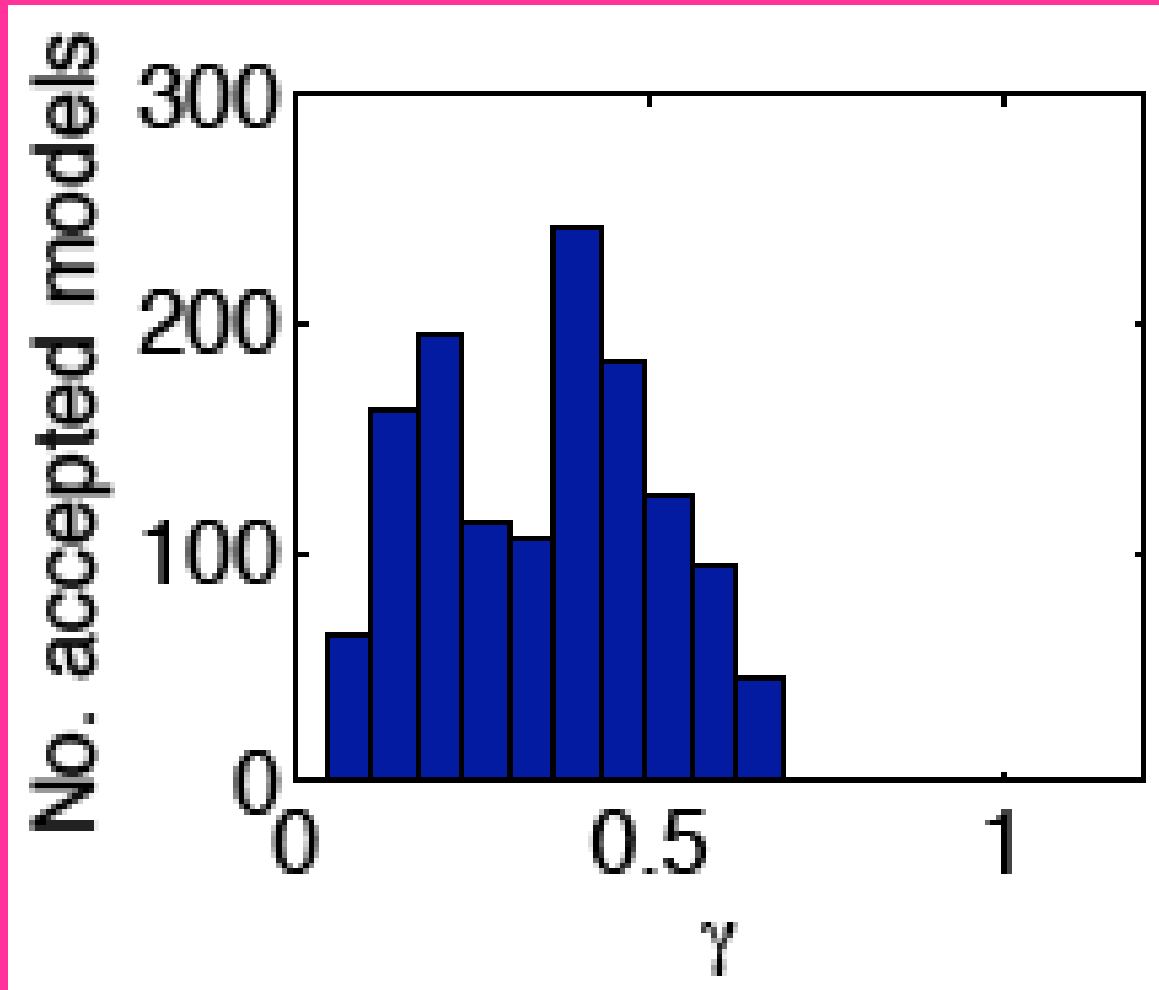
testing distribution function general models, and match data by Markov Chain MC —Wilkinson et al

-they reproduce test models with a conservative inner slope

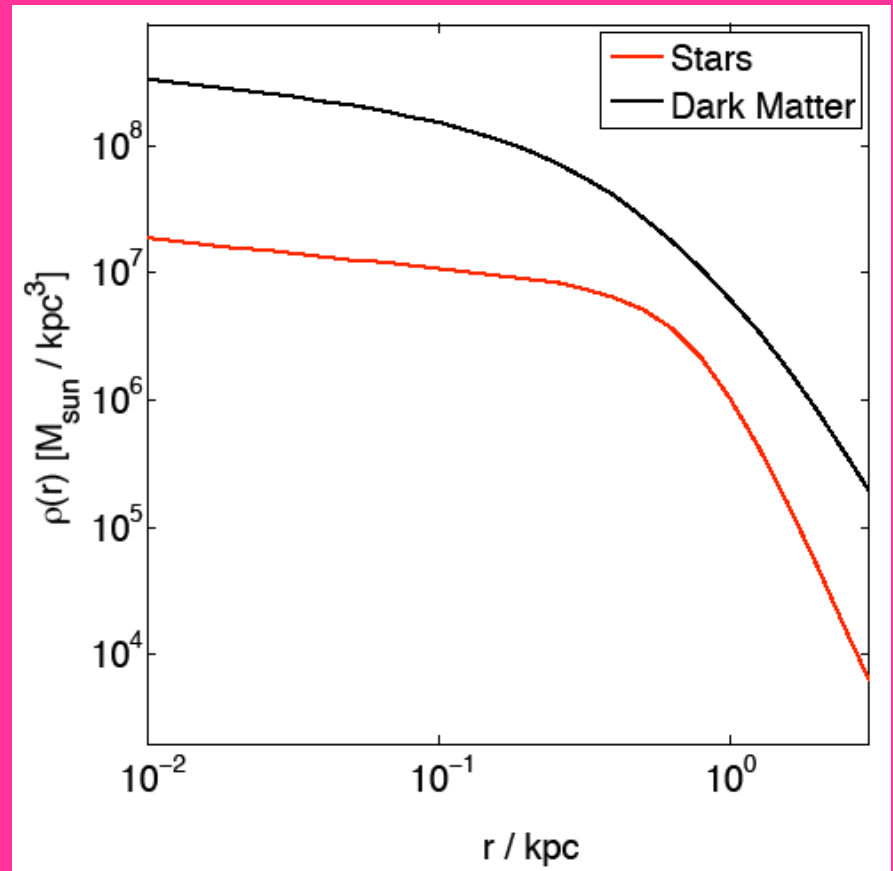
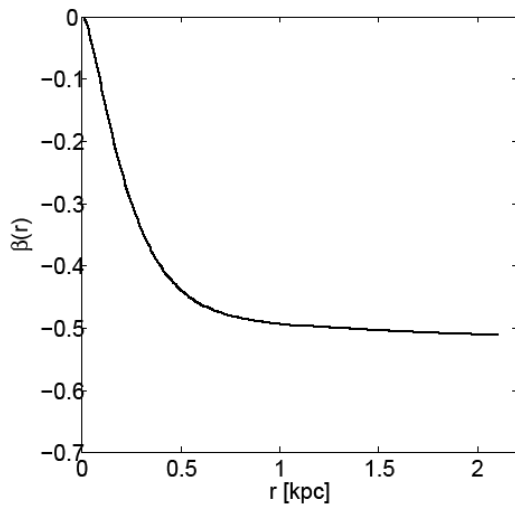


Fornax data analysis – 1600 stars

the answer – the DM inner density distribution in the Fornax dSph has slope ~ 0.3 – core-like, not cusped

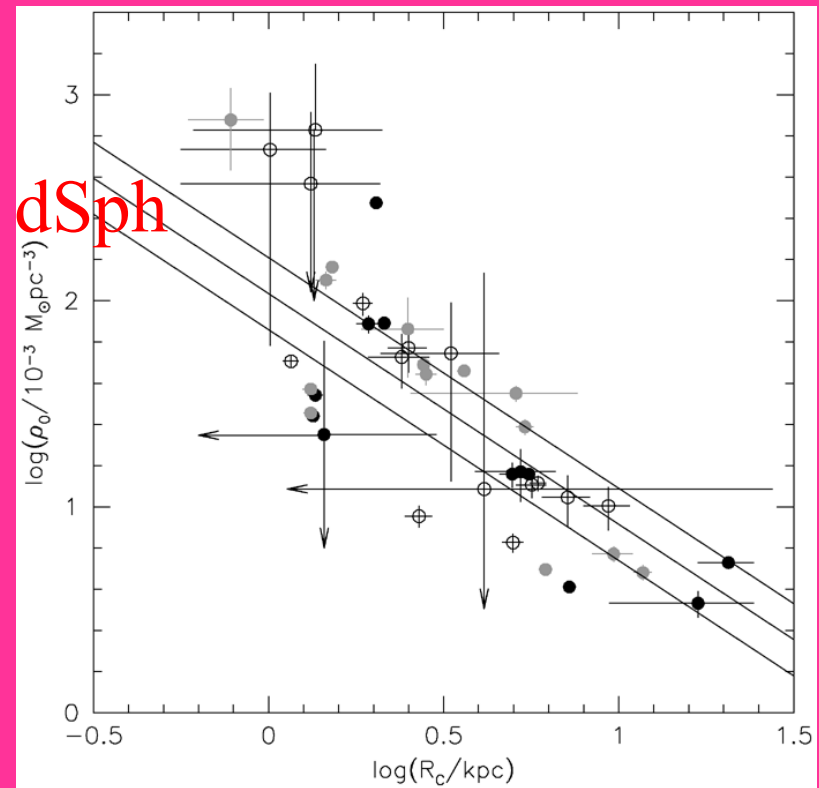
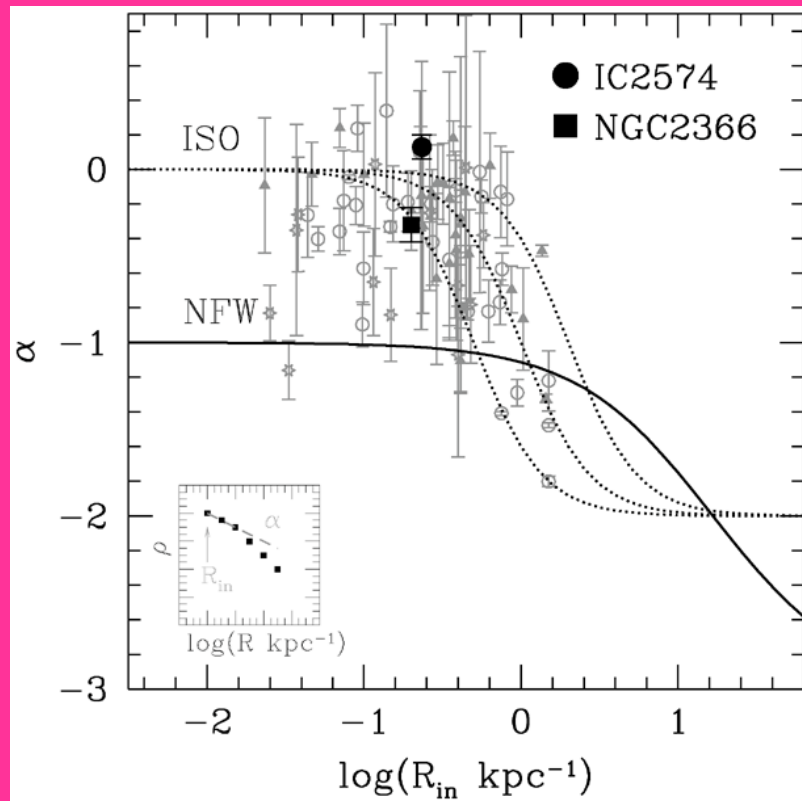


Kinematic profile is centrally isotropic, becoming tangentially biased; half-mass radius ~ 1 kpc, $M_{1/2} = 2.10^7 M_{\text{sun}}$ inside 300 pc



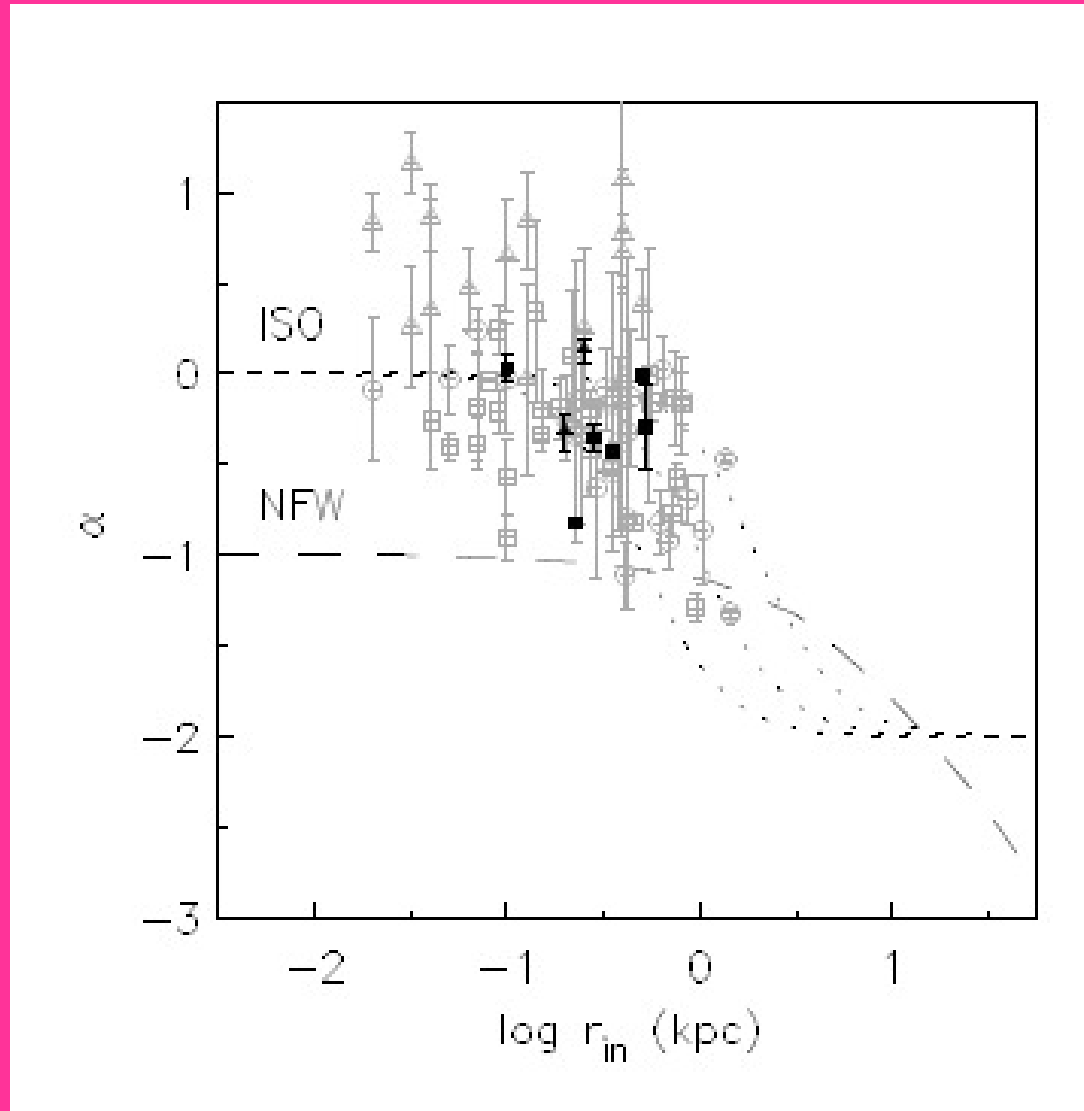
Are the dSph results consistent with other DM measures?

'Things' HI/Spitzer/Galex survey --
low-mass spirals consistent



Oh et al; de Blok et al AJ 2008 v136 2761; 2648

Central mass density profiles in DM-dominated systems are, in every measured case, core-like. The dSph are consistent.

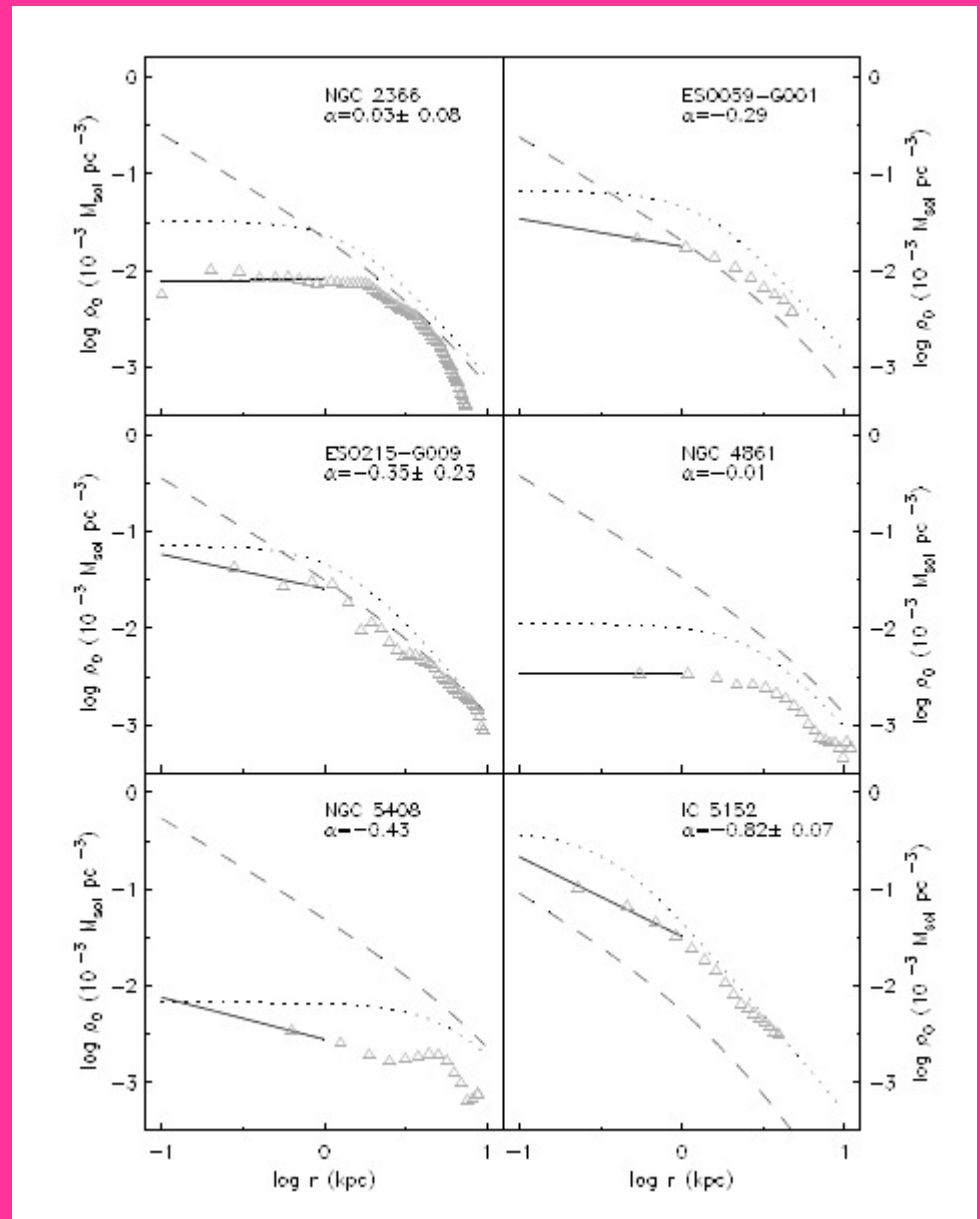


LSB spiral analysis by
Van Eymeren et al
0906.4654

Other data from
deBlok 2001
deBlok&Bosma 2002
Swaters 2003

Dark Matter mass distributions on sub-kpc scales are in every measured case core-like.

Recent LSB disk studies, and dSph analyses agree – DM has a shallow density profile in systems where we understand the astrophysics well-enough to be sure we are measuring initial conditions.



Dynamical analyses

- High-quality kinematic data exist
 - mass analyses → prefers cored mass profiles
 - Substructure, dynamical friction → prefers cores
 - Equilibrium assumption is valid inside optical radius
 - More sophisticated DF analyses agree well
-
- Mass-anisotropy degeneracy broken by DF analysis
 - **Central densities always similar and low**
 - **Central mass profiles are shallow**
 - **Characteristic scale of few x100pc**

Implications for Dark Matter:

- Characteristic Density $\sim 10\text{GeV}/c^2/\text{cm}^3$
 - If DM is very massive particles, they must be extremely dilute (Higgs $> 100\text{GeV}$)
- Characteristic Scale above 100pc, several $10^7 M_\odot$
 - power-spectrum scale break?
 - This would (perhaps!) naturally solve the substructure and cusp problems
- Number counts low relative to CDM
- lots of similar challenges on galaxy scales
- Need to consider a variety of DM candidates?

Summary-1:

- The Galaxy is not built from dSph
- --ages are inconsistent
- -- chemical enrichment history inconsistent
 - Merging happens, and continues today – but is creating a galactic halo which is very different than the extant Pop-II halo we have today. The outer galaxy is becoming young and metal-rich...

Pre-Galactic abundances in lowest-luminosity dSph are resolving very early stars [and re-ionisation?]

The dSph are ancient, have led gentle lives, and continued star formation for a Hubble time
→ no major perturbations to their dark matter

Summary-2:

- A minimum physical scale for galaxies:
 - half-light radius $>100\text{pc}$
 - ◆ mass size scale somewhat larger (x2?)
- Cored mass profiles, with similar low mean mass densities
 - $\sim 0.1 M_{\odot}/\text{pc}^3$, $\sim 10\text{GeV}/\text{cc}$
 - ◆ phase space densities fairly constant, maximum for galaxies – are they the first halos?
 - ◆ We have the first real V_{max} – Fornax, $V_{\text{m}}=20\pm 4\text{km/s}$
 - ◆ We do not know masses for the lowest luminosity systems
 - ◆ But some interesting scaling relations are developing

available analyses always suggest flat inner profiles
– more dSph galaxies under study

Darkness Visible: DM in astro- and particle physics
IoA Cambridge, August 2-6 2010

