

neutrino oscillations and the problem of neutrino masses a status report

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Plan

1. Recent issues in neutrino physics

- active neutrinos [see Fogli's talk]
- sterile neutrinos

2. Theoretical framework for neutrino masses

- purely Dirac neutrino masses
- neutrino masses from $D=5$ operator
- the see-saw mechanism
- tests of $D=5$ operator

} some conservative possibilities

3. Flavour symmetries

- any pattern behind data?
- natural setup for a KeV WDM ν candidate

} very speculative territory

Part 1.
recent issues in neutrino physics

2011/2012 breakthrough

- LBL experiments searching for $\nu_\mu \rightarrow \nu_e$ conversion
- SBL reactor experiments searching for anti- ν_e disappearance

[see Fogli's talk]

	Lisi [NeuTel 2013]	[1209.3023] [G-Garcia, Maltoni, Salvado, Schwetz]
$\sin^2 \vartheta_{13}$	$0.0241^{+0.0025}_{-0.0025}$ (NO) $0.0244^{+0.0023}_{-0.0025}$ (IO)	$0.0227^{+0.0023}_{-0.0024}$
$\sin^2 \vartheta_{23}$	$0.386^{+0.024}_{-0.021}$ (NO) $0.392^{+0.039}_{-0.022}$ (IO)	$0.413^{+0.037}_{-0.025} \oplus 0.594^{+0.021}_{-0.022}$



10 σ away from 0

impact on flavor symmetry (part 3)

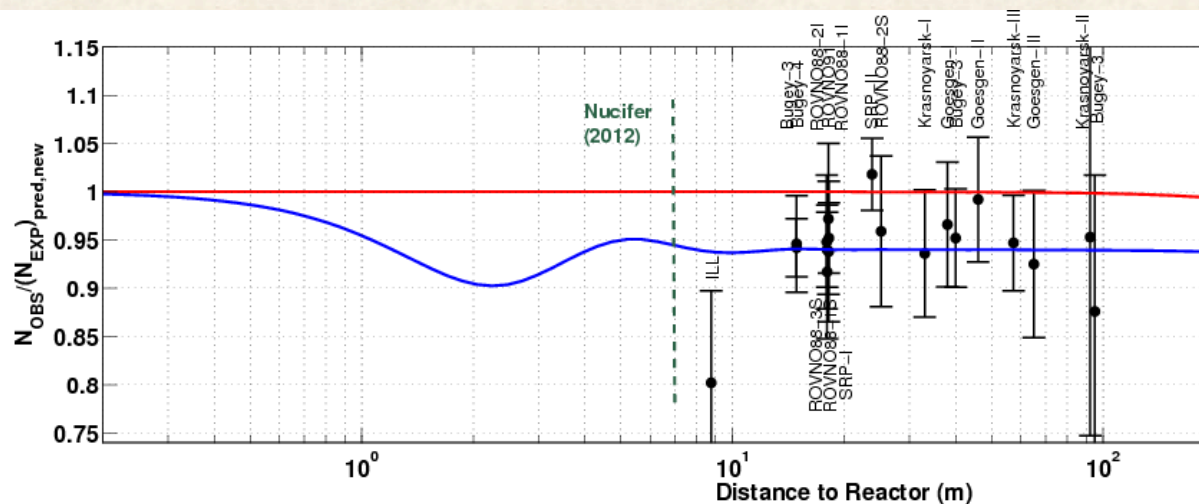


hint for non maximal ϑ_{23}

sterile neutrinos coming back

1 reactor anomaly (anti- ν_e disappearance)

re-evaluation of reactor anti- ν_e flux: new estimate 3.5% higher than old one



$$(\Phi_{\text{exp}} - \Phi_{\text{th}}) / \Phi_{\text{th}} \approx -6\%$$

[th. uncertainty?]

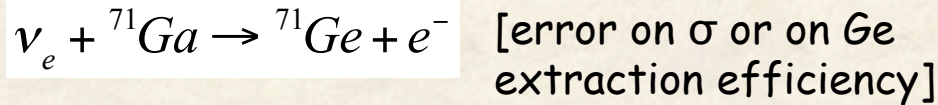
very SBL $L \leq 100$ m

$$\vartheta_{\text{es}} \approx 0.2$$

$$\Delta m^2 \approx m_s^2 \geq 1 \text{ eV}^2$$

supported by the **Gallium anomaly**

ν_e flux measured from high intensity radioactive sources in Gallex, Sage exp



most recent cosmological limits

[depending on assumed cosmological model, data set included,...]

relativistic degrees of freedom at recombination epoch

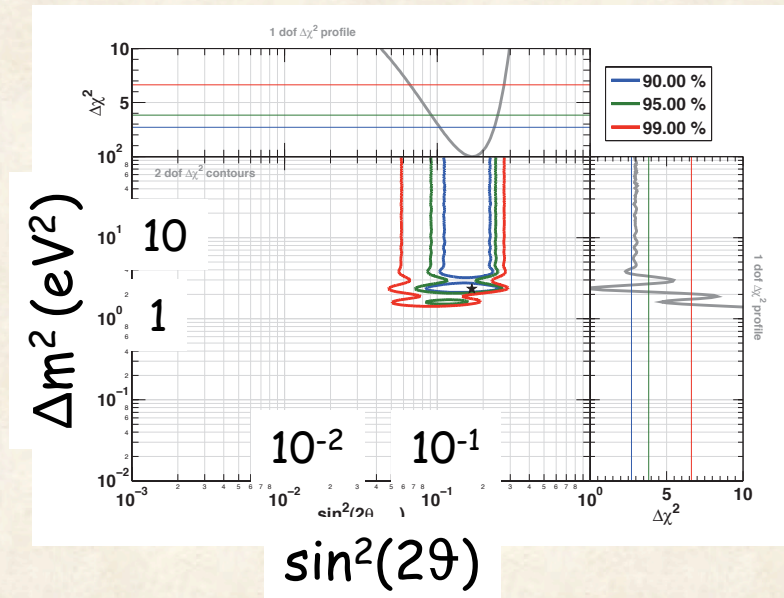
$$N_{\text{eff}} = 3.30 \pm 0.27$$

[Planck, WMAP, BAO, high multiple CMB data]

2 long-standing claim

evidence for $\nu_\mu \rightarrow \nu_e$ appearance in accelerator experiments

exp		$E(\text{MeV})$	$L(\text{m})$
LSND	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	$10 \div 50$	30
MiniBoone	$\nu_\mu \rightarrow \nu_e$	$300 \div 3000$	541
	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$		



fully thermalized non relativistic ν

$$N_{\text{eff}} < 3.80 \quad (95\% \text{ CL})$$

$$m_s < 0.42 \text{ eV} \quad (95\% \text{ CL})$$

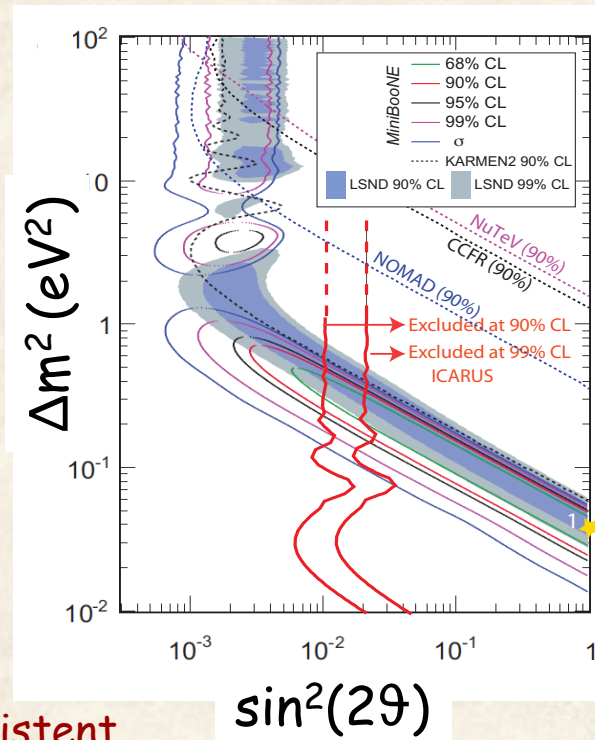
3.8σ

3.8σ [signal from low-energy region]

parameter space limited by
negative results from Karmen
and ICARUS

$$\vartheta_{e\mu} \approx 0.035$$

$$\Delta m^2 \approx 0.5 \text{ eV}^2$$



3

interpretation in 3+1 scheme: **inconsistent**
(more than 1s disfavored by
cosmology)

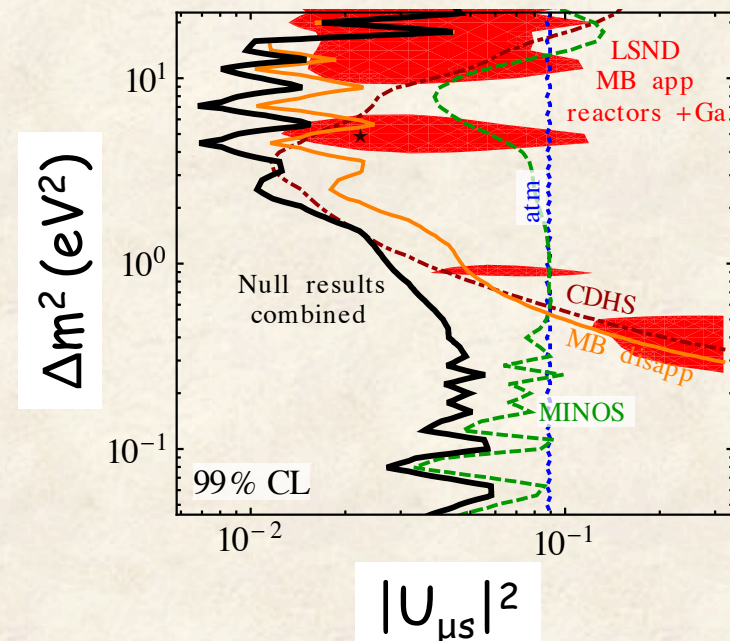
$$\underbrace{\vartheta_{e\mu}}_{0.035} \approx \underbrace{\vartheta_{es}}_{0.2} \times \vartheta_{\mu s}$$



$$\vartheta_{\mu s} \approx 0.2$$

predicted suppression in ν_μ disappearance
experiments: **undetected**

by ignoring LSND/Miniboone data the
reactor anomaly can be accommodated
by $m_s \geq 1 \text{ eV}$ and $\vartheta_{es} \approx 0.2$
[not suitable for WDM, more on this later]



Part 2.

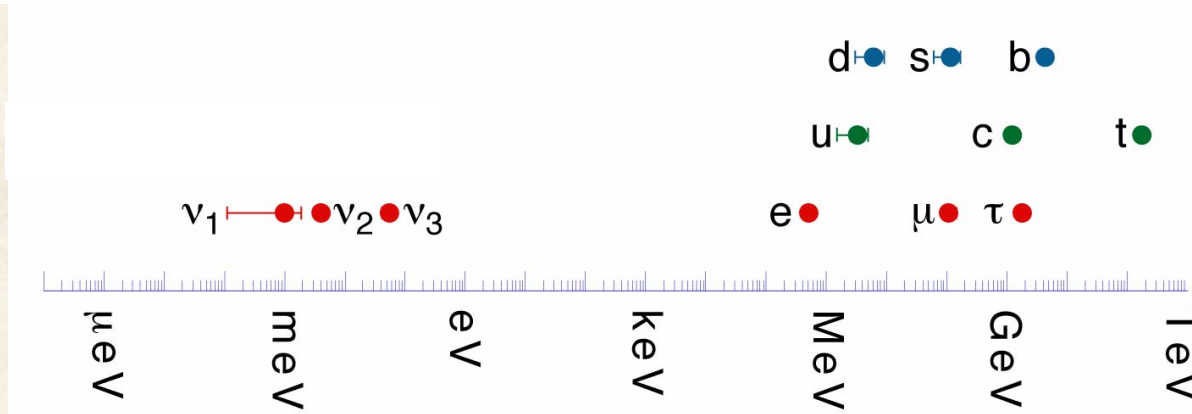
theoretical framework for neutrino masses

a non-vanishing neutrino mass is **evidence of the incompleteness of the SM**

Questions

how to extend the SM in order to accommodate neutrino masses?

why neutrino masses are so small, compared with the charged fermion masses?



why lepton mixing angles are so different from those of the quark sector?

$$|U_{PMNS}| \approx \begin{pmatrix} 0.8 & 0.5 & 0.2 \\ 0.4 & 0.6 & 0.6 \\ 0.4 & 0.6 & 0.8 \end{pmatrix}$$

$$V_{CKM} \approx \begin{pmatrix} 1 & O(\lambda) & O(\lambda^4 \div \lambda^3) \\ O(\lambda) & 1 & O(\lambda^2) \\ O(\lambda^4 \div \lambda^3) & O(\lambda^2) & 1 \end{pmatrix}$$

$\lambda \approx 0.22$

How to modify the SM?

(I) modify the particle content

Example 1

add (three copies of)
right-handed neutrinos

$$\nu^c \equiv (1,1,0)$$

full singlet under
 $G = SU(3) \times SU(2) \times U(1)$

ask for (global) invariance under B-L
(no more automatically conserved as in the SM)

gauge invariant Yukawa interactions

$$L_Y = d^c y_d (\Phi^+ q) + u^c y_u (\tilde{\Phi}^+ q) + e^c y_e (\Phi^+ l) + \nu^c y_\nu (\tilde{\Phi}^+ l) + h.c.$$

$$m_f = \frac{y_f}{\sqrt{2}} v \quad f = u, d, e, \nu$$

$$-\frac{g}{\sqrt{2}} W_\mu^- \bar{e} \sigma^\mu U_{PMNS} \nu + h.c.$$

U_{PMNS} has three mixing angles
and one phase, like V_{CKM}

a generic problem of this approach

the particle content can be modified in several different ways
in order to account for non-vanishing neutrino masses

(additional right-handed neutrinos, new $SU(2)$ fermion triplets, additional $SU(2)$ scalar triplet(s), SUSY particles,...). Which is the correct one?

a problem of the above example

if neutrinos are so similar to the other fermions, why are so light?
[right-handed neutrinos have access to an extra spatial dimension?]

$$\frac{y_\nu}{y_{top}} \leq 10^{-12}$$

(II) abandon renormalizability

and work with an effective field theory valid up to a cut-off Λ

$$L_{SM} \rightarrow L_{SM} + \frac{L_5}{\Lambda} + \frac{L_6}{\Lambda^2} + \dots$$

$$\frac{L_5}{\Lambda} = \frac{(\tilde{\Phi}^+ l)(\tilde{\Phi}^+ l)}{\Lambda} = \frac{v}{2} \left(\frac{v}{\Lambda} \right) \nu \nu + \dots$$

a unique operator!
[up to flavour combinations]
it violates (B-L) by two units

suppressed by a factor (v/Λ)
with respect to the neutrino mass term
of Example 1

$$\frac{m_\nu}{m_{top}} \approx 10^{-12}$$

\updownarrow

$$\Lambda \approx 10^{15} \text{ GeV}$$

L_5 represents the effective, low-energy description of several extensions of the SM

**Example 2:
see-saw**

add (three copies of) $\nu^c \equiv (1,1,0)$

full singlet under
 $G = \text{SU}(3) \times \text{SU}(2) \times \text{U}(1)$

this is like Example 1, but without enforcing (B-L) conservation

$$L(\nu^c, l) = \nu^c y_\nu (\tilde{\Phi}^+ l) + \frac{1}{2} \nu^c M \nu^c + h.c.$$

mass term for right-handed neutrinos: gauge invariant, violates (B-L) by two units.

for $E \ll M$

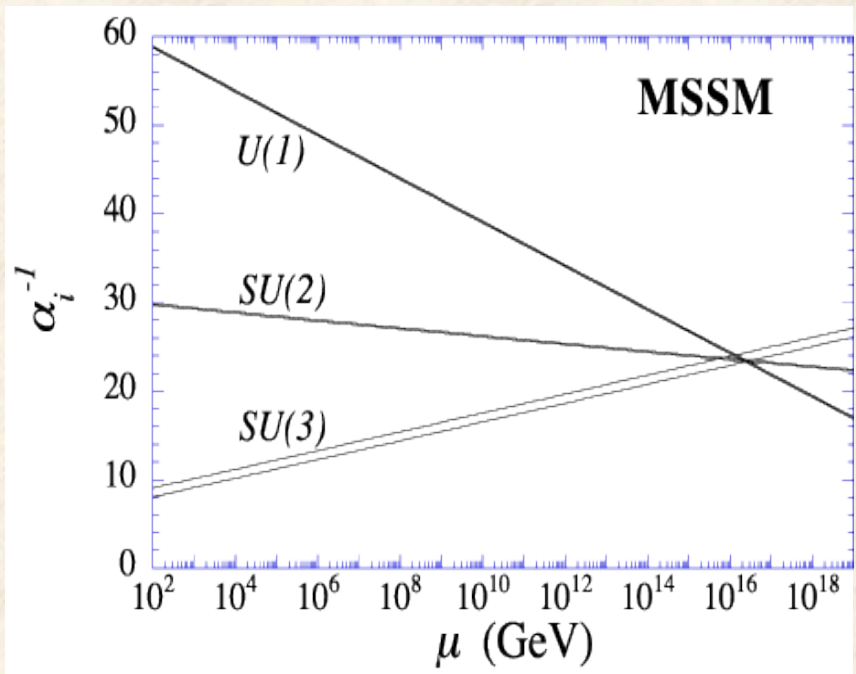
$$L_{eff}(l) = -\frac{1}{2} (\tilde{\Phi}^+ l) \left[y_\nu^T M^{-1} y_\nu \right] (\tilde{\Phi}^+ l) + h.c. + \dots$$

this reproduces L_5 , with M playing the role of Λ
(type I) see-saw

Theoretical motivations for the see-saw

an independent evidence for $\Lambda \approx 10^{15}$ GeV comes from the **unification of the gauge coupling constants** in (SUSY extensions of) the SM.

such unification is a generic prediction of **Grand Unified Theories** (GUTs): the SM gauge group G is embedded into a simple group such as $SU(5)$, $SO(10)$,...



Particle classification: it is possible to unify all SM fermions (1 generation) into a single irreducible representation of the GUT gauge group. Simplest example: $G_{\text{GUT}} = SO(10)$

$$16 = (q, d^c, u^c, l, e^c, \nu^c)$$

a whole family plus a right-handed neutrino!

no experimental evidence so far! Look for **proton decay** (model dependent rates and decay channels)

2 additional virtues of the see-saw

the see-saw mechanism can enhance small mixing angles into large ones

the (out-of equilibrium, CP-violating) decay of heavy right-handed neutrinos in the early universe might generate a net asymmetry between leptons and anti-leptons, partially converted into the observed baryon asymmetry

weak point of the see-saw

full high-energy theory is difficult to test

$$L(\nu^c, l) = \nu^c y_\nu (\tilde{\Phi}^+ l) + \frac{1}{2} \nu^c M \nu^c + h.c.$$

few observables to pin down the extra parameters: η, \dots [additional possibilities exist under special conditions, e.g. Lepton Flavor Violation at observable rates]

easier to test the low-energy remnant L_5

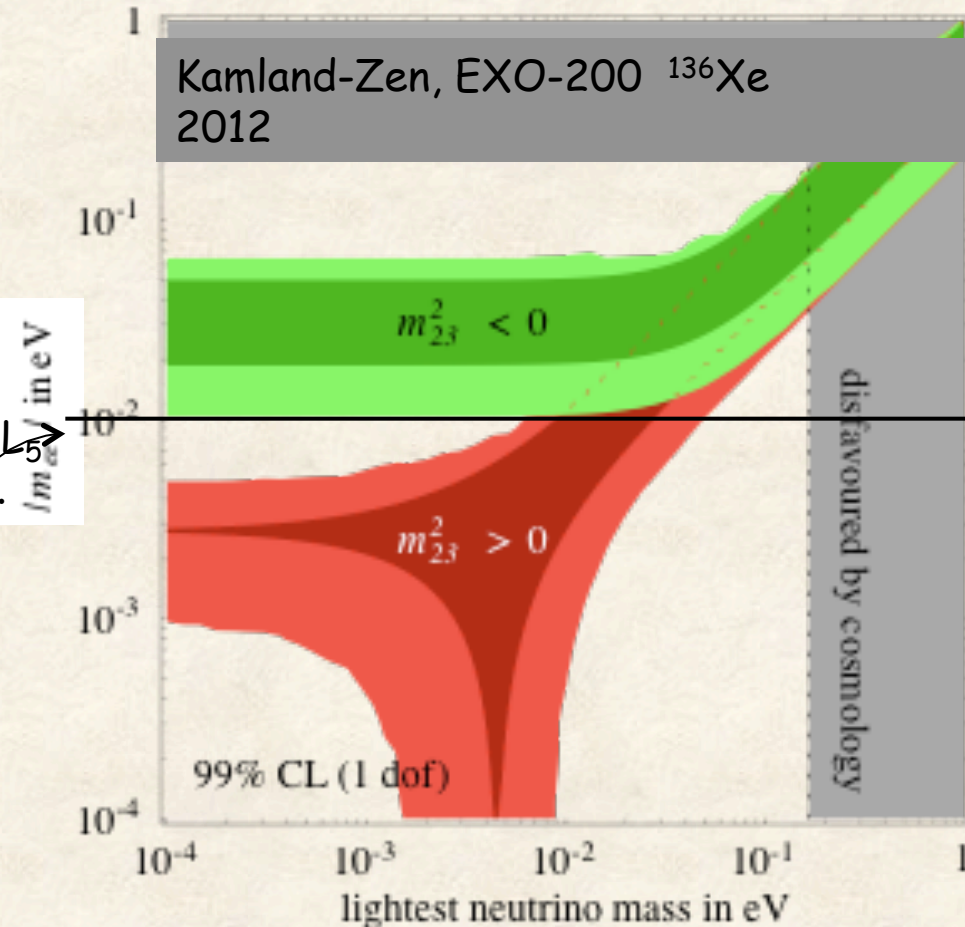
[which however is “universal” and does not implies the specific see-saw mechanism of Example 2]

look for a process where B-L is violated by 2 units. The best candidate is $0\nu\beta\beta$ decay $(A, Z) \rightarrow (A, Z+2) + 2e^-$ this would discriminate L_5 from other possibilities, such as Example 1.

future expected sensitivity
on $|m_{ee}|$ is 10 meV

from the current knowledge of $(\Delta m_{ij}^2, \vartheta_{ij})$ we can estimate the expected range of $|m_{ee}|$

depends on 18 physical parameters, the double of those describing $(L_{SM}) + L_5$:



part 3.
flavor symmetries

Flavor symmetries

can we constrain Yukawa couplings (and Majorana masses) by some flavour symmetry?

largest possible flavour symmetry is obtained in the limit $y = 0$ ($M = 0$)

$$G_{MFV} = \begin{cases} SU(3)^5 & \text{SM} \\ SU(3)^6 & \text{SM} + 3 \nu^c \end{cases}$$

observed fermion masses and mixing angles **break** G_{MFV} **completely**
(only possible exact symmetry beyond **Gauge** \times **Lorentz** \times **CPT** is **B-L**)

flavour symmetry should be **spontaneously** broken (explicit breaking is not predictive)

$$G_{MFV} \supseteq G_f \rightarrow H_f$$

by a set of scalar fields
 $\varphi \rightarrow \varphi_g$ under G_f

$\langle \varphi \rangle$ determined by minimizing an energy functional $V(\varphi)$ invariant under G_f

$$V(\varphi_g) = V(\varphi)$$

$\langle \varphi \rangle$, absolute minimum of $V(\varphi)$, breaks G_f down to H_f

Yukawas promoted to dynamical variables

$$y(\varphi / \Lambda_f)$$

observed Yukawa couplings

$$y(\langle \varphi \rangle / \Lambda_f)$$

huge number of possibilities: choice of G_f (global, local, continuous, discrete,...)
choice of representations for scalars φ and fermions

any empirical evidence for G_f and H_f ?

example I: $G_f = U(1)_{FN}$

[Froggatt, Nielsen 1979]

lessons from the quark sector: mass ratios and mixing angles are small, hierarchical parameters

$$\frac{m_u}{m_t} \ll \frac{m_c}{m_t} \ll 1 \quad \frac{m_d}{m_b} \ll \frac{m_s}{m_b} \ll 1 \quad |V_{ub}| \ll |V_{cb}| \ll |V_{us}| \equiv \lambda < 1$$

easily reproduced by $G_f = U(1)_{FN}$ and $H_f = \{1\}$

mass ratios and mixing angles are powers of a small SB parameter λ

flavon	Q_{FN}
φ	-1

$U(1)_{FN}$ broken by

$$\lambda = \frac{\langle \varphi \rangle}{\Lambda_f} \approx 0.2$$

assign decreasing, non-negative, charges to fermions of increasing generations

field	Q_{FN}
q, u^c	(3, 2, 0)
d^c	(1, 0, 0)

$$y_d = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{pmatrix}$$

entries up to unknown $O(1)$ coefficients

unbroken $U(1)_{FN}$

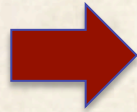
$$y_d = \begin{pmatrix} \lambda^4 & \lambda^3 & \lambda \\ \lambda^3 & \lambda^2 & 1 \\ \lambda^3 & \lambda^2 & 1 \end{pmatrix}$$

broken $U(1)_{FN}$

order of magnitude of most mass ratios and mixing angles correctly reproduced

can be extended to the lepton sector where evidence for hierarchy mainly comes from charged leptons

field	Q_{FN}
e^c	(3,2,0)
l	(1,0,0)



$$y_e \approx y_d^T$$

$$m_\nu \propto \begin{pmatrix} \lambda^2 & \lambda & \lambda \\ \lambda & 1 & 1 \\ \lambda & 1 & 1 \end{pmatrix}$$

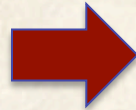
ϑ_{23}	ϑ_{13}	ϑ_{12}	$\Delta m_{12}^2 / \Delta m_{23}^2$
1	λ	λ	1
1	λ	1	λ^2

if $\det(23) \approx \lambda$

Anarchy (neutrino sector is structure-less)

[Hall, Murayama, Weiner 1999]

field	Q_{FN}
l	(0,0,0)



$$m_\nu \propto \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}$$

mixing angles
and mass ratios
are random $O(1)$
quantities

$$|U_{PMNS}| \approx \begin{pmatrix} 0.8 & 0.5 & 0.2 \\ 0.4 & 0.6 & 0.6 \\ 0.4 & 0.6 & 0.8 \end{pmatrix}$$

ϑ_{13} not tiny and ϑ_{23} not maximal predicted

consistent with data

$$G_f = U(1)_{FN}$$

- compatible with $SU(5)$ grand unification
- compatible with known solutions to the gauge hierarchy problem (SUSY, RS,...)
- large number of independent $O(1)$ parameters
- no testable predictions beyond order-of-magnitude accuracy

ν_1^c KeV sterile neutrino [reviews by Merle 1302.2615 and Abazajian et al 1204.5186] as WDM candidate

two small parameters

$$\underbrace{M_1}_{\text{KeV}} \ll \underbrace{M_{2,3}}_{\text{up to } 10^{15} \text{ GeV}}$$

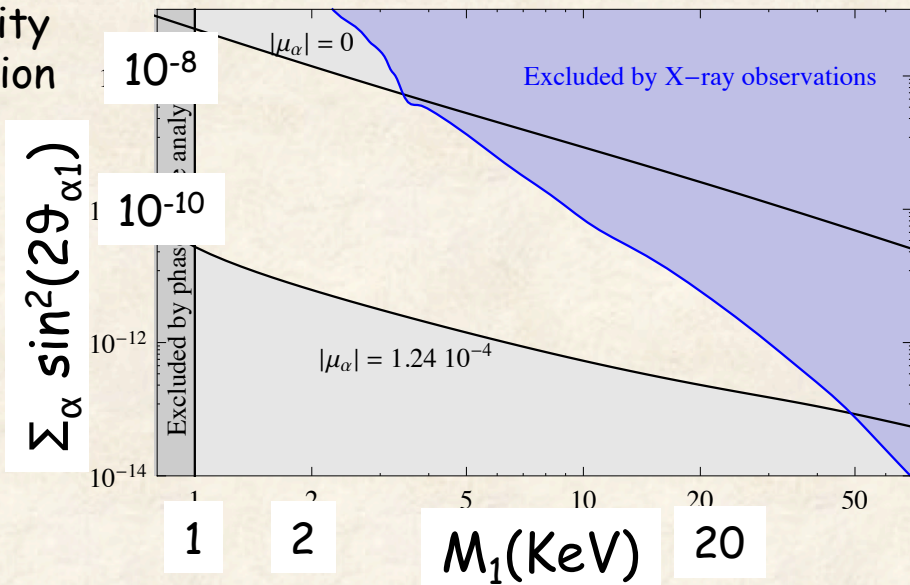
- phase space density
- structure formation

$$\vartheta_1^2 \equiv \sum_{\alpha} |\vartheta_{1\alpha}|^2 < 10^{-7}$$

- DM-abundance
- X-ray limits
- SN cooling
- $\tau_1 < \tau_U$

active-sterile mixing

[Canetti, Drewes, Frossard, Shaposhnikov 1208.4607]



can both be explained by $U(1)_{FN}$?

field	Q_{FN}	
ν^c	$(X, 0, 0)$	$X \geq 0$
l	$(0, 0, 0)$	

in the unbroken phase:

- $M_1 = 0$
- ν_1^c decoupled from ν_{α}

after $U(1)_{FN}$ breaking

$$\xi \equiv \lambda^X$$

$$m_D = \begin{pmatrix} \xi & \xi & \xi \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} m_0$$

$$M = \begin{pmatrix} \xi^2 & \xi & \xi \\ \xi & 1 & 1 \\ \xi & 1 & 1 \end{pmatrix} M_0$$

$$m_i \approx \frac{m_0^2}{M_0} \approx (0.01 \div 0.1) \text{ eV}$$

$$M_1 \approx \xi^2 M_0 \quad M_{2,3} \approx M_0$$

$$\vartheta_1^2 \approx \frac{m_i}{M_1} \approx (10^{-5} \div 10^{-4}) \left(\frac{1 \text{ KeV}}{M_1} \right)$$

not sufficient to match correct DM abundance and X-ray limits

to further suppress ϑ_1^2

tuning

stretch unknown $O(1)$ coefficients to produce an extra suppression factor

additional flavour symmetry

extra suppression of $m_{1\alpha}$ matrix elements, e.g. by a discrete symmetry

$$Z_2: \quad \nu_1^c \rightarrow -\nu_1^c \quad \vartheta' \rightarrow -\vartheta'$$

$$m_D = \begin{pmatrix} \xi \xi' & \xi \xi' & \xi \xi' \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} m_0$$

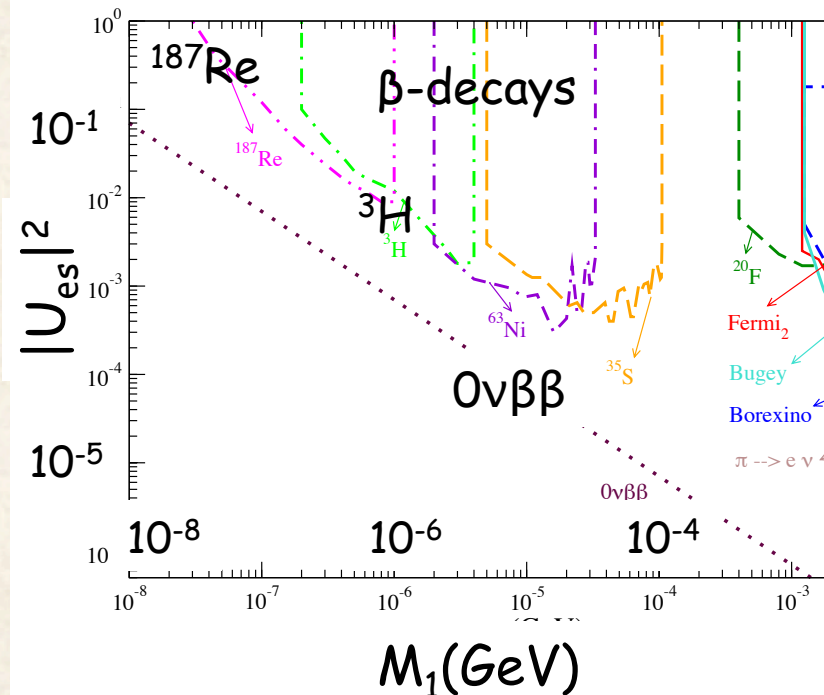
$$M = \begin{pmatrix} \xi^2 & \xi \xi' & \xi \xi' \\ \xi \xi' & 1 & 1 \\ \xi \xi' & 1 & 1 \end{pmatrix} M_0$$

$$\xi' \equiv \frac{\langle \vartheta' \rangle}{\Lambda_f}$$

$$\vartheta_1^2 \approx \xi'^2 \frac{m_i}{M_1}$$

[Merle, Niro 1302.2032
De Vega, Moreno, Moya de Guerra,
Ramon Medrano, Sanchez 1109.3452]

lab searches [Abazajian 1204.5186]



example II: G_f = discrete flavor symmetry

$$U_{PMNS} = U_{PMNS}^0 + \text{corrections}$$



some simple pattern, exactly reproduced by a flavor symmetry

well motivated before 2012

$$U_{PMNS}^0 = U_{TB} \equiv \begin{pmatrix} 2/\sqrt{6} & 1/\sqrt{3} & 0 \\ -1/\sqrt{6} & 1/\sqrt{3} & -1/\sqrt{2} \\ -1/\sqrt{6} & 1/\sqrt{3} & 1/\sqrt{2} \end{pmatrix} \quad \begin{array}{l} \text{Tribimaximal} \\ \text{Mixing} \end{array}$$

discrete flavor symmetries showed very efficient to reproduce U_{PMNS}^0

still justified today?

$$U_{TB} \approx \begin{pmatrix} 0.82 & 0.58 & 0 \\ -0.41 & 0.58 & -0.71 \\ -0.41 & 0.58 & 0.71 \end{pmatrix}$$

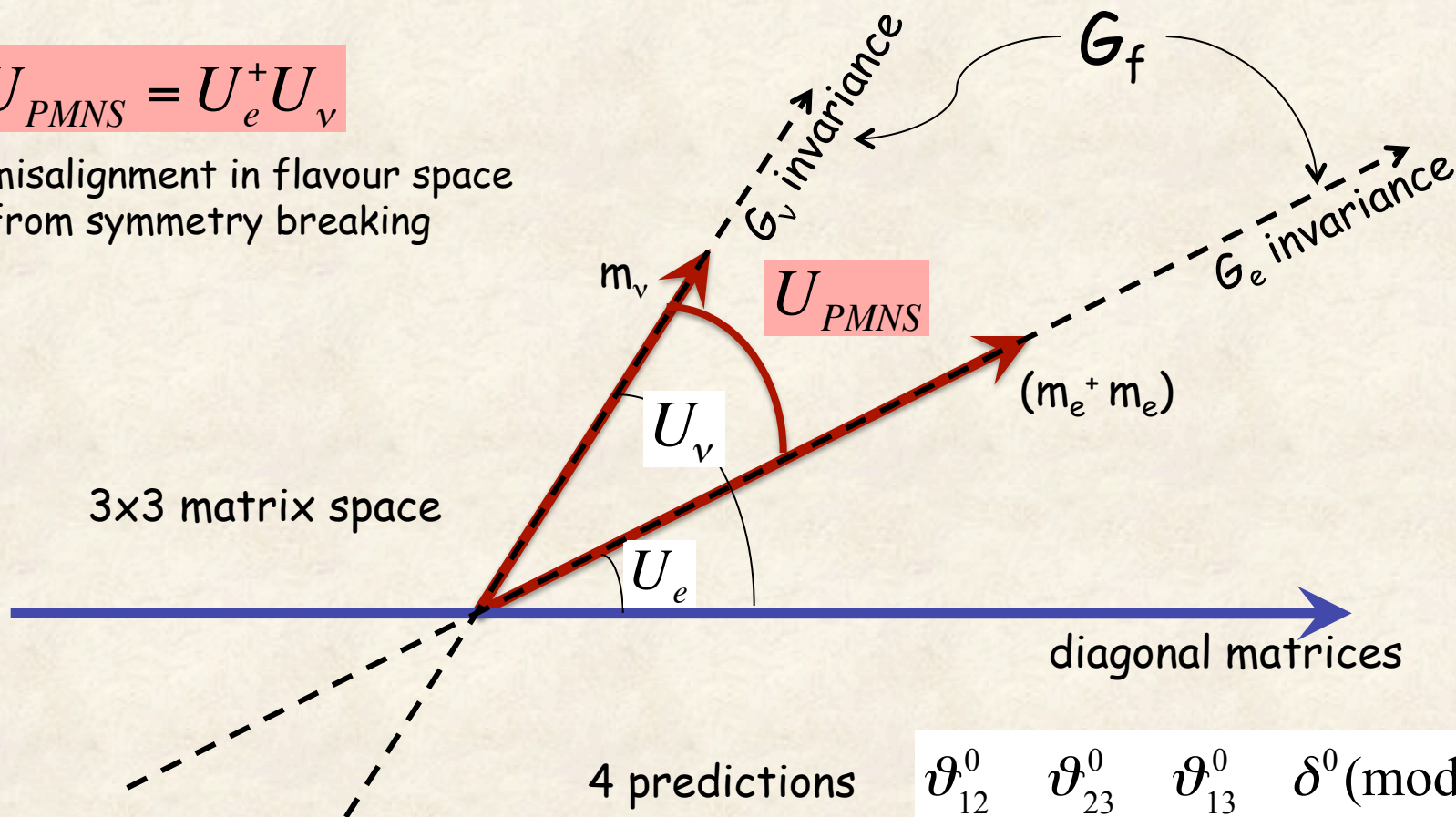
$$|U_{PMNS}| = \begin{pmatrix} 0.80 \div 0.85 & 0.51 \div 0.59 & 0.13 \div 0.18 \\ 0.21 \div 0.54 & 0.42 \div 0.73 & 0.58 \div 0.81 \\ 0.22 \div 0.55 & 0.41 \div 0.73 & 0.57 \div 0.80 \end{pmatrix}$$

[3σ ranges from Gonzalez-Garcia, Maltoni, Salvado, Schwetz 1209.3023]

Mixing patterns U_{PMNS}^0 from discrete symmetries

$$U_{PMNS} = U_e^\dagger U_\nu$$

misalignment in flavour space
from symmetry breaking



4 predictions

$$\vartheta_{12}^0 \quad \vartheta_{23}^0 \quad \vartheta_{13}^0 \quad \delta^0(\text{mod } \pi)$$

the most general group
leaving $v^\dagger m_\nu v$ invariant,
and m_i unconstrained

$$G_\nu = Z_2 \times Z_2$$

Majorana neutrinos
imply G_ν discrete!

G_e can be continuous but the
simplest choice is G_e discrete

$$G_e = \begin{cases} Z_2 \times Z_2 \\ Z_n & n \geq 3 \end{cases}$$

Some mixing patterns

$$G_v = Z_2 \times Z_2$$

G_f	G_e	U_{PMNS}	$\sin^2 \vartheta_{23}$	$\sin \vartheta_{13}$	$\sin^2 \vartheta_{12}$	
A_4	Z_3	$[M]$	$1/2$	$1/\sqrt{3}$	$1/2$	
S_4	Z_3	$[TB]$	$1/2$	0	$1/3$	
	Z_4 $(Z_2 \times Z_2)'$	$[BM]$	$1/2$	0	$1/2$	
A_5	Z_3	$[GR_1]$	$1/2$	0	0.127	
	Z_5	$[GR_2]$	$1/2$	0	0.276	
	$(Z_2 \times Z_2)'$	$[GR_3]$	0.276	0.309	0.276	
		$[Exp\ 3\sigma]$	$0.34 \div 0.67$	$0.13 \div 0.17$	$0.27 \div 0.34$	

[Lam 1104.0055
F., Hagedorn, Toroop]

[TB \leftrightarrow Harrison,
Perkins and Scott]

[$GR_2 \leftrightarrow$ Kajiyama,
Raidal, Strumia 2007]

-- a long way to promote a candidate pattern to a complete model

-- general feature $U_{PMNS} = U_{PMNS}^0 + O(u) \quad u \equiv \frac{\langle \varphi \rangle}{\Lambda} < 1$

-- neutrino masses fitted, not predicted.

expectation for $U_{PMNS}^0 = U_{TB}$

$$\begin{cases} \vartheta_{13}^0 = 0 \\ \vartheta_{23}^0 = \frac{\pi}{4} \end{cases}$$



$$\begin{cases} \vartheta_{13} = O(\text{few degrees}) \\ \vartheta_{23} = \text{close to } \frac{\pi}{4} \end{cases}$$

not to spoil the agreement with ϑ_{12}

wrong!

possibilities

1 add large corrections $O(\vartheta_{13}) \approx 0.2$

- predictability is lost since in general correction terms are many
- new dangerous sources of FC/CPV if NP is at the TeV scale

2 change discrete group G_f

- solutions exist
- special forms of Trimaximal mixing

$$U^0 = U_{TB} \times \begin{pmatrix} \cos\alpha & 0 & e^{i\delta} \sin\alpha \\ 0 & 1 & 0 \\ -e^{-i\delta} \sin\alpha & 0 & \cos\alpha \end{pmatrix}$$

G_f	$\Delta(96)$	$\Delta(384)$	$\Delta(600)$
α	$\pm\pi/12$	$\pm\pi/24$	$\pm\pi/15$
$\sin^2 \vartheta_{13}^0$	0.045	0.011	0.029

F.F., C. Hagedorn, R. de A. Torroop
 hep-ph/1107.3486 and hep-ph/1112.1340
 Lam 1208.5527 and 1301.1736
 Holthausen1, Lim and Lindner 1212.2411
 Neder, King, Stuart 1305.3200

$\delta^0 = 0, \pi$ (no CP violation) and
 α “quantized” by group theory

too big groups?

3 relax symmetry requirements

[Hernandez, Smirnov 1204.0445]

G_e as before

$$G_v = Z_2$$

2 predictions:
2 combinations of

$$\vartheta_{12}^0 \quad \vartheta_{23}^0 \quad \vartheta_{13}^0$$

leads to testable sum rules

$$\sin^2 \vartheta_{23} = \frac{1}{2} + \frac{1}{\sqrt{2}} \sin \vartheta_{13} \cos \delta_{CP} + O(\sin^2 \vartheta_{13})$$

[He, Zee 2007 and 2011, Grimus, Lavoura 2008, Grimus, Lavoura, Singraber 2009, Albright, Rodejohann 2009, Antusch, King, Luhn, Spinrath 2011, King, Luhn 2011, G. Altarelli, F.F., L. Merlo and E. Stamou hep-ph/1205.4670]

4 include CP in the SB pattern

$$G_{CP} = G_f \rtimes CP$$

[F. F., C. Hagedorn and R. Ziegler 1211.5560, 1303.7178
Ding, King, Luhn, Stuart 1303.6180]

$$G_e$$

$$G_v = Z_2 \times CP$$

mixing angles and CP violating phases

$$(\vartheta_{12}^0, \vartheta_{23}^0, \vartheta_{13}^0, \delta^0, \alpha^0, \beta^0)$$

predicted in terms of a single real parameter $0 \leq \vartheta \leq 2\pi$

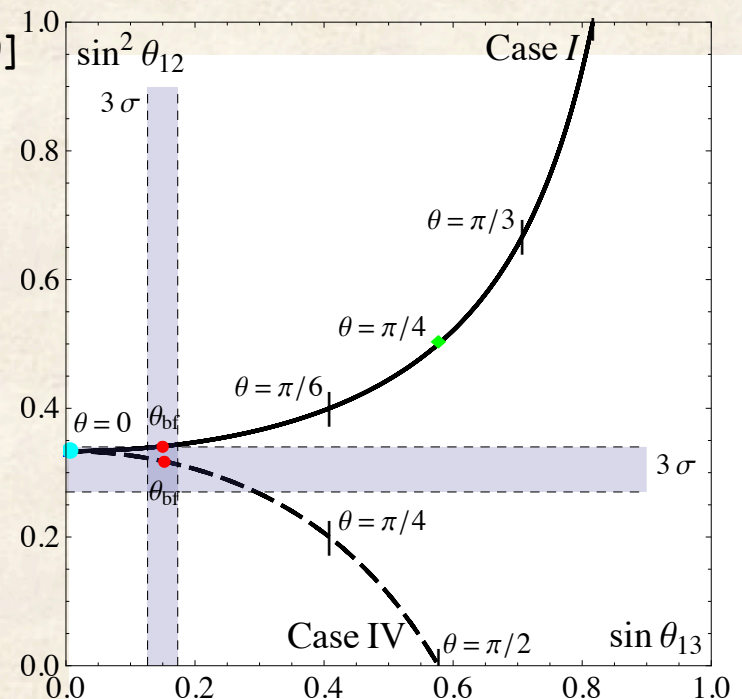
2 examples with $G_f = S_4$ $G_e = Z_3$

$$\sin^2 \vartheta_{23}^0 = \frac{1}{2}$$

$$|\sin \delta^0| = 1$$

$$\sin \alpha^0 = 0$$

$$\sin \beta^0 = 0$$



Conclusion

big progress on the experimental side:

- precisely measured θ_{13} : many σ away from zero!
- potentially interesting implications on θ_{23}
- sterile neutrinos waiting for exp. checks

on the theory side:

neutrino masses represent a unique window on high-energy physics (such as GUTs, B-L violation, leptogenesis,...) but the fundamental theory is hard to identify.

flavour symmetries: a useful tool but

no compelling and unique picture have emerged so far

present data can be described within widely different frameworks

models based on “anarchy” and/or its variants - $U(1)_{\text{FN}}$ models - in good shape: neutrino mass ratios and mixing angles just random $O(1)$ quantities

models based on discrete symmetries are less supported by data now and modifications of simplest realizations are required

-- add large corrections $O(\theta_{13}) \approx 0.2$

-- move to large discrete symmetry groups G_f such as $\Delta(96)$ $\Delta(384)$...

-- relax symmetry requirements

-- include CP in the SB pattern

Backup slides

example III: $G_f = G_{\text{MFV}} = SU(3)_L \times SU(3)_R \times \dots$

(relevant for charged lepton masses)

$$L_Y = -e^c \frac{\varphi}{\Lambda_f} (\Phi^\dagger l) + h.c. + \dots$$

$$l \sim (3, 1) \quad e^c \sim (1, \bar{3}) \quad \varphi \sim (\bar{3}, 3)$$

the most general invariant $V(\varphi)$ admits several natural stationary points closest to the real world is

$$\langle \varphi \rangle = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & a \end{pmatrix}$$

$$H_f = SU(2)_L \times SU(2)_R \times U(1) \times \dots$$

hierarchical spectrum: $m_\tau \neq 0$ $m_e = m_\mu = 0$: good starting point but difficult to turn into a realistic model

- ad hoc breaking terms?
- more SB fields?

some recent progress: Espinosa, Fong, Nardi 1211.6428

Alonso, Gavela, Isidori, Maiani 1306.5927

Mixing matrix $U=U_{PMNS}$ (Pontecorvo, Maki, Nakagawa, Sakata)

neutrino
interaction
eigenstates

$$\nu_f = \sum_{i=1}^3 U_{fi} \nu_i$$

$(f = e, \mu, \tau)$

neutrino mass
eigenstates

U is a 3×3 unitary matrix
standard parametrization

$$U_{PMNS} = \begin{pmatrix} c_{12} c_{13} & s_{12} c_{13} & s_{13} e^{i\delta} \\ -s_{12} c_{23} - c_{12} s_{13} s_{23} e^{-i\delta} & c_{12} c_{23} - s_{12} s_{13} s_{23} e^{-i\delta} & c_{13} s_{23} \\ -c_{12} s_{13} c_{23} e^{-i\delta} + s_{12} s_{23} & -s_{12} s_{13} c_{23} e^{-i\delta} - c_{12} s_{23} & c_{13} c_{23} \end{pmatrix} \times \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha} & 0 \\ 0 & 0 & e^{i\beta} \end{pmatrix}$$

$$c_{12} \equiv \cos \vartheta_{12}, \dots$$

three mixing angles

$$\vartheta_{12}, \vartheta_{13}, \vartheta_{23}$$

three phases (in the most general case)

$$\delta$$

$$\underbrace{\alpha, \beta}$$

do not enter $P_{ff'} = P(\nu_f \rightarrow \nu_{f'})$

oscillations can only test 6 combinations

$$\Delta m_{21}^2, \Delta m_{32}^2, \vartheta_{12}, \vartheta_{13}, \vartheta_{23}, \delta$$

2011/2012 breakthrough

from LBL experiments searching for $\nu_\mu \rightarrow \nu_e$ conversion

T2K: muon neutrino beam produced at JPARC [Tokai]
E=0.6 GeV and sent to SK 295 Km apart [1106.2822]

MINOS: muon neutrino beam produced at Fermilab [E=3 GeV] sent to Soudan Lab 735 Km apart [1108.0015]

$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 \vartheta_{23} \sin^2 2\vartheta_{13} \sin^2 \frac{\Delta m_{32}^2 L}{4E} + \dots$$

both experiments favor $\sin^2 \vartheta_{13} \sim \text{few \%}$

from SBL reactor experiments searching for anti- ν_e disappearance

Double Chooz (far detector):

Daya Bay (near + far detectors):

RENO (near + far detectors):

$$\sin^2 2\vartheta_{13} = 0.109 \pm 0.039$$

$$\sin^2 \vartheta_{13} = 0.089 \pm 0.011$$

$$\sin^2 \vartheta_{13} = 0.113 \pm 0.023$$

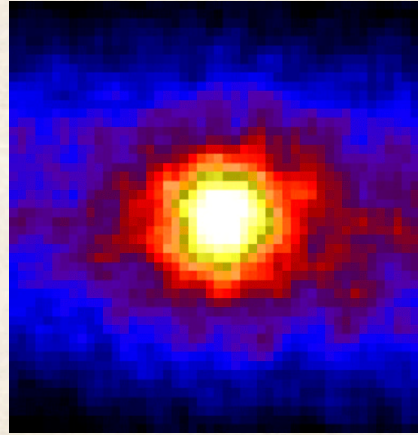
$$P(\bar{\nu}_e \rightarrow \bar{\nu}_e) = 1 - \sin^2 2\vartheta_{13} \sin^2 \frac{\Delta m_{32}^2 L}{4E} + \dots$$

SBL reactors are sensitive to ϑ_{13} only
LBL experiments anti-correlate $\sin^2 2\vartheta_{13}$ and $\sin^2 \vartheta_{23}$
also breaking the octant degeneracy $\vartheta_{23} \leftrightarrow (\pi - \vartheta_{23})$

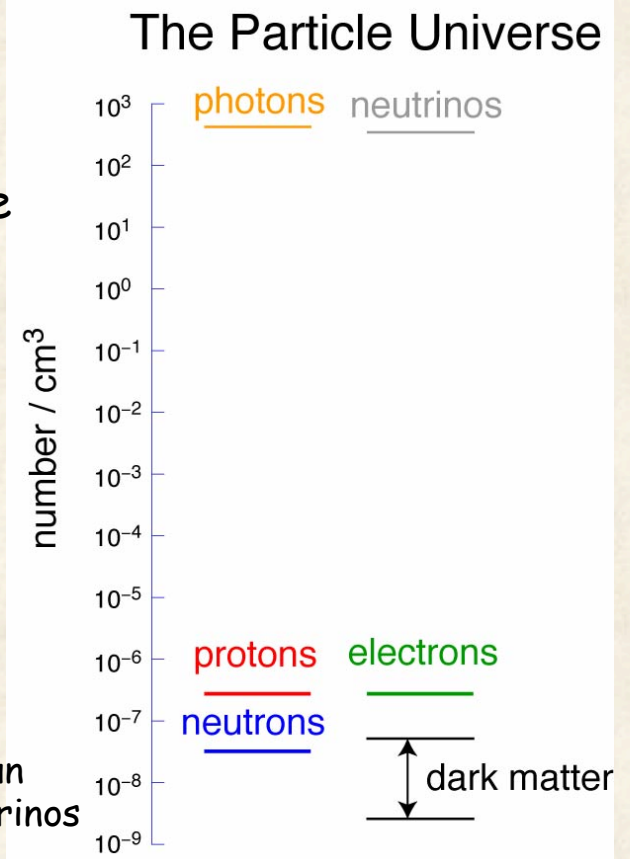
General remarks on neutrinos

the more abundant particles in the universe after the photons: about 300 neutrinos per cm^3

produced by stars: **about 3%** of the sun energy emitted in neutrinos. As I speak more than 1 000 000 000 000 solar neutrinos go through your bodies each second.



this is a picture of the sun reconstructed from neutrinos



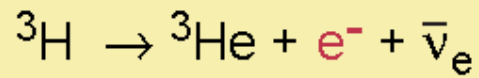
electrically neutral and extremely light:

they can carry information about extremely large length scales
e.g. a probe of supernovae dynamics: neutrino events from a supernova explosion first observed 23 years ago

in particle physics:

they have a tiny mass (1 000 000 times smaller than the electron's mass)
the discovery that they are massive (twelve anniversary now!) allows us to explore, at least in principle, extremely high energy scales, otherwise inaccessible to present laboratory experiments (more on this later on...)

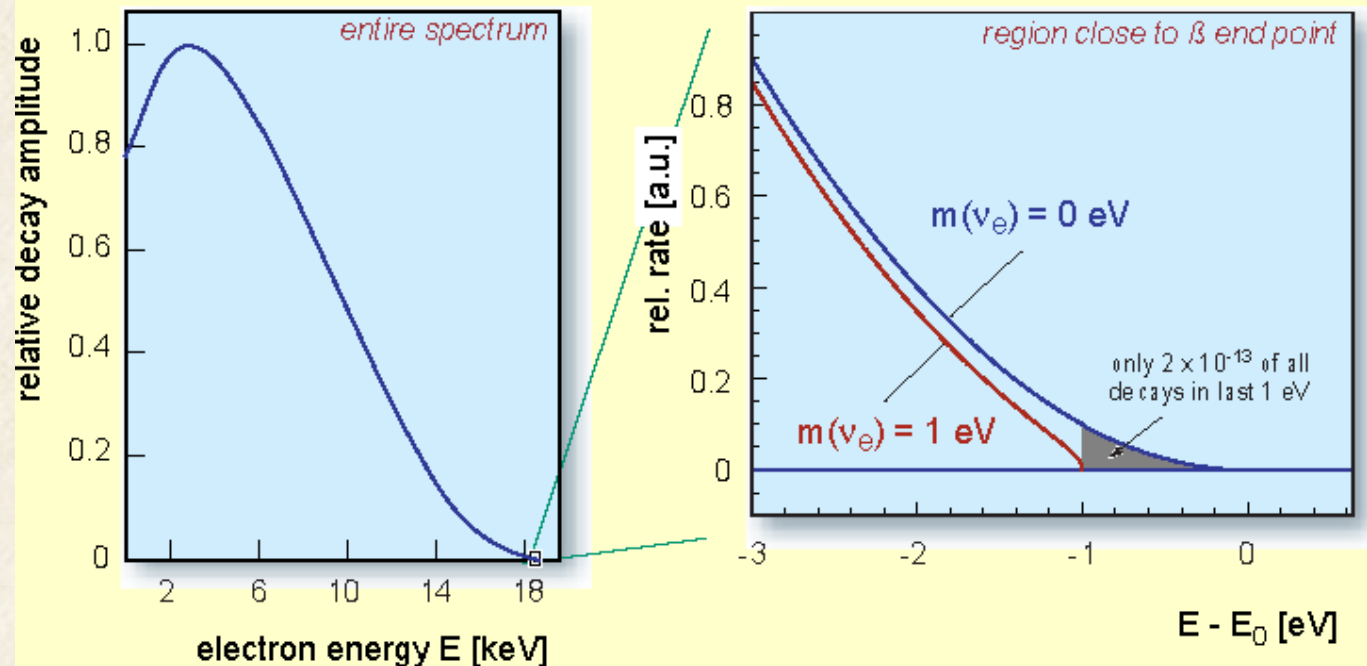
Upper limit on neutrino mass (laboratory)



superallowed

half life : $t_{1/2} = 12.32 \text{ a}$

β end point energy : $E_0 = 18.57 \text{ keV}$



$$m_\nu < 2.2 \text{ eV} \quad (95\% \text{ CL})$$

Upper limit on neutrino mass (cosmology)

massive ν suppress the formation of small scale structures

$$\sum_i m_i < 0.2 \div 1 \text{ eV}$$

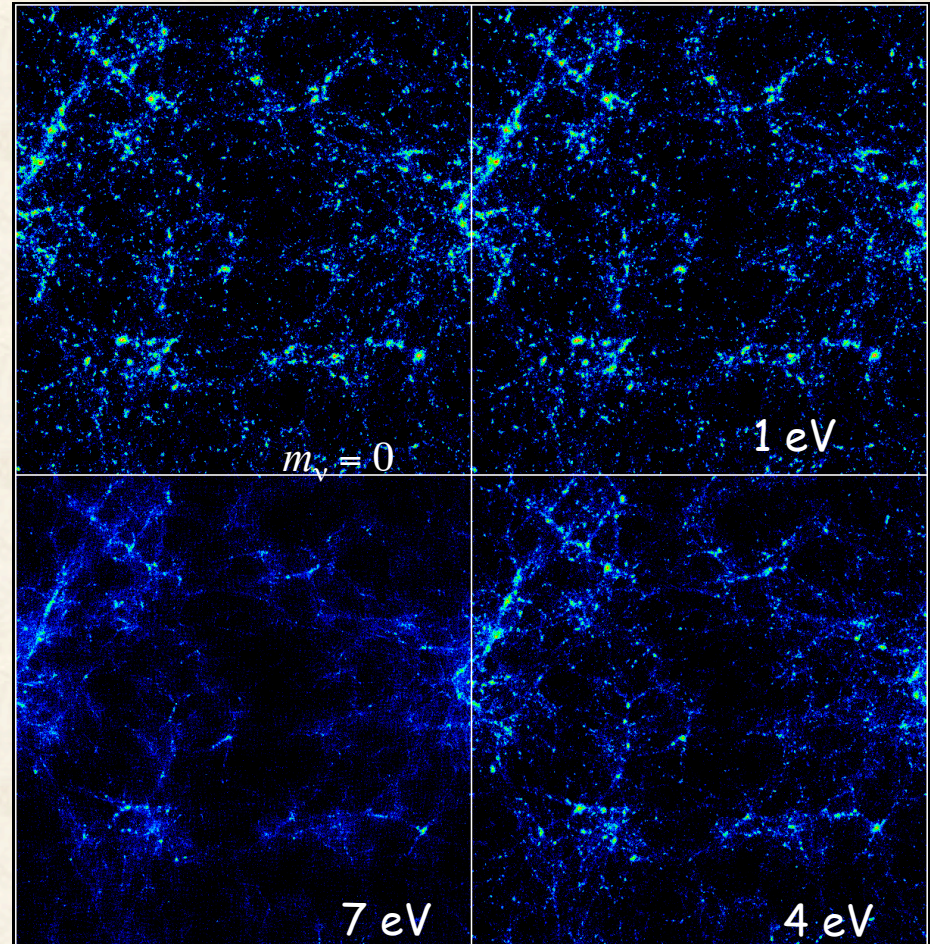
depending on

- assumed cosmological model
- set of data included
- how data are analyzed

$$k_{\text{nr}} \approx 0.026 \left(\frac{m_\nu}{1 \text{ eV}} \right)^{1/2} \Omega_m^{1/2} h \text{ Mpc}^{-1}.$$

The small-scale suppression is given by

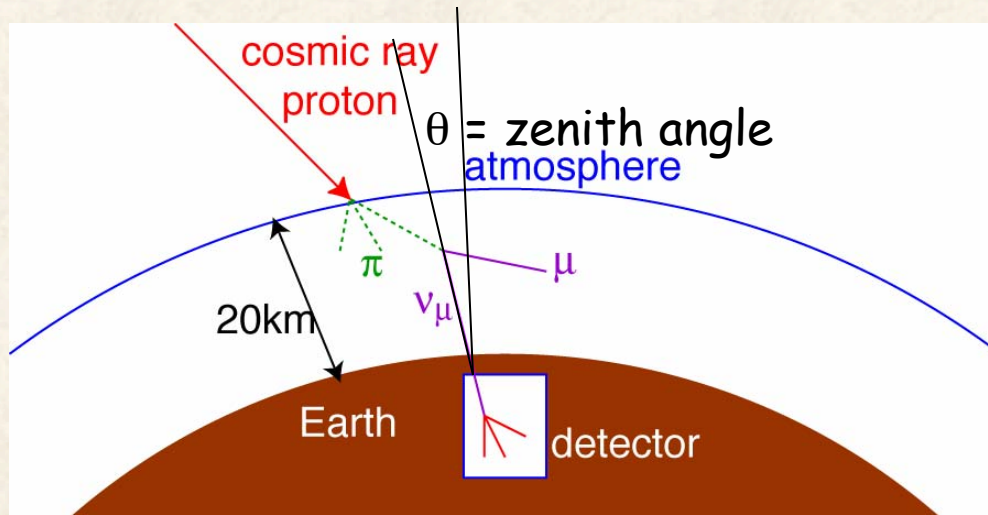
$$\left(\frac{\Delta P}{P} \right) \approx -8 \frac{\Omega_\nu}{\Omega_m} \approx -0.8 \left(\frac{m_\nu}{1 \text{ eV}} \right) \left(\frac{0.1 N}{\Omega_m h^2} \right)$$



$$\delta(\vec{x}) \equiv \frac{\rho(\vec{x}) - \bar{\rho}}{\bar{\rho}}$$

$$\langle \delta(\vec{x}_1) \delta(\vec{x}_2) \rangle = \int \frac{d^3 k}{(2\pi)^3} e^{i\vec{k} \cdot (\vec{x}_1 - \vec{x}_2)} P(\vec{k})$$

Atmospheric neutrino oscillations

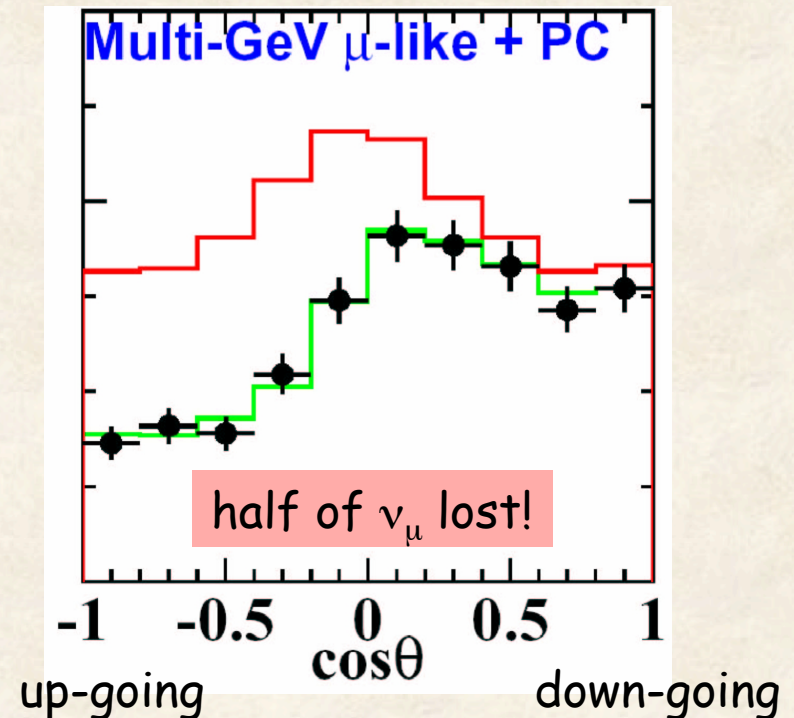
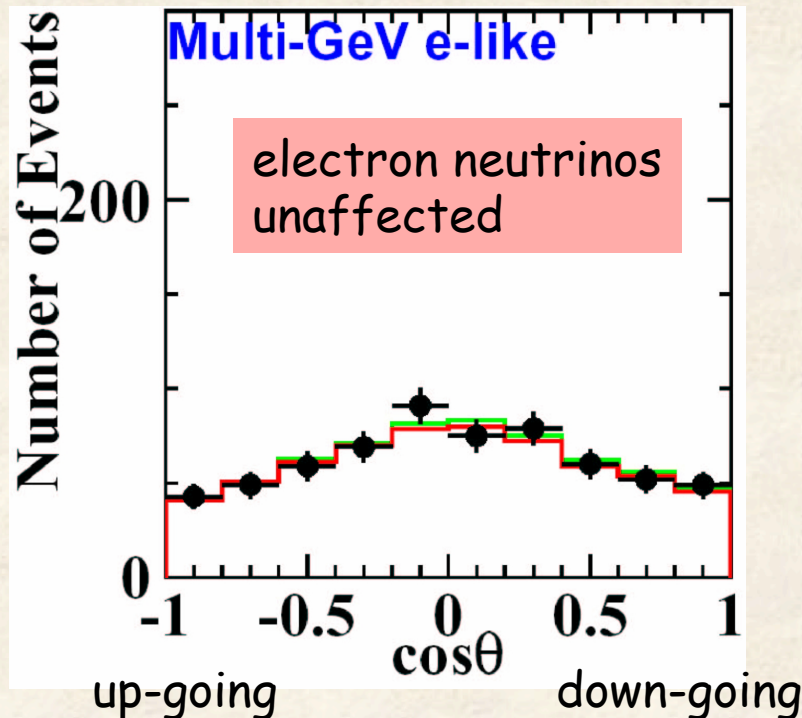


[this year: 10th anniversary]

Electron and muon neutrinos
(and antineutrinos) produced
by the collision of cosmic ray
particles on the atmosphere

Experiment:

SuperKamiokande (Japan)



electron neutrinos do not oscillate

by working in the approximation $\Delta m_{21}^2 = 0$

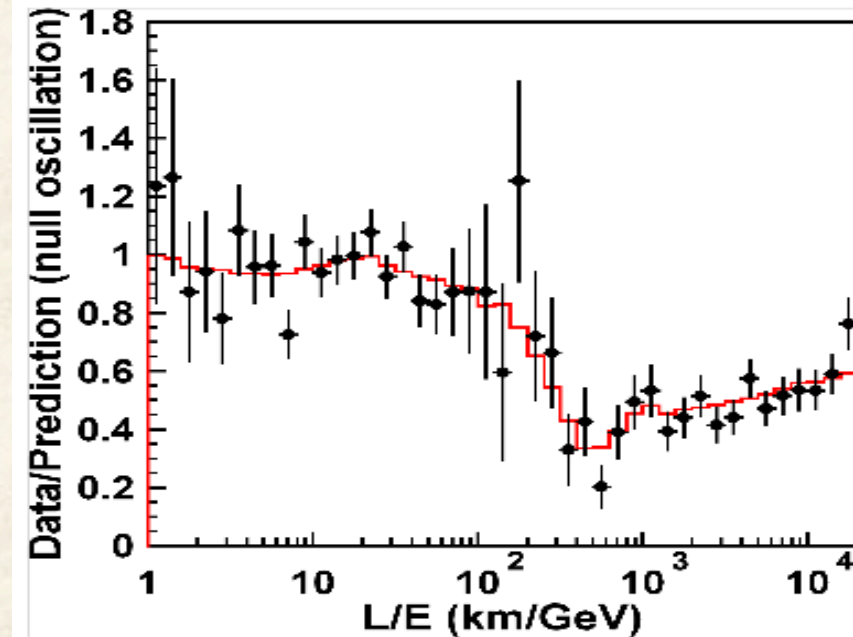
$$P_{ee} = 1 - \underbrace{4|U_{e3}|^2(1-|U_{e3}|^2)}_{\sin^2 2\vartheta_{13}} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right) \approx 1 \quad \text{for } U_{e3} = \sin \vartheta_{13} \approx 0$$

muon neutrinos oscillate

$$P_{\mu\mu} = 1 - \underbrace{4|U_{\mu3}|^2(1-|U_{\mu3}|^2)}_{\sin^2 2\vartheta_{23}} \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right)$$

$$|\Delta m_{32}^2| \approx 2 \cdot 10^{-3} \text{ eV}^2$$

$$\sin^2 \vartheta_{23} \approx \frac{1}{2}$$



$$U_{PMNS} = \begin{pmatrix} \cdot & \cdot & 0 \\ \cdot & \cdot & 1 \\ \cdot & \cdot & -\frac{1}{\sqrt{2}} \\ \cdot & \cdot & 1 \\ & & \frac{1}{\sqrt{2}} \end{pmatrix} + (\text{small corrections})$$

maximal mixing!
not a replica of the quark
mixing pattern

this picture is supported by other terrestrial experiments such as
K2K (Japan, from KEK to Kamioka mine $L \approx 250$ Km $E \approx 1$ GeV)
and **MINOS** (USA, from Fermilab to Soudan mine $L \approx 735$ Km $E \approx 5$ GeV)
that are sensitive to Δm_{32}^2 close to 10^{-3} eV^2 ,

KamLAND

previous experiments were sensitive to Δm^2 close to 10^{-3} eV^2
to explore smaller Δm^2 we need larger L and/or smaller E

KamLAND experiment exploits the low-energy electron anti-neutrinos ($E \approx 3 \text{ MeV}$) produced by Japanese and Korean reactors at an average distance of $L \approx 180 \text{ Km}$ from the detector and is potentially sensitive to Δm^2 down to 10^{-5} eV^2

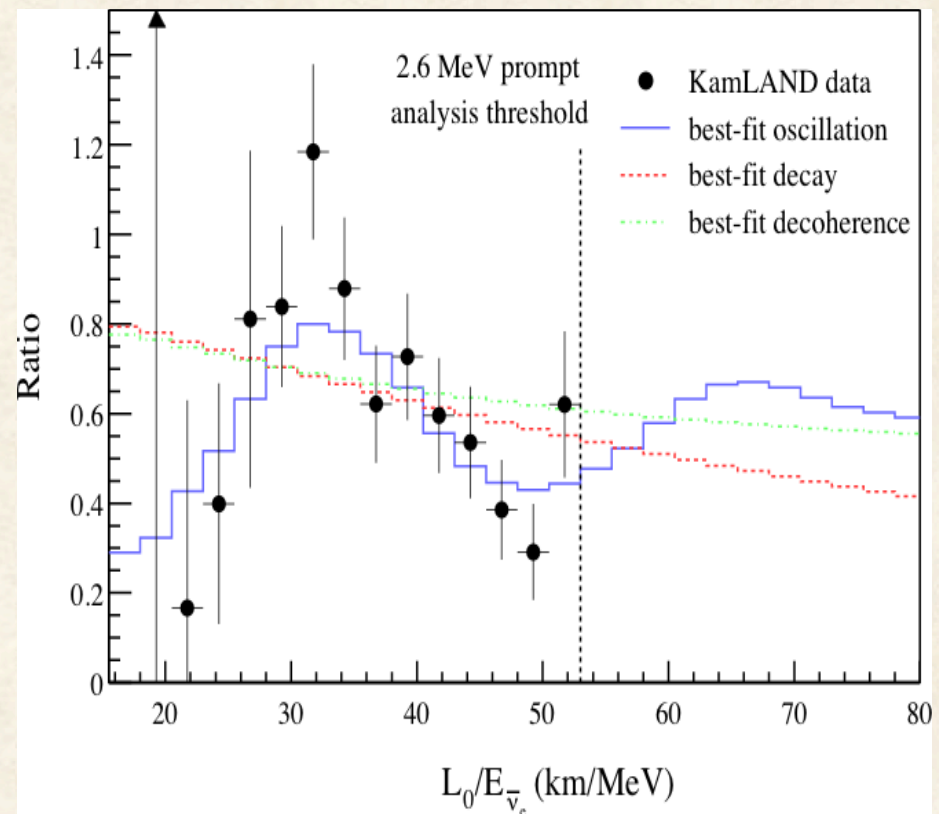
by working in the approximation

$$U_{e3} = \sin \vartheta_{13} = 0 \quad \text{we get}$$

$$P_{ee} = 1 - \underbrace{4|U_{e1}|^2|U_{e2}|^2}_{\sin^2 2\vartheta_{12}} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E} \right)$$

$$\Delta m_{21}^2 \approx 8 \cdot 10^{-5} \text{ eV}^2$$

$$\sin^2 \vartheta_{12} \approx \frac{1}{3}$$



TB mixing from symmetry breaking

it is easy to find a symmetry that forces $(m_e^+ m_e)$ to be diagonal;
a “minimal” example (there are many other possibilities) is

$$G_T = \{1, T, T^2\}$$

$$T = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \omega & 0 \\ 0 & 0 & \omega \end{pmatrix} \quad \omega = e^{i\frac{2\pi}{3}}$$

$[T^3=1]$ and mathematicians call a group with this property Z_3

$$T^+ (m_e^+ m_e) T = (m_e^+ m_e)$$

$$\longrightarrow (m_e^+ m_e) = \begin{pmatrix} m_e^2 & 0 & 0 \\ 0 & m_\mu^2 & 0 \\ 0 & 0 & m_\tau^2 \end{pmatrix}$$

in such a framework TB mixing should arise entirely from m_ν

$$m_\nu(TB) \equiv \frac{m_3}{2} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & -1 \\ 0 & -1 & 1 \end{pmatrix} + \frac{m_2}{3} \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} + \frac{m_1}{6} \begin{pmatrix} 4 & -2 & -2 \\ -2 & 1 & 1 \\ -2 & 1 & 1 \end{pmatrix}$$

most general neutrino mass matrix giving rise to TB mixing

easy to construct from the eigenvectors:

$$m_3 \leftrightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ -1 \\ 1 \end{pmatrix} \quad m_2 \leftrightarrow \frac{1}{\sqrt{3}} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \quad m_1 \leftrightarrow \frac{1}{\sqrt{6}} \begin{pmatrix} 2 \\ -1 \\ -1 \end{pmatrix}$$

a “minimal” symmetry guaranteeing such a pattern [C.S. Lam 0804.2622]

$$G_S \times G_U \quad G_S = \{1, S\} \quad G_U = \{1, U\}$$

[this group corresponds to $Z_2 \times Z_2$ since $S^2 = U^2 = 1$]

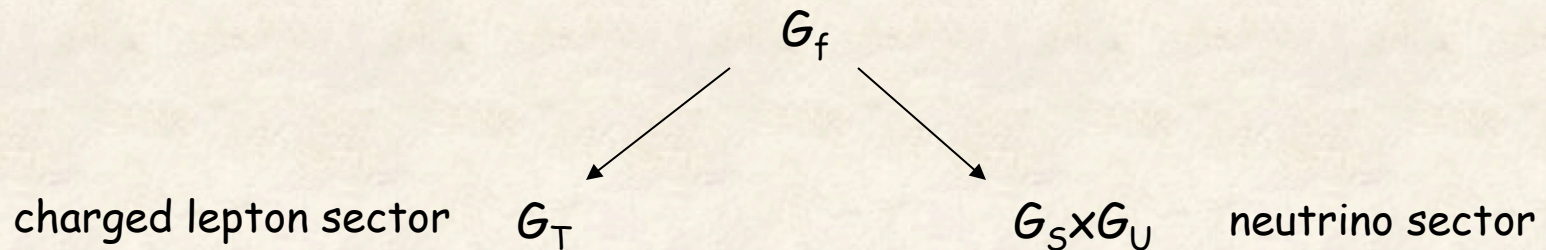
$$S = \frac{1}{3} \begin{pmatrix} -1 & 2 & 2 \\ 2 & -1 & 2 \\ 2 & 2 & -1 \end{pmatrix} \quad U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$$

$$S^T m_\nu S = m_\nu \quad U^T m_\nu U = m_\nu \quad \longrightarrow \quad m_\nu = m_\nu(TB)$$

Algorithm to generate TB mixing

start from a flavour symmetry group G_f containing G_T, G_S, G_U

arrange appropriate symmetry breaking



if the breaking is **spontaneous**, induced by $\langle \varphi_T \rangle, \langle \varphi_S \rangle, \dots$ there is a **vacuum alignment problem**

$\sin^2 \theta_{23}$

$\delta(\sin^2 \theta_{23})$ reduced by future LBL experiments
from $\nu_{\mu} \rightarrow \nu_{\mu}$ disappearance channel

$$P_{\mu\mu} \approx 1 - \sin^2 2\vartheta_{23} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right)$$

$$\vartheta_{23} \approx \frac{\pi}{4}$$



$$\delta\vartheta_{23} \approx \frac{\sqrt{\delta P_{\mu\mu}}}{2}$$

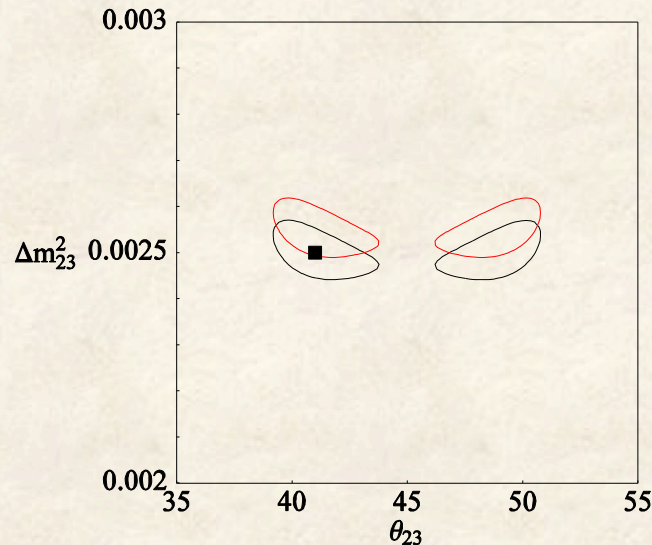
i.e. a small uncertainty
on $P_{\mu\mu}$ leads to a large
uncertainty on θ_{23}

- no substantial improvements from conventional beams
- superbeams (e.g. T2K in 5 yr of run)

$$\delta P_{\mu\mu} \approx 0.01$$

$$\delta\vartheta_{23} \approx 0.05 \text{ rad} \leftrightarrow 2.9^\circ$$

improvement by
about a factor 2



T2K-1
90% CL
black = normal hierarchy
red = inverted hierarchy
true value 41°
[courtesy by
Enrique Fernandez]

