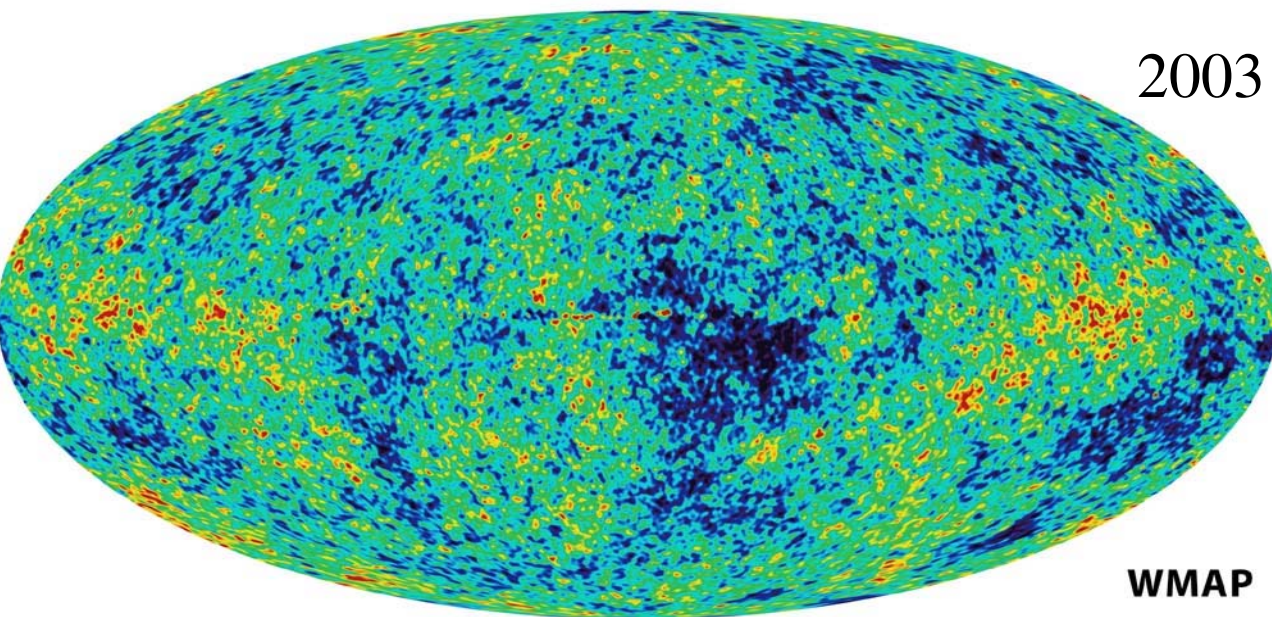


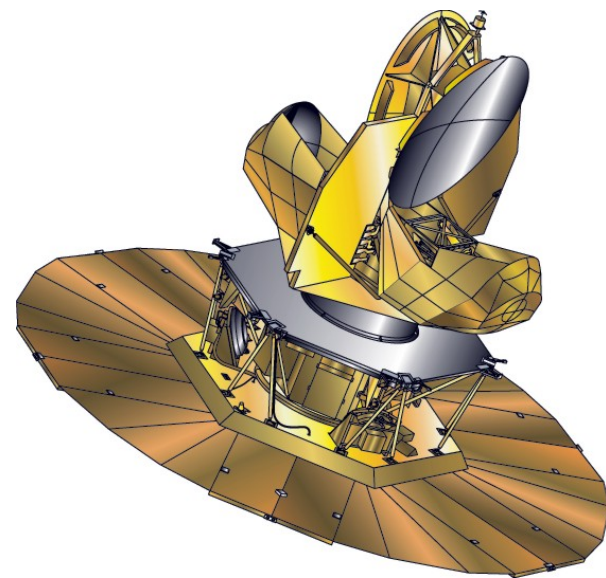
1992

COBE



2003

WMAP



<http://map.gsfc.nasa.gov>

CMB
 γ

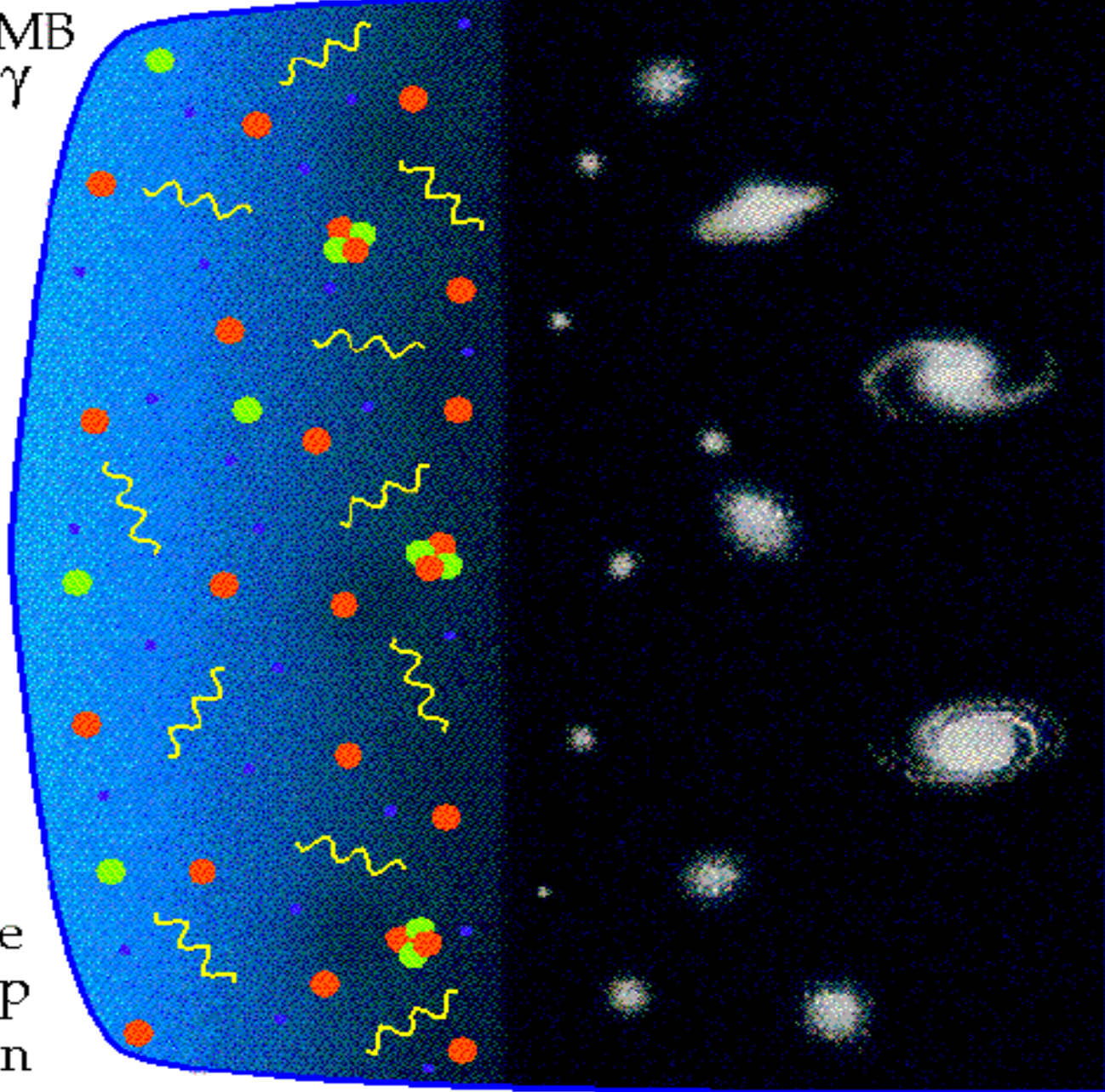
e
p
n
He

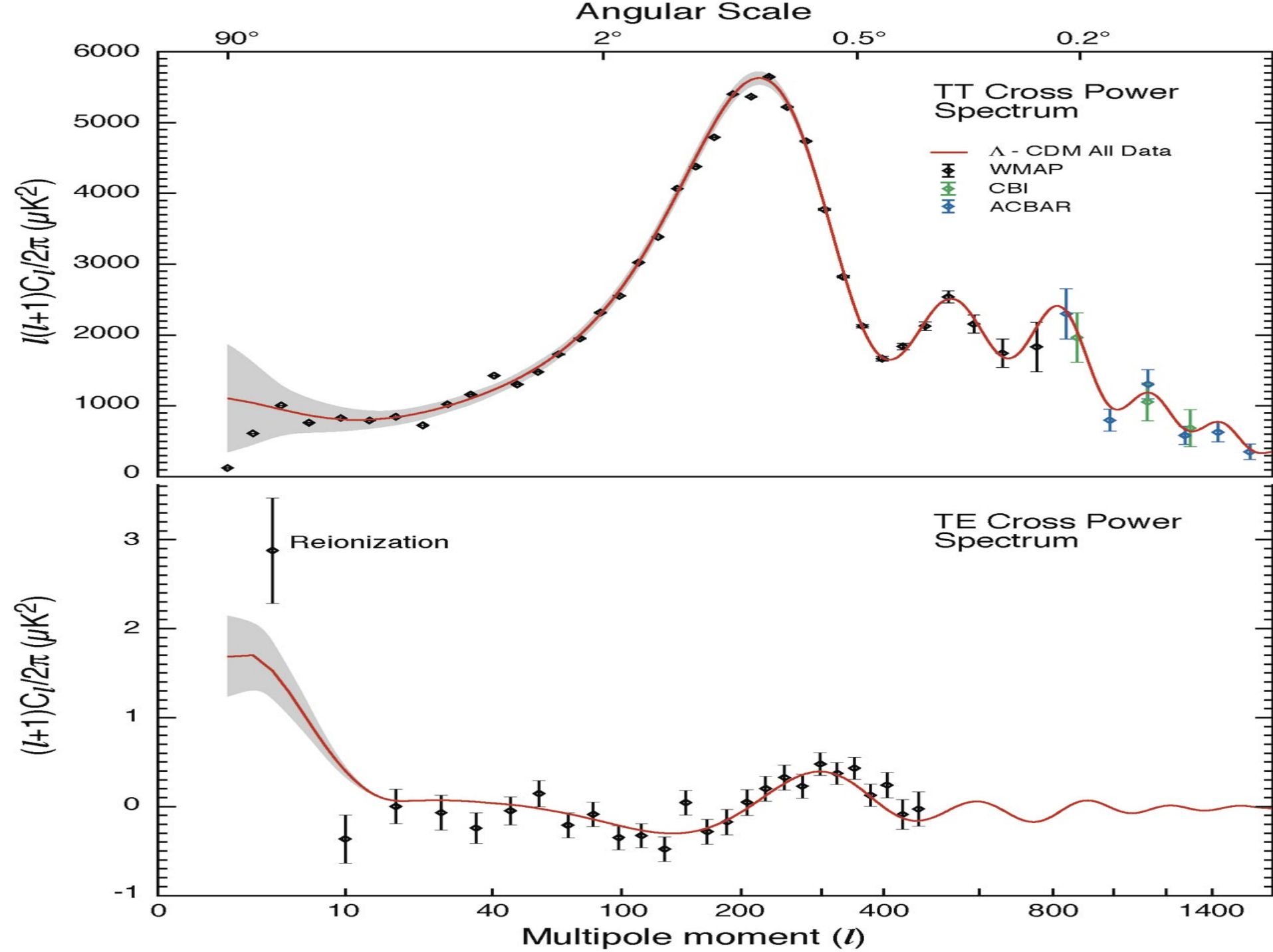
Nucleo-
Synthesis

Last
Scattering

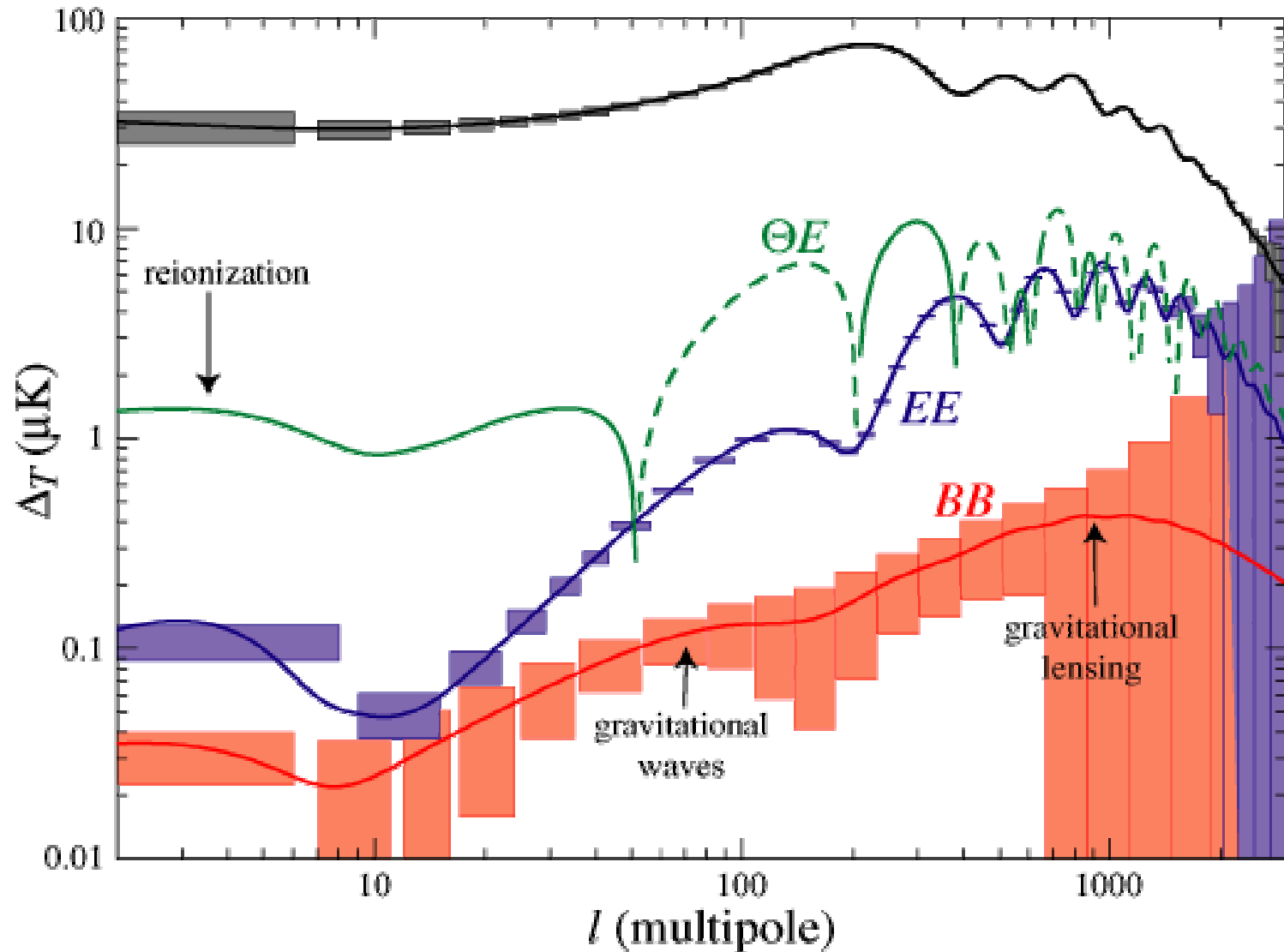
Galaxy
Formation

(Hu)

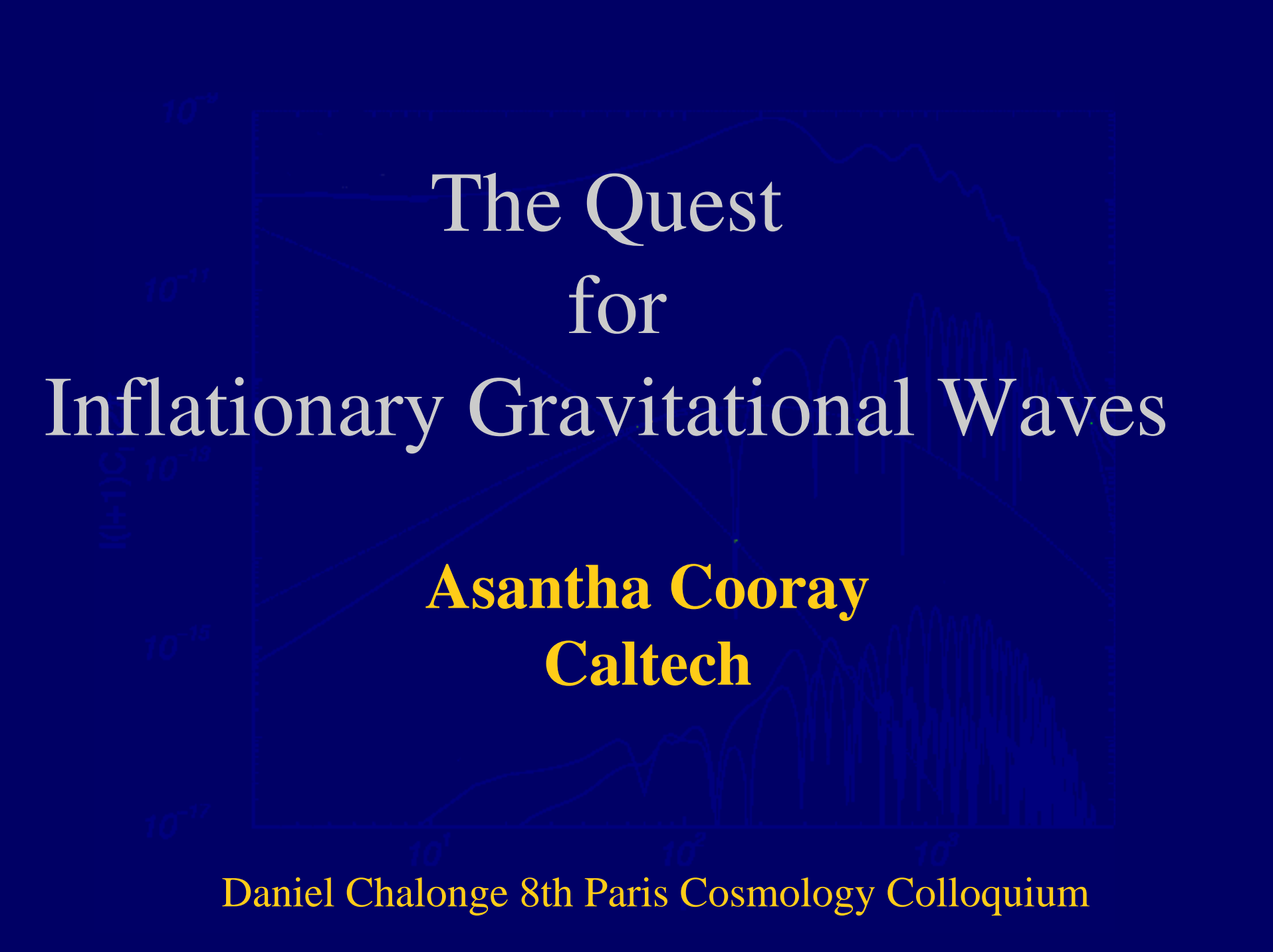




Around ~ 2009 , with Planck (ESA mission)



Hu & Dodelson (Annual Reviews 2002)

The background of the slide features a log-log plot of the inflationary power spectrum. The vertical axis is labeled $l(l+1)C_l$ and ranges from 10^{-17} to 10^{-9} . The horizontal axis represents the multipole moment l and ranges from 10^1 to 10^3 . The plot shows several curves: a solid line with a broad peak around $l \approx 200$, a dashed line with a similar peak, and a series of highly oscillatory lines at higher l values. The title text is overlaid on the upper portion of this plot.

The Quest for Inflationary Gravitational Waves

Asantha Cooray
Caltech

Daniel Chalonge 8th Paris Cosmology Colloquium

The Quest for Inflationary Gravitational Waves

Goal: Determine the energy scale of inflation and other inflationary physics

- CMB Polarization
- Space-Based Gravitational Wave Detectors

(foreground confusions, ultimate limits and where we are going experimentally)

Collaborators: Mark Kamionkowski, Mike Kesden,
Naoki Seto, Tristan Smith (Caltech)

What do we already know?

Presence of harmonic oscillations: coherence of initial fluctuations

Strong evidence for inflation!!!

What do we already know?

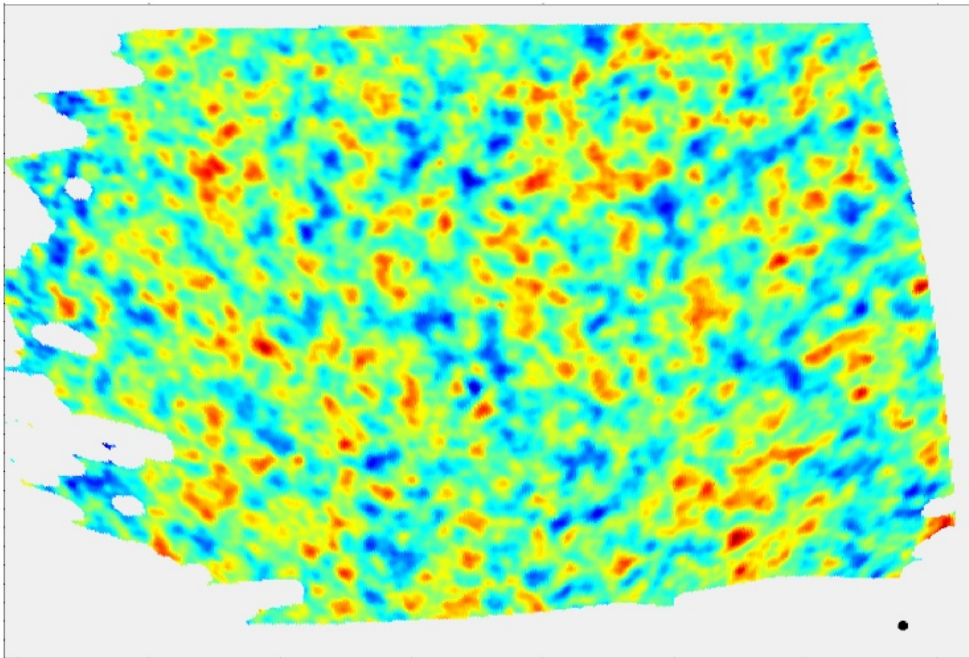
Presence of harmonic oscillations: coherence of initial fluctuations

Strong evidence for inflation!!!

(initial fluctuations: “nearly” scale invariant, adiabatic, Gaussian)

Adiabaticity \Rightarrow fluctuations in pressure are proportional to the density (essentially, particles trace the density field).

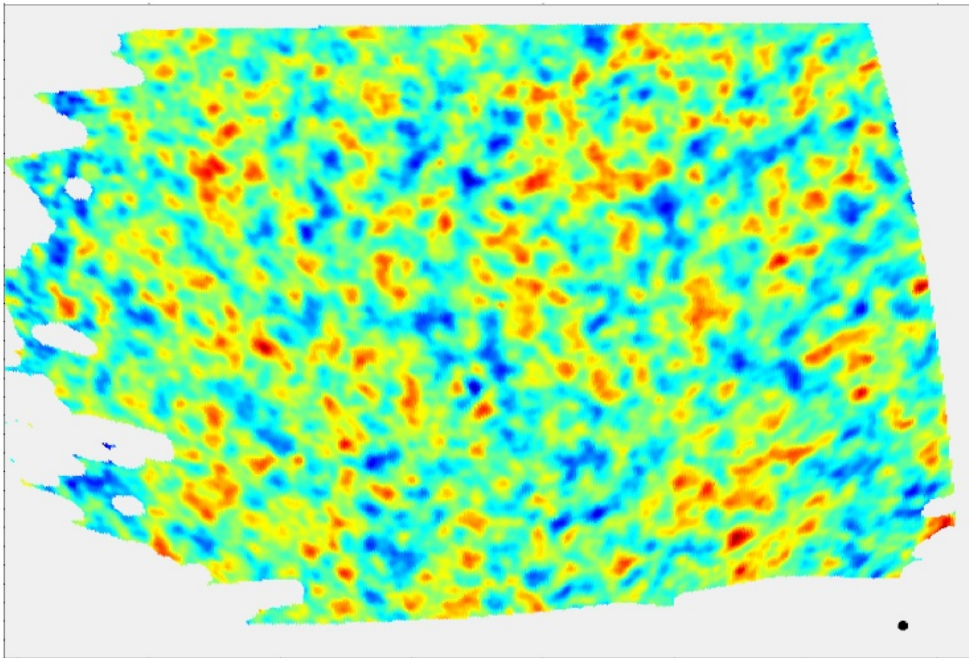
-300 μK -300 -200 -100 0 100 200 300 μK



Highly *coherent* fluctuations

-> preferred size scale
(fluctuations start at the same time)

−300 μK −300 −200 −100 0 100 200 300 μK

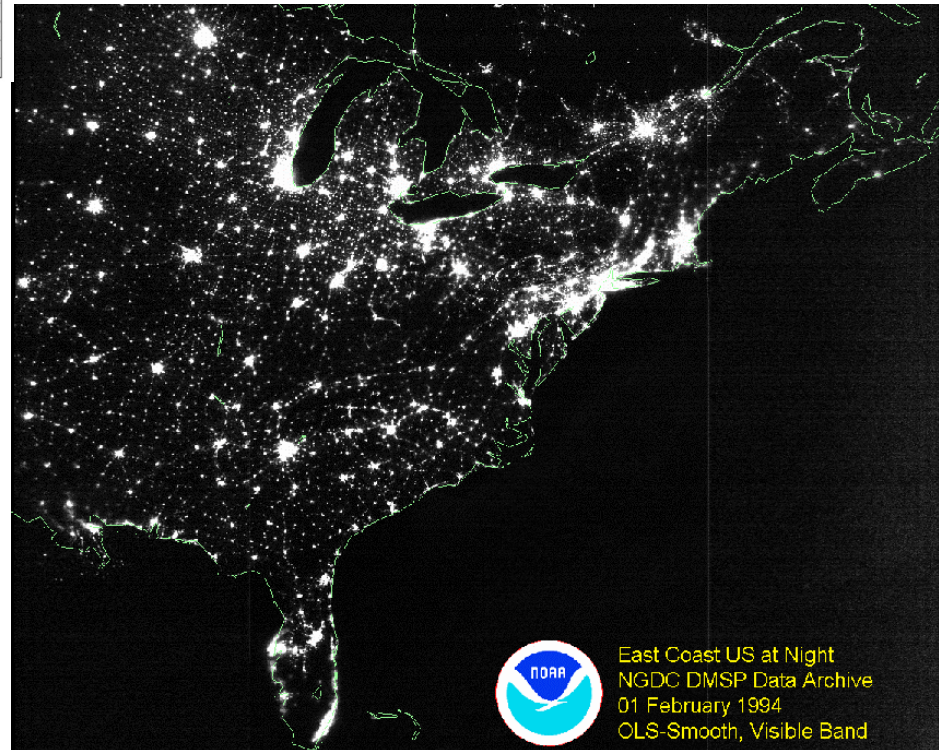


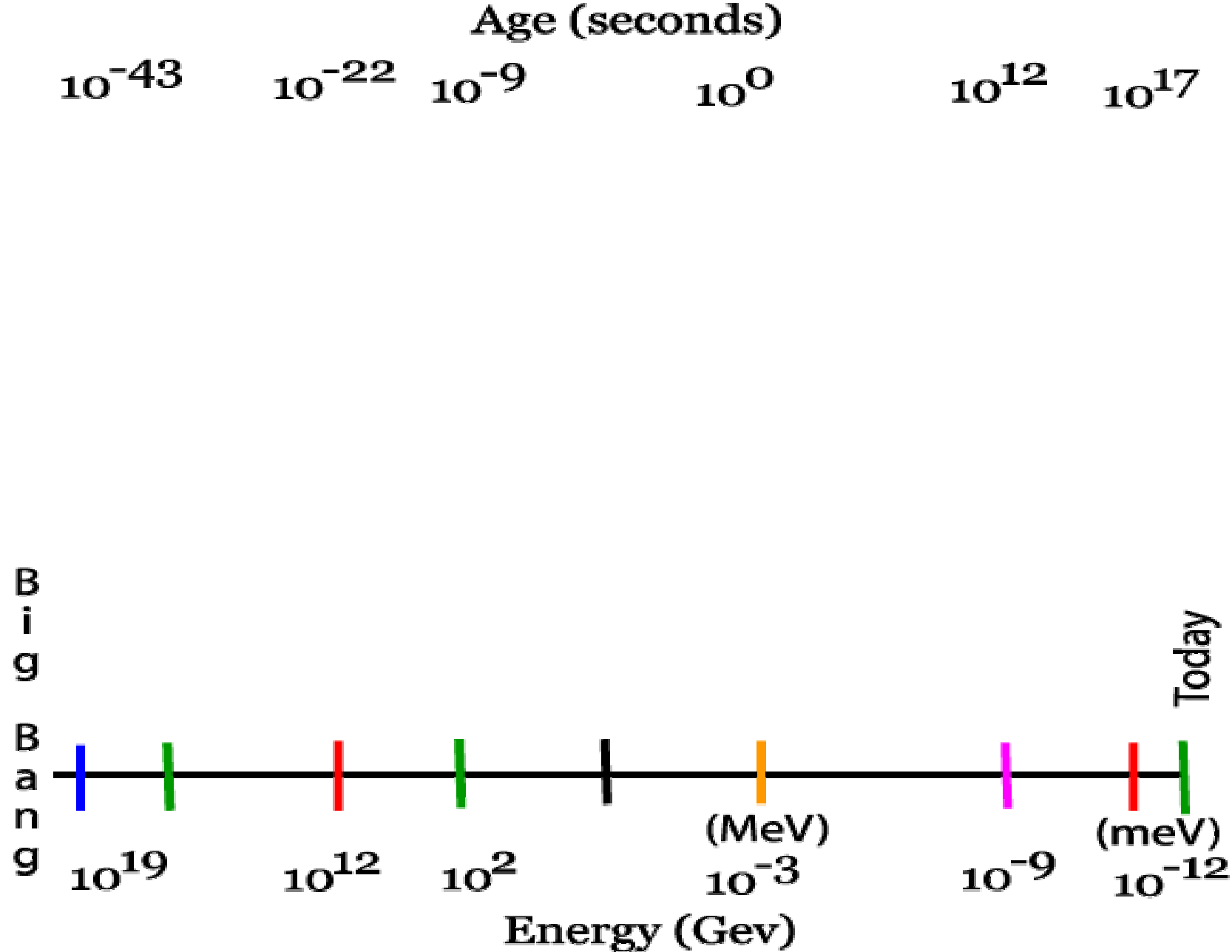
Highly *coherent* fluctuations

-> preferred size scale
(fluctuations start at the same time)

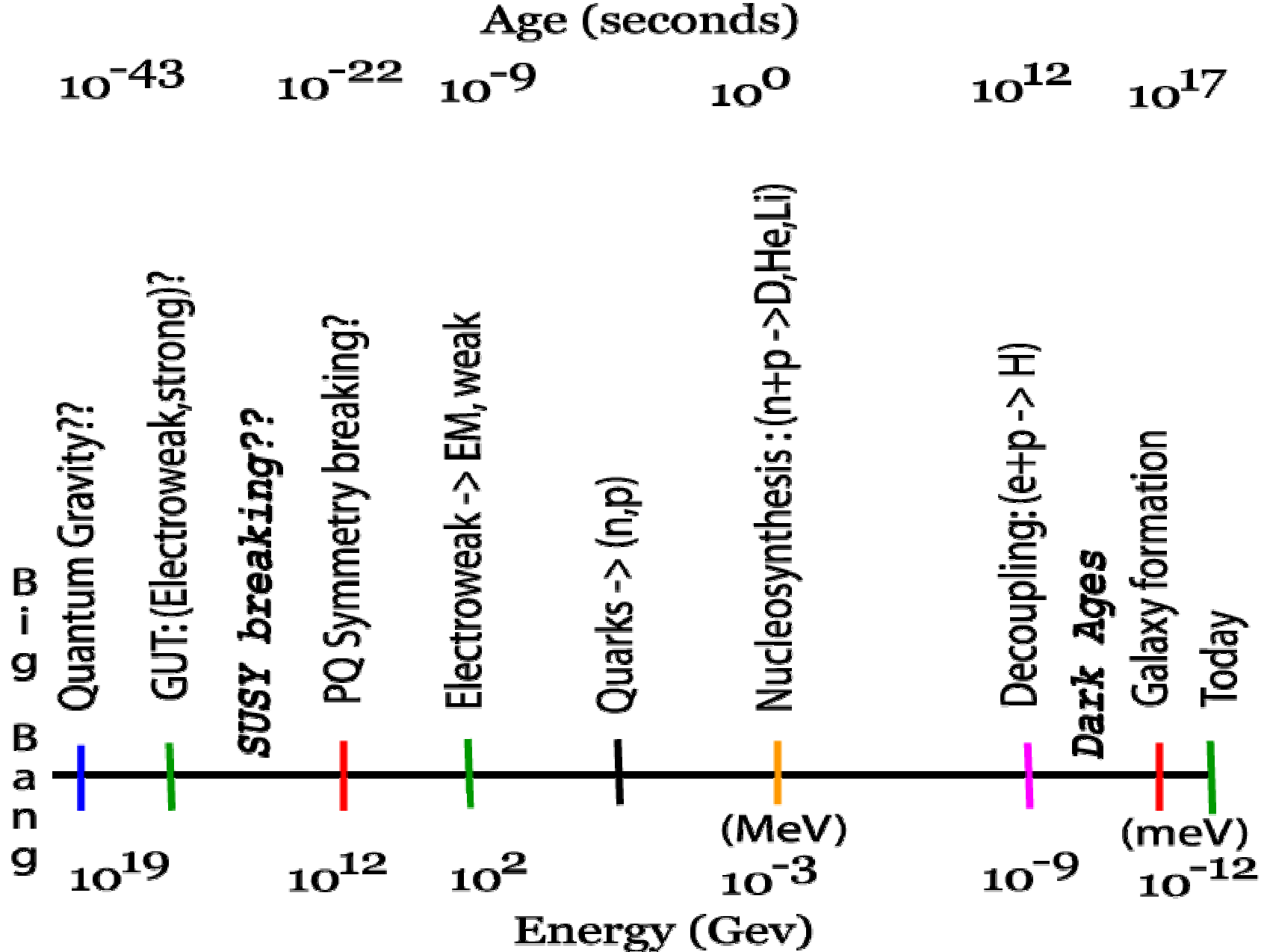
Highly *incoherent* fluctuations

-> fluctuations have varying sizes
(power-law: bigger things get
bigger)
(fluctuations start at different times)

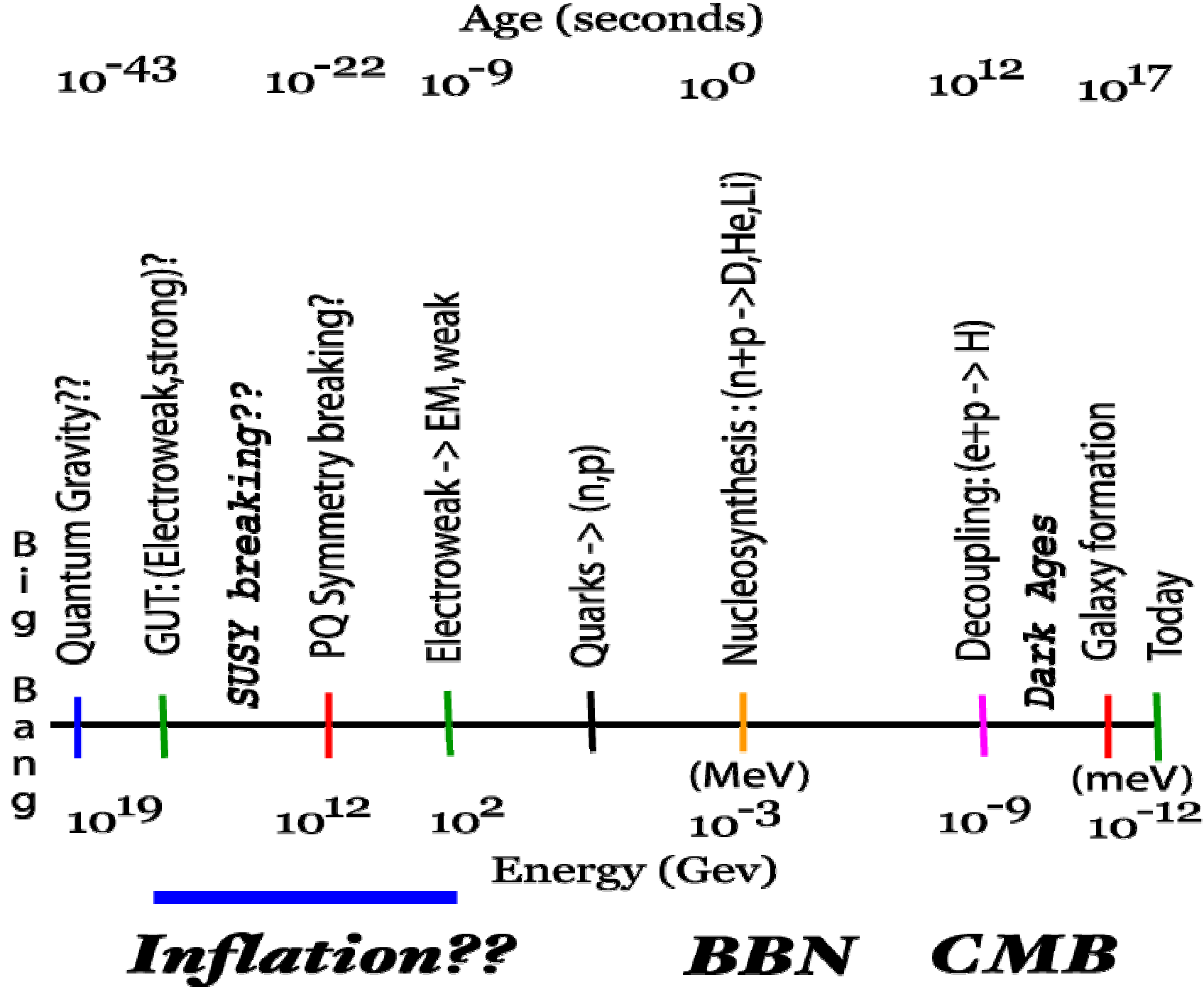




Cosmic Time Line



Cosmic Time Line



Evidence for Inflation

Geometry

Smoothness

*Structure
Formation*

When did inflation happen?

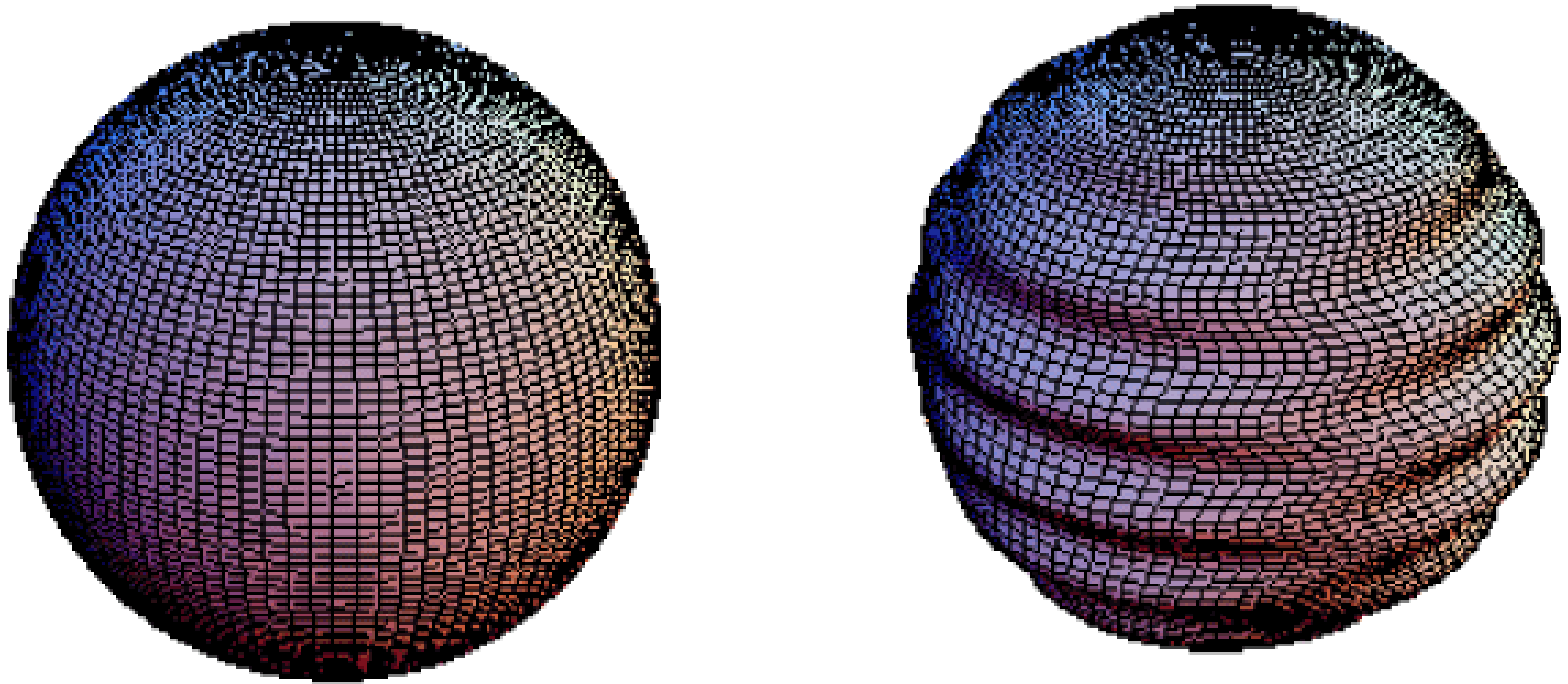
A natural prediction:

A stochastic background of gravitational waves

$$A_{IGW} \propto E_{\text{inflation}}^2$$

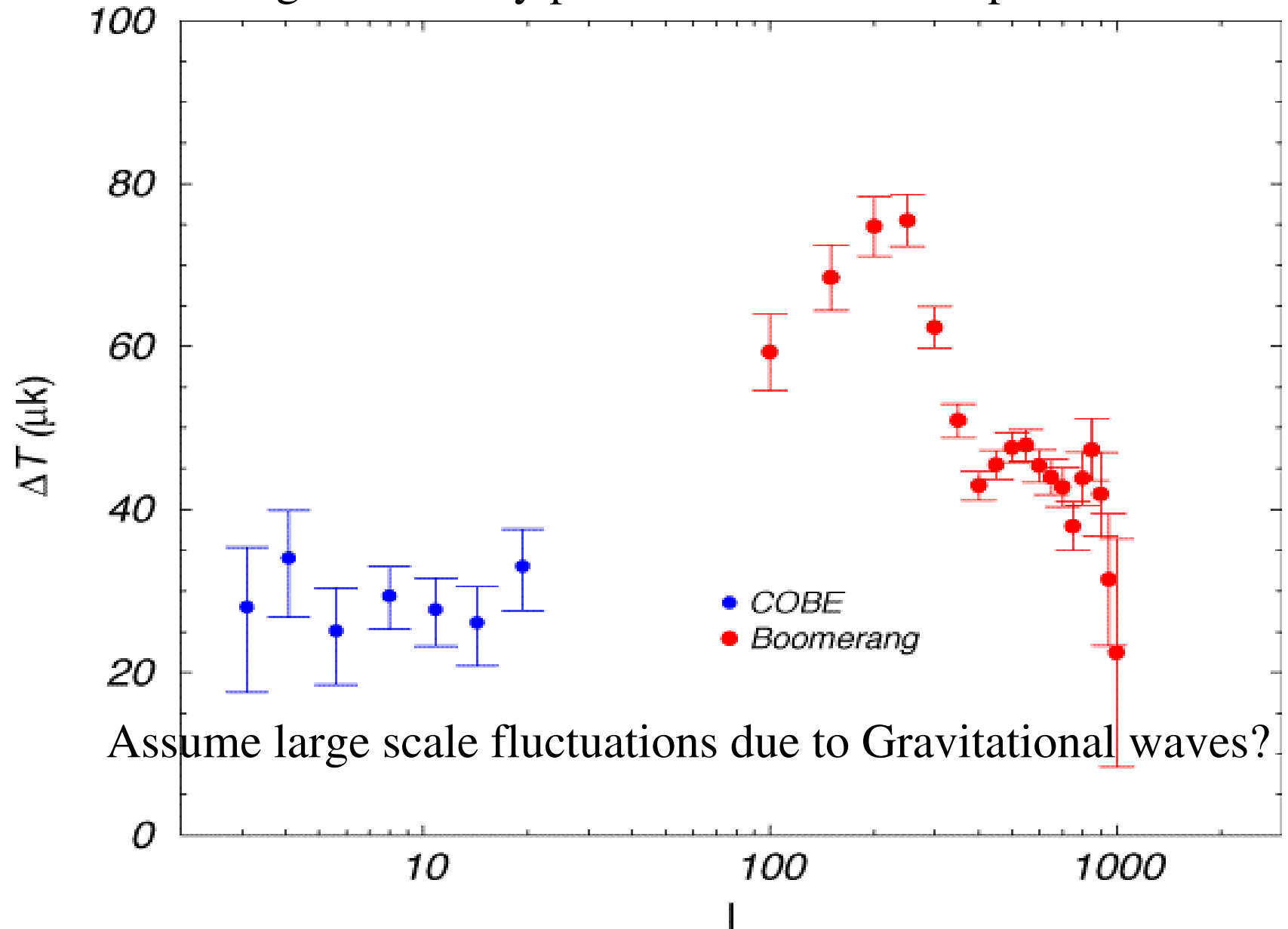
(This is in addition to dominant density perturbations)

Detection of ultralongwavelength GWs from inflation: use plasma at CMB surface of last scatter as sphere of test masses.

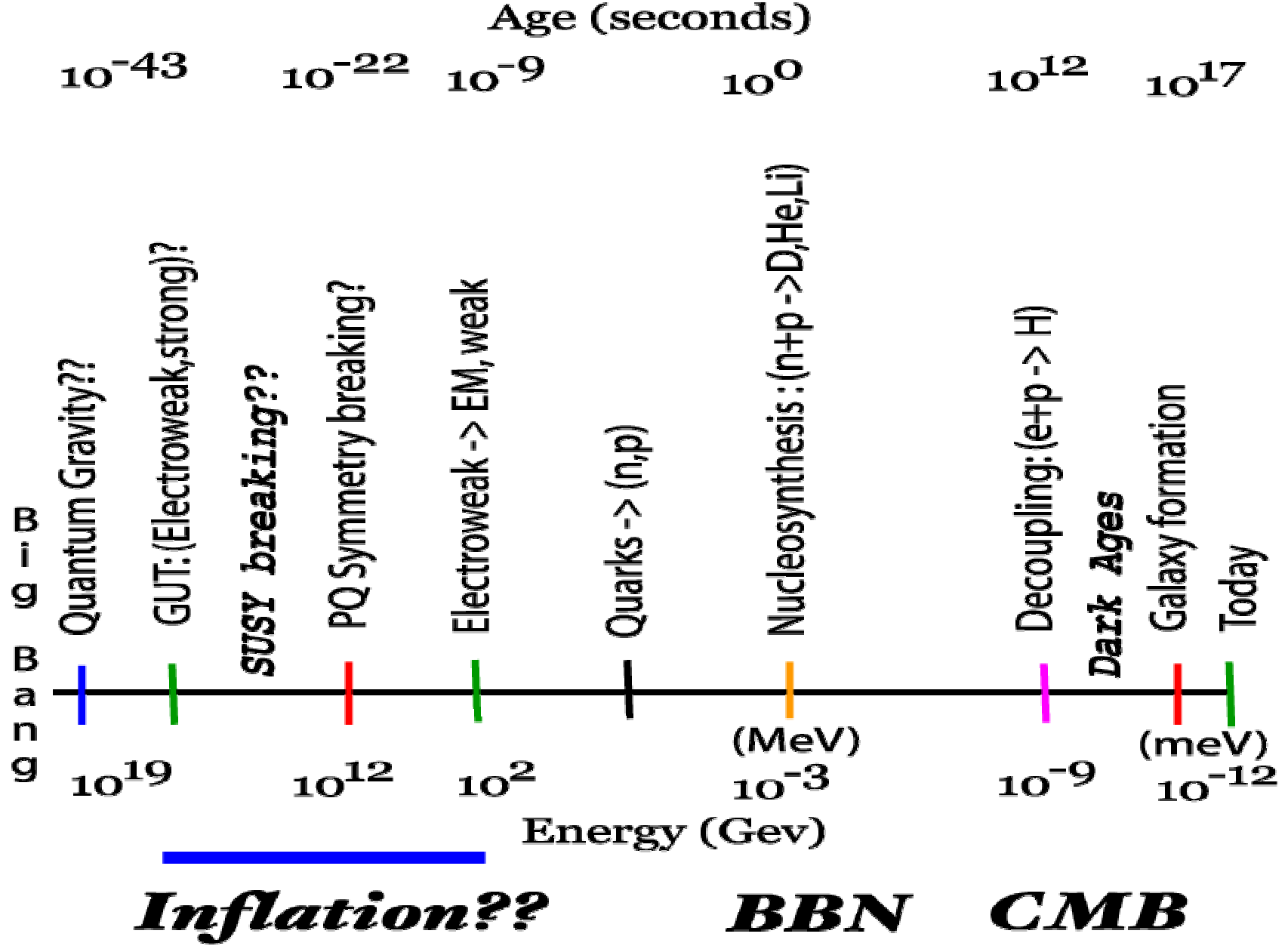


Kamionkowski & Caldwell; Scientific American 2000

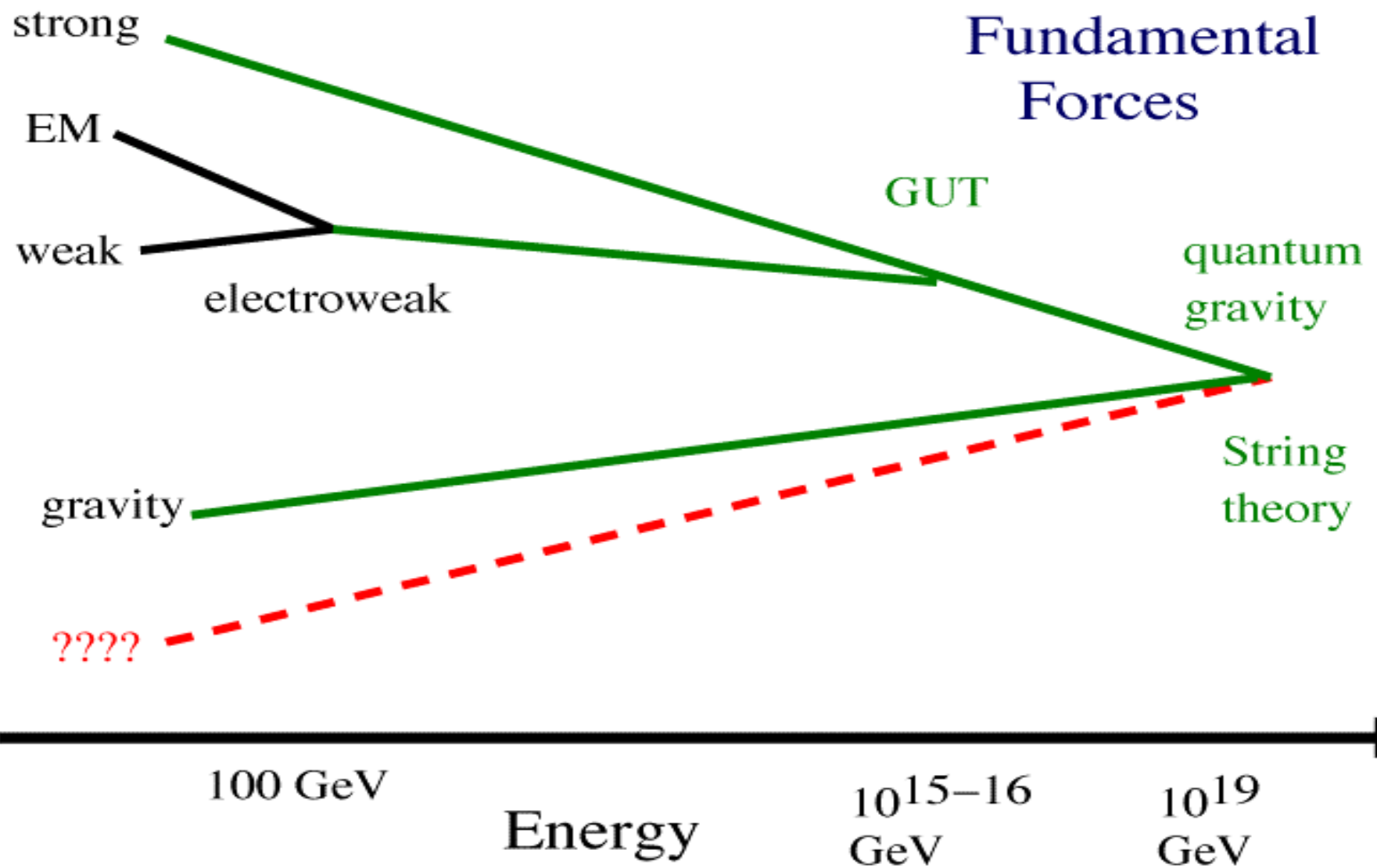
A limit on the GW contribution:
ignore density perturbations/acoustic peaks



Assume large scale fluctuations due to Gravitational waves?

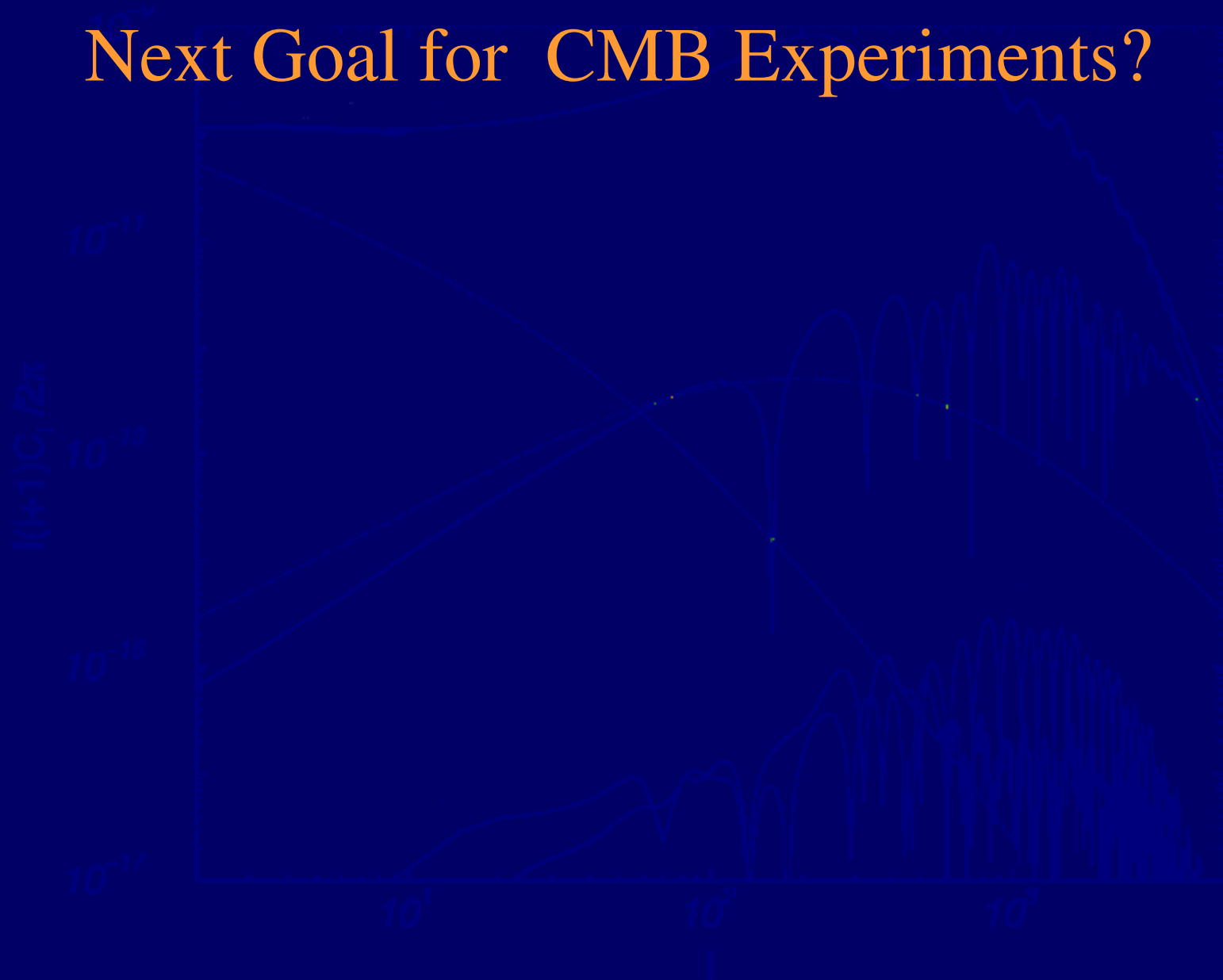


Present limit: $E(\text{Inflation}) < 3 \times 10^{16} \text{ GeV}$



Present limit: $E(\text{infl}) < 3 \times 10^{16}$ GeV

Next Goal for CMB Experiments?



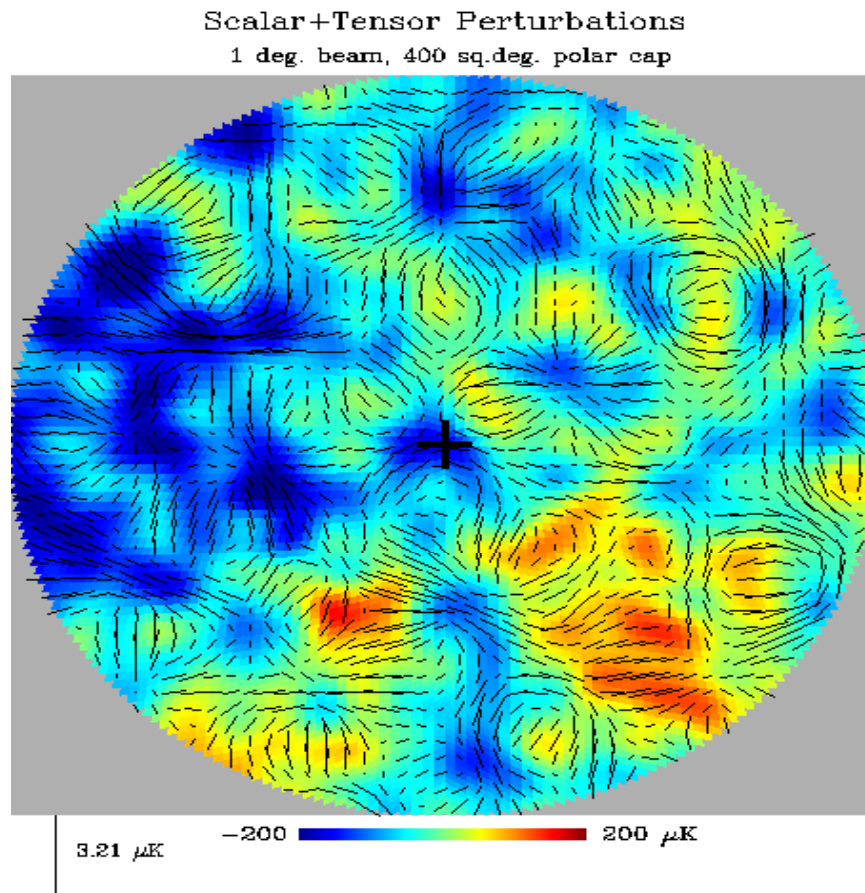
Next Goal for CMB Experiments?

I. Determine the energy scale of inflation

- CMB Polarization
- The role of confusions: weak lensing
- With confusions partly removed

CMB Polarization

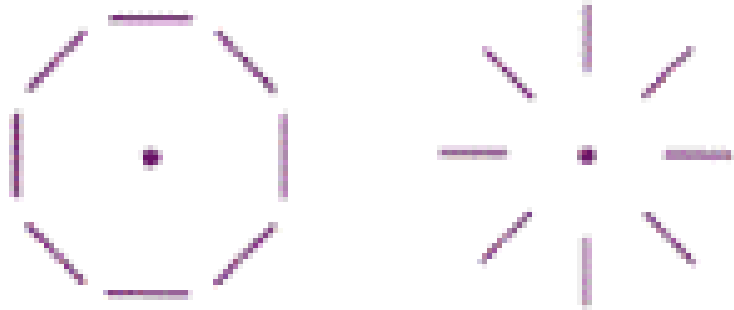
- Polarization is described by Stokes-Q and -U
- These are coordinate dependent
- The two dimensional field is described by a gradient of a scalar (E) or curl of a pseudo-scalar (B).



CMB Polarization

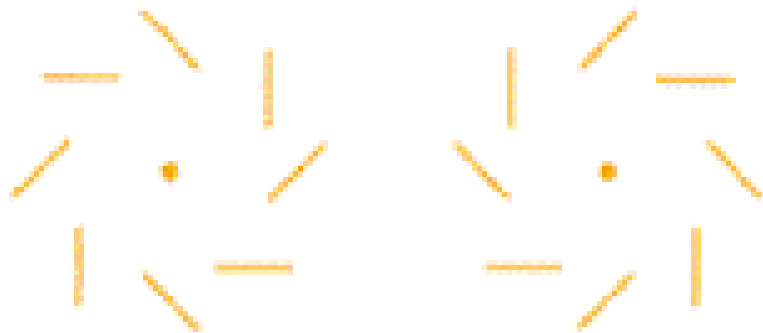
- Polarization is described by Stokes-Q and -U
- These are coordinate dependent
- The two dimensional field is described by a gradient of a scalar (E) or curl of a pseudo-scalar (B).

Grad (or E) modes



Temperature map $T(\hat{n})$

Polarization map $P(\hat{n}) = \vec{\nabla} E + \vec{\nabla} \times \vec{B}$



(density fluctuations have no
handedness, so no contribution
to B-modes)

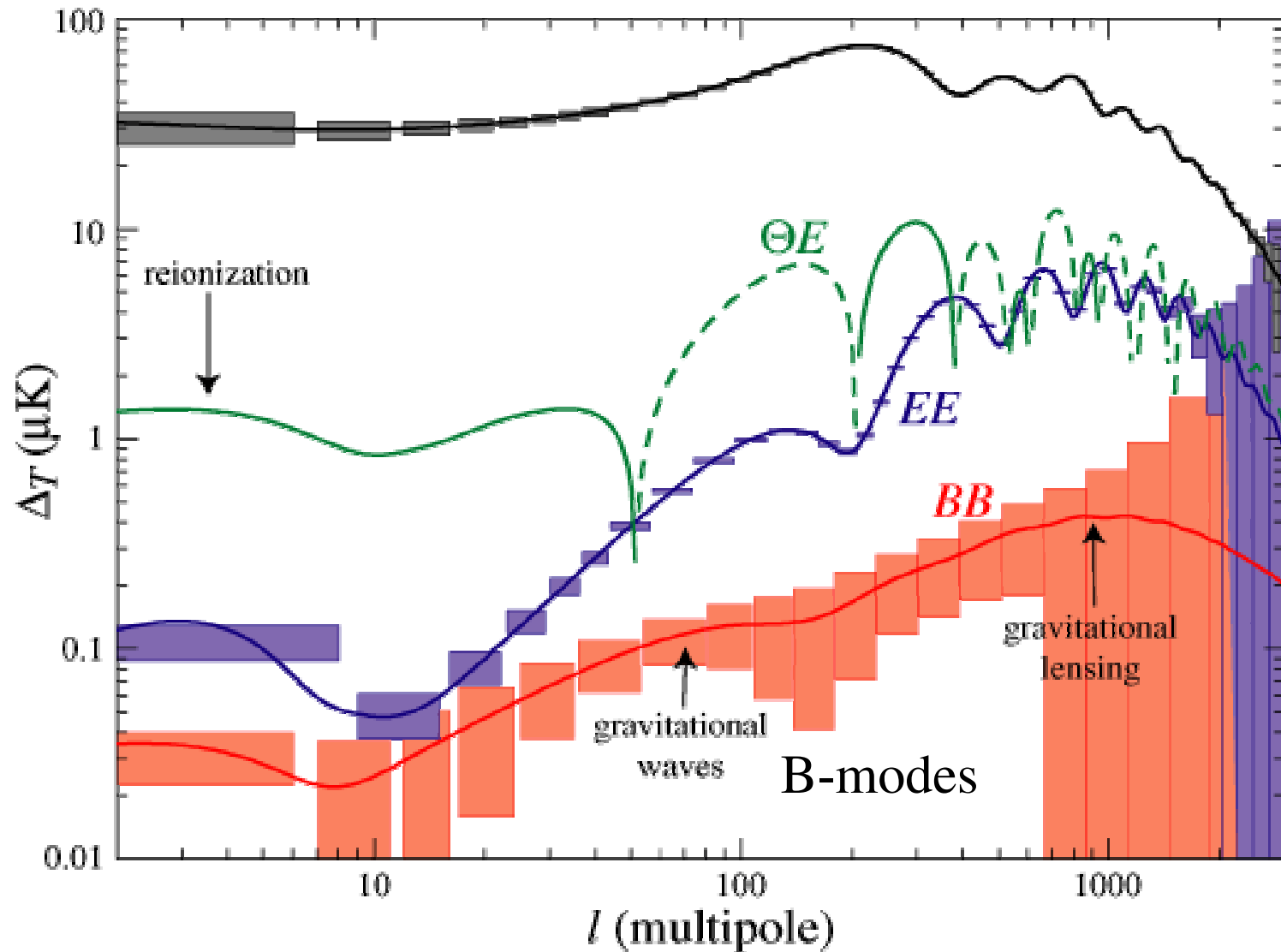
Curl (or B) modes

Kamionkowski et al. 1997;
Seljak & Zaldarriaga 1997

Gravitational-waves

- Inflation predicts tensor perturbations due to primordial gravity waves
- Hard to detect with temperature information alone
(contribute to large angle anisotropies, dominated by cosmic variance)
- **Distinct signature in polarization**
(in terms of curl, or magnetic-like, modes)

EE \rightarrow BB confusions

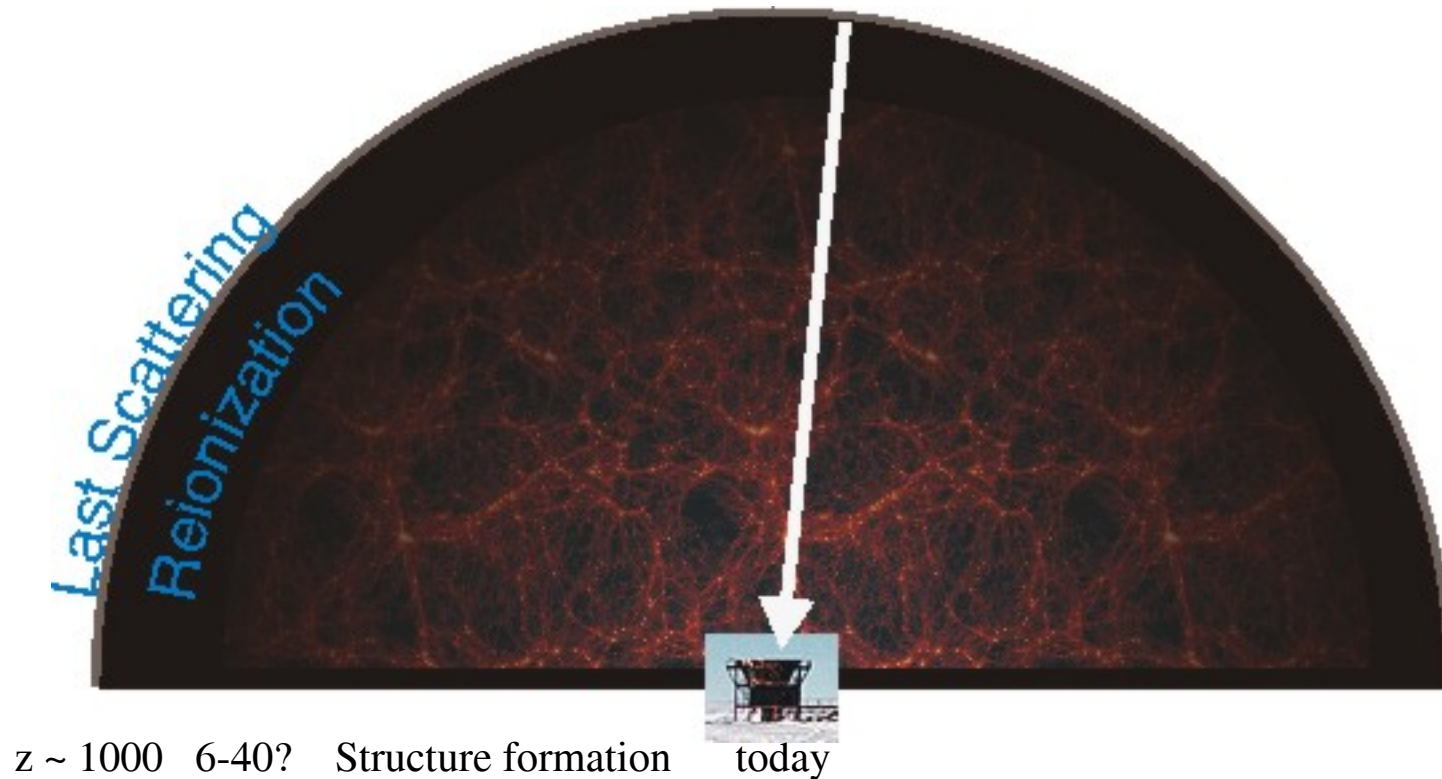


What else can we do with CMB?

I. Determine the energy scale of inflation

- CMB Polarization
- The role of confusions: weak lensing
- With confusions partly removed

Why confusions?

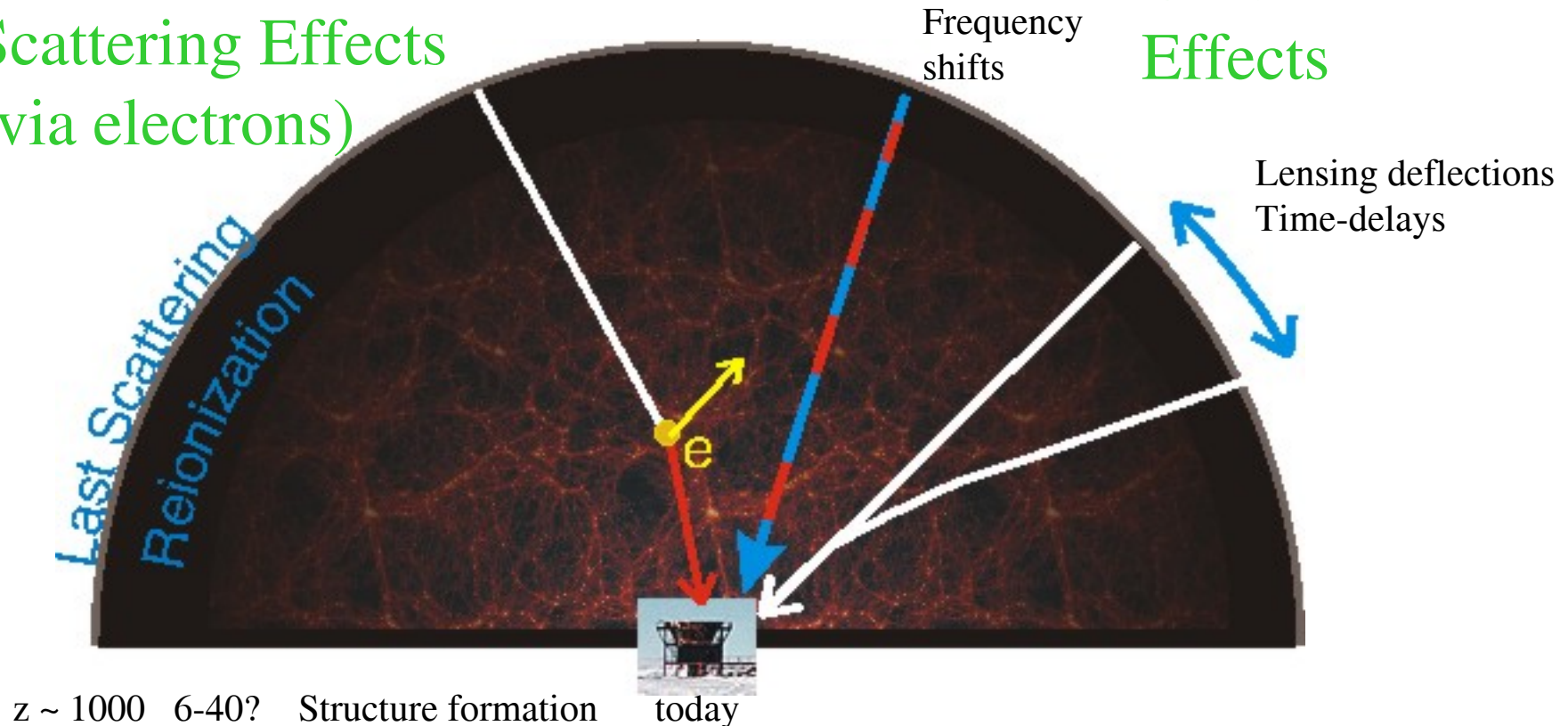


- We are collecting photons from the last scattering surface

Why confusions?

Scattering Effects
(via electrons)

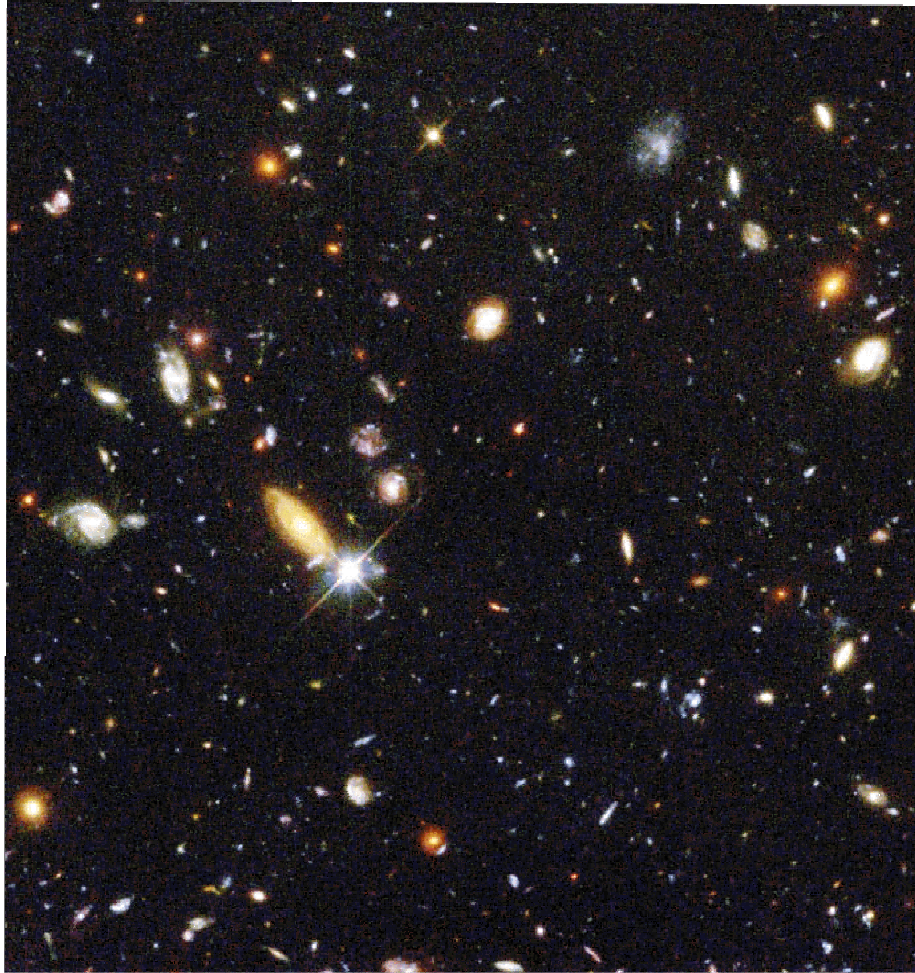
Gravitational
Effects



- *late-time universe: non-linear physics*. Large scale structure modifies CMB properties

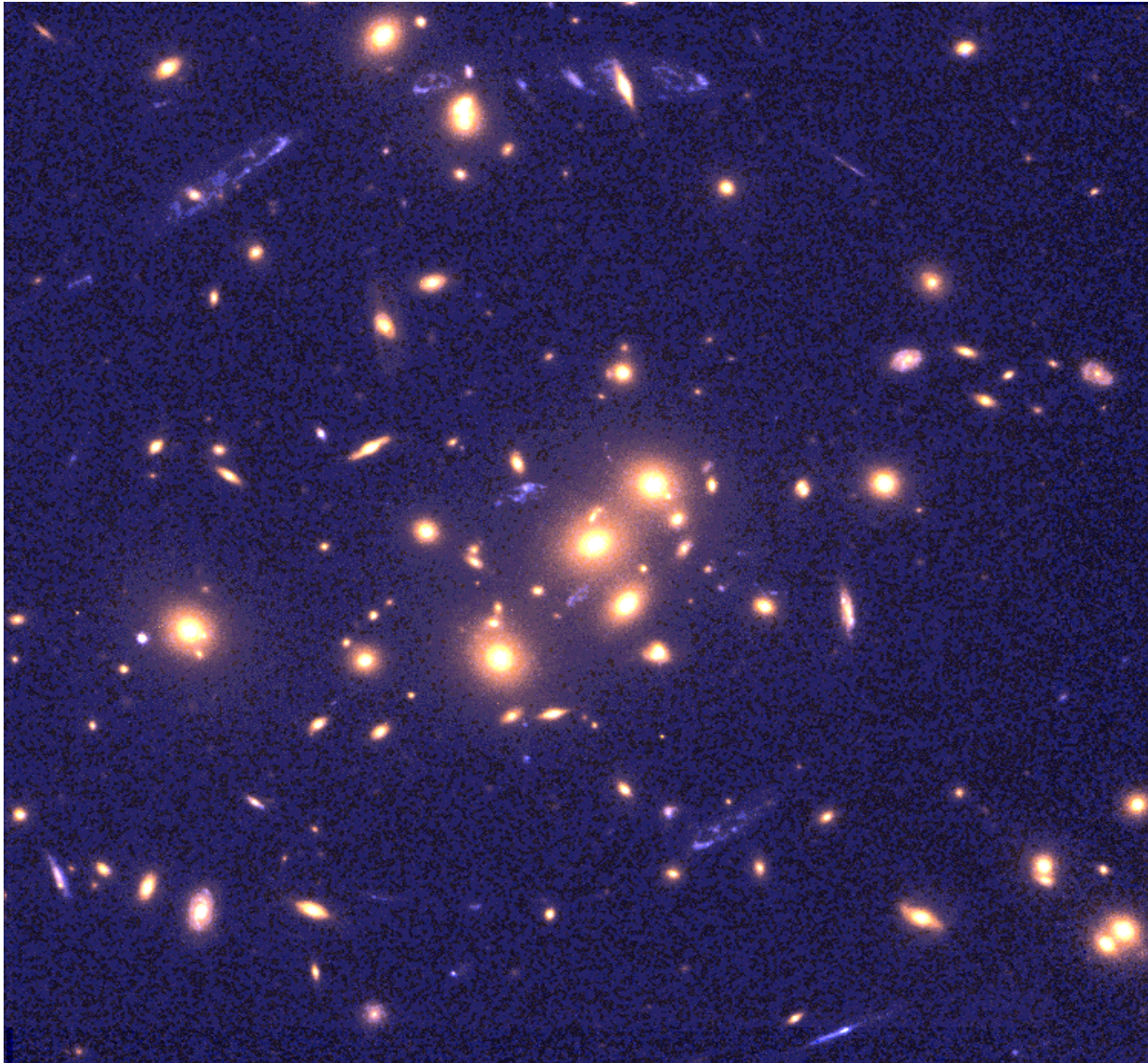
For B-modes, lensing effect is the main concern!!

Gravitational Lensing



GIF decompressor
are needed to see this picture.

Gravitational Lensing



Gravitational Effects

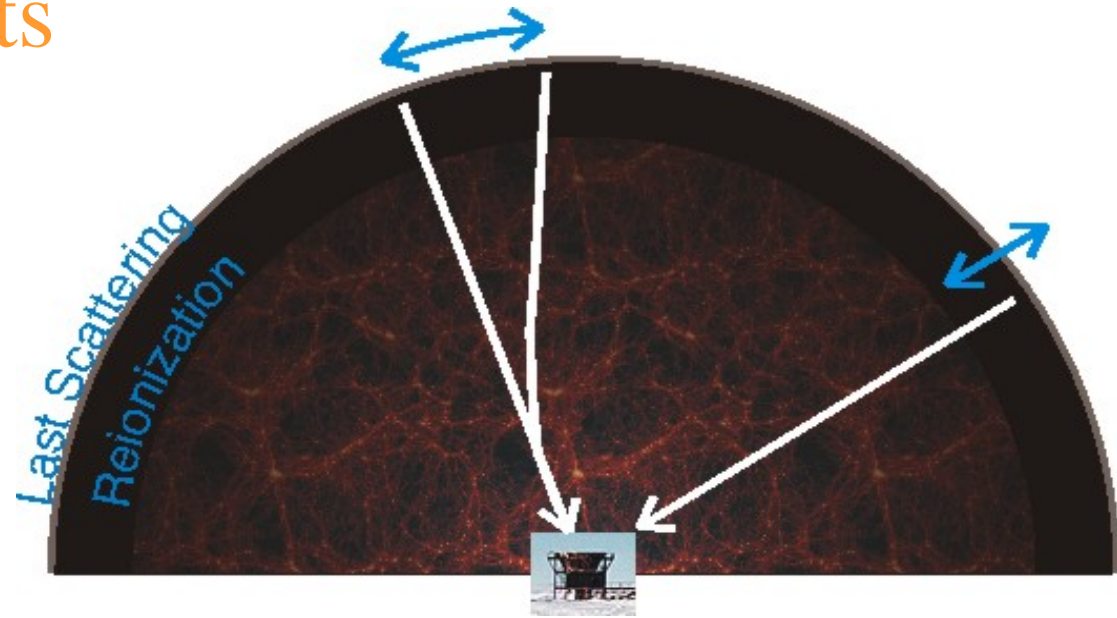
Lensing and time-delay

- Geometric effect

⇒ Angular deflection of
Photons

- Potential effect

⇒ Time delay of photons



Two effects combined lead
to the Fermat potential

(Hu & Cooray 2000)

Gravitational Effects

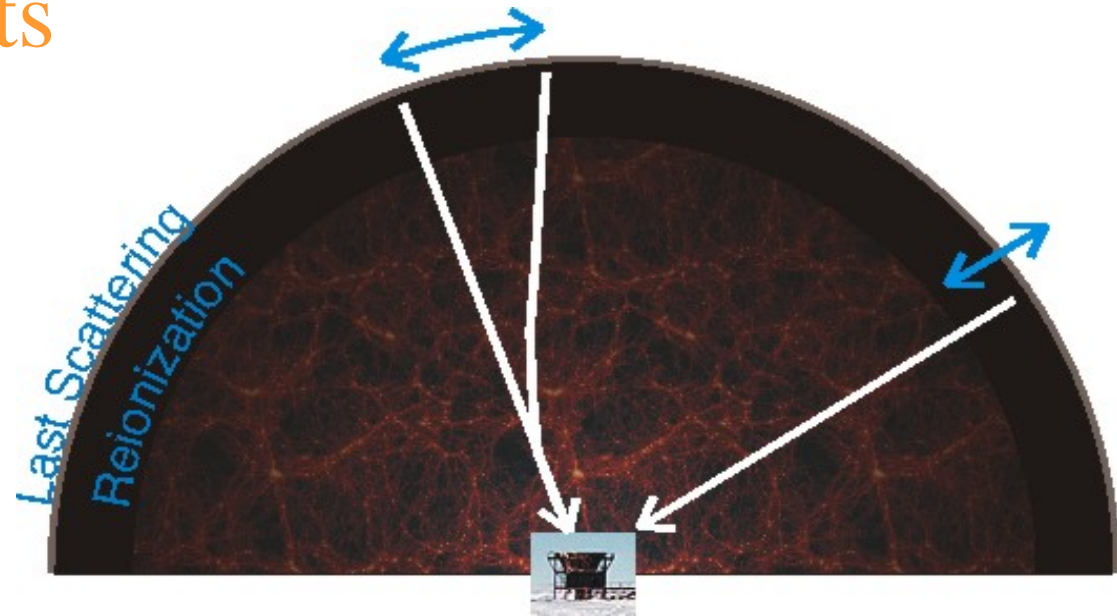
Lensing and time-delay

- Geometric effect

⇒ Angular deflection of Photons

- Potential effect

⇒ Time delay of photons



$$T(\bar{\theta}) \equiv T(\bar{\theta} + \delta\bar{\theta})$$

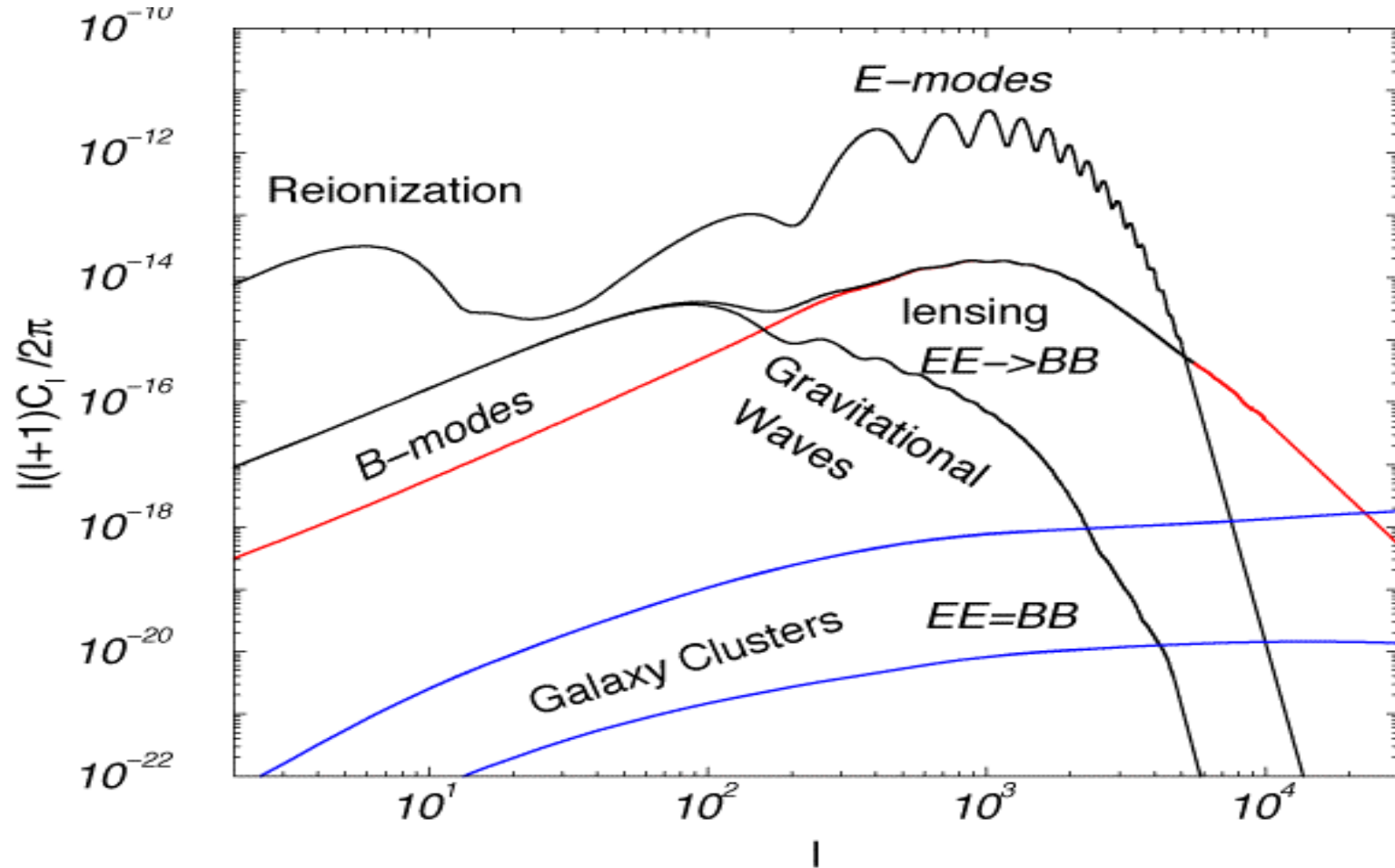
$$\approx T(\bar{\theta}) + \delta\bar{\theta} \bullet \nabla T(\bar{\theta}) + \dots$$

$$\delta\bar{\theta} \equiv \nabla\phi \quad (\text{Deflection ang})$$

Two effects combined lead
to the Fermat potential

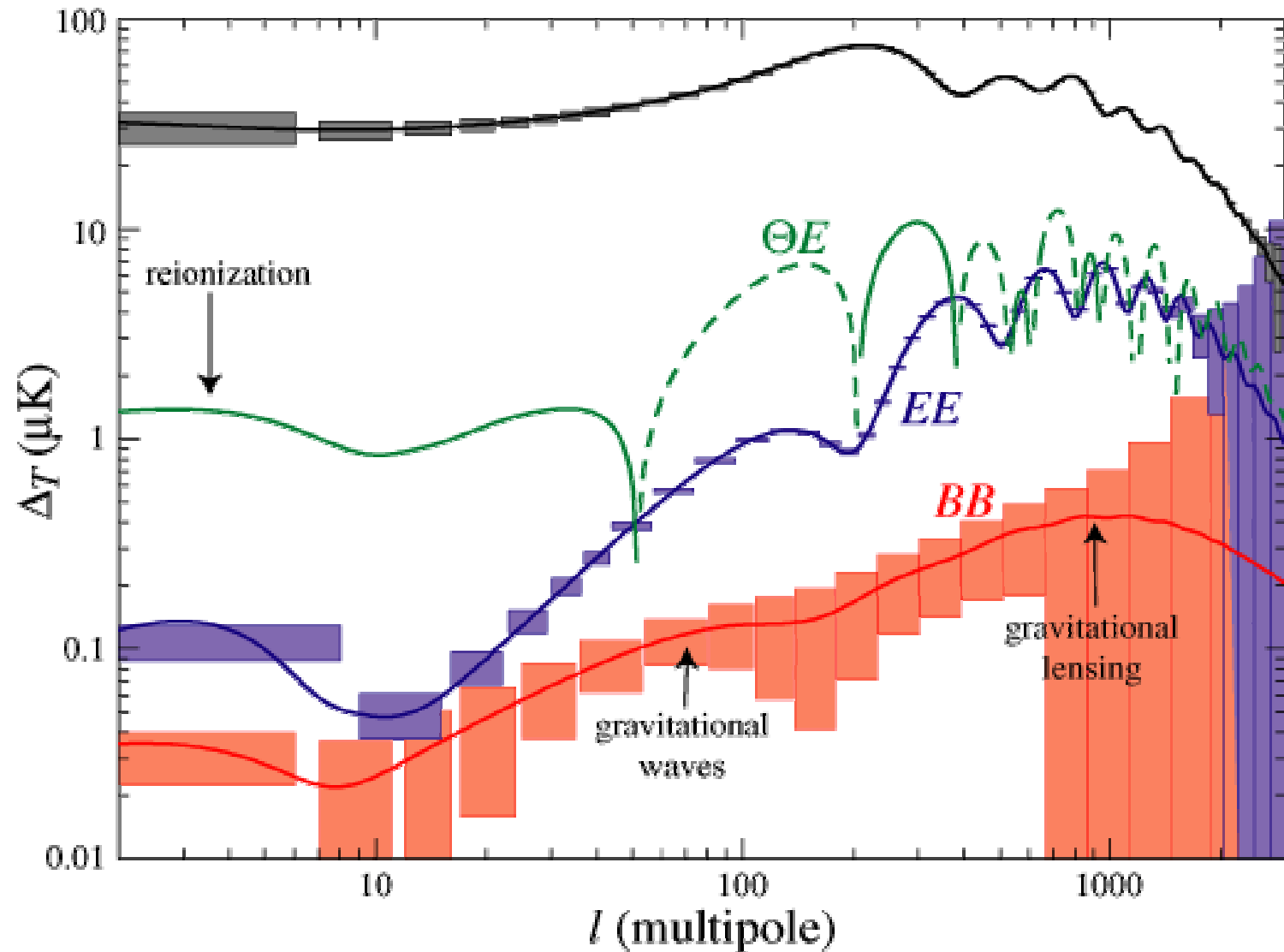
(Hu & Cooray 2000)

Also in Polarization...

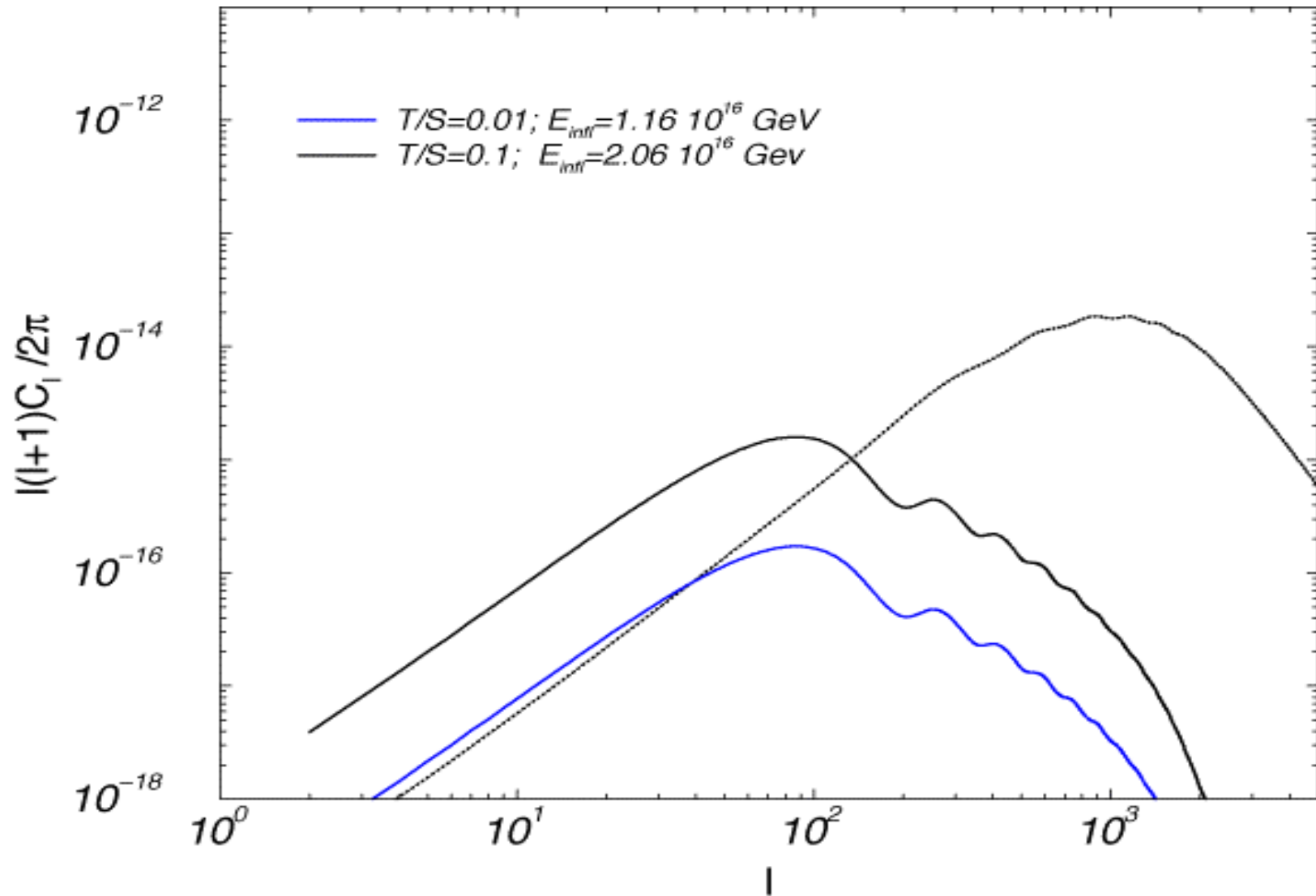


Lensing mixes Stokes-Q and U, or alternatively, between E and B.

Few percent of E-modes converted to B-modes via lensing



Lensing vs. Gravitational-Waves: Which dominates?



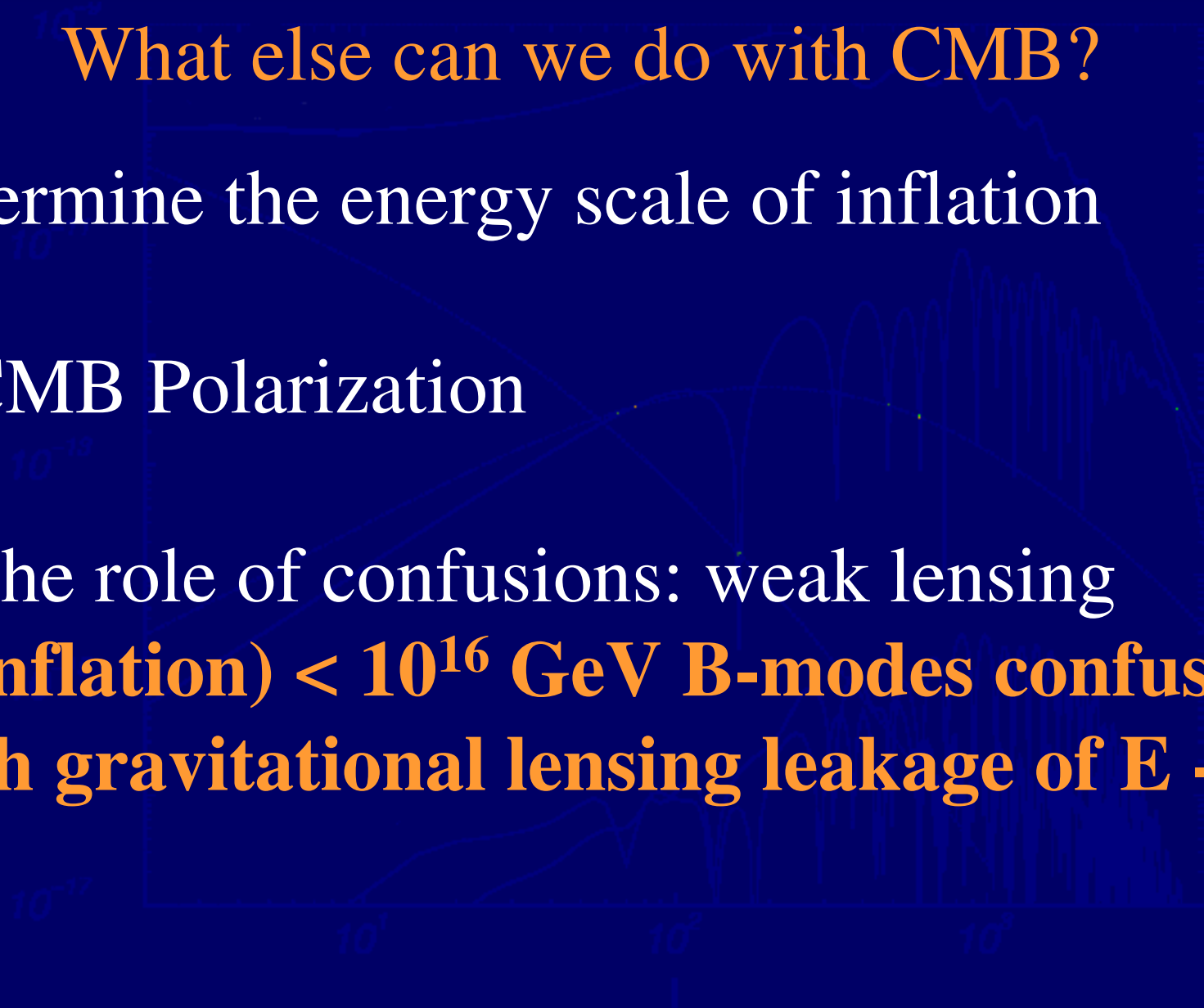
What else can we do with CMB?

I. Determine the energy scale of inflation

- CMB Polarization

- The role of confusions: weak lensing

$E(\text{inflation}) < 10^{16}$ GeV B-modes confused with gravitational lensing leakage of E \rightarrow B

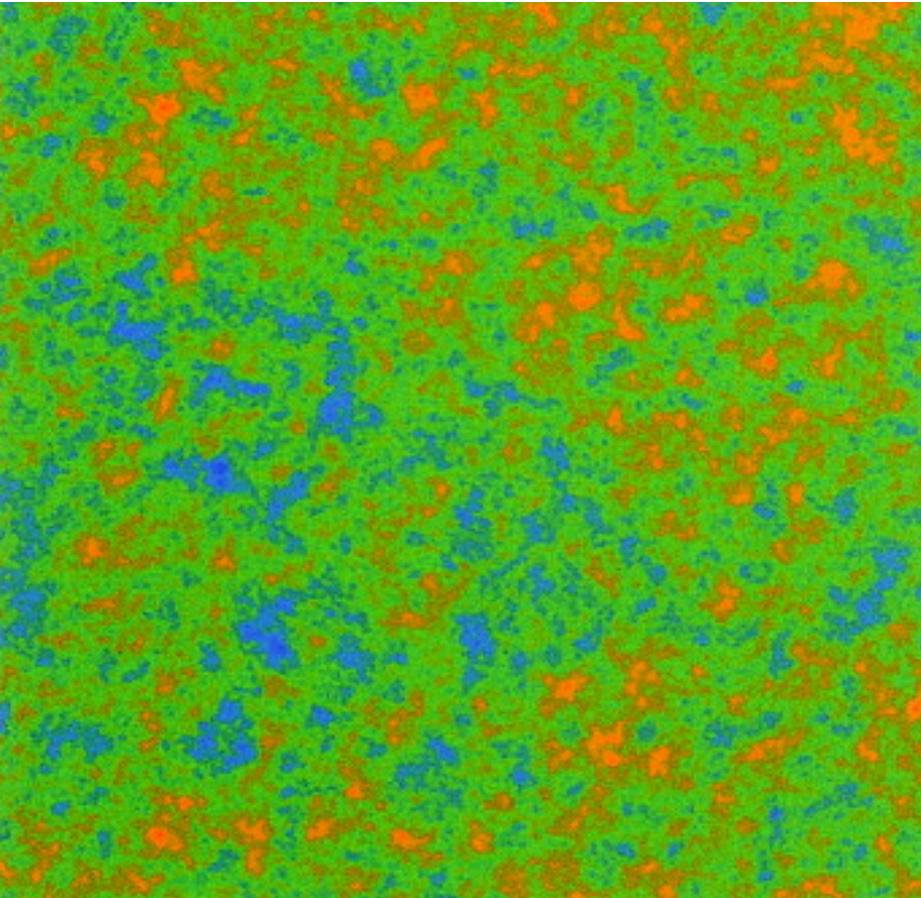


What else can we do with CMB?

I. Determine the energy scale of inflation

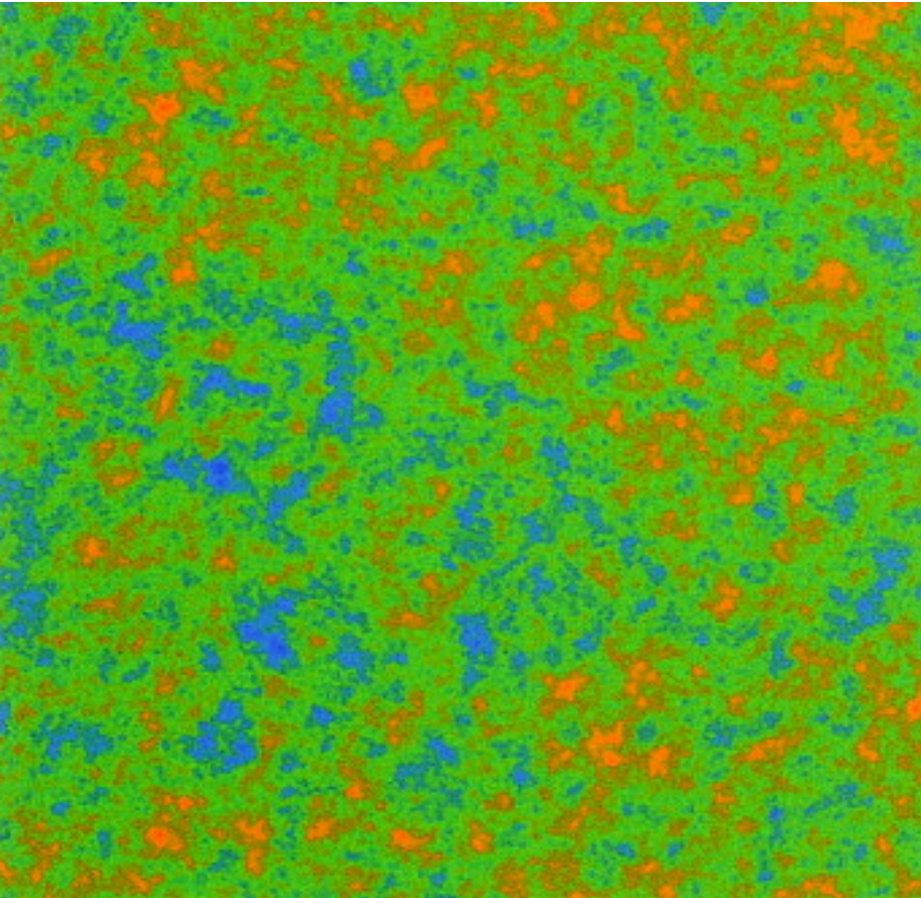
- CMB Polarization
- The role of confusions: weak lensing
 $E(\text{inflation}) < 10^{16} \text{ GeV}$ B-modes confused with gravitational lensing leakage of E \rightarrow B
- With confusions partly removed

Weak Lensing in CMB

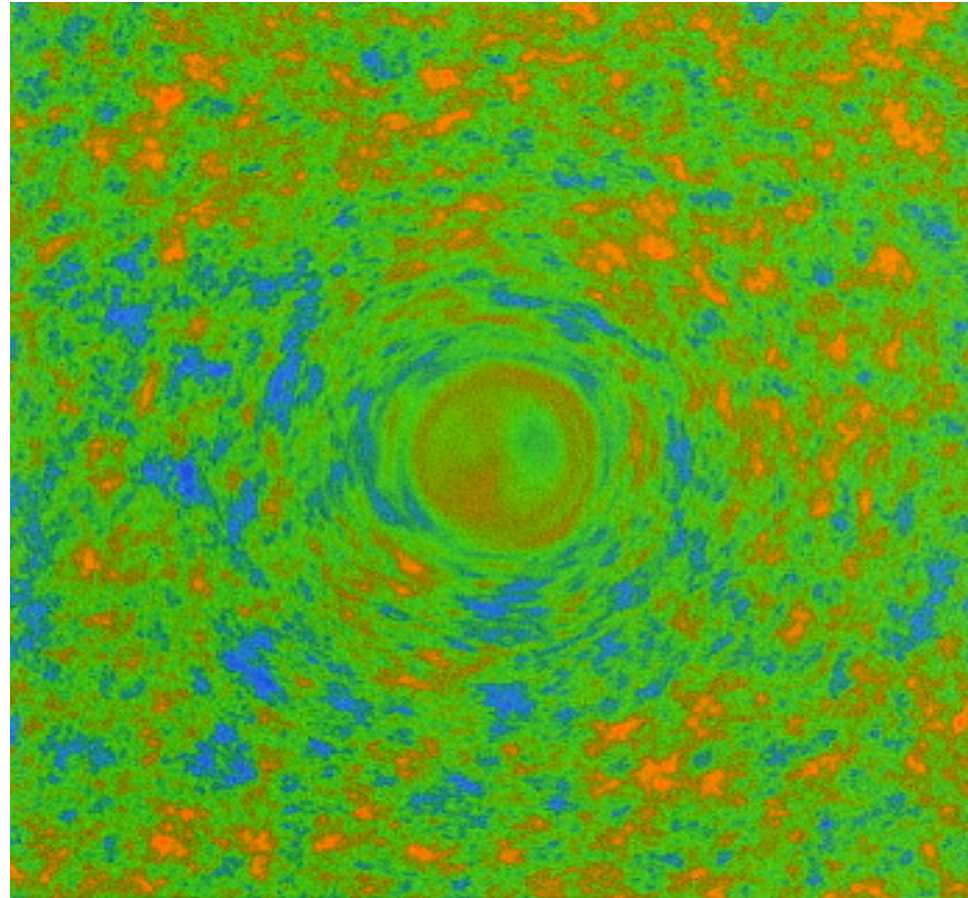


Temperature field

Weak Lensing in CMB



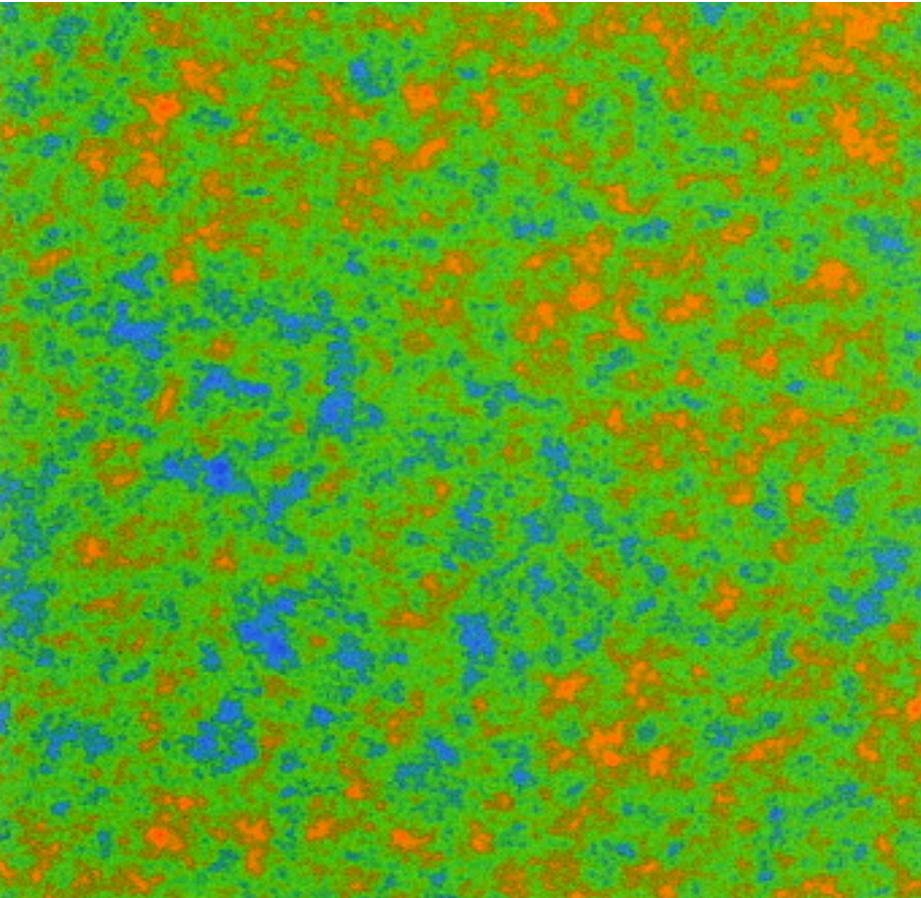
Temperature field



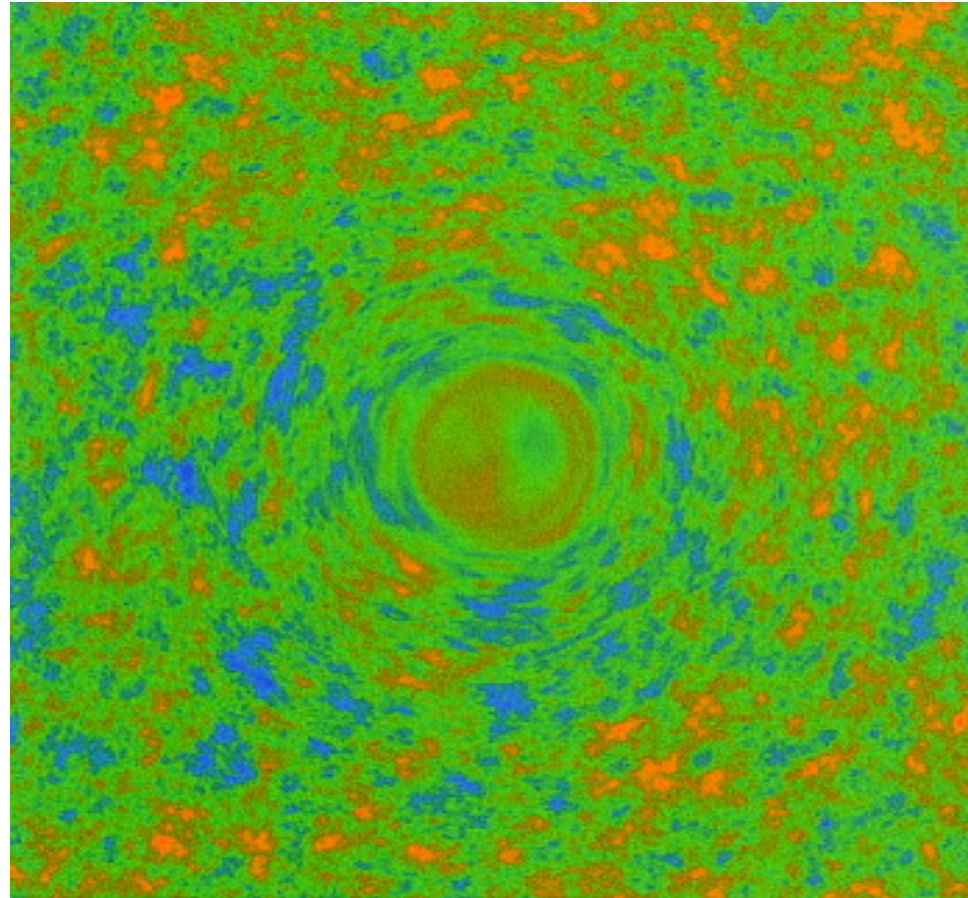
Lensed temperature field

Weak Lensing in CMB

But, this is unrealistic... (requires a massive cluster)

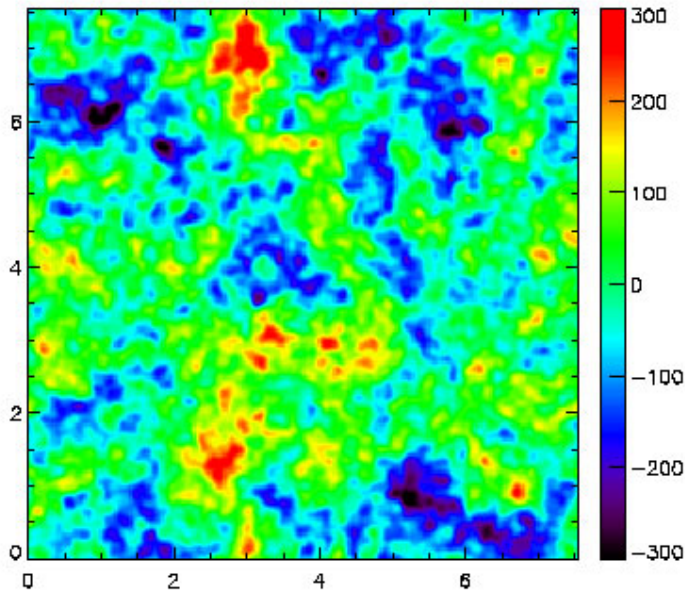


Temperature field

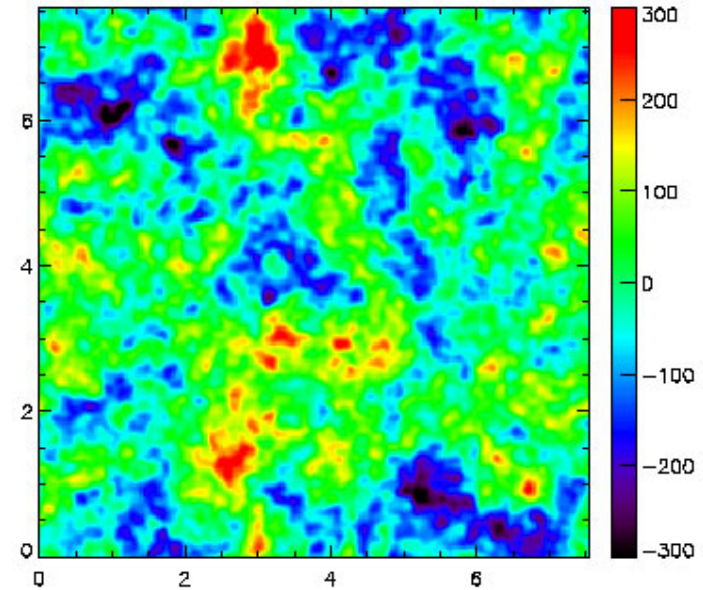


Lensed temperature field

Weak Lensing in CMB



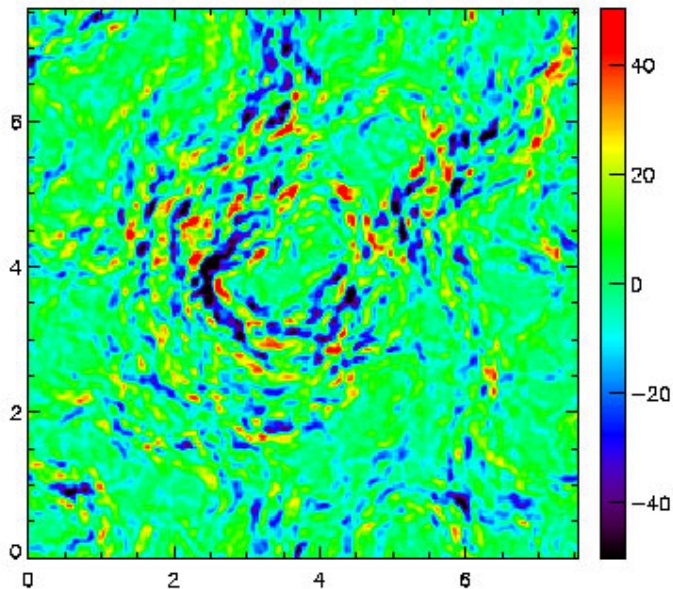
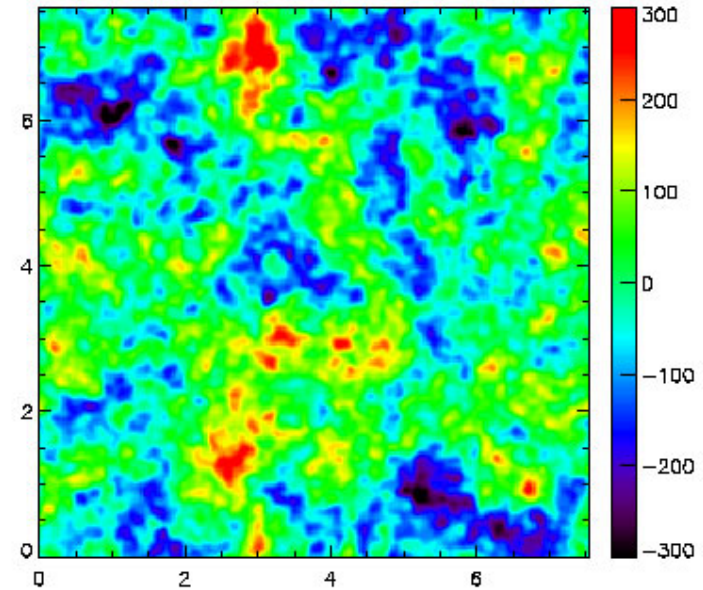
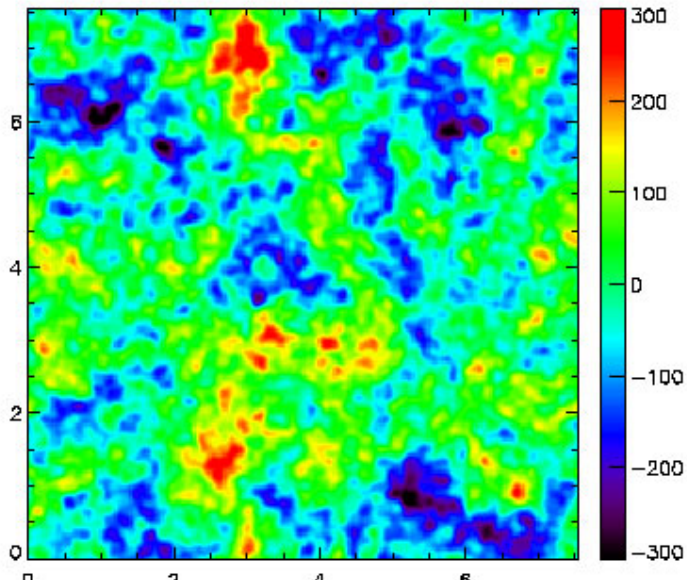
Unlensed



Lensed

The real scenario: difference is very small!!!!

Weak Lensing in CMB



Difference between the two:

- 1) +/- dipolar structure
- 2) Color scale

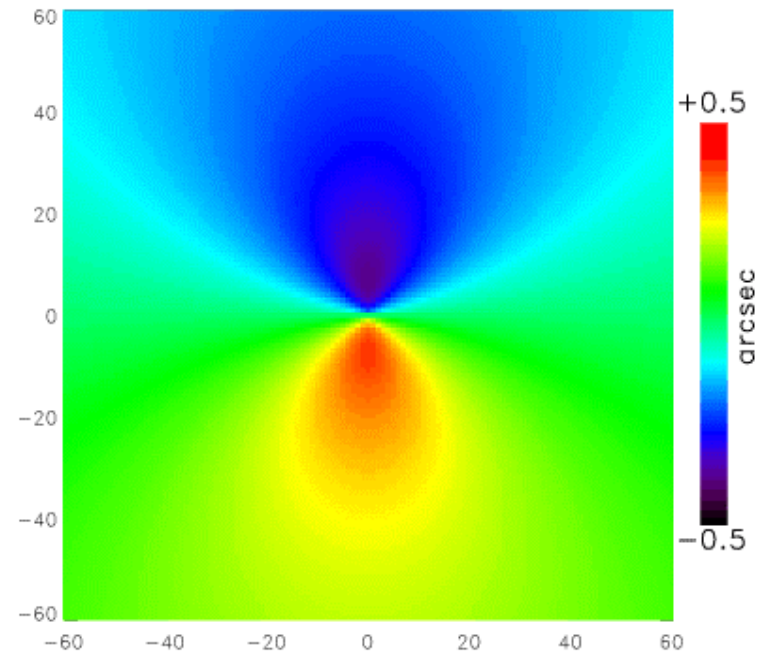
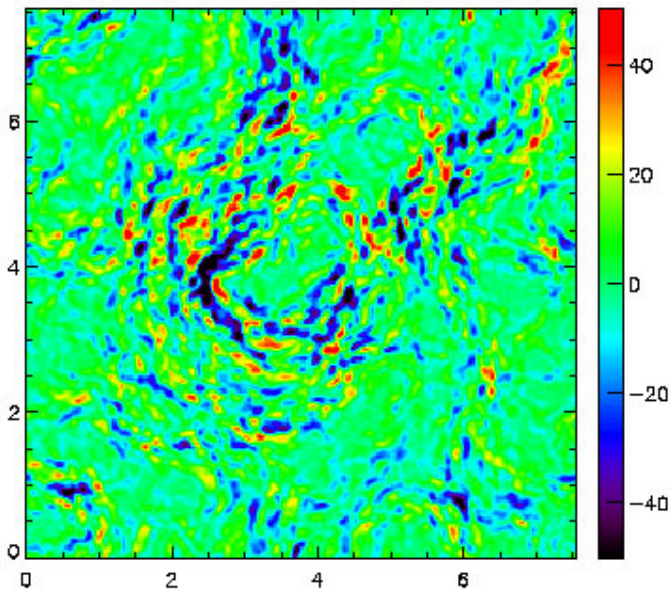
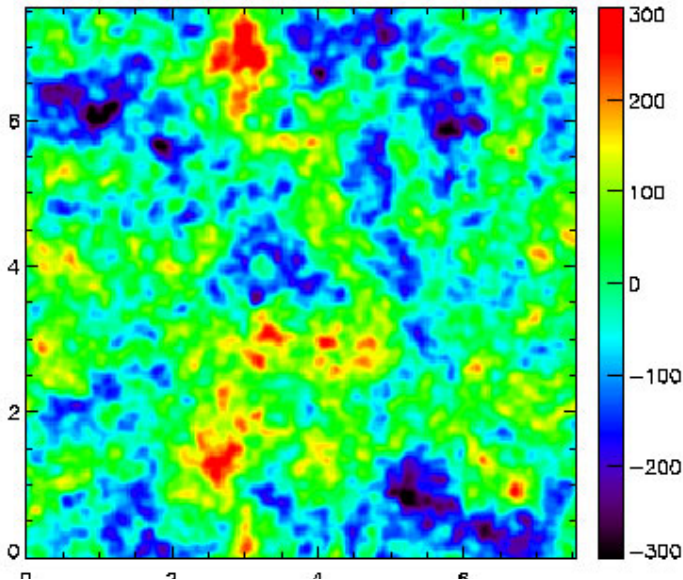
Weak Lensing in CMB

$$T(\bar{\theta}) \equiv T(\bar{\theta} + \delta\bar{\theta})$$

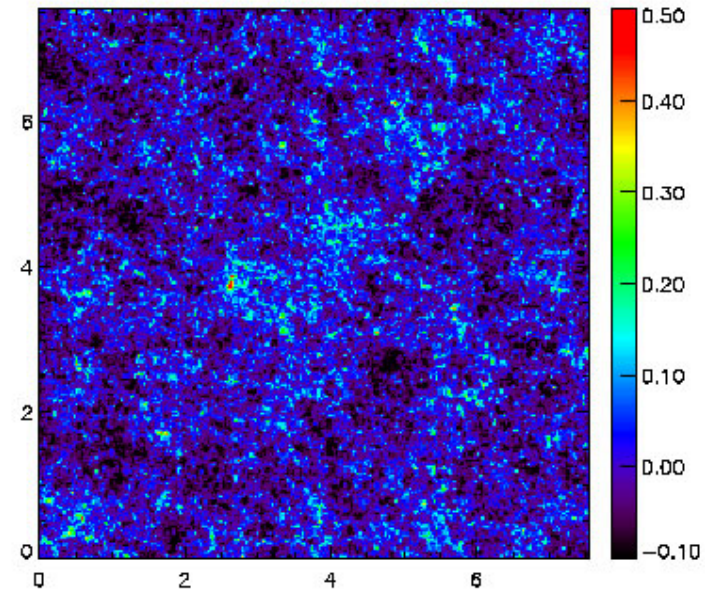
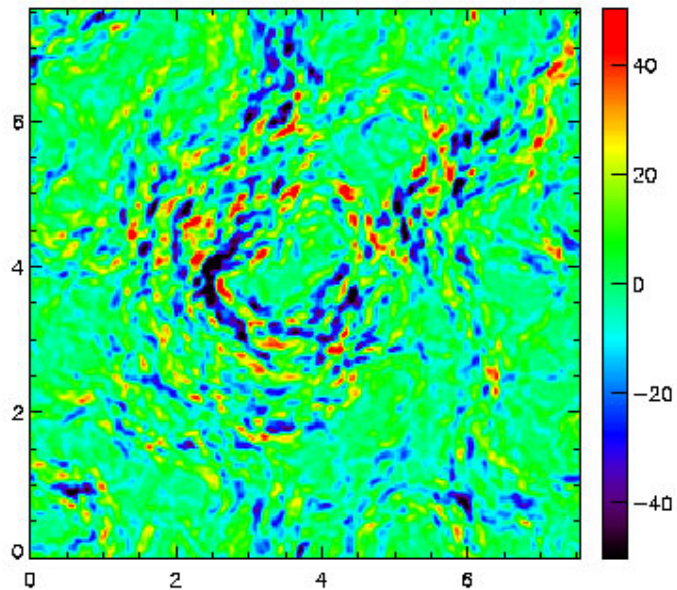
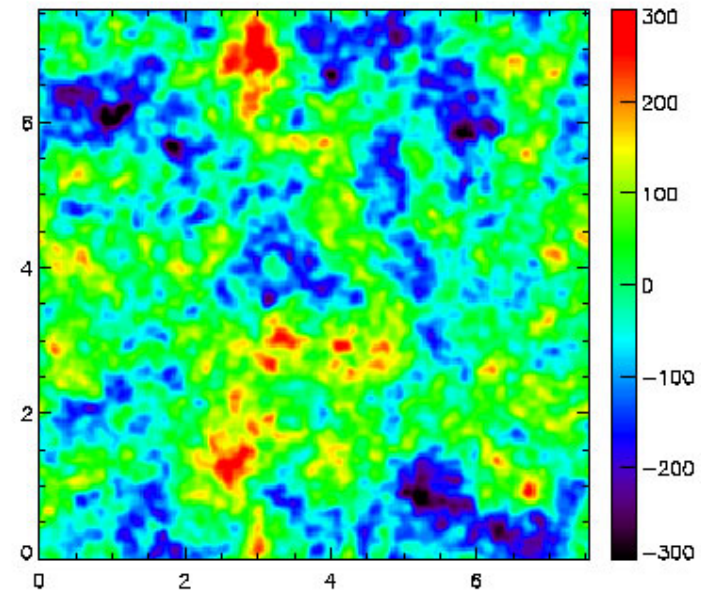
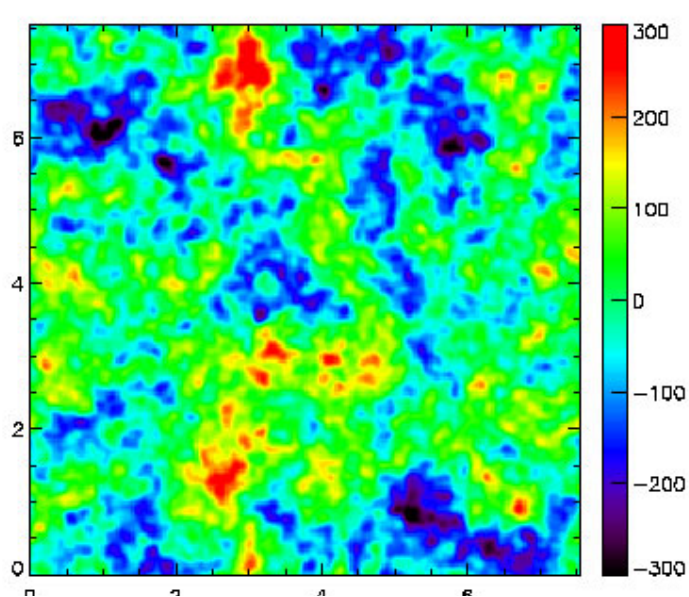
$$\approx T(\bar{\theta}) + \delta\bar{\theta} \bullet \nabla T(\bar{\theta}) + \dots$$

$$\delta\bar{\theta} \equiv \nabla\phi \quad (\text{Deflection ang})$$

1. Modifies CMB gradient
2. Modification is highest when the gradient is highest



Weak Lensing in CMB



Quadratic Statistics as a way to reconstruct lensing deflections

Reconstruction algorithm (basics)

Lensing effect is on the second order - has to be a quadratic statistic

CMB maps are noise dominated - has to be able to understand noise properties easily and be able to extract most information on lensing

(Algorithms in Cooray & Kesden 2002;
Kesden, Cooray & Kamionkowski 2002; Hu & Okamoto 2002;
Seljak & Hirata 2003; among others)

Quadratic Statistics as a way to reconstruct lensing deflections

Reconstruction algorithm (naïve description)

1. Take the temperature map and square it.

$$\begin{aligned}\tilde{T}^2(\bar{l}) &= \int d\bar{\theta} T^2(\bar{\theta}) e^{-i\bar{l} \cdot \bar{\theta}} \\ &= \int \frac{d^2 l_1}{(2\pi)^2} \tilde{T}(\bar{l}_1) \tilde{T}(\bar{l} - \bar{l}_1)\end{aligned}$$

Quadratic Statistics as a way to reconstruct lensing deflections

Reconstruction algorithm (naïve description)

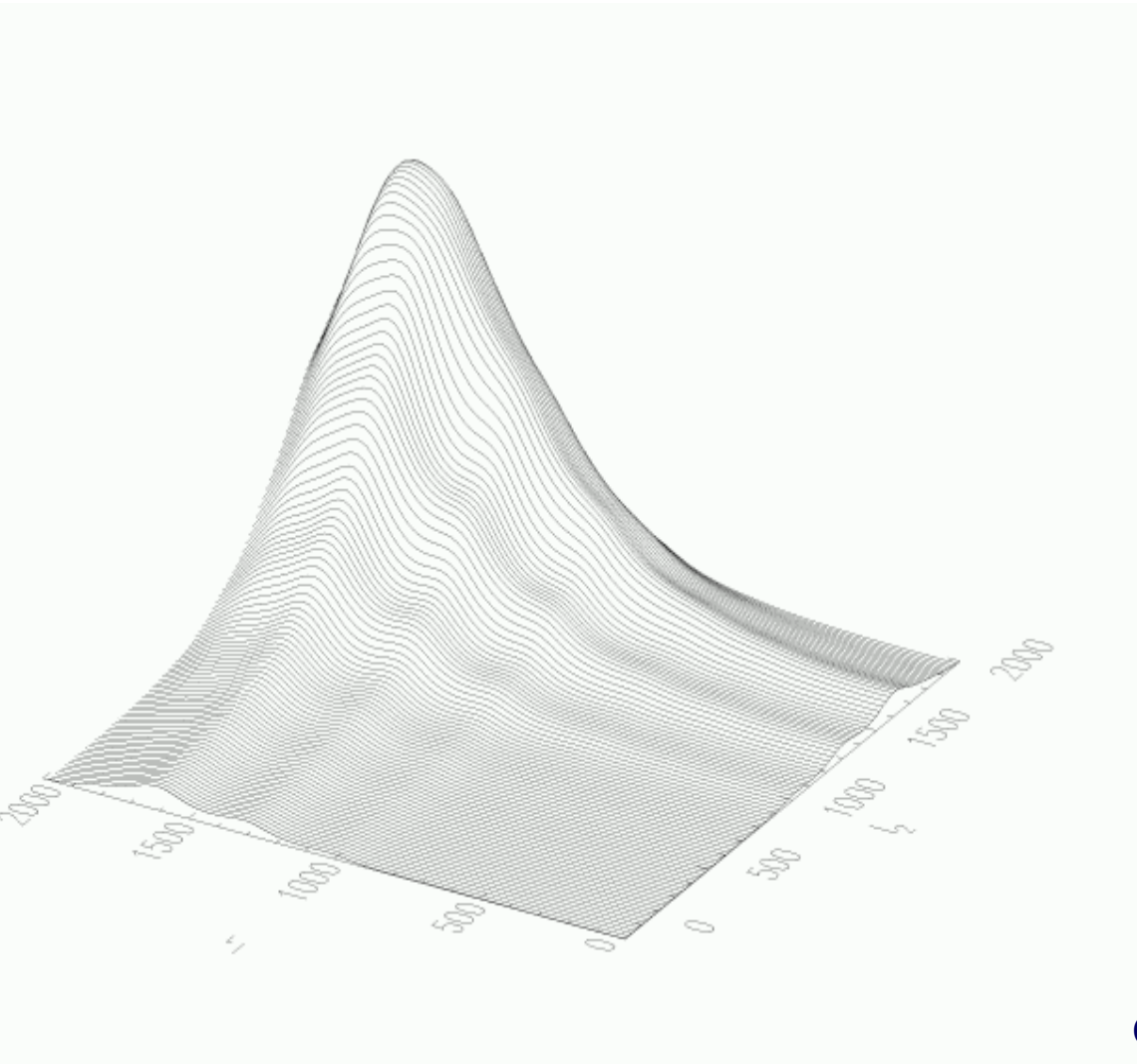
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Homework: $\tilde{T}^2(\bar{l}) \propto \delta\theta(\bar{l})$

Quadratic Statistics as a way to reconstruct lensing deflections

- Filter the CMB^2 map to get rid of the excess high frequency noise



- Optimal filter depends only on the primary CMB anisotropies and behavior of the lensing mode coupling
- Optimal filter returns all info from the trispectrum (*CMB^2 - CMB^2 statistic is not loseless to the extent Gaussian noise is the only noise source*)

Cooray 2001; Cooray & Kesden 2002

Quadratic Statistics as a way to reconstruct lensing deflections

What are we doing here?

Correlation function of the background is expected to be isotropic.

In the presence of lensing, the correlation function is, however, anisotropic.

The proposed statistic is optimized to measure this anisotropy, which can be inverted to reconstruct the deflection angle.

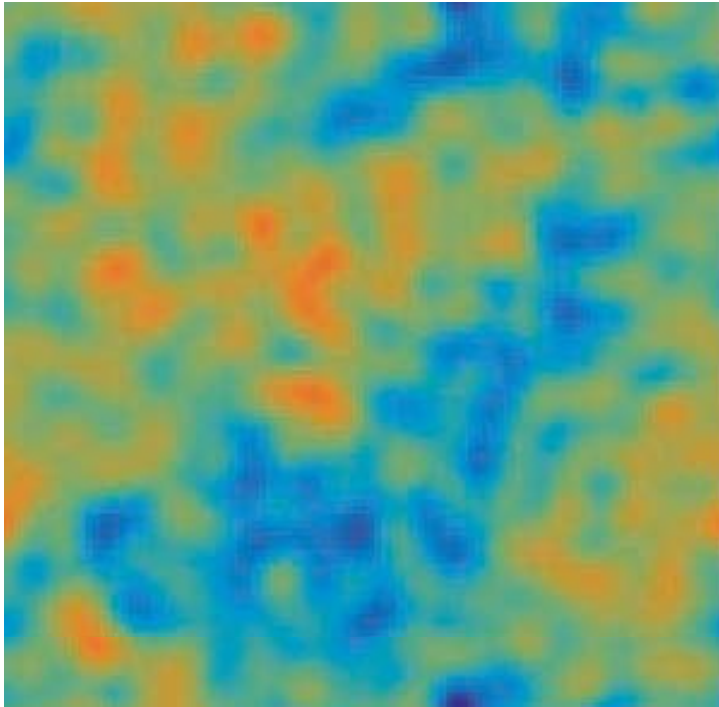
CMB as a weak lensing experiment

Squared Temperature-Squared Temperature Power Spectrum

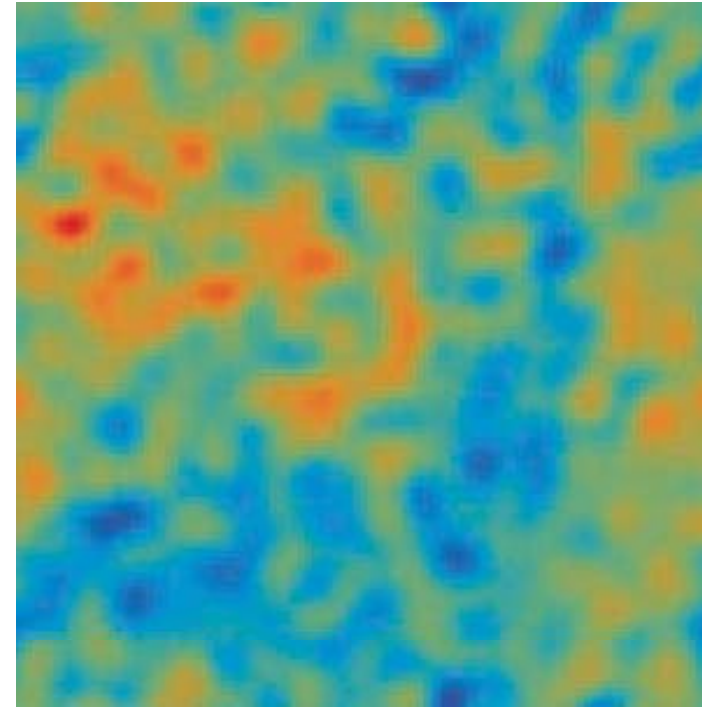
(Other suggestions: temperature gradients
Seljak & Zaldarriaga; Bernardeau et al.)

Hu 2001

Cooray & Kesden 2002



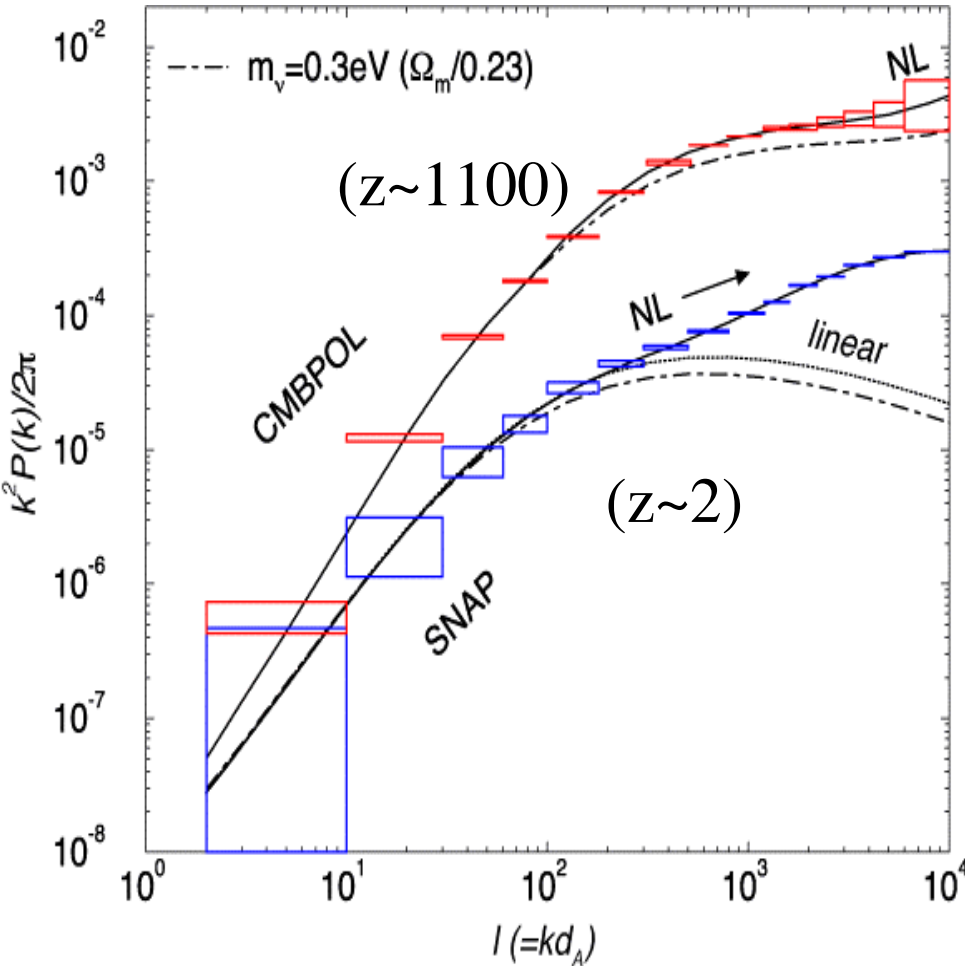
Input deflection (mass) field



Constructed deflection map with 1.5
arcmin beam and $27 \mu K$ arcmin noise

CMB as a weak lensing experiment

Lensing convergence

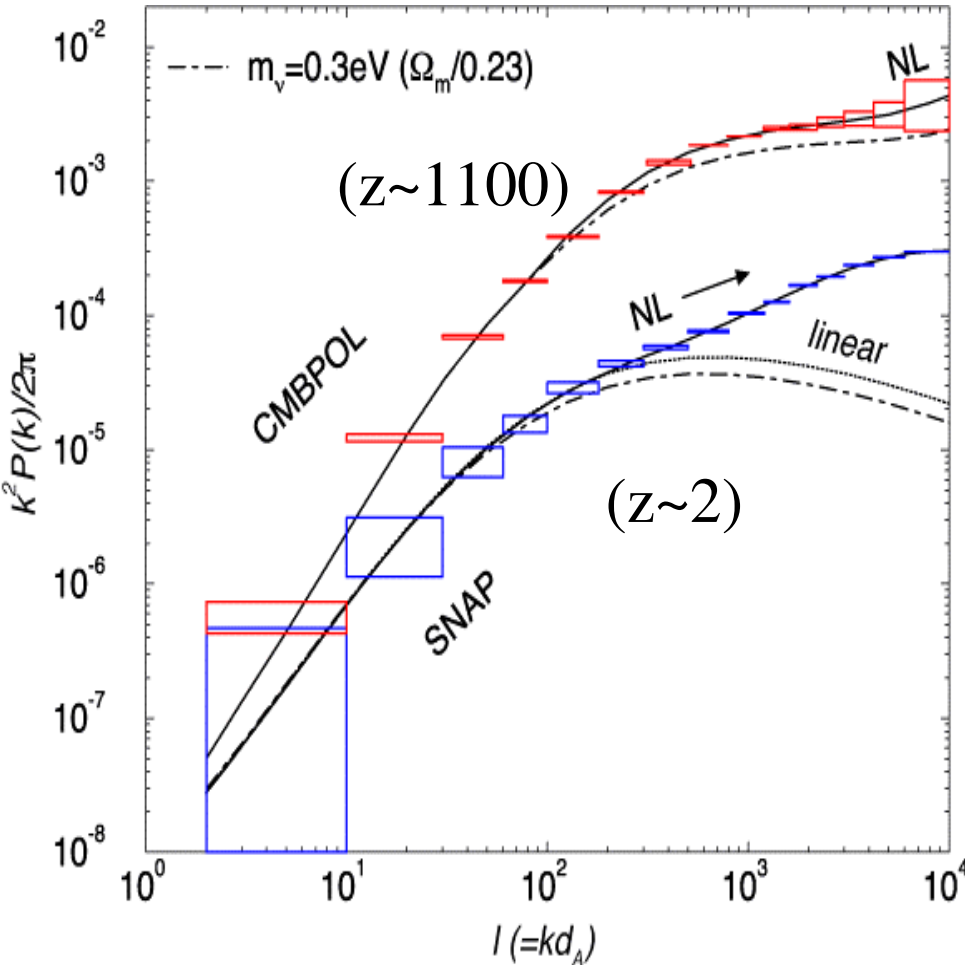


Expected Weak lensing results

(plotted is convergence power spectrum related to the integrated mass responsible for lensing)

CMB as a weak lensing experiment

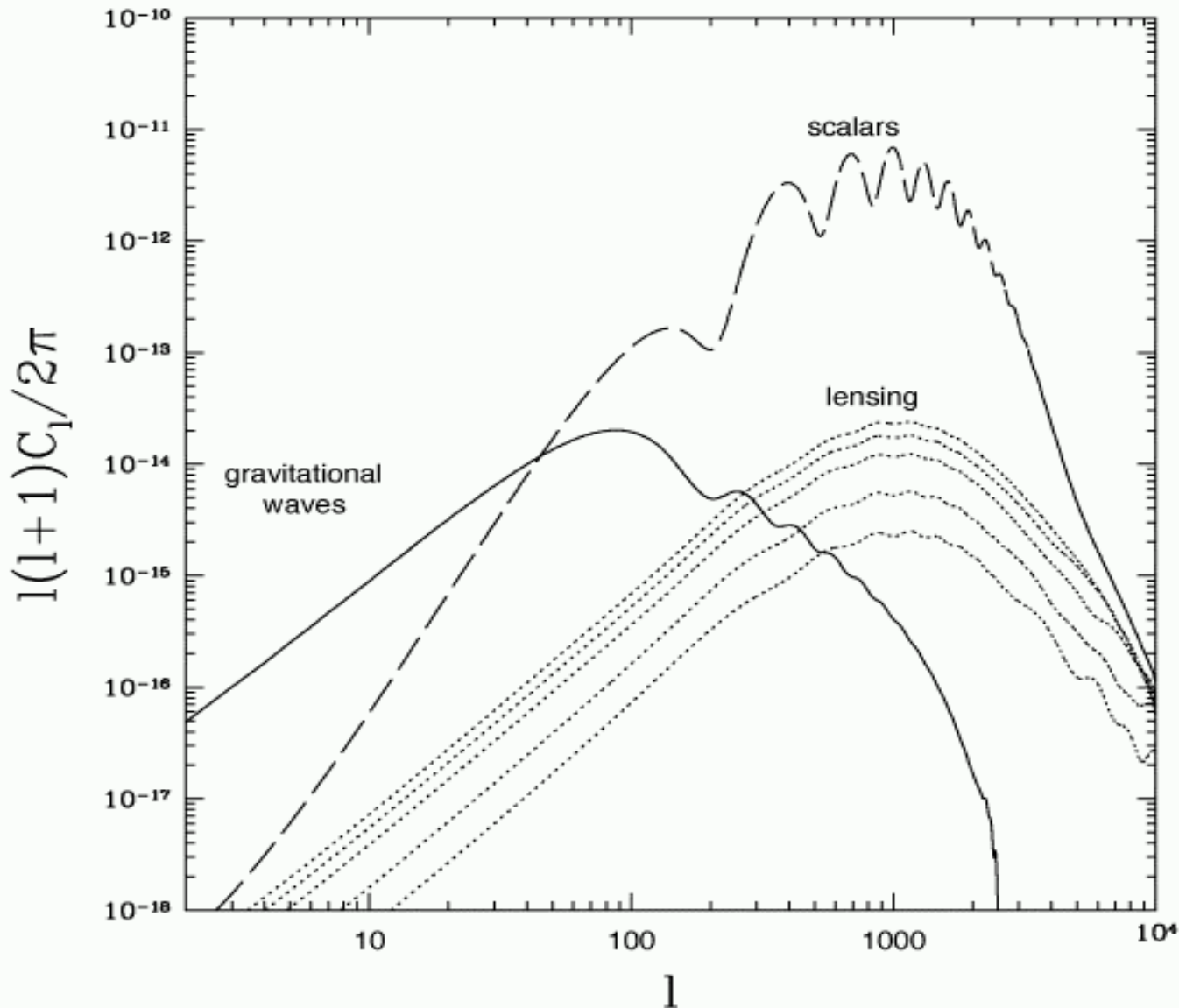
Lensing convergence



Why do this?

1. Source redshift is known (recombination)
2. Linear power spectrum - (cosmology)
3. Test evolution
4. Get this for free

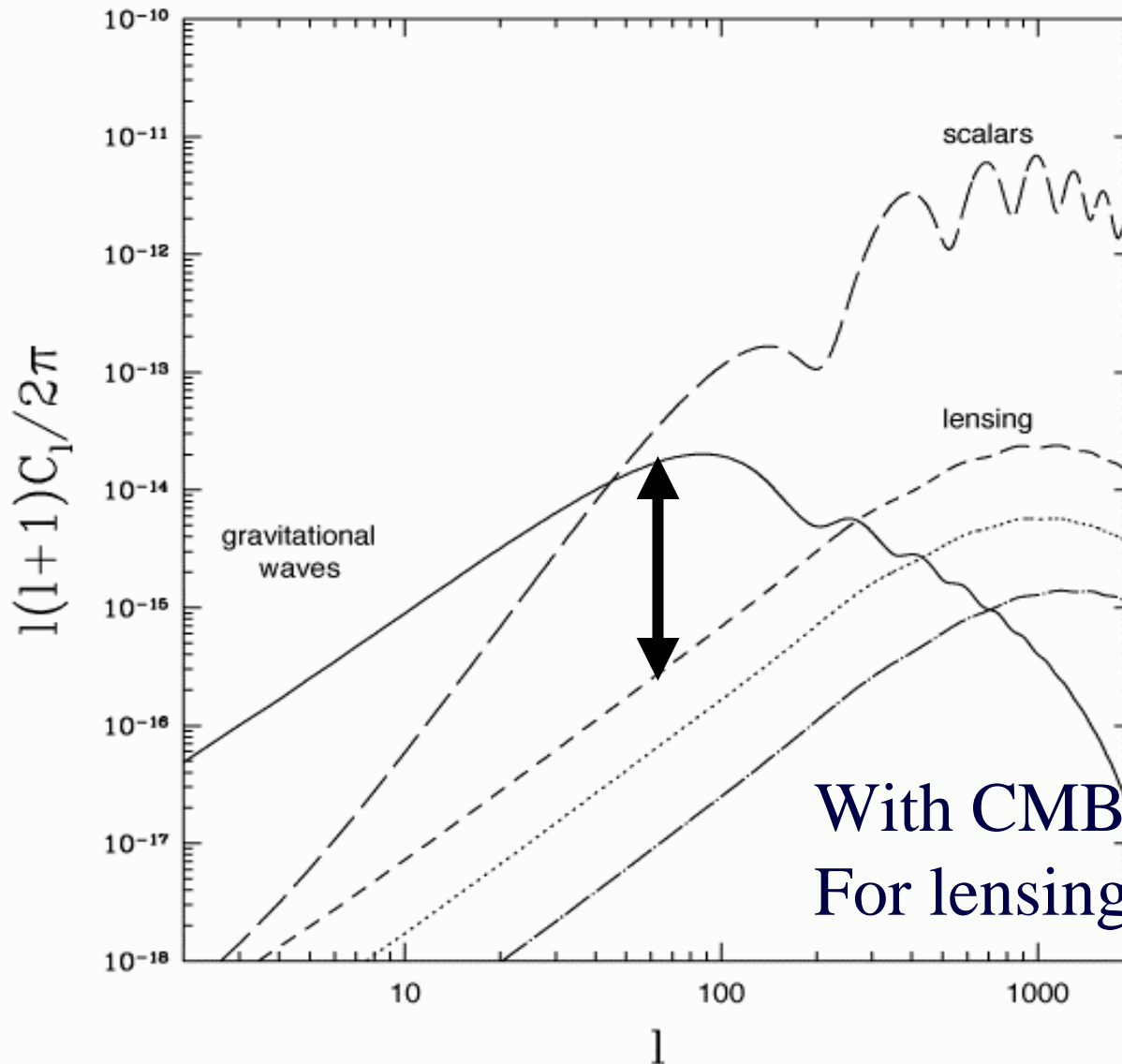
Removing the confusions



As a function of z
 $z > 0$
 $z > 1$
 $z > 2$
 $z > 5$
 $z > 10$

Galaxy lensing cannot be used to correct Polarization

Removing the confusions

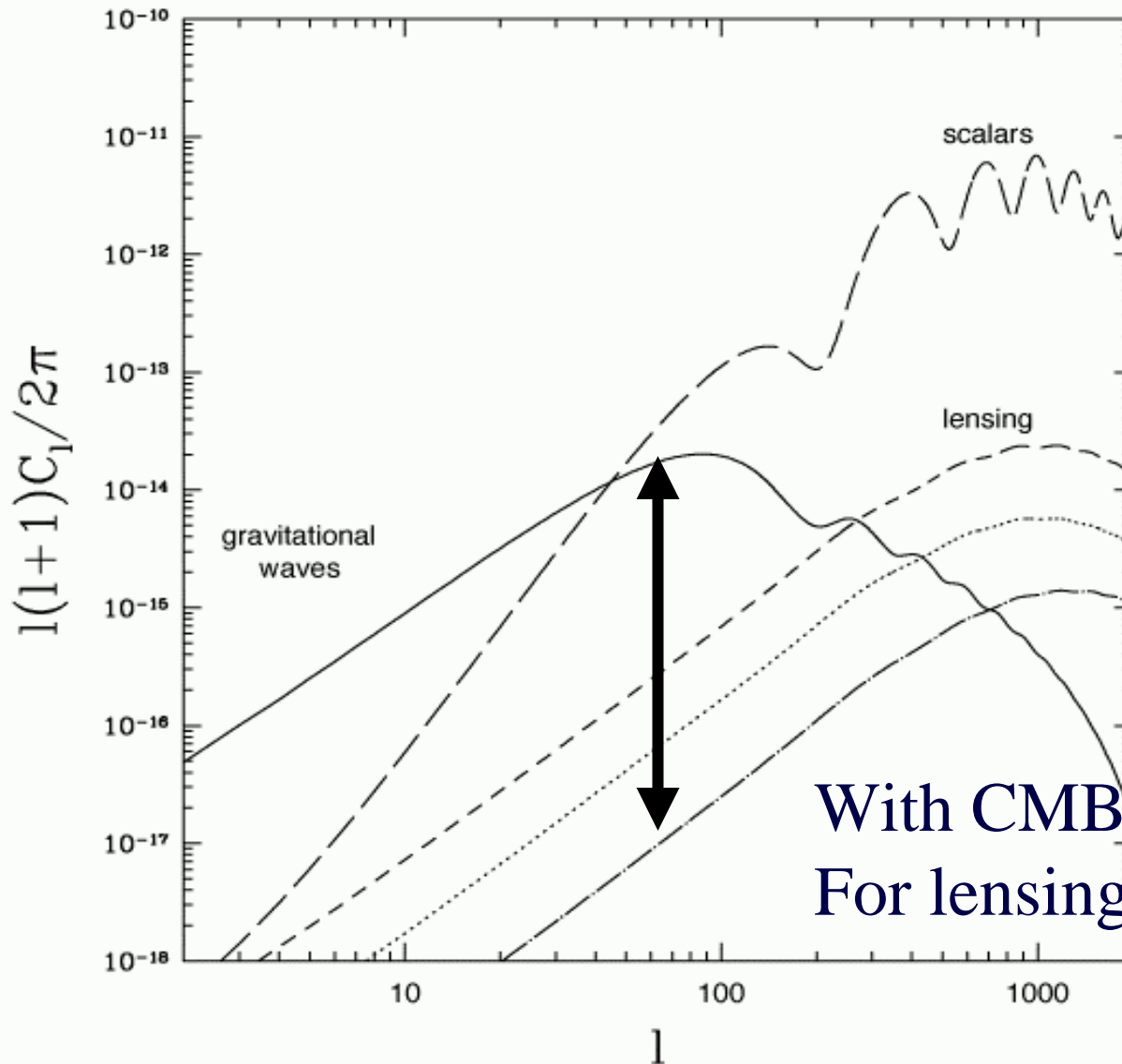


Extract with a noise contribution below an order of magnitude of the signal

(Kesden et al. 2002;
Knox & Song 2002)

With CMB temp. data cleaned
For lensing

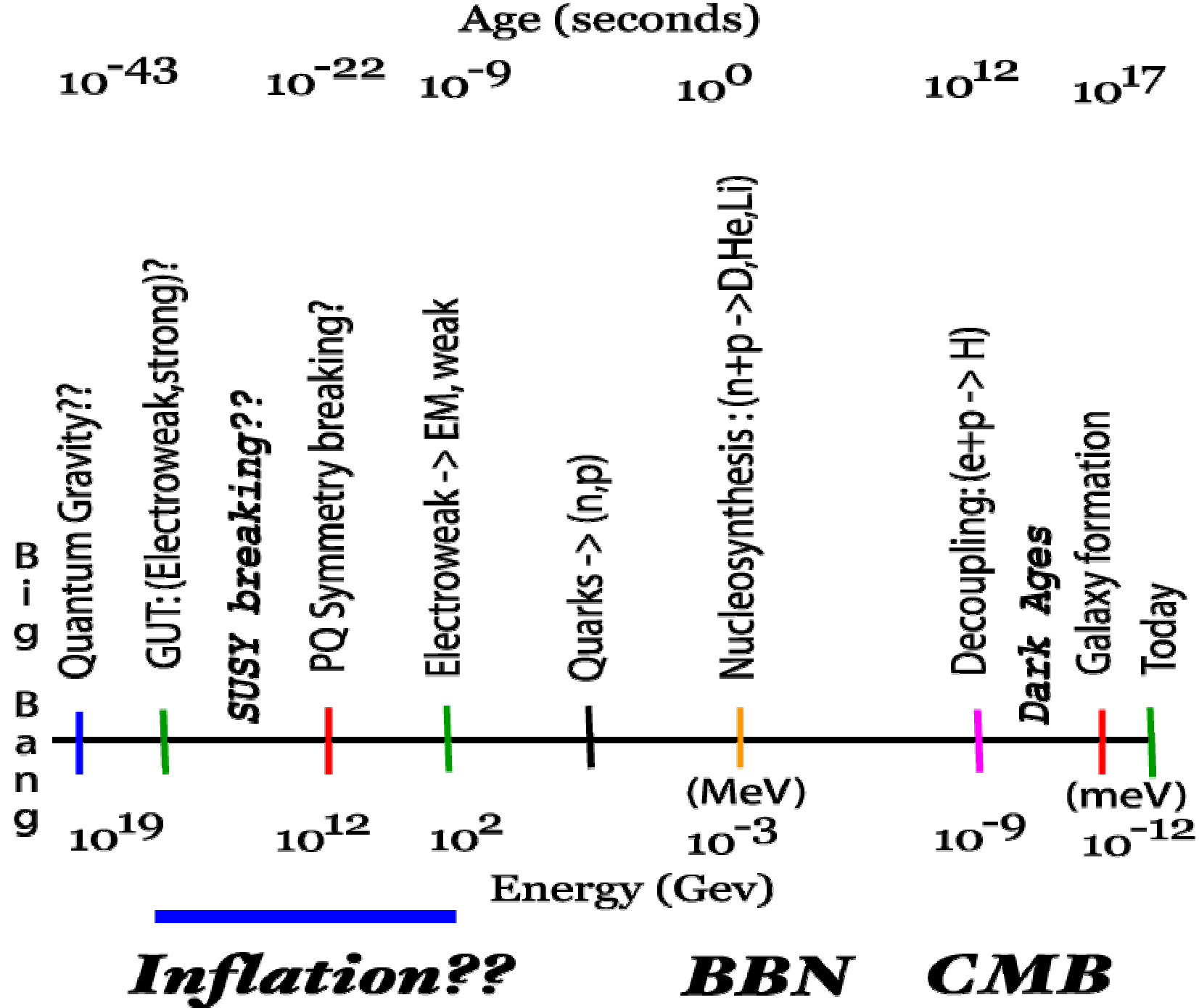
Removing the confusions

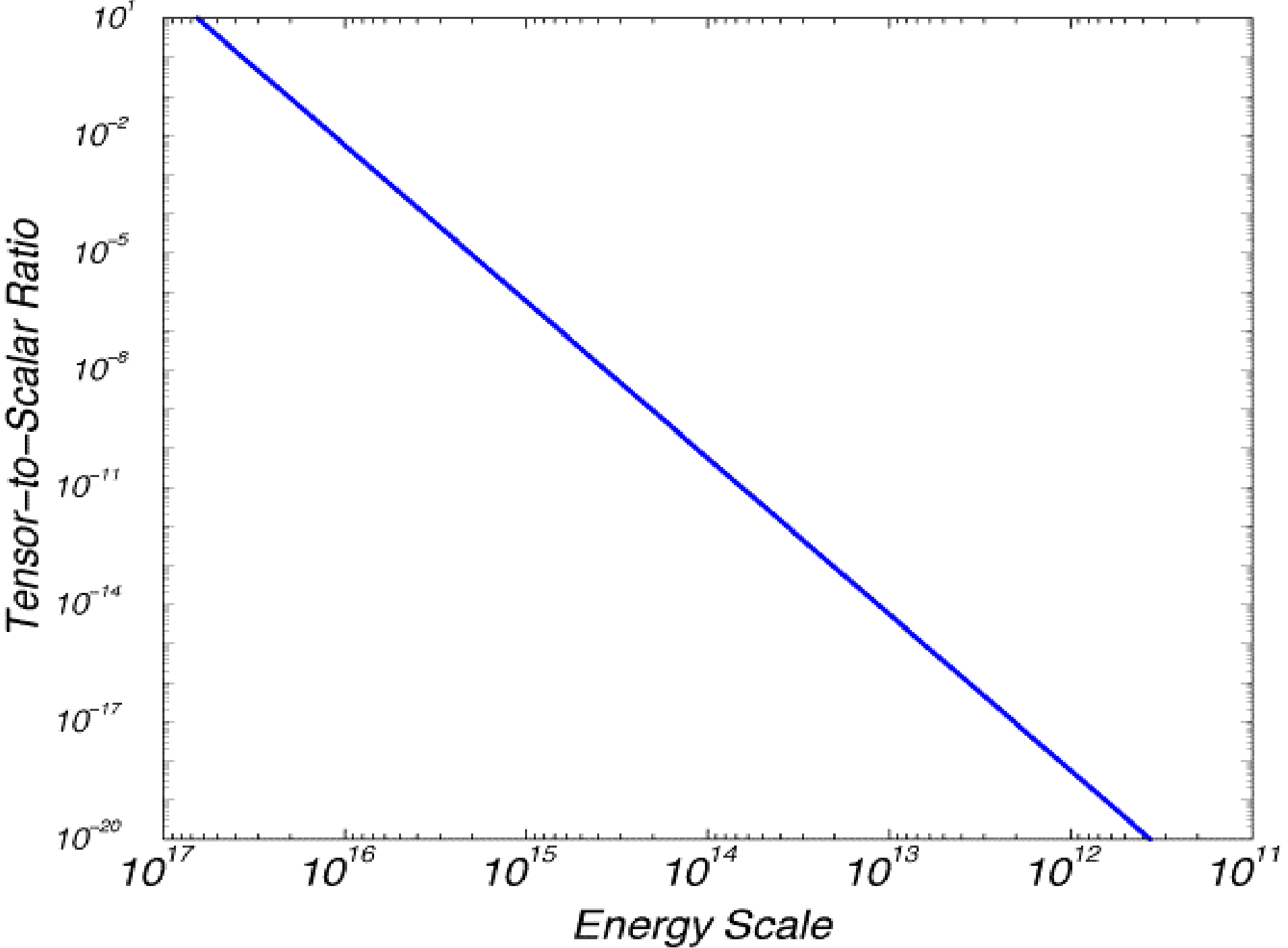


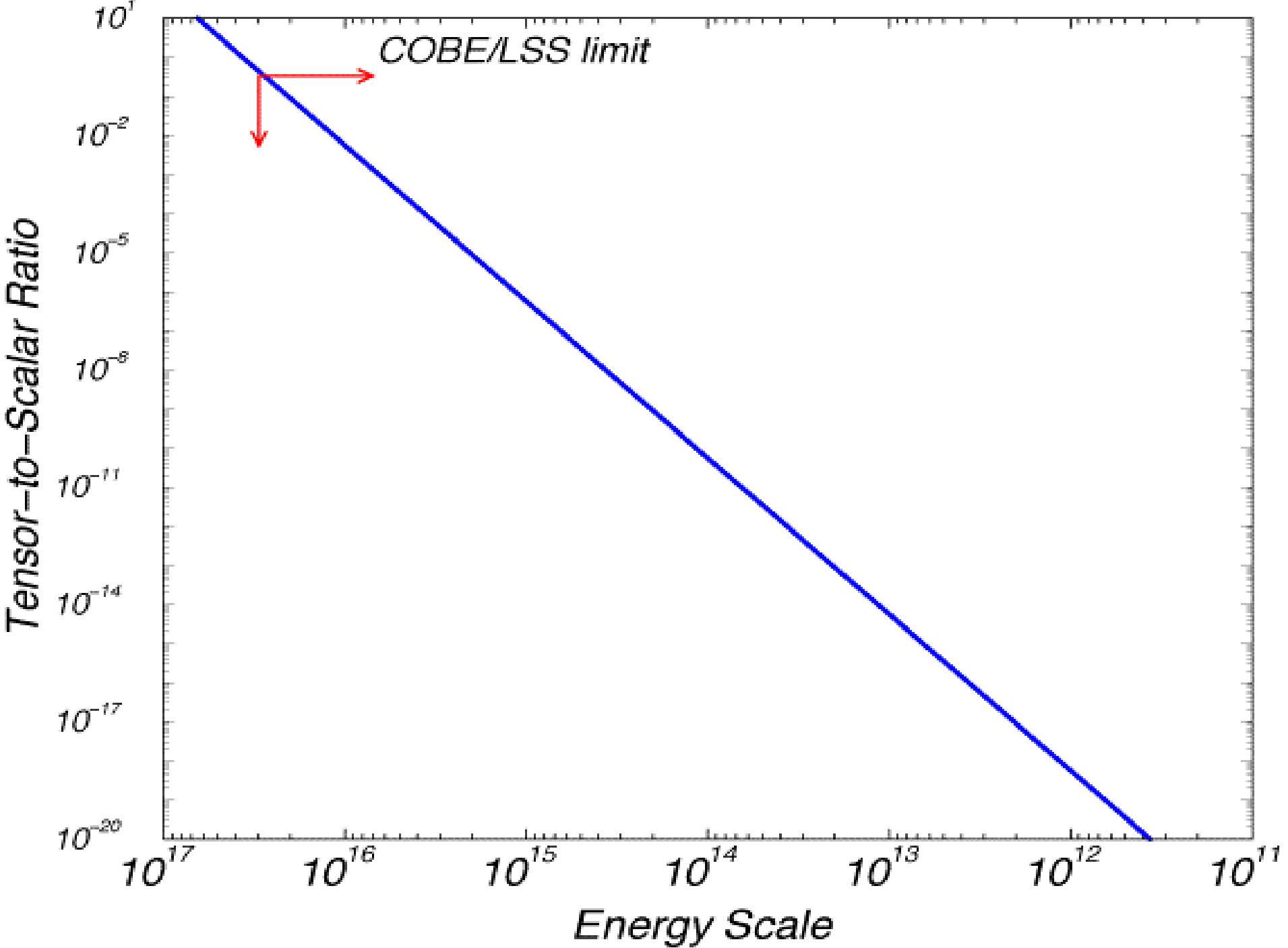
Extract with a noise contribution below an order of magnitude of the signal

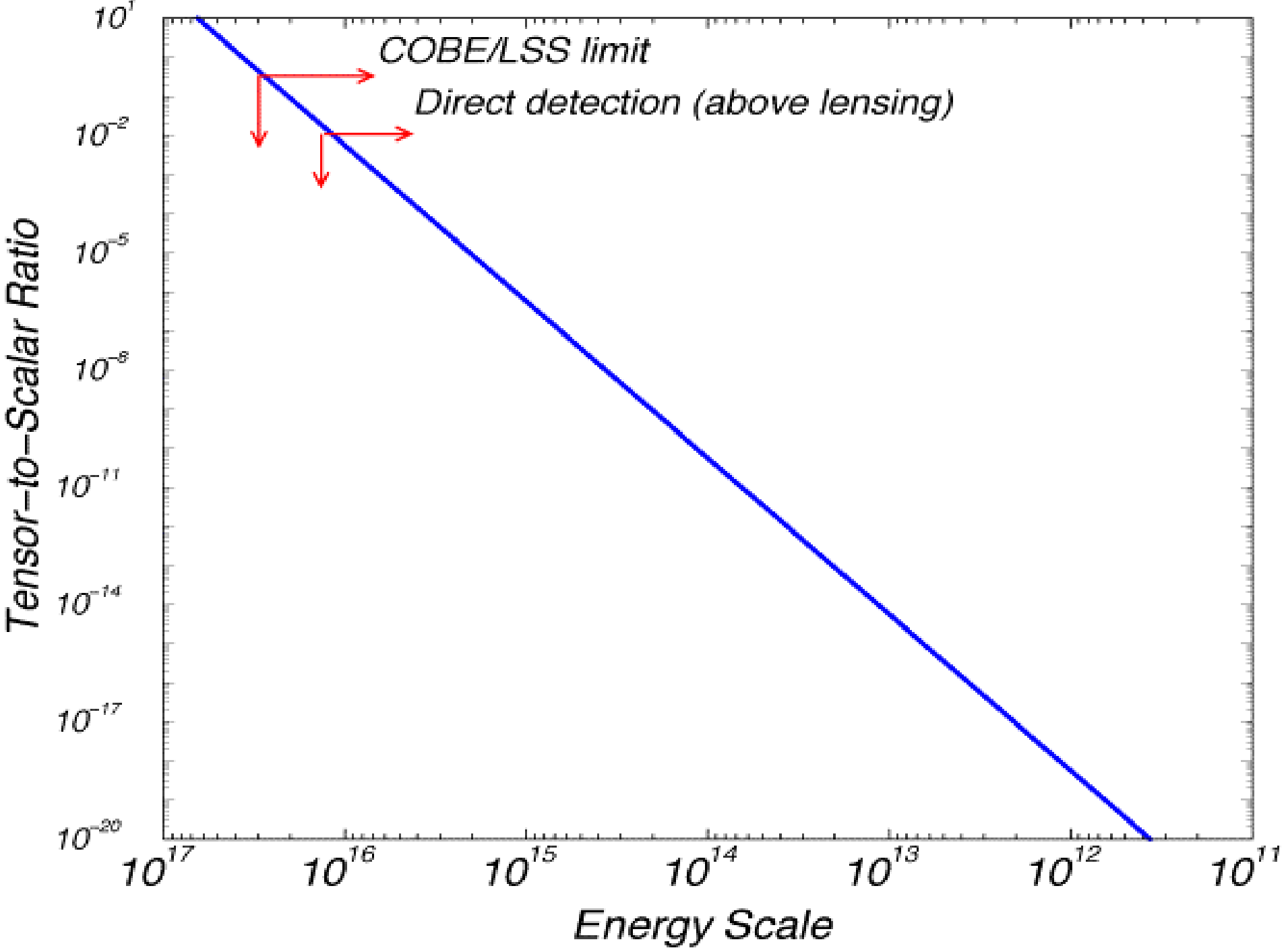
(Kesden et al. 2002;
Knox & Song 2002)

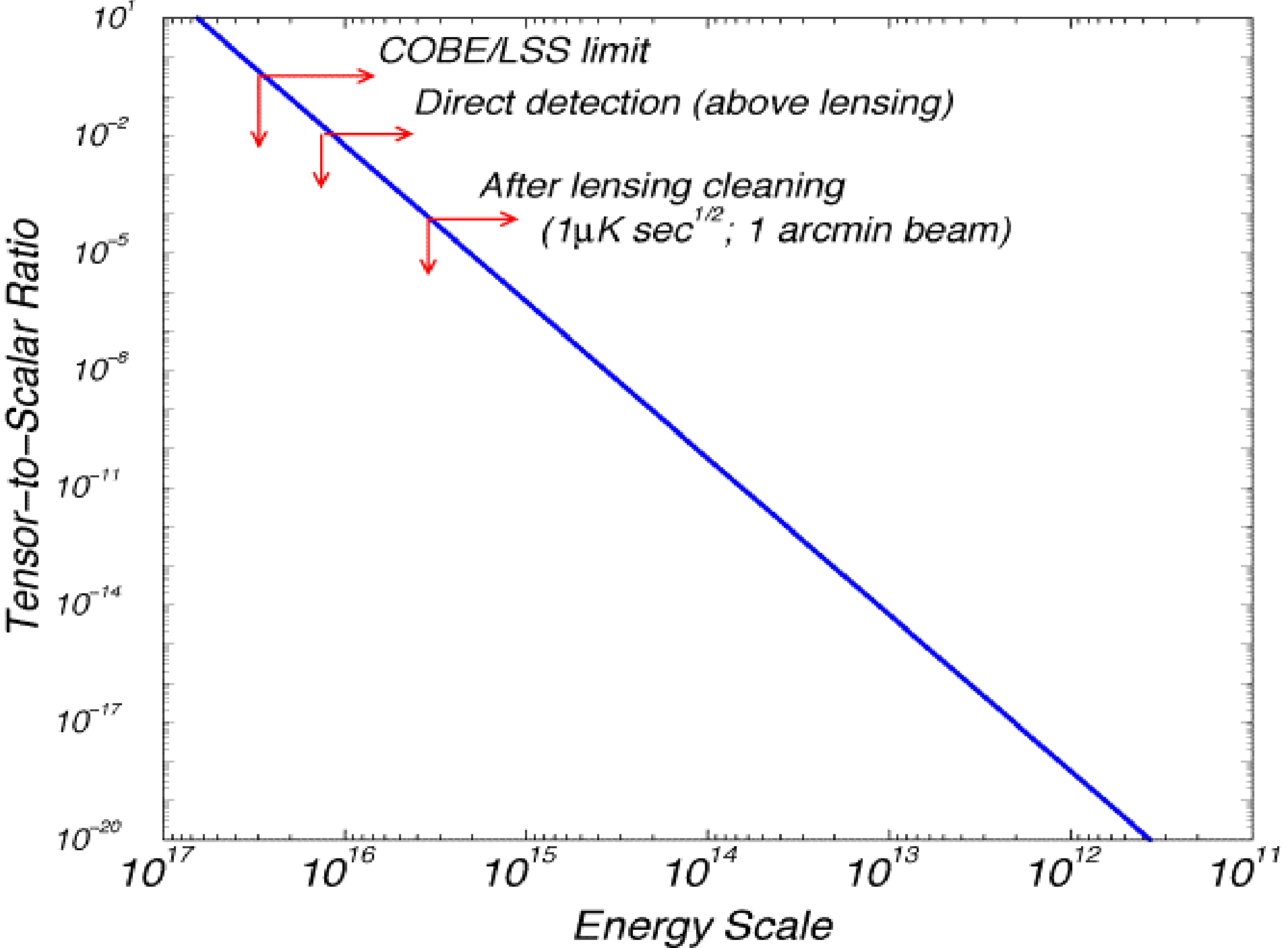
With CMB temp. data cleaned
For lensing

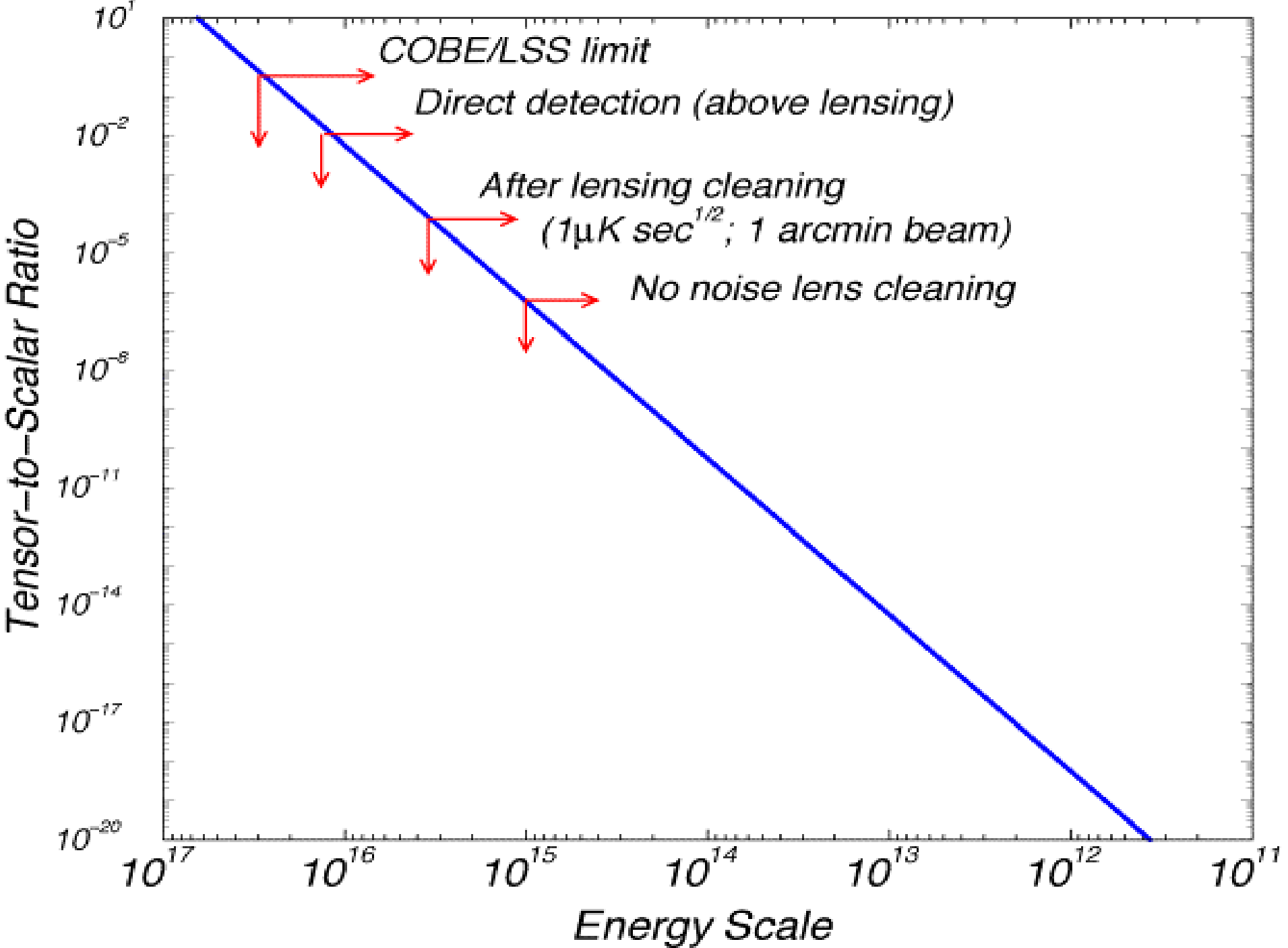


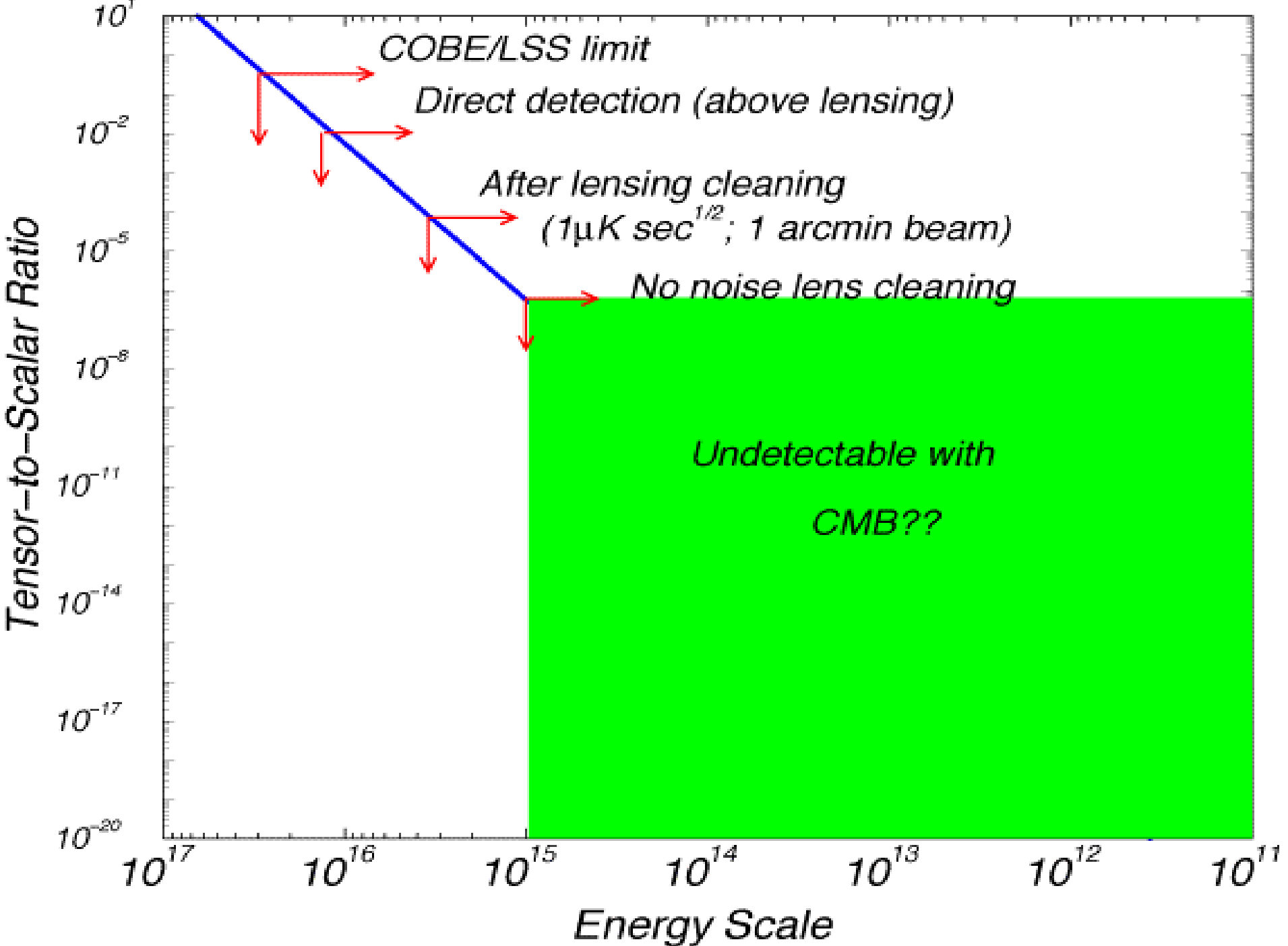


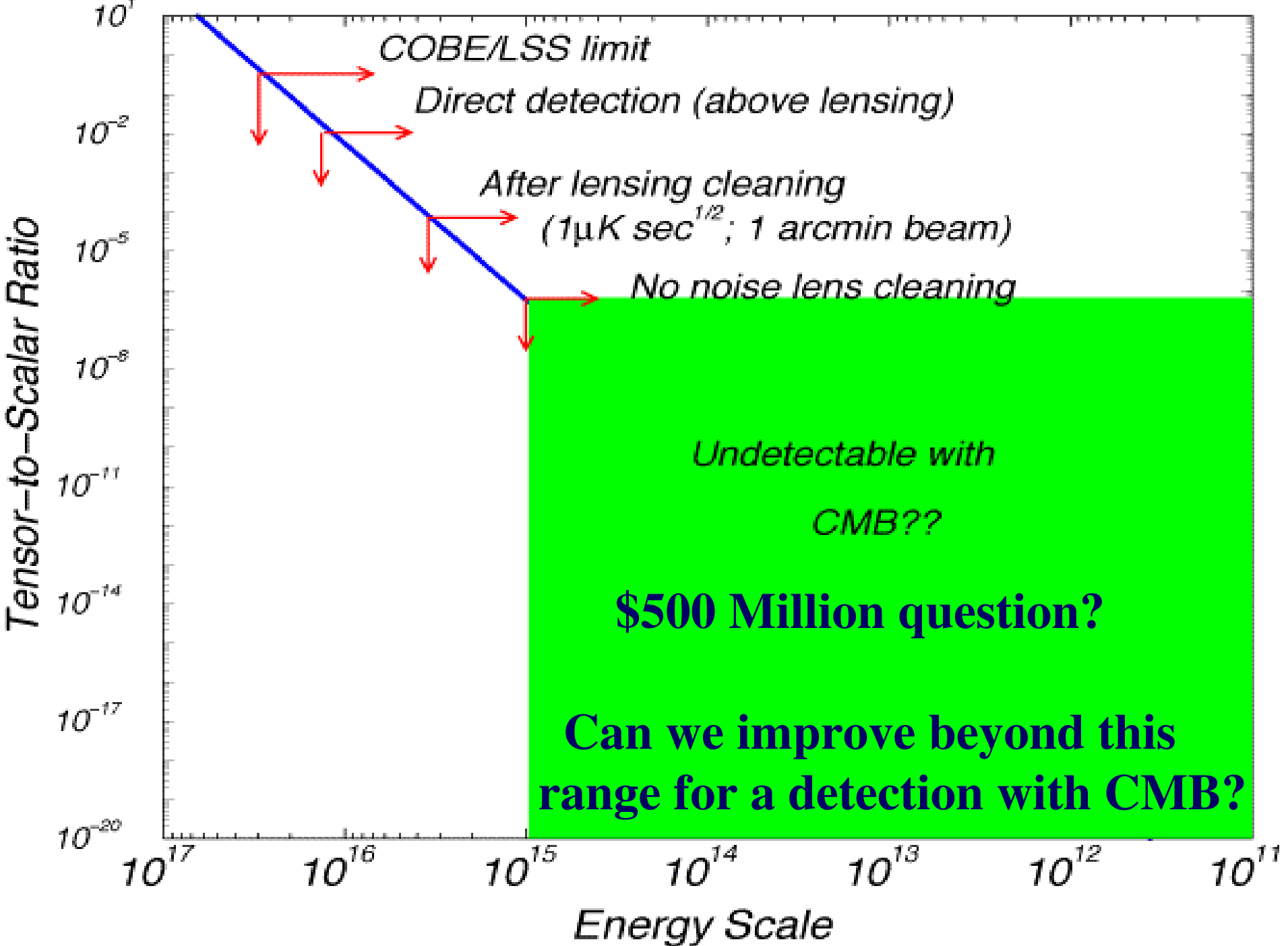


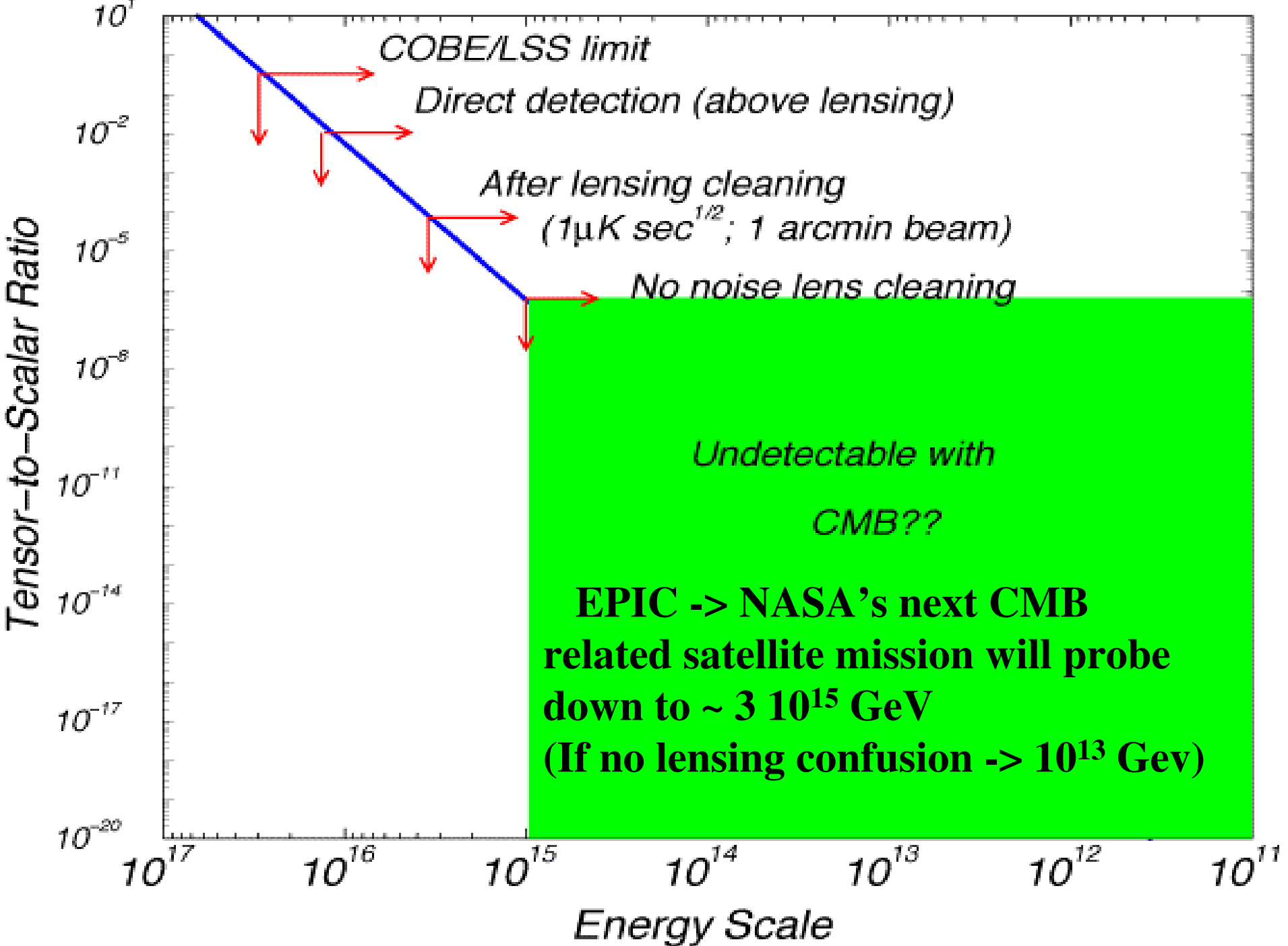


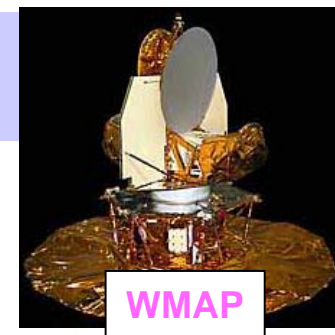
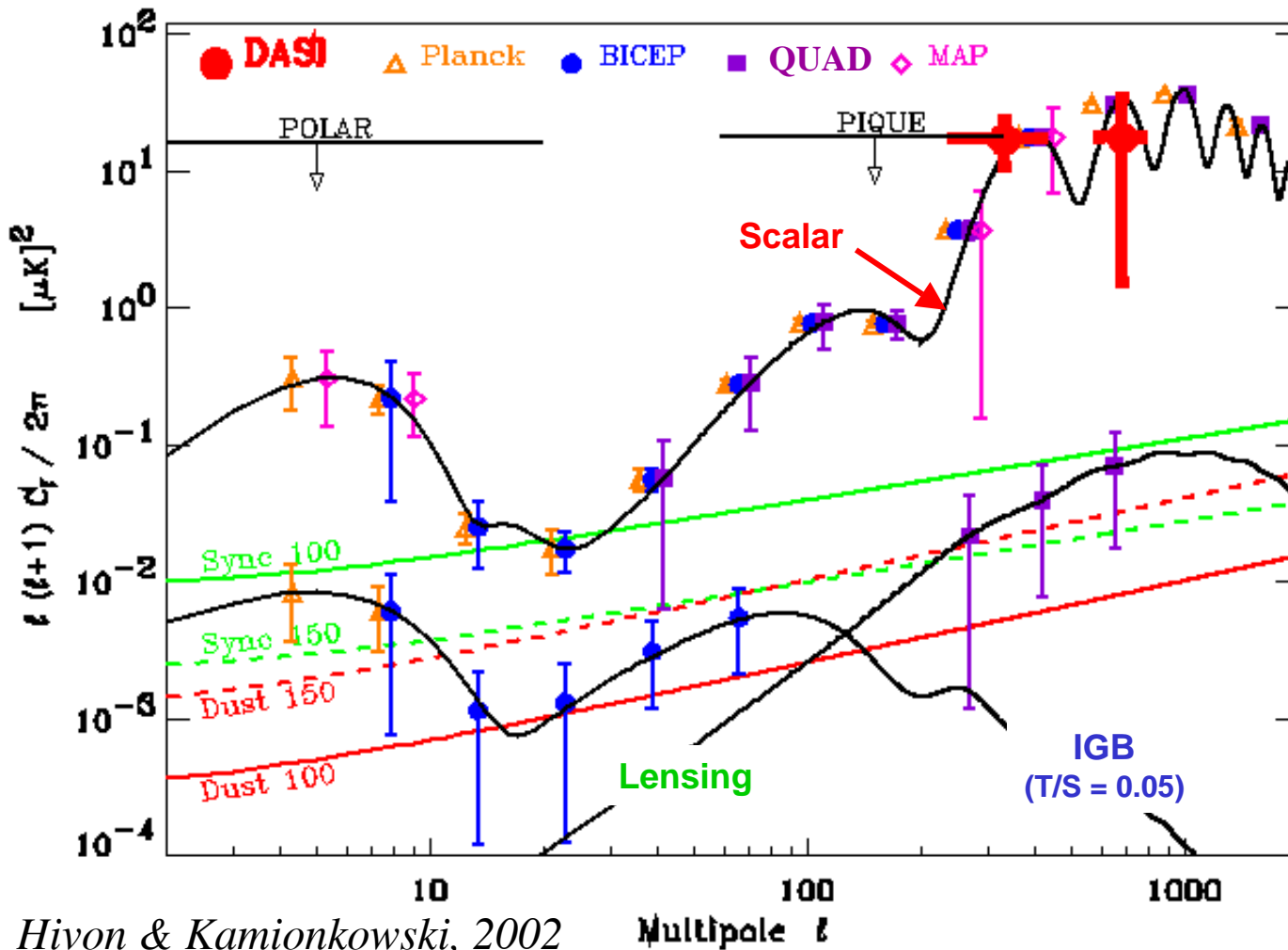








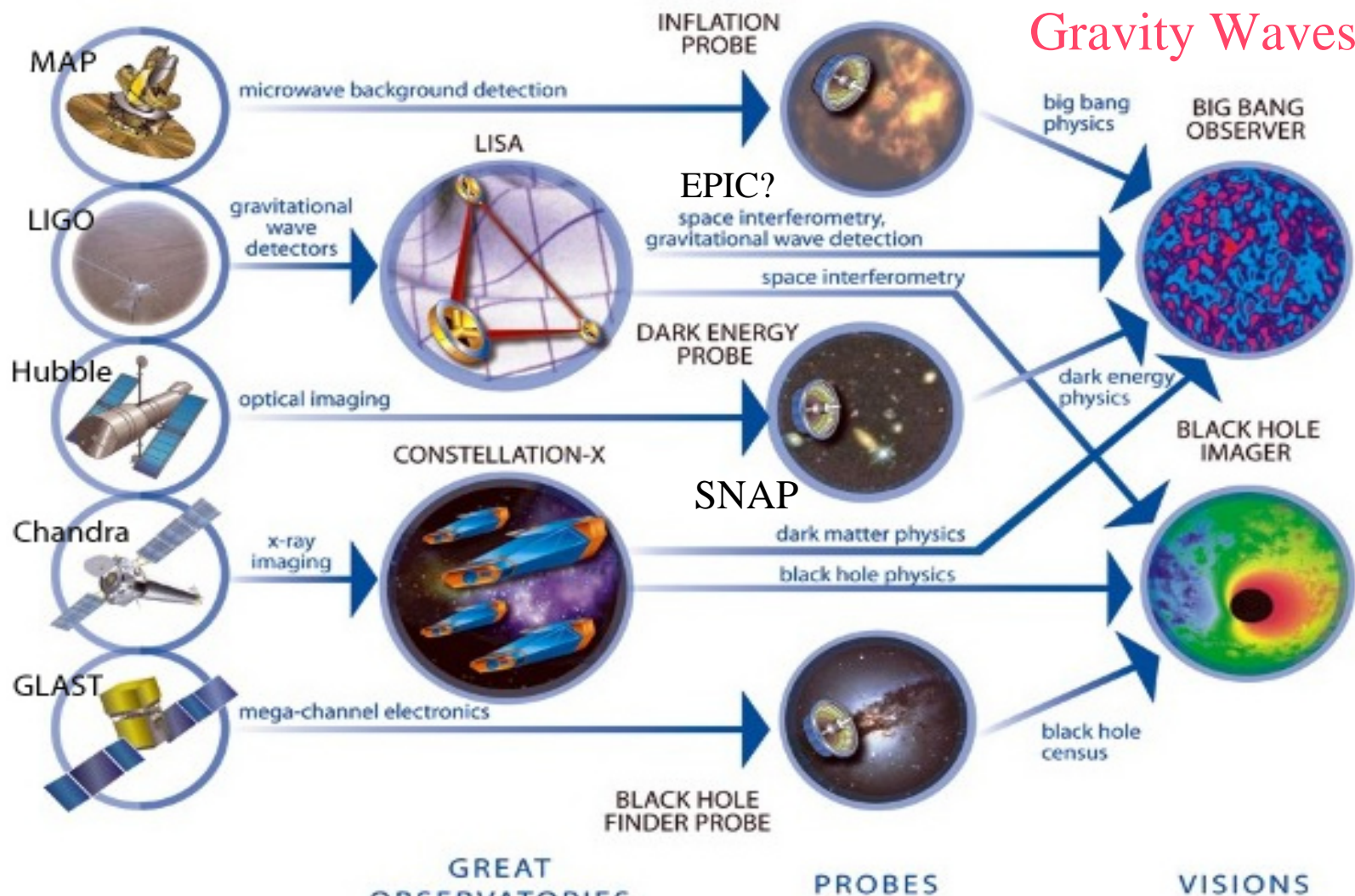




We're soon to learn a great deal more about:

- Scalar and lensing signals
- Methodology
- Foregrounds
- Technology

NASA's *Beyond Einstein* Program

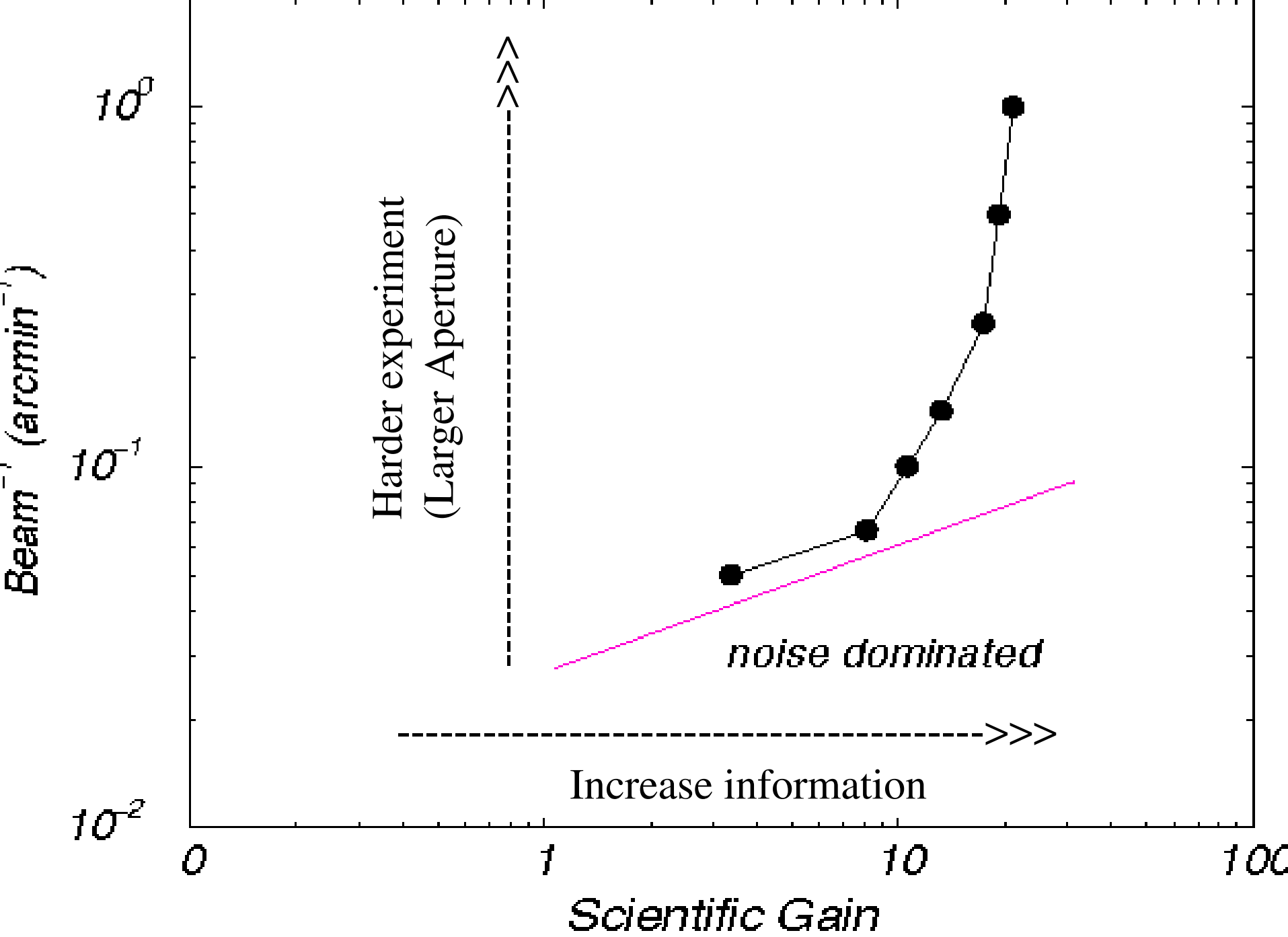


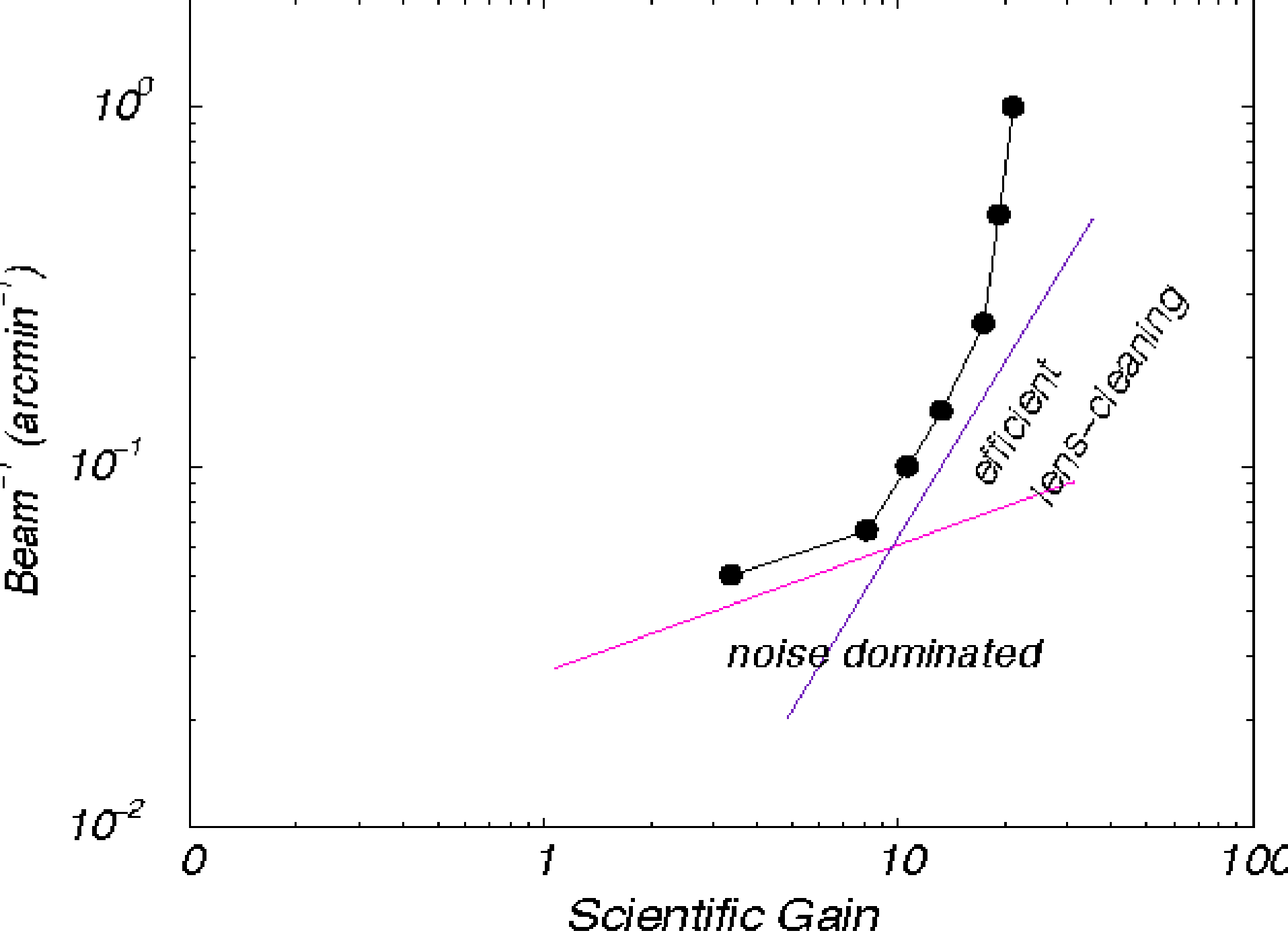
**Current
Missions**

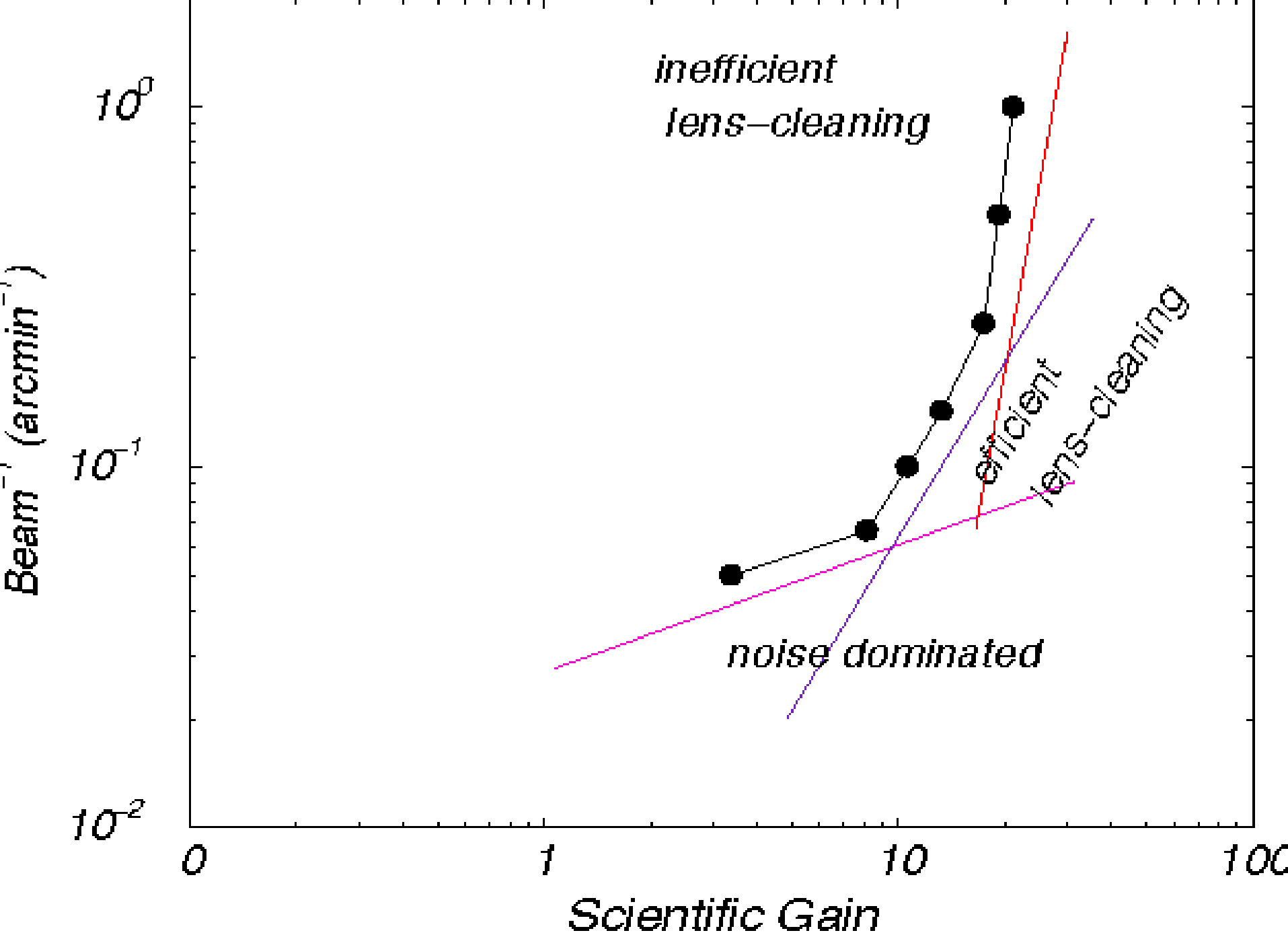
**Broad sciences/
Major resources
Community-class**

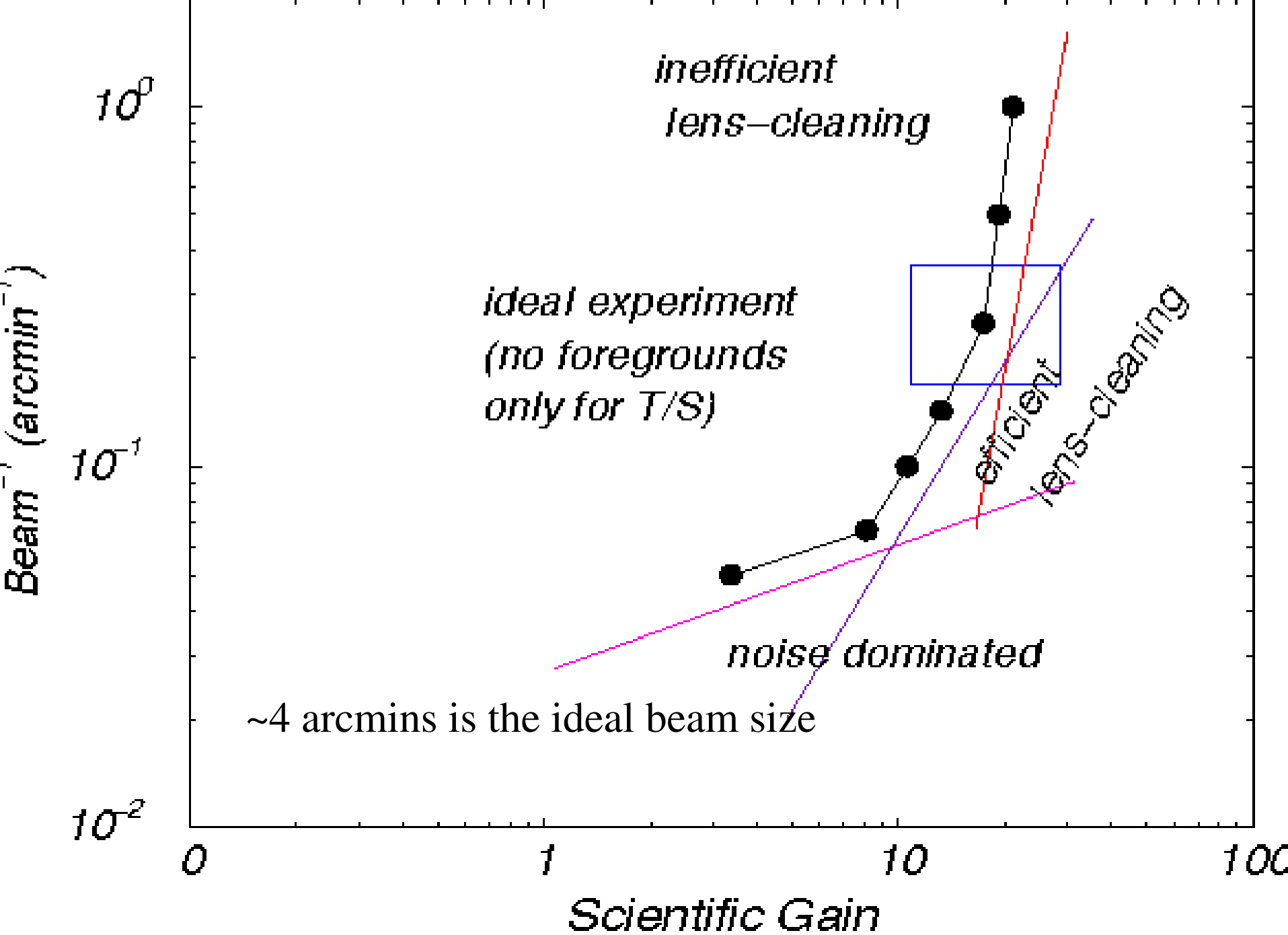
**Focused/narrow
sciences
PI-class**

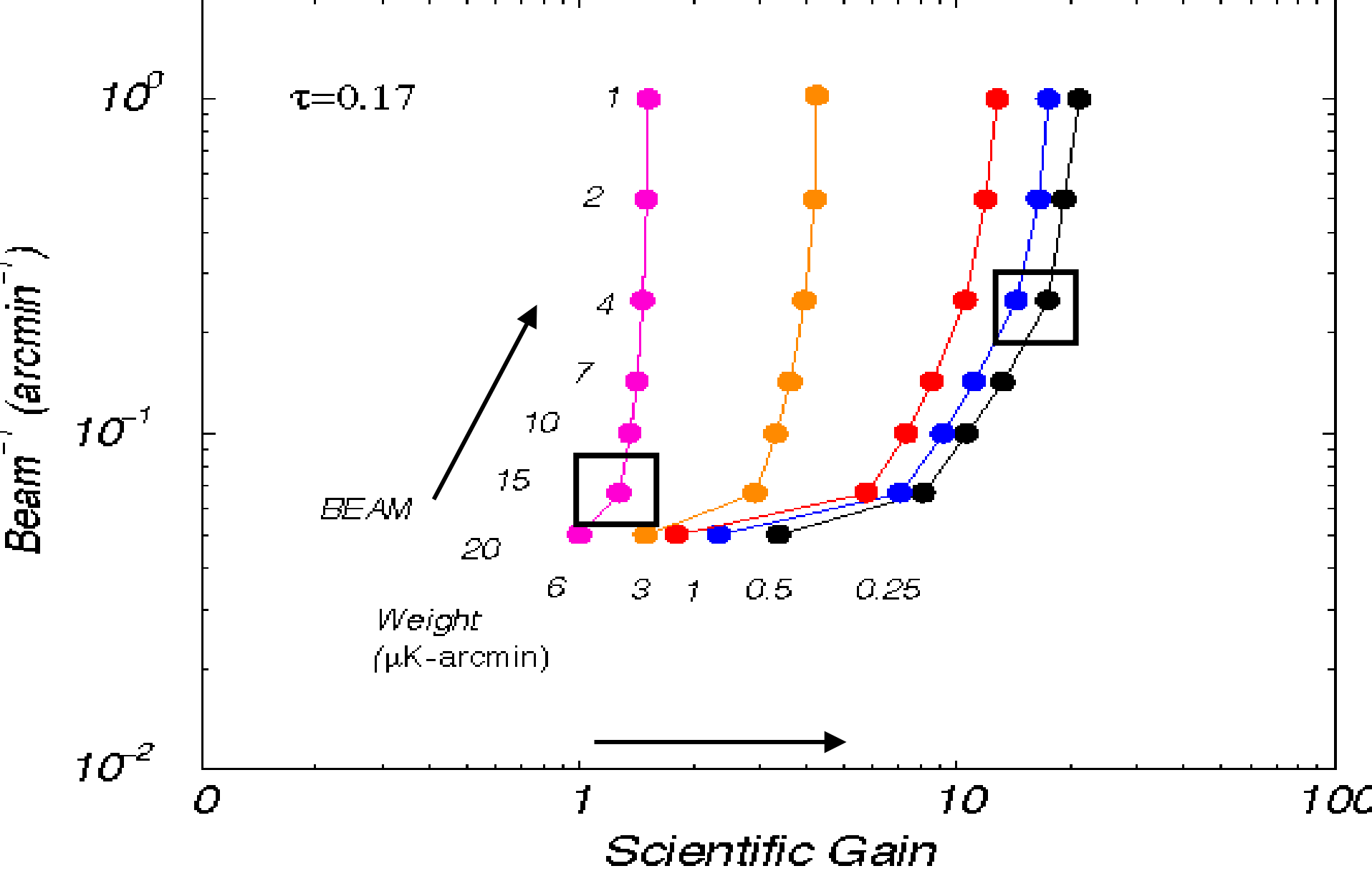
**After significant developments
(both hardware/theory)
> 25 year time-scales**











Ideal beam size depends on noise. For weight < 1 μK-arcmins, 4 arcmins is adequate.

EPIC: Exploration Probe of Inflationary Cosmology

Selected by NASA for Phase A study and technology demonstration

Final selection/decision in about 2-3 years with launch ~ 2014 (?).

Primary working group:

Collaboration of ~60 members.
(mostly west-coast institutions)

James Bock (PI; JPL)

Asantha Cooray

Mark Dragovan

Kris Gorski

Shaul Hanany

Eric Hivon

Marc Kamionkowski

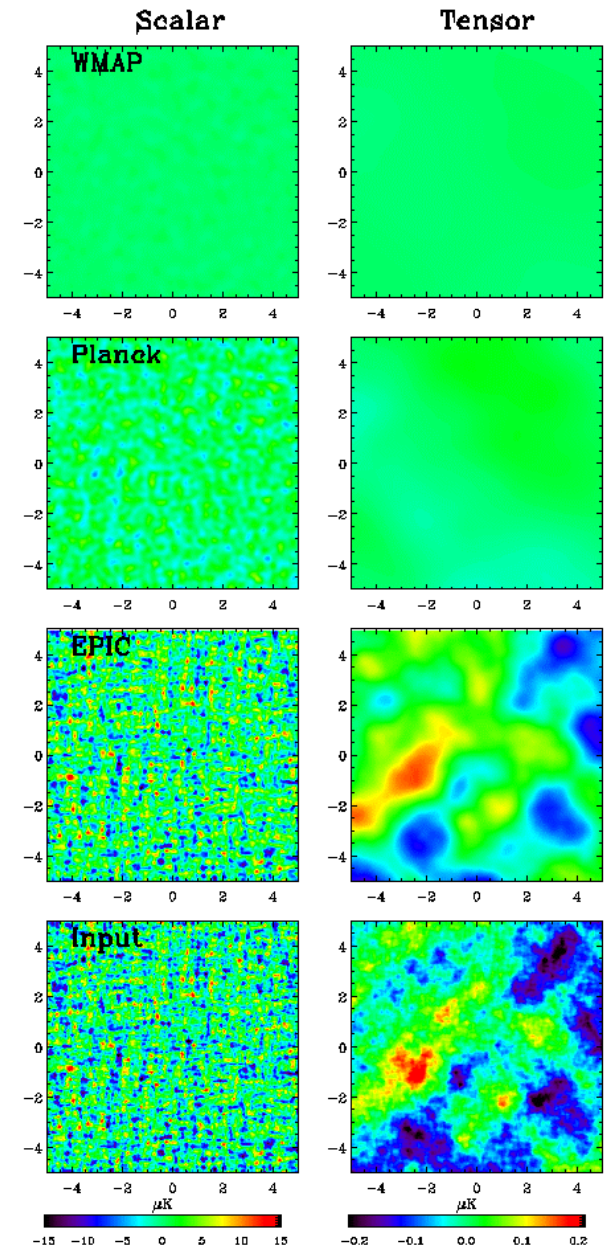
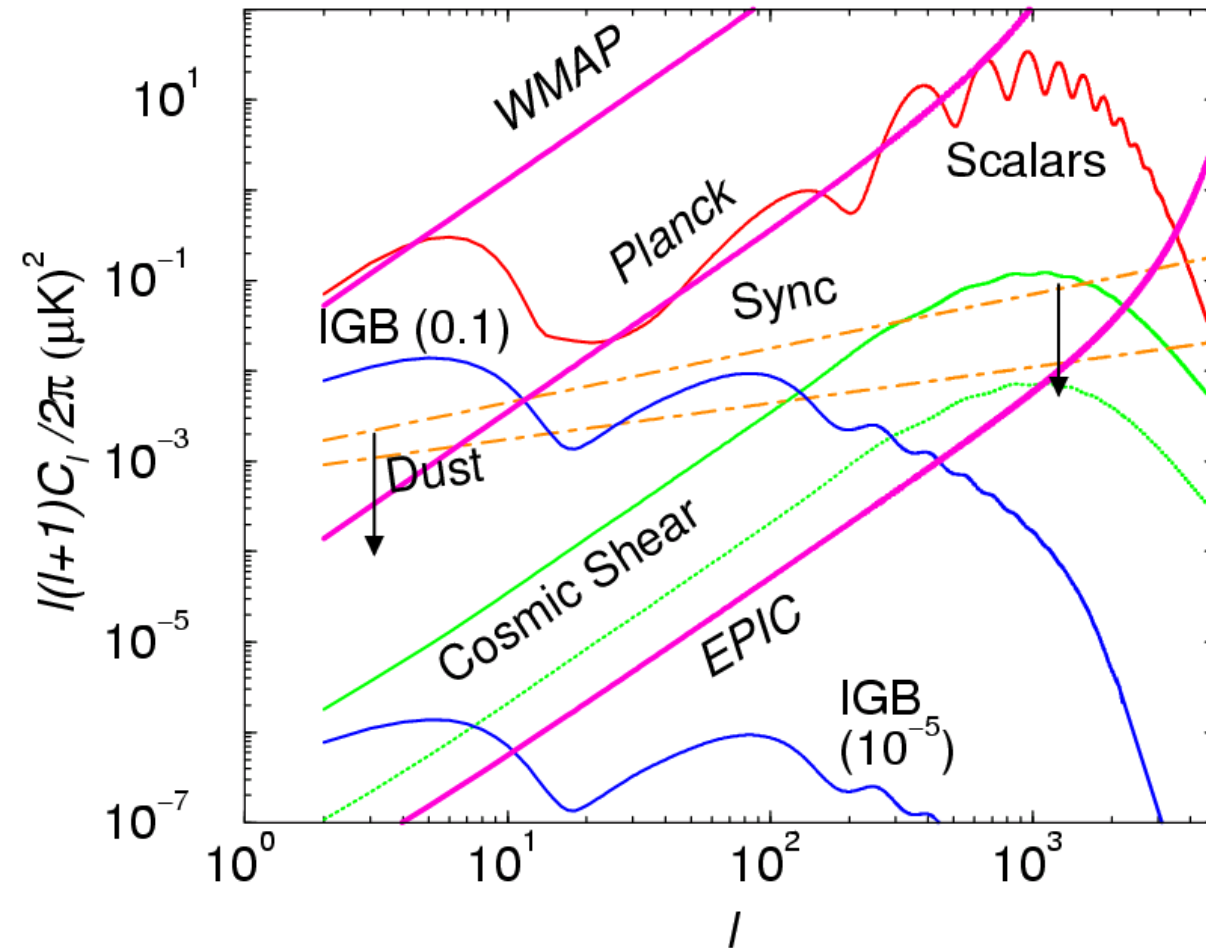
Brian Keating

Andrew Lange

Charles Lawrence

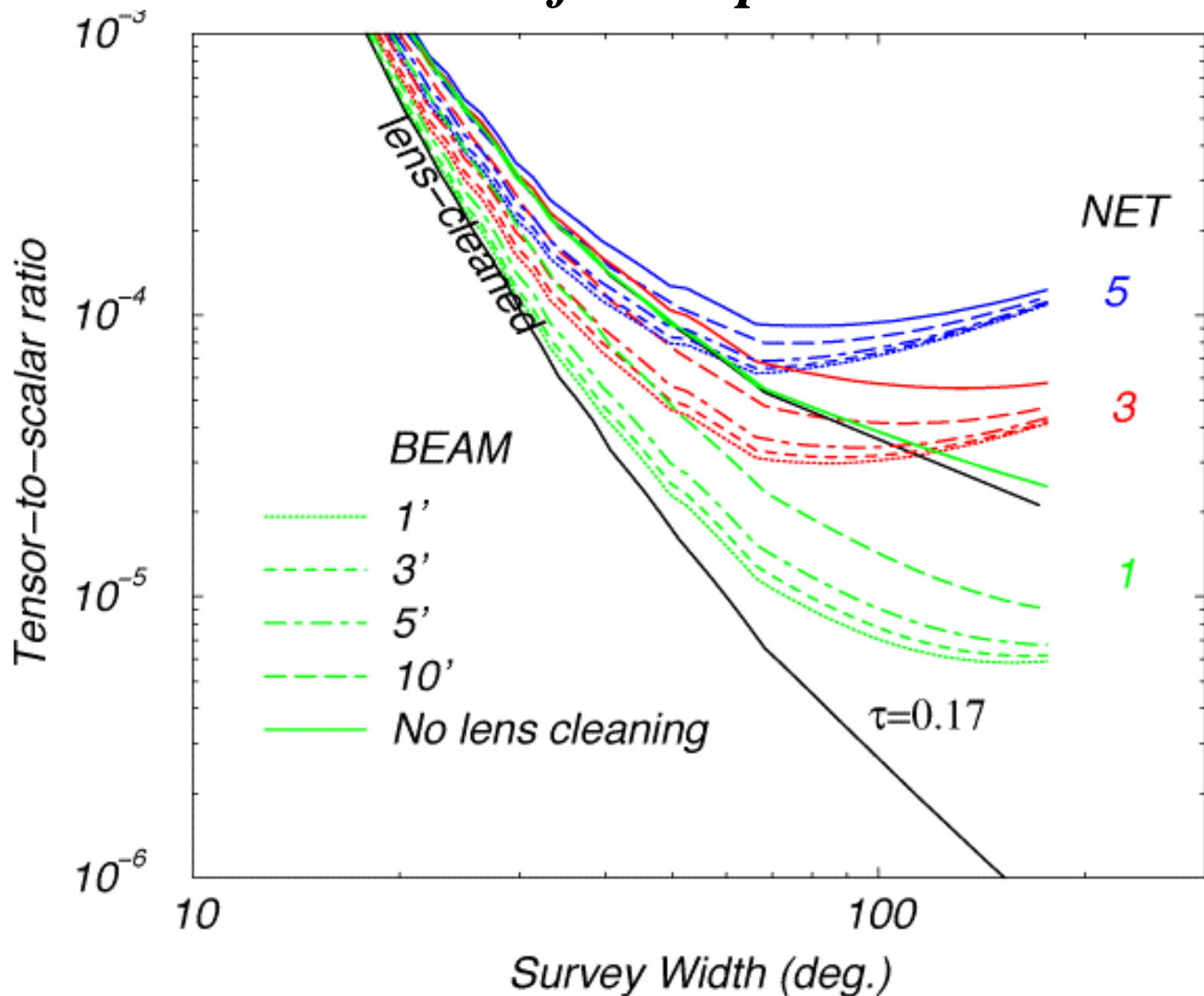
Adrian Lee

Mike Seiffert



Scalars = Polarization from density fluctuations
Cosmic Shear = Gravitational lensing of CMB by matter
IGB = Signal from Inflationary Gravitational-Wave Bkgd.

What kind of an experiment?



Planck bolos near photon noise limit

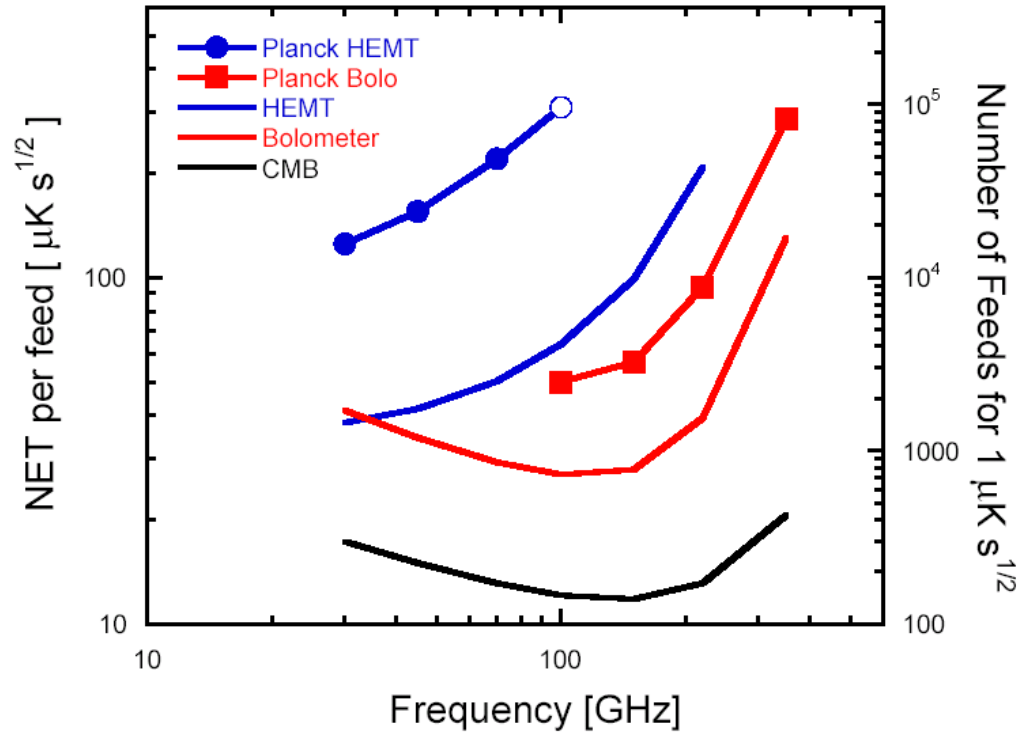
Need arrays for improved sensitivity

- $\sim 10^4$ detectors
- polarization sensitivity
- collimated beams
- physically large
- *no* mixed focal plane technology

Current and future focal planes

Freq	Future		Planck	
	NET (calc)	# feeds for $1 \mu\text{K}\sqrt{s}$	NET (goal)	# feeds
30	38	1500	125	2
45	42	1750	155	3
70	25	750	220	6
100	25	750	55	4
150	25	750	57	4
220	38	1500	95	4
350			290	4

Detectors for CMB Polarimetry



HEMTs

$T_A = 3h\nu/k$
 $\Delta\nu/\nu = 30\%$
 Q&U / feed

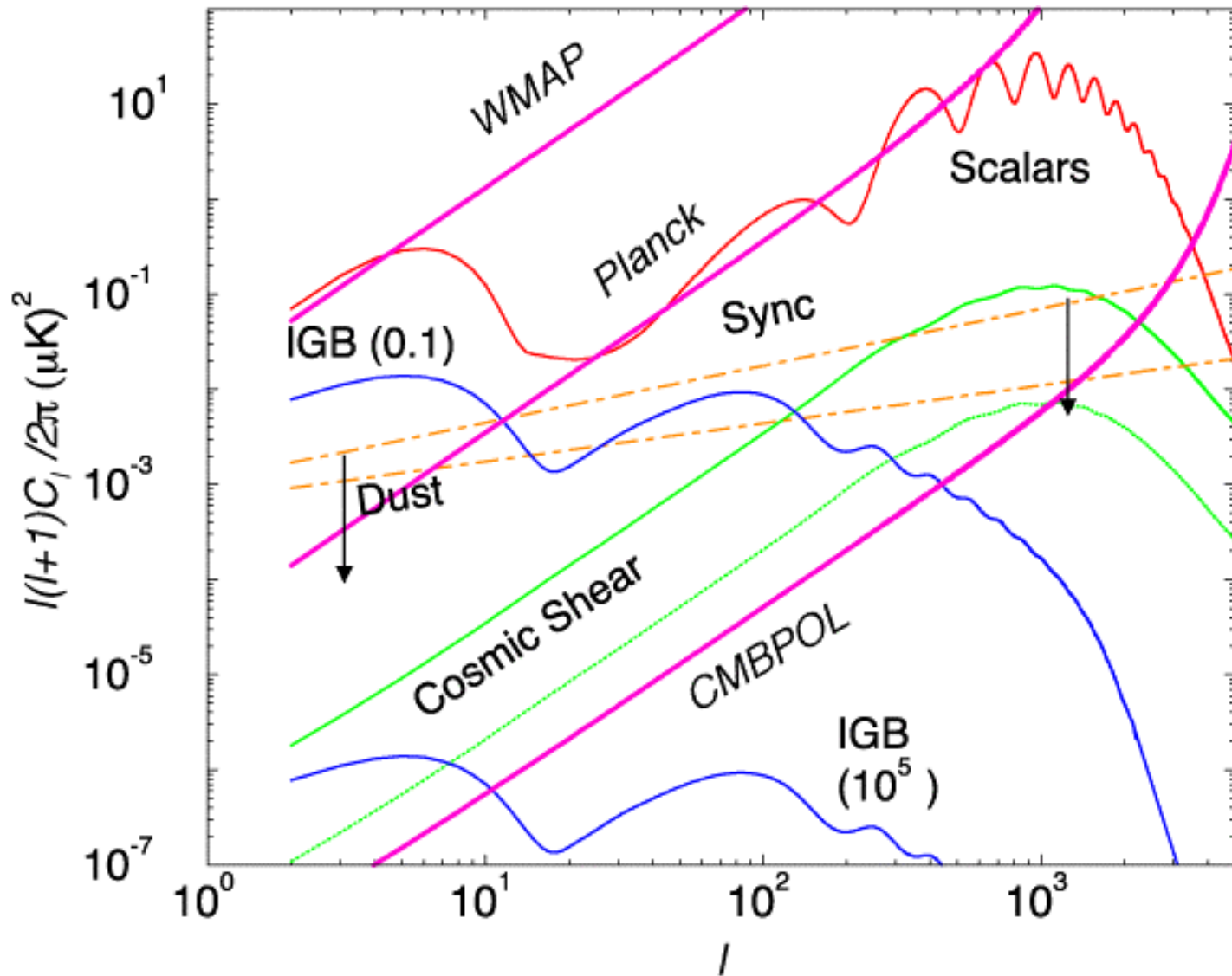
VS.

Bolometers

$\eta_{\text{opt}} = 50\%$
 $\Delta\nu/\nu = 30\%$
 $Q_{\text{max}}/Q_0 = 5$

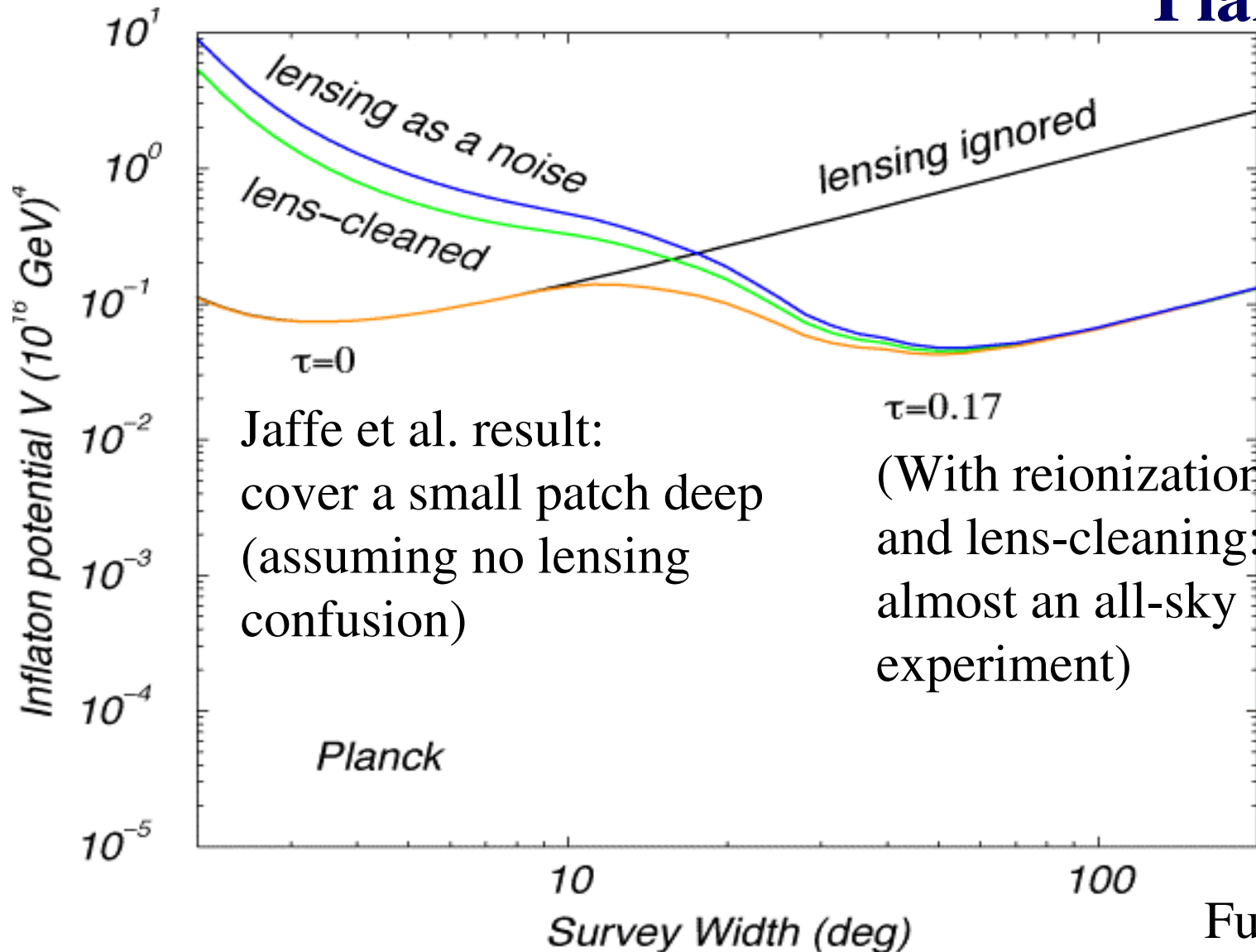
1 % emissive 60 K telescope

Lensing vs. Gravitational-Waves



Why we need EPIC

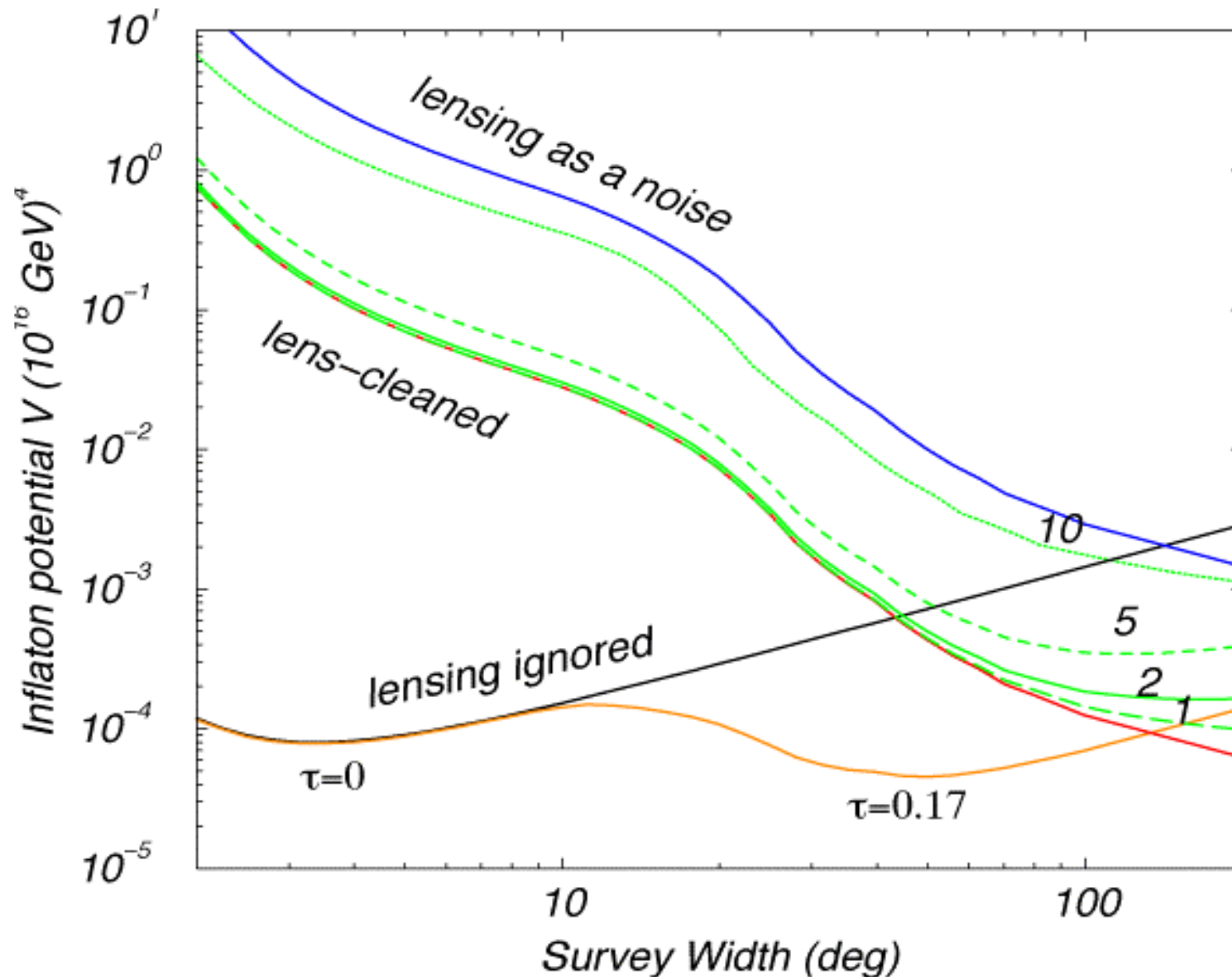
Planck

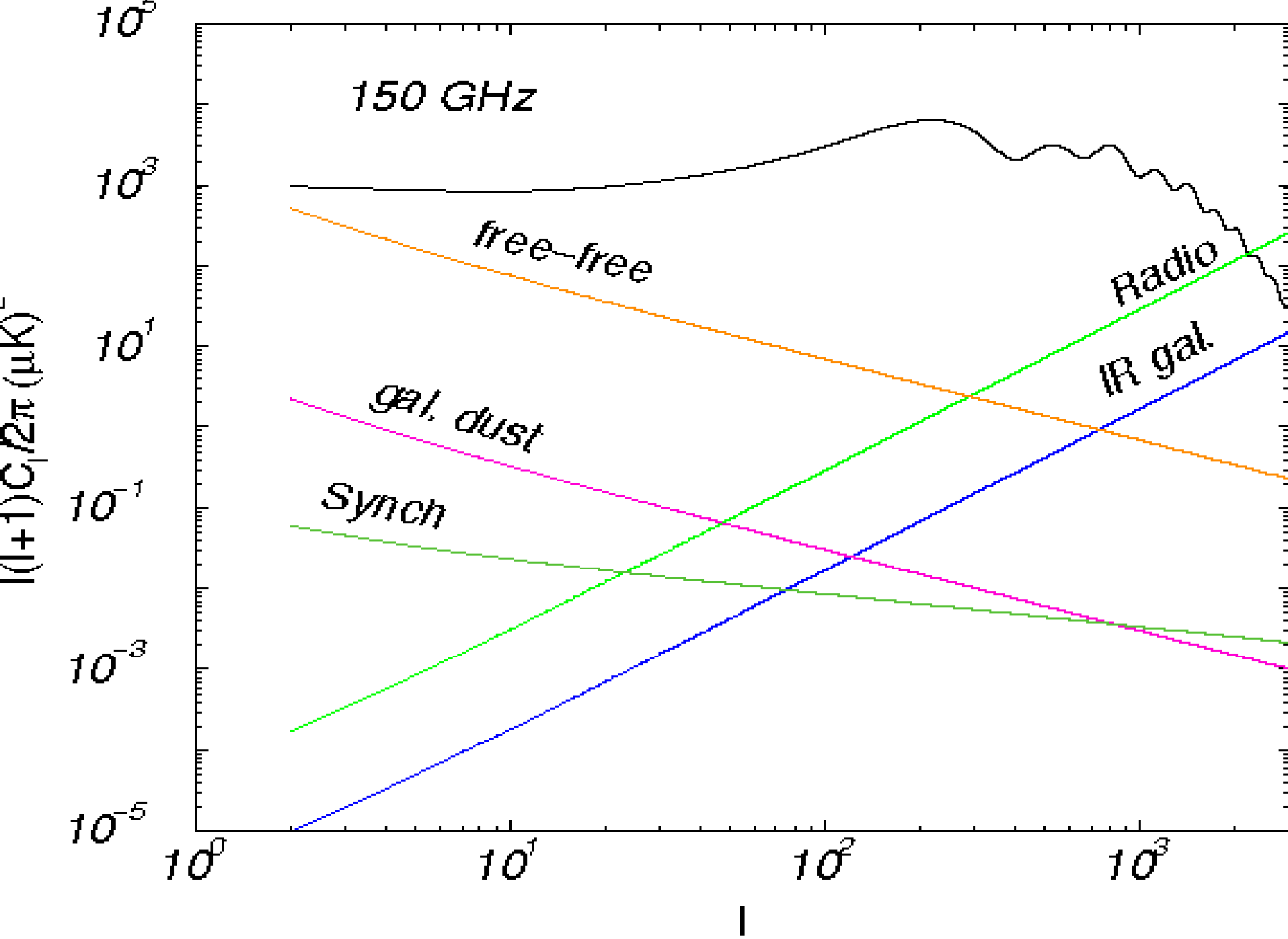


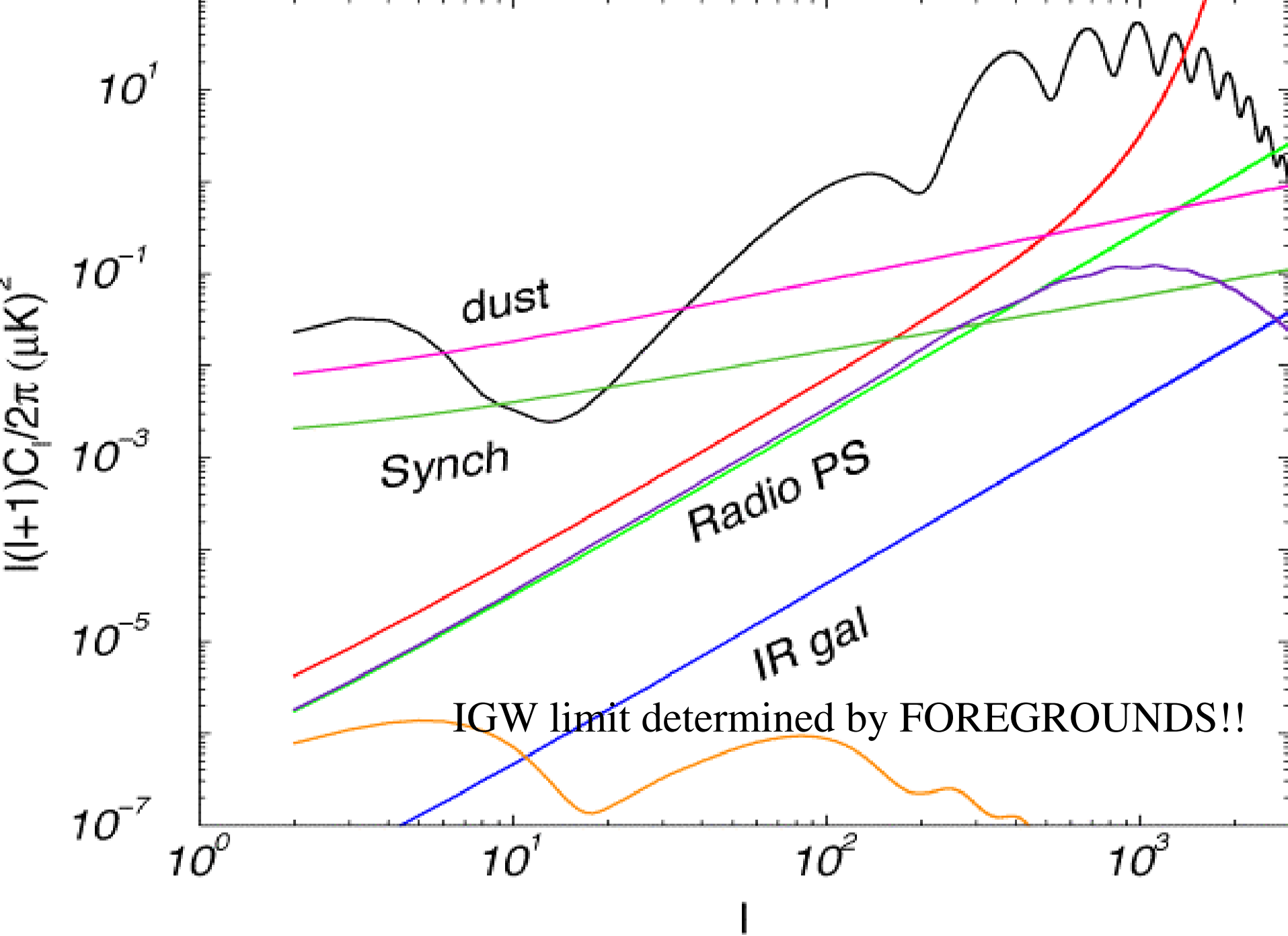
Jaffe et al. result:
cover a small patch deep
(assuming no lensing
confusion)

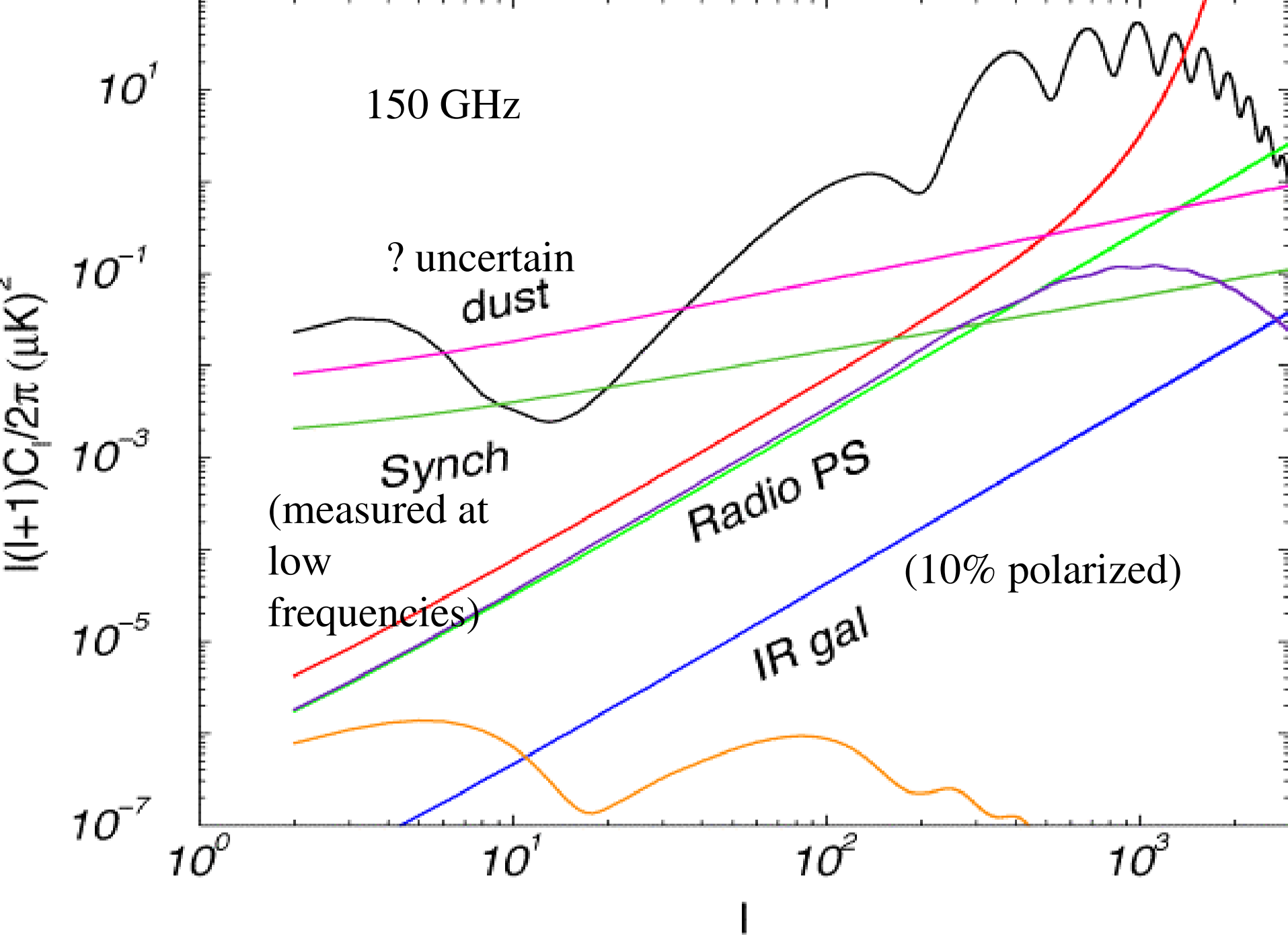
(With reionization
and lens-cleaning:
almost an all-sky
experiment)

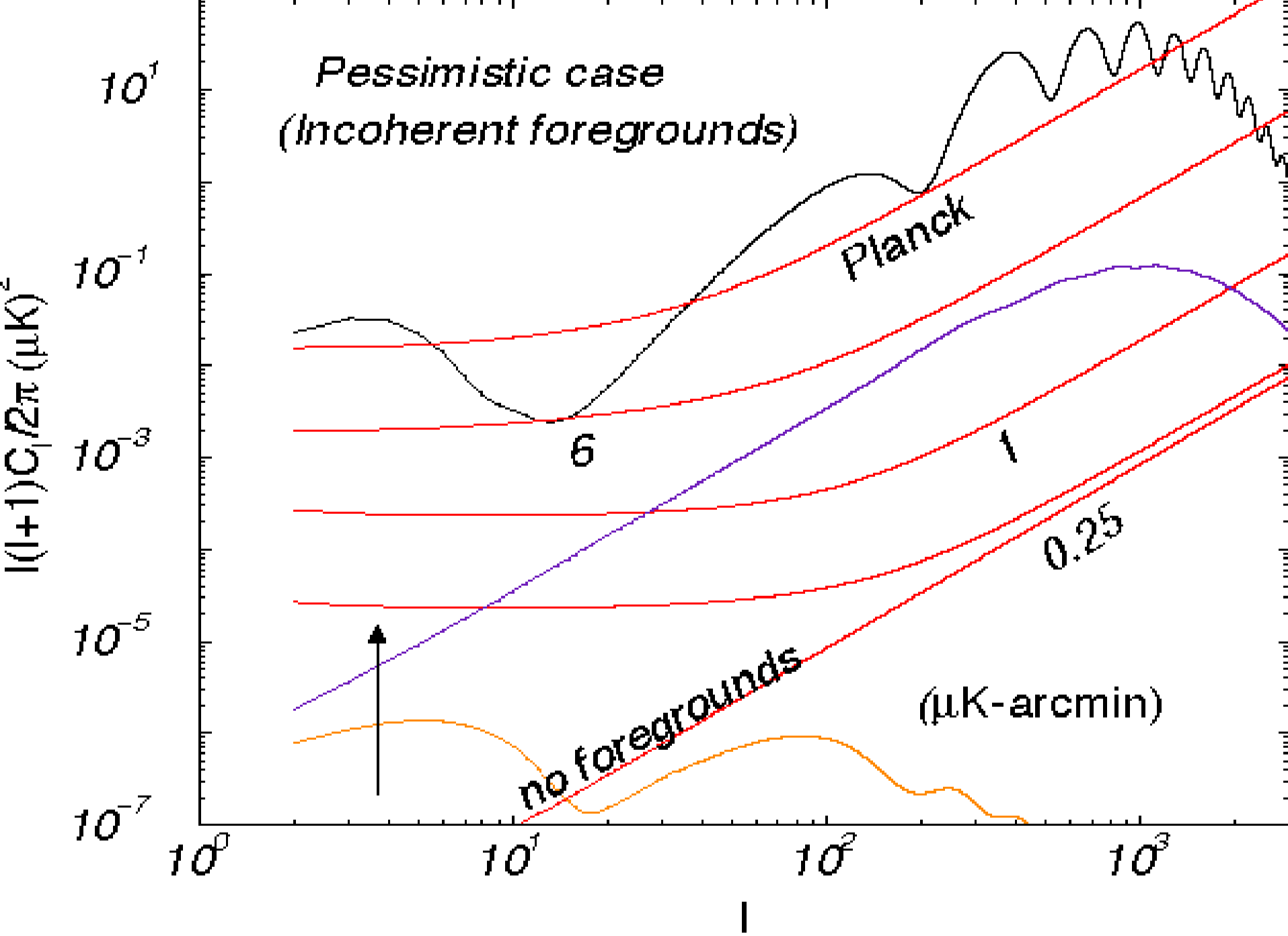
EPIC (Exploration Probe of Inflationary Cosmology)

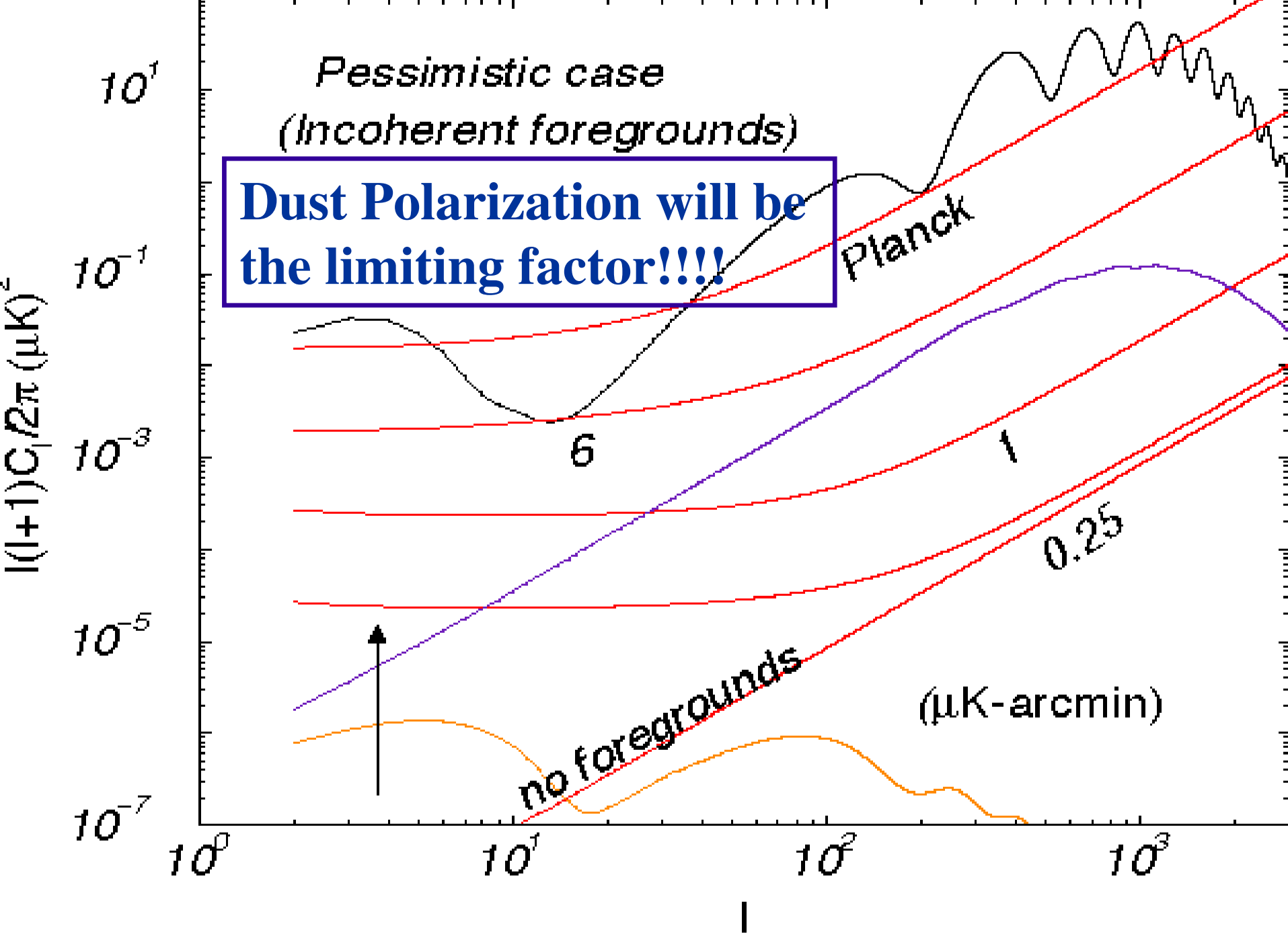




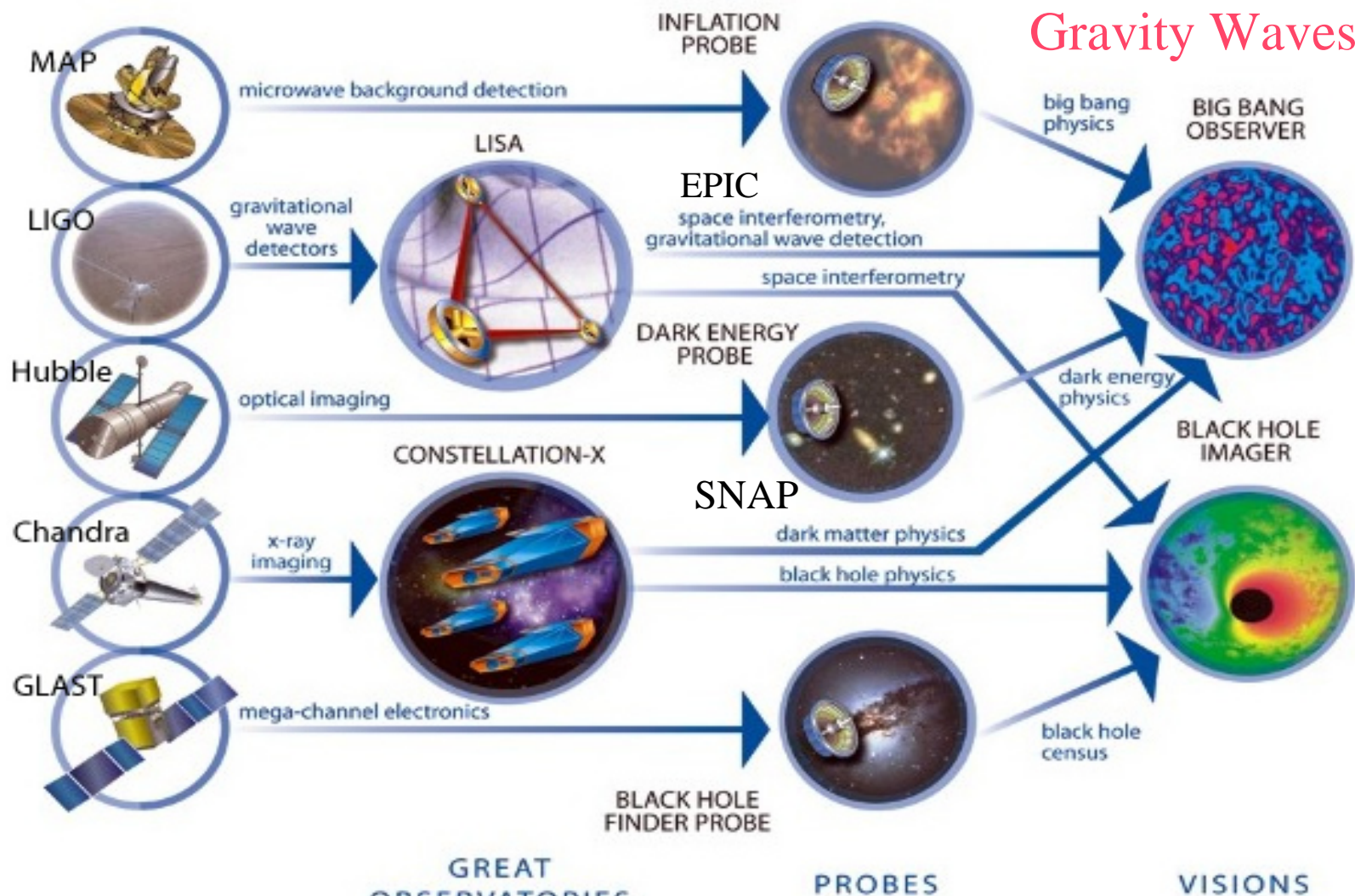








NASA's *Beyond Einstein* Program

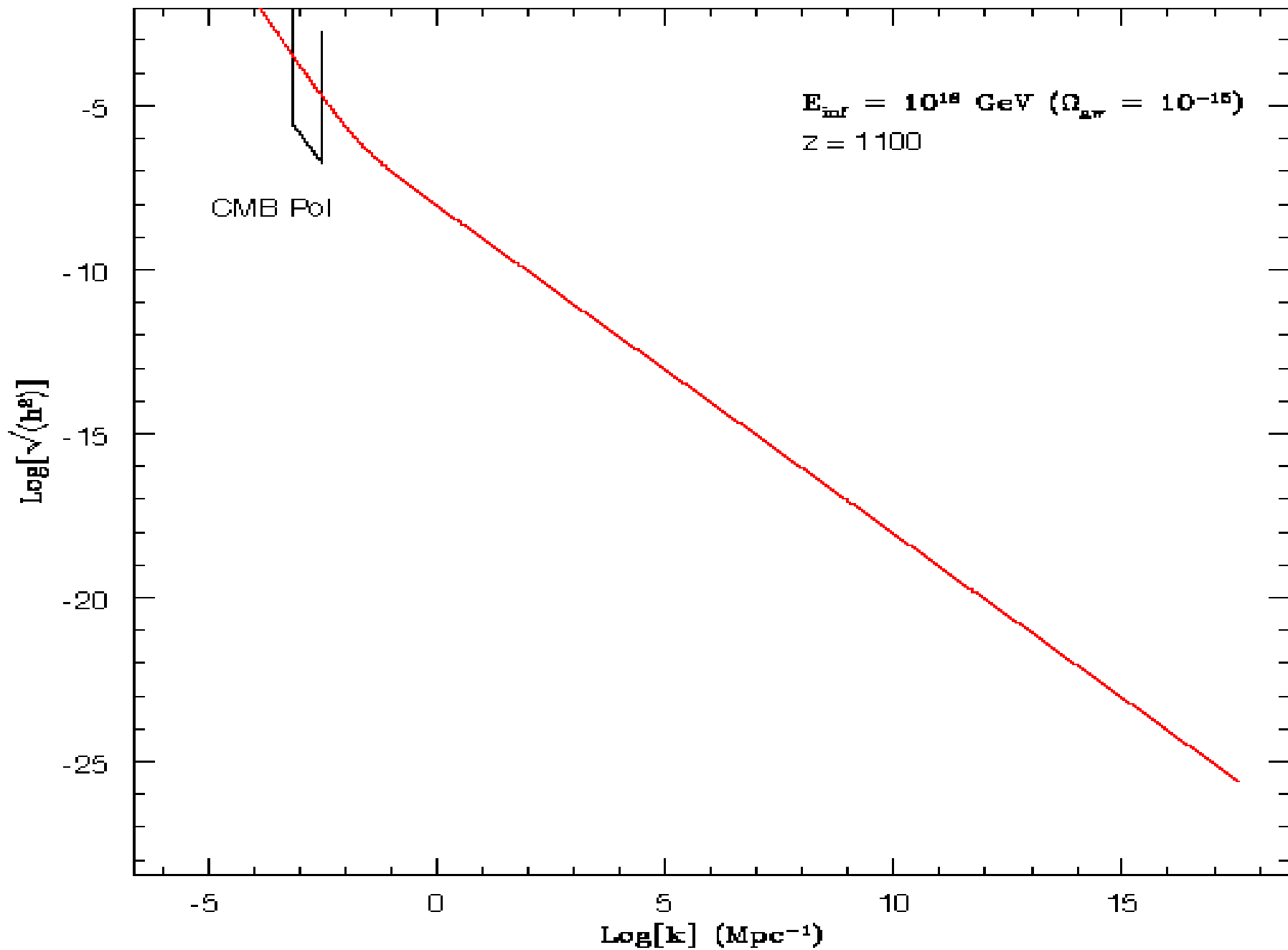


**Current
Missions**

**Broad sciences/
Major resources
Community-class**

**Focused/narrow
sciences
PI-class**

**After significant developments
(both hardware/theory)
> 25 year time-scales**



**Modes entered during matter
domination**

$$h_{rms} \sim k^{-2}$$

$$E_{\text{inf}} = 10^{18} \text{ GeV } (\Omega_{\text{dark}} = 10^{-15})$$
$$z = 1100$$

CMB Pol

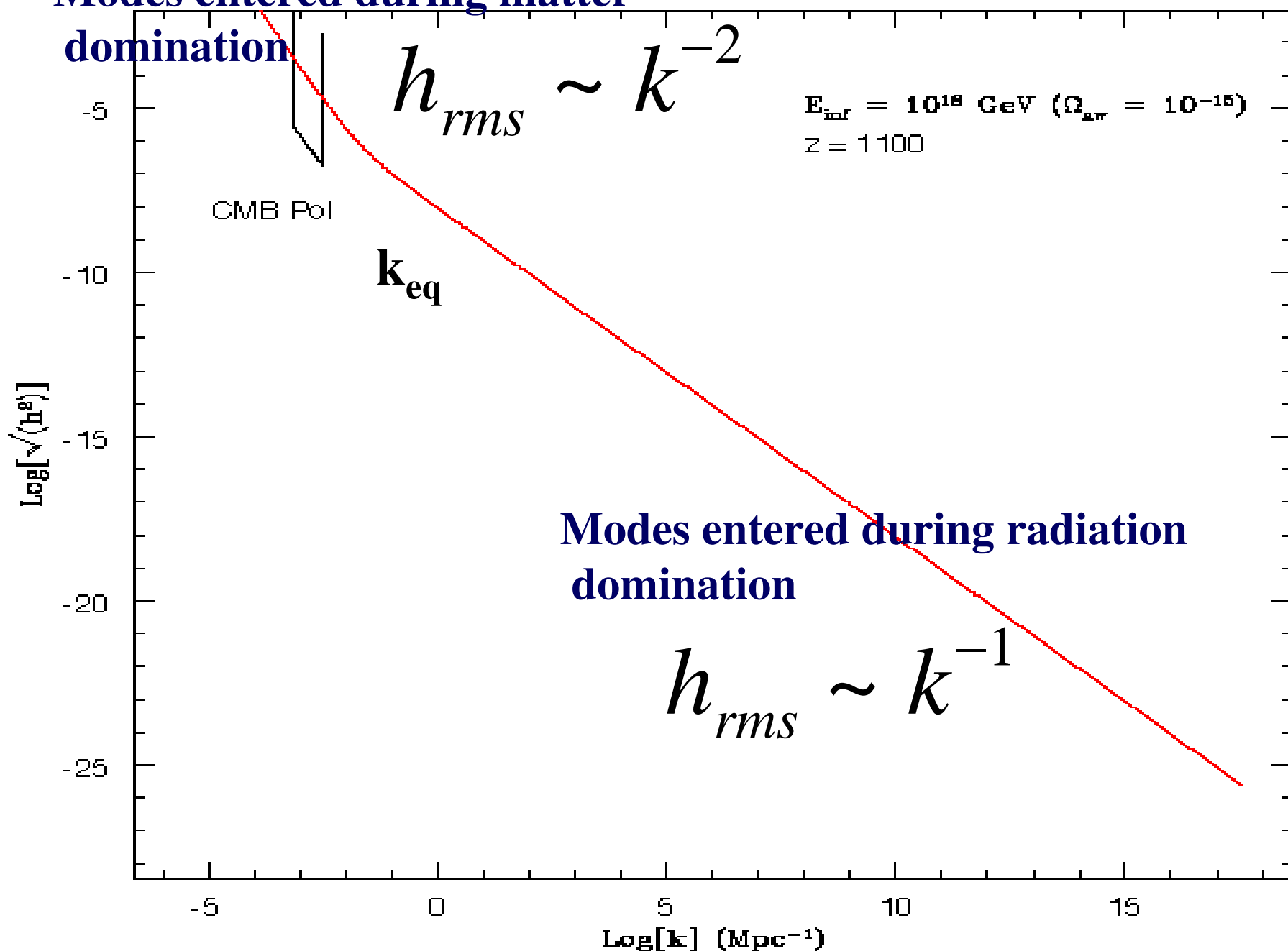
k_{eq}

**Modes entered during radiation
domination**

$$h_{rms} \sim k^{-1}$$

$\text{Log}[\sqrt{\langle h^2 \rangle}]$

$\text{Log}[k] \text{ (Mpc}^{-1}\text{)}$



**Modes entered during matter
domination**

$$h_{rms} \sim k^{-2}$$

$$E_{\text{inf}} = 10^{18} \text{ GeV } (\Omega_{\text{dark}} = 10^{-15})$$
$$z = 1100$$

CMB Pol

k_{eq}

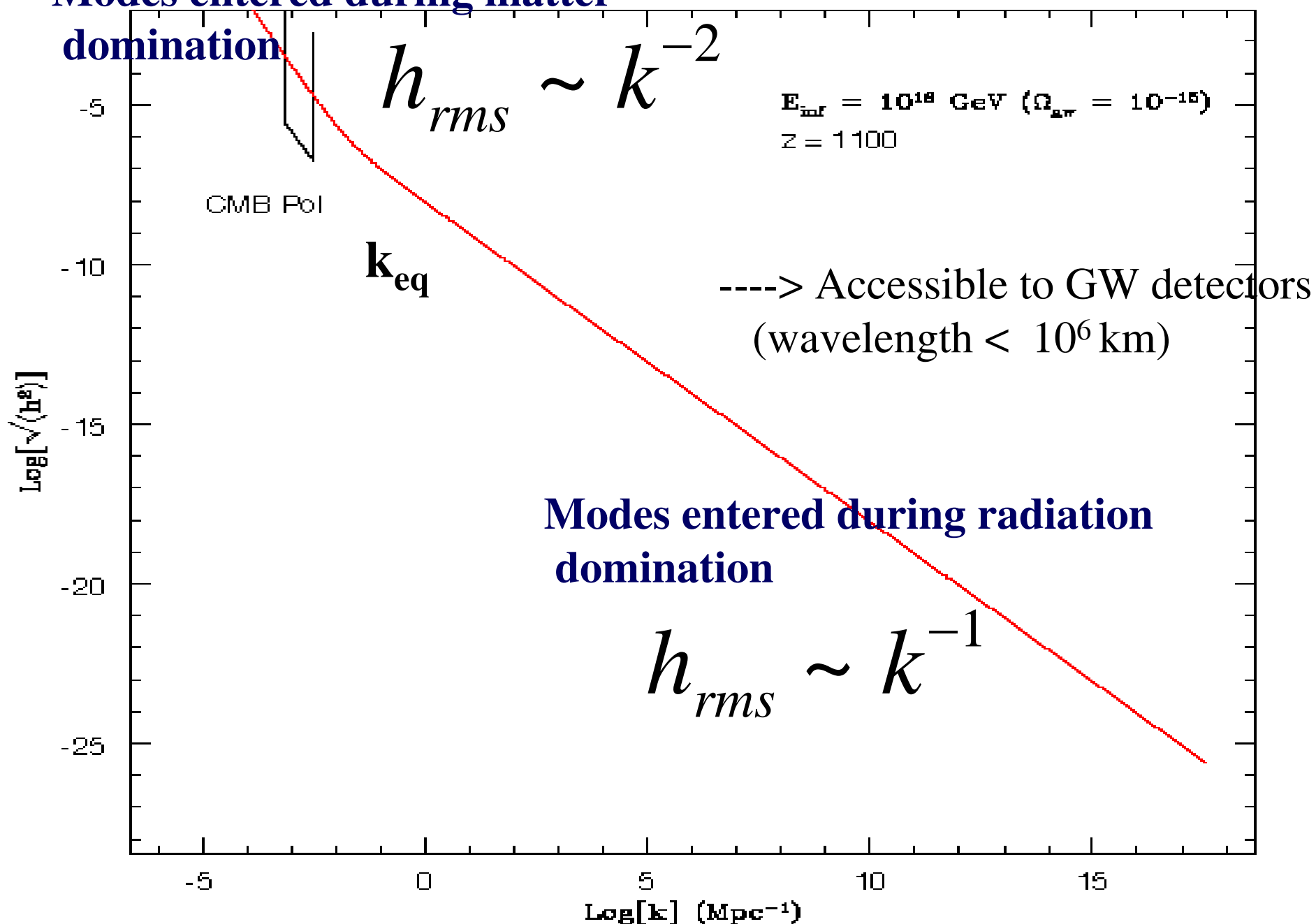
----> Accessible to GW detectors
(wavelength < 10^6 km)

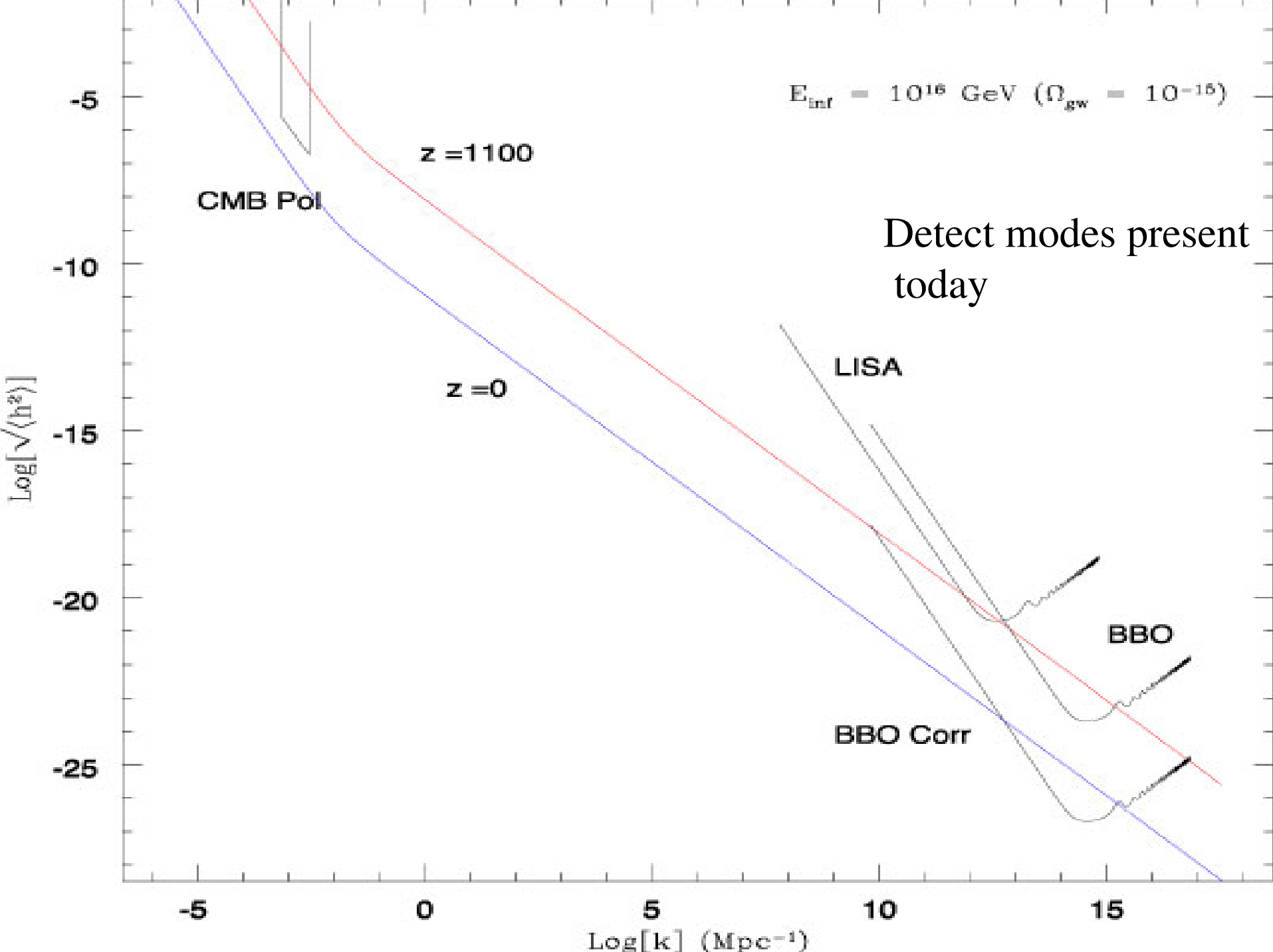
**Modes entered during radiation
domination**

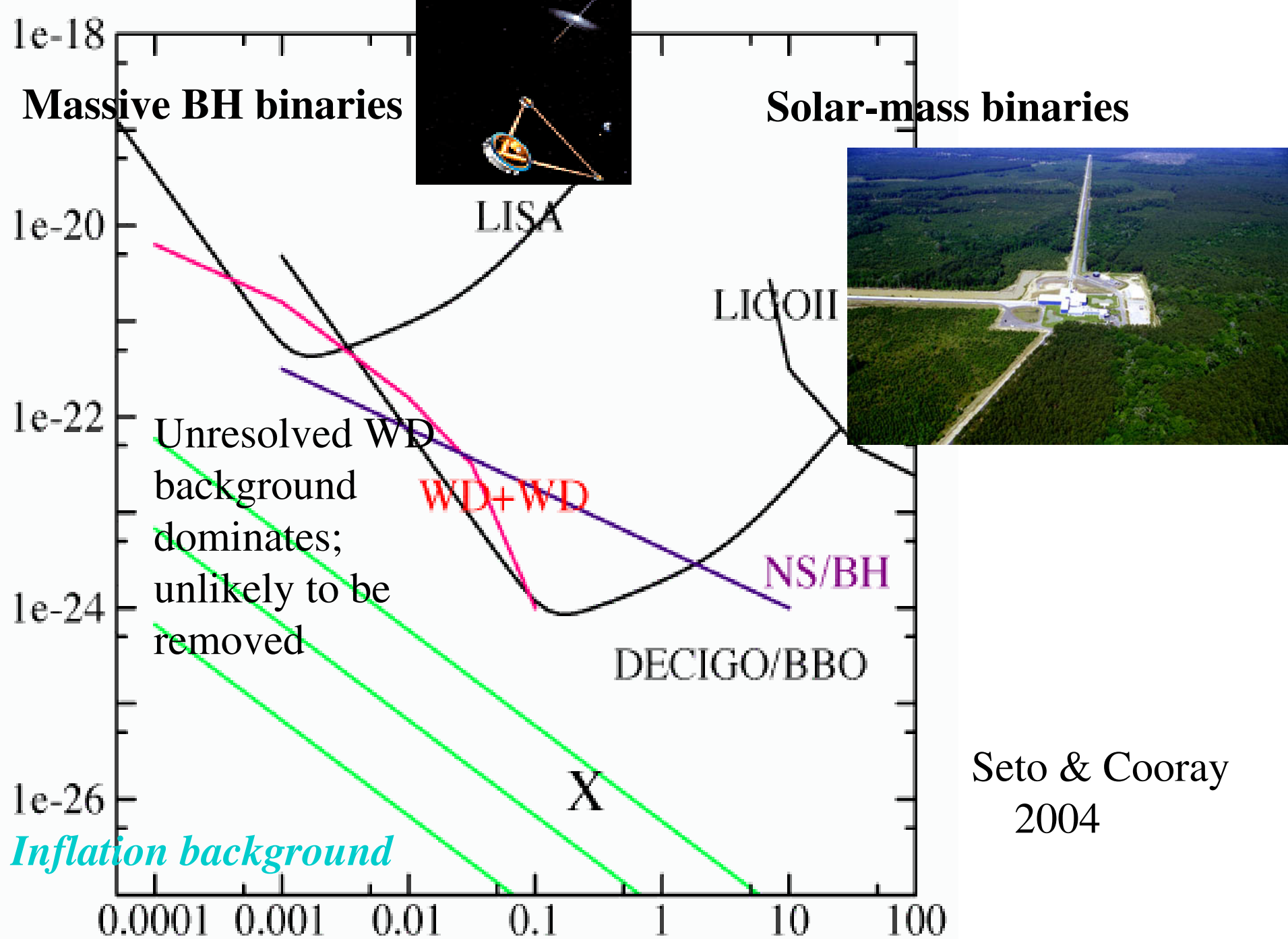
$$h_{rms} \sim k^{-1}$$

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$\text{Log}[k] \text{ (Mpc}^{-1}\text{)}$



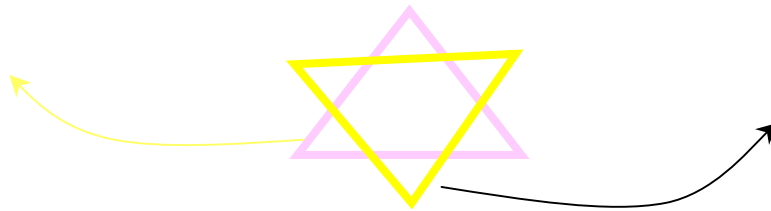




Correlation analysis (with 2 detectors)

$$s_1(t) = h(t) + n_1(t)$$

$$s_2(t) = h(t) + n_2(t)$$

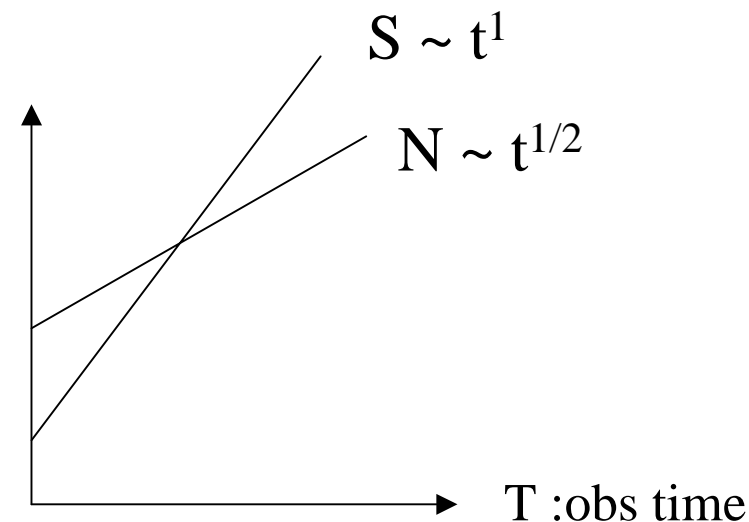
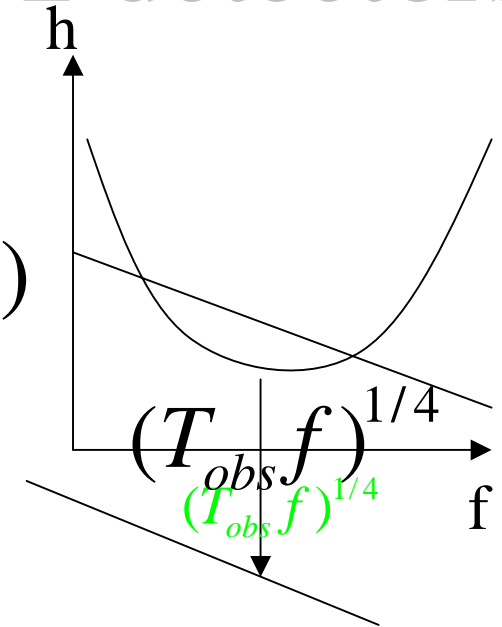


$$S = \int_0^T dt \int_0^T dt' s_1(t) s_2(t') Q(t - t')$$

$$\Rightarrow (h \bullet h) + (n_1 \bullet n_2)$$

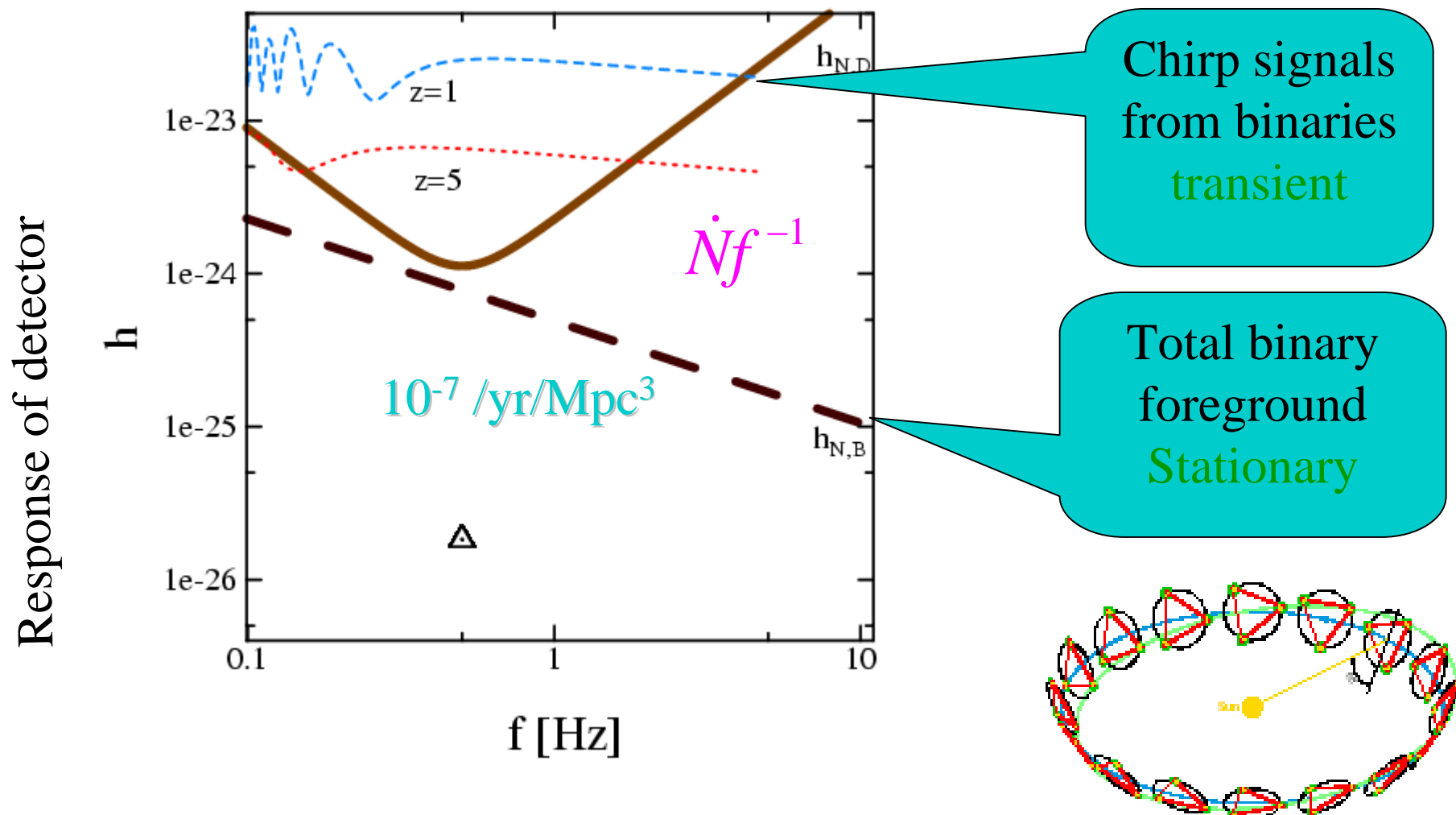
noise $\propto T^{1/2}$

$$\text{signal} \propto T \quad \text{noise} \propto T^{1/2}$$

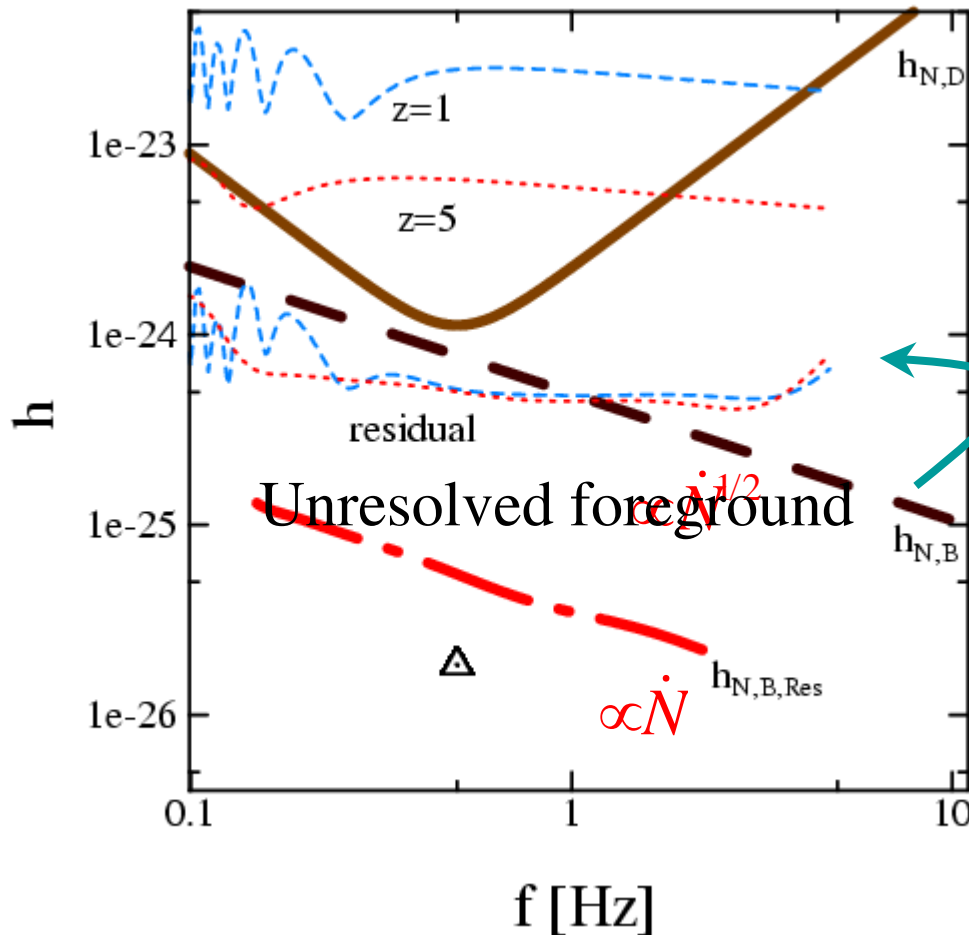


Reducing correlated noise is crucial for correlation analysis

Resolved binaries and their foreground



Residual noise levels after cleaning



Individual resolved NS+NS binaries

Binary foreground is common to two detectors and makes **correlated fitting residual**

■ Foreground reduced to 10% of original

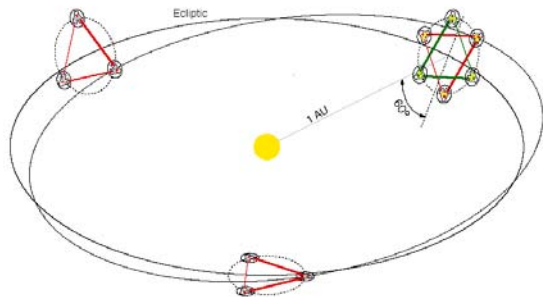
■ Critical coalescence rate around 1Hz

10^{-5} /yr/Mpc³

$$\dot{N}_{obs} f^{-1} \sim 1$$

The Big Bang Observer (BBO)

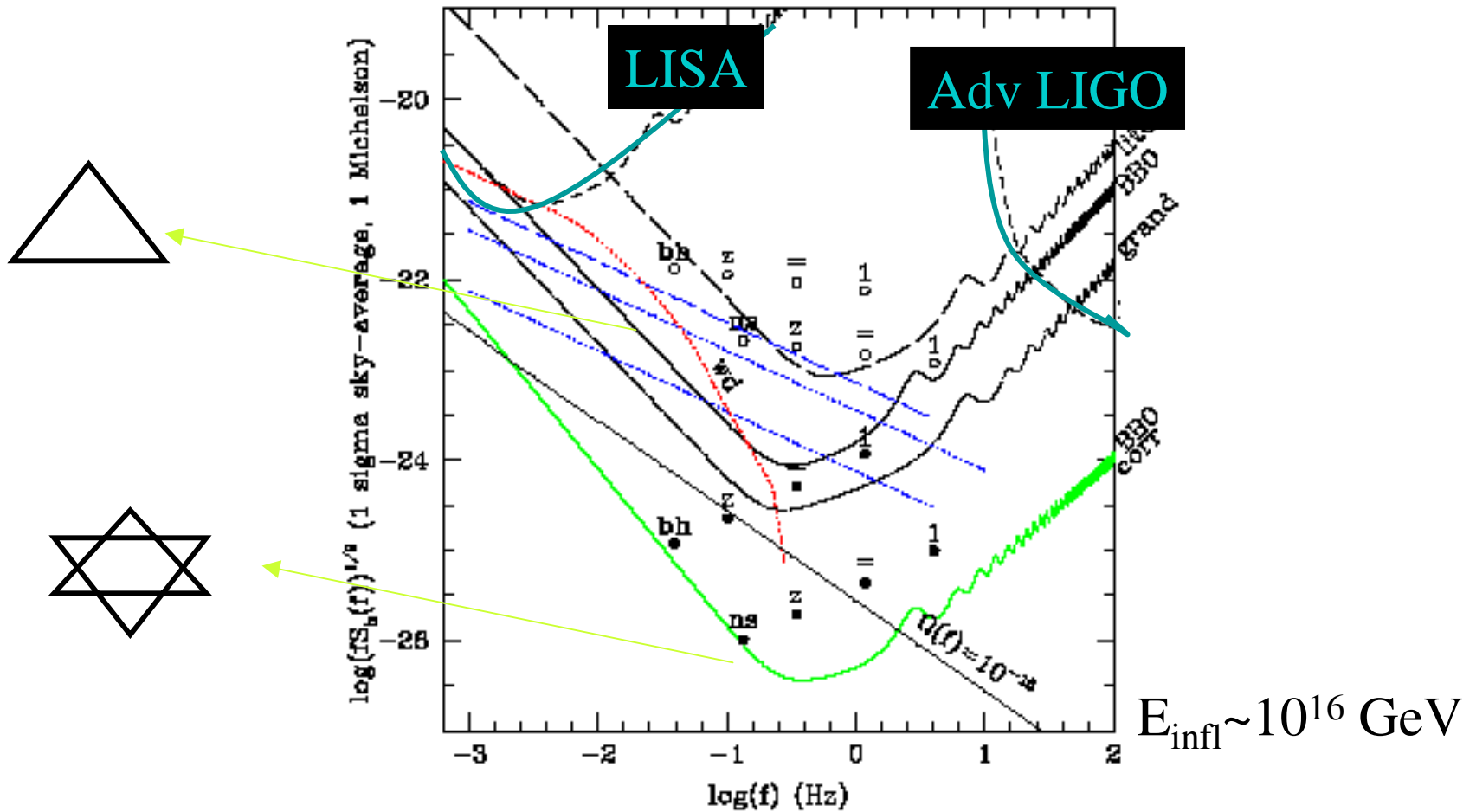
- NASA Vision mission (~2030 launch)
- Primary goal: direct detection of GW from inflation by correlation analysis around 0.1-1Hz
- LISA's follow-on



Example : a plan with 4 units

Phinney et al. 2003

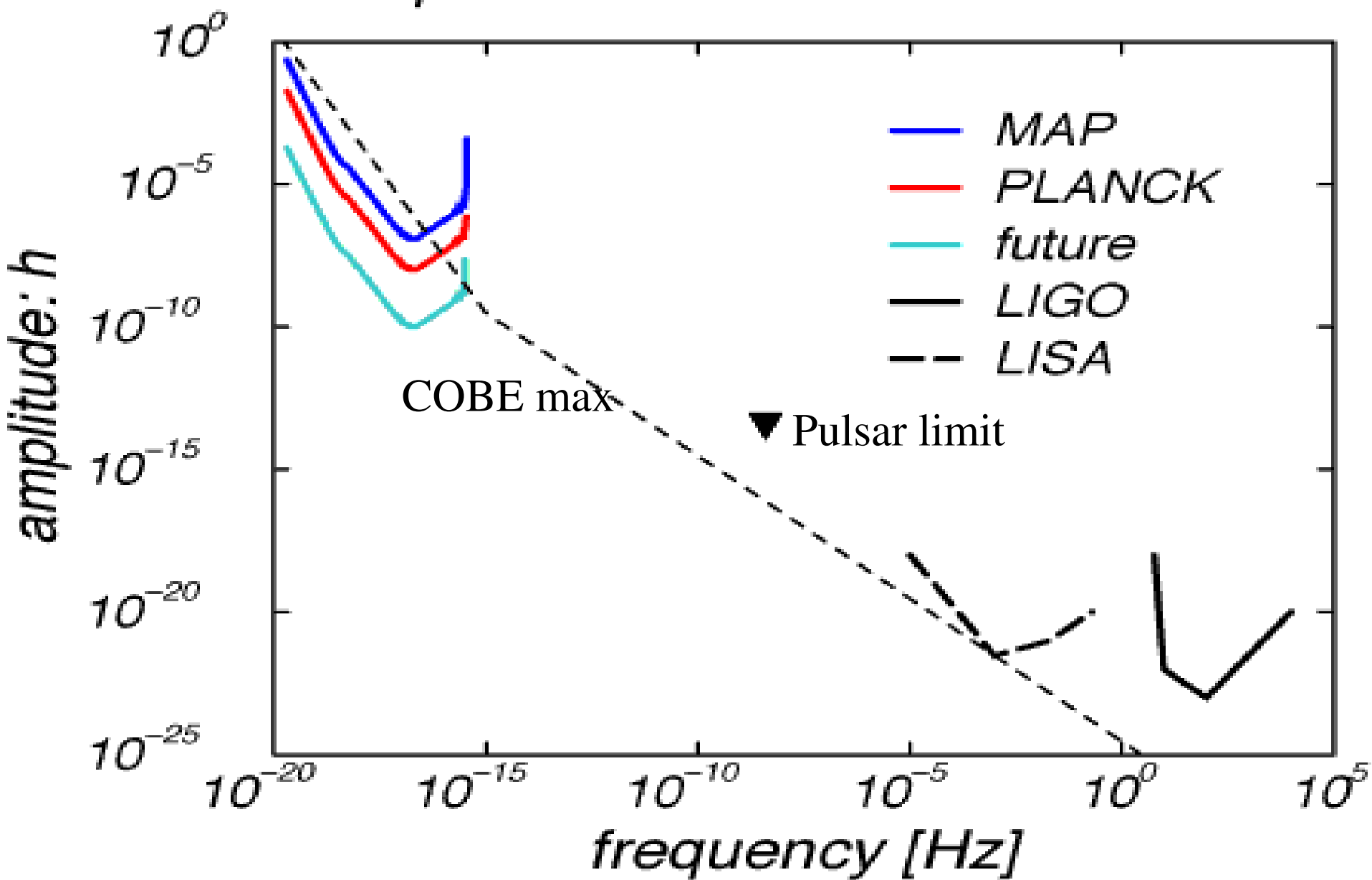
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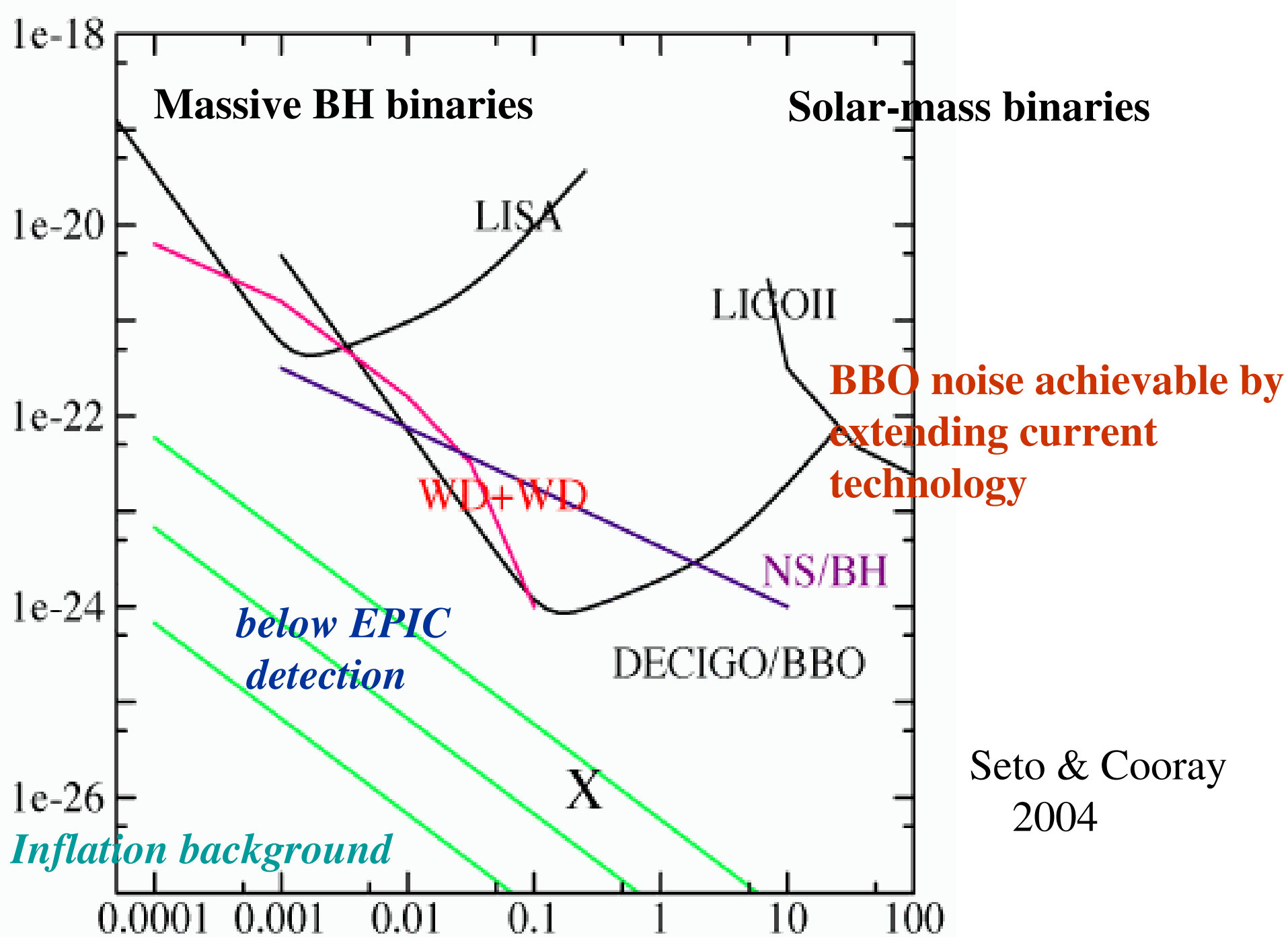


Phinney et al. 2003

Gravitational Wave Detectors

Space-Based and Terrestrial





Future CMB

- CMB polarization provides a measure of inflationary energy scale
- The measurement is hard and can easily be confused with effects due to the local universe (mainly gravitational lensing)
- CMB data can be used for a lensing reconstruction and to reduce the confusion
- Planning/technological studies for EPIC underway. Need to understand large-scale dust polarization!!!
- Brighter future in gravity-wave astronomy (LISA \Rightarrow BBO)

Full talk and details at <http://www.cooray.org>